# Measured and Simulated Prompt Fission Neutron and Photon Correlations 

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> A dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy (Nuclear Engineering and Radiological Sciences) in the University of Michigan

2018

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## Dedication

To my family old and new.

## Acknowledgments

I would like to thank first and foremost my advisor Professor Sara Pozzi for giving me the opportunity to pursue my PhD . I would also like to thank her for the mentorship and for providing many opportunities to grow as a professional.

I would also like to thank everyone in the DNNG for their support since I joined as an undergrad in UROP. Along the way to my dissertation, you've provided immense professional support and offered great friendship.

I would not be here if it weren't for my parents encouragement to follow my interests early in my life and for my wife's encouragement to apply to graduate school. I am thankful for my whole family's support during my long stint as a student and for attempting to understand how I spent my time.

This research was performed under appointment to the Nuclear Nonproliferation International Safeguards Graduate Fellowship Program sponsored by the National Nuclear Security Administrations Next Generation Safeguards Initiative.

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## List of Abbreviations

CFD constant fraction discrimination. 54
DAFCA Data Acquisition For CAEN Apparatuses. 113
DNNG Detection for Nuclear Nonproliferation Group. 3, 54, 113, 127

FWHM full-width half maximum. xi, 23, 116
HFF heavy fission fragment. 15
IAEA International Atomic Energy Agency. 1, 2
LANL Los Alamos National Laboratory. 4, 77, 108, 110
LANSCE Los Alamos Neutron Science Center. 51, 77
LFF light fission fragment. 15

PFNS prompt fission neutron spectrum. 67
PMT photo-multiplier tube. vii, xi, 10, 11, 10, 11, 51, 108, 110, 111
PSD pulse shape discrimination. xi, 5, 7, 9, 10, 54, 55, 113, 116, 118

SNM special nuclear material. xvi, 2
TKE total kinetic energy. vii, 15, 17, 127
TOF time-of-flight. 11, 50, 51, 76, 126
TXE total excitation energy. 17


#### Abstract

An accurate understanding of fission is critical to characterization of special nuclear material (SNM) for nonproliferation and safeguards applications. Noninvasive and nondestructive techniques rely primarily on highly penetrating and relatively abundant fission emissions. Spontaneously and under particle interrogation, SNM emits neutrons and photons from fission, which are characteristic of the fissioning isotopes. Characteristic neutrons and photons are emitted from nuclear fission when a deformed, neutron-rich nucleus divides into two fragments that then de-excite. During de-excitation, neutrons are emitted first, followed by photons; this process gives rise to correlations. New, event-by-event, physics-based models, CGMF (Los Alamos National Laboratory) and FREYA (Lawrence Livermore National Laboratory), predict correlations in prompt fission emissions. Current safeguards and nonproliferation systems do not utilize angular or multiplicity correlations. Little data exist to validate these models; correlated quantities have been measured only for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. My work provides measured correlation data to validate models useful for future system design.

Previous correlation measurements have been limited by the acquisition challenges of a many-detector array and therefore have used simple detector systems. Additionally, few detection methods exist that are simultaneously efficient to neutrons and photons. In this work, I show a many-detector array of pulse-shape-discrimination-capable organic scintillators, sensitive to both fast neutrons and photons, to measure correlations in neutron energy, photon energy, multiplicity, and emission angle. This work is achieved through MCNPX - PoliMi simulations and through use of time-synchronized, high-throughput, multiple-digitizer acquisition systems. I performed experiments sensitive to correlations with a large array of organic scintillators. I performed measurements


of ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ at both the University of Michigan and the Los Alamos National Laboratory; and of ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ spontaneous fission at the Joint Research Centre in Ispra, Italy, and at the Los Alamos National Laboratory.

I measured the ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron-neutron angular distribution and found it to be less anisotropic than the ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutrons. ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ and ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron-neutron angular distribution simulation results indicate that fission models capture the general trend of neutron anisotropy. ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ and ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ experimental multiplicity results suggest weak neutron-photon competition during fragment de-excitation. The measured correlations were compared with MCNPX - PoliMi simulations using the built-in model and two new event-by-event fission models, CGMF and FREYA, which predict correlations in prompt emissions from fission. Simulation results from CGMF and FREYA predict a stronger negative correlation than the experiment result.

## Chapter 1

## Introduction

### 1.1 Motivation

The discovery of fission in 1938 by Hahn and Strassmann [1] and a first explanation by Meitner and Frisch [2] was followed by a rapid development of nuclear technology, both constructive and destructive. Scientists quickly understood the immense potential of fission due to two key features: a large energy release and the emission of multiple neutrons able to form fission chains. Despite 80 years of research, much remains unknown regarding the details of fission and of fission emissions and my work described here contributes to that body of knowledge.

Immediately after the discovery of fission and conception of a fission chain, physicists expressed concerns about proliferation of this new-found technology. Fears of technology abuse materialized as scientists hypothesized, and ultimately demonstrated, that fission chains could be maintained (in the case of a critical fission reactor) or made to grow exponentially (in the case of a fission bomb) [3]. Proliferation concerns were further justified as the world entered World War II and the United States, United Kingdom, Japan, Germany, and Soviet Union pursued fission-based weapons. As those in and out of the nuclear weapons states realized the potential threat of nuclear weapons proliferation, treaties and agreements were later enacted to limit the testing and use of nuclear weapons, while encouraging peaceful nuclear technology.

The first international treaty to indirectly limit nuclear proliferation was the Partial

Test Ban Treaty in 1963 [4]. The treaty's main goal was to limit fallout from atmospheric nuclear testing and did so by forcing nuclear testing underground. Proliferation of nuclear weapons was slowed because testing and diagnostics are more challenging in that environment. The next substantial, international step to prevent nuclear weapons proliferation was the Non-Proliferation Treaty in 1968 [5]. This treaty aimed to prevent the spread of nuclear weapons and technology, to promote cooperation in the peaceful uses of nuclear energy, and to further the goal of achieving nuclear disarmament and of general and complete disarmament. The treaty provided a framework for cooperation between weapons states and non-weapons states to pursue and access peaceful use of technology while preventing the further spread of weapons technology. The treaty established a safeguards system under the International Atomic Energy Agency (IAEA) to verify compliance with the treaty.

The IAEA safeguards intend to verify and to prevent diversion of declared nuclear material, as well as in some cases to identify undeclared nuclear material, within nuclear facilities. These goals are achieved through various means, including physical protection, tamper-proof seals, cameras, and radiation detection. Verification using radiation detection can rely on many different signatures from nuclear material, including emitted gamma rays and neutrons. These nuclear signatures are used to verify declared characteristics such as isotopic composition and mass.

Outside of nuclear facilities and of IAEA safeguards is the threat of illicit nuclear material moving illegally across a nation's borders; radiation detection systems exist to intercept those materials. These detection systems also rely on nuclear material radiations.

Safeguards and nonproliferation radiation detection systems are used to characterize or locate special nuclear material (SNM) which is defined as plutonium, uranium-233, or uranium enriched in isotopes 233 or 235 [6]. These materials emit radiation, particularly from fission, both passively and under active interrogation with particle beams. Fission is unique because it releases both neutrons and photons in multiplicity. Observed properties of fission neutrons and/or photons are used in safeguards and nonproliferation systems.

Most deployed safeguards and nonproliferation radiation detection systems rely on simple or average responses to fission emissions, such as spectra or multiplicity, and are not sensitive to complex correlations between emissions. Monte Carlo particle transport codes are often used to predict experimental outcomes and to design detection systems. These codes use fission models to produce neutron and photon emissions from SNM. Common fission models are limited in detail and do not capture the full physics of the fission fragment de-excitation process $[7,8]$. These models are based on evaluated neutron and photon energy and multiplicity spectra, but they ignore details of fission fragment de-excitation. New event-by-event, physics-based models capture interesting correlations not reflected in these commonly used models [9].

Both the destructive and constructive facets of fission-based technology continue to drive our pursuit of understanding fission and fission emissions. As radiation detector technology has progressed and as greater demands are put on nonproliferation and safeguards systems, increasingly complex detector systems are being developed to meet emerging challenges. Novel safeguards and nonproliferation systems that are inherently more sensitive to fission emissions are currently being developed without the insight of highly detailed fission models. There is, therefore, a need to provide correlated fission data to validate and improve models for the development and improvement of radiation detection systems.

### 1.2 Contributions and overview of this dissertation

In this dissertation, I measure event-by-event correlations in prompt fission emissions relevant to nuclear safeguards applications. Most of the correlations shown here have never been observed before; previous studies and gaps in those studies are detailed in each chapter. The newly-measured correlations are also compared to correlated fission models. The fission models are described in Chapter 3.

While not discussed in this dissertation, work by the Detection for Nuclear Nonproliferation Group (DNNG), including contributions from myself as a co-author, showed
${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron-neutron angle and energy correlations [10]. This work evolved into the first detailed measurement of ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron-neutron angular and energy correlations, discussed here in Chapter 4.

Upon completion of the single particle neutron-neutron measurements, my work transitioned to measuring inter-particle correlations. Detailed in Chapter 5, a measurement was performed at the University of Michigan to explore neutron-photon energy correlations. This work was motivated in part by new event-by-event fission models CGMF [11] and FREYA [12], which exhibit inter-particle correlations, and also by the lack of data to validate these models.

Prompted by interesting results from the University of Michigan experiment and fission model predictions, I experimentally measured neutron-photon competition during fission fragment de-excitation, discussed in Chapter 6. To perform the experiment, I took an acquisition system that I assembled specifically for a summer-long experiment to use the organic scintillator Chi-Nu array at Los Alamos National Laboratory (LANL) [13]. I compared experimental results to CGMF and FREYA simulation results where I integrated fission events into MCNPX - PoliMi.

Once I had measured ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron-photon competition, I approached a more safeguards-relevant isotope, ${ }^{240} \mathrm{Pu}(\mathrm{sf})$, with a similar experiment in mind. Detailed in Chapter 7, I designed a stilbene detector array and acquisition system to measure a small amount of ${ }^{240} \mathrm{Pu}$ at LANL. Again, I compared experimental results to FREYA simulation results.

Finally in Chapter 8, I discuss conclusions from this dissertation work and suggest future work.

## Chapter 2

## Neutron and Photon Detection

Here I explain how I detect radiation, for relevant radiations and detector types, and how I characterize my detectors, specifically for fission experiments. I will restrict discussion to detection of neutrons and photons with energies typical for fission emissions, below approximately 10 MeV .

### 2.1 Organic Liquid Scintillators

Organic scintillators, including EJ-309 [14] and stilbene [15], are composed of organic molecules which create scintillation light when excited by charged particles. Scintillation light is produced after a recoiling charged particle excites molecular states. Organic scintillators are sensitive to photons and neutrons through charged particle recoils. Photons interact primarily through Compton scattering on an electron; photoelectric absorption is unlikely at relevant energies on these small nuclei, shown in Fig. 2.1. Above two times the electron rest-mass energy, pair production is energetically possible and creates an electron-positron pair. The positron will slow down in the surrounding material to subsequently annihilate producing two 511 keV photons. The pair production recoil electron and the annihilation photons can then be detected. Only partial photon energy is deposited in Compton interactions. Neutrons interact primarily via elastic scattering on hydrogen and carbon nuclei, shown in Fig. 2.2; inelastic scattering on carbon and capture on hydrogen are relatively rare. Some organic scintillators, including the EJ-309 and


Figure 2.1: Photon reaction cross sections for stilbene [17]. Low probability reactions are omitted.
stilbene used here, are capable of discriminating between electron and proton recoils, a process known as PSD [16].

### 2.1.1 Reactions and energy deposition

Figure 2.1 shows that fission energy photons are most likely going to interact through Compton (incoherent) scattering. Very low energy photons could be photoelectrically absorbed, but are unlikely to be above acquisition thresholds. Pair production becomes likely as photon energy increases, however Compton scattering is still most common for fission energies. Compton scattering only deposits a fraction of the photon energy $h v$ to
the recoil electron,

$$
\begin{equation*}
h v^{\prime}=\frac{h v}{1+\frac{h v}{m_{0} c^{2}}(1-\cos \theta)}, \tag{2.1}
\end{equation*}
$$

where $m_{0} c^{2}$ is the electron rest mass energy. The maximum energy deposited occurs when the outgoing photon angle $\theta$ is $\pi$ radians, giving a minimum outgoing photon energy $h v^{\prime}$. Using Eqn. 2.1, a $662 \mathrm{keV}{ }^{137} \mathrm{Cs}$ characteristic gamma ray can deposit a maximum of 478 keV . Due to the likely interaction modes and energy deposited by photons in organic scintillators, they are not well suited for photon spectroscopy.

Figure 2.3 shows for an EJ-309 organic scintillator that the detection efficiency to incident photons peaks at low energies and decreases toward higher energies. The energy dependent efficiency is primarily a convolution of interaction cross sections and light production, but also includes other detector readout characteristics. The rising edge in efficiency is due to a lower energy threshold imposed due to acquisition and PSD limitations. The sharp drop in efficiency near 3.5 MeV is due to the upper dynamic range of the waveform digitizer.

Figure 2.2 demonstrates that neutrons primarily interact in organic scintillators through elastic scattering on hydrogen and carbon nuclei. Proton scatters are most likely, but at resonances above a few MeV carbon elastic scattering is more probable. In a nonrelativistic elastic scatter, the recoil nucleus with mass $A$ and energy $E_{R}$ at angle $\theta$

$$
\begin{equation*}
E_{R}=\frac{4 A}{(1+A)^{2}}\left(\cos ^{2} \theta\right) E_{n} \tag{2.2}
\end{equation*}
$$

can only take the full energy of the neutron when $A=1$ and $\theta=0$. Neutrons can deposit their full energy in proton scatters, but a neutron can deposit only $28.4 \%$ of its energy on carbon nuclei.

Figure 2.3 shows for an EJ-309 organic scintillator that the detection efficiency to incident neutrons peaks at low energies and decreases toward higher energies, similar to photons. Again, neutron energy dependent efficiency is primarily a convolution of interaction cross sections and light production, but also includes detector readout characteristics. Small features in the efficiency distribution near $2.5,4,6$, and 7.5 MeV are


Figure 2.2: EJ-309 neutron interaction cross sections to neutrons of fission energies [18]. caused by the resonances in the carbon elastic scattering cross section.

Cross talk occurs when a particle incident on a detector scatters from one detector to another detector and causes a detection event in both. Organic scintillators are susceptible to cross talk because they are sensitive to particles primarily through scattering; further discussion can be found in Chapter 4.4.2.

### 2.1.2 Scintillation light production

The organic scintillator converts charged particle kinetic energy into scintillation light. Energy conversion is linear for electron recoils over fission photon energies, but energy conversion of proton recoils kinetic energy is non-linear, shown in Fig. 2.3. The relevant light emission processes are summarized here, but for a more detailed discussion see Ref. [19].

The fluorescence in organics comes from transitions in the energy level structure of a single molecule [20]. Kinetic energy of a recoiling charged particle can be absorbed by a molecule through exciting the molecule to $\pi$-electronic energy levels. A series of singlet (spin 0 ) and triplet (spin 1) electronic states can be created. Most excitations produce molecules in the first excited singlet or triplet states. Prompt fluorescence occurs in the


Figure 2.3: Calculated neutron and photon detection efficiency and light output distributions used in the detector response code for neutron scattering on a proton and for photon scattering on an electron in a $17.78 \times 5.08 \mathrm{~cm}$ EJ-309 detector.
transition from the first excited singlet state to a ground state. The singlet transition to a ground state has a decay time of 3.5 ns . The triplet state has a much longer decay time to a ground state; however, two triplet states in close proximity can annihilate to form one singlet excited state and one singlet ground state [21]; the new singlet excited state can then decay to ground state on a faster time scale. Excitation energy in the $\pi$-electronic states can transfer from molecule to molecule and not all energy from the excited states is converted to fluorescence.

PSD in organic scintillators arises from differences in scintillation when excited states are formed by electrons and protons. The proton has a higher stopping power than the electron; consequently, the proton creates higher density regions of excited molecules. The higher density regions enable higher rates of triplet-triplet annihilation and singlet state quenching. Therefore, the recoil proton produces relatively less prompt fluorescence and more slightly delayed fluorescence to a recoil electron of the same energy. A proton recoil will produce more total fluorescence than an electron recoil with the same peak intensity, as shown in Figure 2.4. These effects also cause proton recoil kinetic energy


Figure 2.4: Light output intensity in arbitrary units as a function of time after a charged particle recoil in stilbene [23].
conversion to appear as non-linear, shown in Fig. 2.3.
Practically, PSD becomes challenging for small energy depositions. As a proton or electron waveform becomes small, so do the differences in the waveform tails. Here, I used charge integration PSD to discriminate between interaction types [22]. Charge integration PSD compares the waveform tail integral to the total waveform integral of each waveform to a discrimination function.

### 2.1.3 Light collection and readout

Scintillation light from a charged particle recoil must be collected, converted to an electrical signal, amplified, and then read out by a waveform digitizer or analogue electronics.

Scintillation light is emitted in the scintillator volume and must escape to a readout system. In this work, we used a photo-multiplier tube (PMT) to convert scintillation light to an electric signal and to amplify that signal. Each PMT was attached to one face of a right circular cylindrical scintillator. The scintillation light has a relatively long mean free path in the organic material and may scatter many times within the scintillator. To improve light collection in the PMT, a reflective coating is applied to the sides of the scintillator not connected to the PMT.

In Fig. 2.5, a PMT consists of a vacuum tube with a photocathode at one end and at the other end readout and high voltage probes. The face of the PMT, directly attached to the scintillator, contains a photocathode, which converts incident scintillation light


Figure 2.5: (Bottom left) InRad optics stilbene encased in aluminum, (bottom right) ET Enterprises 9214b PMT, and (top) 3D printed case for detector assembly. The PMT and stilbene scintillator are coupled with optical grease and secured with black electrical tape to make the system light tight.
to electrons in the PMT. A vacuum is necessary to allow the low-energy electrons to drift unimpeded through electric fields in the tube. Once electrons are created, they are focused and drifted to a series of dynodes. As an electron strikes a dynode, the energy deposited by the electron may liberate more than one electron, thereby creating a multiplying effect. Multiplication gain for the 9214b PMT from ET Enterprises is on the order of $10^{6}$, depending on applied voltage.

Organic scintillator fluorescence decay times are on the order of nanoseconds and the PMT, given a reasonable choice of PMT and signal acquisition, preserves the fast timing of that signal. Thus, organic scintillators have nanosecond-order time resolution to particle interactions. Good time resolution is useful for neutron time-of-flight (TOF) spectroscopy and for accurate correlation of a fission particle detections with a fission trigger.

## 2.2 $\mathrm{NaI}(\mathrm{Tl})$ scintillators

For a small part of my thesis work, I used an inorganic scintillator, sodium iodide doped with thallium $\mathrm{NaI}(\mathrm{Tl}) \cdot \mathrm{NaI}(\mathrm{Tl})$ is notable for its high light yield of approximately 38,000 photons per MeV energy deposition compared to most inorganic scintillators [20]. While $\mathrm{NaI}(\mathrm{Tl})$ has a fast light decay time compared to most inorganic scintillators, it has a poor light decay time of 230 ns , and thus a poor time resolution relative to organic scintillators such as EJ-309 and stilbene.

Relative to an organic scintillator, $\mathrm{NaI}(\mathrm{Tl})$ is advantageous for photon spectroscopy and for its higher efficiency to photons. $\mathrm{NaI}(\mathrm{Tl})$ is a poor neutron detector, because only a small fraction of neutron energy may be deposited in neutron elastic scattering on sodium or iodine nuclei, respectively $16 \%$ and $3.1 \%$, and the scattering cross sections are on the order of a few barns. Figure 2.6 shows that, due to the higher Z elements, $\mathrm{NaI}(\mathrm{Tl})$ has an appreciable photoelectric absorption cross section over fission photon energy ranges. In photoelectric absorption, the incoming photon is absorbed by the atom and an energetic electron is ejected from one of its bound shells. The ejected electron has kinetic energy equal to the difference of the incoming photon energy and the binding energy of the electron. The binding energy is small relative to fission photon energies; therefore it is assumed that the full photon energy is converted to kinetic energy of the ejected electron. Some photons will interact through Compton scattering. In a $\mathrm{NaI}(\mathrm{Tl})$ pulse height histogram from a monoenergetic photon source, a photopeak and Compton continuum are observed, while in contrast, organic scintillators only exhibit a Compton continuum. A photopeak or full-energy peak is narrow peak that is observed when photoelectrons produced by photoelectric absorption of monoenergetic photons deposit their full energy in the scintillator.


Figure 2.6: Photon reaction cross sections for $\mathrm{NaI}(\mathrm{Tl})$ [17]. Low probability reactions are omitted.

## Chapter 3

## Fission Experiment Modeling

Here, I describe the Monte Carlo particle transport code MCNPX - PoliMi used to model experiment environments and radiation sources, as well as the detector response code MPPost to analyze transport data. I also describe the fission event generators used by MCNPX - PoliMi, including its built-in event generator as well as CGMF and FREYA.

### 3.1 Nuclear fission

Large, neutron-rich nuclei can undergo fission, splitting into two or more fragments, spontaneously or through excitation by particle absorption [24]. Approximately 200 MeV energy is released in fission, the largest of that energy going to fragment kinetic energy ( $150-170 \mathrm{MeV}$ ) and a smaller fraction to various excitations. After scission, the instant


Figure 3.1: Time scale in fission [24].
when the two fragments separate, the fragments are left in an excited state as they are accelerated away from one another by Coulomb forces. The fragments then deexcite through neutron and photon emission where approximately 20 MeV goes to neutron emission and approximately 7 MeV goes to photon emission. First, neutrons are primarily emitted, then there is a transition to photon emission, shown in Figure 3.1. The discussion here is limited to prompt emissions, those from primary fragments, which are typically emitted on the order of nanoseconds after scission.

These large, neutron-rich nuclei are most stable when in an oblong shape as opposed to a sphere, shown by the local minimum at approximately a quadrupole moment of $q_{2}=1$ in Figure 3.2. The quadrupole moment describes elongation of the nucleus, where zero is a sphere. Large nuclei are most stable in oblong shapes because of competing attractive nuclear forces between both neutrons and protons and repulsive Coulomb forces primarily between protons.

The nucleus deformation can oscillate, over saddle points, between different oblong shapes and sometimes progress toward a dumbbell shape, as shown in Figure 3.2. The progression toward a dumbbell shape can occur spontaneously or through absorption. One or more potential energy barriers must be crossed when the oblong nucleus progresses toward a dumbbell shape and finally to scission at high quadrupole moments. Once the nucleus reaches a dumbbell shape, Coulomb forces can overcome nuclear forces and accelerate the two fragments away from one another. Scission occurs when the neck between the two fragments stretches and Coulomb forces begin to dominate. At the scission point, more than two fragments may form, but the most likely outcome is a binary fission.

Figure 3.2 shows a potential surface where the least resistive path to scission produces an asymmetric dumbbell - in other words, the dumbbell ends are unequal. In binary fission, fragment masses are typically asymmetric where there is one light fission fragment (LFF) and one heavy fission fragment (HFF), shown in Figure 3.3.

After scission, the fragments inhabit unique mass, charge, excitation, kinetic, and spin states which influence the neutron and photon emissions. Therefore understanding the


Figure 3.2: ${ }^{236} \mathrm{U}$ calculated potential energy surface as a function of quadrupole moment and a mass-asymmetry parameter [25].


Figure 3.3: Experimental data of ${ }^{235} U\left(n_{t h}, f\right)$ fragment mass yields and average TKE as a function of mass number [26].


Figure 3.4: Experimental data of ${ }^{252} \mathrm{Cf}(\mathrm{sf}) \bar{\nu}$ versus TKE [27].
fragment properties just after scission is important to understanding fission emissions.
Prompt fission neutron properties are strongly correlated to fragment properties, particularly to fragment kinetic energy and mass. Energy is split between total kinetic energy (TKE) and total excitation energy (TXE), therefore we expect fragment TXE to be at a minimum where TKE is at a maximum. Neutron multiplicity decreases with increasing TKE because less excitation energy must be removed through neutron evaporation, shown in Figure 3.4. In Figure 3.5, neutron multiplicity increases with mass number up to a peak at 126 and then sharply decreases, rising again toward high masses. This behavior in neutron multiplicity indicates that larger amounts of excitation energy are present in fragments at and just below 126. Neutron energy is dependent on the nuclear temperature at the time of emission [24].

Prompt fission photon properties are also strongly correlated with fragment properties. Figure 3.6 shows that the total photon energy decreases from approximately 8.5 MeV to 5 MeV over the range of TKEs. Similar to neutron emission, as TKE increases TXE decreases and so less excitation energy must be dissipated through photon emission. Photons also dissipate remaining angular momentum from the fission fragments.

Since both neutrons and photons are removing excitation energy and angular momentum from fission fragments, we expect that on an event-by-event basis those emissions would be correlated. Initially, fragments deexcite most probably through neutron emis-


Figure 3.5: (a) Mean prompt fission neutron multiplicity and (b) mean prompt fission neutron energy in the center of mass frame as a function of fragment mass [9].


Figure 3.6: Experimental data of ${ }^{252} \mathrm{Cf}(\mathrm{sf}) M_{\gamma}$ versus TKE [28].
sion because this process efficiently removes excitation energy. Some event-by-event fission models [12,29] emit neutrons from a fragment until the excitation energy decreases to approximately the neutron separation energy $S_{n}$, shown schematically in Figure 3.7. Following neutron emission, photons are emitted. Statistical photons are emitted until the excitation energy reaches the yrast line, then discrete photons are emitted [30,31]. The exact mode of transition from primarily neutron emission to primarily photon emission, however, is not well understood [9].

Neutrons are emitted within a few femtoseconds after scission, but are also emitted from fully accelerated fission fragments, shown in Figure 3.1. Neutron emission angle relative to the fragment is approximately isotropic in the fragment frame of reference; given the momentum of the fragment, in the laboratory frame neutrons appear to be preferentially emitted in the directions of the fission fragments, shown in Figure 3.8. Also, the energy spectrum in the laboratory frame is slightly harder in the directions of the fragments.

Most photons are emitted from a few femtoseconds to a few nanoseconds after scission; a small fraction of photons are emitted after a few nanoseconds [33,34]. With spin equal to 1 , photons carry away not only excitation energy but also angular excitation. Photons are slightly anisotropic relative to the fragment direction [35,36], however because the anisotropy is weak an experiment without knowledge of fragment characteristics or with


Figure 3.7: Fission fragment deexcitation through neutron and photon emission where neutrons remove excitation energy and photons remove angular momentum [31].


Figure 3.8: Fission neutron yield versus the laboratory neutron energy and versus the cosine of the angle between the direction of movement of the light fragment and the neutron [32].
energy spectroscopy would be insensitive.

### 3.2 MCNPX - PoliMi simulated fission experiments

Radiation detector response tools are used to directly connect radiation particle transport outputs from Monte Carlo N-Particle eXtended (MCNPX) code simulations to laboratory measurements [7]. MCNPX is a general-purpose code used for neutron, photon, electron, and coupled transport in arbitrary three-dimensional materials defined by geometric cells. MCNPX takes a user defined lab geometry, physics models, and source term, shown in Fig. 3.9. The MCNPX code is capable of reliably transporting radiation and recording important interactions in detectors, however MCNPX does not have the ability to translate those reactions to a laboratory-analogous detector signal for most detector types.

The PoliMi code extension to MCNPX was developed to better simulate coincidence measurements and subsequent time analyses by improved event-by-event tracking and conservation of energy and momentum on an event-by-event basis [8]. MCNPX - PoliMi has the option to track and record event information collision-by-collision in specified detector regions. For each collision, key information is recorded: history number, particle number, particle type, collision type, target nucleus, collision cell, and collision time. Recorded collision information can be used to accurately model non-linear detector responses on an event-by-event basis. Additionally, MCNPX - PoliMi samples photons produced in neutron interactions more realistically than MCNPX, because outgoing photons are sampled after the neutron interaction is sampled.

I modified MCNPX - PoliMi to read in arbitrary fission events from file, shown in Fig. 3.9. The fission event file needs to provide particle type, energy, direction, and time of emission. The MCNPX - PoliMi code also includes built-in correlations for key isotope spontaneous fissions (Cf-252, U-238, Pu-240, Pu-242, Cm-242, Cm-244, Pu-238) and ( $\alpha, n$ ) reactions.


Figure 3.9: A block diagram describing the MCNPX - PoliMi and MPPost simulation tools and their inputs to reproduce detected events.

### 3.3 Detector response modeling and MPPost

MPPost is a detector response code used to convert MCNPX - PoliMi interaction file output to a laboratory-analogous detector signal, as illustrated in the Fig. 3.9 work-flow diagram. Depending on the detector being modeled, MPPost uses details recorded in the interaction file including interaction type, particle type, nucleus of interaction, energy deposited, and time of interaction. For scintillators, MPPost converts energy deposition to scintillation light, handles multiple interactions, applies resolutions, and applies thresholds to ultimately record a list of detected pulses. The list of detected pulses includes for each event: particle type, light output, and time of detection.

For scintillators, key detector dependent parameters in MPPost, which the user must input, include upper and lower light output thresholds, energy dependent resolution, light output on electron and proton recoils, and time resolution. The energy or light output resolution, $\Delta E / E$ where $\Delta E$ is the full-width half maximum (FWHM), is energy dependent and follows

$$
\begin{equation*}
\left(\frac{\Delta E}{E}\right)=\sqrt{\alpha^{2}+\frac{\beta^{2}}{E}+\left(\frac{\gamma}{E}\right)^{2}} \tag{3.1}
\end{equation*}
$$

[37]. The energy resolution is assumed to be Gaussian. The time resolution is sampled from a single Gaussian with user specified FWHM.

MPPost has a few models for light output on scatter events: linear, exponential [38], and Birks [39]. The linear model was used to approximate light output from electron
recoils, and the exponential and Birks models were used to approximate light output from proton recoils in the stilbene. The Birks model

$$
\begin{equation*}
L(E)=\int_{E}^{0} \frac{S}{1+k_{B} \frac{d E}{d x}} d E \tag{3.2}
\end{equation*}
$$

takes two coefficients, the scintillation efficiency $S$ and Birks material-dependent constant $k_{B}$ with a material dependent stopping power $d E / d x$ to give the light production $L$ for a recoil energy $E$, shown in Fig. 2.3. The Birks model is a semi-empirical function to account for ionization quenching along the recoil particle's path. Quenching increases with ionization density which also follows stopping power. The exponential, however, takes up to five coefficients. Within a pulse generation window, MPPost converts each interaction that deposits energy to light then sums those light outputs to create a final light output. It is critical that energy is converted to light and then summed because the light output is not linear with energy deposited for proton recoils, shown in Fig. 7.5. Resolution broadening is applied after the light is summed.

MPPost accurately reproduces detector response under most conditions. The code does not treat pulse pile-up or dead time, however one can remove pile-up and dead time events manually from the produced pulse list. Additionally, MPPost assumes perfect pulse classification by particle type, whereas particle discrimination in experiment is typically not ideal and events may be misclassified.

### 3.4 Fission models

Three fission models were used in this work: the built-in MCNPX - PoliMi (referred to as PoliMi), CGMF, and FREYA. See Ref. [9] for more details and model comparisons. The discussion here is focused on event-by-event neutron and photon correlations.

The general purpose transport code MCNPX - PoliMi $[8,40]$ was used to transport particles from all three fission models. The PoliMi spontaneous-fission source uses evaluated multiplicity distributions and energy spectra for prompt neutrons and photons [40]. Because neutrons and photons are sampled independently, no correlation between particle
types is predicted. However, neutrons are correlated with the sampled fission fragment direction in the laboratory frame because of the fragment momentum boost.

MCNPX - PoliMi built-in spontaneous fission sources use evaluated data for the integral energy and multiplicity spectra. The neutron energy spectrum is, however, multiplicity dependent. As multiplicity increases, the energy spectrum softens. MCNPX - PoliMi assumes that, in the fission fragment momentum frame, neutrons are emitted isotropically; therefore in the laboratory frame, with imparted momentum from the fission fragments, neutrons are anisotropic and have slightly higher energies. To impart momentum from the fission fragments, MCNPX - PoliMi assumes constant fragment masses and kinetic energies. The model samples the number of neutrons emitted from each fragment from a symmetric triangle distribution. The triangle distribution is centered around an equal number of neutrons being emitted from each fragment. Photons are emitted isotropically.

The CGMF code [11, 29, 41, 42], developed at Los Alamos National Laboratory, is a Monte Carlo implementation of the statistical Hauser-Feshbach nuclear reaction theory. As input, CGMF takes fragment mass, charge, and total kinetic energy (TKE) yields as well as ground-state masses to calculate excitation energies. The code follows the fission fragments immediately after scission through de-excitation by sequential neutron and photon emission. CGMF uses a mass-dependent parameter to better reproduce the experimental mass-dependent neutron multiplicity and uses a single parameter to fix the initial fragment spin distribution. Because Hauser-Feshbach nuclear reaction theory is used, both neutrons and photons could be emitted during any stage of the de-excitation process. However, as the fragment de-excites, photon emission becomes more likely. The calculated neutron-photon competition is strongly influenced by the spin distribution in each fragment produced. A higher spin leads to more photons being emitted, at the expense of emitted neutrons.

FREYA v2.0.2 (Fission Reaction Event Yield Algorithm), developed at Lawrence Berkeley and Lawrence Livermore National Laboratories, calculates emissions from complete fission events on an event-by-event basis [12,43,44, 45, 46, 47, 48]. Similar to CGMF, FREYA requires fragment mass and charge yields as inputs as well as tabulated ground-state masses.

FREYA also requires the fragment TKE as a function of heavy fragment mass rather than the yields as a function of TKE, as in CGMF. Similar to CGMF, FREYA uses a single parameter to modify the initial spin distribution. As opposed to CGMF, FREYA currently uses a single, fixed parameter to determine fragment excitation energy sharing. Neutron evaporation occurs until the nuclear excitation energy is at or below the neutron separation energy where photon emission takes over. FREYA produces negatively-correlated neutron and photon multiplicities, similar to CGMF.

In Figs. 3.10, 3.11, and 3.12, the calculated distributions for neutron and photon emission from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ are shown for PoliMi, CGMF, and FREYA. Shown in Fig. 3.10, there is no correlation between neutrons and photons with PoliMi. Both CGMF and FREYA exhibit negative correlations between the particle multiplicities on an event-byevent basis. The trends from these two calculations are the same but have different absolute scales.

Figure 3.11 compares the fission model neutron and photon energy spectra. PoliMi uses the Mannhart [49] ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron energy spectrum evaluation, shown in Fig. 3.11(a). The calculated CGMF ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron spectrum is softer than the evaluation spectrum, Mannhart [49], whereas the calculated FREYA spectrum is harder. Figure 3.11(b) compares the photon spectra to an experiment by Billnert et al. [50]. PoliMi uses the Valentine [51] ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ photon evaluation, shown in Fig. 3.11(b). Above 1 MeV , all calculated photon spectra are harder than the Billnert et al. data. The PoliMi and FREYA photon spectra are in agreement with each other, but the CGMF spectrum is slightly higher between 1 and 3 MeV .

Figure 3.12 compares the fission model neutron and photon multiplicity distributions. PoliMi uses the Santi and Miller [52] evaluation for its ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron multiplicity distribution. Reflecting the mean neutron multiplicities shown in Fig. 3.10, the PoliMi and FREYA neutron multiplicity distributions are similar while CGMF shows a slightly higher distribution. PoliMi uses Valentine and Mihalczo [53] for its ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ photon multiplicity distribution. While the PoliMi and FREYA mean photon multiplicities are similar, shown in Fig. 3.10, the FREYA distribution is narrower than the PoliMi distribution. The


Figure 3.10: ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron (y-axis) and photon (x-axis) multiplicities with mean neutron, $\bar{\nu}$, and mean photon, $\bar{\gamma}$, multiplicities from PoliMi (a), CGMF (b), and FREYA (c) with $E[\nu \mid \gamma]$ (x) and $E[\gamma \mid \nu]$ (o) overlaid.


Figure 3.11: ${ }^{252} \mathrm{Cf}($ sf) neutron (a) energy spectra from PoliMi(uses Mannhart [49]), CGMF, and FREYA. ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ photon (b) energy spectra from PoliMi(uses Valentine et al. [51]), CGMF, FREYA, and Billnert et al. [50].

CGMF photon multiplicity distribution is significantly higher than the other data, which is caused by a lower photon threshold than PoliMi or FREYA.


Figure 3.12: ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron (a) multiplicity distributions from PoliMi (uses Santi and Miller [52]), CGMF, and FREYA. ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ photon (b) multiplicity distributions from PoliMi(uses Valentine et al. [53]), CGMF, and FREYA.

## Chapter 4

# Neutron Angular Distribution in ${ }^{240} \mathbf{P u}(\mathrm{sf})$ from the Joint Research Centre Experiment in Ispra, Italy 

This chapter describes work performed to quantify the anisotropy in neutron emission from ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ and is taken from my publication on the work [54]. In this work, J. L. Dolan took measurements of plutonium fission neutrons using an organic scintillator array and acquisition system at the PERLA laboratory at the Joint Research Centre at Ispra, Italy [55]. I analyzed the raw waveform data for angular correlations and modeled the experiment with MCNPX - PoliMi and MPPost to produce the results shown here.

### 4.1 Introduction

Plutonium is a special nuclear material that can be used in the core of a nuclear weapon. The odd-numbered isotopes of plutonium, in particular ${ }^{239} \mathrm{Pu}$, are used to sustain a fissionchain reaction. However, bulk plutonium always contains some percentage of ${ }^{240} \mathrm{Pu}$, which has a relatively high spontaneous fission rate, approximately 40,000 times greater than ${ }^{239} \mathrm{Pu}$. This feature makes plutonium detectable and quantifiable by passive means, and more specifically by counting neutron doubles [56]. In fact, fission generates multiple prompt neutrons emitted in coincidence. Over $70 \%$ of ${ }^{240} \mathrm{Pu}$ spontaneous fissions emit more than one neutron [52].

Detection and characterization of special nuclear material could rely on knowledge of fission neutron anisotropy [8,10,46,57]. In fission, an anisotropic neutron angular distribution is observed in the laboratory reference frame because neutrons emitted isotropically in the fission fragment frame of reference carry momentum from the fully accelerated fission fragment $[24,46]$. Current nonproliferation and verification neutron measurement systems, however, rely on detecting thermalized neutrons; the neutron properties at the time of emission are obscured by down-scattering. When fast neutron detectors are used, the neutron-neutron correlation from fission can be used to characterize fissile samples. Neutron-neutron correlation can distinguish metal from oxide and can estimate the fission to ( $\alpha, \mathrm{n}$ ) rate [58]. In metals, fission neutrons are dominant, while in oxides, fission and ( $\alpha, \mathrm{n}$ ) neutrons are both present. Fission neutrons are emitted anisotropically; $(\alpha, \mathrm{n})$ reactions, present in oxides, emit single neutrons, therefore chance neutron-neutron coincidences from ( $\alpha, \mathrm{n}$ ) reactions are observed isotropically. Only cross-talk neutron coincidences from ( $\alpha, \mathrm{n}$ ) would be observed anisotropically, biased toward zero degree coincidences.

Many fission neutron angular correlation experiments have quantified anisotropy in fission neutron emission $[10,27,59]$; no published work exists, however, that investigates ${ }^{240} \mathrm{Pu}$ spontaneous fission neutrons. Previous experiments characterize neutron correlations in ${ }^{239} \mathrm{Pu}$ thermal neutron induced fission, for which an excited state of ${ }^{240} \mathrm{Pu}$ is formed prior to fission, but conclusions from this data are not directly applicable to ${ }^{240} \mathrm{Pu}$ spontaneous fission [60].

Experimental results are presented here on correlated ${ }^{240} \mathrm{Pu}$ spontaneous fission prompt neutrons, expanding on work performed by Dolan and colleagues [55]. Specifically, we present new results on the angular correlation of prompt neutrons from ${ }^{240} \mathrm{Pu}$ fission. These experimental results are compared to simulations performed with the MCNPX - PoliMi v2.0.0 Monte Carlo code. Cross-talk coincidence effects are estimated with MCNPX - PoliMi simulations and are removed from the experimental neutron-neutron angular distributions.

### 4.2 Experiment

The experiment consisted of two plutonium experiments, using a 0.84 g and 1.63 g ${ }^{240} P u_{\text {eff }}$ sample, hereby designated PM2 and PM3. The quantity ${ }^{240} P u_{\text {eff }}$ mass is a convenient mass definition for neutron coincidence counting [56] where ${ }^{240} P u_{\text {eff }}$ is the weighted sum of even plutonium isotope masses in the sample

$$
\begin{equation*}
{ }^{240} P u_{e f f}=2.52^{238} \mathrm{Pu}+{ }^{240} \mathrm{Pu}+1.68^{242} \mathrm{P} u . \tag{4.1}
\end{equation*}
$$

PM2 and PM3 were encased in aluminum right circular cylinders with inner cavity of 2.6 cm diameter and 3.3 cm height, wall thickness 0.3 mm , and top and bottom of 6.5 mm . The PM2 plutonium metal was 1 cm in diameter and 1.32 cm in height and was 2.23 cm from the bottom of the encasement and was placed 11 cm above the table surface at the center of the array. The PM3 plutonium material was 1.145 cm in diameter and 1.145 cm in height and was 2.23 cm from the bottom of the encasement and was placed 17.02 cm from the table surface at the center of the array. A ${ }^{252} \mathrm{Cf}$ sample was also used and was placed 17 cm above the table surface at the center of the array. At the time of the experiment, the plutonium metal samples had fission rates of 400 and 760 fissions/s for PM2 and PM3, respectively; the ${ }^{252} \mathrm{Cf}$ sample had a fission rate of 26,000 fissions/s. The experiment was performed at the PERLA laboratory at the Joint Research Centre at Ispra, Italy [55].

Shown in Fig. 4.1, $16-7.62 \varnothing \times 7.62 \mathrm{~cm}$ EJ-309 organic liquid scintillation detectors were used to measure neutron-neutron coincidences from the plutonium samples. Two concentric 8-detector rings were stacked; samples were placed along the central detector ring axis. The sample was shielded with a 1-cm thick lead cylinder $13 \mathrm{~cm} \varnothing$ and 31.5 cm in height to reduce the gamma-ray count rate and acquisition dead time. Each detector was approximately 18 cm from the central axis; the top and bottom detector rings are separated by 10.6 cm from detector centers. Two time-synchronized CAEN V1720 digitizers were used to collect 120 -sample pulses. Pulses above a $70-\mathrm{keVee}$ threshold were recorded for offline processing. A 70-keVee acquisition threshold and a 2 V dynamic range
used in this experiment correspond to a range of 0.65 to 6.7 MeV proton recoils.
Pulse shape discrimination by digital charge integration was used to discern neutron detection events from gamma-ray detections $[16,20]$. The pulse tail of a gamma-ray interaction decays faster than a pulse of the same height from a neutron interaction. Waveforms that exhibit pile-up are eliminated, and then a ratio of the pulse tail integral to the total pulse integral was used to distinguish gamma-ray and neutron detection events, shown in Fig. 4.2 for the PM2 sample. The PSD line was assigned using an algorithm described by Polack and colleagues that minimizes particle misclassification by analyzing segments of the tail-to-total integral points grouped by total integral [22]. The photon-to-neutron ratio for this sample was approximately 100:1 making PSD difficult at low pulse heights. The detection time differences of particles in a 60 -ns coincidence window were used to create cross-correlation distributions with 2-ns bins for each detector pair.


Figure 4.1: (a) A photograph of the experiment setup with a plutonium metal sample centered inside a lead shield and (b) the simulated plutonium metal experiment setup with EJ-309 $7.62 \varnothing \times 7.62 \mathrm{~cm}$ organic liquid scintillator detectors, plutonium metal, and lead shield are shown.


Figure 4.2: Experiment pulse shape discrimination plot of tail to total pulse integrals for 290,000 pulses from the PM2 sample. Color scaling is logarithmic ascending to yellow. Neutrons lie above the discrimination line.

### 4.3 Simulation with MCNPX - PoliMi

The MCNPX - PoliMi and MPPost codes were used to model the experiment geometry, the plutonium metal sample, and the detector response [8]. The experiment assembly is shown in Fig. 4.1(a) and the corresponding simulation model is shown in Fig. 4.1(b). The detector photomultiplier tubes, detector holder, aluminum table, and concrete floor were also modeled in simulation, but were omitted from the figure for clarity. The full MCNPX - PoliMi model input file for this experiment can be found in Appendix 1.

Each plutonium metal sample was modeled as a metal cylinder with composition described in Tables 4.1 and 4.2. The cylinder was topped by a void, and the void and cylinder were encased in aluminum.

The full isotopic composition of the samples was modeled in the material definition. Most fissions are from ${ }^{240} \mathrm{Pu}$ spontaneous fissions; only $0.5 \%$ and $0.9 \%$ of the spontaneous fissions are from ${ }^{242} \mathrm{Pu}$ for the PM2 and PM3 samples respectively. Less than 0.002 fissions per second are expected from ${ }^{238} \mathrm{Pu}$ spontaneous fission, therefore that contribution was ignored. The PoliMi mixed-source option, $\operatorname{IPOL}(1)=99$, was specified to sample from ${ }^{240} \mathrm{Pu}$ and ${ }^{242} \mathrm{Pu}$ built-in models. Using the plutonium metal sample MCNP model and the

Table 4.1: Plutonium metal sample isotopic composition.

| Isotope | PM2 Weight Fraction | PM3 Weight Fraction |
| ---: | :---: | :---: |
| Ni | 0.0504 | 0.0167 |
| Cu | 0.0319 | 0.0427 |
| ${ }^{238} \mathrm{Pu}$ | 0.00004 | 0.00023 |
| ${ }^{239} \mathrm{Pu}$ | 0.87367 | 0.85141 |
| ${ }^{240} \mathrm{Pu}$ | 0.04076 | 0.07891 |
| ${ }^{241} \mathrm{Pu}$ | 0.00028 | 0.00089 |
| ${ }^{242} \mathrm{Pu}$ | 0.00013 | 0.00044 |

Table 4.2: Plutonium sample properties.

| Sample property | PM2 | PM3 |
| ---: | :---: | :---: |
| Total Mass $[\mathrm{g}]$ | 20.4 | 26.4 |
| Density $\left[\mathrm{g} / \mathrm{cm}^{3}\right]$ | 19.7 | 22.4 |
| 240 Pu Effective Mass $[\mathrm{g}]$ | 0.84 | 1.63 |

spontaneous fission source term, it was estimated that approximately $8.4 \%$ and $10 \%$ of fissions are induced rather than spontaneous for PM2 and PM3. Also, approximately $88 \%$ and $79 \%$ of fission neutrons in the detectable range escaped the container and metal before interacting.

There are 120 possible detector pairings of 13 unique detector-sample-detector angles. Angles were calculated using the simulated mean neutron scatter position in the detectors for scatters above the minimum detectable energy. Unique angles within 2 degrees of another were combined for 9 unique angle groups for PM2 and 10 groups for both PM3 and ${ }^{252} \mathrm{Cf}$, shown in Table III. Variable sample position along the detector array central

Table 4.3: Detector-sample-detector angles in degrees for each sample position.

| $P M 2$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Angle [ ${ }^{\circ}$ ] | Uncertainty $\left[{ }^{\circ}\right]$ | PM3 | Angle $\left[{ }^{\circ}\right]$ | Uncertainty $\left[{ }^{\circ}\right]$ | ${ }^{252} \mathrm{Cf}$ |
| Angle $\left[{ }^{\circ}\right]$ | Uncertainty $\left[{ }^{\circ}\right]$ |  |  |  |  |
| 28 | 10 | 27 | 11 | 28 | 8 |
| 42 | 12 | 41 | 11 | 44 | 15 |
| 45 | 12 | 45 | 11 | 53 | 11 |
| 52 | 12 | 51 | 12 | 87 | 14 |
| 83 | 13 | 80 | 12 | 93 | 11 |
| 91 | 13 | 91 | 13 | 127 | 14 |
| 120 | 11 | 114 | 9 | 136 | 13 |
| 135 | 11 | 132 | 10 | 149 | 12 |
| 166 | 13 | 158 | 9 | 154 | 14 |
|  |  | 175 | 11 | 177 | 18 |



Figure 4.3: MCNPX - Polimi neutron angular frequency relative to the light fission fragment direction for ${ }^{252} \mathrm{Cf}$ and ${ }^{240} \mathrm{Pu}$ spontaneous fission neutrons.
axis resulted in different angle groups for each sample. Estimated angular uncertainty was determined by the neutron scatter location variance, shown in Table 4.3. The uncertainty varied for each angle grouping with the largest uncertainty being 13 degrees for the PM2 and PM3 cases and 18 degrees for the ${ }^{252} \mathrm{Cf}$ case. The average uncertainty in angle for each sample was 12 degrees, 11 degrees, and 13 degrees for PM2, PM3, and ${ }^{252} \mathrm{Cf}$ respectively.

The MCNPX - PoliMi ${ }^{240} \mathrm{Pu}$ spontaneous fission neutron model includes a multiplicitydependent energy spectrum, multiplicity from zero to six, and anisotropy. Neutron angular distributions relative to the light fission fragment direction for ${ }^{252} \mathrm{Cf}$ and ${ }^{240} \mathrm{Pu}$ are shown in Fig. 4.3.

### 4.4 Results and analysis

Experimental PM3 pulse height and time cross-correlation distributions are compared to simulated results to validate the MCNPX - PoliMi and detector response model. The neutron-neutron coincidence events versus detector pair angle for both experiment and
simulation were compared and are followed by subtraction of cross-talk coincidence events from the experiment results.

### 4.4.1 Simulation Model Validation

Simulated and experimental neutron pulse height distributions, shown in Fig. 4.4, for the top and bottom rings of detectors were binned. Two detectors in the array were removed from the results due to inconsistent pulse height responses. Differences between the integral counts for the top and bottom ring distributions are due to the samples placement slightly below the center plane of the detector array. The simulated pulse height distribution under-predicts the experiment result by approximately $20 \%$ point-bypoint over the dynamic-range, with exception at the lowest pulse height bin. Gamma-ray misclassification increases toward lower pulse heights and is likely the source of larger disagreement at low pulse heights. Consistent under-prediction suggests that the aged fission rate used in the simulation is low. Improved agreement, with a single detector and lower gamma-ray to neutron ratio, was demonstrated in work by Pozzi and colleagues [61] when using a 3.3 cm lead shielded PM3 sample and a $7.62 \varnothing 5.1 \mathrm{~cm}$ EJ-309 detector.

Overall, the MCNPX - PoliMi and MPPost models adequately reproduce experimental pulse height distributions. Underestimation of the singles neutron rate does not impair the ability to model double coincidences including trends in neutron-neutron time or angular correlations.

The PM3 time cross-correlation distributions from simulation agree well with the experiment in shape for the 90 -degree detector pair (Fig. 4.5(a)) and for the 175-degree detector pair (Fig. 4.5(b)). Results show that there are fewer counts in the 90-degree detector pair distribution than the 175-degree pair distribution because of the strong anisotropy in neutrons from spontaneous fission. The simulation result slightly underestimates the experiment count rate for the 175-degree case. Uncertainty in the plutonium sample position and incorrect neutron anisotropy models in simulation contribute to disagreement in Fig. 4.5(b). The distribution agreement in Fig. 4.5(a) and attributed disagreement in Fig. 4.5(b) validates the MCNPX - PoliMi and MPPost models used to rep-


Figure 4.4: Experiment and simulated PM3 neutron pulse height distributions with a 100 keVee threshold for the average of the top ring and the bottom ring. One standard deviation statistical error bars are shown.
resent the laboratory environment and detector response. The accidental neutron-neutron coincidence rate was negligible relative to the true rate and was ignored in coincidence analysis. The accidental rate is shown in Figure 4.5 at large $|\Delta T|$.

For each unique angle, the neutron-neutron cross-correlation time distribution was integrated over a $60-\mathrm{ns}$ window to give the total coincidence count rate, shown in Fig. 4.6. Each neutron-neutron coincidence point is normalized by solid angle, detector pairs, and fission rate. Figure 4.6 highlights that a neutron is more likely to be emitted at small angles or very large angles relative to another neutron than to be emitted at angles around 90 degrees.

The MCNPX - PoliMi distributions in Fig. 4.6 match general features of the experimental distribution. The simulation underestimates the experimental count rate at angles larger than approximately 50 degrees, while the simulation overestimates at angles smaller than 50 degrees. The MCNPX - PoliMi fission model has too many low angle coincidences relative to the experiment result. The simulation result with cross-talk removed shows better agreement over a larger range of angles with the experiment result; cross-talk events are easily identified and removed in simulation space. The cross-talk removed results show that many low angle coincidences are from cross-talk and the cross-talk fraction diminishes toward large angles.

### 4.4.2 Cross-talk Effect

Cross-talk occurs when a single neutron is detected by more than one detector, mimicking a true coincidence of two neutrons. The probability of cross-talk for a given neutron spectrum and detector array can be reduced by inter-detector geometric attenuation, by shielding, or by an increased detection threshold. Inter-detector geometric attenuation or increased thresholds are not feasible, because the true coincidence count rate would also be reduced. The cross-talk fraction is reduced as the light output threshold is increased because the once-or-more scattered, lower-energy neutron falls below threshold more often than a direct, unscattered source neutron. Shielding attenuation was avoided in this work to minimize in-scattering of neutrons.


Figure 4.5: Experiment and simulated (MCNPX - PoliMi) PM3 neutron-neutron crosscorrelation time distributions for 90-degree (a) and 175-degree (b) detector pairs with one standard deviation statistical uncertainty error bars.


Figure 4.6: Simulated and experiment ${ }^{252} \mathrm{Cf}$ (top), PM2 (middle), and PM3 (bottom) neutron-neutron coincidence angular distributions with a 70 keVee threshold. Simulated results are shown with and without cross-talk. Vertical error bars represent one standard deviation statistical uncertainty; simulated vertical error bars are smaller than the symbols.

There is no reliable analysis for this experiment that could isolate cross-talk counts on an event-by-event basis, thus the simulated data were used to remove integral cross-talk counts from the experimental coincidences. The simulation collision history file allows the user to identify multiple detections that arise from a single neutron.

The simulation results in Fig. 4.7 show the number of cross-talk counts divided by the total number of coincidence counts. The 100, 150, and 200 keVee thresholds correspond approximately to $0.8,1$, and 1.2 MeV proton recoils, respectively. At the lowest angles for all thresholds, greater than $20 \%$ of coincidences are from cross-talk. Adjacent detectors share a large solid angle with each other and the cross-talk is correspondingly high, whereas opposing detector pairs near 180 degrees have cross-talk fractions under $10 \%$.

### 4.4.3 Cross-talk corrected angular distributions

Figures 4.8, 4.9, and 4.10 show the experiment neutron-neutron angular coincidence distribution after cross-talk removal. Experiment geometry specific effects in the angular distributions are minimized when coincidences from cross-talk are removed. The simulated cross-talk fraction is reliable because it is primarily dependent on well-modeled factors, the detector array geometry and the incident neutron energy spectrum. The MCNPX - PoliMi cross-talk removed result in Fig. 4.6 has a higher count rate at low angles relative to those near 180 degrees, contrary to the trends observed in Figs. 4.8, 4.9, and 4.10. Therefore, the MCNPX - PoliMi model could be improved.

In Fig. 4.8, the ${ }^{252} \mathrm{Cf}$ coincidence distributions are compared to work by Petrov and colleagues [62]; the Petrov experiment had a $50 \varnothing \times 50 \mathrm{~mm}$ and a $40 \varnothing \times 60 \mathrm{~mm}$ stilbene crystal 50 cm from a ${ }^{252} \mathrm{Cf}$ source. This work compares well qualitatively with the Petrov data set. Differences between the two distributions are attributed to better angular resolution in the Petrov experiment.

For all samples, the neutron-neutron angular distributions with cross-talk coincidences removed show that low angle coincidences are less likely than those at higher angles. Also, the neutron-neutron angular distribution becomes more anisotropic as the pulse height threshold increases.


Figure 4.7: Simulated cross-talk fraction of total coincidences angular distributions for various light output thresholds at each detector angle for ${ }^{252} \mathrm{Cf}$ (top), PM2 (middle), and PM3 (bottom).


Figure 4.8: Experimental ${ }^{252}$ Cf neutron-neutron cross-talk-corrected coincidence angular distributions with a light output threshold varied over 70 to 200 keVee ; experiment data are compared to data normalized by integral and number of points from Petrov et al. (Xs) [62]. Vertical error bars represent one standard deviation statistical uncertainty.

The coincidence data point for PM2 in Fig. 4.9 at 42 degrees is higher than the point at 28 degrees likely because of sample position uncertainty, which affects the simulation estimated cross-talk. At low detector angles, the contribution of cross-talk is very sensitive to small changes in the sample position.

The neutron-neutron distributions for PM2 and PM3 show similar anisotropy, but the ${ }^{252} \mathrm{Cf}$ distribution is slightly more peaked toward 180 degrees. Slight differences in PM2 and PM3 size and isotopic composition do not manifest in the neutron-neutron angular coincidence distributions.

Figure 4.11 shows the ratio of 180 degree to 90 degree coincidences. As the light output threshold increases, the observed neutron-neutron coincidences become more anisotropic. More coincidences in the 90-degree pairs include low energy neutrons than in the 180degree pairs; thus, as threshold increases so does anisotropy. Greater anisotropy is expected because more momentum is imparted to a neutron emitted near the fragment direction than to a neutron emitted perpendicular to the fragment direction. The ${ }^{252} \mathrm{Cf}$ data shows much stronger anisotropy than the ${ }^{240} \mathrm{Pu}$ data, but the slope of increasing anisotropy is similar. The data for the two ${ }^{240} \mathrm{Pu}$ samples, PM2 and PM3, agrees within


Figure 4.9: Experiment PM2 neutron-neutron cross-talk corrected coincidence angular distributions with a light output threshold varied over 70 to 200 keVee. Vertical error bars represent one standard deviation statistical uncertainty.


Figure 4.10: Experiment PM3 neutron-neutron cross-talk corrected coincidence angular distributions with a light output threshold varied over 70 to 200 keVee. Vertical error bars represent one standard deviation statistical uncertainty.


Figure 4.11: Experiment ratio of neutron-neutron coincidences at 180-degree to 90-degree detector pairs as a function of light output threshold.
the statistical uncertainty of this experiment.

### 4.5 Conclusions

Prompt neutron anisotropy from ${ }^{240} \mathrm{Pu}$ was observed and quantified in laboratory experiments for the first time. The experiments were performed using organic liquid scintillators with two plutonium metal samples; the results agreed within statistical uncertainties. ${ }^{252} \mathrm{Cf}$ spontaneous fission neutrons above 0.65 MeV were observed to be significantly more anisotropic than ${ }^{240} \mathrm{Pu}$ spontaneous fission neutrons above that same energy. These experiment results could be used to improve prompt fission neutron models used in Monte Carlo codes for nonproliferation and safeguards applications.

MCNPX - PoliMi simulation of the PM3 laboratory and detector system reproduced experiment pulse height and cross-correlation distributions for 90-degree and 175-degree detector pairs. MCNPX - PoliMi simulations were used to estimate the cross-talk fraction and then to remove that fraction from the neutron-neutron angular distributions. More than $20 \%$ of small angle coincidences were from cross talk because of large relative
detector-to-detector solid angles. ${ }^{252} \mathrm{Cf}$ neutrons were found to be more anisotropic than ${ }^{240} \mathrm{Pu}$ neutrons. The observed anisotropy increased with applied light output threshold for the plutonium metal and ${ }^{252} \mathrm{Cf}$ samples at a similar rate. The ratio of 180 to 90 degree neutron-neutron coincidences from the plutonium experiments varied from approximately 1.3 to 1.5 over a detection threshold of 70 to 200 keVee . Future experiments with reduced uncertainty, especially in detector pair angles, are necessary to further refine anisotropic neutron emission models for ${ }^{240} \mathrm{Pu}$ spontaneous fission.

## Chapter 5

## Neutron and Photon Correlations from the University of Michigan ${ }^{252} \mathbf{C f}($ sf $)$ Experiment

In this work, I measured ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutrons and photons using an array of EJ-309 organic and $\mathrm{NaI}(\mathrm{Tl})$ scintillators. I also modeled the experiment with MCNPX - PoliMi and MPPost. I modified MCNPX - PoliMi to read fission events from CGMF and FREYA into MCNPX - PoliMi and those results were compared to the experiment data. I analyzed both experiment and simulation data for pulse height, time cross-correlation, and multiplicity dependent neutron TOF energy. Portions of this work were published in a review publication of correlated fission data and modeling for transport simulations [9].

### 5.1 Introduction

New event-by-event fission models have prompt neutron and gamma-rays that are correlated in time, energy, and multiplicity, however there is limited measurement data available to validate these models. Measurement of high-order fission neutron and gamma-ray coincidences, those beyond triple coincidence events, is difficult and there has previously been little motivation to measure properties of both particle types simultaneously. A ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ experiment was performed to collect correlated neutron and photon data. Prompt neutrons and photons were measured with an array of organic liquid and $\mathrm{NaI}(\mathrm{Tl})$ scintillator detectors.

High-order ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron and gamma-ray coincidences were measured with an
array of 24 liquid organic and eight sodium iodide scintillation detectors. Measured coincidence data including neutron time-of-flight energy and measured gamma-ray pulse height distributions are compared with MCNPX - PoliMi simulation results from built-in and event-by-event fission models.

### 5.2 Measurement setup

An array of $14-7.62 \varnothing \times 7.62 \mathrm{~cm}$ EJ-309's, $8-7.62 \varnothing \times 5.08 \mathrm{~cm}$ EJ-309's, and $8-$ $7.62 \varnothing \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ scintillators coupled to PMTs was used to measure neutrons and gamma-rays from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. The array in Figure 5.2 had a flightpath of 51 cm for all detectors with the spontaneous fission source at the center axis of the array between the detector planes.

### 5.2.1 Detector array

The detector array, shown in Figures 5.1 and 5.2, was re-purposed from a Los Alamos Neutron Science Center (LANSCE) WNR measurement using a U-235 parallel plate avalanche chamber. The detector holder was designed with a few key parameters in mind: to allow a beam to enter the center of the array; to have reasonable fission neutron time-of-flight with organic liquid scintillators; and to have detector adjustability in height. The array was not designed to be particularly neutron and photon efficient because neutron TOF spectroscopy was prioritized. The array used in LANSCE was completely EJ-309s, but in this measurement eight of the $7.62 \varnothing \times 5.08 \mathrm{~cm}$ EJ-309's were replaced with $\mathrm{NaI}(\mathrm{Tl})$ to improve photon efficiency and to allow for spectroscopy.

The EJ-309 detectors have a chamber that contains the liquid active volume with a small nitrogen bubble to allow for expansion. There is a borosilicate glass window, BK-7, that protrudes in the active volume to prevent the nitrogen bubble from directly touching the active volume to PMT interface; light does not pass efficiently through the bubble to the PMT. The active volume is coupled to a PMT, a ET Enterprises 9821 B on $7.62 \varnothing \times 7.62 \mathrm{~cm}$ and $7.62 \varnothing \times 5.08 \mathrm{~cm}$ EJ-309s. The EJ-309 energy resolution


Figure 5.1: A photograph of the detector holder and 32 detectors, $14-7.62 \varnothing \times 7.62 \mathrm{~cm}$ EJ-309's, $8-7.62 \varnothing \times 5.08 \mathrm{~cm}$ EJ-309's, and $8-7.62 \varnothing \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ scintillators.
is approximately $30 \%$ full-width half maximum at 662 keVee . Using constant fraction discrimination timing, timing resolution of approximately 1 ns full-width half maximum is observed, shown in Figure 5.15.

The detectors were aligned so that there were two horizontal planes of detectors separated by 20 cm from detector center axes. Detectors on a plane are in $20^{\circ}$ increments with $40^{\circ}$ openings for the beam that was used in a prior experiment. Great care was taken to adjust each detector to level and to point at the central system axis.

### 5.2.2 Acquisition

Pulses from the detectors were digitized using four CAEN V1720 waveform digitizers with 250 MHz sampling and 12 bit amplitude resolution over a 2 V range. The internal digitizer clock signals were synchronized so waveform global time stamps were also synchronized. Time synchronization was performed with CAEN provided software and phase lock loop files unique to each board were used.

All detectors output negative voltage, simplifying acquisition. The EJ-309 and $\mathrm{NaI}(\mathrm{Tl})$ photomultiplier tubes have negative signals, but the $\mathrm{NaI}(\mathrm{Tl})$ is often used with a pulse


Figure 5.2: A model of the detector holder and 32 detectors, $14-7.62 \varnothing \times 7.62 \mathrm{~cm}$ EJ-309's, $8-7.62 \varnothing \times 5.08 \mathrm{~cm}$ EJ-309's, and $8-7.62 \varnothing \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ scintillators.
shaper that inverts the signal polarity. This measurement does not use a pulse shaper for the $\mathrm{NaI}(\mathrm{Tl})$ detector signals because the pulse shaper lengthens the waveform and worsens timing resolution. Without a pulse shaper, energy resolution suffers.

Due to the source strength and $\operatorname{NaI}(\mathrm{Tl})$ high efficiency, data throughput limited the waveform size to a 400 ns window. A 400 ns window at 250 MHz sampling results in 100 samples, sufficient for pulse shape discrimination with an EJ-309, but not enough for full integration of a $\mathrm{NaI}(\mathrm{Tl})$ waveform. Each recorded waveform data packet included a global time stamp, channel, and 12-bit amplitude for each sample.

Acquisition is triggered by threshold crossing. The threshold was specified to approximately 40 keVee equivalent. At this level, background contribution is minimal in the $\mathrm{NaI}(\mathrm{Tl})$ detectors and PSD is possible in the EJ-309s. Each channel and board triggers independently; no triggering logic was used to enforce coincidences. Typically, a single channel triggering on a V1720 digitizer board passes a global trigger, acquiring data for all channels, however zero suppression was used.

The Quacq acquisition software, developed within DNNG was used on a Debian Linux desktop. Quacq was developed to partially parallelize acquisition when using multiple digitizers, however, great improvements have been made recently with other software developed within DNNG.

### 5.2.3 High voltage supply

High voltage was applied to each detector with a single supply from Wiener, EHS F 030n. The HV supply was controlled on a desktop via an Ethernet connection. The detectors were gain matched to 478 keVee at 0.3 V . Calibration was automated with a script that fits the Compton edge in pulse height distributions from a Cs-137 667 keVee characteristic gamma ray. Despite this calibration, pulse height regions far from 0.3 V could exhibit very different responses from detector to detector.

### 5.2.4 Waveform post-processing

All digitized waveforms were recorded for post-processing. Pulse shape discrimination was used to discriminate between neutron and gamma-ray events in the liquid organic scintillators [16]. Full digitized waveforms, of 100 samples at 250 MHz , were saved for post-processing. Only pulses above a specified threshold ( 70 keVee ) were analyzed. Double pulses above a fraction of the triggering pulse height were removed, as PSD cannot be reliably performed on double pulses. The double pulse fractional height threshold is $10 \%$ for EJ-309s and $20 \%$ for the $\mathrm{NaI}(\mathrm{Tl})$ s. Pulse timing is determined through constant fraction discrimination (CFD). The CFD value for the EJ-309s is $50 \%$ and for the $\mathrm{NaI}(\mathrm{Tl})$ s is $10 \%$.

EJ-309 waveforms were read into memory, cleaned, integrated for PSD, and then categorized by particle type. First, the maximum of the pulse is found and the baseline is subtracted. The pulse is kept if it is above the specified threshold. The time of the pulse is determined with a constant fraction discriminator, $50 \%$ is generally used. The waveforms were cleaned to remove any waveforms where PSD would be unreliable. Alignment within the window was checked; there must be enough samples to compute a baseline average and to integrate the tail of the pulse. The pulse must be free of double pulses; the tail is searched for peaks that exceed a specified fraction of the maximum pulse height.

After cleaning, the tail and total integrals were computed. The tail starts 11 samples (44 ns) after the maximum and ends 45 samples ( 180 ns ) after the maximum. The total integral begins 5 samples before the maximum.

Figure 5.3 shows that the tail plotted against the total integral produces two bands, one for photons and one for neutrons. The two bands correspond to electron and proton recoils. Electrons fall below protons in tail integral for a given total integral because more singlet states are quenched and more triplet-triplet annihilations occur in the scintillator for the higher stopping power proton recoil. In practice a PSD line is assigned to discriminate between the two particle types. Significant overlap occurs at small integrals, therefore misclassification is most likely in this region. A quadratic line is used to discriminate particle type, as shown in Figure 5.3, and a unique PSD line was assigned for


Figure 5.3: EJ-309 digitized waveform pulse tail integral to total pulse integral heat map with neutron-gamma-ray discrimination line where neutrons lie above the line and gamma rays lie below. Approximately 200,000 waveforms, after cleaning, are represented in the figure.
each detector to account for small differences in pulse shape due to readout.
After post-processing of waveforms including pulse shape discrimination, coincident events using a 200 ns window were collected. The coincident events were analyzed to produce pulse height, cross-correlation, multiplicity, and time-of-flight neutron energy distributions.

### 5.2.5 $\quad{ }^{252} \mathrm{Cf}(\mathrm{sf})$ source

The Cf-252 source was $6001.2 \mu \mathrm{Ci}$, recorded on 05-Aug-1994 and at the start of the measurement campaign was $31.07 \mu \mathrm{Ci}$. Approximately 70 billion fissions were observed from the 35,500 fission $/ \mathrm{s}{ }^{252} \mathrm{Cf}(\mathrm{sf})$ source. The isotopic evaluation on that date is shown in Table 5.1. ${ }^{250} \mathrm{Cf}(\mathrm{sf})$ contributes $5.8 \%$ of the spontaneous fission events. The source was old relative to the creation date, therefore the relative strength of ${ }^{250} \mathrm{Cf}(\mathrm{sf})$ to ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ is increased. The spontaneous fission fraction of ${ }^{250} \mathrm{Cf}$ is estimated to be approximately $6 \%$

Table 5.1: Cf-252 source isotopic evaluation for fission decays, decayed from the 05-Aug1994 evaluation, to the start of the measurement campaign, 05-Sep-2014.

| Isotope | Fissions/s |
| :---: | :---: |
| Cf-252 | 35,500 |
| Cf-250 | 2,200 |
| Cm-248 | 137 |

at the time of measurement. This contribution is not modeled in the MCNPX - PoliMi simulations.

### 5.3 MCNPX - PoliMi model and simulation

MCNPX - PoliMi and MPPost were used to simulate the measurement. MCNPX - PoliMi was used to transport neutrons and photons in the laboratory space and MPPost was used to emulate detector response [8]. The full MCNPX - PoliMi model input file for this experiment can be found in Appendix 2. Simulated MCNPX - PoliMi results using the built-in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ model, the CGMF model [11,29,41, 42], and the FREYA model [12, 12, 43, 45, 46, 47, 48] are compared to experimental results. For more details on the fission models see Chapter 3.

MPPost was used to emulate detector response. MCNPX - PoliMi collision histories are read and evaluated by MPPost to determine the outcome of the interaction and relevant information is recorded. The user provides detection thresholds and resolutions to be applied by MPPost.

Aside from the detector array, laboratory features were modeled. The laboratory has a concrete floor and tall concrete ceilings $(3.5 \mathrm{~m})$ that were included in the model. There were large polyethylene sheets near the detector array, approximately 2 m from the edge of the array that were also included in the model. The polyethylene sheets acted as the moderator in a He -3 detector portal monitor array; the $\mathrm{He}-3$ detector material was not modeled.

### 5.4 Experiment and simulation analysis/comparisons

Experimental and simulation analysis were performed with analogous methods so that similar quantities could be directly compared. Experimental data analysis is described in Section 5.2.4.

Experimental and simulation results were compared. The MCNPX - PoliMi code was used to read fission histories from CGMF, FREYA, and its built-in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ models. After measurement post-processing and simulation collision file processing with MPPost, key experiment quantities were recorded and compared. Pulse height and cross-correlation distribution agreement help to demonstrate basic detector response and geometry accuracy, but higher order quantities were compared to investigate fission model differences.

### 5.4.1 Background considerations

A background experiment was performed to subtract chance events from the ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ signals. Higher-order background coincidences were not as significant; for each increase in coincidence number the rate decreased approximately by an order of magnitude.

The pulse height distribution from each $\mathrm{NaI}(\mathrm{Tl})$ detector is shown in Figure 5.4. The distributions show characteristic background photon peaks. There is a significant difference between detector response at higher heights, away from 0.415 Vns where detectors were gain matched. The uppermost photopeak ranges from 1.2 to 1.5 Vns The different detectors deviate toward large pulse heights because signals were read from the pre-amplifier without further pulse shaping and the $\mathrm{NaI}(\mathrm{Tl})$ response is expected to be slightly non-linear. Pulses were not shaped because pulse shaping worsens time resolution.

Experiment cross-correlation data in Figure 5.5 show that neutron background is significantly less than photon background rates. The correlated background between approximately $\pm 20 \mathrm{~ns}$ is primarily from environmental background neutron cross-talk, whereas outside of that range only uncorrelated chance coincidences are observed. The two peaks on either side of time zero are evidence that photon-photon coincidences arise


Figure 5.4: All eight $\mathrm{NaI}(\mathrm{Tl})$ detector background pulse height distributions over a 100 hour period over the full digital dynamic range.


Figure 5.5: Background cross-correlation distribution between two $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 detectors with 134 degrees between the detectors.
primarily from cross-talk of background photons.
Figure 5.6 shows that the $\mathrm{NaI}(\mathrm{Tl})$ detector count rates are almost an order of magnitude higher than the pair of EJ-309 detectors in Figure 5.5. The double peak feature, indicative of photon cross-talk, is not as evident in Figure 5.6 because the timing resolution is poor.

### 5.4.2 Pulse height distributions

The singles pulse height distributions from the measurement and simulations are shown in Figures 5.7 through 5.11. The distributions are the average of each detector set. The distributions show the background-subtracted pulse height spectra, after PSD in the case of EJ-309s. Non-fission emissions from fission products built up in the Cf- 252 sample


Figure 5.6: Cross-correlation distribution between two $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ detectors with 64 degrees between the detectors.
are included in these spectra; these emissions are primarily photons. A stricter triggering condition, such as higher order coincidences, could improve certainty that detection events are exclusively from fission events, however the best method to ensure detection events are correlated with fission is through the use of a source in an ionization chamber.

As shown in Figures 5.7 through 5.10, results from both EJ-309 detector sizes, $7.62 \times 5.08$ cm and $7.62 \times 7.62 \mathrm{~cm}$, are very similar for both particle types. The discrepancy at the lowest pulse heights is due to a mismatch in the detection threshold. The measured photon spectra agree in shape above $1,000 \mathrm{keVee}$ to each of the models, but agreement with CGMF is best in magnitude. Below 1,000 keVee the models underpredict due to non-fission emissions. The neutron pulse height spectra show good agreement between all models, but above approximately $1,500 \mathrm{keVee}$ the models overpredict the measured result. Above 1500 keVee , the codes diverge from the experimental data. Furthermore, the FREYA results over-predict the results from CGMF and MCNPX - PoliMi.

Figure 5.11 shows the $\mathrm{NaI}(\mathrm{Tl})$ pulse height distribution from measurement and simulation results. Agreement between the measurement and simulation results is poor below $1,000 \mathrm{keVee}$, primarily due to non-fission contributions. Agreement above $1,000 \mathrm{keVee}$ is better, but it is not clear which fission model agrees best. There is significant difference


Figure 5.7: $7.62 \times 5.08 \mathrm{~cm}$ EJ-309 photon pulse height distribution.


Figure 5.8: $7.62 \times 5.08 \mathrm{~cm}$ EJ-309 neutron pulse height distribution.


Figure 5.9: $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 photon pulse height distribution.
between each fission model prediction, however PoliMiand FREYAmodels are most similar.

### 5.4.3 Photon spectra with coincident neutron detection

Conditioning photon pulse height distributions on a coincident neutron detection improves measurement-simulation pulse height distribution agreement, shown in Figures $5.12,5.13$, and 5.14 . The coincidence condition does not impact the shape of the simulation distributions significantly, whereas the measurement distributions are changed. Change in the measurement distribution shape indicates that non-fission emissions from the source are contributing to the distribution.

PoliMi fission model results agree best with the measured result for both EJ-309 detectors, however FREYA agrees best in the $\mathrm{NaI}(\mathrm{Tl})$ distribution. An ionization chamber with a fission foil would further provide better certainty in identifying emissions from fission events.

### 5.4.4 Time cross-correlation distributions

Comparison of time cross-correlation distributions after background subtraction show good agreement between measured and MCNPX - PoliMi simulated results. Figure 5.15 shows a cross-correlation time distribution for neutron-neutron, neutron-photon, photon-


Figure 5.10: $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 neutron pulse height distribution.


Figure 5.11: $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ pulse height distribution.


Figure 5.12: $7.62 \times 5.08 \mathrm{~cm}$ EJ-309 photon pulse height distribution with a neutron coincidence required 5 to 75 ns after the photon detection.


Figure 5.13: $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 photon pulse height distribution with a neutron coincidence required 5 to 75 ns after the photon detection.


Figure 5.14: $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ pulse height distribution with a neutron coincidence required 5 to 75 ns after the photon detection.
neutron, and photon-photon coincidences for both measured and simulated results. The photon-photon distributions disagree outside of approximately $+/-5$ ns due to non-fission, un-modeled photon emissions from the source material, which are not entirely removed through simple background subtraction.

In Figure 5.15, all fission models slightly underpredict neutron-neutron coincidences, but FREYA agrees best. The PoliMi model has good neutron-photon, photon-neutron agreement over the full time range. CGMF has too many low energy neutrons and too few high energy neutrons.

Figure 5.16 shows better fission model agreement to neutron-neutron measurement distributions than in Figure 5.15. The only difference between the two detector sets is the angle between the detectors used to construct the coincidences. The total number of neutron-neutron coincidences was slightly higher at 134 degrees than at 59 degrees because of neutron anisotropy. The higher angle set of 134 degrees should also have a relatively higher energy neutron spectrum because more coincidences arise from fragmentboosted neutrons emitted along the fission fragment axes than in the 59 degree case.

Neutron-photon, photon-neutron, and photon-photon distributions should not be impacted by the difference in detector angle due to fission model features. Neutron-photon and photon-photon angles are isotropic in the fission models. Minor geometry asymme-


Figure 5.15: Cross-correlation distribution between two $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 detectors with 134 degrees between the detectors.
tries could change the distributions slightly.
Time cross-correlation distributions from a $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 and a $7.62 \times 7.62 \mathrm{~cm}$ $\mathrm{NaI}(\mathrm{Tl})$ detector, in Figure 5.17, show similar neutron-photon agreement as previous results. Photon-photon distribution agreement is similar for all models. The photon-photon peak in simulation is broader than the measured result. Again, simulation underpredicts at time differences $+/-10 \mathrm{~ns}$ due to non-fission, un-modeled photon emissions from the source material, which are not entirely removed through simple background subtraction. In the neutron-photon experiment data, a small peak at time zero indicates photon misclassification as neutrons.

Figure 5.18 shows cross-correlation distributions between two $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ detectors. Agreement is poor between the simulation result and measured result because the $\mathrm{NaI}(\mathrm{Tl})$ response is not well emulated by MPPost.

### 5.4.5 Coincidences

A custom script was written to tally coincidences in an 80 ns window for each simulation model and for the measured data. Events were tallied when two or more channels trigger within an 80 ns window. The coincidences were binned by the number of neutrons detected within the coincidence window in Fig. 5.19, with the $\mathrm{C} / \mathrm{E}$ result, the ratio of the simulation result to the experimental result, shown as well. Simulation results for all models over-predict the number of coincidences for all neutron coincidences except zero. There can be zero neutron coincidences when there is a photon coincidence instead. Despite a basic background subtraction, the number of coincidences is underpredicted at zero because background photon coincidences contribute disproportionately. The observed discrepancy does not necessarily indicate a problem with neutron-photon correlation, but may indicate discrepancy in prompt fission neutron spectrum (PFNS). The likely case is a real ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ photon is detected in coincidence with a background photon.

The ratio of the simulated result to the measured result shows that CGMF agrees best over the range of coincidences, but no model agrees well at high neutron coincidences.


Figure 5.16: Cross-correlation distribution between two $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 detectors with 59 degrees between the detectors.


Figure 5.17: Cross-correlation distribution between a $7.62 \times 7.62 \mathrm{~cm}$ EJ-309 and a $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ detector with 74 degrees between the detectors.


Figure 5.18: Cross-correlation distribution between two $7.62 \times 7.62 \mathrm{~cm} \mathrm{NaI}(\mathrm{Tl})$ detectors with 64 degrees between the detectors.

Agreement becomes progressively worse as order of coincidence increases.
The number of photon coincidences from CGMF agrees best with the measured number of coincidences in Figure 5.20. Two photons detected in coincidence is most likely because the number of zero and one photons in a coincidence event is artificially reduced by the overall coincidence condition and the low neutron detection rate.

In Fig. 5.21, the mean number of photons relative to neutron coincidences agrees well, where $\mathrm{C} / \mathrm{E}$ is approximately 1 , for zero and one counts. The agreement is within $10 \%$ up to three neutron counts. Also, the uncorrelated neutron-photon multiplicity model (PoliMi) overpredicts the number of photons toward high neutron coincidences, whereas the negatively correlated models slightly underpredict the number of photons. This result indicates that the true correlation is likely negatively correlated, but weaker than that represented by CGMF and FREYA.

### 5.4.6 Neutron time-of-flight

A script was written to estimate neutron energy spectra through photon tagged time-offlight, which were binned by coincidence multiplicity. The time difference of a photon detection in an EJ-309 and neutron detection in a different EJ-309 was converted to neutron energy assuming the neutron flight path distance, 52.5 cm , from the source to the mean interaction depth in each detector. It is also assumed that the photon originated from the same fission event. Timing resolution is the largest contributor to uncertainty in the estimate of neutron energy, especially for high energy neutrons. This method does not consider late photon emission [34], therefore delayed and scattered photons also contribute to uncertainty in the neutron energy. Ideally, an ionization chamber with a fission foil would be used in this type of measurement. The energy spectra are divided by energy-dependent detector efficiency to estimate the incident neutron spectra.

Figure 5.22 shows the estimated neutron energy spectra from time-of-flight for both measurement and simulation results. The FREYA fission model results agree best with the reference Watt spectrum for Cf-252.

Tables 5.2 and 5.3 show mean neutron energy as a function of coincident detections


Figure 5.19: Neutron coincidences and the ratio of the simulation result to the experimental result, $\mathrm{C} / \mathrm{E}$, for neutron coincidences.


Figure 5.20: Photon coincidences and the ratio of the simulation result to the experimental result, C/E, for photon coincidences.


Figure 5.21: Average number of photon coincidences as a function of neutron coincidences and the ratio of the simulation result to the experimental result, C/E.


Figure 5.22: Neutron energy spectra from measurement and simulation obtained through time-of-flight techniques.

Table 5.2: Average detected neutron energy by time-of-flight over the sensitive range of the detectors, 1.1-8.1 MeV, as a function of neutron coincidences. Omitted entries had insufficient data.

| Number of detected neutrons | Fission model |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | PoliMi | CGMF | FREYA | Experiment |
| 1 | $2.492(2)$ | $2.359(1)$ | $2.563(2)$ | $2.668(2)$ |
| 2 | $2.51(1)$ | $2.422(8)$ | $2.61(1)$ | $2.72(1)$ |
| 3 | $2.49(6)$ | $2.49(6)$ | $2.63(8)$ | $2.7(1)$ |
| 4 | $2.5(6)$ | $2.3(5)$ | $3.2(9)$ | - |

for measured and simulated data. A slight increase in neutron energy is observed with the number of coincident detections in table 5.2 and 5.3. More data is required to resolve any trend in the neutron energy; the upward trend is small relative to the statistical uncertainties.

Table 5.3: Average detected neutron energy by time-of-flight over the sensitive range of the detectors, 1.1-8.1 MeV, as a function of photon coincidences. Omitted entries had insufficient data.

| Number of detected photons | Fission model |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | PoliMi | CGMF | FREYA | Experiment |
| 1 | $2.489(2)$ | $2.358(2)$ | $2.561(2)$ | $2.669(2)$ |
| 2 | $2.57(1)$ | $2.435(7)$ | $2.66(1)$ | $2.68(1)$ |
| 3 | $2.62(5)$ | $2.49(4)$ | $2.70(6)$ | $2.67(7)$ |
| 4 | $2.8(3)$ | $2.6(2)$ | $3.0(5)$ | $2.9(5)$ |

### 5.5 Conclusions and future work

Fission models PoliMi, CGMF, and FREYA captured some key observed features from this experiment. These experimental results indicate that all fission models require improvements to refine neutron and photon energy and multiplicity distributions. PoliMi, however, had the best neutron and photon spectra agreement with experiment data, because it uses evaluated data for its model.

For experimental coincidence distributions, no model result agreed well. Future work should be performed to resolve potential spectral-multiplicity effects in this result. Additionally, future work would benefit from using a fission chamber to better condition coincidence counting. The neutron-photon correlated coincidence result indicates negative correlation, between the uncorrelated PoliMi model and the negatively, but more strongly correlated, CGMF and FREYA models.

The neutron TOF energy data relative to the number of neutron coincidences do not indicate a correlation in mean energy for experiment or simulation results. There is, however, a weak positive trend in mean neutron energy relative to the number of photons in coincidence. This result could be biased because the mean neutron energy is estimated using a photon trigger time. Again, future work would benefit from using a fission chamber to better condition coincidence counting.

## Chapter 6

## ${ }^{252}$ Cf(sf) Neutron-Photon Competition Experiment at LANL

This chapter describes work that I performed to quantify ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron-photon multiplicity correlation on an event-by-event basis. This work is taken from my publication on the work [63]. I designed an acquisition system, consisting of CAEN digitizers, and custom software to take to LANL's LANSCE facility where I employed the Chi-Nu organic scintillator array to measure ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutrons and photons. I also modeled the experiment with MCNPX - PoliMi and MPPost. I modified MCNPX - PoliMi to read fission events from CGMF and FREYA into PoliMi, and those results were compared to the experiment data.

### 6.1 Introduction

In nuclear fission, neutrons are primarily emitted first [59] followed by photon emission [64]. However, the details of the transition from neutron to photon emission are poorly understood. This work seeks to observe and quantify the competition between neutron and photon emission in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. Many studies of prompt emissions, exclusive to one particle type, such as neutrons alone, have been done for key fissioning isotopes [50, $52,65,66,67,68,69,70,71]$, but only a few experiments $[28,72,73,74]$ have measured neutrons and photons simultaneously. In previous work, experiments were performed to correlate both neutron and photon emission with fragment properties. One [28] shows a
positive correlation, another [72] observes a complex fragment-dependent correlation, a third [73] reports a negative correlation, while a fourth [74] found no evidence of correlated emission from specific fragment pairs. The fission event models CGMF [11, 29, 41, 42] and FREYA [12, 12, 43, 45, 46, 47, 48], however, predict a negative correlation. Additionally, only one previous experiment [73] commented on event-by-event correlations; the neutron and photon multiplicity from each fission event was measured and a correlation between the neutron and photon multiplicities was observed. Given the contradictory experimental results, it is clear that the transition from neutron emission to photon emission in fission fragment de-excitation is not well understood or measured.

After fission occurs, during fragment de-excitation, neutrons are primarily emitted until the fragment excitation energy nears the neutron separation energy [24]. Neutrons remove much of the excitation energy, but do little to change the angular momentum. Photons are emitted primarily after neutron emission and, in general, decrease the fragment angular momentum [75]. The transition between neutron and photon dominance could give rise to correlations between them, as were previously measured [28, 72, 73, 74].

Recently, physics-based event-by-event models, capable of calculating neutron and photon correlations, were developed to move beyond empirical models [8, 40, 51] and models limited to single particle distributions [53,76]. These models include CGMF [11,29, 41, 42], FREYA [ $12,43,44,45,46,47,48]$, FIFRELIN [77], and GEF [78]. These event-by-event models follow pairs of fission fragments from scission through the complete de-excitation process, capturing correlations between emitted neutrons, photons, and fragments. Many measured data sets are available to validate single-particle distributions from these event-by-event models but few correlated neutron-photon data sets exist and are currently limited to ${ }^{252} \mathrm{Cf}(\mathrm{sf})[28,72,73,74]$. Correlated data are particularly useful to validate the event-by-event treatment of the transition from neutron emission to photon emission.

This work presents measured neutron-photon correlations event-by-event. Neutrons and photons from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ were measured with an organic scintillator array. The measured neutron-photon correlations are compared to simulations employing the CGMF [11, $29,41,42]$, FREYA [12, 43, 44, 45, 46, 47, 48], and MCNPX - PoliMi [8, 40] fission generators.

Here, the built-in MCNPX - PoliMi fission model source card option $\operatorname{IPOL}(1)=1$ is referred to as PoliMi in the following. MCNPX - PoliMi was used to model the laboratory geometry and to transport fission neutrons and photons provided by three fission event generators. This work is the first dedicated measurement of neutron-photon correlations from all fragments on a fission-by-fission basis and provides new insight into neutronphoton competition.

### 6.2 Previous measurements of neutron-photon correlations

The four previous experiments measuring ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron-photon correlations discussed in the introduction $[28,72,73,74]$ are described in more detail in this section. Nifenecker et al. explored the correlation as a function of fragment mass [28]. Wang et al. studied the correlation in fragment mass and in kinetic energy bins [72]. Glässel et al. determined the correlation as a function of fragment kinetic energy as well as on an event-by-event basis [73]. Bleuel et al. isolated event-by-event multiplicities for two sets of fragment pairs [74].

Nifenecker et al. [28] averaged photon and neutron measurements over fragment properties. Therefore this experiment cannot comment on the event-by-event nature of neutron and photon competition. They concluded, however, that there was a linear relationship between the average total photon energy, $\bar{E}_{\gamma}$, and the average number of neutrons emitted for a given fragment, $\bar{\nu}$, in a ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ event $\bar{E}_{\gamma}(A, \mathrm{KE})=[0.75 \bar{\nu}(\mathrm{~A}, \mathrm{KE})+2] \mathrm{MeV}$, where $A$ is the fragment mass number and KE is the fragment kinetic energy. When averaged over a pair of complementary fragments, they reported a relationship between total photon energy and neutron multiplicity of $\bar{E}_{\gamma}^{\mathrm{tot}}=[0.75 \bar{\nu}+4] \mathrm{MeV}$. They further determine a relationship between photon and neutron multiplicity emitted per fragment of $M_{\gamma}=1.13 \bar{\nu}+3$ assuming a proportionality of 1.55 photons per MeV based on the measurements of prompt [33] and delayed [34] photons, $M_{\gamma}(A)$, summed by John et al. [79]. They suggested that their positive correlation is evidence of an increase in the mean spin


Figure 6.1: The average number of photons emitted given neutron number, $E[\gamma \mid \nu]$ (a), and average number of neutrons emitted given photon number, $E[\nu \mid \gamma]$ (b), for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. Results from fission models are compared to data from Nifenecker et al. [28] (a) and from Glässel et al. [73] (b).
of the fragments with excitation energy while the excitation energy is determined from measured fragment masses and total kinetic energy. Other modes of fragment excitation are ignored in their discussion.

The Nifenecker et al. correlation is shown in Fig. 6.1(a) where $E[\gamma \mid \nu]$ is the expected number of photons emitted given the number of neutrons emitted. If the neutron and photon multiplicity probability matrix is $P(\nu, \gamma)$, then $E[\gamma \mid \nu]$ is the row average while $E[\nu]$ is the average $\nu$ over the entire $P(\nu, \gamma)$ matrix.

Wang et al. [72] expanded upon the study in Ref. [28] by correlating photon and neutron multiplicities with total kinetic energy over three fragment mass regions of interest: light ( $85<A<123$ ); symmetric ( $124<A<131$ ); and heavy ( $132<A<167$ ). The light and symmetric mass regions exhibit a linear trend with a positive slope, qualitatively consistent with Ref. [28], whereas the heavy region is nonlinear with an overall positive trend. Wang et al. also showed that the FREYA results followed general trends of the measured neutron- $\gamma$ correlation binned in fragment mass and TKE, but the overall agreement was poor. While FREYA shows a fragment-dependent, positive correlation following the experimental binning, this result is not indicative of the ability of FREYA to reproduce observed neutron and photon competition on a fission-by-fission basis.

On the other hand, Glässel et al. [73] studied correlations between neutron and photon multiplicities on a fission-by-fission basis as well as based on averages such as studied by Nifenecker et al.. When studying averages, they determined that the photon multiplicity distribution as a function of fragment mass, $M_{\gamma}(A)$, was rather independent of mass, in contradiction to the earlier results of John et al. [79]. Thus, rather than the 1.13 photons per neutron obtained by Nifenecker [28], given above, they found $\sim 0.16$ photons emitted per neutron, a much smaller result. In addition, in event-by-event mode, they determined a decrease in $\bar{\nu}$ of 0.02 per emitted photon, suggesting that neutron multiplicity and photon energy are anticorrelated. While they also suggest, like Nifenecker, that a positive correlation with respect to excitation energy is evidence of an increase in the mean fragment spin with excitation energy, they add the qualification that this conclusion does not have any bearing on neutron-photon competition.

The Glässel et al. correlation is shown in Fig. 6.1(b) where $E[\nu \mid \gamma]$ is the expected number of neutrons emitted given the number of emitted photons. For the probability matrix $P(\nu, \gamma), E[\nu \mid \gamma]$ is the column average while $E[\gamma]$ is the average $\gamma$ over the entire $P(\nu, \gamma)$ matrix.

Bleuel et al. [74] found no significant correlation between neutron and photon multiplicity. Using a high-efficiency photon detector and known gamma-ray energy transitions, they isolated the photon multiplicity distributions for two post-neutron emission fragment pairings: two-neutron ${ }^{106} \mathrm{Mo}+{ }^{144} \mathrm{Ba}$ and four-neutron ${ }^{106} \mathrm{Mo}+{ }^{142} \mathrm{Ba}$. The two-neutron distribution yielded $9.9 \pm 0.7$ photons on average while the four-neutron distribution yielded an average of $9.9 \pm 0.5$ photons. In contrast, Nifenecker et al.would predict an increase of $\sim 1.3$ photons for the four-neutron distribution relative to that of two-neutrons, an effect which should have been detectable. The Bleuel et al. conclusion was, however, based on specific fragment pairs with prominent photon lines rather than averages. It was also limited statistically, giving large uncertainties in the measured multiplicities.

The work presented here focuses on observing neutron-photon correlations on an event-by-event basis rather than averaged over fragment mass or energy to investigate event-by-event competition. We seek to determine if the number of photons detected, $\gamma^{\prime}$, in a given fission event has any implication on the number of neutrons detected, $\nu^{\prime}$.

In Figs. 6.1 and 3.10, the calculated distributions for neutron and photon emission from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ are shown for PoliMi, CGMF, and FREYA. There is no correlation between neutrons and photons with PoliMi. Both CGMF and FREYA, however, exhibit similar negative correlations between the particle multiplicities on a event-by-event basis, as shown in Fig. 6.1. The trends from these two calculations are the same, even though the absolute scales are different.

### 6.3 Experimental method and analysis

We measure correlations between neutrons and photons emitted during spontaneous fission of ${ }^{252} \mathrm{Cf}$. First we describe the experiment and the data acquisition. Then we discuss


Figure 6.2: A model of the Chi-Nu detector holder and the $4517.78 \times 5.08 \mathrm{~cm}$ EJ-309 detectors. Fifty-four detectors are pictured. One of the topmost arcs was in place but its signals were not read out. The fission chamber was placed at the center of the hemisphere for the measurement.
correlated background subtraction. Finally, we present simulations of the experiment.

### 6.3.1 Experiment

The Los Alamos National Laboratory Chi-Nu array [13], consisting of 5417.78 cm diameter by 5.08 cm thick cylindrical EJ-309 scintillators coupled to 12.7 cm diameter photomultiplier tubes (Hamamatsu R4144), was used to measure neutrons and photons from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. In this work, because of the number of data channels available in the electronics, only 45 of the detectors were used. The array, shown in Fig. 6.2, has a flight path of 100 cm from each detector to the fission chamber, located at the center of the hemispherical array.

This experiment used an ionization chamber designed and fabricated in 2010 at Oak Ridge National Laboratory (ORNL) [80]. The californium source, with the composition shown in Table 6.1, was deposited over a hemispherical surface in the chamber. In a fission event, one or two fragments escape the surface and deposit energy through ionization, producing a pulse above a fixed threshold set to exclude alpha particle interactions [81].

Table 6.1: The californium source composition and the fission rates from the sources on the date of assay, November 2010, and the date of the experiment, July 2015.

| Isotope | Nov. 2010 <br> Assay $(\mu \mathrm{g})$ | Nov. 2010 <br> Fiss. Rate $(\mathrm{f} / \mathrm{s})$ | July 2015 <br> Fiss. Rate $(\mathrm{f} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: |
| ${ }^{252} \mathrm{Cf}$ | 1.641 | $9.705 \times 10^{5}$ | $2.986 \times 10^{5}$ |
| ${ }^{250} \mathrm{Cf}$ | 0.265 | $8.19 \times 10^{2}$ | $6.45 \times 10^{2}$ |
| ${ }^{248} \mathrm{Cm}$ | 0.173 | 3.06 | 17.5 |

The chamber was positioned in the center of the array on the end of a metal tube. The ionization chamber signal was used as the fission time trigger.

The experiment was performed shortly after the production of the Californium fission chamber relative to the 2.6 year ${ }^{252} \mathrm{Cf}$ half life. Therefore the ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ rate was high relative to spontaneously fissioning impurities in the sample, as we now describe. The fission rate at the time of measurement was $2.98 \times 10^{5}$ spontaneous fissions per second. The majority of those fissions are ${ }^{252} \mathrm{Cf}[82]$ with small contributions from ${ }^{250} \mathrm{Cf}(\mathrm{sf})(0.2 \%)$ and ${ }^{248} \mathrm{Cm}(\mathrm{sf})\left(6 \times 10^{-5} \%\right)$. The different decay rates result in a growing fraction of ${ }^{250} \mathrm{Cf}$ and ${ }^{248} \mathrm{Cm}$ relative to ${ }^{252} \mathrm{Cf}$. However, the fission contributions from ${ }^{250} \mathrm{Cf}(\mathrm{sf})$ and ${ }^{248} \mathrm{Cm}(\mathrm{sf})$ are negligible and are thus ignored in further analysis.

The fission rate in the ionization chamber was low enough that the fission events and their emissions are assumed to be well separated in time. The pile-up of fission events was approximately $3.5 \%$, given the source rate and a 150 ns window, long enough to acquire neutrons at and below the detector threshold energy. The fission chamber pulse height trigger threshold, however, was set for zero digitizer dead time, resulting in a trigger rate of $65 \%$ of the expected fission rate. There were $3.21 \times 10^{9}$ fission triggers above threshold during the experiment.

Pulses from the detectors and fission chamber were digitized using three CAEN V1730 waveform digitizers with 500 MHz sampling and 14 -bit amplitude resolution over a 2 V range. The detectors were gain-matched to 478 keVee at 0.3 V with a lower threshold of 40 keVee (a 0.62 MeV proton recoil equivalent threshold) and an upper threshold of $3,180 \mathrm{keVee}$ (an 8.1 MeV proton recoil equivalent threshold) determined by the upper limit of the 2 V range. All digitized waveforms were recorded for post-processing. Pulse
shape discrimination (PSD) was used to discriminate between neutron and photon events in the liquid organic scintillators $[16,23]$.

For the organic scintillators, only pulses above a 100 keVee lower threshold (the 0.80 MeV proton recoil equivalent threshold) were analyzed. Double-pulse fractional cleaning [83] was used to remove pile-up events. Pulse pile up is removed because the PSD algorithm does not handle that case; pile-up pulses are usually classified as a neutron regardless of the contributing particle types. After cleaning, charge integration PSD [22] was performed. In charge integration PSD, two integrals are computed: one over the whole waveform and one over the tail of the waveform. The tail integral starts 24 ns after the peak. A quadratic PSD line was assigned to discriminate between the two particle types using an algorithm described by Polack et al. [22]. Figure 6.3 shows the tail integral plotted against the total integral. Two bands are produced, one for photons (below the discrimination line) and one for neutrons (above the discrimination line). Significant overlap occurs at small total integrals (below $\sim 0.5 \mathrm{~V} \mathrm{~ns}$ ) and pulse heights (below $\sim 0.1 \mathrm{MeVee}$ ). Therefore, misclassification is most likely in this region. Misclassification of photons as neutrons was estimated to be $\sim 1 \%$ using time-of-flight. After background is subtracted in the time region from fission to 10 ns after the fission, only photon detections are expected and all neutron detections in that region were considered misclassified photons.

The organic scintillators, in this configuration, were sensitive to neutrons above 0.8 MeV , given a 100 keVee threshold, and had limited sensitivity to neutrons above 8.1 MeV . The detectors are sensitive to approximately $77 \%$ of the neutron spectrum with an intrinsic efficiency of $\sim 32 \%$ for the full spectrum. The detectors are sensitive to the full prompt photon spectrum. The intrinsic efficiency to the full photon spectrum is approximately $23 \%$. Obtaining the correlation between the emitted neutron and photon multiplicities using experimental data was not possible because the inverse problem is poorly posed given the low neutron and photon efficiencies. While organic scintillators are sensitive to most of the photon and neutron spectra, these detectors are not uniformly sensitive to the entire spectral energy distribution. Consequently, correlations in regions


Figure 6.3: (a) The tail integral as a function of the total waveform integral. (b) The tail-to-total ratio as a function of pulse height. Two features are apparent: the upper bands in each panel primarily includes neutron detections while the lower bands indicate photon detections, separated by the discrimination line, in red. More than 730,000 detections are shown.
where the detectors are less sensitive may be unobserved or less proportionately observed.
After post-processing of the waveforms, which includes particle identification based on PSD, neutron and photon events in a 400 ns coincidence window were collected. The coincident events were analyzed to produce pulse height, cross-correlation, multiplicity, and time-of-flight distributions. The experimental distributions were then compared to simulated results from the fission models employed.

### 6.3.2 Correlated background subtraction

The simple assumption in a single bin experiment, such as the neutron multiplicity as a function of fragment mass, that the measured signal is a simple sum of real and accidental
counts, does not hold for these data. Instead, we have a two-dimensional histogram of measured events, M, with each element of the histogram, $m_{i, j}$, having two indices: $i$ for the number of detected neutrons and $j$ for the number of detected photons in each event. Each element $m_{i, j}$ is a sum of contributions from a combination of the real, R , and the accidental, A, histograms with elements $r_{k, l}$ and $a_{i-k, j-l}$ respectively,

$$
\begin{equation*}
m_{i, j}=\sum_{k=0}^{i} \sum_{l=0}^{j} r_{k, l} a_{i-k, j-l} \tag{6.1}
\end{equation*}
$$

The one-dimensional background subtraction method used by Diven et al. [84] is extended here to two dimensions (neutrons and photons) to account for the accidental contributions to $m_{i, j}$.

Given $m_{i, j}$, it is possible to solve for the elements of unknown reals histogram $r_{i, j}$, with $(k, l) \neq(i, j)$ :

$$
\begin{equation*}
r_{i, j}=\frac{m_{i, j}-\sum_{k=0}^{i} \sum_{l=0}^{j} r_{k, l} a_{i-k, j-l}}{a_{0,0}} \tag{6.2}
\end{equation*}
$$

Due to the coincidence logic imposed at data acquisition (only events with one or more triggered detections were saved), the $m_{0,0}$ element could not be measured directly. However, $a_{0,0}$ was directly measurable. Thus, $m_{0,0}$ and $r_{0,0}$ were estimated from the simulation of the experiment. Section 6.4.1 discusses the fidelity of the simulation compared to experiment.

### 6.3.3 Simulation

The PoliMi code was used to model the laboratory geometry and particle transport. PoliMi models the detector system and surrounding laboratory in great detail. The detectors are modeled to almost full detail; the photomultiplier tube electronics are partially homogenized. Ignoring small hardware such as bolts and nuts, the Chi-Nu array structure is fully modeled. The concrete floor was modeled to replicate room-return effects. One topmost detector arc was not used for data acquisition. However, it was left in place during the measurement and therefore was included in the model of the experiment.

The ORNL fission chamber is modeled in detail with the source term sampled over the 1 cm diameter spot on a 304L alloy stainless steel hemispherical surface. A partial MCNPX - PoliMi model input file for this experiment can be found in Appendix 3.

The waveform processing and classification is assumed to be ideal in simulation; particle misclassification is not modeled. Misclassification is most prevalent at low pulse heights. Therefore, a conservative pulse height threshold of 100 keVee was used.

Other fission event generators were also utilized to generate events for transport. The fission event generators (CGMF, FREYA, and PoliMi) were used to produce a history file of fission events which were passed to the full PoliMi model for particle transport. Initial energy, initial direction, and particle type for each particle generated in each individual fission event was passed to PoliMi. The PoliMi code samples a new random fission event when using PoliMi and FREYA. A history file of $1.92 \times 10^{6}$ fission events generated by CGMF were resampled with new, randomly sampled, fission fragment directions.

Following transport, PoliMi records a file detailing interactions within specified detector cells. Details recorded in the interaction file include but are not limited to interaction type, particle type, nucleus of interaction, energy deposited, and time of interaction. This interaction file was passed to a code emulating detector response. The detector response code converts energy deposition to scintillation light, handles multiple interactions, and applies thresholds to ultimately record particle type, light output, and time for each detection. The light output distributions in MeV electron equivalent (MeVee) for energy deposited in MeV from neutron scattering on a proton and from a photon scattering on an electron are shown in Fig. 2.3. The Birks model, a semi-empirical relationship described by Norsworthy et al. [39], was implemented in the detector response code to convert neutron energy deposited on protons to light output in the EJ-309 scintillator. The light output response from photon scattering on electrons was one-to-one. Using PoliMi and the detector response code, the simulated intrinsic efficiency was calculated as a function of incident particle energy and is shown in Fig. 2.3 for neutrons and photons. After detector response is applied, PoliMi simulation results from each ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ event generator were compared to measurement.

### 6.4 Results

We recall that three fission event generators (CGMF, FREYA, and PoliMi) were used to produce a history file of fission events which were passed to the full PoliMi model for particle transport. Initial energy, initial direction, and particle type for each particle generated in each individual fission event was passed to PoliMi for all fission event generators. Experimental and simulated detector results are compared for independent and dependent multiplicities of photons detected, $\gamma^{\prime}$, and neutrons detected, $\nu^{\prime}$, following a fission event.

### 6.4.1 Simulation fidelity

To validate the PoliMi model and the detector response model, EJ-309 detector pulse height and time-of-flight distributions are compared to experiment results in Figs. 6.4-6.7 using PoliMi. PoliMi was used to transport emitted fragments, neutrons and photons from fission events generated by the three models (PoliMi, CGMF, and FREYA). Because evaluated spectra are used in the PoliMi fission source, Mannhart [49] for neutrons and Valentine [51] for photons, we expect agreement with experiment when the geometrical and detector response models are accurate.

The experimental count rates and pulse heights include only events in a specified time range after the fission start signal. A time window of 15 to 150 ns (energy equivalent of 22 to 0.2 MeV ) after the fission events was used for neutrons while, for photons, a time window of 1 to 20 ns after fission was employed. The time regions from -150 to -15 ns and from - 20 to -1 ns before the fission start signal were subtracted as background for neutrons and photons respectively since only accidental detections are expected before the fission start signal.

In Figs. 6.4(a) and 6.5(a), simulated and experimental pulse height distributions are compared and are shown to agree well over most of the pulse height range. The PoliMi result is within $15 \%$ of the experimental result over the entire range for both neutrons and photons. The ratios between the PoliMi and experiment results, C/E,


Figure 6.4: Calculated and experimental mean pulse height neutron distributions (a) and the ratio of the calculation results to the measurement, C/E (b) are shown. The results are averaged over all detectors. The statistical uncertainties are smaller than the points. Approximately $6.1 \times 10^{6}$ detections are shown for the experimental results.


Figure 6.5: Calculated and experimental mean pulse height photon distributions (a) and the ratio of the calculation results to the measurement, C/E (b) are shown. The results are averaged over all detectors. The statistical uncertainties are smaller than the points. Approximately $1 \times 10^{7}$ detections are shown for the experimental results.
shown in Figs. 6.4(b) and 6.5(b), better quantify the agreement. In the neutron pulse height histogram, disagreement above 0.8 MeV is attributed to error in the function to convert proton recoil energy to light output used in the detector response emulator [39]. For photon pulse heights below 0.8 MeV , the simulation overpredicts the count rate. Because low pulse height detections are susceptible to PSD misclassification, some photon events are misclassified as neutron events or vice versa. However, the photon simulations agree within $5 \%$ over most of the range. The mean pulse height distributions in Figs. 6.4(a) and 6.5(a) show that the PoliMi model, including detector response, accurately replicates the experiment.

In Fig. 6.6, the simulated neutron time-of-flight distributions agree well with experiment over most of the time range, with the exception of the region below 20 ns . Given the upper (3,180 keVee or $8,100 \mathrm{keV}$ proton recoil) and the lower ( 100 keVee or 800 keV proton recoil) pulse height thresholds, most neutron time-of-flight counts are expected between 25 and 80 ns for a fission neutron spectrum. The experiment is susceptible to particle misclassification, particularly evident below 20 ns whereas the simulated particle identification is perfect. For $30<\Delta t<75 \mathrm{~ns}$, PoliMi agrees with experiment within $10 \%$. A small peak is seen in Fig. 6.6(b) in C/E in this region because fast neutrons arriving at the detector induce photons in the active volume of the detector and some neutrons may be misclassified as photons. Above 75 ns , room return becomes significant and C/E increases. In Fig. 6.7, the simulated and measured photon time-of-flight distributions agree well over most of the time range except for $\Delta t>75 \mathrm{~ns}$ where the model overestimates room return.

Agreement within $10 \%$ is considered sufficient confidence that the measurement and simulation agree and further analysis on higher-order coincidence and correlation results using simulations may be performed with confidence. The PoliMi simulation agrees with experiment, as is expected, because the built-in model uses evaluated multiplicity and energy spectra. The close agreement between the simulated and measurement for the pulse height and time-of-flight distributions provide confidence in the model of the laboratory and the detector response.


Figure 6.6: (a) The calculated and experimental neutron time-of-flight distributions. (b) The ratio of the calculation to the measurement, C/E. The results are averaged over all detectors. Time zero was the time of the fission start signal. The uncertainties are smaller than the points: $3.6 \times 10^{6}$ detections are shown for the experimental result.


Figure 6.7: (a) The calculated and experimental photon time-of-flight distributions. (b) The ratio of the calculation to the measurement, $\mathrm{C} / \mathrm{E}$. The results are averaged over all detectors. Time zero was the time of the fission start signal. The uncertainties are smaller than the points: $6.2 \times 10^{6}$ detections are shown for the experimental result.

### 6.4.2 Correlated fission model comparisons

Comparison of the simulated and experimental pulse height, time-of-flight, and coincidence distributions are shown for each fission model to demonstrate the effect of detector response on each model and to highlight the differences between the models. Jointparticle distributions are then compared to evaluate the correlation and the effect of neutron and photon competition during fragment de-excitation in experiment and simulation. Differences between the models may be expected in both single and inter-particle distributions.

The CGMF and the FREYA photon and neutron pulse height histograms do not agree well with experiment, as shown in Figs. 6.8 and 6.9. CGMF underestimates neutron pulse heights over the sensitive range and FREYA overestimates over most of the range, especially at high pulse heights. This indicates that the CGMF neutron spectrum is too soft while the FREYA prompt fission neutron spectrum is too hard in the measured energy range. These calculation results are consistent with the emission data in Fig. 3.11(a) where the CGMF result is softer than the evaluation and FREYA is harder than the evaluation. The good agreement with PoliMi is because the model uses the evaluated spectrum.

The photon pulse height histograms, however, show that the CGMF distribution is uniformly too high above 1 MeVee and FREYA, while lower than CGMF, increasingly overestimates toward higher pulse heights. This indicates that both CGMF and FREYA produce too many high energy photons. Both the CGMF and the FREYA photon energy spectra are higher than the PoliMi spectrum toward higher energies in Fig. 3.11(b). Again, the PoliMi model, using evaluated spectra, shows expected good agreement.

The CGMF and FREYA neutron time-of-flight distributions in Fig. 6.10 exhibit poorer agreement than the PoliMi built-in model. FREYA produces too many fast neutrons while CGMF has too few fast neutrons and too many slower neutrons. This result is consistent with the harder FREYA neutron spectrum and with the softer CGMF neutron spectrum relative to the evaluation, shown in Fig. 3.11(a).

The PoliMi, CGMF, and FREYA photon time-of-flight distributions in Fig. 6.11 show similar agreement below 10 ns while CGMF and FREYA show poorer agreement above 18


Figure 6.8: (a) The calculated and experimental neutron pulse height distributions. (b) The ratio of the calculation to the measurement, C/E. The results are averaged over all detectors. The uncertainties are smaller than the points: $6.1 \times 10^{6}$ detections are shown for the experimental result.


Figure 6.9: (a) The calculated and experimental photon pulse height distributions. (b) The ratio of the calculation to the measurement, C/E. The results are averaged over all detectors. The uncertainties are smaller than the points: $1 \times 10^{7}$ detections are shown for the experimental result.


Figure 6.10: (a) The calculated and experimental neutron time-of-flight distributions. (b) The ratio of the calculation to the measurement, C/E. The results are averaged over all detectors. The uncertainties are smaller than the points: $3.6 \times 10^{6}$ detections are shown for the experimental result.


Figure 6.11: (a) The calculated and experimental photon time-of-flight distributions. (b) The ratio of the calculation to measurement, C/E. The results are averaged over all detectors. The uncertainties are smaller than the points: $6.2 \times 10^{6}$ detections are shown for the experimental result.
ns than PoliMi. Above 18 ns , delayed, scattered, and fast-neutron induced photons contribute to the signal. The PoliMi model produces time-distributed photons where a small fraction of photons are delayed according to Maier-Leibnitz et al. [85], whereas the CGMF and FREYA photon emissions only include prompt emission. The PoliMi result agrees between 18 and 75 ns because of a small contribution of delayed photons but beyond 75 ns PoliMi produces too many delayed photons. The region between 18 and 75 ns could also include a small contribution from neutrons misclassified as photons.

On a event-by-event basis, neutron coincidence distributions are shown in Fig. 6.12. The coincidence distribution is a convolution of the emitted multiplicity and the detector system response. Therefore, given the efficiency of the detection system, $\overline{\nu^{\prime}}$, the mean number of detected neutrons, is expected to be much less than $\bar{\nu}$, and $\overline{\gamma^{\prime}}$, the mean number of detected photons, is also expected to be much less than $\bar{\gamma}$. The neutron coincidences in FREYA agree well with experiment, as shown by the $\mathrm{C} / \mathrm{E}$ for all $\nu^{\prime}$ close to unity. Agreement of CGMF and PoliMi are similarly poor, overestimating C/E for more than two neutrons in coincidence, despite the CGMF $\bar{\nu}$ being higher than that for PoliMi.

The photon coincidence distributions are shown in Fig. 6.13. Photon coincidences from PoliMi agree well with experiment. Here CGMF overestimates the number of photon coincidences over the whole range while FREYA underestimates $P\left(\gamma^{\prime}\right)$ for $\gamma^{\prime}>2$. While PoliMi and FREYA have similar $\bar{\gamma}$, shown in Fig. 3.12(b), the impact of the narrower full photon multiplicity of FREYA shows at higher coincidences.

### 6.4.3 Correlations between neutrons and photons

Figure 6.14 compares the calculated $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$, the expected number of photons detected given the number of neutrons detected, as a function of $\nu^{\prime}$ to the experimental result. $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ and $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$, the number of neutrons detected given the number of photons detected and shown in Fig. 6.15, are corrected for detector dead time as more particles are detected.

Figure 6.14 indicates little to no correlation for PoliMi and negative correlation for the other results. The PoliMi model is uncorrelated, therefore the result is expected to


Figure 6.12: (a) Detected neutron multiplicity distribution, $P\left(\nu^{\prime}\right)$, after fission. (b) Calculated results relative to experiment. There are $3.3 \times 10^{8}$ neutron detections in the experimental result. Error bars represent statistical uncertainty only.


Figure 6.13: (a) Detected photon multiplicity distribution, $P\left(\gamma^{\prime}\right)$, after fission. (b) Calculated results relative to experiment. There are $5.6 \times 10^{8}$ photon detections in the experimental result. Error bars represent statistical uncertainty only.


Figure 6.14: Expected number of detected photons given $\nu^{\prime}$ neutrons detected in coincidence, $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$. The experimental data include $7.8 \times 10^{8}$ detected fission events. Error bars represent statistical uncertainty only.
be invariant with neutron coincidences. The negative multiplicity correlation in CGMF and FREYA gives the expected result of decreased $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ for increasing $\nu^{\prime}$. This trend, however, is weak. In particular, since $\nu^{\prime}=4$ is greater than the measured $\bar{\nu}$ for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$, $\sim 3.76$, the uncertainty on the model calculations, combined with the detector efficiencies, leads to large uncertainties on $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ for this value of $\nu^{\prime}$.

Figure 6.15 shows the relationship between $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ and $\gamma^{\prime}$ for the experiment and the simulations. Little to no correlation in PoliMi was observed while a negative correlation is seen for CGMF and FREYA, similar to the result in Fig. 6.14, albeit with a clearer trend in the zoom of $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ in Fig. 6.15(b), as expected. Here $\gamma^{\prime}=4$ is less than the measured average photon multiplicity for ${ }^{252} \mathrm{Cf}(\mathrm{sf}), \sim 7.98$ [53]. Thus one might expect the simulations to have smaller uncertainties for this value of $\gamma^{\prime}$, as shown in Fig. 6.15. The larger CGMF uncertainty on both $\nu^{\prime}=4$ and $\gamma^{\prime}=4$ in Figs. 6.14 and 6.15 due to the reuse of events from the history file.

We now discuss how the results compare to those of previous experiments. Recall that Glässel et al. found a negative neutron and photon multiplicity correlation of 0.02 neutrons per photon [73] on an event-by-event basis while Nifenecker et al. [28] suggested
a positive correlation of 0.89 neutrons per photon. To place these results on Fig. 6.15, a simple forward model was employed to propagate them through an analytic correlation model including detector response.

The analytic model assumed that both the neutron and the photon energy spectra were invariant with multiplicity, a binomial neutron multiplicity distribution [84], a double Poisson photon multiplicity distribution [53], and linear correlation between neutron and photon multiplicity. The photon spectrum is known to soften as photon multiplicity increases [86]. Assuming an invariant photon spectrum would only result in a small bias because the organic scintillators are sensitive to the full photon spectrum.

The photon multiplicity distribution $\Pi(G)$ for $G$ prompt photons emitted was assumed to be a double Poisson distribution [53],

$$
\begin{equation*}
\Pi(G)=C_{1} \frac{\left(C_{2}\right)^{G} e^{-C_{2}}}{G!}+\left(1-C_{1}\right) \frac{\left(C_{3}\right)^{G} e^{-C_{3}}}{G!}, \tag{6.3}
\end{equation*}
$$

where $C_{1}=0.675, C_{2}=6.78$, and $C_{3}=9.92$ [53]. The neutron and photon multiplicities were assumed to be linearly correlated. In the forward model, the photon distribution, Eq. (6.3), was assumed to be unchanged while the neutron multiplicity was adjusted by linearly varying the average number of neutrons emitted, $\bar{\nu}$, for a fixed photon multiplicity $G$. The neutron multiplicity distribution was assumed to be binomial [84] with emission of up to $m=9$ neutrons allowed,

$$
\begin{equation*}
P(\nu)=\frac{m!}{\nu!(m-\nu)!}\left(\frac{\bar{\nu}}{m}\right)^{\nu}\left(1-\frac{\bar{\nu}}{m}\right)^{m-\nu} . \tag{6.4}
\end{equation*}
$$

The neutron and photon efficiencies simulated by PoliMi were applied to the emitted photon and neutron distributions to produce $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ as a function of $\gamma^{\prime}$ for the Nifenecker and Glässel correlations, +0.89 and $-0.02 \bar{\nu}$ per emitted photon, respectively. The agreement between the experimental result and Nifenecker et al. in Fig. 6.15 is poor. Nifenecker et al. lies above the experiment data and all simulations with the discrepancy increasing with $\gamma^{\prime}$. This poor agreement suggests that the positive multiplicity correlation binned with fragment properties observed by Nifenecker does not predict neutron-photon
competition on an event-by-event basis. Thus the strong positive correlation suggested by Nifenecker is excluded by our result. Figure 6.15(b) omits the Nifenecker result to show low $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ to separate other results.

The Glässel correlation, however, shows a slightly negative trend in $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$, smaller than the trends of CGMF, FREYA, and our experimental result.

Using a linear fit to the $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ data and the correlation model outlined in Eqs. (6.3) and (6.4), the experimental result shows a weak negative correlation of $-0.0016 \pm 0.0096$ $\bar{\nu}$ per emitted photon that is small relative to the uncertainty. This result indicates a weaker neutron-photon correlation than the Glässel result, also weaker than the CGMF and FREYA results. The Bleuel et al. data [74], based on measurements of the photon multiplicity distribution with two and four neutrons emitted from $\mathrm{Mo} / \mathrm{Ba}$ fragment pairs, indicated little to no correlation. However, the Bleuel et al. experiment may have been insensitive to the weak correlation measured here. Additionally, it is not clear how selecting fragments with specific neutron multiplicities might bias the result of Ref. [74].

Calculated relative to experiment data, C/E, shown in Figs. 6.8,6.9,6.10, and 6.11, demonstrate some uncertainty in the detector response, both in calculations and in experiment. We expect the uncertainty in detector response to manifest as a discrepancy in the expected magnitude of the calculated $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ or $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ data, but we do not expect uncertainty to affect in the overall trend or correlation of the data. Therefore, the comparison of experiment and calculated trends in $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ or $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ are reliable. If, however, there were energy-multiplicity correlations that produced strong spectral shifts outside of the sensitive range of the detectors, then the trends in $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ and $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ could be unreliable. However, the detectors should be sensitive to most energy-multiplicity correlations; as stated before, the detectors are estimated to be sensitive to $77 \%$ of the ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutron spectrum and to the full photon spectrum.


Figure 6.15: Expected number of detected neutrons given $\gamma^{\prime}$ photons detected in coincidence (a), $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$, and zoomed in to separate the results at low $E\left[\nu^{\prime} \mid \gamma^{\prime}\right]$ (b). The experimental data include $7.8 \times 10^{8}$ detected fission events. Error bars represent statistical uncertainty only.

### 6.5 Conclusions

A dedicated experiment to observe neutron-photon multiplicity correlations in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ was performed and compared to simulations using correlated emission fission models. Using an analytic correlation model, the experiment showed a weak negative neutron-photon multiplicity correlation on an event-by-event basis of $-0.0016 \pm 0.0096 \bar{\nu}$ per emitted photon for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ that is small relative to the uncertainty. While the estimated correlation has large uncertainty, the result suggests possible weak competition between neutron and photon emission.

The simulated results for all employed models agree qualitatively with the pulse height and the time-of-flight distributions, but PoliMi results agree best. Comparison of the experiment and the PoliMi simulation results show that MCNPX - PoliMi with CGMF and FREYA generated events best explain the neutron-photon multiplicity correlation because of their inherent negative correlation. The correlation in the CGMF and FREYA models, however, is stronger than observed in the experiment.

Future work should include experiments that simultaneously measure fragment properties and emissions with high efficiency. Higher neutron and photon efficiency would allow for a more sensitive measurement of the multiplicity correlation. Event-by-event correlations measured with respect to TKE would help to understand how excitation and spin impact emission competition. Additionally, experiments should include measurements of event-by-event energy correlations.

## Chapter 7

## Measured and Simulated ${ }^{240} \mathbf{P u}($ sf $)$ Prompt Neutron-Photon Competition Experiment at LANL

Previous work that I performed, shown in Chapter 6, found weak neutron-photon competition during fragment deexcitation in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. In the case of ${ }^{240} \mathrm{Pu}(\mathrm{sf})$, there are no published experimental data on neutron-photon correlations or competition. Here, I applied similar experimental methods from the ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ work in Chapter 5 and 6 to a new experiment to measure ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutrons and photons with a stilbene scintillator array at LANL. The goal of this work was observe neutron-photon multiplicity correlation in ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ through experiments to measure event-by-event neutron and photon multiplicity and then to compare data to simulation results from correlated and uncorrelated fission models. By reading fission-model-generated events into MCNPX - PoliMi and using the same detector response, I was able to reliably compare simulation data from each fission model to experiment data.

In this work, I designed a stilbene-PMT based scintillator array, pictured in Figure 7.1, to measure neutron-photon multiplicity on a fission-by-fission basis. I also assembled a CAEN-based acquisition system and software package to collect waveform data. I took that array and acquisition system to LANL to measure emissions from a $0.695 \mathrm{~g}, 94 \%$ ${ }^{240} \mathrm{Pu}$ sample. I then wrote analysis scripts to process acquired data for pulse integral and correlated distributions.


Figure 7.1: A photograph of the 24 stilbene detector array. Stilbene scintillators are coupled to ET Enterprises 9214b PMTs with readout bases and are then encased in 3D printed plastic cases. Two rings of eight detectors are arranged around a central axis; four detectors are pointed downward on top of a cavity for the source material; and four detectors are underneath the source cavity.

### 7.1 Introduction

Similar to published work on ${ }^{252} \mathrm{Cf}(\mathrm{sf})$, both neutron and photon emissions from ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ are well studied independently. Multiplicity and energy distributions are well known. However, there are no prior experiments to measure neutrons and photons simultaneously on an event-by-event basis. Many measurements of bulk plutonium material have been performed with organic scintillators, but none focused exclusively on ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ and neutron-photon correlations.
${ }^{240} \mathrm{Pu}(\mathrm{sf})$ is particularly challenging to measure because ${ }^{240} \mathrm{Pu}$ has a small spontaneous fission branching ratio $\left(5 \times 10^{-6} \%\right)$, is difficult to find enriched, and is often contaminated with ( $\alpha, \mathrm{n}$ ) emissions. The plutonium sample used here, described in Ref. [87], is almost ideal for neutron-photon correlation measurements because it is large enough at 0.695 g to be measured in a reasonable time-frame, but is not too large as to have significant contribution from induced fissions or as to self-shield low energy photons. Additionally, the sample is enriched to $94 \mathrm{Wt} \%{ }^{240} \mathrm{Pu}$ and has a small $(\alpha, \mathrm{n})$ contribution with $\alpha=$ 0.142 , where $\alpha$ is defined as the $(\alpha, \mathrm{n})$ rate divided by the spontaneous fission neutron
rate.
A high $\alpha$-decay photon rate is of concern when measuring plutonium samples with organic scintillators. Plutonium isotopes in the sample primarily $\alpha$ decay or produce daughters that also $\alpha$ decay. The $\alpha$ particle, however, will not escape the sample. Many characteristic photons are emitted from the $\alpha$ decays in the sample, however one is of particular concern, a 59.5 keV photon from ${ }^{241} \mathrm{Am}$. Most $\alpha$ decays produce low energy photons that are self-shielded, but the 59.5 keV photon from ${ }^{241} \mathrm{Am}$ is highly probable and can escape the sample.

### 7.2 Experimental Method and Analysis

An array of 24 stilbene scintillators, each coupled to a PMT, were arranged around a 0.695 g plutonium sample enriched in ${ }^{240} \mathrm{Pu}$ to $94 \mathrm{Wt} \%$.

### 7.2.1 Plutonium source description

Bulk plutonium sample emissions are complex relative to those from ${ }^{252} \mathrm{Cf}$ samples. For freshly fabricated ${ }^{252} \mathrm{Cf}$ samples, all emissions are typically assumed to be from ${ }^{252} \mathrm{Cf}(\mathrm{sf})$, whereas emissions from bulk plutonium samples include spontaneous fission from all isotopes, induced fission on all isotopes, $\alpha$ decay, and ( $\alpha, n$ ) in widely varying fractions.

The plutonium sample (LANL identification FCZ-158 [87]) contains plutonium isotopes and a small amount of ${ }^{241} \mathrm{Am}$, described in Table 7.1. The sample mass was decayed to show the masses at the time of the experiment. A significant increase in ${ }^{241} \mathrm{Am}$ occurs because ${ }^{241} \mathrm{Pu} \beta^{-}$decays into ${ }^{241} \mathrm{Am}$ with a 14.3 year half-life. The other plutonium isotopes have relatively long half-lives and have changed insignificantly in weight fraction.

In this experiment analysis, results are focused on coincident detections therefore only sources of coincident emissions were considered. Most of the sample material is ${ }^{240} \mathrm{Pu}$, but the emission rates must be considered. Ideally for this experiment, the sample would only produce ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutrons and photons, however it is also a source of $(\alpha, n)$ and $\alpha$ decay photons. Table 7.3 shows the primary correlated emissions from the plutonium sample,

Table 7.1: The FCZ-158 0.695 g plutonium source composition on the assay date and at the time of the experiment. The composition values at the date of the experiment were obtained through decaying the August 1991 values.

| Isotope | Aug. $1991(\mathrm{Wt} \mathrm{\%})$ | Apr. 2018 (Wt\%) |
| ---: | :---: | :---: |
| ${ }^{238} \mathrm{Pu}$ | 0.016 | 0.013 |
| ${ }^{239} \mathrm{Pu}$ | 0.955 | 0.954 |
| ${ }^{240} \mathrm{Pu}$ | 93.77 | 93.51 |
| ${ }^{241} \mathrm{Pu}$ | 0.699 | 0.193 |
| ${ }^{242} \mathrm{Pu}$ | 4.56 | 4.56 |
| ${ }^{241} \mathrm{Am}$ | 0.001 | 0.4862 |

Table 7.2: The $\alpha$-decay rates from the FCZ-158 plutonium sample at the time of the experiment. The decay rates were obtained through decaying the plutonium sample composition from the August 1991 assay.

| Isotope | $\alpha / \mathrm{s}$ |
| :---: | :---: |
| ${ }^{238} \mathrm{Pu}$ | $5.7 \times 10^{7}$ |
| ${ }^{239} \mathrm{Pu}$ | 232 |
| ${ }^{240} \mathrm{Pu}$ | $1.1 \times 10^{4}$ |
| ${ }^{241} \mathrm{Am}$ | $3.4 \times 10^{7}$ |

where fortunately, most of the emissions were from ${ }^{240} \mathrm{Pu}(\mathrm{sf})$. Using a PoliMi model of the source material, an estimated $3 \%$ of emitted neutrons were from induced fissions. Further simulations include fissions and ( $\alpha, n$ ), but analysis does consider induced fissions. Simulations include ${ }^{239} \mathrm{Pu}(\mathrm{sf})$. The full MCNPX - PoliMi model input file for this experiment can be found in Appendix 4.

Characteristic $\alpha$-decay gamma rays are a significant source of sample emissions, but most are of low energy relative to detector thresholds. Table 7.2 shows the $\alpha$-decay rates at the time of the experiment, and one $\alpha$ decay can produce multiple coincident gamma rays. $\alpha$-decay gamma ray is unlikely to deposit enough energy to trigger waveform acquisition in the detector. These gamma rays are still problematic because they can contribute to pile up and noise in fission signals.

A radiograph of the sample and three layers of stainless steel casing are shown in Figure 7.2, where the outermost casing is 3.11 cm in height and 5.66 cm in diameter. The second layer of casing moves within the outer case, therefore it is difficult to accurately know the sample location.

Table 7.3: Correlated emission rates from the FCZ-158 plutonium sample at the time of the experiment. The emission rates were obtained through decaying the plutonium sample composition from the August 1991 assay.

| Reaction | $\mathrm{n} / \mathrm{s}$ | $\mathrm{\gamma} / \mathrm{s}$ | reactions $/ \mathrm{s}$ |
| ---: | :--- | :---: | :---: |
| ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ | 600 | 1780 | 278 |
| ${ }^{239} \mathrm{Pu}(\mathrm{sf})$ | $1.5 \times 10^{-4}$ | $4.6 \times 10^{-4}$ | $6.6 \times 10^{-5}$ |
| $(\alpha, n)$ | 85 | 57 | 85 |



Figure 7.2: Radiograph image of the plutonium metal sample and casing with dimensions of the casing. The inner cannisters float freely within the outermost cannister.

### 7.2.2 Detector array and acquisition

An array of stilbene scintillators was designed, shown in Fig. 7.1, to efficiently measure high-order neutron and photon multiplets. The stilbene cells measure 5.08 cm diameter by 5.08 cm thick, pictured in the bottom left of Figure 2.5. The cells were wrapped in polytetrafluoroethylene and then cased in aluminum. Each cell was coupled to a 5.08 cm diameter ET Enterprises 9214b PMT, pictured with a readout base in Figure 2.5.

Two rings of eight detectors were arranged 7.25 cm radius from a central axis; four detectors were pointed downward on top of a cavity for the source material, 26.7 cm from the table top; and four detectors were underneath the source cavity. Each detector was held in place with $1 / 8^{\prime \prime}$ aluminum plates. Two plates held the side detectors and one plate held the top four detectors. The aluminum plates were bolted to two hexagons of 1 " square box tubing, one at the top of the plate and one at the bottom.

Two CAEN V1730 16-channel waveform digitizers and four CAEN V6533 VME 6channel high voltage supplies in a CAEN VME8008B 8-slot crate and a desktop acquisition system were used to collect waveform data. The high voltage supplies and digitizers were controlled via USB with the desktop, but acquired data was transmitted via two optical links. The digitizers had DPP-PSD firmware which allows for onboard PSD, zero suppression, and constant fraction discrimination timing. The DNNG acquisition code Data Acquisition For CAEN Apparatuses (DAFCA) was used to communicate with the digitizers and save data to the desktop.

The digitized waveforms for channels $2,4,6$, and 8 on both boards showed large baseline drift between acquisition folders and were not included in the final analysis. Waveforms from these channels could not be used for PSD because the baseline drifted outside of the dynamic range.

The FCZ-158 sample was measured for 88.5 hrs over five days, and a ${ }^{137} \mathrm{Cs}$ calibration source was measured each morning. The ${ }^{137} \mathrm{Cs}$ source was used to gain-match the Compton edge from each detectors pulse integral distribution.

### 7.2.3 Modeling

Similar to previous experiments, the MCNPX - PoliMi code was used to model the laboratory geometry and particle transport in great detail, shown in Figure 7.3. PoliMi models both the detector system and the surrounding laboratory. MPPost was used to model the detector response.

Fission events from FREYA and PoliMi (IPOL(1)=3) were used in PoliMi particle transport to produce the detector collision event file; CGMF fission events were not used. CGMF ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ histories were not available at the time of writing, but this and other isotopes are currently being added to the code. With $\alpha=0.142$, the PoliMifission and $(\alpha, n)$ sources were mixed such that there are $0.142(\alpha, n)$ neutrons per fission neutron. The $(\alpha, n)$ reactions were modeled, as an approximation, as PoliMibuilt-in sources with $63 \%$ ${ }^{238} \mathrm{PuO}_{2}(\operatorname{IPOL}(1)=-38)$ and $37 \%{ }^{241} \mathrm{AmO}_{2}(\operatorname{IPOL}(1)=-41)$. When the $(\alpha, n)$ PoliMi sources are negative, the full $\alpha$-decay gamma-ray chain is ignored and one ( $\alpha, n$ ) occurs per nps . An $1 \mathrm{Wt} \%$ oxygen mass contamination was estimated in the plutonium sample.

The aluminum table with a cadmium sheet and a concrete floor were modeled. The detectors were modeled to almost full detail, but the photomultiplier tube electronics were partially homogenized. The plutonium FCZ-158 sample was modeled according to specifications in Tables 7.1 and 7.3 (ignoring ${ }^{239} \mathrm{Pu}(\mathrm{sf})$ ) and sizes from the radiograph in Figure 7.2.

In simulation, waveform classification is ideal. A 50 keVee pulse integral threshold was used, and is a conservative threshold for stilbene. A conservative threshold was used to account for the high photon-to-neutron ratio and to make a reliable comparison to simulation results.

To properly model the detector system, we need to quantify the system energy resolution and to understand the Compton edge location. The true Compton edge location allows us to convert pulse integrals in Vns to MeVee.

A ${ }^{137} \mathrm{Cs}$ source was measured with a single stilbene scintillator to obtain a pulse integral histogram, which shows a single Compton continuum from the 662 keV photon, shown in Fig. 7.4. The experiment was modeled in MCNPX - PoliMi, including the


Figure 7.3: The MCNPX - PoliMi model of the 24 stilbene detector array with aluminum $1 / 8^{\prime \prime}$ plates and $1 "$ square box tubing to hold the detectors in place. The source was placed in the detector cavity ( 15.5 cm in diameter) and in plane with the center ring of detectors. These cross-sections do not show the top four detectors pictured in Figure 7.1.


Figure 7.4: Experimental and an unbroadened and broadened ${ }^{137} \mathrm{Cs}$ simulation pulse integral histogram result showing the Compton edge at 478 keV and portion of the continuum. The counts above 478 keV are multiple scatter events. The broadening indicates $15.7 \%$ resolution at FWHM and a calibration of 1.53 Vns at 478 keVee .
single detector and ${ }^{137} \mathrm{Cs} 662 \mathrm{keV}$ source, to tally photon energy deposited in the detector cell. The simulated energy deposited histogram shows an unbroadened Compton continuum, however the observed result is broadened due to photoelectron statistics, variable scintillation efficiency, electronic noise from readout, and drift in time of the response [20]. The unbroadened Compton continuum is then Gaussian iteratively broadened to match the experiment histogram. The final broadened result indicates $16 \%$ resolution at 478 keVee and is shown in Fig. 7.4. For this detection system, we found $\alpha=0.0075, \beta=0.026$, and $\gamma=26.96$ in MeVee for Eqn. 3.1. We also found a calibration constant of $3.2 \mathrm{Vns} / \mathrm{MeVee}$. This calibration and the dynamic range of the digitizer gives an upper threshold of 2.52 MeVee .

A ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ source was measured with a single stilbene scintillator to obtain a pulse integral histogram for neutrons, after PSD. The experiment was modeled in MCNPX - PoliMi, including the single detector and ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ source, to tally neutron energy deposited in the detector cell. The Birks model [39] was used to estimate light output from proton recoils in the stilbene with coefficients $S=1.63$ and $k B=11.83$, shown in Fig. 7.5. Electron recoil light output was treated as linear. The simulation and experimental pulse integral


Figure 7.5: Calculated neutron and photon detection efficiency and light output distributions used in the detector response code for neutron scattering on a proton and for photon scattering on an electron in a $5.08 \varnothing x 5.08 \mathrm{~cm}$ stilbene detector. Proton recoil light output uses coefficients $S=1.63$ and $k B=11.83$ from the Birks model [39].
histograms are compared in Fig. 7.6. Experiment and calculation agreement is good with most points differing by less than $10 \%$, but there is larger scatter above 1.5 MeVee due to limited statistics. The good agreement in pulse integral distributions indicates a valid light output response in MPPost.

Figure 7.5 also shows the MCNPX - PoliMiand MPPostcalculated intrinsic efficiency as a function of incident particle energy for neutrons and photons. The neutron efficiency peaks at approximately $50 \%$ near 1 MeV and decreases toward higher energies. The photon efficiency peaks at approximately $35 \%$ just below 1 MeV and decreases to a sharp drop just above 2.5 MeV . The sharp drop in photon efficiency above 2.5 MeV occurs because waveforms were clipped by the upper range of the 2 V digitizer.


Figure 7.6: (left) Pulse integral distribution results and (right) calculated over experiment from a single detector experiment and simulation of ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ neutrons. The uncertainties are smaller than the points in the integral distribution.

### 7.3 Results

Processed ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ experiment and simulation results are shown in Figs. 7.7- ??. Pulse integral distributions are shown to demonstrate a high fidelity model. The mean number of detected neutrons given a detected photon multiplicity are shown to evaluate multiplicity correlation in the experiment and fission models, and to evaluate the magnitude of competition in fission fragment deexcitation.

A histogram of the tail integral as a function of the total integral was used to apply a PSD line, which separates neutron and photon events. The total integral was over 200 ns of the waveform, and the tail was over 152 ns of the waveform. An algorithm based on that described in Polack et al. [22] was used to find the optimal discrimination line. Neutron events lie above the discrimination line because more scintillation light occurs in the tail relative to the total than for photons, due to a greater quantity of longer-lived triplet states produced by neutron events. The photon-to-neutron ratio is 59 for this plutonium sample, making for especially challenging PSD at low pulse integrals, where overlap of the two bands is significant.


Figure 7.7: Experimental ${ }^{240} \mathrm{Pu}(\mathrm{sf}) \mathrm{PSD}$ histogram from 1.7 hrs of data on a single detector. Neutrons lie above the red line and photons lie below. Events at a total integral of 0.5 MeVee and tail of 1 MeVee are pile-up pulses.

### 7.3.1 Correlated fission model comparisons

In Figure 7.8(a), the simulated neutron pulse integral distributions agree well with the experiment data. Good agreement demonstrates that the neutron model is adequate for singles events. Both simulation results diverge from the experiment result above 0.75 MeVee , indicating that both simulated spectra are too hard. The overestimate at high pulse integrals could be partially due to the modeled ( $\alpha, n$ ) spectrum, which is harder than the ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ spectrum. The $(\alpha, n)$ spectrum of this sample is not well characterized.

In Figure 7.8(b), the simulated photon pulse integral distributions underestimate the experiment data over the full range. The simulation result only includes fission photons and photons in coincidence with $(\alpha, n)$, whereas the experiment data also includes unmodeled $\alpha$-decay gamma rays and other fission product decays. Significant Compton edges can be seen near 0.5 MeVee and 1.3 MeVee . The 0.5 MeV Compton edge is from various $\alpha$-decay gamma rays including those from ${ }^{240} \mathrm{Pu}$ at 642 keV and from ${ }^{241} \mathrm{Am}$ at 653 and 662 keV [88]. The Compton edge at 1.3 MeVee is likely from the $\beta+$ decay of ${ }^{19} \mathrm{Ne}$ producing characteristic gamma rays of $1.357,1.444$, and 1.554 MeV [89]. Because this disagreement is largely due to single, uncorrelated photon events, it does not invalidate photon coincidence data from these simulations.

Figure 7.9 shows the photon pulse integral distribution when conditioned on another


Figure 7.8: (a) Neutron and (b) photon experiment and simulation ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ pulse integral distributions summed over all detectors and on a per fission basis. Pulse integrals for all coincidences are shown. The uncertainties are smaller than the points. For neutrons $1.6 \times 10^{7}$ and for photons $9.2 \times 10^{8}$ detections are shown for the experimental results.
detection. The coincidence condition significantly reduces the effect of $\alpha$-decay gamma rays and the agreement with simulation distributions is good. Most of the coincidence photons are from fission rather than $\alpha$ decays, but small Compton edges are still visible near 0.5 and 1.3 MeV .

A two-dimensional histogram of neutron and photon coincidences from the plutonium sample and from background were made using a 300 ns coincidence window and signals from all included detectors. Background coincidences were removed from the plutonium sample coincidences. Figure 7.10 shows the detected neutron coincidence $\nu^{\prime}$ count rates. The simulated results generally follow the experiment data, but diverge toward higher coincidences. The FREYA count rates are slightly less than the PoliMi data, likely due to differences in the neutron multiplicity distributions. The simulated neutron coincidences overpredict for the whole range of observed coincidences. The simulations overpredict because in the neutron pulse integral distributions in Fig. 7.8(a) both fission models also overpredict the experiment count rates.

Figure 7.11 shows the detected photon coincidence $\gamma^{\prime}$ count rates. The simulation data poorly model the experiment data at low coincidences, but agreement improves toward higher coincidences. Many $\alpha$-decay gamma rays were present in the experiment


Figure 7.9: Photons in coincidence with another detection from experiment and simulation ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ pulse integral distributions summed over all detectors and on a per fission basis. The uncertainties are smaller than the points.


Figure 7.10: Background subtracted experiment and simulated ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron coincidence distributions. The uncertainties are smaller than most points and represent statistical uncertainty only.


Figure 7.11: Background subtracted experiment and simulated ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ photon coincidence distributions. The uncertainties are smaller than most points and error bars represent statistical uncertainty only.
data that were not modeled. These unmodeled gamma rays contributed most to low coincidences and would not occur with a correlated neutron. The fission model data are in good agreement.

### 7.3.2 Correlations between neutrons and photons

The mean number of photons detected with respect to the number of neutrons detected $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ is sensitive to neutron-photon multiplicity correlation. Figure 7.12(a) shows $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ increase for the experiment and PoliMi data, but decrease for the FREYA data. The PoliMi data increases at a greater rate than the experiment data. Neither of the simulation results agree well in magnitude, as we would expect, because the experiment includes unmodeled $\alpha$-decay gamma rays. Figure 7.12(b) shows a positive slope in the PoliMi data, suggesting that the PoliMi fission model produces too many photons as neutron multiplicity increases. The slight positive trend in the PoliMi data is caused by induced fissions in the sample which increase the effective observed neutron multiplicity. The effect from induced fissions is also captured in the FREYA calculations, but competes with FREYAs negative neutron-photon multiplicity. The negative slope in the FREYA data suggests that the model produces too few photons as neutron multiplicity increases. In the PoliMi fission model, neutrons and photons are sampled independently, whereas in the


Figure 7.12: (a) Expected number of detected photons $\gamma^{\prime}$ given $\nu^{\prime}$ neutrons detected in coincidence $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ and (b) calculation over experiment. Error bars represent statistical uncertainty only.

FREYA model neutrons and photons are negatively correlated. The data in Fig. 7.12(b) suggest that the true correlation, weak anti-correlation, lies between the PoliMi and FREYA model correlations. Weak anti-correlation in prompt neutron-photon multiplicity is consistent with previous findings of ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ in Ref. [63].

Systematic uncertainties that could contribute to observed trends in $E\left[\gamma^{\prime} \mid \nu^{\prime}\right]$ include strong spectral shifts outside of the sensitive range of the detectors due to energymultiplicity correlations. The detectors are, however sensitive to most of the neutron spectrum and to the full photon spectrum. While the simulations include fission and $(\alpha, n)$ events, $\alpha$-decay gamma rays are unmodeled. The effects of $\alpha$-decay gamma rays are apparent in the data, where the pulse integral distributions are underpredicted and the $\gamma^{\prime}$ multiplicity results are also underpredicted. These $\alpha$-decay gamma rays contribute equally to all $\nu^{\prime}$ because they are uncorrelated with fission events and do not affect the conclusion of anti-correlation in neutron-photon multiplicity.

### 7.4 Conclusions

A dedicated experiment was performed to show, for the first time, anti-correlation in prompt ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron-photon multiplicity. Results from MCNPX - PoliMi simulations
with PoliMi and FREYA fission event generators were compared to the experiment data. The observed anti-correlation is weak and is bounded by the uncorrelated PoliMi model and the more strongly correlated FREYA model.

The simulated neutron pulse integral and multiplicity distributions agree well for both fission event generators. The photon pulse integral and multiplicity distributions do not agree well due to unmodeled gamma rays in the experimental data. The FREYA-generated events best explain the observed data because of their inherent negative correlation. The correlation in the FREYA result is stronger than observed in experiment, similar to previous findings for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ in Ref. [63].

Future work should include experiments with a plutonium sample in a fission ionization chamber or with some other method to trigger only on fission events. A fission triggered data set would reduce the effects of $(\alpha, n)$ and of $\alpha$-decay gamma ray events. Additionally, future work should include simultaneous measurements of fragment properties and of their emissions.

## Chapter 8

## Summary, Conclusions, and Future Work

### 8.1 Summary

In Chapter 1, I discuss the motivation for this work in the context of nuclear safeguards and nonproliferation and in the context fission physics. This discussion highlights how detector technology and sensitivity has outpaced our ability to understand and reliably model fission emissions. I also discuss the specific contributions of this work.

In Chapter 2, I discuss the radiation detectors used in this work. I focus on key photon and neutron reactions in organic and inorganic scintillators. I also discuss the process for producing, converting, and reading out of scintillation light from these detectors.

In Chapter 3, I discuss how MCNPX - PoliMi is used to model particle transport in fission experiments to high fidelity. I also discuss how MCNPX - PoliMi outputs are used in MPPost to emulate detector response for scintillators. I describe how fission event generator outputs were coupled to MCNPX - PoliMi.

In Chapter 4 I show, for the first time, prompt neutron anisotropy from ${ }^{240} \mathrm{Pu}$ was observed and quantified in laboratory experiments. The ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ prompt neutron angular distribution experiment and simulation showed that MCNPX - PoliMi simulations of the laboratory and detector system could be used to reliably estimate neutron cross talk and to ultimately remove the cross-talk contribution. Approximately $20 \%$ of small angle coincidences were from cross talk. ${ }^{252} \mathrm{Cf}$ spontaneous fission neutrons above 0.65 MeV (proton recoil) were observed to be significantly more anisotropic than ${ }^{240} \mathrm{Pu}$ spon-
taneous fission neutrons above that same energy. These experimental results were used to improve the FREYA fission event generator [48]. Results from this work helped to verify ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron-neutron angular distributions and thereby a fragment excitation energy sharing parameter in FREYA. With an improved excitation energy sharing parameter, FREYA can now be reliably used to predict experimental outcomes sensitive to the ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron angular distribution.

In Chapter 5, I show that the fission models PoliMi, CGMF, and FREYA generally captured key observed singles features from this experiment for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. Experiment data were compared to MCNPX - PoliMi simulations using correlated emission fission models. The results indicate that all models could improve neutron and photon energy and multiplicity distributions. PoliMi, however, agreed with experiment data the best for neutron and photon spectra, because PoliMi uses evaluated data for its models. No model result agreed perfectly well to experiment coincidence distributions. Neither experimental nor simulated neutron TOF energy data relative to neutron coincidences indicates a strong correlation in mean energy. A weak, positive trend in mean neutron energy relative to the number of photons in coincidence was observed. However, the trend could be biased because neutron energy is estimated by photon triggered TOF.

Chapter 6 describes a dedicated experiment to observe neutron-photon multiplicity correlations in ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. Experimental data were compared to simulations using correlated emission fission models. The experimental data showed a weak negative neutronphoton multiplicity correlation on an event-by-event basis of $-0.0016 \pm 0.0096 \bar{\nu}$ per emitted photon for ${ }^{252} \mathrm{Cf}(\mathrm{sf})$. This result suggests weak competition between neutron and photon emission. Results also suggest that the MCNPX - PoliMi with CGMF and FREYA generated events best explain the neutron-photon multiplicity correlation. CGMF and FREYA have inherent negative correlation, but the correlation in the models is stronger than observed in the experiment.

Chapter 7 describes another dedicated experiment to show, for the first time, anticorrelation in prompt ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ neutron-photon multiplicity. Results from MCNPX - PoliMi simulations employing PoliMi and FREYA fission event generators were compared to the ex-
periment data. The observed anti-correlation was weak and was bounded by the uncorrelated PoliMi model and the more strongly correlated FREYA model. Again, FREYA generated events best explain the observed data because of their inherent negative correlation.

### 8.2 Conclusions

My fission experiments and simulations are useful and have already been used [90] to improve event-by-event fission models. Ongoing collaboration between DNNG and fission event generator developers will continue to refine fission models with these experiment data. Improved fission models are immensely useful to radiation detector system design and prediction, especially for novel nuclear safeguards and nonproliferation techniques [55, 58,91]. Work in this thesis ultimately contributes to global nuclear security and promoting the safe use of nuclear technology.

Efficient and cost-effective radiation detector system design relies heavily on accurate Monte Carlo particle transport codes, and these codes are only as accurate as the data that they use. Often in nuclear safeguards and nonproliferation detector systems are designed to be sensitive to fission emissions; consequently it is imperative that fission models used to inform design are accurate. ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ is especially important in safeguards and nonproliferation because ${ }^{240} \mathrm{Pu}$ is present in all plutonium samples and is usually the driving source of induced fission chains. ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ is a practical surrogate for fissile isotope emissions in the laboratory, therefore an accurate model is necessary for this isotope.

### 8.3 Future work

Future work should include experiments that simultaneously measure fragment properties and emissions with high efficiency. Higher neutron and photon efficiency would allow for a more sensitive measurement of the correlations. Event-by-event correlations measured with respect to fragment TKE would help to understand how excitation and spin impact emission competition. The CGMF and FREYA models start with fragment initial conditions before deexciting through emissions. Therefore, it would be useful to measure both the
starting condition (fragment properties) and the ending condition (neutron and photon emissions).

## Appendix 1. Neutron Angular Distribution in ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ from the Joint Research Centre Experiment in Ispra, Italy

The full MCNPX - PoliMi model is included.
c DNNG FNMC: PM2 with 1 cm Pb
c
c Cells
c
c EJ-309 Detectors

c 1
$1001-0.935-1211$ imp:n, p=1 \$EJ-309 Liquid
$1019-2.51-10 \mathrm{imp}: n, \mathrm{p}=1$
$1029-2.51-11 \mathrm{imp}: \mathrm{n}, \mathrm{p}=1$
$1035-2.6989 \quad-1312 \mathrm{imp}: \mathrm{n}, \mathrm{p}=1$
$1045-2.6989 \quad-14 \quad 15 \mathrm{imp}: \mathrm{n}, \mathrm{p}=1$
$105 \quad 5-2.6989 \quad-16 \quad 17 \mathrm{imp}: \mathrm{n}, \mathrm{p}=1$
\$Optical Coupling
\$Optical Window
\$Detector casing
\$Large Ring
\$Small Ring
c 2
106 LIKE 100 BUT TRCL=1
107 LIKE 101 BUT TRCL=1
108 LIKE 102 BUT TRCL=1
109 LIKE 103 BUT TRCL=1
110 LIKE 104 BUT TRCL=1
111 LIKE 105 BUT TRCL=1
c 3
112 LIKE 100 BUT TRCL=2
113 LIKE 101 BUT TRCL=2
114 LIKE 102 BUT TRCL=2
115 LIKE 103 BUT TRCL=2
116 LIKE 104 BUT TRCL=2
117 LIKE 105 BUT TRCL=2
c 4
118 LIKE 100 BUT TRCL=3
119 LIKE 101 BUT TRCL=3
120 LIKE 102 BUT TRCL=3

```
    1 2 1 ~ L I K E ~ 1 0 3 ~ B U T ~ T R C L = 3 ~
    122 LIKE 104 BUT TRCL=3
    123 LIKE 105 BUT TRCL=3
c 5
    124 LIKE 100 BUT TRCL=4
    125 LIKE 101 BUT TRCL=4
    126 LIKE 102 BUT TRCL=4
    127 LIKE 103 BUT TRCL=4
    128 LIKE 104 BUT TRCL=4
    129 LIKE 105 BUT TRCL=4
c 6
    130 LIKE 100 BUT TRCL=5
    1 3 1 \text { LIKE } 1 0 1 \text { BUT TRCL=5}
    132 LIKE 102 BUT TRCL=5
    1 3 3 \text { LIKE 103 BUT TRCL=5}
    1 3 4 \text { LIKE 104 BUT TRCL=5}
    135 LIKE 105 BUT TRCL=5
c 7
    136 LIKE 100 BUT TRCL=6
    137 LIKE 101 BUT TRCL=6
    138 LIKE 102 BUT TRCL=6
    1 3 9 \text { LIKE } 1 0 3 \text { BUT TRCL=6}
    140 LIKE 104 BUT TRCL=6
    141 LIKE 105 BUT TRCL=6
c 8
    142 LIKE 100 BUT TRCL=7
    143 LIKE 101 BUT TRCL=7
    144 LIKE 102 BUT TRCL=7
    145 LIKE 103 BUT TRCL=7
    146 LIKE 104 BUT TRCL=7
    147 LIKE 105 BUT TRCL=7
c 9
    148 1 -0.935 -22 21 imp:n,p=1
    149 9 -2.51 -20 imp:n,p=1
    150 9 -2.51 -21 imp:n,p=1
    151 5 -2.6989 -23 22 imp:n,p=1
    152 5 -2.6989 -24 25 imp:n,p=1
    153 5 -2.6989 -26 27 imp:n,p=1
$EJ-309 Liquid
$Optical Coupling
$Optical Window
$Detector casing
$Large Ring
$Small Ring
c 10
154 LIKE 148 BUT TRCL=1
155 LIKE 149 BUT TRCL=1
156 LIKE 150 BUT TRCL=1
157 LIKE 151 BUT TRCL=1
158 LIKE 152 BUT TRCL=1
159 LIKE 153 BUT TRCL=1
c 11
160 LIKE 148 BUT TRCL=2
161 LIKE 149 BUT TRCL=2
```

```
    162 LIKE 150 BUT TRCL=2
    163 LIKE 151 BUT TRCL=2
    164 LIKE 152 BUT TRCL=2
    165 LIKE 153 BUT TRCL=2
c 12
    166 LIKE 148 BUT TRCL=3
    1 6 7 \text { LIKE 149 BUT TRCL=3}
    168 LIKE 150 BUT TRCL=3
    169 LIKE 151 BUT TRCL=3
    1 7 0 \text { LIKE 152 BUT TRCL=3}
    1 7 1 ~ L I K E ~ 1 5 3 ~ B U T ~ T R C L = 3 ~
c 13
    172 LIKE 148 BUT TRCL=4
    173 LIKE 149 BUT TRCL=4
    174 LIKE 150 BUT TRCL=4
    175 LIKE 151 BUT TRCL=4
    176 LIKE 152 BUT TRCL=4
    177 LIKE 153 BUT TRCL=4
c 14
    178 LIKE 148 BUT TRCL=5
    179 LIKE 149 BUT TRCL=5
    1 8 0 \text { LIKE } 1 5 0 \text { BUT TRCL=5}
    181 LIKE 151 BUT TRCL=5
    182 LIKE 152 BUT TRCL=5
    1 8 3 \text { LIKE 153 BUT TRCL=5}
c 15
    184 LIKE 148 BUT TRCL=6
    185 LIKE 149 BUT TRCL=6
    186 LIKE 150 BUT TRCL=6
    1 8 7 \text { LIKE 151 BUT TRCL=6}
    188 LIKE 152 BUT TRCL=6
    1 8 9 ~ L I K E ~ 1 5 3 ~ B U T ~ T R C L = 6 ~
c 16
    190 LIKE 148 BUT TRCL=7
    191 LIKE 149 BUT TRCL=7
    1 9 2 ~ L I K E ~ 1 5 0 ~ B U T ~ T R C L = 7 ~
    1 9 3 ~ L I K E ~ 1 5 1 ~ B U T ~ T R C L = 7 ~
    194 LIKE 152 BUT TRCL=7
    195 LIKE 153 BUT TRCL=7
c
c Table
c
\begin{tabular}{llllll}
201 & 5 & -2.7 & -31 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Surface \\
206 & 5 & -2.7 & -32 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Support \\
207 & 5 & -2.7 & -33 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Support \\
208 & 5 & -2.7 & -34 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Support \\
209 & 5 & -2.7 & -35 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Support \\
215 & 5 & -2.7 & -36 & \(\operatorname{imp}: \mathrm{n}, \mathrm{p}=1\) & \(\$\) Leg
\end{tabular}
```




```
        C Casing
    24 RCC 26.54 0 -5.31 1.54 0 0 5.08 $Large
    Ring Outside
    25 RCC 26.54 0 -5.31
        1.54 0 0 3.9075
    CRing Inside
    26 RCC 24.54 0 -5.31 2 0 0 4.362 $Small Ring
    Outside
    27 RCC 24.54 0 -5.31 2 0 0 0 3.962
    Anside
c
c Table
c
    318 BOX -50 -100 -0.5 100 0 0 0
        4.5 $ Surface
    32 8 BOX -50 -100 -4.9 4.4 0 0 0
        4.4 $ Support
    33 8 BOX 45.6 -100 -4.9 4.4 0 0 0
        4.4 $ Support
    34 8 BOX -45.6 -100 -4.9 91.2 0 0 0
        4.4 $ Support
    35 8 BOX -45.6 95.6 -4.9 91.2 0 0 0
        4.4 $ Support
    36 8 BOX -50 -2.2 -4.9 4.4 0 0 % 0
        \hookrightarrow-85.5 $ Leg
    37 8 BOX 45.6 -2.2 -4.9 4.4 0 0 0
        4-85.5 $ Leg
    38 8 BOX -50 -100 -4.9 4.4 0 0 % 0
        4-85.5 $ Leg
    39 8 BOX 45.6 -100 -4.9 4.4 0 0 0
        \hookrightarrow -85.5 $ Leg
    40 8 BOX -50 95.6 -4.9 4.4 0 0 0
        \hookrightarrow-85.5 $ Leg
    41 8 BOX 45.6 95.6 -4.9 4.4 0 0 0
        4-85.5 $ Leg
c
c Lead Shielding
c
    51 CZ 6.5 $outer cylinder
    52 CZ 5.5 $inner cylinder
    53 PZ 15.25 $top
    54 PZ -16.25 $bottom
c
c Ground
c
    61 PZ -108 $ Floor level
c
c PM Material and Container
```

```
    71 RCC 0 0 -4.02 0 0 0 1.32 0.5 $PM2
    72 RCC 0 0 -5.77 0}0
    73 RCC 0 0 -6.25 0}0
    77 RCC 0 0 0-17.25 0
c
c Detector Structure
c
    90 RPP 22 22.3175 -5.05 5.05 -17.25 13.35
        $front vertical plate
    91 RPP 24.2225 24.54 -5.05 5.05 -17.25 13.35
        @ $ack vertical plate
    106 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 - -15.345
    $ $bottom bar
    107 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    $top bar
    108 1 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    $ $bottom bar
    109 1 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    \rightarrow ~ \$ t o p ~ b a r
    110 2 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    & $bottom bar
    111 2 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    \rightarrow ~ \$ t o p ~ b a r
    112 3 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    @ $bottom bar
113 3 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    $top bar
114 4 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    \hookrightarrow $bottom bar
115 4 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    -> $top bar
116 5 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    $ $ottom bar
117 5 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    & $op bar
118 6 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 - 15.345
    4 $bottom bar
119 6 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    $top bar
120 7 RPP 22.3176 24.2224 -10.0333 10.0333 -17.25 -15.345
    4 $bottom bar
121 7 RPP 22.3176 24.2224 -10.0333 10.0333 11.445 13.35
    $top bar
C ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
c Environment
c
    500 RPP -500 500 -500 500 -500 500
```

c
c Data
c
c Translations
c
$\begin{array}{llllllllllllll}\text { TR1 } & 0 & 0 & 0 & 0.7071 & 0.7071 & 0 & -0.7071 & 0.7071 & 0 & 0 & 0 & 1\end{array}$
$\begin{array}{lllllllllllll}\text { TR2 } & 0 & 0 & 0 & 0 & 1 & 0 & -1 & 0 & 0 & 0 & 0 & 1\end{array}$
$\begin{array}{lllllllllllll}\text { TR3 } & 0 & 0 & 0 & -0.7071 & 0.7071 & 0 & -0.7071 & -0.7071 & 0 & 0 & 0 & 1\end{array}$
$\begin{array}{lllllllllllll}\text { TR4 } & 0 & 0 & 0 & -1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 1\end{array}$
TR5 $00 \begin{array}{llllllllllll}1\end{array}$
$\begin{array}{lllllllllllll}\text { TR6 } & 0 & 0 & 0 & 0 & -1 & 0 & 1 & 0 & 0 & 0 & 0 & 1\end{array}$
$\begin{array}{lllllllllllll}\text { TR7 } & 0 & 0 & 0 & 0.7071 & -0.7071 & 0 & 0.7071 & 0.7071 & 0 & 0 & 0 & 1\end{array}$
TR8 $000-17.25$
TR9 $16.92 \quad 0 \quad 5.31$
c
c Physics
c
MODE n p
PHYS:N J 20
PHYS:P 011
CUT:P 2J 0
c
c Source
c
SDEF cel=701 pos=0 0 -4.02 axs=0 01 rad=d1 ext=d2 erg=d3
SC1 Source radius (inner outer)
SI1 $0 \quad 0.5$
SC2 Source height
SI2 $0 \quad 1.32$
SI3 L 34
SP3 0.99450 .0055
IPOL $\begin{array}{lllllllllllllll}99 & 1 & 2 & 1 & J & 1 & 16 & 100 & 106 & 112 & 118 & 124 & 130 & 136 & 142\end{array}$

| 148 | 154 | 160 | 166 | 172 | 178 | 184 | 190 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

NPS $715403 \$ 1430805=$ Number of reactions in 3600 sec (aged $\hookrightarrow \mathrm{PM}$ src)
FILES 21 DUMN1
DBCN
PRDMP 2J 1
c
c Materials
c
c EJ-309 liquid scintillator $d=-0.916$
c (Eljen Technologies, EJ-309 Fact Sheet)
c
$\mathrm{m} 1 \quad \mathrm{NLIB}=70 \mathrm{c}$ PLIB=04p

| 1001 | 0.555443 | $\$ \mathrm{H}$ |
| :--- | :--- | :--- |
| 6012.50 c | 0.444557 | $\$ \mathrm{C}$ |

c
c Air, Dry (near sea level) d=-1.205E-3
c (Mat. Compendium PNNL)
c

$$
\mathrm{m} 2 \quad \mathrm{NLIB}=70 \mathrm{c} \quad \text { PLIB }=04 \mathrm{p}
$$

```
m3 82000.42c 1
```

c
c Polyethylene $d=-0.9300$
c (Mat. Compendium PNNL)
c
$\mathrm{m} 4 \quad \mathrm{nlib}=60 \mathrm{c} \quad \mathrm{plib}=04 \mathrm{p}$ $1001-0.143716$ $6000-0.856284$
c
c Aluminum table $\mathrm{d}=-2.70$
c

```
m5 nlib=60c plib=04p
```

        13027 - 1
    c
c Concrete (Mat. Compendium PNNL) $\mathrm{d}=-2.3$
c (Mat. Compendium PNNL)
c m6 nlib=60c plib=04p
$1001-0.022100$
$6000-0.002484$
$8016-0.574930$
$11023-0.015208$
$12000-0.001266$
$13027-0.019953$
$14000-0.304627$
$19000-0.010045$
$20000-0.042951$
26000.42c -0.006435
c
c Pu Metal Sample d=-19.7
c (PM2)
c
m7 94238.42c -0.00004
$94239.60 \mathrm{c} \quad-0.87367$
$94240.60 \mathrm{c}-0.04076$

```
            94241.60c -0.00028
            94242.60c -0.00013
            95241.61 c -0.00234
            28058.60 c -0.03466
            28060.60c -0.01335
            28061.60c -0.00058
            28062.60c -0.00185
            29063.60c -0.02209
            29065.60c -0.00985
    c
    c Steel d=-7.92
    c (Mat. Compendium PNNL)
    c m8 26000.55c - 0.6950
        24000.50c -0.1900
        28000.50c -0.0950
        25055.51c -0.0200
    c
    c BK7
    c
        m9 NLIB=70c PLIB=04p
            14028 -0.323138999
            8016 -0.483882614
            5011 -0.033384805
            56138-0.027496631
            11023-0.077153875
            19039 -0.052216449
            33075-0.002726626
c
c Tallies
c
c detectors
c
c F31:n 11.3 12.3 13.3 14.3 15.3 16.3 17.3 18.3 19.3
c E31 0 0.5 0.7 29i 1 899i 10 100
c C31 0 1
c F41:p 11.3
c E41 0 999i 10
c C41 0 1
c
```


# Appendix 2. Neutron and Photon Correlations from the University of Michigan ${ }^{252} \mathrm{Cf}(\mathrm{sf})$ Experiment 

The full MCNPX - PoliMi model is included.
c nps $=1$ e 7 over a 100 cores seems legit
c runs about $2 \mathrm{e} 4 \mathrm{f} / \mathrm{s}$
c June 201432 Detector Cf-252 Measurement
c
c Version: Detectors with PMTs, fully commented. 8/7/14
c
c This model reflects the detector set up used in June 2014
c using the double horizontal rings rig previously used at $\hookrightarrow$ LANSCE
c in 2013 by Andreas Enquist and Brian Wieger. Model was used
c in 2014 by Matt Marcath and Steve Ward.
c
c The $3 x 2$ detectors are in a checkerboard pattern with the NaIs
c on one half ring, with the first $3 x 2$ on the leftmost side (
$\hookrightarrow$ from the
c perspective of the source) being in the upper spot on the pole $\hookrightarrow$
c Refer to the translation section for more details on how these
c are arranged.
c
c Source was at the center of the ring with the upper detectors
c 10 cm above the source height and the lower ring 10 cm below $\hookrightarrow$ the
c source height. Detectors were facing straight with respect to
c the horizon, i.e., not angled up/down to face the source more
c directly. Distance from source to detector face was a radius
c of about 55 cm , equal in all directions. Source is at the
c origin as discussed later.
c
c
c ~~~~~~~~~~ 3 x 21


| 40 | LIKE 7 BUT TRCL=27 | \$ skinny PMT front, mu |
| :---: | :---: | :---: |
| $\hookrightarrow$ metal |  |  |
| 41 | LIKE 8 BUT TRCL=27 | \$ skinny PMT middle |
| 42 | LIKE 9 BUT TRCL=27 | \$ skinny PMT cap |
| 43 | LIKE 10 BUT TRCL=27 | \$ cone |
| 44 | LIKE 11 BUT TRCL=27 | \$ pyrex optical window |
|  |  |  |
| 45 | LIKE 1 BUT TRCL=28 | \$ Al cap front |
| 46 | LIKE 2 BUT TRCL=28 | \$ Al cap sides |
| 47 | LIKE 3 BUT TRCL=28 | \$ detector |
| 48 | LIKE 4 BUT TRCL=28 | \$ Al step |
| 49 | LIKE 5 BUT TRCL=28 | \$ Al ring |
| 50 | LIKE 6 BUT TRCL=28 | \$ large PMT |
| 51 | LIKE 7 BUT TRCL=28 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 52 | LIKE 8 BUT TRCL=28 | \$ skinny PMT middle |
| 53 | LIKE 9 BUT TRCL=28 | \$ skinny PMT cap |
| 54 | LIKE 10 BUT TRCL=28 | \$ cone |
| 55 | LIKE 11 BUT TRCL=28 | \$ pyrex optical window |
| $3 \times 2$ |  |  |
| 56 | LIKE 1 BUT TRCL=31 | \$ Al cap front |
| 57 | LIKE 2 BUT TRCL=31 | \$ Al cap sides |
| 58 | LIKE 3 BUT TRCL=31 | \$ detector |
| 59 | LIKE 4 BUT TRCL=31 | \$ Al step |
| 60 | LIKE 5 BUT TRCL=31 | \$ Al ring |
| 61 | LIKE 6 BUT TRCL=31 | \$ large PMT |
| 62 | LIKE 7 BUT TRCL=31 | \$ skinny PMT front, mu metal |
| 63 | LIKE 8 BUT TRCL=31 | \$ skinny PMT middle |
| 64 | LIKE 9 BUT TRCL=31 | \$ skinny PMT cap |
| 65 | LIKE 10 BUT TRCL=31 | \$ cone |
| 66 | LIKE 11 BUT TRCL=31 | \$ pyrex optical window |
|  |  |  |
| 67 | LIKE 1 BUT TRCL=32 | \$ Al cap front |
| 68 | LIKE 2 BUT TRCL=32 | \$ Al cap sides |
| 69 | LIKE 3 BUT TRCL=32 | \$ detector |
| 70 | LIKE 4 BUT TRCL=32 | \$ Al step |
| 71 | LIKE 5 BUT TRCL=32 | \$ Al ring |
| 72 | LIKE 6 BUT TRCL=32 | \$ large PMT |
| 73 | LIKE 7 BUT TRCL=32 | \$ skinny PMT front, mu metal |
| 74 | LIKE 8 BUT TRCL=32 | \$ skinny PMT middle |
| 75 | LIKE 9 BUT TRCL=32 | \$ skinny PMT cap |
| 76 | LIKE 10 BUT TRCL=32 | \$ cone |
| 77 | LIKE 11 BUT TRCL=32 | \$ pyrex optical window |
| c | $3 \times 28$ |  |
| 78 | LIKE 1 BUT TRCL=35 | \$ Al cap front |
| 79 | LIKE 2 BUT TRCL=35 | \$ Al cap sides |
| 80 | LIKE 3 BUT TRCL=35 | \$ detector |
| 81 | LIKE 4 BUT TRCL=35 | \$ Al step |






| 237 | LIKE 160 BUT TRCL=43 | \$ large PMT |
| :---: | :---: | :---: |
| 238 | LIKE 161 BUT TRCL=43 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 239 | LIKE 162 BUT TRCL=43 | \$ skinny PMT middle |
| 240 | LIKE 163 BUT TRCL=43 | \$ skinny PMT cap |
| 241 | LIKE 164 BUT TRCL=43 | \$ cone |
| 242 | LIKE 165 BUT TRCL=43 | \$ pyrex optical window |
| c |  |  |
| 243 | LIKE 155 BUT TRCL=44 | \$ Al cap front |
| 244 | LIKE 156 BUT TRCL=44 | \$ Al cap sides |
| 245 | LIKE 157 BUT TRCL=44 | \$ detector |
| 246 | LIKE 158 BUT TRCL=44 | \$ Al step |
| 247 | LIKE 159 BUT TRCL=44 | \$ Al ring |
| 248 | LIKE 160 BUT TRCL=44 | \$ large PMT |
| 249 | LIKE 161 BUT TRCL=44 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 250 | LIKE 162 BUT TRCL=44 | \$ skinny PMT middle |
| 251 | LIKE 163 BUT TRCL=44 | \$ skinny PMT cap |
| 252 | LIKE 164 BUT TRCL=44 | \$ cone |
| 253 | LIKE 165 BUT TRCL=44 | \$ pyrex optical window |
| $3 \times 310$ |  |  |
| 254 | LIKE 155 BUT TRCL=45 | \$ Al cap front |
| 255 | LIKE 156 BUT TRCL=45 | \$ Al cap sides |
| 256 | LIKE 157 BUT TRCL=45 | \$ detector |
| 257 | LIKE 158 BUT TRCL=45 | \$ Al step |
| 258 | LIKE 159 BUT TRCL=45 | \$ Al ring |
| 259 | LIKE 160 BUT TRCL=45 | \$ large PMT |
| 260 | LIKE 161 BUT TRCL=45 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 261 | LIKE 162 BUT TRCL=45 | \$ skinny PMT middle |
| 262 | LIKE 163 BUT TRCL=45 | \$ skinny PMT cap |
| 263 | LIKE 164 BUT TRCL=45 | \$ cone |
| 264 | LIKE 165 BUT TRCL=45 | \$ pyrex optical window |
| c ~~~~~~~~~~ 3 x 311 |  |  |
| 265 | LIKE 155 BUT TRCL=46 | \$ Al cap front |
| 266 | LIKE 156 BUT TRCL=46 | \$ Al cap sides |
| 267 | LIKE 157 BUT TRCL=46 | \$ detector |
| 268 | LIKE 158 BUT TRCL=46 | \$ Al step |
| 269 | LIKE 159 BUT TRCL=46 | \$ Al ring |
| 270 | LIKE 160 BUT TRCL=46 | \$ large PMT |
| 271 | LIKE 161 BUT TRCL=46 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 272 | LIKE 162 BUT TRCL=46 | \$ skinny PMT middle |
| 273 | LIKE 163 BUT TRCL=46 | \$ skinny PMT cap |
| 274 | LIKE 164 BUT TRCL=46 | \$ cone |
| 275 | LIKE 165 BUT TRCL=46 | \$ pyrex optical window |
| c | ~ 3x3 12 |  |
| 276 | LIKE 155 BUT TRCL=47 | \$ Al cap front |


| 277 | LIKE 156 BUT TRCL=47 | \$ Al cap sides |
| :---: | :---: | :---: |
| 278 | LIKE 157 BUT TRCL=47 | \$ detector |
| 279 | LIKE 158 BUT TRCL=47 | \$ Al step |
| 280 | LIKE 159 BUT TRCL=47 | \$ Al ring |
| 281 | LIKE 160 BUT TRCL=47 | \$ large PMT |
| 282 | LIKE 161 BUT TRCL=47 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 283 | LIKE 162 BUT TRCL=47 | \$ skinny PMT middle |
| 284 | LIKE 163 BUT TRCL=47 | \$ skinny PMT cap |
| 285 | LIKE 164 BUT TRCL=47 | \$ cone |
| 286 | LIKE 165 BUT TRCL=47 | \$ pyrex optical window |
| c ~~~~~~~~~~~ 3 x 313 |  |  |
| 287 | LIKE 155 BUT TRCL=48 | \$ Al cap front |
| 288 | LIKE 156 BUT TRCL=48 | \$ Al cap sides |
| 289 | LIKE 157 BUT TRCL=48 | \$ detector |
| 290 | LIKE 158 BUT TRCL=48 | \$ Al step |
| 291 | LIKE 159 BUT TRCL=48 | \$ Al ring |
| 292 | LIKE 160 BUT TRCL=48 | \$ large PMT |
| 293 | LIKE 161 BUT TRCL=48 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 294 | LIKE 162 BUT TRCL=48 | \$ skinny PMT middle |
| 295 | LIKE 163 BUT TRCL=48 | \$ skinny PMT cap |
| 296 | LIKE 164 BUT TRCL=48 | \$ cone |
| 297 | LIKE 165 BUT TRCL=48 | \$ pyrex optical window |
| c ~ | $3 \times 314$ |  |
| 298 | LIKE 155 BUT TRCL=49 | \$ Al cap front |
| 299 | LIKE 156 BUT TRCL=49 | \$ Al cap sides |
| 300 | LIKE 157 BUT TRCL=49 | \$ detector |
| 301 | LIKE 158 BUT TRCL=49 | \$ Al step |
| 302 | LIKE 159 BUT TRCL=49 | \$ Al ring |
| 303 | LIKE 160 BUT TRCL=49 | \$ large PMT |
| 304 | LIKE 161 BUT TRCL=49 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 305 | LIKE 162 BUT TRCL=49 | \$ skinny PMT middle |
| 306 | LIKE 163 BUT TRCL=49 | \$ skinny PMT cap |
| 307 | LIKE 164 BUT TRCL=49 | \$ cone |
| 308 | LIKE 165 BUT TRCL=49 | \$ pyrex optical window |
| $3 \times 315$ |  |  |
| 309 | LIKE 155 BUT TRCL=50 | \$ Al cap front |
| 310 | LIKE 156 BUT TRCL=50 | \$ Al cap sides |
| 311 | LIKE 157 BUT TRCL=50 | \$ detector |
| 312 | LIKE 158 BUT TRCL=50 | \$ Al step |
| 313 | LIKE 159 BUT TRCL=50 | \$ Al ring |
| 314 | LIKE 160 BUT TRCL=50 | \$ large PMT |
| 315 | LIKE 161 BUT TRCL=50 | \$ skinny PMT front, mu |
| $\hookrightarrow$ metal |  |  |
| 316 | LIKE 162 BUT TRCL=50 | \$ skinny PMT middle |
| 317 | LIKE 163 BUT TRCL=50 | \$ skinny PMT cap |

319 LIKE 165 BUT TRCL=50

```
c ~~~~~~~~~~~ 3x3 16
```

320 LIKE 155 BUT TRCL=51
321 LIKE 156 BUT TRCL=51
322 LIKE 157 BUT TRCL=51
323 LIKE 158 BUT TRCL=51
324 LIKE 159 BUT TRCL=51
325 LIKE 160 BUT TRCL=51
326 LIKE 161 BUT TRCL=51
$\hookrightarrow$ metal
327 LIKE 162 BUT TRCL=51
328 LIKE 163 BUT TRCL=51
329 LIKE 164 BUT TRCL=51
330 LIKE 165 BUT TRCL=51
\$ cone
\$ pyrex optical window
\$ Al cap front
\$ Al cap sides
\$ detector
\$ Al step
\$ Al ring
\$ large PMT
\$ skinny PMT front, mu
\$ skinny PMT middle
\$ skinny PMT cap
\$ cone
\$ pyrex optical window
c
c
c Space around all the detectors, divided into 4 sections by
$c$ the $x$ and $y$ axis. You can see this from the signs of the $x$ $\hookrightarrow$ and y
c coordinates in the translation cards.
c
c Why go to the trouble of dividing this into 4 sections?
c Because we learned the hard way that there is a limit on how $\hookrightarrow$ many
c characters you enter in a single cell line. It's about 2000, $\hookrightarrow$ but that's
c characters (i.e., $\# 100$ is four characters plus the space $\hookrightarrow$ before and
c after it) so when we were listing every single cell, we $\hookrightarrow$ exceeded that
c limit.
c So this way you should be able to add all the cells you want $\hookrightarrow$ in the
c model and not have that problem.
c
c Cell 996 is for stuff with the x and y coordinates $>0$
$904 \quad 9 \quad-1.84-90 \quad 91-92 \quad 93-94 \quad 95 \quad$ IMP:N, $\mathrm{P}=1$
$914 \quad 9 \quad-1.84 \quad-97 \quad$ IMP:N, $\mathrm{P}=1$
c pvc with a lower desity to account for drawers
$905 \quad 10 \quad-1.1 \quad-96 \quad$ IMP:N, $\mathrm{P}=1$
$996 \quad 0 \quad-999 \quad 901 \quad 902$ \#904

$$
\begin{array}{lllllllllll}
\# 45 & \# 46 & \# 47 & \# 48 & \# 49 & \# 50 & \# 51 & \# 52 & \# 53 & \# 54 & \# 55 \\
\# 56 & \# 57 & \# 58 & \# 59 & \# 60 & \# 61 & \# 62 & \# 63 & \# 64 & \# 65 & \# 66 \\
\# 67 & \# 68 & \# 69 & \# 70 & \# 71 & \# 72 & \# 73 & \# 74 & \# 75 & \# 76 & \# 77 \\
\# 78 & \# 79 & \# 80 & \# 81 & \# 82 & \# 83 & \# 84 & \# 85 & \# 86 & \# 87 & \# 88 \\
\# 123 & \# 124 & \# 125 & \# 126 & \# 127 & \# 128 & \# 129 & \# 130 & \\
\# 131 & \# 132 & \# 133 & \# 134 & \# 135 & \# 136 & \# 137 & \# 138
\end{array}
$$

```
    #139 #140 #141 #142 #143 #144 #145 #146
    #147 #148 #149 #150 #151 #152 #153 #154
    #35 #66 #77 #88 #914
    IMP : N, P=1
c Cell 997 is for stuff with x > 0 and y<0
997 0 -999 901 -902 #904
    #243 #244 #245 #246 #247 #248 #249 #250 #251 #252 #253
    #254 #255 #256 #257 #258 #259 #260 #261 #262 #263 #264
    #265 #266 #267 #268 #269 #270 #271 #272 #273 #274 #275
    #276 #277 #278 #279 #280 #281 #282 #283 #284 #285 #286
    #287 #288 #289 #290 #291 #292 #293 #294 #295 #296 #297
    #298 #299 #300 #301 #302 #303 #304 #305 #306 #307 #308
    #309 #310 #311 #312 #313 #314 #315 #316 #317 #318 #319
    #320 #321 #322 #323 #324 #325 #326 #327 #328 #329 #330
    #264 #319 #286 #297 #308 #275 #330 #253
    IMP : N, P=1
c Cell 998 is for stuff with x and y<0
998 0
    #155 #156 #157 #158 #159 #160 #161 #162 #163 #164 #165
    #166 #167 #168 #169 #170 #171 #172 #173 #174 #175 #176
    #177 #178 #179 #180 #181 #182 #183 #184 #185 #186 #187
    #188 #189 #190 #191 #192 #193 #194 #195 #196 #197 #198
    #199 #200 #201 #202 #203 #204 #205 #206 #207 #208 #209
    #210 #211 #212 #213 #214 #215 #216 #217 #218 #219 #220
    #221 #222 #223 #224 #225 #226 #227 #228 #229 #230 #231
    #232 #233 #234 #235 #236 #237 #238 #239 #240 #241 #242 #905
        61 #176 #187 #198 #209 #220 #231 #242
    IMP : N, P=1
c Cell 999 is for stuff with x < 0 and y > 0
995 0 -999 -901 902 #904
    #1 #2 #3 #4 #5 #6 #7 #8 #9 #10 #11
    #12 #13 #14 #15 #16 #17 #18 #19 #20 #21 #22
    #23 #24 #25 #26 #27 #28 #29 #30 #31 #32 #33
    #34 #35 #36 #37 #38 #39 #40 #41 #42 #43 #44
    #91 #92 #93 #94 #95 #96 #97 #98
    #99 #100 #101 #102 #103 #104 #105 #106
    #107 #108 #109 #110 #111 #112 #113 #114
    #115 #116 #117 #118 #119 #120 #121 #122 #905
    #22 #11 #33 #44
    IMP : N, P=1
9999 0 999 IMP:N,P=0 $void outside space
c BLANK LINE FOLLOWS END OF CELL CARDS
c
c
c ~~~~~~~~~~~~~~~~~~
c
c
```

c Please note that the NaI detectors use surfaces from the $3 x 3 \mathrm{~s}$.
c So if you delete the $3 x 3$ surfaces, the file will crash.
c
c ~~~~~~~~~~~~ EJ309 3x2~~~~~~~~~~~~~~~
10 py $0 . \quad \$$ front outer scint
11 py 0.152 front inner wall
12 py 4.55 \$ scint step
13 py 5.232 \$ ring front
14 py 8.17 \$ large PMT start
15 py 13.53 \$ large PMT end
17 py 13.6316
19 py $28.9475 \$$ skinny PMT end cap
20 py 24.5025 \$ skinny PMT middle
21 py 29.90 \$ PMT outer back
22 cy 3.9625 \$ outer wall scint
23 cy 3.9473 \$ inner wall scint MODIFIED
24 cy 4.0584 \$ inner large PMT
25 cy 4.16 \$ outer large PMT
26 cy $4.52125 \$$ outer scint step
27 cy $5.08 \quad \$$ outer ring
28 cy 2.94 \$ outer skinny PMT
29 cy 2.74 \$ inner skinny PMT middle
30 cy 2.8384 \$ inner skinny PMT front, mu metal
31 RCC $0 \quad 5.2320001 .503 .3 \$$ PYREX Window
c
c ~~~~~~~~~~~NaI
c Note that the NaI cells use surfaces from the EJ309 3x3 below
70 py $0 . \quad \$$ front outer scint
71 py 0.152 front inner wall
72 py 7.09 \$ scint step
73 py 7.73 \$ ring front
74 py 10.71 \$ large PMT start
75 py 16.07 \$ large PMT end
77 py 16.1716
78 py 32.44 \$PMT outer back
79 py 31.4875 \$ skinny PMT end cap
80 py 27.0425 \$ skinny PMT middle
81 py 32.44 \$ PMT outer back
c
c Note the NaIs use some of the $3 x 3$ surfaces so don't delete
c them all if you want the file to run for NaIs.
c ~~~~~~~~~~~~ EJ309 3x3~~~~~~~~~~~~~~
40 py $0 . \quad \$$ front outer scint
41 py 0.152 front inner wall
42 py 7.09 \$ scint step
43 py $7.772 \quad \$$ ring front \$modified
44 py 10.71 \$ large PMT start
45 py 16.07 \$ large PMT end

```
47 py 16.1716
49 py 31.4875 $ skinny PMT end cap
50 py 27.0425 $ skinny PMT middle
51 py 32.44 $ PMT outer back
52 cy 3.9625 $ outer wall scint
53 cy 3.9473 $ inner wall scint MODIFIED
54 cy 4.0584 $ inner large PMT
55 cy 4.16 $ outer large PMT
56 cy 4.52125 $ outer scint step
57 cy 5.08 $ outer ring
58 cy 2.94 $ outer skinny PMT
59 cy 2.74 $ inner skinny PMT middle
60 cy 2.8384 $ inner skinny PMT front, mu metal
61 RCC 0 7.772 0 0 1.2 0 3.25 $ PYREX Window/modified
c
c
c ~~~~~~~~~~~ Other Surfaces
c
c Planes to separate the space around detectors
c into 4 quadrants
c
90 pz -120 $concrete floor 90-95
91 pz -150
92 px 500
93 px -500
94 py 500
95 py -500
901 px 0.001
902 py 0.001
96 rpp -190 -150 -60 60 -120 -20
97 rpp 60 300 140 170 -120 200
c
c Sphere around everything to define void
999 SO 1000.
c BLANK LINE FOLLOWS END OF SURFACE CARDS
c
c
c ~~~~~~~~~~~~~~ The Rest
c
c
mode n p
c ~~~~~~~~~~~~~~}\mathrm{ TRANSLATIONS
c Translations for the double ring holder set work as
c follows (you should read this if you need to move anything):
c
c If you are standing where your source is and
c facing the shorter diameter ring where 3x2s go,
```

c TR20 is the top spot furthest to the left and TR 21 is
c the lower spot on that same pole. TRs 22 and 23 are the
c spots on the second pole from the left, and so on. Thus,
c the top and bottom spots on the right-most pole of that ring
c are TRs 34 and 35 .
c
c If you turn around so you' re facing the other ring for the 3 $\hookrightarrow \mathrm{x} 3 \mathrm{~s}$,
c the system is reversed. TR36 is the upper spot on the RIGHT$\hookrightarrow$ most
c pole (again assuming you are standing in the center of the $\hookrightarrow$ rings).
c So TR36 is the upper detector and TR37 is the lower detector $\hookrightarrow$ on
c the pole furthest to your right. The numbers continue towards $\hookrightarrow$ your left
c until you hit TR50 and TR51 being the top and bottom spots on $\hookrightarrow$ the final
c pole.
c
c Note that in this orientation set-up, the pole with Slots TR20 $\hookrightarrow$ and TR21
c is next to the pole with slots TR36 and TR37. Similarly, the $\hookrightarrow$ pole for
c TR34 and TR35 is next to the pole for TR50 and TR51.
c
c If you move a pole for some reason both translations on that $\hookrightarrow$ pole
c will need to be changed to reflect the new location.
c
c This geometry assumes the detectors are pointed straight level $\hookrightarrow$ with the
c horizontal or z-axis, i.e., how high the detector sits. If $\hookrightarrow$ you want the
c detectors angled toward the source, you'll have to redo the $\hookrightarrow$ translations.
c Because of this imperfect orientation, we kept the detectors $\hookrightarrow$ fairly close
c to the height of the source as noted below.
c
c Also, the vertical orientation assumes your source is at 0 $\hookrightarrow$ height on
c the $z$-axis. Then your detector rings are 10 cm above and 10 $\hookrightarrow \mathrm{cm}$ below
c this plane. All detectors are at one of these two heights.
c
c Every cell that makes up a single detector uses the same $\hookrightarrow$ translation ,
c i.e., all 8 cells for a single NaI should be moved by the same c translation number.
c
c Essentially, one of each detector is built in basically the $\hookrightarrow$ same spot
c and then they have been translated to where they should be. $\hookrightarrow$ Without a
c translation, all detectors would be on top of one another.
c
c Also, the vertical orientation assumes your source is at 0 $\hookrightarrow$ height on
c the $z$-axis. Then your detector rings are 10 cm above and 10 $\hookrightarrow \mathrm{cm}$ below
c this plane. All detectors are at one of these two heights.
c
c Detector faces are 50 cm from the source which is at the $\hookrightarrow$ origin.
c
*TR20 -46.35919 18.73033 10
*TR21 $-46.3591918 .73033-10$
*TR22 -37.15724 33.4565310
*TR23 -37.15724 $33.45653-10$
*TR24 -23.47358 44.1473810
*TR25 -23.47358 $44.14738-10$
*TR26 -6.958655 49.513410
*TR27 -6.958655 $49.5134-10$
*TR28 10.395648 .9073810
*TR29 10.3956 48.90738-10
*TR30 26.49642 .402410
*TR31 26.496 42.4024-10
*TR32 39.4005 30.7830710
*TR33 39.4005 30.78307-10
*TR34 $47.5528 \quad 15.4508510$
*TR35 47.5528 15.45085-10
*TR36 -46.35919 -18.73033 10
$68-2290 \quad 3 \mathrm{~J} \quad 9090 \quad 0$
$68-2290 \quad 3 \mathrm{~J} \quad 90 \quad 90 \quad 0$
$48-42903 \mathrm{~J} 90900$
$48-42903 \mathrm{~J} 90900$
28-62 90 3J 90 90 0
28-62 90 3J 90 90 0
8 -82 90 3J 90900
8 -82 90 3J 90900
$-12-102903 \mathrm{~J} 90900$
$-12-102903 \mathrm{~J} 9090 \quad 0$
$-32-122903 \mathrm{~J} 90900$
$-32-122903 \mathrm{~J} 90900$
$-52 \quad-14290 \quad 3 \mathrm{~J} 9090 \quad 0$
$\begin{array}{lllllll}-52 & -142 & 90 & 3 \mathrm{~J} & 90 & 90 & 0\end{array}$
$-72-162903 \mathrm{~J} 9090 \quad 0$
-72 -162 90 3J 90900
$1122290 \quad 3 \mathrm{~J} \quad 9090 \quad 0$
*TR37 $-46.35919-18.73033-10 \quad 1122290 \quad 3 \mathrm{~J} \quad 9090 \quad 0$
*TR38 $-37.15724-33.4565310 \quad 132 \quad 42 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90 \quad 0$
*TR39 $-37.15724-33.45653-10 \quad 13242 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR40 $-23.47358-44.14738 \quad 10 \quad 152 \quad 62 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR41 $-23.47358-44.14738-10 \quad 1526290 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR42 $-6.958655-49.513410 \quad 1728290 \quad 3 \mathrm{~J} \quad 9090 \quad 0$
*TR43 $-6.958655-49.5134-10 \quad 172 \quad 82 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90 \quad 0$
*TR44 $10.3956-48.9073810 \quad 192 \quad 102 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90 \quad 0$
*TR45 $10.3956-48.90738-10 \quad 192 \quad 102 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR46 $26.496-42.402410 \quad 212 \quad 122 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR47 $26.496-42.4024-10 \quad 212 \quad 12290 \quad 3 \mathrm{~J} \quad 90 \quad 90$
*TR48 $39.4005-30.7830710 \quad \begin{array}{lllllllll}232 & 142 & 90 & 3 J & 90 & 90 & 0\end{array}$
*TR49 39.4005 $-30.78307-10 \quad 232 \quad 142 \quad 90 \quad 3 \mathrm{~J} \quad 90 \quad 90 \quad 0$

```
*TR50 47.5528 -15.4508 10 < 252 162 90 3J 90 90 0
*TR51 47.5528 -15.4508 -10 252 162 90 3J 90 90 0
c ~~~~~~~~~~~~~ END TRANSLATIONS
c
c ~~~~~~~~~~~~~}\mathrm{ General MCNP Stuff
c
c The detectors are arranged for the source to be at the origin
c in all three axis. If you move the source location and want
        the
c detectors evenly spaced around the source, you'll have to redo
        the
c translations to accommodate that.
c
SDEF
c
PRINT 10 40 100}10110 126 128 140 160 117
c void
nps 10000000
c CTME 10.0 $ Stop time in minutes for debugging
c ~~~~~~~~~~~~~ PHYSICS
PHYS:N J 20
PHYS:P 0 1 1
CUT:P 2J 0
c
c
c ~~~~~~~~~~~~~ M
c m1 nlib=60c $ Air, rho=.00093
c 6000 -0.000124
c 7014 -0.755268
c 8016 -0.231781
c 18000.42c -.012827
m2 nlib=60c
    1001 . 5556
        6000 . 4444
m5 13027.60c 1
m6 5011 -0.040064
nlib = 60c $ pyrex
            8016 -0.539562 nlib = 60c
            11023 -0.028191 nlib = 60c
            13027 -0.011644 nlib = 60c
            14000-0.377220 nlib = 60c
            19000-0.003321 nlib = 60c
m7 28000.50c 0.8
        42000.60c 0.05
        14000.60c 0.005
        29063 0.0002 nlib = 60c
        26056 0.1448 nlib = 70c
m21 11023.60c 0.5
        rho}=3.6
```

```
    53127.60c 0.5
m9 1001.60c -0.03 $concrete
    8016.60 c -0.63
    14028.60c -0.24
    20040.60c - 0.1
m10 1001.60c -0.048382 $ PVC
    6000.60c -0.384361
    17000.60c -0.567257
c BK7
m11 NLIB=70c PLIB=04p
    14028-0.323138999
    8016 - 0.483882614
    5011 - 0.033384805
    56138-0.027496631
    11023-0.077153875
    19039-0.052216449
    33075-0.002726626
c
c
c
TALLIES
c
c ~~~~~~~~~~~~~
c Detector cells are tagged for tallies. Each row as written
c below reflects a different group of 8 detectors, so we have
    the
c 3x2s, NaIs, then the 16 3x3s.
C
F8:n 223
IPOL 1 0 1 0 J 1 32 3 14 25 36 47 58 69 80
    93}10110109 117 125 133 141 149 
    157}168179190 201 212 223 23
    245}2556\quad267 278 289 300 311 322
C
RPOL 0.001 0.001
c
FILES 21 DUMN1
    DBCN 1010123
PRDMP 2J 1
c END OF FILE
```


## Appendix 3. ${ }^{252}$ Cf(sf) Neutron-Photon Competition Experiment at LANL

A partial MCNPX - PoliMi model is included. A single detector specification is kept to keep the length of the appendix reasonable. The original input was 10,870 lines.
c cells
c
c Cf ionization chamber
c
$80 \quad 08-8.00 \quad-5 \quad 4 \quad \$$ can cylinder
c $\begin{array}{llllll}81 & 08 & -8.00 & -4 & 6 & -7\end{array} \quad$ \$can front face $\begin{array}{lllll}82 & 08 & -8.00 & -4 & -9 \\ 10\end{array} \quad \$$ back of FC
$8306-9.15 \mathrm{E}-4 \quad-4-10 \quad$ \$inside back cylinder
$8406-9.15 \mathrm{E}-4 \quad-4 \quad 39 \quad$ \$front air space
$8508-8.00 \quad-3 \quad 29 \quad$ \$hemi shell
$860 \quad-2 \quad 18$ Selectrode gap
$87 \quad 08-8.00 \quad-18 \quad$ \$button
$880 \quad-2 \quad-890$ space behind button
c
$990 \quad-22 \quad 23-21 \quad$ \$CCC for source
c
c detector frame
c
c ring L1
$\begin{array}{llllllll}\text { c } 270 & 6 & -9.15 \mathrm{E}-4 & 410 & -409 & 412 & -411 & -413\end{array}$
c 271 1-2.699 $406-405408-407-413(-410: 409:-412: 411$ :
$\hookrightarrow 413)$
c ring L2
c $272 \quad 6 \quad-9.15 \mathrm{E}-4 \quad 420 \quad-419 \quad 422 \quad-421 \quad-423$
с $2731-2.699 \quad 416-415418-417-423(-420: 419:-422: 421$ :
$\hookrightarrow 423$ )
c ring L3
с $274 \quad 6 \quad-9.15 \mathrm{E}-4 \quad 430 \quad-429 \quad 432 \quad-431 \quad-433$
с $2751-2.699 \quad 426-425428-427-433(-430: 429:-432: 431$ : $\hookrightarrow 433)$
c ring R1
$\begin{array}{llllllll}\text { c } 276 & 6 & -9.15 \mathrm{E}-4 & 410 & -409 & 412 & -411 & 414\end{array}$
$\begin{array}{llllllll}\text { c } 277 & 1 & -2.699 & 406 & -405 & 408 & -407 & 414\end{array}$ $\hookrightarrow(-410: 409:-412: 411:-414)$
c ring R2
c $278 \quad 6 \quad-9.15 \mathrm{E}-4 \quad 440 \quad-439 \quad 442 \quad-441 \quad 444$
$\begin{array}{llllllll}\text { c } & 279 & 1 & -2.699 & 436 & -435 & 438 & -437\end{array} 444$ $\hookrightarrow(-440: 439:-442: 441:-444)$
c ring R3
с $280 \quad 6 \quad-9.15 \mathrm{E}-4 \quad 450 \quad-449 \quad 452 \quad-451 \quad 454$
c $281 \quad 1 \quad-2.699 \quad 446-445 \quad 448-447 \quad 454$ $\hookrightarrow(-450: 449:-452: 451:-454)$
c
c support brackets
c
$282 \quad 1 \quad-2.699-455$
$283 \quad 1 \quad-2.699 \quad-456$
$284 \quad 1 \quad-2.699 \quad-457$
$285 \quad 1 \quad-2.699-458$
$286 \quad 1-2.699-459$
$287 \quad 1-2.699-460$
$288 \quad 1 \quad-2.699 \quad-461$
$289 \quad 1 \quad-2.699 \quad-462$
c
c legs
c
$294 \quad 6-9.15 \mathrm{E}-4-465$
$295 \quad 1 \quad-2.699 \quad 465-466$
$296 \quad 1 \quad-2.699 \quad 466-468$
$297 \quad 1 \quad-2.699 \quad 466-467$
$298 \quad 1-2.699-469$
$299 \quad 1 \quad-2.699 \quad-470$
c
$300 \quad 6-9.15 \mathrm{E}-4-471$
$301 \quad 1 \quad-2.699 \quad 471-472$
$302 \quad 1 \quad-2.699 \quad 472-474$
$303 \quad 1 \quad-2.699 \quad 472-473$
$304 \quad 1 \quad-2.699 \quad-475$
$305 \quad 1 \quad-2.699 \quad-476$
c
$306 \quad 6 \quad-9.15 \mathrm{E}-4-477$
$307 \quad 1 \quad-2.699 \quad 477-478$
$308 \quad 1 \quad-2.699 \quad 478-480$
$309 \quad 1 \quad-2.699 \quad 478-479$
$310 \quad 1 \quad-2.699 \quad-481$
$311 \quad 1 \quad-2.699 \quad-482$
c
$312 \quad 6-9.15 \mathrm{E}-4-483$
$313 \quad 1 \quad-2.699 \quad 483-484$

```
314 1 -2.699 484 -486
315 1 -2.699 484 -485
316 1 -2.699 -487
317 1 -2.699 -488
c
318 6 -9.15E-4 -489
319 1 -2.699 489 -490
320 1 -2.699 490 -492
321 1 -2.699 490 -491
322 1 -2.699 -493
323 1 -2.699 -494
c
324 6 -9.15E-4 -495
325 1 -2.699 495 -496
326 1 -2.699 496 -498
327 1 -2.699 496 -497
328 1 -2.699 -499
329 1 -2.699 -500
c
330 6 -9.15E-4 -501
331 1 -2.699 501 -502
332 1-2.699 502 -504
333 1 -2.699 502 -503
334 1 -2.699 -505
335 1 -2.699 -506
c
336 6 -9.15E-4 -507
337 1 -2.699 507 -508
338 1 -2.699 508 -510
339 1 -2.699 508 -509
340 1 -2.699 -511
341 1 -2.699 -512
c
c air space
491 06 -9.15E-4 7999 -8000
    @ $detector space
        (1195)}1295 1395 1495 1595 1695 1795 1895 (1995) (2095) 2195 2295 2395 2495 2595 2695 2795 (2895) 
                            2995 3095 3195 3295 3395 3495 3595 3695
                                    \hookrightarrow 3795
(3895) 3995 4095 4195 4295 4395 4495 4595 (4695)
(4795)}4895 4995 5095 5195 5295 5395 5495 (5595)
                                5695 5795 5895 5995 6095 6195 6295 6395
                                \hookrightarrow 6495
c
\hookrightarrow
c
        \hookrightarrow
        (405:-406:407:-408: 413)
            $ring L1
    (415:-416:417:-418: 423)
                                    $ring L2
```




```
c 1172 01 -2.699 1171 -1170 -1176 $top lid
c 1173 06 -9.15E-4 1174 -1171 -1176
c 1174 19 -0.964 1172 -1174 -1176
c 1175 01 -2.699 1173 -1172 -1176
1184
$air bubble
c
1176 01 -2.699 -1188 1169
    face
1177 01 -2.699 -1189
    face
c
1180 06 -9.15E-4 -1195 2095 $ - 418 $air space with
c
(-1147: 1155: 1156)
(-1156: 1151: 1166)
(-1166: 1169: 1168)
(-1168: 1158: 1159)
(-1159: 1130: 1109)
(-1109: 1134: 1136)
(-1136: 1132: 1163)
(-1163: 1161: 1160)
(-1160: 1132: 1142)
(-1173: 1170: 1175)
( 1177:-1146: 1166)
( 1178:-1146: 1166)
( 1179:-1146: 1166)
( 1180:-1146: 1166)
( 1181:-1146: 1166)
( 1182:-1146: 1166)
1183 $transfer tube
( 1188:-1169) 1189 $mount bracket
c
c Cell cards for detectors #2 through 54 (liquid) were removed
    for printing purposes only. Double space left in their
    place.
c
c
9998 18 -2.25 -7999 -8000
9999 0 8000
c surfaces
c
c
c Cf fission chamber
c
    101 so 0.9271 $button surface 0.365"
    1101 so 0.9273 $button surface++ PoliMi sources fail when
```

```
        sampled on a boundary...
    201 so 1.0541 $inner hemi 0.415"
    301 so 1.1786 $outer hemi 0.464"
c
    4 01 rcc 0 0 1.181 0 0 -6.4678 1.1811
    5 01 rcc 0 0 1.211 0 0 - 6.574 1.27
c
    8 01 pz 0.4801 $back of button
    9 01 pz 0 $front wall of chamber
    1 0 0 1 ~ p z ~ - 0 . 0 7 6 ~ \$ b a c k ~ w a l l ~ o f ~ c h a m b e r ~
c CCC surfaces:
    21 01 cz 0.5000 $1-cm diam deposit
    22 01 pz 1.040
    23 01 pz 0.770
c detector frame rings
c L1,R1:
405 cx 112.8395
406 cx 107.7595
407 px -12.70
408 px -17.78
409 cx 112.522
410 cx 108.077
411 px -13.0175
412 px -17.4625
413 py -22.93
414 py 22.93
c L2:
415 02 cx 112.8395
416 02 cx 107.7595
417 02 px -12.70
418 02 px -17.78
419 02 cx 112.522
420 02 cx 108.077
421 02 px -13.0175
422 02 px -17.4625
423 02 рy -22.93
424 02 py 22.93
c L3:
425 03 cx 112.8395
426 03 cx 107.7595
427 03 px -12.70
428 03 px -17.78
429 03 cx 112.522
430 03 cx 108.077
431 03 px -13.0175
432 03 px -17.4625
433 03 рy -22.93
434 03 ру 22.93
```

```
c R2:
435 04 cx 112.8395
436 04 cx 107.7595
437 04 px -12.70
438 04 px -17.78
439 04 cx 112.522
440 04 cx 108.077
441 04 px -13.0175
442 04 px -17.4625
443 04 py -22.93
444 04 py 22.93
c R3:
445 05 cx 112.8395
446 05 cx 107.7595
447 05 px -12.70
448 05 px -17.78
449 05 cx 112.522
450 05 cx 108.077
451 05 px -13.0175
452 05 px -17.4625
453 05 py -22.93
454 05 py 22.93
c
c frame supports
c
455 06 box -24.5 0.0 41.0
        49 0 0
        0 3.810 0
        0 0 1.164
c
456 06 box -24.5 0.0 -41.0
            49 0 0
        0 3.810 0
        0 0 -1.164
457 07 box -24.5 0.0 41.0
        49 0 0
        0 -3.810 0
        0 0 1.164
c
458 07 box -24.5 0.0 -41.0
    49 0 0
    0}-3.810 
    0 0 -1.164
c
459 08 box -24.5 0.0 41.0
    49 0 0
    0 3.810 0
    0 0 1.164
```

```
c
460 08 box }\begin{array}{c}{-24.5}\\{49}
c
461 09 box -24.5 0.0 41.0
    49
    0 0 1.164
c
```



```
c
c detector frame legs
c
465 rcc -97.155 -30.4767 105.5782 79.375 0 0 2.2225
466 rcc -97.155 -30.4767 105.5782 79.375 0 0 2.54
467 rcc -97.155 -30.4767 105.5782 0.9525 0 0 5.7150
468 box -18.7325 -35.2392 102.7207 0.9525 00 0 0 9.525 0 0 0
    \hookrightarrow.715
469 box -98.4250 -39.3667 99.2282 1.2700 0 00 0
    \hookrightarrow 12.700
470 box -104.50 -44.4467 99.2282 1.2700 0 0 0 27.94 0 0 0
    \longrightarrow 12.700
c
471 rcc -97.155 30.4767 105.5782 79.375 0 0 2.2225
472 rcc -97.155 30.4767 105.5782 79.375 0 0 2.54
473 rcc -97.155 30.4767 105.5782 0.9525 0 0 5.7150
474 box -18.7325 35.2392 102.7207 0.9525 0 0 0 0 -9.525 0 0 0
    \hookrightarrow 5.715
475 box -98.4250 39.3667 99.2282 1.2700 0 0 0 0 -17.78 0 0 0
    \hookrightarrow 12.700
476 box -104.50 44.4467 99.2282 1.2700 0 00 0
        -> 12.700
c
477 rcc -97.155 -30.4767 -105.5782 79.375 0 0 2.2225
478 rcc -97.155 -30.4767 -105.5782 79.375 0 0 2.54
479 rcc -97.155 -30.4767 -105.5782 0.9525 0 0 5.7150
480 box -18.7325 -35.2392 -102.7207 0.9525 0 0 0 9.525 0 0 0
    \hookrightarrow-5.715
481 box -98.4250 -39.3667 -99.2282 1.2700 0 0 0 17.78 0 0 0
    \hookrightarrow-12.700
482 box -104.50 -44.4467 -99.2282 1.2700 0 00 0}27.94 0 0 0
        \hookrightarrow-12.700
c
```



```
    \hookrightarrow - 12.700
C
c
c detector #01 (liquid scint)
c
1101 21 cz 6.65 $PMT front section od
1102 21 cz 6.35 $PMT front section id
1103 21 cz 3.84 $PMT middle section od
1104 21 cz 3.54 $PMT middle section id
1105 21 cz 2.72 $PMT end section od
1106 21 cz 2.42 $PMT end section id
c s
1107 21 pz 0 $PMT front face
1108 21 pz 13.8
1109 21 pz 14.0 $end front section
1110 21 pz 17.9
1 1 1 1 2 1 \mathrm { pz } \mathrm { 18.1 }  \mathrm {  \$ end } \mathrm { mid } \mathrm { section }
1113 21 pz 22.8 $end glass tail section
1114 21 pz 25.9 $end bakelite tail
1115 21 sz 12.8 12.32 $spherical photocathode surface
1116 21 pz 2.05
c
1117 21 pz 7.5
1118 21 SQ 1 1 -0.1759 4J 0 0 21.9021
1119 21 SQ 1 1 -0.1759 4J 0 0 21.7021
c
1120 21 cz 2.32
1121 21 cz 2.22
1128 21 pz 13.8
c
1130 21 cz 7.10 $front mu-metal
1131 21 cz 7.02
1132 21 cz 3.85 $tail mu-meta
1133 21 cz 3.77
1134 21 SQ 1 1 -0.3368 4J 0 0 26.2338
1135 21 SQ 1 1 -0.3368 4J 0 0 26.0838
1136 21 pz 19.6
c
1137 21 cz 3.850 $base outer wall
1138 21 cz 3.557
1139 21 pz 26.5
1140 21 pz 27.135
1141 21 pz 35.265
1142 21 pz 35.9 $base end plate
C
1143 21 cz 7.925 $quartz window
1 1 4 4 2 1 ~ p z ~ - 3 . 6 3 5 ~ \$ b e g i n ~ q u a r t z ~ w i n d o w ,
1145 21 pz -9.0325 $begin liquid
```

```
1146 21 pz -3.9525 $2-in depth
1 1 4 7 2 1 ~ p z ~ - 9 . 2 3 5 7 ~ \$ b e g i n ~ f r o n t ~ w a l l ~ \$ f r o n t ~ f a c e ~ o f
     detector
c
1150 21 cz 8.890 $Al can id
1151 21 cz 10.16 $Al flange od
1155 21 cz 9.0424 $Al can od
c
1156 21 pz - 4.9525 $front flange begin
1158 21 cz 8.25 $third collar od
1 1 5 9 2 1 ~ p z ~ 1 . 2 7 ~ \$ t h i r d ~ c o l l a r ~ e n d
c
1160 21 pz 26.8525 $inner collar start
1161 21 cz 5.3975 $inner collar diam
c
1163 21 pz 25.265 $front plate start
c
1165 21 pz -3.00 $back of quartz window
1166 21 pz - 2.6825 $back of big flange
1167 21 SQ 1 1 -0.89934 4J 0 0 5.3567 $light guide
    cone
1168 21 pz - 2.0475 $back of third flange
1169 21 cz 9.345 $radius of third flange
c
1170 21 px 18.5928 $top of exp chamber
1 1 7 1 2 1 ~ p x ~ 1 7 . 9 5 7 8 ~ \$ i n n e r ~ t o p
1 1 7 2 2 1 ~ p x ~ 1 2 . 8 6 2 8 ~ \$ i n n e r ~ b o t
1173 21 px 11.5928 $bot of exp chamber
1174 21 px 15.4 $liquid level
1175 21 c/x 0 -3.3175 2.54 $od
1176 21 c/x 0 -3.3175 2.2225 $id
c
1177 21 c/z 8.7988 5.08 1.00 $mounting tabs
1178 21 c/z 8.7988 -5.08 1.00
1179 21 c/z 0 10.16 1.40
1180 21 c/z 0 - < 0.16 1.40
1181 21 c/z -8.7988 5.08 1.40
1182 21 c/z -8.7988 -5.08 1.40
c
1183 21 rcc 10.0 0 -3.3175 1.5928 0 0 0.4763 $transfer tube
1184 21 rcc 8.25 0 -3.3175 4.6128 0 0 0.3175
c
1185 21 pz -2.5325 $end of gasket 1
1186 21 pz 0.1500 $end of gasket 2
1187 21 pz -0.6350
c
1188 21 box -12.700 -6.8326 -2.6825 6.350 0 00 0
    \hookrightarrow 0.6350
```

```
1189 21 box -12.700 -6.8326 -2.0475 0.635 0 0 0 0 13.6652 0
    \hookrightarrow 5.715
c
1195 21 box -12.700 -12.000 -9.2357 23.0 0 0 0 24.00 00 0 0
    445.1457
c
c Surface cards for detectors #02 through 54 (liquid scint)
    \hookrightarrowwere removed for printing. Double space left in their
    place.
c
c
7999 px -104.50 $ top floor
8000 rcc -154.50 0 0 310 0 0 250 $detector space boundary
```



```
c
```



```
    J J 0 $det frame L2
```



```
    J J 0 $det frame L3
*TR04 -0.01 0 % 0 % 33 123 00
\hookrightarrow J J 0 $det frame R2
*TR05 -0.01 0 % 0 % [lllllllll
    \hookrightarrow J J 0 $det frame R3
*TR06 14.29 -102.00 0 0 % 5.5
        J J 0
```



```
        J J 0
*TR08 67.6 -77.5 0
         J J 0
*TR09 67.6 7r.5 0
        J J 0
c
*TR10 -7.1124 0 
    \hookrightarrow90 90 0
*TR11 -8.0104 0 
    490 90 0
*TR12 
        40 90 0
*TR13 -8.0104 0 
        90 90 0
c
*TR21 0
```

```
    J 150 $detectors
*TR22 0
    \hookrightarrow 135
*TR23 0
    \hookrightarrow 120
*TR24 0
    \hookrightarrow 105
*TR25 0 -100.3357 0 0 0 90 90 % J J J 0
    \hookrightarrow 90
*TR26 0
    \hookrightarrow 75
*TR27 0 0-88.6253 51.1679 0
    \hookrightarrow 60
*TR28 0
    \hookrightarrow45
*TR29 0
    \hookrightarrow 30
c
```



```
    \hookrightarrow J J 150
*TR31 39.8349 -61.3404 -73.1401 33 57 90 % J J J 45
    J J 135
*TR32 48.1273 -74.1096 
    \hookrightarrow J J 120
*TR33 53.5738 -82.4964 -26.3570 33 5r 57 90 
    | J 105
*TR34 55.3547 -85.2389 0
    J J 90
*TR35 53.7316 -82.7395 26.4347 33 5r 57 90 
    G J J 75
```



```
    G J J 60
*TR37 40.2971 -62.0521 
    \hookrightarrow J J 45
*TR38 28.9028 -44.5065 91.9162 33 57 90 年 (1)
        J J 30
c
*TR39 48.6626 -21.6660 -92.2626 66 24 90 % J % J 60
    \hookrightarrow J J 150
*TR40 67.5919 -30.0939 
        \hookrightarrow J J 135
```



```
        J J 120
*TR42 92.3324 -41.1090 
         J J 105
*TR43 95.5895 -42.5592 0
     J J 90
*TR44 92.3324 -41.1090 
```



```
*TR67 70.5634 31.4169 -77.2413 66 156 90 J J J % 135
     J J 135
*TR68 86.4222 38.4776 -54.6179 66 156 90 % J J J 150 J
    J J 120
*TR69 96.3915 42.9162 -28.2723 66 156 90 J J J 165 J
    \hookrightarrow J 105
*TR70 99.7918 44.4302 0.0000 66 156 90 % J % J 180 J
    J J 90
*TR71 96.3915 42.9162 28.2723 66 156 90 % J % J 165 J
    G J 75
*TR72 86.4222 38.4776 54.6179 66 156 90 % J J 150 J
    J J 60
*TR73 70.5634 31.4169 7
        J J 45
*TR74 49.8959 22.2151 94.6009 66 156 90 J J J 120 J
        J J 30
c
c —_ material cards —_
c
c Aluminum 6061
c
m1 12024 -0.00935
    12025-0.00123
    12026 -0.00141
    13027 -0.98001
    14028-0.00735
    14029 -0.00039
    14030-0.00026
    NLIB=70c
c
c Ti+Al+Pu dens=7.51E-3 cell volume
c
m2 13027-0.49140
    22046 -0.03269
    22047 -0.03012
    22048-0.30484
    22049 -0.02284
    22050-0.02231
        94239 -0.09580
        NLIB=70c
c
c Pt+Al dens=0.3913 end foils
c
m3 13027.70c -0.0365
    78000 -0.9635
c
c Pt+Al dens=0.1045 inner foils
c
```

```
m4 13027.70c -0.0702
    78000 -0.9298
c
c nylon dens=0.712 (threaded rod)
c
m5 1001 -0.097976
    6000-0.636856
    7014-0.123779
    8016 -0.141389
    NLIB=70c
c
c air dens= 9.293E-4 @ 20C 6980 ft
c air from PNNL-15870Rev1
c
m6 6000 -0.000124
        7014 -0.755268
        8016 -0.231781
        18040-0.012827
        NLIB=70c
c
c anodized Al + Teflon posts dens=2.213
c
m7 12024 -0.00436
        12025-0.00057
        12026 -0.00066
        13027 -0.46474
        14028-0.00343
        14029-0.00018
        14030-0.00012
        1001 -0.00027
        8016 -0.00876
        6000 -0.12406
        9019 -0.39285
        NLIB=70c
c
c 304L stainless steel dens=8.000 from PNNL-15870Rev1
c
m8 6000 -0.000150
        14028-0.005000
        15031 -0.000230
        16032 -0.000150
        24050-0.007931 $-0.190000
        24052 -0.159028
        24053 -0.018381
        24054 -0.004661
        25055 -0.010000
        26054 -0.039210 $-0.694480
        26056 -0.638234
```

```
    26057 -0.015001
    26058 -0.002035
    28058 -0.067198 $-0.100000
    28060 -0.026776
    28061 -0.001183
    28062 -0.003834
    28064 -0.001009
    NLIB=70c
c
c brass + teflon
c
m9 6000 -0.0266
    9019 -0.0843
    29063-0.4089
    29065-0.1880
    30000-0.2922
    NLIB=70c
c
c kapton dens=1.42
c
m10 1001 -0.026362
    6000 -0.691133
    7014 -0.073270
    8016 -0.209235
    NLIB=70c
c
c buta-N dens=1.24
c
m11 1001 -0.0841
    6000 -0.7850
    9019 -0.1309
    NLIB=70c
c
c wires: RG-316
c
m12 6000 -0.1015
            9019 -0.3214
            29063 -0.3992
            29065 -0.1779
            NLIB=70c
c
c G10 no Cu dens=1.895
c
m14 1001 -0.03160
    5010 -0.00200
    5011 -0.00893
    6000 -0.31630
    8016 -0.34723
```

```
    12024-0.01017
    12025-0.00134
    12026 -0.00154
    13027 - 0.03915
    14028-0.12150
    14029-0.00639
    14030-0.00436
    17035-0.03322
    17037 -0.01124
    20040-0.06352
    20044 - 0.00151
    NLIB=70c
c
c PE CH2 dens=0.91
c
m15 1001 -0.1429
    6000-0.8571
    NLIB=70c
c
c low carbon steel
c
m16 6000 - 0.00200
        25055 - 0.00900
        26054 -0.05610
        26056 -0.90864
        26057 -0.02137
        26058-0.00289
        NLIB=70c
c
c RG-223 dens=2.40
c
m17 1001 0.0254
        6000 0.1719
        17035 0.0911
        17037 0.0308
        29063 0.4664
        29065 0.2144
        NLIB=70c
c
c concrete LANL MCNP mix dens=2.25
c
m18 01001 -0.00453
        08016 - 0.5126
        14028-0.36036
        13027 - 0.03555
        11023-0.01527
        20040-0.05791
        26056-0.01378
```

$\mathrm{NLIB}=70 \mathrm{c}$
c
c EJ-309 liquid dens $=-0.964 \mathrm{~g} / \mathrm{cm}^{\wedge} 3$
m19 nlib=60c \$ EJ309 Liquid
1001 . 5556
6000 . 4444
c
c 6 Li-silicate glass $96 \%$ detailed spec dens $=2.5$
c
m20 $3006-0.073954$
$3007-0.003594$
$8016-0.507151$
$12024-0.018803$
$12025-0.002480$
12026 -0.002839
$13027-0.095265$
$14028-0.240492$
$14029-0.012647$
$14030-0.008624$
$58140-0.030290$
$58142-0.003861$
$\mathrm{NLIB}=70 \mathrm{c}$
c
c 7 Li -silicate glass $96 \%$ detailed spec dens $=2.5$
c
m21 $3006-0.000007$
$3007-0.077541$
$8016-0.507151$
$12024-0.018803$
$12025-0.002480$
12026 -0.002839
$13027-0.095265$
$14028-0.240492$
$14029-0.012647$
$14030-0.008624$
$58140-0.030290$
58142-0.003861
NLIB $=70 \mathrm{c}$
c
c lucite dens $=1.19$
c
m22 $1001-0.080538$
$6000-0.599848$
$8016-0.319614$
NLIB $=70 \mathrm{c}$
c
c borosilicate glass dens $=2.23$
c

```
m23 5010 -0.00738
        5011 -0.03268
        13027-0.01164
        11023-0.02819
        08016-0.53957
        14028-0.37722
        19039 -0.00310
        19041-0.00022
        NLIB=70c
c
c PVC dens=1.303
c
m24 6000 -0.3844
        1001 -0.0484
        17035-0.4298
        17037-0.1374
        NLIB=70c
c
c mu metal dens=8.74
c
m25 28058 -0.52478
    28060-0.20184
    28062 -0.02772
        28061 -0.00851
        28064 -0.00690
        26056 -0.14680
        26054 -0.00931
        26057 -0.00350
        26058-0.00050
        29063 -0.03462
        29065 -0.01541
        24052 -0.01681
        24053 -0.00190
        24050 -0.00090
        24054-0.00050
        NLIB=70c
c
c Copper
c
m26 29063-0.6850
        29065-0.3150
        NLIB=70c
c
c Cu-C foam (simulate base electronics)
c
m27 6000 -0.5000
        29063-0.3425
        29065-0.1575
```

NLIB $=70 \mathrm{c}$
C
c Neoprene dens $=1.23$
c
m28 $1001-0.056920$
$6000-0.542646$
$17035-0.303432$
17037 -0.097002
$\mathrm{NLIB}=70 \mathrm{c}$
c
c brass dens $=8.7$
c
m29 $29063-0.4599$
$29065-0.2114$
$30000-0.3287$
NLIB $=70 \mathrm{c}$
c
c Physics
c
MODE n p
PHYS:N J 20
PHYS: $\mathrm{P} \quad 0 \quad 11$
CUT:P 30 J 0
CUT:N 30
IMP:N 1 3246R 0
IMP:P 1 3246R 0
c
c Source
c
sdef sur=11
ссс $=99$
dir=d1
vec=1 00
si1 $-1 \quad 1$
sp1 01
IPOL $1412 \begin{array}{llllllllllll} & 1 & 18 & 45 & 1148 & 1248 & 1348 & 1448 & 1548 & 1648 & 1748 & 1848\end{array}$ $\hookrightarrow 1948$

| 2048 | 2148 | 2248 | 2348 | 2448 | 2548 | 2648 | 2748 | 2848 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2948 | 3048 | 3148 | 3248 | 3348 | 3448 | 3548 | 3648 | 3748 |
| 3848 | 3948 | 4048 | 4148 | 4248 | 4348 | 4448 | 4548 | 4648 |
| 4748 | 4848 | 4948 | 5048 | 5148 | 5248 | 5348 | 5448 | 5548 |
| 5648 | 5748 | 5848 | 5948 | 6048 | 6148 | 6248 | 6348 |  |

c $5648 \quad 5748 \quad 5848 \quad 5948 \quad 6048 \quad 6148 \quad 6248 \quad 6348$
$\hookrightarrow 6448$
RPOL 0.0010 .001
NPS 1e7
FILES 21 DUMN1
DBCN 19034044545681
PRDMP 2J 1

## Appendix 4. Measured and Simulated ${ }^{240} \mathrm{Pu}(\mathrm{sf})$ Prompt Neutron-Photon

## Competition Experiment at LANL

The full MCNPX - PoliMi model is included.

## MJM FNMC

| c *** CELLS *** |  |  |
| :---: | :---: | :---: |
| $\hookrightarrow$ |  |  |
| c |  |  |
| $\hookrightarrow$ |  |  |
| $810 \quad 2 \quad-1.205 \mathrm{E}-3-1101$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ innermost cavity |  |  |
| $81180-8.00 \quad 1-2$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ innermost can |  |  |
| $8122-1.205 \mathrm{E}-3 \quad 2-3$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ second can interior |  |  |
| $813 \quad 8 \quad-8.00 \quad 3-4$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ second can |  |  |
| $814 \quad 2 \quad-1.205 \mathrm{e}-3 \quad 4-5$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ third can interior |  |  |
| $815 \quad 8 \quad-8.00 \quad 5-6$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ third can |  |  |
| $816 \quad 2 \quad-1.205 \mathrm{e}-3 \quad 6-7$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ fourth can interior |  |  |
| $817 \quad 8 \quad-8.00 \quad 7-8$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ fourth can |  |  |
| $818 \quad 5 \quad-2.6989 \quad-9$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ |
| $\hookrightarrow$ stage plate |  |  |
| $819 \quad 21-16.5-101-1$ | IMP : $\mathrm{N}, \mathrm{P}=1$ | \$ PuO2 ( |
| $\hookrightarrow$ sort of) |  |  |
| c |  |  |
| c STILBENE Detectors |  |  |
| c |  |  |
| c Det \#01 |  |  |



60 LIKE 20 BUT TRCL=3
c Det \#04
70 LIKE 10 BUT TRCL=4
71 LIKE 11 BUT TRCL=4
72 LIKE 12 BUT TRCL=4
73 LIKE 13 BUT TRCL=4
74 LIKE 14 BUT TRCL=4
75 LIKE 15 BUT TRCL=4
76 LIKE 16 BUT TRCL=4
77 LIKE 17 BUT TRCL=4
78 LIKE 18 BUT TRCL=4
79 LIKE 19 BUT TRCL=4
80 LIKE 20 BUT TRCL=4
c Det \#05
90 LIKE 10 BUT TRCL=5
91 LIKE 11 BUT TRCL=5
92 LIKE 12 BUT TRCL=5
93 LIKE 13 BUT TRCL=5
94 LIKE 14 BUT TRCL=5
95 LIKE 15 BUT TRCL=5
96 LIKE 16 BUT TRCL=5
97 LIKE 17 BUT TRCL=5
98 LIKE 18 BUT TRCL=5
99 LIKE 19 BUT TRCL=5
100 LIKE 20 BUT TRCL=5
c Det \#06
110 LIKE 10 BUT TRCL=6
111 LIKE 11 BUT TRCL=6
112 LIKE 12 BUT TRCL=6
113 LIKE 13 BUT TRCL=6
114 LIKE 14 BUT TRCL=6
115 LIKE 15 BUT TRCL=6
116 LIKE 16 BUT TRCL=6
117 LIKE 17 BUT TRCL=6
118 LIKE 18 BUT TRCL=6
119 LIKE 19 BUT TRCL=6
120 LIKE 20 BUT TRCL=6
c Det \#07
130 LIKE 10 BUT TRCL=7
131 LIKE 11 BUT TRCL=7
132 LIKE 12 BUT TRCL=7
133 LIKE 13 BUT TRCL=7
134 LIKE 14 BUT TRCL=7
135 LIKE 15 BUT TRCL=7
136 LIKE 16 BUT TRCL=7
137 LIKE 17 BUT TRCL=7
138 LIKE 18 BUT TRCL=7
139 LIKE 19 BUT TRCL=7

```
140 LIKE 20 BUT TRCL=7
c Det #08
150 LIKE 10 BUT TRCL=8
151 LIKE 11 BUT TRCL=8
152 LIKE 12 BUT TRCL=8
153 LIKE 13 BUT TRCL=8
154 LIKE 14 BUT TRCL=8
155 LIKE 15 BUT TRCL=8
156 LIKE 16 BUT TRCL=8
157 LIKE 17 BUT TRCL=8
158 LIKE 18 BUT TRCL=8
159 LIKE 19 BUT TRCL=8
160 LIKE 20 BUT TRCL=8
c Det #09
170 LIKE 10 BUT TRCL=9
171 LIKE 11 BUT TRCL=9
172 LIKE 12 BUT TRCL=9
173 LIKE 13 BUT TRCL=9
174 LIKE 14 BUT TRCL=9
175 LIKE 15 BUT TRCL=9
176 LIKE 16 BUT TRCL=9
177 LIKE 17 BUT TRCL=9
178 LIKE 18 BUT TRCL=9
179 LIKE 19 BUT TRCL=9
180 LIKE 20 BUT TRCL=9
c Det #10
190 LIKE 10 BUT TRCL=10
191 LIKE }11\mathrm{ BUT TRCL=10
192 LIKE 12 BUT TRCL=10
193 LIKE 13 BUT TRCL=10
194 LIKE 14 BUT TRCL=10
195 LIKE 15 BUT TRCL=10
196 LIKE 16 BUT TRCL=10
197 LIKE 17 BUT TRCL=10
198 LIKE 18 BUT TRCL=10
199 LIKE 19 BUT TRCL=10
200 LIKE 20 BUT TRCL=10
c Det #11
210 LIKE 10 BUT TRCL=11
211 LIKE 11 BUT TRCL=11
212 LIKE 12 BUT TRCL=11
213 LIKE 13 BUT TRCL=11
214 LIKE 14 BUT TRCL=11
215 LIKE 15 BUT TRCL=11
216 LIKE 16 BUT TRCL=11
217 LIKE 17 BUT TRCL=11
218 LIKE 18 BUT TRCL=11
219 LIKE 19 BUT TRCL=11
```

220 LIKE 20 BUT TRCL=11
c Det \#12
230 LIKE 10 BUT TRCL=12
231 LIKE 11 BUT TRCL=12
232 LIKE 12 BUT TRCL=12
233 LIKE 13 BUT TRCL=12
234 LIKE 14 BUT TRCL=12
235 LIKE 15 BUT TRCL=12
236 LIKE 16 BUT TRCL=12
237 LIKE 17 BUT TRCL=12
238 LIKE 18 BUT TRCL=12
239 LIKE 19 BUT TRCL=12
240 LIKE 20 BUT TRCL=12
c Det \#13
250 LIKE 10 BUT TRCL=13
251 LIKE 11 BUT TRCL=13
252 LIKE 12 BUT TRCL=13
253 LIKE 13 BUT TRCL=13
254 LIKE 14 BUT TRCL=13
255 LIKE 15 BUT TRCL=13
256 LIKE 16 BUT TRCL=13
257 LIKE 17 BUT TRCL=13
258 LIKE 18 BUT TRCL=13
259 LIKE 19 BUT TRCL=13
260 LIKE 20 BUT TRCL=13
c Det \#14
270 LIKE 10 BUT TRCL=14
271 LIKE 11 BUT TRCL=14
272 LIKE 12 BUT TRCL=14
273 LIKE 13 BUT TRCL=14
274 LIKE 14 BUT TRCL=14
275 LIKE 15 BUT TRCL=14
276 LIKE 16 BUT TRCL=14
277 LIKE 17 BUT TRCL=14
278 LIKE 18 BUT TRCL=14
279 LIKE 19 BUT TRCL=14
280 LIKE 20 BUT TRCL=14
c Det \#15
290 LIKE 10 BUT TRCL=15
291 LIKE 11 BUT TRCL=15
292 LIKE 12 BUT TRCL=15
293 LIKE 13 BUT TRCL=15
294 LIKE 14 BUT TRCL=15
295 LIKE 15 BUT TRCL=15
296 LIKE 16 BUT TRCL=15
297 LIKE 17 BUT TRCL=15
298 LIKE 18 BUT TRCL=15
299 LIKE 19 BUT TRCL=15

300
LIKE 20 BUT TRCL=15
c Det \#16
310 LIKE 10 BUT TRCL=16
311 LIKE 11 BUT TRCL=16
312 LIKE 12 BUT TRCL=16
313 LIKE 13 BUT TRCL=16
314 LIKE 14 BUT TRCL=16
315 LIKE 15 BUT TRCL=16
316 LIKE 16 BUT TRCL=16
317 LIKE 17 BUT TRCL=16
318 LIKE 18 BUT TRCL=16
319 LIKE 19 BUT TRCL=16
320 LIKE 20 BUT TRCL=16
c Det \#17
330 LIKE 10 BUT TRCL=17
331 LIKE 11 BUT TRCL=17
332 LIKE 12 BUT TRCL=17
333 LIKE 13 BUT TRCL=17
334 LIKE 14 BUT TRCL=17
335 LIKE 15 BUT TRCL=17
336 LIKE 16 BUT TRCL=17
337 LIKE 17 BUT TRCL=17
338 LIKE 18 BUT TRCL=17
339 LIKE 19 BUT TRCL=17
340 LIKE 20 BUT TRCL=17
c Det \#18
350 LIKE 10 BUT TRCL=18
351 LIKE 11 BUT TRCL=18
352 LIKE 12 BUT TRCL=18
353 LIKE 13 BUT TRCL=18
354 LIKE 14 BUT TRCL=18
355 LIKE 15 BUT TRCL=18
356 LIKE 16 BUT TRCL=18
357 LIKE 17 BUT TRCL=18
358 LIKE 18 BUT TRCL=18
359 LIKE 19 BUT TRCL=18
360 LIKE 20 BUT TRCL=18
c Det \#19
370 LIKE 10 BUT TRCL=19
371 LIKE 11 BUT TRCL=19
372 LIKE 12 BUT TRCL=19
373 LIKE 13 BUT TRCL=19
374 LIKE 14 BUT TRCL=19
375 LIKE 15 BUT TRCL=19
376 LIKE 16 BUT TRCL=19
377 LIKE 17 BUT TRCL=19
378 LIKE 18 BUT TRCL=19
379 LIKE 19 BUT TRCL=19

380 LIKE 20 BUT TRCL=19
c Det \#20
390 LIKE 10 BUT TRCL=20
391 LIKE 11 BUT TRCL=20
392 LIKE 12 BUT TRCL=20
393 LIKE 13 BUT TRCL=20
394 LIKE 14 BUT TRCL=20
395 LIKE 15 BUT TRCL=20
396 LIKE 16 BUT TRCL=20
397 LIKE 17 BUT TRCL=20
398 LIKE 18 BUT TRCL=20
399 LIKE 19 BUT TRCL=20
400 LIKE 20 BUT TRCL=20
c Det \#21
410 LIKE 10 BUT TRCL=21
411 LIKE 11 BUT TRCL=21
412 LIKE 12 BUT TRCL=21
413 LIKE 13 BUT TRCL=21
414 LIKE 14 BUT TRCL=21
415 LIKE 15 BUT TRCL=21
416 LIKE 16 BUT TRCL=21
417 LIKE 17 BUT TRCL=21
418 LIKE 18 BUT TRCL=21
419 LIKE 19 BUT TRCL=21
420 LIKE 20 BUT TRCL=21
c Det \#22
430 LIKE 10 BUT TRCL=22
431 LIKE 11 BUT TRCL=22
432 LIKE 12 BUT TRCL=22
433 LIKE 13 BUT TRCL=22
434 LIKE 14 BUT TRCL=22
435 LIKE 15 BUT TRCL=22
436 LIKE 16 BUT TRCL=22
437 LIKE 17 BUT TRCL=22
438 LIKE 18 BUT TRCL=22
439 LIKE 19 BUT TRCL=22
440 LIKE 20 BUT TRCL=22
c Det \#23
450 LIKE 10 BUT TRCL=23
451 LIKE 11 BUT TRCL=23
452 LIKE 12 BUT TRCL=23
453 LIKE 13 BUT TRCL=23
454 LIKE 14 BUT TRCL=23
455 LIKE 15 BUT TRCL=23
456 LIKE 16 BUT TRCL=23
457 LIKE 17 BUT TRCL=23
458 LIKE 18 BUT TRCL=23
459 LIKE 19 BUT TRCL=23

```
460 LIKE 20 BUT TRCL=23
c Det #24
470 LIKE 10 BUT TRCL=24
4 7 1 ~ L I K E ~ 1 1 ~ B U T ~ T R C L = 2 4
472 LIKE 12 BUT TRCL=24
4 7 3 ~ L I K E ~ 1 3 ~ B U T ~ T R C L = 2 4 ~
474 LIKE 14 BUT TRCL=24
475 LIKE 15 BUT TRCL=24
476 LIKE 16 BUT TRCL=24
477 LIKE 17 BUT TRCL=24
4 7 8 ~ L I K E ~ 1 8 ~ B U T ~ T R C L = 2 4 ~
479 LIKE 19 BUT TRCL=24
480 LIKE 20 BUT TRCL=24
c
c Aluminum plates
c
500 5 -2.6989 -130 131 132 133 TRCL=30 IMP:N,P=1
501 LIKE 500 BUT TRCL=31
c 502 LIKE 500 BUT TRCL=32
502 5 -2.6989 -134 135 136 137 IMP:N,P=1
c 503 LIKE 500 BUT TRCL=33
503 5 -2.6989 -138 135 136 137 IMP:N,P=1
5 0 4 ~ L I K E ~ 5 0 0 ~ B U T ~ T R C L = 3 4 ~
505 LIKE 500 BUT TRCL=35
c 506 LIKE 500 BUT TRCL=36
506 5 -2.6989 -143 144 145 146 IMP:N,P=1
c 507 LIKE 500 BUT TRCL=37
507 5 -2.6989 -147 144 145 146 IMP:N,P=1
508 LIKE 500 BUT TRCL=38
5 0 9 ~ L I K E ~ 5 0 0 ~ B U T ~ T R C L = 3 9 ~
c 510 LIKE 500 BUT TRCL=40
510 5 -2.6989 -148 149 150 151 IMP:N,P=1
c 511 LIKE 500 BUT TRCL=41
511 5 -2.6989 -152 149 150 151 IMP:N,P=1
5 1 2 ~ L I K E ~ 5 0 0 ~ B U T ~ T R C L = 4 2 ~
513 LIKE 500 BUT TRCL=43
c 514 LIKE 500 BUT TRCL=44
514 5 -2.6989 -153 154 155 156 IMP:N,P=1
c 515 LIKE 500 BUT TRCL=45
515 5 -2.6989 -157 154 155 156 IMP:N,P=1
c 1" box tube frame
520 5 -2.6989 (-50 54 -40 41 42 43):(51 -55 -40 41 42 43):
    (-40 44 -50 51 42 43):(\begin{array}{lllllll}{41}&{-45}&{-50}&{51}&{42}&{43}\end{array})
    TRCL=46 IMP:N,P=1
5 2 1 ~ L I K E ~ 5 2 0 ~ B U T ~ T R C L = 4 7 ~
522 LIKE 520 BUT TRCL=48
523 LIKE 520 BUT TRCL=49
524 LIKE 520 BUT TRCL=50
```

```
525 LIKE 520 BUT TRCL=51
526 LIKE 520 BUT TRCL=52
5 2 7 ~ L I K E ~ 5 2 0 ~ B U T ~ T R C L = 5 3 ~
530 5 -2.6989 (52 -56 -40 41 42 43):(-53 57 -40 41 42 43):
    (-40 44 52 -53 42 43):((41 -45 52 -53 42 43)
        TRCL=46 IMP:N,P=1
531 LIKE 530 BUT TRCL=47
5 3 2 ~ L I K E ~ 5 3 0 ~ B U T ~ T R C L = 4 8 ~
5 3 3 \text { LIKE 530 BUT TRCL=49}
5 3 4 ~ L I K E ~ 5 3 0 ~ B U T ~ T R C L = 5 0 ~
535 LIKE 530 BUT TRCL=51
536 LIKE 530 BUT TRCL=52
537 LIKE 530 BUT TRCL=53
c
c Table
c
700 5 -2.6989 -60 61 IMP:N,P=1
701 20-8.65 -60 -61 62 IMP:N,P=1
702 8 -8.00 -60 -62 IMP:N,P=1
c
c Floor
c
800 6 -2.3 -600 -70 IMP:N,P=1 $Floor
c Environment
c
600 2 -1.205E-3 -600 601 -602
    #10 #11 #12 #13 #14 #15 #16 #17 #18 #19 #20
    #30 #31 #32 #33 #34 #35 #36 #37 #38 #39 #40
    #50 #51 #52 #53 #54 #55 #56 #57 #58 #59 #60
    #70 #71 #72 #73 #74 #75 #76 #77 #78 #79 #80
    #90 #91 #92 #93 #94 #95 #96 #97 #98 #99 #100
    #110 #111 #112 #113 #114 #115 #116 #117 #118 #119
                    \hookrightarrow #120
    #130 #131 #132 #133 #134 #135 #136 #137 #138 #139
                    \hookrightarrow #140
    #150 #151 #152 #153 #154 #155 #156 #157 #158 #159
            \hookrightarrow #160
    #500 #501 #502 #503 #504 #505 #506 #507 #508 #509
    #510 #511 #512 #513 #514 #515
    8 9
    IMP:N,P=1
601 2 -1.205E-3 -600 -601
    #410 #411 #412 #413 #414 #415 #416 #417 #418 #419
        \hookrightarrow #420
        #430 #431 #432 #433 #434 #435 #436 #437 #438 #439
        \hookrightarrow #440
    #450 #451 #452 #453 #454 #455 #456 #457 #458 #459
        \hookrightarrow #460
```

```
            #470 #471 #472 #473 #474 #475 #476 #477 #478 #479
                    \hookrightarrow #480
                            #500 #501 #502 #503 #504 #505 #506 #507 #508 #509
            #510 #511 #512 #513 #514 #515
            #530 #531 #532 #533 #534 #535 #536 #537
            60
            7 0
            IMP : N, P=1
602 2 -1.205E-3 -600 602 -603
    #170 #171 #172 #173 #174 #175 #176 #177 #178 #179
                \hookrightarrow #180
                    #190 #191 #192 #193 #194 #195 #196 #197 #198 #199
                    \hookrightarrow #200
                    #210 #211 #212 #213 #214 #215 #216 #217 #218 #219
                \hookrightarrow #220
                    #230 #231 #232 #233 #234 #235 #236 #237 #238 #239
                \hookrightarrow #240
                    #250 #251 #252 #253 #254 #255 #256 #257 #258 #259
                \hookrightarrow #260
            #270 #271 #272 #273 #274 #275 #276 #277 #278 #279
                \hookrightarrow #280
                    #290 #291 #292 #293 #294 #295 #296 #297 #298 #299
                \hookrightarrow #300
            #310 #311 #312 #313 #314 #315 #316 #317 #318 #319
                \hookrightarrow #320
                            #500 #501 #502 #503 #504 #505 #506 #507 #508 #509
                            #510 #511 #512 #513 #514 #515
                    IMP : N, P=1
603 2 -1.205E-3 -600 603
            #330 #331 #332 #333 #334 #335 #336 #337 #338 #339
                \hookrightarrow#340
                    #350 #351 #352 #353 #354 #355 #356 #357 #358 #359
                \hookrightarrow #360
                    #370 #371 #372 #373 #374 #375 #376 #377 #378 #379
                \hookrightarrow #380
                    #390 #391 #392 #393 #394 #395 #396 #397 #398 #399
                \hookrightarrow#400
                    #500 #501 #502 #503 #504 #505 #506 #507 #508 #509
                    #510 #511 #512 #513 #514 #515
                    #520 #521 #522 #523 #524 #525 #526 #527
                    IMP : N, P=1
C
c Graveyard
c ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
999 0 600 IMP:N,P=0
```

c



41 PX 22.225
$42 \quad \mathrm{P} \quad 10.258-24.765 \quad 0 \quad 0$
$43 \quad \mathrm{P} \quad 10.258 \quad 24.765 \quad 0 \quad 0$
44 PX 24.4475
45 PX 22.5425
50 PZ 15.24
51 PZ 12.70
$52 \quad \mathrm{PZ}-15.24$
$53 \quad$ PZ -12.70
54 PZ 14.9225
$55 \quad$ PZ 13.0175
$56 \quad \mathrm{PZ}-14.9225$
$57 \quad$ PZ -13.0175
c
c Table
c
$60 \quad$ BOX $\quad-96.265-44.765 \quad-15.24 \quad 153.5 \quad 0 \quad 0 \quad 0 \quad 76.50000$ $\hookrightarrow-0.84455$
$\begin{array}{lll}61 & \mathrm{PZ} & -15.875 \\ 62 & \mathrm{PZ} & -15.9258\end{array}$
c
c Floor
c
$70 \quad$ PZ $\quad 105.04$
$\hookrightarrow$ \$Floor Level
c
c Environment
c
600 RPP -200 200 -200 200 -200 200
$\hookrightarrow$ \$Environment
601 PZ -3.5755
602 PZ 3.5755
603 PZ 10.7265
c *** END SURFACES $* * *$ $\hookrightarrow$
c *** DATA
c
$\hookrightarrow$
$\hookrightarrow$
c
c
c
TR1 $\quad 7.75 \quad 0 \quad 0$
100
010
$0 \quad 01$
TR2 $5.48008-5.48008 \quad 0$

```
0.707106781186548 -0.707106781186547
    \hookrightarrow}
    0.707106781186547
    \hookrightarrow 0
                                    0
                                    0 1.000000000000000
TR3 0 -7.75 0
    0.0000-1.0000 0
    1.0000 0.0000 0.0000
    0.0000 0.0000 1.0000
TR4 -5.48008 -5.48008 0
    -0.707106781186547 -0.707106781186548
        \hookrightarrow 0
        0.707106781186548 -0.707106781186547
            \hookrightarrow
                0
                            0 1.000000000000000
TR5 -7.75 0 0
    -1.000000000000000 -0.0000000000000000
    \hookrightarrow 0
        0.000000000000000-1.000000000000000
        \hookrightarrow
                    0
                            0 1.000000000000000
TR6 -5.48008 5.48008 0
    -0.707106781186548
            \hookrightarrow
            -0.707106781186547
            \hookrightarrow
                    0
                    0 1.0000000000000000
TR7 0 7.75 0
    -0.000000000000000
        \hookrightarrow
    -1.000000000000000
                            0
            5.48008 5.48008 0
            0.707106781186547
        \hookrightarrow 0
        -0.707106781186548
        \hookrightarrow}
            0 0 1.000000000000000
TR9 7.75 0 7.151
            1 0 0
            0 1 0
            0 0 1
            1
TR10 5.48008 -5.48008 7.151
            0.707106781186548 -0.707106781186547
            \hookrightarrow}
            0.707106781186547
                    0.707106781186548
```

```
        \hookrightarrow}
    1
TR11 0 -7.75 7.151
    0.0000-1.0000 0
    1.0000 0.0000 0.0000
    0.0000 0.0000 1.0000
    1
TR12 -5.48008 -5.48008 7.151
    -0.707106781186547 -0.707106781186548
            \hookrightarrow 0
        0.707106781186548 -0.707106781186547
            \hookrightarrow
                0
    1
TR13 -7.75 0 7.151
    -1.0000 -0.0000 0
    -0.0000 1.0000 -0.0000
    0.0000 -0.0000 -1.0000
    1
TR14 -5.48008 5.48008 7.151
    -0.707106781186548 0.707106781186547
        \hookrightarrow 0
    -0.707106781186547 -0.707106781186548
            \hookrightarrow 0
                0 0 1.000000000000000
    1
TR15 0 7.75 7.151
    -0.000000000000000 1.000000000000000
        \hookrightarrow 0
    -1.000000000000000 -0.000000000000000
                            0
                                0 1.000000000000000
                0
    1
TR16 5.48008 5.48008 7.151
    0.707106781186547 0.707106781186548
        \hookrightarrow}
        -0.707106781186548 0.707106781186547
        \hookrightarrow 0
        0 1.000000000000000
    TR17 4.60 3.89 11.467
        0 0 1
        1 0 0
        0 1 0
TR18 4.60 -3.89 11.467
            0 0 1
            1 0 0
            0 1 0
```

$\begin{array}{llll}\text { TR19 } & -4.60 & -3.89 & 11.467\end{array}$

$$
\begin{array}{lll}
0 & 0 & 1
\end{array}
$$

$$
100
$$

$$
010
$$

$\begin{array}{llll}\text { TR20 } & -4.60 & 3.89 & 11.467\end{array}$
$0 \quad 01$
100
010
TR21 $000-7.151$
TR22 $\quad 0 \quad-3.175-7.151$
$0.0000-1.0000 \quad 0$
$1.0000 \quad 0.0000 \quad 0.0000$
$0.0000 \quad 0.0000 \quad 1.0000$
TR23 $0 \quad 0 \quad-7.151$
$-1.0000-0.0000 \quad 0$
$-0.0000 \quad 1.0000-0.0000$
$0.0000-0.0000-1.0000$
TR24 $03.175-7.151$
$-0.000000000000000 \quad 1.000000000000000$
$\hookrightarrow \quad 0$
$-1.000000000000000-0.000000000000000$
$\hookrightarrow \quad 0$
$0 \quad 0 \quad 1.000000000000000$
TR30 18.16500
TR31 15.62500
TR32 $15.4517-15.4517 \quad 0$
$0.707106781186548 \quad-0.707106781186547$
$\hookrightarrow 0$
$0.707106781186547 \quad 0.707106781186548$
$\hookrightarrow 0$
$0 \quad 0 \quad 1.000000000000000$
TR33 $11.9996-11.9996 \quad 0$

$$
0.707106781186548 \quad-0.707106781186547
$$

$\hookrightarrow 0$
$0.707106781186547 \quad 0.707106781186548$
$\hookrightarrow 0$

|  | 0 |  |  |
| ---: | :---: | ---: | ---: |
| TR34 | $0-21.85$ | 0 |  |
|  | 0.0000 | -1.0000 | 0 |
| 1.0000 | 0.0000 | 0.0000 |  |
|  | 0.0000 | 0.0000 | 1.0000 |

TR35 $0-16.97 \quad 0$
$0.0000-1.0000 \quad 0$
$1.0000 \quad 0.0000 \quad 0.0000$
$0.0000 \quad 0.0000 \quad 1.0000$
TR36 -15.4517 -15.4517 0

$$
\begin{array}{cc}
-0.707106781186547 & -0.707106781186548 \\
\hookrightarrow & 0
\end{array}
$$

|  | 0.707106781186548 $\hookrightarrow$ | $\begin{aligned} & -0.707106781186547 \\ & 0 \end{aligned}$ |
| :---: | :---: | :---: |
|  | 0 | $0 \quad 1.000000000000000$ |
| TR37 | -11.9996 -11.9996 0 |  |
|  | $-0.707106781186547$ | -0.707106781186548 |
|  | $\hookrightarrow$ | 0 |
|  | 0.707106781186548 | -0.707106781186547 |
|  | $\hookrightarrow$ | 0 |
|  | 0 | $0 \quad 1.000000000000000$ |
| TR38 | $-18.16500$ |  |
| TR39 | $-15.62500$ |  |
| TR40 | -15.4517 15.4517 0 |  |
|  | $-0.707106781186548$ | 0.707106781186547 |
|  | $\hookrightarrow$ | 0 |
|  | -0.707106781186547 | -0.707106781186548 |
|  | $\hookrightarrow$ | 0 |
|  | 0 | $0 \quad 1.000000000000000$ |
| TR41 | -11.9996 11.9996 0 |  |
|  | $-0.707106781186548$ | 0.707106781186547 |
|  | $\hookrightarrow$ | 0 |
|  | -0.707106781186547 | -0.707106781186548 |
|  | $\hookrightarrow$ | 0 |
|  | 0 | 01.000000000000000 |
| TR42 | 021.850 |  |
|  | -0.000000000000000 | 1.000000000000000 |
|  | $\hookrightarrow$ | 0 |
|  | $-1.000000000000000$ | -0.000000000000000 |
|  | $\hookrightarrow$ | 0 |
|  | 0 | 01.000000000000000 |
| TR43 | 016.970 |  |
|  | -0.000000000000000 | 1.000000000000000 |
|  | $\hookrightarrow$ | 0 |
|  | $-1.000000000000000$ | -0.000000000000000 |
|  | $\hookrightarrow$ | 0 |
|  | 0 | 01.000000000000000 |
| TR44 | $15.4517 \quad 15.4517 \quad 0$ |  |
|  | 0.707106781186547 | 0.707106781186548 |
|  | $\rightarrow 0$ |  |
|  | $-0.707106781186548$ | 0.707106781186547 |
|  | $\hookrightarrow 0$ |  |
|  | 0 | $0 \quad 1.000000000000000$ |
| TR45 | 11.999611 .99960 |  |
|  | 0.707106781186547 | 0.707106781186548 |
|  | $\rightarrow 0$ |  |
|  | -0.707106781186548 | 0.707106781186547 |
|  | $\hookrightarrow 0$ |  |
|  | 0 | $0 \quad 1.000000000000000$ |
| TR46 | 0.0100 |  |

```
TR47 0.01 -0.01 0
    0.707106781186548 -0.707106781186547
            \hookrightarrow0
            0.707106781186547 0.707106781186548
            \hookrightarrow0
                    0 0 1.000000000000000
TR48 0 0.01 0
            0.0000-1.0000 0
            1.0000 0.0000 0.0000
            0.0000 0.0000 1.0000
TR49 -0.01 -0.01 0
            -0.707106781186547 - 0.707106781186548
            \hookrightarrow 0
                0.707106781186548 -0.707106781186547
                    \hookrightarrow
                    0
                    0 1.000000000000000
TR50
            -0.01 0 0
            -1.000000000000000
            \hookrightarrow
                0.000000000000000
            \hookrightarrow
                    0
                    0 1.000000000000000
TR51 -0.01 0.01 0
            -0.707106781186548
            \hookrightarrow
                        0.707106781186547
                            0
            -0.707106781186547
            \hookrightarrow
                    0
                            0 1.000000000000000
TR52 0 0.01 0
            -0.000000000000000
                                    1.000000000000000
            0
            -1.000000000000000
            \hookrightarrow
                    0
                            0 1.000000000000000
TR53
            0.01 0.01 0
            0.707106781186547
                \hookrightarrow
            -0.707106781186548
                                    0.707106781186547
            \hookrightarrow0
                                    0 1.000000000000000
c
c Physics
C
    MODE n P
    PHYS:N J 20
    PHYS:P 0 1 1
    CUT:P 2J 0
c
```

    SI2 01.02
    SI3 0.06359
    c SDEF POS=0 00.06359
IPOL $31 \begin{array}{llllllllllllll} & 2 & 0 & J & 1 & 24 & 10 & 30 & 50 & 70 & 90 & 110 & 130 & 150\end{array}$

RPOL 0.00020 .0002
NPS 1e6
FILES 21 DUMN1
DBCN
PRDMP 2J 1

```
c
```

c Materials
c EJ-309 liquid scintillator $\mathrm{d}=-0.916$
c (Eljen Technologies, EJ-309 Fact Sheet)
c
m1 nlib=70c plib=04p
$1001 \quad 0.548$
$6000 \quad 0.452$
c
c Air, Dry (near sea level) d $=-1.205 \mathrm{E}-3$
c (Mat. Compendium PNNL)
c
$\mathrm{m} 2 \quad \mathrm{NLIB}=70 \mathrm{c} \quad$ PLIB $=04 \mathrm{p}$
$7014-0.755636 \quad \$ \mathrm{~N}$
$8016-0.231475 \quad \$ \mathrm{O}$
$18040.60 \mathrm{c}-0.012838 \$ \mathrm{Ar}-40$ at 99.6035 percent of natural
$\hookrightarrow \mathrm{Ar}$
$18036.60 \mathrm{c}-0.000043$ \$ $\mathrm{Ar}-36$ at 0.3336 percent of natural
$\hookrightarrow \mathrm{Ar}$
$18038.60 \mathrm{c}-0.000008 \$ \mathrm{Ar}-38$ at 0.00629 percent of natural
$\hookrightarrow \mathrm{Ar}$
c
c Lead Shielding d=-11.34
c
c
m3 82000.60c 1
c tungsten rho $=19.25$
m31 74000.60c 1
c
c Polyethylene $\mathrm{d}=-0.9300$
c (Mat. Compendium PNNL)
c

```
    m4 nlib=70c plib=04p
        1001 -0.143716
        6000-0.856284
C
c Aluminum table d=-2.70
c
    m5 nlib=60c plib=04p
        13027 -1
C
c Concrete (Mat. Compendium PNNL) d=-2.3
c (Mat. Compendium PNNL)
c
    m6 nlib=70c plib=04p
        1001 -0.022100
        6000 - 0.002484
        8016 - - .574930
        11023 -0.015208
        12000 -0.001266
        13027 -0.019953
        14000 - 0.304627
        19000 -0.010045
        20000 - 0.042951
        26000.42c - 0.006435
c
c 304L stainless steel dens=8.000 from PNNL-15870Rev1
c
m8 6000 -0.000150
    14028-0.005000
        15031 -0.000230
        16032 -0.000150
        24050-0.007931 $-0.190000
        24052-0.159028
        24053 - 0.018381
        24054 -0.004661
        25055 -0.010000
        26054 - 0.039210 $-0.694480
        26056 -0.638234
        26057 - 0.015001
        26058-0.002035
        28058-0.067198 $-0.100000
        28060 -0.026776
        28061 -0.001183
        28062 -0.003834
        28064 -0.001009
        NLIB=70c
C
c BK7
c
```

```
    m9 NLIB=70c PLIB=04p
        14028-0.323138999
        8016 -0.483882614
        5011 -0.033384805
        56138.60c -0.027496631
        11023-0.077153875
        19039 -0.052216449
        33075 -0.002726626
c
c mumetal
c
    m10 28000.50c 0.8
        42000.60c 0.05
        14000.60c 0.005
        29063 0.0002 nlib = 60c
        26056 0.1448 nlib = 70c
c
c PTFE rho = 2.25 g/cm3
c
    m11 6000.70c 0.333339
        9019.70c 0.666661
c
c vinyl rho = 1.19
c
    m12 1001.70c .07
        6000.70c . 559
        8016.60c . }37
C
c stilbene rho = 1.16
c
    m13 1001.70c .4615
            6000.70c . }538
C
c wood rho = 0.64
c
    m14 1001.70c -0.059642
            6000.60c -0.497018
            7014.70c -0.004970
            8016.70c -0.427435
            12000.60c -0.001988
            16000.60c -0.004970
            19000.60c -0.001988
            20000.60c -0.001988
c
c fused silica (silicon dioxide) rho = 2.32 g/cm3
c
    m15 8016.70c 0.666667
        14000.70c 0.333333
```

c
c Polyurethane Foam rho $=0.021 \mathrm{~g} / \mathrm{cm} 3$
c
m16 $1001.70 \mathrm{c} \quad 0.360023$
$6000.70 \mathrm{c} \quad 0.400878$
$7014.70 \mathrm{c} \quad 0.076459$
$8016.70 \mathrm{c} \quad 0.162639$
c
c PYREX Glass Corning 7740
c (NIST p $=-2.23$ )
c
m17 nlib=60c plib=04p
$5011-0.040064$
$8016-0.539562$
$11023-0.028191$
$13027-0.011644$
$14000-0.377220$
$19000-0.003321$
c
c lucite dens = 1.19
c
m18 nlib=60c plib=04p
$1001-0.080538$
$6000-0.599848$ $8016-0.319614$
c
c ABS plastic dens $=1.05$
c

$$
\mathrm{m} 19 \quad \mathrm{nlib}=60 \mathrm{c} \quad \mathrm{plib}=04 \mathrm{p}
$$

10010.5151515
60000.4545455
70140.0303030
c
c Cadmium dens $=8.65 \mathrm{~g} / \mathrm{cm} 3$
c
$\mathrm{m} 20 \mathrm{nlib}=60 \mathrm{c} \quad$ plib$=04 \mathrm{p}$ 480001
c
c PuO 2 dens $=11.5 \mathrm{~g} / \mathrm{cm} 3$ or 16.5
c
m21 nlib $=60 \mathrm{c}$ plib=04p
$94238-0.013$
$94239-0.954$
$94240-93.51$
$94241-0.193$
$94242-4.56$
$95241-0.4862$
$8016-0.01$

```
c 8016 -0.134
c
c Tallies
c
    FC11 Source case neutron flux tally
    F11:N 8.1 8.2 8.3
    C11 0 1
    E11 0.0 99 i 10
    FC21 Source case photon flux tally
    F21:P 8.1 8.2 8.3
    C21 0 1
    E21 0.0 99i 10
    FC31 Stilbene surface neutron flux tally
    F31:N 10015.2 15.1 10015.3
    C31 0 1
    E31 0.0 99i 10
    FC41 Stilbene surface photon flux tally
    F41:P 10015.2 15.1 10015.3
    C41 0 1
    E41 0.0 99 i 10
c *** END DATA ***
    \hookrightarrow
c *********** END OF FILE
```


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