ATOMIC EMISSION IN THE ULTRAVIOLET NIGHTGLOW

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<u>Abstract.</u> An observation of the ultraviolet nightglow between 2670 Å and 3040 Å was conducted over White Sands Missile Range on October 22, 1984, at 0020 hours LST during the Orionids meteor shower. A 1/4-meter uv spectrometer operating at 3.5 Å resolution viewed the Earth's limb at tangent heights between 90 km and 110 km for 120 seconds. By inverting the observed limb intensities, a total zenith intensity of 1.4 kR is inferred for the Herzberg I system. Excess emission above the Herzberg I (7,3) band at 2852 Å is identified as the Mg I resonance line. The intensity ratio of the Herzberg I band system to the 2972 Å line from O(¹S) was less than that predicted from the accepted O(¹S) branching ratio and acceptable ratios of Herzberg I to 5577Å emissions. Arguments supporting the identification of the Herzberg III band system are also advanced.

Introduction

The near and middle ultraviolet nightglow results from the recombination of atomic oxygen into molecular oxygen at lower thermospheric altitudes. Initial ground based observation identified the Herzberg I ($A^3\Sigma_{u}^+ - X^3\Sigma_{g}^-$) system (Dufay, 1941) as well as the Chamberlain ($A'^3\Delta_{u} - X^3\Sigma_{g}^-$) system (Chamberlain, 1958). Much later, Slanger and Huestis (1981) identified the presence of Herzberg II ($c^1\Sigma_{u}^- - X^3\Sigma_{g}^-$) emission using synthetic spectra to compare with the ground based data of Broadfoot and Kendall (1968), taken at 5.5 Å resolution. This identification was confirmed when Slanger and Huestis (1983) analyzed some unpublished data taken by Broadfoot at a resolution of 0.5 Å. Most recently, Stegman and Murtagh (1988) have presented high resolution (1.3 Å) Herzberg I data for 28 nights. Since they also measured the 5577 Å emission concurrently, their data set allows the variability of the Herzberg I to $O(^1S)$ ratio to be evaluated.

One limitation of ground based techniques is that observations are limited to near ultraviolet wavelengths longward of the ozone cutoff at 3100 Å. For shorter wavelengths, a number of rocket observations have been made; however, due to the low intensity of the airglow, photometers rather than spectrometers are typically used. There is a spectroscopic measurement of the nightglow at wavelengths less than 3100 Å (Hennes, 1966). Although this was a photographic observation at low resolution (11 Å), he was nonetheless able to identify the Herzberg I band system along with the strong 2972 Å $O({}^{3}P{}^{-1}S)$ transition. Degen (1969) was able to quantify the vibrational population of the $A^{3}\Sigma_{u}^{+}$ state from an analysis of that spectrum. At higher resolution, such as the data to be discussed below, it is possible to separate the bandheads of the Herzberg I and II emissions and therefore one can more readily isolate atomic features that would otherwise be masked by the molecular bands. In this note, the $O(^{3}P^{-1}S)$ transition at 2972 Å is discussed and excess emisson found near 2850 Å is hypothesized to be the resonance line of Mg I. An identification of the Herzberg III band system is also advanced.

Experiment

An instrumented payload to study the airglow produced by recombining oxygen atoms was launched from White Sands Missile Range on October 22, 1984 at 0020 LST. This was during the

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Paper number 89GL03494. 0094-8276/89/89GL-03494\$03.00 period of the Orionids Meteor shower. It also happened that there was a high level of geomagnetic activity with Ap = 47. The complement of instruments included two resonance lamp modules for measuring atomic oxygen and hydrogen, photometers to measure the emission from the

NO₂ continuum, the OH (9,3) band, and O₂ (0,0) Atmospheric Band (7620 Å), and a 1/4-meter uv scanning spectrometer operating at 3.5 Å resolution. The optical axis of each instrument was aligned along the payload roll axis. The wavelength interval scanned by the digital drive of the spectrometer was 2670 Å to 3040 Å. The spectrometer was calibrated in the laboratory with an NBS calibrated tungston lamp. Prior to taking the payload to the launcher, the spectrometer viewed a hollow cathode platinum discharge for the purpose of assigning wavelengths to the data bins. This calibration resulted in the wavelength position of the scan to be accurate to within one grating step (+/- 1.75 Å). The field of view of the telescope was 0.5 by 5.0 degrees.

The payload attitude control system was programmed to do three maneuvers during the flight. First it pointed the payload axis tangent to the trajectory on the upleg after nose cone ejection. Then for 120 seconds centered on apogee the payload was pointed north at a zenith angle of 97° . This placed the field of view for the 90 km tangent height at 41° N latitude (about Boulder, Colorado). While the rocket ascended and descended about apogee, the tangent height changed from 90 km to 110 km. On the downleg portion of the trajectory the payload axis was pointed tangent to the trajectory facing downward.

Results

A total of 41 spectral scans were obtained while the payload was viewing the limb. These were averaged together, calibrated and a mean spectrum is displayed as the solid line in Figure 1a. The obvious features are the Herzberg I bands and the 2972 Å line of $O(^{1}S)$. However, to make a comprehensive identification of other features in the data, synthetic spectra were calculated and compared with the data.

The synthetic calculation of the three Herzberg systems used the molecular constants of Slanger and Cosby (1988), the A-values of Degen (1977) and Bates (1989), rotational formulae from Degen (1969) and Kovacs (1969), and an assumed rotational temperature of 200 °K. For the Herzberg III bands, only the (Ω =2) component of the A'³ Δ_u state was considered. The synthetic spectra were fit to the data using a multiple linear regression routine (Bevington, 1962). First, each vibrational level for the $A^{3}\Sigma_{u}^{+}$ and the $c^{1}\Sigma_{u}^{-}$ states was separately fit to the data and relative vibrational populations were obtained. It was found, however, that the low counting statistics precluded the determination of vibrational populations for the relatively weak Herzberg II system. Therefore, in the second step of the fitting procedure, the derived vibrational population for the Herzberg I system was used as a guide for a Herzberg II vibrational distribution which was assumed to have the same shape as the Herzberg I but was displaced by 2 quanta to higher vibrational levels (see Slanger and Huestis, 1981). The synthetic spectra were again fit to the data and a revised set of Herzberg I vibrational populations were obtained. In practice, the deduced vibrational distributions obtained from each step were quite similar. The vibrational populations of the Herzberg I system are given in column A of Table 1.

This distribution is in good agreement with that deduced by Degen (1969) from the Hennes (1966) data, with the exception of a reduced v'=8 population in our spectrum. This value for the v'=8 population is statistically significant as our fit is guided by the



WAVELENGTH (Å)

Fig. 1 (a) The data (solid line) obtained from the average of 41 spectral scans obtained while the field of view scanned the limb from approximately 90-110 km. Synthetic spectra for the Herzberg I, II, and III and the N₂ VK are summed together (dotted line) to compare with the data. (b) The individual synthetic spectra (on expanded vertical scale) for the Herzberg I (dotted), Herzberg II (bold solid line) and Herzberg III (thin solid line) band systems. The two arrows label the Herzberg III (6,2) band at 2815 Å and the Herzberg II (7,2) band at 2913 Å.

TABLE 1. Relative Herzberg I Vibrational Populations

v'	Α	В
3	0.60 +/20	0.65 +/21
4	1.00 +/08	1.00 +/09
5	0.84 +/06	0.91 +/06
6	0.94 +/05	0.91 +/06
7	0.70 +/04	0.66 +/04
8	0.18 +/04	0.16 +/04
9	0.22 +/04	0.19 +/04

A: Populations without contribution from Herzberg III

B: Populations with contribution from Herzberg III (see text)

relative mix of the (5,1) and (8,2) bands near 2700 Å and our detector is most sensitive at these shorter wavelengths. In addition, our estimate of the intensity in the (5,1) band is constrained by the fit to the relatively bright (5,2) and (5,3) bands.

A search of the data for the previously unobserved Herzberg III

band system was made. This was done by constructing spectra using a Herzberg III vibrational distribution patterned after that used by Slanger and Huestis (1981) for the Chamberlain bands; both emissions arise from the same upper state ($A^{\prime 3}\Delta_{u}$). Inclusion of the the Herzberg III was found to have a small effect on the deduced Herzberg I vibrational populations which are shown in column B of Table 1.

Figure 1b is an enlargement of the three Herzberg band systems. From this it is possible to identify regions where various bands predominate. Because many of the Herzberg III bandheads overlap with those of the Herzberg I, the identification of the Herzberg III was not conclusive. However, it should be noted that the short wavelength shoulder of the Herzberg I (5,2) band at 2815Å does correspond to the location of the Herzberg III (6,2) band, which according to the A-values of Bates (1989) is one of the brightest bands in the Herzberg III system. By contrast, although the fit to the data indicates the Herzberg II to be slightly less bright than the Herzberg III, it is easier to detect because the bandheads are more clearly separated from those of the Herzberg I. Note that while Slanger and Huestis (1981) found the Herzberg II to be 1/4 as bright as the Herzberg I, in this data the Herzberg II are only 1/9 as bright. The most easily identified Herzberg II feature in the spectrum is the (7,2) band at 2913 Å.

Other aspects of the fit to the data include the possible presence of N₂ Vegard-Kaplan band emission which could result from the observation of a distant auroral arc well to the north and behind the tangent layer. A feature near 2760Å is identified as the VK (0,6) band. In addition, the strong line at 2972Å is the $O(^{3}P - ^{1}S)$ line and the excess intensity near 2850Å is proposed to be due to the resonance line of neutral Mg which has a wavelength of 2852Å. These features will be discussed below. The combined fit of the Herzberg I, II, III and N₂ VK bands is shown as the dotted line in Figure 1a.

Table 2 summarizes the observed emission features and their intensities at the peak of the layer. The Herzberg I intensity is for the total band system based on the fraction observed and the resulting vibrational distribution. The vertical intensity of the Herzberg I was obtained from an "onion-peel" inversion of the altitude profile. Our value of 1.4 kR is brighter than a number of other recent measurements which give total intensities between 230 -700 R for the Herzberg I (see Table 3, to be discussed below). This suggests that the atomic oxygen densities were enhanced on the evening of the measurement. While the [O] density measurement during the flight failed, we did measure the zenith intensity of the (0,0) band of the O₂ atmospheric system (7620 Å). Our value of 13 kR for this emission is just larger than the largest value in the range of values recently summarized by Murtagh et al. (1989) and thus provides independent support for our enhanced Herzberg I intensity.

The zenith intensities of the Herzberg II and III systems and the 2972 and 2852 Å lines are deduced from the fraction of those systems required to fit the spectra and the assumption that the layer shapes are the same as the Herzberg I. Because this assumption may not be strictly true, there may be a systematic uncertainty in the derived zenith intensities. On the other hand, the ratio between the various emission features is taken solely from the spectrum shown in Figure 1 and is unlikely to contain significant error. Only the slant intensity of the VK (0,6) band is given since it is a distant emitting surface.

Table 2. Summary of Estimated Emission Rates in Rayleighs

Feature	Slant intensity	Zenith Intensity			
Herzberg I	70,000 +/- 2100	1400 +/- 42			
Herzberg II	7900 +/- 1900	158 +/- 39			
Herzberg III	8900 +/- 700	178 +/- 14			
O(¹ S) 2972Å	3850 +/- 790	77 +/- 16			
Mg I 2852Å	580 +/- 175	11.5 +/- 3.5			
Vegard-Kaplan (0,6)	580	• • • •			

Tabl	e 3:	M	leasurements	of	Nightglo)w	Intensities ((Ra	yleighs)
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			Katio
Photometer Measuremen	n <u>ts</u> :		
Stegman and ba Murtagh, 1988	sed upon (6,7) b see text	and,	2.5-3.0
Ogawa et al., 1987	465	180	2.6
Murtagh, et al.,	230	121	1.9
1986	302	142	2.1
	370	165	2.2
Thomas and Young, 19	81 600 - 700	90	6.6 - 7.8
L. Thomas et al., 1979	5 - 7		
Spectrometer Measurem	ents:		
This work	1400	1800	.78
Hennes (1966)	our reanal	1.0	

Discussion

2972 Å Line

Causia

Table 2 shows that the ratio of the intensity of the Herzberg I bands to the 2972Å is equal to 18. Using the branching ratio of 23.5 (Kernahan and Pang, 1975) between the 5577Å and the 2972Å emissions, we infer a 5577Å zenith intensity of 1800 R. This yields a ratio of Herzberg I to 5577Å of 0.78. While we did not simultaneously measure the 5577Å emission on this rocket flight, there have been numerous other simultaneous measurements of the Herzberg I bands and the $O(^{1}S)$ emission from which the ratio can be deduced. A number of these measurements are presented in Table 3.

Table 3 is divided into two sections. In the first, the 5577 emission was measured with a photometer in conjunction with either a spectroscopic or photometric measurement of the Herzberg I system. In cases where the authors listed the total zenith intensities of both emissions, computation of the ratio was straightforward. For the Stegman and Murtagh (1988) study, they plotted the intensity of the Herzberg (6,7) emission against the green line intensity for 28 separate measurements. Assuming 1.5 % of the total Herzberg emission arises from this single band (Degen, 1977; see also Bates, 1989), we found the ratio to fall within the range 2.5 to 3.0. In general, the mean ratio of Herzberg I to 5577 Å is near 2.5 although Thomas and Young (1981) and L. Thomas et al. (1979) give higher values.

In the second section, the resulting ratio was derived from a simultaneous spectroscopic measurement of both the Herzberg I system and the 2972 Å line where the 5577Å intensity was deduced using the Kernahan and Pang (1975) branching ratio. At the time of the Hennes (1966) measurement, lack of adequate spectroscopic data precluded a reliable fit to the data. Furthermore, Degen's (1969) analysis of that data did not treat the intensity of the 2972Å feature. We have reanalyzed that spectrum using the synthetic code applied to this experiment and find that Hennes' (1966) measured intensity ratio agrees with that reported here. The ratio of the Herzberg I to 5577 Å emission derived in this manner is about 1.0.

It might be argued that due to the presence of the Vegard-Kaplan feature in the data, contamination by high-altitude auroral emission could be a cause of our discrepancy. We may consider the aurora to be at about a latitude of 50° N, which is not inconceivable given the geomagnetic activity level. The line of sight to 50° N would intersect the aurora at a tangent height of 180 km. Using the ratio of 3 for VK (0,6) to 2972 Å at 180 km from Sharp (1970) and a slant intensity of 580 R for the VK(0,6) band, an intensity of 193 R is calculated for the slant intensity of 2972 Å which is only 5% to the signal. An important factor in this discussion is the similarity in the ratio reported here and the Hennes (1966) results. His data were obtained from limb observations also but, they were to the east from White Sands Missile Range where no possibility of auroral contamination exists. Our inferred greenline zenith intensity of 1800 R is significantly greater than previous measurements; the brightest given by Murtagh et al., (1989) is only 400 R. We therefore suggest that there is a problem with the branching ratio for 2972Å from the ¹S state.

Although 2972 Å emission has been measured in a variety of other contexts, such as the terrestrial aurora (Sharp, 1970) and the Venusian dayglow (LeCompte et al. 1989), we note that no simultaneous aeronomic measurements of 2972 Å and 5577 Å exist. Until such a measurement is made and the branching ratio confirmed, the use of the 2972 Å emission to infer the total $O(^{1}S)$ emission could lead to error.

2852 Å Line

Excess emission near 2850 Å is noted in Figure 1a. A comparison of our data with Hennes' (1966) shows that this feature is not present in the earlier spectrum. This can be most clearly seen by noting that in Hennes' spectrum, the (7,2) band at 2732 Å is slightly brighter than the (7,3) band, while in our data the (7,3) appears significantly brighter. As seen in Figure 1b, both of these features are relatively uncontaminated by other Herzberg bands and since the relative intensities of two bands in a given v' progression are fixed by the transition probabilities, the most likely explanation for the excess is a contamination by a heretofore unidentified emission.

An expanded view of this feature is shown in Figure 2 along with an estimate of the error in the data due to counting statistics. The excess intensity encompasses about 5-6 wavelength bins or about 9-10 Å. This is too narrow in spectral extent to be a molecular feature and thus is most likely an atomic line. Since Mg is known to be present in the lower thermosphere (Swider, 1984) and since it has a resonance transition at 2852 Å, the excess emission is postulated to be the Mg I resonance line.

Nightglow from metallic atoms (e.g., Na, K) has been previously discussed (e.g. Swider, 1987). There is a transition to the ground state in sodium (5p-3s) at 2852Å, but the exothermicity of the reaction NaO with O is not sufficient to produce uv photons. The analogous reaction with magnesium is not exothermic enough to produce a uv photon either. Rocket measurements have shown that Mg⁺ is the dominant metal ion in the nighttime lower E region (Aiken and Goldberg, 1973). Thus an ion-chemical mechanism related to the effective recombination of Mg⁺ is a possible source for the emission.



Fig. 2. The wavelength interval around the Mg emission at 2852 Å. The error bar on the data (solid line) represents the 1 sigma counting statistics. The difference between the synthetic spectra (dashed line) and the data at 2870 Å is not statistically significant as it may result from small errors in the wavelength scale of the instrument.

Ferguson and Fehsenfeld (1968) present the chemistry of converting Mg⁺ to Mg through a series of recombinations involving the oxides of the Mg ion. They deduce an expression for the effective recombination rate which is

$$K_{eff} = K_{MgO+} [MgO^+]/[Mg^+]$$
(1)

$$= 7 \text{ K}_{\text{MgO+}} [O_3]/[O]$$
 (2)

where the radiative recombination of Mg⁺ is ignored as is the recombination of MgO2⁺. The rate coefficients measured at 300^oK (Rowe, et al., 1981) were used. To estimate the densities of Mg⁺ and ne required to produce the emission, we express the intensity as

$$4\pi I = K_{eff} [Mg^+] [n_e] \Delta H$$
(3)

 ΔH is the half thickness of the emission layer, taken to be about 10 km. From Table 2, the vertical intensity is 11.5 R so that

$$K_{\text{eff}}[Mg^+][n_e] \cong 11 \tag{4}$$

Using observed nighttime O3 and O densities (Hays and Roble, 1973; Sharp, 1980), we estimate Keff to be about 5 x 10⁻⁹ cm³ sec⁻ ¹ at 95 km. Given the brightness of the Herzberg emission, the [O] is likely to be greater than that observed by Sharp (1980). If the higher MSIS-86 O densities are used, the rate decreases to about 2 x 10^{-9} cm³ sec⁻¹. Assuming that the electrons and Mg ions are equal, one obtains an ion density of $4 - 7 \times 10^4$ cm⁻³ for these rate ranges.

Support for this hypothesis comes from an ionosonde measurement made that night from Boulder, Colorado, which indicated the presence of sporadic E. The peak electron density inferred from the signal of 3.3 MHz at 102 km is 1.5×10^5 cm⁻³. As a result, the identification of this emission feature as coming from the ionic recombination of Mg⁺ is the most likely hypothesis. Since this feature does not appear in the Hennes (1966) data, its presence seems to depend upon significant enhancements of the Mg concentrations, as would be expected during major meteor shower events.

Conclusions

Data gathered from a mid-latitude rocket borne experiment to measure the middle uv nightglow has identified the presence of the Herzberg I, II, and possibly III emission, an anomalously intense 2972Å emission from $O(^{1}S)$ which raises a question about the branching ratio from $O(^{1}S)$, and excess emission at 2850 Å which is identified to be from Mg I.

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