

Computation of Hypersonic Flows Using the Direct Simulation Monte Carlo Method

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The direct simulation Monte Carlo method has evolved over 50 years into a powerful numerical technique for the computation of complex, nonequilibrium gas flows. In this context, “nonequilibrium” means that the velocity distribution function is not in an equilibrium form due to a low number of intermolecular collisions within a fluid element. In hypersonic flow, nonequilibrium conditions occur at high altitude and in regions of flowfields with small length scales. In this paper, the theoretical basis of the direct simulation Monte Carlo technique is discussed. In addition, the methods used in direct simulation Monte Carlo are described for simulation of high-temperature, real gas effects and gas–surface interactions. Several examples of the application of direct simulation Monte Carlo to flows around blunt hypersonic vehicles are presented to illustrate current capabilities. Areas are highlighted where further research on the direct simulation Monte Carlo technique is required.

Nomenclature

A	=	surface element of area, m^2
\bar{C}	=	particle velocity vector, m/s
e_r	=	specific rotational energy, J/kg
f	=	probability density function
g	=	relative velocity, m/s
Kn	=	Knudsen number
k	=	Boltzmann’s constant, J/kg
L	=	characteristic length scale, m
m	=	mass of a particle, kg
\bar{N}	=	average number of particles in a cell
N_p	=	number of particles in a cell
N_t	=	number of iterations
n	=	number density, m^{-3}
P_c	=	collision probability
\bar{r}	=	particle position vector, m
T	=	temperature, K
t	=	time, s
V	=	cell volume, m^3
$\Delta(f)$	=	rate of change due to collision processes
ε_{act}	=	activation energy, J
ε_r	=	rotational energy, J
ε_{tot}	=	total collision energy, J
λ	=	mean free path, m
ζ	=	number of rotational degrees of freedom
σ	=	collision cross section, m^2
τ_r	=	rotational relaxation time, s
ω	=	viscosity temperature exponent

$$\frac{\partial}{\partial t}(nf) + \bar{C} \cdot \frac{\partial}{\partial \bar{r}}(nf) = \Delta(f) \quad (1)$$

The equilibrium solution of the Boltzmann equation is the following Maxwellian VDF:

$$f(\bar{C})d\bar{C} = \left(\frac{m}{2\pi kT}\right)^{3/2} \exp\left(-\frac{mC^2}{2kT}\right)d\bar{C} \quad (2)$$

The physical phenomenon that maintains the VDF in equilibrium is intermolecular collisions, and so a gas falls into a nonequilibrium state under conditions where there are not a large enough number of collisions occurring to maintain equilibrium. The two main physical flow conditions that lead to nonequilibrium are low density and small length scales. A low density leads to a reduced collision rate, while a small length scale reduces the size of a fluid element. The usual metric for determining whether a particular gas flow is in a state of nonequilibrium is the Knudsen number, defined as follows:

$$Kn = \frac{\lambda}{L} \quad (3)$$

The mean free path is the average distance traveled by each particle between collisions and is given for a hard sphere by

$$\lambda = \frac{1}{\sqrt{2}n\sigma} \quad (4)$$

Thus, at low density, the mean free path (and therefore Kn) becomes large. Similarly, for small length scales, L becomes small, and again Kn becomes large. As a guiding rule, it is generally accepted that kinetic nonequilibrium effects become important when $Kn > 0.01$.

At a Knudsen number near zero, the velocity distribution function everywhere in a flowfield has the Maxwellian form, there are no molecular transport processes, such as viscosity and thermal conductivity, and the flow may be modeled using the Euler equations. Indeed, the Euler equations of fluid flow can be derived by taking moments of the Boltzmann equation and evaluating them using the Maxwellian VDF. As the Knudsen number increases up to values below 0.01, the velocity distribution function in the flowfield may be represented as a small perturbation from the equilibrium Maxwellian form that is known as the Chapman–Enskog distribution [1]. Evaluation of moments of the Boltzmann equation using the Chapman–Enskog VDF leads to the Navier–Stokes equations in which shear stress and heat flux depend linearly on the spatial gradients of velocity and temperature, respectively. As the Knudsen number rises above 0.01, these linear transport relations are unable to accurately describe the strong nonequilibrium processes. It is then necessary to

I. Introduction

The analysis of dilute gas flows at all Knudsen numbers can be performed using the Boltzmann equation that describes the evolution of the molecular velocity distribution function (VDF) [1]. In the absence of a body force, the Boltzmann equation is written as

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develop higher-order sets of partial differential equations (such as the Burnett equations) or to solve the Boltzmann equation. Although there has been some success achieved in formulating and solving the Burnett equations [2], there remain issues with boundary conditions, and it is not clear that the amount of additional Knudsen number range provided is worth the significant additional effort in numerical analysis. Unfortunately, development of robust and general numerical solution schemes for the Boltzmann equation for application to aerospace problems has also proved a significant challenge [3]. Again, some progress has been made, but there is still much work to be done to be able to simulate all of the flow physics relevant to hypersonic flows.

The direct simulation Monte Carlo (DSMC) method was first introduced by Bird [4] specifically to analyze high-Knudsen-number flows. Since that time, several books have been written on the method [5,6], and thousands of research papers have been published that report on development and application of the technique. The significance of the DSMC technique has been its ability over 50 years of development to fill the void described previously in gas analysis methodology for high-Knudsen-number flows. The DSMC technique emulates the same physics as the Boltzmann equation without providing a direct solution. The DSMC method follows a representative set of particles as they collide and move in physical space. It has been demonstrated that DSMC converges to solution of the Boltzmann equation in the limit of a very large number of particles [7].

High-Knudsen-number conditions arise in many areas of science and technology including space and atmospheric science, vapor processing of materials, spacecraft propulsion systems, and microscale gas flows. As illustrated in Fig. 1, hypersonic flow conditions may fall into the kinetic nonequilibrium regime at sufficiently low density (that occurs at high altitude in the Earth's atmosphere) and for very small hypersonic objects (e.g., meteoroids that have a diameter on the order of a centimeter [8]). In addition, situations arise where localized regions of a flow may contain low density (e.g., the wake behind a capsule) or small length scales (e.g., sharp leading edges on a vehicle, or shock waves and boundary layers that may have very steep spatial gradients in flowfield properties).

For hypersonic flows, it is an important question to ask whether high-Knudsen-number phenomena lead to effects that are of practical significance. Detailed studies [9–11] have compared DSMC and computational fluid dynamics (CFD) computations of hypersonic flows over cylinders and wedges for global Knudsen numbers ranging from continuum ($Kn = 0.002$) to rarefied ($Kn = 0.25$). Every effort was made in these studies to employ consistent cross sections and transport models in DSMC and CFD, respectively. The focus of the studies was the effect of any nonequilibrium flow

phenomena on surface properties such as drag and heat transfer. It was found at $Kn = 0.002$ that DSMC and CFD gave identical results for all surface properties including drag force and peak heat transfer. However, as Kn was increased, the differences between DSMC and CFD surface results also grew larger. For example, in Mach 25 flow of nitrogen over a cylinder at the highest Knudsen number of 0.25, in comparison to CFD, DSMC predicted a 23% lower drag force and a 29% lower peak heat flux. These differences are clearly significant and indicate that accurate determination of surface properties in high-Knudsen-number hypersonic flows does require a noncontinuum, kinetic approach, such as DSMC.

An important part of the success of the DSMC technique in analyzing high-Knudsen-number hypersonic flows has been the ability to include in the technique models that are effective in simulating high-temperature, real gas effects. Such effects include mixtures of chemical species, relaxation of internal energy modes, and chemical reactions such as dissociation and ionization, radiation, and gas-surface interaction. In this article, the fundamental aspects of the DSMC technique are described with an emphasis on physical modeling issues related to its application to hypersonic problems and the simulation of the associated real gas effects. Examples are provided that illustrate the current capabilities of these models and areas where further work is needed are identified. The application of the DSMC technique to the analysis of flows around hypersonic blunt vehicles is then reviewed.

II. Basic Algorithm of the Direct Simulation Monte Carlo Technique

The DSMC technique emulates the physics of the Boltzmann equation by following the motions and collisions of a large number of model particles. Each particle possesses molecular-level information including a position vector, a velocity vector, and physical information such as mass and size. Particle motion and collisions are decoupled over a time step Δt that is smaller than the local mean free time. During the movement of particles, boundary conditions such as reflection from solid surfaces are applied. The physical domain to be simulated in a DSMC computation is covered by a mesh of cells. These cells are used to collect together particles that may collide. There are a number of DSMC schemes for simulating collisions, and all of them achieve a faster numerical performance than the molecular dynamics method [12] by ignoring the influence of the relative positions of particles within a cell in determining particles that collide. This simplification requires that the size of each cell be less than the local mean free path of the flow. Bird's no-time-counter scheme [6] is the most widely used collision scheme, in which a number of particle pairs in a cell are formed that is given by

$$N_c = \frac{1}{2} n \bar{N} (\sigma g)_{\max} \Delta t \quad (5)$$

Each of the N_c pairs of particles is formed at random regardless of position in the cell, and then a probability of collision for each pair is evaluated using

$$P_c = \frac{\sigma g}{(\sigma g)_{\max}} \quad (6)$$

This procedure reproduces the expected equilibrium collision rate under conditions of equilibrium. It is determined whether the particle pair actually collides by comparing the collision probability to a random number. When a collision occurs, postcollision velocities are calculated using conservation of momentum and energy.

The cells employed for simulating collisions are also often used for the sampling of macroscopic flow properties such as density, velocity, and temperature. There is no necessity to have the collision and sampling cells be identical, however, and sometimes a coarser mesh is used for sampling.

The basic steps in each iteration of the DSMC method are: 1) move particles over the time step Δt ; 2) apply boundary conditions such as introducing new particles at inflow boundaries, removing particles at

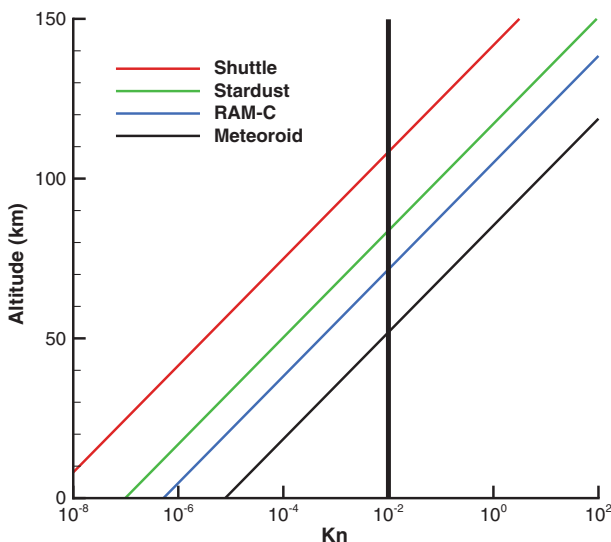


Fig. 1 Knudsen number profiles in the Earth's atmosphere for several hypersonic entry bodies.

outflow boundaries, and processing reflections at solid boundaries; 3) sort particles into cells and process collisions using kinetic theory; and 4) sample average particle information. As an example of how sampled particle information is employed to determine a macroscopic flow property, the average mass density in a computational cell is given by

$$\rho = \frac{\sum_{i=1}^{N_p} m_i}{V \times N_t} \quad (7)$$

where m_i is the mass of particle i , N_p is the total number of particles that have occupied this cell over N_t iterations of the computation. Also, as an illustration of the determination of surface properties, for a surface element of area A , the average shear stress is given by

$$\tau_w = \frac{\sum_j m_j (u_t^i - u_t^r)_j}{A \times N_t \times \Delta t} \quad (8)$$

where u_t^i and u_t^r are the incident and reflected velocity components tangent to the surface element of each particle j to hit the element during N_t iterations of the computation.

A DSMC simulation begins from some initial condition, and a finite number of iterations must elapse for the flow to reach a steady state. Generally, steady state is detected as the total number of particles in the simulation reaches an asymptotic limit. This is either performed manually or by tracking the statistical fluctuations. After steady state is reached, sampling of flowfield and surface properties begins, and the simulation is continued a further number of iterations to reduce the statistical noise in the sampled information to an acceptable level. A typical DSMC computation may employ 1 million particles, reach steady state after 50,000 iterations, and continue sampling for a further 50,000 iterations. On a modern desktop computer, such a simulation should take about 3 h.

Although the ideas behind the DSMC technique are simple, implementation in an algorithm takes on many different forms. Specific DSMC algorithms have been developed for vector computers [13] and parallel computers [14,15]. Bird has focused work on customizing the algorithm to achieve efficient performance on single-processor machines [16]. In addition, a number of more elaborate DSMC procedures have been proposed to improve the handling of specific situations [6]. Examples include subcells, to improve localization of colliding particles; spatially varying time steps, to reduce the cost of flows containing a very broad range of time scales, such as nozzles and plumes; and weighting schemes, to allow resolution of trace species.

Having provided a general overview of the basic elements of the DSMC method, in the following sections, some of the physical models are described that are most critical to the application of the DSMC technique to analyze hypersonic flows.

III. Physical Models of the Direct Simulation Monte Carlo Technique

In this section, the most commonly employed physical models are reviewed for DSMC computation of hypersonic flows. The basic ideas are described for simulation of a number of physical phenomena including momentum exchange, internal energy relaxation, chemical reactions, and gas–surface interactions. Where possible, examples are provided of efforts to validate these models using laboratory data.

A. Elastic Momentum Exchange

In the absence of internal energy exchange and chemical reactions, an elastic collision between two particles leads only to changes in their velocity (or momentum) components. The frequency of such interactions is determined by the collision cross section for which a number of models have been developed for DSMC. The most widely used forms are the variable hard sphere (VHS) [17] and the variable soft sphere (VSS) [18]. For hypersonic flow, the VHS model is considered sufficiently accurate, for which the cross section is given as

$$\sigma = \sigma_{\text{ref}} \left(\frac{g}{g_{\text{ref}}} \right)^{-2\omega} \quad (9)$$

where σ_{ref} and g_{ref} are reference values, and ω is related to the viscosity temperature exponent. Specifically, it is assumed that the gas viscosity is described by a simple temperature relation:

$$\mu = \mu_{\text{ref}} \left(\frac{T}{T_{\text{ref}}} \right)^{0.5+\omega} \quad (10)$$

and the relationship between the reference parameters is provided by Bird [6]. Values of these reference parameters for many common species are listed in [6], and these are generally obtained by comparison with measured or computed viscosity data. For the VHS model, isotropic scattering is assumed in which the unit vector of the postcollision relative velocity is assigned at random on the unit sphere. The VSS model represents an improvement over VHS in that it allows collision parameters to be determined through comparison with both viscosity and diffusivity data. The VSS cross section is the same as the VHS model, but the scattering angle is given by

$$\chi = 2 \cos^{-1} \left\{ \left(\frac{b}{d} \right)^{1/\alpha} \right\} \quad (11)$$

where α is determined from diffusivity data, b is the distance of closest approach, and d is the collision diameter. Again, values of α for common gases are provided by Bird [6]. Note that $\alpha = 1$ corresponds to the VHS model.

One of the most common test cases for evaluation of the DSMC technique in simulating nonequilibrium hypersonic flows involving only elastic momentum exchange are normal shock waves of noble gases. Figure 2a shows the density profile through a normal shock wave at Mach 9 for argon. Detailed measurements were obtained using an electron-beam technique by Alsmeyer at a number of different Mach numbers in both argon and nitrogen [19]. Included in Fig. 2a are both DSMC and CFD results. The DSMC computations used the VHS model, while the CFD results solved the Navier–Stokes equations with the viscosity given by the same VHS parameters used in DSMC. The comparison shows that the DSMC technique is able to reproduce the measured data very accurately, whereas CFD predicts a shock wave that is too thin. Figure 2b shows the reciprocal shock thickness (a measure of the density gradient at $x/\lambda = 0$) for all of the argon shock waves investigated by Alsmeyer [19]. Once again, it is clear that DSMC provides excellent agreement with the measurements for all conditions considered. CFD consistently predicts an inverse shock thickness that is too large (that is, shocks that are too thin) for all Mach numbers above about 1.50. Another compelling validation of the capability of DSMC in simulating nonequilibrium hypersonic flows is provided by the comparisons shown in Figs. 3a and 3b. These plots are reproduced from the study by Pham-Van-Diep et al. [20], in which velocity distribution functions were examined inside a normal shock of helium at Mach 25. Figure 3a shows the distributions in the front of the shock for the parallel (circles and solid line) and perpendicular (triangles and dashed line) velocity components. Symbols represent electron-beam measurements, and lines represent DSMC computations that employed a detailed Maitland–Smith collision model. The horizontal axis in these plots is normalized by the hypersonic upstream velocity so that the parallel velocity distribution has its peak centered around 1.0 toward the right of the figure. The parallel velocity distribution shows a strong nonequilibrium profile with the higher-velocity, lower-temperature peak on the right, and a higher-temperature, lower-velocity peak toward the middle. The distribution of the perpendicular component is centered on zero and consists of two distinct populations from the low-temperature freestream and the high-temperature postshock regions. The profiles in Fig. 3b are obtained further downstream toward the middle of the shock and continue to show strongly nonequilibrium behavior. The Navier–Stokes equations, which are based on a small perturbation from equilibrium, are not able to accurately model such phenomena. The

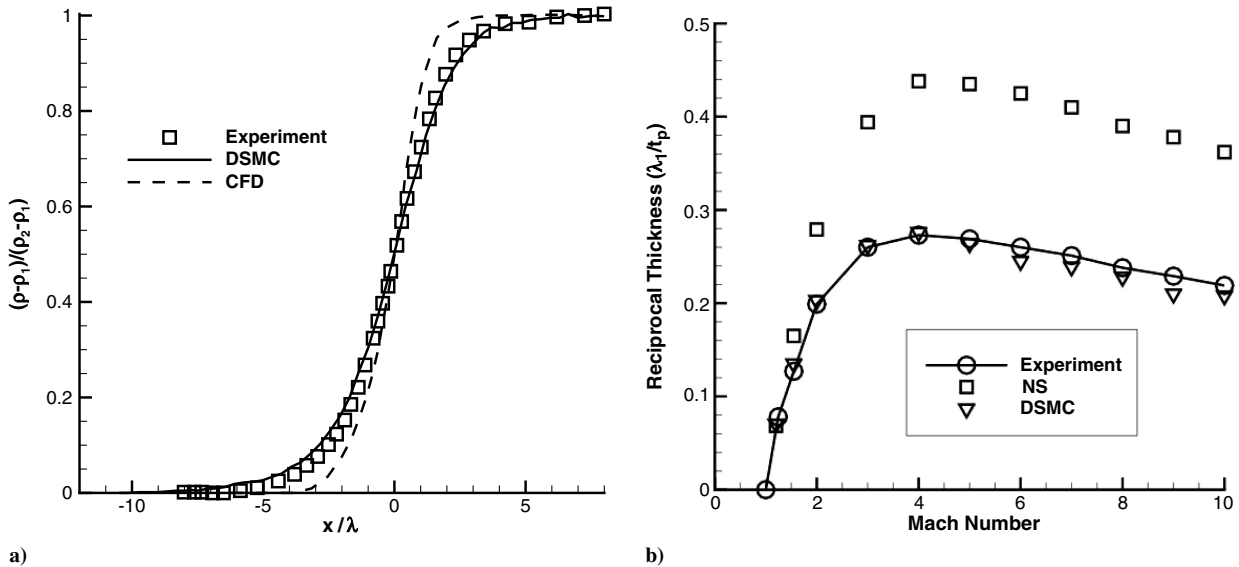


Fig. 2 Argon normal shock wave with measurements from [19]: a) profiles of normalized density at Mach 9, and b) reciprocal shock thickness.

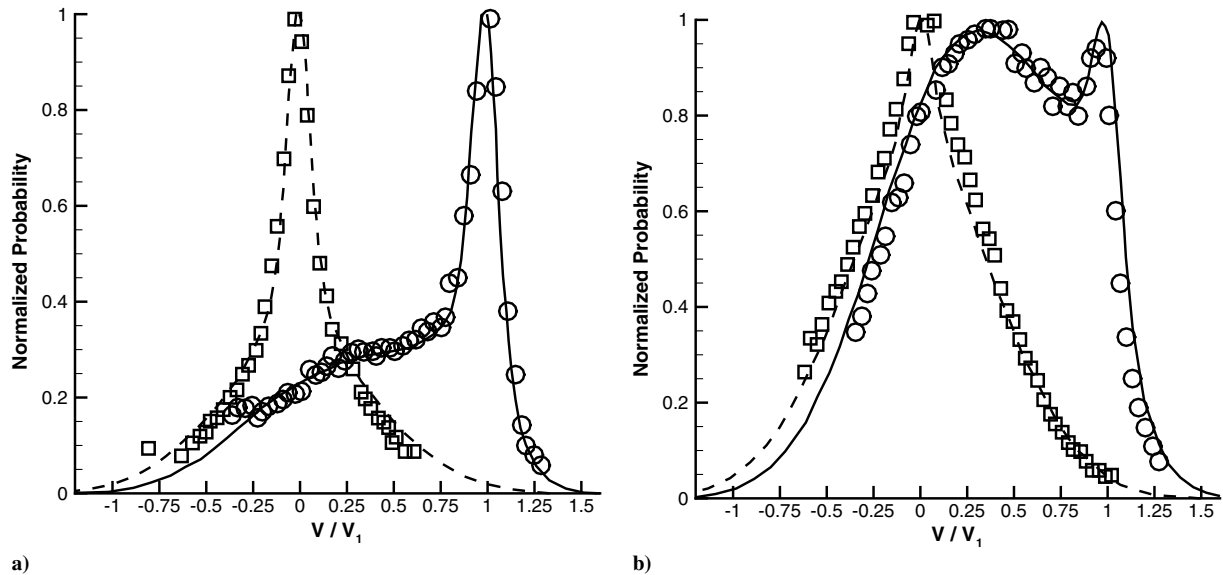


Fig. 3 Velocity distribution functions in a Mach 25 normal shock of helium (symbols are experiments, lines are DSMC [20]): a) shock front, and b) in the shock middle.

excellent agreement with measured data shown in these plots is one of the strongest illustrations of the ability of the DSMC technique to reproduce nonequilibrium flow at the level of the distribution functions.

The main limitation of the VHS/VSS collision models is their reliance on the need to model viscosity and diffusivity using a simple temperature exponent. Even for the common gases for which VHS/VSS parameters are provided by Bird [6], the viscosity dependence on temperature may change over a sufficiently wide temperature range. As an illustration of the types of problems encountered with the VHS/VSS models, Figs. 4a and 4b show collision cross sections as a function of collision energy for two different collisions involving electrons [21]. For such interactions, direct measurements of cross sections are available in the literature. Development of more general and detailed collision cross-section models for use in DSMC computations is an area where further work is required.

B. Rotational Energy Exchange

The DSMC technique usually simulates the internal energy modes of molecules and atoms by assigning rotational, vibrational, and electronic energies to each particle. In hypersonic flows, generally

the electronic modes are ignored, as is the case for CFD studies. Analysis of jet flows including electronic energy is described for example in [22]. We focus here on rotational and vibrational energy exchange.

The rotational mode is usually simulated using a classical physics approach in which the rotational energy ϵ_r is assumed continuously distributed at equilibrium according to a Boltzmann distribution:

$$f(\epsilon_r)d\epsilon_r = \frac{1}{\Gamma(\zeta/2)} \left(\frac{\epsilon_r}{kT}\right)^{\zeta/2-1} \exp\left(-\frac{\epsilon_r}{kT}\right) d\left(\frac{\epsilon_r}{kT}\right) \quad (12)$$

where ζ is the number of rotational degrees of freedom (2 for a diatomic molecule, and 3 for a polyatomic molecule).

When a particle representing a molecule is injected into a DSMC computation, it is given an initial rotational energy sampled from Eq. (12). The rotational energy of the particle can change through collisions with other particles and through collisions with a solid surface (see Sec. III.G). In a continuum analysis of rotational energy exchange, the rotational relaxation equation is usually employed:

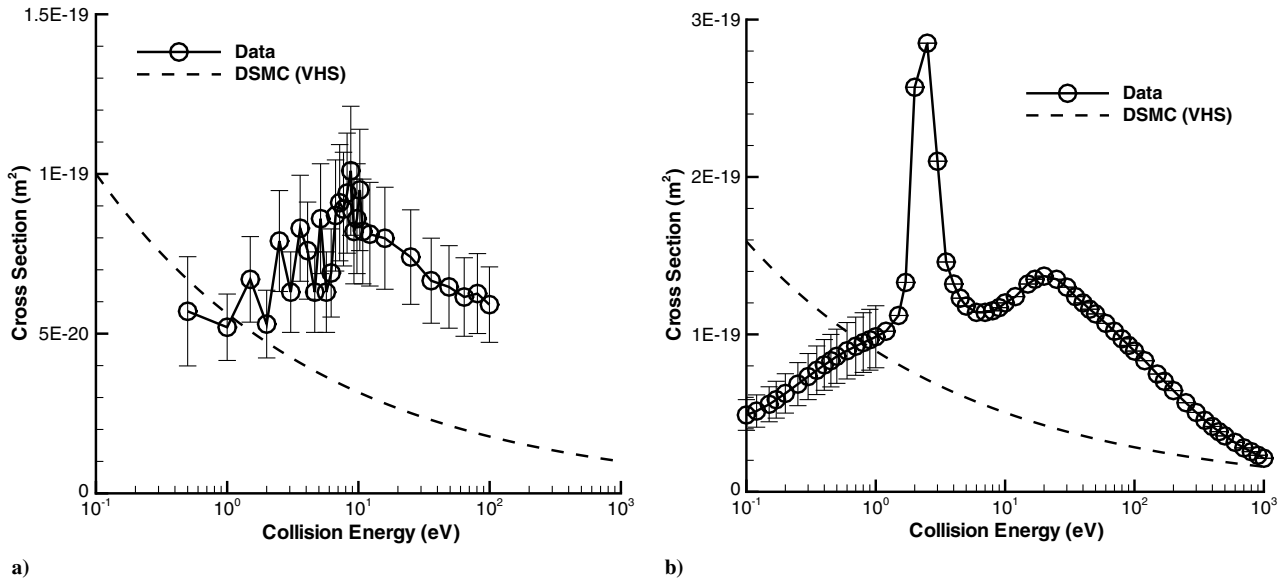


Fig. 4 Electron collision cross sections [21]: a) oxygen atom, and b) nitrogen molecule.

$$\frac{de_r}{dt} = \frac{e_r^* - e_r}{\tau_r} \quad (13)$$

where e_r is the specific rotational energy, e_r^* is the equilibrium value at temperature T , and τ_r is the rotational relaxation time. The equivalent DSMC procedure involves evaluating a probability of rotational energy exchange for each collision followed by appropriate energy exchange mechanics for those collisions that lead to rotational relaxation. The average probability of rotational energy exchange is

$$\langle P_{\text{rot}} \rangle = \frac{1}{Z_{\text{rot}}} = \frac{\tau_t}{\tau_r} = \frac{1}{\tau_r \nu} \quad (14)$$

where Z_{rot} is the rotational collision number, and τ_t is the translational relaxation time that is equal to the inverse of the collision frequency ν . Boyd [23] developed the following instantaneous rotational energy exchange probability based on Parker's model [24] for the rotational collision number and the VHS collision model:

$$P_{\text{rot}} = \frac{1}{(Z_{\text{rot}})_{\infty}} \left(1 + \frac{\Gamma(\zeta + 2 - \omega)}{\Gamma(\zeta + 3/2 - \omega)} \left(\frac{kT^*}{\epsilon_{\text{rot}}} \right)^{\frac{1}{2}} \pi^{\frac{3}{2}} + \frac{\Gamma(\zeta + 2 - \omega)}{\Gamma(\zeta + 1 - \omega)} \left(\frac{kT^*}{\epsilon_{\text{tot}}} \right) \left(\frac{\pi^2}{4} + \pi \right) \right) \quad (15)$$

where ϵ_{tot} is the total collision energy (the sum of the translational collision energy and the rotational energy), T^* is the characteristic temperature of the intermolecular potential, and $(Z_{\text{rot}})_{\infty}$ is the limiting value. After evaluation of the rotational energy exchange probability, a random number is used to decide whether the collision leads to energy exchange. For those collisions involving rotational energy exchange, the Borgnakke–Larsen (BL) model [25] is employed to assign new postcollision rotational energies. The BL model assumes local thermodynamic equilibrium to sample the fraction of the total collision energy due to rotation, $\epsilon_{\text{rot}}/\epsilon_{\text{tot}}$, from the following expression:

$$\frac{P}{P_{\text{max}}} = \left(\frac{\zeta + 1 - \omega}{2 - \omega} \left(1 - \frac{\epsilon_{\text{rot}}}{\epsilon_{\text{tot}}} \right) \right)^{2-\omega} \left(\frac{\zeta + 1 - \omega}{\zeta - 1} \left(\frac{\epsilon_{\text{rot}}}{\epsilon_{\text{tot}}} \right) \right)^{\zeta-1} \quad (16)$$

Once the new rotational energy is assigned, the remaining energy is the new translational energy and hence determines the new post-collision relative velocity. The regular DSMC collision mechanics is then performed to calculate the velocities of the colliding particles.

Lumpkin et al. [26] noted that an additional correction must be applied to any DSMC rotational energy exchange probability to make

Borgnakke–Larsen exchange mechanics consistent with the continuum rotational relaxation equation [Eq. (13)]. The correction applies to a constant number of degrees of freedom ζ , and it is given by

$$P_{\text{particle}} = P_{\text{continuum}} \left(1 + \frac{2\zeta}{4 - 2\omega} \right) \quad (17)$$

that is usually close to a factor of 2.

Although the rotational energy is usually simulated in the classical limit, a quantum mechanical approach for DSMC has also been developed by Boyd [27].

A detailed set of experimental measurements of hypersonic normal shock waves in nitrogen was collected by Robben and Talbot [28]. Again, an optical diagnostic technique was employed to measure both the density and the rotational energy distribution function through the shock wave for a number of different Mach numbers. Figure 5 compares DSMC simulations [27] with the measurements of the density and rotational temperature profiles at a Mach number of 12.9. Clearly, very good agreement between simulation and measurement is obtained. Figure 6 shows rotational energy distribution functions measured at two different locations in this same shock wave. Once again, the excellent agreement obtained between DSMC

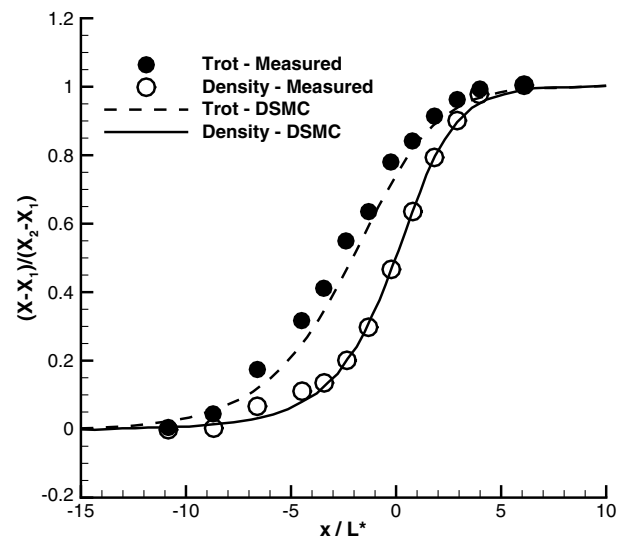


Fig. 5 Profiles of density and rotational temperature in a Mach 12.9 normal shock of N_2 [27].

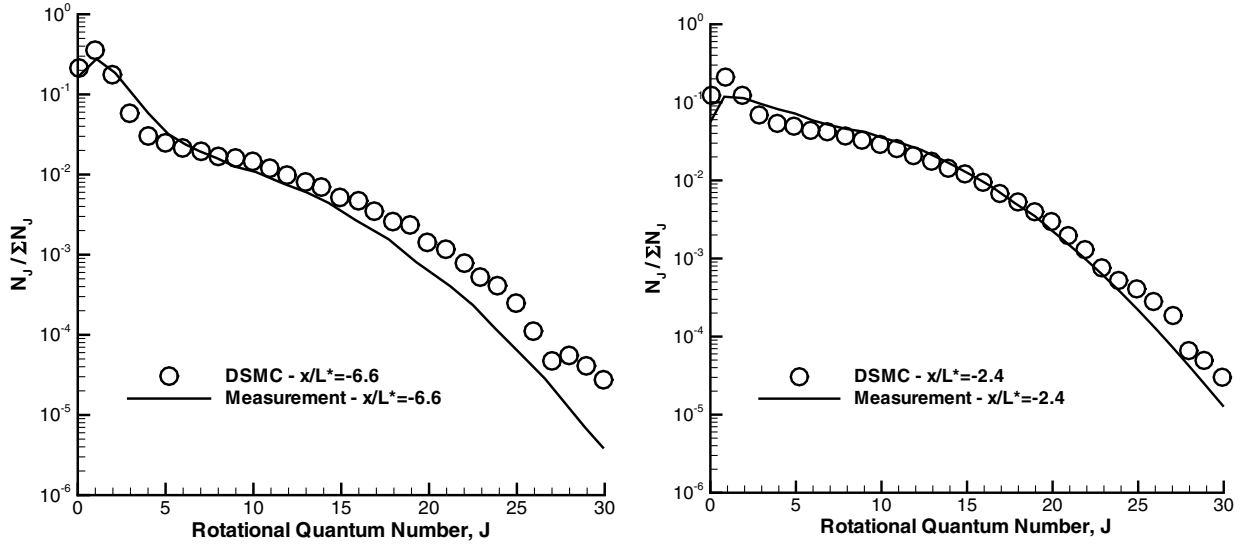


Fig. 6 Rotational energy distribution functions at two different locations in a Mach 12.9 normal shock of N_2 [27].

and experiment at the level of the distribution function is one of the strongest illustrations of the ability of the technique to accurately simulate nonequilibrium phenomena. The main limitation of the Robben and Talbot data is that they were collected for a flow with a total temperature of just 300 K. There is a strong requirement for additional, detailed measured data sets for relevant high-temperature hypersonic conditions that can be used to evaluate DSMC rotational relaxation models.

A more advanced model for rotational nonequilibrium was proposed recently by Valenti et al. [29] in which molecular dynamics modeling was employed to show that the rotational collision number is a function of both translational and rotational temperature. As more detailed models are developed, their validation requires access to suitably detailed experimental measurements.

C. Vibrational Energy Exchange

The simulation of vibrational relaxation follows a similar procedure to that for rotation. The average probability of vibrational energy exchange is typically evaluated using the vibrational relaxation time used in hypersonic CFD models due to Millikan and White [30] with the Park high-temperature correction [31]:

$$\tau_{\text{vib}} = \tau_{\text{MW}} + \tau_{\text{Park}} \quad (18)$$

To accurately reproduce this vibrational relaxation time in a DSMC computation, because of its complex temperature dependence, it is necessary to evaluate a collision averaged vibrational exchange probability [32]. Unlike rotational relaxation, a quantum mechanical approach is almost always employed for simulation of vibrational energy relaxation in hypersonic flows. A quantized vibrational energy exchange model corresponding to the classical Borgnakke-Larsen approach was formulated by Bergemann and Boyd [33]. It involves first determining the maximum vibrational quantum level available based on the total collision energy:

$$v_{\text{max}} = \left\lfloor \frac{\varepsilon_{\text{tot}}}{k\theta_v} \right\rfloor \quad (19)$$

where ε_{tot} is the total collision energy (the sum of the translational collision energy and the vibrational energy), $\lfloor \cdot \rfloor$ means truncation, and θ_v is the characteristic temperature for vibration of the molecule. Then, the postcollision vibrational quantum number v is sampled from

$$\frac{P}{P_{\text{max}}} = \left(1 - \frac{vk\theta_v}{\varepsilon_{\text{tot}}}\right)^{1-\omega} \quad (20)$$

The Lumpkin et al. [26] correction factor must also be applied to the vibrational exchange probability.

More detailed vibrational relaxation models for DSMC have also been developed and applied to hypersonic flows. For example, in [34], the basis for a new, high-fidelity DSMC model is the basic transition probability of the Forced Harmonic Oscillator (FHO) model described by Adamovich et al. [35]. Specifically, in a molecule-molecule collision, the probability of transition from initial vibrational levels (i_1, i_2) to final vibrational levels (f_1, f_2) is given by

$$P_{VVT}(i_1, i_2 \rightarrow f_1, f_2, \varepsilon, \rho) = \left| \sum_{r=0}^n C_{r+1, i_2+1}^{i_1+i_2} C_{r+1, f_2+1}^{f_1+f_2} \times \exp[-i(f_1 + f_2 - r)\rho] P_{VT}^{1/2}(i_1 + i_2 - r \rightarrow f_1 + f_2 - r, 2\varepsilon) \right|^2 \quad (21)$$

where

$$P_{VT}(i \rightarrow f, \varepsilon) = i!f! \varepsilon^{i+f} \exp(-\varepsilon) \left| \frac{(-1)^r}{r!(i-r)!(f-r)!} \frac{1}{\varepsilon^r} \right|^2 \quad (22)$$

and

$$\varepsilon = S_{VT} \frac{4\pi^3 \omega (\tilde{m}^2 / \mu) \gamma^2}{\alpha^2 h} \sinh^{-2} \left(\frac{\pi \omega}{\alpha \bar{v}} \right) \quad (23)$$

$$\rho = \left(S_{VV} \frac{\alpha^2 \bar{v}^2}{\omega_1 \omega_2} \right)^{1/2} \quad (24)$$

In these equations, $C_{a,b}^c$ are transformation matrices defined in [35], S_{VT} and S_{VV} are steric factors, ω is the oscillator frequency, \tilde{m} is the collision reduced mass, μ is the oscillator reduced mass, γ is oscillator mass ratio, α characterizes the intermolecular potential, h is Planck's constant, and \bar{v} is the symmetrized relative velocity. Further definitions and numerical values of the key parameters are provided in [35].

There are no measurements in the literature of vibrational energy distribution functions in hypersonic flows of air that can be used to validate the DSMC vibrational relaxation models. A rare example of this type of experimental data was obtained for carbon monoxide by Meolans and Brun [36] in a shock-tube facility. Using spectroscopy, the population of CO molecules in the fourth vibrational state relative to the ground state was measured behind a Mach 7 shock wave [36]. The measured profiles are compared in Fig. 7 with results obtained

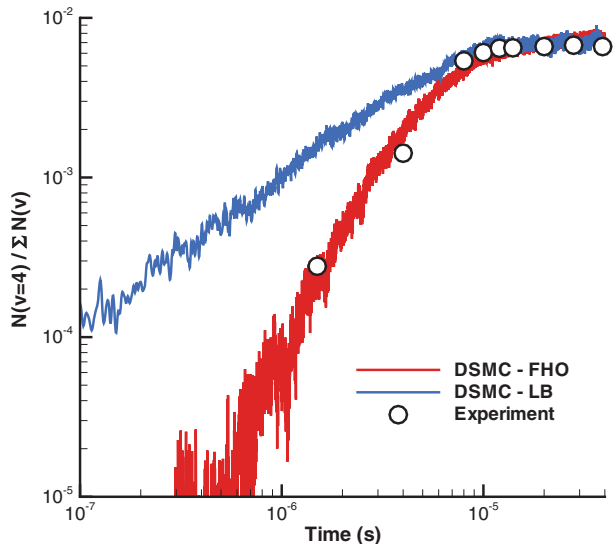


Fig. 7 Profiles of the relative population in the fourth vibrational state for a Mach 7 normal shock wave of carbon monoxide [34].

with two different DSMC vibrational relaxation models: the standard Borgnakke–Larsen (BL) approach and the implementation of the FHO model [34]. The standard BL model populates the fourth excited state much too rapidly, whereas the FHO model provides very good agreement with the measurements. Further detailed experiments of this kind are required to validate the DSMC simulation approach for vibrational relaxation of air molecules.

D. Chemical Reactions

The most commonly used DSMC chemistry model is the total collision energy (TCE) model of Bird [6]. This model is based on a modified Arrhenius rate coefficient of the following form:

$$C = aT^b \exp\left(-\frac{\epsilon_{\text{act}}}{kT}\right) \quad (25)$$

where a and b are constants, and ϵ_{act} is the activation energy of the reaction. By integrating over the equilibrium distribution function for the total collision energy, it may be shown that the form of the reaction probability consistent with Eq. (25) for the VHS collision model is given by

$$P_{\text{TCE}} = A \frac{(\epsilon_{\text{tot}} - \epsilon_{\text{act}})^{b+\zeta+\frac{1}{2}}}{(\epsilon_{\text{tot}})^{\zeta+1-\omega}} \quad (26)$$

where ϵ_{tot} is the total collision energy of all modes of both particles participating in the collision, and the constant A depends on the Arrhenius parameters and molecular constants. The TCE model was extended to include the important physical phenomenon of vibration-dissociation coupling by Haas and Boyd [37] in the vibrationally favored dissociation (VFD) model. The VFD model makes it possible to increase the dissociation probability of particles having large vibrational energy:

$$P_{\text{VFD}} = A \frac{(\epsilon_{\text{tot}} - \epsilon_{\text{act}})^{b+\zeta+\frac{1}{2}}}{(\epsilon_{\text{tot}})^{\zeta+1-\omega}} (\epsilon_{\text{vib}})^\phi \quad (27)$$

Values of the VFD parameter ϕ for air molecules have been determined through comparison with experimental data. For example, Fig. 8 shows comparisons [37] for dissociation incubation distances between DSMC predictions and data measured by Hornung [38] in hypersonic flows of N_2 . The DSMC results show a strong sensitivity to the level of vibrational favoring included in the model, with the incubation distance growing significantly as the model

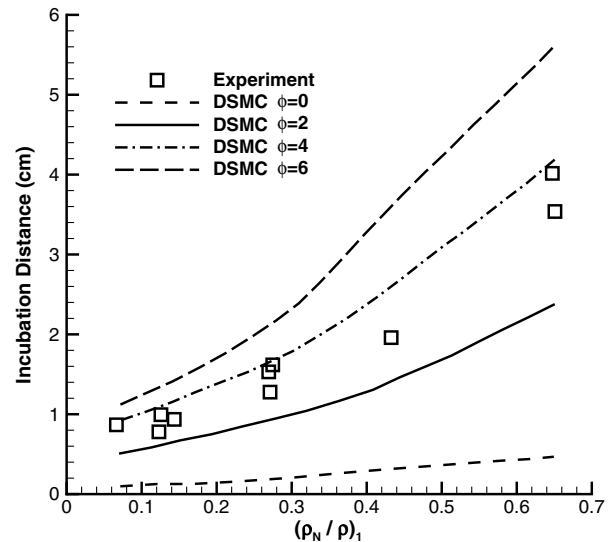


Fig. 8 Dissociation incubation distance as a function of atom mass fraction [37].

parameter ϕ is increased. Based on these comparisons, a value of $\phi = 3$ is generally employed for nitrogen dissociation.

Ideally, the reaction cross sections for use in DSMC would be determined directly rather than through indirect means such as measuring incubation distance as employed in Fig. 8. Measurements of reaction cross sections of interest in hypersonic air flows are not generally available, except for some reactions involving electrons. As ab initio computational chemistry techniques mature, there is the hope in the future that detailed computed databases can be used to help develop more accurate DSMC chemistry models. One example of such a database was constructed using a quasi-classical trajectory (QCT) method by Bose and Candler [39] for the Zeldovich exchange reaction:



This QCT database was employed [40] to perform a detailed evaluation of the TCE model for this particular reaction. Figure 9a shows reaction cross sections as a function of translational collision energy, at a particular rotational energy level ($J = 64$) of the reactant, N_2 , for three different reactant vibrational levels ($v = 0, 7, 13$). Clearly, the TCE model is not at all accurate for this reaction in terms of collision cross section. This poor comparison motivated the development of a new DSMC chemistry model that allows favoring from each of the translational, rotational, and vibrational energy modes. Termed the generalized collision energy (GCE) model, the reaction probability is given by [40]

$$P_{\text{GCE}} = A \frac{(\epsilon_{\text{tot}} - \epsilon_{\text{act}})^{b+\zeta+\frac{1}{2}}}{(\epsilon_{\text{tot}})^{\zeta+1-\omega}} (\epsilon_{\text{vib}})^\phi (\epsilon_{\text{tra}})^\alpha (1 - \epsilon_{\text{rot}}/\epsilon_{\text{tot}})^\beta \quad (29)$$

Figure 9b provides comparisons between the QCT data and the GCE reaction cross sections. Although the comparisons are far from perfect, they represent a significant improvement over the TCE model. For this particular reaction, the GCE model parameter values were $\alpha = 0.2$, $\beta = -0.5$, and $\phi = 0.3$.

The detailed QCT database makes it possible to evaluate several aspects of DSMC chemistry modeling. The second aspect concerns the energy distribution of the particles selected for reaction. Figure 10a shows the vibrational energy distribution function of the reacting N_2 molecules under a thermal equilibrium condition where all mode temperatures are at 5000 K. Clearly, the GCE model provides almost perfect agreement with the QCT data. A similar level of agreement is shown in Fig. 10b for a strongly nonequilibrium condition similar to that expected in hypersonic flow at high altitude.

When it is determined in a DSMC computation that a chemical reaction occurs, the activation energy is removed from the total

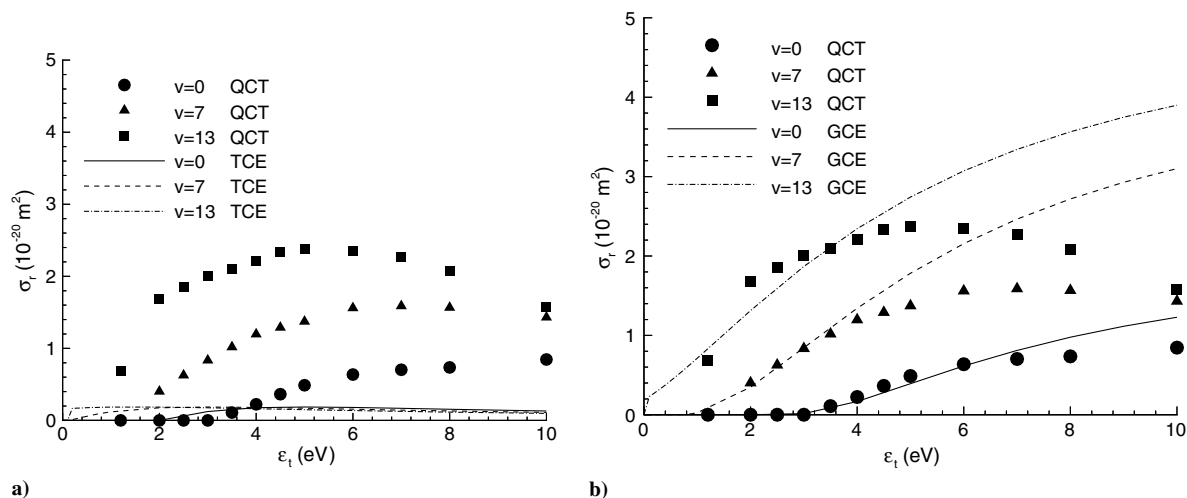


Fig. 9 Comparisons of DSMC chemistry models with QCT data for reaction cross sections for nitric oxide formation at $J = 64$ [40]: a) TCE, and b) GCE.

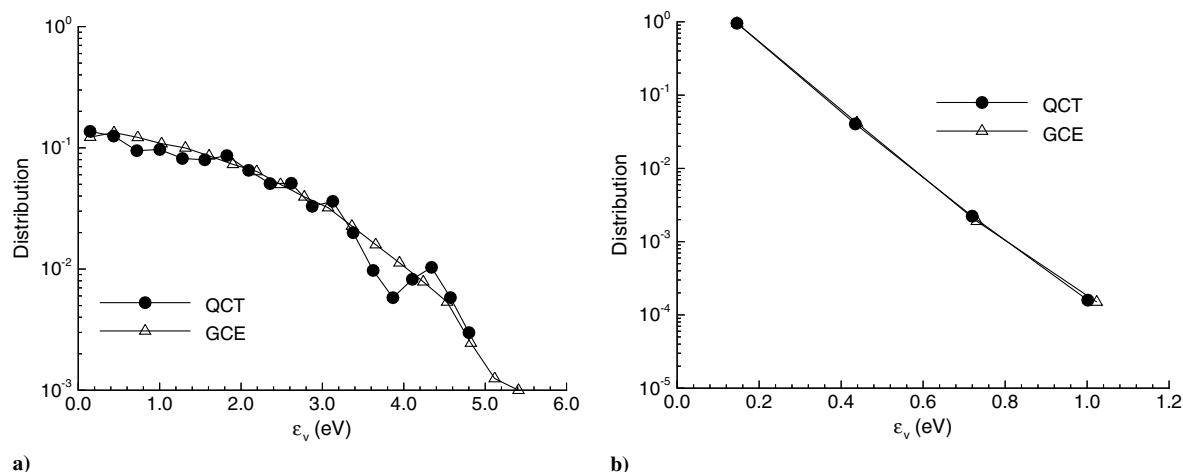


Fig. 10 Vibrational energy distribution function of reactants in nitric oxide formation [40]: a) $T_t = T_r = T_v = 5000$ K, b) $T_t = 14,000$ K, $T_r = 5000$ K, $T_v = 1000$ K.

collision energy, and then Borgnakke–Larsen procedures are used to distribute the remaining energy among the energy modes of the product particles. Once again, the QCT database allows this aspect of DSMC chemistry modeling to be assessed. Figures 11a and 11b show the vibrational energy distributions of the product NO molecules for the same two conditions shown in Figs. 10a and 10b. These comparisons indicate that the GCE model provides remarkably accurate simulation of the detailed phenomena captured by the QCT analysis.

Details of simulating backward chemical rate processes with the DSMC technique have been discussed by Boyd [41]. An important issue here is that the TCE model and its derivatives like VFD and GCE all depend on the use of a rate coefficient expressed in Arrhenius form. Backward rate coefficients are generally evaluated as the quotient of the forward rate coefficient and the equilibrium constant that is usually a highly complex function of temperature. Thus, it is not generally possible to express the backward rate coefficient in the

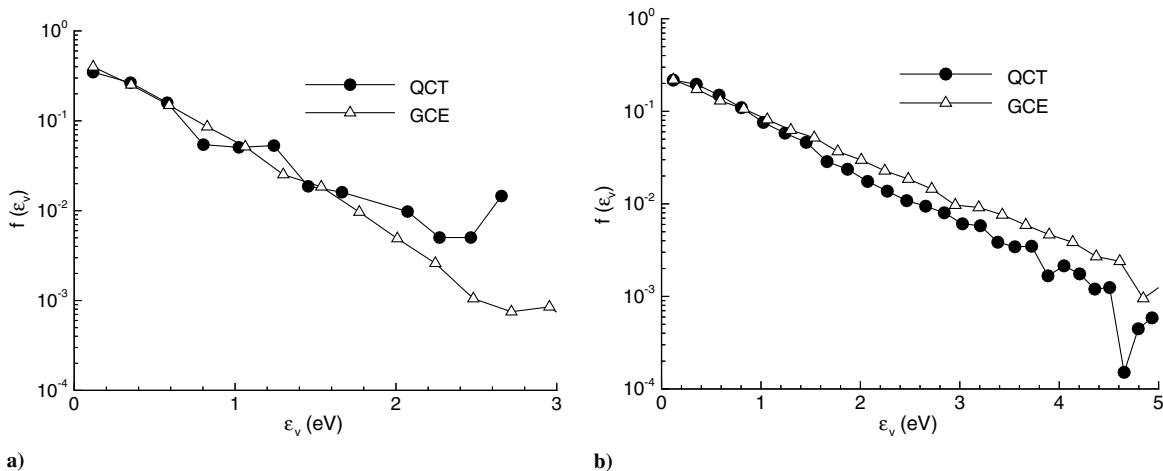


Fig. 11 Vibrational energy distribution function of products in nitric oxide formation [40]: a) $T_t = T_r = T_v = 5000$ K, and b) $T_t = 14,000$ K, $T_r = 5,000$ K, $T_v = 1000$ K.

simple Arrhenius form. This problem is addressed either by performing a best fit of the true backward rate coefficient to an Arrhenius form over a temperature range of interest or by calculating the temperature in each cell of the DSMC computation to evaluate the equilibrium constant exactly [41].

Although the DSMC method is based on the premise of a dilute gas for which three body collisions are ignored, it is sometimes important to include recombination in DSMC calculations, and models for such reactions are presented in [6,32].

Several other DSMC chemistry models relevant to hypersonic flows have been developed including the maximum entropy model [42], the weak vibrational bias model [43], the threshold line model [44], and the quantum kinetic model of Bird [45]. Many of the models are reviewed and evaluated in [46,47].

E. Charged Species

Ions and electrons are formed in sufficiently energetic hypersonic flows first through associative ionization and then through electron impact ionization. Although these reactions can be simulated using the TCE chemistry model with DSMC, the presence of electrons in a DSMC computation presents some special challenges. Specifically, due to their very low mass relative to other species, 1) the thermal velocity of an electron is orders of magnitude higher than for other species, and so 2) the collision frequency of electrons is orders of magnitude higher than for other species. If an electron was not charged, then the first problem would simply require use of a much smaller time step Δt than would be required otherwise. However, electrostatic attraction means that electrons and ions interact with one another such that electron diffusion is reduced and ion diffusion is slightly increased. A common model to describe this behavior is ambipolar diffusion, in which it is assumed that ions and electrons diffuse at the same rate. Bird [48] first introduced a DSMC model for ambipolar diffusion in which every electron particle was tied directly to the ion it was born with. These pairs of charged particles then move throughout the flow domain based on the velocity components of the ion particle. This method is reasonably successful, but it is difficult to implement and has poor performance at high ionization levels. Carlson and Hassan [49] introduced a scheme in which electric fields are evaluated based on averaged charged particle properties. The charged particles are moved in these fields with the electrons processed at a significantly smaller time step than the ions. An alternate approach was proposed by Boyd [50] in which electron particles are moved throughout the domain based on cell-averaged ion velocities. The electron and ion particles are no longer tied together explicitly, making the method much easier to implement, and the approach is found to be generally more robust than Bird's technique. Using either of the Bird [48] or Boyd [50] approaches means that electron particles are moved at the time scale of the heavier species, and so there is no need to reduce the simulation time step. In a more fundamental study under hypersonic conditions, Farbar and Boyd [51] calculated the plasma potential from the Poisson equation that accounts for lack of charge neutrality. Important differences from the standard DSMC models for treating the electrons [48,50] were found in the shock structure and at a sheath formed at a vehicle wall.

The second issue faced in simulating electrons, related to their significantly higher collision frequency, must also be addressed. The obvious choices are as follows: 1) reduce the global time step; 2) allow electron particles to collide more than once over each iteration; or 3) perform subcycling of collisions. Subcycling involves calling the collision subroutine several times over each movement iteration so that the number of collision pairs to be tested is evaluated several times using a subcycling time step Δt_c that is smaller than the global time step Δt , usually by a factor of about 100.

F. Radiation

Radiation is of interest in hypersonic flows in terms of the emission signature and at very high speeds for the radiative component of vehicle heating. Emission signatures are usually simulated decoupled from the flowfield, and examples are discussed of such analysis later in this article. There have been several DSMC studies on emission

signatures where the excited states of interest were simulated directly as additional chemical species [52,53]. A key issue here is the availability, or lack of it, of accurate excitation rate coefficients. For estimation of radiative heating, Bird first included thermal radiation effects in DSMC for analysis of an aeroassist orbital transfer vehicle [48,54], and his ideas were extended by Carlson and Hassan [55]. These models essentially represent an extension of the rotational and vibrational relaxation models using Borgnakke–Larsen energy disposal. As a phenomenological approach, these models performed reasonably well, but this is another area where further research is warranted.

G. Gas–Surface Interaction

The most important outcome from many DSMC analyses of hypersonic flows is the determination of the properties at the vehicle surface, and in particular the aerodynamic forces and moments, and the convective heat transfer. The surface properties are of course very sensitive to the model assumed in DSMC for gas–surface interaction. The most common gas–surface interaction model used in DSMC is fully diffuse reflection, in which a particle reflects from the surface with new velocity components that are sampled from Maxwellian distributions characterized by the wall temperature (note that the velocity component normal to the surface is sampled from a biased Maxwellian distribution). In the diffuse model, the particle's internal energies are also sampled from the appropriate equilibrium distribution, such as Eq. (12) for rotation, using the wall temperature. The opposite limit to diffuse reflection is specular reflection, in which the only change to the particle's properties is its velocity component normal to the surface that is simply reversed in sign. Many DSMC computations use an accommodation coefficient α to simulate a combination of diffuse and specular reflections such that $\alpha = 1$ is fully diffuse and $\alpha = 0$ is fully specular, and this approach is sometimes referred to as the Maxwell model for gas–surface interaction. Real engineering surfaces generally require a value in the range of $\alpha = 0.8$ – 0.9 .

Figure 12 shows a comparison of measured [56] and computed distributions of argon atoms reflecting from a platinum surface. Clearly, the measured pattern is not reproduced by either of the specular or diffuse reflection models (and indeed cannot be reproduced by any combination of the two models). This type of comparison led to the development of more sophisticated gas–surface interaction models for DSMC, for example the Cercignani–Lampis–Lord (CLL) model [57]. Such models tend to have a stronger theoretical basis,

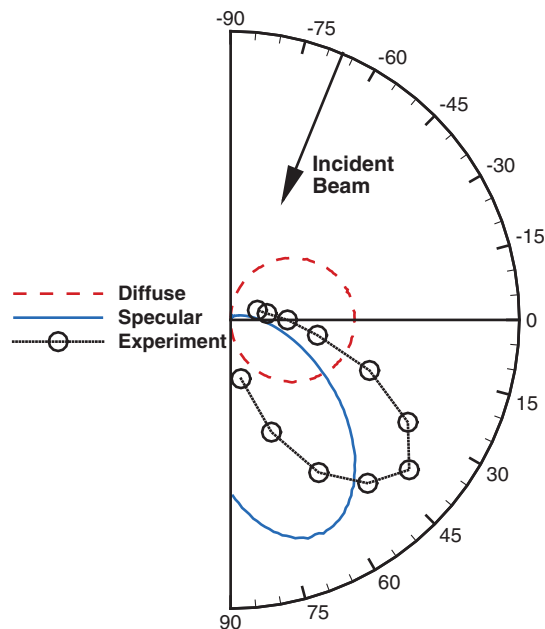


Fig. 12 Distributions of argon scattering from platinum: measurements from [56].

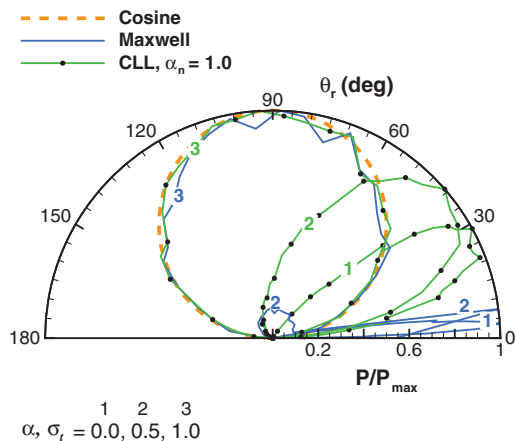


Fig. 13 Computed scattering distributions from a DSMC simulation of hypersonic flow of N_2 over a flat plate [58].

such as using a reciprocity relation, and offer more control through use of additional parameters. Figure 13 shows DSMC computed particle reflection distributions for Mach 10 flow of N_2 over a flat plate [58] for a variety of different gas–surface interaction models. Fully diffuse reflection (Maxwell, $\alpha = 1.0$) gives the cosine distribution. Fully specular reflection (Maxwell, $\alpha = 0$) gives a distribution that is almost tangent to the surface. Through variation of the accommodation coefficient σ_T (a parameter in the CLL model), a wide range of reflected distributions can be generated that lie between the ideal limits of diffuse and specular reflection. Figure 14 compares profiles of the velocity component parallel to the flat plate measured by Cecil and McDaniel [59] using planar laser-induced fluorescence and a number of DSMC computations using the Maxwell and the CLL reflection models with a range of model parameters. Note that, at the surface, both measurements and computations show a significant level of velocity slip. Such comparisons allow identification of appropriate parameter values for use in the CLL model. However, the use of such models is relatively limited due to the lack of this type of basic information to identify parameter values for real systems of interest. This is another area where computational chemistry simulations using molecular dynamics can provide databases that can be used to build more advanced DSMC physical models.

There are two important phenomena arising from gas–surface interaction under high-Knudsen-number conditions: velocity slip and temperature jump. The relatively low number of collisions experienced by a gas at high Kn means that the average velocity at the wall has a finite value, even for a surface with fully diffuse reflection. This phenomenon reduces shear stress and may affect boundary-layer separation. Similarly, due to the low collision rate, the temperature of the gas at the wall is not equilibrated with the surface. In a hypersonic flow where the wall temperature is cooler than the gas, this phenomenon leads to a reduction in heat transfer. These

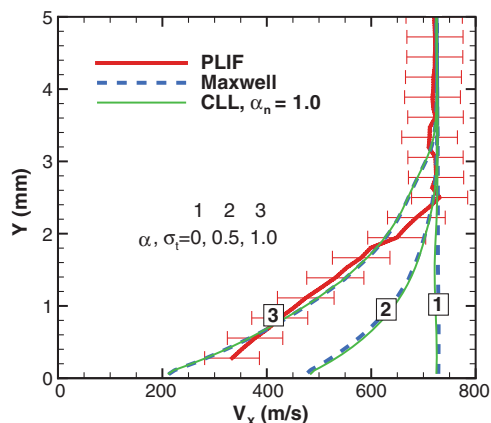


Fig. 14 Velocity profiles for hypersonic flow of N_2 over a flat plate [58].

effects are naturally included in a DSMC simulation using the diffuse reflection and CLL models, whereas the usual approach for CFD is to assume no slip and no temperature jump at a wall. The omission of these high-Knudsen-number surface phenomena in CFD partially explains some of the differences noted in the detailed comparisons under hypersonic flow conditions of DSMC and CFD reported in [9,10]. One approach to try and extend the usefulness of CFD into the high-Knudsen-number range is to employ velocity slip and temperature jump models; see for example [10]. However, although some of these models do improve the agreement between CFD and DSMC results for surface quantities, it is not always achieved with a corresponding improvement in the comparisons of the flow properties. This situation again illustrates the need to perform non-continuum computations of high-Knudsen-number flows using kinetic methods such as the DSMC technique.

IV. Direct Simulation Monte Carlo Analysis of Hypersonic Flows

In the following sections, a review is provided of the status of the application of the DSMC technique to flows around hypersonic blunt vehicles. We first consider the application of DSMC to analyze hypersonic experiments conducted in ground-based facilities. Next, use of DSMC to analyze Earth entry flows is discussed. Finally, a summary of the use of DSMC for analysis of planetary entry is provided.

A. Analyses of Hypersonic Laboratory Experiments

Generation of rarefied, hypersonic flows in ground-based facilities presents a technical challenge, and very few data sets exist that enable a detailed assessment of DSMC codes. One notable code validation activity resulted from a NATO–AGARD working group on hypersonics. A planetary probe geometry was tested under rarefied, hypersonic flow conditions in several different experimental facilities, and a number of research groups generated DSMC results for comparison. Many articles have been published on these studies, and details of the experiments and numerical results are summarized in [60]. Examples of results obtained using the MONACO DSMC code [14] are provided in Figs. 15–17. Figure 15 shows the unstructured mesh that has been adapted to the local mean free path for the experiment conducted in the SR3 wind-tunnel in nitrogen at a Mach number of 20 and a Knudsen number of 0.03 [61]. Despite the high Mach number, this was a low-enthalpy facility with a total temperature of 1100 K. Thus, neither vibrational relaxation nor chemistry occurs in these flows. Although such experiments provide the opportunity to assess the collision cross sections (VHS, VSS) and rotational relaxation models [23], they provide no insight on the DSMC models for vibrational relaxation [32] and chemistry [37]. An electron beam diagnostic was employed in the SR3 wind-tunnel to measure the density field around the capsule geometry, and Fig. 16 shows the excellent agreement obtained between DSMC and the

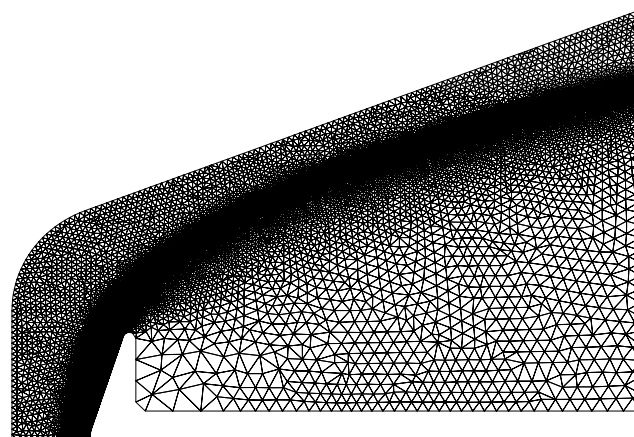


Fig. 15 Adapted mesh for Mach 20, $Kn = 0.03$ flow over a planetary probe.

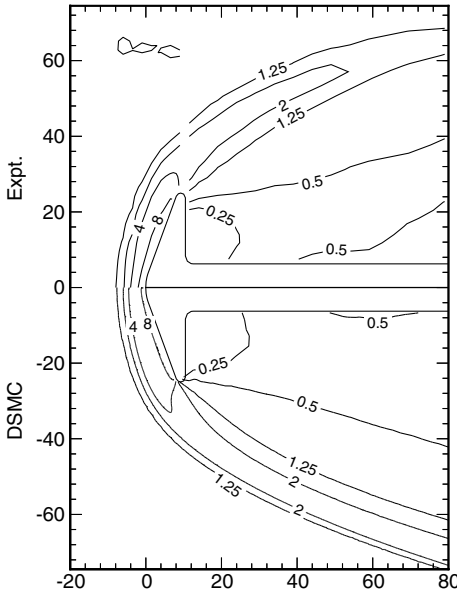


Fig. 16 Contours of ρ/ρ_∞ for Mach 20, $Kn = 0.03$ flow over a planetary probe [14].

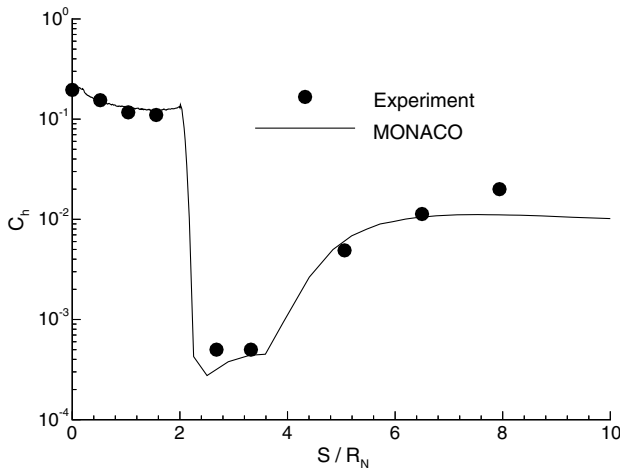


Fig. 17 Heat flux coefficient on a planetary probe at Mach 15.6, $Kn = 0.002$ [14].

measured data. Another experiment was conducted using the same geometry in the Large Energy National Shocktunnel (LENS) facility again in nitrogen at a Mach number of 15.6 and a Knudsen number of 0.002 [62]. This higher-enthalpy experiment had a total temperature of 4350 K so that vibration was activated but there was still no chemistry. Figure 17 shows comparisons between measurements

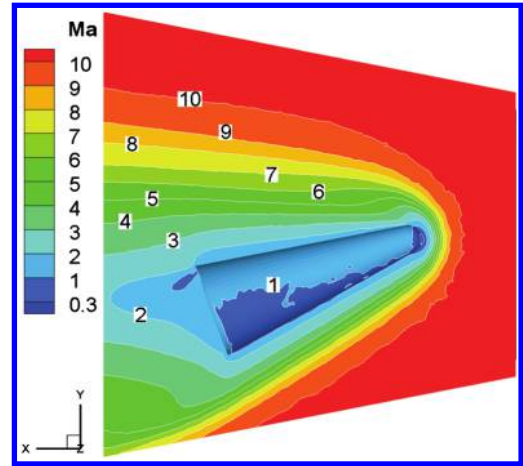


Fig. 18 Contours of Mach number about a cone at angle of attack [67].

from LENS and DSMC computation for the heat flux along the surface of the probe. Again, excellent agreement is obtained. Although studies of this type indicate that the DSMC method is an accurate simulation method, the flows are not energetic enough to permit detailed assessment of DSMC thermochemical models.

There are very few comprehensive data sets measured under rarefied conditions involving three-dimensional (3-D) flows, although the experiments in SR3 did generate some 3-D data sets. Another interesting example concerns data obtained in a low-density, hypersonic wind tunnel in the 1960s as part of the Apollo program [63–66]. A variety of very small models were tested that included cones as well as capsules such as Apollo, Gemini, and Mercury. The MONACO DSMC code [14] was applied to simulate the tests on the cones that were conducted in a Mach 10 flow of nitrogen at a global Knudsen number of 0.065 [67]. Figure 18 shows contours of Mach number computed for an angle of attack of 20 deg. Figures 19a and 19b show comparisons for aerodynamic properties between measurement and simulation. In these figures, “FMF” shows results obtained from free molecular theory, and “MN” indicates modified Newtonian theory [67]. For both the drag and the pitching moment, the 3-D DSMC computations are in excellent agreement with the measured data. The comparisons also show that neither the free molecular theory nor the Newtonian theory provide any useful results for this condition, indicating that the more computationally expensive DSMC approach is required. Figures 20 and 21 show the corresponding results for Mach 10 flow of nitrogen over a model of the Apollo Command Module capsule at a Knudsen number of 0.067 conducted in the exact same facility as the cone studies [67]. In this case, significant differences between simulation and measurement are found for the drag force. Similarly, there is relatively poor agreement between the MONACO DSMC solutions for pitching moment coefficient and the measured values, as shown in Fig. 21b. For example, DSMC predicts a trim angle that is about 15 deg

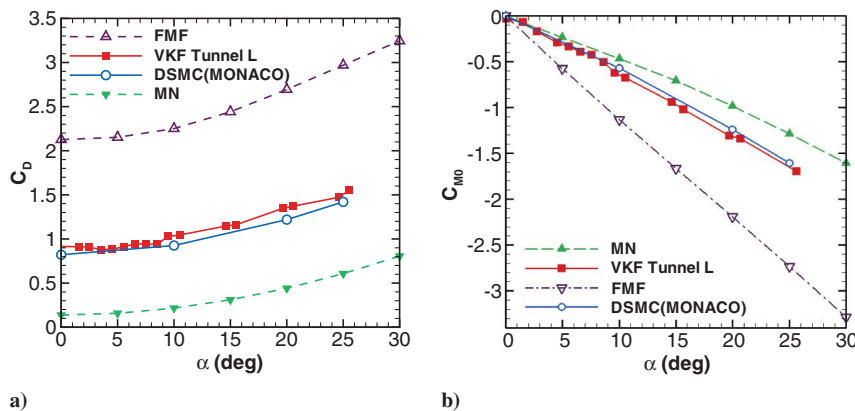


Fig. 19 Aerodynamics for a cone at angle of attack [67]: a) drag coefficient, and b) pitching moment coefficient.

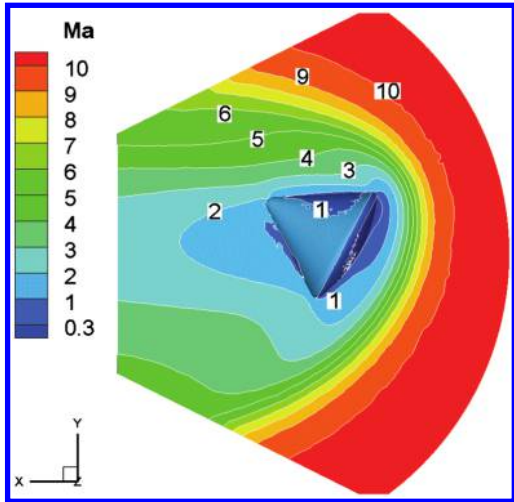


Fig. 20 Contours of Mach number about a capsule at angle of attack [67].

different from the experiments. Independent DSMC computations of the same flows were performed using the DS3V DSMC code, and the results show excellent agreement with the MONACO DSMC profiles. The fact that good agreement between measurement and simulation is obtained in one case and not in another for two tests performed in the same experimental facility illustrates the difficulties involved in validating the DSMC approach using the limited amounts of laboratory data. This situation clearly calls out for additional experiments to be carried out carefully under hypersonic, rarefied flow conditions.

Despite the lack of detailed validation using laboratory data, the DSMC technique has been applied to analyze the aerodynamics and aerothermodynamics of many different spacecraft entering the atmospheres of Earth and of planets in the Solar System. In the following sections, a review is provided of prior DSMC studies of atmospheric entry.

B. Analyses of Earth Entry Flows

The successful return of payloads (including people) from space requires use of blunt vehicle geometries to provide reduced levels of deceleration and heat load. One of the first applications of the DSMC technique to analyze the entry aerodynamics of a full-scale vehicle was performed by Rault [68], who simulated the aerodynamics of the Space Shuttle Orbiter at altitudes from 170 to 100 km, where the Knudsen number ranged from about 2 to 0.005 (see Fig. 1). Performed around 1993, these 3-D computations were extremely expensive for the time. Comparison of the results obtained was made with free molecular theory, with CFD calculations, with aerodynamic bridging relations, and with Space Shuttle flight data. Very good agreement was obtained between DSMC and flight data for lift-to-drag ratio and for the axial force coefficient. Significant discrepancies

were, however, found both for the normal force coefficient and for the pitching moment.

Ivanov et al. [69] describe DSMC analysis using SMILE of the aerodynamics of a Russian entry capsule over the altitude range from 130 to 85 km. Comparisons made between the DSMC results and free-flight experimental measurements for the axial and normal force and pitching moment coefficients revealed excellent agreement. The SMILE code was also applied by Markelov et al. [70] to help in the analysis of deorbiting the Russian space station Mir. The highly complex, 3-D geometry was analyzed using DSMC over the altitude range from 200 to 110 km, for which the effective Knudsen number varies from about 20 to 0.05. It was found that aerodynamic coefficients do not change significantly until about 120 km and that the vehicle is statically stable throughout this altitude range.

Moss [71] applied the DS2V DSMC code to analyze the aerothermodynamics of a proposed ballute deceleration system for Earth entry at velocities from 14 to 7 km/s and altitudes from 200 to 100 km. A number of interesting and important conclusions were drawn from the analyses, including the observation of unsteady flow phenomena for certain capsule-ballute configurations, and that the highest heat fluxes were experienced on the ballute tether.

NASA's Stardust sample return capsule (SRC) entered the Earth's atmosphere at a velocity of about 12.8 km/s, making it the most energetic man-made vehicle to undergo hypersonic entry. The DSMC codes G2 (an earlier form of Bird's DS2V code) and DSMC Analysis Code (DAC) were used by Wilmoth et al. [72] before the flight in 1998 to analyze the entry aerodynamics. Focused on aerodynamics, those early Stardust DSMC computations omitted ionization and employed simple thermochemical models. During the SRC entry in 2006, a suite of spectroscopic instruments measured the radiation emitted from the very strong bow shock wave formed around the vehicle [73]. With the availability of detailed experimental measurements, several further DSMC studies of the SRC entry have been performed recently that employed state-of-the-art thermochemistry modeling including ionization [74–76]. Profiles of the temperatures from the various energy modes (T_t = translation; T_r = rotational; T_v = vibrational; T_e = electron) predicted along the stagnation streamline of the SRC at an altitude of 81 km are shown in Fig. 22a. The separation among these profiles illustrates the strong degree of thermal nonequilibrium of the gas under these extreme conditions. Profiles along the stagnation streamline of the mole fractions of selected chemical species are shown in Fig. 22b, illustrating the high degree of chemical activity present in the flow. The NEQAIR radiation code [77] was employed to estimate the radiation spectra based on the DSMC flowfield results. An example of a direct comparison between the computed and measured spectra at an altitude of 81 km is shown in Fig. 23. Generally, it is found that air plasma atomic line features are quite well predicted by the combination of DSMC and NEQAIR.

C. Analyses of Planetary Entry Flows

Several DSMC studies have been performed of the aerodynamics and heating of vehicles entering the Mars atmosphere that consists of

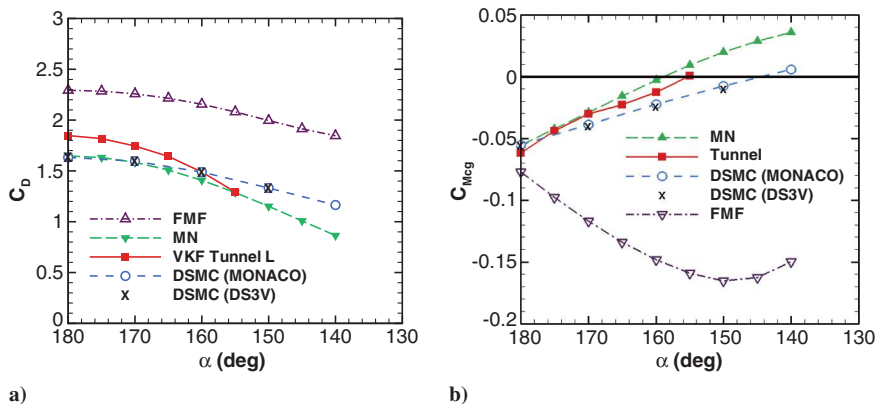


Fig. 21 Capsule at angle of attack [67]: a) drag coefficient, and b) pitching moment coefficient.

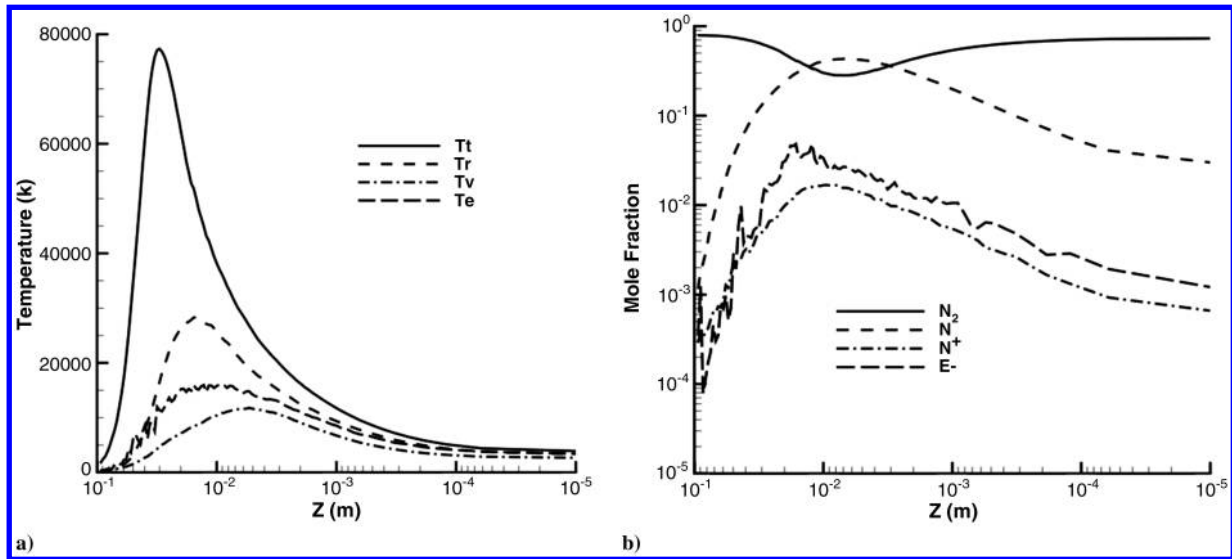


Fig. 22 Profiles along the Stardust SRC stagnation streamline at 81 km [75]: a) temperature, and b) species mole fractions.

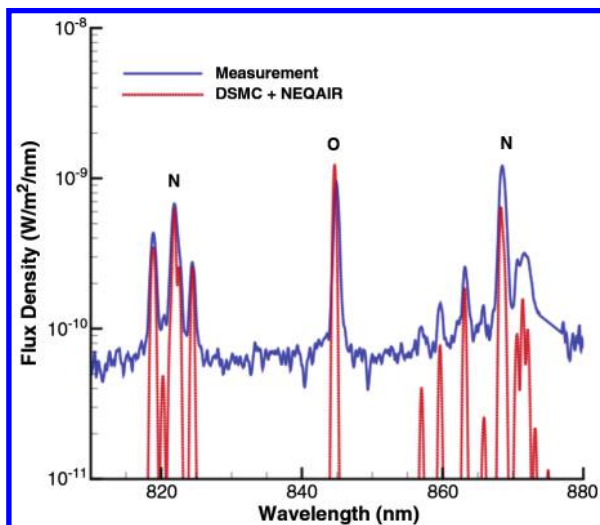


Fig. 23 Comparison of measured and computed spectra for Stardust at 81 km [76].

about 95% of CO₂ and 5% of N₂. Direct comparisons between DSMC predictions obtained using DAC and flight measurements taken during the Viking 1 entry for the ratio of normal to axial aerodynamic force yielded excellent agreement [78]. Similar comparisons for the drag coefficient indicated that the DSMC results were not inconsistent with the measurements, although the flight data were only taken in the continuum regime, and so direct comparison with DSMC was not possible. An extensive aerodynamics database was constructed using G2 and DAC for the Mars Pathfinder mission by Moss et al. [79]. The DSMC analyses traversed a Knudsen number range from 100 to 0.027 and angle of attack variation from 0 to 35 deg. The database was used for Martian atmosphere density reconstruction and spacecraft attitude determination based on in-flight accelerometer data. DAC was again used by Wilmoth et al. [80] to analyze the aerothermodynamics of the Mars Global Surveyor (MGS). The data generated were employed for spacecraft design, mission planning, flight operations, and atmospheric reconstruction. MGS was the first planetary entry mission designed to use aerobraking to customize its orbit by gradually descending into the Mars atmosphere over a period of several months. The Knudsen number during the aerobraking process varied from about 10 down to 0.05 placing the flows firmly in the transition regime. The DSMC generated aerothermodynamic database played a key role in the successful completion of the aerobraking maneuver. Finally, the

DAC and G2 DSMC codes were applied by Moss et al. [81] to generate an aerothermodynamic database for Mars Microprobes. Aerodynamics characteristics and surface heat flux were determined over a Knudsen number range from 80 to 0.002.

DSMC analyses have been performed on the interaction of the Magellan spacecraft with the atmosphere of Venus. The composition of the Venusian atmosphere is 76%CO₂, 9% CO, 9% Ar, and 6%N₂. Near the end of its mission, the Magellan spacecraft for the first time successfully performed an aerobrake maneuver in the atmosphere to circularize its orbit. Rault [82] applied a 3-D DSMC code to compute the aerodynamic characteristics of the complex spacecraft geometry at an altitude of 140 km as part of the assessment of whether to perform the aerobrake maneuver. The flow had a freestream Knudsen number of about 10, and the DSMC results indeed showed only minor departures from free molecular analysis. A similar analysis was reported by Haas and Schmitt [83] using a different 3-D DSMC code. They found relatively small differences of 5–10% between DSMC and free molecular theory for forces, moments, and heating. In a related study, Haas and Feiereisen [84] used DSMC to analyze the heating to the Magellan spacecraft during proposed aeropass maneuvers.

DSMC analysis of the rarefied portion of the entry of the Galileo probe into the atmosphere of Jupiter was performed by Haas and Milos [85]. The Jovian atmosphere consists of 89%H₂ and 11% He. Seven points along the entry trajectory were investigated, with the freestream Knudsen number ranging from 400 to 0.07 and all at zero angle of attack. The purpose of the analysis was to accurately compute the drag coefficient that was needed to infer atmospheric density from an accelerometer experiment. A unique aspect of this study was the coupling of the convective heating predictions from DSMC to a thermal response code to estimate outgassing rates of pyrolyzed gas originating in the thermal protection system of the probe. The predicted flux of pyrolysis products was as much as an order of magnitude higher than the freestream flux and had a significant effect on the probe aerodynamics, for example reducing the drag coefficient by 15%.

V. Conclusions

The direct simulation Monte Carlo method (DSMC) has evolved over more than 50 years into a powerful analysis tool for computation of kinetic nonequilibrium hypersonic flows. The heart of the technique is its detailed treatment of collisional phenomena including momentum exchange, relaxation of internal energy modes, chemistry, radiation, and gas–surface interaction. In this article, the current status of DSMC models for simulating these physical phenomena has been reviewed. It was demonstrated that the DSMC technique is able to simulate accurately highly nonequilibrium

velocity distribution functions generated inside strong shock waves of noble gases. However, there is still a need for development of collision cross section models for large temperature ranges and for specific species interactions. Detailed validation of rotational energy relaxation models was also demonstrated at the level of rotational energy distribution functions measured inside a strong shock wave. However, there are no corresponding measurements of such phenomena at the high-temperature conditions of hypersonic flows with the result that DSMC models of such phenomena are not yet validated. Both phenomenological and detailed, quantum transition DSMC models for vibrational relaxation were discussed. Similar to the situation for rotational relaxation, measurements of vibrational energy distributions in hypersonic flows are required to allow evaluation of the DSMC models. Several different DSMC chemistry models were described and two of them evaluated using detailed information obtained from ab initio computational chemistry analysis. In the absence of detailed measurements of reaction cross sections, such analyses appear very promising to help in the construction and evaluation of detailed DSMC thermochemistry models. Descriptions were also provided of the present status for DSMC computation of charged species (ions, electrons) and radiation. These are also areas where further work is required. The status for DSMC computation of gas–surface interaction was reviewed. It was shown that the idealized Maxwell model employing a combination of diffuse and specular reflection is not able to accurately reproduce reflections measured under hypersonic conditions. Although more sophisticated gas–surface interaction models have been developed, their use is limited due to the difficulty in determining parameters in the models. Again, this is an area where ab initio computational analysis using molecular dynamics may be useful for building improved DSMC modeling capabilities.

In terms of application to hypersonic blunt body flows, assessment of the DSMC technique using ground-based experimental measurements has been largely successful for surface properties (heat flux, pressure) and overall aerodynamics (drag, pitching moment). However, all of these studies are limited to conditions without chemistry due to the technical challenges of generating high-energy, rarefied flows. The DSMC technique has also been applied to analyze the entry into Earth's atmosphere of several different blunt-body configurations, including comparisons with flight measurements for the Space Shuttle, space station Mir, and Stardust. The DSMC technique generally provides excellent comparisons with most of the measured data sets. The confidence obtained in the physical accuracy of the DSMC method has led to its application to analyze the aerothermodynamic performance of proposed vehicles such as ballutes and to aid in the design of entry flight experiments. The DSMC technique has played a key role in the design and flight analysis of several NASA Mars entry missions including the entry of Pathfinder and the aerobraking of Mars Global Surveyor. Further notable applications of the DSMC technique to planetary entries include analysis of the aerobraking maneuver of the Magellan spacecraft in the atmosphere of Venus and entry into Jupiter of the Galileo probe.

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References

- [1] Vincenti, W. G., and Kruger, C. H., *Introduction to Physical Gas Dynamics*, Wiley, New York, 1965.
- [2] Agarwal, R. K., Yun, K.-Y., and Balakrishnan, R., "Beyond Navier–Stokes: Burnett Equations for Simulation of Transitional Flows," *Physics of Fluids*, Vol. 13, 2001, pp. 3061–3085.
- [3] Tcheremissine, F. G., "Solution of the Boltzmann Kinetic Equation for High Speed Flows," *Computational Mathematics and Mathematical Physics*, Vol. 46, No. 2, 2006, pp. 315–329. doi:10.1134/S0965542506020138
- [4] Bird, G. A., "Approach to Translational Equilibrium in a Rigid Sphere Gas," *Physics of Fluids*, Vol. 6, No. 10, 1963, pp. 1518–1519. doi:10.1063/1.1710976
- [5] Bird, G. A., *Molecular Gas Dynamics and the Direct Simulation of Gas Flows*, Oxford Univ. Press, Oxford, England, U.K., 1994.
- [6] Bird, G. A., *The DSMC Method*, 2013.
- [7] Wagner, W., "A Convergence Proof for Bird's Direct Simulation Monte Carlo," *Journal of Statistical Physics*, Vol. 66, Nos. 3–4, 1992, pp. 1011–1044. doi:10.1007/BF01055714
- [8] Boyd, I. D., "Computation of Atmospheric Entry Flow About a Leonid Meteoroid," *Earth, Moon, and Planets*, Vol. 82, No. 3, 1998, pp. 93–108. doi:10.1023/A:1017042404484
- [9] Lofthouse, A. J., Boyd, I. D., and Wright, M. J., "Effects of Continuum Breakdown on Hypersonic Aerothermodynamics," *Physics of Fluids*, Vol. 19, No. 2, 2007, p. 027105. doi:10.1063/1.2710289
- [10] Lofthouse, A. J., Scalabrin, L. C., and Boyd, I. D., "Velocity Slip and Temperature Jump in Hypersonic Aerothermodynamics," *Journal of Thermophysics and Heat Transfer*, Vol. 22, No. 1, 2008, pp. 38–49. doi:10.2514/1.31280
- [11] Holman, T. D., and Boyd, I. D., "Effects of Continuum Breakdown on Hypersonic Aerothermodynamics for Reacting Flow," *Physics of Fluids*, Vol. 23, No. 2, 2011, p. 027101. doi:10.1063/1.3541816
- [12] Alder, B. J., and Wainwright, T. E., "Studies in Molecular Dynamics," *Journal of Chemical Physics*, Vol. 27, No. 5, 1957, pp. 1208–1209. doi:10.1063/1.1743957
- [13] Boyd, I. D., "Vectorization of a Monte Carlo Simulation Scheme for Nonequilibrium Gas Dynamics," *Journal of Computational Physics*, Vol. 96, No. 2, 1991, pp. 411–427. doi:10.1016/0021-9991(91)90243-E
- [14] Dietrich, S., and Boyd, I. D., "Scalar and Parallel Optimized Implementation of the Direct Simulation Monte Carlo Method," *Journal of Computational Physics*, Vol. 126, No. 2, 1996, pp. 328–342. doi:10.1006/jcph.1996.0141
- [15] LeBeau, G. J., "A Parallel Implementation of the Direct Simulation Monte Carlo Method," *Computer Methods in Applied Mechanics and Engineering*, Vol. 174, Nos. 3–4, 1999, pp. 319–337. doi:10.1016/S0045-7825(98)00302-8
- [16] Bird, G. A., "Sophisticated Versus Simple DSMC," *Proceedings of the 25th International Symposium on Rarefied Gas Dynamics*, edited by Ivanov, M. S., and Rebrov, A. K., Russian Academy of Sciences, Novosibirsk, Russia, 2007.
- [17] Bird, G. A., "Monte Carlo Simulation in an Engineering Context," *Rarefied Gas Dynamics, Part 1*, Vol. 74, Progress in Astronautics and Aeronautics, AIAA, New York, 1981, pp. 239–255.
- [18] Koura, K., and Matsumoto, H., "Variable Soft Sphere Molecular Model for Air Species," *Physics of Fluids A*, Vol. 4, No. 5, 1992, pp. 1083–1085. doi:10.1063/1.858262
- [19] Alsmeyer, H., "Density Profiles in Argon and Nitrogen Shock Waves Measured by the Absorption of an Electron Beam," *Journal of Fluid Mechanics*, Vol. 74, No. 3, 1976, pp. 497–513. doi:10.1017/S0022112076001912
- [20] Pham-Van-Diep, G., Erwin, D., and Muntz, E. P., "Nonequilibrium Molecular Motion in a Hypersonic Shock Wave," *Science*, Vol. 245, No. 4918, 1989, pp. 624–626. doi:10.1126/science.245.4918.624
- [21] Farbar, E. D., and Boyd, I. D., "Simulation of FIRE II Reentry Flow Using the Direct Simulation Monte Carlo Method," *40th Thermophysics Conference*, AIAA Paper 2008-4103, June 2008.
- [22] Balakrishnan, J., Boyd, I. D., and Braun, D. G., "Monte Carlo Simulation of Vapor Transport in Physical Vapor Deposition of Titanium," *Journal of Vacuum Science and Technology A*, Vol. 18, No. 3, 2000, pp. 907–916. doi:10.1116/1.582274
- [23] Boyd, I. D., "Analysis of Rotational Nonequilibrium in Standing Shock Waves of Nitrogen," *AIAA Journal*, Vol. 28, No. 11, 1990, pp. 1997–1999. doi:10.2514/3.10511
- [24] Parker, J. G., "Rotational and Vibrational Relaxation in Diatomic Gases," *Physics of Fluids*, Vol. 2, No. 4, 1959, pp. 449–462. doi:10.1063/1.1724417
- [25] Borgnakke, C., and Larsen, P. S., "Statistical Collision Model for Monte Carlo Simulation of Polyatomic Gas Mixture," *Journal of Computational Physics*, Vol. 18, No. 4, 1975, pp. 405–420. doi:10.1016/0021-9991(75)90094-7

- [26] Lumpkin, F. E., Haas, B. L., and Boyd, I. D., "Resolution of Differences Between Collision Number Definitions in Particle and Continuum Simulations," *Physics of Fluids A*, Vol. 3, No. 9, 1991, pp. 2282–2284.
doi:10.1063/1.857964
- [27] Boyd, I. D., "Relaxation of Discrete Rotational Energy Distributions Using a Monte Carlo Method," *Physics of Fluids A*, Vol. 5, No. 9, 1993, pp. 2278–2286.
doi:10.1063/1.858531
- [28] Robben, R., and Talbot, L., "Experimental Study of the Rotational Distribution Function of Nitrogen in a Shock Wave," *Physics of Fluids*, Vol. 9, No. 4, 1966, pp. 653–662.
doi:10.1063/1.1761730
- [29] Valentini, P., Chonglin, Z., and Schwartzentruber, T. E., "Molecular Dynamics Simulation of Rotational Relaxation in Nitrogen: Implications for Rotational Collision Number Models," *Physics of Fluids*, Vol. 24, No. 10, 2012, p. 106101.
doi:10.1063/1.4757119
- [30] Millikan, R. C., and White, D. R., "Systematics of Vibrational Relaxation," *Journal of Chemical Physics*, Vol. 39, No. 12, 1963, pp. 3209–3213.
doi:10.1063/1.1734182
- [31] Park, C., *Nonequilibrium Hypersonic Aerothermodynamics*, Wiley, New York, 1990.
- [32] Boyd, I. D., "Analysis of Vibration-Dissociation-Recombination Processes Behind Strong Shock Waves of Nitrogen," *Physics of Fluids A*, Vol. 4, No. 1, 1992, pp. 178–185.
doi:10.1063/1.858495
- [33] Bergemann, F., and Boyd, I. D., "New Discrete Vibrational Energy Method for the Direct Simulation Monte Carlo Method," *Rarefied Gas Dynamics*, Vol. 158, Progress in Astronautics and Aeronautics, AIAA, Washington, D.C., 1994, p. 174.
- [34] Boyd, I. D., and Josyula, E., "State Resolved Vibrational Relaxation Modeling for Strongly Nonequilibrium Flows," *Physics of Fluids*, Vol. 23, No. 5, 2011, p. 057101.
doi:10.1063/1.3584128
- [35] Adamovich, I. V., Macheret, S. O., Rich, J. W., and Treanor, C. E., "Vibrational Energy Transfer Rates Using a Forced Harmonic Oscillator Model," *Journal of Thermophysics and Heat Transfer*, Vol. 12, No. 1, 1998, pp. 57–65.
doi:10.2514/2.6302
- [36] Meolans, J. G., and Brun, R., "Nonequilibrium Vibrational Population Behind Shock Waves: Comparison Theory—Experiments," *Proceedings of the 15th International Symposium on Rarefied Gas Dynamics*, Teubner, Stuttgart, 1986, p. 345.
- [37] Haas, B. L., and Boyd, I. D., "Models for Direct Monte Carlo Simulation of Coupled Vibration-Dissociation," *Physics of Fluids A*, Vol. 5, No. 2, 1993, pp. 478–489.
doi:10.1063/1.858870
- [38] Hornung, H. G., "Induction Time for Nitrogen Dissociation," *Journal of Chemical Physics*, Vol. 56, No. 6, 1972, pp. 3172–3174.
doi:10.1063/1.1677661
- [39] Bose, D., and Candler, G. V., "Thermal Rate Constants of the $N_2 + O \rightarrow NO + N$ Reaction Using Ab Initio $3A''$ and $3A'$ Potential Energy Surfaces," *Journal of Chemical Physics*, Vol. 104, No. 8, 1996, pp. 2825–2834.
doi:10.1063/1.4711106
- [40] Boyd, I. D., Bose, D., and Candler, G. V., "Monte Carlo Modeling of Nitric Oxide Formation Based on Quasi-Classical Trajectory Calculations," *Physics of Fluids*, Vol. 9, No. 4, 1997, pp. 1162–1170.
doi:10.1063/1.869479
- [41] Boyd, I. D., "Modeling Backward Chemical Rate Processes in the Direct Simulation Monte Carlo Method," *Physics of Fluids*, Vol. 19, No. 12, 2007, p. 126103.
doi:10.1063/1.2825038
- [42] Gallis, M. A., and Harvey, J. K., "Maximum Entropy Analysis of Chemical Reaction Energy Dependence," *Journal of Thermophysics and Heat Transfer*, Vol. 10, No. 2, 1996, pp. 217–223.
doi:10.2514/3.778
- [43] Koura, K., "A Set of Model Cross Sections for the Monte Carlo Simulation of Rarefied Real Gases: Atom-Diatom Collisions," *Physics of Fluids*, Vol. 6, No. 10, 1994, pp. 3473–3486.
doi:10.1063/1.868404
- [44] Boyd, I. D., "A Threshold Line Dissociation Model for the Direct Simulation Monte Carlo Method," *Physics of Fluids*, Vol. 8, No. 5, 1996, pp. 1293–1300.
- [45] Bird, G. A., "The Q–K Model for Gas-Phase Chemical Reaction Rates," *Physics of Fluids*, Vol. 23, No. 10, 2011, p. 106101.
doi:10.1063/1.3650424
- [46] Boyd, I. D., "Nonequilibrium Chemistry Modeling in Rarefied Hypersonic Flows," *Chemical Dynamics in Extreme Environments*, edited by Dressler, R. A., World Scientific Press, Singapore, 2001, pp. 81–137.
- [47] Wysong, I. J., Dressler, R. A., Chiu, Y. H., and Boyd, I. D., "Direct Simulation Monte Carlo Dissociation Model Evaluation: Comparison to Measured Cross Sections," *Journal of Thermophysics and Heat Transfer*, Vol. 16, No. 1, 2002, pp. 83–93.
doi:10.2514/2.6655
- [48] Bird, G. A., "Nonequilibrium Radiation During Re-Entry at 10 km/s," *22nd Thermophysics Conference*, AIAA Paper 1987-1543, June 1987.
- [49] Carlson, A. B., and Hassan, H. A., "Direct Simulation of Re-Entry Flows With Ionization," *Journal of Thermophysics and Heat Transfer*, Vol. 6, No. 3, 1992, pp. 400–404.
doi:10.2514/3.374
- [50] Boyd, I. D., "Monte Carlo Simulation of Nonequilibrium Flow in Low Power Hydrogen Arcjets," *Physics of Fluids*, Vol. 9, No. 10, 1997, pp. 3086–3095.
doi:10.1063/1.869474
- [51] Farbar, E. D., and Boyd, I. D., "Modeling of the Plasma Generated in a Rarefied Hypersonic Shock Layer," *Physics of Fluids*, Vol. 22, No. 10, 2010, p. 106101.
doi:10.1063/1.3500680
- [52] Gallis, M. A., and Harvey, J. K., "Atomic Species Radiation from Air Modeled Using the Direct Simulation Monte Carlo Method," *Journal of Thermophysics and Heat Transfer*, Vol. 9, No. 3, 1995, pp. 456–463.
doi:10.2514/3.687
- [53] Kossi, K. K., Boyd, I. D., and Levin, D. A., "Direct Simulation of High Altitude Ultra-Violet Emission From the Hydroxyl Radical," *Journal of Thermophysics and Heat Transfer*, Vol. 12, No. 2, 1998, pp. 223–229.
doi:10.2514/2.6325
- [54] Bird, G. A., "Direct Simulation of Typical AOTV Entry Flows," *4th Thermophysics and Heat Transfer Conference*, AIAA Paper 1986-1310, June 1986.
- [55] Carlson, A. B., and Hassan, H. A., "Radiation Modeling With Direct Simulation Monte Carlo," *Journal of Thermophysics and Heat Transfer*, Vol. 6, No. 4, 1992, pp. 631–636.
doi:10.2514/3.11544
- [56] Hinchey, J. J., and Foley, W. M., "Scattering of Molecular Beams by Metallic Surfaces," *Rarefied Gas Dynamics*, Vol. 2, edited by de Leeuw, J. H., Academic Press, New York, 1966, p. 505.
- [57] Lord, R. G., "Some Extensions to the Cercignani–Lampis Gas Scattering Kernel," *Physics of Fluids A*, Vol. 3, No. 4, 1991, pp. 706–710.
doi:10.1063/1.858076
- [58] Padilla, J. F., and Boyd, I. D., "Assessment of Gas–Surface Interaction Models for Computation of Rarefied Hypersonic Flow," *Journal of Thermophysics and Heat Transfer*, Vol. 23, No. 1, 2009, pp. 96–105.
doi:10.2514/1.36375
- [59] Cecil, D. E., and McDaniel, J. C., "Planar Velocity and Temperature Measurements in Rarefied Hypersonic Flow Using Iodine LIF," *38th AIAA Thermophysics Conference*, AIAA Paper 2005-4695, June 2005.
- [60] Moss, J. N., and Price, J. M., "Survey of Blunt Body Flows Including Wakes at Hypersonic Low-Density Conditions," *Journal of Thermophysics and Heat Transfer*, Vol. 11, No. 3, 1997, pp. 321–329.
doi:10.2514/2.6252
- [61] Allegre, J., and Birsch, D., "Blunted Cone at Rarefied Hypersonic Conditions—Experimental Density Flowfields, Heating Rates, and Aerodynamic Forces," French National Centre for Scientific Research Rept. RC-95-2, Paris, 1995.
- [62] Holden, M., Kolly, J., and Chadwick, K., "Calibration, Validation, and Evaluation Studies in the LENS Facility," *33rd Aerospace Sciences Meeting and Exhibit*, AIAA Paper 1995-0291, Jan. 1995.
- [63] Boylan, D. E., and Potter, J. L., "Aerodynamics of Typical Lifting Bodies Under Conditions Simulating Very High Altitudes," *AIAA Journal*, Vol. 5, No. 2, 1967, pp. 226–232.
doi:10.2514/3.3946
- [64] Griffith, B. J., "Comparison of Aerodynamic Data from the Gemini Flights and AEDC-VKF Wind Tunnels," *Journal of Spacecraft*, Vol. 4, No. 7, 1967, pp. 919–924.
doi:10.2514/3.28988
- [65] Griffith, B. J., and Boylan, D. E., "Reynolds and Mach Number Simulation of Apollo and Gemini Re-entry and Comparison with Flight," *Proceedings of the Specialists' Meeting on Hypersonic Boundary Layers and Flow Fields of the Fluid Dynamics Panel of AGARD*, NATO, Paris, 1968, pp. 1–21.
- [66] Boylan, D. E., and Griffith, B. J., "Simulation of the Apollo Command Module Aerodynamics at Re-entry Altitudes," *Proceedings of the 3rd National Conference on Aerospace Meteorology*, American Meteorological Society, Boston, 1968, pp. 370–378.

- [67] Padilla, J. F., and Boyd, I. D., "Assessment of Rarefied Hypersonic Aerodynamics Modeling and Windtunnel Data," *9th AIAA/ASME Joint Thermophysics and Heat Transfer Conference*, AIAA Paper 2006-3390, June 2006.
- [68] Rault, D. F. G., "Aerodynamics of the Shuttle Orbiter at High Altitudes," *Journal of Spacecraft and Rockets*, Vol. 31, No. 6, 1994, pp. 944–952. doi:10.2514/3.26542
- [69] Ivanov, M. S., Markelov, G. N., Gimelshein, S. F., Mishina, L. V., Krylov, A. N., and Grechko, N. V., "High-Altitude Capsule Aerodynamics with Real Gas Effects," *Journal of Spacecraft and Rockets*, Vol. 35, No. 1, 1998, pp. 16–22. doi:10.2514/3.26992
- [70] Markelov, G. N., Kashkovsky, A. V., and Ivanov, M. S., "Space Station Mir Aerodynamics Along the Descent Trajectory," *Journal of Spacecraft and Rockets*, Vol. 38, No. 1, 2001, pp. 43–50. doi:10.2514/2.3653
- [71] Moss, J. N., "Direct Simulation Monte Carlo Simulations of Ballute Aerothermodynamics Under Hypersonic Rarefied Conditions," *Journal of Spacecraft and Rockets*, Vol. 44, No. 2, 2007, pp. 289–298. doi:10.2514/1.22706
- [72] Wilmoth, R. G., Mitcheltree, R. A., and Moss, J. N., "Low-Density Aerodynamics of the Stardust Sample Return Capsule," *Journal of Spacecraft and Rockets*, Vol. 36, No. 3, 1999, pp. 436–441. doi:10.2514/2.3464
- [73] Jenniskens, P., "Observations of the STARDUST Sample Return Capsule Entry with a Slit-Less Echelle Spectrograph," *46th AIAA Aerospace Sciences Meeting and Exhibit*, AIAA Paper 2008-1210, Jan. 2008.
- [74] Ozawa, T., Zhong, J., Levin, D. A., Boger, D., and Wright, M. J., "Modeling of the Stardust Reentry Flows With Ionization in DSMC," *45th AIAA Aerospace Sciences Meeting and Exhibit*, AIAA Paper 2007-0611, Jan. 2007.
- [75] Boyd, I. D., Trumble, K. A., and Wright, M. J., "Modeling of Stardust Entry at High Altitude, Part 1: Flowfield Analysis," *Journal of Spacecraft and Rockets*, Vol. 47, No. 5, 2010, pp. 708–717. doi:10.2514/1.37360
- [76] Boyd, I. D., and Jenniskens, P., "Modeling of Stardust Entry at High Altitude, Part 2: Radiation Analysis," *Journal of Spacecraft and Rockets*, Vol. 47, No. 6, 2010, pp. 901–909. doi:10.2514/1.37357
- [77] Whiting, E. E., Park, C., Liu, Y., Arnold, J. O., and Paterson, J. A., "NEQAIR96, Nonequilibrium and Equilibrium Radiative Transport and Spectra Program: User's Manual," NASA Reference Publ. 1389, Dec. 1996.
- [78] Blanchard, R. C., Wilmoth, R. G., and Moss, J. N., "Aerodynamic Flight Measurements and Rarefied-Flow Simulations of Mars Entry Vehicles," *Journal of Spacecraft and Rockets*, Vol. 34, No. 5, 1997, pp. 687–690. doi:10.2514/2.3271
- [79] Moss, J. N., Blanchard, R. C., Wilmoth, R. G., and Braun, R. D., "Mars Pathfinder Rarefied Aerodynamics: Computations and Measurements," *Journal of Spacecraft and Rockets*, Vol. 36, No. 3, 1999, pp. 330–339. doi:10.2514/2.3475
- [80] Wilmoth, R. G., Rault, D. F. G., Cheatwood, F. M., Englund, W. C., and Shane, R. W., "Rarefied Aerothermodynamic Predictions for Mars Global Surveyor," *Journal of Spacecraft and Rockets*, Vol. 36, No. 3, 1999, pp. 314–322. doi:10.2514/2.3473
- [81] Moss, J. N., Wilmoth, R. G., and Price, J. M., "Direct Simulation Monte Carlo Calculations of Aerothermodynamics for Mars Microprobe Capsules," *Journal of Spacecraft and Rockets*, Vol. 36, No. 3, 1999, pp. 399–404. doi:10.2514/2.3459
- [82] Rault, D. F. G., "Aerodynamic Characteristics of the Magellan Spacecraft in the Venus Upper Atmosphere," *Journal of Spacecraft and Rockets*, Vol. 31, No. 4, 1994, pp. 537–542.
- [83] Haas, B. L., and Schmitt, D. A., "Simulated Rarefied Aerodynamics of the Magellan Spacecraft During Aerobraking," *Journal of Spacecraft and Rockets*, Vol. 31, No. 6, 1994, pp. 980–985. doi:10.2514/3.26547
- [84] Haas, B. L., and Feiereisen, W. J., "Particle Simulation of Rarefied Aeropass Maneuvers of the Magellan Spacecraft," *Journal of Spacecraft and Rockets*, Vol. 31, No. 1, 1994, pp. 17–24. doi:10.2514/3.26397
- [85] Haas, B. L., and Milos, F.S., "Simulated Rarefied Entry of the Galileo Probe into the Jovian Atmosphere," *Journal of Spacecraft and Rockets*, Vol. 32, No. 3, 1995, pp. 398–403. doi:10.2514/3.26628

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