

THE LOWEST $T = 0$ STATES IN THE ODD $N = Z$ NUCLEI WITH $A > 40$

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Abstract: There is indication that the lowest $T = 0$ and $T = 1$ states are inverted not only in Cl^{34} but also in Sc^{42} , V^{46} , Mn^{50} and Co^{54} . Isomerism in all these nuclei is likely.

The β -decays of the odd self conjugate nuclei in the $f_{7/2}$ -shell, namely Sc^{42} , V^{46} , Mn^{50} and Co^{54} have superallowed character with ft -values^{1, 2)} close to the ft -value of the O^{14} -decay. Consequently the transitions are $0^+ \rightarrow 0^+$ transitions between states of isobaric spin $T = 1$. There is only little information about the lowest $T = 0$ states in these nuclei.

Fig. 1 shows a plot^{3, 4)} of the known energy differences⁵⁾ Δ_{10} between the lowest $T = 1$ and $T = 0$ states for the odd and even selfconjugate nuclei as a function of A . Some values have been calculated⁵⁾. The lowest $T = 0$ states in the nuclei with $A < 40$ are the ground states except in Cl^{34} . From an extrapolation of the set of values for the odd nuclei and a comparison with the set of values for the even nuclei one would expect the heavy odd nuclei ($A > 40$) to have energies Δ_{10} up to about ± 0.5 MeV. Thus the lowest $T = 0$ states in Sc^{42} , V^{46} , Mn^{50} and Co^{54} should be up to about 0.5 MeV above or below the known states with 0^+ , $T = 1$.

This also has another consequence. Assuming the $T = 0$ states to be lower, these states have to undergo β -decay (allowed or forbidden, but not superallowed). The known $T = 1$ states are thus isomeric states like Al^{26m} or K^{38m} . Spin and parity of 1^+ for a $T = 0$ ground state is excluded from the existence of the superallowed decay. Assuming the lowest $T = 0$ states are higher, you have inversion of the $T = 0$ and $T = 1$ states. This condition was known up to now only in Cl^{34} . Also in this case isomerism is likely if spin and parity of the $T = 0$ states is not 1^+ , but 3^+ , 5^+ or 7^+ .

To get information about the lowest $T = 0$ state in Sc^{42} a search was undertaken for a long-lived activity with emphasis for a 14 d half-life. Walke⁶⁾ in 1940 bombarded KCl with α -particles and found such an activity which he

† Most of this work was carried out while on leave of absence from the Max-Planck-Institut für Kernphysik, Heidelberg.

assigned to Sc^{42} . In our experiment no long-lived Sc^{42} activity could be found †. Instead a weak 14 d activity was found but assigned to P^{32} which was produced from the bombardment of KCl with 43 MeV α -particles †† according to the reaction $\text{Cl}^{35}(\alpha, \alpha 2p n)\text{P}^{32}$. This is the same reaction †) which produces Na^{24} from Al^{27} with relatively high cross section.

Recent measurements †) at another laboratory show the existence of an excited isomeric state in Sc^{42} which undergoes an allowed β^+ -decay with a half-life of 62 ± 4 sec. The spin of Sc^{42m} is probably 7^+ . Also in Co^{54} an excited

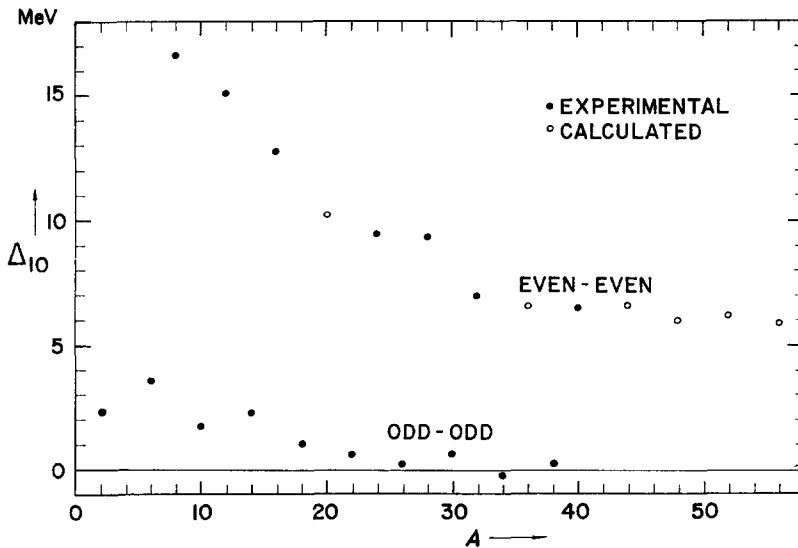


Fig. 1. Energy differences Δ_{10} between the lowest $T = 1$ and $T = 0$ states in the odd and even $N = Z$ nuclei as a function of A . Data taken from ref †) The estimated error for the calculated energies is ± 200 keV. The experimental errors are ± 100 keV for the even nuclei from $A = 24$ on, less for the other nuclei

long-lived isomeric state was found †) with spin 7^+ . These results indicate that it is likely that also in V^{46} and Mn^{50} the lowest $T = 0$ and $T = 1$ states are inverted and that long-lived isomeric states exist. Spins of 3^+ or 5^+ should result in allowed β -transitions with half-lives of the order of 1 min †††. Measurements are in progress.

† Re-examination of a decay curve of the activities obtained from the bombardment of KF with 20 MeV α -particles showed an activity with a half-life of 63.3 ± 1.7 sec. It follows from later experiments (see next paragraph) that this activity has to be interpreted as that of Sc^{42m} .

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††† Note added in proof: The author's attention has been called to the fact that a Mn^{50} activity with a half-life of 2 min has already been observed †)

The selfconjugate odd nuclei belong to those nuclei which follow the revised ¹⁰⁾ Nordheim rule R 2. This rule states that the spin of the ground state should be $J = |J_1 \pm J_2|$. The rule seems to be violated in Cu^{58} , the first odd selfconjugate nucleus in the $2 p_{3/2}$ -shell. Rule R2 favours spins of 0 or 3. From the allowed β -decay ¹¹⁾ with 3.3 sec half-life it follows that the ground state spin for Cu^{58} is 0^+ or 1^+ . A spin of 0^+ however is very likely to imply $T = 1$ and consequently a superallowed β -decay which is in disagreement with the experimental evidence ¹¹⁾. This implication is strictly true only for jj -coupling and with the proton and neutron in equivalent orbits ⁴⁾. The state with 0^+ , $T = 1$ is expected at an excitation ⁵⁾ of 110 ± 150 keV, assuming a discontinuity of 150 keV for the Coulomb energy difference at $A = 54$. If the 0^+ , $T = 1$ state is an excited state, M1 γ -radiation suppresses the superallowed β -transition, which is actually not observed as in P^{30} .

A violation of rule R 2 can be shown from theoretical calculations ¹²⁾ with jj -coupling and extreme δ -function interaction. These calculations show that for the ground states of selfconjugate nuclei spins of 0, 1 and $2J_1$ are possible rather than only 0 and $2J_1$.

In addition these calculations predict for Sc^{42} with a groundstate of 0^+ a spin sequence of 0^+ , 1^+ , 7^+ . Other shell model calculations ¹³⁾ favour the 7^+ state as the lowest odd spin $T = 0$ state. Calculations in terms of the collective model ¹⁴⁾ are not quite conclusive and give negative as well as positive deformation at the beginning of the $f_{7/2}$ -shell, i.e., 7^+ or 1^+ for the level of interest.

The above considerations show that the inversion of the lowest $T = 0$ and $T = 1$ states seems to be restricted to Cl^{34} and the four odd selfconjugate nuclei in the $f_{7/2}$ -shell namely Sc^{42} , V^{46} , Mn^{50} and Co^{54} , and that isomerism in all these nuclei is likely.

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