Thermodynamics of the lanthanide halides II. Heat capacities and Schottky anomalies of SmCl₃, EuCl₃, and GdCl₃ from 5 to 350 K^{*}

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The heat capacities of SmCl₃, EuCl₃, and GdCl₃ have been measured from 5 to 350 K by adiabatic calorimetry. For SmCl₃ and EuCl₃, the calculated Schottky heat capacities may be compared with the difference in heat capacity between LaCl₃ and the paramagnetic members, as before. For GdCl₃ which lacks a Schottky contribution, the difference between the heat capacity of LaCl₃ and GdCl₃ may be discussed in terms of spectroscopic data on lattice vibration. Comparison between the measured entropies and the results of estimation schemes is presented. The values of { $S^{\circ}(298.15 \text{ K}) - S^{\circ}(0)$ } for SmCl₃, EuCl₃, and GdCl₃ are 35.88, 34.43, and 36.19 cal₁th K⁻¹ mol⁻¹, respectively.

1. Introduction

The compounds $SmCl_3$, $EuCl_3$, and $GdCl_3$ differ from the preceding lanthanide trihalides⁽¹⁾ in several respects. Sm(III) and Eu(III) are characterized by low-lying *J*-states which make significant contributions in the temperature range under investigation here. The ${}^8S_{7/2}$ ground state of Gd(III) is little affected by the crystalline field and its next *J*-state is too energetic to contribute heat capacities below 350 K. The thermal properties in the temperature range 10 to 350 K (where the contribution due to its ferromagnetic ordering transition⁽²⁾ at 2.2 K is small) provides a measure of the lattice heat capacity which may be compared with that of LaCl₃. All three salts show the increasing influence of the lanthanide contraction on their thermal properties. This paper will treat the resolution of the heat capacities of SmCl₃ and EuCl₃ similarly to those of the first paper, compare the heat capacity of LaCl₃ and GdCl₃, and discuss the overall energies of these trihalides based on spectroscopic and calorimetric data.

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2. Experimental

SAMPLE PREPARATION AND CHARACTERIZATION

The methods of the previous paper⁽¹⁾ were applied to the samples of this series except for EuCl₃. The sesquioxides were obtained from American Potash and Chemical Co. and were of 99.99 mass per cent stated purity. A slight deficiency of chlorine despite the fact that heating was stopped at 623 K was found in the initial EuCl₃ preparation. This deficiency was reflected in the analytical results which gave a composition of $EuCl_{2.989\pm0.003}$. There was no chemical or crystallographic evidence of contamination; it was concluded that the method was inadequate for europium. This observation is in good agreement with the work of Polyachenok and $Novikov^{(3)}$ on the decomposition pressure of EuCl₃. A crude extrapolation of their results beyond the range of their determination gives an equilibrium chlorine pressure of about 0.1 Pa at 623 K and implies certain chlorine depletion under the conditions of synthesis employed. This result is similar to that of Haschke⁽⁴⁾ for EuBr₃. Hence, the hypostoichiometric EuCl₃ sample was chlorinated in a Pyrex cell connected through a vacuum line with stopcocks to a trap bathed in a CCl₄-slush bath and then to a tank of chlorine gas with a short piece of Tygon tubing. The system and cell were evacuated and briefly purged with chlorine at atmosphere pressure. The cell was isolated and surrounded by the furnace. The temperature was slowly taken to 633 K, held there for 1 h, and then allowed to cool slowly over 4 h with the turned-off furnace in place. The cell was then evacuated, filled with pre-purified nitrogen gas, and sealed off under flame. The treatment gave a stoichiometric product.

In applying the method for lanthanide analysis to the series of this article, it was noted that the masses of recovered oxide samples were slightly high (by about 2 to 5 per cent) but that silver chloride was not precipitated from nitric acid solutions upon addition of $AgNO_3(aq)$. Since firing for several hours in air would bring the sesquioxide masses down to the theoretical, the discrepancy was possibly due to the formation of hydrous oxide phases which dried out on further heating. All three sesquioxides (samarium, europium, and gadolinium) required longer heating periods to reach the theoretical mass. For the oxides of this series, the increased period to convert to sesquioxide (up to 48 h) may have been partly due to an increased tendency of the oxide phase to retain chlorine; it was observed that the extra firing time increased in the order Sm > Eu > Gd. The analytical results obtained are shown in table 1.

		10)²w			
Compound	Cl		Ln		$10^{2}\Sigma w$	<i>n</i> (Cl)/ <i>n</i> (Ln)
-	obs.	calc. ^b	obs.	calc. ^b		
SmCl ₃	41.41 ± 0.06	41.42	58.61 ± 0.28	58.58	100.02 ± 0.28	$\textbf{2.997} \pm \textbf{0.010}$
EuCl ₃	$\textbf{41.17} \pm \textbf{0.04}$	41.17	$\textbf{58.85} \pm \textbf{0.10}$	58.83	$\textbf{100.02} \pm \textbf{0.11}$	$\textbf{2.999} \pm \textbf{0.003}$
GdCl ₃	$\textbf{40.34} \pm \textbf{0.06}$	40.35	$\textbf{59.70} \pm \textbf{0.20}$	59.65	100.04 ± 0.21	$\textbf{2.997} \pm \textbf{0.006}$

TABLE 1. Analysis of the lanthanide trichloride samples; w denotes mass fraction^a

^a Uncertainty indices are two standard deviations.

^b Based on 1971 IUPAC atomic weights.

The only ambiguity in the assignment of the hexagonal UCl₃-type crystal structure to all the light lanthanide trichlorides is presented in the work of Harris and Veale⁽⁵⁾ on GdCl₃. Their observations on the occurrence of the orthorhombic PuBr₃-type structure seem consistent with this structure being a metastable one for GdCl₃. Nevertheless, an attempt was made to obtain the orthorhombic modification. A GdCl₃ sample, prepared as usual, was found to give only UCl₃-type diffraction lines. Samples were sealed in small vials under 3.8 MPa of He gas. One was immersed in liquid nitrogen for 7 h, the other annealed in a drying oven at 367 K for 7 d. Guinier-Häggtype powder X-ray patterns taken on these samples revealed only lines due to the UCl₃-type structure, with no trace of lines due to a PuBr₃-type phase. It was concluded that the results of subsequent heat-capacity measurements could be unambiguously attributed to hexagonal GdCl₃. The lattice parameters found for these halides and a comparison with literature values are shown in table 2.

	SmCl ₃		Eu	EuCl ₃		GdCl ₃	
	<i>a</i> _o /nm	$c_{\rm o}/{ m nm}$	a₀/nm	$c_0/{ m nm}$	$a_{ m o}/{ m nm}$	c₀/nm	
Templeton and Dauben ^a	0.7378 ± 0.0007	0.4171 ± 0.0004	0.7369 <u>0.0004</u>	0.4133 ± 0.0002	0.7363 ± 0.0004	0.4105 ± 0.0002	
Morosin ^{<i>b</i>}			0.73746	0.41323	0.73663	0.41059	
ASTM File ^c	0.7380	0.4169	0.7375	0.4134			
This work	0.7380 ± 0.0007	$\begin{array}{r} 0.4175 \\ \pm \ 0.0001 \end{array}$	0.7370 0.0002	0.4137 ± 0.0004	0.7367 <u>-1-</u> 0.0002	0.4108 1 0.0001	
ho/g cm ⁻³	4.3	30	4.4	14	4.5	42	

TABLE 2. Lattice	parameters of	the la	nthanide	trichl	orides
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^{*a*} Reference 6.

^b Reference 7.

^e Reference 8: ASTM File card numbers: SmCl₃, 12-789; EuCl₃, 12-387.

HEAT-CAPACITY MEASUREMENTS

The heat-capacity measurements were obtained in the chronological order $SmCl_3$, $GdCl_3$, and $EuCl_3$ by the same method as reported earlier.⁽¹⁾ The loading data are given in table 3.

TABLE 3. Calorimeter loading data; m denotes mass of sample M molar mass, " and p pressure of helium

Compound	m/g	$M/g \text{ mol}^{-1}$	<i>p</i> /kPa
SmCl ₃	79.2313	256.8	8.1
EuCl ₃	80.4073	258.319	7.9
GdCl ₃	76.1415	263.61	7.6

^a Based on 1971 IUPAC atomic weights.

3. Results

THERMODYNAMIC FUNCTIONS

No cooperative thermal phenomena were encountered and the only apparent manifestation of non-cooperative effects was a slight increase in the duration of time required for establishment of constant quasi-adiabatic drifts following energy inputs that occurred in the temperature regions of the maxima in these contributions.

The experimental heat capacities were processed by subtraction of the heat capacity due to the empty calorimeter (determined separately) and correction for small differences in amounts of helium gas and Cerroseal solder relative to the calorimeter as run empty. The calorimeter and heater-thermometer assembly represented about 30 to 50 per cent of the total measured heat capacity. Curvature corrections were applied in order to adjust the mean values of $\Delta H/\Delta T$ to the limit $(dH/dT = C_p)$. The heat capacities are listed in chronological sequence in table 4 so that the ΔT 's employed usually can be estimated from adjacent mean temperatures.

These results are depicted in figure 1. The curve-fitting involved computer regression of the measured heat capacities to a power series of orthogonal polynomials in reduced

Т	C_p	Т	C_p	Т	C_p	Т	C_p
ĸ	cal _{th} K ⁻¹ mol ⁻¹	K	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	K c	$al_{th} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	K	cal _{th} K ⁻¹ mol ⁻¹
			Samarium	trichlorid	e		
	Series I	265.60	23.15	10.91	0.309	5.96	0.021
68 05	10.86	275.76	23.35	11.98	0.424	6.58	0.040
74.65	11.95	285.99	23.56	13.10	0.581	7.22	0.055
82.80	13.27	296.16	23.75	14.25	0.755	7.94	0.080
92.30	14.58	306.26	23.94	15.44	0.953	8.74	0.127
102.15	15.70	316.28	24.10	16.76	1.168	9.63	0.208
111.69	16.68	326.28	24.24	18.18	1.417	10.79	0.306
121.82	17.59	336.24	24.38	19.76	1.706	12.04	0.431
132.25	18.42	343.17	24.44	21.67	2.071	13.39	0.624
142.27	19.09	347.13	24.45ª	23.93	2.514	14.75	0.842
151.97	19.66			26.30	2.984	16.17	1.065
161.77	20.14	2	Series III	29.03	3.507	17.65	1.325
171.70	20.58	58 07	0 204			18.87	1.536
181.45	20.96	64.36	10.21	S	Series V	20.91	1.926
191.56	21.32	69.78	11 13	35 56	4 769	23.27	2.385
202.03	21.64	75.95	12.14	39.07	5 425	25.94	2.908
212.37	21.94	15.75	12.17	47 84	6 132	28.90	3.480
222.59	22.24		Sarias IV	46 58	6 847	32.16	4.116
232.71	22.47	•	Series I v	50.41	7 578	35.61	4.772
242.73	22.72	5.62	0.023	54.87	8 416	39.18	5.444
	Contra II	6.64	0.055	59.89	9 367	42.97	6.157
	Series II	7.46	0.078	57.07	2.507	47.04	6.924
235.42	22.51	8.36	0.117	c	orios VI	51.31	7.742
245.35	22,75	9.14	0.169	3	enes vi	56.45	8.718
255.51	22.99	9.92	0.235	5.18	0.018	62.60	9.874

TABLE 4. Experimental heat capacities of SmCl₃, EuCl₃, and GdCl₃

$(cal_{th} = 4.184 J)$

T	Cp	T	C_p	Τ	C_p	T	C _p
K	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	ĸ	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	ĸ	$cal_{th} K^{-1} mol^{-1}$	ĸ	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$
			Europium	trichlor	ide		
	Series I	226.30	24.31	346.44	26.09	20.42	1.034
85.05	13 38	236.27	24.54			22.43	1.287
92.12	14.56	246.16	24.80 ^a		Series III	24.68	1.604
99.72	15.70			4 95	0.012	27.12	1.962
107.97	16.84		Series II	6.06	0.030	29.57	2.351
116.87	17.97	239.80	24.62	6.98	0.043	32.15	2.807
126.22	19.04	249.67	24.78	8.03	0.071	35.19	3.341
136.02	19.98	259.48	24.97	9.08	0 108	38.95	4.052
145.95	20.80	269.35	25.11	10.07	0.157	43.32	4.917
155.87	21.51	279.28	25.29	11.11	0.203	48.12	5.905
165.84	22.10	289.13	25.46	12.18	0.269	53.99	7.161
175.77	22.61	298.94	25.58	13.25	0.353	60.50	8.550
185.69	23.04	308.84	25.71	14.39	0.444	66.80	9.861
195.79	23.42	318.76	25.81	15.65	0.556	73.16	11.11
206.08	23.76	328.66	25.95	17.03	0.678	79.80	12.41
216.24	24.07	338.56	26.04	18.62	0.834	86.98	13.75
			Gadoliniur	n trichlo	ride		
	Series I	311.38	23.54	151.04	19.27	14 37	0 493
152 40	10.25	321.61	23.69	160.73	19.77	15 71	0.455
162.40	10.80	332.05	23.78			17.21	0.745
172 98	20.34	342.02	23.82		Series III	18.95	0.916
182.90	20.34	348.36	23.77°	52.73	6.836	20.83	1 131
192.00	21.08			58.35	7.975	22.83	1.383
202.79	21.00		Series II	64.04	9.132	24.98	1.686
212.67	21.40	66 21	0 5/8	69.68	10.18	27.29	2.025
222.49	21.00	73 32	10.82		Series IV	29.81	2.420
232.28	22.55	80.30	10.02	1 00	0.096	32.40	2.865
242.18	22.17	87 77	12.07	5 /1	0.000	35.23	3.371
252.16	22.56	95 76	14 33	6.40	0.007	38.51	3.979
262.07	22.75	104 14	14.55	7 97	0.111	42.31	4,702
271.90	22.94	112 76	16.27	076	0.150	46.52	5.553
281.78	23.10	121.00	17.17	7.20	0.105	51.00	6.485
291 73	23.26	131 44	17.06	11.05	0.245	56.16	7.536
301.60	23.44	141.21	18.66	13.11	0.389	62.31	8.792
					01200		

TABLE 4.--continued

^a This point was given less weight in the curve-fitting process.

temperature. The resulting power series was integrated appropriately to produce the derived thermodynamic functions at round temperature intervals. These functions (listed in table 5) do not include contributions from nuclear spin or isotropic mixing and are thus suitable for use in ordinary thermochemical calculations. Above 25 K the heat capacities are considered to have standard deviations no greater than 0.1 per cent and the derived thermodynamic properties are considered to be even more reliable over this range, apart from allowance for the presence of effects below the lowest temperature of measurement.



FIGURE 1. Experimental heat-capacity curves. ●, SmCl₃; □, EuCl₃; ○, GdCl₃.

SAMARIUM TRICHLORIDE

The findings of Colwell, Mangum, and Utton⁽⁹⁾ are in substantial disagreement with those of this study. Their heat capacities show a large spike (which they do not believe is a true feature of SmCl₃). They found long relaxation times during measurements. Furthermore, they find a minimum in the heat capacity between 3 and 4 K, and attribute "turn around" in the heat capacity to the lower-temperature side of the Schottky heat capacity. The cause of this rise, the first Kramers' doublet, has been found at 40.7 cm⁻¹ for Sm(III) in LaCl₃.⁽¹⁰⁾ Colwell *et al.*'s data require it to be some 20 per cent lower to produce a minimum to match that observed in their heat-capacity experiments. The heat capacity behavior found at the upper limit of their temperature range (4 K) fits poorly with that of this study. Even allowing

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Т	C,	$\{S^{\circ}(T)-S^{\circ}(0)\}$	$\{H^{\circ}(T)-H^{\circ}(0)\}$	$- \{G^{\circ}(T) - H^{\circ}(0)\}/T$
ĸ	$cal_{th} K^{-1} mol^{-1}$	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	cal _{th} mol ⁻¹	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$
		Samarium trich	nloride	
5	0.017	(1.383)	(0.415)	(1.300)
10	0.229	1.437	0.864	1.351
15	0.875	1.638	3.449	1.408
20	1.750	2.006	9.962	1.508
25	2.726	2.501	21.134	1.656
30	3.694	3.084	37.194	1.844
35	4.660	3.726	58.08	2.066
40	5.597	4.410	83.73	2.316
45	6.543	5.123	114.08	2.588
50	7.496	5.862	149.18	2.879
		5.002	117.10	2.075
60	9.388	7.397	233.64	3.503
70	11.186	8.981	336.62	4.172
80	12.819	10.583	456.80	4.873
90	14.249	12.178	592.3	5.596
100	15.48	13.744	741.1	6.333
110	16.53	15.27	901.3	7 076
120	17.44	16.75	1071.2	7 821
130	18 24	18 18	1249 7	8 563
140	18 94	19 55	1435 7	9 299
150	19.55	20.88	1628 3	10 027
		20.00	1020+5	10.027
160	20.07	22.16	1826.4	10.746
170	20.51	23.39	2029.4	11.454
180	20.90	24.58	2236.5	12.150
190	21.25	25.72	2447.4	12.834
200	21.58	26.81	2661.5	13.506
210	21.88	27.87	2878.9	14,165
220	22.16	28.90	3099.1	14 812
230	22.41	29.89	3321.9	15.45
240	22 64	30.85	3547.2	16.07
250	22.85	31.78	3774 7	16.68
		•••••		10.00
260	23.05	32.68	4004.2	17.28
270	23.25	33.55	4235.7	17.86
280	23.44	34.40	4469.1	18.44
290	23.63	35.23	4704.5	19.00
300	23.82	36.03	4941.8	19.56
310	24.00	36.81	5181	20.10
320	24.16	37.58	5422	20.64
330	24.30	38 37	5664	20.04
340	24.41	39.05	5908	21.10
350	24 50	39.76	6152	21.00
000	21.30	52.10	0154	22.10
273.15	23.31	33.82	4309.0	18.04
298.15	23.79	35.88	4897.7	19.46

TABLE 5. Thermodynamic functions for SmCl_3, EuCl_3, and GdCl_3 $(cal_{th}=4.184~J) \label{eq:cal_th}$

1	C _p	$\{S^{\circ}(T) - S^{\circ}(0)\}$	$\{H^{\circ}(T) - H^{\circ}(0)\}$	$- \{G^{\circ}(T) - H^{\circ}(0)\}/T$
ĸ	cal _{th} K ⁻¹ mol ⁻¹	$cal_{th} K^{-1} mol^{-1}$	cal _{th} mol ⁻¹	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$
		Europium tric	hloride	
5	0.013	(0.005)	(0.019)	(0.002)
10	0.150	0.045	0 341	0.011
15	0 488	0.163	1 860	0.039
20	0.993	0.369	5 502	0.094
25	1 644	0.559	12 037	0.177
2.5	1.077	0.000	12.057	0.177
30	2.426	1.025	22.164	0.287
35	3.310	1.465	36 472	0.423
40	4 260	1 968	55 38	0.584
45	5 256	2 527	79.15	0.768
50	6 200	3 134	108 01	0.700
50	0.477	5.154	106.01	0.7/4
60	8 444	4 473	181 76	1 444
70	10 510	5 932	276 67	1.979
80	10.519	7 464	201.65	2.540
00	14 200	7.404	591.05	2.309
90	14.200	9.034	525.1	3.200
100	15.76	10.612	6/5.0	3.862
110	17 14	12 181	830 7	1 517
120	18 35	12.101	1017 3	5 249
120	10.33	15.720	1017.3	5.059
130	19.40	15.24	1206.2	5.958
140	20.31	16./1	1404.9	6.674
150	21.09	18.14	1612.0	7.391
160	21.76	10.52	1976 2	9 104
170	21,70	19.52	1020.5	0.100
1/0	22.32	20.86	2046.8	8.817
180	22.81	22.15	2272.6	9.522
190	23.22	23.39	2502.8	10.219
200	23.58	24.59	2736.8	10.908
210	22.88	25 75	2074 2	11 597
210	23.00	25.75	2314.4	11.307
220	24.15	20.87	3214.4	12.257
230	24.39	27.95	3457.1	12.916
240	24.61	28.99	3702.1	13.564
250	24.80	30.00	3949.2	14.201
260	24.08	20.07	4108.1	14 929
200	24.30	21.02	4170.1	14.020
270	25.15	31.92	4440.0	15.44
280	25.30	32.84	4/01.0	16.05
290	25.45	33.73	4954.8	16.64
300	25.59	34.59	5210	17.23
210	25 72	35 /3	5467	17.80
220	25.12	26.25	5774	19.26
340	43,03 25,06	30.43	5002	10.30
330	23.90	37.03	2002	10.92
340	26.05	57.85	0243	19.46
350	26.13	38.38	6304	20.00
171 15	25.20	22.21	1570 1	15 63
2/3.13	23.20	32.21	4J20.1 5162	13.03
296.13	43.37	34.43	2102	1/.12

TABLE 5.—continued

Т	C_p	$\{S^{\circ}(T) - S^{\circ}(0)\}$	$\{H^{\circ}(T)-H^{\circ}(0)\}$	$- \{G^{\circ}(T) - H^{\circ}(0)\}/$
ĸ	$\overline{\operatorname{cal}_{\operatorname{tn}} \mathrm{K}^{-1} \operatorname{mol}^{-1}}$	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	cal _{th} mol ⁻¹	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$
		Gadolinium tri	chloride	
5	$(0.209)^{a}$	(3,939) ^a	$(5.9)^{a}$	$(2.75)^{a}$
10	0.218	4 059	6 858	3 373
15	0.536	4.000	8 658	3 623
20	1.038	4.201	12 524	3 703
20	1.030	4,417	10.324	2.735
25	1.088	4./18	19.284	3.947
30	2.456	5.092	29.597	4.106
35	3.321	5.535	44.004	4.278
40	4.262	6.039	62.94	4.466
45	5.252	6.598	86.71	4.671
50	6.271	7.204	115.50	4.894
60	8 310	8 520	188 50	5 387
70	0.317	0.050	188.50	5.027
/0	10.255	9,939	201.51	5.957
80	12.003	11.445	392.97	0.332
90	13.540	12.949	520.9	7.162
100	14.8/1	14.446	663.1	/.816
110	16.01	15.92	817.7	8.486
120	17.00	17.36	982.8	9.165
130	17.84	18.75	1157.1	9.849
140	18.57	20.10	1339.3	10.533
150	19.20	21.40	1528.2	11.215
160	10 74	22.66	1722.0	11 201
170	20.22	22.00	1022.9	11.071
100	20.22	25.87	1922.0	12.300
180	20.63	25.04	2127.1	13.221
190	20.99	26.16	2335.2	13.873
200	21.31	27.25	2546.8	14.515
210	21.60	28.30	2761.4	15.15
220	21.86	29.31	2978.7	15.77
230	22.10	30.28	3198.6	16.38
240	22.32	31.23	3420.7	16.98
250	22.53	32.14	3645.0	17.56
260	22.72	22.02	2971.2	10.17
200	22.72	33.03	3671.2	18,14
270	22.90	33.09	4099.4	18.71
200	23.07	54.75	4329.3	19.27
290	23.24	55.54	4560.8	19.81
300	23.40	36.33	4/94.0	-20.35
310	23.54	37.10	5029	20.88
320	23.67	37.85	5265	21.40
330	23.76	38.58	5502	21.91
340	23.82	39.29	5740	22.41
350	23.87	39.98	5978	22.90
772 15	22.06	2116	A171 C	10 00
213.13	22.90 22'27	34.10	41/1.0	18.89
- 298.13	23.57	30.19	4/50.8	20.25

TABLE 5.—continued

^a Based on thesis data of A. F. G. Wyatt, Oxford, 1963.

for some 50 per cent error at 5 K, the curve of this investigation is lower by a factor of 3 to 4 than any reasonable extrapolation of their curve. No reasonable join could be found even were the points of the present study to be called into question at temperatures as high as 10 K. Indeed, the curve found here implies that the first Schottky level should be some 30 per cent higher than the spectroscopic value. Furthermore, the downward shift of the level suggested by Colwell et al. would displace the maximum of the Schottky peak to lower temperatures whereas an upward shift is required to reproduce the Schottky behavior noted in this work over a much wider range of temperature. The SmCl₃ cooperative magnetic-ordering transition occurs at much lower temperatures than for either PrCl₃ or NdCl₃. Colwell et al. report little success in attempts to fit their results to a theoretical model. The entropy between 0.313 K and 4 K is about 0.68 cal_{th} K⁻¹ mol⁻¹.[†] Since the transition occurs at low temperatures, the separation of cooperative and non-cooperative entropy contributions is evident; the entropy increments below 5 K will be taken as $R \ln 2$ (in preference to the measured values of Colwell et al.) plus a small lattice contribution (0.005 $cal_{th} K^{-1} mol^{-1}$ as that for LaCl₃ and EuCl₃). An approximation in keeping with these results is made in specifying the attendant enthalpy increment; the excess entropy is regarded as a spike of zero width at T = 0.3 K and the enthalpy approximated as $R \ln 2 \times 0.3 \text{ K} = 0.4 \text{ cal}_{th} \text{ mol}^{-1}$. This is reasonable in comparison with the values for $PrCl_3$ and $NdCl_3$ (about 1 cal_{th} mol⁻¹) but is probably a slight overestimate since the "average" magnetic ordering temperature is probably somewhat lower than 0.3 K.

The values of Colwell *et al.* have been ignored almost entirely for $SmCl_3$ in favor of the theoretically formulated values.

EUROPIUM TRICHLORIDE

The ground state of Eu(III), ${}^{7}F_{0}$, is non-degenerate and the first component of the next J-state occurs at 355 cm⁻¹ above the ground state.⁽¹¹⁾ At 5 K, the Boltzmann factor between the ground state and the center of gravity of the ${}^{7}F_{1}$ state shows that the relative population of the ${}^{7}F_{0}$ and ${}^{7}F_{1}$ states is about 10⁴⁷, so that the upper state has negligible effect. Therefore, both LaCl₃ and EuCl₃ are characterized by lattice-only heat-capacity contributions-below 20 K-due mostly to acoustical contributions. This can be justified by the use of the $\Theta_{\rm D}$ value of Varsanyi and Maita⁽¹²⁾ and the lattice vibrational frequencies of Stedman and Newman.⁽¹³⁾ Since heat capacity due to the 21 optical-branch frequencies is very small at the lowest temperatures, the optical contribution is effectively zero at 5 K, 2 per cent of the total at 10 K, 13 per cent at 15 K, and 25 per cent at 20 K. Thus, in the absence of extreme differences in the optical-branch frequencies between LaCl₃ and EuCl₃, such differences in the heat capacities as exist for these two compounds are largely due to differences in acoustical vibrations. A plot of C_p/T against T^2 for both LaCl₃ and EuCl₃ is given in figure 2. The value of Varsanyi and Maita of (118 ± 1) K is in good agreement with the value of this study, (119 ± 8) K. Despite the large uncertainty in the $\Theta_{\rm D}$, it is clear from figure 2 that LaCl₃ and EuCl₃ have nearly identical

† Throughout this paper $cal_{th} = 4.184$ J.



FIGURE 2. Plot of C_p/T against T^2 . \bigcirc , LaCl₃; \bigcirc , EuCl₃.

heat capacities over this range. The range of variation of the molecular weight and molar volume covered by this pair is nearly the entire range of this study. Thus, this pair should show almost the maximum variation in $\Theta_{\rm D}$ but no variation is found. Application of the Lindemann melting formula⁽¹⁴⁾ is precluded by decomposition of solid EuCl₃ with loss of Cl₂. Although the relative magnitude of $\Theta_{\rm D}$ cannot be specified for this pair, application of the Lindemann melting rule to the pair LaCl, and GdCl₃ yields the quantity $\Theta_D(GdCl_3)/\Theta_D(LaCl_3) = 0.874$, or a Θ_D for GdCl₃ of about 102 K. The LaCl₃-GdCl₃ pair spans the entire range of parameters involved in the Lindemann comparison but should be fairly close to that for the pair LaCl₃- $EuCl_3$; a direct comparison for the former pair is not possible due to the enhanced heat capacity from the magnetic ordering found at the lowest temperatures of this study. The near coincidence of the curves for LaCl₃ and EuCl₃ below about 20 K shows much less dependence of $\Theta_{\rm D}$ for this series on the various parameters than the Lindemann rule which suggests no variation at all in the $\Theta_{\rm D}$ values for these compounds; and hence, no difference in the acoustical heat capacity. In the light of figure 2, it seems reasonable to attribute identical $\Theta_{\rm p}$'s to each member of the series. Certainly, in terms of the low-temperature augmentation of the thermodynamic functions, such an assumption will not be serious since the increments will be small.

GADOLINIUM TRICHLORIDE

The high-temperature tail of the prominent ferromagnetic transition at 2.2 K is clearly evident in the heat capacity of this experiment below about 20 K. Even though the experimental measurements of Leask, Wolf, and Wyatt⁽²⁾ extend only to 1.2 K, the magnetic entropy is established by higher-temperature magnetic heat capacity and interaction studies. Leask *et al.* present the heat capacities of Wyatt's thesis,⁽¹⁵⁾ used the experimentally derived value of $\{S^{\circ}(4.2 \text{ K}) - S^{\circ}(1.2 \text{ K})\} = 2.397$

 $\operatorname{cal_{th}} K^{-1} \operatorname{mol}^{-1}$ and an extrapolation of the T^{-2} -dependent high-temperature magnetic heat capacity to find $\{S^{\circ}(1.2 \text{ K}) - S^{\circ}(0)\}$ by subtraction from $R \ln 8$; this gave a value of 1.592 $\operatorname{cal_{th}} K^{-1} \operatorname{mol}^{-1}$. Several later studies have concentrated on the measurement of the magnetic heat capacity and its expression, valid for $T > T_c$, as a power series:⁽¹⁶⁾

$$C_{\rm mag} = R \sum_{n=2}^{n=\infty} C_n / T^n$$

The C_n 's are related to exchange constants. Only C_2 and C_3 are needed and the resulting expression $C_{\text{mag}} = RC_2/T^2 + RC_3/T^3$ has served as the basis for analyzing the high-temperature magnetic heat capacity. Two of the most recent studies are in good agreement on the values of C_2 and C_3 ; Clover and Wolf,⁽¹⁷⁾ and Birgeneau, Hutchings, and Wolf,⁽¹⁸⁾ find C_2 and C_3 values of (3.36 ± 0.012) K² and (-5.3 ± 0.4) K³, and (3.2 ± 0.3) K² and (-4.9 ± 1.0) K³, respectively. The values allow a better value of $\{S^{\circ}(\infty) - S^{\circ}(4.2 \text{ K})\}\$ and hence a more reliable estimate of $\{S^{\circ}(1.2 \text{ K}) - S^{\circ}(0)\}\$ with reference to a total of R ln 8. The former values of C, and C_3 were chosen and determine $\{S^{\circ}(\infty) - S^{\circ}(4.2 \text{ K})\} = 0.236 \text{ cal}_{\text{th}} \text{ K}^{-1} \text{ mol}^{-1}$ and $\{S^{\circ}(1.2 \text{ K}) - S^{\circ}(0)\} = 1.499 \text{ cal}_{th} \text{ K}^{-1} \text{ mol}^{-1}$. The choice of C_2 and C_3 is somewhat arbitrary, but the difference in the entropy increments which it implies is very small. In either case, the value of $\{S^{\circ}(1.2 \text{ K}) - S^{\circ}(0)\}$ is specified within rather narrow limits. An attempt was made to extrapolate judiciously the plot of C_p/T against T for Wyatt's data to T = 0. The entropy was found to be about 1.5 cal_{th} K^{-1} mol⁻¹ below 1.2 K in good agreement with the calculation. From the curve, it seems that such a plot will have a broad maximum at about 1.2 K. One may infer from the heat-capacity plot of Hovi, Vuola, and Salmonpera⁽¹⁹⁾ that the curve of Wyatt's data has too small a temperature dependence as $T \rightarrow 0$ and that a shoulder rather than a maximum might be a more "natural" description of the C_p/T against T plot. However, the estimate from the extrapolation of 1.5 cal_{th} K⁻¹ mol^{-1} is quite reasonable. The enthalpy increment in this region was obtained by a similar extrapolation, and is given rather wide error limits; the enthalpy increment in the region 1.2 to 4.2 K was found directly.

The total heat capacity in the region near 5 K was approximated with the aid of other experiments. The lowest three points of this study seem to be in substantial error, as shown in figure 3. If the high-temperature magnetic-heat-capacity studies are to be regarded as correct, this contribution plus any reasonable lattice estimate forces the curve to reach a minimum between 7 and 8 K. Such calculations, using the Θ_D value of 118 K and the C_2 and C_3 values above were used to arrive at the short-dash curve of figure 3 as the probable heat capacity in the region 4.2 to about 8 K. This curve joins very well on the low-temperature side with Wyatt's data and on the high-temperature side with the curve of the present study at about 8 K. A further check on this drawn curve is that the difference in the heat capacity between GdCl₃ and EuCl₃ agrees fairly well with the calculated magnetic-heat-capacity in the region near 8 K. At higher temperatures, the experimental GdCl₃ curve lies higher but shows similar temperature dependence. This difference could be due to appreciably different acoustical heat-capacity contributions, although this would be



FIGURE 3. Low-temperature heat capacity of GdCl₃. \bigcirc , This research; \bigcirc , Wyatt;^(2, 15) ---, selected heat-capacity curve; ---, C_{mag} (reference 16); ----, $\{C_p(GdCl_3) - C_p(EuCl_3)\}$ for comparison with C_{mag} .

in contradiction to assumptions made for the other lighter halides of this study. There is also strong evidence that the lower lattice vibrational frequencies are smaller for $GdCl_3$ than for $EuCl_3$.⁽²⁰⁾ The dashed curve patching the two sets of calorimetric heat capacities, which, as seen above, has strong justification, was used to evaluate the entropy and enthalpy increments between 4.2 and 9 K as summarized in table 6.

T_1	T_2	$\underline{S^{\circ}(T_2)-S^{\circ}(T_1)}$	$H^{\circ}(T_2) - H^{\circ}(T_1)$	Source
K	К	$\operatorname{cal}_{\operatorname{th}} \mathrm{K}^{-1} \operatorname{mol}^{-1}$	cal _{th} mol ⁻¹	bource
0	1.2	1.499	1.2	a,b
1.2	4.2	2.397	4.463	c
4.2	5	0.043	0.261	d
5	9	0.099	0.734	d
9	298.15	32.15	4744.1	е
Total				
0	298.15	36.19	4750.8	

TABLE 6. Low-temperature entropy and enthalpy increments for $GdCl_3$ ($cal_{th} = 4.184 J$)

^a By difference between ^e and $R \ln 8$ (see text) based upon high-temperature expansion of C_{mag} of reference 16 using coefficients of reference 17.

^b Graphical estimation.

^e Data of Wyatt, references 2 and 15.

^a Graphical evaluation of selected curve.

^e Integration of fitted curve of points of this investigation.

4. Discussion

COMPARISON WITH ENTROPY ESTIMATION SCHEMES

In predicting the cation contribution to $S^{\circ}(298.15 \text{ K})$ to vary logarithmically with mass, the refined Latimer method⁽²¹⁾ implies that Gd(III) will contribute 14.3 cal_{th} K^{-1} mol⁻¹ in comparison with 13.8 cal_{th} K^{-1} mol⁻¹ for La(III). This trend is perhaps the failure of this method in its application to lanthanide salts. It appears that a universal feature of lanthanide-compound thermophysical behavior is that the heat capacity of the Gd(III) salt is lower over most of the temperature range than its La(III) analog. This requires the entropy of the Gd(III) salt to be lower, which is properly taken into account in the method of Westrum;⁽²²⁾ which originated from extension of an earlier scheme for transition element chalcogenides in an analysis of the heat-capacity data for the lanthanide sesquioxides. The scheme proposes a gradual decrease in the cation contribution with atomic number, from 15.2 cal_{th} K^{-1} mol⁻¹ for La(III) to 13.0 cal_{th} K^{-1} mol⁻¹ for Lu(III). The Latimer scheme is still useful in its prediction of the anion contribution. Latimer takes the value of 6.9 cal_{th} K^{-1} mol⁻¹ for Cl⁻ ion in salts of the formula MCl₃; this value was deduced from measurements on only two compounds, CrCl₃ and VCl₃, and thus is drawn from a limited data base which is without lanthanide "representation". The values of $S^{\circ}(298.15 \text{ K})$ available from Latimer scheme information are presented in table 7 under the heading "Latimer". Since the method of Westrum is correct in predicting the decrease in cation contribution and comes from lanthanide sources, it is of interest immediately to compare the Cl^{-} contribution implied by the present study with that of the Latimer scheme; such a comparison shows that a contribution of 5.9 $cal_{th} K^{-1} mol^{-1}$ obtains against that of 6.9 $cal_{th} K^{-1} mol^{-1}$ proposed by Latimer.

The magnetic contribution, as suggested by Westrum, can be approximated as $R \ln(2J+1)$. Addition of these approximate magnetic contributions to the Latimer

Commoniad		S	°(298.15 K) – S°(0)	
Compound			$cal_{th} K^{-1} mol^{-1}$		
	Latimer	Latimer augmented ^a	Westrum ^{a, b} augmented	"Spectro- scopic"	This investigation
LaCl ₃	34.5	34.5	33.1	32.47	32.88
CeCl ₃	34.5	38.1	36.1	35.99	(36.0) ^c
PrCl ₃	34.5	38.9	36.8	36.74	36.64 ^d
NdCl _a	34.6	39.2	36.8	36.84	36.67
PmCl ₃	34.7	39.5	36.8	36.82	(37.0)°
SmCl ₃	34.8	38.4	35.7	36.10	35.88
EuCl ₃	34.8	37.3	34.5	34.70	34.43
GdCl _a	35.0	39.1	36.0	36.60	36.19

TABLE 7. Comparison of some tribalide entropy estimation so

 $(cal_{th} = 4.184 J)$

^a By $R \ln(2J + 1)$; the (Cl₃)³⁻ ion contribution is taken as 20.7 cal_{th} K⁻¹ mol⁻¹.

^b By $R \ln(2J + 1)$; the $(Cl_3)^{3-}$ ion contribution is taken as 17.9 cal_{th} K⁻¹ mol⁻¹.

^e Parentheses denote values involving interpolated lattice and calculated Schottky contributions.

^a Based on 0.294 K.

and Westrum cation values (the latter augmented with the adjusted Cl⁻ contribution) appear in table 7 as "Latimer + $R \ln(2J+1)$ " and "Westrum, augmented", respectively.

A further option represents values obtained by recourse to spectroscopic information. Employing the Θ_D value of Varsanyi and Maita⁽¹²⁾ of 118 K for LaCl₃ as the only "calorimetric" input and using the energy levels of Ln(III) ions in LaCl₃ of Dieke⁽²³⁾ and the calculated frequencies of Stedman and Newman⁽¹³⁾ for LaCl₃, the entropies of the salts can be derived as shown under the heading "Spectroscopic". This last and rather convoluted estimate does not display the established decrease with cation mass but further refinement—although within the bounds of spectroscopic information—would be too heavily biased by hindsight. Hence, this estimate incorporates only previously available information and the cation-attendant decrease is used in proposing the entropy values for CeCl₃ and PmCl₃; these latter are left as a benchmark for comparison with future determinations.

THERMODYNAMICS OF FORMATION AT 298.15 K

The values of $\Delta H_{f}^{\circ}(298.15 \text{ K})$ reported by Schumm, Wagman, Bailey, Evans, and Parker⁽²⁴⁾ in the recent N.B.S. Technical Note 270-7 are used in calculating the values of $\Delta G_{f}^{\circ}(298.15 \text{ K})$. For Cl₂(g) the recommended value from CODATA Bulletin 10⁽²⁵⁾ (53.29 cal_{th} K⁻¹ mol⁻¹) is used for S°(298.15 K); this value is identical to that listed in the JANAF tables⁽²⁶⁾ which is the source of C_{p}° at 298.15 K (8.111 cal_{th} K⁻¹ mol⁻¹). The estimates of C_{p}° and S° at 298.15 K of this study are used for CeCl₃. The values for ΔG_{f}° shown in table 8, are invariably quite negative, well below

Compound	$\Delta H_{ m f}^{ m o}$	ΔS_{f}° b.c	$\Delta G_{ m f}^{\circ}$	$\Delta C_{p, f}$ d	
Compound	kcal _{th} mol ⁻¹	$\operatorname{cal_{th}} K^{-1} \operatorname{mol}^{-1}$	$kcal_{th} K^{-1} mol^{-1}$	$\operatorname{cal}_{\operatorname{th}} \mathbf{K}^{-1} \operatorname{mol}^{-1}$	
LaCl ₃	-256.0	60.65 ^e	-237.9	4.78	
CeCl ₃	-251.8	$(-61.14)^{f}$	(-233.6)	(4.89)	
PrCl ₃	-252.6	-60.79	-234.5	4.98	
NdCl ₃	-248.8	-60.36	-230.8	4.99	
PmCl ₃	$(-245)^{q}$	$(-60.2)^{h}$	(-277)		
SmCl ₃	-245.2	-60.68	-227.1	4.56	
EuCl ₃	-223.7	-63.79	-204.7	6.79	
GdCl ₃	241	-60.01	-223	2.35	

TABLE 8. Thermodynamics of formation for $LnCl_3$ at 298.15 K $Ln(c) + \frac{3}{2}Cl_2(g) = LnCl_3(c)^a$ $(cal_{ch} = 4.184 \text{ J})$

^a Parentheses indicate estimated values employed.

^b Reference 24.

° Table 7 for $S^{\circ}(\text{LnCl}_3, 298.15 \text{ K})$; reference 24 for Ln(c); Stuve, J. M. U.S. Bur. Mines, Rept. Invest. No. 6640 1965, for Cl₂(g).

 $^{\prime}C_{p}^{\circ}(Cl_{2}, g)$ taken from reference 26.

° α-form of La(c), reference 24.

^t γ -form of Ce(c), reference 24.

⁹ Estimated in Feber, R. C. U.S. At. Energy Comm. Rept. LA-3164 1964.

 ${}^{h}S^{\circ}(Pm, c, 298.15 \text{ K})$ estimated in Wicks, C. E.; Block, F. E. Thermodynamic properties of 65 elements—their oxides, halides, carbides and nitrides. Bur. Mines Bull. 605. U.S. Government Printing Office: Washington D. C. 1963.

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 $-200 \text{ kcal}_{th} \text{ mol}^{-1}$. The effect of the $T\Delta S_f^\circ$ term is to raise the ΔG_f° values relative to the ΔH_f° ones due to the large entropy of $\text{Cl}_2(g)$. The trend in ΔG_f° parallels that for ΔH_f° , and indeed $\Delta G_f^\circ \approx \Delta H_f^\circ$.

OTHER THERMODYNAMIC MEASUREMENTS

Serious gaps exist in enthalpy measurements above 298.15 K for the series. Walden and Smith⁽²⁷⁾ have measured the enthalpy of CeCl₃ from 273.15 to 1200 K by the method of mixtures with a Bunsen ice calorimeter receiver. Using a copper-block drop calorimeter, Dworkin and Bredig made enthalpy measurements through the melting temperatures (T_m) for LaCl₃, PrCl₃, and NdCl₃,⁽²⁸⁾ and for GdCl₃,⁽²⁹⁾ but report only the quantities { $H^{\circ}(T_m) - H^{\circ}(298.15 \text{ K})$ }, ΔH_m , and ΔS_m . Data exist on the high-temperature vaporization behavior but the information available concerning gas-phase vibration frequencies is inadequate to allow a third-law analysis of these values.

SAMARIUM TRICHLORIDE

As noted previously, the results of the present investigation seem to disagree with other studies. Unfortunately, the spectroscopic information is somewhat limited compared with that of other members of the series. Experiments which might be able to reconcile the apparent differences have not been performed.

The energy level scheme for Sm(III) (and for Eu(III)) in LaCl₃ is shown in table 9. This is taken from Dieke⁽²³⁾ based on measurements of Magno and Dieke.⁽¹⁰⁾ Their data shows the ${}^{6}H_{5/2}$ ground state to consist of three Kramers' doublets at 0.0 ($\mu = 1/2$), 40.7 ($\mu = 3/2$), and 66.1 cm⁻¹ ($\mu = 5/2$). These levels are quite low and this implies a large Schottky heat capacity at low temperatures. In contrast to the situation for PrCl₃ and NdCl₃, the next J-state, ${}^{6}H_{7/2}$, is not insignificantly populated at 350 K; its lowest level and center of gravity lie at 992.8 and 1080.3 cm⁻¹, respectively. The second-higher J-state, ${}^{6}H_{9/2}$, makes an insignificant contribution, with its lowest level and center of gravity at 2211.7 and 2290.3 cm⁻¹. The calculated

J-state term	$SmCl_3^a \Delta E/cm^{-1}$	μ	g	J-state term	EuCl ₃ ^b $\Delta E/cm^{-1}$	μ	g
⁶ H _{5/2}	0.0	1/2	2	7F0	0.00	0	1
	40.7	3/2	2	${}^{7}F_{1}$	355.05	1	2
1	66.1	5/2	2	· •	405.27	Õ	1
⁶ H _{7/2}	992.8	3/2	2	⁷ F ₂	1022.54	2	2
• • •	1051.2	5/2	2	-	1027.54	1	2
	1104.7	1/2	2		1084.33	ō	1
	1172.6	5/2	2				
N	ext level at 2211	.7 cm ⁻¹		Ne	xt level at 1846.	77 cm ⁻¹	

TABLE 9. Crystal-field levels for SmCl₃ and EuCl₃; ΔE denotes the energy above ground, μ crystal quantum number, and g degeneracy of level

^a Reference 23. ^b Reference 40.

Schottky heat capacity reaches a minimum at 173.2 K and continues to rise beyond the highest temperature of the heat-capacity measurements (350 K) as a consequence of the ${}^{6}\text{H}_{7/2}$ levels. The lower-temperature maximum, due mostly to ${}^{6}\text{H}_{5/2}$ levels, occurs at 28.16 K and has the value 1.386 cal_{th} K⁻¹ mol⁻¹.

The comparison of the calculated and experimental curves is shown in figure 4. The qualitative features of the calculated curve, including the minimum, are reproduced by the experimental one, but there is serious disagreement between the two $T_{\rm max}$ values and in the heat capacities below 20 K. In this region the differences between lattice heat capacities should be small, so that the discrepancy in the region near 10 K, where the experimental Schottky heat capacity is too small by a factor of 2, together with the upward shift of nearly 20 per cent in the value of $T_{\rm max}$ argues strongly against the location of the $\mu = 3/2$ level at 40.7 cm⁻¹. (The single bad point seen in the figure 4 at about 32 K is the result of a mistake in switching on the adiabatic shields in the changeover from manual to automatic operation.) A slight shift in $T_{\rm max}$ might result from a marked difference in lattice heat capacities between LaCl₃ and SmCl₃, but as seen from the figure, this would hardly account for the



FIGURE 4. Schottky heat capacity for SmCl₃. \bigcirc , { $C_p(SmCl_3) - C_p(LaCl_3)$ }; ---, $C_v(Schottky, calc.)$.

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region of near-coincidence which occurs from about 38 to about 55 K. To find the type of behavior observed for $PrCl_3$ and $NdCl_3$, the experimental curve must be "shrunk" but not greatly displaced relative to the calculated one.

In view of the qualitative agreement found between the calculated and experimental curves, and of the solid footing upon which both may be presumed to rest, it is suggested that the rather stark discrepancy stems not from any inaccuracy in either of the two methods, but rather from a failure to meet the "appropriateness" criterion, demonstrated for $PrCl_3$ and $NdCl_3$,⁽¹⁾ whereby the spectroscopic energy levels are assumed not to vary in the process of extrapolation from, say, 2 per cent to 100 per cent of Ln(III). Why this should be so for Sm(III) but not for Nd(III) or Pr(III) is puzzling.

The studies which through measurements or otherwise bear on the positions of the energy levels of ${}^{6}H_{5/2}$ in SmCl₃ are summarized in table 10. These include the optical

μ	Opt. spect. ^b	e.p.r. ^c	i.r. Absorp. ^a	Paramag. Suscept. ^e	Spin-lattice rela Ref. f	exation Ref. g	Ref. h	C _p This study [‡]
5/2	66.1	52.6 ¹ 38.5 ^k	65	Possibly between 11 and 99 cm ⁻¹				70 ± 5
3/2	40.7	49.9 39.0	40	Possibly between 10.7 and 66 cm ⁻¹	Apparently consistent with Dieke and Magno ⁽¹⁰⁾	30.8	32	55 ± 3

TABLE 10. Energy levels of ${}^{6}H_{5/2}$ for SmCl₃, ${}^{a}\Delta E/cm^{-1}$, and crystal quantum number μ

^a In all cases, $\mu = 1/2$ is taken at 0.0 cm⁻¹. ^b By optical spectroscopy; Magno and Dieke, reference 10. ^c By e.p.r.; Hutchison and Wong, reference 30. ^d By far-infrared absorption; reference 31. ^e By paramagnetic susceptibility; Thomas, reference 34. ^f By spin-lattice-relaxation; Mikkelson and Stapleton, reference 32. ^g By spin-lattice-relaxation; Mangum and Hudson, reference 33. ^h By heatcapacity data: Colwell *et al.*, reference 9. ^f By heat-capacity data; this research. ^f Without correction of PrCl₃ crystal field parameters to Z = 62 [Sm(III)]. ^k With this correction.

spectra of Magno and Dieke,⁽¹⁰⁾ on which the calculated curve is based, the e.p.r. work of Hutchison and Wong,⁽³⁰⁾ and far-i.r. absorption study of Hadni,⁽³¹⁾ the heat-capacity results of Colwell, Mangum, and Utton,⁽⁹⁾ the spin-lattice relaxation experiments of Mikkelson and Stapleton⁽³²⁾ and of Mangum and Hudson,⁽³³⁾ and the paramagnetic susceptibility study of Thomas.⁽³⁴⁾ Also shown are the values which provide the best fit to the heat capacities of the present investigation below about 17 K and best reproduce the experimental value of T_{max} . These are found to be $(55 \pm 3) \text{ cm}^{-1}$ for $\mu = 3/2$ and $(70 \pm 5) \text{ cm}^{-1}$ for $\mu = 5/2$. Several alternatives were explored; the heat capacity below 17 K proved to be fairly sensitive to the choice for $\mu = 3/2$ and the value of T_{max} rather less so. This trial-and-error fitting process produced no combination of the two excited levels which fitted the experimental difference well. The difference between the experimental and calculated Schottky curves requires a marked upward shift in the $\mu = 3/2$ level. As for the less-serious

discrepancy observed for PrCl₃⁽¹⁾ the most favorable temperature region over which to compare the trial level spacings and the experimental curve is from about 7 K to 19 K. The shape of the curve is such that it seems to be "too high" at the lower end and "too low" at the high-temperature end. Indeed, by choosing values for $\mu = 3/2$ which fit over successive limited temperature ranges, the experimental curve can be mimicked by a Schottky function in which the $\mu = 3/2$ level rises in value by about $1 \text{ cm}^{-1} \text{ K}^{-1}$. There is certainly no provision for this type of behavior in the simple Schottky model. The studies of references 10 and 30 to 33 employed Sm(III)-doped LaCl₃ in mole percentages of less than 5. References 9 and 34 report studies carried out on pure SmCl₃. Some of the authors acknowledge the presence of Sm(II) as impurity in the crystal preparations. The Sm(II) fluorescence spectrum was first studied by Dieke and Sarup⁽³⁵⁾ in an effort to account for some unclassified lines in the spectra of Sm(III) and Tm(III) in LaCl₂. Eisenstein, Hudson, and Mangum⁽³⁶⁾ reported serious contamination by Sm(II) in their attempts to grow crystals of SmCl₃. Mikkelson and Stapleton⁽³²⁾ note that their crystals of Sm(III) in LaCl₃ were orange in color. Sm(II) salts are reddish-brown, whereas SmCl₃ is cream-colored. The existence of Sm(II) in the crystals should not give rise to spurious levels of low energies since it is isoelectronic with Eu(III) and its lowest level is at 272 cm^{-1} . A more serious consideration is the local distortion in the crystal lattice caused by the presence of the Sm(II), possibly by the occurrence of an interstitial positive ion, as suggested by Dieke,⁽³⁷⁾ which would disturb the hexagonal symmetry of the Ln(III) ion.

The paramagnetic-susceptibility studies were hampered in their flexibility to adjust energy levels to fit the susceptibilities, which unfortunately go down only to about 80 K, somewhat above the temperature region where the levels are being populated most rapidly. The equation used to describe the susceptibility is limited to a definite relation between the $\mu = 3/2$ and $\mu = 5/2$ levels and trial values between rather wide limits ($\mu = 3/2$; 10.7 to 66 cm⁻¹; $\mu = 5/2$; 11 to 99 cm⁻¹) do not give good agreement with the experimental data.

Spin-lattice relaxation measurements are limited in elucidating the separation between the ground and first excited state. For Kramers' salts, this is dependent upon the resolution of the relaxation rate, τ^{-1} , into contributions for each of the three relaxation processes, the direct, the Orbach, and the Raman processes, ⁽³⁸⁾ by an equation of the form:

$$\tau^{-1} = AT + B \exp(-\Delta/kT) + CT^9,$$

where A, B, and C are constants and Δ is the energy increment between the ground and first excited levels ($\mu = 3/2$ in the case of SmCl₃). In their study of LaCl₃ containing 0.2 to 0.5 per cent Sm(III) from 1 to 4.2 K, Hudson and Mangum⁽³³⁾ found that subtraction of direct and Raman rates left an Orbach contribution consistent with $\Delta = 30.8$ cm⁻¹, a value which is in good agreement with a 20 per cent reduction (to 32 cm⁻¹) of the spectroscopic value implied by the heat-capacity data.⁽⁹⁾ In measurements with the magnetic field parallel to the crystal c-axis, Mikkelson and Stapleton⁽³²⁾ find, over the temperature range 1.65 to 4.2 K, a fairly good fit to the above equation for samples containing 0.1 per cent Sm(III). They take the spectroscopic value for Δ , yet their Λ and B constants differ from those of Hudson and Mangum. Thus, the two experiments lead to somewhat different conclusions regarding Δ . The authors of reference 33, in commenting upon their results for Er(III), Ce(III), Nd(III), Ho(III), and Sm(III) ask the questions, also of concern to the present study, ". . . is Δ actually invariant for a particular ion . . .?" and "Can variations in the preparations of dilute crystals cause real variations in Δ ?"

If the higher displacement of the spectroscopic levels suggested by the present study is to be attributed to variation with composition, spectroscopic studies on variable mole fractions of Sm(III) might be expected to resolve the discrepancies. In the absence of such information it is of interest to speculate on possible effects of substitution of the paramagnetic cation into LaCl₃. For the lighter trihalides this substitution is into a matrix which, although isostructural, is characterized by larger lattice parameters; the effects should be greater for the members of larger atomic number. McLaughlin and Conway⁽³⁹⁾ have investigated the shifts in spectral lines of Pr(III) for appreciable mole fractions in LaCl₃, CeCl₃, NdCl₃, SmCl₃, and GdCl₃. The only crystal-field level of ${}^{3}H_{4}$ which was measured was $\mu = 3$ and it was seen to shift nearly linearly to lower energies with decreasing cation radius of the host, from 33.8 cm⁻¹ in LaCl₃ to 25 cm⁻¹ in GdCl₃; this shift to lower energies was found for all of the lines studied. The solution of Sm(III) in LaCl₃, on this argument, would be accompanied by a shift towards higher energies relative to that for pure SmCl₃. Since the spectroscopic levels are so low, no explanation for the observed heat capacity results. The position of T_{max} is not highly dependent on the choice of this lattice heat capacity.

EUROPIUM TRICHLORIDE

The calculated heat capacity for EuCl₃ must include the non-degenerate ⁷F₀ ground state and also the ${}^{7}F_{1}$, ${}^{7}F_{2}$, and ${}^{7}F_{3}$ J-states; the lowest levels and centers of gravity of the last three are at 355.05 and 371.79, 1022.54 and 1036.89, 1846.77, and 1887.13 cm⁻¹, respectively.⁽⁴⁰⁾ The calculated curve is shown in figure 5 together with the difference of the curves for EuCl₃ and LaCl₃. Since the lowest level is so energetic, the Schottky maximum will occur at a relatively high temperature and will be enhanced in width with respect to those for smaller level spacings. Hence, the experimental (total) heat capacity of EuCl₃ (see figure 1) lies above all the others at temperatures above about 150 K. The calculated maximum (2.286 $cal_{th} K^{-1} mol^{-1}$) is at 251 K. The experimental curve reaches a plateau centered at about 250 K, then begins to rise slightly near 300 K. This latter feature may be occasioned in part by the accumulated error in the subtractions which bring out small irregularities in the heat capacities of both EuCl₃ and LaCl₃. If the experimental curve were drawn with the proper curvature through the region where it appears to dip (near 270 K), only the point at 269 K lies outside the 0.2 per cent error limit (the high point at 246 K was not reproduced in subsequent redeterminations). There are no deviations greater than 0.08 per cent from the fitted curve. The third derivative of the total heat capacity will go to zero at about 292 K, and irregularities are exaggerated when the curve for $LaCl_3$ (which is about 92 per cent of the heat capacity of $EuCl_3$) is subtracted. None-



FIGURE 5. Schottky heat capacity for EuCl₃. \bigcirc , { $C_p(SmCl_3) - C_p(LaCl_3)$ }; --, C_v (Schottky, calc).

theless, the dip is slightly outside the stated error limits for the total heat capacity of $EuCl_3$.

The calculated Schottky heat capacity is effectively zero (less than 0.001 cal_{th} K^{-1} mol⁻¹) below about 39 K. This allows the effect of the difference in lattice heat capacity of EuCl₃ and LaCl₃ to be strikingly apparent since the experimental difference reaches a minimum at about 90 K before the rise of the Schottky contribution forces the curve rapidly upward. Similar—but more subtle—behavior was found for NdCl₃ near 20 K; it clearly demonstrates the inadequacy of LaCl₃ as a suitable lattice heat-capacity contribution. The minimum in the experimental Schottky heat capacity for EuCl₃ corresponds to the diminished heat capacity in the same temperature region for the other Schottky-containing compounds. When the lattice heat-capacity differences and experimental errors are allowed for, the irregularities in the experimental Schottky curves are quite small.

Upon heating $EuCl_3$ it transforms from a pale lemon-yellow color at 300 K to a darker and much more intense color. Near 570 K, the color was very intense, and the luster almost metallic. This intensification could be due to increased population of

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the ${}^{7}F_{1}$ J-state (the ${}^{7}F \rightarrow {}^{5}D$ transition is responsible for the color) since it was found that the compound becomes white upon immersion in liquid nitrogen. It might, however, be speculated that some other process becomes important near 300 K. The population change is entirely within the bounds of the Schottky phenomenon and would not be expected to cause anomalous heat-capacity behavior. This would, however, not necessarily be true for a more complicated electronic event. Noting the temperature-dependent color of EuBr₃, Haschke⁽⁴⁾ has suggested a charge-transfer process for that compound, which culminates in the loss of Br₂. Since the same is true for EuCl₃ (although significant loss of Cl₂ occurs only at appreciably higher temperatures), such a mechanism might be responsible for the heat-capacity behavior observed at the high-temperature end of the present investigation. Charge-transfer spectra have been found by Barnes and Pincott⁽⁴¹⁾ for SmCl₃ and EuCl₃; these occur as broad bands in the 300 K powder, reflection spectra at 37200 and 28000 cm⁻¹, respectively, and correlate roughly with the reduction potentials of Ln(III) ions.

LATTICE HEAT CAPACITIES OF LaCl₃ AND GdCl₃

Although there is no Schottky contribution for $GdCl_3$, the difference in heat capacity between LaCl₃ and GdCl₃ is informative. The experimental difference will be strongly affected by the extended "tail" of the ferromagnetic ordering transition, which gives a significant contribution up to about 30 K, as found from the measurements of Clover and Wolf.⁽¹⁷⁾ Over the rest of the temperature region, the difference should



FIGURE 6. Lattice heat capacity for GdCl₃. \bigcirc , { $C_p(GdCl_3) - C_p(LaCl_3)$ }; ---, { $C_v(GdCl_3) - C_v(LaCl_3)$ } based on Raman frequencies; ---, { $C_v(GdCl_3)$, calculated, frequencies of reference 42) - $C_v(LaCl_3)$, calculated, frequencies of reference 13)}.

be a good indication of the difference in lattice heat capacity across the series, for this pair of compounds should exhibit the maximum difference in the series. The quantity $\{C_p(GdCl_3) - C_p(LaCl_3)\}$ is plotted as the solid line in figure 6. Also shown in this figure as the dashed line is the difference in heat capacity calculated by the use of Einstein heat-capacity functions of the 10 Raman frequencies for GdCl₃,^(20, 42) and for LaCl₃.^(43, 44) As expected, this difference is less pronounced since only 10 of the 21 optical frequencies are included. The dot-dash line in the figure is the difference in the complete set of frequencies which have been calculated for LaCl, by Stedman and Newman⁽¹³⁾ and for GdCl₃ by Dawson and Schaack.⁽⁴²⁾ It is seen that the values of T_{\min} determined by the experimental and the two calculated methods agree quite closely, so that spectroscopic values indicate not only that the heat capacity of LaCl₃ is greater than that of GdCl₃, but semi-quantitatively account for the difference. The findings of Cohen and Moos^(45, 46) from the vibronic spectra of Pr(III) in some of the other salts provide another point of comparison, even though the transitions observable in the spectra cannot be unambiguously assigned. If a direct average over the frequencies which have the same assignment (or "ambiguity" of assignment) for LaCl₃ and GdCl₃ is taken, an "average vibronic" frequency results which can be compared with weighted (according to the degeneracy of each mode) "average Raman" and "average calculated" frequencies. The results are summarized in table 11. It is seen that the different experimental methods produce

Summations	LaCl ₃	Difference	
Average Raman ^a	176.9	182.7	5.8
Average vibronic	171.5	176.2	4.7
Average calculated ^a	177.5	184.0	6.5

TABLE 11. Comparison of averaged assigned wavenumbers σ

^a Weighted by degeneracies of each mode.

roughly the same average frequency with approximately the same difference in these quantities for the two compounds. Similar correlations can be made between $LaCl_3$ and the other members of the series, though the effect of differences in lattice heat capacity are not so pronounced as for the $LaCl_3$ -GdCl₃ pair.⁽⁴⁷⁾

LATTICE ENTROPIES

The confidence with which the lattice entropy deduced from the total heat capacity can be specified up to 298.15 K is somewhat limited, since it depends on the quality of the Schottky resolution. By restricting the region of comparison to the interval 10 to 298.15 K. the difficulties associated with extended short-range ordering contributions to the magnetic heat capacity can be avoided (except for GdCl₃ for which the magnetic entropy implied by the expansion formula of Marquard⁽¹⁶⁾ using the coefficients of Clover and Wolf⁽¹⁷⁾ must be deducted). The calculated Schottky entropies are deducted from the total (except for SmCl₃ where the optimal energy levels inferred from the best fit to the experimental difference between the heat capacity of $SmCl_3$ and $LaCl_3$ are used). The remaining monotonic decreasing quantities, designated $S_{lattice}^{\circ}(LnCl_3)$, or lattice entropies, have values 32.84, 32.48, 32.28, 32.20, 32.16, and 32.10 cal_{th} K⁻¹ mol⁻¹ for LaCl₃, PrCl₃, NdCl₃, SmCl₃, EuCl₃, and GdCl₃, respectively. These may be compared graphically with Westrum's cation contributions as in figure 7 by plotting the cation values as the abscissa and the



FIGURE 7. Lattice entropy comparison. —, relationship between lattice entropies of this study and those of Westrum;⁽²²⁾ ---, hypothetical line of equality of measured entropy and Westrum's cation lattice-entropy contributions.

quantity $\{S_{lattice}^{\circ}(LnCl_3) - S_{lattice}^{\circ}(LaCl_3)\}\$ as the ordinate. The points (except for NdCl₃) fall fairly close to the line drawn. The deviation of NdCl₃ (lattice entropy too large by about 0.1 cal_{th} K⁻¹ mol⁻¹) could arise from an imperfect resolution of the Schottky contribution, although no strong argument is made for this. If the experimental differences in $S_{iattice}^{\circ}$ as measured by this investigation were identical to the Westrum values, the line determined by the points would subtend a 45° angle with the abscissa, shown as the dashed line. That this is not the case is not surprising. Coincidence would require at a minimum, that the Ln^{3+} —Cl⁻ and the Cl⁻—Cl⁻ force constants remain the same over the series and that the crystal structure be as "good" for GdCl₃ as for LaCl₃; available evidence seems to deny this. The figure is used to obtain corrected values for $S_{iattice}^{\circ}$ for CeCl₃ and PmCl₃; these are used as the basis for estimation of $S^{\circ}(298.15 \text{ K})$ in the last column of table 7.

An attempt was made to correlate the $S_{lattice}^{\circ}$ values with several parameters such as molar volume, Ln(III) cation radius, density, atomic number, *etc.* As might be expected from the near-linearity of the plot in figure 7, the best correlation was found with the Ln(III) cation radius, though its superiority to those with other parameters was not great. Further correlations of the trends in lattice heat capacities are discussed elsewhere.⁽⁴⁷⁾

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