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Optimal allocation of distributed generation and electric vehicle charging stations based on intelligent algorithm and bi-level programming

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Abstract

To facilitate the development of active distribution networks with high penetration of large-scale distributed generation (DG) and electric vehicles (EVs), active management strategies should be considered at the planning stage to implement the coordinated optimal allocations of DG and electric vehicle charging stations (EVCSs). In this article, EV charging load curves are obtained by the Monte Carlo simulation method. This article reduces the number of photovoltaic outputs and load scenarios by the K-means++ clustering algorithm to obtain a typical scenario set. Additionally, we propose a bi-level programming model for the coordinated DG and EVCSs planning problem. The maximisation of annual overall profit for the power supply company is taken as the objective function for the upper planning level. Then, each scenario is optimised at the lower level by using active management strategies. The improved harmonic particle swarm optimisation algorithm is used to solve the bi-level model. The validation results for the IEEE-33 node, PG&E-69 node test system and an actual regional 30-node distribution network show that the bi-level programming model proposed in this article can improve the planning capacity of DG and EVCSs, and effectively increase the annual overall profit of the power supply company, while improving environmental and social welfare, and reducing system power losses and voltage shifts. The study provides a new perspective on the distribution network planning problem.

KEYWORDS

bi-level programming model, distributed generation, electric vehicle charging station, optimal allocation

1 | INTRODUCTION

With increasing attention on environmental pollution problems and the fossil fuel crisis, an increasing number of applications are being proposed for distributed generation (DG) and electric vehicles (EVs). Furthermore, the necessary infrastructure for EVs, that is, electric vehicle charging stations (EVCSs), is being built with support from government and enterprise. However, the large-scale integration of DG and EVCSs will bring many new problems, such as increasing power losses and voltage sags during power system operation. Therefore, the planning problem of reasonably allocating DG and EVCSs is attracting much attention.

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The work by Gao et al³ uses multiobjective formulations that consider net revenue maximisation, load timing characteristics and the DG output and generates solutions with an adaptive generic algorithm. The work by Kayalvizhi and Vinod⁴ builds a multiobjective optimisation model that simultaneously consider power loss minimisation, voltage shift minimisation and cost minimisation, and the validity of the programming model is verified by three examples. The work by Singh et al⁵ builds an optimal allocation model for DG with constraints for reactive power optimisation and network reconfiguration. The intelligent heuristic algorithm is used to obtain optimal solution. Some Traffic flow models are used in Xiang et al⁶ to determine the capacity of EVCSs with consideration of coupled traffic flow and load demand constraints. In other studies, such as references 7-9, the authors formulate the EVCSs planning goal as a total cost minimisation problem by considering power loss costs and EVCSs investment costs together.

The aforementioned works mainly study the planning problems of DG and EVCSs separately without considering the coupled coordination problem. In practice, the siting and sizing of EVCSs affects not only the power system stability but also the convenience of EV use. In addition, the reasonable planning of EVCSs will benefit local on-site consumption of DG power output. Based on these considerations, the work by Liu et al¹⁰ builds a joint planning model of EVCSs and renewable energy with minimum voltage fluctuations, minimum load fluctuations and maximum capacity for EVCS energy storage connections, and the genetic particle swarm algorithm is used to determine the optimal construction scheme. Other works^{11,12} consider the impacts of increasing the load demand, dynamic electricity pricing and DG power intermittence on the EVCS and DG coordination planning problem.

Large-scale access to renewable DG and the extensive use of EVs have promoted the use of clean energy and enhanced the sustainability of power grid development. However, at the same time, problems such as power quality declines, voltage overruns and an increase in system losses have emerged. The traditional distribution network has the problem of an outdated management mode that cannot completely solve the above problems. To effectively reduce the adverse effects of new grid-connected energy sources and improve the compatibility between these sources and the overall system, the related technologies of active distribution networks (ADNs) have received extensive attention in recent years. ADNs coordinate and control DG, the energy storage system, controllable loads and other power equipment in the distribution network by optimising the system management mode to promote the source absorption of green and clean energy. The planning models in [10-12] do not consider the adjustment ability of ADNs when considering the planning problem, and could not make full use of the positive effects of DG and EVCs on reducing network loss and improving system power flow distribution, which limited the development of DG and EVCS. The work by Zare et al¹³ takes active management measures for DG connected to distribution network and establishes a distributed planning model of DG based on multiobjective two-layer distribution under the active management model. The work by Bo et al14 is based on the master-slave logic structure, aiming at promoting the efficient use of intermittent DG, and established the ADN double-layer scene-planning model. The location and volume of DG and EVCS are closely related to ADN's operation control strategy. Solving the bi-level programming model is an effective means of ADN planning.

In conclusion, there are few studies on joint planning of DG and EVCS and considering active management measures. Therefore, a bi-level planning model of a coupled EVCS and DG system that considers the active management strategy of distribution network is proposed in this article. First, the daily characteristic curve of EV charging load is obtained through Monte Carlo simulation (MCS), and then the total charging load in the planned area is obtained. The K-means++ clustering algorithm is used to construct typical scenarios for DG and conventional loads. On this basis, a two-layer model of joint coordination planning including DG and EVCS is established. The upper planning level sets the objectives of investment cost, power loss cost and environmental and social welfare and the lower level proposes three active management measures to optimise the power flow for typical scenarios. The active management at the lower level proposes three active management measures to optimize the power flow for each typical scenario. The overall problem is solved by improved harmonic particle swarm optimisation (IHPSO) and verified on IEEE-33 node and PG&E-69 node test systems.

2 | EV CHARGING MODEL AND DG OUTPUT MODEL

2.1 | EV charging model

There are four types of typical EVs: buses, taxis, business cars and private cars. The charging load is affected by the charging mode, battery capacity, initial state-of-charge (SOC) and other factors. The charging parameters of four types of EVs are listed in Table 1.

The charging time is determined by the EV parameters, ¹⁵ as shown in (1).

$$T_{c} = \frac{(\beta - SOC_{0})}{\eta \cdot P_{c}} \cdot E_{b} \cdot 60, \tag{1}$$

where T_c indicates the charging time in minutes, β indicates the percentage of batter capacity after charging, SOC_0 indicates the percentage of battery capacity before charging, η indicates the charging efficiency, P_c indicates the charging power and E_b indicates battery capacity.

The charging behaviours of the four types of EVs are listed in Table 2. ¹⁶ Buses and taxis need to charge more than two times due to their longer daily driving distances. The operating time of buses is usually 5:30 to 23:00. To ensure sufficient driving power, it is assumed that buses need to be charged twice a day. In the daytime, to avoid the rush hours of 6:30 to 9:00 and 16:30 to 18:00, the charging time is 10:00 to 16:30. During daytime operation, the time for buses to stop and charge is limited, so fast charging is adopted. During the night, according to the bus operation time, the night charging time can be assumed to be 23:00 to 5:30, and because the charging time in the night is longer, the conventional charging method can be used. Taxis are in operation for most of the day. To ensure sufficient driving power, taxis need to be charged twice a day. In the daytime, they need to be charged from 11:30 to 14:00 and from 2:00 to 5:00 during break time. The fast charging mode is chosen for the limited charging time. Because government departments or enterprises usually perform their official duties in the daytime, the official vehicles will be in the driving state only during the day. The charging time is long from 18:00 to 7:00, so conventional charging is adopted. The charging period of private cars can be divided into a night rest period at home and a daytime work period, that is, 18:00 to 7:00 and 8:00 to 17:00. The charging time is long and can be 19:00 to 22:00 at places such as supermarkets and shopping malls. Considering the shopping and entertainment needs of private EV users, short-term charging time should be applied.

This article estimates the EV charging loads based on MCS. MCS is used to obtain the daily charging load curve of EVs. The MCS is a method used to study the distribution characteristics of time series by setting up random processes, repeatedly generating time series and calculating parameter estimators and statistics. The prediction accuracy depends on the number of simulations, with more simulations resulting in more accurate predictions, and the error method has nothing to do with the dimension of the problem because the dimension error of the problem does not increase with the size of the problem. The method can be used directly to determine the statistical properties of a problem, and it does not need to handle discretisation or continuity problems. The solution process is simple and direct, and the error in the result is the error probability, which can be effectively reduced by increasing the number of simulations. Thus, this method is the most effective way or the only way to resolve some problems.

Based on MCS, the calculation process of EV charging loads is as follows:

- 1. randomly select the beginning charging time and initial SOC of a single EV;
- 2. calculate the charging limit time T_{lim} based on the time period of EV charging behaviour;
- 3. calculate the required charging time $T_{\rm f}$ according to the fully charged expectation;
- 4. obtain the practical charging time $T_{cd} = min(T_{lim}, T_f)$;
- 5. repeat steps 1 to 4 for all other EVs considered and
- 6. aggregate the total EV charging load in a certain region.

2.2 | Intermittent DG output model

If an EV is fully charged by power generation from conventional energy sources, then the indirectly produced CO₂ emissions will not be less than those of conventional vehicles. To date, the most common renewable energy resources

TABLE 1 Charging parameters of electric vehicles

Vehicle type	Battery capacity (kW·h)	Conventional charging power (kW)	Fast charging power (kW)
Bus	200	21	135
Taxi	64	14	90
Official car	32	7	45
Private car	32	7	45

are distributed wind generation (DWG) and photovoltaic generation (PVG), which have strong characteristics of intermittence due to the effects of solar irradiance, wind speed and other environmental factors. To choose optimal EVCS locations, we should consider the weather conditions in certain areas.

The PV power output model is

$$P_{\text{PVG}} = \begin{cases} P_{\text{PVGS}} \frac{g}{g_{\text{s}}} & g \le g_{\text{s}} \\ P_{\text{PVGS}} & g > g_{\text{s}} \end{cases}$$
 (2)

where P_{PVG} denotes the output power of PV, P_{PVGS} indicates the rated output power of PV, g indicates the actual solar irradiance and g_s indicates the rated solar irradiance.

Wind power is closely correlated with wind speed, and the relationship can be described as follows:

$$P_{\text{DWG}} = \begin{cases} 0 & 0 \le \nu < \nu_{i} \cup \nu_{o} \le \nu \\ P_{\text{DWGS}} \frac{\nu - \nu_{i}}{\nu_{s} - \nu_{i}} & \nu_{i} \le \nu < \nu_{s} \\ P_{\text{DWGS}} & \nu_{s} \le \nu < \nu_{o} \end{cases}$$
(3)

where P_{DWG} indicates the wind output power, P_{DWGS} indicates the rated wind output power, ν indicates the actual wind speed, ν_{i} indicates the cut-in wind speed, ν_{o} indicates the cut-off wind speed and ν_{s} indicates the rated wind speed.

2.3 | Selection of typical scenarios

The PV, wind output power and load demand have characteristics of periodicity and uncertainty. Therefore, selecting the typical scenarios according to historical data in certain areas is very important for describing the PV output power, wind output power and demand load. This article uses the K-means++ clustering algorithm¹⁷ for scenario reduction. The K-means++ algorithm has the advantages of simple implementation and good clustering, and compared with other methods, such as the K-means algorithm, this algorithm possesses a selection process of initial clustering centres by the distance maximisation principle that is conducive to improving the clustering effect. We can use 8760 hours of historical data as the original dataset for the PV, wind power and load demand and then divide these 365 daily curves into k scenarios according to the Pseudo F-statistic (PFS) metric.¹⁸ The k scenarios selected are denoted as ξ_1 , ξ_2 , ..., ξ_k . The DG output is calculated according to these k scenarios. The clustering process is as follows:

- 1. Normalisation of PV, wind power and load demand based on the data standardisation method;
- 2. Based on the maximum distance between initial clustering centres, K clustering centres are initialised. The steps are as follows:
- a. A scene from the original scene set N_i , i = 1, 2, 3, ..., 365 is randomly selected as the first cluster ξ_1 .
- b. The shortest Euclidean distance $d(N_i, \xi_j)$ between each original scene and the existing clustering centres is calculated, and $d(N_i, \xi_i)$ of each original scene is accumulated to get the accumulated value sum (d).
- c. The random value rand, rand < sum (d) is generated, and the rand value is updated to rand $d(N_i, \xi_j)$. When rand < 0, N_i is the new cluster centre, which ensures that the original scene farther from the existing cluster centre is selected as the new cluster centre.
- d. Steps 2 and 3 are repeated until the selection of k clustering centres $\xi_1, \xi_2, ..., \xi_k$ is completed.
- e. The Euclidean distance from the remaining original scene to k clustering centres is calculated, and the original scene is divided into the nearest clustering cluster.
- f. The centres of k clusters are calculated, and the k centres to the new generation of clustering centres of ξ_1 , ξ_2 , ..., ξ_k are updated.
- g. Steps 3 and 4 are updated until the clustering results do not change.

TABLE 2 Charging behaviour of electric vehicles

Туре	Charge time period	Charge probability	Initial SOC distribution	Initial charging time distribution	Charge method
Bus	10:00-16:30	1	$N(0.5, 0.1^2)$	Evenly distributed	Fast charge
	23:00-5:30	1	$N(0.5, 0.1^2)$	Evenly distributed	Regular charge
Taxi	11:30-14:00	1	$N(0.3, 0.1^2)$	Evenly distributed	Fast charge
	2:00-5:00	1	$N(0.3, 0.1^2)$	Evenly distributed	Fast charge
Official car	18:00-7:00	1	$N(0.4, 0.1^2)$	Evenly distributed	Regular charge
Private	8:00-17:00	0.2	$N(0.6, 0.1^2)$	$N(9, 0.5^2)$	Regular charge
car	18:00-7:00	0.7	$N(0.6, 0.1^2)$	$N(19, 1.5^2)$	Regular charge
	19:00-22:00	0.1	$N(0.6, 0.1^2)$	Evenly distributed	Regular charge

3 | MATHEMATICAL FORMULATION WITH BI-LEVEL PROGRAMMING

A bi-level programming model is a hierarchical system optimisation model in which the upper and lower levels have their own mathematical models. The lower-level programming problem is based on the scheme given by the upper-level decision-making process. The optimal value of the lower-level decision-making process is fed back to the upper level, and the upper-level decision-making process conforms to the global optimal benefit according to the optimal value response of lower-level decision-making process. Bi-level programming is characterised by considering the entire situation from a holistic point of view, which is conducive to achieving the global optimum.

3.1 | The planning level model

It is assumed that the investment in intermittent DG and EVCSs comes from a power supply company. The decision variables of the upper planning level will be location and capacity, and the objective is the maximisation of annual revenue with considerations for the annual rate of return, power loss and environmental and social welfare. The objective function is shown in (4).

$$\max F = C_{\text{pro}} - C_{\text{loss}} + C_{\text{env}}.$$
 (4)

where C_{pro} indicates the annual rate of return for the power supply company, C_{loss} indicates the power loss and C_{env} indicates the environmental and social welfare. The three cost structures are listed as follows:

1. The annual rate of return for the power supply company C_{pro} is given by

$$C_{\text{pro}} = C_{\text{S}} + C_{\text{B}} - C_{\text{inv}} - C_{\text{OM}} \tag{5}$$

where C_s indicates the profit of the power supply company, C_B indicates government subsidies for renewable energy sources, C_{inv} indicates the investment in intermittent DG and EVCSs and C_{OM} indicates the maintenance fee for DG and EVCSs.

$$C_{\rm S} = 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} (c_{\rm o}(P_{l,t,\rm DWG} + P_{l,t,\rm PVG}) + (c_{\rm o} - c_{\rm i}) \cdot (P_{l,t,L} - P_{l,t,\rm DWG} - P_{l,t,\rm PVG}) + (c_{\rm e} - c_{\rm i}) P_{l,t,\rm EV}),$$
(6)

where k indicates the number of typical scenarios; p_l indicates the probability of the lth typical scenario; c_i and c_o indicate the purchasing and selling prices for the power supply company; c_e indicates the unit selling price for EVCSs; and

 $P_{l,t,L}$, $P_{l,t,DWG}$, $P_{l,t,PVG}$ and $P_{l,t,EV}$ represent the load demand, DWG output power, PVG active power and EVCS charging load, respectively, at time interval t.

$$C_{\rm B} = 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} c_{\rm b,DWG} P_{l,t,\rm DWG} = c_{\rm b,PVG} P_{l,t,\rm PVG}$$
(7)

where $c_{b,DWG}$ and $c_{b,PVG}$ represent units of government subsidies for DWG and PVG.

$$C_{\text{inv}} = \left(\sum_{j=1}^{n_{\text{DWG}}} c_{t1} P_{j,\text{DWG}} + \sum_{j=1}^{n_{\text{PVG}}} c_{t2} P_{j,\text{PVG}} + \sum_{j=1}^{n_{\text{EV}}} \left(c_g + c_{t3} P_{j,EV}\right)\right) \frac{r(1+r)^{n_1}}{(1+r)^{n_1} - 1},\tag{8}$$

where C_{inv} indicates the investment and building costs of DG and EVCSs; n_{DWG} , n_{PVG} and n_{EV} indicate the number of candidate nodes for DWG, PVG and EVCSs, respectively; $P_{j,\text{DWG}}$, $P_{j,\text{PVG}}$ and $P_{j,\text{EV}}$ indicate the capacity for DWG, PVG and EVCSs, respectively, at node j; c_{t1} , c_{t2} and c_{t3} indicate the unit capacity construction costs of DWG, PVG and EVCSs, respectively; c_{g} indicates the fixed investment cost of EVCSs; r indicates the discount rate and n_{1} indicates the service life of the equipment.

$$C_{\text{OM}} = 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} (c_{\text{om1}} P_{l,t,\text{DWG}} + c_{\text{om2}} P_{l,t,\text{PVG}}) + \sum_{j=1}^{n_{\text{EV}}} (c_{\text{om3}} P_{j,\text{EV}})$$
(9)

where $c_{\rm om1}$ and $c_{\rm om2}$ indicate the unit maintenance fees for DWG and PVG, respectively, and $c_{\rm om3}$ indicates the amortised unit maintenance fee for EVCSs.

2. The power loss cost C_{loss} is given by

$$C_{\text{loss}} = 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} c_0 P_{l,t,\text{loss}}$$
 (10)

where $P_{l,t,loss}$ indicates the system loss at time interval t.

3. The environmental and social welfare C_{env} is given by

$$E_{\rm s} = 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} (P_{l,t,\rm DWG} + P_{l,t,\rm PVG})$$
 (11)

$$C_{\text{env}} = E_s \sum_{s=1}^{N_{\text{env}}} x_s (a_s + b_s) + 365 \sum_{l=1}^{k} p_l \sum_{t=1}^{24} \frac{P_{l,t,\text{EV}}}{e_{\text{EV}}} c_{\text{Co}_2} x_{\text{EV}},$$
(12)

where E_s indicates the output power for renewable energy; $C_{\rm env}$ indicates the social welfare of renewable energy sources and reduced emissions from EVs; $N_{\rm env}$ indicates the types of pollution gases; x_s , a_s and b_s denote the emission levels of the sth kind of pollution gas; $e_{\rm EV}$ indicates the energy consumed by an EV in 100 miles; $e_{\rm CO_2}$ indicates the CO₂ trading tax fee in the international market; and $e_{\rm EV}$ indicates the difference between EVs and conventional vehicles.

The constraints in the upper-level optimisation model are

$$P_{\text{DG}i,\text{min}} \le P_{\text{DG}i} \le P_{\text{DG}i,\text{max}} \tag{13}$$

$$\sum_{i=1}^{n_{\text{DG}}} P_{\text{DG}i} \le P_{\text{DG,max}} \tag{14}$$

$$P_{\text{EV}i,\text{min}} \le P_{\text{EV}i} \le P_{\text{EV}i,\text{max}}.\tag{15}$$

3.2 | The active management level model

The lower active management level is based on the upper-level planning decisions, and three active management strategies are proposed for power flow optimisation in typical scenarios, including transformer adjustment, DG output curtailment and reactive power compensation. The curtailment rate of DG is 0% to 30%, the transformer adjustments are $1\% \pm 1.25\%$ *8 and are installed at the system header node, and the reactive power compensation is 50 kvar for a unit capacity with 0 to 10 units. Power flow optimisation based on active management measures impacts network losses, voltage levels, transmission power and other constraints of system operation and thus affects the ability of a system to accept DG and EVCSs. The above effects are ultimately reflected in the objective function. The objective function of the lower-level optimisation model is

$$\max f = C_{l,S} + C_{l,B} - C_{l,OM} - C_{l,loss} + C_{l,env}, \tag{16}$$

where $C_{l,S}$, $C_{l,B}$, $C_{l,OM}$, $C_{l,loss}$ and $C_{l,env}$ denote the profit of the power supply company, the government subsidy for renewable energy sources, the maintenance fee for DG and EVCSs, the power loss fee and the environmental and social welfare in scenario l, respectively.

$$\begin{cases}
P_i - U_i \sum_{j \in i} U_j \left(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \right) = 0 \\
Q_i - U_i \sum_{j \in i} U_j \left(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \right) = 0
\end{cases}$$
(17)

$$U_{\text{imin}} \le U_i \le U_{\text{imax}} \tag{18}$$

$$S_{ij} \le S_{ij\max} \tag{19}$$

$$U_{\rm OLTC}^{\rm min} \le U_{\rm OLTC} \le U_{\rm OLTC}^{\rm max} \tag{20}$$

$$P_{\text{cut}i} \le P_{\text{cut}i}^{\text{max}} \tag{21}$$

$$Q_{ci} \le Q_{ci}^{\max},\tag{22}$$

where P_i and Q_i indicate active power and reactive power injections; U_i and U_j indicate the voltages at nodes i and j, respectively; G_{ij} and B_{ij} indicate conductance and admittance, respectively; θ_{ij} indicates the angle shift between i and j; $U_{i\max}$ and $U_{i\min}$ indicate the upper and lower voltage bounds, respectively, at node i; S_{ij} and $S_{ij\max}$ indicate the transmission power and transmission power limit, respectively; U_{OLTC} indicates the secondary voltage at the transformer; U_{OLTC}^{\max} and U_{OLTC}^{\min} indicate the upper and lower limits of secondary voltage at the transformer, respectively; $P_{\text{cut}i}$ indicates the curtailment for DG at node i; $P_{\text{cut}i}^{\max}$ indicates the allowed curtailment at node i and Q_{ci} indicates the reactive power compensation at node i with an allowed upper limit of Q_{ci}^{\max} .

4 | THE OPTIMAL SOLUTION OF THE PROPOSED BI-LEVEL PROGRAMMING METHOD

4.1 | The solution algorithm for the two-layer model

Particle swarm optimisation (PSO) simulates the principle of bird swarm foraging. It has the advantages of simple calculation and strong direction of optimisation. However, the PSO algorithm has poor global search ability and easily falls into local optima in the later stage of the algorithm. Harmony search (HS) expands the search range in the later stage

of the algorithm, but its directivity is not strong. The new harmony combination principle of the HS algorithm is introduced in the particle optimisation process of the PSO algorithm. In each iteration of the process, the search space is searched for the optimal particle with a certain probability to improve the global search performance of the algorithm. The computational steps of IHPSO algorithm are as follows:

1. Chaotic initialisation of PSO based on formula (23) is used to improve the ergodicity of the initial particle in the search space:

$$x_{i,j} = x_j^{\min} + \left(x_j^{\max} - x_j^{\min}\right) \chi_{i,j}$$
 (23)

$$\chi_{i,j+1} = \lambda \cdot \chi_{i,j} \left(1 - \chi_{i,j} \right), \tag{24}$$

where $x_{i,j}$ indicates the *j*-dimension of particle *i*; x_j^{\max} and x_j^{\min} indicate the upper and lower limit values, respectively, of variable *j*; and $\chi_{i,j}$ indicates the sequences of chaotic variables generated by logistic mode 1, and the chaotic parameters λ are set to 4.

- 2. The fitness value $f(x_i)$ of each particle is calculated, and the individual extreme value P_i of each particle and the global extreme value P_g of the population are obtained.
- 3. The inertia coefficient, learning coefficient and particle position and velocity are updated.
- 4. The fitness value of the new generation particle swarm is calculated, the individual extreme value is updated, and the global extreme value is removed.
- 5. New particles hm^{new} are generated based on Harmony Memory Considering Rate (*HMCR*), Pitch Adjusting Rate (*PAR*), and bandwidth (*BW*).
 - a. If *HMCR* is larger than the random variable, new particle variables are randomly obtained from PSO; otherwise, they are randomly generated from the range of variables.
 - b. If *PAR* is greater than the random variable, then the bandwidth of the new particle variable is adjusted; otherwise, no adjustment is made.
 - c. Steps (b) and (c) are repeated until all new variables are constructed to generate new particles.
- 6. The global extremum P_g is updated. If the fitness value of the new harmony $f(hm^{\text{new}})$ is better than the fitness value of the global extremum $f(P_g)$, then the new harmony hm^{new} is the new global extremum P_g .
- 7. Whether the algorithm satisfies the conditions for achieving the number of iterations is determined; otherwise, return to step 3.

4.2 | The flowchart of the solution process

The coordinated bi-level programming framework for DG and EVCSs is presented in Figure 1. The planning level determines the siting and sizing of DG and EVCSs, and the active management level determines the three active management strategies by using transformer adjustment, DG output curtailment and reactive power compensation. The planning layer transfers the optimal allocation scheme of DG and EVCSs to the active management level. On this basis, the active management level optimises the power flow of four scenarios under the optimal allocation scheme by adjusting the On-load tap changer (OLTC) gear, reducing DG active power and switching reactive power compensation devices. By satisfying the reliability of system operation, the optimal solutions $\max f_1 \sim \max f_4$ of four scenarios is obtained and fed back to the planning level. Combining the optimal solutions $\max f_1 \sim \max f_4$ and the investment and construction costs of the DG and charging stations, the planning level calculates the optimal solution $\max F$ and optimises the decision scheme. By analogy, the optimal joint planning scheme of DG-charging station is determined through multiple information transmissions and feedback between the planning level and the active management level.

5 | CASE STUDY

5.1 | Case study of the IEEE-33 node test system

This article considers the coordinated planning problem for DG and EVCSs on an IEEE-33 node test system, which is shown in Figure 2, using the system parameters described in.²¹

It is assumed that the number of EVs is 600 in the studied region, the running time for the MCS is 50 000, and the parameters of the probability model are shown in Table 2. The ratio of electric buses, electric taxis, electric buses and electric private cars is 1:2.4:10.2:63.5, as in reference [16]. The average charging load of 60 minutes in the hour is used as the charging load of an hour. According to the calculation presented in section A, the total charging load is shown in Figure 3.

The 365*24-hour daily profiles of wind speed, solar irradiance, and conventional load demand are presented in Figure 4 in references 22, 23.

According to the PFS metric (Figure 5) of the clustering results, the number of clusters is set to be 4. The four typical scenarios of wind speed, solar irradiance and conventional load demand are shown in Figure 6, in which normalisation has been completed.

$$PFS = \frac{\text{tr}(N_{\rm B})/(K-1)}{\text{tr}(N_{\rm W})/(S-K)},$$
(25)

where K is the number of clusters; S is the number of original scene samples and tr (N_B) and tr (N_W) are the traces of the interclass and intraclass scatter matrices, respectively. After clustering, if the distance between different clusters is larger and the distance between samples in the same cluster is smaller, then the PFS index is larger, which indicates that the clustering effect is better.

The particle swarm size is 40, the number of iterations time is 100, the inertia coefficients $\omega_{\rm max} = 0.95$ and $\omega_{\rm min} = 0.4$, learning coefficient $c_{\rm 1max} = 2.75$, $c_{\rm 1min} = 1.25$, $c_{\rm 2max} = 2.25$ and $c_{\rm 2min} = 0.5$. In harmony algorithm part, the memory library value probability HMCR = 0.9, the fine-tuning probabilities $PAR_{\rm max} = 0.4$, and $PAR_{\rm min} = 0.9$, and the fine-tuning bandwidths $bw_{\rm max} = 1$ and $bw_{\rm min} = 0.0001$. The wind turbines are installed at nodes 13, 23 and 31; the PV panels are installed at 7, 21, 28; and the EVCS candidate nodes are nodes 20, 4, 8, 14 and 29. The rated power for DG is 100 kW, with a rated solar irradiance of 1 kW/m², and a cut-in wind speed, rated wind speed and cut-off wind speed of 3 m/s, 13.5 m/s and 20 m/s, respectively. The purchasing and selling prices of the power supply company are 0.4 CNY/China Yuan (RMB)/kW·h and 0.5 RMB/kW·h. The unit price of a charging station is 1 RMB/kW·h. The government subsidy price $C_{\rm b,DWG}$ is 0.1 RMB/kW·h, and $C_{\rm b,PVG}$ is 0.36 RMB/kW·h.

The building costs are $c_{t1} = 5381$ RMB/kW, $c_{t2} = 4375$ RMB/kW, $c_{t3} = 6000$ RMB/kW and $c_g = 3\,000\,000$ RMB. The discount rate is 8%, and the equipment life is 20 years. The cost parameters for operation and maintenance are $c_{om1} = 0.0296$ RMB/kW·h, $c_{om2} = 0.0096$ RMB/kW·h and $c_{om3} = 100\,000$ RMB/MW in in reference [23].

The pollution costs of thermal power generation are shown in Table 3, as in reference [24].

Three strategies are employed for optimal allocation.

- Strategy 1: use the active management strategy for the coordinated planning of DG and EVCSs.
- Strategy 2: do not use the active management strategy for the coordinated planning of DG and EVCSs.
- Strategy 3: use the optimal allocation for DG and then for EVCSs.

The results from using these three strategies are shown in Table 4.

In the DG planning scheme, 13(8) indicates that 8 distributed generators are installed in nodes 13, and in the EVCSs planning scheme, 20(237) indicates that the capacity of the charging station in node 20 is 237 kW.

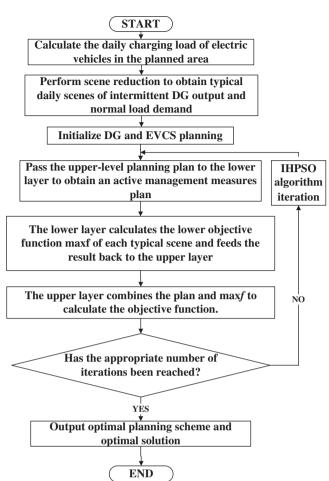
The active management measures of Strategy 1 are shown in Table 5.

In the curtailment rate of DG, 13(23%) indicates that the active outputs of DG on node 13 are reduced by 23%. In the reactive power compensation, 13(400) indicates that 400 kvar of reactive power are compensated in node 13. In the transformer adjustments, -3 indicates that the transformer tap is connected at -3×1.25 %.

1. Result analysis of optimal allocation

Strategy 2 considers coordinated planning for DG and EVCSs, and strategy 3 considers DG planning first and then





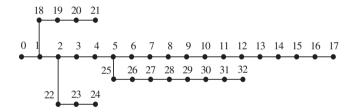


FIGURE 2 IEEE-33 node test system

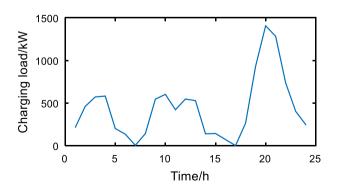


FIGURE 3 Charging load of an electric vehicle

allocates EVCSs based on the DG planning result. Comparing strategy 2 to strategy 3, strategy 2 increases the DG capacity to 300 kW because it considers mutual support for the DG and EV charging loads.

The integration of EVs into the distribution network can help to increase system flexibility by integrating DG and to reduce the possibility of voltage violations caused by DG integration. However, strategy 3 is individual planning strategy, which is limited by the designed capacity.

FIGURE 4 Wind speed, light intensity and load curves

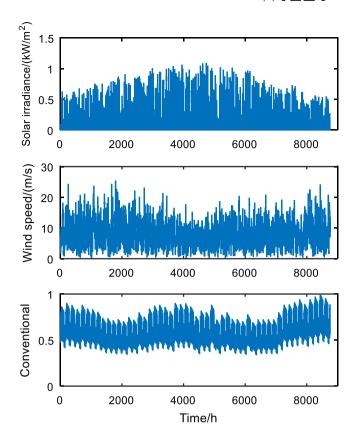
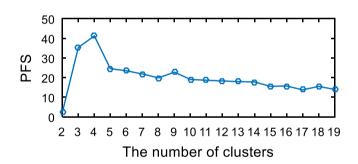
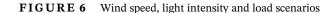


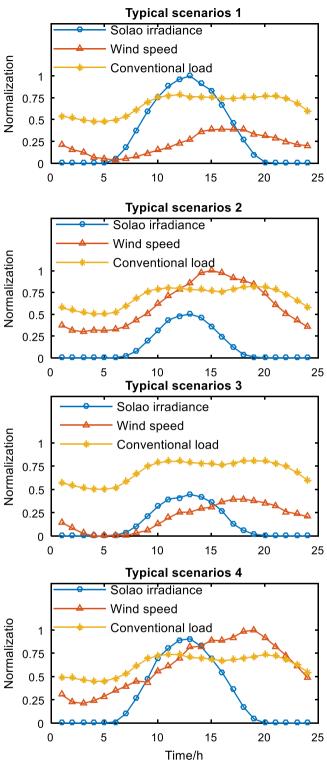
FIGURE 5 PFS of different clustering scene numbers



By comparing strategy 1 to strategy 2, we find that the introduction of an active management strategy increases the DG capacity by 1300 kW and the EVCS capacity by 150 kW. It is believed that the use of active management strategies for DG and EVCS operation can effectively control the allocation of power flow by increasing system flexibility to integrate DG and EVCSs while satisfying various constraints in the distribution network. In traditional methods, the system could easily present some voltage or power violations for the integration of large-scale DG and EVCSs.

- 2. Revenue analysis of distribution network
 - The revenues from the distribution network using different strategies are summarised in Table 6. Comparing strategy 1 to strategy 2, strategy 1 increases the annual revenue by 654 100 RMB, with annual profit increases of 445 900 RMB, power loss decreases of 94 300 RMB and environmental and social welfare increases of 113 900 RMB.
 - a. Regarding the annual profit from the selling price, strategy 1 effectively increases the capacity of DG and EVCSs. Although increasing the capacity increases the investment and system maintenance fees, more DG output can also be consumed. The lower level power supply company will reduce the cost of purchasing electricity from the upper-level power supply company. Furthermore, EVCSs can be more effectively integrated into the power system, with increasing profits for the charging stations. Therefore, strategy 1 will have better annual profits.
- b. The annual power losses caused by these three strategies are presented in Figure 7, in which strategy 1 decreases the power loss by 50.72% and 53.09% compared to strategy 2 and strategy 3, respectively. Because strategy 1 uses active





management for optimising power flow allocation, the power losses in the distribution network are effectively controlled.

c. Regarding clean energy utilisation, strategy 1 consumes 1870 MW·h more DG output power and integrates 85.14 MW·h more EV charging loads than strategy 2, which encourages the consumption of clean energy while reducing the environmental pollution caused by fossil fuels. The emissions of SO_2 , NO_x and CO_2 are reduced by 6707 kg, 2887 kg and 1.20×10^6 kg, respectively, which satisfies the requirements of the Chinese government. The integration capability of clean energy and the pollution reduction ability of different strategies are presented in Table 7.

TABLE 3	Cost parameters of
environmental	pollution

Contaminant	x_s (kg/MW·h)	a_s (RMB/kg)	b_s (RMB/kg)
CO_2	639.2	0.01	0.02
SO_2	3.587	1.00	6.00
NO_x	1.544	2.00	8.00

TABLE 4 Optimal allocation results of different strategies

Strategy	Optimised	Optimised configuration results	
Strategy 1	DG	13(8).23(10).31(10).7(7).21(2).28(6)	4300
	EVCS	20(237).4(194).8(223).14(309).29(203)	1166
Strategy 2	DG	13(10).23(5).31(8).7(7)	3000
	EVCS	20(252).4(197).8(186).14(173).29(208)	1016
Strategy 3	DG	13(9).23(4).31(10).21(3).28(1)	2700
	EVCS	20(185).4(186).8(185).14(184).29(185)	925

TABLE 5 The active management measures of strategy 1

Scenarios	Curtailment rate of distributed generation	Reactive power compensation	Transformer adjustments
Scenarios 1	13(0%).23(0%).31(0%).7(0%).21(0%).28(0%)	13(400).23(50).31(100).7(0).21(250).28 (250)	-3
Scenarios 2	13(23%).23(29%).31(30%).7(23%).21(28%).28 (30%)	13(200).23(50).31(200).7(0).21(50).28(50)	1
Scenarios 3	13(25%).23(10%).31(0%).7(2%).21(8%).28(7%)	13(300).23(50).31(50).7(0).21(500).28(0)	-1
Scenarios 4	13(0%).23(0%).31(0%).7(0%).21(0%).28(0%)	13(250).23(250).31(300).7(0).21(150).28 (200)	1

As seen by comparing strategy 2 to strategy 3, strategy 2 considers the integration capability of EVCSs for DG. Therefore, the DG output power consumption is increased by 410.47 MW·h in strategy 2, with an annual profit increase of 178 900 RMB. The emissions of SO_2 , NO_x and CO_2 are reduced by 1472 kg, 633 kg and 0.26×10^6 kg, respectively.

d. Voltage shift analysis

For the analysis of voltage shift in the active management strategy, strategy 1 for the optimal allocation of DG and EVCSs has two results, which correspond to the cases of considering active management (case a) and not considering active management (case [b]). The absolute values of the maximum voltage shift are presented in Figure 8.

Using $\pm 5\%$ as the limit for node voltage shifts, without the active management strategy, nodes $9 \sim 17$ and $28 \sim 32$ will have voltage limit violations, with a maximum voltage shift of 6.47%. The maximum voltage deviation occurs at node 17 for the 4 typical scenarios, and its 24-hour voltage is shown in Figure 9. Voltage overshoot occurs at 9:00, 10:00, 19:00, 20:00, 21:00 and 22:00. If active management is utilised, the voltage shifts of all nodes are below 5%, with a maximum value of 2.88%. The results demonstrate that, in the scenario of high penetration of DG and EVCSs, the active management strategy can help to reduce the possibility of voltage violations and increase system reliability.

In conclusion, the comparison between strategy 2 and strategy 3 shows that the joint planning of DG and EVCSs is beneficial to the mutual absorption of DG output and EV charging loads and the development of new energy sources. Thus, strategy 2 is superior to strategy 3. By comparing strategy 1 and strategy 2, it can be concluded that in the joint planning of DG and EVCSs, considering active management measures can effectively improve the system's DG and electricity performance. The acceptance capacity of electric vehicle charging loads can meet the needs of distribution companies while reducing environmental pollution and achieving a win–win situation between enterprise interests and environmental protection. Therefore, strategy 1 is superior to strategy 2, and strategy 1 is the best of the three strategies.

5.2 | Case study of the PG&E-69 node test system

To validate the optimised configuration model proposed in this article, the PG&E-69 node test system shown in Figure 10 and the real 30-node distribution system shown in Figure 11 are verified and analysed. The parameters of the two systems are shown in references [25, 26].

For the PG&E-69 node test system, the wind turbines are installed at nodes 10, 33 and 38, the PV panels are installed at 21, 50, 66, and the EVCS candidate nodes are nodes 14, 32, 40, 45 and 61. The planning results and the active management measures of strategy 1 are shown in Tables 8 and 9. The revenues from the distribution network using different strategies are shown in Table 10.

For the real 30-node system, the wind turbines are installed at nodes $8 \sim 14$, the PV panels are installed at nodes $23 \sim 29$, and EVCS candidate nodes are set as nodes 5, 8, 16, 22 and 25. The planning results and the active management measures of strategy 1 are shown in Tables 11 and 12. The revenues from the distribution network by using different strategies are shown in Table 13.

To analyse the voltage shift in the active management strategy, strategy 1 for the optimal allocation of DG and EVCSs has two results, which correspond to the cases of considering active management (case [a]) and not considering active management (case [b]). The absolute values of the maximum voltage shift are presented in Figures 12 and 13.

TABLE 6	Comprehensive income	of different strategies
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	Strategy 1	Strategy 2	Strategy 3
Investment and construction cost/10 000 RMB	449.83	374.68	354.65
Operation and maintenance cost/10 000 RMB	44.52	39.44	38.13
Government subsidy fee/10 000 RMB	174.35	130.28	115.50
Distribution network sales revenue/10 000 RMB	696.09	621.29	694.87
Charging station sales revenue/10 000 RMB	258.46	252.50	248.03
Annual comprehensive sales revenue/10 000 RMB	634.54	589.95	575.62
System network loss cost/10 000 RMB	9.16	18.59	19.53
Environmental benefits/10 000 RMB	83.72	72.33	69.71
Annual comprehensive income/10 000 RMB	709.11	643.69	625.81

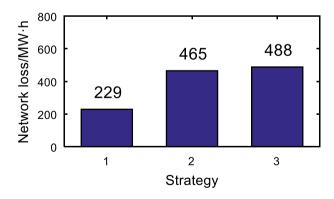


FIGURE 7 Annual network loss of different strategies

TABLE 7 Clean energy acceptance and pollutant reduction

	Strategy 1	Strategy 2	Strategy 3
Distributed generation total consumption (MW·h)	12 407	10 537	10 127
Electric vehicle charging load total acceptance (MW·h)	3692	3607	3543
SO ₂ emission reduction (kg)	44 506	37 799	36 326
NO _x emission reduction (kg)	19 157	16 270	15 636
Carbon emission reduction (×10 ⁶ kg)	8.03	6.83	6.57

FIGURE 8 Maximum voltage shift of IEEE-33 node system

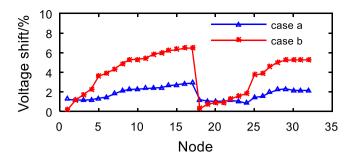


FIGURE 9 Maximum offset of node voltage

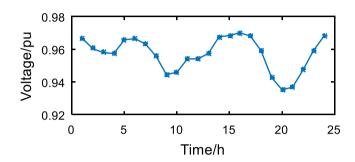


FIGURE 10 PG&E-69 node test system

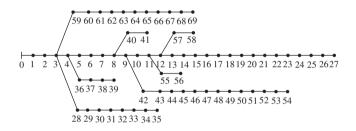
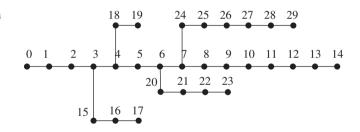


FIGURE 11 Real 30-node distribution system



As seen by comparing the optimal allocation results of the three strategies and the annual comprehensive benefits of the distribution network, strategy 1 has the highest level of clean energy acceptance and the best annual comprehensive benefits. A comparison of the advantages and disadvantages of the three strategies is similar to the simulation results of the IEEE-33 node test system. The proposed model is verified again based on the optimal configuration results of the PG&E-69 node system and a real 30-node distribution system.

5.3 | Performance comparison of algorithms

In this article, the IHPSO algorithm and the PSO algorithm are tested by the test functions $f_1(x) \sim f_4(x)$.

$$f_1(x) = \sum_{i=1}^{n} x_i^2 \tag{26}$$

Strategy	Optimise	Optimise configuration results	
Strategy 1	DG	10(9).33(2).38(10).21(3).50(10).66(10)	4400
	EVCS	14(186).32(273).40(190).45(266).61(339)	1254
Strategy 2	DG	10(2).33(5).38(10).21(4).50(10).66(10)	4100
	EVCS	14(185).32(294).40(238).45(224).61(214)	1155
Strategy 3	DG	10(5).33(2).38(10).21(2).50(9).66(9)	3700
	EVCS	14(190).32(181).40(193).45(188).61(191)	943

TABLE 8 Optimal allocation results of different strategies for the PG&E-69 node system

Abbreviations: DG, distributed generation; EVCS, electric vehicle charging stations.

TABLE 9 The active management measures of strategy 1 in the PG&E-69 node system

Scenarios	Curtailment rate of DG	Reactive power compensation	Transformer adjustments
Scenarios 1	10(0%).33(3%).38(0%).21(0%).50(0%).66(0%)	10(100).33(300).38(0).21(0).50(200).66(50)	-1
Scenarios 2	10(25%).33(29%).38(0%).21(30%).50(0%).66 (0%)	10(50).33(0).38(100).21(300).50(450).66 (200)	-4
Scenarios 3	10(23%).33(0%).38(0%).21(12%).50(0%).66(0%)	10(50).33(300).38(400).21(50).50(250).66 (250)	-4
Scenarios 4	10(0%).33(0%).38(0%).21(0%).50(0%).66(0%)	10(50).33(0).38(300).21(300).50(500).66 (200)	-5

TABLE 10 Comprehensive income of different strategies for the PG&E-69 node system

	Strategy 1	Strategy 2	Strategy 3
Investment and construction cost/10 000 RMB	455.43	432.28	400.03
Operation and maintenance cost/10 000 RMB	39.83	35.66	33.02
Government subsidy fee/10 000 RMB	194.31	189.02	169.32
Distribution network sales revenue/10 000 RMB	652.76	614.36	592.47
Charging station sales revenue/10 000 RMB	260.75	258.63	248.98
Annual comprehensive sales revenue/10 000 RMB	612.57	594.08	577.73
System network loss cost/10 000 RMB	2.73	4.57	4.30
Environmental benefits/10 000 RMB	77.34	71.53	67.90
Annual comprehensive income/10 000 RMB	687.17	661.04	641.33

TABLE 11 Optimal allocation results of different strategies for the 30-node system

Strategy	Optimis	Capacity (kW)	
Strategy 1	DG	8 (13).9 (12).10 (15).11 (15).12 (10).13 (11).14 (15).23 (8).24 (12).25 (11).26 (11).27 (14).28 (15).29 (6)	16 800
	EVCS	5(470).8(494).16(562).22(372).25(660)	2258
Strategy 2	DG	8 (15).9 (15).10 (15).11 (12).12 (7).13 (13).14 (15).23 (8).24 (12).25 (1).27 (7).28 (12).29 (3)	13 500
	EVCS	5(454).8(537).16(316).22(482).25(203)	1992
Strategy 3	DG	8(14).9(14).10(14).11(7).12(13).13(14).14(14).23(2).24(6).25(7).26(3).27(8).28(3).29(7)	12 600
	EVCS	5(375).8(369).16(364).22(371).25(371)	1850

Abbreviations: DG, distributed generation; EVCS, electric vehicle charging stations.

TABLE 12 The active management measures of strategy 1 in the 30-node system

Scenarios	Curtailment rate of distributed generation	Reactive power compensation	Transformer adjustments
Scenarios 1	8(0%).9(0%).10(0%).11(0%).12(0%).13(0%).14(0%).23 (0%).24(0%).25(0%).26(0%).27(0%).28(0%).29(0%)	8(0).9(0).10(450).11(200).12(200).13(100).14 (350).23(0).24(100).25(250).26(200).27(0).28 (350).29(50)	-3
Scenarios 2	8(30%).9(0%).10(0%).11(0%).12(0%).13(28%).14 (0%).23(30%).24(11%).25(30%).26(30%).27(30%).28 (25%).29(30%)	8(0).9(100).10(350).11(0).12(500).13(50).14 (150).23(150).24(0).25(300).26(500).27(450).28 (100).29(150)	0
Scenarios 3	8(0%).9(0%).10(0%).11(0%).12(0%).13(0%).14(0%).23 (16%).24(0%).25(0%).26(30%).27(0%).28(30%).29 (0%)	8(0).9(0).10(300).11(250).12(200).13(0).14(0).23 (400).24(0).25(500).26(500).27(0).28(0).29(0)	1
Scenarios 4	8(0%).9(0%).10(0%).11(0%).12(8%).13(0%).14(0%).23 (0%).24(0%).25(0%).26(0%).27(0%).28(0%).29(0%)	8(400).9(300).10(50).11(500).12(0).13(250).14 (0).23(0).24(250).25(400).26(0).27(0).28(350).29 (0)	-5

TABLE 13 Comprehensive income of different strategy for the 30-node system

	Strategy 1	Strategy 2	Strategy 3
Investment and construction cost/10 000 RMB	1179.19	986.11	932.71
Operation and maintenance cost/10 000 RMB	144.66	139.00	134.19
Government subsidy fee/10 000 RMB	725.77	595.00	552.19
Distribution network sales revenue/10 000 RMB	2782.24	2674.26	2602.63
Charging station sales revenue/10 000 RMB	525.06	491.60	496.00
Annual comprehensive sales revenue/10 000 RMB	2709.21	2635.76	2583.92
System network loss cost/10 000 RMB	27.75	44.65	46.48
Environmental benefits/10 000 RMB	299.66	282.30	271.77
Annual comprehensive income/10 000 RMB	2981.13	2873.41	2809.21

$$f_2(x) = \sum_{i=1}^{n} |x_i| + \prod_{i=1}^{n} |x_i|$$
 (27)

$$f_3(x) = \sum_{i=1}^{n-1} \left[100 \cdot \left(x_{i+1} - x_i^2 \right)^2 + (x_i - 1)^2 \right]$$
 (28)

$$f_4(x) = \sum_{i=1}^{n} \left[x_i^2 - 10 \cdot \cos(2\pi x_i) + 10 \right]. \tag{29}$$

The search parameters of the functions $f_1(x) \sim f_4(x)$ are shown in Table 14.

Using MATLAB programming, the particle swarm size of the algorithm is 50, the number of iterations is 1000, and each algorithm runs 100 times independently. The test results of the two algorithms are shown in Table 15.

According to the simulation results of the $f_1(x)$ function, the IHPSO algorithm is superior to the PSO algorithm in searching for single-peak convex functions. Compared with the PSO algorithm, the IHPSO algorithm has a stronger global searching ability for functions with local extrema such as $f_2(x)$ and $f_3(x)$. Therefore, the indexes of simulation results have been greatly improved. For functions such as $f_4(x)$, for which it is difficult to search for global extrema, the simulation results again verify the IHPSO search. It can be verified that the IHPSO algorithm proposed in this article substantially improves the performance of the algorithm.

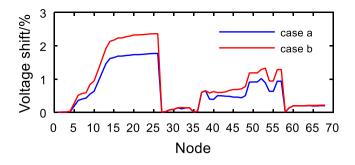


FIGURE 12 Maximum voltage shift of the PG&E-69 node system

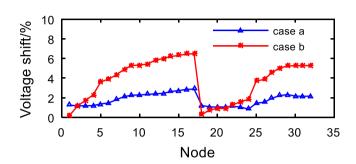


FIGURE 13 Maximum voltage shift of the regional 30-node system

Function	Dimension	Search scope	Theoretical optimum
f_1	10	[-100 100]	0
f_2	10	[-100 100]	0
f_3	10	[-100 100]	0
f_4	10	[-100 100]	0

TABLE 14 Function search parameters

Function	Algorithm	Best value	Worst value	Mean value
f_1	PSO	5.117e-20	3.017e-04	3.246e-06
	IHPSO	1.687e-20	1.660e-07	4.1975e-09
f_2	PSO	0.053	47.321	7.126
	IHPSO	7.310e-04	1.830e-01	2.316e-02
f_3	PSO	3.965e-04	469.222	29.459
	IHPSO	7.685e-05	18.008	3.242
f_4	PSO	0.995	46.763	15.900
	IHPSO	0.995	16.914	6.779

TABLE 15 Algorithm simulation results

Abbreviations: IHPSO, improved harmonic particle swarm optimisation; PSO, particle swarm optimisation.

6 | CONCLUSION

This article proposes a bi-level optimal allocation model for DG and EVCSs with consideration of the variability and stochasticity of the EV charging load, the DG output power and the conventional load. The model is solved by the IHPSO algorithm. Some conclusions can be summarised as follows:

1. Under the assumption that countries attach importance to the development of clean energy DG and EVs, compared to the independent planning of DG, the coordination and complementarity between the charging load and DG should be considered when optimising the allocation of DG, which is conducive to promoting the absorption of clean energy in the system.



- 2. The use of an active management strategy can result in more reasonable plans for optimal DG and EVCS allocation, which increases the capacity of DG and EVCSs over that the reliable system already in operation, increases the profit of the power supply company and reduces power loss while making better use of clean energy for emission reductions under the encouragement of the national energy policy.
- 3. Compared with the traditional PSO algorithm, the IHPSO algorithm established in this article has a strong global optimisation ability, does not easily fall into local optima, and results in improved performance of the algorithm.

ACKNOWLEDGMENTS

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LIST OF SYMBOLS AND ABBREVIATIONS

Abbreviations

DG distributed generation
DWG distributed wind generation

EVs electric vehicles

EVCSs electric vehicle charging station

IHPSO improved harmonic particle swarm optimisation

PVG photovoltaic generation

Variables and parameters

 $T_{\rm c}$ charging time in minutes

B percentage of batter capacity after charging SOC_0 percentage of battery capacity before charging

 η charging efficiency $P_{\rm c}$ charging power $E_{\rm b}$ battery capacity $P_{\rm PVG}$ output power of PV $P_{\rm PVGS}$ rated output power of PV $g/g_{\rm s}$ actual/rated solar irradiance

 $P_{
m DWG}$ wind output power $P_{
m DWGS}$ rated wind output power v actual wind speed $v_{
m i}/v_{
m o}$ cut-in/cut-off wind speed

v_s rated wind speed

 C_{pro} annual rate of return for the power supply company

 C_{loss} power loss

 $C_{\rm env}$ environmental and social welfare $C_{\rm s}$ profit of the power supply company

 C_{B} government subsidies for renewable energy sources

 C_{inv} investment in intermittent DG and EVCSs C_{OM} maintenance fee for DG and EVCSs

k number of typical scenarios

 p_l probability of the lth typical scenario

 c_i/c_o purchasing/selling prices for the power supply company

 $c_{
m e}$ unit selling price for EVCSs $P_{l,t,{
m L}}$ load demand at time interval t DWG output power at time interval t $P_{l,t,{
m DWG}}$ PVG active power at time interval t EVCS charging load at time interval t $c_{
m b,{
m DWG}}$ units of government subsidies for DWG $c_{
m b,{
m PVG}}$ units of government subsidies for PVG



 C_{inv} investment and building costs of DG and EVCSs

 n_{DWG} number of candidate nodes for DWG n_{PVG} number of candidate nodes for PVG n_{EV} number of candidate nodes for EVCSs $P_{i,\mathrm{DWG}}/P_{i,\mathrm{PVG}}/P_{i,\mathrm{EV}}$ capacity for DWG/PVG/EVCSs at node j

 $c_{t1}/c_{t2}/c_{t3}$ unit capacity construction costs of DWG/PVG/EVCSs

 $c_{\rm g}$ fixed investment cost of EVCSs

r discount rate

 n_1 service life of the equipment

 $c_{\text{om1}}/c_{\text{om2}}$ unit maintenance fees for DWG/PVG c_{om3} amortised unit maintenance fee for EVCSs

 $P_{l,t,loss}$ system loss at time interval t E_s output power for renewable energy

 $C_{\rm env}$ social welfare of renewable energy sources and reduced emissions from EVs

 $N_{\rm env}$ types of pollution gases

 $x_s/a_s/b_s$ emission levels of the sth kind of pollution gas e_{EV} energy consumed by an EV in 100 miles c_{CO_2} CO₂ trading tax fee in the international market

 c_{CO_2} CO₂ trading tax fee in the international market x_{EV} difference between EVs and conventional vehicles $c_{l,\text{S}}$ profit of the power supply company in scenario l

 $C_{l,B}$ government subsidy for renewable energy sources in scenario l

 $C_{l,OM}$ maintenance fee for DG and EVCSs in scenario l

 $C_{l, \mathrm{loss}}$ power loss fee in scenario l $C_{l, \mathrm{env}}$ social welfare in scenario l P_i/Q_i active/reactive power injections

 U_i/U_j voltages at nodes i and j G_{ij}/B_{ij} conductance and admittance θ_{ij} angle shift between i and j

 U_{imax}/U_{imin} upper/lower voltage bounds at node i

 S_{ij} transmission power $S_{ii\max}$ transmission power limit

 $U_{\rm OLTC}$ secondary voltage at the transformer

 $U_{
m OLTC}^{
m max}/U_{
m OLTC}^{
m min}$ upper/lower limits of secondary voltage at the transformer

 $P_{\text{cut}i}$ curtailment for DG at node i $P_{\text{cut}i}^{\text{max}}$ allowed curtailment at node i

 Q_{ci} reactive power compensation at node i

 Q_{ci}^{max} allowed upper limit of reactive power compensation at node i

 $x_{i,i}$ j-dimension of particle i

 $x_i^{\text{max}}/x_i^{\text{min}}$ upper and lower limit values of variable j

 $\chi_{i,j}$ sequences of chaotic variables generated by logistic mode 1

 λ chaotic parameters K number of clusters

S number of original scene samples

 ${\rm tr}\,(N_{\rm B})/{\rm tr}\,(N_{\rm W})$ traces of the interclass and intraclass scatter matrices

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