# Vibrational Analysis of Peptides, Polypeptides, and Proteins. XVIII. Conformational Sensitivity of the $\alpha$-Helix Spectrum: $\alpha_{I^{-}}$and $\alpha_{\text {II }}$-Poly(L-alanine) 

ANIL M. DWIVEDI and S. KRIMM, Biophysics Research Division, University of Michigan, Ann Arbor, Michigan 48109

## Synopsis

The $\alpha_{\mathrm{II}}$-helix ( $\phi=-70.47^{\circ}, \psi=-35.75^{\circ}$ ) is a structure having the same $n$ and $h$ as the (standard) $\alpha_{I^{-}}$-helix ( $\phi=-57.37^{\circ}, \psi=-47.49^{\circ}$ ). Its conformational angles are commonly found in proteins. Using an improved $\alpha$-helix force field, we have compared the vibrational frequencies of these two structures. Despite the small conformational differences, there are significant predicted differences in frequencies, particularly in the amide A, amide I, and amide II bands, and in the conformation-sensitive region below $900 \mathrm{~cm}^{-1}$. This analysis indicates that $\alpha_{\text {II }}$-helices are likely to be present in bacteriorhodopsin [Krimm, S. \& Dwivedi, A. M. (1982) Science 216, 407-408].

## INTRODUCTION

Our recent work on $\beta$-sheet polypeptides ${ }^{1,2}$ and on $\beta$-turns ${ }^{3-8}$ has amply demonstrated the sensitivity of the vibrational frequencies of such molecules to relatively large changes in the conformation. Our earlier work on $\alpha$-helical poly(L-alanine) $\left.{ }^{9}[\alpha \text {-(Ala })_{n}\right]$ had also shown that the $\alpha$-helix frequencies can be sensitive to small changes in conformation. In this case, it is the result of changing $h$, the rise per residue, by a very small amount while keeping $n$, the number of residues per turn, constant. Such small structural changes seemed to be responsible for frequency changes that occur as a result of changing the temperature of the sample. ${ }^{9}$
In the present study, we were interested in a specific and relatively small conformational change that the $\alpha$-helix can undergo at constant $n$ and $h$. This occurs because, in general, there are two possible solutions for the dihedral angles $\phi$ and $\psi$ when the above helix parameters are kept constant. ${ }^{10}$ One of these solutions corresponds to the standard helix, which we designate the $\alpha_{\mathrm{I}}$-helix, and the other is a slightly modified structure, which we designate the $\alpha_{\mathrm{II}}$-helix. These differ primarily in that in the $\alpha_{11}$-helix, the plane of the peptide group has more tilt with respect to the helix axis, resulting in an $\mathrm{N}-\mathrm{H}$ bond that distinctly points toward the axis. The consequence is a bent $\mathrm{N} \cdots \mathrm{H} \cdots \mathrm{O}=\mathrm{C}$ hydrogen bond, and in extreme cases, an $\mathrm{N} \cdots \mathrm{O}$ distance that is inconsistent with a hydrogen bond. ${ }^{11}$

Although the difference in $\phi, \psi$ is small, x-ray crystallographic data on several proteins indicate that there are $\alpha$-helical segments that have dihedral angles corresponding to the $\alpha_{\text {II }}$ conformation: three segments (residues 29-35, 93-99, and 120-124) in lysozyme, ${ }^{12}$ two segments (residues

165-172 and 237-243) in $\alpha$-chymotrypsin, ${ }^{13}$ and one segment (residues $28-31)$ in chromatium high-potential iron protein. ${ }^{14}$ In fact, the conformation of $\alpha$-(Ala) $)_{n}$ in hexafluoroisopropanol has been shown to be incompatible with an $\alpha_{\mathrm{I}}$-helix, and an $\alpha_{\mathrm{II}}$-helix conformation has been proposed ${ }^{15}$ in this solvent. It is therefore important to understand the spectroscopic characteristics of these two structures and, in particular, to know whether the vibrational spectrum is sensitive to such small conformational changes.

The force field used in this calculation differs from that developed previously for $\alpha$-(Ala).$^{9}$ The main reasons for doing this further refinement of the force field were to incorporate a better-defined $x$-ray structure, ${ }^{16}$ to include a complete set of hydrogen-bond force constants, and, in the spirit of our earlier work on $\beta$-sheet polypeptides, ${ }^{1,2}$ to employ a force field with maximum transferability between different conformations. We have therefore done a refinement for $\alpha_{1}$-(Ala $)_{n}$ based on the transfer of force constants from $\beta$-(Ala) ${ }_{n}{ }^{2}$ and a consistent prediction of the frequencies of $\alpha_{\mathrm{I}}$-(Ala-ND) ${ }_{n}$. This force field was then used to calculate the frequencies of $\alpha_{\mathrm{II}}-(\mathrm{Ala})_{n}$. During this study, we observed that certain anomalies in the ir spectrum of the purple membrane of Halobacterium halobium ${ }^{17,18}$ could be accounted for by the $\alpha_{\text {II }}$ conformation, and a preliminary description of these conclusions, and their possible relevance to the proton conduction mechanism of this protein, has been reported. ${ }^{19}$

## NORMAL-MODE CALCULATION

## Structure

The helix parameters for the $\alpha_{\mathrm{I}}$-helix are the same as those used in our earlier work, ${ }^{9}$ viz., $n=3.62, h=1.495 \AA$, and $t$ (rotation per residue about the helical axis) $=99.57^{\circ}$, as are the bond lengths and bond angles. ${ }^{2,9}$ However, there is a significant difference in the dihedral angles. In this work, we have used values $\phi=-57.37^{\circ}$ and $\psi=-47.49^{\circ}$ derived by Arnott and Dover ${ }^{16}$ from an $\mathbf{x}$-ray diffraction refinement procedure. In order to keep the helical parameters the same and use Arnott's $\phi, \psi$, the value of $\tau$ (the $\mathrm{NC}^{\alpha} \mathrm{C}$ angle) has to be increased from the ideal tetrahedral value of $109.47^{\circ}$ to $109.87^{\circ}$. Another important difference is in $\chi_{1}$ (the rotation angle about the $\mathrm{C}^{\alpha}-\mathrm{C}^{\beta}$ bond). The value used earlier, ${ }^{9}$ viz., $\chi_{1}=0^{\circ}$, corresponds to an eclipsed position of a $\mathrm{CH}_{3}$ group hydrogen atom with respect to the backbone N atom. We feel that a staggered position is more appropriate and have used $\chi_{1}=60^{\circ}$, a value closer to that ( $\chi_{1}=57.50^{\circ}$ ) determined for $\beta$-(Ala) $)_{n}$ by energy minimization. ${ }^{20}$ A portion of the $\alpha_{\mathrm{I}}$-helix is shown in Fig. 1(a). The $\alpha_{\mathrm{II}}$-helix structure has been obtained using the second set of $\phi, \psi$ values $^{10}\left(-70.47^{\circ},-35.75^{\circ}\right)$ that correspond to the same helical parameters as for $\alpha_{\mathrm{I}}$. The $\alpha_{\text {II }}$ helix is shown in Fig. 1(b). As mentioned earlier, the peptide plane in $\alpha_{\text {II }}$ is tilted such that the $\mathrm{C}=\mathrm{O}$ bond points away from the helix axis and the $\mathrm{N}-\mathrm{H}$ bond points toward the helix

(a)

Fig. 1. $\alpha$-Helical structures of poly(L-alanine): (a) $\alpha_{\mathrm{I}}$-helix, (b) $\alpha_{I^{\prime}}$-helix.
axis. The results of such a structural change are that the hydrogen bonds are weaker in $\alpha_{\text {II }}$ than in $\alpha_{\mathrm{I}}\left(\right.$ for $\alpha_{\mathrm{I}}: r(\mathrm{H} \cdots \mathrm{O})=1.882 \AA, r(\mathrm{~N} \cdots \mathrm{O})=2.857$ $\AA, \angle \mathrm{NHO}=164.19^{\circ}, \angle \mathrm{HNO}=10.34^{\circ}$; for $\alpha_{\mathrm{II}}: r(\mathrm{H} \cdots \mathrm{O})=2.121 \AA, r(\mathrm{~N} \cdots \mathrm{O})$ $=3.001 \AA, \angle \mathrm{NHO}=145.65^{\circ}, \angle \mathrm{HNO}=23.51^{\circ}$ ) and the distance between the H's of adjacent NH groups decreases, from $2.79 \AA$ in $\alpha_{I}$ to $2.53 \AA$ in $\alpha_{\text {II }}$.
It may be worth noting that if the helical parameters are to remain the same, certain values of $\phi, \psi$ for the $\alpha_{\mathrm{I}}$-helix permit a much easier conversion to $\alpha_{\text {II }}$ than do others. If such flexibility is important (for example, allowing for a maximization of entropy), then these values for $\alpha_{I}$ will be favored (at present, variations of $\pm 8^{\circ}$ in $\phi$ and $\psi$ are commonly found in the literature). For example, whereas the $\alpha_{\text {I }}$ conformation that we use ${ }^{16}$ leads to an $\alpha_{\text {II }}$ conformation that is comparably allowed, ${ }^{21}$ the $\alpha_{\text {II }}$ conformation reported by Némethy et al. ${ }^{11}\left(-93^{\circ},-18^{\circ}\right)$, and based on standard bond lengths and angles as well as dihedral angles ( $-53^{\circ},-52^{\circ}$ for $\alpha_{\mathrm{I}}$ ), is not allowed. ${ }^{21}$

(b)

Fig. 1. (continued from the previous page)
For the normal-mode calculation, the internal and local symmetry coordinates of one chemical repeat unit have been defined in a way similar to that in the earlier work, ${ }^{22}$ except that the $\mathrm{H}^{\alpha} \cdots \mathrm{H}^{\alpha}$ interchain stretching coordinate is not required for the $\alpha$-helix. Thus, the chemical repeat unit has 39 internal coordinates compared with the 40 present in $\beta$-(Ala) $n_{n}{ }^{2}$ It is worth pointing out that in the earlier work on $\alpha$-(Ala) ${ }_{n},{ }^{9}$ only 35 internal coordinates of the chemical repeat unit were used, the four intrachain internal coordinates $\mathrm{NH} \cdots \mathrm{O}$ and $\mathrm{CO} \cdots \mathrm{H}$ in-plane angle bends and $\mathrm{NH} \cdots \mathrm{O}$ and CO $\cdots \mathrm{H}$ torsions having been neglected. Once the intrachain hydrogen bond is included in the calculation, a more complete treatment requires that the above-mentioned internal coordinates be included.

The optically active modes are classified into $\mathrm{A}\left(\delta=0^{\circ}\right), \mathrm{E}_{1}\left(\delta=99.57^{\circ}\right)$, and $\mathrm{E}_{2}\left(\delta=199.14^{\circ}\right)$ symmetry species, where $\delta$ is the phase difference between the motions in adjacent residues. The former two species are both ir and Raman active and the last is Raman active only. In the ir dichroic spectrum, the A modes are parallel and the $\mathrm{E}_{1}$ modes are perpendicular to the helical axis. There are $28 \mathrm{~A}, 29 \mathrm{E}_{1}$, and $30 \mathrm{E}_{2}$ modes. ${ }^{23}$

## Force Field

Except for the force constants associated with transition dipole coupling ${ }^{24,25}$ and the $\mathrm{H}^{\alpha} \ldots \mathrm{H}^{\alpha}$ interaction, the force field for $\beta$-(Ala) $)_{n}$ was used as a starting point ${ }^{2}$ for the refinement of the $\alpha$-(Ala $)_{n}$ force field. Appropriate changes were then made in some of the force constants in order to obtain more reasonable agreement between the predicted frequencies and the observed assigned bands. Most of the experimental data have been taken from our earlier work. ${ }^{9}$ For the polarized ir and far-ir spectra, and the relative intensities, the results of other authors have also been used. ${ }^{26-34}$ Transition dipole coupling constants were calculated using the same parameters as in the earlier work. ${ }^{9}$ In the $\alpha_{\mathrm{I}}$-helix, the contributions to the $\mathrm{A}, \mathrm{E}_{1}$, and $\mathrm{E}_{2}$ species for amide I are $-5.53,-7.24$, and $-16.82 \mathrm{~cm}^{-1}$, respectively, and for amide II they are $-9.64,6.17$, and $4.23 \mathrm{~cm}^{-1}$, respectively. In the $\alpha_{I I}$-helix, such contributions are $-0.93,-8.06$, and $-13.38 \mathrm{~cm}^{-1}$ and $-12.79,7.43$, and $5.97 \mathrm{~cm}^{-1}$, respectively. The variations result from the conformational differences between these two structures.

As in the transfer of force constants from (Gly I) $n_{n}(\beta$-structure) to (Gly II) ${ }_{n}\left(3_{1}\right.$-helix) ${ }^{35}$ the required changes in force constants in transferring the force field from $\beta$-(Ala) $n_{n}$ to $\alpha_{\mathrm{I}}$-(Ala) ${ }_{n}$ can be attributed to the differences in conformation and in hydrogen-bond parameters between the two structures. Of a total of 98 force constants transferred from $\beta$-(Ala) $)_{n}, 35$ required modification. A list comparing the unequal force constants of $\alpha$ - and $\beta$-(Ala) ${ }_{n}$ is given in Table I. Eleven force constants-namely, $f(\mathrm{CO})$, $f(\mathrm{NH}), f(\mathrm{H} \cdots \mathrm{O}), f\left(\mathrm{C}^{\alpha} \mathrm{NH}\right), f(\mathrm{CNH}), f\left(\mathrm{C}^{\alpha} \mathrm{CO}\right), f(\mathrm{NH} \cdots \mathrm{O}$ ib), $f(\mathrm{CO}$ ob), $f(\mathrm{NH}$ ob), $f(\mathrm{NCO})$, and $f(\mathrm{CO}$ ob, NH ob) -are directly influenced by the hydrogen bonds, and the differences in their values between $\alpha$ - and $\beta$-(Ala) ${ }_{n}$ are due to the weaker hydrogen bonds in the former $[r(\mathrm{~N} \cdots \mathrm{O})=2.857 \AA$ for $\alpha$-(Ala) $)_{n}$ ] as compared with the latter $\left.[r(\mathrm{~N} \cdots \mathrm{O})=2.732 \AA \text { for } \beta \text {-(Ala })_{n}\right]$. Fermi resonance analysis has been done for the amide $A$ and amide $B$ modes, ${ }^{36}$ and $f(\mathrm{NH})$ was adjusted so that the calculation predicts the unperturbed amide A frequency, ${ }^{36} \nu_{\mathrm{A}}^{\circ}=3279 \mathrm{~cm}^{-1}$. This value is significantly higher than that for $\beta$-(Ala $)_{n}$, viz., $3242 \mathrm{~cm}^{-1}$, consistent with the expectation that a weaker hydrogen bond leads to a stronger $\mathrm{N}-\mathrm{H}$ bond. The $f(\mathrm{NH})$ and $f(\mathrm{H} \cdots \mathrm{O})$ force constants for $\alpha$-(Ala $)_{n}$ are 5.83 and 0.120 $\mathrm{mdyn} / \AA$, respectively, compared to 5.674 and $0.150 \mathrm{mdyn} / \AA$ for $\beta$-(Ala) $)_{n}$. Except for $f\left(\mathrm{C}^{\alpha} \mathrm{H}^{\alpha}\right), f\left(\mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right), f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right), f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right)$, and $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right)_{\mathrm{G}}$, the remaining 19 force constants in Table I reflect the conformational differences between $\beta$ - and $\alpha$-(Ala $)_{n}$. It is interesting that this number is about twice as large as the 10 conformation-dependent force constants that needed changing in going from (Gly I) $n$ to (Gly II)n. ${ }^{35}$ The increase is not surprising, since in the latter case, only $\phi$ changes significantly [for (Gly I) $\phi=149.9^{\circ}$ and $\psi=146.5^{\circ}$, compared with $\phi=-76.9^{\circ}$ and $\psi=145.3^{\circ}$ for (Gly II) $\left.)_{n}\right],{ }^{35}$ whereas the change from $\beta$-(Ala) $)_{n}$ to $\alpha$-(Ala) $)_{n}$ involves a change in both $\phi$ and $\psi$, from $-138.38^{\circ}, 135.73^{\circ}$ to $-57.37^{\circ},-47.49^{\circ}$, respectively. ${ }^{2}$ The force constant $f\left(\mathrm{C}^{\alpha} \mathrm{H}^{\alpha}\right)$ had to be increased in $\alpha$-(Ala) ${ }_{n}$ in order to compensate for the absence of the $\mathrm{H}^{\alpha} \cdots \cdot \mathrm{H}^{\alpha}$

TABLE I
Comparison of Unequal Force Constants for $\alpha$ - and $\beta$-Poly(L-alanine)

| Force Constant ${ }^{\text {a }}$ | $\alpha^{\text {b }}$ | $\beta^{\text {b }}$ |
| :---: | :---: | :---: |
| $f\left(\mathrm{NC}^{\alpha}\right)$ | 4.323 | 4.523 |
| $f(\mathrm{CO})$ | 10.029 | 9.882 |
| $f(\mathrm{NH})$ | 5.830 | 5.674 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{H}^{\alpha}\right)$ | 4.523 | 4.463 |
| $f(\mathrm{H} \cdots \mathrm{O})$ | 0.120 | 0.150 |
| $f\left(\left(\mathrm{NC}^{\alpha} \mathrm{C}\right)\right.$ | 1.119 | 0.819 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{CN}\right)$ | 1.033 | 0.933 |
| $f\left(\mathrm{CNC}^{\alpha}\right)$ | 0.826 | 0.526 |
| $f(\mathrm{NCO})$ | 1.446 | 1.306 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{NH}\right)$ | 0.556 | 0.566 |
| $f(\mathrm{CNH})$ | 0.556 | 0.566 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{CO}\right)$ | 1.046 | 1.306 |
| $f\left(\mathrm{CC}^{\alpha} \mathrm{H}^{\alpha}\right)$ | 0.654 | 0.684 |
| $f\left(\mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right)$ | 0.615 | 0.518 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right)$ | 0.687 | 0.677 |
| $f(\mathrm{NH} \cdots \mathrm{O}$ ib) | 0.020 | 0.036 |
| $f(\mathrm{CO} \mathrm{ob})$ | 0.657 | 0.621 |
| $f(\mathrm{NH}$ ob) | 0.129 | 0.157 |
| $f\left(\mathrm{NC}^{\alpha} \mathrm{t}\right)$ | 0.087 | 0.037 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{Ct}\right)$ | 0.060 | 0.037 |
| $f\left(\mathrm{NC}^{\alpha}, \mathrm{C}^{\alpha} \mathrm{C}\right)$ | 0.100 | 0.300 |
| $f\left(\mathrm{NC}^{\alpha}, \mathrm{NC}^{\alpha} \mathrm{H}^{\alpha}\right)$ | 0.427 | 0.627 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}, \mathrm{CC}^{\alpha} \mathrm{H}^{\alpha}\right)$ | 0.305 | 0.205 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}, \mathrm{C}^{\alpha} \mathrm{CO}\right)$ | 0.100 | 0.200 |
| $f\left(\mathrm{CO}, \mathrm{C}^{\alpha} \mathrm{CN}\right)$ | 0.000 | 0.050 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta}, \mathrm{NC}^{\alpha} \mathrm{C}^{\beta}\right)$ | 0.517 | 0.617 |
| $f\left(\mathrm{NC}^{\alpha} \mathrm{C}, \mathrm{C}^{\alpha} \mathrm{CN}\right)$ | 0.160 | 0.000 |
| $f\left(\mathrm{NC}^{\alpha} \mathrm{C}, \mathrm{CO}\right.$ ob) | -0.073 | -0.173 |
| $f\left(\mathrm{NC}^{\alpha} \mathrm{C}, \mathrm{NH}\right.$ ob) | 0.160 | 0.110 |
| $f\left(\mathrm{NC}^{\alpha} \mathrm{C}^{\beta}, \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right)_{\mathrm{G}}$ | 0.000 | 0.040 |
| $f\left(\mathrm{CC}^{\alpha} \mathrm{H}^{\alpha}, \mathrm{CO} \mathrm{ob}\right)$ | -0.100 | 0.150 |
| $f\left(\mathrm{CC}^{\alpha} \mathrm{C}^{\beta}, \mathrm{CO}\right.$ ob) | -0.050 | 0.162 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right)$ | -0.020 | -0.045 |
| $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right)_{\mathrm{G}}$ | 0.000 | 0.100 |
| $f(\mathrm{CO}$ ob, NH ob) | -0.050 | 0.000 |

${ }^{\text {a }} f(\mathrm{AB})=\mathrm{AB}$ bond stretch, $f(\mathrm{ABC})=\mathrm{ABC}$ angle bend, $f(\mathrm{X}, \mathrm{Y})=\mathrm{XY}$ interaction; $\mathrm{ib}=\mathrm{in}-$ plane bend, $\mathrm{ob}=$ out-of-plane bend, $\mathrm{t}=$ torsion, $\mathrm{G}=$ gauche .
${ }^{\mathrm{b}}$ Units are mdyn/ $\AA$ for stretch and stretch, stretch force constants, mdyn for stretch, bend force constants, and mdyn $\AA$ for all others.
interaction. Although we do not have a good understanding of the reasons for changes in $f\left(\mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right), \quad f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right), f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}\right)$, and $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right)_{\mathrm{G}}$, we were forced to modify these force constants. This was a consequence of the low predicted frequency for a band observed near $1310 \mathrm{~cm}^{-1}$ and assignable to $\mathrm{H}^{\alpha}$ bend, as is a similar band in $\beta$-(Ala) $)_{n}$. In order to raise the low predicted value in $\alpha$-(Ala) $)_{n}$, and to keep an assignment similar to that in $\beta$-(Ala $)_{n}$, the $f\left(\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{H}, \mathrm{H}^{\alpha} \mathrm{C}^{\alpha} \mathrm{C}^{\beta}\right)_{\mathrm{G}}$ force constant, which
was found to be the most influential, had to be reduced to zero. When this was done, the other three force constants required only slight adjustments.
It should be noted that this refinement preserves a high degree of transferability in the basic force field. When we consider $\alpha_{\mathrm{I}}$-(Ala $)_{n}$ in the context of the global refinement for (Gly I) $)_{n},{ }^{1}(\mathrm{Gly} \mathrm{II})_{n},{ }^{35} \beta$-(Ala) $)_{n},{ }^{2}$ and $\beta$-(Ala Gly) (unpublished results), we find that about 550 frequencies have been fitted by 193 values in a set of 113 force constants. The observed frequencies below $1700 \mathrm{~cm}^{-1}$ are predicted with an average error of about $5 \mathrm{~cm}^{-1}$, which suggests that conformational changes giving rise to larger frequency differences than this should be determinable from the vibrational spectrum.

For the $\alpha_{\mathrm{II}}$-helix, all of the above force constants were used without alteration, except for $f(\mathrm{CO}), f(\mathrm{NH})$, and $f(\mathrm{H} \cdots \mathrm{O})$. The hydrogen-bond force constant was given a value, $f(\mathrm{H} \cdots \mathrm{O})=0.0858$, that is proportional to the $r(\mathrm{~N} \cdots \mathrm{O})$ distance in the $\alpha_{\mathrm{II}}$-helix, using the comparable values in $\beta$-(Ala $)_{n}$ (Ref. 2) and the $\alpha_{\mathrm{I}}$-helix for purposes of extrapolation. The other two force constants have to be increased, since the hydrogen bond is weaker in $\alpha_{\text {II }}$ than in $\alpha_{1}$; the particular values chosen, viz., $f(\mathrm{CO})=10.129$ and $f(\mathrm{NH})=$ 5.908 , brought the respective frequencies into agreement with the observations on the ir spectra of $H$. halobium. ${ }^{17,18}$ Splittings in the amide I and amide II modes due to transition dipole coupling were calculated using the same parameters as for the $\alpha_{\mathrm{I}}$-helix but with the geometry of the $\alpha_{\mathrm{II}^{-}}$ helix.

## RESULTS AND DISCUSSION

## $\alpha_{\mathrm{I}}-\mathrm{Poly}(\mathrm{L}-$ alanine $)$

It is appropriate to note first how well the new force field predicts the spectrum of $\alpha_{I^{-}}(\text {Ala })_{n}$ before considering its application to studying the $\alpha_{I}$ to $\alpha_{\text {II }}$ conformational change. The calculated and observed frequencies of (Ala) ${ }_{n}$ and (Ala-ND) $)_{n}$ in the $\alpha_{I}$ conformation are listed in Table II.

As mentioned earlier, Fermi resonance analysis ${ }^{36}$ gives an unperturbed amide A mode, $\nu_{A}^{\circ}=3279 \mathrm{~cm}^{-1}$, which was used to refine the value of $f(\mathrm{NH})$. When the same force constant is used to calculate $\nu(\mathrm{ND})$, it gives a value of $2409 \mathrm{~cm}^{-1}$, about $40 \mathrm{~cm}^{-1}$ lower than the observed $\nu_{A}^{\circ}(\mathrm{ND}),{ }^{36}$ viz., 2449 $\mathrm{cm}^{-1}$. This is similar to the case of $\beta$-(Ala-ND),$^{2}$ for which the calculated value of the ND stretch is about $50 \mathrm{~cm}^{-1}$ lower than the observed $\nu_{A}^{\circ}(\mathrm{ND})$, and is explainable by the presence of different anharmonicities in (Ala) $n_{n}$ and (Ala-ND) ${ }_{n}$. In the CH stretching region, the agreement with the observed values is quite good for the $\mathrm{CH}_{3}$ antisymmetric and $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha}$ modes, but the calculation does not reproduce the splittings of $\sim 12 \mathrm{~cm}^{-1}$ in the $\mathrm{CH}_{3}$ symmetric stretch region. As suggested earlier, ${ }^{9}$ this discrepancy may be due to the presence of $\mathrm{CH}_{3} \cdots \mathrm{CH}_{3}$ nonbonded interactions between the
TABLE II
Observed and Calculated Frequencies (in $\mathrm{cm}^{-1}$ ) of $\alpha_{\mathrm{I}}$-Poly(L-alanine)

| Observed ${ }^{\text {a }}$ |  | Calculated |  |  | Potential Energy Distribution ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Raman | ir | A | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ |  |
| $\left[\mathrm{NHCH}\left(\mathrm{CH}_{3}\right) \mathrm{CO}\right]_{n}$ |  |  |  |  |  |
| 2988S | 3279VS ${ }^{\text {c }}$ | 3279 | 3279 | 3279 | NH s(98) |
|  |  | (2984 |  |  | $\mathrm{CH}_{3}$ as 1 (96) |
|  |  |  | 2984 |  | $\mathrm{CH}_{3}$ asl(99) |
|  | 2983VS \|| |  |  | 2984 | $\mathrm{CH}_{3}$ asl(98) |
|  |  | 2984 |  |  | $\mathrm{CH}_{3}$ as2(96) |
|  |  |  | 2984 |  | $\mathrm{CH}_{3}$ as2(99) |
|  |  |  |  | 2984 | $\mathrm{CH}_{3}$ as2(98) |
| 2930M,sh | 2925M \|| | 2930 |  |  | $\mathrm{CH}_{3} \mathrm{ss}(100)$ |
| 2942VS | 2939 M $\perp$ |  | 2930 |  | $\mathrm{CH}_{3} \mathrm{ss}(100)$ |
|  |  |  |  | 2930 | $\mathrm{CH}_{3} \mathrm{ss}(100)$ |
| 2880M | 2883W $\\|$, 1 | $\{2884$ |  |  | $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}$ (99) |
|  |  |  | 2884 |  | $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}$ (99) |
|  |  |  |  | 2884 | $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}(99)$ |
| 1655 S | 1658VS \|| | 1657 |  |  | CO s(82), CN s(10), $\mathrm{C}^{\alpha} \mathrm{CN}$ d(10) |
|  |  |  | 1655 |  | CO s(82), CN s(11), $\mathrm{C}^{\alpha} \mathrm{CN}$ d(10) |
|  |  |  |  | 1645 | CO s(83), CN s(12), $\mathrm{C}^{\alpha} \mathrm{CN}$ d(10) |
|  |  |  |  | 1540 | $\mathrm{NH} \mathrm{ib}(46), \mathrm{CN} \mathrm{s}(31), \mathrm{CO} \mathrm{ib}(12), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(11)$ |
| 1543VW | $\begin{aligned} & 1545 \mathrm{VS} \perp \\ & 1516 \mathrm{M}, \mathrm{sh} \end{aligned}$ |  | 1538 |  | NH ib(46), $\mathrm{CN} \mathrm{s}(33), \mathrm{CO} \mathrm{ib}(11), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(10)$ |
|  |  | 1519 |  |  | $\mathrm{NH} \mathrm{ib}(45), \mathrm{CN} \mathrm{s}(34), \mathrm{CO} \mathrm{ib}(11)$ |
|  |  | (1452 |  |  | $\mathrm{CH}_{3} \mathrm{ab1}(47), \mathrm{CH}_{3} \mathrm{ab} 2(41), \mathrm{CH}_{3} \mathrm{rl}$ (10) |
|  |  |  | 1452 |  | $\mathrm{CH}_{3} \mathrm{ab} 2(54), \mathrm{CH}_{3}$ ab1(31) |
| 1458 S | $1458 \mathrm{VS} \\|, \perp$ |  |  | 1452 | $\mathrm{CH}_{3} \mathrm{ab} 2$ (59), $\mathrm{CH}_{3} \mathrm{ab1}$ (26) |
|  |  | 1451 |  |  | $\mathrm{CH}_{3} \mathrm{ab} 2(45), \mathrm{CH}_{3}$ ab1 (41), $\mathrm{CH}_{3} \mathrm{r} 2$ (10) |
|  |  |  | 1451 |  | $\mathrm{CH}_{3}$ ab1(57), $\mathrm{CH}_{3} \mathrm{ab} 2$ (31) |
|  |  |  |  | 1451 | $\mathrm{CH}_{3} \mathrm{ab} 1(62), \mathrm{CH}_{3} \mathrm{ab2} 26$ ) |
| 1377W | 1381 S 」 | 1379 | 1379 | 1379 | $\mathrm{CH}_{3} \mathrm{sb}(100)$ |



1338M,sh
1326 S

1308M
1278 W
127 W
1261 W
1167 M

1105S
1050W
1017 W
970 W
940 VW
908 VS
TABLE II (continued)

| Observed ${ }^{\text {a }}$ |  | Calculated |  |  | Potential Energy Distribution ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Raman | ir | A | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ |  |
| 756W |  | 754 |  |  | CO ob(38), CN t(30) |
| 693M | 691W,sh ! | 700 |  |  | $\mathrm{NC}^{\alpha} \mathrm{C} d(36), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(26)$ |
|  |  |  |  | 675 | CN t(32), $\mathrm{CO} \mathrm{ib}(18), \mathrm{C}^{\alpha} \mathrm{C}$ s(14) |
| 662W | 658 S 」 |  | 660 |  | CNt (37), NH ob(21), $\mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(12)$ |
|  |  |  |  | 637 | CN t(59), NH ob (43), NH . . O ib(13) |
|  | $618 \mathrm{~S} \perp$ |  | 608 |  | CN t(47), NH ob(23), CO ob(15), CO ib(12) |
|  |  | 589 |  |  | CN t(68), NH ob(36), CO ob(26), $\mathrm{NH} \cdots \mathrm{CO} \mathrm{Ob}(11)$ |
|  |  | \| 537 |  |  | $\mathrm{CO} \mathrm{ib}(29), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{~d}(21), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{~s}(17), \mathrm{C}^{\beta} \mathrm{b} 2(17),$ |
| 530 VS | $526 \mathrm{~S} \\|, \perp$ |  |  |  | NH ob(11) |
|  |  |  | 522 |  | $\mathrm{NC}^{\alpha} \mathrm{C} d(31), \mathrm{C}^{\alpha} \mathrm{C} s(14), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(11), \mathrm{CO} \mathrm{ib}(11)$ |
|  |  |  |  | 492 | $\mathrm{NC}^{\alpha} \mathrm{Cd}$ (37), $\mathrm{CO} \mathrm{ib}(17), \mathrm{C}^{\alpha} \mathrm{C} s(16)$ |
| 375S | $375 \mathrm{~S} \perp$ |  | 374 |  | CO ob(16), NH ob(16), $\mathrm{C}^{\beta} \mathrm{b} 2(15), \mathrm{C}^{\alpha} \mathrm{CN}$ d(15), CO ib(15), $\mathrm{CNC}^{\alpha} \mathbf{d}(10)$ |
|  | $\sim 366 \mathrm{M}$,sh | 367 |  |  | $\begin{aligned} & \mathrm{CO} \text { ob(21), } \mathrm{C}^{\beta} \mathrm{b} 1(17), \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{~d}(14), \mathrm{NH} \text { ob(13), } \\ & \mathrm{C}^{\beta} \mathrm{b} 2(11) \end{aligned}$ |
|  |  |  |  | 366 | $\mathrm{C}^{\beta} \mathrm{b} 2(49), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(22), \mathrm{C}^{\beta} \mathrm{b} 1(16)$ |
| 328W | $324 \mathrm{~S} \perp$ |  | 326 |  | $\mathrm{C}^{\beta} \mathrm{b} 2(42), \mathrm{C}^{\beta} \mathrm{b} 1(19), \mathrm{CO} \mathrm{ib}(16)$ |
| 310 S |  |  |  | 310 | $\mathrm{CNC}^{\alpha} \mathrm{d}(30), \mathrm{CO} \mathrm{ib}(20), \mathrm{C}^{\beta} \mathrm{b} 1(20), \mathrm{CO}$ ob(17) |
| 294M | $290 \mathrm{M} \\|$ | 307 |  |  | $\mathrm{C}^{\beta} \mathrm{b} 2(34), \mathrm{CO} \mathrm{ib}(29), \mathrm{CNC}^{\alpha} \mathrm{d}(15)$ |
| 260M | 259W,sh | 264 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}(35), \mathrm{C}^{\beta} \mathrm{b} 2(14)$ |
|  | 240W |  | 245 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (91) |
|  |  |  |  | 244 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}(95)$ |
|  | 223 VW | 230 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (63) |
| 209W |  |  |  | 205 | $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(27), \mathrm{C}^{\beta} \mathrm{b} 2(25), \mathrm{C}^{\beta} \mathrm{b} 1(12), \mathrm{CO}$ ob(10) |
| 189M | $188 \mathrm{M} \perp$ |  | 197 |  | $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(15), \mathrm{C}^{\beta} \mathrm{b} 2(12), \mathrm{CO}$ ob(12) |
| 165M | $163 \mathrm{M} \perp$ |  | 155 |  | $\begin{aligned} & \mathrm{CNC}^{\alpha} \mathrm{d}(33), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{~d}(19), \mathrm{C}^{\beta} \mathrm{b} 1(14), \mathrm{NH} \text { ob(14), } \\ & \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{~d}(12) \end{aligned}$ |
| 159S |  |  |  | 151 | NH ob(43), $\mathrm{CNC}^{\alpha} \mathrm{d}(20), \mathrm{NC}^{\alpha} \mathrm{Cd}$ d(11) |
|  | 120S \|| | 136 |  |  | $\mathrm{CNC}^{\alpha} \mathrm{d}(34), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(21), \mathrm{NC}^{\alpha} \mathrm{Cd}$ d(16), $\mathrm{C}^{\beta} \mathrm{b} 1$ (12) |

NH ob(24), $\mathrm{C}^{\alpha} \mathrm{Ct}(20), \mathrm{NC}^{\alpha} \mathrm{t}(18), \mathrm{CN} \mathrm{t}(18)$,
H...Os(10)
CN t(27), $\mathrm{NC}^{\alpha} \mathrm{t}(23), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{t}(22), \mathrm{H} \cdots \mathrm{O}$ s(15),
NH ob(33), NH $\ldots$ O ib(20), $\mathrm{C}^{\beta}$ b1(12),
NH
$\mathrm{NH}^{\beta} \mathrm{ob}(38), \mathrm{NC}^{\alpha} \mathrm{t}(24), \mathrm{H} \cdots \mathrm{O}(23), \mathrm{CN} \mathrm{t}(15)$,
NH ob(58), $\mathrm{C}^{\beta}$ b1(20), $\mathrm{H} \cdots \mathrm{O}$ s(11)
$\mathrm{C}^{\alpha} \mathrm{Ct}$ (53), $\mathrm{H} \cdots \mathrm{O}$ s(18)
$\mathrm{CH}_{3}$ as1 (98)
$\mathrm{H}_{3}$ as1 $(94)$
$\mathrm{H}_{3}$ as2(98)

$\mathrm{H}_{3} \mathrm{ss}(100)$
$\mathrm{CH}_{3} \mathrm{ss}(100)$
$\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}(99)$ $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}(99)$
$\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}(99)$
CO s(84), CN s(13)
CO s(84), CN s(14)
CN s(35), $\mathrm{C}^{\alpha} \mathrm{C}$ s(22), $\mathrm{CO} \mathrm{ib}(15)$
(continued)

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TABLE II (continued)

| Observed ${ }^{\text {a }}$ |  | Calculated |  |  | Potential Energy Distribution ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Raman | ir | A | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ |  |
| 1477 | 1470M,sh | $\{$ | 1473 |  | $\mathrm{CNs}(33), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(19), \mathrm{CO} \mathrm{ib}(15), \mathrm{CH}_{3} \mathrm{ab} 2(12)$ |
| 1477 | $1470 \mathrm{M}, \mathrm{sh}$ | $\{1470$ |  |  | CNs (30), $\mathrm{CH}_{3} \mathrm{ab} 2(18), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(15), \mathrm{CO} \mathrm{ib}(14)$ |
| 1455 | 1454 M sh | $\{1452$ |  |  | $\mathrm{CH}_{3} \mathrm{ab1}$ (72), $\mathrm{CH}_{3} \mathrm{ab} 2(17)$ |
|  | 1454M,sh |  | 1452 |  | $\mathrm{CH}_{3} \mathrm{ab} 1(59), \mathrm{CH}_{3} \mathrm{ab2} 28$ ) |
|  |  |  |  | 1452 | $\mathrm{CH}_{3} \mathrm{ab} 1(51), \mathrm{CH}_{3} \mathrm{ab} 2(35), \mathrm{CH}_{3} \mathrm{r} 2(11)$ |
|  | 1439S |  | 1445 |  | $\mathrm{CH}_{3} \mathrm{ab} 2(47), \mathrm{CH}_{3} \mathrm{ab} 1(25), \mathrm{CN} \mathrm{s}(10)$ |
|  |  |  |  | 1445 | $\mathrm{CH}_{3}$ ab2(43), $\mathrm{CH}_{3} \mathrm{ab1}$ (32) |
| 1430 |  | 1444 |  |  | $\mathrm{CH}_{3}$ ab2(53), CN s(14), $\mathrm{CH}_{3}$ ab1(13) |
| 1373 | 1379S | 1379 | 1379 | 1379 | $\mathrm{CH}_{3} \mathrm{sb}$ (100) |
|  |  |  |  | 1328 | $\mathrm{H}^{\alpha} \mathrm{bl}(54), \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(10)$ |
|  |  |  | 1326 |  | $\mathrm{H}^{\alpha} \mathrm{b} 1(38), \mathrm{H}^{\alpha} \mathrm{b} 2(30)$ |
| 1326 | 1328S | 1319 |  |  | $\mathrm{H}^{\alpha} \mathrm{b} 2(74), \mathrm{H}^{\alpha} \mathrm{b} 1(11)$ |
|  |  |  |  | 1307 | $\mathrm{H}^{\alpha} \mathrm{b} 2(90)$ |
| 1296 | 1293W |  | 1304 |  | $\mathrm{H}^{\alpha} \mathrm{b} 2$ (63), $\mathrm{H}^{\alpha} \mathrm{b} 1$ (23) |
|  | 1293 W | 1299 |  |  | $\mathrm{H}^{\alpha}$ b1 (55), $\mathrm{H}^{\alpha}$ b2 (15) |
|  | 1178M,sh | 1176 |  |  | $\mathrm{NC}^{\alpha} \mathrm{s}(29), \mathrm{CH}_{3} \mathrm{rl}(19), \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(18)$ |
|  | 1170 S |  | 1168 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(26), \mathrm{NC}^{\alpha} \mathrm{s}(21), \mathrm{CH}_{3} \mathrm{r} 1$ (16) |
| 1158 |  |  |  | 1161 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(35), \mathrm{NC}^{\alpha} \mathrm{s}(18), \mathrm{CH}_{3} \mathrm{r}$ (14), $\mathrm{H}^{\alpha}$ b1 (11) |
|  |  |  |  | 1147 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(25), \mathrm{CH}_{3} \mathrm{r} 2(20), \mathrm{ND} \mathrm{ib}(13)$ |
|  | 1140 M |  | 1136 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(35), \mathrm{CH}_{3} \mathrm{r} 2(21)$ |
| 1095 | 1098M | 1121 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(51), \mathrm{CH}_{3} \mathrm{r} 2(22)$ |
| 1065 | 1062S | $\{1051$ |  |  | $\mathrm{CH}_{3} \mathrm{r} 2(20), \mathrm{ND} \mathrm{ib}(18), \mathrm{H}^{\alpha} \mathrm{bl}(17), \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(13)$ |
|  | 1062S |  | 1045 |  | $\mathrm{CH}_{3} \mathrm{r} 1$ (29), $\mathrm{H}^{\alpha}$ bl(22), $\mathrm{CH}_{3} \mathrm{r} 2(15)$ |
|  |  |  |  | 1045 | $\mathrm{CH}_{3} \mathrm{r} 1(40), \mathrm{H}^{\alpha} \mathrm{b} 1(23), \mathrm{CH}_{3} \mathrm{r} 2(12)$ |
| 1001 | 999M | 984 |  |  | $\mathrm{CH}_{3} \mathrm{r} 1(44), \mathrm{ND} \mathrm{ib}(26), \mathrm{NC}^{\alpha} \mathrm{s}(15), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(12)$ |
| 975 | 974M |  | 972 |  | ND ib(43), $\mathrm{CH}_{3} \mathrm{r} 1(23), \mathrm{C}^{\alpha} \mathrm{C}$ s(10) |
|  |  |  |  | 961 | ND ib(59), $\mathrm{CH}_{3} \mathrm{r} 1$ (12) |
|  |  |  |  | 941 | $\mathrm{CH}_{3} \mathrm{r} 2$ (37), $\mathrm{NC}^{\alpha} \mathrm{s}(21)$ |


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TABLE II (continued)

| Observed ${ }^{\text {a }}$ |  | Calculated |  |  | Potential Energy Distribution ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Raman | ir | A | $\mathrm{E}_{1}$ | $\overline{\mathrm{E}_{2}}$ |  |
|  |  |  |  |  | ND ob(14),CN t(12) |
|  |  | 260 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}(41), \mathrm{C}^{\beta} \mathrm{b} 2(10)$ |
|  |  |  | 244 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (92) |
|  |  |  |  | 244 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (95) |
|  |  | 229 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (57) |
|  |  |  |  | 205 | $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(27), \mathrm{C}^{\beta} \mathrm{b} 2(25), \mathrm{C}^{\beta} \mathrm{b} 1(12), \mathrm{CO}$ ob(10) |
|  |  |  | 195 |  | $\mathrm{C}^{\alpha} \mathrm{CN}$ d(15), CO ob(12), $\mathrm{C}^{\beta} \mathrm{b} 2(11), \mathrm{C}^{\beta} \mathrm{b} 1(10)$ |
|  |  |  | 154 |  | $\mathrm{CNC}^{\alpha} \mathrm{d}(33), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{~d}(19), \mathrm{C}^{\beta} \text { b1(14),,ND ob(14), }$ $\mathrm{NC}^{\alpha} \mathrm{C}$ d(12) |
|  |  |  |  | 149 | ND ob(41), $\mathrm{CNC}^{\alpha} \mathrm{d}(19), \mathrm{NC}^{\alpha} \mathrm{C} d(11)$ |
|  |  | 135 |  |  | $\mathrm{CNC}^{\alpha} \mathrm{d}(34), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(22), \mathrm{NC}^{\alpha} \mathrm{C} d(16), \mathrm{C}^{\beta} \mathrm{bl}$ (12) |
|  |  |  | 95 |  | ND ob(24), $\mathrm{C}^{\alpha} \mathrm{C} t(20), \mathrm{NC}^{\alpha} \mathrm{t}(19), \mathrm{CN} \mathrm{t}(16)$, |
|  |  | 94 |  |  | CN t(25), $\mathrm{NC}^{\alpha} \mathrm{t}(24), \mathrm{C}^{\alpha} \mathrm{C}$ t(22), D. . O os(15) |
|  |  |  |  | 88 | $\begin{aligned} & \text { ND ob(33), ND } \cdots \mathrm{O} \text { ib(21), } \mathrm{C}^{\beta} \mathrm{b} 1(12), \mathrm{NC}^{\alpha} \mathrm{C} d(10) \\ & \mathrm{CNC}^{\alpha} \mathrm{d}(10) \end{aligned}$ |
|  |  |  |  | 49 | ND ob(37), D. . O s $(24), \mathrm{NC}^{\alpha} \mathrm{t}$ (24), $\mathrm{CN} \mathrm{t}(15)$ |
|  |  |  |  |  | $\mathrm{C}^{\beta} \mathrm{b} 1(13)$ |
|  |  |  | 40 |  | ND ob(57), $\mathrm{C}^{\beta} \mathrm{b} 1(20), \mathrm{D} \cdots \mathrm{Os}(11)$ |
|  |  |  |  | 37 | $\mathrm{C}^{\alpha} \mathrm{C}$ t(54), $\mathrm{D} \cdots \mathrm{O} \mathrm{s}(18)$ |

[^0]adjacent chains in the crystal, which has not been included in the present force field (the $\beta$ force field ${ }^{2}$ does not require such interactions).

The amide I modes (mainly CO stretch) are very well predicted, and their downfield shift of about $8 \mathrm{~cm}^{-1}$ on N -deuteration is better accounted for than previously. ${ }^{9}$ The calculated frequencies in the $1550-1370 \mathrm{~cm}^{-1}$ region, which contains amide II ( NH in-plane bend +CN stretch) and methyl bending modes, fit the observed data satisfactorily. In fact, the present calculation shows an improvement for methyl bend modes as compared with the earlier work. ${ }^{9}$ For example, the fit is much better for the $\mathrm{CH}_{3}$ symmetric bend mode at $\sim 1380 \mathrm{~cm}^{-1}$, and its potential energy distribution (PED) now shows that it does not mix with any other mode.

As mentioned earlier, transition dipole coupling was included to determine the complete splitting between observed $A$ and $E_{1}$ species amide I and amide II modes. This splitting is smaller for $\alpha$-(Ala $)_{n}$ than for $\beta$-(Ala $)_{n} .{ }^{2}$ This may be a general feature of helical structures: a similar trend is seen for $3_{1}$-helical (Gly II) ${ }_{n} .{ }^{35}$ In amide I of $\alpha$-(Ala) $)_{n}$, the observed and predicted splittings between ir-active A and $\mathrm{E}_{1}$ modes are zero and $2 \mathrm{~cm}^{-1}$ respectively, compared with 62 and $65 \mathrm{~cm}^{-1}$ (for $\mathrm{B}_{1}$ and $\mathrm{B}_{2}$ species) in $\beta$-(Ala) $)_{n}{ }^{2}$ Although the splitting in ir-active amide II modes is larger compared with amide I, it is smaller compared to amide II splittings in $\beta$-(Ala) $n_{n}{ }^{2}$ Our present assignment of modes in the $1550-1370-\mathrm{cm}^{-1}$ region is almost the same as reported earlier, ${ }^{9}$ but our force field gives a slightly better fit. Rabolt et al. ${ }^{9}$ attributed the origin of bands at 1470 and 1440 $\mathrm{cm}^{-1}$ to a resonance between the $\mathrm{CH}_{3}$ asymmetric bend at $1458 \mathrm{~cm}^{-1}$ and the unperturbed amide II' mode (which these authors estimated at $\sim 1451$ $\mathrm{cm}^{-1}$ ). Also, they had to reduce the force constant $f(\mathrm{CN})$ by $0.500 \mathrm{mdyn} / \AA$ in order to fit the data in this region. There do not now seem to be compelling reasons for this interpretation. Our recent ${ }^{2}$ ir spectrum of $\beta$ -(Ala-ND) $)_{n}$ does not indicate any splitting in the $\mathrm{CH}_{3}$ asymmetric bend mode, and our transferring of the force field from $\beta$-(Ala) $)_{n}$ to $\alpha$-(Ala) $)_{n}$ required no alteration in $f(\mathrm{CN})$. The experimental data in this region look similar for both structures: in $\beta$-(Ala-ND) $)_{n}$, the $\mathrm{CH}_{3}$ symmetric bend mode at $\sim 1380 \mathrm{~cm}^{-1}$ remains unchanged, two new bands appear at 1488 and $1464 \mathrm{~cm}^{-1}$, and the methyl asymmetric bend doublet of $\beta$-(Ala) ${ }_{n}$ is replaced by one peak at $\sim 1445 \mathrm{~cm}^{-1}$. The two new peaks at 1488 and 1464 $\mathrm{cm}^{-1}$ are assignable to amide $\mathrm{II}^{\prime}$ in $\beta$-(Ala-ND) $n$, and our calculation indicates that the two new frequencies in $\alpha$-(Ala-ND) $)_{n}$, at $\sim 1470$ and 1440 $\mathrm{cm}^{-1}$, can also be assigned to amide $\mathrm{II}^{\prime}$, although their PED shows that there is considerably more mixing between the $\mathrm{CH}_{3}$ asymmetric bend and CN stretch than in $\beta$-(Ala) $)_{n}$.

The overall fit in the range $1340-940 \mathrm{~cm}^{-1}$ is the same as reported by Rabolt et al., 9 but the PEDs of some bands show considerable differences. The observed bands at 1338(R), 1326(R), 1328(ir), 1308(R), and 1307(ir) are now distinctly assignable to two types of modes: the first three are due to $\mathrm{H}^{\alpha}$ bend and $\mathrm{C}^{\alpha} \mathrm{C}$ stretch mixed with some NH in-plane bend, whereas the other two are due to pure $\mathrm{H}^{\alpha}$ bend. In the earlier assignment, ${ }^{9}$ these
bands were of a much more mixed type. Although the PEDs of these modes do not have large contributions from NH in-plane bend, small downward frequency shifts occur in the N -deuterated molecule, and these are reproduced moderately well. The observed bands at 1278(R), 1271(R), 1270(ir), 1265 (ir), and $1261(\mathrm{R})$ are assignable to the amide III mode, both in the present and the earlier ${ }^{9}$ work, but the present PEDs have a significantly higher contribution from NH in-plane bend. On N -deuteration, these modes shift to $\sim 1000 \mathrm{~cm}^{-1}$, which is reasonably well predicted by the present force field. The observed bands near 1170 and $1100 \mathrm{~cm}^{-1}$ are well predicted for $\alpha$-(Ala) $)_{n}$, and their shifts on N -deuteration, especially the new band at 1140 M (ir), are reasonably well reproduced. The $\mathrm{CH}_{3}$ rocking region of $\alpha$-(Ala) $)_{n}, 1050$ to $940 \mathrm{~cm}^{-1}$, is satisfactorily reproduced. Some of the assignments in the comparable region of $\alpha-(\text { Ala-ND })_{n}$ are still uncertain.

The frequency region below $900 \mathrm{~cm}^{-1}$ begins to show contributions from skeletal stretches, bends, and torsions. The observed bands at $908(\mathrm{R})$, 909(ir), 893(ir), and $882(\mathrm{R})$ are mainly due to skeletal stretch and bend modes. Although they do not have any contribution from NH motion, they do show downward shifts on N -deuteration, and it is gratifying to note that the present force field predicts these shifts very well. The observed bands at $773(\mathrm{R}), 774(\mathrm{ir})$, and $756(\mathrm{R})$ are due mainly to CO out-of-plane bend, their predicted values and shifts on N -deuteration being very satisfactorily predicted. The same is true for the pure skeletal bend mode at $690 \mathrm{~cm}^{-1}$. The $670-600-\mathrm{cm}^{-1}$ region is predominantly due to amide V (CN torsion +NH out-of-plane bend). The assignment in this region is almost the same as that reported earlier. ${ }^{9}$ The major difference is the presence of an NH. . OO in-plane-bend contribution in the present work, this coordinate having been neglected earlier. ${ }^{9}$ We find that the force constants associated with NH. . O in-plane-bend are very crucial for amide V frequencies, and their exclusion is most likely to affect the force-field refinement. The agreement between the predicted and observed amide $\mathrm{V}^{\prime}$ modes is also better than previously reported. ${ }^{9}$ The band near $530 \mathrm{~cm}^{-1}$ has long been considered a characteristic mode of the $\alpha$-helix. The ir dichroic spectrum shows that this band has equally intense parallel and perpendicular components. Our present calculation predicts modes near this value in both the $A$ and $E_{1}$ species, which was not the case in the earlier work. ${ }^{9}$ Below $500 \mathrm{~cm}^{-1}$, the modes are predominantly due to skeletal bends and torsions. The NH out-of-plane bend mode makes a very wide-ranging contribution in this region, where it shows significant mixing with most of the modes. Apart from slight variations in PED, our predictions in this region are almost the same as in our earlier report. ${ }^{9}$ We note finally that, as in our earlier work, ${ }^{9}$ we have no explanation for weak Raman bands observed at 1397,1070 , and $929 \mathrm{~cm}^{-1}$.

## $\alpha_{\text {II }}-$ Poly(L-alanine)

The relatively good agreement between observed and calculated frequencies for $\alpha_{\mathrm{I}}$ (Ala) $)_{n}$ provides a basis for judging whether predicted
frequency differences for $\alpha_{\mathrm{II}}$ (Ala) $n_{n}$ will be meaningful. The calculated normal-mode frequencies and their assignments for $\alpha_{\mathrm{II}}-(\mathrm{Ala})_{n}$ are presented in Table III. No experimental data on this particular form of poly(L-alanine) are available; however, since there is evidence for the presence of this conformation in proteins, it will be useful to have the predicted frequencies so that they can be used for characterizing this conformation. As noted above, a comparison of the experimental data on the amide A, I, and II modes with the theoretical predictions for the $\alpha_{\mathrm{I}}$ and $\alpha_{\text {II }}$ conformations indicates that the bacteriorhodopsin in the purple membrane of $H$. halobium probably has the $\alpha_{\mathrm{II}}$ conformation. ${ }^{19}$

The presence of weaker hydrogen bonds in $\alpha_{\text {II }}$ than in $\alpha_{\text {I }}$ results in higher NH stretch and amide I frequencies, and in changes in the amide II frequencies. (Since we reported our analysis of the ir spectrum of bacteriorhodopsin, ${ }^{19}$ we have made some slight adjustments in the force field; this has shifted the calculated amide I and II frequencies by $1-2 \mathrm{~cm}^{-1}$, but not modified our earlier conclusions. ${ }^{19}$ ) We note, as before, ${ }^{19}$ that although the $\mathrm{E}_{1}$ species amide II frequency is predicted to remain approximately the same ( $1538 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{I}}$ vs $1540 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$ ), the splitting between A and $\mathrm{E}_{\mathrm{I}}$ is predicted to increase ( $19 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{I}}$ vs $25 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$ ). The amide III frequencies decrease slightly as a result of the weaker hydrogen bond: 1262(A), $1278\left(\mathrm{E}_{1}\right)$, and $1287\left(\mathrm{E}_{2}\right) \mathrm{cm}^{-1}$ in $\alpha_{1}$ vs $1260(\mathrm{~A}), 1272\left(\mathrm{E}_{1}\right)$, and $1281\left(\mathrm{E}_{2}\right) \mathrm{cm}^{-1}$ in $\alpha_{\mathrm{II}}$. And while, as expected, most of the $\mathrm{CH}_{3}$ modes are essentially unaffected by the small conformational change, $\mathrm{CH}_{3}$ rock modes at $1026(\mathrm{~A}), 1037\left(\mathrm{E}_{1}\right)$, and $1043\left(\mathrm{E}_{2}\right) \mathrm{cm}^{-1}$ in $\alpha_{1}$ are predicted to increase slightly, to $1031(\mathrm{~A}), 1040\left(\mathrm{E}_{1}\right)$, and $1047\left(\mathrm{E}_{2}\right) \mathrm{cm}^{-1}$ in $\alpha_{\mathrm{II}}$.

The effects of the small conformational difference between $\alpha_{\mathrm{I}}$ and $\alpha_{\mathrm{II}}$ show up more obviously in the lower-frequency regions. The $896\left(\mathrm{E}_{2}\right) \mathrm{cm}^{-1}$ skeletal mode of $\alpha_{\mathrm{I}}$ is predicted to shift down to $887 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$. The 780 ( $\mathrm{E}_{1}$ ) $\mathrm{cm}^{-1} \mathrm{CO}$ out-of-plane bend mode of $\alpha_{\mathrm{I}}$ shifts down to $770 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$, while the 700 (A) $-\mathrm{cm}^{-1}$ skeletal bending mode of $\alpha_{1}$ is predicted to shift down to $690 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$. Since the amide V modes of $\alpha_{\mathrm{I}}$, at $660\left(\mathrm{E}_{1}\right)$ and $608\left(\mathrm{E}_{1}\right) \mathrm{cm}^{-1}$, are expected to shift up in $\alpha_{I I}$, to $666\left(\mathrm{E}_{1}\right)$ and $615\left(\mathrm{E}_{1}\right) \mathrm{cm}^{-1}$, the relative separation of the $700(\mathrm{~A})$ and $660\left(\mathrm{E}_{1}\right)$ modes $\left(40 \mathrm{~cm}^{-1}\right.$ in $\alpha_{\mathrm{I}}$ vs $24 \mathrm{~cm}^{-1}$ in $\alpha_{\mathrm{II}}$ ) may serve as a useful indication of the conformational change. Another sensitive feature may be the predicted inversion in order of the $374\left(\mathrm{E}_{1}\right)$ - and $367(\mathrm{~A})-\mathrm{cm}^{-1}$ modes of $\alpha_{\mathrm{I}}$ to $369\left(\mathrm{E}_{1}\right)$ and $376(\mathrm{~A}) \mathrm{cm}^{-1}$ in $\alpha_{\text {II }}$. Finally, we note that the calculated $43-\mathrm{cm}^{-1}$ separation between the $307(\mathrm{~A})$ - and $264(\mathrm{~A})-\mathrm{cm}^{-1}$ modes of $\alpha_{I}$ is predicted to decrease to 28 $\mathrm{cm}^{-1}$ in $\alpha_{\mathrm{II}}$. Though each of the above changes may be small in itself, we would expect that their combined presence would provide strong evidence for the $\alpha_{\text {II }}$ conformation.

## CONCLUSIONS

The present force field for $\alpha_{\mathrm{I}}$ ( Ala$)_{n}$ reproduces the observed frequencies somewhat better than did our previous force field, ${ }^{9}$ the average discrepancy for frequencies below $1700 \mathrm{~cm}^{-1}$ being $6.0 \mathrm{~cm}^{-1}$ compared with $7.6 \mathrm{~cm}^{-1}$

TABLE III
Calculated Frequencies (in $\mathrm{cm}^{-1}$ ) of $\alpha_{\mathrm{II}}$-Poly(L-alanine)

| Calculated |  |  | Potential Energy Distribution ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: |
| A | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ |  |
| 3288 | 3288 | 3288 | NH s(99) |
| 2984 |  |  | $\mathrm{CH}_{3}$ as1(97) |
|  | 2984 |  | $\mathrm{CH}_{3}$ as1(99) |
|  |  | 2984 | $\mathrm{CH}_{3}$ asi (98) |
| 2984 |  |  | $\mathrm{CH}_{3}$ as2(97) |
|  | 2984 |  | $\mathrm{CH}_{3}$ as2(99) |
|  |  | 2984 | $\mathrm{CH}_{3}$ as2(99) |
| 2930 | 2930 | 2930 | $\mathrm{CH}_{3} \mathrm{ss}(100)$ |
| 2884 | 2884 | 2884 | $\mathrm{C}^{\alpha} \mathrm{H}^{\alpha} \mathrm{s}$ (99) |
| 1667 |  |  | CO s(83), CN s (10) |
|  | 1660 |  | COs s(83), CN s(12) |
|  |  | 1654 | COs s(83), CN s (13) |
|  |  | 1543 | NH ib(45), $\mathrm{CN} \mathrm{s}(31), \mathrm{C}^{\alpha} \mathrm{C}$ s(12), $\mathrm{CO} \mathrm{ib}(11)$ |
|  | 1540 |  | NH ib(44), $\mathrm{CN} \mathrm{s}(32), \mathrm{CO} \mathrm{ib}(11), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(10)$ |
| 1515 |  |  | NH ib(43), $\mathrm{CN} s(34), \mathrm{CO} \mathrm{ib}(11)$ |
|  |  | 1453 | $\mathrm{CH}_{3} \mathrm{ab} 2(48), \mathrm{CH}_{3} \mathrm{ab1}(37), \mathrm{CH}_{3} \mathrm{r} 2(10)$ |
| 1452 |  |  | $\mathrm{CH}_{3} \mathrm{ab} 2(51), \mathrm{CH}_{3} \mathrm{ab1}(36), \mathrm{CH}_{3} \mathrm{rl}$ (10) |
|  | 1452 |  | $\mathrm{CH}_{3} \mathrm{ab2}$ (51), $\mathrm{CH}_{3} \mathrm{ab1}(34)$ |
| 1451 |  |  | $\mathrm{CH}_{3}$ ab1(52), $\mathrm{CH}_{3} \mathrm{ab} 2(34), \mathrm{CH}_{3} \mathrm{r} 2(10)$ |
|  | 1451 |  | $\mathrm{CH}_{3}$ abl(54), $\mathrm{CH}_{3} \mathrm{ab} 2(34)$ |
|  |  | 1451 | $\mathrm{CH}_{3} \mathrm{ab1}$ (51), $\mathrm{CH}_{3} \mathrm{ab} 2$ (37) |
| 1379 | 1379 | 1379 | $\mathrm{CH}_{3} \mathrm{sb}(100)$ |
|  |  | 1347 | $\mathrm{H}^{\alpha} \mathrm{b} 1(40), \mathrm{NH}$ ib(14), $\mathrm{C}^{\alpha} \mathrm{C}$ s(13), $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}$ (11) |
|  | 1346 |  | $\mathrm{H}^{\alpha} \mathrm{b} 1(26), \mathrm{H}^{\alpha} \mathrm{b} 2(23), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(15), \mathrm{NH}$ ib(11) |
| 1339 |  |  | $\mathrm{H}^{\alpha} \mathrm{b} 2(53), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(16)$ |
|  |  | 1315 | $\mathrm{H}^{\alpha} \mathrm{b} 2(78)$ |
|  | 1308 |  | $\mathrm{H}^{\alpha} \mathrm{b} 2(51), \mathrm{H}^{\alpha} \mathrm{b} 1(26)$ |
| 1300 |  |  | $\mathrm{H}^{\alpha} \mathrm{bl}$ (60) |
|  |  | 1281 | $\mathrm{NH} \mathrm{ib}(28), \mathrm{NC}^{\alpha} \mathrm{s}(17), \mathrm{H}^{\alpha} \mathrm{b} 2(12), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(11), \mathrm{H}^{\alpha} \mathrm{bl}(10)$ |
|  | 1272 |  | NH ib(32), $\mathrm{H}^{\alpha} \mathrm{b} 2(17), \mathrm{NC}^{\alpha} \mathrm{s}(13)$ |
| 1260 |  |  | $\mathrm{NH} \mathrm{ib}(42), \mathrm{H}^{\alpha} \mathrm{b} 2(31)$ |
| 1175 |  |  | $\mathrm{NC}^{\alpha} \mathrm{s}(32), \mathrm{CH}_{3} \mathrm{rl}(21), \mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(14)$ |
|  | 1169 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(28), \mathrm{NC}^{\alpha} \mathrm{s}(22), \mathrm{CH}_{3} \mathrm{r} 1(16), \mathrm{H}^{\alpha} \mathrm{bl}(10)$ |
|  |  | 1164 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(36), \mathrm{NC}^{\alpha} \mathrm{s}(17), \mathrm{CH}_{3} \mathrm{rl}(13), \mathrm{H}^{\alpha} \mathrm{b} 1(12)$ |
| 1114 |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(65), \mathrm{CH}_{3} \mathrm{r} 2(15)$ |
|  | 1101 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(42), \mathrm{CH}_{3} \mathrm{r} 2(18)$ |
|  |  | 1092 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(29), \mathrm{CH}_{3} \mathrm{r} 2(22), \mathrm{NH} \mathrm{ib}(10)$ |
|  |  | 1047 | $\mathrm{CH}_{3} \mathrm{rl}$ (48), $\mathrm{H}^{\alpha} \mathrm{bl}$ (19) |
|  | 1040 |  | $\mathrm{CH}_{3} \mathrm{rl}$ (39), $\mathrm{H}^{\alpha} \mathrm{b} 1(20), \mathrm{CH}_{3} \mathrm{r} 2$ (13) |
| 1031 |  |  | $\mathrm{CH}_{3} \mathrm{r} 2(25), \mathrm{H}^{\alpha} \mathrm{b} 1(23), \mathrm{CH}_{3} \mathrm{r} 1(23)$ |
| 961 |  |  | $\mathrm{CH}_{3} \mathrm{r}$ (34), $\mathrm{NC}^{\alpha} \mathrm{s}(29), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(16), \mathrm{CH}_{3} \mathrm{r} 2(16)$ |
|  | 953 |  | $\mathrm{CH}_{3} \mathrm{r} 2(35), \mathrm{NC}^{\alpha} \mathrm{s}(21), \mathrm{CH}_{3} \mathrm{r} 1(13)$ |
|  |  | 951 | $\mathrm{CH}_{3} \mathrm{r} 2(44), \mathrm{NC}^{\alpha} \mathrm{s}(16)$ |
| 909 |  |  | $\mathrm{CN} s(23), \mathrm{CNC}^{\alpha} \mathrm{d}(16), \mathrm{CH}_{3} \mathrm{r} 2(15), \mathrm{CO} \mathrm{ib}(10)$ |
|  | 900 |  | CN s(18), $\mathrm{C}^{\alpha} \mathrm{C}$ s(14), $\mathrm{CO} \mathrm{ib}(11)$ |
|  |  | 887 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{s}(19), \mathrm{C}^{\alpha} \mathrm{C} s(17), \mathrm{CN} \mathrm{s}(15), \mathrm{NC}^{\alpha} \mathrm{s}(12), \mathrm{CO} \mathrm{ib}(12)$ |
|  | 770 |  | CO ob(42), CN t(14) |
|  |  | 759 | CO ob(51) |

TABLE III (continued)

| Calculated |  |  | Potential Energy Distribution ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: |
| A | $\mathrm{E}_{1}$ | $\mathrm{E}_{2}$ |  |
| 753 | 666 | 689 | CO ob(39), CN t(35) |
| 690 |  |  | $\mathrm{NC}^{\alpha} \mathrm{C}$ d(31), $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(29), \mathrm{NH}$ ob(12) |
|  |  |  | $\mathrm{CN} \mathrm{t}(34), \mathrm{CO} \mathrm{ib}(16), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(12)$ |
|  |  |  | CN t(44),NH ob(26) |
|  |  | 651 | CN t(52), NH ob(43),NH...O ib(11) |
|  | 615 |  | CN t(33), CO ob(18), NH ob(18), CO ib(15) |
| 592 |  | 480 | CN t(61), NH ob(30), CO ob(28), $\mathrm{C}^{\beta} \mathrm{b} 1(11)$ |
| 536 | 518 |  | $\mathrm{CO} \mathrm{ib}(33), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(20), \mathrm{C}^{\beta} \mathrm{b} 2(18), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(17), \mathrm{NC}^{\alpha} \mathrm{s}(10)$ |
|  |  |  | $\mathrm{NC}^{\alpha} \mathrm{Cd}$ (32), $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(15), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(12)$ |
|  |  |  | $\mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}$ (38), $\mathrm{CO} \mathrm{ib}(16), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(15)$ |
| 376 | 369 |  | $\mathrm{C}^{\beta} \mathrm{b} 1(22), \mathrm{CO}$ ob(21), $\mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(18), \mathrm{NH}$ ob(17) |
|  |  | 363 | CO ob(16), $\mathrm{C}^{\beta}$ b1(15), NH ob(15), $\mathrm{C}^{\beta} \mathrm{b} 2(14), \mathrm{CNC}^{\alpha} \mathrm{d}(12)$, $\mathrm{C}^{\alpha} \mathrm{CN}$ d(11), $\mathrm{CO} \mathrm{ib}(11)$ |
|  | 331 |  | $\mathrm{C}^{\beta} \mathrm{b} 2(50), \mathrm{C}^{\beta} \mathrm{b} 1(21), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(18)$ |
|  |  |  | $\mathrm{C}^{\beta} \mathrm{b} 2(46), \mathrm{CO} \mathrm{ib}(20), \mathrm{C}^{\beta} \mathrm{bl}(14)$ |
|  |  | 308 | $\mathrm{CNC}^{\alpha} \mathrm{d}(27), \mathrm{CO} \mathrm{ib}(22), \mathrm{CO}$ ob(18), $\mathrm{C}^{\beta} \mathrm{bl}(17)$ |
| 302 |  | 245 | $\mathrm{C}^{\beta} \mathrm{b} 2(50), \mathrm{CO} \mathrm{ib}(25)$ |
| 274 | 244 |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}(20), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{s}(10), \mathrm{C}^{\beta} \mathrm{b} 2(10), \mathrm{CNC}^{\alpha} \mathrm{d}(10)$ |
|  |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (93) |
|  |  |  | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (91) |
| 233 |  | 210 | $\mathrm{C}^{\alpha} \mathrm{C}^{\beta} \mathrm{t}$ (77) |
|  | 201160 |  | $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(28), \mathrm{C}^{\beta} \mathrm{b} 2(24), \mathrm{C}^{\beta} \mathrm{b} 1(10)$ |
|  |  |  | $\mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(14), \mathrm{CO}$ ob(12), $\mathrm{C}^{\beta} \mathrm{b} 2(11)$ |
|  |  |  | $\mathrm{CNC}^{\alpha} \mathrm{d}(36), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(20), \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(12), \mathrm{C}^{\beta} \mathrm{b} 1(11), \mathrm{NH}$ ob(11) |
|  |  | 157 | NH ob(32), $\mathrm{CNC}^{\alpha} \mathrm{d}(28), \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(13), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}$ (12) |
| $\begin{aligned} & 140 \\ & 106 \end{aligned}$ | 101 |  | $\mathrm{CNC}^{\alpha} \mathrm{d}(35), \mathrm{C}^{\alpha} \mathrm{CN} \mathrm{d}(21), \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(14), \mathrm{C}^{\beta} \mathrm{b} 1(10)$ |
|  |  |  | $\mathrm{CN} t(34), \mathrm{H} \ldots \mathrm{O}$ s(27), $\mathrm{NC}^{\alpha} \mathrm{t}(19), \mathrm{C}^{\alpha} \mathrm{C} \mathrm{t}(16)$ |
|  |  |  | CN t(25), $\mathrm{H} \cdots \mathrm{O} \mathrm{O}(22), \mathrm{NH}$ ob(19), $\mathrm{C}^{\alpha} \mathrm{C} \mathrm{t}(16), \mathrm{NC}^{\alpha} \mathrm{t}(13)$ |
|  |  | $82$ | NH ob(24), NH $\cdots$ O O ib(15), $\mathrm{H} \cdots \mathrm{O}$ s(13), $\mathrm{NC}^{\alpha} \mathrm{t}(12), \mathrm{C}^{\alpha} \mathrm{C}$ t(10) |
|  | 40 | 51 | NH ob(67), $\mathrm{C}^{\beta} \mathrm{bl}(24), \mathrm{H} \cdots \mathrm{O}$ s(20), CN t t(18), $\mathrm{NC}^{\alpha} \mathrm{t}$ (11) |
|  |  |  | NH ob(67), $\mathrm{C}^{\beta} \mathrm{bl}(24), \mathrm{H} \cdots \mathrm{O} \mathrm{s}(19), \mathrm{NC}^{\alpha} \mathrm{C} \mathrm{d}(10), \mathrm{NC}^{\alpha} \mathrm{t}(10)$ |
|  |  | 35 | $\mathrm{C}^{\alpha} \mathrm{C} \mathrm{t}(51), \mathrm{NH} \ldots \mathrm{O} \mathrm{O}$ ib(15), H . . O s s(14), $\mathrm{NC}^{\alpha} \mathrm{t}(12)$ |

${ }^{a_{s}}=$ stretch, as $=$ antisymmetric stretch, $\mathrm{ss}=$ symmetric stretch, $\mathbf{b}=$ angle bend, $\mathrm{ib}=$ inplane angle bend, $o b=$ out-of-plane angle bend, $a b=$ antisymmetric angle bend, $s b=s y m-$ metric angle bend, $\mathrm{r}=$ rock, $\mathrm{d}=$ deformation, $\mathrm{t}=$ torsion. Only contributions $10 \%$ or greater are included.
[for $\alpha_{\mathrm{I}}$-(Ala-ND) ${ }_{n}$ the average discrepancy is $5.9 \mathrm{~cm}^{-1}$ ]. This level of agreement compares with those for our recent refinements of (Gly I) $n(5.4$ $\left.\mathrm{cm}^{-1}\right)^{1}$ and $\beta$-(Ala) $)_{n}\left(4.6 \mathrm{~cm}^{-1}\right) .{ }^{2}$ It therefore provides a good basis for examining the effects of small conformational changes on the vibrational spectrum.

This force field was transferred unchanged to the calculation of the normal modes of the $\alpha_{\mathrm{II}}$-helix, except for small alterations in $f(\mathrm{CO}), f(\mathrm{NH})$, and $f(\mathrm{H} \cdots \mathrm{O})$ (small changes in other hydrogen-bond force constants are probably warranted, but these cannot be determined at this time because of lack of data). This transfer is probably justified, since there is such a
small conformational difference between the $\alpha_{\mathrm{I}^{-}}$and $\alpha_{\mathrm{II}}$-helices. Nevertheless, there are significant predicted differences between the vibrational frequencies of these two structures, not only in the amide I and II regions as a result of different transition dipole coupling contributions, but particularly in the conformation-sensitive region between 900 and $200 \mathrm{~cm}^{-1}$ (where changes in hydrogen-bond force constants have no influence on the frequencies). This result emphasizes the sensitivity of the vibrational spectrum to even small changes in conformation of the polypeptide chain.

The predicted spectral differences between the $\alpha_{\mathrm{II}^{-}}$and $\alpha_{\mathrm{I}^{-}}$-helices indicate that the helices in the bacteriorhodopsin of H. halobium are probably $\alpha_{\mathrm{II}}$-helices, ${ }^{19}$ which, in turn, led to the suggestion ${ }^{19}$ that the helix itself may be the proton "conductor" in this protein.

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[^0]:    a $\mathrm{S}=$ strong, $\mathrm{M}=$ medium, $\mathrm{W}=$ weak, $\mathrm{V}=$ very, $\mathrm{sh}=$ shoulder, $\|=$ parallel dichroism, $\perp \pm$ perpendicular dichroism.
    $\mathrm{b}_{\mathrm{s}} \mathrm{x}$ stretch, as $=$ antisymmetric stretch, $\mathrm{ss}=$ symmetric stretch, $\mathrm{b}=$ angle bend, $\mathrm{ib}=$ in-plane angle bend, ob $=$ out-of-plane angle bend, $a b=a n t i s y m m e t r i c$ angle bend, $\mathrm{sb}=$ symmetric angle bend, $\mathrm{r}=$ rock, $\mathrm{d}=$ deformation, $\mathrm{t}=$ torsion. Only contributions $10 \%$ or greater are included.
    c Unperturbed frequency.

