# Simulation of gain-switched picosecond pulse generation from quantum well lasers

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Circuit models for gain-switched quantum well laser diodes are developed and simulated using the circuit analysis program SPICE2. Effects of cavity length and number of wells on the output pulse shape are analysed. Picosecond pulses of 7 and 2 ps full-width at half-maximum (FWHM) are observed, corresponding to second and third quantized level transitions, respectively. A remarkable reduction in the output pulse width observed for the third quantized level transition, demonstrates the significance of higher sub-band transitions for ultrashort pulse generation.

## 1. Introduction

Picosecond pulse generation in multiple quantum well (QW) semiconductor lasers using the gain switching (GS) technique is gaining popularity, because enhanced differential gain in these lasers is effective for obtaining ultrashort pulses. So far, the gain switching characteristics of QW lasers have been investigated either experimentally or theoretically by the numerical solution of rate equations [1–4]. However, these methods suffer from the limitations of non-inclusion of substrate parasitics, package parasitics and device circuit interactions in the calculations. An alternate approach that overcomes these limitations is to transform the rate equations into a circuit model that can then be solved using standard circuit analysis techniques. In this paper, we have developed circuit models corresponding to multiple quantized state transitions (QST) for the generation of picosecond optical pulses in QW lasers. The model was simulated using the circuit simulation program SPICE2, and the effects of cavity length, L, and number of wells,  $N_{\rm w}$ , on the output pulse shape, for various injection, I, current levels, were investigated.

# 2. Discussion

The optical gain function of single QW lasers shows a step-like behaviour in the transition

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TABLE | List of principal symbols and element values for the gain-switched model

Symbol	Definition	Value
c	Speed of light in vacuum	
$c_{g}$	Speed of light in the lasing medium	
$C_{\mathrm{D}}$	Capacitance, diffusion (pf)	10.0000
$C_{p}$	Capacitance, photon (pf)	0.0672
$C_{\rm p}$ $C_{\rm pp}$ $E_0$	Capacitance, package parasitics (pf)	0.2300
$E_0$	Permittivity, free space	
$f_{ m c}$	Fermi distribution function, conduction band	
$f_{ m v}$	Fermi distribution function, valance band	
$g_{m1,2}$	Optical gain	
h	Planck's constant	
I	Injection current	
K	Boltzmann constant	
$L_{ m pp}$	Inductance, package parasitics (nh)	0.63
$L_{\rm z}$	Active layer thickness (nm)	10
$m_{\rm c}^*$	Effective mass, conductive band $(m_e)$	0.067
$m_{\rm e}$	Electron mass	
$m_{\rm r}$		
$m_{\rm v}^*$	Effective mass, valence band $(m_e)$	0.450
n	Carrier density	
P	Photon density	
q	Electron charge	
$R_{\rm IN}$	Resistance, pulse generator $(\Omega)$	100,000
$R_{\rm p}$	Resistance, photon $(\Omega)$	21.182
$R_{\rm pp}$	Resistance, package parasitics ( $\Omega$ )	1.000
t T	Temperature (K)	300
$\widetilde{V}_{ m a}$	Volume, active region	500
W	Laser width $(\mu m)$	20
Q	Contangous amission coefficient	$2 \times 10^{-4}$
$rac{eta}{\Gamma}$	Spontaneous emission coefficient	0.03
$\mathcal{E}$	Optical confinement factor	$4 \times 10^{-23}$
_	Gain compression factor (m³) Refractive index	
$_{-}^{\mu}$		3.55
$ au_{ m n}$	Carrier lifetime (ns)	3
$ au_{ m p}$	Photon lifetime	
$\omega$	Radian frequency	

regime between n=1 and n=2 quantized state [5]. Therefore, the differential gain, dg/dn, that is responsible for the generation of short optical pulses, depends strongly on the operation conditions. The value of dg/dn can be higher by a factor of two for n=2, in comparison to n=1 sub-band transitions [6]. To model the gain switching process, including the effect of n=1 and n=2 quantized level interactions, we used a two-mode rate equation for the photon densities [3], given by:

$$\frac{\mathrm{d}P_i}{\mathrm{d}t} = \Gamma c_{\mathrm{g}} g_{\mathrm{m}i} (1 - \mathcal{E}P_i) P_i - \frac{P_i}{\tau_{\mathrm{p}}} + \beta_i \frac{n}{\tau_{\mathrm{p}}} \tag{1}$$

$$\frac{\mathrm{d}n}{\mathrm{d}t} = \frac{I}{qV_{\mathrm{a}}} - c_{\mathrm{g}} \sum g_{\mathrm{m}i} (1 - \mathcal{E}P_{i}) P_{i} - \frac{n}{\tau_{\mathrm{n}}}$$
 (2)

where i = 1, 2, and the remaining terms are defined in Table I. Following the methodology described in [7], the above equations were transformed into the equivalent circuit shown in

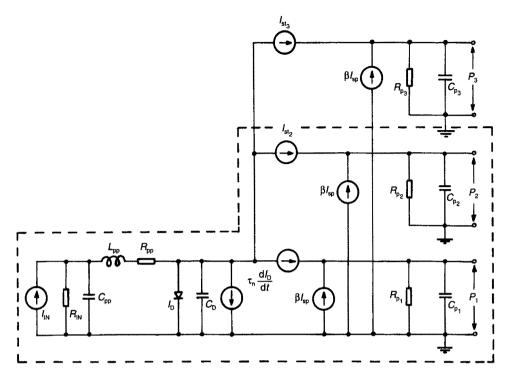


Figure 1 Circuit model representing the multiple quantized level in a QW laser diode.  $P_1$ ,  $P_2$  and  $P_3$  are the output nodes for the n = 1, 2 and 3 levels, respectively.

Fig. 1 (enclosed within dashed lines): where the diode models the spontaneous recombination current; while the current generator, proportional to the time derivative of the spontaneous injection current, models the charge storage effects in the active layer. The diffusion capacitance is represented by  $C_D$  and the current component  $I_{sp} = I_D$  represents the spontaneous emission.  $I_{\text{stim}}$  represents a polynomial current-controlled current source. Photon loss and storage are modelled by resistance,  $R_{\rm p}$ , and capacitance,  $C_{\rm p}$ , respectively. Figure 1, combined with package parasitics (where  $R_{\rm IN}$  represents the resistance of the pulse generator;  $L_{\rm pp}$ , the inductance;  $R_{pp}$ , small loss resistance; and  $C_{pp}$ , capacitance), is associated with the laser package [8, 9]. Each branch of the optical section corresponds to a quantized transition level in a QW laser. The spontaneous emission coefficient,  $\beta_l$ , is assumed to be a constant and the current generators,  $I_{st}$ . and Ist, are dependent on the gain. This gain is non-linear and is represented as a current source in the circuit model. Hence, the two branches of the optical section (for i = 1 and 2), that correspond to the n=1 and 2 quantized state transitions, respectively, differ only in the differential gain coefficients. The model corresponds to a QW laser with an active layer thickness, L<sub>2</sub>, of 10.0 nm, and it is validated by simulating the response to a direct current (d.c.) sweep as shown in Fig. 2. The input pulse amplitude is varied and simulations are performed. For a single QW laser (number of wells,  $N_{\rm w}=1$ ) with cavity length  $L=160\,\mu{\rm m}$ , the result demonstrates that the laser emits only in the n=1 quantized state at low injection levels (equivalently, I<0.5 A), as shown in Fig. 3. Gain-switched picosecond pulses were observed when the input pulse amplitude was increased to I = 0.5 A (Fig. 4a). By reducing L to  $140 \,\mu\text{m}$ , the critical amplitude of the input pulse required to achieve gain switching (Fig. 4b) is reduced to I = 0.25 A. Similar effects were observed in the case of a multiple QW laser. The dependency of the second level transition

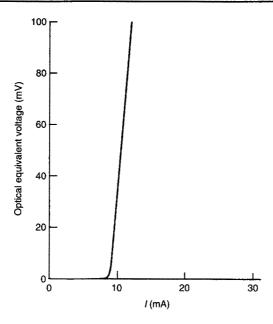


Figure 2 The d.c. L-I characteristics of a QW laser.

on the number of wells was determined by modifying the circuit model to represent a QW laser with two wells ( $N_{\rm w}=2$ ). The results of the simulation are shown in Fig. 5. Gain-switched pulses were observed at I=1 A and 0.5 A for L=80 and 70  $\mu$ m, respectively. Comparison of Figs 4 and 5 shows that gain switching is achieved at a lower value of input pulse amplitude in the case of a single QW laser. The above results, that indicate the importance of cavity length and number of wells, respectively, for observation of ultrashort pulses, are in excellent agreement with those obtained by other methods [1].

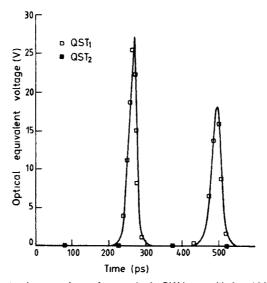


Figure 3 Simulated output pulse waveforms from a single QW laser with L = 160 μm: (□) QST1, (■) QST2.

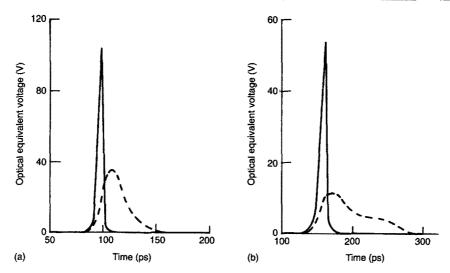


Figure 4 Output pulse waveforms from a gain-switched single QW laser with cavity length, L: (a) 160  $\mu$ m and (b) 140  $\mu$ m. (- - -) QST1, (----) QST2.

Further, the above model was simulated to study the effect of bias current on the output pulses. Figure 6 shows the total output corresponding to QST1 and QST2 for various bias currents. As the bias level increases, the pulse width decreases due to the increased domination of the QST2 transition, which gives an inherently sharper peak due to its higher differential gain.

It has been predicted that pulses generated due to higher-level transitions (n > 2) are particularly attractive for high-speed applications. Our calculations show that lasers with  $L_z$  below 10 nm lase at the second quantized state; whereas for  $L_z$  in excess of about 14.5 nm, the effect of the third quantized state transition (QST3) is observed. The gain-carrier density relationship for this level (for an AlGaAs laser with Al mole fraction x = 0.25) is shown in Fig. 7a. The

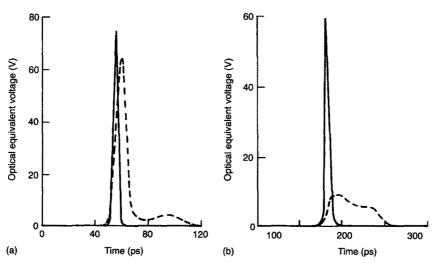


Figure 5 Simulated pulse waveform from a gain-switched multiple QW laser with  $N_{\rm w}=2$ . L: (a) 80  $\mu$ m and (b) 70  $\mu$ m. (---) QST1, (----) QST2.

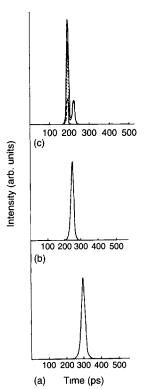


Figure 6 Simulated total optical output from a QW laser diode operating at two quantized levels, QST1 (---) and QST2 (----), at  $I_{\text{bias}}$ : (a) 0.1, (b) 0.4, and (c) 0.8  $I_{\text{TH}}$ .

gain-carrier density relationship is determined for the n=1 transition by considering the gain expression [10-12]:

$$g_{\rm m1} = K[f_{\rm c}(E_{f_{\rm c}}, E_{\rm c_1}) - f_{\rm v}(E_{f_{\rm v}}, E_{\rm v_1})]$$
(3)

where  $K = 4\pi q^2 m_{\rm r}/E_0 m_{\rm e}^2 c\mu h L_{\rm z} E_{\rm p}$ .  $|M_{\rm b}|^2$  is independent of carrier density and the quantity  $|M_{\rm b}|^2 = 1.3 \, m_{\rm c} E_{\rm q}$  is the momentum matrix element of transition between the band edges.  $f_{\rm c} (E_{f_{\rm c}}, E_{\rm c})$  and  $f_{\rm v} (E_{f_{\rm v}}, E_{\rm v})$  are the Fermi distribution functions in conduction and valence bands, respectively; and  $E_{\rm c}$  and  $E_{\rm v}$  are given as:

$$E_{\rm c} = \frac{m_{\rm r}}{m_{\rm c}^*} (E_{\rm p} - E_{\rm g}) \tag{4}$$

$$E_{\rm v} = \frac{m_{\rm r}}{m_{\rm v}^*} (E_{\rm p} - E_{\rm g}) \tag{5}$$

$$m_{\rm r} = \frac{m_{\rm c}^* m_{\rm v}^*}{(m_{\rm c}^* + m_{\rm v}^*)} \tag{6}$$

$$E_{\rm p} = h\omega \tag{7}$$

Considering the lowest-order quantum transition, the electron density in the QW is obtained from [13]:

$$n = \frac{m_{\rm c}^* KT}{\pi h^2 L_{\rm z}} \ln \left[ 1 + \exp\left(\frac{E_{f_{\rm c}} - E_{c_{\rm i}}}{KT}\right) \right]$$
 (8)

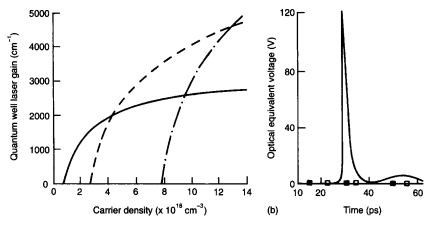


Figure 7 (a) Variation of gain with carrier density for various quantized levels. n: (——) 1, (– –) 2, (· – ·) 3. (b) Observation of gain-switched picosecond pulse due to the third quantized level transition. Cavity length,  $L = 140 \,\mu\text{m}$ . FWHM = 2 ps. ( $\Box$ ) QST1, ( $\blacksquare$ ) QST2.

Using Equation 8 for carrier density,  $f_c - f_v$  can be expressed as:

$$f_{c} - f_{v} = 1 - \exp\{-(n/D1)\} - \exp\{-(n/D2)\}$$
(9)

where D1 and D2 are constants given by:

$$D1 = \frac{4\pi m_{\rm c}^* KT}{h^2 L_{\rm z}} \tag{10}$$

$$D2 = \frac{4\pi m_{\rm v}^* KT}{h^2 L_{\rm z}} \tag{11}$$

substituting Equation 9 into Equation 3, the gain for the n = 1 transition can be written as:

$$g_{m1} = K[1 - \exp\{-(n/D1)\} - \exp\{-(n/D2)\}]$$
 (12)

As the density of the states in the second quantized level transition is double that of the n = 1 transition [14], the expression for optical gain for n = 2 can be written as:

$$g_{\rm m2} = 2K[f_{\rm c}(E_{f_{\rm c}}, E_{\rm c_2}) - f_{\rm v}(E_{f_{\rm v}}, E_{\rm v_2})] \tag{13}$$

where  $E_{c_2}$  and  $E_{v_2}$  are the energy levels of the second conduction and valence sub-band, respectively; and  $f_c$  and  $f_v$  are Fermi distribution functions, that can be expressed as a function of carrier concentrations for the second quantized level transition in the following manner [15]:

$$N = D1\{\ln[1 + \exp(E_{f_c} - E_{c_1})/KT] + \ln[1 + \exp(E_{f_c} - E_{c_2})/KT]\}$$
 (14)

where D1 is a constant as defined in Equation 10.  $E_{c_1}$  and  $E_{c_2}$  are confinement energies for n=1 and n=2 transitions, respectively.  $E_{f_c}$  is related to the density of electrons injected into the well. The expression for  $f_c(E_{f_c}, E_{c_r})$  is given by:

$$f_{c} = \{1 + \exp[(E_{c_2} - E_{f_c})/KT]\}^{-1}$$
 (15)

Using Equations 14 and 15,  $f_c$  can be written as:

$$f_{\rm c} = \frac{[(x-1)^2 + 4xy]^{1/2} - (x+1)}{[(x-1)^2 + 4xy]^{1/2} + (x-1)}$$
(16)

where  $x = \exp(E_{c_2} - E_{c_1}/KT)$  and  $y = \exp(n/D1)$ .

The expression for  $f_v$  can be obtained in a similar way:

$$f_{\rm v} = \frac{2u}{(u-1)[(u-1)^2 + 4uv]^{1/2}} \tag{17}$$

where  $u = \exp(E_{v_2} - E_{v_1}/KT)$  and  $v = \exp(n/D2)$ .

Substituting  $f_c$  and  $f_v$  from Equations 16 and 17 in Equation 13, the gain-carrier density relationship can be obtained for the n=2 transition. Similarly, following the steps used for n=1 and 2, the gain-carrier density relationship for the third quantized transition level (n=3) can be evaluated.

Equations 1 and 2 for i = 1, 2 and 3 are used to construct the circuit model that includes the effect of QST3. Using the circuit model given in Fig. 1, the FWHM of the output pulse (observed at output node P3, Fig. 7b) has been reduced by about 70 per cent. Typical values used in the simulation are given in Table I.

# 3. Conclusions

In conclusion, circuit models that include the effects of the second and third quantized level transitions in quantum well lasers have been developed. Further, gain-switched picosecond pulses for 7 and 2 ps FWHM for the two quantized levels, respectively, were observed by simulating the models. The results indicate the applicability of the circuit modelling technique to the study of the gain-switching characteristics of multiple QW lasers.

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