

# Chemistry—A European Journal

## Supporting Information

### [ $\text{Ga}^{3+}$ <sub>8</sub> $\text{Sm}^{3+}$ <sub>2</sub>, $\text{Ga}^{3+}$ <sub>8</sub> $\text{Tb}^{3+}$ <sub>2</sub>] Metallacrowns are Highly Promising Ratiometric Luminescent Molecular Nanothermometers Operating at Physiologically Relevant Temperatures

Elvin V. Salerno,<sup>[a]</sup> Justyna Zeler,<sup>[b, c]</sup> Svetlana V. Eliseeva,\*<sup>[d]</sup> Miguel A. Hernández-Rodríguez,<sup>[b]</sup> Albano N. Carneiro Neto,<sup>[b]</sup> Stéphane Petoud,\*<sup>[d]</sup> Vincent L. Pecoraro,\*<sup>[a]</sup> and Luís D. Carlos\*<sup>[b]</sup>

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## Experimental

*Metallacrown synthesis.* [MC:Sm] and [MC:Tb] were synthesized following the previously described procedure and correspond to the general composition  $[Ga_8Ln_2(shi)_8(ip)_4(DMF)_2(H_2O)_2](NH_4^+)_2 \cdot 12DMF$  ( $Ln = Sm, Tb$ ; where  $ip = [isophthalate]^{2-}$ ,  $shi = [salicylhydroxamate]^{3-}$ ).<sup>[1]</sup>

*Encapsulation of [MC:Ln] in polystyrene beads.* 100 nm diameter amino-functionalized polystyrene beads ( $PS/NH_2$ ) were purchased from micromod Partikeltechnologie GmbH (Rostock, Germany). An encapsulation of [MC:Ln] inside  $PS/NH_2$  beads was performed following a procedure that we have previously developed.<sup>[1]</sup> In general, a water suspension of  $PS/NH_2$  beads (10 mg/mL, 300  $\mu L$ ) was mixed with solutions of either [MC:Sm], [MC:Tb] or [MC:Sm,Tb] (10 mM, 50  $\mu L$ ) dissolved in dimethylformamide (DMF) and vortexed for 1 hour. In the case of [MC:SmTb], the solution was prepared in 0.5 [MC:Sm] and 0.5 [MC:Tb] proportions. Next, 300  $\mu L$  of water was added and the suspension was centrifuged (15200 rpm, 30 min). The supernatant was removed and [MC:Ln] $@PS/NH_2$  beads were washed with 300  $\mu L$  of water three times and were finally resuspended in  $H_2O$  at a concentration of 10 mg/mL. Each washing step was accompanied by 30 min of sonication at room temperature. The supernatants collected after centrifugation and washings were checked by absorption spectroscopy and no detectable bands corresponding to [MC:Ln] absorption were observed indicating that the encapsulation step was complete.

*Photoluminescence and Temperature Control.* Emission and excitation spectra for the 10 mg/mL aqueous suspensions of [MC:Ln] $@PS/NH_2$  beads were recorded with a modular double grating excitation spectrofluorimeter with a TRIAX 320 emission monochromator (Fluorolog-3, Horiba Scientific) coupled to a R928 Hamamatsu photomultiplier using a front face configuration. A 450 W Xe arc lamp was used as the excitation source. Both emission and excitation spectra were corrected for the spectrofluorimeter optical spectral response and the spectral distribution of the lamp intensity using a photodiode reference detector, respectively. For the temperature-dependent (298-328 K) luminescence experiments performed on aqueous suspensions of [MC:Ln] $@PS/NH_2$  beads, the sample was in contact with a heating stage (Linkam, THMS 600).

For measurements of luminescence lifetimes, samples were placed into a closed-cycle Sumitomo cryostat (Janis Research CCS-500/204), while the temperature was controlled by a LakeShore temperature controller (Model 331). Luminescence lifetimes were determined under excitation at 355 nm provided by a Nd:YAG laser (YG 980; Quantel), the signals in the visible at 490 nm (Tb,  $^5D_4$  level) and 702 nm (Sm,  $^4G_{5/2}$  level) were detected by a Hamamatsu R928 PMT connected to

an iHR320 monochromator (Horiba Scientific). The output signals from the detector were fed into a 500 MHz bandpass digital oscilloscope (TDS 754C; Tektronix) and transferred to a PC for data processing using Origin 8® software. Luminescence lifetimes are averages of three independent measurements.

*Repeatability.* The repeatability of 10 mg/mL aqueous suspensions of [MC:Ln]@PS/NH<sub>2</sub> beads were estimated by cycling the temperature from 298 K up to 328 K, ensuring that each measurement is performed with the samples in thermal equilibrium with the temperature controller. The repeatability upon temperature cycling was quantified using the following expression:

$$R = 1 - \frac{\delta\Delta_m}{\bar{\Delta}} \quad (\text{S1})$$

where  $\delta\Delta_m$  is the maximum standard deviation in  $\Delta$  and  $\bar{\Delta}$  is the mean value of  $\Delta$  during the temperature cycling. The precision of R is derived from  $\delta\Delta_m$ .

## Theoretical

### Ligand-to-Ln energy transfer

The intramolecular energy transfer (IET) rates were calculated taking into account the dipole–dipole ( $W_{d-d}$ ), dipole–multipole ( $W_{d-m}$ ), and exchange mechanisms ( $W_{ex}$ ) in coordination compounds.<sup>[2–6]</sup> The coordination compounds herein analyzed are based on structural data and first excited states obtained from the experimental data. More details on the quantities in the equations below are in Refs. [2–8].

[Eq. \(S2\)](#) provides the dipole–dipole IET while the dipole–multipole ones ( $2^K$ -poles,  $K = 2, 4$ , and  $6$ , respectively) is given by [Eq. \(S3\)](#):

$$W_{d-d} = \frac{S_L(1 - \sigma_1)^2}{(2J + 1)G} \frac{4\pi e^2}{\hbar R_L^6} \sum_K \Omega_K^{FED} \langle \psi^* J^* \parallel U^{(K)} \parallel \psi J \rangle^2 F \quad (\text{S2})$$

$$W_{d-m} = \frac{S_L}{(2J + 1)G} \frac{2\pi e^2}{\hbar} \sum_K (K + 1) \frac{\langle r^K \rangle^2}{(R_L^{K+2})^2} \langle f \parallel C^{(K)} \parallel f \rangle^2 (1 - \sigma_K)^2 \langle \psi^* J^* \parallel U^{(K)} \parallel \psi J \rangle^2 F \quad (\text{S3})$$

where the intensity parameters  $\Omega_K^{FED}$  are obtained by using only the forced electric dipole mechanism (Judd-Ofelt theory<sup>[9,10]</sup>). The sets of  $\Omega_K^{FED}$  (in units of  $10^{-20} \text{ cm}^2$ ) values were obtained using the Simple Overlap model<sup>[11,12]</sup> (considering the charge factors equal 1): Sm<sup>3+</sup> { $\Omega_2 = 0.056$ ;  $\Omega_4 = 0.787$ ;  $\Omega_6 = 1.379$ } and Tb<sup>3+</sup> { $\Omega_2 = 0.028$ ;  $\Omega_4 = 0.273$ ;  $\Omega_6 = 0.458$ }.

$S_L$  is the dipole strength of the ligand transition concerning IET,  $\langle r^K \rangle$  are the  $4f$  radial integrals,  $G$  is the ligand state degeneracy,  $R_L$  (5.98 Å) is the donor–acceptor states distance,  $\langle f \parallel C^{(K)} \parallel f \rangle$  is the reduced matrix element of Racah's tensor operator,  $(1 - \sigma_K)$  are the shielding factors, and  $\langle \psi^* J^* \parallel U^{(K)} \parallel \psi J \rangle^2$  are the squared reduced matrix elements from Carnall *et al.*<sup>[13]</sup>.

The IET rate by the exchange interaction ([Eq. S4](#)) can be calculated by:

$$W_{ex} = \frac{\langle 4f | L \rangle^4}{(2J + 1)} \frac{8\pi e^2}{3\hbar R_L^4} \langle \psi^* J^* \parallel S \parallel \psi J \rangle^2 \sum_m |\langle \phi | \sum_j \mu_z(j) s_m(j) | \phi^* \rangle|^2 F \quad (\text{S4})$$

where  $\langle 4f | L \rangle$  is the overlap integral between the ligand donor state and the  $4f$  acceptor state at  $R_L$  distance,  $s_m$  the spin operator of electron  $j$  in the ligand,  $\mu_z$  is the dipole operator ( $z$ -component), and  $\langle \psi^* J^* \parallel S \parallel \psi J \rangle$  is the reduced matrix elements of the spin operator obtained using free-ion wavefunctions in the intermediate coupling scheme<sup>[14,15]</sup>.

$F$  (quantity in Eqs. S2, S3, and S4) is the energy mismatch condition which contains a sum over Franck-Condon factors.<sup>[3,6]</sup> In the case of IET involving lanthanide complex,  $F$  can be obtained by:

$$F = \frac{1}{\hbar\gamma_L} \sqrt{\frac{\ln(2)}{\pi}} e^{-\left(\frac{\Delta E}{\hbar\gamma_L}\right)^2 \ln(2)} \quad (\text{S5})$$

Eq. (S5) can be assumed only when the corresponding bandwidth at half-height for the ligand ( $\gamma_L$ ) is much larger than the lanthanide ( $\gamma_{Ln}$ ) ion<sup>[6,16]</sup>,  $\gamma_L \gg \gamma_{Ln}$ .  $\Delta$  (in  $\text{cm}^{-1}$ ) is the band maximum energy difference between ligand donor state and lanthanide ion acceptor state,  $\Delta E = E_L - E_{Ln}$ .

The forward IET for the  $i$ -th pathway ( $W_i$ ) is calculated by the sum over all Eqs. (S2), (S3), and (S4):

$$W_i = W_{d-d} + W_{d-m} + W_{ex} \quad (\text{S6})$$

The backward IET ( $W_i^b$ ), that is, the energy returned from acceptor to donor state, is obtained with the same above equations, except for multiplying the energy mismatch factor  $F$  (Eq. (S5)) by the energy barrier factor  $e^{-\left(\frac{|\Delta|}{k_b T}\right)}$ , where  $k_b$  is the Boltzmann's constant in units of  $\text{cm}^{-1}\cdot\text{K}^{-1}$ . The IET values for [MC:Sm] and [MC:Tb] are presented in Table S7 and S8.

### ***Ln-to-Ln energy transfer***

The non-radiative energy transfer rates between lanthanide ions were calculated taking into account the dipole–dipole ( $W_{d-d}$ ), the dipole–quadrupole ( $W_{d-q}$ ), the quadrupole–quadrupole ( $W_{q-q}$ ), and the exchange ( $W_{ex}$ ) mechanisms<sup>[5]</sup>:

$$W_{d-d} = \frac{(1 - \sigma_1^D)^2 (1 - \sigma_1^A)^2}{[J_D^*][J_A]} \frac{4\pi}{3\hbar} \frac{e^4}{R_L^6} \left( \sum_K \Omega_K^D \langle \psi_D J_D \parallel U^{(K)} \parallel \psi_D^* J_D^* \rangle^2 \right) \times \\ \times \left( \sum_K \Omega_K^A \langle \psi_A J_A^* \parallel U^{(K)} \parallel \psi_A J_A \rangle^2 \right) F \quad (\text{S7})$$

$$W_{d-q, q-d} = \frac{(1 - \sigma_1^{D,A})^2 (1 - \sigma_2^{A,D})^2}{[J_D^*][J_A]} \frac{\pi}{\hbar} \frac{e^4}{R_L^8} \langle f \| C^{(2)} \| f \rangle^2 \\ \times \left[ \left( \sum_K \Omega_K^D \langle \psi_D J_D \| U^{(K)} \| \psi_D^* J_D^* \rangle^2 \right) \langle r^2 \rangle_A^2 \langle \psi_A J_A^* \| U^{(2)} \| \psi_A J_A \rangle^2 \right. \\ \left. + \left( \sum_K \Omega_K^A \langle \psi_A J_A \| U^{(K)} \| \psi_A^* J_A^* \rangle^2 \right) \langle r^2 \rangle_D^2 \langle \psi_D^* J_D^* \| U^{(2)} \| \psi_D J_D \rangle^2 \right] F \quad (\text{S8})$$

$$W_{q-q} = \frac{(1 - \sigma_2^D)^2 (1 - \sigma_2^A)^2}{[J_D^*][J_A]} \frac{28\pi}{5\hbar} \frac{e^4}{R_L^{10}} \times \times \langle r^2 \rangle_D^2 \langle r^2 \rangle_A^2 \langle f \| C^{(2)} \| f \rangle^4 \langle \psi_D J_D \| U^{(2)} \| \psi_D^* J_D^* \rangle^2 \\ \times \langle \psi_A^* J_A^* \| U^{(2)} \| \psi_A J_A \rangle^2 F \quad (\text{S9})$$

$$W_{ex} = \frac{2\pi}{\hbar} \left[ \left( \frac{e^2}{R_L} \right) \rho_{f-f}^2 \right]^2 F \quad (\text{S10})$$

where the intensity parameters  $\Omega_K$  are the same obtained for the IET rates, once in Kushida's expressions the appearance of the  $\Omega_K$  parameters is due to opposite parity configuration mixing, by the odd components of the ligand field, like in the Judd-Ofelt theory [17].

In Eq. (S10),  $\rho_{f-f}$  is the overlap integral between the  $4f$  subshells of the donor and acceptor lanthanide ions. Figure S8 shows the behavior of the  $\rho_{f-f}$  with the distance of for the pair Tb–Sm. Each value was calculated with the ADF (Amsterdam Density Functional) program [18]. A DFT level of theory with the GGA BP86 functional [19,20] (Becke for the exchange and Perdew for the correlation effects), TZ2P Slater-Type basis set [21], and the inclusion of ZORA (zero-order regular approximation) scalar relativistic effects [22–24].  $\langle r^K \rangle$  are the  $4f$  radial integrals [25].

In the case of energy transfer between two lanthanide ions the following analytical expression for  $F$  has been used [5]:

$$F = \frac{\ln(2)}{\sqrt{\pi}} \frac{1}{\hbar^2 \gamma_D \gamma_A} \left\{ \left[ \left( \frac{1}{\hbar \gamma_D} \right)^2 + \left( \frac{1}{\hbar \gamma_A} \right)^2 \right] \ln(2) \right\}^{-\frac{1}{2}} \\ \times \exp \left[ \frac{1}{4} \frac{\left( \frac{2\Delta E}{(\hbar \gamma_D)^2} \ln 2 \right)^2}{\left[ \left( \frac{1}{\hbar \gamma_A} \right)^2 + \left( \frac{1}{\hbar \gamma_D} \right)^2 \right] \ln 2} - \left( \frac{\Delta E}{\hbar \gamma_D} \right)^2 \ln(2) \right] \quad (\text{S11})$$

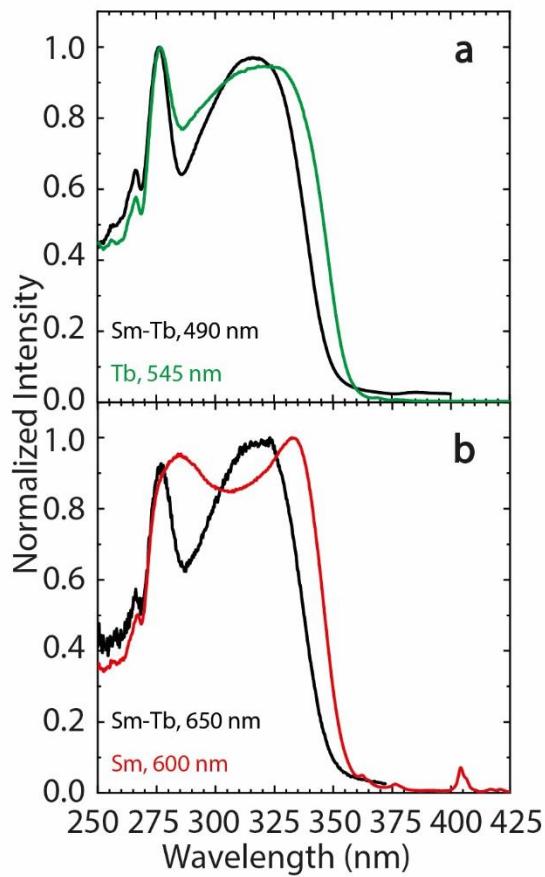
where  $\hbar\gamma_D$  and  $\hbar\gamma_A$  correspond to the bandwidths at half-height (in erg) of the donor and acceptor. For the present analysis, we considered  $\gamma_D = \gamma_A = 400 \text{ cm}^{-1}$ .  $\Delta E$  is the energy difference between donor and acceptor transitions,  $\Delta E = E_D - E_A$ .

The energy transfer mechanisms, pathways and their respective donor and acceptor states ([Figure S9](#)) were selected according to energy mismatch conditions and selection rules on the  $J$  quantum numbers. These selection rules are: for the multipolar mechanisms ( $W_{d-d}$ ,  $W_{d-q}$  and  $W_{q-q}$ )  $|J - J'| \leq K \leq J + J'$ ; for the exchange mechanism ( $W_{ex}$ ) no defined selection rules on  $J$  appear. [\[26\]](#)

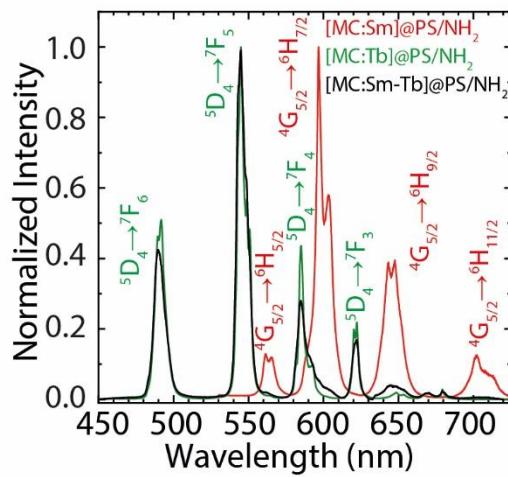
The energy transfer rates, in the same pathway, were calculated by the sum over [Eqs. \(S7\)–\(S10\)](#) ( $W = W_{d-d} + W_{d-q} + W_{q-q} + W_{ex}$ ) multiplying by the barrier factor if  $\Delta$  is negative ([Figure S9](#)).

Since the [MC:Sm][MC:Tb] is a mixture of [MC:Sm] and [MC:Tb] samples, the shortest plausible distance Tb–Sm is  $R_L = 12.82 \text{ \AA}$ , coming from the closest intermolecular  $\text{Ln}^{3+}$ - $\text{Ln}^{3+}$  distance in the  $\text{Ln}_2\text{Ga}_8$  crystal structure. [\[27\]](#) The values of  $W$  at this distance are presented in [Table S9](#) and [Figure S10](#). The highest energy transfer rate is the  $\text{Tb}^{3+}(^5\text{D}_4 \rightarrow ^7\text{F}_6) \rightarrow \text{Sm}^{3+}(^6\text{H}_{5/2} \rightarrow ^4\text{I}_{9/2})$  pathway with an inexpressive rate of  $4.18 \times 10^{-3} \text{ s}^{-1}$ . For the sake of comparison, in a cubic system  $\text{Cs}_2\text{NaLnCl}_6$  ( $\text{Ln} = \text{Yb}^{3+}$ ,  $\text{Er}^{3+}$ ) elpasolite, the energy transfer rate at the shortest Yb–Er distance ( $7.7 \text{ \AA}$ ) is  $2.15 \times 10^2$  and  $2.60 \times 10^2 \text{ s}^{-1}$  (depending on the  $\text{Er}^{3+}$  acceptor levels) [\[28\]](#), five orders of magnitude higher than Tb–Sm rates in [MC:Sm][MC:Tb]. This supports the nullity of  $\text{Tb}^{3+}$ - $\text{Sm}^{3+}$  energy transfer.

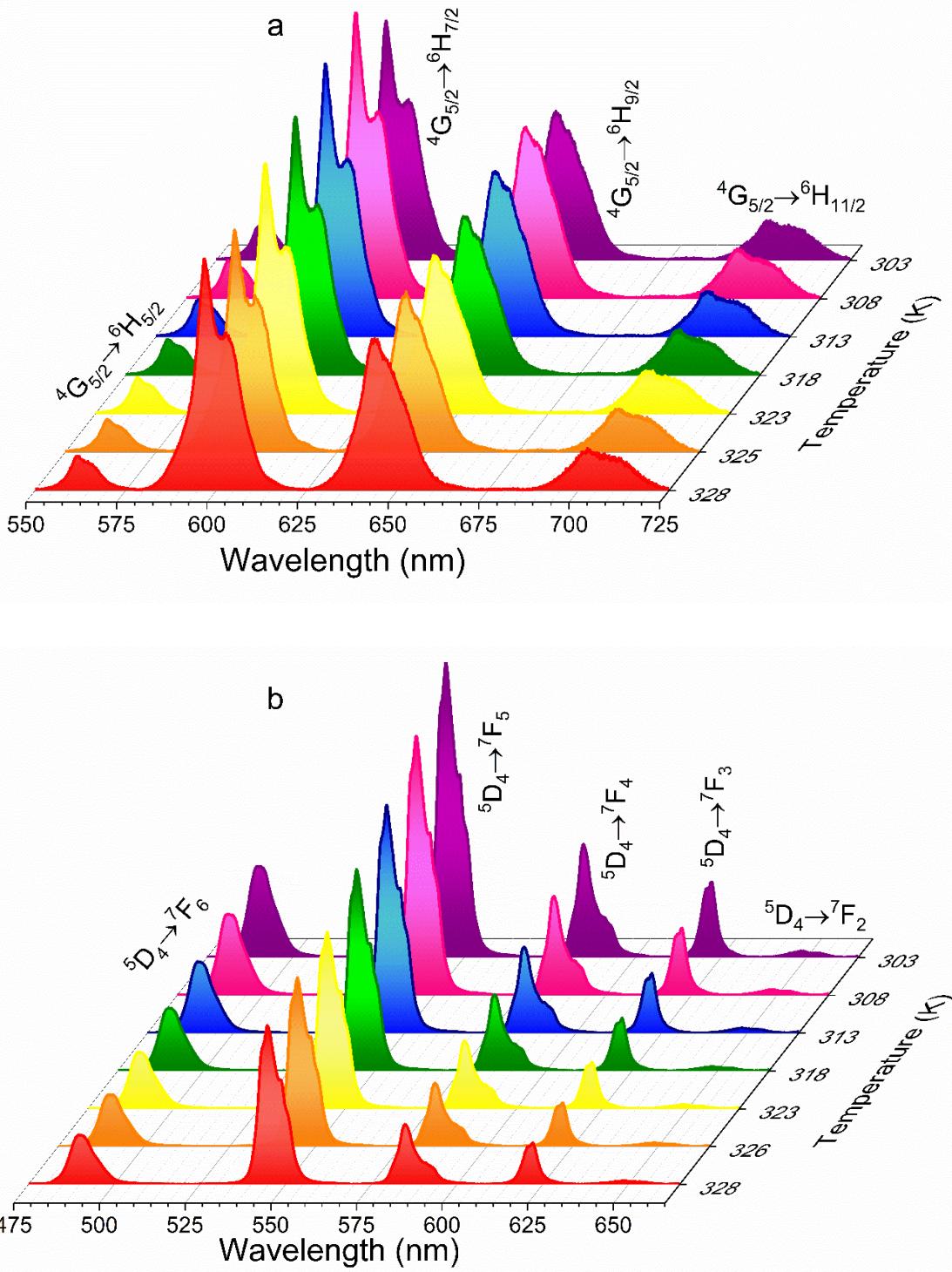
## Figures



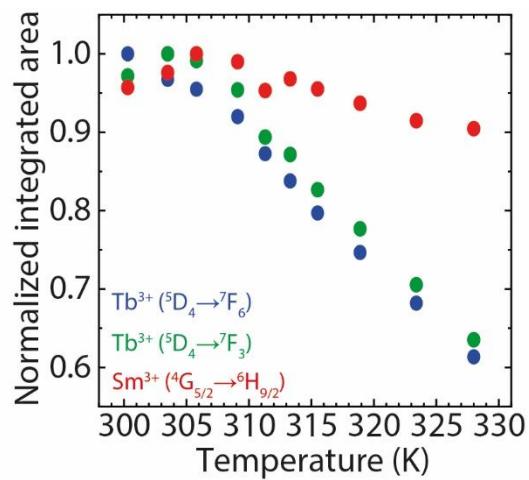
**Figure S1.** Excitation spectra of the 10 mg/mL aqueous suspension of  $[\text{MC:Sm,Tb}]@\text{PS/NH}_2$ ,  $[\text{MC:Tb}]@\text{PS/NH}_2$ , and  $[\text{MC:Sm}]@PS/\text{NH}_2$  beads while monitoring the main emission bands of the (a)  $\text{Tb}^{3+}$  and (b)  $\text{Sm}^{3+}$  cations at room temperature. The monitored wavelengths are indicated.



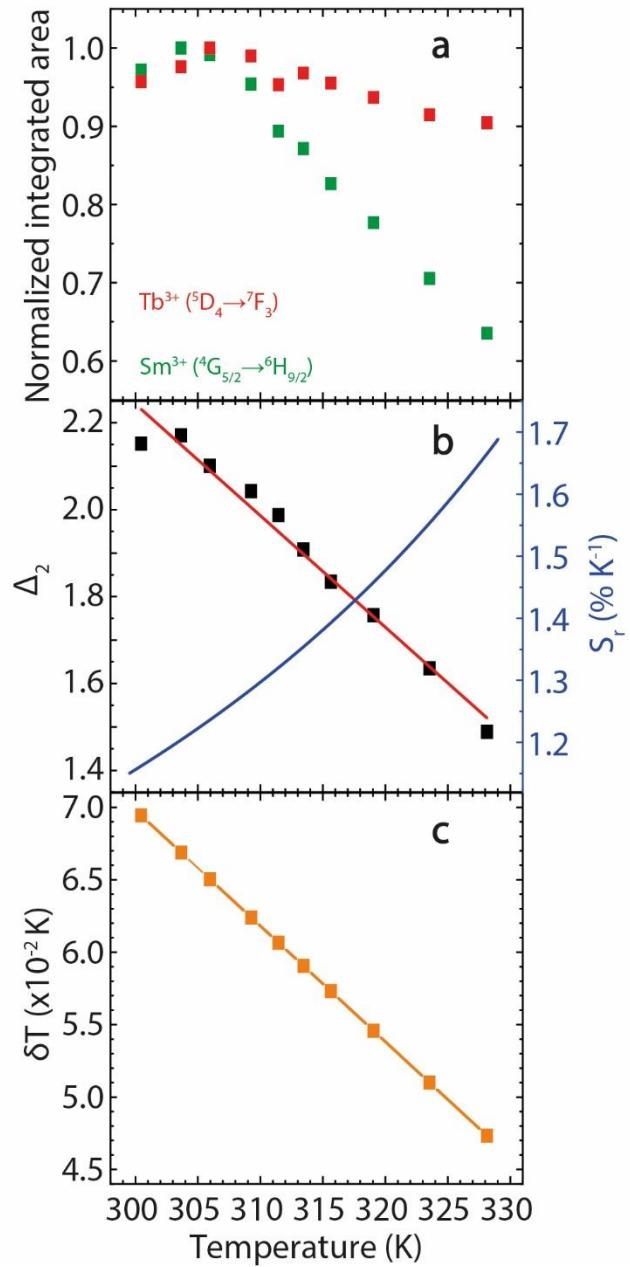
**Figure S2.** The normalized emission spectra of  $[\text{MC:Sm}]@PS/\text{NH}_2$ ,  $[\text{MC:Tb}]@PS/\text{NH}_2$  and  $[\text{MC:Sm,Tb}]@PS/\text{NH}_2$ , under 340 nm excitation with indicated emission transitions of  $\text{Sm}^{3+}$  in red and  $\text{Tb}^{3+}$  in green.



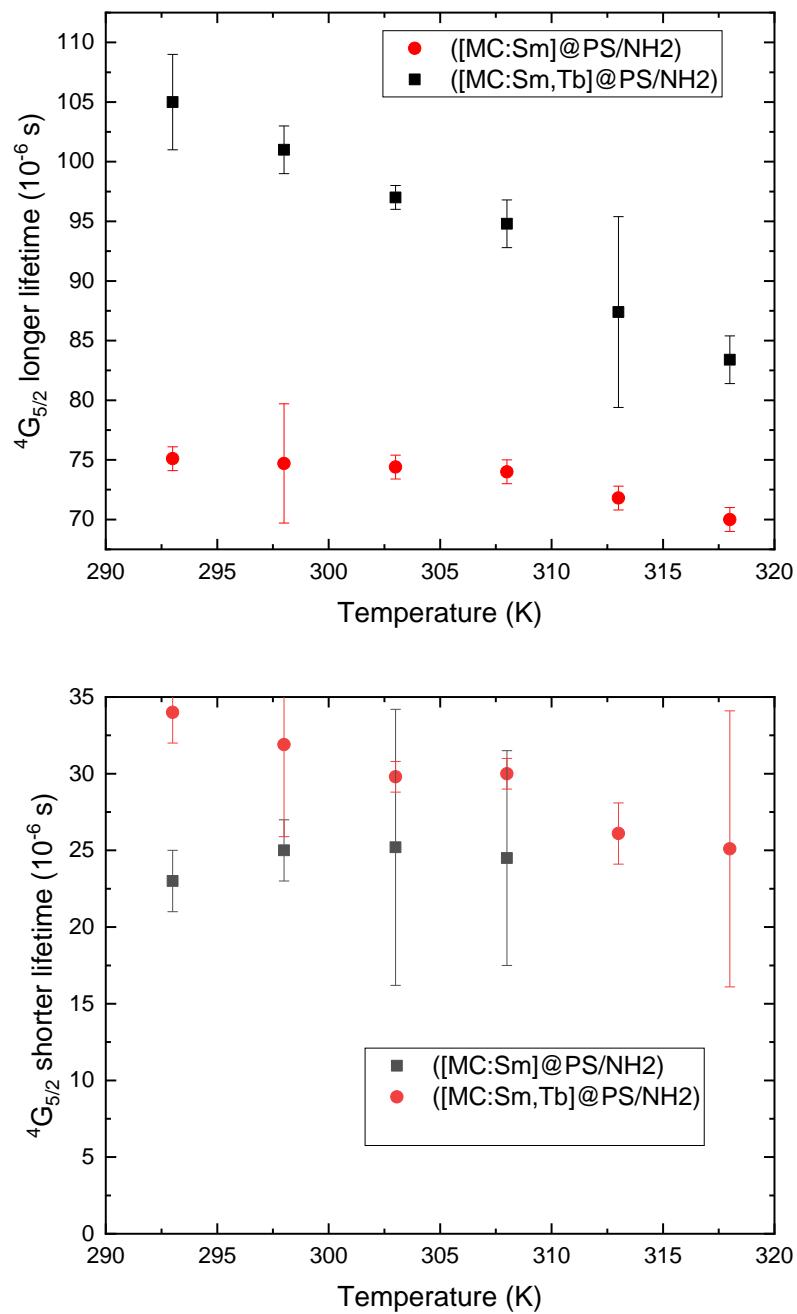
**Figure S3.** The temperature dependent emission spectra of a)  $[MC:Sm]@PS/NH_2$  and b)  $[MC:Tb]@PS/NH_2$  beads under 340 nm excitation.



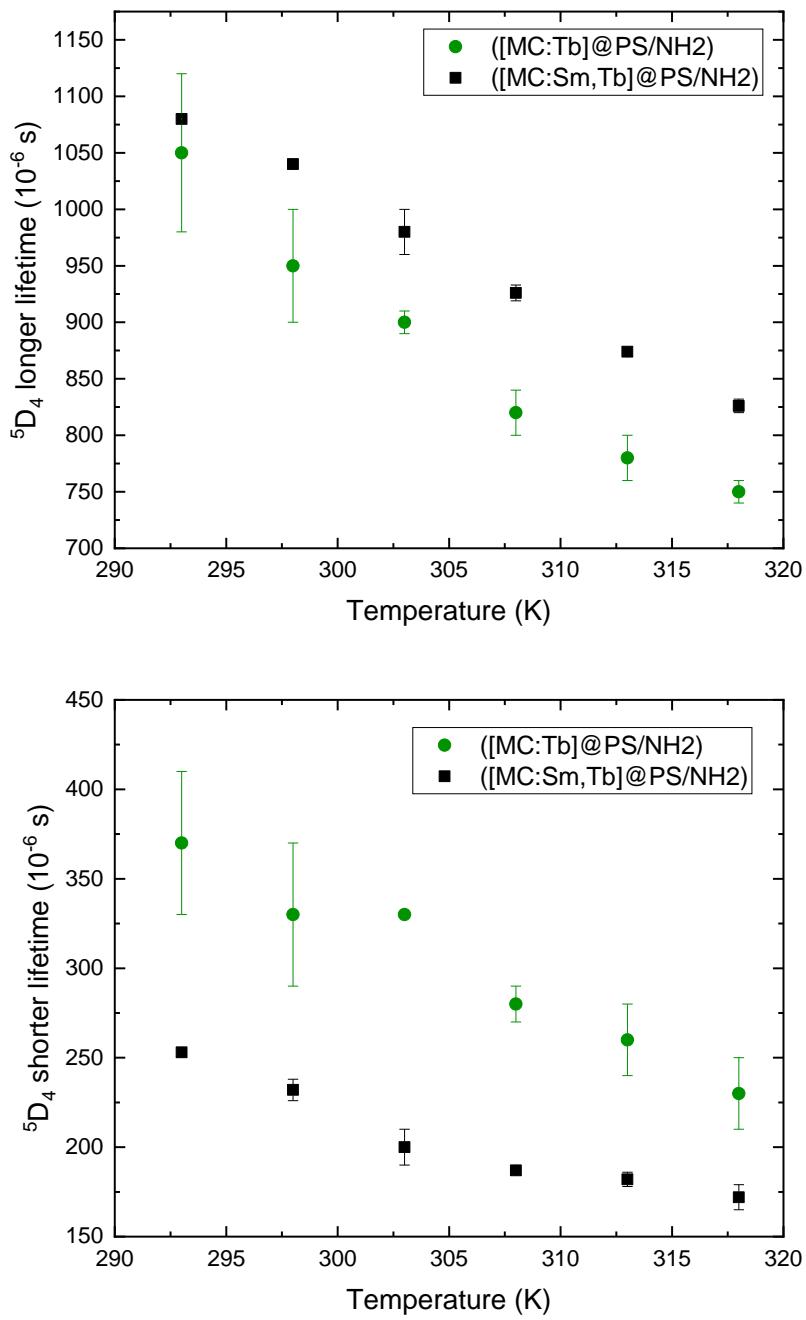
**Figure S4.** Luminescent behaviour of the 10 mg/mL aqueous suspension of [MC:Sm,Tb]@PS/NH<sub>2</sub> beads upon excitation at 340 nm at temperatures ranging from 298 K to 328 K.



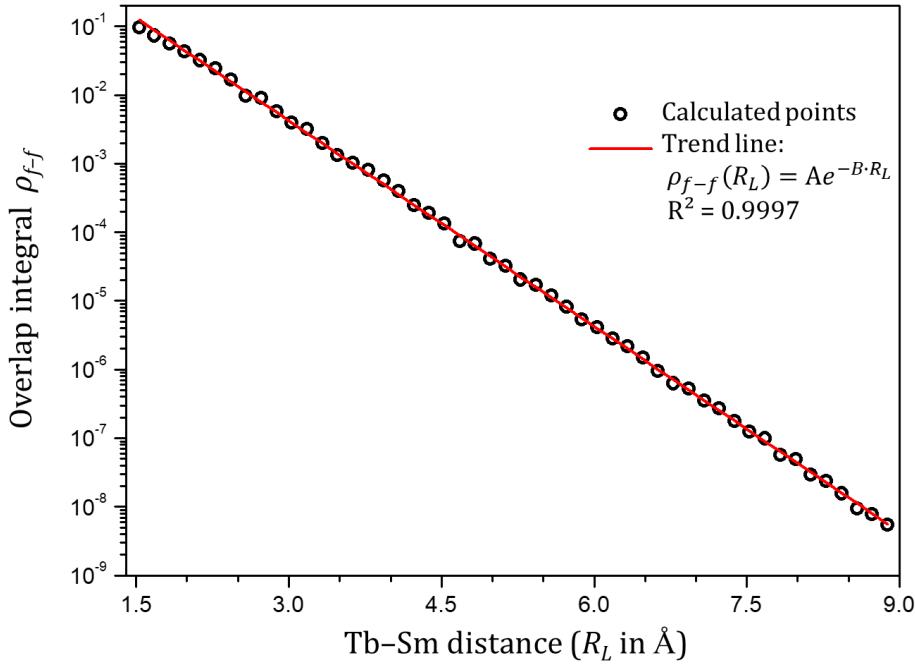
**Figure S5.** Thermometric behaviour of the 10 mg/mL aqueous suspension of [MC:Sm,Tb]@PS/NH<sub>2</sub> beads upon excitation at 340 nm in the temperature range 298 - 328 K. **(a)** Temperature evolution of the normalized integrated area of the emissions associated to Sm<sup>3+</sup> ( ${}^4\text{G}_{5/2} \rightarrow {}^6\text{H}_{9/2}$ ) (red) and Tb<sup>3+</sup> ( ${}^5\text{D}_4 \rightarrow {}^7\text{F}_3$ ) (green) from 298 K to 328 K. **(b)** Ratio of the normalized integrated areas of the  ${}^5\text{D}_4 \rightarrow {}^7\text{F}_3$ / ${}^4\text{G}_{5/2} \rightarrow {}^6\text{H}_{9/2}$  ( $\Delta_2$ ) transitions as well as its corresponding  $S_r$  (blue curve), obtained from the linear fits (red curve) of the experimental thermometric parameter. **(c)** The temperature uncertainty,  $\delta T$ , vs. temperature.



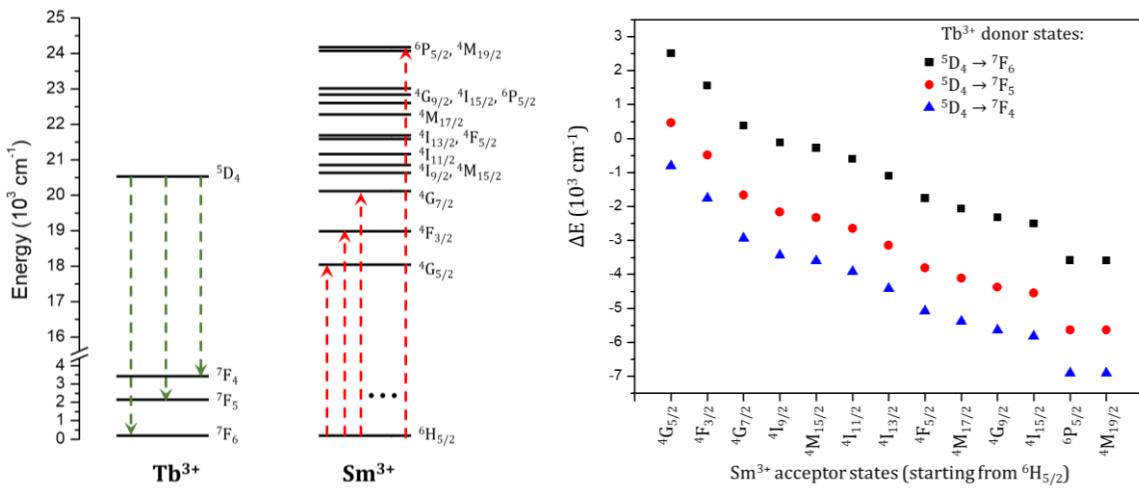
**Figure S6.** Luminescence lifetimes versus temperatures for the  ${}^4G_{5/2}$  level in the mixed  $([MC:Sm,Tb]@PS/NH_2)$  and pure  $([MC:Sm]@PS/NH_2)$  samples. Longer component ( $\tau_1$ ), shorter component ( $\tau_2$ ) from Tables S3, S4.



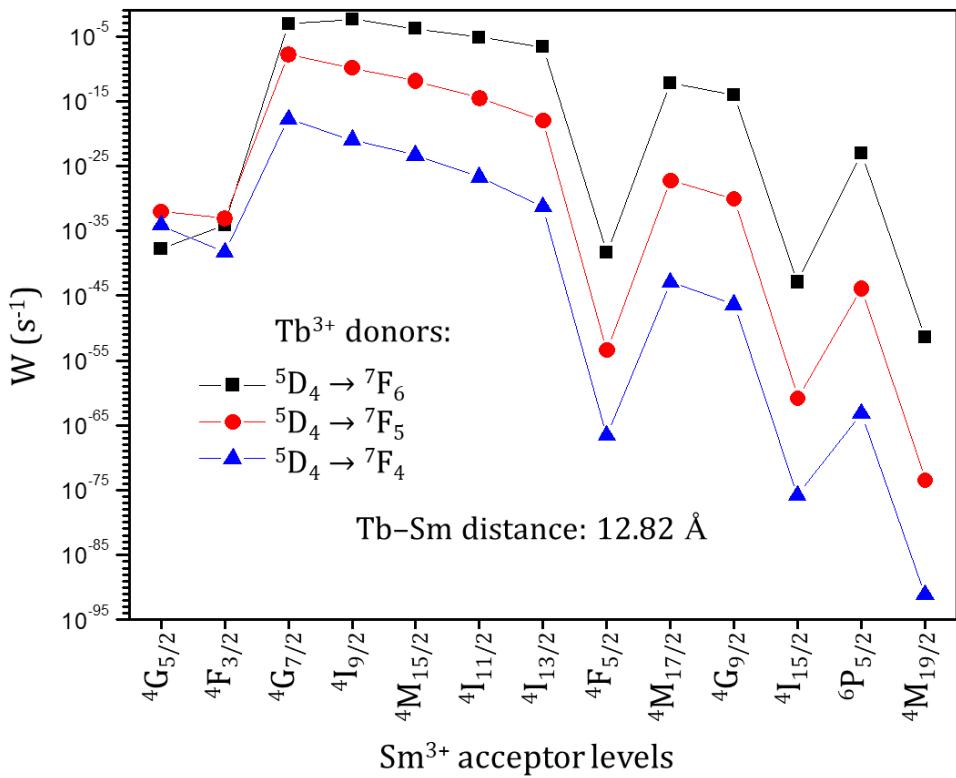
**Figure S7.** Luminescence lifetimes versus temperatures for the the  ${}^5D_4$  level in the mixed ([MC:Sm,Tb]@PS/NH<sub>2</sub>) and pure ([MC:Tb]@PS/NH<sub>2</sub>) samples. Longer component ( $\tau_1$ ), shorter component ( $\tau_2$ ) from Tables S5, S6.



**Figure S8.** Log-linear graph of 4f-4f overlap integral ( $\rho_{f-f}$ ) versus Tb-Sm distance ( $R_L$ ). Each point was calculated with the ADF program [18] using a DFT level of theory (BP86 functional [19,20], TZ2P basis set [21], and the inclusion of ZORA scalar relativistic effects [22–24]). The trend line has as parameters  $A = 4.176$  and  $B = 2.299$ .



**Figure S9.** Schematic energy level diagram showing the energy levels of the donor ( $Tb^{3+}$ ) and the acceptor ( $Sm^{3+}$ ) involved in the energy transfer processes (left panel). The values of  $\Delta E$  (used in Eq. (S11)) for the selected energy transfer pathways (right panel).



**Figure S10.** Log scale of the  $W$  values according to each pathway. The highest energy transfer rate is the  $Tb^{3+}(^5D_4 \rightarrow ^7F_6) \rightarrow Sm^{3+}(^6H_{5/2} \rightarrow ^4I_{9/2})$  pathway with a rate of  $4.18 \times 10^{-3} s^{-1}$ . This only reinforces that the energy transfer between  $Tb^{3+}$  and  $Sm^{3+}$  ions can be neglected.

## Tables

**Table S1.** Parameters of the  $\Delta(T)$  calibration curves (straight lines) of the [MC:Sm,Tb]@PS/NH<sub>2</sub> beads. Ratios of the integrated areas of the  $^5D_4 \rightarrow ^7F_6$  (Tb<sup>3+</sup>)/ $^4G_{5/2} \rightarrow ^6H_{9/2}$  (Sm<sup>3+</sup>) ( $\Delta_1$ ) and  $^5D_4 \rightarrow ^7F_3$  (Tb<sup>3+</sup>)/ $^4G_{5/2} \rightarrow ^6H_{9/2}$  (Sm<sup>3+</sup>) ( $\Delta_2$ ) transitions were compared.

Thermometric parameter	Intercept	Slope	$r^2$
$\Delta_1$	11.79±0.13	-0.109 ± 0.003	0.99
$\Delta_2$	2.93±0.06	-0.026 ± 0.001	0.97

**Table S2.** Selected ratiometric Ln<sup>3+</sup>-based luminescent nanothermometers. Excitation wavelength ( $\lambda_x$ ), form of the samples, transitions involved, maximum relative sensitivity,  $S_m$ , in physiological range and the temperature ( $T_m$ ) in which it occurs.

Optical sensor	Form	$\lambda_x$ (nm)	Transitions	Physiological range (298–323 K)		References
				$S_m$ (% K <sup>-1</sup> )	$T_m$ (K)	
Er-Yb@LaF <sub>3</sub> :Yb-Tm nanoparticles <sup>c</sup>	Aqueous suspension	690	$^2F_{5/2} \rightarrow ^2F_{7/2}$ $^4I_{13/2} \rightarrow ^4I_{15/2}$	5	293	[29]
MOF: Nd <sub>0.866</sub> Yb <sub>0.134</sub> BTB <sup>c</sup>	Powder	808	$^2F_{5/2} \rightarrow ^2F_{7/2}$ $^4F_{3/2} \rightarrow ^4I_{11/2}$	4.755	333	[30]
Eu <sub>0.058</sub> Tb <sub>0.942</sub> BPT <sup>a</sup>	Powder	325	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	2.3	323	[31]
[MC:Sm,Tb]@PS/NH <sub>2</sub> <sup>b</sup>	Aqueous suspension	340	$^5D_4 \rightarrow ^7F_6$ $^4G_{5/2} \rightarrow ^6H_{9/2}$	1.7	323	This work
Eu <sup>3+</sup> -Tb <sup>3+</sup> functionalized SAM <sup>b</sup>	Powder	280	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	1.4	323	[32]
MOF-5: Eu <sup>3+</sup> -Tb <sup>3+</sup> <sup>b</sup>	Powder	325	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	0.7	323	[33]
LnMOF Eu <sub>0.37</sub> Tb <sub>0.63</sub> -BTC-a <sup>b</sup>	Powder	296	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	0.5	313	[34]
Na[(Gd <sub>0.8</sub> Eu <sub>0.1</sub> Tb <sub>0.1</sub> )SiO <sub>4</sub> ] <sup>c</sup>	Powder	483.5	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	0.3	300	[35]
MOF: Tb <sup>3+</sup> -Eu <sup>3+</sup> <sup>c</sup>	Spray-dried	377	$^5D_4 \rightarrow ^7F_5$ $^5D_0 \rightarrow ^7F_2$	0.078	300	[36]

<sup>a</sup> Ligand-to-Ln<sup>3+</sup> energy transfer. No information about temperature uncertainty is available.

<sup>b</sup> Ligand-to-Ln<sup>3+</sup> energy transfer.

<sup>c</sup> Ln<sup>3+</sup>-to-Ln<sup>3+</sup> energy transfer.

**Table S3.** Observed luminescence lifetimes of the  ${}^4G_{5/2}$  level ( $\lambda_{\text{em}} = 702$  nm) for a 10 mg/mL suspension of 100 nm [MC:Sm]@PS/NH<sub>2</sub> beads in water upon excitation at 355 nm (2 $\sigma$  values between parentheses).

T (K)	$\tau_1$ (μs)	$B_1$ (%)	$\tau_2$ (μs)	$B_2$ (%)
293	75.1(1)	97.1(4)	23(2)	2.9(4)
298	74.7(5)	96.5(2)	25(2)	3.5(2)
303	74.4(1)	96.2(4)	25.2(9)	3.8(4)
308	74(1)	95.6(4)	24.5(7)	4.4(4)
313	71.8(1)	100		
318	70(1)	100		

**Table S4.** Observed luminescence lifetimes of the  ${}^4G_{5/2}$  level ( $\lambda_{\text{em}} = 702$  nm) for a 10 mg/mL suspension of 100 nm [MC:Sm,Tb]@PS/NH<sub>2</sub> beads in water upon excitation at 355 nm (2 $\sigma$  values between parentheses).

T (K)	$\tau_1$ (μs)	$B_1$ (%)	$\tau_2$ (μs)	$B_2$ (%)
293	105(4)	75.7(3)	34(2)	24.3(3)
298	101(2)	76.6(3)	31.9(6)	23.4(3)
303	97(1)	78.3(1)	29.8(1)	21.7(1)
308	94.8(2)	76(1)	30(1)	24(1)
313	87.4(8)	78.3(5)	26.1(2)	21.7(5)
318	83.4(2)	78(2)	25.1(9)	22(2)

**Table S5.** Observed luminescence lifetimes of the  ${}^5D_4$  level ( $\lambda_{\text{em}} = 490$  nm) for a 10 mg/mL suspension of 100 nm [MC:Tb]@PS/NH<sub>2</sub> beads in water upon excitation at 355 nm (2 $\sigma$  values between parentheses). Bi-exponential fit.

T (K)	$\tau_1$ (μs)	$B_1$ (%)	$\tau_2$ (μs)	$B_2$ (%)
293	950(50)	93(1)	178(9)	7(1)
298	840(30)	91(1)	164(1)	9(1)
303	770(30)	90(2)	149(2)	10(2)
308	700(30)	89(1)	136(3)	11(1)
313	640(20)	87(2)	121(3)	13(2)
318	580(20)	85(2)	105(7)	15(2)

**Table S6.** Observed luminescence lifetimes of the  $^5D_4$  level ( $\lambda_{\text{em}} = 490$  nm) for a 10 mg/mL suspension of 100 nm [MC:Sm,Tb]@PS/NH<sub>2</sub> beads in water upon excitation at 355 nm ( $2\sigma$  values between parentheses). Bi-exponential fit.

T (K)	$\tau_1$ (μs)	$B_1$ (%)	$\tau_2$ (μs)	$B_2$ (%)
293	830(10)	76.9(7)	142(7)	23.1(7)
298	813(7)	76.5(5)	134(5)	23.5(5)
303	775(1)	79.1(5)	107(3)	20.9(5)
308	751(4)	81.5(5)	94(4)	18.5(5)
313	707(7)	83.4(1)	81.8(8)	16.6(1)
318	668(3)	84.9(4)	72(1)	15.1(4)

**Table S7.** Forward and backward IET rates (in s<sup>-1</sup>) for [MC:Sm],  $\Delta E$  (in cm<sup>-1</sup>) is the donor–acceptor energy difference and the predominant mechanism is shown in the last column. The most effective pathways and the total contribution (from S<sub>1</sub> and T<sub>1</sub>) are highlighted in bold.

Pathway	Donor	Acceptor	$\Delta E$	W (forward)	W (backward)	Mechanism
1	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{5/2}$	13320	$8.27 \times 10^5$	$1.49 \times 10^{-22}$	exchange
2	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4F_{3/2}$	12369	0.00	0.00	dipole-dipole
3	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{7/2}$	11190	$5.72 \times 10^6$	$2.82 \times 10^{-17}$	exchange
4	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{9/2}$	10691	$1.49 \times 10^4$	$8.02 \times 10^{-19}$	dipole-multipole
5	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4M_{15/2}$	10526	$1.06 \times 10^3$	$1.27 \times 10^{-19}$	dipole-dipole
6	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{11/2}$	10204	$4.91 \times 10^2$	$2.74 \times 10^{-19}$	dipole-dipole
7	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{13/2}$	9707	$1.79 \times 10^3$	$1.08 \times 10^{-17}$	dipole-dipole
8	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4F_{5/2}$	9050	$5.18 \times 10^7$	$7.33 \times 10^{-12}$	exchange
9	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4M_{17/2}$	8739	$7.94 \times 10^2$	$4.99 \times 10^{-16}$	dipole-dipole
10	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{9/2}$	8478	$6.14 \times 10^2$	$1.35 \times 10^{-15}$	dipole-dipole
11	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4L_{13/2}$	6675	$9.18 \times 10^3$	$1.15 \times 10^{-10}$	dipole-dipole
12	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4F_{7/2}$	6356	$1.32 \times 10^8$	$7.60 \times 10^{-6}$	exchange
13	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^6P_{3/2}$	6287	$9.65 \times 10^4$	$7.75 \times 10^{-9}$	dipole-dipole
14	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4K_{11/2}$	6150	$2.13 \times 10^3$	$3.30 \times 10^{-10}$	dipole-dipole
15	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4L_{15/2}$	5684	$5.56 \times 10^3$	$8.05 \times 10^{-9}$	dipole-dipole
16	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{11/2}$	5522	$1.16 \times 10^3$	$3.66 \times 10^{-9}$	dipole-dipole
17	S <sub>1</sub>	$^6H_{5/2} \rightarrow ^6P_{7/2}$	<b>4565</b>	<b><math>1.20 \times 10^9</math></b>	<b><math>3.73 \times 10^{-1}</math></b>	<b>exchange</b>
<b>Total contribution from S<sub>1</sub></b>				<b><math>1.39 \times 10^9</math></b>	<b><math>3.73 \times 10^{-1}</math></b>	
18	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{5/2}$	<b>4050</b>	<b><math>1.90 \times 10^{10}</math></b>	<b><math>6.96 \times 10^1</math></b>	<b>exchange</b>
19	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4F_{3/2}$	3099	0.00	0.00	dipole-dipole
20	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{7/2}$	1920	$3.69 \times 10^8$	$3.69 \times 10^4$	exchange
21	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{9/2}$	1421	$7.24 \times 10^1$	$7.94 \times 10^{-2}$	dipole-multipole
22	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4M_{15/2}$	1256	4.00	$9.67 \times 10^{-3}$	dipole-dipole
23	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{11/2}$	934	1.43	$1.63 \times 10^{-2}$	dipole-dipole
24	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4I_{13/2}$	437	3.52	$4.33 \times 10^{-1}$	dipole-dipole
25	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4F_{5/2}$	-220	$7.26 \times 10^7$	$2.09 \times 10^8$	exchange
26	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4M_{17/2}$	-531	$4.39 \times 10^{-3}$	$5.60 \times 10^{-2}$	dipole-dipole
27	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4G_{9/2}$	-792	$2.29 \times 10^{-4}$	$1.02 \times 10^{-2}$	dipole-dipole
28	T <sub>1</sub>	$^6H_{5/2} \rightarrow ^4L_{13/2}$	-2595	$2.44 \times 10^{-11}$	$6.20 \times 10^{-6}$	dipole-dipole
<b>Total contribution from T<sub>1</sub></b>				<b><math>1.94 \times 10^{10}</math></b>	<b><math>2.09 \times 10^8</math></b>	

**Table S8.** Forward and backward IET rates (in  $s^{-1}$ ) for [MC:Tb],  $\Delta E$  (in  $cm^{-1}$ ) is the donor–acceptor energy difference and the predominant mechanism is shown in the last column. The most effective pathways and the total contribution (from  $S_1$  and  $T_1$ ) are highlighted in bold.

Pathway	Donor	Acceptor	$\Delta E$	$W$ (forward)	$W$ (backward)	Mechanism
1	<b><math>S_1</math></b>	$^7F_6 \rightarrow ^5L_6$	1640	<b><math>4.27 \times 10^5</math></b>	$1.64 \times 10^2$	exchange
2	<b><math>S_1</math></b>	$^7F_6 \rightarrow ^5H_7$	-129	<b><math>2.87 \times 10^5</math></b>	<b><math>5.32 \times 10^5</math></b>	exchange
3	$S_1$	$^7F_6 \rightarrow ^5H_6$	-1641	$1.46 \times 10^3$	$3.82 \times 10^6$	exchange
4	$S_1$	$^7F_6 \rightarrow ^5H_5$	-2517	0.00	0.00	dipole-dipole
5	$S_1$	$^7F_6 \rightarrow ^5F_5$	-3684	$1.03 \times 10^{-1}$	$4.87 \times 10^6$	exchange
6	$S_1$	$^7F_5 \rightarrow ^5L_6$	3688	$4.27 \times 10^4$	$8.90 \times 10^{-4}$	exchange
7	$S_1$	$^7F_5 \rightarrow ^5H_7$	1919	0.00	0.00	dipole-dipole
8	<b><math>S_1</math></b>	$^7F_5 \rightarrow ^5H_6$	<b>407</b>	<b><math>6.50 \times 10^5</math></b>	<b><math>9.23 \times 10^4</math></b>	exchange
9	<b><math>S_1</math></b>	$^7F_5 \rightarrow ^5H_5$	<b>-469</b>	<b><math>8.51 \times 10^5</math></b>	<b><math>8.07 \times 10^6</math></b>	exchange
10	$S_1$	$^7F_5 \rightarrow ^5F_5$	-1636	$3.18 \times 10^3$	$8.12 \times 10^6$	exchange
<b>Total contribution from <math>S_1</math></b>				<b><math>2.26 \times 10^6</math></b>	<b><math>2.55 \times 10^7</math></b>	
11	$T_1$	$^7F_6 \rightarrow ^5D_4$	1536	9.60	$6.07 \times 10^{-3}$	dipole-multipole
12	$T_1$	$^7F_6 \rightarrow ^5D_3$	-4256	$2.07 \times 10^{-11}$	$1.52 \times 10^{-2}$	dipole-dipole
13	<b><math>T_1</math></b>	$^7F_6 \rightarrow ^5G_6$	<b>-4443</b>	<b><math>2.33 \times 10^{-3}</math></b>	<b><math>4.19 \times 10^6</math></b>	exchange
14	$T_1$	$^7F_6 \rightarrow ^5L_{10}$	-4991	$1.64 \times 10^{-11}$	$4.08 \times 10^{-1}$	dipole-dipole
15	$T_1$	$^7F_6 \rightarrow ^5G_5$	-5787	$1.40 \times 10^{-7}$	$1.58 \times 10^5$	exchange
16	$T_1$	$^7F_6 \rightarrow ^5G_4$	-6307	$1.78 \times 10^{-14}$	$2.43 \times 10^{-1}$	dipole-multipole
17	$T_1$	$^7F_5 \rightarrow ^5D_4$	3584	$6.14 \times 10^5$	$2.10 \times 10^{-2}$	exchange
18	$T_1$	$^7F_5 \rightarrow ^5D_3$	-2208	$1.44 \times 10^{-4}$	5.72	dipole-multipole
19	<b><math>T_1</math></b>	$^7F_5 \rightarrow ^5G_6$	<b>-2395</b>	<b><math>1.22 \times 10^1</math></b>	<b><math>1.19 \times 10^6</math></b>	exchange
20	$T_1$	$^7F_5 \rightarrow ^5L_{10}$	-2943	$1.86 \times 10^{-8}$	$2.50 \times 10^{-2}$	dipole-dipole
21	<b><math>T_1</math></b>	$^7F_5 \rightarrow ^5G_5$	<b>-3739</b>	<b><math>4.53 \times 10^{-2}</math></b>	<b><math>2.78 \times 10^6</math></b>	exchange
22	$T_1$	$^7F_5 \rightarrow ^5G_4$	-4259	$3.94 \times 10^{-4}$	$2.93 \times 10^5$	exchange
<b>Total contribution from <math>T_1</math></b>				<b><math>6.14 \times 10^5</math></b>	<b><math>8.61 \times 10^6</math></b>	

**Table S9.** Energy transfer rates ( $s^{-1}$ ) from  $Tb^{3+}$  to  $Sm^{3+}$  for each mechanism using the crystallographic closest distance  $R_L = 12.82 \text{ \AA}$ .  $W$  is the sum over all mechanisms considering the barrier factor (if applicable). One should notice that the energy transfer  $Tb^{3+}(^5D_4 \rightarrow ^7F_6) \rightarrow Sm^{3+}(^6H_{5/2} \rightarrow ^4I_{9/2})$  has the highest contribution (pathway 4, highlighted in bold).

Pathway Label	Donor	Acceptor	$W_{d-d}$	$W_{d-q}$	$W_{q-q}$	$W_{ex}$	$W$
1	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4G_{5/2}$	0.00	0.00	0.00	$1.72 \times 10^{-38}$	$1.72 \times 10^{-38}$
2	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4F_{3/2}$	0.00	0.00	0.00	$7.63 \times 10^{-35}$	$7.63 \times 10^{-35}$
3	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4G_{7/2}$	$2.47 \times 10^{-6}$	$5.74 \times 10^{-5}$	$7.31 \times 10^{-4}$	$1.10 \times 10^{-32}$	$7.90 \times 10^{-4}$
<b>4</b>	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4I_{9/2}$	<b><math>1.79 \times 10^{-6}</math></b>	<b><math>8.31 \times 10^{-5}</math></b>	<b><math>7.16 \times 10^{-3}</math></b>	<b><math>1.47 \times 10^{-32}</math></b>	<b><math>4.18 \times 10^{-3}</math></b>
5	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4M_{15/2}$	$2.79 \times 10^{-5}$	$5.96 \times 10^{-4}$	0.00	$1.28 \times 10^{-32}$	$1.63 \times 10^{-4}$
6	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4I_{11/2}$	$5.25 \times 10^{-6}$	$1.12 \times 10^{-4}$	0.00	$6.92 \times 10^{-33}$	$6.54 \times 10^{-6}$
7	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4I_{13/2}$	$1.93 \times 10^{-6}$	$4.13 \times 10^{-5}$	0.00	$1.11 \times 10^{-33}$	$2.22 \times 10^{-7}$
8	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4F_{5/2}$	0.00	0.00	0.00	$1.91 \times 10^{-35}$	$4.19 \times 10^{-39}$
9	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4M_{17/2}$	$5.35 \times 10^{-10}$	$1.14 \times 10^{-8}$	0.00	$1.45 \times 10^{-36}$	$5.93 \times 10^{-13}$
10	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4G_{9/2}$	$2.66 \times 10^{-11}$	$5.67 \times 10^{-10}$	0.00	$1.21 \times 10^{-37}$	$8.41 \times 10^{-15}$
11	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4I_{15/2}$	0.00	0.00	0.00	$1.94 \times 10^{-38}$	$1.19 \times 10^{-43}$
12	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^6P_{5/2}$	$1.14 \times 10^{-17}$	$2.43 \times 10^{-16}$	0.00	$1.19 \times 10^{-44}$	$8.58 \times 10^{-24}$
13	$^5D_4 \rightarrow ^7F_6$	$^6H_{5/2} \rightarrow ^4M_{19/2}$	0.00	0.00	0.00	$1.09 \times 10^{-44}$	$3.57 \times 10^{-52}$
14	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4G_{5/2}$	0.00	0.00	0.00	$9.48 \times 10^{-33}$	$9.48 \times 10^{-33}$
15	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4F_{3/2}$	0.00	0.00	0.00	$9.11 \times 10^{-33}$	$8.90 \times 10^{-34}$
16	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4G_{7/2}$	$1.77 \times 10^{-8}$	$2.88 \times 10^{-6}$	$3.94 \times 10^{-5}$	$3.77 \times 10^{-35}$	$1.45 \times 10^{-8}$
17	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4I_{9/2}$	$1.53 \times 10^{-10}$	$2.85 \times 10^{-8}$	$4.62 \times 10^{-6}$	$6.02 \times 10^{-37}$	$1.45 \times 10^{-10}$
18	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4M_{15/2}$	$5.53 \times 10^{-10}$	$8.88 \times 10^{-8}$	0.00	$1.21 \times 10^{-37}$	$1.27 \times 10^{-12}$
19	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4I_{11/2}$	$5.97 \times 10^{-12}$	$9.60 \times 10^{-10}$	0.00	$3.76 \times 10^{-39}$	$2.92 \times 10^{-15}$
20	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4I_{13/2}$	$2.68 \times 10^{-14}$	$4.30 \times 10^{-12}$	0.00	$7.32 \times 10^{-42}$	$1.21 \times 10^{-18}$
21	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4F_{5/2}$	0.00	0.00	0.00	$3.70 \times 10^{-46}$	$4.42 \times 10^{-54}$
22	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4M_{17/2}$	$1.38 \times 10^{-21}$	$2.22 \times 10^{-19}$	0.00	$1.78 \times 10^{-48}$	$6.00 \times 10^{-28}$
23	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4G_{9/2}$	$6.76 \times 10^{-24}$	$1.09 \times 10^{-21}$	0.00	$1.47 \times 10^{-50}$	$8.40 \times 10^{-31}$
24	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4I_{15/2}$	0.00	0.00	0.00	$4.98 \times 10^{-52}$	$1.65 \times 10^{-61}$
25	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^6P_{5/2}$	$4.08 \times 10^{-35}$	$6.55 \times 10^{-33}$	0.00	$2.04 \times 10^{-62}$	$1.21 \times 10^{-44}$
26	$^5D_4 \rightarrow ^7F_5$	$^6H_{5/2} \rightarrow ^4M_{19/2}$	0.00	0.00	0.00	$1.76 \times 10^{-62}$	$3.14 \times 10^{-74}$
27	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4G_{5/2}$	0.00	0.00	0.00	$3.78 \times 10^{-33}$	$8.11 \times 10^{-35}$
28	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4F_{3/2}$	0.00	0.00	0.00	$1.96 \times 10^{-35}$	$4.41 \times 10^{-39}$
29	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4G_{7/2}$	$4.19 \times 10^{-14}$	$2.12 \times 10^{-13}$	$1.85 \times 10^{-12}$	$1.26 \times 10^{-40}$	$1.65 \times 10^{-18}$
30	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4I_{9/2}$	$2.34 \times 10^{-17}$	$6.63 \times 10^{-16}$	$1.40 \times 10^{-14}$	$1.30 \times 10^{-43}$	$1.06 \times 10^{-21}$
31	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4M_{15/2}$	$3.42 \times 10^{-17}$	$1.09 \times 10^{-16}$	0.00	$1.05 \times 10^{-44}$	$4.66 \times 10^{-24}$
32	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4I_{11/2}$	$6.30 \times 10^{-20}$	$2.01 \times 10^{-19}$	0.00	$5.59 \times 10^{-47}$	$1.83 \times 10^{-27}$
33	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4I_{13/2}$	$1.85 \times 10^{-23}$	$5.89 \times 10^{-23}$	0.00	$7.12 \times 10^{-51}$	$4.96 \times 10^{-32}$
34	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4F_{5/2}$	0.00	0.00	0.00	$9.78 \times 10^{-57}$	$2.68 \times 10^{-67}$
35	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4M_{17/2}$	$4.69 \times 10^{-33}$	$1.50 \times 10^{-32}$	0.00	$8.55 \times 10^{-60}$	$1.21 \times 10^{-43}$
36	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4G_{9/2}$	$5.48 \times 10^{-36}$	$1.75 \times 10^{-35}$	0.00	$1.68 \times 10^{-62}$	$4.05 \times 10^{-47}$
37	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4I_{15/2}$	0.00	0.00	0.00	$2.18 \times 10^{-64}$	$1.66 \times 10^{-76}$
38	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^6P_{5/2}$	$3.30 \times 10^{-50}$	$1.05 \times 10^{-49}$	0.00	$2.33 \times 10^{-77}$	$5.82 \times 10^{-64}$
39	$^5D_4 \rightarrow ^7F_4$	$^6H_{5/2} \rightarrow ^4M_{19/2}$	0.00	0.00	0.00	$1.95 \times 10^{-77}$	$7.96 \times 10^{-92}$
<i>Total Tb-Sm energy transfer</i>							<b><math>5.14 \times 10^{-3}</math></b>

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