Heat capacities of iron disulfides Thermodynamics of marcasite from 5 to 700 K, pyrite from 300 to 780 K, and the transformation of marcasite to pyrite'

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(Received 26 March 1976)

The heat capacity of purified natural marcasite has been determined by adiabatic-shield calorimetry in the region 5 to 700 K where it transforms to pyrite exothermically. Values of thermodynamic functions at 298.15 K are C_p , $\{S^{\circ}(T) - S^{\circ}(0)\}$, and $\{H^{\circ}(T) - H^{\circ}(0)\}$ are 14.92 cal_{th} K⁻¹ mol⁻¹, 12.88 cal_{th} K⁻¹ mol⁻¹, and 2328 cal_{th} mol⁻¹, respectively, for marcasite (FeS_a). Our earlier measurements on pyrite have been extended to 770 K, and show that the heat capacity of marcasite is slightly higher than that of pyrite over the entire range of mutual existence. The transformation to pyrite is significantly exothermic at 700 K, $\Delta H_t = -(1.05 \pm 0.05) \text{ kcal}_{th} \text{ mol}^{-1}$, and correspondingly, $H^{\circ}(T = 0, \text{ marcasite}) - H^{\circ}(T = 0, \text{ pyrite}) = (0.99 \pm 0.05) \text{ kcal}_{th} \text{ mol}^{-1}$. Marcasite is thus metastable with regard to pyrite over the whole temperature region and owes its formation and persistence to kinetic factors. At 298.15 K the standard enthalpies, entropies, and Gibbs energies of formation for FeS_a phases are:

	Pyrite	Marcasite	
$\Delta H_{\rm f}^{\circ}/{\rm kcal_{th}} {\rm mol}^{-1}$	-41.5 ± 0.5	-40.5 ± 0.5	
$\Delta S_{\rm f}^{\circ}/{\rm cal_{th}} {\rm K}^{-1} {\rm mol}^{-1}$	$-9.0_7 \pm 0.1$	$-8.8_4\pm0.1$	
$\Delta G^{\circ}/\text{kcal}_{\text{th}} \text{ mol}^{-1}$	-38.8 ± 0.5	-37.9 ± 0.5	

1. Introduction

Iron disulfide occurs in nature (and can be prepared in the laboratory also) in two polymorphic forms, marcasite and pyrite. While a considerable amount of thermodynamic data exists for pyrite,^(1, 2) such data are virtually unknown for marcasite, except for some measurements of its enthalpy of combustion.⁽³⁻⁵⁾ In order to remedy this situation and to evaluate the stability conditions for the polymorphs, the heat capacity of marcasite has been determined from 5 K to the temperature region where

^a The research at the University of Michigan was supported initially by the Division of Research of the U.S. Atomic Energy Commission and more recently by the Chemical Thermodynamics Program of the Chemistry Section of the National Science Foundation.

it transforms to pyrite. Measurements on the previously studied pyrite sample⁽⁶⁾ have been extended to 770 K.

Pyrite is formed under widely varying conditions, while the formation of marcasite is subject to strict limitations. Hydrothermal laboratory experiments have shown⁽⁷⁻¹⁰⁾ that the formation of pyrite is favored at elevated temperatures in neutral or slightly basic solutions, while marcasite forms in colder, more acidic solutions. The results of Rickard⁽¹¹⁾ indicate that the formation of marcasite depends on the reaction between sulfur and a pre-existing iron sulfide, the tetragonal $Fe_{1+1}S^{(12)}$ (mackinawite). Marcasite has so far not been prepared by dry methods, and this prompted Kullerud⁽¹³⁾ to speculate that H-S bonds were of importance for its formation. Rickard⁽¹¹⁾ contends that water may be of importance in the formation of marcasite, but relates this to an enhanced formation reaction at temperatures where the marcasite-to-pyrite transformation is slow. In accordance with this, pyrite and marcasite are often found together both under laboratory conditions and in nature, as is commonly the case for monotropic polymorphic forms. It should also be noted that some natural crystals of the marcasite habit have, in fact, already undergone transformation to pyrite or do so on crushing.^(14, 15) While Wöhler⁽¹⁶⁾ was not able to observe marcasite transforming to pyrite or vice versa at 720 K, and both Cavazzi⁽³⁾ and Mixter⁽⁴⁾ reported that the enthalpy of combustion of marcasite is equal to that of pyrite, Allen et al.⁽⁷⁾ contended that marcasite transforms monotropically and exothermically to pyrite above 700 K. The inversion of marcasite has been studied by X-ray single crystal methods by Fleet.⁽¹⁷⁾ Experience with several samples indicated that the transformation was partially complete after heating for 12 h at 700 K and essentially complete within less than 4 h at 750 K. The irreversibility of this transformation has been noted by many investigators, but quantitative information about the instability of marcasite from heat-capacity and enthalpy-of-transformation measurements is obviously needed. Furthermore, the possibility of a limited stability range of marcasite at lower temperature as a consequence of subtle differences in vibrational properties should not be overlooked, although it seems a priori more reasonable that the heat capacity of marcasite be higher than that of structurally related pyrite due to the larger molar volume of the former.

Finally, the question of compositional differences between pyrite and marcasite needs to be considered. After an evaluation of the available analytical data by Buerger⁽¹⁸⁾ the composition $\text{FeS}_{1.985}$ was claimed for marcasite, while pyrite was judged to be stoichiometric. From decomposition-pressure measurements and magnetic results Juza and Biltz⁽¹⁹⁾ concluded that pyrite had a range of homogeneity from FeS₂ to FeS_{1.94}. In the absence of further confirmation the latter conclusion seems doubtful. A slight compositional difference between marcasite and pyrite might, however, well be present but has not been conclusively established.^(13, 20)

2. Experimental

SAMPLE

1040

The natural marcasite sample from near Carterville, Jasper County, Mo., consisted of crystal fragments of varying mass up to about 5 g. It was kindly supplied by Dr R. A. Robie of the U.S. Geological Survey.

Repeated chemical analyses of some crystal fragments by Laura Reichen gave (46.04 ± 0.1) mass per cent iron and (53.10 ± 0.1) mass per cent sulfur (theoretical 46.55 and 53.45 mass per cent, respectively). In addition, a trace of manganese and a small insoluble residue were noted. The iron to sulfur ratio is seen to be very closely stoichiometric (1/2.00). Semiquantitative spectrographic analyses by H. W. Worthing revealed mass percentages: Ag, 0.0007; Al, 0.005; Ba, 0.003; Ca, 0.0007; Cr, 0.00015; Cu, 0.015; Mn, 0.0001; Ni, 0.001; Pb, 0.2; Si, 0.01; Sn, 0.007. The following elements were not found: As, Au, B, Be, Bi, Cd, Ce, Co, Ga, Ge, Hf, Hg, In, K, La, Li, Mo, Na, Nb, P, Pd, Pt, Re, Sb, Sc, Ta, Te, Th, Ti, Tl, U, V, W, Y, Yb, Zn, Zr. Thus, the only significant concentration of trace metal detected was that of lead, probably present in the form of galena.

X-ray photographs and polished sections of different crystals used in the determinations showed the presence of the orthorhombic marcasite phase as the major component. The lattice constants, determined in an 11.46 cm diameter Straumanistype camera with iron radiation $[\lambda(\text{FeK}\alpha_1) = 193.597 \text{ pm}]$ are: $a = (444.4\pm0.1)$, $b = (542.5\pm0.1), c = (338.6\pm0.1)$ pm. They compare well with the recent results by Brostigen and Kjekshus:⁽²¹⁾ $a = (444.31\pm0.09), b = (542.45\pm0.09), c = (338.71\pm0.06)$ pm]. In addition, smaller amounts of pyrite were present. An estimate of the average amount was obtained by comparing X-ray powder photographs of small fragments from about 10 per cent of the crystals with those of prepared mixtures containing 5 and 10 per cent pyrite. The amount of pyrite in the sample was found on this basis to be (6.5 ± 2.5) per cent.

After heating to 770 K in the calorimeter, only pyrite-lines were found on the powder photographs and the lattice constant of the sample was $a = (540.6 \pm 0.1)$ pm.

The pyrite sample was the same as used in the low-temperature heat-capacity study by Grønvold and Westrum.⁽⁶⁾ It was from the Bosmo Mine, Nordland, Norway.

CALORIMETRIC TECHNIQUE

5 to 350 K, University of Michigan. The Mark II cryostat and adiabatic method employed have been described.⁽²²⁾ A gold-plated copper calorimeter (W-17) with a volume of 93 cm³ was used. Helium gas was added (76 Torr at 300 K) to improve thermal equilibration.[†] The calorimeter was surrounded by a shield system provided with automatic temperature control. Temperatures were measured with a capsule-type platinum resistance thermometer (A-3) located in a central well in the calorimeter.

300 to 700 K, University of Oslo. The calorimetric apparatus and measuring technique have been described.⁽²³⁾ The calorimeter was intermittently heated, and surrounded by electrically heated and electronically controlled adiabatic shields. The substance was enclosed in an evacuated and sealed quartz tube of about 50 cm³ volume, tightly fitted into the silver calorimeter. A central well in the tube served for the heater and platinum resistance thermometer.

Calibrations and adjustments. The platinum resistance thermometer for the lowtemperature calorimeter had been calibrated by the U.S. National Bureau of Stan-

† Throughout this paper Torr = (101.325/760) kPa; atm = 101.325 kPa; cal_{th} = 4.184 J.

1042 F. GRØNVOLD AND E. F. WESTRUM, JR.

dards, and that for the high-temperature calorimeter locally, at the ice, steam, and zinc points. Temperatures are judged to correspond to IPTS-68 within 0.02 K from 4 to 300 K, and within 0.05 K above this temperature. Energy inputs were measured with reference to instruments calibrated by the U.S. National Bureau of Standards.

The heat capacities of the empty calorimeters were determined in separate series of experiments. It represented from 45 to 80 per cent of the total for the low-temperature calorimeter, and about 54 per cent for marcasite and 50 per cent for pyrite for the high-temperature calorimeter.

Small corrections were applied for temperature excursions of the shields from the calorimeter temperature and for "zero drift" of the calorimeter temperature. Further small corrections were applied for differences in amounts of indium+tin solder, helium gas, and Apiezon-T grease for the low-temperature calorimeter and for differences in mass of the quartz containers for the high-temperature calorimeter. The mass of marcasite sample used was 130.833 g in the low-temperature calorimeter and 117.184 g in the high-temperature calorimeter, and the mass of pyrite used in the high-temperature calorimeter was 139.974 g.

3. Results and discussion

HEAT CAPACITIES AND THERMODYNAMIC PROPERTIES

The measured molar heat capacities for FeS₂ (marcasite) in the region 5 to 700 K and for pyrite in the region 330 to 770 K are presented in table 1. The temperature increments of the measurements can usually be deduced from the adjacent mean temperatures. When necessary, corrections have been applied for the finite temperature increments to obtain the limiting values of $\Delta H/\Delta T$. The measurements are considered to have a standard deviation of about 5 per cent at 5 K, 1 per cent at 10 K, and less than 0.1 per cent in the region 25 to 350 K for the low-temperature calorimeter and 0.3 per cent for the high-temperature calorimeter.

The heat capacity of marcasite is slightly higher than that of pyrite over its entire range of existence. This is shown as a difference plot in figure 1 over the region 5 to 350 K. The experimental heat capacities at higher temperatures are shown in figure 2.

Values of the heat capacity C_p , entropy $\{S^{\circ}(T) - S^{\circ}(0)\}$, enthalpy $\{H^{\circ}(T) - H^{\circ}(0)\}$, and function $-\{G^{\circ}(T) - H^{\circ}(0)\}/T$ are given for selected temperatures in table 2. They were obtained by appropriate computer evaluation of polynomials representing the heat capacity and extrapolation below 5 K for marcasite. Above 100 K the lowtemperature heat capacity is characterized by a precision of ± 0.2 per cent, and the thermodynamic functions of ± 0.15 per cent equal to twice the standard deviation. In the higher temperature region, the corresponding precision indices are 0.4 and 0.2, respectively.

Coughlin⁽²⁴⁾ measured the enthalpy of pyrite from 298 to 980 K. The tabulated enthalpy increments are 4.2 per cent higher than the present at 400 K, 1.8 per cent higher at 500 K, 0.4 per cent higher at 600 K, and 0.3 per cent lower at 700 K. For marcasite only a mean heat capacity from drop-calorimetric experiments from 373 K to room temperature has been reported by Neumann⁽²⁵⁾ (15.98 cal_{th} K⁻¹ mol⁻¹).

T	Cp	Т	C_p	T	C,	T	C_p
ĸ	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	ĸ	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	ĸ	calth K ⁻¹ mol ⁻¹	K	cal _{th} K ⁻¹ mol ⁻¹
		Fe	S2, Marcasite (Un	iversity	of Michigan)		
	Series I	7.64	0.0038	49.63	3 0.7331		Series V
121.38	6.548	8.56	0.0049	54.10	0.9500	227.58	3 12.951
130.28	3 7.312	9.52	0.0070	59.20) 1.243	235.94	13.251
137.84	7.931	10.54	0.0096	64.40	5 1.591	244.64	13.544
145.18	8 8.499	11.65	0.0106	69.95	5 1.984	253.54	13.814
152.37	7 9.028	12.88	0.0146	75.67	7 2.430	262.42	2 14.046
159.51	9.519	14.26	0.0190	80.72	2.866	271.02	. 14.282
167.06	5 10.010	15.79	0.0242	89.92	3.423	280.04	14.506
173.47	7 10.409	17.51	0.0320	93.18	3.985	289.13	14.721
182.79	10.939	19.43	0.0429	99.77	4.582	298.20) 14.914
191.63	11.398	21.56	0.0575	106.78	3 5.228	305.47	15.05
200.14	11.793	23.79	0.0771	114.32	2 5.915	315.37	1 15.27
208.41	12.180	26.14	0.1021	122.49	6.640	325.01	15.44
216.44	12.518	28.78	0.1353			334.42	2 15.60
224.48	3 12.832	31.68	0.1773		Series III	341.90	15.71
		34.20	0.2260	$\Delta H \mathrm{de}$	etn A	347.52	15.79
	Series II	37.87	0.3127			• • • • • • •	
6.06	5 0. 0025	41.88	0.4301		Series IV		
7.02	2 0.0027	45.81	0.5708	$\Delta H d$	etn B		
				T			
			res ₂ , marcasite (Univers	ity of Usio)		
	Series I	429.43	16.79	557.77	7 17.57	651.67	7 18.12
314.46	5 15.25	440.79	16.90	570.08	3 17.63	663.73	18.20
326.20) 15.44	452.27	16 .99	582.29	9 17.76	675.80) 18.24
337.97	15.62	463.85	17 .0 7	594.48	3 17.79	687.92	18.34
349.72	2. 15.79	475.45	17.16	606.45	5 17.87	700.19	17.78
361.08	3 16.07	487.07	17.26	618.48	3 17.90	ΔH de	tn
372.72	2 16.22	498.74	17.33	630.56	5 17.93	736.32	18.34
384.08	3 16.38	510.44	17.44	642.68	3 18.05	748.73	18.50
395.42	2 16.45	522.14	17.47			761.09	18.49
406.76	5 16.65	533.86	17.52		Series II	773.44	18.58
418.09	16.72	545.70	17.55	639.61	l 18.00		
FeS ₂ , Pyrite (University of Oslo)							
	Series I	464.47	17.03	604.70) 17.77	749.80	18 40
337.88	15.56	475.09	17.03	615.67	17.82	761 71	18 44
348.55	5 15.74	485.76	17.12	626.68	17.85	773 56	18.51
359.18	15.92	496.47	17.20	637.73	17.92	//0.00	10.51
369.77	16.07	507.22	17.23	648.82	17.95		Series II
380.32	2 16.21	517.97	17.30	659.94	18.01	300.38	14.93
390.84	16.34	528.73	17.38	671.08	18.14	311.19	15 19
401.3	16.47	539.50	17.45	682.24	18.20	321.94	15.32
411.84	16.61	550.30	17.51	693 44	5 18.18	332 64	15 53
422.33	16.70	561 11	17.53	704 7	18 71	343 30	15.60
432.82	2 16.87	571 04	17.63	716.04	18 27	5-5.30	15.07
443 33	16.91	582.84	17 70	727 22	1832		
453.88	16.96	593 75	17 76	738 19	18.37		
	10.20	575.75	11110	/20.10	. 10.57		

TABLE 1. Heat capacities of marcasite and pyrite $[M(\text{FeS}_2) = 119.98 \text{ g mol}^{-1}; \text{ cal}_{\text{th}} = 4.184 \text{ J}]$



FIGURE 1. Deviation of the low-temperature heat capacity of marcasite (\bigcirc) from the smoothed values for pyrite. The dashed line indicates 0.1 per cent deviation.



FIGURE 2. Heat capacities of marcasite (\bullet) and pyrite (\bigcirc) at higher temperatures.

HEAT CAPACITIES OF MARCASITE AND PYRITE

TABLE 2.	Thermodynamic	properties of	marcasite and	pyrite

K Calla K $^{-1}$ mol $^{-1}$ Calla M C $^{-1}$ mol $^{-1}$ Calla M C $^{-1}$ mol $^{-1}$ Marcasite 5 (0.0016) (0.0005) (0.002) (0.0001) 10 0.0072 0.0030 0.022 0.0099 15 0.0213 0.0083 0.089 0.0024 20 0.0470 0.0176 0.254 0.0049 25 0.0885 0.0322 0.3555 0.0088 30 0.1517 0.0536 1.175 0.0144 35 0.2438 0.0834 2.150 0.0220 40 0.3714 0.1239 3.672 0.0321 45 0.3391 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.06615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 35.51 0.1690 80 2.805 0.3940 59.39 0.2516 90 3.696 1.376 <th>$\frac{T}{T}$</th> <th><i>C</i>,</th> <th>$\frac{\{S^{\circ}(T) - S^{\circ}(0)\}}{1 + 1 + 1 + 1 + 1 + 1}$</th> <th>$\{H^{\circ}(T) - H^{\circ}(0)\}$</th> <th>$- {G^{\circ}(T) - H^{\circ}(0)}/T$</th>	$\frac{T}{T}$	<i>C</i> ,	$\frac{\{S^{\circ}(T) - S^{\circ}(0)\}}{1 + 1 + 1 + 1 + 1 + 1}$	$\{H^{\circ}(T) - H^{\circ}(0)\}$	$- {G^{\circ}(T) - H^{\circ}(0)}/T$
Marcasite 5 (0.0016) (0.0005) (0.002) (0.0009) 10 0.0072 0.0030 0.022 0.0009 20 0.0470 0.0176 0.254 0.0049 25 0.0885 0.0322 0.585 0.0020 30 0.1517 0.0356 1.175 0.0144 35 0.2438 0.0834 2.150 0.0220 40 0.3714 0.1239 3.672 0.0321 45 0.3391 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 3.5.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1	ĸ	calth K ⁻ mol ⁻	calth K ⁻¹ mol ⁻¹	calth mol-1	$\operatorname{cal}_{\operatorname{th}} \mathbb{K}^{-1} \operatorname{mol}^{-1}$
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30 0.1517 0.0536 1.175 0.0144 35 0.2438 0.0834 2.150 0.0220 40 0.3714 0.1239 3.672 0.0321 45 0.5391 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1663 70 1.988 0.6764 35.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 685.0 1.798 180 10.78 6.309 824.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.09 10.897 177.8 4.067 270 </td <td>25</td> <td>0.0885</td> <td>0.0322</td> <td>0.585</td> <td>0.0088</td>	25	0.0885	0.0322	0.585	0.0088
35 0.2438 0.0834 2.150 0.0220 40 0.3714 0.1239 3.672 0.0321 45 0.5391 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 35.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.788 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.267 8.668 1241.3 3.0026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.49 10.897 1775.8 4.067 270 <	30	0.1517	0.0536	1.175	0.0144
40 0.3714 0.1239 3.672 0.0321 45 0.5391 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 35.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 </td <td>35</td> <td>0.2438</td> <td>0.0834</td> <td>2.150</td> <td>0.0220</td>	35	0.2438	0.0834	2.150	0.0220
45 0.3591 0.1769 5.931 0.0451 50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 35.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.772 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 </td <td>40</td> <td>0.3714</td> <td>0.1239</td> <td>3.672</td> <td>0.0321</td>	40	0.3714	0.1239	3.672	0.0321
50 0.7492 0.2442 9.134 0.0615 60 1.294 0.4265 19.21 0.1063 70 1.988 0.6764 35.51 0.1690 80 2.805 0.9940 59.39 0.2516 90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.772 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 80.66 2.273 200 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 17.33 15.346 12.67	45	0.5391	0.1769	5.931	0.0451
601.2940.426519.210.1063701.9880.676435.510.1690802.8050.994059.390.2516903.6961.37691.870.35471004.6121.812133.40.47821105.5292.295184.10.62111206.4242.815243.90.78201307.2823.363312.50.95931408.0933.933389.41.1511508.8514.517474.11.3561609.5525.111566.21.57217010.205.710665.01.78818010.786.309824.62.23519011.326.907880.62.27320011.817.501996.32.51921012.268.0881116.72.77122012.678.6681241.33.02623013.049.2391369.93.28324013.389.8011502.03.54325013.6910.3541637.43.80525013.9910.8971775.84.06727014.2611.4301917.24.330273.1514.3411.6019624.41328014.5111.9532060.94.59329013.6910.3541637.43.80529014.7412.4662207.24.855	50	0.7492	0.2442	9.134	0.0615
701.9880.676435.510.1690802.8050.994059.390.2516903.6961.37691.870.35471004.6121.812133.40.47821105.5292.295184.10.62111206.4242.815243.90.78201307.2823.363312.50.95931408.0933.933389.41.1511508.8514.517474.11.3561609.5525.111566.21.57217010.205.710665.01.79818010.786.309824.62.15219011.326.907880.62.27320011.817.501996.32.51921012.268.0881116.72.77122012.678.6681241.33.02623013.6910.3541637.43.80526013.9910.8971775.84.06727014.2611.4301917.24.330273.1514.3411.6019624.41328014.5111.9532060.94.593298.1514.9212.8823285.06930014.7412.4662207.24.855298.1514.9212.8823285.06930014.7412.4663126.86.41245015.8315.3463126.86.412<	60	1.294	0.4265	19.21	0.1063
802.8050.994059.390.2516903.6961.37691.870.33471004.6121.812133.40.47821105.5292.295184.10.62111206.4242.815243.90.78201307.2823.363312.50.95931408.0933.933389.41.1511508.8514.517474.11.3561609.5525.111566.21.57217010.205.710665.01.79818010.786.309824.62.15219011.326.907880.62.27320011.817.501996.32.51921012.268.0881116.72.77122013.049.2391369.93.28324013.389.8011502.03.54325013.6910.3541637.43.80526013.9910.8971775.84.06727014.2611.4301917.24.330273.1514.3411.6019624.41328014.5111.9532060.94.59328014.5111.9532060.94.59328014.5111.9532060.94.59328014.5111.9532060.94.59328014.5315.3463126.86.41240016.5217.5123937.47.668<	70	1.988	0.6764	35.51	0.1690
90 3.696 1.376 91.87 0.3547 100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9993 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.006 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 450 16.59 19.4499 7392.1 1.128 600 17.33 21.296 563	80	2.805	0.9940	59.39	0.2516
100 4.612 1.812 133.4 0.4782 110 5.529 2.295 184.1 0.6211 120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 80.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500	90	3.696	1.376	91.87	0.3547
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	100	4.612	1.812	133.4	0.4782
120 6.424 2.815 243.9 0.7820 130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 47	110	5,529	2.295	184.1	0.6211
130 7.282 3.363 312.5 0.9593 140 8.093 3.933 389.4 1.151 150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.33 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.81 24.499 <td< td=""><td>120</td><td>6.424</td><td>2.815</td><td>243.9</td><td>0.7820</td></td<>	120	6.424	2.815	243.9	0.7820
1408.0933.933389.41.151150 8.851 4.517 474.1 1.356 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 397.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.81 24.499 7392.1	130	7.282	3.363	312.5	0.9593
150 8.851 4.517 474.1 1.336 160 9.552 5.111 566.2 1.572 170 10.20 5.710 665.0 1.798 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 500 17.38 22.935 6807.4 11.128 <tr<< td=""><td>140</td><td>8.093</td><td>3.933</td><td>389.4</td><td>1.151</td></tr<<>	140	8.093	3.933	389.4	1.151
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	150	8.851	4.517	474.1	1.356
170 10.20 5.711 50.2 1.372 180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142 <td>160</td> <td>9 552</td> <td>5 111</td> <td>566 7</td> <td>1 577</td>	160	9 552	5 111	566 7	1 577
180 10.78 6.309 824.6 2.152 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.81 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	170	10.20	5.710	665.0	1.372
130 16.76 0.305 0.273 2.132 190 11.32 6.907 880.6 2.273 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 397.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	180	10.20	6 309	824.6	2 152
17.00 11.32 0.501 996.3 2.213 200 11.81 7.501 996.3 2.519 210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	190	11 32	6 907	820.6	2.132
21011.0111.0111.0111.0111.01210 12.26 8.081 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	200	11.81	7.501	996 3	2.273
210 12.26 8.088 1116.7 2.771 220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142		10.00			2.517
220 12.67 8.668 1241.3 3.026 230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	210	12.26	8.088	1116.7	2.771
230 13.04 9.239 1369.9 3.283 240 13.38 9.801 1502.0 3.543 250 13.69 10.354 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	220	12.67	8.668	1241.3	3.026
24013.389.8011502.03.543 250 13.6910.3541637.43.805 260 13.9910.8971775.84.067 270 14.2611.4301917.24.330 273.15 14.3411.6019624.413 280 14.5111.9532060.94.593 290 14.7412.4662207.24.855 298.15 14.9212.8823285.069 300 14.9612.9702355.75.118 350 15.8315.3463126.86.412 400 16.5217.5123937.47.668 450 16.9919.4874775.98.874 500 17.3321.2965634.510.027 550 17.5822.9596507.411.128 600 17.8124.4997392.112.179 650 18.0925.9358289.213.182 700 18.4027.2879201.614.142	230	13.04	9.239	1369.9	3.283
250 13.69 10.334 1637.4 3.805 260 13.99 10.897 1775.8 4.067 270 14.26 11.430 1917.2 4.330 273.15 14.34 11.60 1962 4.413 280 14.51 11.953 2060.9 4.593 290 14.74 12.466 2207.2 4.855 298.15 14.92 12.88 2328 5.069 300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	240	13.38	9.801	1502.0	3.543
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	230	13.69	10.354	1637.4	3.805
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	260	13.99	10.897	1775.8	4.067
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	270	14.26	11.430	1917.2	4.330
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	273.15	14.34	11.60	1962	4.413
29014.7412.466 2207.2 4.855 298.15 14.9212.88 2328 5.069 300 14.9612.970 2355.7 5.118 350 15.8315.346 3126.8 6.412 400 16.5217.512 3937.4 7.668 450 16.9919.487 4775.9 8.874 500 17.3321.296 5634.5 10.027 550 17.5822.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.0925.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	280	14.51	11.953	2060.9	4.593
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	290	14.74	12.466	2207.2	4.855
300 14.96 12.970 2355.7 5.118 350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	298.15	14.92	12.88	2328	5.069
350 15.83 15.346 3126.8 6.412 400 16.52 17.512 3937.4 7.668 450 16.99 19.487 4775.9 8.874 500 17.33 21.296 5634.5 10.027 550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	300	14.96	12.970	2355.7	5.118
40016.5217.5123937.47.66845016.9919.4874775.98.87450017.3321.2965634.510.02755017.5822.9596507.411.12860017.8124.4997392.112.17965018.0925.9358289.213.18270018.4027.2879201.614.142	350	15.83	15.346	3126.8	6.412
45016.9919.4874775.98.87450017.3321.2965634.510.02755017.5822.9596507.411.12860017.8124.4997392.112.17965018.0925.9358289.213.18270018.4027.2879201.614.142	400	16.52	17.512	3937.4	7.668
50017.3321.2965634.510.02755017.5822.9596507.411.12860017.8124.4997392.112.17965018.0925.9358289.213.18270018.4027.2879201.614.142	450	16.99	19.487	4775.9	8.874
550 17.58 22.959 6507.4 11.128 600 17.81 24.499 7392.1 12.179 650 18.09 25.935 8289.2 13.182 700 18.40 27.287 9201.6 14.142	500	17.33	21.296	5634.5	10.027
60017.8124.4997392.112.17965018.0925.9358289.213.18270018.4027.2879201.614.142	550	17.58	22,959	6507.4	11.128
65018.0925.9358289.213.18270018.4027.2879201.614.142	600	17.81	24.499	7392.1	12.179
700 18.40 27.287 9201.6 14.142	650	18.09	25.935	8289.2	13.182
	700	18.40	27.287	9201.6	14.142

 $(cal_{th} = 4.184 \text{ J})$

F. GRØNVOLD AND E. F. WESTRUM, JR.

\underline{T}	<i>C</i> _p	$\{\underline{S^{\circ}(T)-S^{\circ}(0)}\}$	$\{H^{\circ}(T)-H^{\circ}(0)\}$	$- \{G^{\circ}(T) - H^{\circ}(0)\}/T$
K	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	cal_{th} mol ⁻¹	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$
		Pyrite		
10	0.0056	0.0018	0.0139	0.0004
25	0.0735	0.0239	0.4406	0.0062
50	0.6705	0.2057	7.820	0.0493
100	4.471	1.693	126.1	0.4324
200	11.72	7.300	977.3	2.413
273.15	14.28	11.37	1937	4.277
298.15	14.86	12.65	2302	4.926
300	14.90	12.740	2329.7	4.974
350	15.66	15.111	3097.3	6.255
400	16.45	17.264	2905.2	7.501
450	16.91	19.230	4740.1	8.697
500	17.24	21.030	5594.2	9.842
550	17.49	22.685	6462.6	10.935
600	17.74	24.218	7343.4	11.979
650	18.00	25.648	8236.7	12.976
700	18.24	26.990	9142.7	13.929
750	18.42	28.255	10059.3	14.843
780	18.51	28,979	10613.2	15.373

TABLE 2-continued

THE MARCASITE-TO-PYRITE TRANSFORMATION

The higher-temperature heat-capacity measurements on marcasite were quite normal until the sixth energy input of Series II produced a somewhat higher temperature increment and brought the temperature up to 706.43 K. Here the drift-rate gradually changed from a slightly negative value of about -0.0009 K min⁻¹ to large positive values after a period of 2 h. The subsequent gradual temperature increase was followed for a further 96 h, figure 3, at which time the temperature was estimated to be not more than (0.15 ± 0.25) K from the limiting value, T_{∞} . The enthalpy of transformation (including -8.3 cal_{th} mol⁻¹ from Series II, run 6) was (-979 ± 25) cal_{th} mol⁻¹ for the sample which contained (6.5 ± 2.5) per cent of pyrite. Hence, the enthalpy of transformation of marcasite to pyrite at 700 K is $\Delta H_t = (-1050\pm50)$ cal_{th} mol⁻¹.

When the heat-capacity measurements were continued after 96 h a slight positive drift was noted due to the transformation of the remaining amount of marcasite, but this decay was not studied further. The heat capacity corresponded closely to that of pyrite, and X-ray powder photographs taken of the sample after completion of the measurements showed the presence of pyrite only.

The heat capacity of the pyrite sample increased gradually over the temperature range 350 to 770 K without any sign of transformation. The values were 0.5 to 1.0 per cent lower than for marcasite at the corresponding temperature. They joined very well with the low-temperature measurements. In the absence of a zero-point entropy in this system, marcasite even in the vicinity of the transformation temperature is



FIGURE 3. Equilibration times τ for the marcasite-to-pyrite transformation.

thermodynamically metastable with respect to pyrite; hence the transformation is monotropic and irreversible. Consequently, we cannot ascribe an entropy increment to the transformation and instead utilize an enthalpy cycle for the marcasite-pyrite system through T = 0. Taking into account the enthalpy increment for the marcasite to pyrite transformation at 700 K, the $\{H^{\circ}(T = 0, \text{ marcasite}) - H^{\circ}(T = 0, \text{ pyrite})\}$ is found to be (0.99 ± 0.05) kcal_{th} mol⁻¹. This value should, therefore be incorporated into $\{G^{\circ}(T) - H^{\circ}(0)\}/T$ for marcasite for chemical thermodynamic calculations. Moreover, marcasite is seen to be clearly metastable with respect to pyrite above T = 0. For example, at 298.15 K the value of $\Delta G^{\circ}(\text{marcasite} \rightarrow \text{pyrite})$ is (-0.95 ± 0.05) kcal_{th} mol⁻¹.

Our results together with the critically evaluated values of $\Delta H_f^{\circ}(\text{pyrite})$ from Mills's⁽¹⁾ and from Robie and Waldbaum's⁽²⁾ reviews together with entropies for iron⁽²⁶⁾ and sulfur⁽²⁶⁾ yield the following standard enthalpies, entropies, and Gibbs energies of formation for FeS₂ at 298.15 K:

	Pyrite	Marcasite
$\Delta H_{\rm f}^{\circ}/{\rm kcal_{th}} {\rm mol}^{-1}$	-41.5 ± 0.5	-40.5 ± 0.5
$\Delta S_{\rm f}^{\circ}/{\rm cal_{th}}{\rm K}^{-1}{\rm mol}^{-1}$	$-9.0_7 \pm 0.1$	$-8.8_{4}\pm0.1$
$\Delta G_{\rm f}^{\circ}/{\rm kcal_{th}} {\rm K}^{-1} {\rm mol}^{-1}$	-38.8 ± 0.5	-37.9 ± 0.5

Hence, the geological occurrence of pyrite pseudomorphs after marcasite is consistent with above interpretation, since marcasite presumably occurs in low-temperature hydrothermal deposits and apparently occasionally transforms at temperatures well below 700 K to pyrite.

We appreciate the support provided by the Atomic Energy Commission and the National Science Foundation, the provision of the marcasite sample and analysis by Dr Richard Robie. We thank Bjørn Lyng Nielsen for assistance with the hightemperature measurements. 1048

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