## RESEARCH ARTICLE





## gsSKAT: Rapid gene set analysis and multiple testing correction for rare-variant association studies using weighted linear kernels

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#### ABSTRACT

Next-generation sequencing technologies have afforded unprecedented characterization of low-frequency and rare genetic variation. Due to low power for single-variant testing, aggregative methods are commonly used to combine observed rare variation within a single gene. Causal variation may also aggregate across multiple genes within relevant biomolecular pathways. Kernel-machine regression and adaptive testing methods for aggregative rare-variant association testing have been demonstrated to be powerful approaches for pathway-level analysis, although these methods tend to be computationally intensive at high-variant dimensionality and require access to complete data. An additional analytical issue in scans of large pathway definition sets is multiple testing correction. Gene set definitions may exhibit substantial genic overlap, and the impact of the resultant correlation in test statistics on Type I error rate control for large agnostic gene set scans has not been fully explored. Herein, we first outline a statistical strategy for aggregative rare-variant analysis using component gene-level linear kernel score test summary statistics as well as derive simple estimators of the effective number of tests for family-wise error rate control. We then conduct extensive simulation studies to characterize the behavior of our approach relative to direct application of kernel and adaptive methods under a variety of conditions. We also apply our method to two case-control studies, respectively, evaluating rare variation in hereditary prostate cancer and schizophrenia. Finally, we provide open-source R code for public use to facilitate easy application of our methods to existing rare-variant analysis results.

#### KEYWORDS

gene set, next-generation sequencing, pathway, rare variation

#### 1 | INTRODUCTION

Next-generation sequencing (NGS) is rapidly emerging as a primary technology for evaluating the role of genetic variation in human phenotypes. Unlike the standardized genotyping arrays used in genome-wide association studies, which interrogate tagging single nucleotide polymorphisms (SNPs) to indirectly capture the majority of common variation (i.e., minor allele frequency [MAF] > 5%) via linkage disequilibrium, NGS studies provide nucleotide-resolution information of the targeted DNA through massively parallel short-read sequencing, capable of directly identifying causal variation. This is a critical advantage with the recent interest in the role of rare genetic variation in complex traits. Many arguments exist that not only support this model of genetic association from a population genetics perspective (Gibson, 2011), due to a rapidly increasing population size and weak purifying selection, but suggest that rare variation may constitute a large portion of the so-called missing heritability observed in many complex traits (Bodmer & Bonilla, 2008; Schork, Murray, Frazer, & Topol, 2009). There is now a growing list of examples where high-impact rare variants have been identified in complex diseases (Holm et al., 2011; Rivas et al., 2011).

Although sequencing costs continue to decline as technology improves, NGS studies still remain quite expensive and sample sizes are often too small to be sufficiently powered for gene-based aggregative rare-variant testing (Wu & Zhi, 2013). However, aggregative gene set analyses informed by molecular pathways and/or perturbation studies may be

sufficiently powered by combining genetic variation across functionally related genes. Moreover, they may capture genetic heterogeneity of etiological mechanisms at a larger systematic level, as these complex traits are likely multifactorial and could be driven by the disruption of one of any number of key genes in a particular molecular pathway. Analyses involving aggregation of rare variants across large gene sets have recently been applied in studies of nonobstructive azoospermia (Li et al., 2015), adolescent idiopathic scoliosis (Haller et al., 2016), and schizophrenia (Richards et al., 2016).

Various extensions of rare-variant testing to the pathway level using self-contained testing have previously been explored (Wu & Zhi, 2013). Yan et al. (2014) recently proposed adaptive rank-truncation product (ARTP) methods in conjunction with kernel-machine regression testing, which demonstrated statistical power improvements over direct application of the popular sequence kernel association test (SKAT; Wu et al., 2011). However, these approaches are permutation-based and consequently computationally demanding, with moderately sized (80-100 genes) gene sets requiring thousands of minutes of compute time. Pan, Kwak, and Wei (2015) extended their adaptive score power test (aSPU) to genetic pathways (aSPUpath), which is also based upon score tests and applicable to common and rare variation, with permutation or parametric bootstrap applied to obtain gene set P values. Although these adaptive methods have demonstrated advantages in statistical power over competing approaches, their implementation requires access to the complete datasets to conduct gene set testing, limiting their application.

Evaluation of Type I error rate control for gene set analysis is also understudied. In contrast to gene-based rare-variant tests, which can justifiably be assumed to be independent due to anticipated low linkage disequilibrium among rare variation, multiple testing correction for gene set aggregative testing is complicated by the potential for substantial genic overlap. Examination of the latest version (v5.1) of the C2-curated gene set collection present in the Molecular Signatures Database (Liberzon, 2014; Liberzon et al., 2011; MSigDB, http://software.broadinstitute.org/gsea/msigdb) reveals 4,726 total gene sets, in addition to the 1,454 gene ontology (GO; Ashburner et al., 2000) gene sets. A total of 13,311 gene sets encompass the entire available list. An agnostic scan of all available gene sets could result in thousands of correlated test statistics, for which traditional multiple testing correction methods (e.g., Bonferroni) may be overly conservative without acknowledging this correlation structure.

Wu et al.'s examination of rare-variant pathway analysis strategies identified the direct application of SKAT to the union of rare-variant genotypes across the gene set (i.e., "super gene" approach) to perform well across a variety of conditions (Wu & Zhi, 2013). An advantage of this approach is that linear kernels can easily be combined to form composite kernels, supporting the hierarchical framework for gene set kernel construction. Herein, we first outline a computationally efficient strategy for conducting gene set based rarevariant association analyses and evaluate estimators of the effective number of gene set tests based on SKAT and its burden/kernel optimized variation, SKAT-O (Lee et al., 2012). We then conduct simulation studies under null conditions to characterize the properties of our gene-level P-value aggregation approach relative to direct application of kernel-based tests as well as demonstrate proper control of the family-wise error rate (FWER) for simultaneous analysis of large numbers of overlapping gene sets. We also investigate comparative power relative to approaches using complete data as well as any practical impacts on study design when proper FWER control is implemented relative to conservative Bonferroni's adjustment. Finally, we apply our approach to a case-control sequencing study of hereditary prostate cancer and previously published results from a case-control study of schizophrenia using exome chip array data.

## 2 | METHODS

# 2.1 | Kernel-machine association testing for rare variants

Consider a rare-variant association study of sample size N with a given  $N \times 1$  phenotype vector  $\mathbf{Y}$ , such that genotype dosages are available on N subjects for L genes. Let,  $\hat{\mathbf{Y}}$ 

correspond to a vector of fitted phenotype values (if Y is continuous) or trait probabilities (if Y is dichotomous) from a relevant regression model taking into account adjusting covariates (e.g., age and sex). Hypothesis testing for genelevel rare-variant association analysis may be conducted using an aggregative variance component testing approach, such as SKAT, such that a kernel test score statistic for a given gene  $l \in 1, ..., L$  is defined as  $Q_l = (Y - \hat{Y})' K_l(Y - \hat{Y})$ , where  $K_l$  is a kernel representation of  $M_l$  variants within the tested region(s) of gene l. For a weighted linear kernel function, we explicitly define  $K_l$  to be represented as  $K_l = G_l W_l G_{l'}$ , where G is an  $N \times M_l$  matrix of variant genotypes and  $W_l$  is an  $M_l \times M_l$  diagonal weight matrix. The test statistic  $Q_l$  then follows a mixture chi-square distribution under the null hypothesis.

## 2.2 | Extension to gene set analyses

Define the set  $S \subset \{1, \dots, L\}$  to represent a given gene set or pathway, such that it is defined by the subset of  $U \leq L$  total genes. A gene set test statistic may be defined similarly to that conducted at the gene-level, whereby  $G_S$  is an  $N \times M_S$  composite matrix formed by appending the genotype matrices of the U component genes that comprise S, given as  $(G_{S_1} \dots G_{S_U})$ . Then, we define the gene set test statistic  $Q_S = (Y - \hat{Y})' K_S (Y - \hat{Y})$ , where

$$\begin{split} \boldsymbol{K}_{\mathcal{S}} &= \boldsymbol{G}_{\mathcal{S}} \boldsymbol{W}_{\mathcal{S}} \boldsymbol{G}_{\mathcal{S}}' = \left(\boldsymbol{G}_{\mathcal{S}_{1}} \dots \boldsymbol{G}_{\mathcal{S}_{U}}\right) \operatorname{diag} \left(\boldsymbol{W}_{\mathcal{S}_{1}}, \dots, \boldsymbol{W}_{\mathcal{S}_{U}}\right) \\ &\times \begin{pmatrix} \boldsymbol{G}_{\mathcal{S}_{1}}' \\ \vdots \\ \boldsymbol{G}_{\mathcal{S}_{U}}' \end{pmatrix} = \sum_{l \in \mathcal{S}} \boldsymbol{K}_{l} \; . \end{split}$$

Thus,  $K_S$  is a linear composite kernel matrix of the component gene-level kernel matrices, and  $Q_S =$  $(Y - \hat{Y})'(\sum_{l \in S} K_l)(Y - \hat{Y}) = \sum_{l \in S} Q_l$ . For rare variation, it is reasonable to assume that the gene-level score statistics  $\{Q_l : l \in S\}$  are independent, so long as the variant sets are nonoverlapping. Under these conditions, a simple solution to deriving gene set level test P values is to combine precomputed gene-level P values,  $p_l$ , using P-value aggregation approach, such as Fisher's (1925) method or Stouffer's (1949) combined Z-score. We elect the latter, as it affords working with multivariate normality and gene-based weights, if warranted, are easily supported. Moreover, Stouffer's method tends to be more powerful than Fisher's when a large proportion of testing results are moderately significant (Abelson, 1995), which may more likely reflect the underlying biology in pathway-directed analysis. Define  $Z_1$  =  $\Phi^{-1}(1-p_1)$ , where  $\Phi^{-1}(\cdot)$  is the inverse cumulative density function (CDF) of the standard Gaussian distribution, such that under the null condition  $Z_l \ N(0,1)$ , For a given gene set S with k genes,  $Z_S = \frac{\sum_{l \in S} Z_l}{\sqrt{k}}$  and  $Z_S$  also follows a standard

Gaussian distribution under the gene set null condition, from which a gene set *P*-value can be easily computed. Note that in addition to SKAT, these results also generalize to SKAT-O (Lee et al., 2012), as  $\boldsymbol{W}_{l}$  can simply be substituted by  $\boldsymbol{W}_{l}^{0.5}((1-\rho_{l})\boldsymbol{I}+\rho_{l}\boldsymbol{1}\boldsymbol{1}')\boldsymbol{W}_{j}^{0.5}$  with the caveat that  $\rho_{l}$  is preselected gene-wise rather than optimized over the entire set of variants  $\boldsymbol{G}_{S}$ . We refer to this approach generally as gsSKAT.

#### 2.3 | Multiple testing correction

When testing a large number of gene sets, R, such as via an agnostic scan of multiple curated gene sets (e.g., GO), significance threshold adjustment such as a Bonferroni correction is very likely to be overly conservative due to substantial overlap of genes across gene sets. Consider a second gene set  $S^*$  with  $k^*$  genes such that  $S^* \cap S \neq \emptyset$ . The covariance  $Cov(Z_S, Z_{S^*})$  may be derived using the bilinearity of covariance, such that

$$\begin{aligned} \operatorname{Cov} \ \left( Z_{S}, Z_{S^{*}} \right) &= \operatorname{Cov} \left( \frac{1}{\sqrt{k}} \sum_{u \in S} Z_{u}, \frac{1}{\sqrt{k^{*}}} \sum_{v \in S^{*}} Z_{v} \right) \\ &= \sum_{u \in S} \sum_{v \in S^{*}} \operatorname{Cov} \left( \frac{1}{\sqrt{k}} Z_{u}, \frac{1}{\sqrt{k^{*}}} Z_{v} \right). \end{aligned}$$

Because we make the underlying assumption that  $Q_u$  and  $Q_v$  are independent for all u,v where  $u \neq v$ , Cov  $(\frac{1}{\sqrt{k}}Z_u,\frac{1}{\sqrt{k^*}}Z_v)=0$  for  $u \neq v$ . If we denote  $S^{INT}=S \cap S^*$ , then

Cov 
$$(Z_S, Z_{S^*}) = \sum_{u \in S^{INT}} \text{Cov} \left(\frac{1}{\sqrt{k}} Z_u, \frac{1}{\sqrt{k^*}} Z_u\right)$$
$$= \frac{|S^{INT}|}{\sqrt{k} \sqrt{k^*}},$$

where  $|S^{INT}|$  corresponds to the cardinality of the intersection of S and  $S^*$ , equivalent to the number of overlapping genes. More generally, we derive the correlation matrix of the pathway-level Z-scores by defining a  $R \times L$  pathway design matrix, D, for R unique pathways, such that matrix element  $D_{ji} = \frac{1}{\sqrt{k_j}}$  if gene i is in  $S_j$ , where  $k_j$  is the total number of genes in pathway j, and 0 otherwise. Then,  $Z \sim MVN(0, \Sigma)$ , where  $\Sigma = DD'$ . We consider estimates of the effective number of tests via the Galwey (2009) method and the modification of the Gao approach described by Hendricks, Dupuis, Logue, Myers, and Lunetta (2014) Let  $\Lambda$  be the vector of eigenvalues corresponding to the eigendecomposition of  $\Sigma$ . A Galwey estimate for the effective number of gene set level tests,  $R_{\text{Galwey}}^{\text{eff}}$ , is given by  $R_{\text{Galwey}}^{\text{eff}} = \frac{(\sum \sqrt{\lambda_r})^2}{\sum \lambda_r}$  for  $\lambda_r > 0$ , where  $\lambda_r$  indicates the rth largest eigenvalue. For the Gao estimator,  $R_{\text{Gal}}^{\text{eff}}$  is equivalent to the smallest  $R^*$  that satisfies

TABLE 1 Gene Set Properties and Gene Overlap for 10 Randomly Selected Reactome GENE-SETS

				Gene Overlap									
Gene Set	$L_{\mathcal{S}}$	$M_{\mathcal{S}}$	cMAF	$\overline{S_1}$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$	$S_8$	$S_9$	S <sub>10</sub>
$S_1$	6	227	0.443	-	0	0	0	0	0	0	0	0	0
$S_2$	10	473	0.895	-	-	0	0	3	4	0	0	0	3
$S_3$	12	634	0.790	-	-	-	0	0	0	0	0	0	6
$S_4$	19	868	1.386	-	-	_	-	0	9	0	0	0	0
$S_5$	25	1,255	1.888	-	-	-	-	-	8	0	0	3	15
$S_6$	27	1,174	1.997	-	-	-	-	-	-	0	0	3	8
$S_7$	32	1,879	5.477	-	-	-	-	-	-	-	0	0	0
$S_8$	37	2,130	3.027	-	-	-	-	-	-	-	-	34	1
$S_9$	47	2,611	4.097	_	_	-	_	-	_	-	_	-	4
$S_{10}$	47	2,621	4.591	-	-	-	-	-	-	-	-	-	-

 $\frac{\sum_{r=1}^{R^*} |\lambda_r|}{\sum_{r=1}^{R} |\lambda_r|} < C$ , where C is set to the recommended value of 0.995. Estimates of  $R^{\rm eff}$  may in turn be applied as a Bonferroni correction factor for adjusting the statistical significance threshold to maintain proper FWER control. Despite the potentially large dimensionality of DD', efficient computation of  $\Lambda$  can easily be conducted by exploiting sparse matrix algebra.

## 2.4 | Simulation study

To simulate genotypes under realistic rare-variant distributions and frequencies, empirical MAF data were downloaded from the NHLBI-ESP Exome Variant Server (release ESP6500). We isolated the European American MAFs for all observed polymorphic sites, and all variants with MAF > 0.05 were excluded as common SNPs. To simulate genotype data for genes that would likely pass traditional gene-level rarevariant testing criteria (e.g., sufficient number of minor alleles and variant positions), we first identified the subset of genes with a cumulative MAF (cMAF) > 0.01 and total number of variant positions between 10 and 100. We then randomly sampled 10 gene sets corresponding to 181 unique genes from the Reactome (Croft et al., 2014) pathway database ranging in gene set size from 6 to 47 as well as varying degrees of overlap (Table 1).

To characterize the P-value aggregative approach under a variety of study conditions, we simulated rare-variant genotypes for the 181 genes for an underlying population of 20,000 samples. Genotypes were simulated independently across samples and variant sites under assumptions of Hardy-Weinberg equilibrium. We employed a similar simulation strategy for phenotypes as defined in Wu et al. (2011), such that we defined continuous outcome  $y_i$  independently as:

$$y_i = X_{i1} \times 0.5 + X_{i2} \times 0.5 + G_i' \beta + \epsilon_i,$$

where  $X_{i1} \sim N\left(0,1\right)$ ,  $X_{i2} \sim$  Bernoulli (0.5), and  $\epsilon_i \sim N(0,1)$  were all independently sampled for each simulated subject. For power simulations, we defined causal genetic effects  $\boldsymbol{\beta} = (\beta_1, \dots, \beta_M)'$  for M total gene set variants such that  $|\beta_m| = 0.4 \times |\log_{10}(\text{MAF}_m)|$  if the variant m was designated to be causal and 0 otherwise, where MAF $_m$  is the population MAF of the mth variant. For binary traits with trait probability  $p_i$ , we modeled  $\log \text{it}(p_i)$  the same as continuous outcome  $y_i$ , with the exception that we additionally included an intercept  $\beta_0$  such that disease prevalence was approximately 10%.

## 2.5 | Type I error and FWER

To characterize the behavior of gsSKAT under null conditions, we considered total sequencing study sample sizes of N=1,000 and 2,000, which were randomly drawn from the larger population of 20,000 samples with replacement for each simulation iteration. SKAT and SKAT-O kernel testing was conducted for all individual genes as well as the 10 gene sets under all simulation conditions, while Stouffer's combined P values were also computed for the gene sets based on the component gene-level P values. Finally, SKAT-O has a tendency to produce P values of 1.00, which would yield negative infinity values from  $\Phi^{-1}(\cdot)$ . In the event of p=1.00, we set p=0.95 to avoid this issue. For these simulations, 5,000 iterations were conducted per analysis.

To evaluate proper control of the FWER rates for a given  $\alpha$  using the adjusted multiple testing correction factor  $R^{\text{eff}}$ , we additionally simulated uniformly distributed P values for 19,399 genes present in the ESP6500 dataset as the basis for gene set analysis. We considered three separate magnitudes of analyses defined by the total number of gene sets under consideration, denoted  $A_1$ ,  $A_2$ ,  $A_3$ , that were, respectively, composed of all gene sets with 5 < |S| < 1000 in Reactome (673 gene sets), Reactome and GO (2,109 total gene sets), and MSigDB C2 and GO (6,124 total gene sets). We presumed that these analyses would be typical of most agnostic gene set scans conducted by an investigator. For each analysis, we enumerated the number of instances a Type I error occurred at an adjusted  $\alpha$ -level of 0.05 using each of the two  $R^{\text{eff}}$  estimates as a Bonferroni correction factor. A total of 10,000 replications were conducted for each analysis.

## 2.6 | Statistical power

There are myriad configurations of genetic architectures (e.g., causal variant proportion, direction of effects, relationship between effect magnitude and MAF) under which statistical power may be calculated for aggregate rare-variant testing methods. To investigate relative statistical power of our *P*-value aggregation method compared to direct applications of competing approaches using available genetic, covariate, and phenotypic data, we conducted a variety of simulations based

on continuous (N = 1,000) and dichotomous (N = 2,000) outcomes for a limited set of realistic conditions using data for gene sets  $(S_2, S_4, S_6, S_8, S_{10})$ . We defined the genetic architecture of a causal genetic pathway hierarchically, such that a gene set is comprised of causal and null genes, and causal genes are comprised of causal and null variants. For our purposes, we randomly selected approximately 5% of the variants to be causal for a given causal gene for continuous outcomes and 10% for binary in order to achieve adequate power, and considered causal gene proportions across the gene set to be 100%,  $\sim 50\%$ , and  $\sim 25\%$ . Finally, we considered effects to be either all positive or a randomly selected mixture of positive and negative. Genetic profiles were randomly selected from the population of 20,000 previously generated genotype vectors, while a larger population of 50,000 subjects was generated for binary outcomes by sampling with replacement. In addition to SKAT-O and gsSKAT using gene-level SKAT-O P values, we also applied the aSPUpath adaptive test using the aSPU R package. The aSPUpath test was applied using 10,000 permutations, with all other settings set to defaults. A total of 1,000 simulation iterations were performed per analysis, and all testing results were considered significant at an  $\alpha$  level of 0.05.

Quantifying potential improvements in power via correct selection of an adjusted  $\alpha$  level is another statistical power consideration of direct relevance to this work. To evaluate the practical impact of proper FWER control using  $R^{\rm eff}$  relative to a conservative Bonferroni adjustment on power, we estimated statistical power for an example gene set,  $S_4$ , as part of a hypothetical agnostic scan of a gene set associations for each of the three gene set analyses  $(A_1, A_2, A_3)$  described above. Specifically, power was estimated at Bonferroni-corrected  $\alpha$ levels of 0.05, where the correction factor was set as either R or  $R^{\rm eff}$ . We applied the built-in power calculation functions in the SKAT R package to calculate power estimates under specific  $\alpha$  levels under a causal variant percentage of 0.10, causal variant MAF threshold of 0.05, and even mixture of positive and negative effects, with all other settings set to default parameters. We calculated statistical power for continuous and dichotomous outcomes for samples sizes of (500, 1,000) and (2,000, 4,000), respectively, as well as the minimum sample size necessary to achieve 80% power under both adjusted significance thresholds, based upon simulated haplotype data for variants included in  $S_4$ .

## 2.7 | Application: Prostate cancer risk

We first applied our gsSKAT approach to 333 cases and 349 controls using data from a whole-exome sequencing (WES) case-control study of hereditary prostate cancer (PRCA) conducted by the International Consortium of Prostate Cancer Genetics (ICPCG), previously detailed elsewhere (Larson et al., 2016). Briefly, WES was performed using the Agilent 50Mb SureSelect Human All Exon chip or the Agilent

SureSelect V4+UTR kit. Eligible variants for association testing were then identified as corresponding to MAF < 0.05 and corresponding to functional status of nonsense, missense, or splice site variation. SKAT-O was then applied at a genelevel to all genes with  $\geq 1$  eligible variant position, adjusting for capture kit (dichotomous) and the first five principal components derived from the complete genotype data. Variant weighting was defined by functional impact, such that nonsense and splice-site variants received weights of 1.0 and missense variants were weighted using random forest classification trees built using 15 features from dbNSFP, including seven functional prediction scores. Additional processing details are presented in the Supplemental Information. We considered all gene sets with set size between 5 and 1,000 genes within the curated pathways (CPs) subset of the MSigDB C2 list, which includes 1,330 gene set definitions from Reactome, Kyoto Encyclopedia of Genes and Genomes (KEGG) (Kanehisa, 2002), Pathway Interaction Database (PID) (Schaefer et al., 2009), and other online gene set databases, along with gene sets from GO.

## 2.8 | Application: Schizophrenia

A primary advantage of gsSKAT is that it can easily be applied to previously published gene-level rare-variant analysis results. Recently, Richards et al. (2016) conducted a large case-control study of schizophrenia using the Illumina (San Diego, CA) HumanExome Array on 8,103 controls and 5,585 cases from the Schizophrenia Working Group of the Psychiatric Genomics Consortium (PGC, 2014). Notably, the authors had applied SKAT-O at both a gene and gene set level, with complete results from the former reported as supplemental material. For purposes of comparison and to explore the utility of applying gsSKAT to preexisting results of other studies, we applied gsSKAT to the reported SKAT-O *P* values from Richards et al. using the same settings selected for the PRCA analysis.

#### 3 | RESULTS

#### 3.1 | Gene set P values

Gene set P values derived from direct application of SKAT on  $G_S$  demonstrated high correlation with those computed using the Stouffer combined Z approach, with Spearman's correlation coefficients ranging from 0.84 to 0.92. Results were comparable across gene set size, sample size, and outcome type. In contrast, the results for SKAT-O, while still highly correlated, demonstrated a sizable reduction in rank correlation between the directly computed and Stouffer combined results (Fig. 1). The degree of correlation also reduced with the gene set size, with rank correlations for  $S_1$  (six genes) ranging from 0.59 to 0.62, while those for  $S_{10}$  (47 genes) ranged from 0.45 to

0.50. This is not altogether surprising, since as we previously noted, the correlation parameter  $\rho_j$  in SKAT-O is estimated independently for each component gene in the gene set prior to P-value aggregation, thus resulting in a different underlying hypothesis. Moreover, it is expected that the correlation between direct application of SKAT-O and aggregation of gene-level SKAT-O P values would degrade as the number of genes increases. Finally, empirical correlation patterns of simulation P-values across overlapping gene sets for SKAT and gsSKAT were both highly comparable to expectation (Fig. 2).

## 3.2 | Type I error rate

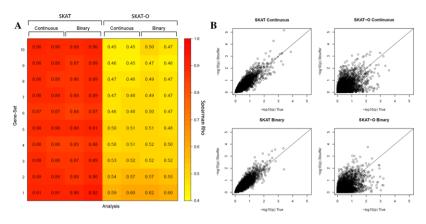
Table 2 presents the empirical false-positive rates (FPRs) for each of the 10 example Reactome gene sets across the various conditions in our simulation study. Overall, direct application of SKAT or SKAT-O to the aggregated genotype data tended to be conservative, with binomial testing relative to the expected FPR at an  $\alpha$  level of 0.05, resulting in significant  $(P \le \frac{0.05}{160} \approx 0.0003)$  deviation for multiple simulation scenarios. This degree of conservative bias demonstrated a trend with gene set size, with larger gene sets trending to more conservative results. The conservative bias also appeared to be more prevalent and severe for continuous rather than binary outcomes. In contrast, the Stouffer's combined Z P values from gsSKAT were largely within expectation under the null, with one instance of a simulation condition resulting in significantly inflated type I errors ( $S_{10}$  for a binary outcome using SKAT and N = 2,000: FPR = 0.0632).

#### 3.3 | Multiple testing correction

For the three separate gene set lists, estimates of the effective number of tests were approximately half the quantity of respective gene sets themselves using  $R_{\rm Galwey}^{\rm eff}$ , whereas  $R_{\rm Gao}^{\rm eff}$  ranged between 72% and 81% of the total number of gene sets  $R({\rm Table~3})$ . With respect to FWER control using R and the two effective test number estimates, binomial testing indicated significantly ( $P \leq \frac{0.05}{9} = 0.0056$ ) conservative FWER control using R as a Bonferroni correction factor but significantly liberal results for  $R_{\rm Galwey}^{\rm eff}$ . In contrast, use of  $R_{\rm Gao}^{\rm eff}$  resulted in FWER estimates that were approximately equal to the assumed testing size, regardless of which list of gene sets was applied.

#### **3.4** | Power

Complete simulation results for all gene sets under similar are presented in Table 4. Overall, we observed a trend of a reduction in power for the gsSKAT analysis of genelevel *P* values relative to methods using complete data, with differentials as high as 15–20% in isolated instances. This was observed notably for continuous outcomes under simulation scenarios where gene sets comprised relatively few genes and causal variant effects that were in the same



**FIGURE 1** (A) Tileplot of Spearman's correlation coefficients between P values derived from the true kernel test statistic (i.e., SKAT or SKAT-O applied to  $G_S$ ) with the P values from the Stouffer combined Z approach based on gene-level P values. Tiles are colored by degree of correlation as indicated by the key, with correlation estimates included in the tiles. Adjacent columns corresponding to a particular analysis configuration (indicated by brackets on top of the figure) are for N = 1,000 (left) and N = 2,000 (right). (B) Example scatterplots for -log 10 transformed P values corresponding to the true kernel gene set analysis test (x-axis) and the Stouffer combined Z P-value (y-axis) for gene set  $S_S$  under N = 2,000.

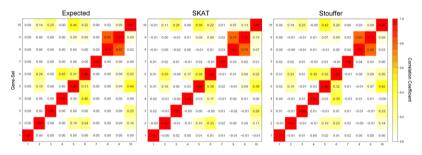


FIGURE 2 Visualization of expected and example observed correlation structures from the gene set rare-variant association simulation study. Correlation matrices corresponding to (from left to right) the design matrix D for the 10 Reactome gene sets, Spearman's rank correlations from the SKAT analysis P values of continuous outcomes based on N=2,000, and the Spearman's rank correlations for the Stouffer combined ZP values under the same simulations conditions.

direction, while differences in power for binary outcomes tended to be less pronounced. For larger gene sets with a mixture of effect directions, the gsSKAT approach using SKAT-O P values was competitive even with aSPUpath, especially for binary outcomes when the proportion of causal genes was lower. Given that median gene set size for pathway collections defined by  $A_1$ ,  $A_2$ , and  $A_3$  ranged from 26 to 34 genes, results for gene sets  $S_4$ ,  $S_6$ , and  $S_8$  are likely most relevant for broad characterization of relative power. Although the adaptive approach aSPUpath did not demonstrate substantially strong power advantages over the SKAT kernel-regression methods as previously reported, it is important to note that our simulation conditions supported the default variant weighting assumptions of SKAT-O by establishing a negative correlation between effect size and MAF.

In general, selection of  $R^{\rm eff}$  (based upon the Gao approach) versus R as a Bonferroni correction factor yielded minimal advantages in statistical power over the various study conditions (Table 5), with realized gains in power ranging from 0.009 to 0.017. Similarly, the minimum sample sizes to achieve 80% power using the  $R^{\rm eff}$  correction factor resulted in 0.8–2.5% decrease in number of necessary samples across the simulations. Results were comparable across the nature of the phenotype (binary or continuous) and exhibited reduced

benefit as sample size increased. Results for other example gene sets and simulation conditions produced similar results (data not shown).

## 3.5 | Data applications

Gene set analyses for both PRCA and schizophrenia, respectively, returned one and two significant findings (Fig. 3). For PRCA, the GO gene set regulation of apoptosis (GO:0042981), which interestingly would not have been declared significant by standard Bonferonni adjustment, consisted of 305 genes with observed genetic variation of 341 total genes. A Manhattan-style plot of the component genelevel P values is presented in Figure S1, with FASTK (P =  $8.6 \times 10^{-5}$ ) corresponding to the most significant result. The two significant results from the schizophrenia analysis were also GO gene sets, Membrane Lipid Biosynthetic Process (GO:0046467) and Lipid Biosynthetic Process (GO:0008610), the former nested within the latter. For GO:0046467, a total of 13 of 35 genes corresponded to a Pvalue < 0.1. Comparisons between the subset of reported gene sets by Richards et al. that overlap with our results are reported in Table S2.



TABLE 2 Empirical false-positive rates for the direct application of SKAT/SKAT-O (i.e., "True") and stouffer combined Z gene set P values from the null simulation study-based upon an alpha level of 0.05

Pheno.	N	Method	P-value	$S_1$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$	$S_8$	$S_9$	$S_{10}$
Cont.	1,000	SKAT	True	0.0440	0.0442	0.0416	0.0396	0.0356	0.0348	0.0258	0.0272	0.0228	0.0224
			Stouffer	0.0518	0.0526	0.0498	0.0484	0.0536	0.0542	0.0512	0.0474	0.0530	0.0472
	2,000	SKAT	True	0.0466	0.0474	0.0444	0.0412	0.0422	0.0396	0.0352	0.0334	0.0312	0.0352
			Stouffer	0.0452	0.0464	0.0486	0.0514	0.0550	0.0502	0.0494	0.0462	0.0446	0.0558
	1,000	SKAT-O	True	0.0536	0.0494	0.0502	0.0448	0.0490	0.0404	0.0362	0.0396	0.0392	0.0318
			Stouffer	0.0546	0.0510	0.0462	0.0446	0.0382	0.0368	0.0396	0.0376	0.0348	0.0346
	2,000	SKAT-O	True	0.0494	0.0530	0.0464	0.0458	0.0508	0.0446	0.0430	0.0414	0.0372	0.0430
			Stouffer	0.0444	0.0480	0.0436	0.0450	0.0462	0.0392	0.0434	0.0354	0.0332	0.0382
Binary	1,000	SKAT	True	0.0626	0.0512	0.0548	0.0526	0.0528	0.0566	0.0484	0.0586	0.0574	0.0566
			Stouffer	0.0594	0.0518	0.0572	0.0504	0.0500	0.0564	0.0494	0.0552	0.0556	0.0520
	2,000	SKAT	True	0.0472	0.0448	0.0444	0.0416	0.0392	0.0432	0.0348	0.0374	0.0366	0.0360
			Stouffer	0.0492	0.0468	0.0510	0.0536	0.0530	0.0558	0.0496	0.0520	0.0584	0.0632
	1,000	SKAT-O	True	0.0622	0.0534	0.0558	0.0536	0.0442	0.0534	0.0482	0.0504	0.0482	0.0560
			Stouffer	0.0522	0.0500	0.0552	0.0556	0.0512	0.0558	0.0454	0.0532	0.0532	0.0530
	2,000	SKAT-O	True	0.0494	0.0440	0.0458	0.0520	0.0428	0.0474	0.0456	0.0466	0.0412	0.0428
			Stouffer	0.0480	0.0450	0.0432	0.0448	0.0422	0.0366	0.0364	0.0402	0.0340	0.0348

Error Rates Significantly Different from the Expectation of 0.05 Based upon a Bonferroni-Adjusted (160 tests) Two-Sided Binomial Test Are Highlighted in Bold

TABLE 3 Gene set analysis summaries and empirical FWER results by bonferroni's correction factor using the total number of gene set test R as well as two effective test number estimates,  $R_{\text{Gao}}^{\text{eff}}$  and  $R_{\text{Galwev}}^{\text{eff}}$ 

Number of Gene Sets					FWER by	$(\alpha = 0.05)$	
Analysis	R	Reff Galwey	Reff Gao	Number of Unique Genes	R	Reff Galwey	Reff Gao
$A_1$	673	368.7	500	5,637	0.0416	0.0731	0.0550
$A_2$	2,109	1,084.2	1,515	9,701	0.0398	0.0727	0.0537
$A_3$	6,124	3,885.1	4,966	17,272	0.0418	0.0674	0.0511

FWERs significantly different from the expectation of 0.05 based upon a Bonferroni-adjusted (nine tests) two-sided binomial tests that are highlighted in bold.

## 3.6 | Computational efficiency

Conditional on the availability of precomputed gene-level P values, computational timing for computing the gene set P values and deriving  $R_{\rm eff}$  is largely trivial. The average analysis time for the FWER simulations per replication of the  $A_3$  scale analysis was approximately 170 sec on a desktop computer with an Intel<sup>®</sup> Core<sup>TM</sup> i5-6500 processor and 8 GB of RAM. Computing gene set P values from gene-level results also precludes the need to apply SKAT to potentially high-dimensional genotype matrices under large  $M_S$ , as these analyses may incur hours of compute time per gene set when  $M_S > 1,000$ .

#### 4 | DISCUSSION

As sequencing costs diminish and the number of published rare-variant association studies continues to grow, secondary analysis of gene-level testing results may identify significant aggregation of rare-variant associations in relevant biological pathways. Herein, we have outlined a simple and effective strategy for conducting large-scale gene set analyses using gene-level kernel testing results while simultaneously investigating multiple testing correction and correlated test statistics due to genic overlap. From our simulations, we found P-value aggregation using Stouffer's combined Z method to be highly correlated with results corresponding to direct application of kernel-machine testing across a wide variety of conditions, particularly for SKAT. These methods also demonstrated proper test size across various sizes of gene sets. Results were expectedly less correlated for SKAT-O, for which the parameter that determines the optimal combination of burden and kernel testing is estimated per gene rather than across the entirely of the gene set. This distinction is subtle yet clearly relevant to the end result of the hypothesis test. Accommodating gene-level control of this parameter is equivalent to allowing the distribution of variant weight parameters to vary by gene with respect to distribution of effect directionality and causal status, which may have biological justification.

**TABLE 4** Power simulation results for binary and continuous outcomes for analysis conditions defined by effect direction (one-way or randomly mixed), causal gene percentage (100%, 50%, or 25%), and gene set

			Continuous Outcome			]	Binary Outcom	e
<b>Effect Direction</b>	Causal Gene (%)	Gene set	SKAT-O	aSPUpath	gsSKAT	SKAT-O	aSPUpath	gsSKAT
One-way	100	$S_2$	0.570	0.487	0.450	0.635	0.492	0.480
		$S_4$	0.581	0.463	0.453	0.664	0.458	0.478
		$S_6$	0.825	0.666	0.608	0.903	0.715	0.725
		$S_8$	0.991	0.971	0.915	0.984	0.960	0.939
		$S_{10}$	0.972	0.898	0.889	0.993	0.917	0.927
	50	$S_2$	0.275	0.285	0.218	0.305	0.257	0.257
		$S_4$	0.298	0.267	0.209	0.282	0.204	0.221
		$S_6$	0.486	0.385	0.359	0.521	0.385	0.401
		$S_8$	0.712	0.742	0.600	0.764	0.707	0.658
		$S_{10}$	0.674	0.596	0.542	0.755	0.595	0.628
	25	$S_2$	0.138	0.161	0.118	0.091	0.119	0.088
		$S_4$	0.171	0.190	0.128	0.138	0.127	0.145
		$S_6$	0.194	0.226	0.176	0.215	0.213	0.180
		$S_8$	0.328	0.479	0.293	0.316	0.364	0.309
		$S_{10}$	0.280	0.362	0.239	0.356	0.315	0.312
Mixed	100	$S_2$	0.529	0.473	0.447	0.403	0.349	0.359
		$S_4$	0.526	0.457	0.447	0.401	0.315	0.332
		$S_6$	0.752	0.627	0.608	0.638	0.492	0.561
		$S_8$	0.955	0.957	0.915	0.924	0.883	0.872
		$S_{10}$	0.937	0.882	0.889	0.899	0.775	0.871
	50	$S_2$	0.274	0.266	0.229	0.216	0.212	0.175
		$S_4$	0.261	0.250	0.206	0.176	0.191	0.171
		$S_6$	0.418	0.380	0.339	0.314	0.257	0.298
		$S_8$	0.630	0.733	0.547	0.533	0.545	0.518
		$S_{10}$	0.601	0.607	0.559	0.469	0.418	0.492
	25	$S_2$	0.131	0.164	0.122	0.091	0.105	0.082
		$S_4$	0.158	0.167	0.148	0.113	0.109	0.106
		$S_6$	0.192	0.210	0.158	0.144	0.148	0.150
		$S_8$	0.299	0.464	0.316	0.193	0.267	0.227
		$S_{10}$	0.217	0.342	0.234	0.189	0.238	0.257

Empirical power estimates are derived at the  $\alpha$  level of 0.05, with highest level per scenario highlighted in bold.

Our simulation results indicated that, while proper control of Type I errors is preserved in our gsSKAT *P*-value aggregation testing strategy, a moderate degree of statistical power may be lost relative to direct application of leading gene set testing methods on the raw data. Consequently, ideal analysis conditions would involve access to all genetic, covariate, and phenotype information to apply methods such as aSPUpath. However, gsSKAT did perform competitively for gene sets that are typical of large pathway definition sets such as KEGG or Reactome, and may also prove useful as a complementary analytical approach for sizable gene sets that present computational issues for kernel testing. Additionally, the major advantage of our approach is that it can easily be applied to existing sequencing studies for which gene-level

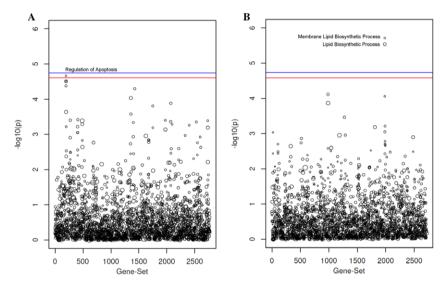
P values are readily available. Given the growing number of sequencing studies and wide-scale adoption of kernel testing for gene-level rare-variant testing, gsSKAT provides an efficient approach for hypothesis generation using simple summary statistics from prior studies.

Our results also suggest that the practical implications of proper estimation of the effective number of tests for large agnostic scans of available gene sets appear largely inconsequential. Although strict Bonferroni adjustment resulted in significantly conservative control of the FWER, the degree of this deviation was relatively marginal. As demonstrated by our proposed typical analyses of up to 6,124 gene sets, the effective number of tests tends to be approximately 70–80% of the total gene set count, based upon the Gao estimator

TABLE 5 Estimates of statistical power and minimum sample size to achieve 80% power for gene set  $S_4$  under a variety of sample size and total gene set conditions

		Continuous			Binary				
Analysis	Corr. Factor	N = 500	N = 1,000	$Min N (\beta = 0.8)$	N = 2,000	N = 4,000	$Min N (\beta = 0.8)$		
$A_1$	R	0.214	0.666	1,345	0.356	0.789	4,118		
	$R_{ m Gao}^{ m eff}$	0.229	0.680	1,320	0.373	0.799	4,014		
$A_2$	R	0.165	0.614	1,427	0.295	0.749	4,458		
	$R_{ m Gao}^{ m eff}$	0.178	0.629	1,405	0.311	0.760	4,367		
$A_3$	R	0.129	0.566	1,491	0.245	0.711	4,781		
	$R_{ m Gao}^{ m eff}$	0.136	0.575	1,480	0.254	0.719	4,721		

Results are presented at alpha levels defined by Bonferroni's correction using total number of gene sets R per analysis  $A_1, A_2$ , and  $A_3$ , as well as corresponding estimate of effective number of tests  $R_{\text{Circ}}^{\text{eff}}$ .



**FIGURE 3** Gene set Manhattan-style plot based upon gene-level SKAT-O analysis results for (A) hereditary PRCA and (B) schizophrenia case-control studies. Gene sets for each figure are initially sorted by significance and then reordered on the basis of expected correlation structure due to overlapping genes as well as *P*-value. The blue and red lines indicate Bonferroni-adjusted significance thresholds based upon the total number and effective number of gene set tests, respectively, while the size of each point is a function of the total number of genes per gene set. Gene sets declared significantly associated by the latter are highlighted by gene set name.

of  $R^{\rm eff}$ . However, targeted analyses of relatively few highly overlapping gene sets may induce a stronger correlation structure. Consequently, estimation of  $R^{\rm eff}$  may be useful on a case-by-case basis to evaluate the test statistic correlation structure for a given analysis when designing a pathway-centric sequencing study.

We applied gsSKAT to two different case-control studies of rare variation: the ICPCG case-control WES study of hereditary PRCA as well as a previously published large case-control study of schizophrenia using exome chip data by the PGC. For the former, we identified one significant result, the GO gene set GO:0042981, which encompasses 341 genes that modulate the occurrence and/or rate of apoptotic processes. Programmed cell death is a fundamental mechanism of tumor suppression, and genetic damage of apoptotic pathways is a key stage in tumorigenesis (Brown & Attardi, 2005). Although the scale of this finding in regards to number of genes renders interpretation relatively difficult, follow-

up custom-capture sequencing of the gene set members in a replication cohort could assist in resolving what elements of apoptotic pathways are relevant to hereditary PRCA.

The schizophrenia analysis results from gsSKAT are unexpected in that Richards et al. (2016) also conducted exploratory gene set analyses on these data, albeit by directly applying SKAT-O to the complete variant sets. However, neither of the two hits we identified were among the subset of moderately associated (P < 0.01) gene sets reported by Richards et al., despite their inclusion in the afore-mentioned analyses. Although the correlation between direct SKAT-O results and those obtained via gene-level P-value aggregation is markedly reduced in comparison to SKAT, it is nonetheless surprising to observe such a disparity. The gene set in question is the GO set GO:0046467, a biological process gene set corresponding to reactions or molecular pathways involved in the formation of membrane lipids. There is a large body of literature indicating membrane lipids play a role in the

development of schizophrenia (Dodd, 1996; Fenton, Hibbeln, & Knable, 2000; Solberg, Bentsen, Refsum, & Andreassen, 2015). Recently, Steen et al. (2016) also published research implicating SREBP-mediated lipid biosynthesis via genetic variation in transcription factor genes SREBF1 and SREBF2 in the development of schizophrenia. The top gene-level result within this pathway was phosphatidylinositol glycan anchor biosynthesis class  $G(PIGG: P = 1.8 \times 10^{-4})$ , which belongs to a class of genes involved in glycosylphosphatidylinositol biosynthesis. Pathogenic genetic variation in PIGG was recently identified to cause intellectual disability with hypotonia (Makrythanasis et al., 2016). Interestingly, multiple PIG genes were also recently identified to overlap copy number variations associated with schizophrenia (Morris & Pratt, 2014).

A notable shortcoming of our strategy is that it necessitates the use of linear kernel functions in the kernel-based score testing to satisfy the underlying assumptions. Extensions to nonlinear kernel functions, such as the Gaussian kernel, are limited by the inability to decompose the composite gene set kernel matrix into a linear combination of gene-level component kernels. Consequently, not only must  $Q_S$  be explicitly computed from the complete data, but deriving the covariance structure of gene set statistics requires much more rigor. However, this could still be obtained relatively efficiently using parallel computing and/or trace inequalities. Extending meta-analytic strategies for SKAT (Lee, Teslovich, Boehnke, & Lin, 2013) to aggregate results not only across genes in gene sets, but also across different studies is another research avenue of interest. Finally, we would recommend to investigators with access to complete data to adopt previously mentioned adaptive approaches for rare-variant gene set analyses, such as SKAT-ARTP (Yan et al., 2014) or aSPUpath (Pan et al., 2015), as the corresponding improvements in statistical power reported by the authors likely justify the computational costs. Additionally, permutation schemes that adapt to the estimated null tail probability can render these approaches feasible for larger agnostic scans, although careful consideration is necessary for sufficient permutations to appropriately control the Type I error rate under high multiple testing dimensionality (Phipson & Smyth, 2010). We have conveniently provided an R implementation for the above-described methods with code available in the Supporting Information. We have also currently built in support for the Gene Matrix Transposed (GMT) file format to easily import gene set definitions and readily enable rare-variant gene set scans of popular curated gene sets available on the MSigDB website.

As our understanding of molecular pathways and their modularity continues to improve, leveraging-curated gene sets may improve rare-variant association studies of complex traits where genetic heterogeneity is plausible. Our work demonstrates that applying *P*-value aggregation methods to gene-level kernel testing results can be an effective strategy

for large-scale evaluation of gene sets using summary statistics from rare-variant association studies.

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#### CONFLICT OF INTEREST

The authors declare no conflict of interest.

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#### SUPPORTING INFORMATION

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