# **Techniques for Frequency Synthesizer-Based Transmitters**

by

Mohammad Mahdi Ghahramani

A dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy (Electrical Engineering) in The University of Michigan 2015

Doctoral Committee:

Professor Michael P. Flynn, Chair Professor Jerome P. Lynch Associate Professor David D. Wentzloff Assistant Professor Zhengya Zhang © Mohammad Mahdi Ghahramani 2015

All Rights Reserved

To Simintaj Fasihiani and Arsalan Ghahramani

#### ACKNOWLEDGEMENTS

Muchas gracias!

The completion of this PhD was only possible with the help, support, and encouragement of many wonderful souls.

First, I would like to express my deepest gratitude to my adviser, Professor Michael P. Flynn, for giving me the opportunity to pursue a PhD in this finest of institutions. I thank Mike for tirelessly reading papers, revising slides, and editing manuscripts—often during weekends and holidays. Also, for his technical and non-technical advice and insight, and for supporting me throughout this somewhat unorthodox path towards the PhD.

I would like to sincerely thank my committee members, Professor David D. Wentzloff, Professor Zhengya Zhang, and Professor Jerome P. Lynch, for taking time out of their busy schedules to attend meetings and presentations; and for their invaluable advice along the way.

Big thanks to my group members, past and present. That is, Dr. Mark Ferriss, Dr. Jorge Pernillo, Aaron Rocca, Dr. Li Li, Dr. David T. Lin, Jaehun Jeong, Professor Hyungil Chae, Jeffery Fredenburg, Nick Collins, Dr. Hyo Gyuem Rhew, Andres Tamez, Dr. Chun Lee, Dr, Joshua Kang, John Bell, Chunyang Zhai, Aramis P. Alvarez, Dr. Shahrzad Naraghi, Fred Buhler, Batuhan Dayanik, Sunmin Jang, Yong Lim, Steven Mikes, Daniel Weyer, and Adam Mendrela.

Furthermore, I would like to thank my circuit design colleagues in other Michigan groups. That is, Dr. Hassan Ghaed, Dr. Muhammad Faisal, Dr. Kuo-Ken Huang, Dr. Osama Ullah Khan, Elnaz Ansari, and Avish Kosari.

I would like to thank the administrative staff at the University of Michigan for always taking care of me. That is, Fran Doman, Beth Stalnaker, Steven Pejuan, Nicole Frizzle, and the wonderful folks at the international center.

I would like to thank my dear friends in Michigan for making my stay so memorable. That is, Dan Cohen, Dr. Mohammad Fallahi-Sichani, Dr. Ali Kakhbod, Dr. Ali Nazari, Sepehr Entezari, Dr. Morteza Nick, Dr. Hamid Ossareh, Mahmood Barangi, Dr. Danial Ehyaie, Dr. Razi Haque, Dr. Shima Hossein Abadi, Dr. Hadi Katebi, Kaveh Monajemi, Dr. Aria Ghasemian Sahebi, and Dr. Ali Besharatian.

I could not have completed this PhD without the support and encouragement of wonderful friends and colleagues at Qualcomm. That is, Dr. Mazhareddin Taghivand, Dr. Beomsup Kim, Arezou Khatibi, Amir Parayandeh, Yashar Rajavi, Dr. Pouya Kavousian, and Dr. Alireza Khalili.

I would also like to thank Professor Michael Peter Kennedy of University College Cork, Ireland for encouraging me not only to pursue a PhD, but to do it in a top tier US university and also for guiding and supporting me throughout the application process.

I would also like to thank my extended Irish family. That is, Ian Coombes, Alan Williams, Carmel Collins, and Damien Collins.

Most importantly, I would like to thank my parents, Simin Fasihiani and Arsalan Ghahramani, and my brother, Ali Ghahramani, for their unconditional love. For believing in me even at times when I seized to believe in myself. It is to them that I dedicate this humble dissertation.

I came to Michigan to earn a PhD and make life-long friends. I am grateful that I have succeeded in both.

# TABLE OF CONTENTS

DEDICATION	ii
ACKNOWLED	GEMENTS
LIST OF FIGU	<b>RES</b>
LIST OF TABL	<b>ES</b>
LIST OF ABBR	<b>EVIATIONS</b>
ABSTRACT	xiii
CHAPTER	
I. Introd	uction
1.1	Background and Motivation
1.2	Wireless Transmitters
1.3	RF Transmitter Architectures
1.4	PLL Based Transmitters
	1.4.1 Digital PLL Based Transmitters
1.5	Thesis Contributions
II. A 192	MHz Differential XO Based Frequency Quadrupler with Sub-
Picose	cond Jitter in 28nm CMOS
2.1	Introduction
2.2	Frequency Quadrupler Operation
2.3	Differential Crystal Oscillator
2.4	Duty Cycle Correction Operation
2.5	XO Design Considerations
2.6	Measurement Results
2.7	Analysis
	2.7.1 Crystal Oscillator Small Signal Analysis for $\omega \ll \omega_{r_p}$ . 33

	2.7.2 Crystal Oscillator Small Signal Analysis for $\omega_{r_s} < \omega < \omega_{r_a}$	36	
	2.7.3 Low Frequency Design Considerations	42	
	2.7.4 Parallel Resonance Mode Design Considerations	44	
	2.7.5 Duty Cycle Correction Analysis	46	
III. A Low	Voltage Sub 300 $\mu$ W 2.5GHz Current Reuse VCO	51	
3.1	Introduction	51	
3.2	Design Methodology	53	
3.3	Practical Design Considerations	55	
3.4	Implementation and Measurement	56	
IV. A 2.4G	Hz 2Mb/s Digital PLL-based Transmitter for 802.15.4 in 130nm		
CMOS		65	
4.4		<b>~ -</b>	
4.1	Background	65	
4.2	Transmitter Architecture	67	
4.3	Phase Detector Overview	6/	
4.4	Frequency Switching Scheme		
4.5	Power Amplifier	71	
4.6	Voltage Controlled Oscillator		
4.7	$\Sigma\Delta$ Digital to Analog Converter	73	
4.8	PLL Small Signal Frequency Domain Model	74	
	4.8.1 Phase Detector Model	75	
	4.8.2 Digital Integrator, DAC, VCO, and Divider Models	80	
	4.8.3 PLL Transfer Function	82	
4.9	PLL Phase Noise Analysis	84	
	4.9.1 Noise Transfer Function for PLL Blocks	85	
	4.9.2 PLL Output Noise Calculation	86	
4.10	Implementation Details and Test Setup	87	
4.11	Measurement Results		
V. Conclu	sion	95	
5.1	Ideas for Future Work	96	
BIBLIOGRAPH	Υ	99	

# **LIST OF FIGURES**

## Figure

1.1	Internet of Things (IoT) [1]	2
1.2	Categorization of IoT design space [2]	3
1.3	A direct conversion transmitter	6
1.4	A dual conversion (two step) transmitter	7
1.5	A generic PLL-based transmitter	9
1.6	A common type-II analog PLL that is popular in PLL based transmitters .	10
1.7	A digital PLL that is common in RF transmitters	11
1.8	A modern high performance PLL based transmitter	14
2.1	Differential XO based Frequency Quadrupler (F4Xer)	18
2.2	Active inductor based differential XO schematic	19
2.3	Differential XO small signal model, magnitude of active inductor impedance	
	$(Z_{active_l})$ , and combined impedance $(Z_{total})$	22
2.4	Measured phase noise of the new active inductor based 48MHz differential	
	XO using 5052B signal source analyzer	23
2.5	Measured phase noise of 96MHz clock (double of XO and input to final	
	doubler) using 5052B signal source analyzer	24
2.6	Measured 48MHz differential XO waveform probed at XO I/O pins	25
2.7	Measured 96MHz, 50% duty cycle 2X clock with DCC enabled	26
2.8	Measured 192MHz quadrupler waveform (red) generated from the 50%	
	duty cycle 96MHz, 2X clock (blue)	27
2.9	Frequency quadrupler FoM vs active area comparison [3], [4], [5]	28
2.10	Die photo including 50 $\Omega$ o/p buffers, ESD, and bypass caps. The XO and	
	F4Xer total active area is $0.045$ mm <sup>2</sup>	29
2.11	Differential crystal oscillator schematic	30
2.12	Equivalent circuit model for a crystal together with circuit model for	
	different operation regions	32
2.13	Small signal model of the differential crystal oscillator	33
2.14	Small signal model of differential crystal oscillator for $\omega \ll \omega_{r_n}$	34
2.15	Small signal model of differential crystal oscillator for parallel resonance	
	region	36
2.16	The duty cycle correction scheme used in the frequency quadrupler	47
3.1	The proposed AC coupled current reuse VCO	52

3.2	Small signal model of the proposed AC coupled VCO	54
3.3	Chip photo of AC coupled VCO	57
3.4	Measured VCO phase noise and power consumption at 2.53GHz for	
	different supply voltages	58
3.5	Measured VCO FoM at 2.53GHz and power consumption for different	
	supply voltages	60
3.6	Instrument screen shot of phase noise measurement with a 0.85V supply .	61
3.7	Measured phase noise at 2.53GHz over temperature	62
3.8	Measured phase noise at 2.53GHz versus NMOS gate bias voltage with a	
	0.85V supply	63
4.1	The prototype 802.15.4 transmitter	68
4.2	The digital phase detector and equivalent model which is a delta modulator	
	[6]	68
4.3	The two point frequency modulation scheme operation and an example	
	settling behavior [6]	70
4.4	Implementation details for the two point modulation scheme [6]	70
4.5	The two stage resistor feedback inverter based power amplifier	71
4.6	The VCO used in the transmitter	73
4.7	The $\Delta\Sigma$ DAC block diagram $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$	74
4.8	Simplified PLL block diagram	75
4.9	Phase detector operation	76
4.10	Phase detector feedforward path	78
4.11	Frequency domain model of PLL	82
4.12	Frequency domain model of PLL, re-drawn for straightforward transfer	
	function and noise calculations	82
4.13	Frequency domain model of PLL with various noise insertion points	85
4.14	The DPLL based transmitter die photo	88
4.15	Measured transmitter spectrum without modulation	89
4.16	Measured PLL spectrum w/ 2Mb/s MSK modulation	90
4.17	Measured PLL phase noise at 2.405GHz	91
4.18	Measured PLL spur at 2.405GHz	92
4.19	Measured trellis diagram for 2Mb/s MSK modulation	93
5.1	An ultra high performance PLL leveraging the reference quadrupler	97
5.2	Low voltage AC coupled active inductor based crystal oscillator	98

# LIST OF TABLES

## **Table**

1.1	RF transmitter functions and specifications
1.2	Comparison of transmitter architectures
1.3	Comparison of analog and digital PLLs 14
2.1	Differential XO summary and comparison
2.2	Frequency quadrupler results summary
3.1	VCO performance comparison
4.1	Transmitter performance and comparison with prior art

## LIST OF ABBREVIATIONS

CMOS Complementary Metal-Oxide Semiconductor

CP Charge Pump

**CPU** Central Processing Unit

DAC Digital-to-Analog Converter

**DPLL** Digital PLL

**DCC** Duty-Cycle Correction

EVM Error Vector Magnitude

FoM Figure of Merit

**GPS** Global Positioning System

I In-phase

**IF** Intermediate Frequency

**IIR** Infinite Impulse Response

**IoT** Internet of Things

LF Loop Filter

LP Low Pass

LO Local Oscillator

MEMS Micro-Electro-Mechanical Systems

MSK Minimum Shift Keying

MMD Multi-Modulus Divider

MDLL Multiplying Delay-Locked-Loop

**OTA** Operational Trans-conductance Amplifier

O-QPSK Offset-Quadrature Phase Shift Keying

PA Power Amplifier

**PD** Phase Detector

**PDF** Probability Density Function

**PFD** Phase-Frequency Detector

**PI** Proportional-Integral

PLL Phase-Locked-Loop

**PSR** Power Supply Rejection

**PVT** Process, Voltage, and Temperature

**Q** Quadrature-phase

**RF** Radio Frequency

**RX** Receiver

**RFID** Radio-Frequency IDentification

SoC System-on-Chip

TDC Time-to-Digital Converter

TX Transmitter

VCO Voltage Controlled Oscillator

**XTAL** Crystal

**XO** Crystal Oscillator

## ABSTRACT

Techniques for Frequency Synthesizer-Based Transmitters

by

Mohammad Mahdi Ghahramani

Chair: Michael P. Flynn

Internet of Things (IoT) devices are poised to be the largest market for the semiconductor industry. At the heart of a wireless IoT module is the radio and integral to any radio is the transmitter. Transmitters with low power consumption and small area are crucial to the ubiquity of IoT devices. The fairly simple modulation schemes used in IoT systems makes frequency synthesizer-based (also known as PLL-based) transmitters an ideal candidate for these devices. Because of the reduced number of analog blocks and the simple architecture, PLL-based transmitters lend themselves nicely to the highly integrated, low voltage nanometer digital CMOS processes of today. This thesis outlines techniques that not only reduce the power consumption and area, but also significantly improve the performance of PLL-based transmitters. The main contributions of this thesis are three fold.

First, we introduce a novel frequency quadrupler with sub-picosecond jitter. The 192MHz quadrupler is ideal for generating a fast, low jitter reference for a low phase

noise PLL. The quadrupler requires far less power and area than existing methods.

Second, the CMOS current reuse VCO is modified to reduce the supply voltage and achieve good phase noise with very low power consumption. A 2.5GHz prototype achieves the best phase noise-power efficiency figure of merit for any current reuse VCO.

Third, a fully integrated 2.4GHz transmitter for ZigBee based on a digital fractional-*N* PLL is presented. The prototype achieves an MSK modulation rate of 2Mb/s, delivers -2dBm of output power, and is free of in-band fractional spurs.

## **CHAPTER I**

# Introduction

#### 1.1 Background and Motivation

Internet of Things (IoT) is increasing the connectivity of people and things on a scale that once was unimaginable. The physical world itself is becoming a type of information system where sensors and actuators embedded in physical objects—from roadways to pacemakers—are linked through wireless networks, often using the same protocols as the internet.

Internet of things devices are poised to become the largest market for the semiconductor industry [2]. As shown pictorially in Figure 1.1, IoT devices aim to make us and our electronic devices ever more connected to the physical world around us. The applications span several industries such as smart buildings, industrial control, health care, military, and environmental monitoring. In home automation, IoT devices use light or Radio Frequency (RF) energy to power motion detectors which turn lights off if nobody is detected in a room, to dim lights depending on the light level in a room, and to sense and report temperature for air conditioning or heating [7]. In industrial control, IoT devices use vibration energy or



Figure 1.1: Internet of Things (IoT) [1]

thermal energy to monitor and report the condition of rotating machines. In location tracking, they use vibration energy or solar power to enable Global Positioning System (GPS) to sense and the cellular network to report the position of containers, trucks, or rail cars [8].

The diverse set of applications leads to a diverse set of requirements for the electronic devices and in particular for the integrated circuits that are at the heart of these modules. These requirements are elegantly summarized in Figure 1.2. For successful large-scale deployment of wireless IoT systems, each device must have low power consumption and a small form factor. Small form factor results in low cost which leads to mass production and the ubiquitous use of these devices. Low power consumption allows a long battery life, which is imperative in many IoT applications such as wireless sensors [9]. It is due to these requirements that nanometer Complementary Metal-Oxide Semiconductor (CMOS) technology offers the perfect platform to design IoT devices.

Sensor Property	Sub categories	Range of values	
	Туре	Pressure, temperature, strain, chemical, imaging, sound, etc.	
Sensing / Actuation	Duty Cycle	$\textbf{Continuous} \leftrightarrow \textbf{Infrequent, on-demand}$	
Modality	Trigger	Timer based (accuracy?); event in monitored value; external trigger (wakeup radio, battery condition, etc.)	
Computational Performance		Sub-kHz $\leftrightarrow$ 100's of MHz	
Form Factor / Size		Submillimeter $\leftrightarrow$ tens of centimeter scale	
Energy Source / Life Time		Wired (permanently, intermittently); battery (primairy, secondary); energy scavenging (continuous or as available); lifetime of hrs, days, years	
	Туре	Wired vs. wireless (communication distance, communication standard)	
Communication Connectivity	Data Rate / Packet Size	kbps $\leftrightarrow$ Gbps; Bytes $\leftrightarrow$ MBytes	
	Communication Interval	Continuous ↔ Infrequent; triggered by monitored event or external request	

Figure 1.2: Categorization of IoT design space [2]

At the heart of any wireless device is the radio that enables the communication of information. A wireless Micro-Electro-Mechanical Systems (MEMS) sensor that collects temperature readings and then must transfer this information to the base station receiver, is one example. Depending on the data rate and packet size, the radio typically consumes the majority of energy in a wireless device [10]. A wireless radio is usually partitioned into two major blocks 1) the Receiver (RX), and 2) the Transmitter (TX). Although reducing the area and power consumption for both the receiver and transmitter is important, most recent work has been focused on optimizing the receiver. However, there are several applications (such as Bluetooth Low-Energy) where power and area of the transmitter become the system bottleneck [11], [12]. For instance, Radio-Frequency IDentification (RFID) tags communicate with a host that is usually free of any power efficiency requirements. However, each RFID tag has a transmitter that needs to be very low power to achieve sufficient battery life time. The improvement in battery life is important as it facilitates a low cost perpetual

Function	Specification	
Modulation	Accuracy	
Frequency Translation	Spectral Mask	
Power Amplification	Output Power Level	

Table 1.1: RF transmitter functions and specifications

operation of RFID tags.

#### **1.2** Wireless Transmitters

The transmitter is one of the key blocks in any wireless radio. In a wireless sensor node, the power consumption and area requirements of the transmitter are stringent. State of the art wireless sensor nodes typically perform some computation and signal processing on chip [13], therefore it is desirable for the radio to be integrated with the sensor's Central Processing Unit (CPU) to reduce cost. Radio frequency electromagnetic waves are chosen to enable a sufficiently long range of communication. In addition, RF transmitters lend themselves to integration due to their small size. It is for this reason that we focus on integrated RF transmitters for IoT devices.

An RF transmitter performs modulation, upconversion, and power amplification of the baseband signal before the antenna. The design of integrated RF transmitters entails several challenges at both system and circuit levels. Spectral emission mask requirements that are often specified by Federal Communications Commission (FCC), TX to RX leakage, output power level, and linearity are some of the parameters that impact the choice of transmitter architecture [14]. Typical transmitter functions and required specifications are summarized in Table 1.1.

The Modulation type exhibits trade-offs between bandwidth and power. The require-

ments of the wireless communication system impacts the selection of modulation type. Communication requirements can be talk time, maximum range, channel capacity, *etc*. There are two modulation types in an RF transmitter today 1) constant envelope (or nonlinear), and 2) variable envelope (or linear). A modulated signal  $x(t) = A \cos(\omega_c t + \phi(t))$  is considered constant envelope if the envelope (amplitude), *A*, is constant. In linear modulation schemes, *A* is a function of time and therefore contains information. Constant envelope modulation is usually the adopted modulation type in IoT systems (such as ZigBee [15] and Bluetooth LE [16]) due to its simplicity. Such waveforms contain information only in the zero crossings and can therefore be processed by a nonlinear Power Amplifier (PA) with higher power efficiency<sup>1</sup>.

#### **1.3 RF Transmitter Architectures**

Three RF transmitter architectures are common in modern nanometer CMOS integrated circuits [17]: 1) Direct conversion, 2) Dual conversion, and 3) Phase-Locked-Loop (PLL) based. In this section, we study all 3 architectures and justify the selection of a PLL based TX for this work.

A generic direct conversion TX is shown in Figure 1.3. Information, in the form of In-phase (I) and Quadrature-phase (Q) binary bits, is converted to the analog domain using a Digital-to-Analog Converter (DAC). The DAC output gets amplified and conditioned by a low pass or band pass filter in the baseband circuits<sup>2</sup>. The low frequency analog baseband signal is upconverted to RF frequency using a mixer that is driven by I and Q Local

<sup>&</sup>lt;sup>1</sup>Power amplifiers with a constant envelope input are free of any voltage linearity requirements. Therefore, a highly nonlinear PA, such as a class D PA, can be used without the loss of information.

<sup>&</sup>lt;sup>2</sup>Baseband circuits typically include trans-impedance amplifiers, filters, and programmable gain amplifiers.



Figure 1.3: A direct conversion transmitter

Oscillator (LO) signals. The mixer output goes through a PA to to drive a  $50\Omega$  antenna. The PA output is sometimes band pass filtered before transmission. The final band pass filter is used to reduce the out of band emissions.

A direct conversion transmitter is the most common architecture used today. This transmitter is versatile since it can support any modulation type. It is fairly low power and lends itself to integration due to its relatively simple design. However, it suffers from two main problems: One is the Voltage Controlled Oscillator (VCO) pulling by the PA modulated spectrum. Since the PA and VCO operate at the same frequency, the PA spectrum can corrupt the VCO spectrum which degrades the transmitter Error Vector Magnitude (EVM). A second issue is that although this TX is rather simple, it still requires two DACs, two amplifiers, two filters, and two analog mixers. In addition, a PLL and a divide by 2 circuit is needed to generate the I and Q LO signals. Since the power and area requirements for a sensor network TX are stringent, a simpler TX that is more amenable to integration in nanometer CMOS is desired.

In order to eliminate the pulling issue in a direct conversion transmitter, the baseband signal is upconverted in two or more stages. One popular architecture is the dual conversion



Figure 1.4: A dual conversion (two step) transmitter

(or two-step) transmitter shown in Figure 1.4. After the DAC and baseband circuits, the signal is first upconverted by LO1 to an Intermediate Frequency (IF) and then upconverted to RF by LO2. This two-step transmission eliminates VCO polling as the LO1 and LO2 frequencies are now different (often by a large amount). However, the main difficultly is the band pass filter between first and second upconversion. This band pass filter needs to attenuate unwanted side-bands by a large amount, *e.g.*, 50-60dB [14]. Furthermore, the addition of new blocks such as an IF mixer results in a large power consumption and bulky area, making this transmitter architecture unsuitable for IoT and sensor applications.

The third architecture is the PLL based transmitter shown in Figure 1.5. A  $\Delta\Sigma$  Fractional-N (Frac-N) PLL performs modulation, frequency translation, and upconversion, all in one block. Information, in the form of binary bits, is applied to a digital  $\Delta\Sigma$  modulator ( $\Delta\Sigma$ M) which in turn modulates the output frequency of the PLL through a Multi-Modulus Divider (MMD). The Phase-Frequency Detector (PFD), Charge Pump (CP), and Loop Filter (LF) compare and condition the reference and divider phase difference. When the loop is closed and the PLL is locked, the VCO outputs an RF frequency dictated by the digital information. Therefore, frequency and phase modulation can simply be performed with a PLL based transmitter by altering the  $\Delta\Sigma$ M divide value.

rr				
ТХ Туре	Power	Area	Complexity	Major Concerns
Direct conversion	Low	Medium	Low	Frequency pulling
Dual conversion	High	High	High	Complex filtering needed
PLL based	Low	Low	Medium	PLL design can be complex

Table 1.2: Comparison of transmitter architectures

Because the PLL now performs the entire transmitter functions all in one block, several trade-offs arise that often complicate the design of PLL-based transmitters. For instance, a small PLL bandwidth is typically desired to achieve low integrated phase noise. However, low PLL bandwidth reduces the maximum modulation rate which limits the communication data rate. Therefore, circuit and system techniques are typically used to break this trade-off. One popular approach is to use a fast reference to reduce he  $\Delta\Sigma M$  quantization noise (which allows increasing the PLL bandwith without a phase noise penalty). However, reference multipliers can be complex, power hungry, and bulky. Therefore, new techniques to generate a fast reference can dramatically improve the performance, lower the power consumption, and reduce the area of PLL-based transmitters.

PLL based transmitters lend themselves nicely to the constant envelope modulation schemes that are widely used in IoT systems. It is important to note that several analog blocks such as DACs, mixers, and bandpass filters are eliminated. In addition to improving the area, the elimination of the analog circuits results in a simpler transmitter which leads to a low power consumption. It is for these reasons that a PLL based transmitter is the architecture of choice in this work.

Table 1.2 compares the three common transmitter architectures in terms of power, area, and design requirements.



Figure 1.5: A generic PLL-based transmitter

#### **1.4 PLL Based Transmitters**

A PLL based transmitter is an ideal candidate for wireless IoT and sensor network devices as the simplicity of this architecture results in small area and low power consumption. Within the PLL based transmitter design space, there are two options available 1) An analog PLL, and 2) A Digital PLL (DPLL)<sup>3</sup>.

Figure 1.6 shows a generic fractional-*N* analog PLL [18]. The PFD acts as the summing node in the feedback loop where it compares the phase of the reference and the divider and generates an error signal that is proportional to the phase difference. The charge pump

<sup>&</sup>lt;sup>3</sup>There are several acronyms and names used for a digital PLL such as All Digital PLL (ADPLL), digitaldominant PLL, and digitally-assisted PLL. In the author's opinion, digital PLL is a misnomer since both the input and output, as well as several building blocks of an "ADPLL" are still analog. What we mean by a digital PLL is that the Proportional-Integral (PI) controller in the PLL is in the digital domain, *i.e.*, the charge pump and loop filter are replaced by digital equivalents. We will refer to this type of PLL as a DPLL throughout the thesis.



Figure 1.6: A common type-II analog PLL that is popular in PLL based transmitters

(proportional controller) gains up the PFD output and converts the error signal to the current domain. The loop filter, comprised of passive components  $C_0$  (integrator capacitor),  $R_1 C_1$  (which form the first pole-zero pair), and  $R_2 C_2$  (which form the second pole, usually to attenuate the VCO control voltage ripple), converts the charge pump current to voltage. The loop filter also stabilizes the feedback loop (loop filter is essentially a lead lag compensator). The loop filter output is applied to a VCO (via a varactor) to generate the RF phase/frequency modulated signal. Typically, an *LC* VCO which has low phase noise is used to meet EVM requirements. A fractional divider, formed by a digital  $\Delta\Sigma$  modulator and a multi modulus divider, is placed in the feedback loop. By dynamically changing the division ratio, a fractional divider is used to achieve both phase and frequency modulation. This is because the PLL output phase/frequency and the reference phase/frequency are related by the division



Figure 1.7: A digital PLL that is common in RF transmitters

ratio, N (i.e.,  $F_{PLL}(t) = N(t) \times F_{REF}$  and  $\phi_{PLL}(t) = N(t) \times \phi_{REF}$ ).

#### 1.4.1 Digital PLL Based Transmitters

A schematic of a typical digital PLL is shown in Figure 1.7. Since their introduction in 2003 [19], DPLLs have received ample attention in industry and academia. This is primarily because the more digital nature of a DPLL makes it an attractive architecture for use in a nanometer CMOS System-on-Chip (SoC). Analog building blocks such as charge pumps and loop filters pose design and verification challenges in modern technologies. This will add significant implementation cost in a high volume digital dominant environment of IoT devices.

A Time-to-Digital Converter (TDC) replaces the PFD in a DPLL. A TDC outputs a digital word (instead of an analog error signal) that is proportional to the phase difference

between the reference and divider. This digital word can readily be applied to a digital loop filter, which in this example is a simple single pole single zero Infinite Impulse Response (IIR) filter cascaded by an accumulator (equivalent of integrator in an analog PLL). The output of the digital loop filter needs to be applied to the VCO varactor. Typically, a DAC converts the loop filter output to an analog voltage that sets the varactor capacitance.

A DPLL architecture is chosen for the transmitter in this work for the following reasons: the charge pump used in an analog PLL suffers from output resistance variation with respect to Process, Voltage, and Temperature (PVT). Mismatch in up and down currents (which results in spurs and added phase noise) is also another impediment to using a charge pump. Both these effects are further pronounced in today's nanometer CMOS nodes since the supply voltage is as low as 1V. Improving the mismatch and output resistance of a charge pump results in large area and increased power consumption. This makes the charge pump an undesirable block in sensor network transmitters. The loop filter in an analog PLL is comprised of several passive components that can have large values (*e.g.*, 30-100k $\Omega$  for R<sub>1</sub>, and 100pF for C<sub>1</sub>). Therefore, using an analog passive loop filter results in a large area. In addition to a large area, the leakage current through the capacitors cause spurs thereby degrading the TX fidelity.

In contrast, DPLLs use a compact digital loop filter which is insensitive to leakage. Also, unlike analog PLLs, the power consumption and area of a digital loop filter improves with scaling. Another advantage is that adopting a DPLL makes possible the use of digital signal processing algorithms to improve the transmitter functions and features. However, using a digital PLL is not without challenges. Based on the DPLL architecture chosen, implementation of a linear high resolution TDC can be difficult and results in large area and increased power consumption [20]. This will in turn degrade the already aggressive area and power budget of an IoT system. In addition, the quantization noise and added spurs of DPLLs usually result in an inferior phase noise compared to analog PLLs. Nevertheless, DPLLs are suitable candidates for IoT systems as the simple modulation schemes used in IoT standards result in a fairly relaxed EVM requirement.

It is important to note that even in a DPLL, there are still three analog blocks: a DAC, a Crystal Oscillator (XO) reference, and a VCO. A DAC is typically a simple circuit which can be designed to have low power consumption and small area. Therefore, it can be used in a low power, compact IoT system without much overhead.

The VCO is often a bulky block that consumes several milliWatts of power. In addition, most VCOs need a high supply voltage for safe startup which limits their use in a low voltage IoT environment. Therefore, a low voltage, low current VCO architecture is desirable for a wireless sensor network device.

It is imperative to note that an often neglected part of any PLL based transmitter (analog or digital) is the power and area dedicated to the reference path (clock generation) which includes the crystal oscillator and a reference multiplier (Figure 1.8). A crystal oscillator is an electronic oscillator circuit that uses the mechanical resonance of a vibrating crystal of piezoelectric material to create an electrical signal with a very precise frequency. In most modern SoCs, the XO active circuits (such as start up, tuning capacitors, and loss compensation) are placed on chip. On chip XO circuits typically operate from a large supply (*e.g.*, 1.8V). This is to isolate the supply voltage of sensitive RF circuits (which typically run from a 1.1V supply) from the large XO spurs that would otherwise exist if the supply was shared. Integrated XO circuits are bulky and consume milliWatts of power [21].



Figure 1.8: A modern high performance PLL based transmitter

Table 1.3: Comparison of analog and digital PLLs		
Analog PLL	Digital PLL	
Large area	Compact	
No benefit from scaling	Improves with scaling	
Excellent phase noise	Moderate phase noise	
Charge pump problems	Free of charge pump	
Bulky and leakage prone loop filter	Digital loop filter	
Little benefit from DSP	DSP used to improve performance/features	

Furthermore, the design of PVT insensitive injection locked reference multipliers is complex which results in a large power and area penalty [22]. Therefore, reducing the supply voltage and power consumption of the crystal oscillator, as well as improving the performance of the XO and reference generation circuits has an immense impact on the overall power and area of a PLL based transmitter.

In summary, the difficultly of implementing traditional analog circuits, and the many opportunities, such as compact filters and digitally assisted analog circuits, presented by DPLLs in low supply nanometer CMOS processes makes DPLL the architecture of choice in this work. Table 1.3 outlines the typical tradeoffs between analog and digital PLLs.

#### **1.5 Thesis Contributions**

New techniques proposed in this thesis dramatically reduce the power consumption, shrink the area, and also improve the performance of PLL based transmitters.

The main contributions of this work are three fold:

# A 192MHz Differential XO Based Frequency Quadrupler with Sub-Picosecond Jitter in 28nm CMOS

A low jitter 192MHz crystal reference quadrupler leverages a new active inductor based 48MHz differential XO, two skewed inverters, a new duty cycle correction circuit, and a frequency doubler. The 192MHz quadrupler can serve as a fast, low jitter reference for a low phase noise PLL and requires far less power and area than reference multiplying PLL or MDLL circuits. The measured RMS jitter is 168fs for the XO, and 184fs for 96MHz output (192MHz divide by 2). The entire circuit, including the XO, draws 5.5mA from a 1V supply and occupies 0.045mm<sup>2</sup>. To our best knowledge, this is the first reference frequency quadrupler with sub-picosecond jitter.

#### A Low Voltage Sub 300µW 2.5GHz Current Reuse VCO

The two transistor CMOS current reuse VCO is modified with the addition of an AC coupling capacitor to reduce the supply voltage and achieve good phase noise with very low power consumption. A 2.17GHz to 2.9GHz prototype VCO operates with a supply voltage as low as 0.6V. At 2.53GHz, with a 0.7V supply and a  $185\mu$ W power consumption, the measured phase noise at 3MHz offset is -122.6dBc/Hz and varies by only 2.2dB over a temperature range from -30 to  $120^{\circ}$ C. For a 0.85V supply, phase noise is improved to -126.1dBc/Hz with a 280 $\mu$ W power consumption which corresponds to a Figure of Merit (FoM) of 190.2dB. This is the lowest reported power

consumption and supply voltage for any current reuse VCO<sup>4</sup>. Fabricated in 65nm CMOS, the prototype occupies 0.13mm<sup>2</sup> [23].

#### A 2.4GHz 2Mb/s Digital PLL-based Transmitter for 802.15.4 in 130nm CMOS

A fully integrated 2.4GHz transmitter for 802.15.4 based on a digital  $\Sigma\Delta$  fractional-*N* PLL is presented. A self calibrated two point modulation scheme enables modulation rates much larger than the loop bandwidth. An oversampled 1-bit quantizer is used as a phase detector, reducing spurs and nonlinearity associated with some TDC based digital PLLs. The prototype achieves an MSK modulation rate of 2Mb/s, delivers -2dBm of output power, and is free of in band fractional spurs. The transmitter, implemented in 130nm CMOS, consumes 17mW from a 1.2V supply and occupies an active area of 0.6mm<sup>2</sup> [24].

<sup>&</sup>lt;sup>4</sup>As of the date of publication in [23].

## **CHAPTER II**

# A 192MHz Differential XO Based Frequency Quadrupler with Sub-Picosecond Jitter in 28nm CMOS

#### 2.1 Introduction

High performance frequency synthesizers often use a multiple of the Crystal Oscillator (XO) frequency as a reference input to meet stringent phase noise requirements [25], [26], [22]. A high reference frequency reduces the fractional-*N* modulator quantization noise. Because high frequency crystal oscillators are expensive, it is preferable to more than double the XO frequency. However, the use of multiple frequency doublers in series is best avoided due to high jitter. For example, when two frequency doublers are used in series, both the rising and falling edges are corrupted by long delays and therefore have high jitter.

In LO frequency synthesizers with GHz range outputs, an injection locked integer-*N* PLL or Multiplying Delay-Locked-Loop (MDLL) reference multiplier is cascaded with an *LC* fractional-*N* PLL to achieve low phase noise [22]. Nevertheless, the power consumption and area of these reference multipliers is high because of the complexity needed for PVT insensitive reference injection, to achieve low jitter and spurs [22], [27]. Although the



Figure 2.1: Differential XO based Frequency Quadrupler (F4Xer)

injection locked fractional-*N* MDLL in [28] has a 1.5GHz output, the use of a ring VCO means that the far offset phase noise is much worse than when a reference multiplier is cascaded with an *LC* PLL.

We introduce a new low power, compact differential XO that achieves a measured RMS jitter of 168fs. We also propose a new method to multiply the XO frequency by four with less than half the power consumption and less than a quarter of the area of conventional methods. This 192MHz quadrupler circuit achieves low edge jitter making it an ideal fast reference for low noise synthesizers.

#### 2.2 Frequency Quadrupler Operation

Figure 2.1 shows the new differential XO based Frequency Quadrupler (F4Xer). A new active inductor based XO generates a 48MHz differential sinusoid. This work uses the differential XO outputs in a unique way to double the frequency. The differential XO outputs



Figure 2.2: Active inductor based differential XO schematic

are fed to two skewed inverters, with thresholds adjusted by Duty-Cycle Correction (DCC) feedback, to produce two 25% duty cycle 48MHz square waves (*i.e.*, at the XO frequency). The two 25% duty cycle clocks are XORed to form a 50% duty cycle, 96MHz, 2X clock (*i.e.*, double the XO frequency). Both the rising and falling edges of the 2X clock have low jitter since they are directly generated from the XO outputs. It is important to note that this is unlike a standard frequency doubler where one edge per cycle is corrupted by a long delay. After an inverter buffer, a conventional XOR-plus-delay based frequency doubler generates a 192MHz, 4X clock. As seen in Figure 2.1, the 4X clock has one low jitter edge per cycle (directly from XO). Therefore, the 192MHz, 4X clock can serve as a clean reference in any edge-triggered system such as a PFD or PD based PLL or DLL.

#### 2.3 Differential Crystal Oscillator

Figure 2.2 shows the new differential XO circuit. Compared to single-ended XOs, differential XOs have several advantages such as reduced spurs and better Power Supply Rejection (PSR) [29]. A differential cross-coupled oscillator circuit cannot be used because

when a crystal replaces the *LC* tank, the circuit latches up due to the lack of a low impedance DC path. The differential XO in [29] solves this latch-up problem by AC coupling the cross-coupled transistors. However, this method is susceptible to noise injection since a separate DC voltage biases the cross coupled pair in the XO core. Furthermore, it requires a large die area to reduce the noise of this on-chip DC bias voltage.

Instead, we introduce a low power, compact active inductor to provide a low impedance DC path and prevent latch up. Two single ended active inductors are formed by placing a resistor,  $R_1$ , between the gate and drain of diode-connected transistors, M1 and M2. Crosscoupled transistors, M3 and M4, provide negative resistance to sustain XO oscillation.  $C_L$ , a programmable 6-bit binary capacitor bank with an LSB of 200fF, is placed on both sides of the XO for fine tuning.  $C_0$  is a 10pF off chip capacitor for XO coarse tuning. Resistor  $R_1$ , used in the active inductor, is a programmable 6 bit binary weighted resistor with an LSB of 0.5k $\Omega$ .

### 2.4 Duty Cycle Correction Operation

Two offset 25% duty cycle clocks at the XO frequency are XORed to form the 50% duty cycle 2X clock. The duty cycle of this 96MHz, 2X clock must be 50% as both its rising and falling edges are used to generate the clean edges of the 192MHz, 4X clock (Fig. 2.1). The new DCC circuit ensures the generation of the 25% duty cycle 1X clocks so that when these are combined, the duty cycle of the 96MHz, 2X clock is 50%. The DCC feedback loop forces the average (*i.e.*, DC component) of the 96MHz, 2X clock and its inverse,  $\overline{2X}$  (formed by an extra inverter) to be the same to achieve a 50% duty cycle. Two RC Low Pass (LP)

filters extract the DC of 2X and  $\overline{2X}$  clocks. The DCC uses a folded cascode Operational Trans-conductance Amplifier (OTA) as an error amplifier to generate a feedback voltage based on DC values of 2X and  $\overline{2X}$ . This feedback voltage sets the switching thresholds of the skewed inverters so that the duty cycle of both 1X clocks is 25%. The switching threshold is set by applying the DCC feedback voltage to the gates of zero  $V_T$  NMOS transistors, M3 and M6, at the bottom of the skewed inverters. The RC LP filters set the dominant pole of the DCC loop in the kHz range for easy stability.

This differential method of duty cycle correction, based on comparing DC values, does not require a precise bias voltage and is insensitive to PVT. The switching threshold of each skewed inverter is set below  $V_{DD}/2$  by using high  $V_T$  PMOS transistors, M1 and M4, and zero  $V_T$  NMOS transistors, M2 and M5 (Fig. 2.1). The skewed inverters are sized large to reduce noise. The large size, in addition to a symmetric layout, yields good matching. The input stage of OTA is sized large to reduce the DC offset which manifests itself as a static duty cycle error. The DCC operation is unaffected by the extra inverter delay in the  $\overline{2X}$  path since the DC value of  $\overline{2X}$  remains unchanged.

#### 2.5 XO Design Considerations

Figure 2.3 shows the small signal model for the differential XO. The crystal is modelled as a series RLC network with motion inductance  $L_x$ , motion capacitance  $C_{x1}$ , and equivalent series resistance  $R_x$ , in shunt with parasitic capacitance  $C_{x2}$ .  $C_L/2$  is the equivalent series combination of on-chip fine tune capacitors. The impedance of the cross coupled pair,  $Z_{CC}$ , is  $-2/g_{m_{3,4}}$  at low frequency. The active inductor small signal impedance,  $Z_{active_L}$ , has a


Figure 2.3: Differential XO small signal model, magnitude of active inductor impedance  $(Z_{active_L})$ , and combined impedance  $(Z_{total})$ 

zero at  $\omega_z = 1/R_1C_{gs_{1,2}}$  and a pole at  $\omega_p = g_{m_{1,2}}/C_{gs_{1,2}}$ .  $Z_{total}$  is the combined impedance of crystal and active inductor.

As shown in the magnitude plot of  $Z_{active_L}$  vs frequency in Figure 2.3, the low frequency impedance of the active inductor is  $1/g_{m_{1,2}}$  and the high frequency impedance is  $R_1$ . M1 and M2 are sized large to achieve low impedance at DC to avoid latch up (*i.e.*, DC loop gain less than 1). The active inductor impedance increases with frequency, and this affects the total impedance as shown in the plot of  $Z_{total}$  in Figure 2.3. The  $R_1$  value of the active inductor is judiciously chosen to 1) avoid crystal loading at oscillation frequency and 2) set  $\omega_z$  to prevent oscillation at any frequency other than crystal's high Q, parallel resonance frequency (*i.e.*, avoids large loop gain at any frequency other than crystal's oscillation frequency).





#### 2.6 Measurement Results

Figure 2.4 shows the measured phase noise of the 48MHz differential XO signal using an Agilent 5052B signal analyzer. The RMS jitter, measured over an integration bandwidth from 10kHz to 10MHz, is only 168.1fs. The measured phase noise is -147.7dBc/Hz, -155.8dBc/Hz, and -158.5dBc/Hz at 10kHz, 100kHz, and 1MHz offsets, respectively. Figure 2.5 shows the measured phase noise of 96MHz clock (the input to final doubler). The measured RMS jitter is 183.6fs. The phase noise of the 192MHz, 4X clock cannot be directly measured using a signal source analyzer because one edge per cycle is noisy due to



Figure 2.5: Measured phase noise of 96MHz clock (double of XO and input to final doubler) using 5052B signal source analyzer

the delay in final doubler [22] (most clock inputs are edge- triggered and require one low jitter edge). The last stage XOR-plus-delay based frequency doubler adds little phase noise [17] since the low jitter edges of the 192MHz, 4X clock are merely buffered versions of the rail-to-rail 96MHz, 2X clock edges which have low measured phase noise. Figure 2.6 shows a scope capture of the differential waveforms at the XO I/O pins, measured with an active probe. Figure 2.7 shows a scope capture of the 96MHz, 2X clock with a measured duty cycle of 50% with DCC enabled. Figure 2.8 captures the 192MHz, 4X clock that is generated from the 96MHz, 50% duty cycle 2X clock. The rising and falling edges of 2X clock are used to generate a 192MHz, 4X clock with clean falling edges. Figure 2.9 compares the



Figure 2.6: Measured 48MHz differential XO waveform probed at XO I/O pins







Figure 2.8: Measured 192MHz quadrupler waveform (red) generated from the 50% duty cycle 96MHz, 2X clock (blue)



Figure 2.9: Frequency quadrupler FoM vs active area comparison [3], [4], [5]

F4Xer FoM vs area. Figure 2.10 shows the die photo. The entire circuit, including the XO, occupies an active area of 0.045mm<sup>2</sup>. Table 2.1 summarizes the performance of differential XO and compares with recent work. Table 2.2 outlines the F4Xer measured results.

## 2.7 Analysis

In this section, the theoretical analysis and detailed design considerations for the new differential crystal oscillator are outlined. The differential crystal oscillator of Figure 2.2 is re-drawn<sup>1</sup> as shown in Figure 2.11.

As shown in Fig. 2.12, the crystal is modeled as a series *RLC* equivalent circuit (referred to as the motional arm) where  $R_1$ ,  $L_1$ , and  $C_1$  are the motional resistance, inductance, and capacitance, respectively; in parallel with a static capacitance,  $C_0$ . The motional resistance,  $R_1$ , represents the loss in the crystal. The static capacitance,  $C_0$ , is the measured capacitance associated with the crystal, its electrodes, and the stray capacitance internal to the crystal

<sup>&</sup>lt;sup>1</sup>Component names are changed to make the theoretical analysis easier to follow.



Figure 2.10: Die photo including  $50\Omega$  o/p buffers, ESD, and bypass caps. The XO and F4Xer total active area is 0.045mm<sup>2</sup>

Parameter	This Work	JSSC'12	RFIC'10
		[29]	[21]
Differential?	Yes	Yes	No
CMOS tech.	28nm	65nm	65nm
Power (mW)	1.5	2.16	7
Supply voltage (V)	1	1.8	1.4
Active area (mm <sup>2</sup> )	0.0133	0.15 <sup>†</sup>	0.09
Crystal freq. (MHz)	48	26	38.4
Phase noise (dBc/Hz)	-147.7	-146.4*	-144*
@ 10kHz			
Phase noise (dBc/Hz)	-155.8	-150.7*	_
@ 100kHz			
Phase noise (dBc/Hz)	-158.5	-151.3*	_
@ 1MHz			
RMS jitter (fS)	168	420 <sup>‡</sup>	_
10kHz-10MHz BW			
Tuning range (ppm)	±35	±45	280
Avg. tuning step (ppm)	1	0.005	0.002

Table 2.1: Differential XO summary and comparison

\*Referred to 48MHz for fair comparison

<sup>†</sup>Includes coarse tuning capacitors

<sup>‡</sup>10kHz to 5MHz integration bandwidth

rubie 2.2. i requeile y quadrapter results summary			
Technology	28nm CMOS		
Total power (mW)	5.5		
Supply voltage (V)	1		
	Total	5.5	
Current (mA)	XO	1.5	
	F4Xer	4	
	Total	0.045	
Active area (mm <sup>2</sup> )	XO	0.013	
	F4Xer	0.032	
	10kHz	-139.8	
Phase noise (dBc/Hz) <sup>†</sup>	100kHz	-148.3	
	1MHz	-151.9	
RMS jitter <sup>†</sup> (fS)	183.6		
96MHz 2X clock duty cycle(%)	50		

 Table 2.2: Frequency quadrupler results summary

<sup>†</sup>Measured @ 96MHz (quadrupler divide by 2)



Figure 2.11: Differential crystal oscillator schematic

enclosure. The equivalent circuit model is specified in a datasheet by the crystal manufacturer. If we define  $Z_0 = 1/j\omega C_0$ , and  $Z_1 = R_1 + jwL_1 + 1/j\omega C_1$ , then the impedance of crystal is obtained as

$$Z_{xtal} = \frac{Z_1 Z_0}{Z_1 + Z_0}.$$
 (2.1)

Even though the crystal equivalent circuit results in both a series resonance and a parallel resonance, the crystal is typically used in the parallel resonance region with the resonance frequency given by:

$$\omega_{r_p} \approx \frac{1}{\sqrt{L_1 C_1}} \left( 1 + \frac{C_1}{2(C_0 + C_L)} \right).$$
 (2.2)

Capacitor  $C_L$ , specified by the manufacturer, is the total capacitance that is to be presented to the crystal for oscillation in the parallel-resonance mode<sup>2</sup>. At frequencies much below resonance, the crystal impedance is capacitive with impedance,  $Z_{xtal}(\omega \ll \omega_{r_p}) \approx 1/j\omega C_0$ . The crystal, however, becomes inductive in a certain frequency range called the parallelresonance region. The parallel-resonance region is where frequency is between  $1/\sqrt{L_1C_1}$ (also known as the series resonance frequency,  $\omega_{r_s}$ ) and  $\omega_{r_p}$ . In this region, the crystal is modeled by an inductor,  $L_e$ , in series with a resistor,  $R_e$ . This region is important since most on-chip crystal oscillators are designed to oscillate in the parallel-resonance mode. The equivalent series impedance in parallel region is be used later in the differential crystal oscillator loop gain analysis. An equivalent circuit model for the crystal in different operation regions is shown in Figure 2.12.

The overall small signal model of the XO is shown in Figure 2.13. The impedance of

<sup>&</sup>lt;sup>2</sup>It is important to note that  $C_L$  is different from the physical external capacitor,  $C_{ext}$ , placed across the crystal. Rather,  $C_L$ , is  $C_{ext}$  plus the sum of capacitances (including, for example, the crystal buffer input capacitance) across the crystal.



Figure 2.12: Equivalent circuit model for a crystal together with circuit model for different operation regions

the active inductor in Figure 2.13 is obtained as

$$Z_{L_a}(\boldsymbol{\omega}) = \frac{2}{g_{m_p}} \frac{1 + j\boldsymbol{\omega}/\boldsymbol{\omega}_z}{1 + j\boldsymbol{\omega}/\boldsymbol{\omega}_p},$$
(2.3)

where  $\omega_z = -1/R_{L_a}C_{gg_p}$ , and  $\omega_p = -g_{m_p}/C_{gg_p}$ . The pole frequency,  $\omega_p$ , is equivalent to PMOS transit frequency,  $\omega_{T_p}$ .

The impedance of cross-coupled pair in Figure 2.13 is given by

$$Z_{cc}(\boldsymbol{\omega}) = \frac{-2}{g_{m_n}} \frac{1}{1 - j\boldsymbol{\omega}/\boldsymbol{\omega}_p},$$
(2.4)

where  $\omega_p = g_{m_n}/C_{gg_n}$ . The pole frequency,  $\omega_p$ , is equivalent to NMOS transit frequency,  $\omega_{T_n}$ .



Figure 2.13: Small signal model of the differential crystal oscillator

# 2.7.1 Crystal Oscillator Small Signal Analysis for $\omega \ll \omega_{r_p}$

We first begin by looking at the total admittance,  $Y_t$ , at frequencies much below the resonance (*i.e.*,  $\omega \ll \omega_{r_p}$ ). This analysis is later used to outline a set of design considerations to avoid parasitic oscillation (*i.e.*, oscillation at any frequency other than the desired frequency).

Using the crystal equivalent circuit for  $\omega \ll \omega_{r_p}$  (Figure 2.12), the XO small signal model is re-drawn as shown in Figure 2.14. Using this small signal model,  $\text{Im}\{Y_t\}$ , is obtained as



Figure 2.14: Small signal model of differential crystal oscillator for  $\omega \ll \omega_{r_p}$ 

$$\operatorname{Im}\{Y_{t}\}(\boldsymbol{\omega})|_{\boldsymbol{\omega}\ll\boldsymbol{\omega}_{rp}} = \frac{\boldsymbol{\omega}}{2\boldsymbol{\omega}_{T_{n}}\boldsymbol{\omega}_{T_{p}}\left(\boldsymbol{\omega}^{2}+\boldsymbol{\omega}_{z}^{2}\right)} \left[\boldsymbol{\omega}^{2}\left(g_{m_{n}}\boldsymbol{\omega}_{T_{p}}+2\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{T_{n}}\left(C_{0}+C_{x}\right)\right)\right.$$
$$\left.+g_{m_{p}}\boldsymbol{\omega}_{T_{n}}\boldsymbol{\omega}_{z}^{2}+g_{m_{n}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{z}^{2}\right.$$
$$\left.-g_{m_{p}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{T_{n}}\boldsymbol{\omega}_{z}\right.$$
$$\left.+2\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{T_{n}}\boldsymbol{\omega}_{z}^{2}\left(C_{0}+C_{x}\right)\right],$$
$$(2.5)$$

and  $\operatorname{Re}\{Y_t\}$  is obtained as

$$\operatorname{Re}\{Y_{t}\}(\boldsymbol{\omega})|_{\boldsymbol{\omega}\ll\boldsymbol{\omega}_{rp}} = \frac{\boldsymbol{\omega}^{2}}{2\boldsymbol{\omega}_{T_{p}}\left(\boldsymbol{\omega}^{2}+\boldsymbol{\omega}_{z}^{2}\right)}\left[\left(g_{m_{p}}\boldsymbol{\omega}_{z}-g_{m_{n}}\boldsymbol{\omega}_{T_{p}}\right)\right.\\\left.+g_{m_{p}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{z}^{2}-g_{m_{n}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{z}^{2}\right].$$

$$(2.6)$$

It is important to note that the denominators in Equation 2.5 and Equation 2.6 are always positive. Therefore, they are omitted from the analysis as they have no effect on the sign of  $\operatorname{Re}\{Y_t\}$  and  $\operatorname{Im}\{Y_t\}$ . We define

$$C_x \triangleq C_{ext} + C_{par} + \frac{C_{tune}}{2}, \qquad (2.7)$$

where  $C_{ext}$  is the external capacitor placed across the Crystal (XTAL), and  $C_{par}$  is the equivalent parasitic capacitor across the crystal I/O pins, *e.g.*, including the XO buffer input capacitance<sup>3</sup>.  $C_{tune}/2$  is the series combination of on-chip tuning capacitors.

<sup>&</sup>lt;sup>3</sup>It is important to note that active inductor and cross-coupled pair capacitances are already accounted for in Equation 2.3 and Equation 2.4, respectively.



Figure 2.15: Small signal model of differential crystal oscillator for parallel resonance region

# **2.7.2** Crystal Oscillator Small Signal Analysis for $\omega_{r_s} < \omega < \omega_{r_p}$

The equivalent small signal model for  $\omega_{r_s} < \omega < \omega_{r_p}$  (*i.e.*, parallel-resonance mode) is shown in Figure 2.15. First, we obtain the real part of the crystal oscillator total impedance,

 $Y_t$ , for  $\omega_{r_s} < \omega < \omega_{r_p}$ . This is defined as

$$\operatorname{Re}\{Y_{t}\}(\omega)|_{\omega_{r_{s}}<\omega<\omega_{r_{p}}} = \operatorname{Re}\{Y_{xtal}\}|_{\omega_{r_{s}}<\omega<\omega_{r_{p}}} + \operatorname{Re}\{Y_{cc}+Y_{L_{a}}\}$$
(2.8)

Using Figure 2.12,  $Y_{xtal}$  in parallel resonance mode is given by

$$Y_{xtal}(\omega)|_{\omega_{r_s} < \omega < \omega_{r_p}} = \frac{1}{R_e + j\omega L_e}$$
(2.9)

In order to obtain Re{ $Y_{xtal}$ }, a series-to-parallel transformation is needed to obtain the equivalent parallel resistance,  $R_p^4$ . The equivalent parallel resistance,  $R_p$ , is given by

$$R_p = Q^2 R_e$$
$$= \frac{\omega^2 L_e^2}{R_e}.$$
(2.10)

Using the fact that  $L_e = 1/(\omega^2 C_L)$  at resonance,

$$R_p = \frac{1}{\omega^2 R_e C_L^2}.$$
(2.11)

Since  $R_e$  is related to  $R_1$  by

$$R_e = R_1 \left( 1 + \frac{C_0}{C_L} \right)^2,$$
 (2.12)

<sup>&</sup>lt;sup>4</sup>This is because  $\operatorname{Re}\{Y_{xtal}\}$  is  $1/R_p$ .

we obtain

$$R_p = \frac{1}{\omega^2 R_1 \left( C_0 + C_L \right)^2}.$$
 (2.13)

Therefore, we obtain the first term in Equation 2.8, *i.e.*,  $\text{Re}\{Y_{xtal}\}$  as  $1/R_p$  given by

$$\operatorname{Re}\{Y_t\}(\boldsymbol{\omega})|_{\boldsymbol{\omega}_{r_s}<\boldsymbol{\omega}<\boldsymbol{\omega}_{r_p}}=\boldsymbol{\omega}^2 R_1 \left(C_0+C_L\right)^2. \tag{2.14}$$

Secondly, we obtain the remaining two terms in Equation 2.8, *i.e.*,

$$\operatorname{Re}\{Y_{cc}+Y_{L_{a}}\}(\boldsymbol{\omega}) = \frac{1}{2\boldsymbol{\omega}_{T_{p}}\left(\boldsymbol{\omega}^{2}+\boldsymbol{\omega}_{z}^{2}\right)} \times \left[\left(g_{m_{p}}\boldsymbol{\omega}_{z}-g_{m_{n}}\boldsymbol{\omega}_{T_{p}}\right)\boldsymbol{\omega}^{2}+g_{m_{p}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{z}^{2}-g_{m_{n}}\boldsymbol{\omega}_{T_{p}}\boldsymbol{\omega}_{z}^{2}\right]. \quad (2.15)$$

Now that the real part of the total admittance is obtained, we look at the imaginary part of  $Y_t$  which, using Figure 2.15, is

$$Im\{Y_t\}|_{\omega_{rs} < \omega < \omega_{rp}} =$$

$$Im\{Y_{xtal}\}|_{\omega_{rs} < \omega < \omega_{rp}}$$

$$+ Im\{Y_{cc} + Y_{La} + Y_{C_x}\}.$$
(2.16)

The imaginary part of crystal admittance is simply given by

$$\operatorname{Im}\{Y_{xtal}\}|_{\omega_{r_s} < \omega < \omega_{r_p}} = (L_e)^{-1}.$$
(2.17)

However, since the crystal manufacturers already specify an equivalent parallel capacitance

that ensures a parallel-mode resonance (*i.e.*,  $C_L$ ), the crystal equivalent inductance,  $L_e$ , has little significance in our analysis.

Similar to the approach for  $\operatorname{Re}\{Y_t\}$ , we obtain the imaginary part the cross-coupled pair and active inductor admittance. Using the small signal model of Figure 2.15, we obtain

$$\operatorname{Im}\{Y_{cc} + Y_{L_a} + Y_{C_x}\}(\omega) =$$

$$\frac{g_{m_p}\omega}{2\omega_{T_p}\left(1 + \frac{\omega^2}{\omega_z^2}\right)}$$

$$+ \frac{g_{m_n}\omega}{2\omega_{T_n}} - \frac{g_{m_p}\omega}{2\omega_z\left(\frac{\omega^2}{\omega_z^2} + 1\right)}$$

$$+ \omega C_x. \qquad (2.19)$$

Before we provide a set of design considerations, two conditions need to be satisfied: 1)  $Im\{Y_{cc} + Y_{L_a} + Y_{C_x}\}$  should yield a capacitive admittance equal to the admittance of  $C_L$ at resonance to result in oscillation, and 2) the chosen design parameters must lead to a positive value for  $C_{ext}$  since this is a physical capacitor placed across the crystal. That is,  $Im\{Y_{cc} + Y_{L_a} + Y_{C_x} - Y_{C_{ext}}\} < Y_{C_L}$ . Using Equation 2.18, Equation 2.7, and simplifying, we get

$$\frac{g_{m_p}}{2} \frac{\frac{1}{\omega_{T_p}} - \frac{1}{\omega_z}}{1 + \frac{\omega^2}{\omega_z^2}} + \frac{g_{m_n}}{2\omega_{T_n}} + (C_x - C_{ext}) - C_L < 0.$$
(2.20)

Expanding the terms, we obtain

$$\frac{1}{2\omega_{T_n} \left(\omega^2 + \omega_z^2\right)} \times \\ -\omega_z^2 \left[-g_{m_p} \omega_{T_n} - g_{m_n} \omega_{T_p} + 2\omega_{T_n} \omega_{T_p} \left(C_L - \left(C_x - C_{ext}\right)\right)\right] \\ -\omega_z \left(g_{m_p} \omega_{T_n} \omega_{T_p}\right) \\ + g_{m_n} \omega^2 \omega_{T_p} - 2\omega^2 \omega_{T_p} \omega_{T_n} \left(C_L - \left(C_x - C_{ext}\right)\right) < 0. \quad (2.21)$$

The inequality in Equation 2.21 is a second order polynomial of  $\omega_z$ . In order to satisfy the inequality, we ensure that there are no real solutions that can violate the inequality. We let

$$a = -g_{m_p}\omega_{T_n} - g_{m_n}\omega_{T_p} + 2\omega_{T_n}\omega_{T_p} \left(C_L - \left(C_x - C_{ext}\right)\right), \qquad (2.22)$$

$$b = g_{m_p} \omega_{T_n} \omega_{T_p}, \qquad (2.23)$$

and

$$c = -g_{m_n}\omega^2\omega_{T_p} + 2\omega^2\omega_{T_p}\omega_{T_n}(C_L - (C_x - C_{ext})); \qquad (2.24)$$

and ensure that a > 0, and  $b^2 - 4ac < 0$ , to satisfy Equation 2.21. This derivation is presented below:

Using Equation 2.22, for a > 0, we have

$$2\left(C_L - \left(C_x - C_{ext}\right)\right) > \frac{g_{m_p}}{\omega_{T_p}} + \frac{g_{m_n}}{\omega_{T_n}}$$

$$(2.25)$$

Since  $g_{m_p}/\omega_{T_p} = C_{gg_p}$ , and  $g_{m_n}/\omega_{T_n} = C_{gg_n}$ , we obtain

$$2(C_L - (C_x - C_{ext})) > C_{gg_p} + C_{gg_n}$$
(2.26)

This condition is easily satisfied since  $C_L$  is large (e.g., 20pF).

Using Equation 2.23, and Equation 2.24, we want  $b^2 - 4ac < 0$ , that is

$$b^{2} - 4ac =$$

$$g_{m_{p}}^{2} \omega_{T_{n}}^{2} \omega_{T_{p}}^{2}$$

$$-4 \left[ -g_{m_{p}} \omega_{T_{n}} - g_{m_{n}} \omega_{T_{p}} \right]$$

$$+ 2\omega_{T_{p}} \omega_{T_{n}} \left( C_{L} - (C_{x} - C_{ext}) \right) \right]$$

$$\left[ -g_{m_{n}} \omega^{2} \omega_{T_{p}} \right]$$

$$+ 2\omega^{2} \omega_{T_{n}} \omega_{T_{p}} \left( C_{L} - (C_{x} - C_{ext}) \right) \right] < 0. \qquad (2.27)$$

Multiplying out the terms in Equation 2.27,

$$g_{m_{p}}^{2}\omega_{T_{n}}^{2}\omega_{T_{p}}^{2} - 4g_{m_{p}}g_{m_{n}}\omega^{2}\omega_{T_{p}} - 4g_{m_{n}}^{2}\omega^{2}\omega_{T_{p}}^{2}$$

$$+ 8g_{m_{n}}\omega^{2}\omega_{T_{p}}^{2}\omega_{T_{n}}(C_{L} - (C_{x} - C_{ext}))$$

$$+ 8g_{m_{p}}\omega^{2}\omega_{T_{n}}^{2}\omega_{T_{p}}(C_{L} - (C_{x} - C_{ext}))$$

$$+ 8g_{m_{n}}\omega^{2}\omega_{T_{p}}^{2}\omega_{T_{n}}(C_{L} - (C_{x} - C_{ext}))$$

$$- 16\omega^{2}\omega_{T_{n}}^{2}\omega_{T_{p}}^{2}(C_{L} - (C_{x} - C_{ext}))^{2} < 0. \quad (2.28)$$

After cancellations, we obtain

$$g_{m_p}^{2} + (16\omega^{2}C_{gg_{n}} + 8\omega^{2}C_{gg_{p}})(C_{L} - (C_{x} - C_{ext}))$$

$$< 16\omega^{2}(C_{L} - (C_{x} - C_{ext}))^{2}$$

$$+ 4\omega^{2}C_{gg_{n}}C_{gg_{p}} + 4\omega^{2}C_{gg_{n}}^{2}. \quad (2.29)$$

#### 2.7.3 Low Frequency Design Considerations

At low frequencies, (*i.e.*,  $\omega \ll \omega_{r_s}$ ) we must choose the design parameters to avoid a parasitic oscillation. With an incorrect set of design parameters, the active inductor in parallel with  $C_0$  can form an *LC* tank. The combination of this *LC* tank and the negative resistance of the cross-coupled pair can result in an undesired oscillation.

A sufficient condition to avoid a parasitic oscillation is to choose the design parameters such that  $\text{Im}\{Y_t\} \neq 0$  for  $\omega \ll \omega_{r_s}$ . Nevertheless, even if  $\text{Im}\{Y_t\}$  is equal to 0 at a certain frequency, parasitic oscillation is still avoided if we ensure that  $\text{Re}\{Y_t\} > 0$  for that frequency (*i.e.*, avoid parasitic oscillation by depriving the circuit of the necessary loop gain).

If we let  $\text{Im}\{Y_t\}$  in Equation 2.5 equal to zero, three solutions for  $\omega$  are obtained. Firstly, at  $\omega = 0$  (*i.e.*, DC),  $\text{Im}\{Y_t\}$  becomes zero. Therefore,  $\text{Re}\{Y_t\}$  must be made positive (*i.e.*, resistive to avoid loop gain) to prevent latch-up. Using Equation 2.6 and simplifying,

$$@ \omega = 0, \quad \operatorname{Re}\{Y_t\} > 0 \Rightarrow \boxed{g_{m_p} > g_{m_n}}$$

$$(2.30)$$

This makes intuitive sense as the positive resistance of the active inductor should dominate over the negative resistance of the cross-coupled pair to result in a low loop gain at DC to

prevent latch-up.

Secondly, we consider the  $\omega^2$  coefficient in Equation 2.5. We select the design parameters such that there is no real frequency which can result in Im $\{Y_t\}$  equal to zero. Therefore, it is ensured that,

$$\omega^{2} = \frac{\omega_{z}}{\omega_{T_{p}}} \frac{-1}{g_{m_{n}} + 2\omega_{T_{n}} (C_{0} + C_{x})} \left[ g_{m_{p}} \omega_{T_{n}} \omega_{z} - g_{m_{p}} \omega_{T_{p}} \omega_{T_{n}} + g_{m_{n}} \omega_{T_{p}} \omega_{z} + 2\omega_{T_{p}} \omega_{T_{n}} \omega_{z} (C_{0} + C_{x}) \right], \qquad (2.31)$$

is always negative to prevent parasitic oscillation. This yields the following inequality:

$$g_{m_p}\omega_{T_n}\omega_z - g_{m_p}\omega_{T_p}\omega_{T_n} + g_{m_n}\omega_{T_p}\omega_z + 2\omega_{T_p}\omega_{T_n}\omega_z (C_0 + C_x) > 0.$$
(2.32)

Rearranging, we obtain

$$g_{m_p}\omega_{T_n}\omega_z + 2\omega_{T_p}\omega_{T_n}\omega_z (C_0 + C_x) > g_{m_p}\omega_{T_p}\omega_{T_n} - g_{m_n}\omega_{T_p}\omega_z$$
(2.33)

Assuming  $g_{m_p}\omega_{T_n} \gg g_{m_n}\omega_z$ , and some factoring, we obtain

$$\omega_{z} > \frac{g_{m_{p}}}{C_{gg_{p}} + 2(C_{0} + C_{x})}.$$
(2.34)

It is interesting to note that Equation 2.34 depends on the active inductor parameters. Therefore, we need to choose the active inductor PMOS transistor size and the active inductor resistance,  $R_{L_a}$ , judiciously to avoid a parasitic oscillation.

#### 2.7.4 Parallel Resonance Mode Design Considerations

In the parallel-resonance mode, we need to ensure that  $\operatorname{Re}\{Y_t\} \ll 0$  for oscillation startup. In order to simplify Equation 2.15, we assume that the active inductor zero frequency,  $\omega_z$ , is much smaller than the PMOS transit frequency,  $\omega_{T_p}$  (*i.e.*, ,  $\omega_z \ll \omega_{T_p}$ ). At resonance (*i.e.*,  $\omega = \omega_{xo}$ ), we obtain

$$\operatorname{Re}\{Y_{cc}+Y_{L_a}\}(\boldsymbol{\omega}=\boldsymbol{\omega}_{xo})\approx\frac{-g_{m_n}}{2}\cdot\frac{\boldsymbol{\omega}_{xo}^2}{\boldsymbol{\omega}_z^2+\boldsymbol{\omega}_{xo}^2}.$$
(2.35)

If we choose the design parameters such that  $\omega_{xo} \gg \omega_z$ , we obtain

$$\operatorname{Re}\{Y_{cc}+Y_{L_a}\}(\boldsymbol{\omega}=\boldsymbol{\omega}_{xo})\approx\frac{-g_{m_n}}{2}.$$
(2.36)

It is important to note that it is indeed desirable to set  $\omega_{xo} \gg \omega_z$ . This is to avoid loading the crystal with the active inductor circuit at resonance. Essentially,  $\omega_{xo} \gg \omega_z$ , means that the active inductor impedance is large at resonance. Using Equation 2.14 and Equation 2.36, we obtain a start-up condition (Re{ $Y_t$ }  $\ll 0$ ) at resonance which is

$$\frac{-g_{m_n}}{2} + \omega_{xo}^2 R_1 \left( C_0 + C_L \right)^2 \ll 0, \qquad (2.37)$$

which results in

$$\left| g_{m_n} \cdot \frac{1}{2\omega_{x_0}^2 R_1 \left( C_0 + C_L \right)^2} \gg 1 \right|,$$
 (2.38)

which is, in an essence,  $G_m R_P \gg 1$ .

Since  $Y_{xtal}$  is inductive in this region, we need to choose the design parameters (such as

 $g_{m_n}$ ,  $g_{m_p}$ , and  $R_{L_a}$ ) such that the combined admittance presented to the crystal is positive (*i.e.*, capacitive) in the parallel resonance regime. The admittance should precisely be equal to the admittance of  $C_L$  to result in oscillation at the desired frequency. Using Equation 2.29, we make the following assumptions to formulate a set of design equations to satisfy Equation 2.21. We assume that

$$4(C_L - (C_x - C_{ext}))^2 \gg C_{gg_n} C_{gg_p} + C_{gg_n}^2.$$
(2.39)

This is a reasonable assumption, since  $C_L$  is often much larger than the NMOS and PMOS gate capacitances. Using this assumption, Equation 2.29 simplifies to

$$\frac{g_{m_p}^2}{\omega^2 \left(C_L - (C_x - C_{ext})\right)} + 16C_{gg_n} + 8C_{gg_p} < 16\left(C_L - (C_x - C_{ext})\right).$$
(2.40)

In order to make (2.40) more tractable, we make the following design choice. If we ensure that,

$$8\left(\frac{\omega_{xo}}{\omega_{T_p}}\right)^2 \gg \frac{C_{gg_p}}{C_L - (C_x - C_{ext})},\tag{2.41}$$

a simple design condition is achieved. That is

$$C_L - (C_x - C_{ext}) > C_{gg_p} + C_{gg_n},$$
 (2.42)

yields a positive external capacitor for parallel region oscillation.

#### 2.7.5 Duty Cycle Correction Analysis

The new duty cycle correction scheme used in the frequency quadrupler is shown in Figure 2.16. The new DCC circuit ensures the generation of the 25% duty cycle 1X clocks so that when these are combined, the duty cycle of the 96MHz, 2X clock is 50%. A non-50% duty cycle 2X clock will result in unwanted spurs in the 4X clock. If the duty cycle of the input to an XOR plus delay-based frequency doubler in non-50%, the output of the frequency doubler will have large unwanted spurs. And, if the quadrupler is used as a PLL reference, these spurs can then degrade, often severely, the synthesizer integrated phase noise. Therefore, the duty cycle of the 2X clock must be tightly controlled.

We will now outline the small signal analysis of the DCC. In order to obtain the loop gain, the DCC loop is broken at the error amplifier output. The transfer function from the break point all the way to the return point is then calculated. This transfer function is indeed the loop gain.

We need to know how the DCC control voltage,  $v_c$ , affects the 2X clock duty cycle. This derivation requires a few steps. First, it is required to obtain a relationship between the skewed inverter switching point,  $t_{sw}^5$ , and the DCC control voltage,  $v_c^6$ , *i.e.*,  $\frac{\delta t_{sw}}{\delta v_c}$ . This relationship is written as

$$\frac{\delta t_{sw}}{\delta v_c} = \frac{\delta t_{sw}}{\delta v_{in}} \times \frac{\delta v_{in}}{\delta v_c}.$$
(2.43)

<sup>&</sup>lt;sup>5</sup>Defined as the time when the skewed inverter output is equal to  $V_{DD}/2$ .

<sup>&</sup>lt;sup>6</sup>Since the inputs to the skewed inverters are differential and the 25% duty cycle clocks are a dual of one another, it is sufficient to analyze the behavior of one skewed inverter and apply the results throughout the analysis.



Figure 2.16: The duty cycle correction scheme used in the frequency quadrupler

The changes in the 1X, 25% duty cycle clock,  $\delta_{DC_{1X}}$ , can then be readily obtained as

$$\frac{\delta_{DC_{1X}}}{\delta v_c} = -2\frac{\delta t_{sw}}{\delta v_c} \times \frac{1}{T_{xo}},\tag{2.44}$$

where  $T_{xo}$  is the XO period. The factor of 2 multiplier accounts for the fact that since both the rising and falling edges move with respect to changes in  $v_c$ , the resulting change in 1X duty cycle is doubled. The negative sign is due to the inverter operation.

We assume a sinusoidal waveform for the XO given by  $v_{XO}(t) = A_{XO} \sin(\omega_{XO}t)$ , where  $A_{XO}$  is the XO amplitude, and  $\omega_{XO}$  is the XO frequency. Using the XO sinusoidal waveform equation,

$$\frac{\delta v_{XO}}{\delta t} = A \omega_{XO} \cos(\omega_{XO} t).$$
(2.45)

For  $t = t_{sw}$ ,  $v_{XO} = v_{in}$ , and using Equation 2.45 we obtain

$$\frac{\delta t_{sw}}{\delta v_{in}} = \frac{1}{A\omega_{XO}\cos\left(\omega_{XO}t_{sw}\right)}.$$
(2.46)

We now obtain the second term in Equation 2.43, *i.e.*,  $\frac{\delta v_{in}}{\delta v_c}$ .  $\frac{\delta v_{in}}{\delta v_c}$  is obtained in two steps: First, the skewed inverter small signal output current change with respect to changes in DCC control voltage,  $v_c$ , is obtained. Second, the skewed inverter small signal output current change with respect to input voltage,  $v_{in}$ , is obtained. That is,

$$\frac{\delta v_{in}}{\delta v_c} = \frac{\frac{\delta I_d}{\delta v_c}\Big|_{v_{in}=0}}{\frac{\delta I_d}{\delta v_{in}}\Big|_{v_c=0}},$$
(2.47)

where

$$\left. \frac{\delta I_d}{\delta v_c} \right|_{v_{in}=0} = g_{m_c} \frac{g_{m_n}}{g_{m_n} + \frac{1}{r_{o_c}}},\tag{2.48}$$

and

$$\frac{\delta I_d}{\delta v_{in}}\Big|_{v_c=0} = g_{m_p} + \frac{g_{m_n}}{1 + g_{m_n} r_{o_c}}.$$
(2.49)

Parameters  $g_{m_p}$ ,  $g_{m_n}$ ,  $g_{m_c}$ , and  $r_{o_c}$  are the trans-conductance of skewed inverter PMOS, trans-conductance of skewed inverter NMOS, trans-conductance of skewed inverter bottom current control NMOS, and output resistance of skewed inverter bottom current control NMOS transistors, respectively. Therefore,

$$\frac{\delta v_{in}}{\delta v_c} = \frac{g_{m_c} \frac{g_{m_n}}{g_{m_n} + \frac{1}{r_{oc}}}}{g_{m_p} + \frac{g_{m_n}}{1 + g_{m_n} r_{oc}}}.$$
(2.50)

Using Equations 2.43, 2.44, 2.46, and 2.50. For a 25% duty cycle switching point (*i.e.*,  $t_{sw} = T_{XO}/8$ ),

$$\frac{\delta_{DC_{1X}}}{\delta v_c} = \frac{-\sqrt{2}}{A\pi} \frac{g_{m_c} \frac{sm_n}{g_{m_n} + \frac{1}{r_{o_c}}}}{g_{m_p} + \frac{g_{m_n}}{1 + g_{m_n} r_{o_c}}}.$$
(2.51)

Equation 2.51 establishes the relationship between the duty cycle of 1X clock ( $DC_{1X}$ ) and the DCC control voltage,  $v_c$ .

Since the pair of 25% duty cycle 1X clocks are XORed to form a 50% duty cycle clock at twice the frequency (*i.e.*, the 2X clock), we need another factor of 2 multiplier to obtain the changes in the duty cycle of 2X clock. Therefore,

$$\frac{\delta_{DC_{2X}}}{\delta v_c} = 2 \frac{\delta_{DC_{1X}}}{\delta v_c}.$$
(2.52)

Now that we have established the relationship between the duty cycle of 2X clock ( $DC_{2X}$ ) and the DCC control voltage,  $v_c$ , we continue the loop gain transfer function calculation from the output of the XOR gate. Using Figure 2.16, the average (DC) of the 2X clock,  $v_p$ , is obtained as

$$v_p(\omega) = DC_{2X} \cdot \frac{V_{DD}}{1 + j\omega RC},$$
(2.53)

where *RC* is the time constant of the averaging low pass filter. Similarly, the average (DC) of the  $\overline{2X}$  clock,  $v_n$ , is obtained as

$$v_n(\boldsymbol{\omega}) = -DC_{2X} \cdot \frac{V_{DD}}{1 + j\boldsymbol{\omega}RC}.$$
(2.54)

The OTA output voltage,  $V_{out_{OTA}}$ , is then obtained as

$$V_{out_{ota}}(\boldsymbol{\omega}) = 2 \cdot DC_{2X} \cdot \frac{V_{DD}}{1 + j\boldsymbol{\omega}RC} \cdot A_{OTA}, \qquad (2.55)$$

where  $A_{OTA}$  is the voltage gain of the OTA<sup>7</sup>.

Using equations 2.51, 2.52, and 2.55, we obtain the DCC loop gain as

$$\left| LG_{DCC}(\omega) \frac{-4\sqrt{2}}{A_{XO}\pi} \cdot \frac{g_{m_c} \frac{g_{m_n}}{g_{m_n} + \frac{1}{r_{o_c}}}}{g_{m_p} + \frac{g_{m_n}}{1 + g_{m_n}r_{o_c}}} \frac{V_{DD}}{1 + j\omega RC} \cdot A_{OTA}. \right|$$
(2.56)

<sup>&</sup>lt;sup>7</sup>Since the dominant pole of the DCC feedback loop is set by the averaging low pass filters in the kHz range, (*i.e.*, much lower than the OTA bandwidth) we ignore the frequency response of the OTA for loop gain analysis.

# **CHAPTER III**

# A Low Voltage Sub 300µW 2.5GHz Current Reuse VCO

## 3.1 Introduction

Low supply voltages due to process scaling are an impediment to reducing the VCO power consumption, because they limit the choice of VCO topologies to those that do not have a high DC to RF conversion efficiency. VCO topologies such as CMOS current reuse and cross coupled CMOS have excellent DC to RF efficiencies, often a factor of two better than NMOS or PMOS only VCOs [30]. However, the standard implementation of such VCOs, where a PMOS transistor is stacked on top of an NMOS transistor, requires a supply voltage larger than the sum of the threshold voltages of the two transistors,  $V_{th_n} + V_{th_p}$ . In order to have reliable operation over PVT, the minimum supply voltage is more than this sum and can be as high as 1.1V in a 65nm digital CMOS process. In addition, VCOs are highly sensitive to supply noise, pushing, and pulling, and therefore a regulated voltage is always required. This further lowers the available internal voltage supply for VCOs and makes the use of CMOS VCOs operating from a low supply even more difficult.

In recent years, researchers have reported a number of VCOs using AC coupling capaci-



Figure 3.1: The proposed AC coupled current reuse VCO

tors to achieve better phase noise and higher FoM by operating the transistors in class C regime. However, low start up gain restricts the VCO topology to NMOS or PMOS only for low voltage operation [31], or else the penalty of a high supply voltage if the more efficient CMOS topology is used [32].

This work offers a simple technique to enable CMOS current reuse VCOs to operate at very low supply voltages by adding an AC coupling capacitor to achieve good phase noise at low power consumption. Introduced in [33], a 1.25V two-transistor current reuse VCO uses a PMOS and an NMOS transistor to provide negative resistance to sustain oscillation in an LC tank. Figure 3.1 shows the proposed current reuse VCO which operates with a supply voltage as low as 0.6V, which is much lower than the sum of NMOS and PMOS threshold voltages. In steady state, the operation of the VCO can be divided into two parts during each cycle: in the first half cycle, both MN and MP are on, injecting energy into the *LC* tank; and in the second half cycle, both transistors are off, and energy is dissipated through the loss of

the tank.

In the modified current reuse VCO, the voltage at node *P* is AC coupled to gate of MN (node *P'*) through capacitor  $C_C$ . A separate DC bias is applied to the gate of MN through resistor  $R_{bias}$  to independently set its gm to ensure start up at lower supply voltages. This enables both MN and MP to operate in saturation even at supply voltages as low as 0.6V and still provide the needed start up gain. This in turn reduces the power consumption while enabling low phase noise operation.

#### **3.2 Design Methodology**

The focus of this design is to minimize power consumption while meeting the phase noise requirement for a desired application at a very low voltage supply. A large inductance is desired to achieve a very low power VCO. However, the inductance cannot be arbitrarily increased as VCO phase noise is limited by kT/C and Q, where C is the total tank capacitance, and Q the quality factor of the VCO tank. For a fixed oscillation frequency and constant Q, as inductance is increased, total tank capacitance C is reduced, therefore increasing kT/C and degrading the phase noise. The tank quality factor of the VCO shown in Figure 3.2 is given by  $Q_{tank} = R_p \sqrt{\frac{C}{L}}$ , where it is dominated by the inductance L and its equivalent parallel resistance  $R_p$ . The power consumption of an LC VCO is directly proportional to  $R_p$ .

In a conventional current reuse VCO [33], meeting the startup condition over PVT for a supply voltage lower than 1V is difficult. An AC coupling capacitor,  $C_C$ , enables the VCO to work at much lower supply voltages because  $g_{m_n}$  can be independently adjusted to meet



Figure 3.2: Small signal model of the proposed AC coupled VCO

the startup condition in Equation 3.1 by increasing the bias voltage  $V_{bias}$ . In order to operate the VCO at the lowest voltage supply, the start up gain needs to be maximized by choosing large values for  $C_C$  and  $R_{bias}$ . This is explained by looking at the impedance  $Z_P$  at node P at resonance using the small signal model in Figure 3.2. Impedance  $Z_P$  should be negative to ensure start up so that

$$Z_P = \left(\frac{1}{R'_{bias}} + |\alpha|g_{m_n} + g_{m_p} - |\alpha|g_{m_n}g_{m_p}R_P\right)^{-1} < 0,$$
(3.1)

where  $g_{m_n}$  and  $g_{m_p}$  are the trans-conductances of MN and MP,  $R'_{bias}$  the equivalent resistance seen at node P due to  $R_{bias}$ , and  $\alpha = v'_p/v_p$  is the voltage divider ratio between nodes P and P'. It is important to choose the optimum values for  $C_C$  and  $R_{bias}$  to have sufficient start up gain. In an ideal case  $v'_p/v_p$  must be close to one. As suggested by Figure 3.2,  $C_C$  should be bigger than  $C_{gs}$  (capacitance at node P') by a large factor so to maximize the transfer function

as

$$\frac{v'_p}{v_p} = |\alpha| = \left(1 + \beta + \frac{1}{sR_{bias}C_C}\right)^{-1},\tag{3.2}$$

where  $\beta = C_{gs}/C_C$ . Using Equation 3.2, a lower bound for bias resistance  $R_{bias}$  is derived

$$R_{bias} \ge \frac{1}{\omega C_C} \left( \frac{|\alpha|}{\sqrt{1 - |\alpha|^2 (1 + \beta)^2}} \right).$$
(3.3)

In addition,  $R_{bias}$  should be large to avoid degrading the tank quality factor by reducing the impedance at node *P*. Using Figure 3.2,  $R'_{bias}$  at resonance is given by

$$R'_{bias} = \left(\frac{1+Q^2}{Q^2}\beta^2 + 2\beta + 1\right)R_{bias},\tag{3.4}$$

where  $Q = R_{bias}C_{gs}\omega$  is the quality factor of parallel combination of  $C_{gs}$  and  $R_{bias}$ . For  $\beta \ll 1$  ( $C_{gs} \ll C_C$ ), we can assume that  $R'_{bias} \approx R_{bias}$ . To avoid degrading the tank Q by more than 10%,  $R'_{bias}$  should be approximately 10 times larger than  $R_P$ . This is a conservative approximation because it only considers the inductor parallel resistance  $R_p$  and not the loading effect of MN, MP, and the capacitor bank. Therefore,  $R_{bias} \approx 10 \cdot R_p$  is more than enough to avoid significant Q degradation.

### 3.3 Practical Design Considerations

The prototype VCO, implemented in 65nm CMOS, uses a compact 5 turn 8nH inductor with a quality factor of 11. This results in an equivalent parallel tank resistance  $R_P \approx 1.4k\Omega$ .

Considerably higher Q values can be obtained at the cost of larger inductor area, which will further improve the phase noise and lower the power consumption.

Transistors MN (4.8 $\mu$ m/80nm) and MP (18 $\mu$ m/80nm) are sized so to meet the startup condition in Equation 3.1 for a voltage supply as low as 0.6V. Flicker noise upconversion is reduced by avoiding the use of minimum length transistors. Using longer transistors also improves the VCO loaded Q and reduces the noise contribution of MN and MP by reducing their effective  $g_{ds}$  [30]. An AC coupling capacitor  $C_C$ =250fF ( $\beta \approx 0.02$ ) is used, which is large enough to result in a voltage divide ratio  $|\alpha| \approx 0.96$  from Equation 3.2. From Equation 3.3, a resistor bias value  $R_{bias} \ge 1.4k\Omega$  is sufficient for start up; and according to Equation 3.4,  $R_{bias} \approx 10 \cdot R_P = 14k\Omega$  for minimum Q degradation of the tank. The analysis to optimize the start up gain and minimize the tank Q degradation, leads to  $R_{bias}$  values ranging from 1.4k $\Omega$  to 14k $\Omega$ . However, the thermal noise of  $R_{bias}$  is also important. Considering sufficient start up gain, minimal Q degradation, and the thermal noise contribution of  $R_{bias}$ , an optimum value of 5k $\Omega$  is chosen.

### **3.4** Implementation and Measurement

The prototype VCO (Figure 3.3) is implemented in a 1P9M 65nm digital CMOS process and occupies a core area of 0.13mm<sup>2</sup>. The inductor is formed with thick metal 9 and tuning is achieved with a 5 bit bank of MIM capacitors. The varactor is formed with an N type MOS capacitor biased at 0.55V for all measurements. The simulated VCO gain is approximately 45MHz/V. The device is packaged in a 40 pin 6×6 QFN package. Phase noise is measured using an Agilent E5052B source analyzer, and current is sensed with a Keithley 2400 source



Figure 3.3: Chip photo of AC coupled VCO

meter.

The measured tuning range is 2.17GHz to 2.9GHz and the VCO operates with supply voltage as low as 0.6V. Figure 3.4 shows the measured phase noise and power consumption at 2.53GHz for different supply voltages. With a 0.7V supply, the measured VCO phase noise at a 3MHz offset is -122.6dBc/Hz with a power consumption of  $185\mu$ W. For a 0.85V supply, phase noise is improved to -126.1dBc/Hz with a  $288\mu$ W power consumption. For applications requiring better performance, a phase noise of -130.1dBc/Hz is achieved by increasing the supply to 1.3V with a 0.9mW power consumption.


Figure 3.4: Measured VCO phase noise and power consumption at 2.53GHz for different supply voltages

The oscillator Figure of Merit (FoM) and FoMT defined as

FoM = 
$$20\log\left(\frac{f_0}{\Delta f}\right) - 10\log(P) - \mathscr{L}\{\Delta f\}$$
 (3.5)

and

$$FoMT = FoM + 20\log\left(\frac{F_T}{10}\right)$$
(3.6)

where

$$F_T = 2\frac{F_{max} - F_{min}}{F_{max} + F_{min}} \tag{3.7}$$

are used to characterize the VCO at a frequency  $f_0$ , where  $\mathscr{L}{\Delta f}$  is the phase noise at  $\Delta f$  offset, and P, the power consumption in mW. Figure 3.5 shows the FoM associated with phase noise measurements in Figure 3.4. The VCO FoM is 188.5dB for supply voltage of 0.7V. At 0.85V, FoM is 190.2dB with phase noise of -126.1dBc/Hz at 3MHz consuming 280 $\mu$ W. This is the highest FoM reported for a current reuse VCO with power consumption below  $300\mu$ W<sup>1</sup>.

An instrument screen shot of phase noise measurement for the peak FoM is shown in Figure 3.6.

Figure 3.7 shows the measured phase noise at 2.53GHz with a 0.7V supply at -30, 25 and 120°C. At 3MHz offset, worst phase noise is -120dBc/Hz at 120°C with FoM of 185dB. Phase noise variation across temperature is 2.2dB.

Figure 3.8 shows the variation in phase noise for different  $V_{bias}$  values (MN gate bias) along with the corresponding power consumption. The best phase noise power tradeoff is

<sup>&</sup>lt;sup>1</sup>As of the date of publication in [23].



Figure 3.5: Measured VCO FoM at 2.53GHz and power consumption for different supply voltages



Figure 3.6: Instrument screen shot of phase noise measurement with a 0.85V supply



Figure 3.7: Measured phase noise at 2.53GHz over temperature



Figure 3.8: Measured phase noise at 2.53GHz versus NMOS gate bias voltage with a 0.85V supply

obtained with  $V_{bias}$  set to 0.5V. Increasing  $V_{bias}$  beyond a certain point degrades the phase noise while increasing the power consumption as MN enters the triode region.

Table 3.1 summarizes the performance of the prototype VCO with comparison to some recent low power counterparts. At 0.85V, the proposed AC coupled current reuse VCO achieves a phase noise of -126.1dBc/Hz at 3MHz offset for an oscillation frequency 2.53GHz and consumes  $280\mu$ W. This corresponds to a FoM of 190.2dB which is comparable to the state of the art. Considering the 2.17GHz to 2.9GHz (29%) tuning range, the Figure of Merit with Tuning (FoMT) is 199.4dB, which is the highest, reported for any current reuse VCO<sup>2</sup>.

 $<sup>^{2}</sup>$ As of the date of publication in [23].

ruble bill v e e performance comparison							
Parameter	This	CICC '11	CICC '11	ISSCC '12	LMWC '11	LMWC '09	ISSCC '05
	Work	[34]	[35]	[32]	[31]	[36]	[33]
Freq. (GHz)	2.53	1.6	5.6	3.92 (7.84/2)	3.1	3	1.97
F <sub>T</sub> (%)	29	26	4	33	20	21	-
PN (dBc/Hz)	-126.1	-130	-132.3	-132.5	-121	-131	-125
at 3MHz							
$V_{DD}(V)$	0.85	1	0.6	1.5	1	1.5	1.25
Power (mW)	0.28	2.6	4.2	6	0.56	1.7	1
FoM (dB)	190.2	180.4	191.5	185.6	183.9	188.7	181.3
FoMT (dB)	199.4	188.7	183.5	195.9	189.8	195.2	-
Area (mm <sup>2</sup> )	0.13	-	0.48	0.49	0.77	0.3	-
					(w/ pads)	(w/ pads)	
Tech.	65nm	65nm	0.13µm	55nm	0.18µm	0.18µm	0.18µm
Topology	CMOS	NMOS	NMOS	N/PMOS	PMOS	CMOS	CMOS
	AC coupled	QVCO	QVCO w/	combined for	Class C	Current	Current
	current reuse		cap coupling	constant FoM	w/ startup cct	reuse	reuse

Table 3.1: VCO performance comparison

# **CHAPTER IV**

# A 2.4GHz 2Mb/s Digital PLL-based Transmitter for 802.15.4 in 130nm CMOS

#### 4.1 Background

The IEEE 802.15.4 standard specifies a 2.4GHz PHY that uses Offset-Quadrature Phase Shift Keying (O-QPSK) modulation with half sine pulse shaping [15]. This modulation is equivalent to Minimum Shift Keying (MSK) and MSK transmitters are typically implemented using cartesian or fractional-*N* PLL based modulators. Cartesian transmitters use in phase and quadrature paths requiring DACs, low pass filters, and RF mixers. These tend to be power hungry and the use of analog components makes this approach unsuitable for nanometer CMOS processes.

Although many 2.4GHz band transmitter/PLL designs are reported, most have some limitations. [37] and [38] are based on analog fractional-*N* PLLs and use components such as charge pumps and analog low pass filters, making them less suitable for nanometer CMOS. Although [39] employs a digital fractional-*N* PLL, it suffers from fractional spurs due to nonlinearity and finite resolution of the time-to-digital converter (TDC). Furthermore,

TDC based digital PLLs require extensive calibration of delay elements to reduce spurs.

The digital PLL in this work is based on the design reported in [6, Ferriss, Flynn]. However, there are several important improvements distinguishing the ZigBee TX presented here:

- A low power compact 0dBm PA is designed to drive a 50Ω antenna discussed in Section 4.5. This is more than 20dB improvement compared to [6, Ferriss, Flynn]
- The VCO used in [6, Ferriss, Flynn] is unable to meet the ZigBee center frequency and tuning range. Therefore, the VCO in this work is re designed to have better phase noise, accurate center frequency, and ZigBee compliant tuning range. This is mainly due to new *LC* tank outlined in Section 4.6
- The current draw of the DAC is reduced by 66% to improve the TX efficiency
- The frequency modulation rate in this work is 2Mb/s, twice what is reported in [6, Ferriss, Flynn]

In this work, a digitally dominant  $\Sigma\Delta$  fractional-*N* PLL based transmitter achieves an MSK modulation rate of 2Mb/s. A compact power amplifier that does not require an output matching network delivers -2dBm of output power to a 50 $\Omega$  load. The prototype transmitter is largely comprised of synthesized digital logic and the only analog components are a VCO, two DACs, and a multiplexer. An oversampled one bit phase quantizer is used instead of a TDC as a phase detector. Because the phase detector is formed with a single flip-flop, it does not require calibration of delay elements and is more linear therefore reducing spurs associated with the use of multi bit TDCs. Furthermore, a high reference frequency places

the fractional spurs out of band. A self calibrated two point PLL modulation scheme allows modulation rates that far exceed the loop bandwidth.

### 4.2 Transmitter Architecture

Figure 4.1 shows a block diagram of the prototype transmitter. The transmitter is comprised of a mostly digital fractional-*N* PLL modulator and a two stage power amplifier. A digital Phase Detector (PD) compares the reference clock and the divided down VCO output. A digital integrator averages the PD output. This averaged output sets the VCO varactor voltage. The output of the integrator is converted to the analog domain by a resistor string  $\Sigma\Delta$  DAC. As explained later, two control paths, incorporating two DACs and a digital sampler, enable a self calibrated two point modulation scheme. A two stage PA delivers an output power of up to -2dBm to a 50 $\Omega$  load. A programmable divider is controllable from 8 to 15. A second order  $\Delta\Sigma$  modulator controls the divider.

## 4.3 Phase Detector Overview

Figure 4.2 shows a block diagram of the phase detector first presented in [40]. A single flip-flop oversamples the phase difference,  $\Delta \phi$ , between the reference and the divided down VCO. The quantized phase information is also fed back to the input of the  $\Sigma\Delta$  divider to keep the phase difference between the reference and divider output small. The operation of this feedback loop is similar to that of a delta modulator (Figure 4.2) which consists of a feedback loop with a quantizer in forward path, and an integrator in the feedback path. Integration in the feedback path is achieved by feeding quantized phase information back to



Figure 4.1: The prototype 802.15.4 transmitter

the frequency control of the divider. The delta modulator helps keep  $\Delta \phi$  smaller than one quantization step. The quantization noise from the fractional- $N \Sigma \Delta$  modulator of the divider acts as dither for the oversampled phase quantizer. The integrated output (digital) of the phase detector is a digital word equal to the phase difference between reference clock and divided down VCO.



Figure 4.2: The digital phase detector and equivalent model which is a delta modulator [6]

# 4.4 Frequency Switching Scheme

MSK modulation is a form of FSK with frequency deviation of  $1/(2 \times T_C)$ . For 802.15.4, the bit period  $T_C$  is 1/(2MHz) giving a frequency deviation of 500kHz relative to the channel frequency. A two point self calibrated frequency switching modulation scheme enables modulation rates much higher than the PLL bandwidth. A block diagram of the frequencyswitching scheme is shown in Figure 4.3 [6]. VCO control is split into two paths, one path for each frequency  $f^+$  and  $f^-$ . During each bit period the loop attempts to settle to either  $f^+$  or  $f^-$ . At the end of each bit period, the digital value of the VCO control is sampled. The difference, delta, between the control word for  $f^+$  and  $f^-$ , is calculated and updated. This difference, delta, is added to the VCO control for frequency  $f^+$  to give an initial VCO control value for frequency  $f^-$ . As the modulation continues to switch between  $f^+$  and  $f^-$  , the estimate of delta converges to the correct VCO input difference for the required frequencies  $f^+$  and  $f^-$ . When delta converges, then to a first order, the frequency switching rate is no longer dependent on the settling time of the PLL because the correct input to the VCO is readily applied for each frequency change. An example of settling behavior is shown in Figure 4.3, where after some data transitions, accurate VCO control inputs for the two frequencies are determined.

Figure 4.4 shows a more detailed block diagram of the modulation scheme. A digital IIR filter averages the difference between  $f^+$  and  $f^+$  and two control paths for the VCO are formed with  $\Sigma\Delta$  resistor string DACs. An analog multiplexer switches between the two VCO control voltages generated by the DACs at each data transition.



Figure 4.3: The two point frequency modulation scheme operation and an example settling behavior [6]



Figure 4.4: Implementation details for the two point modulation scheme [6]



Figure 4.5: The two stage resistor feedback inverter based power amplifier

# 4.5 **Power Amplifier**

Figure 4.5 depicts the power amplifier used in this work. The PA is comprised of two stages. The first stage is an inverter amplifier with resistive feedback. Because of the feedback resistor  $R_f$ , the first stage of the PA is self biased. Linearity is improved as the bias point of the first stage is set at the middle of the analog (high gain) swing range. The input resistance of the first stage is approximated by  $R_{in} \approx 1/(gm_1 + gm_2)$ , and the first stage is sized to have a large input resistance to avoid loading the VCO. The second stage is sized to deliver 0dBm to a 50 $\Omega$  load.

There are no internal/external matching circuits or inductors used in this PA yielding a compact area. The PA efficiency is defined as the output power divided by average DC power given by Equation 4.1 where  $I_{avg}$  is estimated to be half of  $I_p$ , the peak current delivered to the load. The PA is designed to have a 0dBm output power with simulated efficiency of 17%.

PA Efficiency = 
$$\frac{P_{out}}{P_{DC}} \approx \frac{I_p^2 \cdot R_L}{V_{DD} \cdot I_{avg}}$$
 (4.1)

# 4.6 Voltage Controlled Oscillator

The voltage controlled oscillator used in this transmitter is shown in Figure 4.6. An NMOS, voltage biased *LC* topology is chosen due to its simplicity and good phase noise. A 6nH inductor with center tap provides the DC bias and an NMOS cross coupled pair compensates the tank loss during oscillation. The varactors are formed by NMOS devices in an n-well. The source and drain of the varactor is shorted together and VCO control voltage,  $V_{ctrl}$ , is applied to the gate. Coarse tuning is achieved by a 5 bit binary weighted bank of differential MiM capacitors with a series NMOS switch.

An example of a coarse tuning capacitor circuit used in this work is shown in Figure 4.6 [41].  $V_{sw}$  is set to  $V_{DD}$  when the switch is OFF and to GND when the switch is ON. This method results in the largest achievable voltage difference (within the oxide breakdown limits) across the NMOS switch during both the ON and OFF states. The large overdrive during ON stage improves the Quality factor (*Q*) of the tank by reducing the NMOS switch ON resistance. The large overdrive during the OFF state avoids leakage based noise injection. Under steady state oscillation where a coarse tuning capacitor is OFF, leakage current is greatly reduced since both  $V_{GS}$  and  $V_{GD}$  of the NMOS switch are biased around a negative voltage ( $-V_{DD}$ ). This results in a significantly improved phase noise compared to [6, Ferriss, Flynn].



Figure 4.6: The VCO used in the transmitter

# **4.7** $\Sigma \Delta$ Digital to Analog Converter

A first order  $\Sigma\Delta$  DAC is used to apply the digital loop filter output word to the analog VCO used in the DPLL. An alternative approach is to directly modulate a number of small capacitors in the *LC* tank. However, this method is complex and results in a large power consumption [42]. This is mainly due to the difficulty of reducing the capacitor switching noise (*i.e.*, the effective quantization noise of the capacitor DAC) at the VCO output. Methods such as dynamic element matching and use of a high frequency (*e.g.*, 400MHz), high order  $\Sigma\Delta$  modulator are needed to reduce this noise. Therefore, we use a simple  $\Sigma\Delta$  DAC at the digital filter output to set the VCO varactor voltage [40].

A block diagram of the  $\Delta\Sigma$  DAC is shown in Figure 4.7. The 32 bit digital loop filter output word is converted to a 5 bit word using a first order digital  $\Delta\Sigma$  modulator. The  $\Delta\Sigma$ modulator clock is 200MHz which is the same as the PLL reference frequency. A first



Figure 4.7: The  $\Delta\Sigma$  DAC block diagram

order  $\Delta\Sigma$ M is intentionally chosen as the output increments by only one value at each clock edge for a DC input.<sup>1</sup> When the PLL is settled and locked, the digital loop filter outputs a constant DC (or very close to DC) value. Therefore, only one DAC code changes most of the time. This greatly simplifies the resistor string DAC design as it eliminates the need for high linearity which could otherwise increase the power consumption and area. A reference frequency of 200MHz is chosen to sufficiently shape the the  $\Delta\Sigma$ M quantization noise to higher frequencies. It is important to note that the DAC clock frequency is not limited to the PLL reference frequency. This is because the DAC can be clocked from the VCO and divider path which can run at a much higher rate than the overall PLL reference. In this work, PLL reference of 200MHz, together with some RC low pass filters resulted in sufficient reduction of the  $\Delta\Sigma$  DAC noise at the PLL output.

#### **4.8 PLL Small Signal Frequency Domain Model**

In this section, we derive the frequency domain small signal model for the DPLL. First, the frequency domain models for various sub blocks used in the DPLL are outlined. Then,

<sup>&</sup>lt;sup>1</sup>This is in contrast to a higher order  $\Delta\Sigma M$  that has a wider output range for a DC input [43]



Figure 4.8: Simplified PLL block diagram

the overall frequency domain small signal model for the PLL is presented. It is important to note that because of the feed forward path from phase detector output to the  $\Delta\Sigma M$  input, the transfer function of the flip flop phase detector based DPLL is different than a generic PLL. The methodology for small signal modeling and noise calculation is adopted from Perrott's classic work [44].

The simplified DPLL block diagram (two point modulation removed) is shown in Figure 4.8. For small signal analysis, the low pass filter at DAC output (which is there to suppress the DAC quantization noise) is ignored since its corner frequency is well outside the PLL bandwidth and therefore has little effect on the loop. In our small signal analysis, the phase detector gain is  $K_{PD}$ , the digital integrator transfer function is H(z), and the VCO transfer function is VCO(f).

#### 4.8.1 Phase Detector Model

Perhaps the most interesting transfer function derivation belongs to the phase detector, so we begin there. The phase detector used in this DPLL is a single D-type flip flop where a



Figure 4.9: Phase detector operation

clean reference is applied to the clock input, and the PLL divider output is applied to the D input. Therefore, VCO edges (at the divider output), which have jitter, are sampled by the clean reference edges as shown in Figure 4.9. For a large phase difference (time difference)  $\Delta\phi$  ( $\Delta t$ ) between ref and div, the flip flip will act as a limiter where the output, Q, is stuck at +1 if div is early, and -1 if div is late. This behavior is large signal and therefore useless in deriving a small signal model for the DPLL. In a phase locked synthesizer,  $\Delta\phi$  is small. And, because div edges have jitter, Q is no longer stuck at +1 or -1. Rather, it will toggle between +1 and -1 with a distribution that depends on the jitter of div edges (Figure. 4.9).

To derive the small signal phase detector gain,  $K_{PD}$ , we must look at the statistical behavior of the flip flop output, Q. We define the average of the phase detector output as  $\mu \triangleq \langle Q \rangle$ . This parameter is useful in PLL small signal calculations. We need a statistical method to calculate  $\mu$ . If we assume a certain Probability Density Function (PDF) for divider jitter<sup>2</sup> as shown in Figure 4.9, the probability that div is early, Pr(early), and the probability that div is late, Pr(late), is the area under +1 and -1, respectively. We obtain

$$\boldsymbol{u} = (+1)Pr(\text{late}) + (-1)Pr(\text{early}). \tag{4.2}$$

<sup>&</sup>lt;sup>2</sup>The PDF will be calculate later

As a quick check, in the case where div is early half the time, and late the other half,  $\mu$  becomes zero since Pr(early) = Pr(late) = 0.5. A different  $\mu$  is obtained when  $\Delta \phi$  is changed by a small amount. Therefore, the phase detector small signal gain is defined as

$$K_{PD} = \frac{\delta\mu}{\delta\phi}.$$
(4.3)

Phase detector gain,  $K_{PD}$ , calculation is outlined below for the case where the div edges have a Gaussian distribution.<sup>3</sup>. Starting with Pr(late) calculation, first, an expression for average output  $\mu$  is obtained. Then,  $K_{PD}$  is obtained using the expression for  $\mu$ .

$$Pr(\text{late}) = \frac{1}{\sigma\sqrt{2\pi}} \int_{0}^{\infty} e^{\frac{(-x+\phi)^2}{2\sigma^2}} dx, \qquad (4.4)$$

where  $\sigma$  is the standard deviation of div jitter, and  $\phi$  the phase difference at phase detector input. A change of variables yields

$$Pr(\text{late}) = \frac{1}{\sqrt{2\pi}} \int_{\frac{\phi}{\sigma}}^{\infty} e^{\frac{-y^2}{2}} dy.$$
(4.5)

Using the Q function,

$$Pr(\text{late}) = Q\left(\frac{\phi}{\sigma}\right) \approx \frac{1}{2} - \frac{\phi}{\sigma\sqrt{2\pi}}.$$
 (4.6)

Using the relationship  $\mu = 2 \times Pr(\text{late}) - 1$ , letting  $\sigma = \sigma_{\Delta t}$  (where  $\Delta t = \Delta \phi \frac{T_{ref}}{2\pi}$ ), and taking the derivative,

$$K_{PD} = \frac{1}{\sigma_{\Delta t} \sqrt{2\pi}}.$$
(4.7)

<sup>&</sup>lt;sup>3</sup>This is a reasonable assumption for frac- $N \Delta \Sigma$  PLLs as shown in [45]



Figure 4.10: Phase detector feedforward path

This expression is similar to the result reported by Da Dalt in [46].

Since the derived the phase detector small signal gain depends on standard deviation of phase detector input,  $\sigma_{\Delta t}$  (*i.e.*, standard deviation of  $[t_{ref} - t_{div}]$ ), we need to obtain  $\sigma_{\Delta t}$  to calculate  $K_{PD}$ .

In a Bang Bang (BB) integer-*N* PLL that uses a similar phase detector, the calculation of  $\sigma_{\Delta t}$  is rather straightforward. As outlined in [47],  $\sigma_{\Delta t}$  is directly related to the VCO jitter (phase noise). Therefore,  $\sigma_{\Delta t}$  (and consequently  $K_{PD}$ ) is readily obtained from stand-alone VCO phase noise simulations. However, we are unable to use this method to obtain  $\sigma_{\Delta t}$  for the DPLL in this work because the  $\Delta \Sigma M$  in the feedback divider affects  $\sigma_{\Delta t}$ . The time difference at the input of the phase detector due to the  $\Delta \Sigma M$  is given by

$$T_{VCO}\sum_{k=0}^{n-1} e_{\Delta\Sigma}[k], \qquad (4.8)$$

where  $T_{VCO}$  and  $e_{\Delta\Sigma}[k]$  are VCO period and  $\Delta\Sigma M$  quantization noise, respectively. It is important to note that because of the fractional divider, this variation is now larger than that of an integer-*N* PLL. Therefore, the PD gain (which is is function of the variance of this variation) is different compared to the integer-N PLL. The variance is given by

$$\sigma_{\Delta t,\Delta\Sigma}^2 = \frac{T_{VCO}^2}{6},\tag{4.9}$$

and

$$\sigma_{\Delta t,\Delta\Sigma}^2 = \frac{T_{VCO}^2}{2},\tag{4.10}$$

for a  $\Delta\Sigma M$  order of 2 or 3, respectively [48]. The  $\Delta\Sigma M$  used in DPLL is second order. In addition to the deterministic jitter of  $\Delta\Sigma M$ , the VCO jitter also contributes to the overall  $\Delta t$  at the phase detector input. An approximate relationship for contribution of VCO jitter ( $\sigma_{VCO}$ ), based on loop parameters is derived in [47] given by

$$\sigma_{\Delta t,VCO} \approx \sqrt{\frac{\pi}{8}} \frac{\sigma_{VCO}^2}{\beta K_T},\tag{4.11}$$

where  $\sigma_{VCO}^2$ ,  $\beta$ , and  $K_T$  are variance of open loop VCO jitter, loop filter proportional gain, and VCO time domain gain, respectively. VCO time domain gain,  $K_T$  can be obtained from the more common VCO frequency domain gain,  $K_v$ , as follows:

$$F_{VCO} = F_0 + K_v * V_{in}, \tag{4.12}$$

where  $F_{VCO}$ ,  $V_{in}$ , and  $F_0$  are the VCO frequency, the varactor voltage, and the VCO frequency with  $V_{in} = 0$ V, respectively.  $K_T$ , defined as  $\frac{\delta T_{VCO}}{\delta V_{in}}$  is calculated below: Using Equation 4.12,

$$T_{VCO} = \frac{1}{F_0 + K_v V_{in}}.$$
(4.13)

Factoring out  $F_0$ , we obtain

$$T_{VCO} = \frac{1}{F_0} \frac{1}{1 + V_{in} \frac{K_v}{F_0}},\tag{4.14}$$

assuming  $V_{in} \frac{K_v}{F_0} \ll 1$ ,

$$T_{VCO} \approx \frac{1}{F_0} \left( 1 + V_{in} \frac{K_v}{F_0} \right). \tag{4.15}$$

Therefore,  $K_T$  is obtained by taking the derivative wrt to  $V_{in}$ , that is

$$K_T \approx \frac{K_v}{F_0^2}.\tag{4.16}$$

The standard deviation of jitter at phase detector input is the sum of the two contributions given by

$$\sigma_{\Delta t} = \sigma_{\Delta t, VCO} + \sigma_{\Delta t, \Delta \Sigma}. \tag{4.17}$$

# 4.8.2 Digital Integrator, DAC, VCO, and Divider Models

The digital accumulator transfer function is given by

$$H(z) = K_I \frac{z^{-1}}{1 - z^{-1}} \approx \frac{K_I}{j2\pi fT},$$
(4.18)

where  $K_I$  is the integrator gain.

The  $\Sigma\Delta M$  transfer function is unity. The DT to CT conversion of the DAC is approximated as 1/T.

The VCO is modeled as

$$VCO(f) = \frac{K_{\nu}}{jf},\tag{4.19}$$

where  $K_v$  is the VCO gain often in units of MHz/V.

The integer part of the divider is simply modeled as

$$DIV(f) = \frac{1}{N},\tag{4.20}$$

where *N* is the divider value. The fractional part of the divider, however, is a discrete time signal because of the  $\Delta\Sigma$  modulator and is therefore modeled as

$$\frac{\phi_n[k]}{n[k]} = 2\pi \frac{z^{-1}}{1 - z^{-1}},\tag{4.21}$$

where n[k] is the deviation in divider value and  $\phi_n[k]$  is the output of the divider after a discrete time accumulator. The discrete time accumulator in the transfer function is because the divider output is a phase signal, whereas n[k] causes an incremental change in frequency of divider output. Therefore, an integration from frequency to phase is needed.

In DPLL, we often go between Continuous Time (CT) and Discrete Time (DT) blocks. By using a pseudo-continuous approximation, the frequency domain transfer function are given by

$$CT \longrightarrow DT = \frac{1}{T},$$
 (4.22)

and

$$DT \longrightarrow CT = T.$$
 (4.23)



Figure 4.11: Frequency domain model of PLL





Figure 4.12: Frequency domain model of PLL, re-drawn for straightforward transfer function and noise calculations

#### 4.8.3 **PLL Transfer Function**

A block diagram of the overall PLL frequency domain model is shown in Figure 4.11. The addition is  $\frac{T}{2\pi}$  before  $K_{PD}$  is to convert from phase to time since the earlier  $K_{PD}$  derivation is in terms on input time difference,  $\Delta t$ . The frequency domain model is re-drawn using signal flow rules as shown in Figure 4.12. This not only helpful in intuitive understanding of the effect of the feed forward path in overall transfer function, it will also allow for easier signal and noise transfer function calculations. First, we derive the PLL overall transfer

function,  $\frac{\phi_{out}}{\phi_{ref}}$ . To obtain the transfer function from PLL input to output, we first ignore the fractional divider (*i.e.*, let n[k] = 0). It is helpful to obtain the loop gain, LG(f) right away as it is used in all signal and noise transfer function calculations that follow. Using the frequency domain model depicted in Figure 4.12, loop gain is obtained

$$LG(f) = \frac{T}{2\pi} K_{PD}H(z) T VCO(f) \left( 1/T + \frac{1}{H(z) T VCO(f)} 2\pi \frac{z^{-1}}{1 - z^{-1}} \right) DIV(f) \quad (4.24)$$

Expanding using Equations 4.7, 4.18, 4.19, and 4.20,

$$LG(f) = \frac{T}{2\pi} K_{PD} \frac{K_I}{j2\pi fT} T \frac{K_v}{jf} \left( 1/T + \frac{1}{K_I \frac{z^{-1}}{1-z^{-1}}} T \frac{K_v}{jf} 2\pi \frac{z^{-1}}{1-z^{-1}} \right) \frac{1}{N},$$
(4.25)

which simplifies to

$$LG(f) = \frac{1}{2\pi} K_{PD} \frac{K_I}{j2\pi f} \frac{K_v}{jf} \left( 1 + \frac{1}{K_I} \frac{j2\pi f}{K_v} \right) \frac{1}{N}.$$
 (4.26)

In order to obtain the poles and zeros, it is helpful to convert Equation 4.26 to S-domain, *i.e.*,

$$LG(s) = K_{PD} \frac{K_I K_v}{s^2} \left( 1 + \frac{s}{K_I K_v} \right) \frac{1}{N}.$$
 (4.27)

The loop gain, LG(s), has two poles at  $\omega_{p1}$ ,  $\omega_{p2}$  equal to zero, and one zero at  $\omega_z = -K_I K_v$ . Therefore, appropriate selection of  $K_I$  and  $K_v$  results in a stable transfer function when feedback loop is closed. It is also important to not that it is the feedforward path that results in a zero in the loop gain transfer function. Without the feedforward path, loop gain will have two integrators and no zeros, and is therefore always unstable. Using Equation 4.27, PLL transfer function is readily obtained as

$$\frac{\phi_{out}}{\phi_{ref}}(s) = \frac{N}{1 + \frac{s}{K_l K_\nu}} \frac{LG(s)}{1 + LG(s)},\tag{4.28}$$

with a DC gain equal to division ratio, N.

# 4.9 PLL Phase Noise Analysis

In this section, we will use the PLL small signal frequency domain model to calculate the overall PLL noise. First, we derive the output referred transfer function for major noise sources. Then, we compute the noise contribution at the PLL output due to each noise source. Finally, we add all the output referred noise power spectral densities to obtain the total PLL output phase noise. The noise sources considered are

- 1. Reference noise,  $\phi_r$
- 2. DAC  $\Delta\Sigma$  quantization noise,  $\phi_{DAC}$
- 3. VCO phase noise,  $\phi_{vco}$
- 4.  $\Delta\Sigma$  divider quantization noise,  $\phi_{div}$

The noise insertion points are shown in Figure 4.13

Furthermore, since both discrete time and continuous time signals are present, the following equations need to be applied properly for power spectral density calculations [49].

Case 1) CT input x(t) fed to CT filter H(f) to produce a CT output y(t):

$$S_{v}(f) = |H(f)|^{2} S_{x}(f).$$
(4.29)



Figure 4.13: Frequency domain model of PLL with various noise insertion points

Case 2) DT input x(k) fed to CT filter H(f) to produce a CT output y(t):

$$S_{y}(f) = \frac{1}{T} |H(f)|^{2} S_{x}(e^{2\pi fT}).$$
(4.30)

#### 4.9.1 Noise Transfer Function for PLL Blocks

The noise transfer function from reference to output of the PLL is obtained as

$$\frac{\phi_{out}}{\phi_r}(f) = \frac{N}{1 + \frac{j2\pi f}{K_I K_v}} \frac{LG(f)}{1 + LG(f)}.$$
(4.31)

The noise transfer function from DAC quantization noise to PLL output is given by

$$\frac{\phi_{out}}{\phi_{dac}}(f) = \frac{N}{\frac{T}{2\pi} \cdot K_{PD} \cdot \frac{K_I}{j2\pi fT} \left(1/T + \frac{j2\pi f}{TK_I K_\nu}\right)} \frac{LG(f)}{1 + LG(f)}.$$
(4.32)

It is noted that due to DT to CT signal flow, Equation 4.30 is used later on for the PSD

calculation.

The noise transfer function from VCO output to PLL output is given by

$$\frac{\phi_{out}}{\phi_{vco}}(f) = \frac{1}{LG(f)} \frac{LG(f)}{1 + LG(f)}.$$
(4.33)

The  $\Delta\Sigma M$  quantization noise transfer function to PLL output is calculated

$$\frac{\phi_{out}}{\phi_{div}}(f) = 2\pi \frac{e^{-j2\pi fT}}{1 - e^{-j2\pi fT}} \frac{T}{\left(1 + \frac{j2\pi f}{K_I K_v}\right)} \frac{LG(f)}{1 + LG(f)}.$$
(4.34)

#### 4.9.2 PLL Output Noise Calculation

Now that all the relevant noise transfer functions are obtained, we can calculate the power spectral density of noise at PLL output because of each noise source.

A PLL reference with noise density,  $S_r(f)$ , contributes to the PLL output noise given by

$$S_{out,r} = \left|\frac{\phi_{out}}{\phi_r}(f)\right|^2 S_r(f).$$
(4.35)

PLL reference, commonly in the form of a crystal oscillator in the MHz range, comes with a well defined noise density  $S_r(f)$ .

A  $\Sigma\Delta$  DAC with white quantization noise density,  $S_{dac}(f) = \frac{1}{12}$ , and a first order noise shaping transfer function,  $NTF = 1 - z^{-1}$ , contributes to the PLL output noise given by

$$S_{out,dac} = \frac{1}{T} \left| \frac{\phi_{out}}{\phi_{dac}}(f) \right|^2 \left| 1 - e^{-2\pi fT} \right|^2 S_{dac}(f).$$
(4.36)

Similar to the DAC, a  $\Sigma\Delta$  divider with white quantization noise density,  $S_{div}(f) = \frac{1}{12}$ ,

and a second order noise shaping transfer function,  $NTF = (1 - z^{-1})^2$ , contributes to the PLL output noise given by

$$S_{out,div} = \frac{1}{T} \left| \frac{\phi_{out}}{\phi_{div}}(f) \right|^2 \left| \left( 1 - e^{-2\pi fT} \right)^2 \right|^2 S_{div}(f).$$
(4.37)

To obtain the VCO noise contribution, SpctreRF transistor level simulation are performed on a phase noise optimized VCO to obtain the noise density  $S_{vco}(f)$ . Once  $S_{vco}(f)$  is available, the VCO noise contribution at PLL output is:

$$S_{out,vco} = \left|\frac{\phi_{out}}{\phi_{vco}}(f)\right|^2 S_{vco}(f).$$
(4.38)

Since the considered noise sources are uncorrelated, the overall noise density of PLL can be obtained by summing the individual noise contributions:

$$S_{out} = S_{out,r} + S_{out,dac} + S_{out,div} + S_{out,vco}.$$
(4.39)

# 4.10 Implementation Details and Test Setup

The prototype transmitter (Figure 4.14) is implemented in 130nm mixed-mode CMOS and occupies an active area of  $0.6 \text{mm}^2$ , and a total area of  $2\text{mm}^2$  including pads. The device is packaged in a 32 pin QFN package. The  $\Sigma\Delta$  modulators, the low pass filters, the modulation scheme and chip encoder are implemented as synthesized logic and occupy  $0.07\text{mm}^2$ , which is a small fraction of the overall area.

A reference clock of 200MHz is used, with a nominal output frequency of 2.405GHz,



Figure 4.14: The DPLL based transmitter die photo

which corresponds to a division ratio of 12.025. The phase detector gain  $K_{PD}$  is set to 0.01, and the loop filter gain is set to 0.03, resulting in a loop bandwidth of 145kHz. The simulated VCO gain is 25MHz/V. The VCO gain is kept small in order to prevent the DAC quantization noise from corrupting the output phase noise. A high reference clock is required, so that the phase quantizer adequately oversamples the phase information. In order to convert from the digital to analog domain, a first order modulator controls a 5-bit resistor-string DAC. The programmable divider used is similar to [50]. The division ratio is controllable from 8 to 15 using 2/3 divider cells.

IEEE 802.15.4 packets are generated in an FPGA. The modulation chip sequence is then sent to the prototype device for transmission. An on-chip encoder converts the O-QPSK chip codes to MSK equivalents. The output of the transmitter is demodulated using a TI CC2420 evaluation board [51] for verification. Output spectrum is measured with an Agilent E4405B spectrum analyzer.



Figure 4.15: Measured transmitter spectrum without modulation

# 4.11 Measurement Results

Figure 4.15 shows the measured output spectrum of the PLL without modulation. The measured output power at 2.405GHz is -2dBm.

Figure 4.16 shows the MSK spectrum when a 2Mb/s PRBS modulation data is applied to the PLL through the FPGA. The IEEE 802.15.4 mask requirements are fulfilled. Multiple packets are successfully demodulated using the CC2420 evaluation board. Although the PLL loop bandwidth is only 145KHz, the self-calibrated two point modulation scheme enables modulation at rate of 2Mb/s.



Figure 4.16: Measured PLL spectrum w/ 2Mb/s MSK modulation



Figure 4.17: Measured PLL phase noise at 2.405GHz

Figure 4.17 shows the measured phase noise of the PLL. The phase noise at 3.5MHz offset is -120dBc/Hz which meets the 802.15.4 requirement. The PLL is free of in-band fractional spurs. The closest measured fractional spur is -60.2dBc at 5MHz offset as shown in Figure 4.18.

Figure 4.19 shows the trellis diagram of the PLL for 2Mb/s MSK modulation.

The synthesized logic draws 4mA. For a -2dBm output power, the PA consumes 4.5mA. A current consumption of 5.7mA is attributed to the divider, the VCO, and the DACs. The total power consumption of the transmitter is measured to be 17mW with 12.5mW attributed to the PLL. The chip operates with an analog and digital supplies of 1.2V.

The performance of the transmitter is summarized and compared to some recent papers



Figure 4.18: Measured PLL spur at 2.405GHz



Figure 4.19: Measured trellis diagram for 2Mb/s MSK modulation
Parameter	This	ISSCC '09	CICC '09	JSSC '10	JSSC '08
	Work	[37]	[38]	[39]	[6]
Tech.	130nm	180nm	150nm	65nm	130nm
V <sub>DD</sub>	1.2V	1.8V	1.55V	1.2V	1.4V
PA Power	-2	4	N/A	N/A	-22
(dBm)					
Modulation	2Mb/s MSK	2Mb/s GMSK	2Mb/s MSK	2Mb/s FSK	1Mb/s FSK
Frequency	2.4-2.5	2.48 center	2.405-2.480	2.29-2.92	2.24 max.
(GHz)					
Power (mW)	12.5/4.5	13.32/16.39	8.525	12	14
PLL/PA					
Phase noise					
(dBc/Hz)	-120	-126	-116	-132	-122
3MHz offset					
Core Area	0.6	1.1	0.88	0.27	0.7
mm <sup>2</sup>					

Table 4.1: Transmitter performance and comparison with prior art

in Table 4.1.

### **CHAPTER V**

## Conclusion

This thesis proposes circuit and system techniques that not only improve power consumption and reduce the form factor, but also significantly improve the performance of PLL based transmitters. The main contributions of this work are three fold.

In Chaper II, we present a new low power, low jitter, compact 192MHz reference frequency quadrupler that leverages a new low phase noise, active inductor based 48MHz differential XO. This 192MHz clock is an excellent clean reference for a low phase noise PLL. The prototype needs significantly less power and area compared to conventional methods.

In Chapter III, a versatile, compact, low voltage, low power 2.5GHz VCO with low phase noise is presented [23]. A conventional CMOS current reuse VCO is modified with the introduction of an AC coupling capacitor to reduce the supply voltage and achieve comparable phase noise at a much lower power consumption. The 2.17GHz to 2.9GHz VCO is capable of operating with a supply voltage as low as 0.6V. With a 0.7V supply and a  $185\mu$ W power consumption, the phase noise at a 3MHz offset is -122.6dBc/Hz, which is suitable for applications such as ZigBee. Increasing the supply voltage to 1.3V results in a

phase noise of -130.1dBc/Hz with a 0.9mW power consumption. This phase noise meets the requirements for applications such as Bluetooth, GPS, and even some lower data rate WLAN applications. At 0.85V, the VCO phase noise is -126.1dBc/Hz with a 190.2dB FoM, the highest reported for power levels as low as  $280\mu$ W. This is the lowest reported power consumption and supply voltage for any current reuse VCO<sup>1</sup>. Implemented in 65nm CMOS, the VCO occupies a core area of 0.13mm<sup>2</sup>.

Chapter IV presents a fully integrated 2.4GHz transmitter in 130nm CMOS that meets the requirements of 802.15.4 standard [24]. The  $\Delta\Sigma$  fractional-*N* PLL is largely comprised of synthesized digital logic and the amount of analog circuitry is minimized. The transmitter achieves a 2Mb/s MSK modulation, and delivers -2dBm to a 50 $\Omega$  load using a compact two-stage PA that requires no output matching. The prototype is implemented in 0.13 $\mu$ m CMOS and occupies an active area of 0.6mm<sup>2</sup>. The transmitter consumes 17mW from a 1.2V supply.

#### 5.1 Ideas for Future Work

There are several avenues to further pursue the techniques presented in this thesis. A few ideas are outlined here.

A complete frequency synthesizer can be built around the frequency quadrupler work presented in Chapter II. This will further highlight the performance improvements as well as power and area saving in the overall PLL due to this fast, low phase noise reference. A high performance PLL, leveraging the frequency quadrupler circuit, can be realized as shown in Figure 5.1. The reference quadrupler generates a 160MHz low phase noise

<sup>&</sup>lt;sup>1</sup>As of the date of publication in [23].



Figure 5.1: An ultra high performance PLL leveraging the reference quadrupler

reference from a standard 40MHz crystal (*e.g.*, for a Wi-Fi application). For most low phase noise PLLs, the 160MHz reference is adequate for reducing the fractional modulator noise. Nevertheless, for ultra high performance applications (such as MU-MIMO IEEE 802.11ac) it might be desirable to more than quadruple the reference. The frequency quadrupler can then be cascaded by an integer-*N* ring PLL. It is important to note that unlike the existing methods, the requirements for this integer-*N* PLL are now quite relaxed. This is because the already quadrupled 160MHz reference allows a wide loop bandwidth for the integer-*N* PLL, therefore significantly reducing the power and area requirements for the ring VCO. In addition, reference injection is no longer needed (although it can still be used if desired) since a high loop bandwidth will significantly reduce the integer-*N* ring PLL phase noise.

Another proposal, building on the new active inductor based differential XO presented in Chapter II, is to use the AC coupling technique introduced in the current reuse VCO of Chapter III to further reduce the supply voltage and power consumption of the differential XO. The schematic for such crystal oscillator is envisioned in Figure 5.2. The minimum supply voltage needed for this circuit is now reduced to  $V_{dsat_n} + V_{dsat_p} + V_{T_p}$ . This is lower than the differential XO presented in Chapter II, where minimum supply is  $V_{dsat_n} + V_{T_n} +$ 



Figure 5.2: Low voltage AC coupled active inductor based crystal oscillator

 $V_{dsat_p} + V_{T_p}$ . This XO circuit can now operate with a sub 1V supply and is therefore suitable for ultra low voltage applications. However, the addition of an AC coupled path and reducing the supply needs rigorous analysis; and careful design choices must be made to ensure sufficient start up and loop gain.

# BIBLIOGRAPHY

#### **BIBLIOGRAPHY**

- [1] "IoT wiki page," https://en.wikipedia.org/wiki/Internet\_of\_Things.
- [2] D. Blaauw, D. Sylvester *et al.*, "IoT design space challenges: Circuits and systems," in *Proc. IEEE Symposium on VLSI Circuits*, Jun. 2014.
- [3] C. Liang and K. Hsiao, "An injection-locked ring PLL with self-aligned injection window," in *Proc. International Solid-State Circuits Conference*, 2011, pp. 90–92.
- [4] A. Elshazly *et al.*, "A 1.5GHz 890µW digital MDLL with 400fs rms integrated jitter, -55.6dBc reference spur and 20fs/mV supply-noise sensitivity using 1b TDC," in *Proc. International Solid-State Circuits Conference*, 2012, pp. 242–243.
- [5] B. Helal *et al.*, "A low jitter programmable clock multiplier based on a pulse injection locked oscillator with a highly-digital tuning loop," *IEEE Journal of Solid-State Circuits*, vol. 44, no. 5, pp. 1391–1400, May 2009.
- [6] M. A. Ferriss and M. P. Flynn, "A 14 mW fractional-N PLL modulator with a digital phase detector and frequency switching scheme," *IEEE Journal of Solid-State Circuits*, vol. 43, no. 11, pp. 2464–2471, Nov. 2008.
- [7] "EEtimes," http://www.eetimes.com/document.asp?doc\_id=1278106.
- [8] "Retrievor," http://retrievor.com/small-and-lightweight-gps-tracking.
- [9] M. Hempstead, M. Lyons, D. Brooks, and G. Wei, "Survey of hardware systems for wireless sensor networks," *Journal of Low Power Electronics*, vol. 4, pp. 1–10, Jun. 2008.
- [10] N. Roberts and D. Wentzloff, "A 98nW wake-up radio for wireless body area networks," in *Proc. IEEE Radio Frequency Integrated Circuits Symposium*, Jun. 2012, pp. 373– 376.
- [11] Y. Liu *et al.*, "A 3.7mW-RX 4.4mW-TX fully integrated bluetooth low energy/IEEE802.15.4/proprietary soc with an ADPLL-based fast frequency offset compensation in 40nm cmos," in *Proc. International Solid-State Circuits Conference*, 2015, pp. 236–237.
- [12] J. Prummel et al., "A 10mW bluetooth low-energy transceiver with on-chip matching," in Proc. International Solid-State Circuits Conference, 2015, pp. 238–239.

- [13] M. Ghaed, G. Chen *et al.*, "Circuits for a cubic-millimeter energy-autonomous wireless intraocular pressure monitor," *IEEE Transactions on Circuits and Systems I*, vol. 60, pp. 3152–3162, Dec. 2013.
- [14] B. Razavi, "RF transmitter architectures and circuits," in *Proc. IEEE Custom Integrated Circuits Conference*, Sep. 1999, pp. 197–204.
- [15] "IEEE 802.15 standard web page," http://www.ieee802.org/15/.
- [16] "Bluetooth Interest Group Web Page," https://www.bluetooth.org/.
- [17] B. Razavi, *RF Microelectronics (2nd Edition)*. Upper Saddle River, NJ, USA: Prentice Hall, 2011.
- [18] T. A. Riley, M. A. Copeland, and T. A. Kwasniewski, "Delta-sigma modulation in fractional-N frequency synthesis," *IEEE Journal of Solid-State Circuits*, vol. 28, no. 5, pp. 553–559, May 1993.
- [19] R. Staszewski, D. Leipold, M. K, and P. Balsara, "Digitally controlled oscillator (DCO)-based architecture for RF frequency synthesis in a deep-submicrometer CMOS process," *IEEE Transactions on Circuits and Systems II*, vol. 50, no. 11, pp. 815–828, Nov. 2003.
- [20] M. Lee and A. A. Abidi, "A 9 b, 1.25 ps resolution coarse-fine time-to-digital converter in 90 nm CMOS that amplifies a time residue," *IEEE Journal of Solid-State Circuits*, vol. 43, pp. 769–777, Apr. 2008.
- [21] D. Griffith *et al.*, "A 65nm CMOS DCXO system for generating 38.4MHz and a real time clock from a single crystal in 0.09mm<sup>2</sup>," in *Proc. IEEE Radio Frequency Integrated Circuits Symposium*, 2010, pp. 321–324.
- [22] D. Park and S. Cho, "14.2 mW 2.55-to-3 GHz cascaded PLL with reference injection and 800 MHz delta-sigma modulator in 0.13μm CMOS," *IEEE Journal of Solid-State Circuits*, vol. 47, no. 12, pp. 2989–2998, Dec. 2012.
- [23] M. Taghivand, M. Ghahramani, and M. P. Flynn, "A low voltage sub 300µw 2.5 GHz current reuse VCO," in *Proc. Asian Solid-State Circuits Conference*, Nov. 2012, pp. 369–372.
- [24] M. Ghahramani, M. A. Ferriss, and M. P. Flynn, "A 2.4GHz 2Mb/s digital PLL-based transmitter for 802.15.4 in 130nm CMOS," in *Proc. IEEE Radio Frequency Integrated Circuits Symposium*, 2011, pp. 1–4.
- [25] G. Shu et al., "A 4-to-10.5Gb/s 2.2mW/Gb/s continuous-rate digital CDR with automatic frequency acquisition in 65nm CMOS," in Proc. International Solid-State Circuits Conference, 2014, pp. 150–151.
- [26] Y. Hsueh *et al.*, "A 0.29mm<sup>2</sup> frequency synthesizer in 40nm CMOS with 0.19psrms jitter and <-100dBc reference spur for 802.11ac," in *Proc. International Solid-State Circuits Conference*, 2014, pp. 472–473.

- [27] P. Park *et al.*, "An all-digital clock generator using a fractionally injection-locked oscillator in 65nm CMOS," in *Proc. International Solid-State Circuits Conference*, 2012, pp. 336–337.
- [28] G. Marucci *et al.*, "A 1.7GHz MDLL-based fractional-N frequency synthesizer with 1.4ps RMS integrated jitter and 3mW power using a 1b TDC," in *Proc. International Solid-State Circuits Conference*, 2014, pp. 360–361.
- [29] Y. Chang *et al.*, "A differential digitally controlled crystal oscillator with a 14 bit tuning resolution and sine wave outputs for cellular applications," *IEEE Journal of Solid-State Circuits*, vol. 47, no. 2, pp. 421–434, Feb. 2012.
- [30] D. Murphy, J. J. Rael, and A. A. Abidi, "Phase noise in LC oscillators: A phasor-based analysis of a general result and of loaded Q," *IEEE Transactions on Circuits and Systems I*, vol. 57, no. 6, pp. 1187–1203, Dec. 2010.
- [31] J. Chen, F. Jonsson, M. Carlsson, C. Hedenas *et al.*, "A low power, startup ensured and constant amplitude class-C VCO in 0.18μm CMOS," *IEEE Microwave and Wireless Components Letters*, vol. 21, no. 8, pp. 427–429, Aug. 2011.
- [32] A. Liscidini, L. Fanori, P. Andreani, and R. Castello, "A 36mW/9mW power-scalable DCO in 55nm CMOS for GSM/WCDMA frequency synthesizers," in *Proc. International Solid-State Circuits Conference*, Feb. 2012, pp. 348–350.
- [33] S. Yun, S. Shin, H. Choi, and S. Lee, "A 1mW current-reuse CMOS differential LC-VCO with low phase noise," in *Proc. International Solid-State Circuits Conference*, Feb. 2005, pp. 540–616.
- [34] S. Wang *et al.*, "A combined VCO and divide-by-two for low-voltage low-power 1.6 GHz quadrature signal generation," in *Proc. IEEE Custom Integrated Circuits Conference*, Sep. 2011, pp. 1–4.
- [35] F. Zhao and F. Dai, "A 0.6V quadrature VCO with optimized capacitive coupling for phase noise reduction," in *Proc. IEEE Custom Integrated Circuits Conference*, Sep. 2011, pp. 1–4.
- [36] M. Wei *et al.*, "An amplitude-balanced current-reused CMOS VCO using spontaneous transconductance match technique," *IEEE Microwave and Wireless Components Letters*, vol. 19, no. 6, pp. 395–397, Jun. 2009.
- [37] H. Shanan, G. Retz, K. Mulvaney, and P. Quinlan, "A 2.4GHz 2Mb/s versatile PLLbased transmitter using digital pre emphasis and auto calibration in 0.18μm CMOS for WPAN," in *Proc. International Solid-State Circuits Conference*, 2009, pp. 420–421.
- [38] R. Yu *et al.*, "A 5.5mA 2.4-GHz two-point modulation zigbee transmitter with modulation gain calibration," in *Proc. IEEE Custom Integrated Circuits Conference*, 2009, pp. 375–378.

- [39] L. Xu, S. Lindfors, K. Stadius, and J. Ryynanen, "2.4GHz low-power all-digital phaselocked loop," *IEEE Journal of Solid-State Circuits*, vol. 45, no. 8, pp. 1513–1521, Aug. 2010.
- [40] M. A. Ferriss and M. P. Flynn, "A 14 mW fractional-N PLL modulator with a digital phase detector and frequency switching scheme," in *Proc. International Solid-State Circuits Conference*, 2007, pp. 352–608.
- [41] H. Sjoland, "Improved switched tuning of differential CMOS VCOs," *IEEE Transactions on Circuits and Systems II*, pp. 352–355, 2002.
- [42] R. B. Staszewski *et al.*, "All-digital PLL and transmitter for mobile phones," *IEEE Journal of Solid-State Circuits*, vol. 40, no. 12, pp. 2469–2482, 2005.
- [43] S. R. Norsworthy, R. Schreier, and G. C. Temes, *Delta-Sigma Data Converters: Theory, Design, and Simulation.* Wiley, 1996.
- [44] M. H. Perrott, M. D. Trott, and C. G. Sodini, "A modeling approach for Σ-Δ fractional-N frequency synthesizers allowing straightforward noise analysis," *IEEE Journal of Solid-State Circuits*, vol. 37, no. 8, pp. 1028–1038, Aug. 2002.
- [45] J. A. Crawford, *Advanced Phase-Lock Techniques*. Boston, MA, USA: Artech House, 2007.
- [46] N. D. Dalt, "Markov chains-based derivation of the phase detector gain in bang-bang PLLs," *IEEE Transactions on Circuits and Systems II*, vol. 53, no. 11, pp. 1195–1199, Nov. 2006.
- [47] M. Zanuso, D. Tasca, S. Levantino, A. Donadel *et al.*, "Noise analysis and minimization in bang-bang digital PLLs," *IEEE Transactions on Circuits and Systems II*, vol. 56, no. 11, pp. 835–839, Nov. 2009.
- [48] "Fractional-N PLLs," ISSCC 2010 Short Course.
- [49] E. A. Lee and D. G. Messerschmitt, *Digital Communication*. Norwell, MA, USA: Kluwer, 1994.
- [50] C. S. Vaucher, I. Ferencic, M. Locher, S. Sedvallson, U. Voegeli, and Z. Wang, "A family of low-power truly modular programmable dividers in standard 0.35-μm CMOS technology," *IEEE Journal of Solid-State Circuits*, vol. 35, no. 7, pp. 1039–1045, Jul. 2000.
- [51] "Texas Instrument single-chip 2.4 GHz IEEE 802.15.4 compliant and zigbee ready RF transceiver," http://www.ti.com/product/cc2420.