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## Cavitation Patterns on a Plano-Convex Hydrofoil in a High-Speed Cryogenic Cavitation Tunnel

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#### **ABSTRACT**

Cavitation around a plano-convex hydrofoil has been observed using a cryogenic cavitation tunnel of a blowdown type. An approximately 300mm long test section with flow visualization was set between the 100L upper and lower tanks. The working fluids were water and liquid nitrogen. Experiments with emphasis on periodical shedding of cloud cavitation were performed for three channels, 20, 30 and 60 mm in width, and two hydrofoils, 20 and 60mm in chord length  $L_C$ . Inlet velocity  $u_{in}$  and cavitation number  $\sigma$  were varied between 3.8 and 19.5 m/sec, and -1.83 and 19.35, respectively. Incident angle was fixed at 8°. Observed cavitation patterns are sorted according to the maximum cavitation length  $L_{max}$ compared to  $L_C$ . Type X is defined as no cavitation, type A as  $0 < L_{max} \le L_C$ , type B as  $L_C < L_{max} \le 2L_C$ , and type C as  $L_{max} > 2L_C$ . Type B has either the periodical shedding mode or the steady mode, so type PB is defined as type B with periodical shedding and type SB as type B under steady condition. Apparently types A and C are almost steady. Type PB solely occurs in the case that  $L_{max}$  is comparable to  $L_C$ . The cavitation patterns are mapped in the diagram of the degree of subcooling  $P_{in}$ - $P_{sat}$ versus the dynamic pressure  $\rho u_{in}^2/2$  because they are not organized only by  $\sigma = (P_{in} - P_{sat})/(\rho u_{in}^2/2)$ . It is suggested that the maximum cavitation thickness is controlled by the similarity laws of hydrofoils for types SB and C.

#### INTRODUCTION

Cavitation is one of the most difficult problems to be surmounted in the development of turbo-pumps for liquid fuel rocket engines. Because high performance engines require high combustion pressure, their turbo-pumps have to operate at high rotating speed. The best performance of the pump can be obtained when cavitation occurs stably at high rotating speed, therefore it is necessary to allow controllable cavitation to form in the pump. Although conventional design methods of pumps against cavitation are available for water, current large size main engines utilize cryogens as a fuel and an oxidizer, for examples, LH<sub>2</sub> and LOX for U.S. RS-68, U.S. SSME, Japan's LE-7A and Europe's Valcain2, or kerosene and LOX for Russia's RD-180. Because cryogens have thermodynamic features called "thermodynamic effects" different from ordinary fluids like water, cryogenic cavitation is complicated, and it is hard to control cryogenic cavitation without deeply understanding its behavior and its influences on the pump performance. Consequently, experiments on cryogenic cavitation with visualization play a very important role in clarifying the features of cryogenic cavitation at the moment, and in getting knowledge of how to allow controllable cavitation in the near future.

Wade et al. (1966) [1] carried out a visualization study on water cavitation around a plano-convex hydrofoil, as well as measurements of lift and drag coefficients. Their photos of cavitation on the hydrofoil are very useful to recognize the cavity oscillation. Le et al. (1993) [2] noted the difference of cavitation profiles by means of flow visualization in cases of various cavitation numbers  $\sigma$  and angles of the incidence AOI. Kjeldsen et al. (1999) [3] mapped cavitation types and cavity length by combination of  $\sigma$  and AOI, and indicated the region of periodical shedding of cloud cavitation by using the Strouhal number. Franc (2001) [4] showed a relationship that gives the frequency of periodical oscillation as a function of cavitation compliance, and the length and area of the upstream duct from

the viewpoint of system instability. Callenaere (2001) [5] used a diverging step in a water tunnel to investigate the instability of a partial cavity induced by a re-entrant jet. He revealed that an adverse pressure gradient plays an important role to trigger the re-entrant jet, and the interaction between the re-entrant jet and the cavity causes periodical shedding of the cloud cavitation.

Furthermore, some cryogenic experiments have been reported for various flow configurations. Hord (1973) [6] performed experimental studies with flow visualization on a cryogenic cavitating flow around a two-dimensional symmetric thick hydrofoil by using LN<sub>2</sub> and LH<sub>2</sub>. Thereafter, in order to study a high-speed chocked flow of LN<sub>2</sub>, LOX and LCH<sub>4</sub> with cavitation, experiments with three nozzles of different shape were carried out by Simoneau and Hendricks (1979) [7], who made no effort to visualize the flow patterns. Several U.S. groups (1988-1994) [8-11] reported on a subsonic flow of LHe, however measurements were only for pressure or mass flow rate, not for flow visualization. There have been only a few studies to visualize cryogenic cavitation, because of difficulty

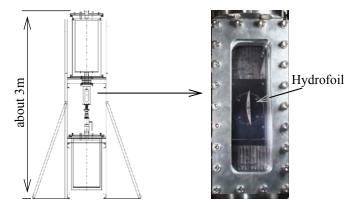


Figure 1: Cryogenic cavitation tunnel and test section

in the experiments. Hori et. al. (2000) [12] performed visualized experiments on the  $LN_2$  cavitating flow by employing the same nozzle profile as Simoneau and Hendricks. Ishii and Murakami (2003) [13] reported He I and II flows in a nozzle with flow visualization successfully.

The objective of present study has been therefore to understand the cavitation behavior around a hydrofoil in a comparative way of flow visualization between the cryogen and the ordinary fluids to elucidate the distinction for periodical shedding of cloud cavitation on the hydrofoil. The authors (2005, 2009) [14, 15] reported cavitation flow patterns on the plano-convex hydrofoil using LN<sub>2</sub> and water as working fluids in a cryogenic cavitation tunnel as shown in figure 1(a). Periodical shedding of cloud cavitation from the hydrofoil surface was observed in the case of the positive angle of incident AOI, which is defined by the angle between the approaching flow and the plane surface of the plano-convex hydrofoil (see figure 2). In the present study, experiments with emphasis on periodical shedding were performed for the cases of various channel widths and hydrofoil sizes, as well as flow velocities, in order to clarify the mechanism of periodical shedding from a hydrofoil.

#### **EXPERIMENTAL SETUP**

In order to investigate the difference between cryogenic

**Table 1:** Arrangement of hydrofoils and channel widths

|                            | W=20mm   | W = 30 mm  | W = 60 mm  |  |
|----------------------------|--|--|--|--|
| $L_C$ =20mm                | $d_{min}$ =8.8mm<br>$d_{max}$ =12.4mm<br>$d_{min}/d_{max}$ =0.71 | $d_{min} = 13.8 \text{mm}$<br>$d_{max} = 17.4 \text{mm}$<br>$d_{min}/d_{max} = 0.79$ | $d_{min}$ =28.8mm<br>$d_{max}$ =32.4mm<br>$d_{min}/d_{max}$ =0.89                    |  |
| <i>L<sub>C</sub></i> =60mm | _  | $d_{min} = 11.3 \text{mm}$<br>$d_{max} = 22.1 \text{mm}$<br>$d_{min}/d_{max} = 0.51$ | $d_{min} = 26.3 \text{mm}$<br>$d_{max} = 37.1 \text{mm}$<br>$d_{min}/d_{max} = 0.71$ |  |

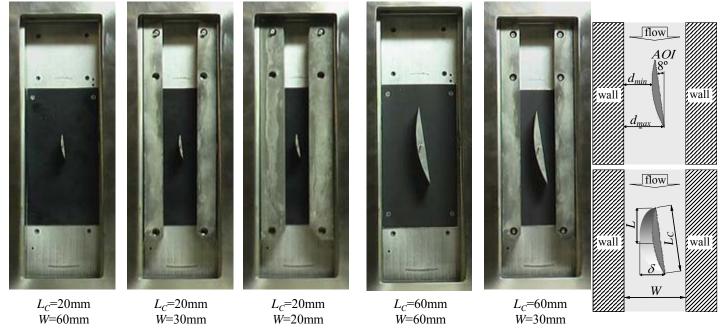
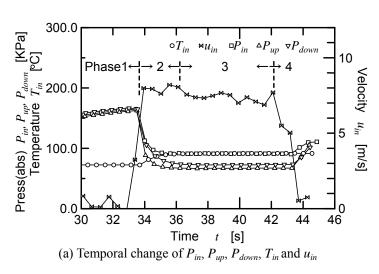


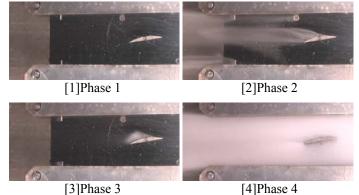
Figure 2: Hydrofoil and channel profiles

cavitation and ordinary fluid cavitation, liquid nitrogen as cryogen and water as ordinary fluid were employed because of easy handling and affordability. The experiments were conducted using a cryogenic cavitation tunnel of a blowdown type as shown in figure 1. This tunnel has 100L upper and lower tanks for liquid nitrogen and water. A test section, 288mm in length, 60mm in width, and 20mm in depth, with flow visualization was set between the tanks. Two sizes of plano-convex hydrofoils, which have a plane surface on one side, a convex on the other side, sharp leading and trailing edges, and thin thickness like an inducer impeller of a turbopump for a rocket engine, were used. Their chord lengths  $L_C$ , radii of the convex surfaces, and thicknesses were 20 and 60mm, 26 and 78mm, 2 and 6mm, respectively. The angle of their leading and trailing edges was 22.6°. In addition, the cannel width W was varied by inserting blocks in the channel. Five combinations of  $L_C$  and W were employed as shown in table 1 and figure 2. Especially the channels with  $L_C$ =W=60mm and  $L_C$ =W=20mm were similar to each other. In the experiments for various AOI ranging from -8° to 8°, periodical shedding of cloud cavitation was observed most notably at 8° (see figure 2). Therefore, in this paper, the results for  $AOI=8^{\circ}$ are reported. Inlet velocity  $u_{in}$ , inlet temperature  $T_{in}$ , and inlet pressure Pin were varied to control cavitation number  $\sigma = \{P_{in} - P_{sat}\}/\{\rho u_{in}^2/2\}$ , where  $P_{sat}$  and  $\rho$  are saturation pressure and liquid density, respectively, for the inlet condition.  $u_{in}$  was altered by the pressure in the upper tank, which was pressurized by high-pressure gaseous nitrogen.  $u_{in}$  was evaluated by measurement of liquid level in the upper tank using a liquid level gage of a differential pressure type.  $T_{in}$  was set with an electric heater in the case of water. In the case of liquid nitrogen, heat inflow from the surroundings was balanced by evacuating the upper tank until a desired saturation temperature and pressure were achieved. This method can reduce the liquid nitrogen temperature 5K below the saturation temperature of 78K at atmospheric pressure.  $T_{in}$  and  $P_{in}$  were measured at 60mm upstream from the center of the hydrofoil. The temperature was measured by a RTD (Resistance Temperature Detector). The backpressure in the lower tank was changed by adjusting the valve opening at the outlet pipe from the lower tank to the atmosphere. It was monitored by an electronic pressure gage. In addition, there were two pressure taps on the convex surface of the hydrofoil. They were located at 3mm upstream  $(P_{up})$  and downstream  $(P_{down})$  from the center of the hydrofoil with  $L_C$  =20mm, and at 9mm with  $L_C$  =60mm. Flow pattern of cavitation was recorded using an ordinary digital video camera and a high-speed video camera. Their recording rates were 30 and 1000 flames per second, respectively. A trigger signal of the high-speed video camera,  $u_{in}$ ,  $T_{in}$  and the other pressure signals were recorded by a data logger and PC.

### **RESULTS**

Figure 3(a) shows a temporal change of  $P_{in}$ ,  $P_{up}$ ,  $P_{down}$ ,  $T_{in}$  and  $u_{in}$  in the case of water,  $L_C$  =20mm, W=30mm, and  $P_{back}$ =101.3KPa as an example. In phase 1, the liquid in the upper tank was pressurized by closing the main valve between the test section and the lower tank until the pressure reached the target value. After that, in phase 2, the main valve was instantaneously opened, and the liquid flowed downward





(b) Cavitation profiles **Figure 3:** Timing of data acquisition (water,  $L_c$ =20mm, W=30mm,  $P_{back}$ =101.3KPa)

|   |                            | <b>♦</b> I | Ι <sub>2</sub> Ο,<br>Ι <sub>2</sub> Ο, | $T_{in}$ = $T_{in}$ = | =70°C<br>=80°C<br>=90°C<br>=77K |  | MH | <sub>2</sub> O, T | <sub>in</sub> =75°(<br><sub>in</sub> =85°(<br><sub>in</sub> =95°( |   |
|---|----------------------------|------------|--|-----------------------|---------------------------------|--|----|-------------------|---|---|
| Reynolds number <i>Re</i> x10 <sup>-6</sup> 0.0 c.0 c.0 c.0 c.0 c.0 c.0 c.0 c.0 c.0 |                            | DO 5       |  | <u>1</u><br>1         | <b>~</b>                        |  | *  | 3                 | Δ   | 4 |
|   | Cavitation number $\sigma$ |            |  |                       |                                 |  |    |                   |   |   |

Figure 4: Characteristics of the cavitation tunnel

through the test section. Large-scale cavitation as shown in figure 3(b)[2] occurred for a few seconds due to rapid acceleration by the steep pressure gradient. Then in phase 3, steady cavitation was achieved as shown in figure 3(b)[3]. The

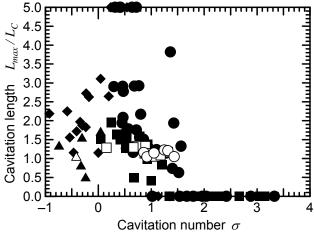
cavitation region was smaller than that in phase 2, and unless otherwise stated, the pictures recorded by a high-speed video camera in phase 3 were used for picking up  $L_{max}$ . After the liquid in the upper tank had almost flowed out, it switched to mist flow as shown in figure 3(b)[4] and the experiment was over.

Figure 4 shows a relationship between the Reynolds number  $Re=u_{in}L_C/\nu$  and  $\sigma$  in the case of  $L_C=W=20$ mm, and  $P_{back}=101.3$ KPa. Experiments for a wide range of  $\sigma$  can be performed at small Re, whereas at large Re experiments only for a narrow range of  $\sigma$  can be performed due to the characteristics of the current apparatus. In other combinations of the hydrofoil and channel width, similar tendencies were observed.

Figure 5 shows a relationship between the non-dimensional cavitation length  $L_{max}/L_C$  and  $\sigma$  for W=20 and 60mm using the same foil with  $L_c$ =20mm. Data points at the upper limit of the ordinate  $(L_{max}/L_C=5.0)$  denote that the cavity region exceeds the visualization window and the real cavitation lengths were larger than  $L_{max}/L_C$ =5.0. In the case of W=20mm cavitation occurred for  $\sigma \leq 1.56$ , however, in the case of W=60mm it occurred for  $\sigma \leq 1.21$ . It is apparent that cavitation in the narrower channel easily occurs at the higher  $\sigma$ . The periodical shedding of cloud cavitation mainly occurs in a range of  $L_{max}/L_{C}=1.0$  to 1.3. This result indicates that the cavitation whose  $L_{max}$  is nearly the same as  $L_C$  is especially unstable and tends to a result in periodical shedding of cloud cavitation. In the case of steady cavitation, the non-dimensional cavitation length  $L_{max}/L_C$  for W=20mm is larger than that for W=60mm. In the case of the larger hydrofoil  $L_C$  =60mm, the similar tendency was observed.

Figure 6 shows a relationship between  $L_{max}/L_C$  and Re. Figures 6(a) and (b) show results of  $L_C$ =20mm and 60mm, respectively. Data points at the upper limit of the ordinate in these figures denote that the cavity region exceeds the

|        |                  | Periodical cavitation | Steady cavitation |
|--------|------------------|-----------------------|-------------------|
| W=20mm | $H_2O$           | 0                     | •                 |
|        | $LN_2$           | _                     | <b>*</b>          |
| W=60mm | H <sub>2</sub> O |                       |                   |
|        | LN <sub>2</sub>  | Δ                     | <b>A</b>          |



**Figure 5:** Cavitation length v.s. cavitation number (H<sub>2</sub>O and LN<sub>2</sub>,  $L_C$  =20mm,  $P_{back}$ =101.3KPa)

visualization window. In  $H_2O$  as well as  $LN_2$ , there was no cavitation at small Re. Cavitation inception occurred at a certain Re depending on W and  $L_C$  although cavitation did not occur even at high Re in some cases.  $L_{max}/L_C$  was generally getting larger with increasing Re for the same condition. Based on a comparison of figures 6(a) (b), cavitation for  $L_C$ =20mm

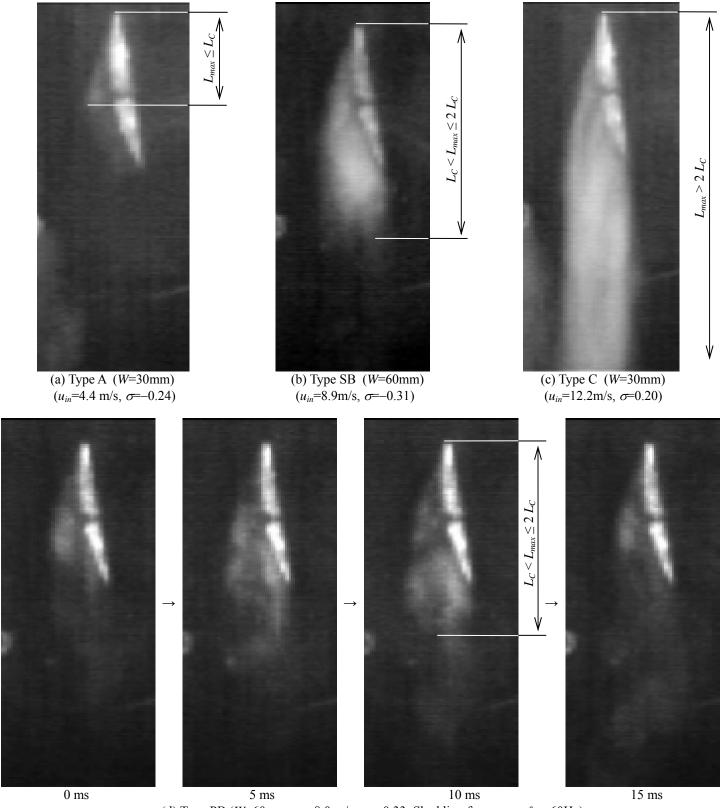
|                            |                          | -        |  | _          |             |          |       |                          |          |
|----------------------------|--------------------------|----------|--|------------|-------------|----------|-------|--------------------------|----------|
|                            |                          |          |  |            |             |          |       | H <sub>2</sub> O         | $LN_2$   |
|                            |                          |          | $L_C$ =  | =20m       | m, W        | =20mm    | l     | 0                        |          |
|                            |                          |          |  |            |             | =30mm    |       | $\Diamond$               | •        |
|                            |                          |          |  |            |             | =60mm    |       |                          |          |
|                            | <b>5</b> 0               |          |  |            |             |          |       |                          |          |
|                            | 5.0                      | F        |  |            | T           |          |       | 1111                     |          |
|                            |                          | F        |  |            |             |          |       |                          |          |
|                            | 4.5                      | F        |  |            |             |          |       |                          | 7        |
|                            |                          | F        |  |            |             |          |       |                          | 7        |
|                            | 4.0                      | F        |  |            |             |          |       |                          | 7        |
|                            | 4.0                      | F        | _  |            |             |          |       |                          |          |
|                            |                          | ļ.       | 0  |            |             |          |       |                          |          |
| 7                          | 3.5                      | Ė.       |  |            |             |          |       |                          |          |
| 7                          | ,                        | ţ        |  | $\Diamond$ |             |          |       |                          | 1        |
| , 20                       | 3                        | ţ        |  | •          |             |          |       |                          | -        |
| $L_n$                      | 3.0                      | F        | a  | ဘ          | •           |          |       |                          |          |
| _                          |                          | Ŀ        |  | Ž.         | 0           | _        |       |                          |          |
| at d                       | 25                       | Ł        | `  |            |             | •        |       |                          | _        |
| e                          | 3.5<br>3.0<br>2.5<br>2.0 | F        |  | Ň          |             |          |       |                          | 3        |
| _<br>                      |                          | E        |  | <b>%</b>   | _           | `        |       |                          |          |
| ξi                         | 2.0                      | F        | ₽  | <b>^</b>   | ο ,         | ,        |       |                          | -        |
| Ĭ;                         |                          | E        | •  | <b>*</b>   | )           |          |       |                          | 3        |
| Ö                          | 1.5                      | E        | ַ  |            | <b>)</b>    |          |       |                          | 3        |
| ·                          | 1.5                      | F        | _ <  | <b>14</b>  | •           |          |       |                          | -        |
|                            |                          | F        | だ。<br>かい<br>かい<br>かい<br>かい<br>かい<br>かい<br>かい<br>かい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい<br>りい | 30         |             |          |       |                          |          |
|                            | 1.0                      | F        | 98   | <b>,</b>   |             |          |       |                          |          |
|                            |                          | F        |  |            |             |          |       |                          | 7        |
|                            | ٥.                       | F        | _ <u>&amp;</u> `   |            |             |          |       |                          | 7        |
|                            | 0.5                      | F        |  | ]          |             |          |       |                          | 7        |
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|                            | 0.0                      | ┖        |  |            | ben-        |          | ىلىت  | لمبت                     | تىب      |
|                            | (                        | )        | 0.5  |            | 1           | 1.5      | 2     | 2.5                      | 5 3      |
|                            |                          |          | F  | Reyno      | olds l      | Numbe    | er Re | 2.5<br>×10 <sup>-6</sup> |          |
|                            |                          |          |  | (a         | $L_C$       | =20mm    |       |                          |          |
|                            |                          |          |  | (          | , .         |          |       | 11.0                     | T 3.7    |
|                            |                          |          | · ·  | (0         | ***         | 20       |       | H <sub>2</sub> O         | $LN_2$   |
|                            |                          |          |  |            |             | =30mm    |       | $\Diamond$               | _        |
|                            |                          | <u> </u> | $L_C$ =  | =60mi      | m, <i>W</i> | =60mm    | !     | <u> </u>                 |          |
| $\zeta$                    | 1.5                      | E        |  | רייי       | _,,,        | TTX      |       | ئىتىت                    |          |
| 7                          | 1.5                      | F        |  |            |             | _0       | 百二    |                          | 7        |
| $L_{max}$                  |                          | F        |  | Ę          | ] [         |          |       |                          | 7        |
| Sué                        | 1.0                      | F        |  | <b>V</b>   | ₽◊          | ,<br>FLU |       |                          | $\dashv$ |
| n<br>F                     |                          | E        |  |            | 异           | •        |       |                          | =        |
| Ęį                         | 0 5                      | Ē        |  |            | 华           | ]        |       |                          |          |
| Cavitation length $L_m^{}$ | 0.5                      | E        |  | _          |             |          |       |                          | 7        |
| á                          |                          | E        |  | [          | 4           |          |       |                          | 7        |
| O                          | 0.0                      | ᄓ        | بليب   | 렆坎         | اکاتِ       | ┸┇╇┸╌    | ىلىت  | ليسب                     | لسب      |
|                            | (                        | )        | 0.5  | _          | 1           | 1.5      | 2     | 2.5                      | 5 3      |
|                            |                          |          | F  | Reyno      | olds        | Numbe    | er Re | x10¯°                    |          |
|                            |                          |          |  | (b         | $L_C$ :     | =60mm    |       |                          |          |
|                            | T7.                      |          | - C. Car   | ritatia    | 1           | -41      | D     | 1.1                      | -1       |

**Figure 6:** Cavitation length v.s. Reynolds number  $(H_2O \text{ and } LN_2, P_{back}=101.3\text{KPa})$ 

occurred at smaller Re than that for  $L_c$ =60mm. In addition,  $L_{max}/L_C$  for LN<sub>2</sub> was less than that for H<sub>2</sub>O at the same Re.

Cavitation patterns were sorted into types A, PB, SB and C mainly based on  $L_{max}$  compared to  $L_C$ . Type X was defined as

no cavitation ( $L_{max}$  =0mm), and type A as  $0 < L_{max} \le L_C$ . Types SB and PB are defined as  $L_C < L_{max} \le 2L_C$ , of which SB means "Steady B" and PB means "Periodical B". Type C was defined as  $L_{max} > 2L_C$ . Figure 7 shows examples of these patterns.



(d) Type PB (*W*=60mm,  $u_{in}$ =8.0 m/s,  $\sigma$ =-0.33, Shedding frequency:  $f_{cav}$ =60Hz) **Figure 7:** Cavitation patterns (LN<sub>2</sub>,  $L_C$  =20 mm)

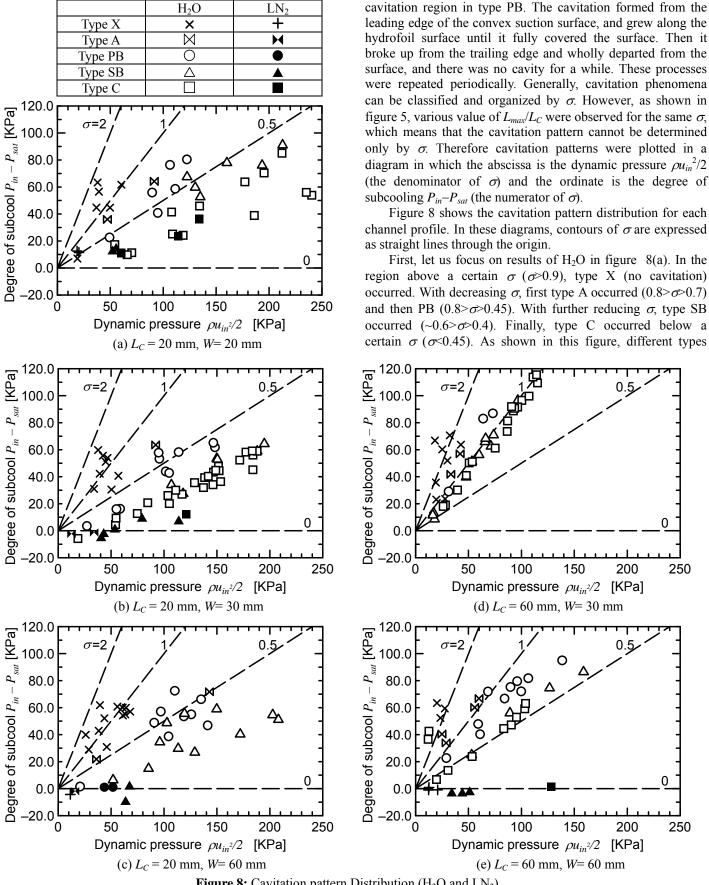


Figure 7(d) shows a temporal change of the shape of the

Figure 8: Cavitation pattern Distribution (H<sub>2</sub>O and LN<sub>2</sub>)

were mixed in some regions of  $\sigma$ . For example, in the region of  $0.8 > \sigma > 0.7$  (the mixed region of types A and PB), type A was observed for smaller  $\rho u_{in}^2/2$ , and type PB for larger  $\rho u_{in}^2/2$ . In the region of  $\sim 0.6 > \sigma > 0.45$  (the mixed region of types PB and SB), type PB was observed for smaller  $\rho u_{in}^2/2$ , and type SB for larger  $\rho u_{in}^2/2$ . In the region of  $0.45 > \sigma > 0.4$  (the mixed region of types SB and C), type SB was observed for smaller  $\rho u_{in}^2/2$ , and type C for larger  $\rho u_{in}^2/2$ . Such tendencies of transition of cavitation types were commonly observed in the results of H<sub>2</sub>O for the other channel profiles although the locations of mixed regions of  $\sigma$  depend on the channel profile.

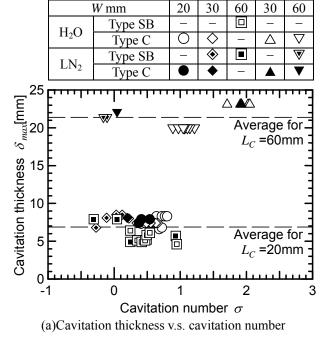
Second, let us focus on results of LN<sub>2</sub>, in figure 8. There are only a few results for LN<sub>2</sub> because it was not easy to control the LN<sub>2</sub> temperature below the saturation value using the vacuum pump and to conduct experiments at various temperature of LN<sub>2</sub>. However, the same tendencies as observed for the water results can be seen. In figures 8(a) and (b), type SB cavitation was observed at smaller  $\rho u_{in}^{2}/2$ , while type C was observed at larger  $\rho u_{in}^{2}/2$  along a straight line of constant  $\sigma$ . In figure 8(c), type PB occurred at smaller  $\rho u_{in}^{2}/2$ , while type SB occurred at larger  $\rho u_{in}^{2}/2$  for the same  $\sigma$  (nearly equals 0 in this case).

These results (types A and PB occurred at the same  $\sigma$ , and so did types PB and SB, and types SB and C) correspond to the fact that at given  $\sigma$  the longer cavitation cloud occurred at

 $L_C \, \mathrm{mm}$ 

20

60





(b)Example of cavity profile in each condition ( $L_C$  =60mm) **Figure 9:** Cavitation thickness at types SB and C (H<sub>2</sub>O and LN<sub>2</sub>)

higher  $u_{in}$ , as also found in figure 6.

Figure 9(a) shows a relationship between the maximum cavitation thickness  $\delta_{max}$  and  $\sigma$ , in the case of types SB and C, where  $\delta_{max}$  denotes the maximum distance from the trailing edge of the hydrofoil to the outer edge of the cavitation region (see figure 2). For each channel, profile (combination of  $L_C$  and W)  $\delta_{max}$  remains almost constant against a change of  $\sigma$ . Moreover, for each hydrofoil  $\delta_{max}$  virtually did not vary with W. Furthermore, this was valid even when the fluid was switched from  $H_2O$  to  $LN_2$ . In other words,  $\delta_{max}$  was roughly decided by the hydrofoil size ( $\delta_{max}\approx7$ mm for  $L_C=20$ mm, and  $\delta_{max}\approx21$ mm for  $L_C=60$ mm). Figure 9(b) shows cavitation profiles of  $L_C=60$ mm operating in  $H_2O$  and  $LN_2$ . It is apparent that switching the fluid from  $H_2O$  to  $LN_2$  and changing W from 60mm to 30mm did not affect  $\delta_{max}$ .

Figure 10(a) shows a relationship of  $\sigma$  versus the frequency of periodical shedding of cloud cavitation  $f_{cav}$ . There was no predominant tendency between  $\sigma$  and  $f_{cav}$ . Then, relationships of  $\rho u_{in}^2/2$  versus  $f_{cav}$ , and  $P_{in}-P_{sat}$  versus  $f_{cav}$  were shown in figures 10 (b) and (c), respectively. Although the data were scattered in a wide range, tendencies might be identified that for each condition.  $f_{cav}$  was low for the small values of  $\rho u_{in}^2/2$  and  $P_{in}-P_{sat}$ , and  $f_{cav}$  was high for the large values of  $\rho u_{in}^2/2$  and  $P_{in}-P_{sat}$ .

#### **DISCUSSION**

First, the effect of channel width on cavitation is discussed. As mentioned in relation to figure 5, when W=20mm, the cavitation inception occurred at larger  $\sigma$ ,  $L_{max}$  was longer, and  $L_{max}$  more suddenly increased with decreasing  $\sigma$  than when W=60mm. The above tendencies can be explained by the blockage effect of the hydrofoil and cavitation, that is, the flow acceleration due to the blockage effect is larger for the narrower channel that promotes the onset and growth of cavitation as illustrated in figure 11. In the case of  $L_C$  =20mm, the blockage ratios of the hydrofoil are 18% and 6% for W=20mm and 60mm, respectively. Then the increase of flow velocity due to the blockage effect for liquid single-phase flow is roughly estimated as follows:

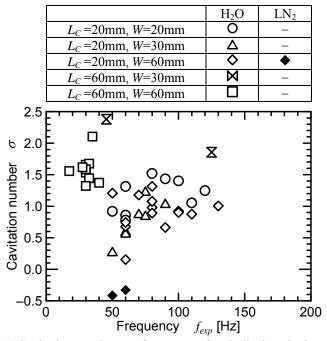
$$u_{20mm} = u_{in}/(1-0.18) = 1.22u_{in}$$
 when  $W = 20$ mm  $u_{60mm} = u_{in}/(1-0.06) = 1.064u_{in}$  when  $W = 60$ mm

Therefore, it is confirmed that the flow acceleration is significant especially for the narrower channel. When cavitation occurs, the flow acceleration due to the blockage becomes more pronounced as illustrated in figure 11. Such a larger blockage effect for the narrower channel causes the onset of cavitation at larger  $\sigma$  and the rapid increase of  $L_{max}$  with the decrease of  $\sigma$ .

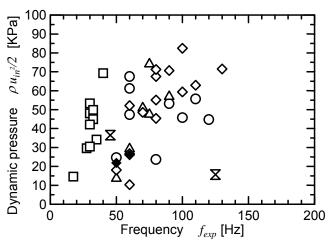
Second, the frequency of periodical shedding of cloud cavitation is discussed. A vortex of wake type like Karman vortex could cause the periodical shedding of cloud cavitation. The frequency of vortex shedding  $f_{vor}$  from a circular cylinder is given by the following empirical correlation [16].

$$f_{vor} = 0.198 \frac{u_{in}}{D} \left( 1 - \frac{19.7}{Re_D} \right) \tag{1}$$

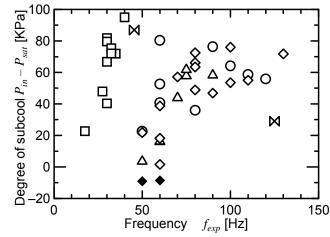
where, D is the diameter of a cylinder, and  $Re_D$  is defined as  $Re_D = u_{in}D/\nu$ . Equation (1) was applied to the present



(a) Cavitation number v.s. frequency of periodical cavitation



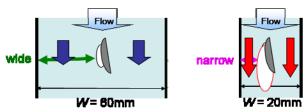
(b)Dynamic pressure v.s. frequency of periodical cavitation



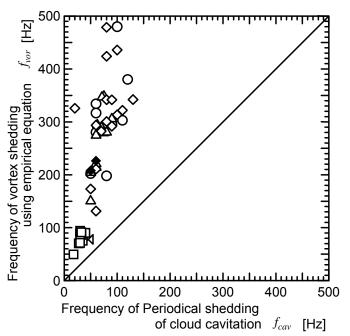
(c)Degree of subcool v.s. frequency of periodical cavitation **Figure 10:** Frequency of periodical cavitation, i.e. type PB

experiment by replacing D with the maximum cavitation thickness  $\delta_{max}$ , and the resulting  $f_{vor}$  is compared with  $f_{cav}$  in figure 12.  $f_{vor}$  is much higher than  $f_{cav}$  of the periodical shedding of cloud cavitation. Therefore the periodical shedding of cloud cavitation seems to be controlled by another mechanism rather than the vortex shedding of the wake.

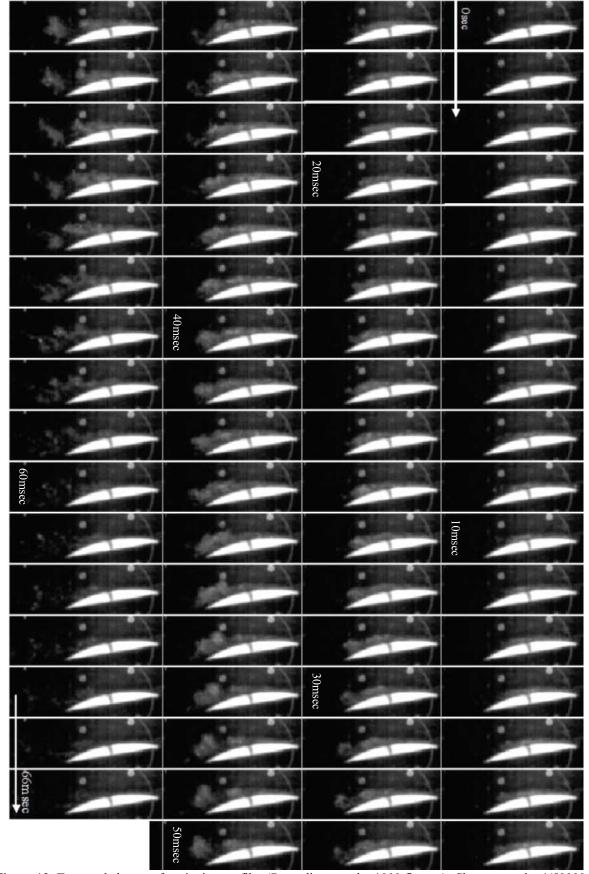
A reverse liquid flow on the hydrofoil could also cause the periodical shedding of cloud cavitation. It is well known that periodical shedding of cloud cavitation in partial cavitation is caused by a reverse liquid flow called as a re-entrant jet [5]. In conventional cloud cavitations, the length of cavity is shorter than the hydrofoil chord length, and the liquid jet emerges at the reattachment point of liquid flow on the hydrofoil. However, the reverse liquid flow in this experiment is not the conventional re-entrant jet because the periodical shedding of cloud cavitation occurs even when the cavitation fully covers the hydrofoil surface. Figure 13 shows a temporal change of cavitation profiles in the case of type PB. Cavitation forms from the leading part of the hydrofoil and gradually grows up along the hydrofoil (0-25msec). When the cavitation reaches a certain size (26msec), the rear part of the cavitation begins to detach from the hydrofoil surface due to a reverse liquid flow between the hydrofoil surface and the cavitation region. The rear part of the cavitation continues to grow with the reverse liquid flow beneath the cavitation until the cavitation fully



**Figure 11:** Schematic figures of flow velocity around the hydrofoil for wide and narrow channels



**Figure 12:** Comparison of frequencies between Experimental and Theoretical results



**Figure 13:** Temporal change of cavitation profiles (Recording speed = 1000 flames/s, Shutter speed = 1/50000s)  $(H_2O, L_C = 60 \text{mm}, W = 60 \text{mm}, T_{in} = 95 ^{\circ}C, u_{in} = 4.5 \text{m/s}, \sigma = 0.6)$ 

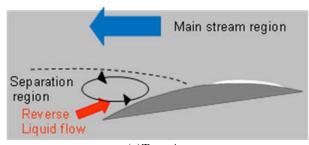
covers the hydrofoil, and finally the rear part of the cavitation is torn off and shed (at 30msec). Although it is not clear in the still photographs, a circulating flow was observed in the rear part of the cavitation in the high-speed movie, which means that flow separation occurs in the cavitation region. The reverse liquid flow and circulation are caused by an adverse pressure gradient along the hydrofoil as indicated by  $P_{up}$  and  $P_{down}$  in figure 3. Such an interaction between the flow separation and cavitation region seems to be essential for the occurrence of periodical shedding of cloud cavitation. The growth and shedding of cavitation is repeated, and cavitation is almost completely disappears at last (at 66msec).

Based on the experimental observations, the mechanism of periodical shedding of cloud cavitation (type PB) and the flow structures of other types (A, SB and C) can be explained as illustrated in figure 14. In the case of type A, cavitation region does not reach the flow separation point, as shown in figure 14(a), which results in a stable cavitation. In the case of type PB shown in figure 14(b), cavitation reaches the flow separation region. In the separation region, the rear part of cavitation is shed by the reverse liquid flow and carried by the main liquid flow. In the case of types SB and C, thick and long cavitation covers the whole separation region as shown in Figure 14(c). Although the flow separation and circulation flow exist in the cavitation region, the shape of the cavitation region is not affected greatly by the separation region because of the large size of the cavitation. Therefore, periodical shedding of cloud cavitation (type PB) occurs when the length of cavitation region is nearly the same as the hydrofoil chord length as shown in figure 5.

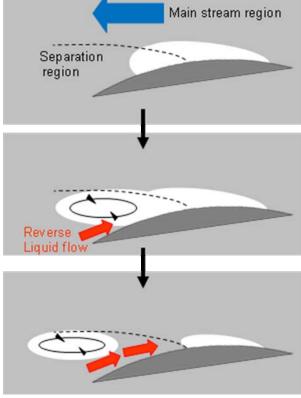
#### CONCLUSION

A visualization study of cavitation on the convex surface of a plano-convex hydrofoil has been made for several channel widths and foil sizes using water and liquid nitrogen as the working fluid. The conclusions are summarized as follows:

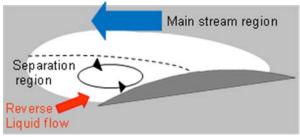
- (1) Cavitation patterns are sorted mainly based on the maximum cavitation length and mapped with reference to subcooling and dynamic pressure of the inlet flow. Generally, the cavitation length increases with the decrease of cavitation number. In addition, the cavitation length tends to become larger for larger inlet velocity under the same cavitation number.
- (2) Periodical shedding of cloud cavitation was observed when the cavitation length was nearly the same as the hydrofoil length. Its frequency is much smaller than that estimated by an empirical equation for the vortex shedding from a bluff body. The visualization by a high-speed video revealed that a flow separation and circulating flow occur in the rear part of cavitation, and a reverse liquid flow on the hydrofoil surface tears off the cavitation resulting in the periodical shedding. For longer and thicker cavitation the circulation region exists stably in the cavitation, and periodic shedding does not occur.
- (3) The cavitation number at the onset of cavitation increases with the decrease of channel width due to the blockage effect. In addition, the maximum length of cavitation region increases more rapidly with the decrease of cavitation number for the narrower channel.



(a)Type A



(b)Type PB



(c)Types SB and C

**Figure 14:** Schematic figures of interaction between the cavity and the separation region

(4) The maximum cavitation thickness depends solely on the hydrofoil size for sufficiently long, thick and stable cavitation compared to the separation region, and it is independent of other experimental conditions.

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#### **NOMENCLATURE**

- A a type of cavitation region,  $L_{max} \le L_C$
- AOI angle of the incidence between the approaching flow and the hydrofoil plane surface
- B a type of cavitation region,  $L_C \le L_{max} \le 2 L_C$
- C a type of cavitation region,  $L_{max} \ge 2 L_C$
- d distance
- D diameter of circular cylinder
- $f_{cav}$  frequency of periodical shedding of cloud cavitation frequency of vortex shedding calculated by empirical equation based on the Strouhal number
- H<sub>2</sub>O water
- L cavity length
- $L_C$  chord length of the hydrofoil
- LCH<sub>4</sub> liquid methane
- LH<sub>2</sub> liquid hydrogen
- LHe liquid helium
- LN<sub>2</sub> liquid nitrogen
- LOX liquid oxygen
- P pressure
- $P_{back}$  pressure at the lower tank
- $P_{down}$  pressure on the hydrofoil at 0.15  $L_C$  downstream from the center of the hydrofoil
- $P_{up}$  pressure on the hydrofoil at 0.15  $L_C$  upstream from the center of the hydrofoil
- *Re* Reynolds number with respect to  $L_C$
- $Re_{\delta}$  Reynolds number with respect to  $\delta$
- St Strouhal number
- T temperature
- t time
- u velocity
- W width

#### **Greek characters**

- $\Delta$  difference
- $\delta$  cavitation thickness
- $\rho$  density
- v kinetic viscosity

## **Subscripts**

in value at the inletmax value at maximummin value at minimumsat saturation value

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