

GNSS-R Non-Local Sea State Dependencies: Model and Empirical Verification

David D. Chen-Zhang, Christopher S. Ruf, Fabrice Ardhuin, and Jeonghwan Park

Abstract

Global Navigation Satellite System Reflectometry (GNSS-R) is an active, bistatic remote sensing technique operating at L-band frequencies. GNSS-R signals scattered from a rough ocean surface are known to interact with longer surface waves than traditional scatterometry and altimetry signals. A revised forward model for GNSS-R measurements is presented which assumes an ocean surface wave spectrum that is forced by other sources than just the local near-surface winds. The model is motivated by recent spaceborne GNSS-R observations that indicate a strong scattering dependence on significant wave height, even after controlling for local wind speed. This behavior is not well represented by the most commonly used GNSS-R scattering model, which features a one-to-one relationship between wind speed and the mean-square-slope of the ocean surface. The revised forward model incorporates a third generation wave model that is skillful at representing long waves, an anchored spectral tail model, and a GNSS-R electromagnetic scattering model. In comparisons with the spaceborne measurements, the new model is much better able to reproduce the empirical behavior.

1 Introduction and Overview

Global Navigation Satellite System Reflectometry (GNSS-R) is a relatively young remote sensing technique proposed to measure geophysical quantities such as ocean surface roughness and wind speed. With it quickly gaining momentum [Zavorotny et al., 2014], there has been rapid and ongoing development of instrumentation [e.g., Gleason et al., 2016], retrieval algorithms [e.g., Clarizia et al., 2014] and scattering models [e.g., Zavorotny and Voronovich, 2000; Lin and Katzberg, 1999]. GNSS-R is a relatively low-cost technique which leverages existing navigation signals as the transmitter half of the bistatic radar system. This technique makes use of a forward scattering geometry, in contrast to conventional monostatic scatterometers and altimeters, which use a back scattering geometry. The frequency of operation is dictated by the transmitters, which are typically L-band (1-2 GHz) navigation satellites.

The combination of L-band signals and forward scattering geometry has been rarely used in the past by remote sensing instruments, and thus brings about new implications for electromagnetic interaction with surface features. In particular, bistatic L-band radar return is dominated by quasi-specular scattering, which is dictated by waves longer than about 3 times the electromagnetic wavelength [e.g., Valenzuela, 1978; Brown, 1978]. In the ocean, L-band GNSS-R is therefore sensitive to surface waves of about 50 cm in wavelength and longer. In contrast, for radar scatterometers, according to two-scale models, these 50 cm waves are tilting waves that bring about mostly secondary effects compared to the primary Bragg scatterers. Although radar altimeter scattering is also primarily quasi-specular, they typically operate at higher C-band (5 GHz) or Ku-band (13 GHz) frequencies (e.g., TOPEX/Poseidon ALT [Fu et al., 1994]), which correspond to wavelengths of order one centimeter. For typical ocean roughness spectra, these centimeter scale features dominate the roughness, so the ~50 cm scale waves in most cases play only a minor role for altimetric sensors.

43 Modelling GNSS-R ocean scattering at L-band presents novel challenges. Short gravity waves tens of
44 centimeters long are in a different regime than the millimeter capillary waves, because they are
45 governed by different physics. With surface tension being negligible, these short gravity waves take
46 longer to dissipate and propagate further before decaying. There have been questions [Cardellach, 2014]
47 and results showing non-negligible GNSS-R sensitivity to long gravity waves. However, such waves have
48 yet to be taken into account in GNSS-R forward models. For example, the end-to-end simulator for the
49 upcoming Cyclone Global Navigation Satellite System (CYGNSS) mission [Ruf et al., 2016a] uses the
50 Katzberg relationship to model the roughness, which assumes that the scattering cross section is
51 determined by the local, instantaneous wind speed alone [Ruf et al., 2016b]. The limitation of this
52 assumption is illustrated in Section 3, below, in which spaceborne scattering measurements are shown
53 to exhibit large differences from those predicted by the Katzberg-model (e.g., Figure 8 and Figure 9). The
54 differences are most pronounced, and considered significant, at lower wind speeds.

55
56 In this paper, our objective is to develop, and then experimentally validate, a more accurate GNSS-R
57 forward model by incorporating forcing effects other than local winds. In Section 2, we present the
58 model, which includes a third-generation wave model that has not previously been incorporated into a
59 GNSS-R forward model. The rationale for the choice of the surface model and parameters therein are
60 discussed. In Section 3, we compare spaceborne measurements with our model predictions and with the
61 predictions produced by the Katzberg model. We conclude with a discussion of some of the non-local
62 effects that contribute to the scattering measurements predicted by our model, and consider other,
63 second-order, effects that have not been incorporated into the model but could be as future work.

64 2 The Forward Model

65 2.1 Surface Wave Models

66 For phase-averaging surface wave models, one important goal is to quantify the spectral energy
67 accurately in the form of a wave spectrum, which can range from a one-dimensional directionally-
68 integrated spectrum in the simplest case to a full three-dimensional frequency-wavenumber-direction
69 spectrum for linear and nonlinear waves. These models can generally be divided into two types: 1.
70 empirical models based on dimensional analysis and parameterized by wind speed and, possibly, wave
71 age, and 2. spectral evolution models based on the energy-balance equation.

72
73 The first type constrains the shape of the spectrum, which is typically a smooth function of the input
74 parameters. Usually, conditions are classified as duration- or fetch-limited [Hwang and Wang, 2004], and
75 the wave age is computed accordingly. The wave age and windspeed are then used to parameterize the
76 wave spectrum. The Pierson-Muskowitz [Pierson and Moskowitz, 1964], JONSWAP [Hasselmann et al.,
77 1973], Elfouhaily [Elfouhaily et al., 1997], and Hwang [Hwang et al., 2013] spectra are of this type. The
78 second type of model includes WAVEWATCH3 [Tolman et al., 2014] (denoted by WW3 hereafter),
79 University of Miami Wave Model [Donelan et al., 2012], SWAN [Booij et al., 1999], and WAM [Komen et
80 al., 1994]. These models solve the energy balance equation numerically, a Eulerian form of which in
81 simple cases (conditions given below) may be expressed as

$$82 \quad \frac{\partial E(k, x, t)}{\partial t} + c_g \frac{\partial E(k, x, t)}{\partial x} = S(k, x, t) , \quad (1)$$

83 where E is the one-dimensional wavenumber-direction spectrum with SI units of m^3 , with the
84 wavenumber energy spectrum being $\rho g E$ with units of J/m . ρ is the mass density of sea water, and g is
85 the gravitational constant. c_g is the group velocity in the x direction. $S(k, x, t)$ is the collective source
86 term combining the effects of wind input, whitecapping dissipation, and non-linear wave-wave

87 interaction. Equation (1) models the temporal evolution and spatial propagation of the elevation
 88 variance of a one-dimensional wave in deep water and neglects the effects of currents. In practice, an
 89 equation of this type is discretized and integrated in time and space to solve for the wave spectrum at
 90 each time step and grid point. The source terms, with improved understanding of wave physics, have
 91 undergone significant development in the last 50 years, and are now in their “3rd generation” [Komen et
 92 al., 1994].

93
 94 For the second type of wave model, rather than having an a-priori form, the individual source terms are
 95 crafted, and the spectrum is left free to evolve. Before the 1950s, models of the first kind were used for
 96 wave forecasting. However, several aspects are challenging for the parametric models to handle, such as
 97 the accounting for swell generated afar, and irregular bathymetry and coastlines [Ardhuin, 2016 p.52].
 98 In addition, Chen et al. [2016] found that two such empirical models show significant errors in modelling
 99 the response time of waves to wind in general conditions, while later investigations showed the third-
 100 generation model WW3 performs significantly better in comparisons with in-situ measurements.

101
 102 Despite its shortcomings, the parametric models and the associated experiments that led to them, are
 103 widely used when modelling idealized duration and fetched-limited cases. These ideal cases have been
 104 invaluable in the development of the spectral-evolution models’ source terms, and they continue to
 105 serve as reference calibration points for the state-of-the-art third generation models. Moreover, these
 106 parametric models are considered the current state-of-the-art models for high frequency waves. The
 107 form and shape of the spectral tail assumed in the model is still an area of active research [Ex. Plant,
 108 2015, Reichl et al., 2015, Hwang et al., 2013], partly due to the challenges in their accurate
 109 measurement [Hwang, 2005]. Many electromagnetic models to-date have incorporated these
 110 parametric models [e.g., Voronovich and Zavorotny, 2001; Apel, 1994; Hwang and Fois, 2015] as the
 111 surface wave model, with the inverse wave age often set to 0.84 for “well-developed” conditions. It
 112 should be noted that formulations of source term balance of short Bragg waves have been attempted
 113 [e.g. Lyzenga et al., 1988], but much uncertainty remain [Hwang et al., 2013].

114
 115 For GNSS-R, the surface roughness of relevance is the low-pass-filtered mean square slope (mss)

$$116 \quad LP_{mss}(k_u) = \int_0^{k_u} k^2 S(k) dk \quad (2)$$

117
 118 Empirically, Brown [1978] found $k_u = \frac{2\pi \cos \theta}{3\lambda}$ to be a suitable cutoff, with λ being the
 119 electromagnetic wavelength and θ denoting the incidence angle of the observation. For the GPS L1
 120 carrier with a frequency of 1.575 GHz, and typical incidence angles of less than 35 degrees, $k_u \approx 10$
 121 rad/m, so waves of about 60 cm and longer are sensed by GNSS-R. We mention in passing that the
 122 quantity significant wave height, usually denoted as H_s and used in our analysis in Section 3, can be
 123 computed from the wavenumber spectrum as
 124

$$125 \quad H_s = 4 \sqrt{\int_0^{\infty} S(k) dk} \quad (3)$$

126 Once the wave spectrum is known, LP_{mss} can be readily calculated. Katzberg et al. [2013] developed a
 127 semi-empirical, one-to-one relationship between windspeed and mean squared slope by fitting data
 128 provided by airborne GNSS-R experiments and an adjusted high resolution windspeed model. The

129 Katzberg model is even simpler than the parametric wave models because it does not involve the wave
130 spectrum. This relationship is expressed as follows

131

$$LP_{mss} = 0.45(0.00316f(U_{10}) + 0.00192f(U_{10}) + 0.003)$$

132

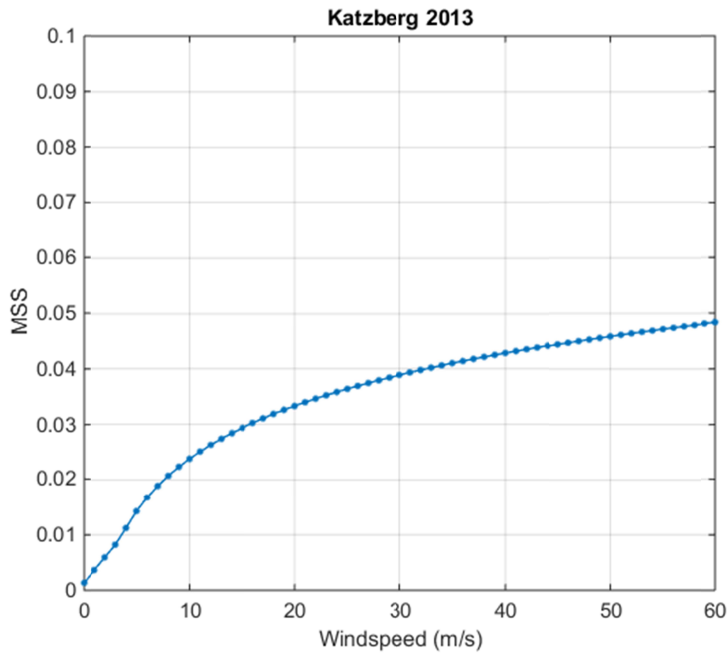
$$f(U_{10}) = U_{10}, \quad 0 < U_{10} < 3.49 \text{ m/s}$$
$$f(U_{10}) = 6 \ln(U_{10}) - 4, \quad 3.49 < U_{10} < 46$$
$$f(U_{10}) = 0.411U_{10}, \quad 46 < U_{10}$$

133

134

(4)

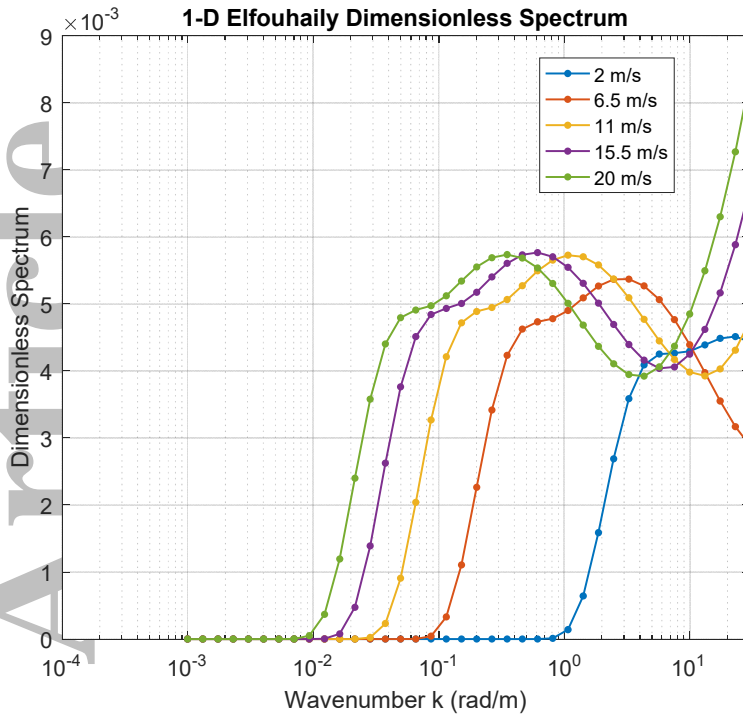
135 where U_{10} is the windspeed at 10 m height. It is plotted in Figure 1.



136 Figure 1 The Katzberg U_{10} -mss relationship

137 The end-to-end simulator for CYGNSS [Ruf et al., 2016a], which ingests windspeed and generates the
138 delay-Doppler-map, currently uses the Katzberg relationship.

139 According to the Elfouhaily spectra shown in Figure 2, the long waves contribute a considerable portion
140 of the LP_{mss} sensitivity to wind. Such characteristics are similar to other spectra [e.g., Fig. 6 of Apel,
141 1994].



145
146 *Figure 2: Elfouhaily slope spectrum in area-conservative form. The relevant portion for GNSS-R is about 10 rad/m and below.*

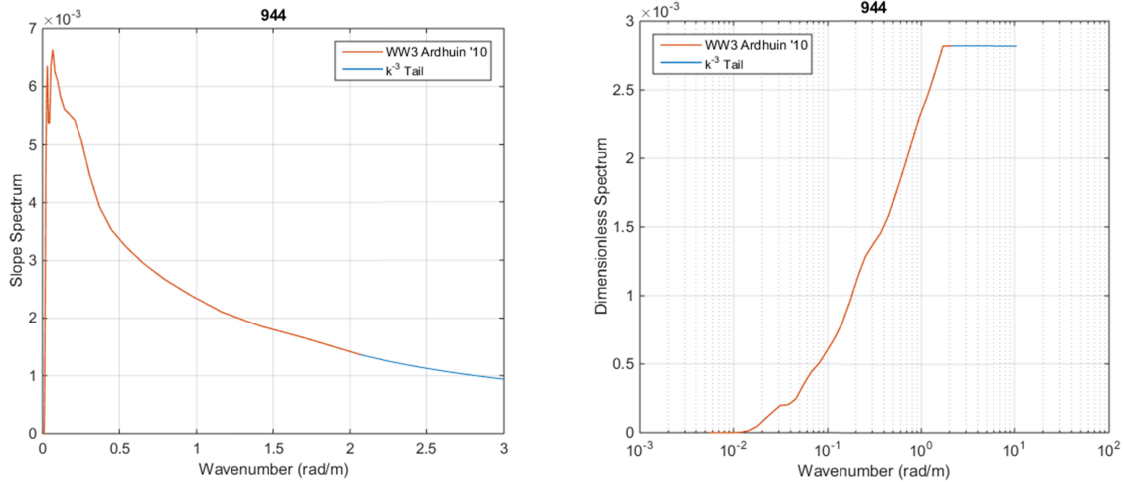
147 As noted above, the inclusion of a third-generation model, which focuses on the energy-containing long
 148 waves, has not been necessary for other sensing techniques. Whether a model would benefit GNSS-R is
 149 a question we explore in this work. As third-generation wave models have demonstrated considerable
 150 skill in forecasting wave properties near the spectral peak (such as H_s and T_p) [e.g., The WAMDI Group,
 151 1988; Ardhuin et al. 2010; Chu et al., 2004], we make use of this type of model in our work. In particular,
 152 we select WAVEWATCH III® (WW3) as the low-frequency wave model, which is run operationally by the
 153 National Weather Service (NWS). The source terms of WW3 include wind input, dissipation, non-linear
 154 interaction, bottom friction, ice scattering, among others.

155
 156 Since our interest is in mss, we use the Ardhuin et al. [2010] source term package, which is the only
 157 reported source term package for WW3 validated for mss. Along with WW3, this package is open-source
 158 to users in most countries. As mentioned earlier, the spectral tail of high frequency waves is not
 159 completely resolved at the time of writing. All third-generation waves thus explicitly model the wave
 160 spectrum only up to a certain frequency, and attach a high-frequency tail thereafter. We select a simple
 161 k^{-3} spectral tail, which is suggested by the work of Banner et al. [1989], Forristall [1981], and Phillips
 162 [1958]; it was also used recently by Reichl et al. [2015] in a high-frequency model based on WW3. The
 163 tail is attached at the last frequency modeled by WW3, and thus is completely determined by the value
 164 of the spectrum at that frequency. A more elaborate model may include a high-frequency model like
 165 that of Plant [2015], Hwang et al. [2013], or Elfouhaily [1997], but this option is not pursued here.

166
 167 Our WW3 run is driven by the ECMWF operational wind analysis, and has 3-hour temporal output
 168 resolution and 0.5-degrees latitude and longitude spatial resolution. The last wavenumber before
 169 spectral tail attachment is 2.06 rad/m. The k^{-3} spectral tail ends at k_u , which is determined by the
 170 incidence angle of the track under consideration. For our simulation, the model is driven by wind only;
 171 currents play a minimal role globally [Bidlot, personal communication, 2016] - however, in hurricane

172 conditions, currents can have a significant role [Fan et al., 2009]. We limit ourselves to non-hurricane
 173 conditions in this work, and thus neglect currents. In the following, we refer to the WW3 with spectral
 174 tail attached as the extended WW3 model.

175
 176 An example of the attachment of the spectral tail is shown in Figure 3.
 177



178
 179 Figure 3: Example of extended WW3 slope spectrum with a) linear scale (plot upper limit adjusted to 3 rad/m), b) area
 180 conservative form.

181 2.2 GNSS-R Electromagnetic Scattering and Signal Processing Model

182 The ZV model developed by Zavorotny and Vornovich [2000] is a widely used scattering and signal
 183 processing model for the GNSS-R received signal. This model is based on geometrical optics (GO) and is
 184 valid for a sufficiently rough surface and non-grazing incidence. In practice, the ocean surface can be
 185 considered sufficiently rough at wind speeds above about 3 m/s and non-grazing incidence angles are
 186 those below about 70 degrees. The received signal is a function of delay and frequency. A two-
 187 dimensional plot of the signal power is known as a Delay Doppler Map (DDM) (explained in greater
 188 detail in Section 3). Because the ZV model connects the wave model and the observables and is
 189 pertinent to our signal processing methods, we discuss it here in some detail.

190
 191 The signal power intercepted by the receiver antenna can be expressed as
 192

$$193 \quad P_s(\tau, f) = CP_t \iint \frac{G_t G_{rant}}{R_t^2 R_r^2} \chi^2(\Delta\tau, \Delta f) \sigma_0(\vec{s}) dA \quad (5)$$

194
 195 where $P_s(\tau, f)$ is the signal power for delay τ and frequency f . C is a constant that depends on the
 196 electromagnetic wavelength and coherent integration period of the receiver. P_t is the GPS transmitter
 197 power and is assumed to be constant, as is G_t , the product of transmitter antenna and instrument gains.
 198 G_{rant} is the receiver antenna gain. and R_t, R_r are the distances from the dummy integration position
 199 on the grid to the transmitter and receiver, respectively. The surface integral is performed over an area
 200 large enough for the desired τ and f ranges, and is known as the glistening zone. For us, τ ranges over
 201 about 30 μ s and f ranges over about 10 kHz. The glistening zone is chosen to be 200 km by 200 km

202 centered at the specular point, which is sufficient for most scattering geometries of the TDS-1
 203 instrument considered in Section 2.3.

204
 205 $\Delta\tau = |\tau_g - \tau|$, with τ_g being the delay associated with the location of the differential surface element,
 206 dA. $\tau_g = (R_t + R_r)/c$ and for a given geometry, it is a constant for a given surface location,
 207 independent of τ and f . Similarly, $\Delta f = f_g - f$, and $f_g = -f_{CW} / c(\vec{u}_R \cdot \vec{v}_R + \vec{u}_T \cdot \vec{v}_T)$. f_{CW} is the
 208 frequency of the carrier wave; for the GPS L1 carrier, it is 1.575 GHz. \vec{u}_R is the unit vector from the
 209 specular point to the receiver, \vec{v}_R is the receiver velocity vector, \vec{u}_T is the unit vector from the specular
 210 point to the transmitter, and \vec{v}_T is the transmitter velocity vector.

211
 212 $\chi^2(\Delta\tau, \Delta f)$ is known as the ambiguity function and models the selectivity of the radar system. Letting
 213 τ_0 and f_0 be the delay and Doppler shift corresponding to the specular point, respectively, if the

214 selectivity is sufficiently high such that $\frac{G_t G_{rant}}{R_t^2 R_r^2} \sigma_0$ is constant for some small area ΔA around the
 215 specular point, then, because $\chi^2(0,0) = 1$

$$216 \quad 217 \quad 218 \quad P_{s0} = P_S(\tau_0, f_0) = CP_t \frac{G_t G_{rant}}{R_t^2 R_r^2} \sigma_0 \Delta A \quad (6)$$

219
 220 We make use of this equation in Section 2.3.

221
 222 Similar to τ_g , f_g , G_t , G_{rant} , R_t , and R_r , \vec{s} is also a constant for a given location (independent of τ , f)
 223 – it specifies the favorable orientation (two perpendicular slope components) of a facet that reflects the
 224 incident ray toward the receiver. The scattering cross section $\sigma_0(\vec{s})$ is where the surface roughness
 225 enters – under geometric optics, σ_0 is proportional to the PDF of slopes as well as the square of the
 226 Fresnel surface reflectivity. The PDF of slopes and its measurement remain an active area of research
 227 [e.g., Cardellach and Rius, 2008; Liu et al., 1997]. To a first order, the PDF of slopes can be approximated
 228 by a bivariate Gaussian

$$229 \quad 230 \quad pdf(s_u, s_c) = \frac{1}{2\pi\sqrt{mss_u mss_c}} \exp\left\{-\frac{1}{2}\left(\frac{s_u^2}{mss_u} + \frac{s_c^2}{mss_c}\right)\right\} \quad (7)$$

231
 232 where the subscripts u and c denote the upwind and crosswind components. This assumption is also
 233 used in Zavorotny and Voronovich [2000]. At the specular point, $pdf(0,0)$ is proportional to the inverse
 234 of the geometric mean of the mss components. It should be noted that more complex PDFs have also
 235 been considered.

236 In this work, we further assume that the seas are isotropic and the two components of mss are equal.
 237 Equivalently, the two-dimensional PDF is rotation-invariant in the sense that it only depends on the
 238 magnitude of \vec{s} . Note that the mss is obtained from WW3 using equation (2).

239

240 2.3 Model Configuration and Post-Processing for TDS-1

241 TechDemoSat-1 (TDS-1) is a technology demonstration mission operated by Surrey Satellite Technology
242 Limited (SSTL) [Unwin et al., 2016]. One of its payloads is the Space GNSS Receiver Remote Sensing
243 Instrument (SGR-ReSI), the GNSS-R instrument of interest. TDS-1 has a circular orbit with an altitude of
244 about 630 km. Because there are other instruments on the TDS-1 mission, the SGR-ReSI has limited
245 operating time, so the data it collects are limited. In this paper, all references to TDS measurements
246 refer to data collected by the SGR-ReSI.

247

248 From Section 2.2, several pieces of information are required to compute the received signal. The GPS
249 transmitted power is not published, so it is assumed to be constant. The other parameters needed are:

- 250 - transmitter position and velocity,
- 251 - receiver position and velocity,
- 252 - receiver antenna and instrument (RF and IF) gains, and
- 253 - mss.

254

255 All these quantities are functions of time. For a moving receiver, the specular point traces out a
256 trajectory in time across the ground known as a track. In this work, two surface models are used for
257 computing the mss: the Katzberg model and the extended WW3 model. The GPS transmitter and TDS
258 receiver positions and velocities, along with the TDS receive antenna pattern, are furnished by SSTL.
259 However, the instrument gain is not available; in fact, the receiver has automatic gain control (AGC)
260 turned on, so the instrument gain changes with signal level, and this time-varying gain is not recorded.
261 We therefore process the DDMs in a way that is not sensitive to the gain value, by forming the ratio
262 between their signal and noise regions. The resulting DDMs are of relative received power, normalized
263 by the noise floor of the measurements. They are still sufficiently sensitive to changes in the surface
264 conditions, provided variations in the receiver noise floor are small enough over relevant time scales.

265

266 The glistening zone is set to 200 km by 200 km. This determines the surface area over which the
267 numerical integration is taken in the model. The wind and mss are assumed to be constant over the area
268 of integration.

269

270 In addition to the contribution to the received signal power by scattering from the ocean surface, P_s in
271 Equation (5) also contains other components due to radiometric thermal emission by the scene, noise
272 due to the receiver instrumentation (including the antenna), and radio-frequency interference (RFI) [e.g.,
273 Chen et al. 2015]. We neglect RFI in this paper. The total received signal (in uncalibrated units of counts)
274 can then be modelled as

275

$$276 C_T(\tau, f) = G_{ri}(P_N + P_s) \quad (8)$$

277

278 where G_{ri} is the receiver instrument gain (excluding the antenna gain) and P_N is the total noise power.

279 P_N includes the radiometric thermal emission from the scene referred to the output of the antenna and

280 the noise due to receiver instrumentation. P_s is the GNSS-R signal power, given by the ZV model in

281 Equation (5). To be precise, P_s is the ensemble mean of the signal power. In practice, there will also be

282 speckle noise present in the measurements. Our model neglects the speckle noise and estimates the

283 ensemble mean.

284
 285
 286
 287
 288
 289
 290
 291
 292
 293
 294
 295
 296
 297
 298
 299
 300
 301
 302
 303
 304
 305
 306
 307
 308
 309
 310
 311
 312
 313
 314
 315
 316
 317
 318
 319
 320
 321
 322
 323
 324
 325

The noise contributions to the measurements are estimated by examining pixels of the DDM at delay values that correspond to altitudes higher than the surface. As such, these pixels contain no scattered surface signal and $P_s=0$ can be assumed. In that case, the uncalibrated measurements can be written as

$$C_N = G_{ri}(P_N) \tag{9}$$

The pixel in the DDM with the highest power is assumed to correspond to the specular point location. This is only approximate, as the peak power originates from a region near but not necessarily at the specular point. With two equations $C_T(\tau_0, f_0) = G_{ri}(P_N + P_s(\tau_0, f_0))$ and $C_N = G_{ri}(P_N)$, we cannot completely resolve the three unknowns, $P_s(\tau_0, f_0)$, G_{ri} , and P_N . It should be noted that the upcoming CYGNSS mission carries an augmented version of the receiver that incorporates calibration targets and fixed receiver gain, so these unknowns can be determined. For TDS, no absolute calibration can be performed and the DDMA observable [Clarizia et al., 2014] is not easily computed. (An observable is a single number characterization of the DDM.)

Because of this, a proxy for the DDMA, known as the SNR [Jales, 2015], is now being used in the TDS community. It is defined by

$$SNR = \frac{C_T(\tau_0, f_0) - C_N}{C_N} = \frac{G_{ri}(P_N + P_s) - G_{ri}(P_N)}{G_{ri}(P_N)} = \frac{G_{ri}(P_s)}{G_{ri}(P_N)} = \frac{P_s}{P_N} \tag{10}$$

We see that the SNR observable is independent of gain as desired, but depends on the noise power. Gain varies much faster than the noise power – the dominant factor is changes due to instrument temperature and AGC adjustments.

For our simulations, we only model P_s and do not model the thermal noise. To estimate P_N , we compute the ratio between the measured SNR and the modeled P_s over an entire track. Thus:

$$P_N = \frac{E[P_s^{sim}]}{E[SNR^{TDS}]} \tag{11}$$

where $E[.]$ is the time average operator, P_s^{sim} is the simulated signal power, and SNR^{TDS} is the TDS-measured SNR. This assumes that P_N is constant over the track, and there are no biases to P_s . With P_N known, the simulated SNR can then be computed.

The computation of modelled SNR requires the extraction of a single parameter from the measurements. Note that there are other observables that could alternately be used, such as the DDM volume observable [Marchan-Hernandez et al, 2008]. This observable, fundamentally, makes use of the ratio of the signal powers from DDM bins far away from the specular point to those at or near the specular point. We have considered this observable in our analysis and the results are similar in character to those using the SNR presented in Section 3, but they are found to exhibit a large noise level than the SNR observable. For this reason, we will use an SNR-related observable in the following discussions.

326 To focus on the effects of sea state, we define the Scaled SNR as:
 327

$$328 \quad SSNR = SNR \frac{R_{tSP}^2 R_{rSP}^2}{G_{rant}} \quad (12)$$

329
 330 where R_{tSP} and R_{rSP} are the distances from the specular point to the transmitter and receiver,
 331 respectively.

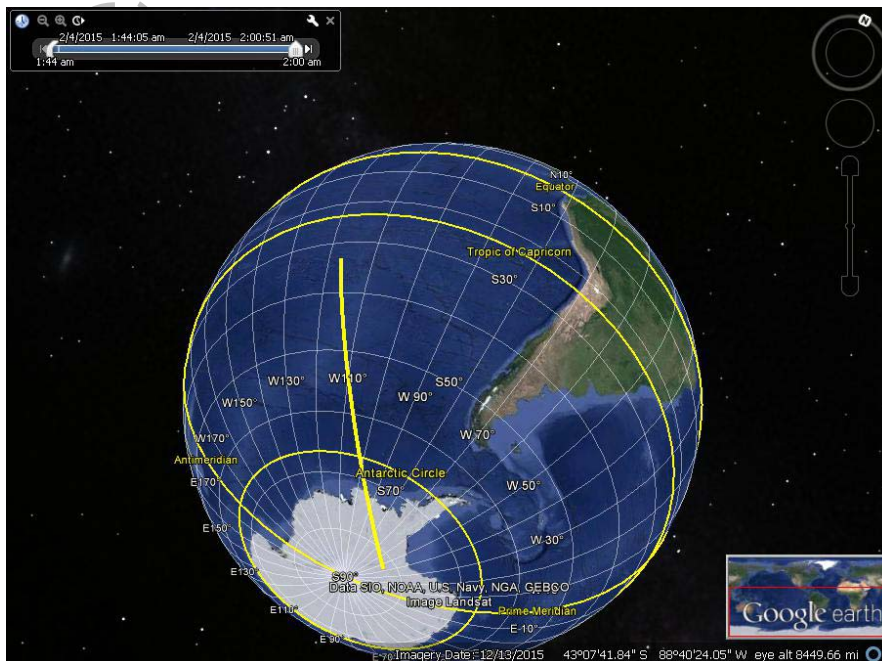
332
 333 We neglect scaling corrections for scattering area and incidence angle-dependent Fresnel reflectivity for
 334 simplicity and because the measurement geometries present in the TDS sample population do not
 335 exhibit significant variations.

336
 337 Lastly, we note that for a given geometry, higher mss values (greater roughness) correspond to smaller
 338 SNR values.

339 3 Results and Discussion

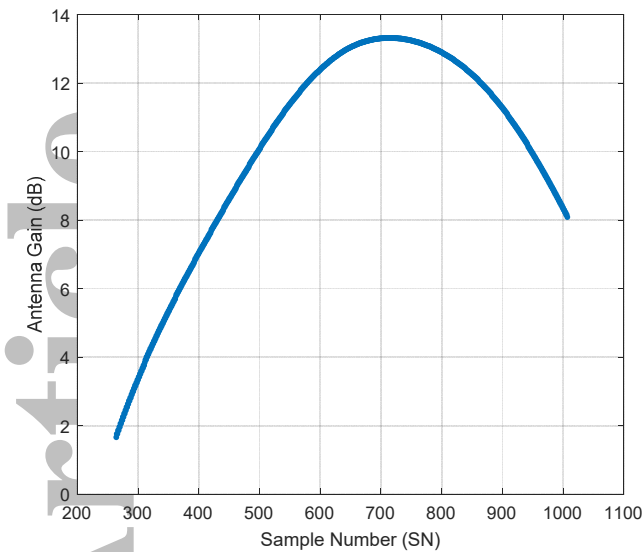
340 We analyze one TDS track in this work: Track 407 in RD 17 of SSTL's Version 0.3 dataset. This track
 341 contains about 16 minutes of continuous data, collected by a single receiver channel and a single GPS
 342 transmitter (GPS PRN #10 and Receiver Channel #2, per SSTL's numbering conventions). One DDM is
 343 produced every second. This track exhibits a good variation of coastal and oceanic conditions, as well as
 344 a variety of sea states. The track of the specular point is plotted in Figure 4.

345



346
 347 *Figure 4: The specular point track for RD17 TR407 is shown as the bold yellow line running from Antarctica into the South Pacific.*
 348 *The data is numbered from 1 to 1007, which we call sample number (SN). The transition from land to ocean occurs at SN 264.*

349 The receive antenna gain along the track is plotted in Figure 5. The variation in gain results from the
 350 progression of transmitter and receiver locations, and the resulting change in measurement geometry,
 351 over time.



352
353 *Figure 5: Along-track antenna gain for RD17 TR407 for specular points in the ocean; the SN ranges from 264 to 1007.*

354 Because antenna gain can affect the signal quality, we consider only measurements with gain greater
 355 than 3 dB in our analysis. In addition, since our interest is in ocean GNSS-R, we filter out any data with its
 356 specular point located less than 100 km away from the coast. The resulting dataset has sample numbers
 357 ranging from 293 to 1007. This is the rationale for restricting the grid size to be 200 km by 200 km as
 358 mentioned in Section 2. Relative to the specular point, delay and Doppler bins with less than 18 us and
 359 5000 Hz in either direction are considered, and this is the range plotted in the DDMs shown below. The
 360 average incidence angle for the track under consideration is 13.8 degrees, which results in a cut-off
 361 wavenumber, k_w , of 10.59 rad/m or 59 cm in wavelength.

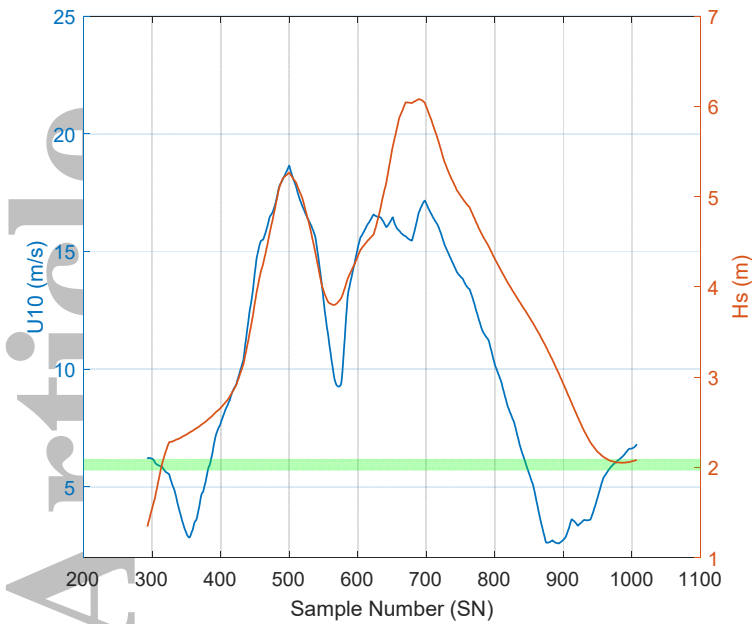
362

363 3.1 Empirical Evidence of Measurement Sensitivity to Significant Wave Height

364 As seen from Equations (2) and (3), significant wave height, H_s , is much more sensitive to long waves
 365 than the mean square slope. These long waves include swell that is not correlated with wind. In this
 366 subsection, we explore the dependence of SSNR (and thus mss) on H_s using TDS measurements.

367

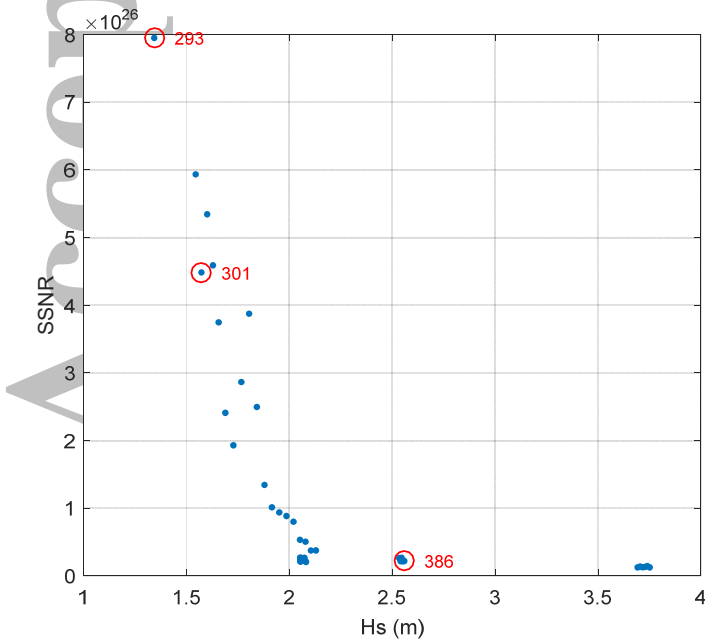
368 In Figure 6, U_{10} and H_s are plotted against sample number (SN) for Track 407. Each SN is separated by
 369 approximately one second, and, for this track, the specular points of two consecutive measurements are
 370 spaced about 6000 m apart. H_s is obtained from spatial interpolation of the same WW3 model run, as
 371 WW3 is skillful in modelling H_s . U_{10} comes from the same ECMWF wind reanalysis product that is used
 372 to force the WW3 model.



373
 374 Figure 6: Along track U_{10} (left axis) and H_s (right axis). The green band denotes a narrow range of U_{10} values, the relevance of
 375 which is discussed in the text.

376 Although U_{10} exhibits some correlation with H_s , there are many points where they deviate from one
 377 another. To control for U_{10} and examine the variance of the SSNR explained by H_s alone, we restrict our
 378 analysis to measurements for which U_{10} lies in the narrow range between 5.7 and 6.2 m/s. This region is
 379 shaded by a horizontal green band in Figure 6. A scatterplot of the measured SSNR vs. H_s values in this
 380 region is shown in Figure 7.

381
 382



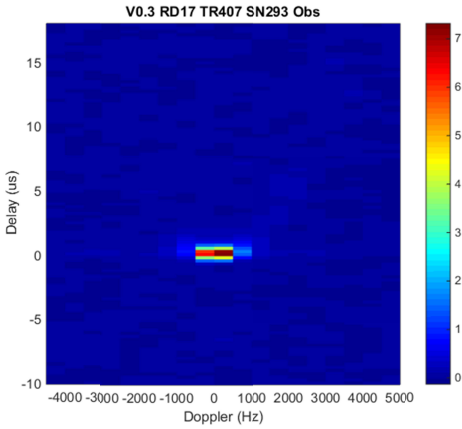
383
 384 Figure 7: Measurement SSNR observable vs. H_s with U_{10} between 5.7 and 6.2 m/s - this range is shown by the green band in
 385 Figure 6.

386 Hs is seen to have a strong effect on SSNR that cannot be accounted for solely by windspeed. This
387 behavior has been noted previously [Soisuvarn et al., 2016]. Some scatter is also seen, indicating that
388 SSNR has additional variability explained by neither Hs nor windspeed. In the figure, we have picked
389 three representative measurements; these are circled in red with their SNs indicated. We examine their
390 DDMs in this and the next subsections.

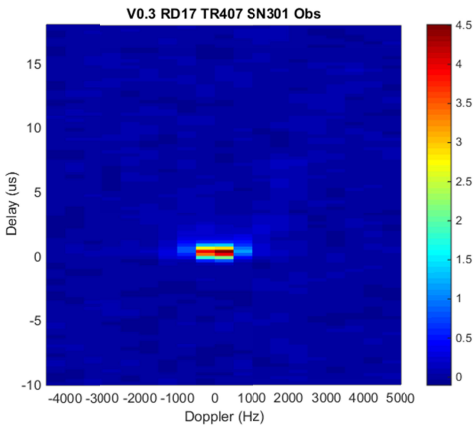
391
392 The three DDMs measured by TDS are presented in Figure 8. Both the magnitude and shape of the
393 DDMs change significantly. The magnitude decreases monotonically as Hs increases, which is consistent
394 with theoretical expectations. The mss corresponding to each of the DDMs can be estimated using
395 either the Katzberg or WW3 model. In the case of Katzberg, all three wind speeds are nearly the same,
396 so the mss is, too. It is 0.0172. With the WW3 model, mss is not solely dependent on wind speed and
397 the mss is found to be 0.00028, 0.00063, and 0.0122 for SN 293, 301, and 386, respectively. The
398 significant differences in mss with the WW3 model are due to other influences on the local sea state
399 than simply the wind speed there. In particular, note that the significant wave height varies significantly
400 between the three cases.

401
402

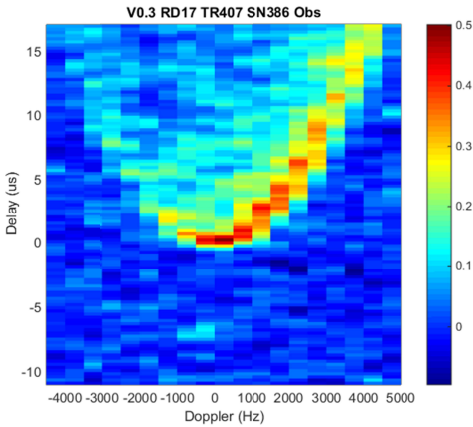
Accepted Article



403



404



405

406

407

Figure 8: TDS Measurements. Top panel: SN 293 with $H_s=1.34$ m and $U_{10}=6.19$ m/s. Middle panel: SN 301 with $H_s=1.57$ m and $U_{10}=6.18$ m/s. Bottom panel: SN 386 with $H_s=2.13$ m and $U_{10}=5.70$ m/s.

408

3.2 Modeling the Effect of Significant Wave Height on the Measurement

409

410

411

412

413

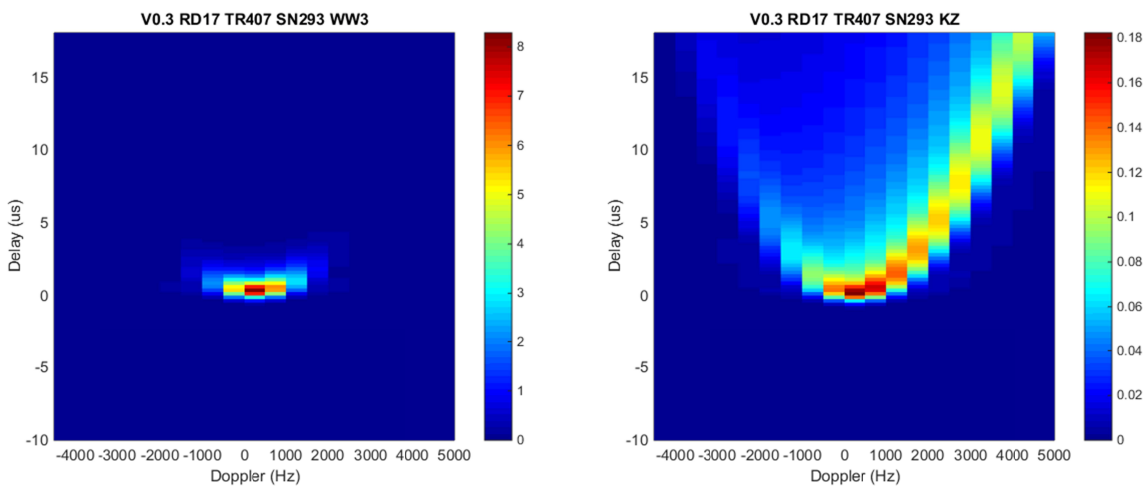
414

415

In this subsection, we examine modelled results and compare them to the measurements in the previous subsection. First, we look at the modelled DDMs of the three cases considered. Second, we look at the dependence on H_s predicted by the models. Lastly, we look at the along-track plots of the SSNR.

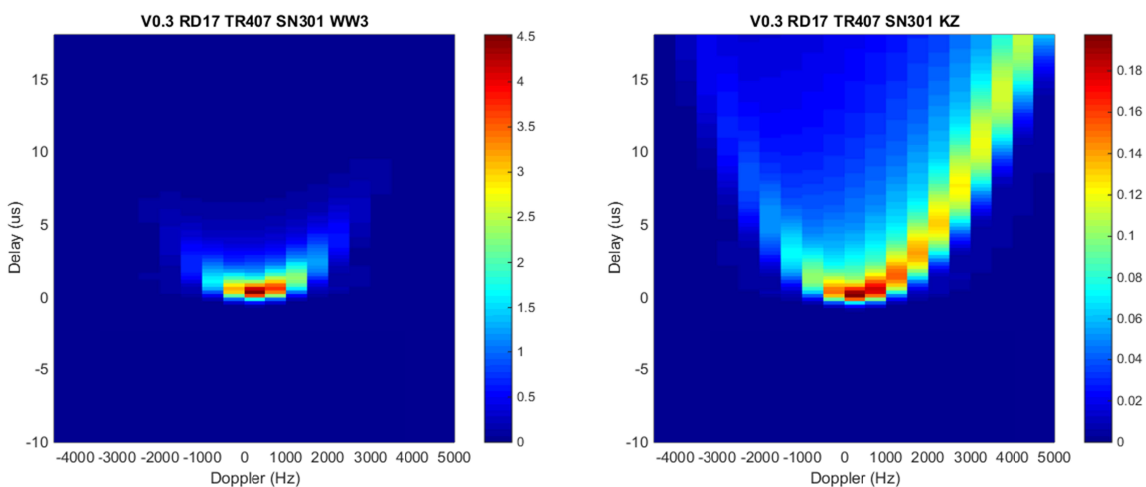
Because the windspeed is essentially the same in all three cases, the Katzberg DDMs should all look about the same. This is indeed the case, as seen the modelled DDMs in Figures 9-11 (right panels). The

416 left panels show the results of the extended WW3 model. Comparing to the TDS measurements in
417 Figure 8, it is seen that the WW3-based model is much better able to represent the behavior of the
418 measurements, compared to the Katzberg model, in both the magnitude and shape of the DDMs.
419



420
421 *Figure 9: DDMs predicted by the two forward models: WW3 (left) and Katzberg (right) given ocean conditions $H_s=1.34$ m and*
422 *$U_{10}=6.19$ m/s consistent with observation SN 293. Compare to the top panel in Figure 8. For WW3, the DDM is in good*
423 *agreement with the observation. For Katzberg, both the shape and signal magnitude show large discrepancies.*

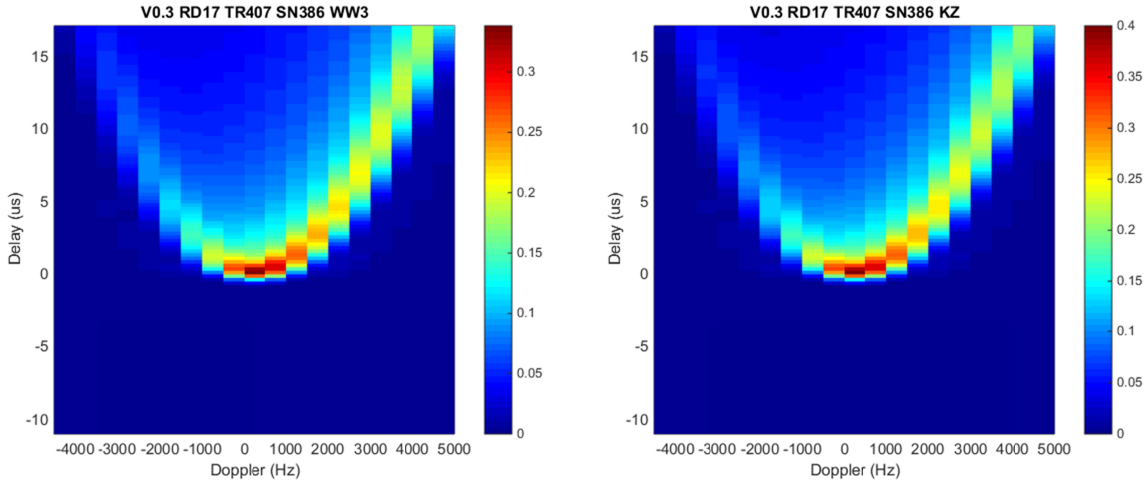
424



425
426 *Figure 10: DDMs predicted by the two forward models: WW3 (left) and Katzberg (right) given ocean conditions $H_s=1.57$ m and*
427 *$U_{10}=6.18$ m/s consistent with observation SN 301. Compare to the middle panel in Figure 8. For WW3, the DDM is in good*
428 *agreement with the observation. For Katzberg, both the shape and signal magnitude show large discrepancies.*

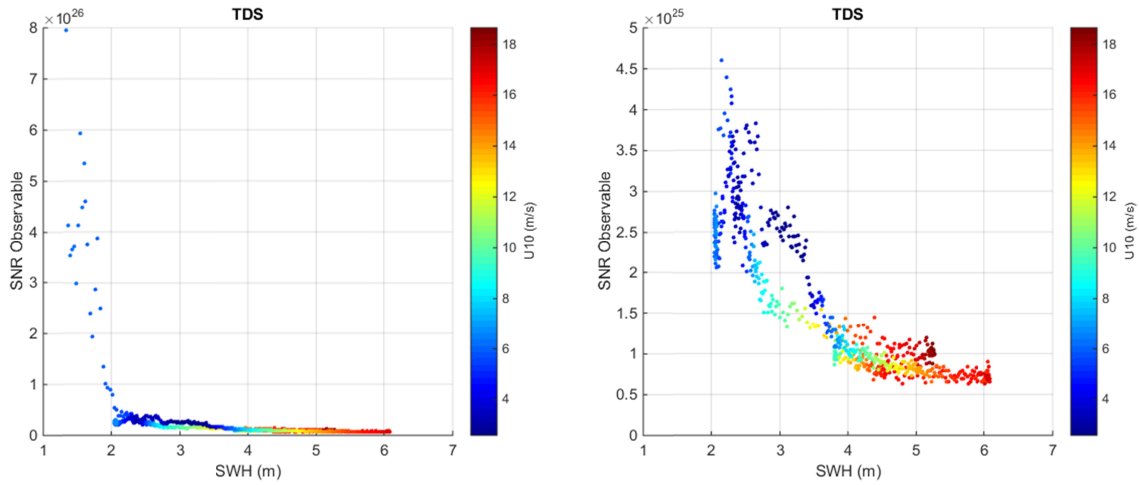
429

430

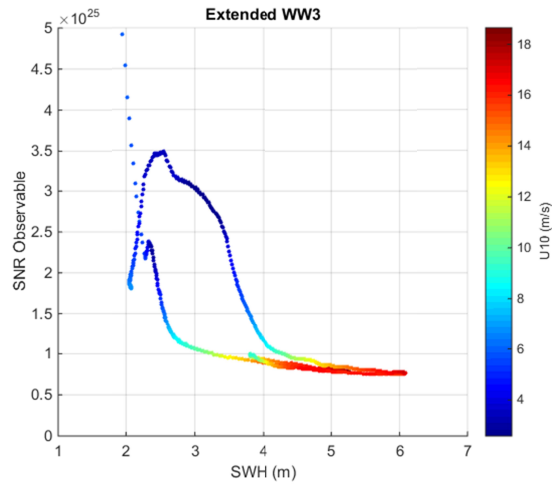
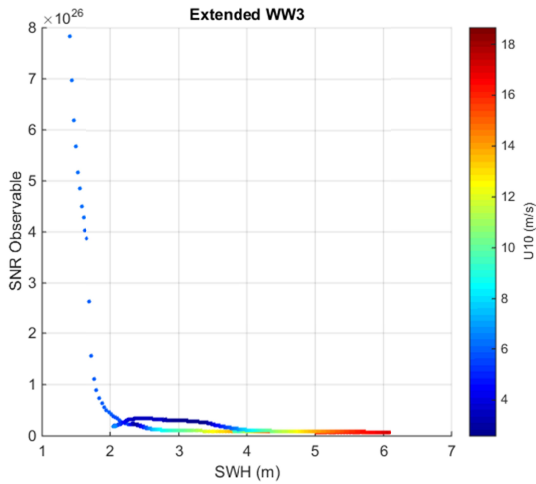


431
 432 *Figure 11: DDMs predicted by the two forward models: WW3 (left) and Katzberg (right) given ocean conditions $H_s=2.13$ m and*
 433 *$U_{10}=5.70$ m/s consistent with observation SN 386. Compare to the bottom panel in Figure 8. Both models are both in good*
 434 *agreement with the observations.*

435 We now plot modelled SSNR vs. H_s in Figure 12. These plots reaffirm WW3's skill over the Katzberg
 436 model. In particular, significant improvement is seen for low H_s values; these were found to occur at the
 437 beginning of the track near the coast. In addition, the Katzberg model demonstrates deficiencies in the
 438 "branch" near $H_s=3$ m and $SSNR=3e25$; these correspond to very low windspeeds of less than 3 m/s.
 439

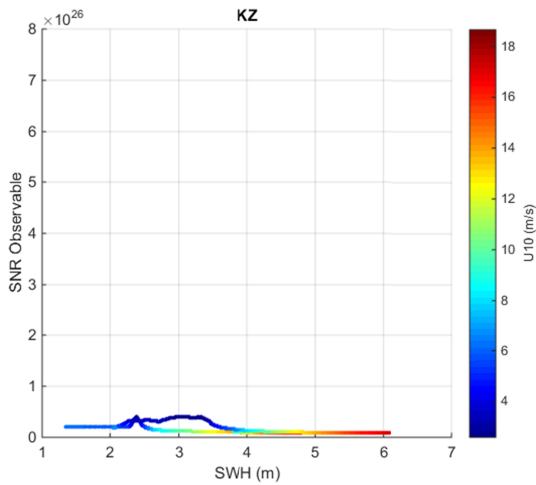


440
 441
 a.

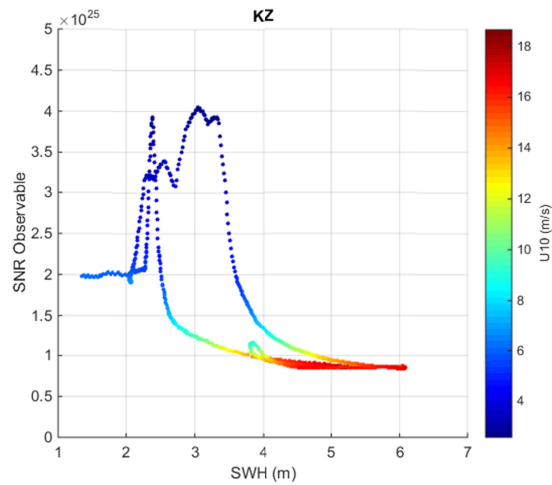


442

443



b.



444

445

c.

446 *Figure 12: SSNR vs. SWH, with U10 colorcoded. The figures in the right column are zoomed in versions of the ones on the left. a)*
 447 *TDS – these two plots are characteristically the same as Figure 7, but no filtering is done based on U10 b) Extended WW3 c)*
 448 *Katzberg. Because of the inverse dependence of mss, SNR is much more sensitive to mss changes when mss is small.*

449 To gain additional insight, we plot the SSNR vs. along-track SN for the TDS measurements and both
 450 models in Figure 13. This figure should be used in conjunction with Figure 6, which shows the along-
 451 track U_{10} and Hs. Using the variance of the difference between simulations and measurements as the
 452 metric, the extended WW3 model shows a 68.7% improvement over the Katzberg model over the entire
 453 track. The improvements in the coastal region at the start of the track is one significant contributor. If
 454 we consider only SN 342 and higher, we still see a 30.2% improvement in the skill of the extended WW3
 455 model. This improvement can largely be attributed to the SNs 850 to 900, for which the windspeed is
 456 very low.

457

458

459

460

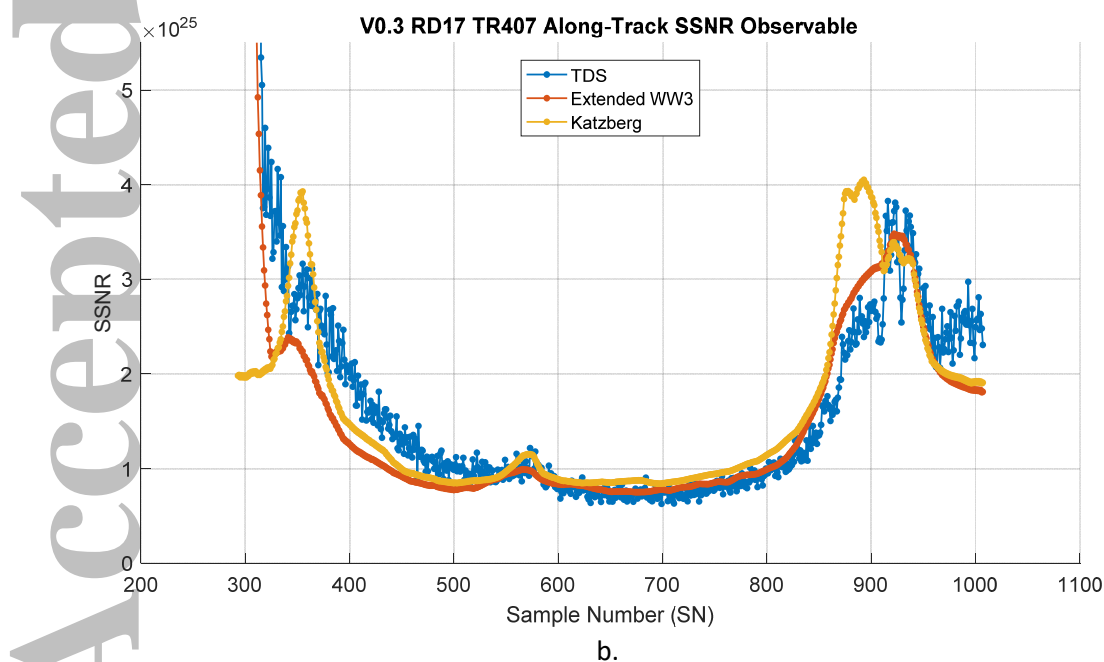
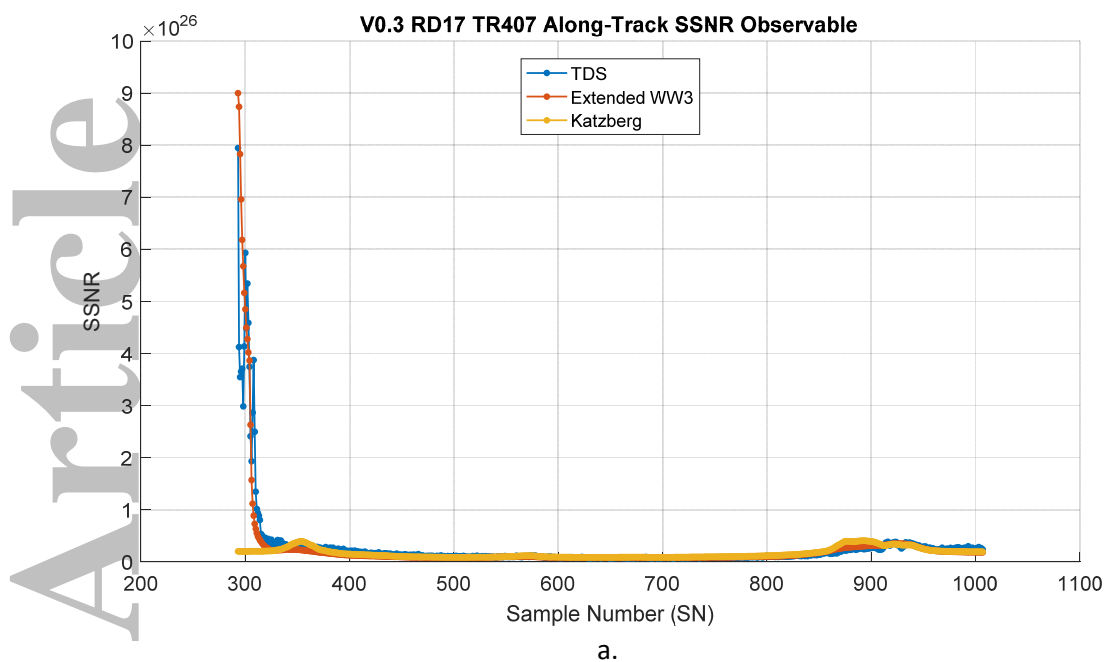


Figure 13. a. Along track plot of measured SSNR, extended WW3 SSNR, Katzberg SSNR, and scaled H_s and U_{10} . b. Zoomed in version of a.

468 Another insight is that despite the attachment of a diagnostic tail, we see WW3 is also responsive to
469 local wind: at SNs from about 900 to 950, H_s is decreasing but windspeed is increasing (see Figure 6).
470 WW3 is able to model the decreasing behavior of the observable correctly.
471

472 This analysis shows that the extended WW3 model has considerable skill modelling the GNSS-R
473 observable, derived from its ability to take non-local long waves into account, and in modelling the sea
474 state in low windspeed conditions.

475
476 One implication of our results is that much of the sensitivity of the GNSS-R observable to the sea state
477 derives from long and intermediate-scale waves of wavenumber 2 rad/m and lower. This is consistent
478 with predictions of the parametric Elfouhaily model shown in Figure 2. However, it should be noted that
479 this track does not contain winds that change quickly in time. A track with rapid changes in wind
480 temporally and spatially will be able to better evaluate whether the diagnostic tail should be replaced
481 one that has an explicit wind speed dependence. Fast changes in wind may also necessitate that the
482 model be run at a higher spatial and temporal resolution with the corresponding wind speed products.

483
484 Lastly, we note that both models show overly low SSNRs between serial numbers 350 and 500, while a
485 slightly positive bias is seen between 600 and 850. These discrepancies can be the result of an overall,
486 constant bias that is not removed before determining and applying the SSNR scale factor in Equation
487 (11). Such a bias may be due to errors in the cutoff k_u , or the spectral level. This bias may also
488 contribute to the difference in shapes of the measured and WW3 DDMs shown in Figure 8 and Figure 10.

489 4 Conclusions and Future Work

490 In this work, we have developed a GNSS-R forward model that incorporates a third-generation surface
491 wave model. The analysis of one track of TDS measurements, with over 700 consecutive DDMs, shows
492 that this model can account for observable dependencies on the local wind as well as other, non-local
493 effects. In contrast to conventional remote sensing techniques, the non-local effects are significant for
494 GNSS-R due to frequency and geometry. The model demonstrates improved skill over the widely used
495 Katzberg one-to-one windspeed-mss model. Significant improvements are seen in low wind conditions,
496 in particular. The novelty and strength of the model is derived from the WW3 model, the source terms
497 of which are the result of decades of work by the wave modeling, experimental, and remote sensing
498 communities. Conversely, given the demonstrated sensitivity of GNSS-R to ocean surface wave spectra,
499 the assimilation of its measurements into numerical wave models may also provide valuable constraints
500 on the derived sea state.

501
502 The use of a third generation wave model in GNSS-R forward modelling has great potential for future
503 work. Some ideas include:

- 504 - Retrieval of mss from the measurements, and taking into account scattering area and Fresnel
505 reflectivity,
- 506 - Modelling of anisotropic seas with two mss components and a more sophisticated pdf of slopes, in
507 effect creating a tighter coupling between the scattering and wave models,
- 508 - Relaxation of assumption of uniformity of wind and mss fields over the 200 km by 200 km glistening
509 zone,
- 510 - Augmenting the scattering model by taking the coherent scattering component into account for low
511 windspeeds,
- 512 - Usage of CYGNSS data when it becomes available; with absolute calibration, better signal quality can
513 be achieved, and
- 514 - Addition of wave-current interactions in the wave model.

515
516 To understand the underlying physical phenomena modelled by WW3 that allows it to produce better
517 long-wave mss, it would be helpful to examine the two-dimensional wave spectra, as well as the source

518 term spectra. Those insights may lead to the development of ancillary parameters that could be helpful
519 in constructing better wind retrieval algorithms for GNSS-R.

520
521 The model presented here can also be used to improve our understanding of surface waves with GNSS-R
522 measurements. Possibilities include the tuning of the spectral tail and development of appropriate
523 source terms. The model is also expected to be helpful in the design of future GNSS-R missions and
524 experiments.

525 5 Acknowledgements

526
527 This work was funded in part by the National Aeronautics and Space Administration (grant NNX13AP93H
528 and contract NNL13AQ00C). TechDemoSat-1 data used in this study are available from the publically
529 accessible MERRByS web site at <http://www.merrbys.co.uk>. Wavewatch III data used in this study are
530 available from the publically accessible NOAA web site at
531 <http://polar.ncep.noaa.gov/waves/ensemble/download.shtml>.

532 6 References

533 Apel, J. R. (1994), An improved model of the ocean surface wave vector spectrum and its effects on
534 radar backscatter, *J. Geophys. Res.*, 99(C8), 16269–16291, doi:10.1029/94JC00846.

535
536 Arduin, Fabrice, Erick Rogers, Alexander V. Babanin, Jean-François Filipot, Rudy Magne, Aaron Roland,
537 Andre van der Westhuysen, Pierre Queffelec, Jean-Michel Lefevre, Lotfi Aouf, and Fabrice Collard,
538 2010: Semiempirical Dissipation Source Functions for Ocean Waves. Part I: Definition, Calibration, and
539 Validation. *J. Phys. Oceanogr.* 40, 1917–1941, doi: 10.1175/2010JPO4324.1.

540
541 Arduin, Fabrice (2016), Ocean Waves in Geosciences Available:
542 ftp://ftp.ifremer.fr/ifremer/ww3/COURS/waves_in_geosciences_2016.pdf Accessed: July 29, 2016

543
544 Banner, M. L., I. S. F. Jones, and J. C. Trinder (1989), Wavenumber spectra of short-gravity waves, *J. Fluid*
545 *Mech.*, 198, 321–344, doi:10.1017

546
547 Booij, N., R. C. Ris and L. H. Holthuijsen, 1999, A third-generation wave model for coastal
548 regions, Part I, Model description and validation, *J. Geophys. Res.*, 104, C4, 7649–7666

549
550 Brown, G. "Backscattering from a Gaussian distributed perfectly conducting rough surface," *IEEE Trans.*
551 *Antennas Propag.*, vol. AP-26, no. 3, pp. 472–482, May 1978.

552
553 Cardellach and Rius, 2008, A new technique to sense non-Gaussian features of the sea surface from L-
554 band bi-static GNSS reflections, *Remote Sensing of Environment*, Volume 112, Issue 6, 16 June 2008,
555 Pages 2927–2937, ISSN 0034-4257, <http://dx.doi.org/10.1016/j.rse.2008.02.003>.

556
557 Cardellach, E., S. G. Jin, and F. Xie, Chapter 9 of *GNSS Remote Sensing: Theory, Methods and*
558 *Applications*. New York, London: Springer, 2014.

559
560 Chen, D. D.; C. S. Ruf; S. T. Gleason (2016), Response time of mean square slope to wind forcing: An
561 empirical investigation, *J. Geophys. Res. Oceans*, 121, 2809–2823, doi:10.1002/2016JC011661.

562

563 Chen, D.D.; Ruf, C.S., "Adaptive Control of Undetected Radio Frequency Interference With a Spaceborne
564 Microwave Radiometer," in *Geoscience and Remote Sensing, IEEE Transactions on*, vol.53, no.9,
565 pp.4972-4984, Sept. 2015 doi: 10.1109/TGRS.2015.2414395
566

567 Peter C. Chu, Yiquan Qi, Yuchun Chen, Ping Shi, and Qingwen Mao, 2004: South China Sea Wind-Wave
568 Characteristics. Part I: Validation of Wavewatch-III Using TOPEX/Poseidon Data. *J. Atmos. Oceanic
569 Technol.*, 21, 1718–1733, doi: 10.1175/JTECH1661.1.
570

571 Clarizia, M. P., Ruf, C.; Jales, P. and Gommenginger, C., "Spaceborne GNSS-R Minimum Variance Wind
572 Speed Estimator," *IEEE Trans Geosci. Remote Sens.*, 52(11), 6829-6843, doi:
573 10.1109/TGRS.2014.2303831, Nov. 2014.
574

575 Donelan, M. A., M. Curcic, S. S. Chen, and A. K. Magnusson, 2012, Modeling waves and wind stress, *J.
576 Geophys. Res.*, 117, C00J23, doi:10.1029/2011JC007787.
577

578 Elfouhaily, Chapron, Katsaros and Vandemark, 1997, "A unified directional spectrum for long and short
579 wind-driven waves", *Journal of Geophysical Research*, Vol 102, No. C7, pp 15,781-15,796, July 15, 1997.
580

581 Yalin Fan, Isaac Ginis, and Tetsu Hara, 2009: The Effect of Wind–Wave–Current Interaction on Air–Sea
582 Momentum Fluxes and Ocean Response in Tropical Cyclones. *J. Phys. Oceanogr.*, 39, 1019–1034, doi:
583 10.1175/2008JPO4066.1.
584

585 Forristall, G. Z. (1981), Measurements of a saturated range in ocean wave spectra, *J. Geophys. Res.*,
586 86(C9), 8075–8084, doi:10.1029
587

588 Fu, L.-L., E. J. Christensen, C. A. Yamarone Jr., M. Lefebvre, Y. Ménard, M. Dorrer, and P. Escudier (1994),
589 TOPEX/POSEIDON mission overview, *J. Geophys. Res.*, 99(C12), 24369–24381, doi:10.1029/94JC01761.
590

591 Gleason, S., C. Ruf, M. P. Clarizia, A. O'Brien, "Calibration and Unwrapping of the Normalized Scattering
592 Cross Section for the Cyclone Global Navigation Satellite System (CYGNSS)," *IEEE Trans. Geosci. Remote
593 Sens.*, doi: 10.1109/TGRS.2015.2502245, 2016.
594

595 Hasselmann, K. et al., 1973, "Measurements of wind-wave growth and swell decay during the Joint
596 North Sea Wave Project (JONSWAP)", *Dtsch. Hydrogh. Z., Suppl. A*, 8, 12, 95pp.
597

598 Hwang, P.A., and David W. Wang, 2004: Field Measurements of Duration-Limited Growth of Wind-
599 Generated Ocean Surface Waves at Young Stage of Development*. *J. Phys. Oceanogr.*, 34, 2316–2326.
600 doi: [http://dx.doi.org/10.1175/1520-0485\(2004\)034<2316:FMODGO>2.0.CO;2](http://dx.doi.org/10.1175/1520-0485(2004)034<2316:FMODGO>2.0.CO;2)
601

602 Hwang, P. A. (2005), Wave number spectrum and mean square slope of intermediate-scale ocean
603 surface waves, *J. Geophys. Res.*, 110, C10029, doi:10.1029/2005JC003002.
604

605 Hwang, P.A., Derek M. Burrage, David W. Wang, and Joel C. Wesson, 2013: Ocean Surface Roughness
606 Spectrum in High Wind Condition for Microwave Backscatter and Emission Computations*. *J. Atmos.
607 Oceanic Technol.*, 30, 2168–2188. doi: <http://dx.doi.org/10.1175/JTECH-D-12-00239.1>
608

609 Hwang, P. A., and F. Fois (2015), Surface roughness and breaking wave properties retrieved from
610 polarimetric microwave radar backscattering, *J. Geophys. Res. Oceans*, 120, 3640–3657,
611 doi:10.1002/2015JC010782.
612

613 Jales, P., (2015), “MERRByS Product Manual - GNSS Reflectometry on TDS-1 with the SGR-ReSI,” Tech.
614 Rep. SSTL report No. 0248366 Revision 001, Surrey Satellite Technology Ltd; Available from
615 <http://www.merrbys.co.uk>.
616

617 Katzberg, S. J., J. Dunion, and G. G. Ganoë (2013), The use of reflected GPS signals to retrieve ocean
618 surface wind speeds in tropical cyclones, *Radio Sci.*, 48, 371–387, doi:10.1002/rds.20042.
619

620 Komen, G. J., L. Cavaleri, M. Donelan, K. Hasselmann, S. Hasselmann, and P. A. E. M. Janssen, Eds.,1994:
621 *Dynamic and Modelling of Ocean Waves*. Cambridge University Press, 532 pp.
622

623 Lin, B., S. J. Katzberg, J. L. Garrison, and B. A. Wielicki (1999), Relationship between GPS signals reflected
624 from sea surfaces and surface winds: Modeling results and comparisons with aircraft measurements, *J.*
625 *Geophys. Res.*, 104(C9), 20713–20727, doi:10.1029/1999JC900176.
626

627 Liu, Y., Yan, X. H., Liu, W. T., & Hwang, P. A. (1997). The probability density function of ocean surface
628 slopes and its effects on radar backscatter. *Journal of physical oceanography*, 27(5), 782-797.
629

630 Lyzenga, D. R., and J. R. Bennett (1988), Full-spectrum modeling of synthetic aperture radar internal
631 wave signatures, *J. Geophys. Res.*, 93(C10), 12345–12354, doi:10.1029/JC093iC10p12345.
632

633 Marchan-Hernandez, N. Rodriguez-Alvarez, A. Camps, X. Bosch-Lluis, I. Ramos-Perez and E. Valencia,
634 "Correction of the Sea State Impact in the L-Band Brightness Temperature by Means of Delay-Doppler
635 Maps of Global Navigation Satellite Signals Reflected Over the Sea Surface," in *IEEE Transactions on*
636 *Geoscience and Remote Sensing*, vol. 46, no. 10, pp. 2914-2923, Oct. 2008.
637 doi: 10.1109/TGRS.2008.922144
638

639 Pierson W.J., and L. Moskowitz, “A proposed spectral form for fully developed wind seas based on the
640 similarity theory of S.A. Kitaigorodskii”, *Journal of Geophysical Research* 69: 5181–5190, 1964.
641

642 Phillips, O. M. (1958), The equilibrium range in the spectrum of wind generated waves, *J. Fluid Mech.*, 4,
643 426–434.
644

645 Plant, W. J. (2015), Short wind waves on the ocean: Wavenumber-frequency spectra, *J. Geophys. Res.*
646 *Oceans*, 120, doi:10.1002/2014JC010586.
647

648 Reichl, B. G., T. Hara, and I. Ginis (2014), Sea state dependence of the wind stress over the ocean under
649 hurricane winds, *J. Geophys. Res. Oceans*, 119, 30–51
650

651 Ruf, C. S., R. Atlas, P. S. Chang, M. P. Clarizia, J. L. Garrison, S. Gleason, S. J. Katzberg, Z. Jelenak, J. T.
652 Johnson, S. J. Majumdar, A. O’Brien, D. J. Posselt, A. J. Ridley, R. J. Rose, V. U. Zavorotny, 2016a “ New
653 Ocean Winds Satellite Mission to Probe Hurricanes and Tropical Convection,” *Bull. Amer. Meteor. Soc.*,
654 doi:10.1175/BAMS-D-14-00218.1, pp385-395, Mar 2016.
655

656 Ruf, C., P. Chang, M.P. Clarizia, S. Gleason, Z. Jelenak, J. Murray, M. Morris, S. Musko, D. Posselt, D.
657 Provost, D. Starkenburg, V. Zavorotny, 2016b. CYGNSS Handbook, Ann Arbor, MI, Michigan Pub., ISBN
658 978-1-60785-380-0, 154 pp, 1 Apr 2016.
659
660 Soisuvarn, S., Z. Jelenak, F. Said, P. S. Chang, and A. Egido, "The GNSS reflectometry response to the
661 ocean surface winds and waves," IEEE J. Sel. Topics Appl. Earth Observ. Remote Sens., 9(10), 2016.
662
663 Tolman, H. L. and the WAVEWATCH III Development Group, March 2014: User manual and system
664 documentation of WAVEWATCH III version 4.18. NOAA / NWS / NCEP / MMAB Technical Note 316.
665
666 Unwin, M., P. Jales, J. Tye, C. Gommenginger, G. Fotti and J. Rosello, "Spaceborne GNSS-Reflectometry
667 on TechDemoSat-1: Early Mission Operations and Exploitation," IEEE J. Sel. Topics Appl. Earth Observ.
668 Remote Sens., doi: 10.1109/JSTARS.2016.2603846, 9(10), 2016.
669
670 Valenzuela, G.R. "Theories for the Interaction of Electromagnetic and Oceanic Waves: A Review," Bdry-
671 Layer Met., 13, p. 61, 1978.
672
673 The Wamdi Group, 1988: The WAM Model—A Third Generation Ocean Wave Prediction Model. J. Phys.
674 Oceanogr., 18, 1775–1810, doi: 10.1175/1520-0485(1988)018<1775:TWMTGO>2.0.CO;2.
675
676 Voronovich, A. G., and V. U. Zavorotny (2001), Theoretical model for scattering of radar signals in Ku and
677 C bands from a rough sea surface with breaking waves, Waves Rand. Media, 11, 247– 269.
678
679 Zavorotny, V.U.; Voronovich, A.G., 2000, "Scattering of GPS signals from the ocean with wind remote
680 sensing application," in Geoscience and Remote Sensing, IEEE Transactions on , vol.38, no.2, pp.951-964,
681 Mar 2000 doi: 10.1109/36.841977
682
683 Zavorotny, S. Gleason, E. Cardellach and A. Camps, "Tutorial on Remote Sensing Using GNSS Bistatic
684 Radar of Opportunity," in IEEE Geoscience and Remote Sensing Magazine, vol. 2, no. 4, pp. 8-45, Dec.
685 2014.
686 doi: 10.1109/MGRS.2014.2374220

Figure 1.

Accepted Article

Katzberg 2013

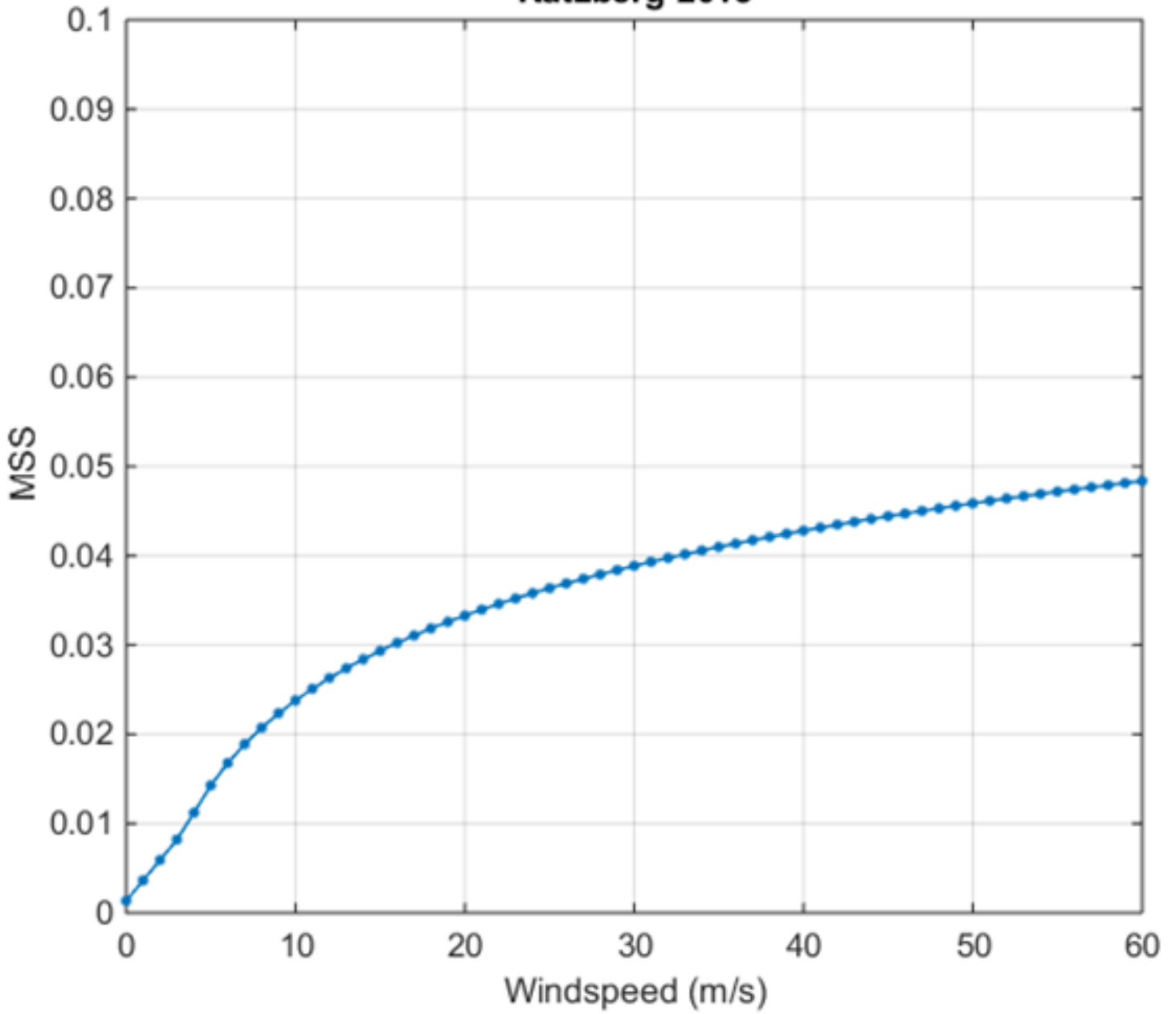


Figure 2.

Accepted Article

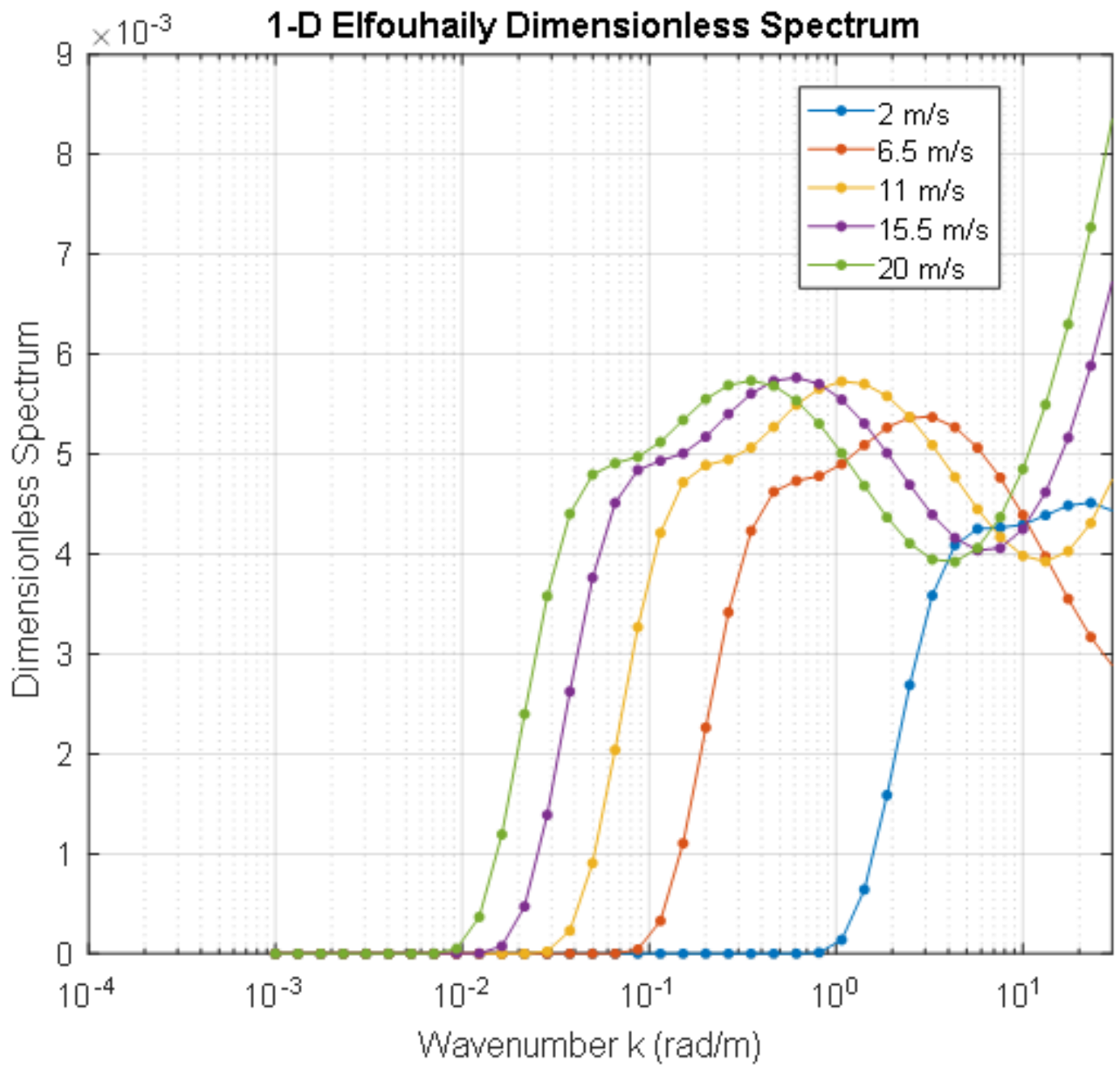


Figure 3.

Accepted Article

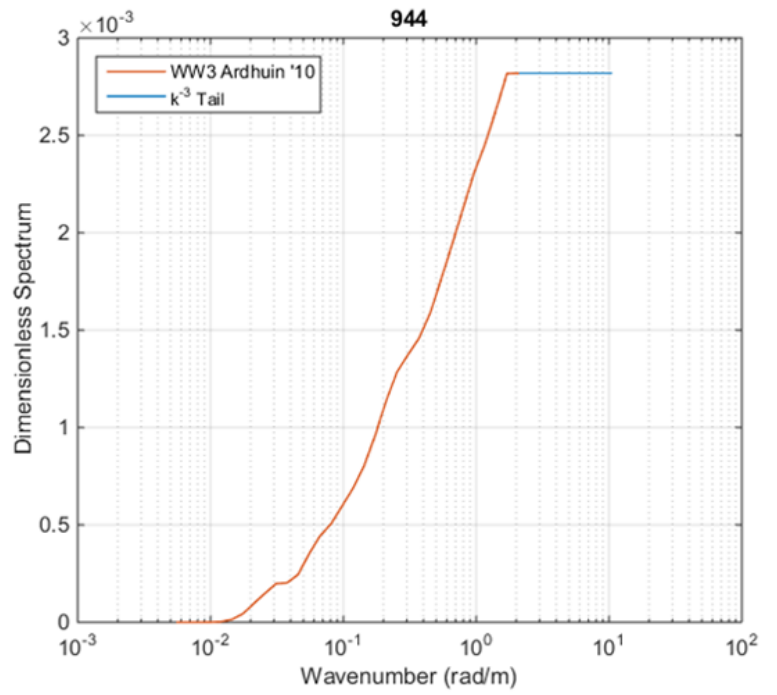
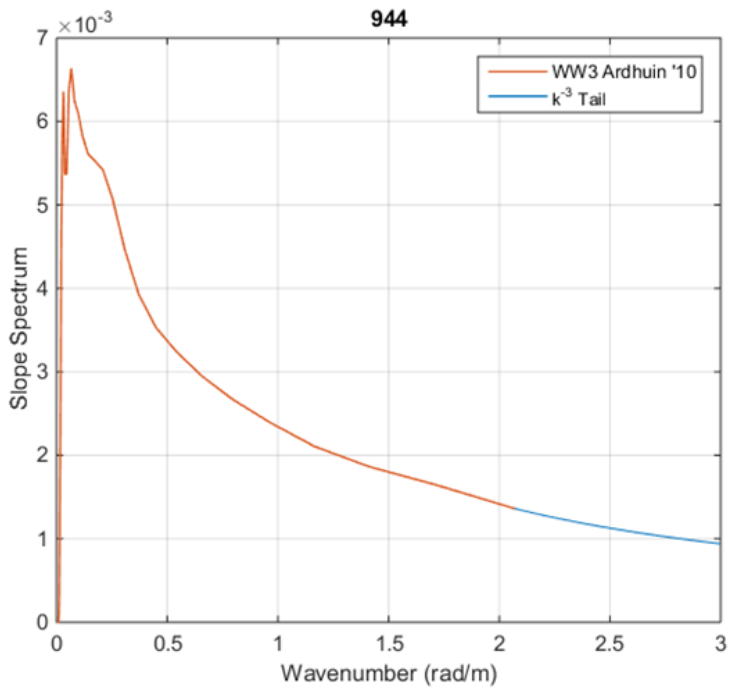
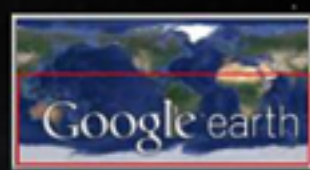
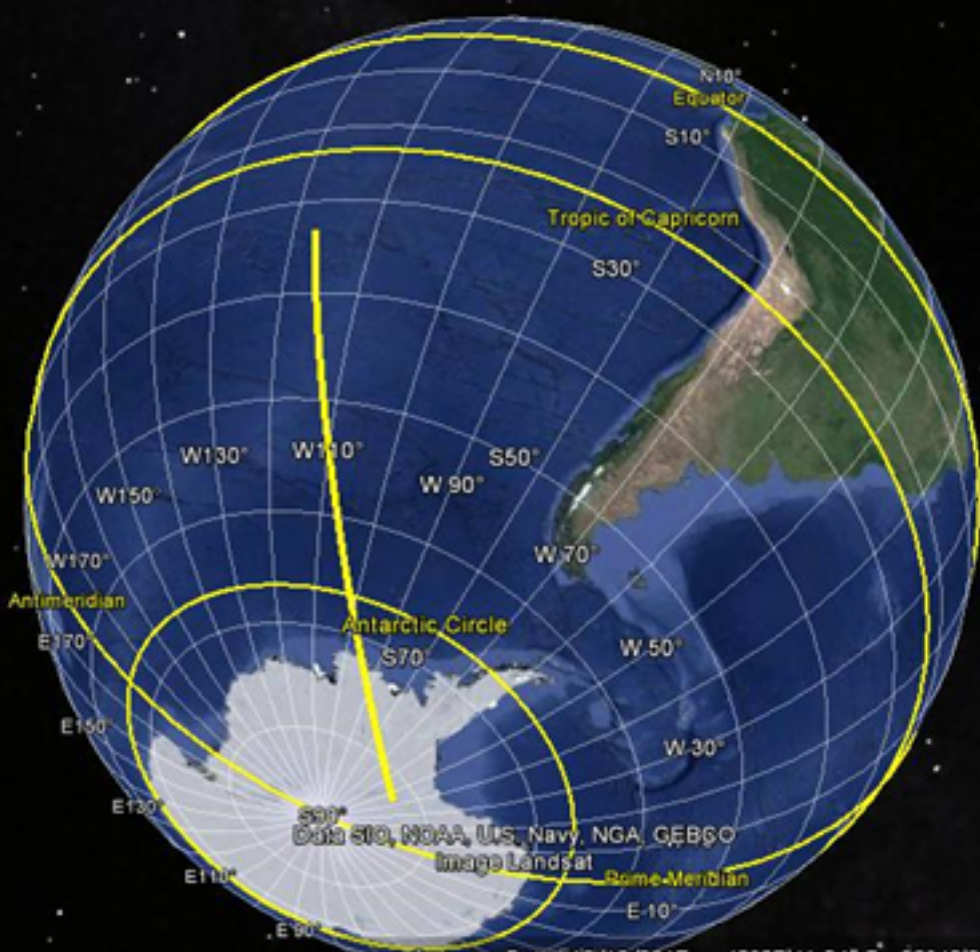


Figure 4.

Accepted Article

2/4/2015 1:44:05 am — 2/4/2015 2:00:51 am
1:44 am 2:00 am



Imagery Date: 12/13/2015 43°07'41.84" S 88°40'24.05" W eye alt: 8449.66 mi

Figure 5.

Accepted Article

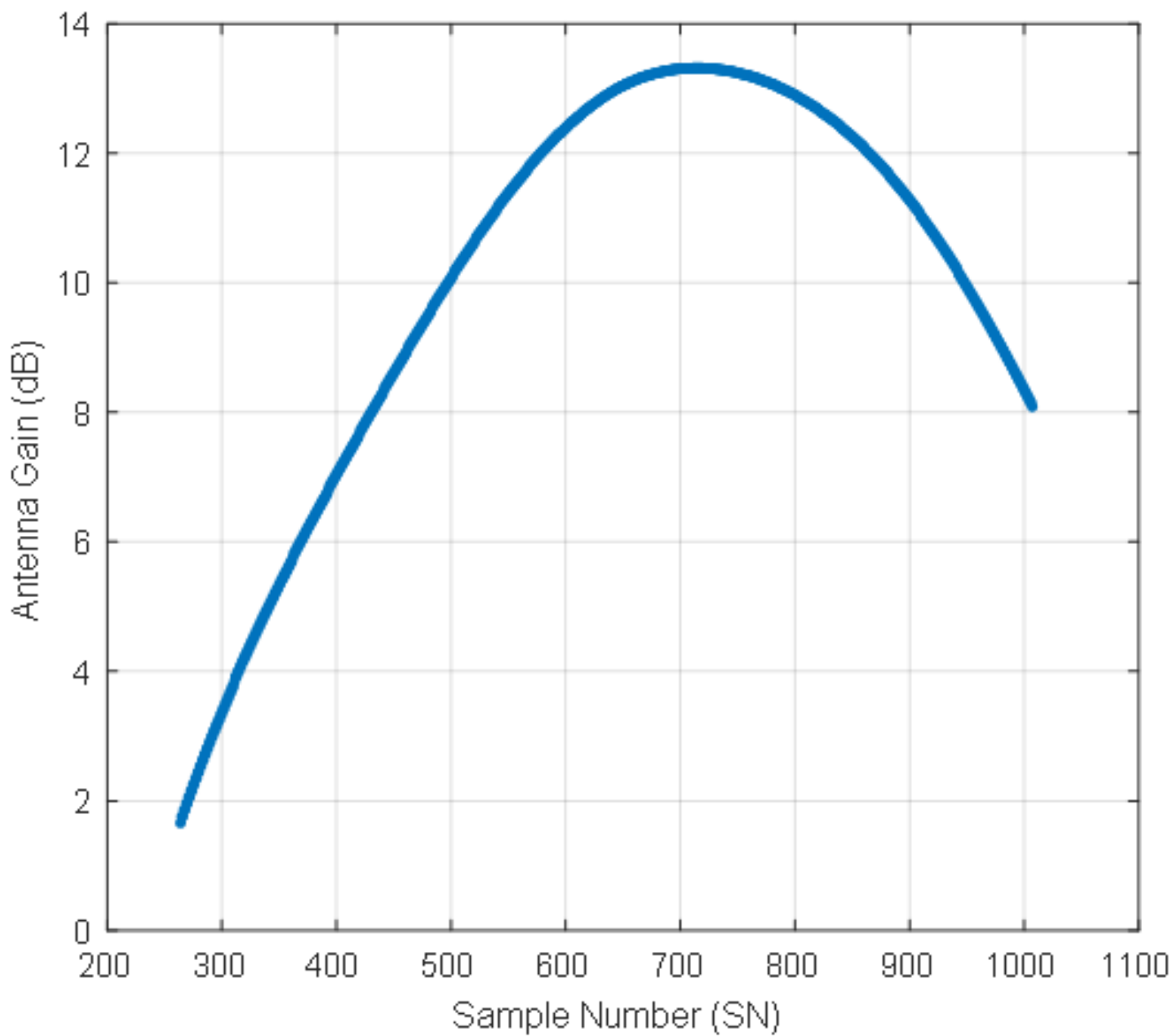


Figure 6.

Accepted Article

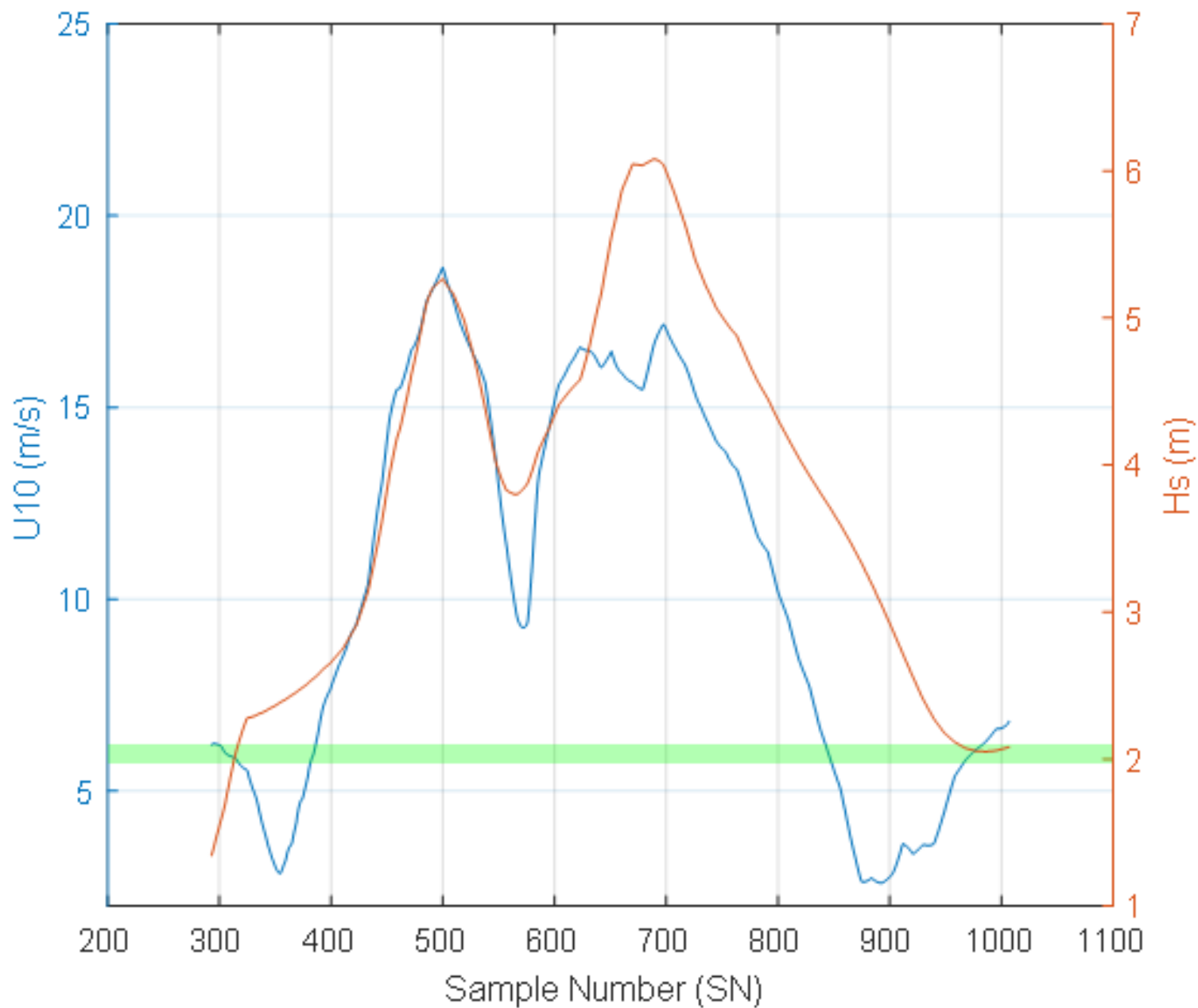


Figure 7.

Accepted Article

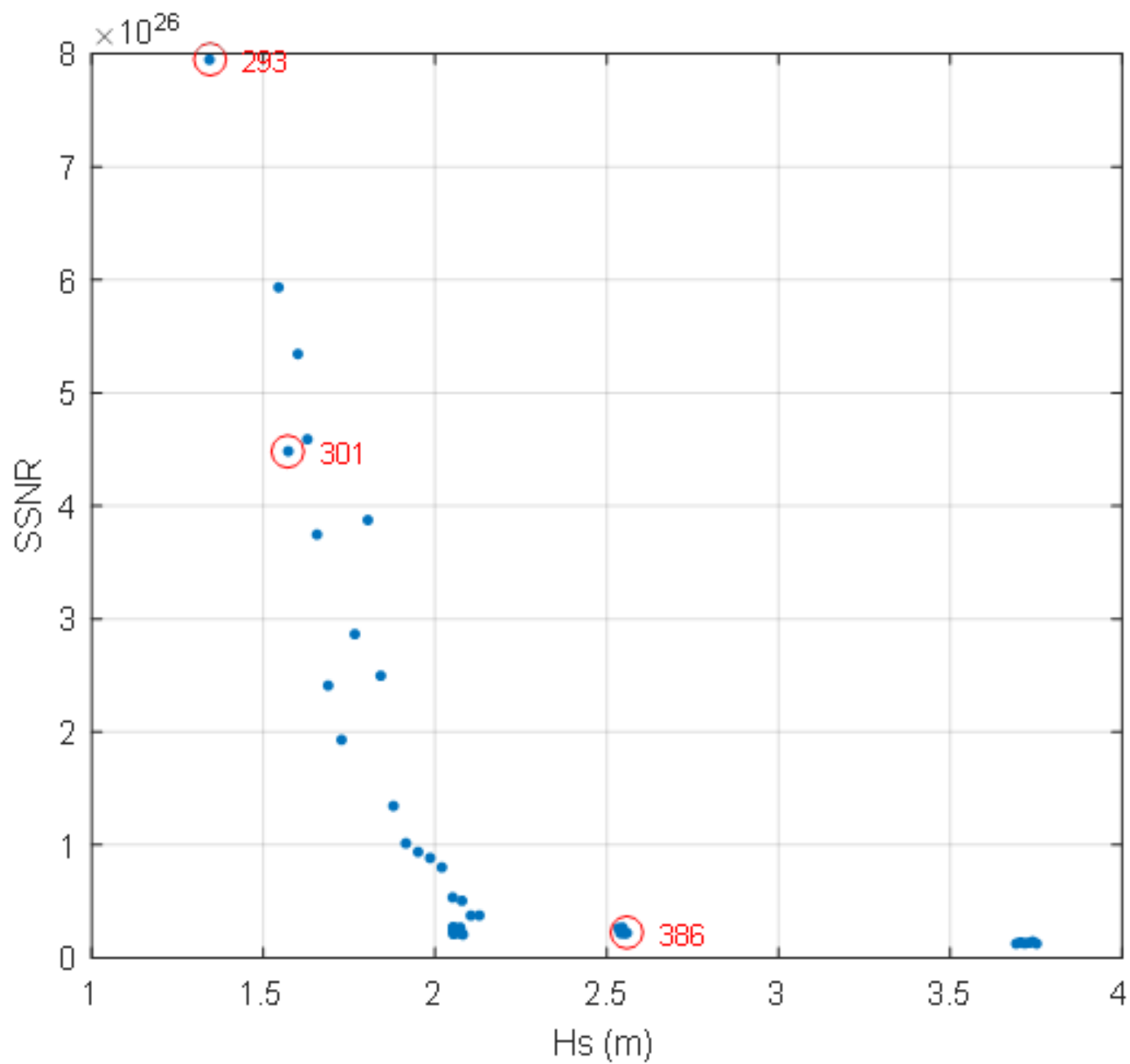


Figure 8.

Accepted Article

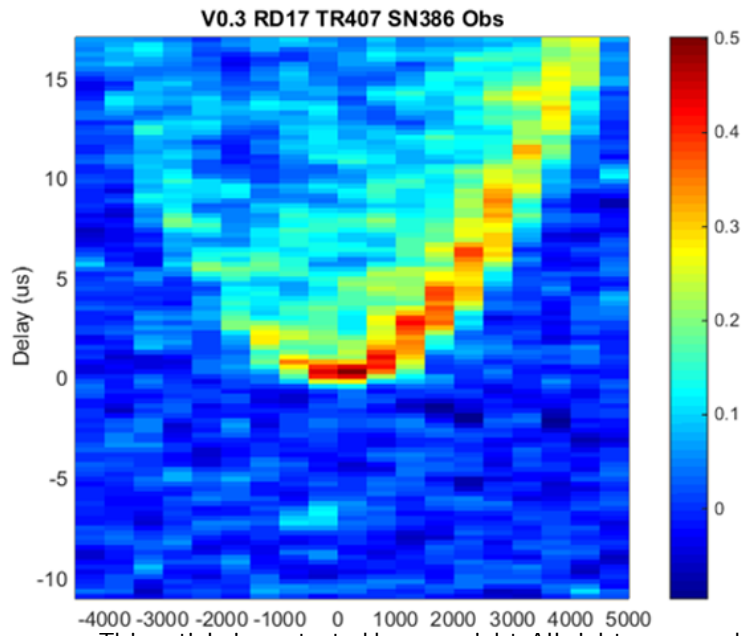
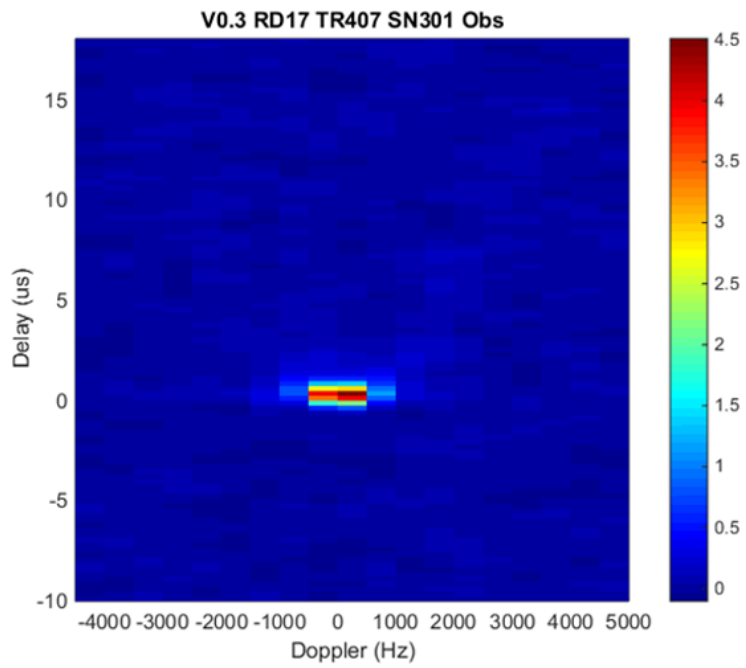
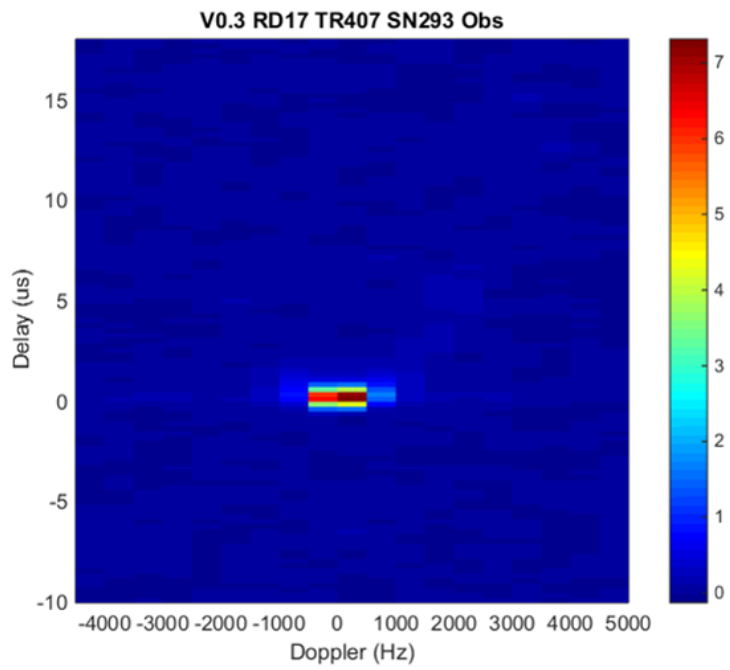
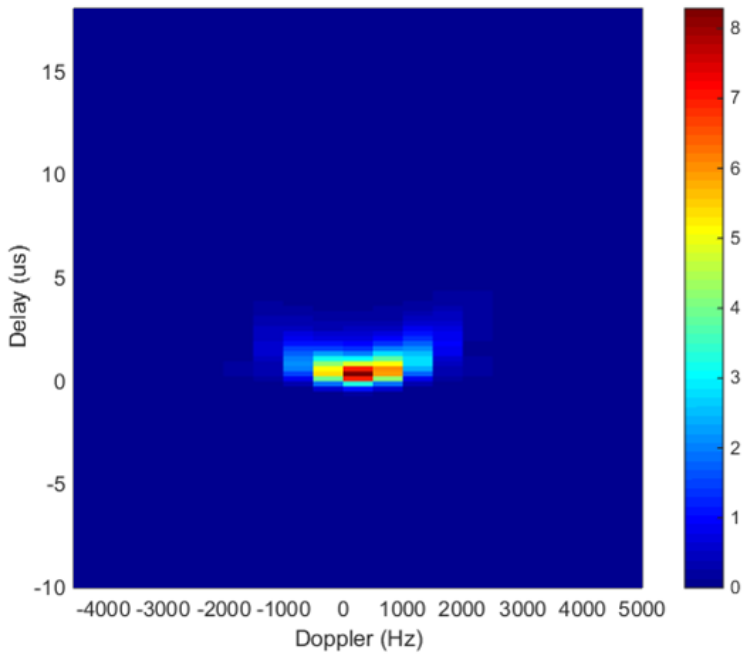


Figure 9.

Accepted Article

V0.3 RD17 TR407 SN293 WW3



V0.3 RD17 TR407 SN293 KZ

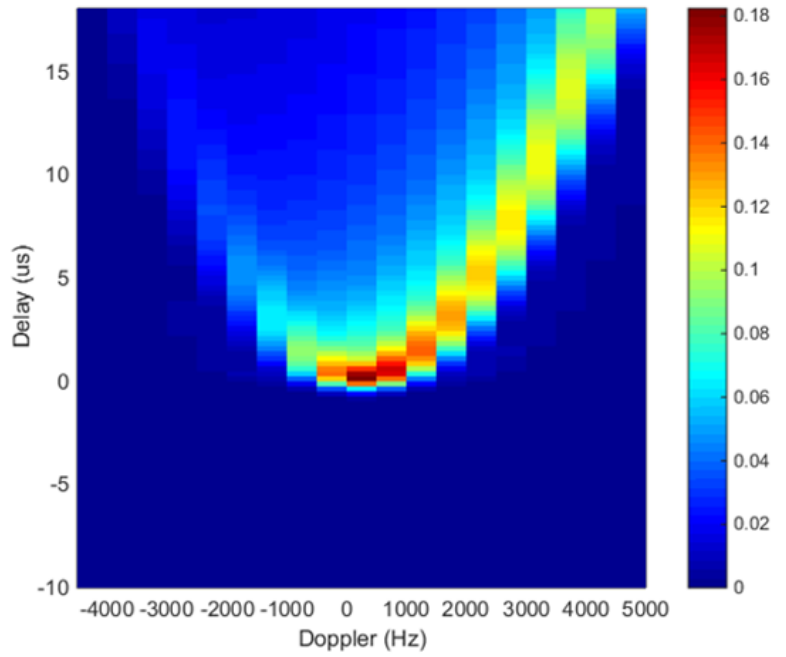
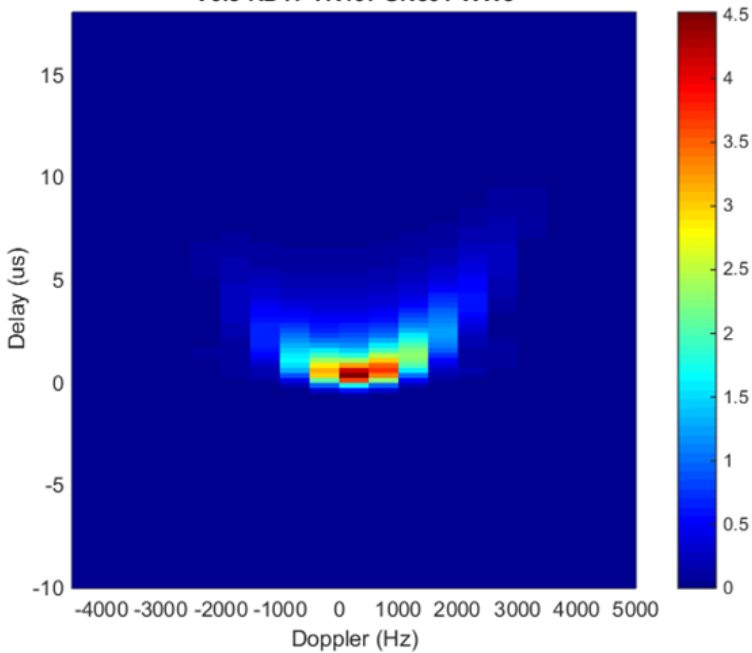


Figure 10.

Accepted Article

V0.3 RD17 TR407 SN301 WW3



V0.3 RD17 TR407 SN301 KZ

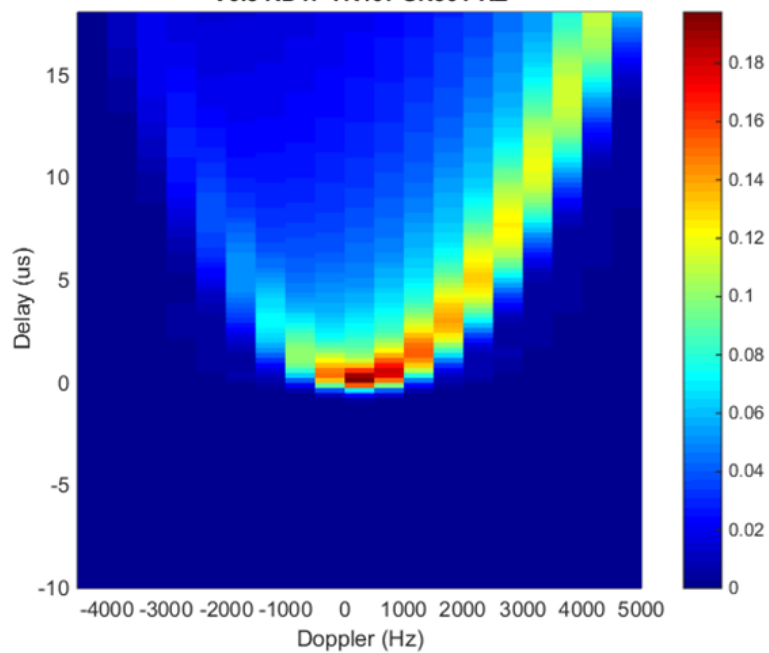
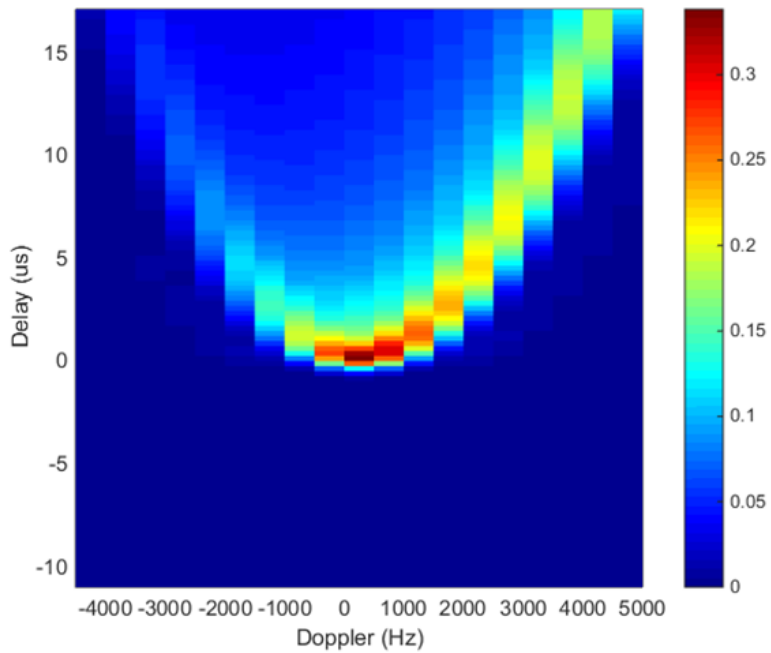


Figure 11.

Accepted Article

V0.3 RD17 TR407 SN386 WW3



V0.3 RD17 TR407 SN386 KZ

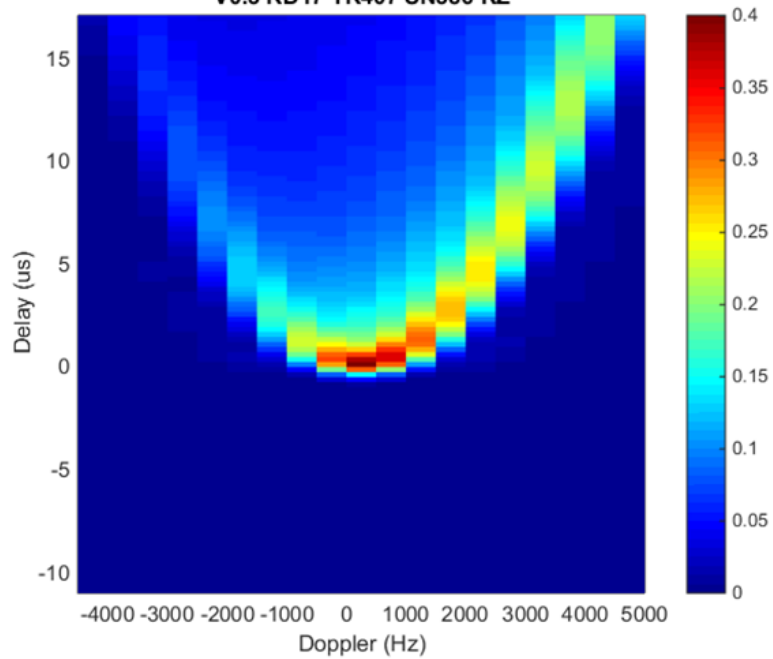


Figure 12.

Accepted Article

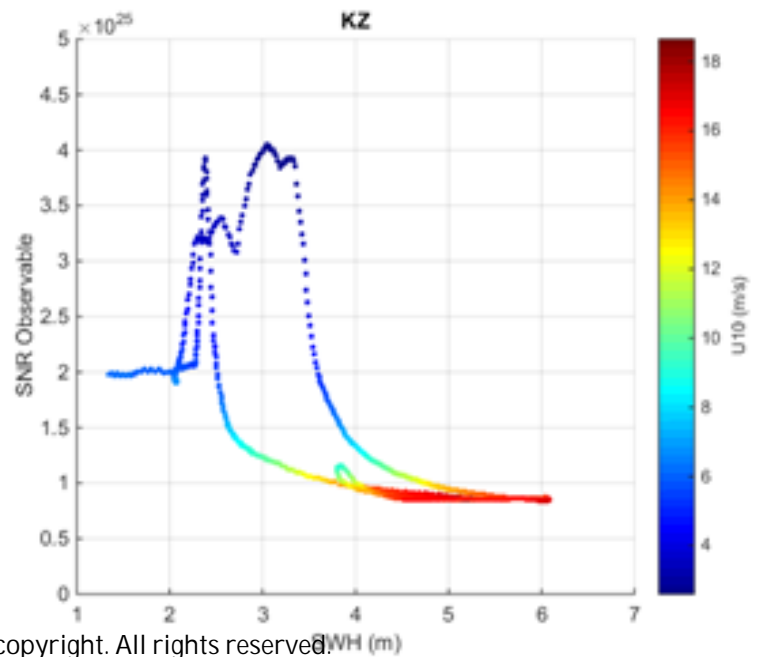
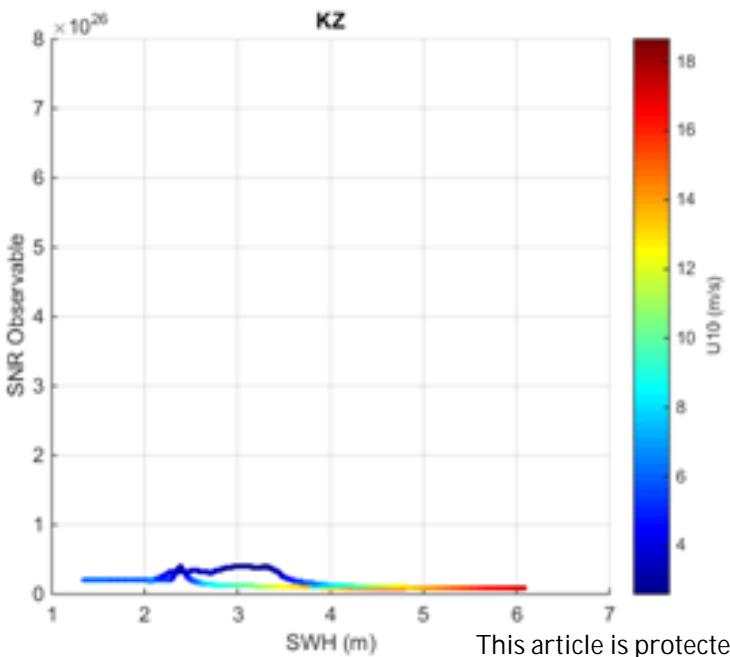
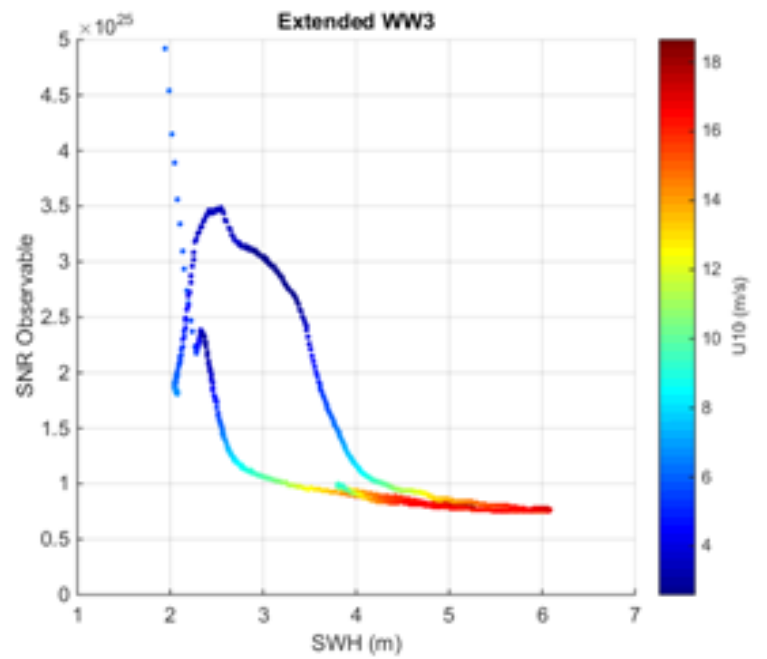
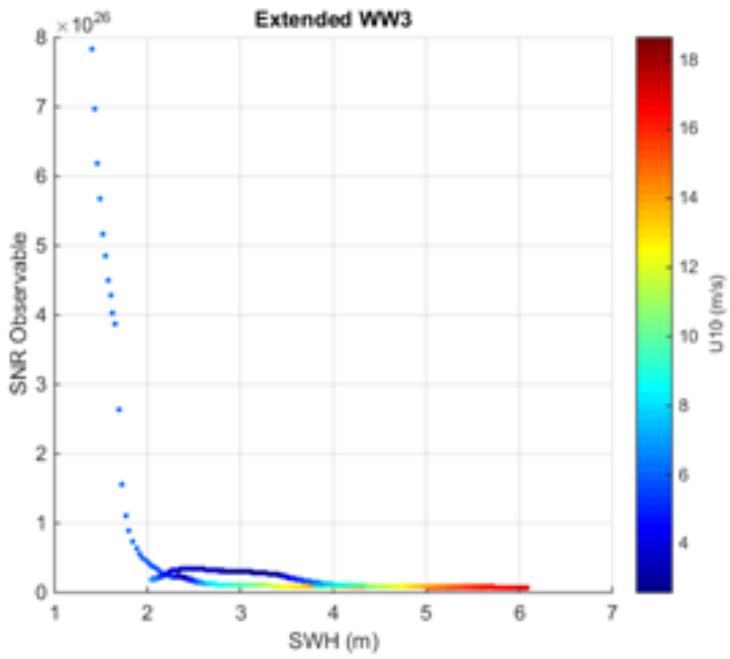
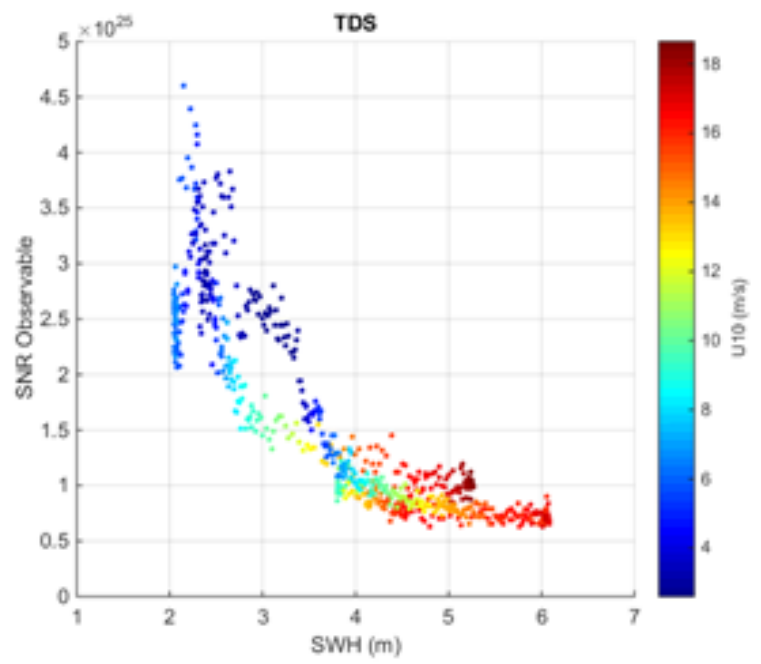
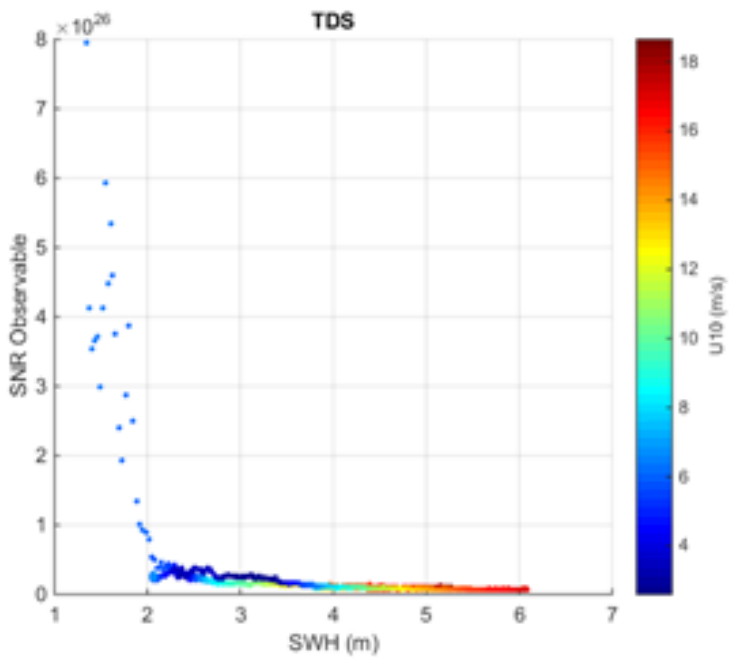


Figure 13.

Accepted Article

