# Finding General Patterns in Fitness Landscapes 

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## Dedicación

Para Mami Dina y Papa Manuel. Me dieron la fuerza para estudiar.

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#### Abstract

Biological phenomena can be examined at multiple levels of organization. For example, the role of individual amino acids in protein function representing a low level, the interactions between genes underlying complex traits as an intermediate level, and evolutionary processes across taxa at the highest level. Phenomena at each level must emerge from processes at lower levels. Thus, understanding this emergence is crucial for a full understanding of any biological phenomenon, including the genetic basis of disease and the course of evolution. My thesis focuses on how mutational effects propagate across these levels of organization.


My second chapter develops a null theory for how mutational effects scale to complex phenotypes, from which universal evolutionary patterns emerge. Although mutational effects have predictable, deterministic effects on lower level phenotypes, the complexity of interactions that determine phenotypes like fitness results in a seeming randomness of mutational effects, or idiosyncrasy, at this higher level. Universal evolutionary patterns in adaptation, mutation accumulation, and the effects of mutations across fitness levels then emerge as statistical laws from this randomness. This null theory of "idiosyncratic interactions" resolves a paradox in the common, but mistaken, interpretation of these universal evolutionary patterns. My third and fourth chapters capture a deviation from this null theory, showing that a feature at the lowest level, the radical- or conservative-ness of amino acid substitutions, leads to predictable fitness differences and may bias phylogenetic patterns. Across most phyla, there is a substitution bias towards transitions versus transversions; there has been a long-standing debate over whether this
bias is due to a mutational bias or selection. In my third chapter I show that transversions are more detrimental to fitness in two RNA viruses, influenza virus and HIV. This can be partly explained by their greater likelihood to cause radical amino acid changes, which are more detrimental. Thus, selection is likely a major contributor to the transition-transversion substation bias. My fourth chapter examines further consequences of radical versus conservative amino acid changes. Uncovering the molecular constraints on proteins and the changes responsible for adaptations are major goals in molecular evolution. I find that while proteins are constrained in accepting radical amino acid changes in influenza virus, HIV, and additionally in Zika virus, such radical changes are also the most beneficial, conditional on being beneficial. Multinucleotide mutations, which are more likely to cause radical changes due to the genetic code, show the same pattern as radical changes. These findings have implications for viral evolution, phylogenetic inference of selection, and the evolution of the genetic code. Our null theory of idiosyncratic epistasis may help guide future work on how deviations from our predictions at the level of evolutionary patterns reflect the organization of interactions at the level of complex phenotypes and the biological properties of individual genes or mutations at the lowest level.

## Chapter 1 Introduction

Note: This chapter is a modified version of the published article:
Lyons DM, Lauring AS. 2018. Mutation and Epistasis in Influenza Virus Evolution. Viruses. 10(8):407. doi:10.3390/v10080407.

## Overview

The diversity of life is amazing, from the wings of a ruby-throated hummingbird flapping at hundreds of times per second to the intricate geometric shapes of viral capsids. Perhaps even just as beautiful is the fact that all of life's diversity is generated by the same evolutionary processes. To understand how life's diversity is produced through evolution, understanding the effects of mutations is crucial. Because all life originated from a common ancestor, this diversity must be generated by the accumulation of mutations through billions of years. However, it is not only the accumulation of single mutations that contribute to diversity, but the interactions between mutations. The same mutation can have varying effects depending on the other mutations present.

Epistasis refers to the genetic interactions between two or more mutations in a genome. It is useful to think about epistasis using the image of a mountainous landscape (Phillips 2008). Here, each point on the landscape is a genotype, and the height represents the fitness of the genotype (Figure 1-1). If there were no epistasis, then this fitness landscape would have a single peak, and populations might adapt, or climb up that peak, linearly with each mutation (Figure 11A). However, because of epistasis, these landscapes are more rugged, with different peaks and valleys representing unexpected fitness effects of mutational combinations (Figure 1-1B). The
shape of this landscape determines how a population will evolve (Phillips 2008). For example, how quickly it can climb a peak or which peaks are accessible without crossing a low fitness valley. The combinatorics of mutations vastly increases the potential diversity of life. The space of possible genotypes is enormous. Even the collection of all genomes of all organisms that have ever lived, represents a tiny point in a vast space of possible genotypes. For a genome the size of the influenza virus, the number of possible genotypes is larger than the number of particles in the observable universe.


Figure 1-1. Schematic of fitness landscapes
A smooth fitness landscape without epistasis (A) and a rugged one with epistasis (B). In both, height represents fitness and the orthogonal axes represent genetic distance.

How can we understand this vast space in which evolution occurs? The projects in this dissertation advance our understanding from two perspectives. The first nearly dispenses with biological details, showing how universal patterns in evolutionary trajectories and mutational effects uncovered over the last decade can emerge from underlying randomness in mutational effects. The second turns to the biological details of mutational effects in RNA viruses, showing that the structure of the genetic code and properties of amino acids likely contribute to
widespread patterns in molecular evolution. Below, I review the literature on mutational effects and epistasis in general and as it pertains to the influenza virus, an RNA virus.

## Mutational Effects and Epistasis

Enormous successes in molecular biology and biomedical science have been made by probing the effects of individual genes or mutations in model systems, from our basic understanding of bacterial gene regulation to the hormonal control of metabolism (Stent 1964; Pelleymounter et al. 1995). Life-saving cures have been developed by probing the structure and function of individual molecules with single mutations. A classic example is cystic fibrosis, which is commonly caused by a single amino acid deletion (Boyle and De Boeck 2013). Understanding how this mutation causes a misfolded protein led to the development of effective drug treatments.

Despite its historical success, the limits of research into the impact of single mutations and the function of individual molecules have become clear. No single gene or mutation can account for the development of complex traits or diseases like diabetes (Manolio et al. 2009). Often, a polymorphism linked to a trait in one population is unimportant in other populations, likely due to interactions with other polymorphisms (Moore 2003; Carlborg and Haley 2004). Findings in model systems like mice often do not translate to humans (Perel et al. 2007), partly due to epistasis with human-specific substitutions. Disease-causing polymorphisms in humans are frequently the wild-type in other species (Xu and Zhang 2014). While we can often understand the effect of individual mutations or interactions (Figure 1-2, bottom), it is extremely difficult to predict how such effects scale to higher levels of biological organization that involve many interactions - like the metabolism of an organism, complex phenotypes, or fitness (Figure 1-2, middle). If we cannot understand how the effects of individual mutations scale to intermediate
phenotypes or fitness, their effects on evolutionary processes are even more opaque (Figure 1-2, top).


Adaptive Mutations


Random Mutations


Background Fitness

Evolutionary Patterns


Fitness \& Complex Phenotypes
$\uparrow$


Individual mutational effects

Figure 1-2. How mutational effects scale across levels of biological organization.

At the bottom level, the function of individual genes or effects of individual mutations are largely predictable given sufficient biophysical knowledge. Here, the red mutation towards a larger amino acid diminishes the function of the blue enzyme. Despite their deterministic actions, mutational effects at the level of fitness or complex phenotypes are highly unpredictable (middle). Somehow, unpredictability in the effect of mutations at the intermediate level leads to universal patterns during evolution. (top).

## Defining and measuring epistasis

Epistasis ( $\epsilon$ ) refers to the genetic interactions between two or more mutations in a genome. Epistasis is most commonly defined as the difference between the observed fitness of the genome with both mutations i and $\mathrm{j}\left(\mathrm{w}_{\mathrm{ij}}\right)$ and the expected fitness given independent multiplicative effects of each single mutation (Figure 1-3A) (Mani et al. 2008). Thus, $\epsilon=\mathrm{w}_{\mathrm{ij}}$ $w_{i} \times w_{j}$, where $\epsilon=0$ indicates no genetic interaction. Negative epistasis $(\epsilon<0)$ occurs when the fitness of a double mutant is less than expected. Positive epistasis $(\epsilon>0)$ occurs when the fitness of the double mutant is greater than expected. As we mainly discuss epistasis as either positive or
negative below, we refer the reader to (Mani et al. 2008) for a more detailed review of epistasis terminology.


Figure 1-3. Identifying epistasis.
(A) Epistasis is defined based on deviation from the expected fitness assuming independent multiplicative effects. Black, red, and blue mutations are each deleterious (filled individual circles) and the expected fitness of pairwise combinations (empty circles) is shown. Black and red mutations exhibit positive epistasis because combining them is not as deleterious as expected and may even increase fitness. Black and blue mutations exhibit negative epistasis because combining them is more deleterious than expected. (B) Positive epistasis can be inferred phylogenetically. Red and blue mutations interact positively as they are always present together and occur closely in time. In contrast, yellow and purple mutations do not occur closely in time and are not necessarily present together.

Mutational fitness effects can be measured in a variety of ways. Site-directed mutagenesis allows for precise control of the identity and number of mutations created. This is usually combined with a competitive fitness assay that provides a precise measure of the fitness of a given mutant relative to the wild-type (Sanjuán 2010; Visher et al. 2016), an approach that is reliable, but labor-intensive. Deep mutational scanning (DMS) combines large-scale mutagenesis with bulk fitness measurements of a mutagenized library through next generation sequencing (Fowler and Fields 2014). This method allows for a nearly complete sampling of single mutations across a gene. To detect epistasis, DMS results can be compared across different genetic backgrounds (Doud et al. 2015; Haddox et al. 2018). Alternatively, a short region that can be covered by a
single sequencing read can be used to detect linkage between multiple mutations. However, DMS is less sensitive for lethal and low fitness mutations. A third strategy that can uncover mutational effects in natural environments is to examine patterns of polymorphism in a population, such as during viral infections by deep sequencing, or to examine substitution patterns phylogenetically (Zhang 2000; Gojobori et al. 2007; Keightley and Halligan 2011; Chen et al. 2019). These approaches interrogate the effect of mutations in a realistic environment (Nielsen and Yang 2003; Tamuri et al. 2012; Poon et al. 2016; McCrone et al. 2018). However, they often cannot assign fitness effects to individual mutations or determine the strength of interactions. Thus, these three approaches therefore provide complementary insights into the mutational fitness effects and epistasis.

## Theories of epistasis and fitness landscapes

Theoretical work on the structure of fitness landscapes falls on a continuum from general mathematical models of interactions between elements of complex systems to theories informed by biological observations.

## Mathematical models

The most general models include the NK-landscape, the House-of-Cards model, and the Rough Mount Fuji model, among others. In the NK-landscape, each of N loci (which could be genomic sites, genes, or even molecules in a magnet) interacts with K other randomly chosen loci (Kauffman and Weinberger 1989). A fitness contribution of each of the N loci is chosen randomly for each combination of the allelic states of each site's K interacting loci. The fitness of a genotype is the average of the fitness contributions of all N loci. When K is less than N , a single mutation does not change all the fitness contributions and thus fitness is correlated among related genotypes. The House-of-Cards model is a special case of the NK landscape, where $\mathrm{K}=$
$\mathrm{N}-1$ and the fitness of each genotype is chosen randomly, with no correlation among related genotypes (Fragata et al. 2019). Fitness correlation among genotypes is also tunable in the Rough Mount Fuji Model, but without an explicit model of interactions (Neidhart et al. 2014). This model begins with non-epistatic landscape and an optimal genotype and linearly decreasing fitness of each genotype with genetic distance from the optimum (like in Figure 1-1A). To introduce epistasis, a random variable akin to "noise" is added to the fitness of each genotype, creating a landscape more like Figure 1-1B. This noise variable can be tuned to introduce varying levels of epistasis.

The utility of these models has been to guide our intuition of how epistatic interactions influence the structure of the fitness landscape (Kryazhimskiy et al. 2009; Fragata et al. 2019). For example, how does fitness of peaks and the number of different peaks and their accessibility, or the ruggedness of the landscape, scale with epistasis (K or noise) (Kauffman and Levin 1987; Kauffman 1993; Neidhart et al. 2014)? The fitness of the best genotype in the landscape increases with epistasis and the number of loci. However, the mean fitness of peaks is the highest when there is epistasis, but only a small amount (e.g. $0<\mathrm{K} \ll \mathrm{N}$ ). Moreover, the number of peaks increases exponentially with more epistasis, leading to lower accessibility of each individual peak as adaptive walks get stuck at a peak more quickly. Thus, although increasing N and K leads to higher fitness of the optimum genotype, adaptation will terminate at lower and lower fitness peaks. Interestingly, this can be thought of as a cost to complexity, as increasing the number of interacting parts ( N and K ) makes adaptation more difficult. The NK model has also been modified to investigate how genetic architecture influences landscape structure by choosing the interacting K sites non-randomly, say from neighboring sites. Some studies have shown that
a modular architecture can circumvent this cost to complexity (Earl and Deem 2004; Nowak and Krug 2015; Hwang et al. 2018). These models are also ideal for studying evolutionary processes that depend on epistasis and which require more knowledge of the fitness landscape than can be obtained from empirical data, such as the benefits of sexual recombination or the ability of drift to promote the crossing of fitness valleys (Kryazhimskiy et al. 2009; Nahum et al. 2015; Zagorski et al. 2016; Agarwala and Fisher 2019; Fragata et al. 2019; Reia and Campos). Another hope for these models has been to extrapolate global properties from small empirical landscapes (Kauffman and Weinberger 1989). Some studies have gauged the ruggedness of real landscapes by fitting these models to real data, but without much success beyond the unsurprising result that real landscapes lie somewhere between additive and the House-of-Cards model in terms of ruggedness (Fragata et al. 2019). A complementary use of these models is to gauge the reliability and properties of various measures of ruggedness and adaptability that can then be used to analyze empirical data (Siliang Song, personal correspondence). While the theoretical implications of these models have been important, their use in uncovering the parameters of empirical landscapes remains a challenge. Additionally, none of these models make predictions about the general sign of epistasis.

## Biologically-grounded theories

More biologically informed theories make predictions about the general sign of epistasis and are more easy to connect to specific biological cases. However, some suffer from a lack of generality and they cannot be used as readily as mathematical models to investigate how epistasis influences global properties of the fitness landscape such as ruggedness.

The multiple hit hypothesis holds that epistasis depends on genome complexity and the extent of functional redundancy (Figure 1-4A) (Sanjuán and Elena 2006; Sanjuán and Nebot 2008). At one extreme are simple viral genomes encoding a small number of mostly essential, multifunctional proteins. Here, the first mutation may have a large effect, but the impact of additional mutations is smaller, since they cannot further break functions already broken by the first mutation. This is positive epistasis. In contrast, eukaryotes or organisms with larger genomes may have redundant pathways and regulatory mechanisms such as feedback inhibition, which tend to buffer the impact of single mutations but less so for multiple mutations, leading to negative epistasis.


Figure 1-4. Patterns of epistasis.
(A) Distinct epistatic patterns are predicted based on how phenotypic effects (red dashed lines) correspond to fitness effects (black solid lines). Small genomes may encode a single mechanism for a particular function, such as receptor binding in HA (left). Without a backup mechanism, initial mutations have a large impact on receptor binding and fitness. Additional mutations have little further impact, as the function has already been destroyed, resulting in positive epistasis. Other phenotypes, like protein stability, can be reduced without affecting fitness until a threshold is reached (right). Thus, each additional mutation impacts protein stability similarly but increasingly impacts fitness, resulting in negative epistasis. (B) A viral population consisting of an unmutated genotype and two variants each with a slightly deleterious mutation (red and blue
circles) on different segments (black lines). Reassortment between the two variants can combine the two deleterious mutations. If epistasis is positive (left), the reassortant will have higher fitness than expected and the deleterious mutations may persist in the population, lowering the average fitness of the population. If epistasis is negative (right), the reassortant will be quickly purged from the population, leaving the unmutated genotype and raising the average fitness of the population.

In contrast, theories of selection for robustness predict that that high mutation rates can select for distinct mechanisms that buffer the impact of single mutations and lead to negative epistasis, even in simple genomes (Figure 1-4A) (Wilke and Christoph 2001; Wilke et al. 2003; Bershtein et al. 2006; Gros et al. 2009). For example, if fitness is reduced only when an underlying phenotype reaches a threshold, then the full deleterious impact of mutations affecting that phenotype will only be revealed when enough mutations accumulate to cross the threshold, resulting in negative epistasis (Bershtein et al. 2006).

The modular life model focuses on a different feature of complex organisms, modularity (Wei and Zhang 2019). This theory posits that an organism is composed of functionally and genetically distinct modules, for example, how well it metabolizes sugar or its resistance to environmental toxins. These modules each contribute to fitness separately but their contribution has an upper limit. Negative epistasis among beneficial mutations arises: A beneficial mutation improving functionality of a particular module will increase fitness greatly if the module is far from maximum functionality, but the same beneficial mutation will be less advantageous if the module's functionality is already near the maximum. This model has not been extended to detrimental mutations.

Fisher's geometric model (FGM) focuses on yet another property of organismal complexity - that mutations are highly pleiotropic. FGM posits that phenotypes are under stabilizing selection for an optimum. The predicted distribution of epistasis for an organism at optimal fitness is
approximated by a symmetric, normal distribution with mean 0 (Martin et al. 2007). FGM originated as a model for adaptation by small steps, which has found much support (Burch and Chao 1999).

Other biologically-based theories of epistasis only apply to particular functions of an organism, such as its metabolism, or only to epistasis within genes. For example, metabolic control theory applies to pathways in which the function depends on the functionality at each sequential step. Here, positive epistasis is predicted for mutations in serial steps of a pathway, negative epistasis for mutations in related but different (somewhat redundant) pathways, and no epistasis for unrelated pathways (Kacser and Burns 1981; Segrè et al. 2005; Maclean 2010). The reasoning is similar to that of the multiple hit hypothesis, with mutations in single pathway corresponding to those in a simple organism with no redundancy and mutations in related, redundant pathways corresponding to those in a complex organism. The final major theory of epistasis focuses on intragenic epistasis and is based on the thermodynamic threshold known to be important for protein folding stability (Bloom et al. 2005; Sarkisyan et al. 2016) (Figure 1-4A). Here, single mutations may not lower stability below the required threshold and will only have small effect on protein function and fitness. However, multiple mutations will push stability below the threshold, leading to a malformed protein and thus exhibiting high fitness effects and negative epistasis.

## Emerging patterns of epistasis across phyla

The measurement of a complete fitness landscape for any organism and most genes is impossible due to their size. Furthermore, limited discriminatory power of most fitness assays and the feasibility of generating and testing large numbers of mutation pairs makes any quantitative studies of epistasis difficult. Thus, most studies have probed the fitness landscape either by
inference from evolutionary patterns or by focusing on a small number of variants or a gene of manageable size.

## Epistasis across the genome

Over the last decade, some general patterns concerning adaptive mutations have been observed across nearly all phyla, from viruses to fungi (Couce and Tenaillon 2015). In the famous longterm evolution experiment with E. coli, fitness increase generally slows with time or with the number of fixed mutations (Barrick et al. 2009) (Figure 1-2, top-left plot). In addition, high fitness backgrounds increase in fitness to a lesser degree than do lower fitness backgrounds, given the same amount of time or number of mutations (Sanjuán et al. 2005; Barrick et al. 2009; MacLean et al. 2010; Wiser et al. 2013; Perfeito et al. 2014; Wünsche et al. 2017) (Figure 1-2, top-right plot). Other experiments have put beneficial mutations on backgrounds of varying fitness and found that beneficial fitness effect negatively correlates with background fitness; this is termed diminishing returns epistasis (Bull et al. 2000; MacLean et al. 2010; Chou et al. 2011; Khan et al. 2011; Kvitek and Sherlock 2011; Rokyta et al. 2011; Pearson et al. 2012; Flynn et al. 2013; Schenk et al. 2013; Wang, Yinhua et al. 2013; Caudle et al. 2014; Chou et al. 2014: 20; Kryazhimskiy et al. 2014; Schoustra et al. 2016; Wang et al. 2016; Wünsche et al. 2017). These observations are widely interpreted as a bias towards negative epistasis (concaved fitness landscape), as combining multiple beneficial mutations is less beneficial than expected.

Nearly universal patterns concerning detrimental mutations have also emerged, but they are thought to indicate a bias towards positive, not negative, epistasis in the fitness landscape. During mutation accumulation, which fixes successive detrimental mutations by subjecting an organism to extreme drift, fitness decrease generally slows with time or number of mutations
(deVisser et al. 1997; Burch and Chao 1999; Lenski et al. 1999; Poon and Otto 2000; Crotty et al. 2001; Wilke and Christoph 2001; You and Yin 2002; Wilke et al. 2003; Bonhoeffer et al. 2004; Burch and Chao 2004; Maisnier-Patin et al. 2005; Iglesia and Elena 2007; Perfeito et al. 2014) (Figure 1-2, top-middle plot). The corollary to diminishing returns has also been found, increasing costs, in which detrimental mutations are more detrimental in higher fitness backgrounds (Johnson et al. 2019) (Figure 1-2, top-right plot). These patterns are thought to indicate a bias towards positive epistasis in the fitness landscape and a convex shape.

Thus, these nearly universal patterns seem contradictory. Theories of epistasis can find both support and refutation for their predictions as to the sign of epistasis. No theory has been able to reconcile the opposite signs of epistasis inferred from beneficial and detrimental mutations. In fact, despite a decade or more of these observations, this apparent paradox was only recognized in the literature this past year (Miller 2019).

## Epistasis within genes

In contrast to methods which track evolutionary change, DMS is more useful for identifying the interacting mutations and the strength of interaction and can infer the sign of epistasis directly. However, it is largely limited to intragenic epistasis. General findings are that epistasis is ubiquitous and is usually the strongest for pairwise interactions, although strong higher-order interactions are common as well.

Most studies attempt to explain the interactions they find from biological principles. Some mutational interactions can be explained by steric or charge interactions after close examination of protein structure (Melamed et al. 2013; Wu et al. 2017). A slight bias towards negative
epistasis seems common and can be predicted by the folding energy of the gene product (RNA or protein), supporting the thermodynamic threshold hypothesis (Bershtein et al. 2006; Araya et al. 2012; Olson et al. 2014; Li et al. 2016; Puchta et al. 2016; Sarkisyan et al. 2016; Bendixsen et al. 2017; Bendixsen et al. 2017). However, prediction is not straightforward - a novel biophysical model seems to be constructed for each new protein landscape - and how well each model explains the data is highly variable. Certainly the most common finding is that mutational effects and their interactions are very difficult to predict, or idiosyncratic (Domingo et al. 2018).

Is this unpredictability due to limited knowledge of the biophysical and chemical processes governing protein function? Or are biological interactions so numerous and complex that predicting their outcome is like predicting the outcome of die roll by tracking the collisions of all the air molecules in a room? Indeed, just as the sure knowledge that a die will come up a six one-sixth of the time, a statistical approach to epistasis can sometimes be more fruitful. One study used the statistical co-occurrence of amino acid variants in functional sequences to predict phenotypes with the same accuracy as using all experimentally-determined second-order epistasis terms (Poelwijk et al. 2019).

## Mutational Effects and Epistasis in Influenza virus

Influenza viruses infect a large number of hosts, have high mutation rates, and frequently reassort. As a result, they have a tremendous capacity to explore a large number of potential sequences. Indeed, the ability of influenza populations to adapt to new hosts and to escape the immune system seems unlimited. However, mutations are often deleterious, which presents a barrier to viral adaptation. Furthermore, epistasis determines the mutational paths available and can make some adaptations inaccessible. Understanding how mutation and epistasis present both
barriers and opportunities for influenza virus evolution is essential in predicting viral evolution and designing better vaccines and antivirals.

Influenza A has a negative-sense, single stranded RNA genome of 14 kb consisting of 8 sexually reassorting segments encoding a total of 11-12 proteins (Medina and García-Sastre 2011; Fields et al. 2013). The influenza envelope contains two interacting glycoproteins encoded by the haemagglutinin (HA) and neuraminidase (NA) segments. HA binds to sialic acids of cellular receptors, while NA facilitates the release of nascent virions by cleaving HA from bound sialic acids. Three proteins encoded by the PB2, PB1, and PA segments form the RNA-dependent RNA polymerase protein complex (RdRp). Nucleoprotein, encoded by the (NP) segment, packages the RNA and interacts with the RdRp complex. The matrix (M) segment encodes the M2 ion channel important for fusion of the virus with the cell and uncoating of RNA-NP complexes. The M1 protein, encoded by the M segment, is involved in assembly of virus particles. The non-structural segment NS encodes NS1, an antagonist of anti-viral responses, and the nuclear export protein NEP.

## Effects of Single Mutations

The distribution of mutational fitness effects (DMFE) reveals the extent of genetic constraint on the influenza virus genome, how constraints vary between and within influenza proteins, and the structural and functional impacts of mutations.

## The genome-wide DMFE in influenza virus

Site-directed mutagenesis has been used to characterize the genome-wide DMFE of singlemutations in a variety of viruses (Sanjuán 2010). Our laboratory applied this technique to an H1N1 influenza strain (Visher et al. 2016). We generated a library of 95 randomly selected point
mutations distributed across the influenza genome. We also generated 33 additional mutations in the segments encoding the hemagglutinin (HA) and neuraminidase (NA) proteins to compare the DMFE of these surface-exposed antigenic proteins ( $n=57$ ) to the internal proteins encoded by the remaining 6 segments $(\mathrm{n}=71)$.

We measured fitness relative to the wild-type in a pairwise competition assay and used repeated transfection to distinguish true lethal mutations (fitness $=0$ ) from failed viral rescue. In our dataset, $31.6 \%$ of all mutations were lethal. Approximately $40 \%$ of all viable mutations were highly detrimental ( $<0.85$ ), $50 \%$ mildly detrimental or neutral ( $0.85-1.05$ ), and only seven were beneficial (> 1.05). The fitness among all viable mutations ranged from 0.26-1.13 with a mean of 0.82. Non-synonymous mutations were more deleterious than synonymous mutations, consistent with reduced genetic constraint at the level of RNA relative to protein. Two of the three noncoding mutations were lethal, consistent with the conserved roles of these regions in RNA packaging and genome replication (Watanabe et al. 2003; Dawson et al.).

In general, the DMFE for influenza virus is similar to those documented for other viruses with a variety of genomic structures, from single-stranded RNA viruses to DNA phages (Sanjuán et al. 2004; Carrasco et al. 2007; Domingo-Calap et al. 2009; Peris et al. 2010; Sanjuán 2010; Visher et al. 2016). The lethal fraction for influenza virus falls within the $20-40 \%$ range observed for other viruses. When scaled to exponential growth rate - the fitness surrogate in many studies the average fitness effect in influenza virus is $12 \%$, squarely within the $10-13 \%$ range found in other viruses (Sanjuán 2010; Visher et al. 2016). These large effects stand in marked contrast to those seen in cellular organisms (Eyre-Walker and Keightley 2007) and may reflect shared
genetic constraints across viruses, possibly related to the small size of their genomes (Sanjuán and Elena 2006).

While genome-wide patterns in the DMFE are similar across viruses, the DMFE varies between and within individual influenza genes. The antigenic proteins, HA and NA, evolve much more rapidly than other influenza proteins. This rapid evolution could be due to a history of stronger positive selection and/or an inherently greater mutational tolerance (Plotkin and Dushoff 2003). In our comparative study, we found that the antigenic proteins were generally more tolerant of mutation. The mean fitness of mutations in the surface proteins $(0.88)$ was higher than for the internal proteins (0.78). Furthermore, the head region of HA, which is immunodominant and exhibits the greatest sequence diversity, had a higher mean fitness $(0.77)$ than the stalk region (0.56), which exhibits lower sequence diversity. Other groups have also documented the relative mutational tolerance of HA. For example, Heaton et. al. mutagenized the entire influenza genome with 15-nucleotide insertions (Heaton et al. 2013). A disproportionate number of recovered variants had insertions in the head region of HA (7/20 recovered variants). DMS studies have further confirmed the mutational tolerance of rapidly-evolving HA regions, revealing high tolerance in antigenic domains and very low tolerance in the slower-evolving HA receptor binding pocket and stalk domain (Thyagarajan and Bloom 2014; Lee et al. 2018 Apr 10). These data suggest that mutational tolerance in HA and NA, particularly in the HA head, contributes to their greater evolutionary potential. It will be interesting to compare these patterns to those in the major antigenic proteins of other viruses (Fulton et al. 2015).

In influenza virus, other protein regions with immunodominant epitopes do not always recapitulate the trends in HA. For example, the solvent-exposed region of the nonstructural protein 1 (NS1), which likely interacts with host proteins to modulate immune responses, also has greater tolerance to insertions (Heaton et al. 2013). However, immune-targeted sites in the nucleoprotein (NP) do not show unusually high mutational tolerance (Bloom 2014; Thyagarajan and Bloom 2014). Perhaps these NP regions are less tolerant because they experience lower diversifying selection from the immune system. Alternatively, these sites could be inherently more constrained. Understanding the causes and consequences of varied mutational tolerance is highly relevant to vaccine design, as the lower mutational tolerance of the HA receptor-binding pocket and stalk make them attractive targets for a universal vaccine (Erbelding et al.).

Overall, the vast majority of mutations in influenza virus are lethal or deleterious. Given the virus's high mutation rate of 2-3 per genome replicated, a large proportion of newly replicated genomes will contain a lethal mutation, and many more will harbor one or more deleterious mutations (Visher et al. 2016; Pauly, Procario, et al. 2017). Within hosts, the constraints of deleterious mutations are manifest as high levels of purifying selection and limited genetic variation (Iqbal et al. 2009; Murcia et al. 2010; Dinis et al. 2016; Debbink et al. 2017; Leonard et al. 2017; Xue et al. 2017; McCrone et al. 2018; Xue and Bloom 2018 Jul 8). Deleterious mutations also impact influenza evolution at the global scale, because purifying selection does not always efficiently purge them from the population. Deleterious mutations may reach fixation by drift (e.g. during transmission bottlenecks) or by hitchhiking with adaptive mutations. Influenza virus phylogenies show a high deleterious mutation load (Pybus et al. 2007), and
models suggest that this load can slow antigenic evolution (Koelle and Rasmussen 2015; Raghwani et al. 2017).

## Deep mutational scanning of influenza proteins

While site-directed mutagenesis has provided an overview of the genome-wide DMFE, DMS can interrogate nearly all amino acid substitutions in a single protein. In DMS studies, fitness is usually calculated as the change in frequency of a mutation in a pool of variants before and after passage or selection, relative to wild-type. This method is analogous to pairwise competition assays, and fitness measurements across studies are well correlated (Visher et al. 2016; Lyons and Lauring 2017). DMS studies by Bloom and colleagues include saturation mutagenesis of the HA and NP proteins from H1N1 and H3N2 strains (Bloom 2014; Thyagarajan and Bloom 2014; Doud et al. 2015; Doud and Bloom 2016; Lee et al. 2018 Apr 10). Studies by Sun and colleagues investigated many substitutions in nearly all sites in the six other influenza proteins (Wu et al. 2013; Wu, Young, Al-Mawsawi, Olson, Feng, Qi, Luan, et al. 2014; Wu, Young, Al-Mawsawi, Olson, Feng, Qi, Chen, et al. 2014; Wu et al. 2015; Du et al. 2016; Wu et al. 2016; Du et al. 2018). We are now close to a complete map of the fitness effects of all possible amino acid substitutions for an entire influenza virus genome.

Both sets of DMS studies clearly show that mutational tolerance varies widely across sites within a protein; some sites strongly prefer a single amino acid and others accept many different amino acids. The effect of any particular amino acid substitution is also highly site-specific. Wu et. al. investigated the link between protein stability and mutational effects in PA to shed light on why constraints may vary across sites (Wu et al. 2015). They found two categories of amino acid residues; those in which substitutions affected overall protein stability and those in which
substitutions were detrimental but did not affect stability. The latter were termed "functional" residues as they likely affected enzymatic functions of a protein (e.g. polymerase activity) or important protein-protein interactions (e.g. solvent-exposed sites).

More recent studies have used DMS in innovative ways. DMS-informed site-specific and parameter-free evolutionary models dramatically improve the fit of phylogenies (Bloom 2014; Doud et al. 2015; Hilton and Bloom 2018 Apr 17) and the inference of sites under positive selection (Bloom 2017; Hilton et al. 2017). Another promising avenue is the application of DMS to phenotypes other than fitness (Wu et al. 2013; Wu, Young, Al-Mawsawi, Olson, Feng, Qi, Luan, et al. 2014). Du et al. used DMS to identify mutations that increase IFN sensitivity while preserving replicative fitness and immunogenicity, leading to a potentially safe and effective vaccine strain (Du et al. 2018). Bloom and colleagues have used DMS to study the potential mutational pathways of antibody escape in HA and avian to human host-adaptation in PB2 (Doud et al. 2017; Doud et al. 2018; Soh et al. 2019).

There is now extensive data on the effects of single mutations in influenza virus. The vast majority of mutations are deleterious, with similar effects as in other viruses. Greater mutational tolerance in some antigenic sites may enable their rapid evolution whereas lower mutational tolerance makes other sites promising vaccine targets. The challenge now is to better understand the biological basis of mutational effects. Mutational fitness effects in the laboratory correlate with mutational frequency in nature (Visher et al. 2016; Lee et al. 2018); thus, these data could be used to improve predictive models of influenza evolution (Łuksza and Lässig 2014; Morris et al. 2017; Lee et al. 2018).

## Epistasis in influenza viruses

Studies have employed site-directed mutagenesis to study interactions among small numbers of mutations, usually those implicated in adaptation to immune pressure or antiviral drugs (Bloom et al. 2010; Gong et al. 2013; Pauly, Lyons, et al. 2017). DMS been used for studying a small region in HA. DMS has also been used to compare mutational effects across different NP and HA genetic backgrounds (Bloom 2014; Lee et al. 2018 Apr 10). Shifts in mutational effects at a given site across different genetic backgrounds reflect epistatic interactions involving that site. However, comparative DMS studies can only detect epistatic interactions involving at least one divergent site and cannot precisely identify the interacting mutations.

Phylogenetic inference can be used to identify epistatic interactions in the virus's natural replication environment. One approach is to identify co-evolving sites (Shapiro et al. 2006; Akand and Downard 2018). If substitutions at one site are followed by second site substitutions more quickly than expected by chance, these substitutions likely enhance each other's beneficial effects (Figure 1-3B) (Kryazhimskiy et al. 2011). This approach can only detect positive epistasis and has limited power for rarer polymorphisms and weaker epistatic interactions. Furthermore, it has typically been applied to studies of within-gene epistasis, given the added complexity of reassortment and the computational costs of genome-wide scans (but see (Neverov et al. 2015)). Phylogenetic inference of between-gene epistasis in influenza relies on observed patterns of reassortment. Here, non-random patterns of reassortment among genome segments suggest incompatible interactions (Rambaut et al. 2008). These incompatibilities can also be detected as accelerated rates of evolution in reassortant lineages, as the newly combined
segments adapt to their new genetic environment (Neverov et al. 2014). While these studies identify gene-level epistasis, they typically do not identify the interacting sites.

## General epistatic patterns in influenza viruses

Recent studies have elucidated patterns of within-gene epistasis. Comparative DMS of NP and HA in H3N2 and H1N1 backgrounds have found that both short-range physical interactions and long-range functional interactions within these proteins are common (Doud et al. 2015; Lee et al. 2018 Apr 10). Phylogenetic studies also find many long-range epistatic interactions (Shapiro et al. 2006; Nshogozabahizi et al. 2017). Additionally, sites exhibiting epistasis cluster with each other, which can be explained by structural changes affecting a particular region of the protein (Doud et al. 2015; Lee et al. 2018 Apr 10). Less is known about the type and magnitude of epistasis. A DMS study of 11 sites in the receptor binding region of HA found positive epistasis to be ubiquitous (Wu et al. 2017). This is in contrast to studies in other taxa showing that a folding stability threshold generally leads to negative epistasis across entire proteins (Figure 14A) (Bershtein et al. 2006; Lehner 2011; Li et al. 2016; Puchta et al. 2016; Sarkisyan et al. 2016).

The theoretical costs and benefits of reassortment largely depend on the type and magnitude of epistasis between mutations on different segments. Reassortment is advantageous in the setting of negative epistasis because combining deleterious mutations through reassortment will accelerate the rate at which they are purged from a population (Figure 1-3B) (Chao 1988; Kondrashov 1988; Kouyos et al. 2007). Conversely, positive epistasis slows the rate at which deleterious mutations are purged, making reassortment disadvantageous. Reassortment also underlies the process of antigenic shift and the associated spread of avian and swine viruses to
humans (Morens et al. 2009; Campbell et al. 2014; Danzy et al. 2014). However, segments do not reassort freely (Rambaut et al. 2008; Zeldovich et al. 2015), and differential pairwise epistasis among segments reflects their genetic incompatibilities. Here, epistasis imposes a fitness cost to reassortment, even between strains of the same subtype, and could limit host-range expansion (Ward et al. 2013; Neverov et al. 2014; Villa and Lässig 2017).

## Epistasis in the adaptive evolution of influenza virus

Most studies of epistasis in influenza virus have focused on its role in antigenic evolution. HA evolution is characterized by a series of mutations with little apparent change in antigenicity, forming an antigenic cluster, followed by a mutation that leads to significant antigenic drift, called a cluster transition. Models show that epistatic interactions among individually neutral mutations can explain this pattern of evolution (Koelle et al. 2006; Taggi et al. 2013; Tria et al. 2013). The epistatic interactions in these antigenic clusters can lead to historical contingency. Mutations involved in a cluster transition also interact with mutations involved in the subsequent cluster transition, forming chains of interacting mutations (Nshogozabahizi et al. 2017). These chains suggest that the fixation of each substitution is contingent on the fixation of prior substitutions.

Studies employing site-directed mutagenesis and experimental evolution demonstrate how epistasis in HA leads to this historical contingency. First, the impact of a given mutation on antigenicity or receptor binding varies with genetic background (Nakajima et al. 2005; Das et al. 2013). This context dependence makes it harder to predict HA evolution and generalize molecular findings between strains. Second, mutations that mediate antigenic escape often have pleiotropic effects, and their success is contingent upon mutations that restore fitness. Antigenic

escape variants in HA can decrease protein folding
stability or alter sialic acid binding (Underwood et
al. 1987; Mitnaul et al. 2000; Das et al. 2011;
Myers et al. 2013; Wu et al. 2017; Kosik et al. 2018), and fitness can be restored by mutations in HA or NA with opposing effects (Mitnaul et al.

Figure 1-5. Epistasis can constrain adaptation.

The ancestral identity of loci (1) and (2) are shown as unfilled red and blue shapes. A mutation at locus 2 mediates immune escape (filled circle) but is detrimental if it occurs on the ancestral background. Thus, a compensatory mutation at locus 1 (filled square) is required before the escape mutation, limiting the accessibility of the higher fitness genotype (filled square and filled circle). The compensatory mutation also becomes entrenched. Once the antigenic mutation arises, reversion of the compensatory mutation to its ancestral state (unfilled square) would cause a fitness decrease, even though it was initially neutral. Such interactions can occur within or between genes and involve more than two loci.

2011; Myers et al. 2013; Wu et al. 2017; Kosik et al. 2018). In many cases, the deleterious side effects of an antigenic mutation are larger than its beneficial effects. This constrains adaptation, as the novel, but deleterious, antigenic mutation can only be selected if a compensatory mutation arises first (Figure 1-5) (Weinreich et al. 2005). Since many compensatory mutations are neutral, this often requires that the initial compensatory mutation arise by random drift, hitchhiking, or simultaneously with the novel antigenic mutation.

The adaptive evolution of HA is also constrained by entrenchment, whereby a substitution can no longer revert to its ancestral state without compromising fitness (Figure 1-5). For example, Wu et al. found that a substitution in the receptor binding site of H3, E190D, was reversible to the ancestral state within 10 years after the substitution arose, but not in more recent strains (Wu et al. 2018). Apparently, more recent mutations in the receptor binding site have altered its
structure such that E190 is no longer tolerated. Interestingly, all of the epistatically interacting mutations were located in antigenic sites and could explain why mutations that lead to antigenic changes in HA rarely revert.

Epistasis also influences the adaptive evolution of NA. Neuraminidase phylogenies reveal chains of interacting substitutions similar to those in HA cluster transitions, and resistance to oseltamivir and other neuraminidase inhibitors is constrained by epistasis. Resistance mutations reduce fitness by altering NA stability or enzymatic activity and are contingent on compensatory mutations in HA or NA (Bloom et al. 2010; Abed et al. 2011; Hensley et al. 2011; Ginting et al. 2012; Duan et al. 2014; Neverov et al. 2015). While oseltamivir was first introduced in 1999, the H274Y resistance mutation only arose 8 years later in a much different genetic background (Bloom et al. 2010; Abed et al. 2011; Duan et al. 2014). It then swept the population in a single year. This single epistatic interaction demonstrates how the starting genotype of a strain can have profound effects on whether it can adapt to a new selective pressure.

There are fewer examples of epistasis in other influenza proteins. Contingency has been identified in M2 and NP phylogenies and immune escape mutations in NP (Gong et al. 2013; Nshogozabahizi et al. 2017). We have found that mutations in PA and PB1 interact epistatically to mediate high-level resistance to mutagenic drugs in vitro (Pauly, Lyons, et al. 2017). Epistatic interactions in M2 may also mediate increased resistance to amantadine and/or increase virulence in amantadine-resistant strains (Abed et al. 2005; Dong et al. 2015; Durrant et al. 2015). For example, two mutations associated with amantadine resistance co-occur more frequently than predicted by chance (Durrant et al. 2015); the double mutant has become more prevalent in
recent years (Durrant et al. 2015) and has higher virulence in mice than either single mutant (Abed et al. 2005). Finally, recent work suggests that selection on non-antigenic phenotypes encoded by the remaining six segments can have profound effects on antigenic evolution of influenza virus (Koelle and Rasmussen 2015; Raghwani et al. 2017). Thus, defining epistasis across the genome is an important area for future study.

In contrast to single mutational effects, models and theoretical work on epistasis have outpaced empirical data in influenza virus. A handful of examples in several influenza genes demonstrate that epistasis is common and can lead to evolutionary flexibility via compensation, while at the same time constraining evolution through entrenchment and contingency. However, the general distribution of epistatic effects, including the sign and magnitude of epistasis, across the influenza genome is unknown. The general patterns of epistasis determine the likelihood of compensatory mutation and accessibility of adaptations, the consequences of reassortment, and thus the evolutionary fate of influenza populations. Novel methods are needed to investigate epistasis more extensively across the entire influenza virus genome.

## From idiosyncrasy to general patterns in fitness landscapes

There are several puzzles in our picture of how mutational effects scale across levels of biology (Figure 1-2). How does the deterministic action of individual mutations lead to their highly variable effects in different genetic backgrounds at the level of complex phenotypes like fitness? The transition to the level of evolution presents a further problem. How can unpredictable and idiosyncratic individual effects give rise to the predictable and universal patterns in the collective effects of mutations and evolutionary trajectories? The universal patterns are themselves puzzling. According to common intuition, patterns involving beneficial versus detrimental
mutations suggest contradictory biases in epistasis. Current theories of epistasis do not resolve this contradiction and ignore the idiosyncrasy of mutational effects.

My next chapter resolves these puzzles, showing how the universal patterns can arise out of the idiosyncrasy, or near randomness, of mutational effects, without epistatic bias. Furthermore, it presents a null theory of epistasis that explains why deterministic mutational effects are idiosyncratic at higher phenotypic levels. The subsequent two chapters cut through the thicket of idiosyncrasy to find generalizations about mutational effects in RNA viruses. These generalizations help answer long-standing questions in molecular evolution and have implications for phylogenetic inferences and the evolution of the genetic code.

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# Chapter 2 Idiosyncratic Epistasis Creates Universals in Mutational Effects and Evolutionary Trajectories 

Note: This chapter is a modified version of the article under review:
Daniel M. Lyons*, Zhengting Zou*, Haiqing Xu, and Jianzhi Zhang. Idiosyncratic epistasis creates universals in mutational effects and evolutionary trajectories. Under review at Nature Ecology and Evolution.


#### Abstract

Patterns of epistasis and shapes of fitness landscapes are of wide interest because of their bearings on a number of evolutionary theories. The common phenomena of slowing fitness increases during adaptations and diminishing returns from beneficial mutations are believed to reflect a concave fitness landscape and a preponderance of negative epistasis. Paradoxically, fitness drops tend to decelerate and harm from deleterious mutations shrinks during accumulation of random mutations, patterns thought to indicate a convex fitness landscape and a predominance of positive epistasis. Current theories cannot resolve this apparent contradiction. Here we show that the phenotypic effect of a mutation varies substantially depending on the specific genetic background and that this idiosyncrasy in epistasis creates all of the above trends without requiring a biased distribution of epistasis. The idiosyncratic epistasis theory explains the universalities in mutational effects and evolutionary trajectories as emerging from randomness due to biological complexity.


## Introduction

Epistasis, or genetic interaction among a set of mutations, impacts the phenotypic effects of mutations and shapes fundamental evolutionary processes ${ }^{1}$. Epistasis is said to be positive (or
negative) for a particular trait such as fitness if the trait value of the individual with multiple mutations is greater (or smaller) than the expectation from the corresponding single mutants under no epistasis ${ }^{1}$. A number of evolutionary theories such as the mutational deterministic hypothesis of the evolution of sexual reproduction ${ }^{2}$ and the hypothesis of reduction in mutational load by truncation selection against deleterious mutations depend on assumptions of general trends of epistasis ${ }^{3}$. Universal patterns involving epistasis are emerging from decades of intense investigations ${ }^{4,5}$. For instance, many experimental evolution studies have shown that fitness increase slows during the organismal adaptation to a constant environment ${ }^{6}$. While the speed of fitness increase is typically measured per unit time ${ }^{6}$, the same trend is observed when the speed is measured per mutation accrued ${ }^{7}$. This phenomenon of slowing adaptation is at least in part due to diminishing returns epistasis, a common observation that advantageous mutations are less beneficial on fitter genetic backgrounds ${ }^{8-11}$. Because diminishing returns epistasis is a form of negative epistasis, the above observations are thought to indicate a preponderance of negative epistasis between beneficial mutations and a concave fitness landscape ${ }^{12}$. If the process of adaptation is reversed by reverting the accepted beneficial mutations, one should see accelerating fitness drops and negative epistasis between deleterious mutations. Contrary to this expectation, mutation accumulation experiments in the near absence of selection have revealed decelerating fitness declines ${ }^{13-15}$ and manipulative experiments have demonstrated that deleterious mutations tend to be less harmful in less fit genetic backgrounds (a.k.a. increasing costs epistasis because of the higher costs of deleterious mutations in fitter genotypes) ${ }^{16}$. These observations concerning deleterious mutations are thought to indicate a convex fitness landscape and a predominance of positive epistasis ${ }^{12,13}$.

Apparently, the inferred shape of the fitness landscape and distribution of epistasis from climbing fitness peaks contrast the shape and distribution inferred from going down fitness peaks ${ }^{12}$. We term this contradiction the uphill-downhill paradox. Although several theoretical models have been proposed to explain the inferred prevalence of either negative or positive epistasis ${ }^{9,10,13,16-20}$, these models cannot simultaneously explain both in the same species, leaving the uphill-downhill paradox unresolved. For instance, some authors have suggested that the negative epistasis among beneficial mutations accumulated during adaptations are not representative of the entire fitness landscape, due to the biased sampling of mutations ${ }^{21,22}$. But this explanation does not apply to mutations randomly accrued in mutation accumulation experiments so cannot fully resolve the uphill-downhill paradox. Below we propose and demonstrate that epistasis is generally idiosyncratic and that this idiosyncrasy is responsible for the general trends in both climbing and descending from fitness peaks.

## Results

## Why epistasis could be highly idiosyncratic

Let $g$ be the population growth rate (a.k.a. Malthusian fitness, logarithm of Wrightian fitness, or fitness for short) of a genotype in an environment and let $n$ be the number of nucleotide sites in the genome that impact $g$. In general, $g$ can be expressed as the sum of $2^{n}-1$ terms of fitness effects, including the additive effect of every site, the interactive effect of every pair of sites, the interactive effect of every triplet of sites, and so on (see Methods). We refer to this model of fitness landscape as the $n$-order model, because it includes all terms up to the $n$-order interaction. It can be shown that a mutation at a single site changes up to $2^{n-1} /\left(2^{n}-1\right) \approx 50 \%$ of all terms of effects making up $g$. Under the assumption that the interactive terms are idiosyncratic (i.e., varying with the interacting nucleotides involved), a single mutation can differentially alter as
many as $2^{n-2}$ (or $\sim 25 \%$ of) terms of effects in two genotypes that differ by only one nucleotide; this number can rise up to $2^{n-1}$ (or $\sim 50 \%$ of) terms if the two genotypes are more different (see Methods). Given the potential of such a large fraction of differentially affected terms of $g$, it is not surprising that the same mutation could have vastly different effects in different genotypes. As long as the idiosyncrasy assumption holds, the same argument can be made for any phenotypic trait whose value is expressed as the sum of all additive and interactive terms of effects. Of course, not all $2^{n}-1$ terms of effects are of the same magnitude, which would increase or decrease the effective fraction of terms differentially altered by a mutation. Regardless, the above consideration elucidates why mutational effects could be highly sensitive to the genetic background when biological interactions are complex.


Figure 2-1 Idiosyncratic index of a wide variety of phenotype landscapes.
(A) Frequency distribution of the fitness effects of the mutation from G to A at position 10 across all available genetic backgrounds (purple) and the corresponding distribution of the fitness difference between two random genotypes for the same number of genotype pairs (grey) in the yeast tRNA fitness landscape. (B) Frequency distribution of the standard deviation (SD)based idiosyncrasy index (Iid), which is the ratio of the SD of fitness effects of a particular mutation on different backgrounds to the SD of fitness differences between random genotype pairs, for all individual mutations in the yeast tRNA landscape. (C) SDbased Iid of various phenotype landscapes. Error bars show standard errors. Detailed information of each landscape is provided in Table S1. (D) Schematic of a highly idiosyncratic fitness landscape. Genotypes are represented by circles, and the fitness of a genotype is represented by the circle size. The three black circles labeled with H, I, L respectively indicate three focal genotypes with relatively high, intermediate, and low fitness values, whereas the grey circles represent one-mutation neighbors of the focal genotypes. Each light-green outlined area encompasses a focal genotype and some one-mutation neighbors. Solid arrows indicate single mutations, whereas dotted arrows indicate multiple mutations. Solid arrows of the same color indicate the same mutation.

## Epistasis is highly idiosyncratic

To quantify the above sensitivity that originates from idiosyncratic epistasis, we define an idiosyncratic index $\left(I_{\mathrm{id}}\right)$ for a mutation as the variation in the fitness difference between genotypes that differ by the mutation, relative to the variation in the fitness difference between random genotypes for the same number of genotype pairs. Here, the variation may be measured by standard deviation (SD), range, or other statistics. We can further compute the $I_{\mathrm{id}}$ for a fitness landscape by averaging $I_{\mathrm{id}}$ of individual mutations considered. The $I_{\mathrm{id}}$ for a landscape varies from 0 to 1 , corresponding to the minimal and maximal levels of idiosyncrasy, respectively. We first estimated $I_{\mathrm{id}}$ for the fitness landscape of a yeast tRNA gene that includes experimentally measured fitness of over 65,000 genotypes ${ }^{23}$. For example, the G-to-A mutation at site 10 has a fitness effect varying from -0.53 to $0.29(\mathrm{SD}=0.13)$ on 88 different backgrounds. For comparison, the fitness difference between a randomly picked genotype and another randomly picked genotype varies from -0.59 to $0.74(\mathrm{SD}=0.26)$ for 88 genotype pairs sampled (Fig. 21A). So, the ratio of the two SDs is 0.49 . This analysis was repeated for 828 single mutations (considering reverse mutations) (Fig. 2-1B), and the average ratio of SD is $I_{\mathrm{id}}=0.612 \pm 0.005$ (SE). $I_{\mathrm{id}}$ can be similarly defined for non-fitness traits, and we estimated $I_{\mathrm{id}}$ for a variety of empirical phenotype landscapes that are experimentally determined ${ }^{23-31}$ and one that is computationally predicted (RNA-folding) (Table 2-S1). Overall, $I_{\text {id }}$ varies from 0.18 to 0.80
among the 12 landscapes examined, with a mean of 0.43 (Fig. 2-1C). Hence, in an average phenotype landscape, a particular mutation's effects across different backgrounds are $43 \%$ as variable as if they are randomly drawn from the effects of any number of mutations on any genetic background. To exclude the possibility that the observed idiosyncrasy is largely due to imprecise phenotyping, we computed $I_{\text {id }}$ for the same 828 mutations in the tRNA landscape, but used fitness estimates from different numbers of experimental replicates, because the measurement error should decrease with the number of replicates. We found that $I_{\mathrm{id}}$ is insensitive to the number of replicates (Fig. 2-S1A), suggesting that the high idiosyncrasy is not explained by potentially imprecise phenotyping. Additionally, phenotypic values in the RNAfolding landscape were computed deterministically without measurement error, but mutationaleffects are still a quarter as idiosyncratic as the maximum $\left(I_{\mathrm{id}}=0.25\right)$. We similarly observed high idiosyncrasy when range instead of SD of effects was used in estimating $I_{\text {id }}$ (Fig. 2-S1B).

## Expected consequences of idiosyncratic epistasis

The substantial idiosyncrasy observed suggests that phenotype landscapes are quite rugged (Fig. 2-1D). Below we demonstrate its consequences with regard to fitness, but the same applies to other traits. In a maximally idiosyncratic fitness landscape such as the one described by the house-of-cards model ${ }^{32}$, fitness values (circle sizes in Fig. 2-1D) of neighboring genotypes connected through single mutations are uncorrelated. The fitness of a neighboring genotype of a high- or a low-fitness focal genotype is expected to be the same. Hence, the fitness difference between a neighboring genotype (grey circle) and the focal genotype (black circle) is expected to be less positive or more negative as the fitness of the focal genotype rises. In other words, beneficial mutations are less beneficial and deleterious mutations are more deleterious on fitter genotypes, causing diminishing returns and increasing costs, respectively. These arguments
apply not only to the effects of the same mutation on different genetic backgrounds but also to the effects of different mutations on different backgrounds. That is, an arbitrary mutation on a relatively fit background is expected to be less beneficial or more detrimental than another arbitrary mutation on a relatively unfit background. Under the foregoing model of $g$, one can mathematically prove that, in the presence of idiosyncrasy of at least one interactive term, the correlation between the fitness effect of a mutation and the background fitness is negative, for both the same and different mutation(s) (see Methods). In the case of different mutations, among-site/state variation in the additive effect further contributes to the negative correlation (see Methods). Importantly, all of the above occurs even with no bias toward positive or negative epistasis in the fitness landscape and no fitness estimation error.

## Idiosyncratic epistasis causes the trends of diminishing returns and increasing costs

To examine whether the extent of idiosyncratic epistasis in an actual fitness landscape is sufficient to explain the observed diminishing returns and increasing costs, we simulated a series of 16 fitness landscapes with $n=16$ binary sites, under the $n$-order model of $g$. In the $k$ th landscape in the series $(1 \leq k \leq 16)$, we considered up to the $k$ th order of interaction. That is, each term of effect from the first to the $k$ th order interaction is a random variable independently drawn from the standard normal distribution whereas all other terms are set to 0 . When $k$ rises from 1 to $16, I_{\text {id }}$ increases from 0 to $0.69(\mathbf{F i g} .2-2 A)$, which is close to the theoretically predicted value (see Methods). In all simulated landscapes except the one with $I_{\mathrm{id}}=0$, most if not all mutations exhibit a negative Pearson's correlation between fitness effect and background fitness (boxes in Fig. 2-2A). In addition, the larger the $k$ and $I_{\mathrm{id}}$, the more negative the correlations (boxes in Fig. 2-2A), supporting the role of idiosyncratic epistasis in creating the negative correlations. For comparison, $87.8 \%$ of mutations from the yeast tRNA fitness landscape show a
negative correlation between fitness effect and background fitness (Fig. 2-2B). A similar trend is seen in other empirical phenotype landscapes (Fig. 2-S2A, B). Separating mutations that are beneficial or detrimental on the wild-type background or an arbitrary background reveals the familiar patterns of diminishing returns and increasing costs in both the simulated and empirical landscapes (Fig. 2-S3).


Figure 2-2 Negative correlation between mutational effect and background fitness as a result of idiosyncratic epistasis.
(A) Boxplot showing the distribution of Pearson's correlation coefficient (r) between mutational effect and background fitness for individual mutations in a series of n -order landscapes. The lower and upper edges of a box represent the first (qu1) and third
(qu3) quartiles, respectively, the horizontal line inside the box indicates the median (md), the whiskers extend to the most extreme values inside inner fences, $\mathrm{md} \pm 1.5$ (qu3 - qu1), and the grey dots represent values outside the inner fences (outliers). Green diamonds represent $r$ values for all mutations pooled in each landscape, while red circles indicate SD-based Iid of the landscapes. (B) Distribution of r for 828 individual mutations in the tRNA fitness landscape. (C) Relationship between background fitness and mutational effect for 414 mutations (reversions not considered) in the tRNA fitness landscape. The red line depicts the running mean in non-overlapping X -axis bins of width $=0.02$, in all bins with more than 10 data points. To avoid a spurious correlation due to shared measurement error on the X - and Y -axis, we used three replicates of background fitness measures for the X -axis and three other replicates for the Y -axis in (B) and (C). For each mutation and its reversion, a randomly picked one is considered in (C).

Furthermore, the effects of different mutations also negatively correlate with background fitness in the simulated landscapes (green diamonds in Fig. 2-2A; see Methods), as well as in the tRNA fitness landscape (Fig. 2-2C) and other empirical phenotype landscapes (Fig. 2-S2C, D). As mentioned, the negative correlation in the simulated landscape with $I_{\mathrm{id}}=0$ (green diamond in Fig. 2-2A) is due to the contribution from the among-site/state variation in additive effect; in the absence of this variation, all genotypes are equally fit, so the correlation disappears.

## Idiosyncratic epistasis causes slowing fitness drops in mutation accumulation

When random mutations accrue in a relatively fit population in the near absence of selection, population fitness is expected to decline. Because idiosyncratic epistasis renders random mutations on average less deleterious on relatively unfit genotypes than on relatively fit genotypes, the fitness drop of the population is expected to decelerate during mutation accumulation until it reaches the mean fitness of all genotypes in the landscape, around which the fitness should subsequently fluctuate. We confirmed this prediction in the simulated $n$-order landscapes: As $k$ and $I_{\text {id }}$ increase, the slowing curvature becomes more prominent (Fig. 2-3A). A change in mutational supply explains why the fitness decline is decelerating even when $I_{\mathrm{id}}=0$ (see Methods), and as expected, this trend diminishes as $n$ rises (Fig. 2-S4). For comparison, decelerating fitness declines are apparent during simulated mutation accumulations in the tRNA fitness landscape (Fig. 2-3B) and other empirical phenotype landscapes (Fig. 2-S5).


Figure 2-3 Fitness declines decelerate during mutation accumulation as a result of idiosyncratic epistasis.
(A) Average fitness trajectories simulated in a series of n-order landscapes. (B) Ten thousand fitness trajectories of mutation accumulation simulated in the tRNA fitness landscape, with the average fitness of all trajectories at each step shown in black. Dotted lines indicate the mean fitness of all genotypes in the corresponding landscape.

The drop in fitness to the mean of all genotypes during mutation accumulation is observed in the $n$-order landscapes (Fig. 2-3A) and RNA-folding landscape (Fig. 2- S5B), while the average mutation accumulation trajectory in tRNA (Fig. 2-3B) and GFP (Fig. 2-S5A) landscapes fluctuates above the mean of all genotypes. This latter phenomenon is due to preferential sampling of genotypes close to the wild-type in the experimental data, "trapping" many simulated mutation accumulation trajectories around the wild-type. The former two theoretically simulated/calculated landscapes do not have such biases.

## Idiosyncratic epistasis causes slowing fitness gains in adaptation

Idiosyncratic epistasis, in combination with certain distributions of genotype fitness or interactive effects, creates the phenomenon of decelerating fitness gains during adaptation. In a solely additive landscape with $I_{\mathrm{id}}=0$, each adaptive trajectory is basically a random ordering of the beneficial mutations. Thus, the mean fitness increase of every step is the mean of the effect
of all beneficial mutations, leading to a linear average trajectory regardless of the fitness distribution (Fig. 2-4A). In an idiosyncratic landscape with $I_{\mathrm{id}}>0$, the mutation fixed at each step during adaptation is a random draw from beneficial mutations instead of all mutations. Because of this bias, the shape of the adaptive trajectory, unlike that of mutation accumulation, is dependent on the distribution of genotype fitness or interactive effects. For example, in a house-of-cards model (a special case of $n$-order landscapes with only the highest-order interaction term), when fitness of all genotypes is gamma distributed with shape parameter $>1,=1$, or $<1$ (Fig. 2-S6A), fitness rises sublinearly, linearly, and superlinearly with the number of mutations accumulated, respectively (Fig. 2-S6B) (see also ${ }^{33}$ ). Although not sufficient for creating a decelerating adaptive trajectory, idiosyncrasy causes a decelerating trajectory in a wide range of full $n$-order landscapes, including, for example, those with normal- (Fig. 2-4A), gamma-, and beta-distributed interaction effects (Fig. 2-S6C, D). As expected, adaptation slows more dramatically with greater $I_{\text {id }}$ (Fig. 2-4A; Fig. 2-S6C, D). Simulated adaptation also decelerates in the tRNA fitness landscape (Fig. 2-4B) as well as in other empirical phenotype landscapes (Fig. 2-S7), suggesting that the empirical cases fulfill both the idiosyncrasy and fitness distribution requirements.


Figure 2-4 Adaptation slows as a result of idiosyncratic epistasis.
(A) Average adaptive trajectories simulated in a series of $n$-order landscapes. (B) A total of 15,878 adaptive trajectories simulated in the tRNA fitness landscape, with the average fitness of all trajectories shown in black, at each step when the trajectory number exceeds 10 .

## Discussion

In summary, we proposed a simple theory that uses the idiosyncrasy of epistasis to explain some of the most commonly observed patterns of mutational effects and evolutionary trajectories. Phenotype landscapes of a variety of genes and taxa confirm our assumption of idiosyncratic epistasis. Contrary to the common intuition, our work shows that diminishing returns and decelerating adaptations do not suggest a bias toward negative epistasis in the underlying fitness landscape or a concave landscape. Similarly, increasing costs and slowing fitness declines during mutation accumulation do not indicate a bias toward positive epistasis or a convex landscape. Thus, our theory resolves the uphill-downhill paradox.

Although the idiosyncrasy of epistasis is a major characteristic of empirical phenotype landscapes (Fig. 2-1C), biological interactions are not completely idiosyncratic. Rather, idiosyncratic epistasis should serve as a null model for the role of epistasis in mutational effects and evolution. For example, the relationship between the mutational robustness of a genotype (i.e., fitness insensitivity to mutation) and its adaptability/evolvability to environmental challenges is debated ${ }^{34-36}$. Our theory reveals an intrinsic positive correlation between robustness and adaptability due to idiosyncratic epistasis, because, as the fitness of a genotype rises, deleterious mutations are more detrimental (i.e., lower robustness) and advantageous mutations are less beneficial (i.e., lower adaptability). Deviations from this null expectation may reveal interesting forms of epistasis beyond idiosyncrasy. Similarly, because slowing fitness drops during mutation accumulation naturally emerge from idiosyncratic epistasis, such
observations need not be explained by selection for "genomic buffering against the fitness reduction caused by accumulated mutations ${ }^{\prime 13}$. Rather, when this trend is absent or when the opposite trend is observed, selection for mutational robustness of the wild-type may be invoked ${ }^{37}$. Additionally, other processes such as clonal interference ${ }^{38}$ and changes in mutational supply ${ }^{39}$ may enhance some of the universals caused by idiosyncratic epistasis.

How does the idiosyncrasy of epistasis arise from the underlying deterministic biological interactions? The $n$-order model reveals that the number of interactive terms determining the phenotype of a genotype is potentially astronomical and that the same mutation differentially alters a substantial fraction of these terms in even slightly different genotypes. Consequently, it is difficult to predict the mutational effect in any particular genotype despite the underlying deterministic biological interactions, much like the apparently random outcome of a die roll that is deterministically shaped by myriad factors such as the movement of air molecules. That the universal trends of mutational effects and evolutionary trajectories emerge from this randomness due to idiosyncratic epistasis is no more surprising than the tendency of observing a smaller number in a second roll of a die when the first roll yields a five.

## Methods

## Number of terms of phenotypic effects altered by a mutation

Let $g$ be the Malthusian fitness (fitness for short) of a genotype in an environment and let $n$ be the number of nucleotide sites in a genome that are relevant to $g$. Here $g$ equals the sum of the additive fitness effect of every site (i.e., first order interaction), the interactive effect of every pair of sites (i.e., second order interaction), the interactive effect of every triplet of sites (i.e., third order interaction), and so on. That is, $g$ contains $\binom{n}{k}$ terms of effects of the $k^{\text {th }}$ order of
interaction $(1 \leq k \leq n)$, for a total of $2^{n}-1$ terms. Among these terms, $2^{n-1}$ terms involve any particular site. Thus, a mutation at a single site potentially changes $2^{n-1} /\left(2^{n}-1\right) \approx 50 \%$ of all terms making up $g$.

## Differentially altered terms of effects in two genotypes caused by the same mutation

When the same mutation of allele $P$ changing to $Q$ at site $i$ occurs on two different genotypes that differ at $m$ sites ( $i$ is not one of the $m$ sites), the differentially altered terms of effects in these genotypes must involve site $i$ and at least one of the $m$ sites, and may also involve site(s) identical between the two genotypes. The total number of differentially altered terms equals the number of terms involving $i$ and at least one other site minus the number of terms involving $i$ and at least one other site that is identical between the two genotypes. The resulting number is ( $2^{n-1}$ $-1)-\left(2^{n-m-1}-1\right)=\left(2^{m}-1\right) 2^{n-m-1}$. When $m=1$, the above number is $2^{n-2}$. That is, up to $2^{n-}$ ${ }^{2} /\left(2^{n}-1\right) \approx 25 \%$ of terms are differentially altered by the same mutation in two genotypes that differ at only one site. When $m=n-1$, the above number is $2^{n-1}-1$. That is, up to $\left(2^{n-1}-1\right) /\left(2^{n}-1\right)$ $\approx 50 \%$ of terms are differentially altered by the same mutation in two maximally different genotypes.

## The fitness effect of a given mutation is negatively correlated with background fitness

Let us consider the $n$-order landscape model and focus on the mutation from the $P$ allele to the $Q$ allele at site $k$ of the genome. We examine the fitness effect of this mutation on different genetic backgrounds. Let $X$ represent any genotype with the $P$ allele at site $k$. Among them, $x_{i}$ is the $i^{\text {th }}$ genotype whose Malthusian fitness is $R_{x_{i}} . R_{x_{i}}$ can be written as $R_{x_{i}}=A_{x_{i}}+I_{x_{i}}+I_{x_{i}}^{\prime}$, where $A_{x_{i}}$ is the sum of additive (i.e., $1^{\text {st }}$ order interactive) effects, $I_{x_{i}}$ is the sum of the $2^{\text {nd }}$ to $n^{\text {th }}$ order interactive effects involving the focal site $k$, and $I^{\prime}{ }_{x_{i}}$ is the sum of the $2^{\text {nd }}$ to $n^{\text {th }}$ order interactive effects that do not involve site $k$.

Similarly, let $Y$ represent any genotype with the $Q$ allele at site $k$. For each genotype $x_{i}$, we have a corresponding genotype $y_{i}$ that is identical to $x_{i}$ except that site $k$ now has the $Q$ allele. $R_{y_{i}}$, the fitness of $y_{i}$, can be written as $R_{y_{i}}=A_{y_{i}}+I_{y_{i}}+I_{y_{i}}^{\prime}$, where $A_{y_{i}}$ is the sum of additive (i.e., $1^{\text {st }}$ order interactive) effects, $I_{y_{i}}$ is the sum of the $2^{\text {nd }}$ to $n^{\text {th }}$ order interactive effects involving site $k$, and $I^{\prime} y_{i}$ is the sum of the $2^{\text {nd }}$ to $n^{\text {th }}$ order interactive effects that do not involve site $k$.

Note that the difference in the additive effect between alleles $P$ and $Q$ is a constant that is not influenced by sites other than $k$. That is, $A_{y_{i}}-A_{x_{i}}=C$. Therefore, we have

$$
\begin{aligned}
\operatorname{Cov}\left(A_{Y}, A_{X}\right)= & \frac{1}{N} \sum_{i=1}^{N}\left(A_{y_{i}}-E\left(A_{Y}\right)\right)\left(A_{x_{i}}-E\left(A_{X}\right)\right) \\
& =\frac{1}{N} \sum_{i=1}^{N}\left(A_{x_{i}}+C-E\left(A_{X}+C\right)\right)\left(A_{x_{i}}-E\left(A_{X}\right)\right) \\
= & \frac{1}{N} \sum_{i=1}^{N}\left(A_{x_{i}}-E\left(A_{X}\right)\right)\left(A_{x_{i}}-E\left(A_{X}\right)\right)=\operatorname{Var}\left(A_{X}\right) .
\end{aligned}
$$

Here, $N$ is the total number of pairs of $\left(x_{i}, y_{i}\right)$ and equals $4^{n-1}$ for a genome with $n$ sites each with four states, Cov stands for covariance, and Var stands for variance.

Also note that, because $x_{i}$ and $y_{i}$ are the same except at site $k, I_{x_{i}}^{\prime}=I_{y_{i}}^{\prime}$. Let $\operatorname{Cor}\left(I_{X}, I_{Y}\right)$ be the Pearson correlation between $I_{X}$ and $I_{Y}$. We have $\operatorname{Cor}\left(I_{X}, I_{Y}\right)=\operatorname{Cov}\left(I_{X}, I_{Y}\right) / \sqrt{\operatorname{Var}\left(I_{X}\right) \operatorname{Var}\left(I_{Y}\right)} \leq$ 1. Hence, $\operatorname{Cov}\left(I_{X}, I_{Y}\right) \leq \sqrt{\operatorname{Var}\left(I_{X}\right) \operatorname{Var}\left(I_{Y}\right)}$. Under the reasonable assumption that the corresponding interactive terms of $x_{i}$ and $y_{i}$ are sampled from the same distribution, $\operatorname{Var}\left(I_{X}\right)$ and $\operatorname{Var}\left(I_{Y}\right)$ are expected to be equal. Hence, $\operatorname{Cov}\left(I_{X}, I_{Y}\right) \leq \sqrt{\operatorname{Var}\left(I_{X}\right) \operatorname{Var}\left(I_{X}\right)}=\operatorname{Var}\left(I_{X}\right)$. Thus, $\operatorname{Cov}\left(I_{X}, I_{Y}\right)=\operatorname{Var}\left(I_{X}\right)$ when $I_{X}$ and $I_{Y}$ have a correlation of 1 ; otherwise $\operatorname{Cov}\left(I_{X}, I_{Y}\right)<\operatorname{Var}\left(I_{X}\right)$.

When epistasis is to some extent idiosyncratic, $I_{Y}$ does not correlate perfectly with $I_{X}$, resulting in $\operatorname{Cov}\left(I_{X}, I_{Y}\right)<\operatorname{Var}\left(I_{X}\right)$.

Under the assumption of independence among the interactive terms of a genotype, we have $\operatorname{Cov}($ mutational effect, fitness of the background genotype $)=\operatorname{Cov}\left(R_{Y}-R_{X}, R_{X}\right)=$ $\operatorname{Cov}\left(\left(A_{Y}-A_{X}\right)+\left(I_{Y}-I_{X}\right)+\left(I_{Y}^{\prime}-I_{X}^{\prime}\right), A_{X}+I_{X}+I_{X}^{\prime}\right)=\operatorname{Cov}\left(C, A_{X}\right)+\operatorname{Cov}\left(I_{X}, I_{Y}\right)-$ $\operatorname{Var}\left(I_{X}\right)+\operatorname{Cov}\left(0, I_{X}^{\prime}\right)=\operatorname{Cov}\left(I_{X}, I_{Y}\right)-\operatorname{Var}\left(I_{X}\right)<0$. This mathematical result means that, when epistasis is to some extent idiosyncratic, for any given mutation, we expect a negative correlation between the background fitness and mutational effect, which is exactly what diminishing returns of beneficial mutations and increasing costs of deleterious mutations are. The above result holds when fitness is replaced with any phenotypic trait as long as the trait value of each genotype can be expressed as the sum of the $2^{n}-1$ terms of effects.

## Mutational effect is generally negatively correlated with background fitness

Below we show that the preceding result about a given mutation also applies to different mutations. That is, we expect a negative correlation between the mutational effect and background fitness even when different mutations are considered. $R_{t}$, the Malthusian fitness of genotype $t$, can be expressed by $R_{t}=I_{t}^{1}+I_{t}^{2}+\cdots+I_{t}^{n}+I_{t}^{1,2}+I_{t}^{1,3}+\cdots+I_{t}^{n, n-1}+\cdots+$ $I_{t}^{1,2, \cdots, n}$. Here, the superscript indicates the site(s) involved in an additive or interactive term. For instance, $I_{t}^{2}$ stands for the additive effect of site 2 and $I_{t}^{1,2}$ stands for the interactive effect between sites 1 and 2 .

Let $X$ represent an arbitrary genotype and $Y$ represent another genotype that differs from $X$ by a particular mutation named $W$ that occurs at site $k$. We have

$$
\begin{aligned}
& R_{X}=I_{X}^{1}+I_{X}^{2}+\cdots+I_{X}^{n}+I_{X}^{1,2}+I_{X}^{1,3}+\cdots+I_{X}^{n-1, n}+\cdots+I_{X}^{1,2, \cdots, n} \\
& R_{Y}=I_{Y}^{1}+I_{Y}^{2}+\cdots+I_{Y}^{n}+I_{Y}^{1,2}+I_{Y}^{1,3}+\cdots+I_{Y}^{n-1, n}+\cdots+I_{Y}^{1,2, \cdots, n}
\end{aligned}
$$

In the above, all corresponding terms between $I_{X}$ and $I_{Y}$ are equal except for the terms involving k. So, $R_{Y}-R_{X}=\left(I_{Y}^{k}-I_{X}^{k}\right)+\left(I_{Y}^{1, k}-I_{X}^{1, k}\right)+\cdots+\left(I_{Y}^{n, k}-I_{X}^{n, k}\right)+\cdots+\left(I_{Y}^{(1,2, \cdots, n), k}-\right.$ $\left.I_{X}^{(1,2, \cdots, n), k}\right)$.

Under the assumption that all $I$ terms in an $R$ are independent from one another, $\operatorname{Cov}$ (mutational effect, background fitness $)=\operatorname{Cov}\left(R_{Y}-R_{X}, R_{X}\right)=\operatorname{Cov}\left(I_{Y}^{k}-I_{X}^{k}, I_{X}^{k}\right)+\operatorname{Cov}\left(I_{Y}^{1, k}-I_{X}^{1, k}, I_{X}^{1, k}\right)+$ $\cdots+\operatorname{Cov}\left(I_{Y}^{n, k}-I_{X}^{n, k}, I_{X}^{n, k}\right)+\cdots+\operatorname{Cov}\left(I_{Y}^{(1,2, \cdots, n), k}-I_{X}^{(1,2, \cdots, n), k}, I_{X}^{(1,2, \cdots, n), k}\right)$.

According to the law of total variance and the law of total covariance, we can expand each term in the above equation. Let us use the second order interaction between site $s$ and site $k$ as an example. $\operatorname{Cov}\left(I_{Y}^{s, k}-I_{X}^{s, k}, I_{X}^{s, k}\right)=\operatorname{Cov}\left(I_{Y}^{s, k}, I_{X}^{s, k}\right)-\operatorname{Var}\left(I_{X}^{s, k}\right)=E\left(\operatorname{Cov}\left(I_{Y}^{s, k}, I_{X}^{s, k} \mid W\right)\right)+$ $\operatorname{Cov}\left(E\left(I_{Y}^{s, k} \mid W\right), E\left(I_{X}^{s, k} \mid W\right)\right)-E\left(\operatorname{Var}\left(I_{X}^{s, k} \mid W\right)\right)-\operatorname{Var}\left(E\left(I_{X}^{s, k} \mid W\right)\right)=$ $E\left(\operatorname{Cov}\left(I_{Y}^{s, k}, I_{X}^{s, k} \mid W\right)-\operatorname{Var}\left(I_{X}^{s, k} \mid W\right)\right)+\operatorname{Cov}\left(E\left(I_{Y}^{s, k}-I_{X}^{s, k} \mid W\right), E\left(I_{X}^{s, k} \mid W\right)\right)$.

As shown in the section about a given mutation, as long as there is some degree of idiosyncrasy, $\operatorname{Cov}\left(I_{Y}^{s, k}, I_{X}^{s, k} \mid W\right)<\operatorname{Var}\left(I_{X}^{s, k} \mid W\right)$. So, $E\left(\operatorname{Cov}\left(I_{Y}^{s, k}, I_{X}^{s, k} \mid W\right)-\operatorname{Var}\left(I_{X}^{s, k} \mid W\right)\right)<0$. Further, $\operatorname{Cov}\left(E\left(I_{Y}^{s, k}-I_{X}^{s, k} \mid W\right), E\left(I_{X}^{s, k} \mid W\right)\right)=0$, because $E\left(I_{Y}^{s, k}-I_{X}^{s, k} \mid W\right)=0$ under the reasonable assumption that, given $W, I_{X}^{s, k}$ and $I_{Y}^{s, k}$ follow the same distribution. Hence, $\operatorname{Cov}\left(I_{Y}^{s, k}-\right.$ $\left.I_{X}^{s, k}, I_{X}^{s, k}\right)<0$. The same conclusion applies to all terms except the first-order interactive
(additive) term, which is $\operatorname{Cov}\left(I_{Y}^{k}-I_{X}^{k}, I_{X}^{k}\right)=E\left(\operatorname{Cov}\left(I_{Y}^{k}, I_{X}^{k} \mid W\right)-\operatorname{Var}\left(I_{X}^{k} \mid W\right)\right)+$ $\operatorname{Cov}\left(E\left(I_{Y}^{k}-I_{X}^{k} \mid W\right), E\left(I_{X}^{k} \mid W\right)\right)$. Because additive effects are independent of the genetic background, given $W, I_{Y}^{k}$ and $I_{X}^{k}$ are both fixed and are two randomly sampled values from the same distribution. Hence, $\operatorname{Cov}\left(I_{Y}^{k}, I_{X}^{k} \mid W\right)=0$ and $\operatorname{Var}\left(I_{X}^{k} \mid W\right)=0 . \operatorname{So} E\left(\operatorname{Cov}\left(I_{Y}^{k}, I_{X}^{k} \mid W\right)-\right.$ $\left.\operatorname{Var}\left(I_{X}^{k} \mid W\right)\right)=0 . E\left(I_{Y}^{k} \mid W\right)=I_{Y}^{k} \mid W$ and $E\left(I_{X}^{k} \mid W\right)=I_{X}^{k} \mid W$. As $W$ varies, $I_{Y}^{k} \mid W$ and $I_{X}^{k} \mid W$ are two random variables from the same distribution. They have the same variance and are not usually completely correlated. So, $\operatorname{Cov}\left(E\left(I_{Y}^{k}-I_{X}^{k} \mid W\right), E\left(I_{X}^{k} \mid W\right)\right)=\operatorname{Cov}\left(I_{Y}^{k}-I_{X}^{k}\left|W, I_{X}^{k}\right| W\right)=$ $\operatorname{Cov}\left(I_{Y}^{k}, I_{X}^{k} \mid W\right)-\operatorname{Var}\left(I_{X}^{k} \mid W\right)<0$. Under the special case when all additive terms are equal, $\operatorname{Cov}\left(E\left(I_{Y}^{k}-I_{X}^{k} \mid W\right), E\left(I_{X}^{k} \mid W\right)\right)=0$.

Thus, $\operatorname{Cov}($ mutational effect, background fitness $)=E\left(\operatorname{Cov}\left(I_{Y}^{k}, I_{X}^{k} \mid W\right)-\operatorname{Var}\left(I_{X}^{k} \mid W\right)\right)+$ $\operatorname{Cov}\left(E\left(I_{Y}^{k}-I_{X}^{k} \mid W\right), E\left(I_{X}^{k} \mid W\right)\right)+E\left(\operatorname{Cov}\left(I_{Y}^{1, k}, I_{X}^{1, k} \mid W\right)-\operatorname{Var}\left(I_{X}^{1, k} \mid W\right)\right)+$ $\operatorname{Cov}\left(E\left(I_{Y}^{1, k}-I_{X}^{1, k} \mid W\right), E\left(I_{X}^{1, k} \mid W\right)\right)+\cdots+E\left(\operatorname{Cov}\left(I_{Y}^{n, k}, I_{X}^{n, k} \mid W\right)-\operatorname{Var}\left(I_{X}^{n, k} \mid W\right)\right)+$ $\operatorname{Cov}\left(E\left(I_{Y}^{n, k}-I_{X}^{n, k} \mid W\right), E\left(I_{X}^{n, k} \mid W\right)\right)+\cdots+E\left(\operatorname{Cov}\left(I_{Y}^{(1,2, \cdots, n), k}, I_{X}^{(1,2, \cdots, n), k} \mid W\right)-\right.$ $\left.\operatorname{Var}\left(I_{X}^{(1,2, \cdots, n), k} \mid W\right)\right)+\operatorname{Cov}\left(E\left(I_{Y}^{(1,2, \cdots, n), k}-I_{X}^{(1,2, \cdots, n), k} \mid W\right), E\left(I_{X}^{(1,2, \cdots, n), k} \mid W\right)\right)=$ $\operatorname{Cov}\left(I_{Y}^{k}-I_{X}^{k}\left|W, I_{X}^{k}\right| W\right)+E\left(\operatorname{Cov}\left(I_{Y}^{1, k}, I_{X}^{1, k} \mid W\right)-\operatorname{Var}\left(I_{X}^{1, k} \mid W\right)\right)+\cdots+E\left(\operatorname{Cov}\left(I_{Y}^{n, k}, I_{X}^{n, k} \mid W\right)-\right.$ $\left.\operatorname{Var}\left(I_{X}^{n, k} \mid W\right)\right)+\cdots+E\left(\operatorname{Cov}\left(I_{Y}^{(1,2, \cdots, n), k}, I_{X}^{(1,2, \cdots, n), k} \mid W\right)-\operatorname{Var}\left(I_{X}^{(1,2, \cdots, n), k} \mid W\right)\right)<0$.

Therefore, in the $n$-order model, mutational effect is negatively correlated with background fitness even for different mutations. As shown in the above mathematical derivation, this
negative correlation has two sources: unequal additive effects and idiosyncratic epistasis. Given the same additive effects, increasing the idiosyncrasy in epistasis strengthens the negative correlation. As in the preceding section, the result here applies to any phenotypic trait as long as the trait value of a genotype can be expressed as the sum of the $2^{n}-1$ terms of effects.

## Expected idiosyncrasy index under the $\boldsymbol{n}$-order landscape model

The variance of the effect of a particular mutation across all genetic backgrounds can be calculated as follows. Let $X$ represent an arbitrary genotype and $Y$ represent another genotype that differs from $X$ at site $k$ only. We have shown earlier that

$$
\begin{aligned}
& R_{X}=I_{X}^{1}+I_{X}^{2}+\cdots+I_{X}^{n}+I_{X}^{1,2}+I_{X}^{1,3}+\cdots+I_{X}^{n-1, n}+\cdots+I_{X}^{1,2, \cdots, n} \\
& R_{Y}=I_{Y}^{1}+I_{Y}^{2}+\cdots+I_{Y}^{n}+I_{Y}^{1,2}+I_{Y}^{1,3}+\cdots+I_{Y}^{n-1, n}+\cdots+I_{Y}^{1,2, \cdots, n} .
\end{aligned}
$$

In the above, all corresponding terms between $I_{X}$ and $I_{Y}$ are equal except for the terms involving
k. So, $R_{Y}-R_{X}=\left(I_{Y}^{k}-I_{X}^{k}\right)+\left(I_{Y}^{1, k}-I_{X}^{1, k}\right)+\cdots+\left(I_{Y}^{n, k}-I_{X}^{n, k}\right)+\cdots+\left(I_{Y}^{(1,2, \cdots, n), k}-\right.$
$\left.I_{X}^{(1,2, \cdots, n), k}\right)$ and $\operatorname{Var}\left(R_{y}-R_{x}\right)=\operatorname{Var}\left(I_{Y}^{k}-I_{X}^{k}\right)+\operatorname{Var}\left(I_{Y}^{1, k}-I_{X}^{1, k}\right)+\cdots+\operatorname{Var}\left(I_{Y}^{n, k}-I_{X}^{n, k}\right)+$ $\cdots+\operatorname{Var}\left(I_{Y}^{(1,2, \cdots, n), k}-I_{X}^{(1,2, \cdots, n), k}\right)$. If we assume that all interactive terms for $X$ and $Y$ are independent with the same variance $\sigma^{2}, \operatorname{Var}\left(R_{Y}-R_{X}\right)=2^{n} \sigma^{2}$.

If there are $M$ states at each site, among the $k^{\text {th }}$ order interactive terms, $\binom{n}{k}(1 / M)^{k}$ terms are expected to be the same between two random genotypes. One can show that $\sum_{k=1}^{n}\binom{n}{k}(1 / M)^{k}=$ $\sum_{k=1}^{n} \frac{n!}{k!(n-k)!} \cdot(1 / M)^{\mathrm{k}} \approx \sum_{k=1}^{n} \frac{n^{k}}{k!} \cdot(1 / M)^{k} \approx e^{\frac{n}{M}}$. Thus, two random genotypes are expected to differ by approximately $2^{n}-1-e^{n / M}$ terms. Hence, the variance of the fitness difference between two random genotypes is $\operatorname{Var}\left(R_{Y}-R_{X}\right)=2\left(2^{n}-1-e^{\frac{n}{M}}\right) \sigma^{2}$. Because $M \geq 2, e^{\frac{n}{M}}<$
$2^{n}$. So, when $n$ is large, $\operatorname{Var}\left(R_{Y}-R_{X}\right)$ is approximately $2^{n+1} \sigma^{2}$. Therefore, the idiosyncrasy index becomes $\frac{\sqrt{2^{n}} \sigma}{\sqrt{2^{n+1}} \sigma}=\frac{1}{\sqrt{2}}=\sim 0.71$. Our numerical finding (the most right red dot in Fig. 2A) confirms this result.

## Mutational supply and evolutionary trajectories

During adaptation, if the supply of beneficial mutations diminishes as the fitness of a population rises, the speed of population fitness increase per unit time will decline. However, if the speed of fitness increase is measured per beneficial mutation accrued as in the present study, the reducing supply of beneficial mutations will not reduce the speed of fitness increase.

During mutation accumulation in the near absence of selection, as the population fitness declines, the supply of beneficial mutations should increase and the supply of deleterious mutations should decrease. Thus, even under a purely additive model, the speed of population fitness drop slows. When only the first few mutations accrued are examined, however, this phenomenon of slowing fitness drops should be minimal under the purely additive model unless the number of possible mutations is very limited

## Empirical phenotype landscapes

An unbiased search for phenotype landscape data published between 2000 and 2019 was preformed using Google Scholar with words such as "epistasis", "fitness landscape", or "genetic interaction". A total of 18 datasets were found for which quantitative phenotype values were published or could be calculated without extensive analysis (e.g., studies reporting only sequencing reads were excluded) and which included genotypes with at least two mutations in comparison with the reference genotype. Measured phenotypes included protein function such
as $\log$ (fluorescence), $\log$ (Wrightian fitness) or growth rate, and colony size. For landscapes reporting genotypes with nucleotide mutations, all 12 classes of single mutations were considered. For landscapes reporting genotypes with amino acid mutations, all 380 mutations between any two amino acids were considered as single mutations. Genotypes with fitness at the minimum detection limit (e.g., non-fluorescent GFP genotypes) or that were lethal or nongrowing (e.g., tRNA genotypes with Wrightian fitness relative to the wild-type $=0.5$ ) were excluded. A final set of 12 studies with at least 10 single mutations and at least an average of 10 fitness effects measured per mutation were used for further analysis. Table S1 lists the basic information of these phenotype landscapes. The original study of the tRNA fitness landscape reported Wrightian fitness relative to the wild-type; we computed Malthusian fitness = $\log$ (Wrightian fitness) in the present study.

To map the RNA-folding landscape, we studied a sequence of 72 nucleotides, the length of the tRNA gene used in the tRNA fitness landscape. The phenotype studied was the absolute value of the minimum free energy (MFE) of a sequence, calculated using ViennaRNA (https://www.tbi.univie.ac.at/RNA/). Two single mutants and the corresponding double mutant were randomly created for each of 2 million random background genotypes, and this set of genotypes was used for subsequent analyses.

## Simulating idiosyncratic fitness landscapes

We simulated a series of 16 -site fitness landscapes under $n$-order models with two states (A/T) per site, including all 65,536 genotypes. The fitness of a genotype is determined by additive effects (referred to as first order interactions) and interactive effects. For the $k^{\text {th }}$ order interaction $(1 \leq k \leq 16)$, there are $\frac{16!}{(16-k)!k!}$ interactive terms. For each of these terms, there are $2^{k}$ possible
state combinations. The fitness effect of each state combination of each interaction term for each order of interaction is drawn independently from the standard normal distribution, and the fitness of the genotype concerned is the sum of all these terms. Sixteen landscapes were made by including successively increasing orders of interactions. For instance, the first landscape contains only $1^{\text {st }}$ order interactions (purely additive), the second landscape contains only $1^{\text {st }}$ and $2^{\text {nd }}$ order interactions, and the sixteenth landscape contains all orders of interactions. As expected, $I_{\mathrm{id}}$ increased with the number of orders of interactions included (orange circles in Fig. 2A). In each landscape, fitness values are linearly scaled to the interval of [0, 1]. In each of these landscapes, epistasis between mutations is symmetrically distributed with the mean equal to 0 . We also simulated additive landscapes with larger $n$ values to examine the linearity of fitness drops during mutation accumulation.

## Estimating idiosyncrasy index

For each single mutation in a fitness landscape, we calculated its fitness effects on all genetic backgrounds available. For each mutation, we also derived a control set of fitness effects by randomly sampling (with replacement) the same number of pairs of genotypes from the landscape as used for the mutation and computing the fitness difference for each pair. We then calculated the range of fitness effects and standard deviation (SD) of fitness effects for each mutation and its control dataset. For each mutation, we calculated the ratio in the SD (or range) between the actual data and the control data. The average ratio across all single mutations is the $I_{\mathrm{id}}$ of the landscape, and the error bars in Fig. 1C are the standard error of the mean (SE). The same method is used to estimate $I_{\text {id }}$ of other phenotype landscapes. Although empirical phenotype landscape data typically include only a small fraction of nonrandomly sampled genotypes and their phenotypes, this nonrandom sampling is not expected to substantially affect
$I_{\text {id }}$ estimation, because both the variation of the effect of a mutation and the variation in the control data are estimated using the available landscape data.

## Examining correlation between background fitness and mutational effect

For the simulated $n$-order landscapes and empirical landscapes (tRNA fitness, GFP activity, and RNA-folding), Pearson's correlation coefficient was calculated between mutational effect on a particular trait and background trait value for each single mutation. Mutations appearing on less than four backgrounds were excluded. Pearson's correlation coefficient was also calculated between all mutational effects and background trait values for each landscape.

In the tRNA fitness landscape, the fitness of each genotype was measured in six replicates. To exclude artificial correlation due to measurement error, the background fitness of each case of a single mutation is calculated using the mean fitness value from replicates $1-3$, while the mutational effect is computed using mean fitness from replicates 4-6. Additionally, two mutations which are the reverse of each other on the same backgrounds can automatically create a negative correlation between all mutational effects and background fitness. Hence, in each landscape where this could occur we randomly chose a mutation or its reversion when pooling all mutations together (green diamonds in Fig. 2A; Fig. 2C; Fig. S2C-D).

For analysis of diminishing returns and increasing costs, mutations were deemed beneficial or detrimental depending on their effect on the wild-type genotype in GFP and tRNA, or a random arbitrary genotype in RNA-folding, or on a genotype with fitness value closest to the average fitness in the $n$-order landscapes.

## Simulating evolutionary trajectories in mutation accumulation (MA)

For each empirical landscape, MA from an initial genotype was simulated by randomly choosing single mutations until the resulting genotype was non-functional (GFP) or for a maximum of 10 mutational steps (tRNA) or 50 mutational steps (RNA-folding). For all plots concerning MA, the mean phenotype value of the landscape was calculated from all genotypes.

For the GFP landscape, genotypes were not allowed to be revisited within a trajectory. If an MA trajectory was part of another simulated trajectory, the shorter trajectory was discarded. A total of 3,069 MA trajectories were simulated from each of 3,069 initial genotypes with activity equal to or greater than that of the wild-type. In the tRNA fitness landscape, $10,000 \mathrm{MA}$ trajectories were simulated starting from the wild-type genotype. In the $n$-order fitness landscapes, 10,000 MA trajectories were simulated starting from the genotype with fitness closest to the $90^{\text {th }}$ percentile. For the RNA-folding landscape, a total of 350 MA trajectories were simulated starting with the final genotypes from the simulated adaptations.

## Simulating adaptive trajectories

For each empirical landscape, adaptation from an initial genotype was simulated by randomly choosing a single beneficial mutation, which increased the value of the trait concerned, until no more single beneficial mutations were available. A total of 5,000 adaptive trajectories starting from 3,441 initial genotypes chosen from the bottom $15 \%$ of genotypes (activity $\leq-0.4$ ) were simulated for the GFP landscape. A total of 350 adaptive trajectories starting from 350 initial genotypes chosen from the bottom $0.0175 \%$ of genotypes in the RNA-folding landscape were simulated. In the tRNA fitness landscape, we simulated five adaptive trajectories starting from each genotype with fitness $=0.5$; trajectories longer than two steps were retained, totaling 15,878
trajectories. In the $n$-order fitness landscapes, adaptations start from all genotypes in the bottom $20 \%$ of fitness distribution; among 10 adaptation simulations starting from each genotype, trajectories equal to or longer than two steps were retained.

## Data and code availability

Data analysis and simulations for all landscapes except the tRNA and model landscapes were performed using R version 3.5.2. Analysis and simulations for the tRNA and model landscapes were performed using Python version 3.6.9. All figures were made with matplotlib package in Python and Keynote. Code and new data are available at https://github.com/lyonsdm/idiosyncrasy.

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## Supplementary Materials



Supplemental Figure 2-1 The high idiosyncrasy indices (Iid) observed are not due to phenotype measurement errors or the use of standard deviation (SD) instead of range of mutational effects.
(A) SD-based Iid of the yeast tRNA fitness landscape is insensitive to the number of experimental replicates used in the fitness estimation. Boxplots show the distribution of Iid values of 828 single mutations in the tRNA landscape, calculated based on different numbers of replicates. The lower and upper edges of a box represent the first (qu1) and third (qu3) quartiles, respectively, the horizontal line inside the box indicates the median (md), the whiskers extend to the most extreme values inside inner fences, $\mathrm{md} \pm 1.5$ (qu3 - qu1), and the grey dots represent values outside the inner fences (outliers). Violet dots show mean lid of all mutations calculated based on respective numbers of replicates. (B) Range-based lid for various phenotype landscapes. Error bars show standard errors. Detailed information of each landscape is provided in Table S1.


Supplemental Figure 2-2 Negative correlation between mutational effect and background phenotype in GFP and RNAfolding landscapes.
(A) Distribution of Pearson's correlation coefficient (r) between mutational effect and background phenotype for individual mutations in the GFP landscape. (B) Distribution of r for individual mutations in the RNA-folding landscape. (C) Relationship between background phenotype and mutational effect for all mutations in the GFP landscape. (D) Relationship between background phenotype and mutational effect for all mutations in the RNA-folding landscape. MFE, minimum free energy. The red line depicts the running mean in non-overlapping X-axis bins of width $=0.02$ and 2 in (C) and (D), respectively, in all bins with more than 10 data points. There is no measurement error in the RNA-folding landscape. Shared measurement error between mutational effect and background fitness cannot be controlled for in GFP as replicate fitness measurements are not available. For each mutation and its reverse, we considered a random one of them in (C) and (D).


Supplemental Figure 2-3 Fig. S3. Patterns of correlation between mutational effect and background fitness/phenotype for individual beneficial or deleterious mutations in various landscapes.
(A) Boxplots showing distributions of correlations in a series of $n$-order landscapes of 16 sites (where the highest order of nonzero interaction is indicated on the X -axis) for beneficial (blue) and deleterious (red) mutations, respectively. The lower and upper edges of a box represent the first (qu1) and third (qu3) quartiles, respectively, the horizontal line inside the box indicates the median (md), the whiskers extend to the most extreme values inside inner fences, $\mathrm{md} \pm 1.5$ (qu3 - qu1), and the dots represent values outside the inner fences (outliers). (B-D) Frequency distributions of correlations for individual beneficial mutations (blue) and deleterious mutations (red) in the tRNA (B), GFP (C), and RNA-folding (D) landscapes. Whether a mutation is beneficial or deleterious is determined in reference to the wild-type (tRNA and GFP) or an arbitrary reference genotype ( n -order and RNAfolding). The wider distribution for deleterious than beneficial mutations is at least in part due to the larger number of deleterious than beneficial mutations.


Supplemental Figure 2-4 Average fitness trajectories of mutation accumulation simulated in various n-order additive landscapes $(k=1)$ with different numbers of sites $(\mathbf{n})$.

The mean trajectories are scaled so that the minimum fitness appearing in the trajectory is 0 and the maximum is 1 to allow direct comparison.


Supplemental Figure 2-5 Fitness declines decelerate during mutation accumulation as a result of idiosyncratic epistasis.
(A) A total of 5000 fitness trajectories of mutation accumulation simulated in the GFP landscape, with the average trajectory shown in black, at each step when the trajectory number exceeds 10. (B) A total of 350 fitness trajectories of mutation accumulation simulated in the RNA-folding landscape, with the average trajectory shown in black. The dotted lines indicate the mean phenotypic value of all genotypes in the landscape, excluding non-active genotypes in the GFP landscape. For comparison, the dashed line in (A) or (B) represents the predicted linear decline given the slope in the first mutational step.


Supplemental Figure 2-6 Idiosyncratic epistasis is necessary but not sufficient to cause decelerating adaptations.
(A) Gamma distributions of genotype fitness for house-of-cards landscapes, with different values of the gamma shape parameter lalpha. (B) Theoretically computed mean fitness trajectories of adaptation on landscapes in (A) with corresponding colors. (C) Average adaptive trajectories starting from the genotype with the lowest fitness (0), simulated in a series of $n$-order landscapes of 16 sites where each nonzero interaction term of each genotype is drawn from a gamma distribution of \alpha $=1$. (D) Average adaptive trajectories starting from the genotype with the lowest fitness ( 0 ), simulated in a series of $n$-order landscapes of 16 sites where each nonzero interaction term of each genotype is drawn from a beta distribution with $\mathrm{a}=\mathrm{b}=0.25$. For each landscape in (C) and (D), the distribution of epistasis between mutations is symmetrical with mean equal to 0 .


Supplemental Figure 2-7 Adaptation slows in empirical phenotype landscapes.
(A) A total of 5000 adaptive trajectories simulated in the GFP landscape, with the average trajectory shown in black, at each step when the trajectory number exceeds 10. (B) A total of 350 adaptive trajectories simulated in the RNA-folding landscape, with the average trajectory shown in black, at each step when the trajectory number exceeds 10. For comparison, the dashed line in (A) or (B) represents the predicted linear increase given the slope in the first mutational step.

Supplemental Table 2-1 Description of empirical landscapes, ordered by idiosyncrasy indices shown in Figure 2-1C

| Landscape name | Description | Phenotype | $\begin{gathered} \# \text { of } \\ \text { genotypes } \end{gathered}$ | \# of single mutations | References |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\lambda$ Repressor - high | Phage lambda repressor (CI) at high expression | Repression of GFP expression | 887 | 174 | 24 |
| Fungal tRNA | tRNA- $\operatorname{Arg}(\mathrm{CCU})$ of post-whole-genome-duplication yeast species | $\log$ (fitness) | 4,175 | 36 | 25 |
| Yeast tRNA | S. cerevisae tRNA-Arg(CCU) | $\log$ (fitness) | 65,537 | 828 | 23 |
| GFP | A.victoria green fluorescent protein | $\log$ (fluorescence) | 30,123 | 2,314 | 26 |
| Yeast, PAB1-RRM2 | S. cerevisae RNA-recognition motif 2 of poly(A)-binding protein 1 | Fitness relative to wild-type (relative enrichment score) | 40,722 | 10,668 | 27 |
| E. quadricolor, flourescence | Entacmaea quadricolor fluorescent protein | $\log$ (fluorescence) | 8,191 | 26 | 28 |
| Human, FOS | Physical interaction between human FOS and JUN proteins, with mutations in FOS | Strength of FOSJUN protein physical interaction | 17,685 | 1,594 | 29 |
| $\lambda$ Repressor - low | Phage lambda repressor (CI) at low expression | $\begin{gathered} \text { Repression of GFP } \\ \text { expression } \end{gathered}$ | 887 | 174 | 24 |
| Human, FOS \& JUN | Physical interaction between human FOS and JUN proteins, with mutations in the two genes | Strength of FOSJUN protein physical interaction | 108,833 | 12,160 | 29 |
| RNA-folding | 72-nucleotide sequence, folding predicted by ViennaRNA | Minimum free energy | 2,000,000 | 864 | Present study |
| Streptococcus, GB1 | IgG-binding domain of protein G | $\underset{\text { IgG-FC }}{\text { Biding affinity to }}$ | 536,962 | 20,900 | 30 |
| Yeast Double-KO | S. cerevisae double gene deletions, genomewide | Fitness relative to wild-type (colony size) | 14,578,495 | 10,564 | ${ }^{31}$ |

## Chapter 3 Evidence for the Selective Basis of Transition-to-Transversion Substitution Bias in Two RNA Viruses

Note: This chapter is a modified version of the published article:
Lyons DM, Lauring AS. 2017. Evidence for the Selective Basis of Transition-to-Transversion Substitution Bias in Two RNA Viruses. Mol Biol Evol. 34(12):3205-3215. doi:10.1093/molbev/msx251.


#### Abstract

The substitution rates of transitions are higher than expected by chance relative to those of transversions. Many have argued that selection disfavors transversions, as nonsynonymous transversions are less likely to conserve biochemical properties of the original amino acid. Only recently has it become feasible to directly test this selective hypothesis by comparing the fitness effects of a large number of transition and transversion mutations. For example, a recent study of six viruses and one beta-lactamase gene did not find evidence supporting the selective hypothesis. Here we analyze the relative fitness effects of transition and transversion mutations from our recently published genome-wide study of mutational fitness effects in influenza virus. In contrast to prior work, we find that transversions are significantly more detrimental than transitions. Using what we believe to be an improved statistical framework, we also identify a similar trend in two HIV datasets. We further demonstrate a fitness difference in transition and transversion mutations using four deep mutational scanning datasets of influenza virus and HIV, which provided adequate statistical power. We find that three of the most commonly cited radical/conservative amino acid categories are predictive of fitness, supporting their utility in studies of positive selection and codon usage bias. We conclude that selection is a major contributor to the transition:transversion substitution bias in viruses and that this effect is only


partially explained by the greater likelihood of transversion mutations to cause radical as opposed to conservative amino acid changes.

## Introduction

Fifty years ago, Walter Fitch noted that the nucleotide substitution pattern in cytochrome c is non-random (Fitch 1967). If random, transversions (purine-pyrimidine changes) should be observed twice as often as transitions (purine to purine or pyrimidine to pyrimidine changes) solely due to the accessible mutations. However, Fitch observed that transitions are more common than transversions. In fact, this transition-transversion (Ts:Tv) substitution bias has been noted across many proteins and phyla, and phylogenetic inferences account for this bias by weighting transversions more than transitions (Gojobori et al. 1982; Kumar 1996; Wakeley 1996; Petrov and Hartl 1999; Rosenberg et al. 2003; Lynch 2010; Duchêne et al. 2015).

The underlying reasons for this widespread $\mathrm{Ts}: T \mathrm{v}$ substitution bias are largely unknown. Two main hypotheses, which are not mutually exclusive, have emerged to explain this phenomenon: the mutational hypothesis and the selective hypothesis. The mutational hypothesis holds that the transition mutation rates of polymerases are higher than the transversion rates. This hypothesis is supported by the observation of a transitional bias in both coding and non-coding regions (Zhang and Gerstein 2003; Jiang and Zhao 2006) as well as mutation rate analyses showing higher transition mutation rates (Denver et al. 2004; Pauly, Procario, et al. 2017). The selective hypothesis posits that natural selection disfavors transversions. This hypothesis is based on the observation that, depending on codon usage, non-synonymous transitions are more likely to conserve important biochemical properties of the original amino acid (Vogel and Kopun 1977; Miyata et al. 1979; Zhang 2000). For example, a mutation that changes the charge of an amino
acid is a "radical" change, while one that does not is a "conservative" change. However, this provides only indirect evidence for the selective hypothesis and the extent to which radical/conservative distinctions are predictive of fitness is unclear. Radical changes do occur less often than conservative ones during protein evolution. Arguments based on this observation can be circular (Dagan et al. 2002; Yampolsky and Stoltzfus 2005). If the transition mutation rate is higher and transitions are more likely to be conservative, then conservative changes will occur more often simply due to the transitional mutation bias. Furthermore, the radical/conservative amino acid distinctions may be overly broad and arbitrary. For example, the hydrophobicity of amino acids may be more constrained for some proteins while their size may be more constrained for other proteins. One could arbitrarily choose a biochemical distinction that would suggest transversions are more likely to be conservative.

Only recently has it become experimentally tractable to test directly the selective hypothesis by comparing the fitness effects of a large number of transition and transversion mutations. A recent study (Stoltzfus and Norris 2016) compared the fitness effects of missense transitions and transversions reported in eight studies of mutational fitness effects. This metaanalysis included: a beta-lactamase gene (TEM1), two HIV genes (integrase and capsid), and five genome-wide studies of viruses (Sanjuán et al. 2004; Purificación Carrasco et al. 2007; P. Carrasco et al. 2007; Domingo-Calap et al. 2009; Peris et al. 2010; Jacquier et al. 2013; Rihn et al. 2013; Rihn et al. 2015). Stoltzfus and Norris did not identify a statistically significant difference in the fitness effects of transitions and transversions (Ts-Tv) in any of the viral datasets (2016). They did find a statistically significant difference after combining the data, which was deemed to be of questionable biological significance.

Here, we revisit this question using our recently published library of randomly distributed point mutations in influenza A virus (Visher et al. 2016). In contrast to other viral datasets, we find that transitions are significantly less detrimental than transversions. We apply what we believe is an improved statistical framework and identify a similar trend in the HIV integrase and capsid datasets (Rihn et al. 2013; Rihn et al. 2015). We expand our analysis to include deep mutational scanning studies of one HIV gene and two genes from two different strains of influenza (Bloom 2014; Doud et al. 2015; Doud and Bloom 2016; Haddox et al. 2016). The distribution of fitness effects of transversions is shifted toward more detrimental effects compared to transitions at some points along the fitness distribution in each gene, and transitions are never more detrimental. Three of the most commonly cited radical/conservative distinctions are predictive of mutational fitness effects. However, transversions are more detrimental than transitions even when controlling for their greater likelihood to be radical.

## Results

## Transitions are less detrimental in influenza $\mathbf{A}$ virus

We recently published a library of 128 point mutants in influenza A virus (Visher et al. 2016). As in other studies of viral mutational fitness effects, the substitution types were chosen at random and the fitness values were assessed individually. Our library contains 95 mutants distributed across the eight genomic RNA in proportion to the size of each segment and an additional 33 random mutations in the segments encoding the surface proteins hemagglutinin (HA) and neuraminidase (NA). Thus, a total of 57 mutations occur in HA and NA and 71 in the other six segments. For the present study, we excluded 27 synonymous mutations and 6
beneficial missense mutations and considered the remaining 95 missense transitions and transversions that had fitness values equal to or less than one. We performed our analyses on the total library $(\mathrm{N}=95)$, the genes encoding the internal proteins only $(\mathrm{N}=53)$, and the genes encoding the surface proteins only $(\mathrm{N}=42)$ (Supplemental Table 3-1; Total, Internal, and Surface datasets, respectively). Each of these data subsets is larger than the analogous genomewide datasets of other viruses.

As described by Stoltzfus and Norris (Stoltzfus and Norris 2016), we identified differences in the fitness effects of Ts and Tv by calculating the area under the curve (AUC) of a receiver operating characteristic (ROC) curve. An ROC curve plots the true positive rate against the false positive rate of a binary classifier system as the discrimination threshold varies. Consider a hypothetical example using a binary classifier system to predict whether a mutation is a transition or a transversion without prior knowledge of its identity. If the fitness of the mutation is above a fitness level threshold, it is categorized as a transition, and if it is below the threshold, it is categorized as a transversion. The AUC is equivalent to the probability that a randomly chosen transition is more fit than a randomly chosen transversion. The AUC can be calculated from the Mann-Whitney U test statistic (see Materials and Methods) (Hanley and McNeil 1982; Mason and Graham 2002). An AUC of 1 would indicate that all transitions are more fit than all transversions, and an AUC of 0 would indicate that all transversions are more fit than all transitions. The null expectation is an AUC of 0.50 . To identify the points along the fitness distribution at which there is a Ts-Tv difference, we calculated the AUC among mutations at or above 10 successively higher fitness thresholds, starting at 0 and increasing each threshold by 0.10 .


Figure 3-1 Differences in Ts and Tv Fitness Effects as measured by AUC
Transition-transversion (Ts-Tv) fitness differences as measured by area under the curve of an ROC curve (AUC) for the total, internal, and surface influenza datasets. To identify the points along the fitness distribution at which there is a Ts-Tv difference, the AUC was calculated among mutations at or above 10 successively higher fitness thresholds, starting at 0 and increasing by 0.10 . Filled circles denote $p<0.05$ for a one-sided Mann-Whitney $U$ test where the alternative is transitions are more fit at that threshold. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.

Using the AUC criterion, we did not find a statistically significant difference between the fitness effects of transition and transversion mutations across the total dataset, the internal dataset, or the surface (HA/NA) dataset (Figure 3-1, relative fitness threshold of 0). However, we detected a significant difference when we examined only non-lethal mutations (Figure 3-1, relative fitness threshold of 0.1 ; there were no mutations with a fitness value between 0 and 0.1 ). Among the viable fraction, transitions are significantly more fit than transversions ( $\mathrm{AUC}=0.65$,
$\mathrm{p}=0.03$ ). This fitness difference is more pronounced in the internal dataset $(\mathrm{AUC}=0.74, \mathrm{p}=$ 0.02 ) but is not present among the surface dataset. As the thresholds approach 1 , the $\mathrm{Ts}-\mathrm{Tv}$ difference approaches 0.5 and loses significance (perhaps due to decreasing sample size) in both the genome-wide and internal datasets. In contrast, we never found transversions to be significantly more fit than transitions. Thus, viable transitions are more fit than viable transversions, and this fitness difference varies between the internal and surface datasets.

Our findings in influenza differ from those in other viruses (HIV integrase, HIV capsid, TEV, F1, VSV, Q $\beta$, $\phi$ X174) (Stoltzfus and Norris 2016). While selective constraints could potentially differ among these viruses, another factor could be the greater statistical power of our influenza dataset due to our larger sample size as compared to the other genome-wide viral datasets. Our influenza virus datasets were smaller, however, than those in the HIV integrase and capsid studies.

## An alternative statistical approach better captures Ts-Tv fitness differences

The fact that we could only identify a significant difference in influenza by excluding lethal mutations suggests an inherent bias in the AUC threshold analysis and led us to reexamine our statistical framework. If transitions are more likely to be lethal in influenza, this would offset their advantage among viable mutations. More generally, as the fitness threshold increases, the AUC reflects only the Ts-Tv differences at the higher end of the fitness distribution. In fact, when we applied decreasing, as opposed to increasing, thresholds, many of our conclusions were opposite from those obtained with increasing thresholds (Supplemental Figure 3-1). In this case, the influenza total dataset is weighted by strongly detrimental transitions and no fitness differences between Ts and Tv were detected at any threshold. In the larger HIV capsid and
combined integrase and capsid datasets, we observed a previously unrecognized, and statistically significant, Ts-Tv difference at decreasing thresholds driven by the inclusion of strongly detrimental transversions (Stoltzfus and Norris 2016).


Figure 3-2 Comparisons of the Distribution of Ts and Tv Fitness Effects
Empirical cumulative distribution functions of transitions (solid line) and transversions (dotted line) in our influenza datasets (A, top) and the HIV combined, integrase (IN), and capsid (CA) datasets (B, top). Odds ratios indicate the odds of a transversion versus a transition to be at or below each of 10 relative fitness thresholds as estimated by a Fisher test for our influenza datasets (A, bottom) and HIV datasets (B, bottom). Filled circles denote p < 0.05 for a two-sided test with Holm-Bonferroni correction. Lines shown to clarify trends only.

To capture differences in the distribution of fitness effects between transitions and transversions more completely, we compared the empirical cumulative distribution functions (CDF) of each mutation type. The CDF reveal only subtle differences between transitions and transversions in the total influenza dataset, with more transitions at low fitness levels and more transversions at intermediate fitness levels (Figure 3-2A, top). The difference between transitions and transversions is greater for the internal dataset, where $75 \%$ of transversions have a lower fitness compared to only $50 \%$ of transitions at a fitness threshold of 0.8 . However, transitions are proportionally over-represented below a fitness of 0.3. In contrast, the AUC threshold analysis for the internal influenza dataset seems to suggest a Ts-Tv fitness difference
starting at 0.1 and decreasing to no difference at 0.8 (Figure 3-1), precisely the opposite of the differences in the distributions (Figure 3-2A).

Recognizing these issues, we implemented a different statistical approach that is an explicit comparison of the Ts and Tv CDF and is therefore better able to resolve differences in the distributions of fitness effects. We used 10 fitness thresholds from 0 to 0.9 with a step of 0.1 . At each fitness level, we performed a Fisher test to compare the proportion of transversions and transitions at or below the threshold. The estimated effect size is the odds ratio for transversions to be at or below the threshold compared to transitions. As this approach never excludes data, it is less biased by the fitness values at the tails of the distributions. Unlike the AUC (see Figure 31), the odds ratios closely follow the divergence in the corresponding CDF (compare top and bottom panels in Figure 3-2).

We used this approach to reanalyze data from our influenza datasets as well as those for HIV integrase (IN) and capsid (CA). Using a conservative Holm-Bonferroni correction for multiple comparisons, we did not find a statistically significant difference between transition and transversion mutations in influenza at any fitness level (Figure 3-2A, bottom). The CDF suggests that the impact of transitions relative to transversions at low fitness levels (0-0.3) is indeed offset by their impact at higher ones (0.6-1). There are no significant $\mathrm{Ts}-\mathrm{Tv}$ differences in either of the two HIV datasets or in the combined dataset. However, there is a trend across the HIV datasets suggesting that transversions are more likely to be lethal as compared to transitions (Figure 3-2B, bottom, first threshold), an effect missed by the AUC analysis. We note that while the original HIV studies considered a fitness below 0.02 to be lethal (Rihn et al. 2013; Rihn et al. 2015); we
applied a strict and consistent criterion for lethality across the datasets and considered a fitness of 0 to be lethal.

## Transversions are more detrimental in larger influenza and HIV datasets

While the influenza and HIV datasets are relatively large for studies of viral mutational fitness effects, they sample only a small fraction of the total number of possible point mutations. The influenza library contains a median of 11 missense mutations per gene and the HIV IN and CA datasets have 156 and 135 missense mutations, respectively. To increase our power, we analyzed available data from deep mutational scanning (DMS) studies of four viral proteins: the nucleoprotein (NP) of influenza A/Puerto Rico/8/1934 H1N1 and influenza A/Aichi/2/1968 H3N2, the HA protein from the same strain as our mutants (influenza A/WSN/1933 H1N1), and the HIV envelope (ENV) protein (Bloom 2014; Doud et al. 2015; Doud and Bloom 2016; Haddox et al. 2016). Importantly, these four studies all used the same approach and were performed in the same laboratory.

DMS uses high-throughput mutagenesis to introduce every single amino acid substitution in a given gene followed by deep sequencing to measure the change in frequency of each mutation after passage or selection. The effect of each mutation is often reported as a site preference, which represents the expected proportion of an amino acid at a site if all amino acids at that site were present at equal proportions prior to passaging. We derived a relative site preference from these data by dividing the site preference for each mutant by the site preference for the "wild type" amino acid. We found that relative site preference is a reasonable surrogate for relative fitness, as they are well correlated for mutations in the WSN33 HA gene (Spearman correlation $0.71, \mathrm{p}=2.5 \times 10^{-5}$, Table 1). Our fitness values for WSN33 NP also exhibit a
statistically significant correlation with the DMS data from the closely related PR8 H1N1 strain, but not with the more distant H3N2 strain.

The DMS studies report changes at the amino acid level. Therefore, for each codon in the nucleotide sequence, we asked which amino acid substitutions could only be made by a single transition (Ts-only) and which could only be made by a single transversion (Tv-only). We excluded the amino acid substitutions that were accessible by both transitions and transversions as well as those that required more than one mutation per codon. We then compared the relative site preferences of Ts-only amino acid changes to those of Tv-only using the Fisher threshold strategy. We used an initial threshold of 0.05 rather than 0 , since there are no site preferences of 0 in these datasets, and DMS studies are known to under-sample the lethal fraction. The large sample sizes of the DMS studies (Supplemental Table 3-1) allowed us to use more thresholds (increasing each by 0.05 instead of 0.01 ), thereby identifying Ts-Tv differences in the CDF with greater precision.

We found transversions to be significantly more detrimental than transitions at a subset of relative site preference levels in three of the four DMS datasets (Figure 3-3). In NP (H3N2), transversions tend to be more detrimental than transitions across most of the fitness distribution, but no threshold achieved statistical significance using a Holm-Bonferroni correction (Figure 33A). In NP (H1N1), transversions are significantly more likely to be highly detrimental than transitions (first threshold), and there is a trend for transversions to be more detrimental at higher relative site preferences as well (Figure 3-3A). Contrary to the trend in our smaller influenza study, the Ts-Tv fitness differences are larger and more broadly distributed in genes coding for
the two surface proteins, HA and HIV ENV (Figure 3-3B), as compared to the genes coding for the internal influenza NP proteins. In HA (H1N1), transversions are significantly more detrimental than transitions across most of the fitness distribution. The Ts-Tv difference is especially pronounced in HIV ENV, for which the odds of a transversion being highly detrimental (thresholds from 0.05-0.20) is 2-5 times greater than those of a transition. Across the four datasets, we never found transitions to be significantly more detrimental than transversions, and the odds ratio is rarely below 1 for any of the datasets. Thus, with an improved statistical approach and greater power, we found transitions to be less damaging than transversions in proteins from two viruses.

## Differences in Ts and Tv fitness effects within radical and conservative substitution classes

We next asked why transversions are more detrimental than transitions. The genetic code constrains the type of amino acid substitutions accessible by mutation, and it has been proposed


Figure 3-3 Distribution of Ts and Tv Fitness Effects in Deep Mutational Scanning Datasets
Empirical cumulative distribution functions of transitions (solid line) and transversions (dotted line) in two nucleoprotein (NP) proteins (A, top) and two antigenic surface proteins influenza hemagglutinin (HA) and HIV envelope (ENV) (B, top). Odds ratio estimated by a Fisher test comparing the odds of a transversion versus a transition to be at or below each of 19 fitness thresholds, beginning at a fitness of 0.05 and increasing by 0.05 , for the same datasets (A and B, bottom). Filled circles denote $\mathrm{p}<0.05$ for a two-sided test with Holm-Bonferroni correction. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.
that transversions are more detrimental because they are more likely to cause substitutions that radically alter biochemical properties of the original amino acid. We therefore examined whether the observed fitness differences could be explained by the differences in the accessibility of radical versus conservative amino acid changes by transitions and transversions.

We used the Fisher threshold strategy to test whether radical amino acid changes are more detrimental than conservative changes for three of the most commonly cited biochemical distinctions, which categorize amino acids based on charge, polarity, and polarity and size, (Miyata et al. 1979; Zhang 2000) (see Supplemental Table 3-2). Similar categories have been used in other studies of protein evolution (Epstein 1967; Grantham 1974). Radical amino acid substitutions of all three types are more detrimental than conservative changes in the two NP proteins across much of the fitness distribution (Figure 3-4). Radical changes of polarity (red) and polarity and size (blue) are also more detrimental than conservative changes in the two surface proteins HA (H1N1) and HIV ENV. Radical charge changes (black) have similar effects on fitness as compared to conservative changes in both HA (H1N1) and HIV ENV. Despite this variation in the impact of changes in charge, these simple categories are remarkably predictive of fitness effects across these four proteins.

Transversions may be more detrimental than transitions in these four proteins if they are more likely than transitions to cause a radical amino acid change. As above, we considered amino acid substitutions that could only be made by a single transition (Ts-only) or by a single transversion (Tv-only). Using a Fisher test, we compared the odds that a Tv-only amino acid is radical to the odds that a Ts-only amino acid change is radical as defined by each of the three


Figure 3-4 Distribution of Radical and Conservative Amino Acid Changes
Empirical cumulative distribution functions (CDF) of conservative (solid lines) and radical (dotted lines) amino acid changes in deep mutational scanning datasets of two NP proteins (A, top) and two antigenic surface proteins (B, top). Shown for amino acid changes classified by charge (black), polarity (red), and polarity and size (blue). Odds ratio estimated by a Fisher test comparing the odds of a radical versus a conservative amino acid change to be at or below each of 19 fitness thresholds, beginning at a fitness of 0.05 and increasing in steps of 0.05 , for the same datasets (A and B, bottom). Color scheme is the same as in the CDFs. Filled circles denote p < 0.05 for a two-sided test with Holm-Bonferroni correction. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.
categories above. We considered all possible Tv-only and Ts-only amino acid changes in these four proteins. For all four proteins, the odds of a transversion causing a radical change of any of these three types is significantly greater than the odds of a transition causing a radical change (Table 2). This difference is greatest for amino acid substitutions that affect polarity for all genes.

We next examined whether the fact that transversions are more likely to be radical explains all of the observed differences in Ts-Tv fitness effects in the DMS studies. If the fitness differences can be accounted for by this bias, the differences should be eliminated when comparing both radical Ts to radical Tv and conservative Ts to conservative Tv. Alternatively, if this bias does not account for the difference, one would see a difference in fitness between transitions and transversions among radical or among conservative changes of a given category.

We first compared radical transitions to radical transversions. In NP (H3N2), there are no significant Ts-Tv differences among radical charge (black) or radical polarity and size (blue) changes. However, among radical polarity (red) changes, transversions are more detrimental than transitions-an effect not seen in the overall dataset (Figure 3-3A). In NP (H1N1), radical transversions are more detrimental than radical transitions for all three amino acid classifications at the first threshold (Figure 3-5A). In both NP proteins, the Ts-Tv fitness difference is greater in magnitude among radical polarity changes as compared to the differences among all mutations (the odds ratio is $>3$ in Figure 3-5A but is $\leq 2$ in Figure 3-3A), indicating that controlling for radical transversions can increase rather than eliminate Ts-Tv differences. In HA (H1N1), there are no significant $\mathrm{Ts}-\mathrm{Tv}$ differences among radical charge changes. However, among radical polarity and polarity and size changes, transversions are more detrimental than transitions.


Figure 3-5 Distribution of Radical Ts and Radical Tv
Empirical cumulative distribution functions of radical transitions (solid lines) and radical transversions (dotted lines) in deep mutational scanning datasets of two NP proteins (A, top) and two antigenic surface proteins (B, top). Computed for radical amino acid changes classified by charge (black), polarity (red), and polarity and size (blue). Odds ratio estimated by a Fisher test comparing the odds of a radical transversion versus a radical transition to be at or below each of 19 fitness thresholds, beginning a $t$ a fitness of 0.05 and increasing by 0.05 , for the same datasets (A and B, bottom). Color scheme is the same as in the CDFs. Filled circles denote p < 0.05 for a two-sided test with Holm-Bonferroni correction. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.

Similarly, in HIV ENV, there are no Ts-Tv differences among radical charge changes (Figure 35B). Transversions are more detrimental than transitions among radical polarity and polarity and size changes, although to a lesser degree as compared to overall in Figure 3-3. Thus, even among radical substitutions of three different amino acid categories, transitions tend to be less detrimental than transversions.

We then compared conservative transitions to conservative transversions (Figure 3-6). In both NP proteins, there are no significant Ts-Tv differences among conservative changes of all three amino acid classes (Figure 3-6A). In HA (H1N1), there are no significant Ts-Tv differences among conservative polarity or polarity and size changes. However, transversions are more detrimental than transitions among conservative charge changes. In HIV ENV, transversions are more detrimental than transitions among conservative changes of all three types (Figure 3-6B). Among conservative polarity and size changes, the odds ratio at the second threshold (>6) is


Figure 3-6 Distribution of Conservative Ts and Conservative Tv
Empirical cumulative distribution functions of conservative transitions (solid lines) and conservative transversions (dotted lines) in deep mutational scanning datasets of two NP proteins (A, top) and two antigenic surface proteins (B, top). Computed for conservative amino acid changes classified by charge (black), polarity (red), and polarity and size (blue). Odds ratio estimated by a Fisher test comparing the odds of a conservative transversion versus a conservative transition to be at or below each of 19 fitness thresholds, beginning at a fitness of 0.05 and increasing by 0.05 , for the same datasets ( A and B, bottom). Color scheme is the same as in the CDFs. Filled circles denote p < 05 for a two-sided test with Holm-Bonferroni correction. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.
higher than the odds ratios when comparing all Ts and Tv mutations (Figure 3-3B, <4), indicating that controlling for the conservation of transitions can increase rather than eliminate Ts-Tv differences. However, the Ts-Tv differences are reduced among conservative polarity changes as compared to overall (compare the first thresholds-the odds ratio is $\sim 2$ in Figure 36 B but $\sim 5$ in Figure 3-3B). Thus, conservative transversions are more detrimental than conservative transitions for these three categories in some of the datasets.

In sum, transversions are more detrimental than transitions either among radical or among conservative changes of all three amino acid classes in all four proteins (Table 3). In some cases, Ts-Tv fitness differences were increased when we constrained the analysis to just radical or conservative changes. For NP (H3N2), the constrained analysis revealed a Ts-Tv fitness difference among radical polarity changes that was not observed overall. In other cases, Ts-Tv fitness differences were eliminated or reduced, mostly when constraining the analysis to conservative changes. Thus, these three amino acid categories at best only partially explain the Ts-Tv fitness differences in these proteins, with conservative transitions and transversions generally being more similar in fitness than overall.

## Discussion

We addressed a longstanding question in molecular evolution, whether the observed $\mathrm{Ts}: \mathrm{Tv}$ substitution bias is due to a mutational bias or to selection disfavoring transversions. We found that missense transversions are more detrimental to fitness than transitions in two RNA viruses, influenza and HIV. Our study therefore provides direct support for the selective hypothesis. Furthermore, transversions are more detrimental even when controlling for their
greater likelihood of causing a radical amino acid change. These data demonstrate that commonly used classifications of amino acid changes may not adequately capture the varying selective constraints on different proteins.

The fitness differences between transitions and transversions can be measured in multiple ways and are not well described by a single summary statistic. In four analyzed DMS datasets, the distribution of fitness effects of transversions is shifted toward more deleterious effects. However, they differ at the fitness level at which the shift occurs. We suggest that one explanation for finding a null result is the use of AUC as a summary statistic, which can overweight effects at the ends of the fitness distribution and obscure differences in other regions. In contrast, our use of a Fisher test and large DMS datasets allowed for explicit comparisons of Ts and Tv fitness effects along the distributions without sacrificing power.

Several observations support the idea that the small but significant Ts-Tv fitness differences we identify are biologically relevant and can plausibly explain the $\mathrm{Ts}: \mathrm{Tv}$ substitution bias. First, despite variation in the Ts-Tv fitness differences, transitions are never more detrimental than transversions, and transversions are either similar to transitions or more detrimental (Table 3). This consistent trend suggests that we are identifying a biologically important generality in the effects of transitions and transversions and not simply subtle variations in effects in the highly powered DMS datasets. Second, the Ts-Tv fitness differences in many cases are similar to or even greater than those between radical and conservative amino acid changes. For example, at the low-fitness end of the HIV ENV distribution, the Ts-Tv fitness difference (Figure 3-3) is greater than that between radical and conservative changes of any type
at any fitness level for any gene studied (Figure 3-4). The radical/conservative distinction has widely accepted evolutionary consequences-conservative substitutions occur more often than radical ones in proteins under purifying selection (Epstein 1967; Clarke 1970; Miyata et al. 1979; Eyre-Walker et al. 2000; Zhang 2000; Miller and Kumar 2001; Duda et al. 2002; Popadin et al. 2007). If the fitness differences between radical and conservative changes have consequences for protein evolution, then the similar or greater fitness differences between transversions and transitions are likely to be consequential as well. Finally, the biological relevance of these effects is also supported by our own and other measurements of Ts and Tv mutation rates in several influenza strains (Bloom 2014; Pauly, Procario, et al. 2017). The Ts:Tv mutational bias is 2-3.6, significantly less than the average observed Ts:Tv substitution ratio of 5.24 in influenza (Duchêne et al. 2015). These measured mutational biases demonstrate that the selective and mutational hypotheses for the Ts:Tv substitution bias are not mutually exclusive. An important area for future work will be to determine the relative impact of the transitional mutational and selective biases on the overall Ts:Tv substitution bias, particularly in varying genomic contexts (e.g. coding vs. noncoding regions).

While transversions are more likely to be radical than transitions, this bias only partially accounts for the observed differences in fitness effects. This is perhaps not surprising, as the radical/conservative distinction may not capture the varying constraints on proteins of diverse structure and function. For example, the radical/conservative distinction did not always predict fitness in viral genes. We suggest that the Ts-Tv distinction might be able to better capture these differing functional constraints because transversions are more likely to be radical for a number of different amino acid categories, not just the three analyzed here (Stoltzfus and Norris 2016).

Dozens of amino acid categories and many other metrics, such those provided by Polyphen and SIFT, exist for predicting the fitness effects of amino acid substitutions (Kawashima et al. 2008; Kumar et al. 2009; Stoltzfus and Norris 2016). Any one of our simple categories cannot themselves explain the $\mathrm{Ts}-\mathrm{Tv}$ fitness difference, but their combination, represented in the $\mathrm{Ts}-\mathrm{Tv}$ distinction, can be quite generally predictive of fitness. Therefore, just as the radical/conservative substitution ratio has been used to detect relaxed selection or positive selection (Hughes et al. 1990; Eyre-Walker et al. 2000; Zhang et al. 2002; Pupko et al. 2003; Zhang and Webb 2004; Tennessen 2005; Shen et al. 2009; Wernegreen 2011), our data support the use of the Ts:Tv ratio as an independent, and perhaps more general, test of selection.

We focused on non-synonymous point mutations because the available evidence suggests that these have greater fitness impacts than synonymous or non-coding mutations (Cuevas et al. 2012). Significant fitness effects from synonymous substitutions are more often observed with large scale changes rather than individual mutations; for example, a complete change in the codon usage of a gene (Lauring et al. 2012). Other selective pressures on synonymous or noncoding sequences include regulation of replication and translation (Groeneveld et al. 1995; Klovins et al. 1998), targeting by host RNAses (Klovins et al. 1997), and G+C content and thermostability of RNA structures with various functions (Schultes et al. 1997; Smit et al. 2009; Watts et al. 2009). While it is possible that these selective pressures also contribute to the observed fitness disadvantage of transversions, the main factor is likely the amino acid change.

Our data suggest that the predictive value of the radical/conservative amino acid distinctions may vary due to differing functions of the structural and nonstructural proteins of
viruses. Genes encoding for the surface proteins often have a history of intense frequencydependent selection and may exhibit tolerance to mutations that allow for immune escape while preserving their essential functions of binding and fusion (Stephens and Waelbroeck 1999; Plotkin and Dushoff 2003; Thyagarajan and Bloom 2014; Doud and Bloom 2016; Visher et al. 2016). We therefore expected radical amino acid changes, which may allow for immune escape, to exhibit a less pronounced fitness disadvantage in the surface proteins (HA and ENV) as compared to the internal NP proteins. This is true for charge changes, but not for polarity and polarity and size changes. This observation is also in agreement with two studies of codon usage bias in HA and HIV ENV (Stephens and Waelbroeck 1999; Plotkin and Dushoff 2003). These studies found that, as compared to non-antigenic regions or genes, the antigenic regions exhibit a bias toward codons that tend to mutate non-synonymously, but not toward codons that tend to mutate to radical polarity and size changes. Charge changes were not evaluated. Thus, these genes may be more tolerant of charge changes that allow for immune escape. If correct, one might expect a bias toward codons that preferentially mutate to radical charge changes and that charge changes, rather than polarity and/or size changes, more often lead to escape from host immune pressure.

The observed Ts-Tv fitness differences suggest an evolutionarily-informed approach to improving antiviral strategies. Mutagenic drugs have been used to cause extinction of a variety of viruses in cell culture, a strategy called lethal mutagenesis (Anderson et al. 2004; Bull et al. 2007). There has been little consideration regarding the choice of mutagenic drug, and most commonly employed mutagens cause transitions (Crotty et al. 2001; Ruiz-Jarabo et al. 2003; Graci and Cameron 2008; Dapp et al. 2009). We suggest that the most effective way to achieve
lethal mutagenesis may be by using drugs that increase the rate of the more deleterious transversion mutations. In fact, a previous report from our lab showed that the influenza RNA polymerase makes fewer transversions than transitions (Pauly and Lauring 2015). Additionally, 5-azacytidine, a mutagenic drug that causes transversions, is more effective at reducing viral infectivity than two drugs that cause transitions (Pauly and Lauring 2015). Given our results, we speculate that the same may be true for HIV.

Here we find that despite being broad mutational categories, transitions and transversions can capture functional constraints in very different proteins in two viruses. Although the underlying reason for the relative fitness advantage of transitions likely depends on the structure of the genetic code and the accessibility of different types of amino acids, we have shown that the reason is not as simple as the lower likelihood of a transition causing radical changes of certain broad categories. One possibility is that the codon usage in RNA viruses may have evolved in part to buffer a transitional mutation load (Sanjuán 2010; Lauring et al. 2012) due to their high mutation rates and underlying transitional mutation bias (Drake and Holland 1999; Pauly, Procario, et al. 2017). Identifying the combination of biochemical factors that lead to the fitness advantage of transitions, the relative effects of selection and mutational biases on the overall Ts:Tv substitution bias, and the degree to which these results extend beyond RNA viruses will be important areas of further research.

## Materials and Methods

## Data

All fitness and site preference data were obtained from supplementary material in the published articles or provided by the authors directly. Please see the original papers for details on measurements fitness and site preference (Rihn et al. 2013; Thyagarajan and Bloom 2014; Doud et al. 2015; Rihn et al. 2015; Doud and Bloom 2016; Haddox et al. 2016). To identify transitiononly and transversion-only accessible amino acid substitutions for the mutational scanning data, we obtained the backbone nucleotide sequence of the genes in which the amino acid substitutions were made. These were provided in supplemental files in the published articles for HA (H1N1), NP (H3N2) and HIV ENV. The sequence for NP (H1N1) was obtained from Genbank (Accession number EF467822.1). All sequences can be found online at https://github.com/lauringlab/tstv_paper. For all our analyses, we excluded beneficial mutations, synonymous mutations, and amino acid substitutions accessible by both transitions and transversions or requiring more than one nucleotide mutation.

## AUC Analysis

Our AUC analysis was performed exactly as in Stoltzfus and Norris 2016. An ROC curve plots the true positive rate against the false positive rate of a binary classifier system as the discrimination threshold varies. The AUC is the area under this curve. Consider a hypothetical example in which a fitness value between 0 and 1 serves as a discrimination threshold used to predict whether a mutation is a transition or a transversion. A mutation with a fitness value above the threshold level will be classified as a transition and below the threshold level as a transversion. Thus, the true positive rate is the proportion of transitions above the threshold and the false positive rate is the proportion of transversions above the threshold. If transitions and
transversions do not differ in their fitness effects, the true positive rate will be equal to the false positive rate at all threshold levels and an ROC curve would show a 1:1 line. The AUC in this null case is half of the total ROC plot area, or 0.5 . If transitions generally have a higher fitness than transversions, the true positive rate will be higher than the false positive rate at most threshold levels. The corresponding ROC curve would have a steeper slope than a 1:1 line and have an AUC greater than 0.5. The greater the difference in fitness between transitions and transversions, the greater the difference between the true positive rates and the false positive rates, leading to a steeper ROC curve and a greater AUC. The AUC is mathematically equivalent to the chance that a randomly chosen positive instance of the classifier system is ranked higher than a randomly chosen negative instance (Hanley and McNeil 1982; Mason and Graham 2002). Thus, for our analysis, the AUC is the probability that a randomly chosen transition has a higher fitness value than a randomly chosen transversion. The AUC is calculated from the MannWhitney U test (Hanley and McNeil 1982; Mason and Graham 2002): $A U C=($ pairs statistic)/pairs, where pairs $=$ number of transitions $\times$ number of transversions and statistic is the Mann-Whitney U test statistic comparing the fitness values of transitions and transversions. Statistics were calculated using the wilcox.test() function in R. All p values are for a one-sided Mann-Whitney U test where the alternative hypothesis is that transitions are ranked higher than transversions.

## Empirical CDF and Odds Ratios

Empirical CDF were computed using the ggplot2 stat_ecdf function in R. Odds ratios were estimated by Fisher's exact test using the fisher.test() function in R. When the odds ratio was calculated as infinite (e.g. when transversions fall below a relative fitness threshold but no transitions fall below the threshold), the estimated lower 95\% confidence interval of the odds
ratio was plotted. All p values are for a two-sided test. Holm-Bonferroni correction was implemented when comparisons were performed at multiple fitness level thresholds for a given dataset.

## Availability of Computer Code and Data

$R$ version 3.3.2 was used for all data analysis and to create all figures. Scripts and data are available online at https://github.com/lauringlab/tstv_paper as are all plotted data along with unadjusted p values for all figures.

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## Supplemental Figures and Tables



Supplemental Figure 3-1 Differences in Ts and Tv Fitness Effects as measured by AUC using Decreasing Thresholds
Ts-Tv fitness differences as measured by AUC among mutations at or below successively lower fitness thresholds in our influenza datasets (top) and the HIV datasets (bottom). Thresholds decrease by a fitness of 0.1 , starting at 1 and ending at 0.1 . Filled circles denote $p<0.05$ for a one-sided Mann-Whitney $U$ test where the alternative is transitions are more fit. Lines shown to clarify trends only. Plotted data and raw p-values can be found at https://github.com/lauringlab/tstv_paper.

Supplemental Table 3-1 Sample size of datasets

| Dataset | $\mathrm{Ts}^{\mathrm{a}}$ | $\mathrm{Tv}^{\mathrm{b}}$ | Total |
| :--- | :---: | :---: | :---: |
| HIV Combined | 143 | 138 | 281 |
| HIV IN | 73 | 73 | 146 |
| HIV CA | 70 | 65 | 135 |
| Influenza Total | 23 | 72 | 95 |
| Influenza Internal | 14 | 39 | 53 |
| TEV | 20 | 27 | 47 |
| F1 | 16 | 28 | 44 |
| Influenza Surface | 9 | 33 | 42 |
| VSV | 7 | 24 | 31 |
| Qß | 2 | 27 | 29 |
| $\phi$ X174 | 3 | 18 | 21 |
| HA (H1N1) | 934 | 2064 | 2998 |
| NP (H1N1) | 878 | 1870 | 2748 |
| NP (H3N2) | 849 | 1833 | 2682 |
| HIV ENV | 684 | 1794 | 2478 |

[^0]Supplemental Table 3-2 Amino Acid classifications

| CHARGE |  |
| :--- | :--- |
| negative | $\mathrm{D}, \mathrm{E}$ |
| neutral | $\mathrm{A}, \mathrm{P}, \mathrm{G}, \mathrm{S}, \mathrm{T}, \mathrm{F}, \mathrm{W}, \mathrm{Y}, \mathrm{I}, \mathrm{L}, \mathrm{M}, \mathrm{V}, \mathrm{N}, \mathrm{Q}, \mathrm{C}$ |
| positive | $\mathrm{R}, \mathrm{H}, \mathrm{K}$ |, | POLARITY |  |
| :--- | :--- |
| nonpolar | $\mathrm{A}, \mathrm{P}, \mathrm{F}, \mathrm{W}, \mathrm{I}, \mathrm{L}, \mathrm{M}, \mathrm{V}$ |
| polar | $\mathrm{G}, \mathrm{S}, \mathrm{T}, \mathrm{Y}, \mathrm{R}, \mathrm{H}, \mathrm{K}, \mathrm{D}, \mathrm{E}, \mathrm{N}, \mathrm{Q}, \mathrm{C}$ |
| POLARITY \& SIZE |  |
| neutral \& small | $\mathrm{A}, \mathrm{P}, \mathrm{G}, \mathrm{S}, \mathrm{T}$ |
| nonpolar \& large | $\mathrm{F}, \mathrm{W}, \mathrm{Y}$ |
| nonpolar \& small | $\mathrm{I}, \mathrm{L}, \mathrm{M}, \mathrm{V}$ |
| polar \& large | $\mathrm{R}, \mathrm{H}, \mathrm{K}$ |
| polar \& small | $\mathrm{D}, \mathrm{E}, \mathrm{N}, \mathrm{Q}$ |
| special | C |

## Chapter 4 The Best Substitutions are also the Worst and Hardest to Make


#### Abstract

Understanding the evolutionary constraints on proteins and the properties of mutations and genes responsible for adaptive changes are major goals in molecular evolution. Many such studies have assumed that amino acid classifications based on simple biochemical properties can capture differences in fitness effects between substitutions that radically versus conservatively change these biochemical properties. For example, like the non-synonymous to synonymous substitution ratio, the ratio of radical to conservative substitutions has been used to detect positive selection. Similarly, studies examining whether adaptation proceeds by large or small steps have assumed that these radical/conservative distinctions reflect mutational effect size. However, there is some doubt as to the extent to which radical/conservative distinctions are predictive of fitness effects. Phylogenetic evidence that radical substitutions are more deleterious may instead reflect mutational biases or the structure of the genetic code. Here, using deep mutational scanning studies of several RNA viruses, we show that common radical/conservative classifications are in fact predictive of fitness differences. Interestingly, radical substitutions are both more detrimental and more beneficial, when beneficial. These same patterns hold for multi-nucleotide codon mutations, which are more likely to cause a radical substitutions, as compared to singlenucleotide mutations. Thus, our results validate the use of radical/conservative classifications in the study of protein evolution and support the hypothesis that the structure of the genetic code evolved to minimize errors.


## Introduction

Decades of work in molecular evolution have assumed that radical versus conservative changes in the biochemical properties of amino acids correspond to their fitness effects. In the 1960's Woese and Crick proposed that the genetic code evolved to minimize the detrimental effect of single nucleotide mutations because more similar amino acids (in terms of polarity or other properties) have more similar codons (Woese 1965; Woese et al. 1966; Crick 1968). Studies on how protein evolution is shaped by purifying selection make the same assumption that substitutions between amino acids that are more similar in biochemical properties have less detrimental fitness effects (Epstein 1967; Clarke 1970; Miyata et al. 1979; Eyre-Walker et al. 2000; Zhang 2000; Miller and Kumar 2001; Duda et al. 2002; Popadin et al. 2007; Chen, Lan, et al. 2019).

Radical/conservative amino acid classifications have also been important in the study of adaptive evolution. For example, does adaptive evolution proceed through small or large steps? A number of conflicting conclusions on this question at the molecular level have arisen (Hughes et al. 2000; Rand et al. 2000; Bergman and Eyre-Walker 2019; Chen, He, et al. 2019; Chen, Lan, et al. 2019). Such studies have assumed that simple radical/conservative classifications capture true differences in the size of phenotypic and fitness effects. Like the ratio of non-synonymous to synonymous substitutions ( $\mathrm{ns} / \mathrm{s}$ ), the ratio of radical to conservative substitutions has been used to detect positive selection (Hughes et al. 1990; Eyre-Walker et al. 2000; Hughes et al. 2000; Zhang et al. 2002; Pupko et al. 2003; Zhang and Webb 2004; Tennessen 2005; Gojobori et al. 2007; Shen et al. 2009; Wernegreen 2011). Possibly the first example is Nei and colleagues’ detection of positive selection at MHC antigen-binding loci, helping explain the maintenance of
polymorphisms due to host-pathogen coevolution (Hughes et al. 1990). Additionally, the ns/s ratio is unreliable when synonymous substitutions are saturated, making the radical/conservative substitution ratio particularly useful for investigating selection in highly diverged sequences (Hanada et al. 2007).

Despite their widespread use, there is some doubt about the extent to which radical/conservative distinctions are predictive of fitness effects. Radical substitutions occur less often during protein evolution than radical ones, supporting the idea that they are more detrimental (Epstein 1967; Clarke 1970; Grantham 1974; Miyata et al. 1979; Zhang 2000). However, this bias may simply reflect the structure of the genetic code or mutational biases, rather than selection (Dagan et al. 2002; Yampolsky and Stoltzfus 2005). There is widespread evidence of a mutational bias towards transitions (Zhang and Gerstein 2003; Jiang and Zhao 2006; Baer et al. 2007; Denver et al. 2009; Pauly et al. 2017), and transitions are more likely to cause conservative substitutions (Vogel and Kopun 1977; Miyata et al. 1979; Zhang 2000). The assumption that radical substitutions are more highly beneficial also requires validation - evidence of positive selection for radical substitutions can be affected by mutational or codon usage biases (Dagan et al. 2002).

With the advent of high-throughput mutation screens, it now possible to directly test the assumptions underlying the use of radical/conservative distinctions. Recently, we showed that radical substitutions are more detrimental than conservative ones in several proteins of two RNA viruses. Here, using three of the most commonly used radical/conservative classifications, we extend this analysis to additional proteins, and viral strains and species, and we test the additional assumptions about the beneficial effects of radical substitutions. We find that radical
substitutions are more likely to be detrimental and more highly detrimental, yet are also more highly beneficial. Furthermore, we provide direct evidence that the structure of the genetic code minimizes detrimental effects, albeit with a tradeoff with the size of beneficial effects.

Substitutions requiring two or more nucleotide mutations are both more detrimental and more highly beneficial.

## Results

## Mutational fitness effects in RNA viruses

To directly test whether radical/conservative amino acid distinctions are predictive of fitness differences, a large dataset of mutational fitness effects with no biases towards the type of mutations included is crucial. Recent deep mutational scanning (DMS) studies of RNA viruses from the Bloom lab meet this requirement. These studies introduce every single amino acid substitution in a given gene followed by deep sequencing to measure the change in frequency of each substitution after selection. We curated ten DMS datasets of various strains of three RNA viruses, Influenza A, Zika, and HIV-1 (Doud et al. 2015; Doud and Bloom 2016; Haddox et al. 2016; Haddox et al. 2018; Lee et al. 2018; Soh et al. 2019; Sourisseau et al. 2019: 19). Fitness was usually reported as amino acid preference which we transformed to a proxy for relative fitness, relative preference, by dividing by the wild-type amino acid preference (Bloom 2015; Lyons and Lauring 2017). Relative preference correlates well with relative fitness measured in lower-throughput experiments (Visher et al. 2016; Lyons and Lauring 2017). We then transformed relative preference to fitness effect by taking the log of the relative preference values as in (Soh et al. 2019). Basic information about the ten datasets are in Table 4-1 with more details in Supplemental Tables 4-1 thru 4-6.

Table 4-1 Viral DMS Datasets

| Species | Strain | Gene | Total Mutations | Avg. Deleterious Effect | Avg. Beneficial Effect |
| :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | 12578 | -1.546 | 0.304 |
|  | BG505 | ENV | 12711 | -2.01 | 0.408 |
|  | LAI | ENV | 13540 | -1.828 | 0.904 |
| Influenza A virus | $\begin{gathered} \text { A/PR8/1934 } \\ \text { (H1N1) } \end{gathered}$ | NP | 9462 | -4.065 | 0.726 |
|  | $\begin{gathered} \text { A/Aichi/2/196 } \\ 8 \text { (H3N2) } \end{gathered}$ | NP | 9462 | -3.278 | 0.732 |
|  | A/WSN/1933 <br> (H1N1) | HA | 10716 | -3.191 | 0.55 |
|  | $\begin{aligned} & \text { A/Perth/16/20 } \\ & 09 \text { (H3N2) } \end{aligned}$ | HA | 10755 | -2.474 | 0.525 |
|  | A/Greenwinged Teal/Ohio/175 /1986 (Avian) | PB2 | 14421 | -2.705 | 0.467 |
|  | A/Greenwinged Teal/Ohio/175 /1986 (Avian) | PB2 | 14421 | -2.432 | 0.47 |
| Zika virus | MR766 | ENV | 9576 | -4.31 | 0.829 |

## Radical amino acid substitutions are more frequently and more highly detrimental than

## conservative ones

We classified amino acids according to their charge, polarity, or polarity and size (polarity-size) as in (Miyata et al. 1979; Zhang 2000; Lyons and Lauring 2017). Radical amino acid substitutions are substitutions between amino acids with different classes (e.g. from a negative to a positively charged amino acid) while conservative substitutions are those between amino acids in the same category. We hypothesized that radical substitutions are more detrimental than conservative ones, in terms of the likelihood they are detrimental and their effect size.

For each of the ten DMS datasets, we first calculated the percent of radical or conservative substitutions that are detrimental and plotted the difference in this percentage (radical minus


Figure 4-1. Difference in percent detrimental between radical and conservative substitutions.

Difference is calculated as the percentage of radical charge, polarity, or polarity and size changes that were detrimental minus that for conservative changes. Colors correspond to different datasets as in Figure S-1
conservative) (Figure 4-1). Radical substitutions were more likely to be detrimental than conservative ones in 27 of 30 comparisons (ten datasets across the three classifications) (Figure 41). Considering the average across datasets, the percentage that are detrimental for radical substitutions is significantly greater than that for conservative ones based on polarity and polaritysize ( $\mathrm{p}<.05, \mathrm{t}$-test) and trends greater for charge.

We determined whether radical substitutions are more highly detrimental than conservative substitutions by comparing the detrimental mutational effects for each type of substitution in each dataset. Figure 4-2A shows the difference in average detrimental effect (Table 4-S3) between radical and conservative substitutions for all datasets for the three amino acid classifications. Radical substitutions were more detrimental for 28 out of 30 comparisons and significantly so for each of the ten datasets for polarity and polarity-size, and for six of the ten datasets for charge ( $\mathrm{p}<.05$, t -test). Additionally, radical substitutions were significantly less detrimental than conservative ones for only one dataset and only for charge.

To see whether the difference in detrimental effect sizes between radical and conservative substitutions are substantial biologically, we calculated this difference as a percentage of the overall average detrimental effect size. This was done for the 28 comparisons in which radical substitutions were more detrimental. The differences were quite large, representing on average from 10-25\% of the overall average detrimental effect (Figure 4-2B). In other words, the difference in effect size between radical and conservative substitutions is $10-25 \%$ of the entire effect size of an average detrimental mutation.

Notably, the polarity-size classification was the most predictive of both the likelihood a radical substitution would be detrimental and its detrimental effect size, whereas charge was the least predictive.


Figure 4-2 Differences in mutational effects between radical and conservative substitutions.
Differences in average mutational effects were calculated as the average effect of radical substitutions minus that for conservative substitutions for each dataset in each amino acid classification, conditional on being detrimental (A) or beneficial (C). The difference in effects between radical and conservative amino acids as a percentage of the overall average effect size for detrimental (B) or beneficial (B) substitutions.

## Radical amino acid substitutions are more highly beneficial than conservative ones

To test the common assumption that radical substitutions are more beneficial, conditional on being beneficial, we compared the mutational effects of radical versus conservative beneficial mutations in each dataset. Figure 4-2C shows the difference in average beneficial effect (Table 4-S5) between radical and conservative substitutions for all datasets for the three amino acid classifications. Radical substitutions were more beneficial than conservative ones in 25 out 30 comparisons and significantly more beneficial for six and three out of ten datasets for charge and polarity-size, respectively ( $\mathrm{p}<.05$, t-test). The differences in beneficial effect sizes were quite large, representing on average from 5-20\% of the effect size of an average beneficial mutation (Figure 4-2D). Finally, conservative substitutions were never significantly more beneficial than radical ones.

Non-synonymous multi-nucleotide mutations recapitulate findings for radical amino acid substitutions

Due to the structure of the genetic code, single nucleotide mutations are more likely to cause a conservative amino acid substitutions than a radical one. Given our results on radical/conservative mutational effects, we hypothesized that amino acid substitutions requiring two or three nucleotide mutations are more likely to be detrimental and more highly detrimental, but more beneficial when beneficial.

We classified amino acid substitutions as requiring only one, two, or three nucleotide mutations based on the standard genetic code. We then performed the same analyses as for radical/conservative substitutions, but comparing multi-nucleotide (MTN) to single nucleotide (SN) codon changes.

Both two- and three-MTN changes were more likely to be detrimental than SN changes for all but one dataset in the two-MTN class (Figure 4-3). Considering the average across datasets, the percentage that was detrimental was significantly greater for all classes of MTN changes than for SN changes ( $\mathrm{p}<.05$, t-test). MTN changes were also significantly more detrimental than SN changes for all datasets and all MTN classes ( $\mathrm{p}<.05, \mathrm{t}$-test) (Figure 4-4A). The differences in detrimental effect sizes represented on average from 10-15\% of the effect size of an average detrimental


Figure 4-3 Difference in percent detrimental between MTN and SN substitutions.

Difference is calculated as the percentage of substitutions that were detrimental among those requiring at minimum 2 or 3 MTN mutations minus that for substitutions requiring only one nucleotide mutation. mutation (Figure 4-4B, Table 4-S4).

MTN changes were also more beneficial than SN changes, conditional on being beneficial, for 15 of 20 comparisons ( 10 datasets across two or three MTN changes) (Figure 4-4C, Table 4-S6). This was significant for only one dataset for two- and three-MTN changes, but SN changes were never significantly more beneficial than MTN changes ( $\mathrm{p}<.05$, t -test). The differences in

## beneficial effect sizes (when MTN was more beneficial than SN) represented on average from 5-

$10 \%$ of the effect size of an average beneficial mutation (Figure 4-4D).


Figure 4-4 Differences in mutational effects between MTN and SN substitutions.
Differences in average mutational effects were calculated as the average effect of substitutions requiring at minimum 2 or 3 MTN mutations minus that for substitutions requiring only one nucleotide mutation, conditional on being detrimental (A) or beneficial (C). The difference in effects between MTN and SN substitutions as a percentage of the overall average effect size for detrimental (B) or beneficial (B) substitutions.

## Discussion

Here, we used experimental data to verify the long assumed fitness differences between radical and conservative substitutions for three commonly used classifications across a variety of genes in three viral species. Radical substitutions are more likely to be detrimental and more detrimental, but also more beneficial, than conservative substitutions. Multi-nucleotide codon changes, which are more likely to be radical, show the same pattern as compared to singlenucleotide codon changes.

It is difficult to know whether the fitness differences we detect are large enough to impact substitutions rates, but one line of reasoning suggests so. The effective population size is estimated at 500 for influenza virus in the human population and 1000 for the intra-host HIV-1 population (Rouzine and Coffin 1999; Kouyos et al. 2006; Bedford et al. 2011). Thus, the threshold fitness effect for a mutation that is more governed by selection than drift $(1 / \mathrm{Ne})$ is approximately . 002 (1/500), using the lower Ne estimate. Given an average mutational effect size of .2 for viable mutations across the influenza genome (Visher et. al., 2016), a 1\% effect size difference would make the difference between a neutrally evolving conservative mutation and a negatively (or positively) selected radical mutation. On average, the differences we observe are 5-25 times greater than this difference. Of course, this reasoning considers only the situation when the conservative mutation is nearly neutral, but not the situation when they are both detrimental or beneficial. Simulations using the determined mutational biases in these viruses could be used to further predict the consequences of these fitness differences and compare to phylogenetic data.

These viral DMS datasets are ideal for studying radical versus conservative and MTN vs SN changes because they measure fitness effects for all 19 amino acid substitutions at each position. Expanding this analysis to genes from other taxa would be helpful; however, many datasets do not contain all possible amino acid substitutions. For example, a recent GFP dataset only contains about 6 amino acid substitutions per position and no substitutions that require three nucleotide changes (data not shown) (Sarkisyan et al. 2016). Whether the included substitutions are random or not is unclear and bias against some substitutions due to low fitness would make interpretation challenging. Thus, more empirical work is needed in other taxa.

Our results support the use of radical/conservative distinctions in positive selection (Hughes et al. 1990; Eyre-Walker et al. 2000; Hughes et al. 2000; Zhang et al. 2002; Pupko et al. 2003; Zhang and Webb 2004; Tennessen 2005; Gojobori et al. 2007; Shen et al. 2009; Wernegreen 2011). Future work could analyze more radical/conservative classifications to identify the best ones for detecting positive selection. The results of one of the most widely used tests for positive selection, the branch-site test (Zhang et al. 2005), have recently come under scrutiny because it assumes that MTN codon changes are due to successive single substitutions. Instead, MTN codon changes may be due to a bias in polymerases to cause simultaneous multiple mutations in nearby sites. This mutational bias has been observed in taxa from yeast to humans (Schrider et al. 2011). One study has found that the positive signals from this test can be almost completely explained by this mutational bias (Venkat et al. 2018). On the other hand, a recent phylogenetic analysis suggest that multiple substitutions within a codon are enriched compared to multiple substitutions straddling two adjacent codons (Zhengting Zou, personal correspondence). This suggests positive selection for MTN codon changes even in the setting of simultaneous multiple
nucleotide mutations. Our data that MTN codon changes are more beneficial than SN changes further support this hypothesis.

The long-standing debate between saltationism versus gradualism has a corollary at the molecular level in terms of whether adaptive evolution proceeds through small, i.e. conservative, or large, radical, steps (Bell 2009). Fisher's geometric theory (FGM) supposes that most beneficial mutations must be of small effect in order to minimize pleiotropic detrimental effects (Tenaillon 2014). Under FGM, more radical changes have pleiotropic tradeoffs which diminish both their chance of being beneficial and their beneficial effect size. We find that radical substitutions are indeed less likely to be beneficial, but contrary to FGM, they are also the most beneficial compared to conservative substitutions. Thus, the largest improvements in fitness might require large phenotypic changes, such as those from radical substitutions. Furthermore, adaptive evolution may be biased towards higher effect mutations because they have a higher probability of fixation (Kimura 1983). Conflicting conclusions have been made as to how these factors play out during adaptive evolution (Hughes et al. 2000; Rand et al. 2000; Bergman and Eyre-Walker 2019; Chen, He, et al. 2019; Chen, Lan, et al. 2019). A possible resolution to the debate is our finding that while radical substitutions are more beneficial, they are less frequently beneficial and more detrimental. This pattern may lead to different conclusions depending on how negative selection is controlled for and whether the question is about the relative frequency or importance of large versus small steps (Chen, He, et al. 2019).

In new or more stressful environments where wildtype fitness is lower, the supply and effect size of beneficial mutations are often higher (Bell 2009). It is hypothesized that radical phenotypic
changes may be more necessary for fitness improvement, as the fitness peak may lie in very different phenotypic region. Thus, adaptive evolution may proceed by larger steps in this circumstance. Indeed, radical amino acid substitutions are enriched in cases of environmental stress (Luo et al. 2017; Xu et al. 2017). DMS studies of viral strains under the stress of drugs, antibodies, or new cell types could be used to experimentally test the prediction that radical substitutions are less detrimental and even more beneficial under such environmental stresses. Moreover, such analyses could help identify the types of mutations important in the evolution of drug or immune resistance and host-switching, with implications for public health.

Interestingly, comparison between experimental data and previous phylogenetic results on radical/conservative differences may reveal biological differences in protein constraints or selection pressures across taxa and genes. For example, in mammals, radical versus conservative charge changes showed the largest differences in substitutions rates among the three types of radical changes (Zhang 2000). However, in the viral datasets, radical versus conservative changes in charge show the least differences in detrimental fitness differences. Insensitivity to radical charge changes seems to be most pronounced among the antigenic surface proteins HA and ENV compared to the internal NP protein. These proteins have a long history of immune selection and have evolved robustness to changes that allow for immune escape (Stephens and Waelbroeck 1999; Plotkin and Dushoff 2003; Thyagarajan and Bloom 2014; Doud and Bloom 2016; Visher et al. 2016). Thus, differences from mammalian genes may reflect the antigenic role of these viral genes. It is possible such differences are also reflected in phylogenetic patterns, and monitoring viral populations for charge substitutions may improve predictions of vaccine escape.

Selection for error minimization is a major hypothesis for the evolution of the genetic code, but has relied on the assumption that radical substitutions are more detrimental (Woese 1965; Woese et al. 1966; Crick 1968; Haig and Hurst 1991; Freeland and Hurst 1998; Geyer and Mamlouk 2018; Tripathi and Deem 2018). Our results provide direct evidence that the genetic code minimizes the detrimental effects of single-nucleotide changes. Interestingly, this comes with a greater likelihood of mutations being beneficial, but a tradeoff in terms of the size of beneficial effects. How might these factors enhance or impede adaptive evolution? Has the genetic code traded evolvability for robustness? Whatever the origin of the genetic code, its structure and the properties of amino acids lead to the pattern that the best substitutions are also the worst and hardest to make.

## Methods

## Data

All amino acid preference data were obtained from supplementary material in the published articles. Please see the original papers for details on measurements of amino acid preference. For all of our analyses, we excluded synonymous mutations.

## Statistical Analyses

All $P$ values are for a two-sided t -test using the t.test() function in R. All statistical tests compared radical/MTN or SN/conservative substitutions within each individual dataset, with the exception of the percent detrimental. The percent of radical/MTN or SN/conservative substitutions that were detrimental was calculated for each dataset and the results were then pooled for the statistical test.

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## Supplemental Figures \& Tables

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            HIV-1, BF520, ENV
            HIV-1, BG505, ENV
-HIV-1, LAI, ENV
- Zika virus, MR766, ENV
- Influenza A virus, A/Perth/16/2009 (H3N2), HA
- Influenza A virus, AWSN/1933 (H1N1), HA
- Influenza A virus, A/Aichi/2/1968 (H3N2),NP
- Influenza A virus, A/PR8/1934 (H1N1), NP
    Influenza A virus, A/Green-winged Teal/Ohio/175/1986 (Avian), PB2
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Supplemental Table 4-1 Numbers of radical/conservative detrimental and beneficial substitutions

| Species | Strain | Gene | Overall | Con. Charge | Radical Charge | Con. Polarity | Radical <br> Polarity |  | Radic <br> Polar <br> \& Si |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | 12578 | $\begin{gathered} 6811, \\ 843 \end{gathered}$ | $\begin{gathered} 4319, \\ 605 \end{gathered}$ | $\begin{gathered} 5438, \\ 780 \end{gathered}$ | $\begin{gathered} 5692, \\ 668 \end{gathered}$ | $\begin{gathered} 1700, \\ 286 \end{gathered}$ | $\begin{aligned} & 9431 \\ & 116 \end{aligned}$ |
|  | BG505 | ENV | 12711 | $6599,$ | $\begin{gathered} 4180, \\ 817 \end{gathered}$ | $\begin{aligned} & 5198, \\ & 1101 \end{aligned}$ | $\begin{gathered} 5581, \\ 831 \end{gathered}$ | $\begin{gathered} 1591, \\ 422 \end{gathered}$ | $918$ |
|  | LAI | ENV | 13540 | $\begin{aligned} & 5757, \\ & 2105 \end{aligned}$ | $\begin{aligned} & 4193, \\ & 1485 \end{aligned}$ | $\begin{aligned} & 4415, \\ & 1948 \end{aligned}$ | $\begin{aligned} & 5535, \\ & 1642 \end{aligned}$ | $\begin{gathered} 1332, \\ 715 \end{gathered}$ | $\begin{gathered} 861 \\ 287 \end{gathered}$ |
| Influenza A virus | $\begin{gathered} \text { A/PR8/ } \\ \text { 1934 } \\ \text { (H1N1) } \end{gathered}$ | NP | 9462 | $\begin{gathered} 5170, \\ 136 \end{gathered}$ | 4088, 68 | $\begin{gathered} 4616, \\ 114 \end{gathered}$ | 4642, 90 | 1472, 53 | $\begin{gathered} 778! \\ 151 \end{gathered}$ |
|  | A/Aichi <br> /2/196 <br> 8 <br> (H3N2) | NP | 9462 | $\begin{gathered} 5039, \\ 241 \end{gathered}$ | $\begin{gathered} 4022, \\ 160 \end{gathered}$ | $\begin{gathered} 4492, \\ 230 \end{gathered}$ | $\begin{gathered} 4569, \\ 171 \end{gathered}$ | $\begin{gathered} 1421, \\ 104 \end{gathered}$ | $\begin{array}{r} 7641 \\ 29 \end{array}$ |
|  | $\begin{aligned} & \text { A/WSN } \\ & \text { /1933 } \\ & \text { (H1N1) } \end{aligned}$ | HA | 10716 | $\begin{gathered} 5948, \\ 353 \end{gathered}$ | $\begin{gathered} 4174, \\ 241 \end{gathered}$ | $\begin{gathered} 5042, \\ 334 \end{gathered}$ | $\begin{gathered} 5080, \\ 260 \end{gathered}$ | $\begin{gathered} 1536, \\ 156 \end{gathered}$ | $\begin{gathered} 858! \\ 438 \end{gathered}$ |
|  | $\begin{gathered} \text { A/Perth } \\ \text { /16/20 } \\ 09 \\ \text { (H3N2) } \end{gathered}$ | HA | 10755 | $\begin{gathered} 5850, \\ 432 \end{gathered}$ | $\begin{gathered} 4151, \\ 321 \end{gathered}$ | $\begin{gathered} 4987, \\ 391 \end{gathered}$ | $\begin{gathered} 5014, \\ 362 \end{gathered}$ | $\begin{gathered} 1523, \\ 160 \end{gathered}$ | $\begin{array}{r} 8478 \\ 59 \end{array}$ |
|  | A/Gree $n-$ winged Teal/Oh io/175/ 1986 (Avian) | PB2 | 14421 | $\begin{gathered} 7536, \\ 579 \end{gathered}$ | $\begin{gathered} 5879, \\ 427 \end{gathered}$ | $\begin{gathered} 6531, \\ 554 \end{gathered}$ | $\begin{gathered} 6884, \\ 452 \end{gathered}$ | $\begin{gathered} 2103, \\ 221 \end{gathered}$ | $\begin{array}{r} 1131 \\ 785 \end{array}$ |
|  | A/Gree n- winged Teal/Oh io/175/ 1986 (Avian) | PB2 | 14421 | $\begin{gathered} 7601, \\ 514 \end{gathered}$ | $\begin{gathered} 5952, \\ 354 \end{gathered}$ | $\begin{gathered} 6601, \\ 484 \end{gathered}$ | $\begin{gathered} 6952, \\ 384 \end{gathered}$ | $\begin{gathered} 2128, \\ 196 \end{gathered}$ | $\begin{array}{r} 1142 \\ 672 \end{array}$ |
| Zika virus | MR766 | ENV | 9576 | $\begin{gathered} 5393, \\ 244 \end{gathered}$ | $\begin{gathered} 3832, \\ 107 \end{gathered}$ | $\begin{gathered} 4520, \\ 208 \end{gathered}$ | $\begin{gathered} 4705, \\ 143 \end{gathered}$ | $\begin{gathered} 1449, \\ 106 \end{gathered}$ | $\begin{array}{r} 7775 \\ 245 \end{array}$ |

Supplemental Table 4-2 Numbers of SN and MTN detrimental and beneficial substitutions

| Species | Strain | Gene | Overall | SN | 2 MTN | 3 MTN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | $\begin{gathered} 4619, \\ 577 \end{gathered}$ | $\begin{gathered} 5912, \\ 797 \end{gathered}$ | 599, 74 | $\begin{gathered} 4619, \\ 577 \end{gathered}$ |
|  | BG505 | ENV | $\begin{gathered} 4404, \\ 881 \end{gathered}$ | $\begin{gathered} 5775, \\ 973 \end{gathered}$ | 600, 78 | $\begin{gathered} 4404 \\ 881 \end{gathered}$ |
|  | LAI | ENV | $\begin{aligned} & 3935, \\ & 1742 \end{aligned}$ | $\begin{aligned} & 5469, \\ & 1693 \end{aligned}$ | $\begin{aligned} & 546, \\ & 155 \end{aligned}$ | $\begin{aligned} & 3935, \\ & 1742 \end{aligned}$ |
| Influenza A virus | A/PR8/1934 (H1N1) | NP | $\begin{gathered} 3936, \\ 101 \end{gathered}$ | $\begin{gathered} 4844, \\ 98 \end{gathered}$ | 478, 5 | $\begin{gathered} 3936 \\ 101 \end{gathered}$ |
|  | A/Aichi/2/1968 (H3N2) | NP | $\begin{gathered} 3836, \\ 189 \end{gathered}$ | $\begin{gathered} 4757, \\ 190 \end{gathered}$ | 468, 22 | $\begin{gathered} 3836, \\ 189 \end{gathered}$ |
|  | A/WSN/1933 (H1N1) | HA | $\begin{gathered} 4183, \\ 295 \end{gathered}$ | $\begin{gathered} 5400, \\ 283 \end{gathered}$ | 539,16 | $\begin{gathered} 4183, \\ 295 \end{gathered}$ |
|  | A/Perth/16/2009 (H3N2) | HA | 4129, | $\begin{gathered} 5317, \\ 355 \end{gathered}$ | 556, 34 | $4129 \text {, }$ |
|  | A/Green-winged Teal/Ohio/175/1986 (Avian) | PB2 | $\begin{gathered} 5664, \\ 480 \end{gathered}$ | $\begin{gathered} 7085, \\ 475 \end{gathered}$ | 666, 51 | $\begin{gathered} 5664, \\ 480 \end{gathered}$ |
|  | A/Green-winged Teal/Ohio/175/1986 (Avian) | PB2 | $\begin{gathered} 5758, \\ 386 \end{gathered}$ | $\begin{gathered} 7120, \\ 440 \end{gathered}$ | 675, 42 | $\begin{gathered} 5758 \\ 386 \end{gathered}$ |
| Zika virus | MR766 | ENV | $\begin{gathered} 3764, \\ 221 \end{gathered}$ | $\begin{gathered} 4985 \\ 121 \end{gathered}$ | 476, 9 | $\begin{gathered} 3764, \\ 221 \end{gathered}$ |

Supplemental Table 4-3 Average detrimental effects of radical/conservative substitutions

| Species | Strain | Gene | Overall | Con. Charge | Radical Charge | Con. Polarity | Radical Polarity | Con. <br> Polarity <br> \& Size | Radic <br> Polar <br> \& Si |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | -1.546 | -2.008 | -1.846 | -2.087 | -2.162 | -2.012 | -1.5 |
|  | BG505 | ENV | -2.01 | -1.569 | -1.435 | -1.591 | -1.651 | -1.509 | -1.25 |
|  | LAI | ENV | -1.828 | -1.751 | -1.627 | -1.895 | -1.989 | -1.934 | -1.35 |
| Influenza A virus | $\begin{gathered} \text { A/PR8/ } \\ \text { 1934 } \\ \text { (H1N1) } \end{gathered}$ | NP | -4.065 | -3.832 | -3.926 | -4.215 | -4.204 | -4.36 | -3.2i |
|  | $\begin{gathered} \text { A/Aichi } \\ \text { /2/196 } \\ 8 \\ \text { (H3N2) } \end{gathered}$ | NP | -3.278 | -3.073 | -3.21 | -3.375 | -3.345 | -3.535 | -2.75 |
|  | $\begin{aligned} & \text { A/WSN } \\ & \text { /1933 } \\ & \text { (H1N1) } \end{aligned}$ | HA | -3.191 | -3.215 | -2.989 | -3.3 | -3.391 | -3.157 | -2.5i |
|  | $\begin{gathered} \text { A/Perth } \\ \text { /16/20 } \\ 09 \\ \text { (H3N2) } \end{gathered}$ | HA | -2.474 | -2.467 | $-2.346$ | -2.552 | -2.601 | -2.484 | -2.0 ミ |
|  | A/Gree n- winged Teal/Oh io/175/ 1986 (Avian) | PB2 | $-2.705$ | -2.606 | -2.555 | -2.799 | -2.848 | -2.832 | -2.2C |
|  | A/Gree n - winged Teal/Oh io/175/ 1986 (Avian) | PB2 | -2.432 | -2.308 | -2.301 | -2.526 | $-2.557$ | -2.592 | -1.92 |
| Zika virus | MR766 | ENV | -4.31 | -4.199 | -4.117 | -4.438 | -4.494 | -4.466 | -3.62 |

Supplemental Table 4-4 Average Detrimental Effects of SN and MTN Substitutions

| Species | Strain | Gene | Overall | SN | 2 MTN | 3 MTN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | -1.546 | -1.863 | -2.096 | -2.255 |
|  | BG505 | ENV | -2.01 | -1.481 | -1.591 | -1.596 |
|  | LAI | ENV | -1.828 | -1.681 | -1.921 | -1.955 |
| Influenza A virus | A/PR8/1934 (H1N1) | NP | -4.065 | -3.575 | -4.428 | -4.422 |
|  | A/Aichi/2/1968 (H3N2) | NP | -3.278 | -3.095 | -3.414 | -3.397 |
|  | A/WSN/1933 (H1N1) | HA | -3.191 | -2.91 | -3.378 | -3.493 |
|  | A/Perth/16/2009 (H3N2) | HA | -2.474 | -2.295 | -2.585 | -2.744 |
|  | A/Green-winged Teal/Ohio/175/1986 (Avian) | PB2 | -2.705 | -2.506 | -2.869 | -2.68 |
|  | A/Green-winged <br> Teal/Ohio/175/1986 (Avian) | PB2 | -2.432 | -2.25 | -2.582 | -2.386 |
| Zika virus | MR766 | ENV | -4.31 | -4.028 | -4.527 | -4.268 |

Supplemental Table 4-5 Average Beneficial Effects of Radical/Conservative Substitutions
$\left.\begin{array}{|c|c|c|c|c|c|c|c|c|c|}\hline \text { Species } & \text { Strain } & \text { Gene } & \text { Overall } & \begin{array}{c}\text { Con. } \\ \text { Charge }\end{array} & \begin{array}{c}\text { Radical } \\ \text { Charge }\end{array} & \begin{array}{c}\text { Con. } \\ \text { Polarity }\end{array} & \begin{array}{c}\text { Radical } \\ \text { Polarity }\end{array} & \begin{array}{c}\text { Colarity } \\ \text { R Size }\end{array} \\ \text { Polar } \\ \text { \& Si }\end{array}\right)$

Supplemental Table 4-6 Average Beneficial Effects of SN and MTN Substitutions

| Species | Strain | Gene | Overall | SN | 2 MTN | 3 MTN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HIV-1 | BF520 | ENV | 0.304 | 0.425 | 0.383 | 0.471 |
|  | BG505 | ENV | 0.408 | 0.31 | 0.292 | 0.33 |
|  | LAI | ENV | 0.904 | 0.921 | 0.883 | 0.967 |
| Influenza A virus | A/PR8/1934 (H1N1) | NP | 0.726 | 0.752 | 0.696 | 0.817 |
|  | A/Aichi/2/1968 (H3N2) | NP | 0.732 | 0.716 | 0.753 | 0.696 |
|  | A/WSN/1933 (H1N1) | HA | 0.55 | 0.565 | 0.536 | 0.543 |
|  | A/Perth/16/2009 (H3N2) | HA | 0.525 | 0.506 | 0.543 | 0.52 |
|  | A/Green-winged Teal/Ohio/175/1986 (Avian) | PB2 | 0.467 | 0.47 | 0.454 | 0.549 |
|  | A/Green-winged Teal/Ohio/175/1986 (Avian) | PB2 | 0.47 | 0.475 | 0.461 | 0.503 |
| Zika virus | MR766 | ENV | 0.829 | 0.801 | 0.841 | 0.912 |

## Chapter 5 Discussion

## Overview

The projects in my thesis have resolved major puzzles on how mutational effects scale across levels of biological organization (Figure 5-1). At the lowest level, the impact of individual mutations can be understood deterministically from biological principles, just as the trajectory of an individual air molecule can be predicted from its collisions with several other molecules. However, at a higher phenotypic level, this determinism breaks down into seeming randomness, or idiosyncrasy. My first chapter quantifies this idiosyncrasy and explains why it occurs. A single site contributes to a phenotype via a potentially astronomical number of interactions. Consequently, a single mutation has unpredictable effects in the context of other mutations, just as the deterministic movement of a single air molecule scales to the random outcome of a die roll in a room full of molecules. At the highest level, due to the same statistical laws that govern a game of dice, we find that randomness in mutational effects leads to universal patterns in their collective effects across fitness levels and in evolutionary trajectories during adaptation and drift.

While idiosyncrasy is a major influence on fitness landscapes, it is not the only one. My second and third chapters revisit the deterministic biological effects of mutations and their impact on fitness and evolutionary patterns (Figure 5-1, right). I find that radical versus conservative


Figure 5-1 The role of the idiosyncratic epistasis theory and conservative versus radical mutations in the scaling of mutational affects across levels of biology.

Left and middle: the idiosyncratic epistasis theory posits that individual mutational effects are like the interactions between individual air molecules. At the lowest level, mutations have predictable consequences, but seeming randomness arises at a higher level due to complex interactions. However, predictability re-emerges as statistical laws at the level of evolution. Right: Conservative versus radical amino acid substitutions represent a deviation from idiosyncrasy, as this distinction at the lowest level leads to predictable fitness differences and biased phylogenetic patterns and evolution.
changes in amino acid properties have consistent differences in fitness effects, helping to explain widespread phylogenetic patterns and supporting the error-minimization hypothesis for the evolution of the genetic code.

How can we use the theory of idiosyncratic epistasis to further understand fitness landscapes?
What are the further implications of the differences between radical and conservative amino acid substitutions?

## Idiosyncratic epistasis as a null theory

Idiosyncratic epistasis could be used as a null model to uncover biased forms of epistasis and their impact on evolution.

First, evidence for various biologically-based theories of epistasis may need re-examination (Kacser and Burns 1981; Martin et al. 2007; Sanjuán and Nebot 2008; Gros et al. 2009; Wei and Zhang 2019). Most theories posit a bias towards either negative or positive epistasis and find support from observations involving beneficial or detrimental mutations, respectively. Our theory shows that that the patterns involving beneficial and detrimental mutations must be understood together. They also arise naturally from idiosyncrasy without the need for specific biological mechanisms or selection for robustness as posited by various theories.

However, many of the assumptions of these biologically-based theories still hold - biological systems do show modularity as in the modular life theory (Wei and Zhang 2019), viruses do encode less functional redundancy than eukaryotes as in the multiple hit theory (Sanjuán and Elena 2006), and so on. Thus, they are likely useful for understanding cases in which our null expectations are violated or why idiosyncrasy levels vary between fitness landscapes (Figure 21C). For example, idiosyncrasy predicts a negative correlation between mutational effects and background fitness, but we find that the strength of this correlation varies across mutations, and is even positive for some mutations (Figures 2-2B, S2A). This variation is likely not all due to limited empirical information. What are the properties of organisms, genes, sites or individual mutations that determine their level of idiosyncrasy and cause them to deviate from our null expectations? The biological mechanisms other theories posit may hold answers. However,
more work will be needed to understand how such mechanisms combine with idiosyncrasy. Mathematical models of fitness landscapes like the NK-model may be helpful to test hypotheses; for example, how modular genetic architectures may affect idiosyncrasy.

In comparison to an additive null model, the finding of negative epistasis/diminishing returns among beneficial mutations is commonly thought to slow adaptation (Couce and Tenaillon 2015). However, an idiosyncratic landscape may be a more appropriate null model to investigate the role of epistasis during adaptation. Consider a hypothetical organism that has evolved biological mechanisms which in isolation would lead to positive epistasis between beneficial mutations. However, these mechanisms must work against the inherent diminishing returns due to idiosyncrasy, perhaps resulting in overall negative epistasis between beneficial mutations, but less so than our null expectation. Comparing adaptation in this organism to an additive null model would reveal diminished adaptability, when in reality, the organism had evolved to lessen the inherent constraints of idiosyncrasy.

A recent paper on adaptation in a fungus made this same, potentially misguided conclusion (Schoustra et al. 2016). Fisher's geometric model was able to predict the negative epistasis among adaptive mutations while a House-of-Cards landscape (a completely idiosyncratic landscape) predicted stronger negative epistasis than was found. The authors concluded that the pattern of epistasis in the fungus constrained its adaptation, when in fact the bias towards less negative epistasis could have sped up its adaptation relative to our null prediction.

Our theory also makes a null prediction for the relationship between adaptability and robustness (the insensitivity to detrimental mutations). Lower fit organisms will have both higher adaptability and higher robustness due to the negative correlation between mutational fitness effects and background fitness. Some theories that posit the opposite relationship, based on the idea that insensitivity of fitness to detrimental mutations cuts both ways, coinciding with insensitivity to beneficial mutations (Ancel and Fontana 2000; Lenski et al. 2006; Sumedha et al. 2007). Other theories resolve the tension between robustness and evolvability by noting that robustness enhances evolvability by enabling exploration of neutral sequence space and providing a bank of diversity upon environmental change (Wagner 2008). This could combine synergistically with the higher evolvability of more robust, lower fit organisms due to idiosyncrasy. Deviations from our null expectation may reveal interesting forms of epistasis or other biological mechanisms. For example, our finding that radical amino acid substitutions are both more detrimental and more beneficial in the same genotype fits better with the theory that (in)sensitivity to mutation cuts both ways.

It will be essential to create a model of idiosyncratic epistasis that can be fit to empirical data. This would enhance our ability to uncover deviations from null expectations and compare the importance of idiosyncrasy relative to other biological mechanisms. However, the $n$-order model is not easily adapted for this purpose. Because of the vast number of potential terms, the model cannot be simulated beyond 20 or so interacting sites. In some ways there is also too much flexibility in the model; for example, the same level of idiosyncrasy could be achieved by many different schemes for weighting the interaction terms. Our idiosyncrasy index may provide a starting point, but it is unclear how the size of a landscape, missing data, or variation in
idiosyncrasy among sites affects its calculation. Thus, much work is needed to develop the theory of idiosyncrasy into a model capable of direct comparison with empirical data.

## Implications of Radical/Conservative Fitness Differences

We have shown that substitutions which radically change amino acid properties are both more detrimental and more highly beneficial than conservative changes, at least in RNA viruses. The difference in detrimental effects likely contributes to the widespread transition-transversion (Ts/Tv) substitution bias. It is interesting to speculate on the impact of radical/conservative differences on other evolutionary processes.

There is widespread evidence of a transitional mutation bias across taxa (Zhang and Gerstein 2003; Jiang and Zhao 2006; Baer et al. 2007; Denver et al. 2009; Pauly et al. 2017). For example, the experimentally determined $\mathrm{Ts} / \mathrm{Tv}$ mutational bias in influenza is 2-3.6 (Bloom 2014; Pauly et al. 2017). Is it possible that the more radical nature of transversions has led to selection for a reduced transversion mutation rate? The causation could work in reverse, or in both ways - an underlying higher transition rate could have selected for robustness to transitional substitutions via codon usage bias or other mechanisms. Simulations could determine whether the transversion/transition fitness differences are high enough to select for reduced transversion rates (Lynch 2010). This could indicate ongoing selection on the mutation rate which could be verified. Mutational effects in rare organisms in which the transversion rate is higher could also illuminate this question (Keller et al. 2007).

Similarly, the evolution of the genetic code is hypothesized to have involved selection for errorminimization (Woese 1965; Woese et al. 1966; Crick 1968; Haig and Hurst 1991; Freeland and

Hurst 1998; Geyer and Mamlouk 2018; Tripathi and Deem 2018). Our results support this hypothesis, showing that single nucleotide codon mutations indeed cause less damage than the more radical, multi-nucleotide mutations. However, radical mutations are also more beneficial. Did selection for robustness in the genetic code consign all subsequent life forms to lower adaptability? Alternatively, this particular genetic code could have been under selection for evolvability as well as robustness. For example, recent studies have questioned the errorminimization hypothesis because only slightly different genetic codes can minimize radical changes even more than the universal code (Di Giulio and Medugno 2001). However, this study ignored adaptability - perhaps the current genetic code is a more optimal solution to this tradeoff than these alternatives.

The fitness differences between radical/conservative and $\mathrm{Ts} / \mathrm{Tv}$ substitutions have implications for viral evolution. Radical charge changes showed the least differences from conservative ones in terms of their detrimental effects (Figures 2-4, 4-1, 4-2A-B). This was particularly true for the viral surface proteins HA and ENV as compared to the internal NP proteins (Figures 2-4, 4-1, 4-2A-B). These surface proteins have a history of immune selection and exhibit tolerance to mutations allowing for immune escape (Stephens and Waelbroeck 1999; Plotkin and Dushoff 2003; Thyagarajan and Bloom 2014; Doud and Bloom 2016; Visher et al. 2016). Charge changes were also some of the most beneficial type of radical changes (Figure 4-2); it is interesting to speculate whether this advantage is enhanced under selection for immune escape. DMS data is available to answer this question, which could be incorporated into further work. Furthermore, studies of codon usage have also found a bias towards non-synonymously mutating codons in the HA protein (Plotkin and Dushoff 2003) or that enhance evolvability and robustness (Lauring et
al. 2012), but a potential bias towards codons with a propensity for charge changes was not evaluated. DMS data could be used to further investigate the advantages or disadvantages of the wild-type codon usage compared to simulated alternatives. The role of radical changes in cluster-transition mutations, which are those that drastically change the antigenic properties of influenza and prompt vaccine updates (Koelle et al. 2006), could also be investigated.

## Conclusion

In contrast to biased forms of epistasis in other theories, the crucial idea of idiosyncratic epistasis is that the immense number of interactions that determine a phenotype leads to unpredictability of mutational effects. Phrased another way, more idiosyncratic epistasis makes quite different phenotypes accessible by fewer mutational steps. From this perspective, idiosyncrasy may promote the evolvability and great phenotypic diversity of life. Perhaps it contributes to the surprising genetic similarity of quite different organisms (King and Wilson 1975) or speeds up phenotypic evolution in response to environmental changes. Furthermore, as any phenotype becomes more accessible from any genotype, idiosyncrasy also means that very different genotypes may have similar phenotypes. Perhaps this underlies convergence at the phenotypic level. Indeed, ancient proteins with conserved functions have continued to diverge over billions of years seemingly without limit on sequence dissimilarity (Povolotskaya and Kondrashov 2010). In the midst of the idiosyncrasy we find, it is surprising that simple radical versus conservative distinctions in amino acid substitutions have predictable differences. However, if such biological features never mattered to fitness - if idiosyncrasy was complete - the fitness landscape may become too rugged to sustain adaptation for long and any drift would be drastically deleterious. Similar to Kauffman's idea that the most evolvable systems lie at the
boundary "between order and chaos" (Kauffman 1993), might the right balance of idiosyncrasy distinguish evolvable complex systems from non-living ones?

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[^0]:    ${ }^{a}$ Number of transition mutations
    ${ }^{b}$ Number of transversion mutations

