1. Report No.	2. Government Accession No.	3. Recipient's Catalog No.
FAA-RD-78-82		
4. Title and Subtitle		5. Report Date
Critical Assessment o	f Emissions from	June 1979
Aircraft Piston Engin	es	6. Performing Organization Code
7. Author(s)		8. Performing Organization Report No.
W. Mirsky, R. J.A. Nicholls,	Pace, R. Ponsonby, D.E. Geister	FAA-NA-78-166
9. Performing Organization Name and Address Department of Aerospa	ce Engineering	10. Work Unit No. (TRAIS)
The University of Mic Ann Arbor, Michigan 4	3	DOTFA74NA-1102
		13. Type of Report and Period Covered
12. Sponsoring Agency Name and Address U.S. Department of Tr Federal Aviation Admi	nistration	Final Report June 1974 - May 1978
Systems Research and Washington, D.C. 2059	_	14. Sponsoring Agency Code

The contract was administered by the National Aviation Facilities Experimental Center, Atlantic City, New Jersey 08405.

16. Abstract

A comprehensive mathematical analysis for evaluating the measured emissions from piston type general aviation aircraft engines is presented and discussed. The analysis is used to calculate the fuel-air ratio, molecular weight of the exhaust products, and water correction factor. Further, a sensitivity analysis is presented which shows the effects of emission measurement errors on calculated fuel-air ratio.

The University's test facility is briefly described and the associated emissions instrumentation is discussed in detail. The experimental results obtained in this facility on the AVCO-Lycoming LIO-320 engine are presented. This includes baseline and lean-out emissions data and the influence of sampling probe location in the exhaust pipe. The influence of leaks in the exhaust system or emissions console are investigated and evaluated in terms of the mathematical model.

Experimental data obtained from various facilities are compared and evaluated.

General Aviation Aircra Emissions (Pollution) Piston Engines	Document is a public through Technical Inspringfield,	gh the Nati formation S	ional Service	
19. Security Classif. (of this report)	sif. (of this page)	21. No. of Pages	22. Price	
UNCLASSIFIED	UNCL	ASSIFIED	149	

METRIC CONVERSION FACTORS

	Symbol		.S .S	z '	₽.'Ē			2 _{ni}	Å45	mi ²				20	₽					# 05	£ 5	- 3	F.	, p			ě	-					
ic Measures	To Find		inches	feet	yards miles			sanare inches	square yards	square miles	acres			Ounces	spunod	short tons				fluid ounces	quarts	gallons	cubic feet	cubic yards			o de la contraction de la cont	temperature		F 6	160 200	001 08 09	
rsions from Metr	Multiply by		0.04	3.3	1.1 0.6		AREA	0.16	1.2	0.4			MASS (weight)	0.035	2.2	7		VOLUME		0.03	1.06	0.26	35	1.3		TEMPERATURE (exact)	9/E (these	3/3 (uren add 32)		•	98.6	20 440	
Approximate Conversions from Metric Measures	When You Know		millimeters centimeters	meters	meters kilometers			square centimeters	square meters	square kilometers	nectares (10,000 m ⁻)		2	grams	kilograms	tonnes (1000 kg)				milliliters	liters	liters	cubic meters	cubic meters		TEMP		temperature			0 40	0 02-	
	Symbol		E E	Ε	e \$			cm ²	a ₂	~ 5.	Pa Pa			σ	, g	•				Ē.		_	E.	² E			Ç	J		į	4 - 0 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	T 4.	
EZ	zz z	OZ	61		8T	Zī	9	T	5 1		* I	ε 	t	73 	T	τ	0	t 	6			2		9		9	•		ε		z 	T wa	
' ' ']''' '	' ' ' ' 8	'l' 	'1'	' ' 7	'l' 	.1.1.	' ' 	' '	l' '	'l'	'l' 	' ' ' 5	!' <u> </u> '	!	' '	' ' 4	' '	' '	"	3	' '	' '	"	'1'	' ' ₂	' '	'l'	' '	1	' '	inche	5
	Symbol			E	E 6	.		ć	, Cm,	E ~E	km ²	ha			o 2	Î _				Ē.	ĒĒ	· -	-		_ ~	. °E			္စပ			286,	
Measures	To Find			centimeters	centimeters	kilometers			square centimeters	square meters	square kilometers	hectares			grams	tonnes				milliliters	milliliters	liters	liters	liters	liters Cubic meters	cubic meters			Celsius	temperature		tables, see NBS Misc. Publ.	
Approximate Conversions to Metric Measures	Multiply by	LENGTH		*2.5	30	1.6	AREA		r. 6	9.0	2.6	0.4	MASS (weight)	38	0.45	6.0		VOLUME	•	ıo i	<u>.</u> 8	0.24	0.47	0.95	3.8	0.76	TEMPERATURE (exact)		5/9 (after	subtracting	Ì	ersions and more detailed in Catalog No. C13.10:286	
Approximate Con	When You Know			inches	feet	miles			square inches	square reer	square miles	acres	2	South	ponuds	short tons	(2000 lb)			teaspoons	fluid ounces	cups	pints	quarts	garrons cubic feet	cubic yards	TEMP		Fahrenheit	temperature		•1 in = 2.54 (exactly), For other exact conversions and more detailed tables, see NBS Misc. Publ. 286, Units of Weights and Messures, Price \$2.25, SD Catalog No. C13.10:286.	
	Symbol			.5	# ⁷	Ē			± 27	بر موء	mi ²			ŧ	g <u>e</u>	!				tsp.	fl oz	v	ŭ.	# d	ga.	, p.			.			*1 in = 2.54 (exa Units of Weights a	

1 in ± 2.54 lexactly). For other exact conversions and more detailed tables, see NBS Misc. Publ. 285, Units of Weights and Measures, Price \$2.25, SD Catalog No. C13.10:286.

PREFACE

This investigation was conducted by personnel of the Aerospace Engineering and Mechanical Engineering Departments of The University of Michigan, Ann Arbor, Michigan under contract No. DOTFA74NA-1102. Professor J.A. Nicholls served as Project Director with Professor W. Mirsky as the Principal Investigator. The contract was administered by the National Aviation Facilities Experimental Center, Atlantic City, New Jersey.

ABSTRACT

comprehensive mathematical analysis for evaluating the measured emissions from piston type general aviation aircraft engines is presented and discussed. The analysis is used to calculate the fuel-air ratio, molecular weight of the exhaust products, and water correction factor. Further, a sensitivity analysis is presented which shows the effects of emission measurement errors on calculated fuel-air ratio.

The University's test facility is briefly described and the associated emissions instrumentation is discussed in detail. The experimental results obtained in this facility on the AVCO-Lycoming LIO-320 engine are presented. This includes baseline and lean-out emissions data and the influence of sampling probe location in the exhaust pipe. The influence of leaks in the exhaust system or emissions console are investigated and evaluated in terms of the mathematical model.

Experimental data obtained from various facilities are compared and evaluated.

TABLE OF CONTENTS

			Page
1.	Intro	oduction	1-1
2.	Data	Analysis and Evaluation	2-1
	2.1	Development of Combustion Equation Models	2-1
		2.1.1 The Simple Combustion Reaction Equation	2-1
		2.1.2 Combustion Air 2.1.3 Computational Procedure for Ambient Air	2-3 2-4
		2.1.3.1 Air Molecular Weight 2.1.3.2 Inclusion of Atmospheric Moisture	2-4 2-6
		2.1.3.3 Detailed Expression for Combustion Air	2-6
		2.1.4 The Expanded Combustion Equation 2.1.5 Methods for Computing Fuel-Air Ratio 2.1.5.1 Development of Method 1.1 2.1.5.2 Development of Method 2.1 2.1.5.3 Development of Method 2.1 2.1.5.4 Development of Method 3.1 2.1.5.5 Development of Method 3.2 2.1.5.6 Matrix Solutions 2.1.5.7 Effect of Hydrocarbon Loss in the Water Trap 2.1.5.8 Effect of Dilution Air (Mixing without Reaction) 2.1.5.9 Comments on Computational Methods	2-6 2-7 2-8 2-11 2-15 2-16 2-16 2-17 2-19 2-19
	2.2	Sensitivity Analysis of Fuel-Air Ratio Computational Models	2-24
	2.3	Evaluation of Data Reliability	2-32
		2.3.1 Comparison of Michigan and Eltinge Methods	2-35
	2.4	Calculation of Exhaust Molecular Weight	2-43
	2.5	Calculation of Water Correction Factors for Exhaust Concentration Measurements	2-47
3.	Univ	ersity of Michigan Test Facility	3-1

			Page
4.	Inst	rumentation for Emission Measurements	4-1
	4.1	Emission Measurement Console	4-1
	4.2	Instrumentation Problems	4-2
		4.2.1 CO Infrared Analyzer 4.2.2 CO2 Infrared Analyzer 4.2.3 O2 Analyzer 4.2.4 Total Hydrocarbon Flame Ionization	4-4 4-4 4-5 4-5
		Detector (FID) 4.2.5 NO/NOX Chemiluminescence Analyzer	4-6
	4.3	Comments	4-7
5.	Univ	ersity of Michigan Engine Emission Data	5-1
	5.1	Avco-Lycoming LIO-320 Baseline Runs	5-1
	5.2	Avco-Lycoming LIO-320 Lean-Out Runs	5-24
	5.3	Effect of Probe Location on Air-Dilution of Exhaust Sample	5-38
	5.4	Check for Air Leaks	5-40
		5.4.1 Leak Check of Gas Analysis System 5.4.2 Leak Check of Engine Exhaust System	5-40 5-41
6.	Inte	r-Facility Data Analysis	6-1
	6.1	Data Analysis Charts - AE versus XTC	6-1
	6.2	Data Analysis Charts - E(1.2) versus XTC	6-5
7.	Summ	nary	7-1
8.	Refe	rences	8-1
Appe	ndix	A Computer Program FAA	A-1
Appe	ndix	B Computer Program FARAT	B-1
Appe	ndix	C Computer Subroutine CRT4	C-1
Appe	ndix	D Computer Subroutine CRT12	D-1
Appe	ndix	E Computer Subroutine CRT15	E-1
Appe	ndix	F Computer Subroutine CRT16	F-1

LIST OF ILLUSTRATIONS

Figure		Page
2.1	Variation of the Water-Gas Equilibrium Constant with Temperature	2-10
2.2	Matrix for the Governing Equations of Method 1.2	2-14
2.3	Matrix for the Governing Equations of Method 3.2	2-18
2.4	Specific Sensitivity vs CO2 Concentration	2-26
2.5	Specific Sensitivity vs CO Concentration	2-27
2.6	Specific Sensitivity vs 02 Concentration	2-27
2.7	Specific Sensitivity vs HCC Concentration	2-28
2.8	Δ E vs XTC: Lycoming Data	2-34
2.9	E(1.2) vs XTC: Lycoming Data	2-36
2.10	E(3.1) vs XTC: Lycoming Data	2-37
2.11	Eltinge Chart	2-38
2.12	XTC and Δ E vs EIE: Eltinge Data	2-40
2.13	Calculated Exhaust Molecular Weight vs Equivalence Ratio	2-44
3.1	Engine Test Stand	3-2
3.2	Engine Control Room	3-3
3.3	Cooling Air Flow Schematic	3-4
3.4	Intake Air Flow Schematic	3-5
3.5	Exhaust Gas Flow Schematic	3-6
5.1.A	LIO-320 Baseline Results: Run 4, Method 1.2	5-3
5.1.B	LIO-320 Baseline Results: Run 4, Method 2.1	5-4
5.1.C	LIO-320 Baseline Results: Run 4, Method 3.1	5-5
5.2.A	LIO-320 Baseline Results: Run 7, Method 1.2	5-6
5.2.B	LIO-320 Baseline Results: Run 7, Method 2.1	5-7
5.2.C	LIO-320 Baseline Results: Run 7, Method 3.1	5-8
5.3.A	LIO-320 Baseline Results: Run 16, Method 1.2	5-9
5.3.B	LIO-320 Baseline Results: Run 16, Method 2.1	5-10
5.3.C	LIO-320 Baseline Results: Run 16, Method 3.1	5-11
5.4	LIO-320 Lean-Out Results for CO	5-25
5.5	LIO-320 Lean-Out Results for UHCC	5-26
5.6	LIO-320 Lean-Out Results for NOX	5-27

		Page
5.7	LIO-320 Lean-Out Results for CO2	5-28
5.8	LIO-320 Lean-Out Results for O2	5-29
5.9	Effect of Probe Location on O2 Concentration	5-39
5.10	Effect of Probe Location on Calculated F/A	5-39
6.1	Δ E vs XTC: Lycoming Data	6-2
6.2	Δ E vs XTC: Michigan Data	6-3
6.3	Δ E vs XTC: Eltinge Data	6-4
6.4	E(1.2) versus XTC: Idle Mode	6-6
6.5	E(1.2) versus XTC: Taxi Mode	6-6
6.6	E(1.2) vs XTC: Take-Off Mode	6-7
6.7	E(1.2) vs XTC: Climbout Mode	6-7
6.8	E(1.2) vs XTC: Approach Mode	6-7

LIST OF TABLES

Table		Page
2.1	Composition of Dry Air	2-3
2.2	Positive and Negative Signs of Specific Sensitivity	2 -25
2.3	Values of Specific Sensitivity	2-30
2.4	Effect of Changes of N2O2 and W on FACAL	2 -31
2.5	Comparison of Michigan and Eltinge Analyses	2-39
2.6	Calculated F/A Errors for Eltinge Zero-EIE Data Points	2-41
2.7	Calculated Exhaust Properties - Lean Mixtures	2-45
5.1	Error Analysis of Runs 4, 7 and 16	5-2
5.2	Computer Print-Out: Run 4	5-12
5.3	Computer Print-Out: Run 7	5-16
5.4	Computer Print-Out: Run 16	5-20
5.5	Computer Print-Out: Lean-Out Results, Mode 2	5-30
5.6	Computer Print-Out: Lean-Out Results, Mode 3	5-33
5.7	Computer Print-Out: Lean-Out Results, Mode 4	5-34
5.8	Computer Print-Out: Lean-Out Results, Mode 5	5-36
5.9	Error Analysis of Exhaust System Leak Tests	5-41
6.1	Computer Print-Out: Run 5	6-8

LIST OF ABBREVIATIONS AND SYMBOLS

AA	Quantity of air in the combustion equation. Defined by Equation (2.4).
AIRO2	Moles dry air per mole oxygen in the dry combustion air.
ARA	Mole-percent argon in the dry combustion air.
ARAS	Standard value for mole-percent argon in the dry combustion air.
ARO2	Moles argon per mole oxygen in the combustion air.
Cl	- (2 + 2 * CO2O2 + H2OO2)
C2	- CO2O2
C3	EHCC
C4	- 2 * H2OO2
C5	- HTCR
C6	EHCC * EHCR
C7	- PSAT/PTRP
C8	- 2 * N2O2
C9	- ARO2
C10	K(CO2W + CO2D + CO2DD)/(COW + COD + CODD)
C11	1 + CO2O2 + (H2OO2/2) + N2O2
COW, COD, CODD	Measured values of exhaust carbon monoxide concentration (wet, dry and dried).
CO2A	Mole-percent carbon dioxide in the dry combustion air.
CO2O2	Moles carbon dioxide per mole oxygen in the combustion air.
CO2W,CO2D, CO2DD	Measured values of exhaust carbon dioxide concentrations (wet, dry and dried).
dAO2	Moles dilution air per mole oxygen in the combustion air.

E(1.2), E(3.1) Fuel-air ratio errors when using

Methods 1.2, 3.1.

EHCC Moles carbon per mole exhaust hydrocarbon.

EHCR Exhaust hydrocarbon hydrogen-carbon ratio,

mole basis.

EIE Eltinge instrument error. See

Section 2.3.1.

FACAL Calculated fuel-air ratio, mass basis.

FAM Measured fuel-air ratio, mass basis.

F/A Fuel-air ratio.

FCHC Fraction condensed, exhaust hydrocarbons,

in the water trap.

FdA Fraction dilution air, mixed with cold

non-reacting exhaust sample

FF Quantity of fuel in the combustion equation.

Defined by equation (2.3).

H2002 Moles water vapor per mole oxygen in the

combustion air.

HC Hydrocarbon

HCCW, HCCD, Measured values of exhaust hydrocarbon

HCCDD concentration, carbon base

(wet, dry or dried).

HTCR Moles hydrogen per mole carbon in the fuel.

Same as Z.

K Water-gas reaction equilibrium constant.

KWD Water correction factor for

dry-to-wet measurements.

KWDD Water correction factor for

dried-to-wet measurements.

(M) Used in describing a concentration.

M = W when wet; M = D when dry;

M = DD when dried.

m Moles hydrogen per mole fuel.

MWAIR Molecular weight of dry combustion air.

MWEXH Molecular weight of the exhaust.

MWH20 Molecular weight of water.

N Used as a prefix to indicate number of moles of a substance (e.g. NCO2). n Moles carbon per mole fuel. N2A Mole-percent nitrogen in the dry combustion air. N2AS Standard value for mole-percent nitrogen in the dry combustion air. N202 Moles nitrogen per mole oxygen in the combustion air. NdAM Moles dilution air in the measured sample. NGD Moles of gaseous dry products. **NGDD** Moles of gaseous dried products. NGM Moles of gaseous products in the measured sample. Moles of gaseous wet products (total). NGT NOW, NOD, Measured values of exhaust nitrogen oxide NODD concentrations (wet, dry and dried). NOXW, NOXD, Measured values of NOX concentrations (wet, NOXDD dry and dried). NT Total moles of products. NY Moles of any specie Y. 02A Mole-percent oxygen in the dry combustion air. 02AS Standard value for mole-percent oxygen in the dry combustion air. 02W,02D,02DD Measured values of exhaust oxygen concentrations (wet, dry and dried).

Calculated equivalence ratio. PHICAL

Measured equivalence ratio. PHIM

Saturation pressure of water at the water **PSAT**

trap temperature.

Measured water trap pressure. PTRP

Eltinge mixture-distribution parameter. S

Specific sensitivity. Defined by equation 2.63. SS

Specific humidity of the combustion air. W

X	Mole-fraction.
XD	Total mole fraction of dry products (wet basis). Also $\mathrm{XD}\left(W\right)$.
XDD	Total mole fraction of dried products (wet basis). Also $XDD(W)$.
XGD	Total mole-fraction of dry gaseous products (wet basis). Also XGD(W). In the analyzer.
XGDD	Total mole-fraction of dried gaseous products (wet basis). Also XGDD(W). In the analyzer.
XGW	Total mole-fraction of wet gaseous products (wet basis). Also $XGW(W)$. By definition $XGW(W) = 1$. In the analyzer.
XT	Total mole-fraction of products (wet basis). Also $XT(W)$.
XY(D)	Mole-fraction of specie Y on a dry gaseous basis.
XY (DD)	Mole-fraction of specie Y on a dried gaseous basis.
XY (W)	Mole-fraction of specie Y on a wet gaseous basis.
XY(T)	Mole-fraction of specie Y on a total mole basis.
XYd(M)	Mole-fraction of specie Y in the air-diluted sample. (M) indicates wet, dry or dried measurement.
YO2	Moles specie Y per mole oxygen.
Z	Moles hydrogen per mole carbon in the fuel. Same as HTCR.
ΔΕ	Fuel-air ratio error difference. $\Delta E = E(3.1) - E(1.2)$.
Σ	Summation.
ф	Equivalence ratio. $\phi = (F/A)/(F/A)_{stoich}$
*	Multiplication sign.

1. INTRODUCTION

The Environmental Protection Agency (EPA) promulgated aircraft exhaust emission standards for piston engines in the Federal Register of July 17, 1973, Volume 38, Number 136, Part II (the EPA Standards). The Federal Aviation Administration (FAA), in assuming its role assigned by Public Law in implementing and enforcing the EPA standards, had to insure that any attempts to reduce the exhaust emissions from light aircraft piston engines did not result in lowered safety of operation.

In accordance with the above FAA contracted with two engine manufacturers, AVCO-Lycoming and Teledyne-Continental, to ascertain the baseline emissions levels actually being produced by a number of their engines. In addition lean-out emissions levels were to be determined. National Aviation Facilities Experimental Center (NAFEC), the experimental arm of FAA, was also to measure the emissions levels from the same engines as tested by the companies.

In addition to the above, FAA contracted with The University of Michigan to establish correct emission measurement techniques, to establish correct procedures for analyzing the measured emissions data, and to verify the type of instrumentation that would insure compliance with the EPA regulations. The University was also directed to establish baseline and lean-out data for the AVCO-Lycoming LIO-320 engine. This program went into effect on June 1, 1974. This report represents the final formal report on the project.

The major thrust of this report, then, is the comprehensive treatment given to the analysis of the measured emissions data. In this way conclusions can then be drawn with confidence as to the sensitivity of the predictions to simplifying assumptions, instrument errors, and measurement errors. Measurements made in the University facility are examined in this light.

2. DATA ANALYSIS AND EVALUATION

An expression for combustion air, which takes into account the variable composition due to ambient carbon dioxide and water vapor, is developed. This is followed by the development of five methods for calculating fuel-air ratio from measured exhaust gas constituents. The sensitivity of these methods to variations of input quantities is then examined and the methods are next applied to a representative sample of data from various sources to illustrate the applicability of these methods in determining data reliability. The calculations of exhaust molecular weights and water correction factors for exhaust measurements are also discussed.

2.1 DEVELOPMENT OF COMBUSTION EQUATION MODELS

2.1.1 The Simple Combustion Reaction Equation

The complete combustion of a hydrocarbon fuel $C_{n\ m}^{\ H}$ with air in a stoichiometric mixture is represented by the combustion equation,

$$C_n H_m + \left(\frac{m}{4} + n\right) [02 + 3.764 \text{ N2}] \rightarrow n \text{ CO2} + \frac{m}{2} \text{ H2O}$$

+ 3.764 $\left(\frac{m}{4} + n\right) \text{ N2}$

In a non-stoichiometric mixture, leading to incomplete combustion, we have,

where the prefix N before each exhaust product is used to indicate moles of each product. The products NO and NO2 are included because of their importance in air pollution.

It is desirable to convert the above expression from a mole basis to a mole-fraction basis by dividing through by

some specified total number of moles, which could be any of the following quantities:

- 1. NT Total number of moles of exhaust products in the instrument analyzers, including both gaseous and solid products. The mole fraction would be on a total-mole basis and would be indicated by symbols such as XCO2(T).
- 2. NGW Total number of moles of wet gaseous exhaust products in the instrument analyzers. The mole fraction would be on a wet basis and would be indicated by XCO2(W). Since most of the development in this report will be on a wet basis, we shall drop the (W) for convenience and simply use XCO2. Mole fractions on any other basis shall be properly identified.
- 3. NGDD Total number of moles of <u>dried gaseous</u> exhaust products in the instrument analyzers, containing saturated water at the water trap temperature. Indicated by XCO2(DD).
- 4. NGD Total number of moles of <u>dry gaseous</u> exhaust products in the analyzers (all water removed). Indicated by XCO2(D).

The need for these distinctions arises because different instruments make measurements on different bases. For example, the instrument cart at The University of Michigan makes the following measurements:

CO2, O2 dried basis
CO dry basis
HCC,NO,NOX wet basis

Converting equation 2.1 to mole-fractions based on wet gaseous products, we have

$$\frac{\phi}{NGW} C_{n}^{H} H_{m} + \frac{1}{NGW} \left(\frac{m}{4} + n\right) [02 + 3.764 \text{ N2}] \rightarrow XCO2 + XCO$$

$$+ XCXHY + XO2 + XH2O + XH2 + XN2 + XNO + XNO2 (2.2)$$

where the prefix X is used to indicate mole-fractions. Next let

$$\frac{\phi}{NGW} C_n H_m = \frac{\phi * n}{NGW} CH_{m/n} = FF * CHZ$$
 (2.3)

where the symbol * is used as the multiplication sign, Z is the molar hydrogen-to-carbon ratio (m/n) of the fuel, and

$$\frac{1}{NGW} \left(\frac{m}{4} + n \right) = AA \tag{2.4}$$

Note that both AA and FF are defined on a wet gaseous basis. The simple form of the combustion reaction then becomes,

FF * CHZ + AA
$$[O2 + 3.764 \text{ N2}] \rightarrow \text{XCO2} + \text{XCO} + \text{XCXHY} + \text{XO2} + \text{XH2O} + \text{XH2} + \text{XNO} + \text{XNO2}$$
 (2.5)

HTCR shall also be used for the molar hydrogen-to-carbon ratio of the fuel.

2.1.2 Combustion Air

The treatment of combustion air as consisting of 3.764 moles of N2 per mole of O2 lumps all of the inert gases with the nitrogen. In this report nitrogen shall be treated as a pure gas and the only inert gases to be considered will be argon and carbon dioxide. Other inerts in atmospheric air such as neon and helium will be neglected because of their very low concentrations.

A search of the literature shows lack of agreement on the exact composition of air, two examples being given in table 2.1. These differences are negligibly small for our purposes, and the values from reference 1 shall be used. The suffix AS in the symbols in table 2.1 is used to indicate the standard value for atmospheric air.

TABLE 2.1. COMPOSITION OF DRY AIR MAJOR CONSTITUENTS: MOLE PERCENT

Constituent	Symbol	Ref. 1	Ref. 2
N2	N2AS	78.09	78.084
02	O2AS	20.95	20.946
AR	ARAS	0.93	0.934
CO2	CO2A	0.03	0.033

The amount of CO2 in the atmosphere will vary from location-to-location, being somewhat higher in urban areas (reference 3). At locations where engines are being tested, the CO2 levels may be even higher. However, since calculated fuel-air ratios are insensitive to ambient CO2 (see table 2.3 for CO2A specific sensitivity values), a background value in the range 0.03 to 0.05 mole percent can be used when ambient measurements are not made.

The treatment of air involving the more accurate composition and possible variation in CO2 levels will lead to more accurate atom-balances when calculating fuel-air ratios and a better value for the calculated molecular weight of air.

2.1.3 Computational Procedure for Ambient Air

2.1.3.1 Air Molecular Weight

Let

N2AS = percent N2 in the standard dry intake air

O2AS = percent O2 in the standard dry intake air

ARAS = percent AR in the standard dry intake air

CO2A = percent CO2 in the existing dry intake air

Then define,

$$N2O2 = \frac{\text{moles } N2}{\text{mole } O2} = \frac{N2AS}{O2AS}$$
 (2.6)

$$ARO2 = \frac{\text{moles AR}}{\text{mole O2}} = \frac{ARAS}{O2AS}$$
 (2.7)

$$CO2O2 = \frac{\text{moles } CO2}{\text{mole} O2} = \frac{CO2A}{O2A}$$
 (2.8)

For any ambient CO2 level, the following relations must hold for dry air (the actual value will be slightly less than 100% in the first relation because of the neglect of other minor constituents of air).

$$N2A + O2A + ARA + CO2A = 100$$
 (2.9)

The symbols represent the mole percent of each constituent in the dry ambient air, allowing for variable CO2 concentration. For the fixed constituents,

$$\frac{N2A}{N2AS} = \frac{O2A}{O2AS} = \frac{ARA}{ARAS}.$$
 (2.10)

Then

$$O2A = \frac{O2AS}{N2AS} * N2A$$
 (2.11)

and

$$ARA = \frac{ARAS}{N2AS} * N2A. \qquad (2.12)$$

Substituting in equation 2.9,

$$N2A + \frac{O2AS}{N2AS} * N2A + \frac{ARAS}{N2AS} * N2A = 100 - CO2A$$
 (2.13)

we get

$$N2A = \frac{100 - CO2A}{1 + \frac{O2AS}{N2AS} + \frac{ARAS}{N2AS}}$$
 (2.14)

Using the following atomic weights based on carbon-12 (reference 2),

MOTA	ATOMIC WEIGHT
AR	39.948
С	12.01115
H	1.00797
N	14.0067
0	15.9994

the molecular weights for the various exhaust gas constituents become,

MOLECULE	MOLECULAR WEIGHT
CO2	44.00995
N2	28.0134
02	31.9988
H20	18.01534

The molecular weight of dry combustion air is then given by:

$$MWAIR = 0.319988 * O2A + 0.280134 * N2A + 0.39948 * ARA + 0.4400995 * CO2A (2.15)$$

2.1.3.2 Inclusion of Atmospheric Moisture

From the definition of specific humidity (W) we have

$$W = \frac{\text{lbm atmospheric moisture}}{\text{lbm dry air}} = \frac{\text{(moles H2O) (MWH2O)}}{\text{(moles dry air) (MWAIR)}}$$
(2.16)

Multiplying by AIRO2, which is defined as,

AIRO2 =
$$\frac{\text{moles dry air}}{\text{mole atmospheric O2}}$$
 (2.17)

we have

$$W * AIRO2 = \frac{\text{(moles H2O) (MWH2O)}}{\text{(moles dry air) (MWAIR)}} \cdot \frac{\text{(moles dry air)}}{\text{(mole O2)}}$$
$$= \frac{\text{moles H2O}}{\text{mole O2}} \frac{\text{MWH2O}}{\text{MWAIR}}$$
(2.18)

Solving for (moles H2O/mole O2) = H2OO2, we get

$$H2002 = \frac{\text{moles } H20}{\text{mole } O2} = W * AIRO2 * \frac{MWAIR}{MWH20}$$
 (2.19)

where

$$AIRO2 = 1 + N2O2 + ARO2 + CO2O2$$
 (2.20)

2.1.3.3 Detailed Expression for Combustion Air

From the above analysis, the detailed expression for the number of moles of wet combustion air per mole of O2 becomes:

2.1.4 The Expanded Combustion Equation

By expanding the combustion equation to include the more accurate composition of air, we more accurately model the combustion process. Furthermore, in addition to introducing argon into the products, we shall also allow for the possibility of atomic carbon in the products. A further complication is introduced by considering the exhaust products in the three different states, "wet", "dried" and "dry". The expanded combustion

equation is then written as,

FF [CHZ] + AA [1 * 02 + N202 * N2 + AR02 * AR + CO202 * CO2 + H2002 * H20]
$$\rightarrow$$

Wet Products	Dried Products	Dry Products
XCO2	XCO2	XCO2
хсо	XCO	XCO
XHC	XHC	XHC
XO2	XO2	XO2
XH2O	XH2ODD	
XH2	XH2	XH2
XN2	XN2	XN2
XNO	XNO	XNO
XNO2	XNO2	XNO2
XAR	XAR	XAR
XC	XC	XC
$\Sigma X = XT$	$\Sigma X = XDD$	$\Sigma X = XD (2.21)$

where the sums of mole fractions (ΣX) include carbon. When carbon is in the <u>solid</u> state, we have for the sum of mole-fractions of <u>gaseous</u> products

XGW = total mole-fraction of wet gaseous products

XGDD = mole-fraction of dried gaseous products

XGD = mole-fraction of dry gaseous products

2.1.5 Methods for Computing Fuel-Air Ratio

Five methods for computing fuel-air ratio will be considered. These will be divided into:

- Group 1. Those methods based on the use of the water-gas reaction equilibrium constant K.
- Group 2. The method based on the sum of the gaseous-product mole-fractions XGW.
- Group 3. The methods which combine the use of K and XGW.

To illustrate the computational procedure, we shall start with the simple case and progress to the more complex conditions.

2.1.5.1 Development of Method 1.1

Consider the combustion reaction in the simple form, FF [CHZ] + AA [1 * O2 + 3.764 N2] \rightarrow XCO2 + XCO + XHC + XO2 + XH2O + XH2O

In this case, the simplified air composition is used and we neglect NO, NO2, AR and C in the exhaust. We assume that measurements are made of CO2, CO, HC on a mole carbon basis (HCC), and O2 which give or can be coverted to XCO2, XCO, XHCC and XO2 (i.e. a wet basis).

The calculated fuel-air ratio, FACAL, can then be determined from

FACAL =
$$\frac{\text{FF * [12.011 + 1.008 * Z]}}{\text{AA * [31.999 + 3.764 * 28.013]}}$$
 (2.23)

The unknown quantities are FF and AA, so we proceed to determine these from the known measurements. We have the following governing equations:

(1) C-Balance
$$FF = XCO2 + XCO + XHCC$$

(2) O-Balance
$$AA * 2 = XCO + XH2O + 2 * (XCO2 + XO2)$$

(3) H-Balance FF *
$$Z = XHCC * EHCR + 2 * (XH2O + XH2)$$

In addition to the unknown quantities FF and AA, these equations introduce the unknown quantities XH2O and XH2. Since we now have four unknowns (FF, AA, XH2O and XH2) and only three equations in these unknowns, it becomes necessary to find one additional equation.

At this point we introduce the equilibrium constant for the water-gas reaction,

$$CO2 + H2 + CO + H2O$$
. (2.24)

The equilibrium constant is given by

$$K = \frac{[XCO][XH2O]}{[XCO2][XH2]} \bullet \qquad (2.25)$$

Even though the equilibrium constant varies considerably with temperature, as shown in figure 2.1, the reaction tends to freeze out at a relatively constant temperature during the expansion stroke. This permits the use of a fixed value for K and values of 3.5 (reference 4) and 3.8 (reference 5) appear in the literature. We shall use K = 3.5. Table 2.3 shows how changes in K will affect the calculated fuel-air ratio.

It should be recognized that some variation in freeze-out temperature will occur so that equilibrium conditions may not be reached, necessitating some changes in the value of K to get good agreement between calculated and measured fuel-air ratios.

At this point we have a system of four equations in the four unknowns, so that the equations may be solved for these four unknowns.

To accomplish this, and to establish the procedure for the more complex system of equations to come, we set up the equations in matrix form for solution. The matrix is derived from the system of four equations, each equation being written in terms of the four unknown and a constant for the right-hand-side of the equation, i.e. having the general form,

$$C_{i1}$$
 * AA + C_{i2} * FF + C_{i3} * XH2O + C_{i4} * XH2 = Const (2.26)

where i is the equation number. The system of four equations becomes:

O-Balance 2 * AA + 0.0 * FF - 1 * XH2O + 0.0 * XH2
=
$$XCO + 2 * (XCO2 + XO2)$$
 (2.27)

C-Balance
$$0.0 * AA + 1 * FF + 0.0 * XH2O + 0.0 * XH2$$

= $XCO2 + XCO + XHCC$ (2.28)

H-Balance 0.0 * AA + Z * FF - 2 * XH2O - 2 * XH2
$$= XHCC * EHCR$$
 (2.29)

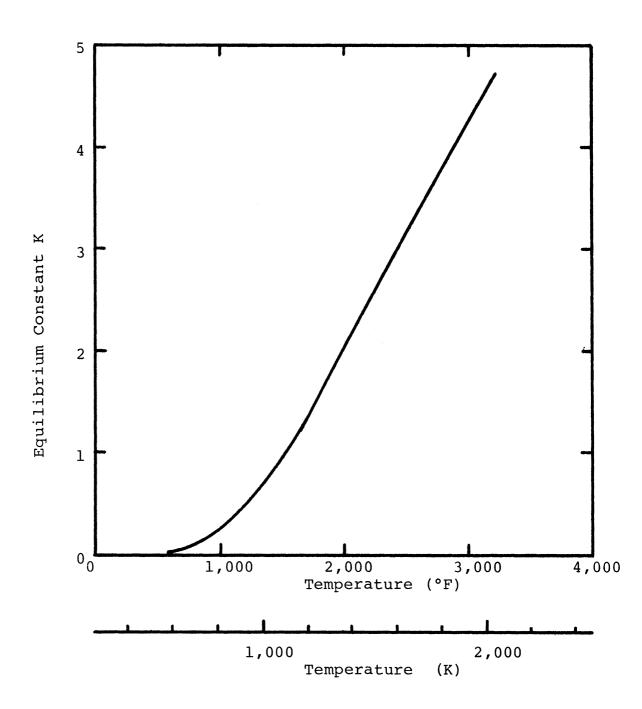


Figure 2.1. Variation of the Water-Gas Equilibrium Constant with Temperature.

In matrix form this becomes:

	AA	$\underline{\mathbf{FF}}$	XH2O	XH2	Const
O-Balance	2	0.0	- 1	0.0	XCO + 2 * (XCO2 + XO2)
C-Balance	0.0	1	0.0	0.0	XCO2 + XCO + XHCC
H-Balance	0.0	Z	- 2	- 2	XHCC * EHCR
K-Equation	0.0	0.0	1	$-\frac{K * XCO2}{XCO}$	0.0. (2.31)

Solutions for AA, FF, XH2O and XH2 can then be obtained for given measured quantities of XCO, XCO2, XO2 and XHCC. A value for EHCR (exhaust hydrocrabon hydrogen-to-carbon ratio) is assumed and is usually taken to be 1.85, as recommended in the Federal Register. The values of AA and FF are used in computing fuel-air ratio using equation 2.23. In addition the water correction factor KWD, which is used to correct dry-to-wet exhaust gas measurements, is obtained from from

The above method, although developed in a different manner, essentially corresponds to the solution presented by Spindt (reference 4). A comparison of his results, with results obtained by the method developed in this section, shows excellent agreement.

2.1.5.2 Development of Method 1.2

The method developed in the previous section will now be expanded to include the following features:

- 1. Detailed expression for the combustion air.
- 2. Addition of products NO, NO2 and AR, but not atomic carbon.
- 3. Use of concentrations based on wet, dried or dry measurements.

The combustion reaction is as given by equation 2.21, with the exclusion of atomic carbon. For this case, the number of unknown quantities grows to fifteen. These are:

	1. X	KGD	6.	XCO	11. XH2O	
	2. 3	KGDD	7.	XHC	12. XH2ODI	D
	3. A	ΛA	8.	XO2	13. XN2	
	4. F	F	9.	XNO	14. XAR	
	5. X	CO2	10.	XNO2	15. XH2	
The	requir	ed fifteen	equations	which govern t	hese unknow	wns are:
1.	Equat	ion defini	ng XGD			
			XGD + XI	120 = XGW		(2.33)
2.	Equat	ion defini	ng XGDD			
			XGD + XH20	ODD = XGDD		(2.34)
3.	0 x yge	n balance				
	AA [2	+ 2 * CO2	O2 + H2OO2]	= 2 * XCO2 +	XCO	
		+ 2 *	XO2 + XH2O	+ XNO + 2 * XN	02	(2.35)
4.	Carbo	n balance				
		FF + CO2O2	* AA = XC	02 + XCO + EHCC	* XHC	(2.36)
5.	CO2 m	easurement	(measured	value on left)		
		CO2W =	XCO2	(if wet measure	ement)	(2.37a)
	or	CO2DD =	XCO2/XGDD	(if dried meas	urement)	(2.37b)
	or	CO2D =	XCO2/XGD	(if dry measure	ement)	(2.37c)
6.	CO me	asurement	(measured	value on left)		
		COW =	XCO	(if wet measure	ement)	(2.38a)
	or	CODD =	XCO/XGDD	(if dried meas	urement)	(2.38b)
	or	COD =	XCO/XGD	(if dry measure	ement)	(2.38c)
7.	HCC m	easurement	(measured	value on left)		
		HCCW =	XHC * EHCC	(if wet measure	ement)	(2.39a)
	or	HCCDD =	XHC * EHCC/	XGDD (if dried meas	uromon+)	(2 20h)
	or	HCCD =	XHC * EHCC/		urement,	(2.390)
				(if dry measure	ement)	(2.39c)
8.	O2 me	asurement	(measured	value on left)		
		02W =	XO2	(if wet measure	ement)	(2.40a)
	or	O2DD =	XO2/XGDD	(if dried meas	urement)	(2.40b)
	or	O2D =	XO2/XGD	(if dry measure	ement)	(2.40c)

9. NO measurement (measured value on left)

$$NOW = XNO$$
 (if wet measurement) (2.41a)

or
$$NOD = XNO/XGD$$
 (if dry measurement) (2.41c)

10. NOX measurement (measured values on left)

$$(NOXW - NOW) = XNO2$$
 (if wet measurement) (2.42a)

or

$$(NOXDD - NODD) = XNO2/XGDD$$
 (if dried measurement) (2.42b)

or

$$(NOXD - NOD) = XNO2/XGD$$
 (if dry measurement) (2.42c)

11. Hydrogen balance

12. Condition in water trap

$$XH2ODD/XGDD = PSAT/PTRP$$
 (2.44)

13. Nitrogen balance

$$2 * N2O2 * AA = 2 * XN2 + XNO + XNO2$$
 (2.45)

14. Argon balance

$$ARO2 * AA = XAR$$
 (2.46)

15. Water-gas equilibrium

$$K = (XCO * XH2O) / (XCO2 * XH2)$$
 (2.47)

This system of equations is shown in matrix form in figure 2.2. Symbols are defined in the List of Abbreviations and Symbols. Since we have fifteen equations involving the fifteen unknowns, a solution of the matrix will give values for the fifteen unknowns for the given input values of

- (a) Measured CO2, CO, HCC, O2, NO and NOX.
- (b) Fuel HTCR and exhaust hydrocarbon EHCC and EHCR.
- (c) Water trap conditions PSAT and PTRP (saturation pressure and total pressure of sample in the water trap).
- (d) Computed air properties N2O2, ARO2, CO2O2 and H2OO2.
- (e) Water gas equilibrium constant K.

NOXW -NOW CONST CO2W XGW COW HCW MON 02W 0 0 0 0 0 0 0 0 XH2 C10 ~ XAR H XN2 2 XH20DD XH20 7 \vdash 7 XN02 7 XNO \vdash X02 7 XHC C390 XC0 Н \vdash XC02 FF 7 **C**5 C1* C2 C4 C8 AA 60 -NOXDD +NODD -C02DD XGDD -HCDD -02DD -NODD -CODD 乊 C2 -C02D -NOXD +NOD XGD -COD -HCD -02D -NOD \vdash Water-AR-Bal 0-Bal N-Bal C-Bal H-Bal Trap XGDD C02 XGD HCC 00 02

*See List of Abbreviations and Symbols.

Figure 2.2. Matrix for the Governing Equations of Method 1.2.

It should be pointed out that Method 1.2 will reduce to Method 1.1 by proper selection of some of the input quantities. This is accomplished when

$$N2O2 = 3.764$$
 $H2OO2 = 0$ $ARAS = 0$ $NO = 0$ $CO2A = 0$ $NOX = 0$

Since Method 1.2 is more general than Method 1.1, it is used as one of the four methods in The University of Michigan data reduction program FAA (see appendix A). The other three methods, Methods 2.1, 3.1, and 3.2, are developed in the following sections.

2.1.5.3 Development of Method 2.1

In Methods 1.1 and 1.2 we introduced the equation for the water-gas equilibrium constant to come up with an additional equation governing the unknowns. This was done so that the number of equations equaled the number of unknowns. We can also use other reasonable constraints. The one selected for study in what we call Method 2.1 is that the sum of the molefractions of the gaseous wet products is equal to XGW, i.e.

$$\Sigma XY (W) = XGW \qquad (2.48)$$

The value of XGW is generally taken to be 1, but can be less because of omitted unknown minor gaseous products.

This appeared to be a more reasonable constraint than the water-gas equilibrium equation, because of the possible variation of the equilibrium constant K due to changes in freeze-out temperature. In addition, all of the major stable gaseous species are accounted for in the products, making it reasonable to assume that the summation of the gaseous mole fractions should be very nearly equal to 1.

We again have 15 equations for the same 15 unknowns shown in Section 2.1.5.2, and the corresponding matrix is similar to

that shown in figure 2.2. The only change occurs when equation 2.47 for the water-gas equilibrium constant is replaced by the summation

$$XCO2 + XCO + XHC + XO2 + XNO + XNO2 + XH2O$$

+ $XN2 + XAR + XH2 = XGW = 1.$ (2.49)

2.1.5.4 Development of Method 3.1

This method was developed after finding that Method 2.1 often led to negative values of XH2. It was felt that this occurred because of the neglect of carbon in the products. By including carbon as an additional unknown, an additional equation also had to be introduced to make the number of governing equations equal to the number of unknowns. Therefore, the equation for the water-gas equilibrium constant was re-introduced to the system of equations in Method 2.1.

We further assume that by the time the exhaust measurements are made, the carbon would be in solid form and would be filtered from the sample stream. Thus, the equations involving mole fractions of gaseous products are not affected by the presence of solid carbon and only the carbon balance equation is affected.

The addition of solid carbon, XC, and the introduction of the water gas equilibrium constant equation gives us a system of 16 unknowns and 16 equations. The resulting matrix is similar to that shown in figure 2.2, with the addition of equation 2.49.

2.1.5.5 Development of Method 3.2

This method is a modification and expansion of the method presented by Stivender (reference 5). Its value lies in the fact that it does not require an oxygen measurement of the exhaust products. An examination of Stivender's paper shows that the method falls into the category of Group 3, in that both the water-gas-equilibrium-constant and sum-of-mole-fraction equations are used. Being the second method in Group 3, it is identified as Method 3.2.

Development of this method starts with the combustion reaction equation as given by equation 2.21 and the system of sixteen unknowns and governing equations of Method 3.1. The development then proceeds as follows:

1. Equation 2.48 is solved for XO2 and the result is substituted into the other governing equations, eliminating two equations [equation 2.48 and equation 2.40] and one unknown (XO2). Two of the resulting equations of interest are the O-N-balance equations.

From the O-balance we get,

$$AA(2 + 2 * CO2O2 + H2OO2) = 2 * (XGW - XHC - XH2 - XAR)$$

- $XCO - XH2O - (2 * XN2 + XNO)$ (2.50)

while the N-balance equation remains unchanged,

$$AA(2 * N2O2) = (2 * XN2 + XNO) + XNO2$$
 (2.51)

2. Equation 2.51 is solved for (2 * XN2 + XNO), the result is substituted in equation 2.50 and the equation is divided by 2 to give,

$$AA(1 + CO2O2 + \frac{H2OO2}{2} + N2O2) = (XGW - XHC - XH2 - XAR) + \frac{1}{2} (XNO2 - XCO - XH2O)$$
 (2.52)

This step eliminates the unknowns XN2 and XNO as well as equation 2.45 or 2.51 and 2.41.

Thus, this procedure has eliminated four equations [2.48, 2.40, 2.45, and 2.41] but only three unknowns (XO2, XN2 and XNO). An additional unknown has to be eliminated and we select the mole fraction of carbon, XC, thereby ending up with a system of twelve equations in twelve unknowns. The corresponding matrix is shown in figure 2.3.

2.1.5.6 Matrix Solutions

The matrices thus formed in Methods 1.1, 1.2, 2.1, 3.1, and 3.2 represent systems of linear equations in the unknown quantities. Standard methods are available for the solution of such a system of equations. The method selected for our programs is called Crout's Method and the subroutines are included with our programs - FAA and FARAT (for fuel-air ratio), and are listed

CONST	XGW	0	1	0	CO2W	COW	HCW	NOXW -NOW	0	0	0	0
хн2			τ						-2			C10
XAR			1								-1	
XH20 DD		-1								1		
XH20	1		5.0						-2			ij
XN02			5.0-					1				
хнс			Τ	-C3			1		90-			
XC0			0.5	-1		1						
XC02				-1	П			·				
FF				1					-C5			
AA		:	C11*	-C2					-C4		60-	-
ХСОО		1			-со2р -со2рр	-сорр	-нсрр	-NOXD -NOXDD +NOD +NODD		۲۵		
XGD	1	-1		·	-C02D	-сор	HCD	-NOXD				
	XGD	XGDD	0-Bal	C-Bal	XC02	XC0	ХНС	XN02	H-Bal	Trap	Ar-Bal	Water- Gas

*See List of Abbreviations and Symbols.

Figure 2.3. Matrix for the Governing Equations of Method 3.2.

in the appendices. They are,

SUBROUTINE CRT4

SUBROUTINE CRT12

SUBROUTINE CRT15

SUBROUTINE CRT16

for solving the system of 4, 12, 15 and 16 equations, respectively.

2.1.5.7 Effect of Hydrocarbon Loss in the Water Trap

The question of possible loss of some of the exhaust sample hydrocarbons by condensation in the water trap and the resulting effect on calculated fuel-air ratio is considered next. It turns out that the required modification to the computer program FARAT is extremely simple. It involves only a redefinition of the sum-of-mole-fractions of dry gaseous products in the analyzers from

$$XGD + XH2O = XGW (2.33)$$

to

$$XGD + XH2O + FCHC * XHC = XGW$$
 (2.53)

where

FCHC = fraction condensed hydrocarbons

- = 0 for zero condensation
- = 1 for total condensation of exhaust hydrocarbons.

That is, the total mole-fraction of dry gaseous products in the instrument analyzers consists of what is left of the gaseous exhaust sample after all of the water and a portion of the hydrocarbons have been removed from the exhaust sample. The effects of FCHC on FACAL are presented in table 2.3 in terms of specific sensitivities.

2.1.5.8 Effect of Dilution Air (Mixing without Reaction)

The possibility of dilution of the cooled exhaust sample with air without further reaction, such as might result from an air leak in the instrumentation package, was examined. This was accomplished by means of a modification to the computer program FARAT. Measured concentrations are modified to simulate the

effect of air dilution, and the resulting diluted concentrations are used to compute fuel-air ratio. In this manner, the effect of varying degrees of dilution on computed fuel-air ratio can be determined.

The development begins with a definition of fraction dilution air (FdA),

FdA = moles wet dilution air/moles gaseous wet products
 in the undiluted sample

or

$$FdA = NdAW/NGW$$
 (2.54)

Next, recalling that the composition of air per mole of oxygen is given by,

1 mole oxygen per mole oxygen

N2O2 moles nitrogen per mole oxygen

ARO2 moles argon per mole oxygen

CO2O2 moles carbon dioxide per mole oxygen

H2002 moles water vapor per mole oxygen

we get for the moles dilution air per mole oxygen, in dilution air,

$$dAO2 = 1 + N2O2 + ARO2 + CO2O2 + H2OO2$$

= AIRO2 + H2OO2 (2.55)

It is assumed that the dilution air has the same composition as the combustion air, so that the value of AIRO2 used in this section is the same as used in section 2.1.3.2 for the combustion air.

In the diluted sample the concentration of any specie Y will be given by

$$\frac{NY + NdAW * (YO2/dAO2)}{NGM + NdAM} = XYd(M)$$
 (2.56)

where M is used to indicate the "measurement" condition, i.e. either wet, dry or dried. The various terms are defined by,

NY moles of specie Y in the undiluted sample

NdAW * (YO2/dAO2) moles of specie Y in the dilution air

NGM moles of gas in the undiluted sample

NdAM moles of dilution air in the diluted sample

XYd(M) mole-fraction of specie Y in the diluted sample.

Dividing numerator and denominator by NGW gives,

$$\frac{XY(W) + FdA * (YO2/dAO2)}{XGM(W) + (NdAM/NGW)} = XYd(M)$$
 (2.57)

For dry or dried measurements, the wet mole fraction XY(W) must be replaced by its equivalent in terms of the dry or dried measurement. To accomplish this we use

$$\frac{NY}{NGW} = \frac{NY}{NGD} * \frac{NGD}{NGW}$$

to get

$$XY(W) = XY(D) * XGD(W)$$
 (2.58)

for dry measurements, and in a similar manner we get

$$XY(W) = XY(DD) * XGDD(W)$$
 (2.59)

for dried measurements. Substitution leads to the following set of equations for wet, dry and dried measurements. For wet measurements, we have

$$\frac{XY(W) + FdA * (YO2/dAO2)}{1 + FdA} = XYd(W)$$
 (2.60)

For dry measurements, from equations 2.57 and 2.58,

$$\frac{XY(D) * XGD(W) + FdA * (YO2/dAO2)}{XGD(W) + \frac{NdAD}{NGW}} = XYd(D)$$

But the number of moles of dry dilution air is given by

$$NdAD = FdA * NGW * (AIRO2/dAO2)$$

Therefore, for dry measurements,

$$\frac{XY(D) * XGD(W) + FdA * (YO2/dAO2)}{XGD(W) + FdA * (AIRO2/dAO2)} = XYd(D)$$
 (2.61)

Finally, for dried measurements, from equations 2.57 and 2.59,

$$\frac{XY(DD) * XGDD(W) + FdA * (YO2/dAO2)}{XGDD(W) + \frac{NdADD}{NGW}} = XYd(DD)$$

To simplify the computation without introducing a serious error, we can assume that the number of moles of dried dilution air is equal to the number of moles of dry dilution air, so that

$$\frac{\text{NdADD}}{\text{NGW}} = \frac{\text{NdAD}}{\text{NGW}} = \text{FdA} * (AIRO2/dAO2)$$

Therefore, for dried measurements,

$$\frac{XY (DD) * XGDD (W) + FdA * (YO2/dAO2)}{XGDD (W) + FdA * (AIRO2/dAO2)} = XYd (DD)$$
 (2.62)

To determine the effects of dilution air on calculated fuel-air ratio, the actual measurements, XY(W), XY(D) and XY(DD), of the undiluted sample are used to compute fuel-air ratio, XGD(W) and XGDD(W). With these values and assumed values of FdA and YO2, the diluted concentrations are computed using equations 2.60, 2.61 and 2.62. These are then used to calculate the fuel-air ratio as determined from the diluted concentrations. The results of this analysis are presented in table 2.3 in terms of specific sensitivities for the variable FdA (fraction dilutionair).

2.1.5.9 Comments on Computational Methods

Each of the methods developed above possesses unique desirable properties to be considered when selecting one method over the other.

Method 1.1 is the easiest to use and gives results equal to those obtained by the conventional Spindt method(reference 4). In addition the mole fractions of H2 and H2O are computed and the latter can be used to compute the dry-to-wet water correction factor using equation 2.32. One drawback is that the method, as developed, requires that all concentration measurements be on a "wet" basis. However, modifications to permit the use of any combination of "wet" and "dry" measurements could easily be made.

Method 1.2 is based on a more accurate combustion model and was used as the principal means for calculating fuel-air ratio at Michigan. The main features of this method are:

- 1. Any combination of "wet", "dry" or "dried" measurements can be used. Conversions to the "wet" measurement are handled within the program.
- 2. Mole fractions of the principal stable exhaust species, except solid carbon, are computed. This information is used when computing exhaust molecular weight (see section 2.4).
- 3. The computed sum of exhaust mole-fractions (XTC) serves as an excellent internal check on data validity. A value of XTC which deviates by more than +3% from a value of about 1.02 (a value that should be established by each test facility and should be based on the average value from a large number of test data) is a good indication of poor data.

This last feature has been used extensively at Michigan to quickly spot poor data and is the main reason for adopting this as the principal method at Michigan.

Method 2.1 has most of the features of Method 1.2 except that XTC is not computed and is thus not available as an internal check. This is considered to be a major deficiency of this method. However, the method is one of the more sensitive to errors in concentration measurements (see figures 2.4 to 2.7) and the use of XTC in place of the water-gas reaction equilibrium constant may be desirable in some cases.

Method 3.1 is similar to Method 2.1 in that XTC is assigned a fixed value and is thus not available as an internal check on data validity. The added feature of this method is that the mole-fraction of solid carbon is computed. Visual checks of carbon deposited on filter paper from sampling line filters shows good qualitative agreement with calculated concentrations of solid carbon.

The main feature of Method 3.2 is that it does not require an O2 concentration measurement. Neither XTC nor solid carbon concentrations are computed by this method.

2.2 SENSITIVITY ANALYSIS OF FUEL-AIR RATIO COMPUTATIONAL MODELS

The four principal models for calculating fuel-air ratio were subjected to a sensitivity analysis to determine how strongly small changes in the various input quantities affected the calculated fuel-air ratio. This was accomplished by selecting several runs covering a broad range of exhaust pollutant concentrations and then calculating fuel-air ratio while varying one of the input variables at a time. The effects of the following thirteen variables on all four models were determined and the results are given

Variable Name

1.	Measured CO2 concentration	CO2DD
2.	Measured CO concentration	COD
3.	Measured 02 concentration	O2DD
4.	Measured HCC concentration	HCCW
5.	Measured NO concentration	MOM
6.	Combustion air nitrogen-oxygen ratio	N202
7.	Combustion air CO2 content	CO2A
8.	Combustion air water vapor content	W
9.	Fuel hydrogen-to-carbon ratio	HTCR
10.	Exhaust hydrocarbon carbon number	EHCC
11.	Exhaust hydrocarbon hydrogen-carbon ratio	EHCR
12.	Sum of wet gaseous exhaust mole-fractions	XGW

in figures 2.4 to 2.7 and in table 2.3.

Results are reported in terms of what we shall call specific sensitivity (SS) for the particular variable. Specific sensitivity is defined by

Water gas reaction equilibrium constant

SS =
$$\frac{\text{Percent change in calculated fuel-air ratio}}{1\% \text{ increase in variable}}$$
 (2.63)

Specific sensitivity is strongly dependent upon the method used for computing fuel-air ratio, somewhat less dependent upon the magnitude of the variable being tested (e.g. the level of concentration of a pollutant) and to a lesser extent upon the magnitude of the other pollutant concentrations.

Figures 2.4 through 2.7 show plots of specific sensitivity versus concentration for the exhaust products CO2, CO, O2 and HCC. The fact that the specific sensitivity shows various combinations of being plus and minus for the various pollutants, as shown in table 2.2, introduces the possibility of determining which pollutant measurement contributes most strongly to the calculated fuel-air ratio error.

TABLE 2.2. POSITIVE AND NEGATIVE SIGNS OF SPECIFIC SENSITIVITY

Method	CO2	CO	02	HCC
1.2	-	+		+
2.1	+	+	+	+
3.1	-	-	-	+
3.2	+	+	**	+

^{**}The O2 measurement is not involved in Method 3.2.

As an example, one test run of the Lycoming 0-320 engine resulted in the following fuel-air ratio errors:

Method	Original Error
	Percent
1.2	3.030
2.1	24.733
3.1	-10.053
3.2	10.477

For the concentrations involved, the specific sensitivities are:

	CO2	CO	02	HCC
Concentration (PPM)	67022	129820	4310	15688
Method				
1.2	-0.15	+0.24	-0.02	+0.094
2.1	+1.10	+1.77	+0.05	+0.150
3.1	-1.28	-0.95	-0.08	+0.054
3.2	+0.32	+0.78	0.00	+0.115

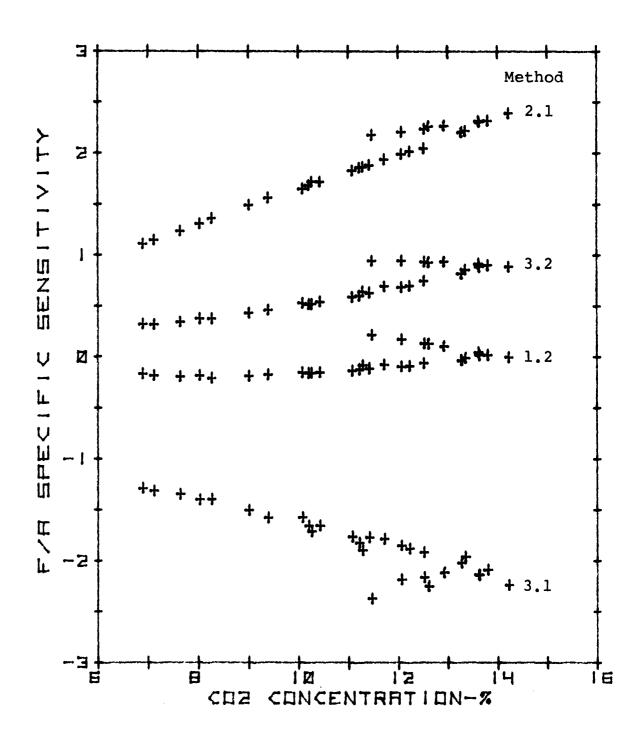


Figure 2.4. Specific Sensitivity vs CO2 Concentration

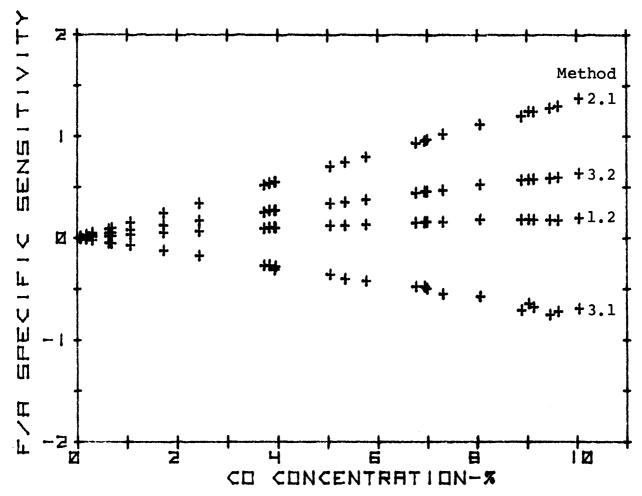


Figure 2.5. Specific Sensitivity vs CO Concentration

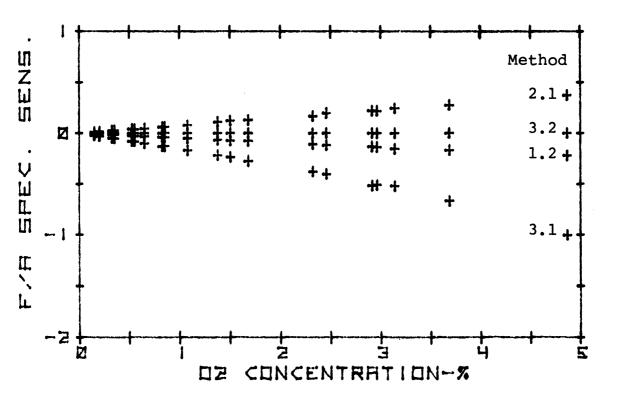


Figure 2.6. Specific Sensitivity vs O2 Concentration

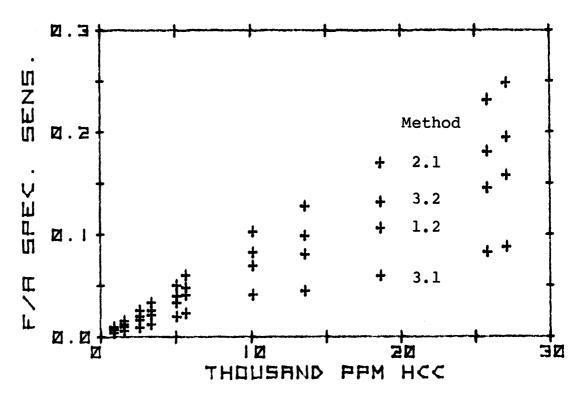


Figure 2.7. Specific Sensitivity vs HCC Concentration

The data is next examined for a possible change in one concentration measurement which would reduce fuel-air ratio errors from all four methods to essentially zero. The required changes in concentration is determined by dividing each fuel-air error by the corresponding specific error and taking the negative of these values.

Percent Change =
$$-\frac{\text{fuel-air ratio error}}{\text{specific sensitivity}}$$

REQUIRED CONCENTRATION CHANGES (%)

Method	<u>CO2</u>	<u>co</u>	<u>02</u>	HCC
1.2	20.20	-12.63	151.5	-32.33
2.1	-22.48	-13.97	-494.66	-164.89
3.1	- 7.85	-10.58	-125.66	186.17
3.2	-32.74	-13.43		-91.10

Only the CO changes are reasonably consistent. Therefore, considering the fact that the CO specific sensitivity for Method 2.1 is much larger than the others and deserves a higher weighting factor, a CO concentration correction of about -12% is chosen. A computer check using a CO reduction of 11.8% did in fact reduce all errors to below 1% as shown.

ERROR AFTER AN 11.8% REDUCTION IN CO

Method	Percent
1.2	0.632
2.1	0.850
3.1	0.483
3.2	0.717

Shown in table 2.3 are the values for specific sensitivity for the remaining variables checked. As stated earlier, these will vary somewhat from one test case to another, but in general the magnitudes are accurate enough for comparative predictions.

Given in the table are the maximum values obtained from a large number of test runs.

TABLE 2.3. VALUES OF SPECIFIC SENSITIVITY

Specific Sensitivity

<u>Variable</u>	Method 1.2	Method 2.1	Method 3.1	Method 3.2
NOW	0.0080	-0.0075	0.023	0.0016
N2O2	-0.78	1.3	-3.0	0.0027
CO2A	-0.0012	-0.0082	0.0064	-0.0037
W	0.012	0.0025	0.020	0.0075
HTCR	-0.20	0.69	-0.85	0.15
EHCC	0.0	-0.082	0.074	-0.032
EHCR	0.048	-0.076	0.16	0.0031
XGW	-0.16	-0.25	-0.088	1.2
K	-0.093	0.0	-0.16	-0.058

An examination of the specific sensitivity values for Method 1.2 shows that the method is most sensitive to changes in the N2O2 ratio (the ratio of atmospheric nitrogen to oxygen). If we consider the effect of going from a value of 3.7274 to a value of 3.76 (the value in common use), where the change in N202 is a +0.875 percent change, we find that the resulting contribution to the Method 1.2 fuel-air error is about -0.6%. Neglect of combustion air humidity, at a specific humidity level of about 0.008, would contribute approximately another -1.0% to Together, these two contributions would amount to the error. approximately -1.6%. The actual computed results are shown in table 2.4 where the original FACAL of 0.05145 was reduced to 0.05111 by assuming that N2O2 is 3.76 and was further reduced to 0.05079 by neglecting atmospheric moisture. Thus, the non-negligible effects on calculated fuel-air ratio of seemingly minor assumptions becomes obvious. In this example the effect was to reduce the calculated fuel-air ratio by -1.28%.

TABLE 2.4. EFFECTS OF CHANGES OF N2O2 AND W ON FACAL

	RUN: 5.1 DRY MEASUREMENTS DRIED MEASUREMENTS WET MEASUREMENTS HTCR EHCC 2.190 1.000	C02	co	02	HCC	NO	NOX
	DRY MEASUREMENTS	0.	17656.	O .	0.	O .	0.
	DRIED MEASUREMENTS	51214.	0.	109523.	0.	0.	0.
	WET MEASUREMENTS	0.	О.	0.	31808.	173.	223
	HTCR EHCC	EHCR	C02A	PSAT	PTRP	W	N202
	2. 190 1. 000	1, 850	0. 030	0. 08866	19,000	0.0081	3 7274
	XCO2 XCO XHC	X02	XH2O XH2	2 XN2	XNO XNO	2 YAR	YC.
Ο.	0474 0.0163 0.0318	0. 1014 0.	0788 0.0077	7 0. 7091 0	0007 0 000	1 0 0084 0	0000
	MTD XTC K	FCHC	FDA PHI	MWEXH	KWD FA	CAI FA	M FRROR
	1. 2 1. 0013 3. 5000	0. 0000 O.	0000 0 7742	2 27 8375 0	9211 0 05	145 0 0525	1 -2 011
					. ,	140 0. 0020	2.011
	RUN: 5. 1	C02	CO	02	HCC	NO	NOX
	DRY MEASUREMENTS	0.	17656.	0.	0.	0.	0.
	DRIED MEASUREMENTS	51214.	0.	109523.	0.	0.	0.
	DRY MEASUREMENTS DRIED MEASUREMENTS WET MEASUREMENTS	0.	0.	0.	31808.	173.	223.
	HILK EHUL	EHUR	CUZA	PSAI	PTRP	W	N202
	2. 190 1. 000	1. 850	0. 030	0. 08866	19, 000	0. 0081	3. 7600
	XCO2 XCO XHC	X02	XH20 XH2	2 XN2	XNO XNO	2 XAR	XC
0.	0474 0.0163 0.0318	0. 1014 0.	0789 0.0077	7 0. 7152 0.	0002 0.000	1 0.0085 0	. 0000
	MTD XTC K	FCHC	FDA PHI	MWEXH	KWD FA	CAL FA	M ERROR
	1. 2 1. 0075 3. 5000	0.0000 0.	0000 0. 7743	3 27, 8384 0	9211 0.05	111 0.0525	1 -2.659
	RUN: 5.1 DRY MEASUREMENTS DRIED MEASUREMENTS WET MEASUREMENTS HTCR EHCC	C02	CO	02	HCC	NO	NOX
	DRY MEASUREMENTS	0.	17656.	О.	0.	O .	Ο.
	DRIED MEASUREMENTS	51214.	О.	109523.	Ο.	O .	О.
	WET MEASUREMENTS	0.	O .	Ο.	31808.	173.	223.
	HTCR EHCC	EHCR	CO2A	PSAT	PTRP	W	N202
	2. 190 1. 000	1.850	0. 030	0. 08866	19. 000	0. 0000	3. 7600
	XCO2 XCO XHC	XO2	XH2O XH2	2 XN2	XNO XNO	2 XAR	XC
O.	0479 0.0164 0.0318	0. 1025 0.	0688 0.0067	7 0. 7250 0.	0002 0.000	1 0.0086 0	. 0000
	MTD XTC K	FCHC	FDA PHI	MWEXH	KWD FA	ICAL FA	M ERROF
	1. 2 1. 0081 3. 5000	0.0000 0.	0000 0. 7694	1 27. 9789 C). 9312 <u>0. 05</u>	079 0.0525	1 -3. 27C

2.3 EVALUATION OF DATA RELIABILITY

An important aspect of this study was the problem of determining the uncertainty associated with the reliability of the collected engine emission test data. It is implicit in the Federal Register that agreement between the measured and calculated values of fuel-air ratio would be taken as a measure of data reliability. However, as the study at The University of Michigan progressed and the study led to the development of four seemingly equally reliable methods for calculating fuel-air ratio, the question arose as to which of the four calculated fuel-air ratios was to be compared with the measured value.

Analysis of engine emission data demonstrated that quite frequently the four computational methods led to four appreciably different values of fuel-air ratio. At times the error from Method 1.2 (essentially an expanded Spindt method) would be acceptably very low while the other methods gave errors that were unacceptably very high. Values for an extreme case are shown. (See table 5.4, run 16, mode 4.)

Method	Fuel/Air Error Percent	XTC
1.2	0.570	0.73928
2.1	-51.906	
3.1	56.095	
3.2	-28.482	

Since the Spindt method is quite commonly used to calculate fuelair ratio, it is important to realize that cases can arise where the calculated Spindt error is not in itself a sufficient check of data reliability. (Note that XTC differs appreciably from 1.0.)

In the search for a more acceptable method for determining data reliability, the following factors were taken into consideration:

1. Since all four fuel-air calculation methods are based on sound chemical and mathematical principles, all errors should be essentially zero when the correct input

quantities are used. However, because of the different specific sensitivity values for the different methods (see Section 2.2) all four errors would change at different rates as one of the input quantities is changed from its correct value. Therefore, it appeared that the difference between two errors quantities would be a measure of how far the input variables were from their correct values. This was tested by selecting the errors of Methods 1.2 and 3.1 for evaluation.

Method 1.2 was selected because of its common usage and low sensitivity to variable changes and Method 3.1 was selected because it constituted the most complete specification of the system. The error difference [E(3.1) - E(1.2)] is identified by ΔE in this report.

2. The sum of mole fractions (XTC) was also selected as a possible indicator of data reliability because it seemed reasonable to assume that the value should be close to unity since all major stable species are included in the analysis. Because the mole fractions normally referred to in this report are based on the sum of gaseous wet products, the total sum XTC should have a maximum value of unity when only gaseous products are included, i.e. not including solid carbon. It is this value of XTC which is calculated by Method 1.2 and which is used in the following test of data reliability.

Data from various sources were next examined by plotting ΔE versus XTC as shown in figure 2.8. The result shows that the data is well correlated by a straight line.

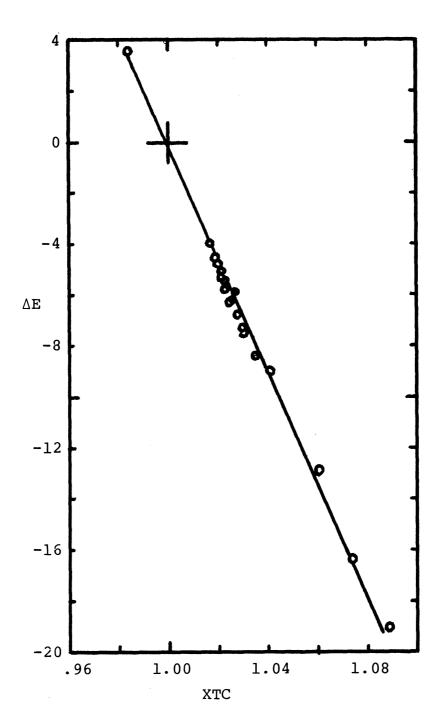


Figure 2.8. ΔE vs XTC: Lycoming Data. (Reference 12) Runs 153-159, 448-454, 467-473 (all modes included).

Additional plots were made to determine whether any correlations existed between fuel-air errors from the other methods and XTC. Figure 2.9 for Method 1.2 (expanded Spindt Method) shows no correlation while figure 2.10 for Method 3.1 shows a reasonable correlation, although not as good as that in figure 2.8 for ΔE vs XTC.

Our conclusion is that either XTC or ΔE is a better indicator of data validity than either the Spindt or Method 3.1 fuelair errors alone. Since XTC can be obtained from the application of only one method, Method 1.2, it is considered to be the more practical indicator of good data.

2.3.1 Comparison of Michigan and Eltinge Methods

A limited comparison of the Michigan method and the method reported by Eltinge(reference 7) was made. In the Eltinge method one enters one of several charts, see figure 2.11, with corrected (for UHC) values of percent CO2, O2 and CO. The lines representing these values form a triangle such that the centroid falls on a line representing the calculated fuel-air ratio and the height of the triangle gives an indication of "instrument error" in terms of percent CO. In this report EIE shall be used when referring to the Eltinge instrument error. In figure 2.11 the fuel-air ratio for the example is 0.0669 and the EIE is +0.45, which are in good agreement with Eltinge's results (reference 7).

The initial part of the comparison consisted of analyzing some of Eltinge's engine data using the Michigan method and comparing the Eltinge and Michigan results. These results are tabulated in table 2.5 while figure 2.12 shows both ΔE and XTC plotted against EIE.

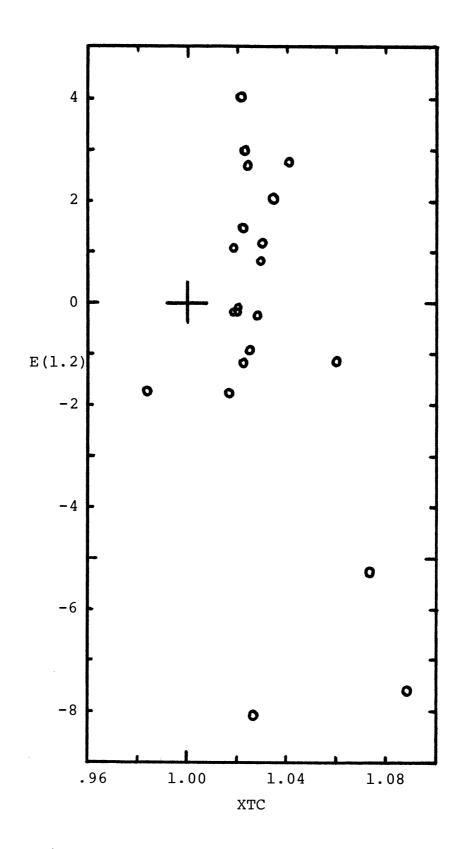


Figure 2.9. E(1.2) vs XTC: Lycoming Data

(Reference 12) Runs 153-159, 448-454, 467-473 (all modes included).

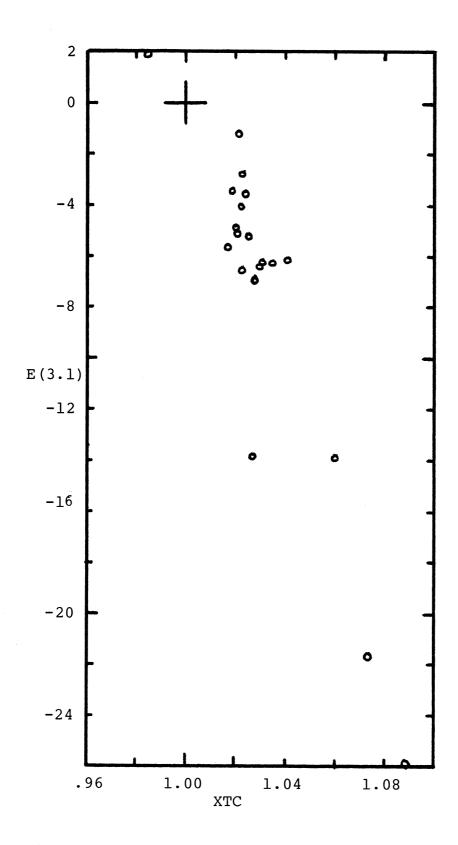


Figure 2.10. E(3.1) vs XTC: Lycoming Data

(Reference 12) Runs 153-159, 448-454, 467-473 (all modes included)

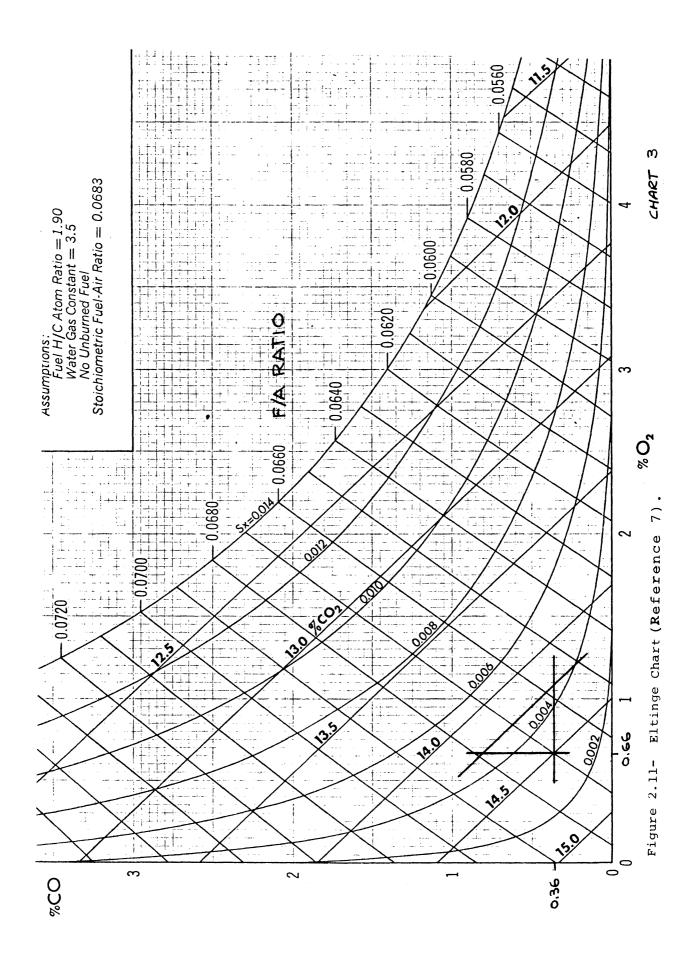


TABLE 2.5. COMPARISON OF MICHIGAN AND ELTINGE ANALYSES

Eltinge	È	ltinge	Michigan			
Run*	EIE	Spindt Error	E(1.2)	<u>Δ</u> E	XTC	
1	+0.4	1.671	1.667	4.394	.983	
2	+0.4	0.600	0.567	5.384	.982	
3	+0.3	1.356	1.214	5.030	.985	
4	-0.2	0.887	0.858	-0.494	1.002	
5	+0.6	1.751	1.639	8.437	.977	
6	+0.1	0.156	0.009	1.640	.995	
7	+0.1	1.727	1.625	2.395	.994	
8	+0.4	-1.560	-1.672	5.777	.982	
9	+0.3	1.605	1.510	3.561	.989	
10	+0.5	2.087	2.128	7.243	.977	
11	+0.3	2.100	1.906	4.653	.986	
12	-0.1	1.902	1.973	0.517	.998	
13	-0.1	1.170	1.169	-0.400	1.001	

The data spread in figure 2.12 is due in part to the fact that Eltinge reports EIE only to the first decimal place.

Table 2.5 shows good agreement between Eltinge's Spindt error and the error E(1.2). Furthermore, an examination of figure 2.12 shows that both ΔE and XTC correlate well with EIE, so that any one of the three parameters EIE, ΔE or XTC could be used as an indicator of "instrument error."

Having related ΔE and XTC to EIE, the second part of the comparison was made in order to answer the following question. If we were to select an ideal run according to the Eltinge criteria, i.e. one having zero instrument error, and use the corresponding exhaust concentrations in the four Michigan methods, would there be differences in the calculated fuel-air ratio and what would be the magnitudes of the errors? Five points were selected from chart 5 of reference 7. These points were along the line of constant F/A equal to 0.066 and at CO2 concentrations of 14.0, 13.5, 13.0, 12.5 and 12.0 percent. Corresponding

^{*}See table 1 in reference 7.

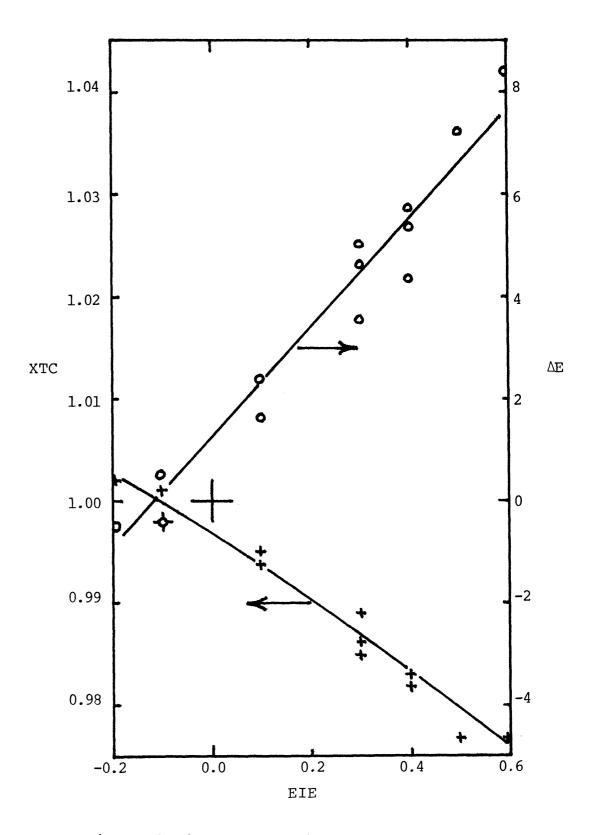


Figure 2.12. XTC and ΔE vs EIE: Eltinge Data (Reference 7)

values of percent CO and O2 were selected from the chart and these values were used in computing fuel-air ratio using the four Michigan methods. The results, together with ΔE and XTC are shown in Table 2.6.

TABLE 2.6. CALCULATED FUEL/AIR ERRORS FOR ELTINGE ZERO-EIE DATA POINTS*

	F/A Percent Error						
Method	Point 1	Point 2	Point 3	Point 4	Point 5		
1.2	0.143	-0.061	-0.234	-0.316	-0.426		
2.1	-0.392	-0.534	-0.638	-0.670	-0.626		
3.1	0.410	0.343	0.116	-0.006	-0.249		
3.2	-0.119	-0.237	-0.384	-0.447	-0.500		
$\Delta {f E}$	0.367	0.404	0.350	0.310	0.177		
XTC	0.9985	0.9984	0.9986	0.9988	0.9993		

^{*}See chart 5 in reference 7.

The fact that all fuel-air errors are below one percent indicates excellent agreement between the Eltinge and Michigan methods over the region checked. On the basis of the above analysis, we come to the following conclusions:

- There is excellent agreement between the Eltinge and Michigan methods for calculating fuel-air ratio and determining data validity.
- When valid emission data is obtained, all four of the Michigan methods will give essentially the same calculated fuel-air ratio.
- 3. An indication of data validity is given by either XTC, ΔE or EIE. Ideal runs will result in the following values:

XTC ~ 1.00

 $\Delta E \sim 0.0$

EIE ~ 0.0

4. The Spindt error, in itself, is not a good indicator of data validity since some runs showing small Spindt errors can have excessively large fuel-air errors when calculated by the other Michigan methods. Under these conditions, values of XTC will be appreciably different from 1.0 (see section 2.3) and values of both ΔE and EIE will differ appreciably from 0.0.

2.4 CALCULATION OF EXHAUST MOLECULAR WEIGHT

One of the benefits of the Michigan computational procedure is the ability to compute exhaust molecular weight. This is made possible because the procedure determines the mole-fraction values of the ten major stable gaseous species in the exhaust. With these values, exhaust gas molecular weight is computed using the sum of products of mole fractions and molecular weights, $\text{MWEXH} = \sum_{i} X(i) * \text{MW}(i)$ (2.64)

Figure 2.13 shows calculated exhaust molecular weights, based on emission data from several sources, versus equivalence ratio. Also included is a curve based on equilibrium calculations by Teledyne-Continental Motors (reference 8) and a slightly modified curve used by AVCO-Lycoming (reference 9). It is evident that all values tend to agree within ± 1% at the high equivalence ratios. However, there is appreciable differences at the low equivalence ratios. Molecular weights calculated by the Michigan method using Eltinge's data, from automotive engine measurements, show excellent agreement with the curve based on the TCM equilibrium calculations. Results from lean-mixture runs at Michigan show much lower values. Lean runs from other sources were not examined.

The reason for the differences for lean mixtures becomes apparent when one examines the data in table 2.7. Eltinge's data, which was obtained for a 389 in. V-8 engine, shows high values of CO2 concentration (11.25%) and low values of UHC and O2. This indicates relatively complete combustion. However, the Michigan data for the LIO-320 shows relatively low CO2 and high CO, UHC and O2. This results from poor combustion because of poor mixing during the idle operation. Therefore, this difference will affect the relative amounts of light and heavy molecular components in the exhaust, as also shown in table 2.7. The Michigan data shows a much lower mole-fraction of the heavy molecular specie CO2 and higher mole-fractions of the lighter species H2 and UHC. This will naturally result in a lower exhaust molecular weight.

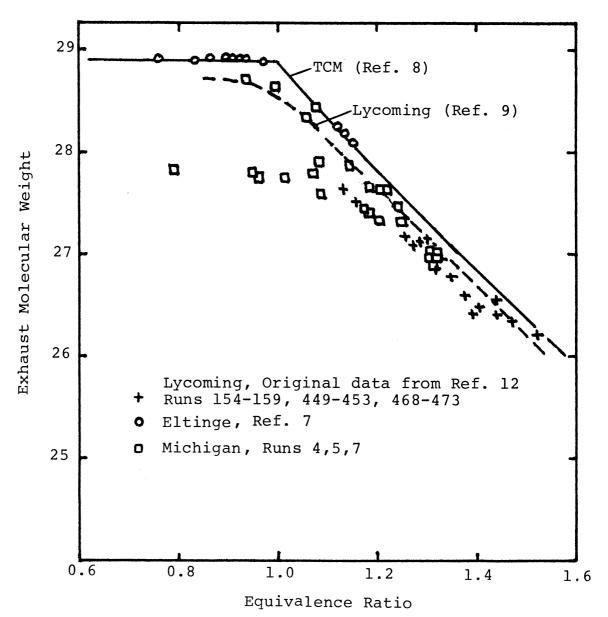


Figure 2.13. Calculated Exhaust Molecular Weight vs Equivalence Ratio

TABLE 2.7. CALCULATED EXHAUST PROPERTIES-LEAN MIXTURES

A. Eltinge Data

RUN: 7. ()	C02	co	02	HCC	NO	NOX
DRY MEASU	JREMENTS	112500.	1000.	53000.	Ο.	O .	Ο.
DRIED MEA	ASUREMENTS	Ο.	Ο.	Ο.	Ο.	Ο.	Ο.
WET MEASI	JREMENTS	Ο.	O .	Ο.	1788.	Ο.	Ο.
HTCR	EHCC	EHCR	CO2A	PSAT	PTRP	W	N202
1. 900	1, 000	1, 850	0. 030	0. 08866	19, 000	0. 0000	3. 7274

MTD XTC K KWDD KWD PHIM MWEXH PHICAL FACAL FAM ERROR 1.2 0.9964 3.5000 0.9073 0.9031 0.7629 28.9371 0.7745 0.05289 0.05210 1.515 XC02 XC0 XHC X02 XH20 XH2 XN2 XN0 XN02 XAR XC 0.1016 0.0009 0.0018 0.0479 0.0969 0.0002 0.7383 0.0000 0.0000 0.0087 0.0000

B. Michigan Data

RUN: 5. 1		002	CO	02	HCC	NO	NOX
DRY MEASL	JREMENTS	Ο.	17656.	Ο.	Ο.	Ο.	Ο.
DRIED MEA	ASUREMENTS	51214.	Ο.	109523.	O.	Ο.	Ο.
WET MEASUREMENTS		0.	O.	Ο.	31808.	173.	223.
HTCR	EHCC	EHCR	COZA	PSAT	PTRP	W	N202
2. 190	1 000	1. 850	0. 030	0. 08866	19, 000	0 0081	3 7274

MTD XTC K KWDD KWD PHIM MWEXH PHICAL FACAL FAM ERROR 1, 2 1 0013 3,5000 0,9254 0,9211 0,7901 27,8375 0,7742 0,05145 0,05251 -2,011 XC02 XC0 XHC X02 XH20 XH2 XN2 XN0 XN02 XAR XC 0,0474 0,0163 0,0318 0,1014 0,0788 0,0077 0,7091 0,0002 0,0001 0,0084 0,0000

This leads to the conclusion that reasonably large differences in exhaust molecular weights can occur at low equivalence ratios, depending on the completeness of combustion. It appears that any value is possible in the range from about 27.75 to 28.95. Therefore, values based on equilibrium calculations are valid only when combustion is reasonably complete while a method such as the Michigan method, which is applicable under all conditions, should give better values of molecular weights over a broad range of combustion conditions.

These results therefore indicate that exhaust molecular weight can be used as an indicator of completeness of combustion. For any equivalence ratio, the exhaust molecular weight tends to approach the value given by the equilibrium calculation as the completeness of combustion improves. This is also brought out in our analysis of the data in chart 5, reference 7, where a direct correlation was found between Eltinge's mixture distribution parameter $\mathbf{S}_{\mathbf{x}}$ and the calculated exhaust molecular weight. The results, for a fixed fuel-air ratio of 0.0660, show that as the mixture distribution improves (lower $\mathbf{S}_{\mathbf{x}}$), the molecular weight increases.

Sx	MWEXH		
0.0116	28.356		
0.0092	28.430		
0.0067	28.503		
0.0044	28.573		
0.0022	28.643		

2.5 CALCULATION OF WATER CORRECTION FACTORS FOR EXHAUST CONCENTRATION MEASUREMENTS

The computational procedures as set up in Section 2.1.5 of this report eliminate the need for water correction factors since the methods permit the use of either wet, dry or dried measurements. However, when desired for comparison purposes, water correction factors can be easily obtained from the computed values of XGD and XGDD since

$$KWD = XGD = 1 - XH2O$$
 (2.65)

and
$$KWDD = XGDD = XGD + XH2ODD$$
 (2.66)

The dry-to-wet correction factor is given by KWD and the dried-to-wet by KWDD. Some values are shown in table 2.7. Values for KWD are also shown in the various computer print-outs throughout this report.

3. UNIVERSITY OF MICHIGAN TEST FACILITY

The engine emissions test facility is located in a two room concrete structure within the Gas Dynamics Laboratories of the Department of Aerospace Engineering. The engine, dynamometer, and related instrumentation are located in a 22 ft x 13 ft test cell (figure 3.1) while the test operator, data acquisition system, and emission instrumentation are located in an adjacent 22 ft x 10 ft air conditioned control room (figure 3.2). Support equipment for the facility includes a 3000 psi high pressure air supply, water, electrical power (440, 220, and 110 volt circuits), and a Data General Nova computer.

Engines requiring dynafocal or bed mounts can be easily installed in the test stand. The present engine (Lycoming LIO-320-BlA), which required dynafocal mounting, was installed using a production aircraft engine mount with machined aluminum bushings in place of the standard rubber Lord bushings.

An eddy current — dry gap dynamometer with a 350 HP and 5000 RPM continuous operation capability is used as a solid state blending type system which allows the dynamometer to be operated in speed control, load control or a blend of these two modes. In the speed control mode the controller holds a desired RPM by varying the load in conjunction with engine power changes. In the load control mode the operator selects a given constant load level to apply to the engine regardless of speed. The blending option allows the selection of any combination of load and speed control.

The air flow distribution system, which includes the cooling air and engine induction air, is shown schematically in figures 3.3 - 3.5. The cooling air is supplied by a ceiling mounted centrifugal blower which has a capacity approaching 10,000 CFM at 10 in. $\rm H_2O$. A damper system on the blower allows control of the blower pressure output over the range of 0 - 10 in. $\rm H_2O$. The cooling air temperature can be controlled over a limited range by using two air intakes for the blower system, one intake drawing outside

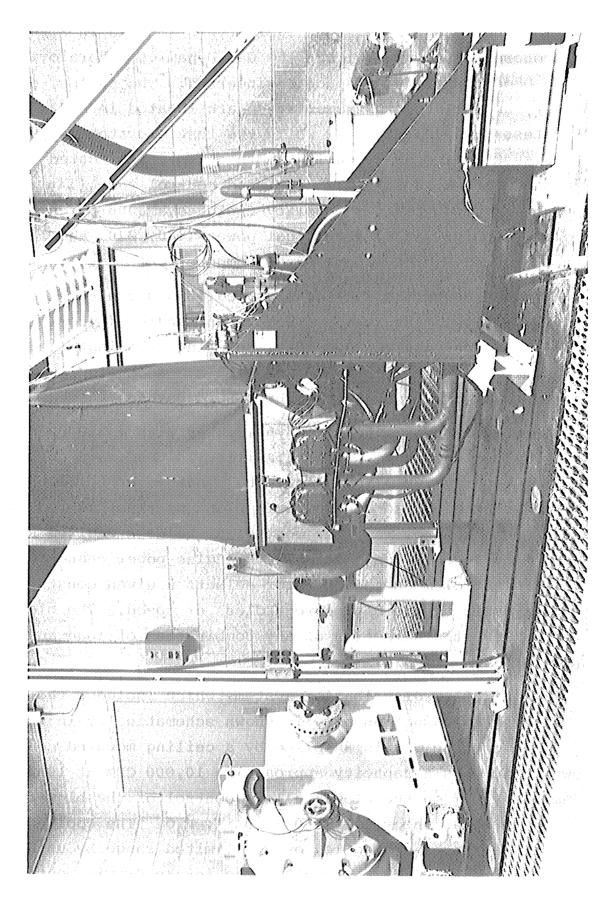


Figure 3.2 Engine Control Room

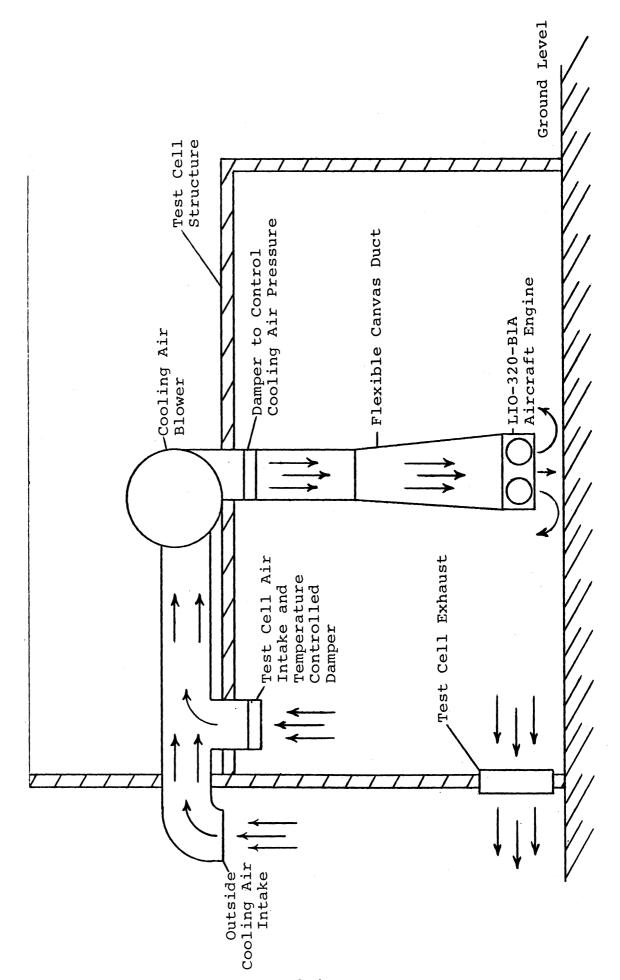


Figure 3.3. Cooling Air Flow Schematic

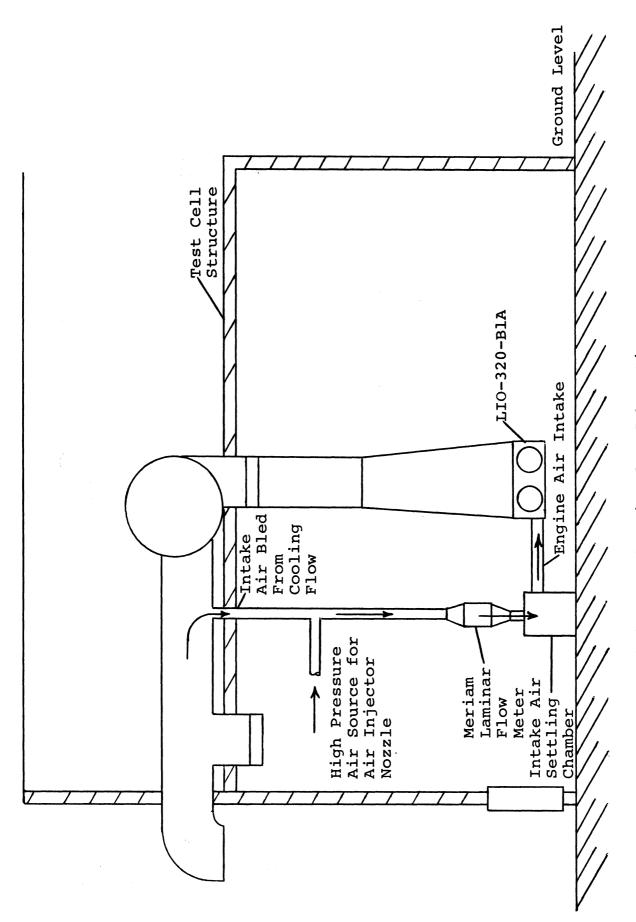
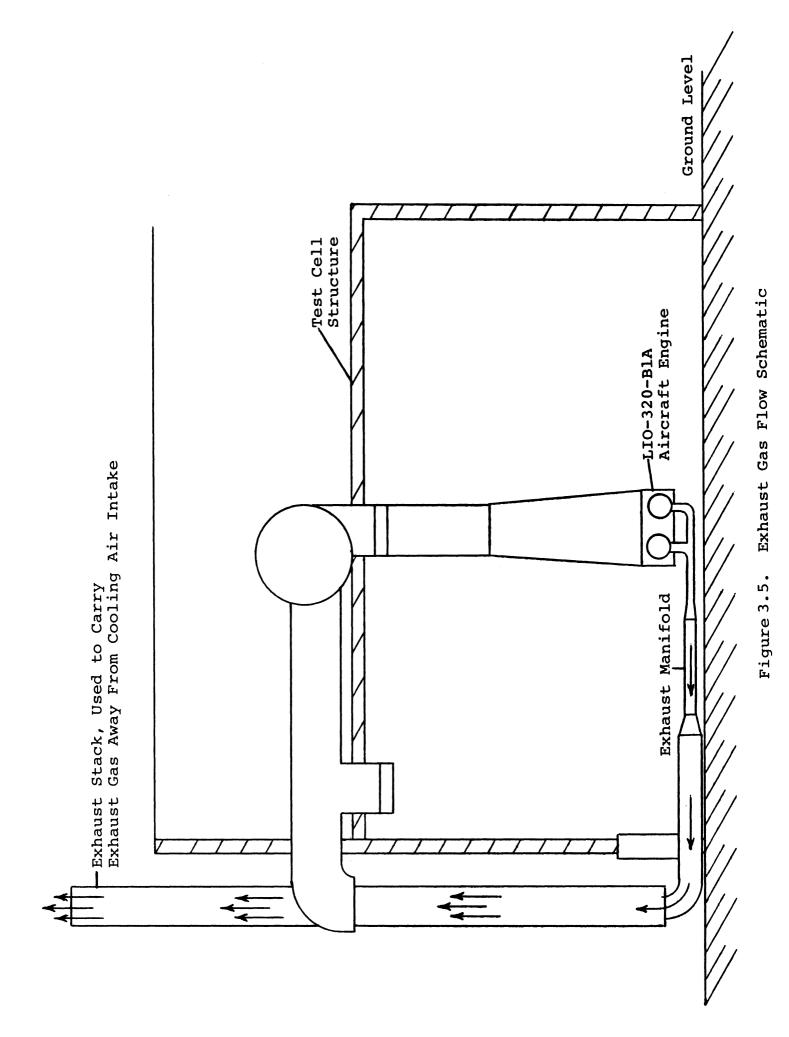


Figure 3.4. Intake Air Flow Schematic



3-6

air and the other drawing air from inside the test cell. By varying the mixture of the test cell air and the outside air, it is possible to obtain a cooling air temperature in the range between the test cell temperature and the outside air temperature. To minimize any temperature differences between the induction air and cooling air, the induction air is obtained by bleeding air from the cooling air system.

Induction air flow rates are measured using a 2 in. Meriam laminar flow meter. Air flow rates are obtained by measuring the pressure drop across the meter and utilizing the previously obtained meter calibration curve. Calibration tests were periodically performed to check accuracy. A 2 in. flow meter was chosen to insure accuracy of the low air flow rates encountered in the idle and taxi modes. Due to the small size of this device, large pressure drops result from the high air flow rates encountered during the takeoff, climbout, and approach modes. pressure drops across the meter cause a low engine intake air pressure. In order to correct for this low pressure, a supersonic air injector was installed upstream of this device. By varying the flow through this injector, it is possible to set the induction air total pressure at the engine intake to the desired pressure level for all test conditions. This pressure is usually set to ambient pressure.

Fuel flow rates are measured using an electronic timer and a weight and balance system. As a check on this method, flow rotameters have been installed and are monitored during testing.

The following pressure and temperature measurements are also recorded during engine operations.

Pressure

Temperature

- Intake Air △P 1. 1. Cylinder Head Intake Air, Total 2. 2. Exhaust Gas Intake Air, Static 3. 3. Cooling Air 4. Engine Manifold Intake Air, Dry Bulb 4.
- 5. Fuel 5. Intake Air, Dew Point
- 6. Cooling Air, Total 6. Fuel Intake
- 7. Engine Oil 7. Oil
- 8. Induction Air 8. Dynamometer Cooling Water Injector, Upstream 9. Ambient (Barometer)
- 9. Barometric

A high speed data acquisition system is being integrated into the facility. This system consists of a high speed analog processor, an analog to digital converter, a small mini-computer, and a high speed paper tape punch. This system has the capability of obtaining two to three high speed (up to 20,000 samples/sec) data scans for a given steady state operating level and storing these points in memory. While in memory, the capability is available to perform some data scaling or reduction. This data can then be transferred to the paper tape punch for further data reduction using either the laboratories' "in-house" computer system or by using the University's time sharing computer system.

The emissions measuring system used in this facility is a modified Scott model 108-H and is described in Section 4 of this report. This system was designed to meet the specifications pertaining to sampling procedures, particularly with regard to response times, as given in the Federal Register (reference 6). A more detailed description and discussion of this equipment is given in section 4 of this report.

To provide the capability of rapidly changing from one probe position to another from which the exhaust sample is to be taken, an electrically heated system of stainless steel valves was assembled. This valving system allows convenient selection during a test of any one of four gas sample probes, located at different positions in the exhaust system. The valve system is controlled from the control room of the test facility, thereby allowing maximum safety and flexibility during the sampling procedure.

A variable position sampling probe, which allows an exhaust gas sample to be taken at any position within the engine exhaust tailpipe, is also available.

4. INSTRUMENTATION FOR EMISSION MEASUREMENTS

The objectives of this program are met only when reliable emission measurements are made. Therefore, a considerable portion of our effort was directed at the problems associated with the instrumentation, which included problems of design, construction and usage. Examples of problem areas are:

- 1. Reliable NOX-converter performance.
- 2. Water condensation at various points in the system.
- 3. Response times associated with sample flow rates and possible reactions in the sampling line.
- 4. Manufacturing quality control.
- 5. Reliability and frequency of repair.

Our conclusion is that some efforts should be made to improve the overall reliability of the instrumentation package and to standardize the instrument package and operating procedures.

4.1 EMISSION MEASUREMENT CONSOLE

A Scott Laboratories Emission Measurement Console, a modified Model No. 108-H, was used in this test program. The unit is pictured in figure 3.2 and houses the following five major analytical components.

- 1. Beckman Model 864 Infrared Analyzer for CO2.
- 2. Beckman Model 865 Infrared Analyzer for CO.
- 3. Beckman Model 741 Oxygen Analyzer.
- 4. Scott Model 125 Chemiluminescence Analyzer for NO/NOX.
- 5. Scott Model 415 Hydrocarbon Analyzer.

The sample gas, after entering the console, is split three ways. One portion passes directly to the total hydrocarbon analyzer resulting in a wet hydrocarbon measurement. The second portion passes to the NOX analyzer, where it can go directly to the analzer or can first pass through the NOX converter. This provides wet measurements of either NO or

NOX. The third portion passes through the water trap where most of the water vapor is condensed, resulting in a dried sample, and then the sample is further split. One portion passes in series through the CO2 and O2 analyzers to give dried measurements, the other portion passes through a drier and then to the CO analyzer, resulting in a dry measurement. The sample lines are either heated or insulated to minimize condensation, the temperatures being in the range from 300 to 390°F.

4.2. INSTRUMENTATION PROBLEMS

A large number of problems were encountered with the emissions measurement console, some of which were the result of poor quality control during assembly while others were because of inadequate design. Following is a list of major problems encountered and their solutions if found:

- 1. Fittings must be checked periodically for tightness to eliminate leakage. Fittings covered with insulation are difficult to check.
- 2. The reed valve in the external pump requires frequent checks for failure. Heat at the pump distorts the teflon seal such that the reed valve is stuck open and the pump's efficiency is drastically reduced. Also, air leakage may occur past the teflon seal diluting the sample.
- after several months of operation the two internal pumps began an on-off cycle during operation due to overheating. This produced drastic changes in flows throughout the system requiring the operators to continually correct flows. This problem can be avoided by eliminating the internal pumps from the system and increasing the external pump capacity. This solution is desirable since it will decrease the possible problems of emission sample dilution due to air leakage since the system will be under positive pressure.

- 4. Valves were insufficient to hold pressure resulting in leakage when spanning and zeroing.
- 5. Excessive dirt accumulation led to valve failures. See item 9.
- 6. Water condensation in the flow lines occurred during initial emissions sampling. System corrections were required.
- 7. The emissions measurement system contained two pumps internal to the console and an external boost pump was added to increase the sample flow rates and thus meet the response times required by the Federal Register. The resulting increased flow through the system exceeded the capacity of the condensation coils in the trap causing condensation at various points in the measurement system. The condensation problem was partially alleviated by using two traps in series.
- 8. Bypass vents are required because the analyzer flow requirements are much smaller than the sample flow This was especially true on our system since its sample flow rate was increased to reduce system response time. These bypass systems were not heated nor sized to the higher flow rates. they served as condensation points in the system. Since all bypasses but one have a flow meter, condensed droplets passing through the meter would strike the floats and induce an oscillation in the measurement systems. When this would occur data taking had to be stopped and the system purged with dry nitrogen. After the system was dried out, data could again be taken. This condensation particularly affected the NO/NOX line. The problem has been effectively overcome by adding insulation to some lines and heating additional lines. The NO/NOX line temperature was increased to 390°F and the external sample line temperature was increased to 370°F.

9. The probe-purge system as originally designed bypassed the external filter. Valving did not allow
for sufficient purge pressure to avoid drawing
exhaust gases into the measurement console bypassing
the filter. This resulted in dirt accumulation
in some valves, during purging, leading to leakage.
This system was redesigned using a 1500 psi valve and
directing all flow through the filter.

4.2.1. CO INFRARED ANALYZER

We have found two main causes for failure of the CO measurement system. First, dirt accumulation in the check valves between the CO flow line and the CO2 flow line resulted in a leak between the two lines causing the CO analyzer to be very sensitive to the sample flow rate. This problem was corrected by cleaning the check valves. This problem could occur in field tests if the operating personnel are unaware of the problem.

The second problem was leakage between the high concentration sample cell and the low concentration sample cell resulting in a continuously increasing CO reading as sample gas (or span gas) leaks from the HI cell to the LO cell. The analyzer cannot be properly zeroed unless both cells are then purged with N2. This problem, due to a poorly cemented window between the two cells, occurred twice within nine months. A temporary fix consisting of a slow purge of the low concentration cell with N2 permits satisfactory operation.

CO2 interference with the CO analyzer was tested by passing a 13.11% CO2 span gas through the CO analyzer after initial calibration. A zero reading was obtained indicating no interference at this concentration level. Thereafter, the use of Ascarite for removal of CO2 as an interference gas was discontinued.

4.2.2. CO2 INFRARED ANALYZER

No problems have been encountered with the CO2 analyzer

in our testing.

CO interference with the CO2 analyzer was tested by passing a span gas of 10.70% CO through the CO2 analyzer after initial calibration. This resulted in a reading of approximately 0.2 of a chart unit. This indicates that during emissions measurement CO interference would be within the noise level of the recorder trace. This error can be neglected since the span gas for calibration is accurate to within only ± 5.0%.

4.2.3. O2 ANALYZER

In terms of the instrumentation sensitivity, the O2 detector does not have the sensitivity required to make good measurements in the fuel rich environment of an aircraft engine. The O2 detector has the slowest response time of all the components, on the order of 2.5 seconds, somewhat higher than the 2 second response time required by the Federal Register.

4.2.4. TOTAL HYDROCARBON FLAME IONIZATION DETECTOR (FID)

The FID is very sensitive to sample pressure. A change in sample pressure of 2 or 3 inches of water out of 40 inches of water can result in a 10% to 15% change in the total hydrocarbon (HCC) reading when sampling or spanning. Careful regulation of this pressure is required.

Condensation was a problem encountered with the FID when sampling at engine high power modes. To alleviate this problem a bleed valve was installed immediately ahead of the FID to allow only necessary flow through the FID. Also a surge tank (6 ounce volume) was installed between the bleed valve and the FID to collect the small amount of condensed water. The valve and upper section of the surge tank were insulated.

At idle and taxi modes, chart readings consisted of a wide band of "hash" occupying up to 70% of the chart scale. The surge tank afforded better mixing of the low and high

THC concentration pulses allowing easier and more accurate determination of the average of the chart reading.

O2 interference with the HCC measurement was tested. The FID was calibrated on range 1K and a 99.6% O2 span gas was passed through the FID resulting in a HCC reading of approximately 75 ppm carbon. At a concentration of 5% O2 (roughly equivalent to the O2 level at idle and taxi) interference would result in an increase of the HCC measurement of only about 3 ppm carbon. This compares with measurements on the order of 25000 ppm carbon at idle. At higher power levels the O2 concentration falls to about 0.15%, so the effect is negligible.

4.2.5. NO/NOX CHEMILUMINESCENCE ANALYZER

The central problem encountered with the NO analyzer was condensation and the resultant oscillations as mentioned previously. Heating and insulating additional segments of the sample lines, increasing the line temperature to 390°F and increasing the external sample line temperature to 370°F has largely eliminated the condensation problem.

The flow lines in the interior of the NO analyzer were also insulated and heated, helping to decrease the effect of changes of viscosity between sampling hot exhaust gases and spanning with gas at room temperature. Pre-heating of the span gas should also improve performance, decreasing span drift, but as yet has not been tried.

Efforts at EPA, Ann Arbor, Michigan, have shown that for accurate measurement of NO/NOX in exhaust gases the sample flow supplied by the external pump should be, at a minimum, 60 scfh. Otherwise, reactions will significantly reduce the concentrations of NO/NOX. Also, EPA testing has shown that no effects on NO/NOX measurements result by passing the sample through a condenser which would alleviate the condensation problem. This needs to be looked into further at varying levels of NO/NOX.

Measurement of NOX has been generally unsuccessful. Only at high power modes is a NOX reading usually obtainable. At idle and taxi the NOX reading is usually lower than the separate NO reading indicating other reactions are taking place other than conversion of NOX to NO. Some tests reported in

the literature indicate that NOX reacts with CO to eliminate NO2 in a sample. We have run tests mixing known amounts of CO with an NO/NO2 span gas to determine the extent of this effect. CO dilution of the NO/NO2 gas was increased for a series of experiments. The results show that very high concentrations of CO are required in order for an appreciable effect to occur. However, these experiments were conducted with cold gases and the possibility remains that hot sample gases would lead to a different conclusion. While this problem is worth further investigation, it is not critical to the problem at hand in that NOX levels are well below EPA standards and, further, our sensitivity analysis shows that NO has no significant effect on calculated fuel/air ratio.

4.3. COMMENTS

- 1. To obtain accurate measurements, constant control is required of the flow rates and engine temperatures. Constant monitoring is also required for the detection of partial failures which are not always obvious, e.g. small leaks in flow lines or analyzers.
- When an open engine exhaust pipe is used, probe location is important, especially during the idle and taxi modes. If the probe is not far enough upstream of the open end of the exhaust, engine pulsations will draw ambient air into the region of the probe and dilute the sample.
- 3. An automated data acquisition system is highly desirable since the time consumed in manual reduction of the data on the recorder charts is great. It is also desirable to have on-line capabilities to obtain quick feedback of the computed fuel/air ratio in order to have quick evaluation of the test run.
- 4. Experience has demonstrated that the emission instrument console should be checked at frequent intervals for leaks and other malfunctions.

- 5. There is a need for a standardized design for the emissions measurement console and for greatly improved quality control in its manufacture.
- 6. A standardized test procedure should be developed specifying the operational steps for both the instrument console and the engine.
- 7. If the emission measurement package is viewed in its entirety, a number of shortcomings were found which would reflect not only on the accuracy of the data taken but also on whether or not data taken by other systems is indeed comparable. This included those data taken from emission systems made by the same manufacturer.
 - It was found that the emission packages made by the same manufacturer varied as a function of when they were made. We found different types of NO and HC detectors used on supposedly identical systems. Different recorders were used. And, most importantly, if the sample lines flow rates vary between units, the time response and effect of condensation will be a strong variable.
- 8. It was found that when spanning the CO, FID, and NO/NOX analyzers, particularly after sampling hot exhaust gases, that the span reading would quickly respond towards the correct span reading until reaching about 90% of the span value, after which the reading gradually increases approaching the correct span reading. This could be cause for error in the chart readings. Heated span gas should be tested to determine the effect on readings.

5. UNIVERSITY OF MICHIGAN ENGINE EMISSION DATA

5.1 AVCO-LYCOMING LIO-320 BASELINE RUNS

Test results for two low error baseline runs (runs 4 and 7) and one high error baseline run (run 16) on the AVCO-Lycoming LIO-320 BlA engine are included in the form of bar charts, figures 5.1.A-5.3 C, and computer outputs, tables 5.2-5.4, at the end of this section. Test facilities for running the tests are shown in figures 3.1 and 3.2 in section 3 of this report.

The bar charts show the fraction of EPA standard contributed by each of the modes for each of the pollutants. At the extreme right are the total emissions relative to the EPA standard for the 7-mode cycle. The Federal Standards used are:

Hydrocarbons	0.00190	<pre>lb/rated power/cycle</pre>
Carbon Monoxide	0.042	<pre>lb/rated power/cycle</pre>
Oxides of Nitrogen	0.0015	lb/rated power/cycle

A separate chart is shown for **each** of the computational procedures, Methods 1.2, 2.1, and 3.1, and it is obvious that the three methods show good agreement for the low error runs but poor agreement for the high error run.

Table 5.1 shows the results of an error analysis of these runs. Shown are the fuel-air percent errors for Methods 3.1 and 1.2, the differences between these values (ΔE) and the sums of gaseous mole-fractions (XTC). An examination of E(1.2) values for the three baseline runs shows relatively small differences. Neglecting the idle runs, the values are in general below about 2.5%, implying that the Spindt error shows these runs to be of equal reliability. However, an examination of ΔE and XTC values shows that only runs 4 and 7 have acceptable values, but that run 16 does not. This is further evidence that the Spindt error in itself is not a good indicator of data reliability.

The bar chart results for runs 4 and 7 show that the levels of CO far exceed the Federal Standards, that HC is a borderline pollutant which may measure above or below the Standard and that ${\rm NO}_{_{_{\mathbf{X}}}}$ is far below the Standard.

TABLE 5.1. ERROR ANALYSIS OF RUNS 4, 7 AND 16

Run	E(3.1)	E(1.2)	ΔE	XTC
4.1	17.332	7.204	10.128	0.969
4.2	2.707	-2.099	4.806	0.980
4.3	1.918	0.678	1.240	0.995
4.4	-1.128	-1.198	0.070	0.999
4.5	-2.572	-2.202	-0.370	1.002
4.6	1.671	-1.443	3.114	0.987
4.7	21.718	11.484	10.234	0.970
7.1	-11.579	1.884	-13.463	1.039
7.2	-5.565	-2.180	-3.385	1.013
7.3	3.746	1.537	2.209	0.990
7.4	-0.059	-0.295	0.236	0.999
7.5	-0.711	-1.249	0.538	0.998
7.6	-6.991	-1.354	-5.637	1.023
7.7	-8.582	0.107	-8.689	1.028
16.1	60.171	-14.658	74.829	0.763
16.2	48.539	0.043	48.496	0.784
16.3	56.581	2.815	53.766	
16.4	56.095	0.570		0.752
16.5	51.188	-1.157	55.525	0.739
16.6	47.140		52.345	0.751
16.7		-5.785	52.925	0.770
TO • 1	52.759	-15.091	67.850	0.776

Attention is called to run 7.4 in the computer print-outs at the end of this section. Note that the four methods of computation give excellent agreement, not only for fuel-air ratio, but for all computed values as well. Because of such runs it is felt that all four methods of computation will give similar results if measurements of exhaust concentrations are accurate. However, it is possible that slight changes of the water gas equilibrium constant may be required for the different modes of operation to reflect possible differences in freeze-out temperatures of the exhaust products. This may be most important at idle and taxi modes. Because of the complex interaction of the many input variables, the problem of selecting the proper value of the equilibrium constant for the various operating modes cannot be solved without further study.

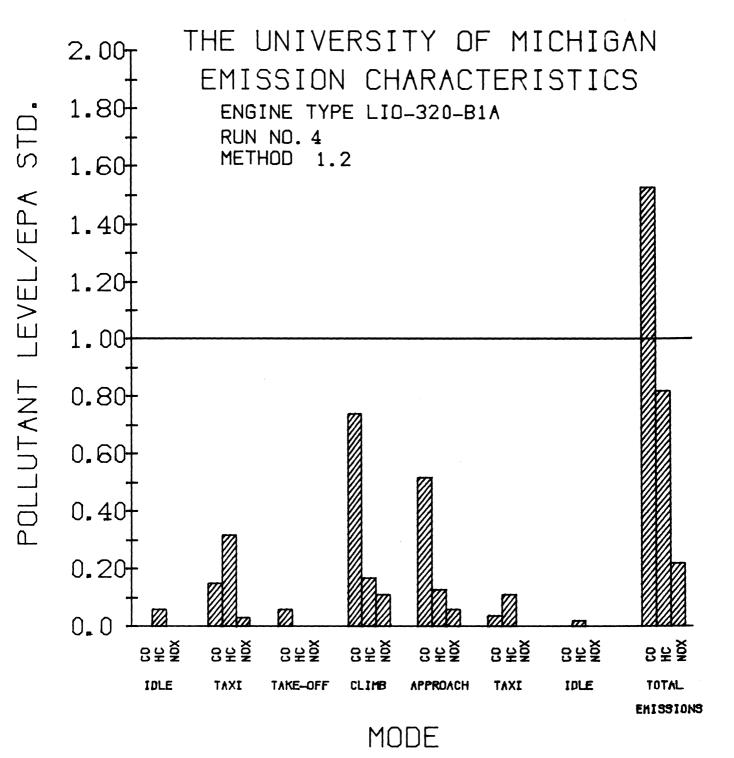


Figure 5.1.A. LIO-320 Baseline Results: Run 4, Method 1.2.

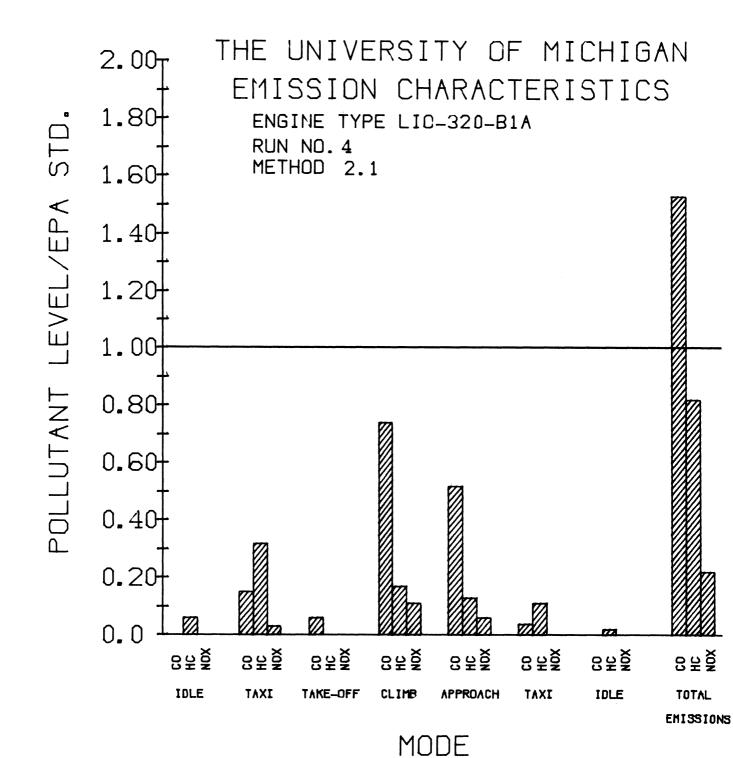


Figure 5.1.B. LIO-320 Baseline Results: Run 4, Method 2.1.

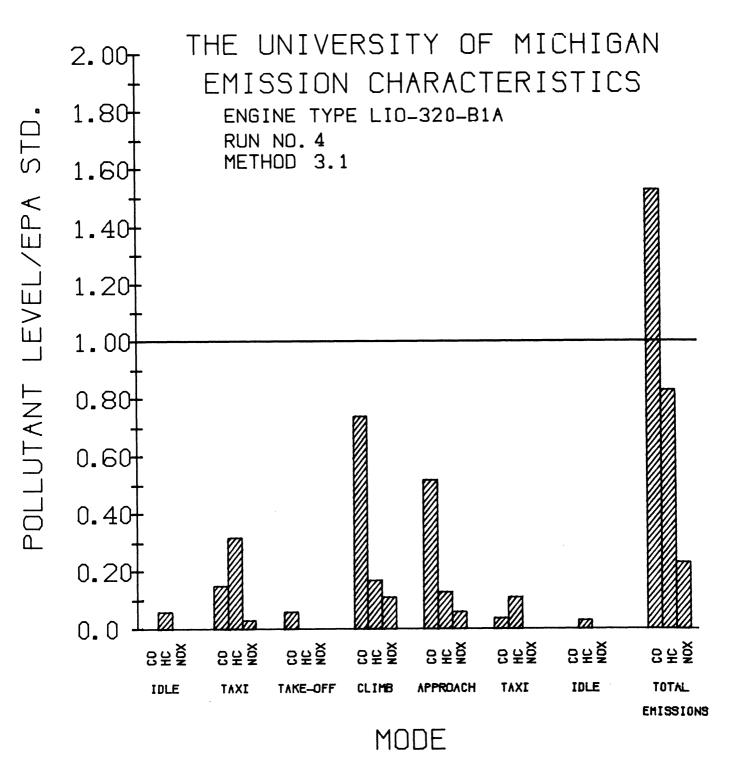


Figure 5.1.C. LIO-320 Baseline Results: Run 4, Method 3.1.

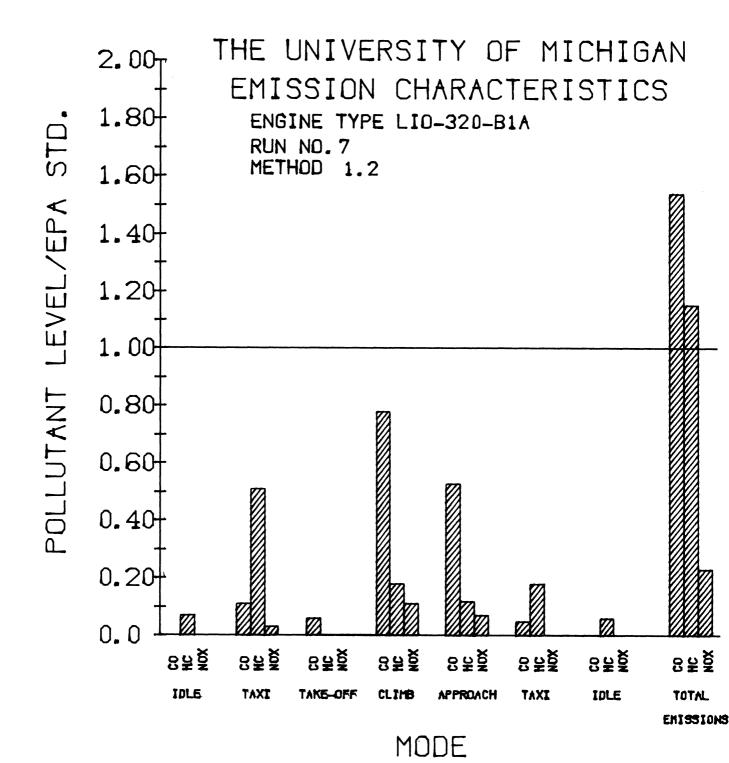


Figure 5.2.A. LIO-320 Baseline Results: Run 7, Method 1.2.

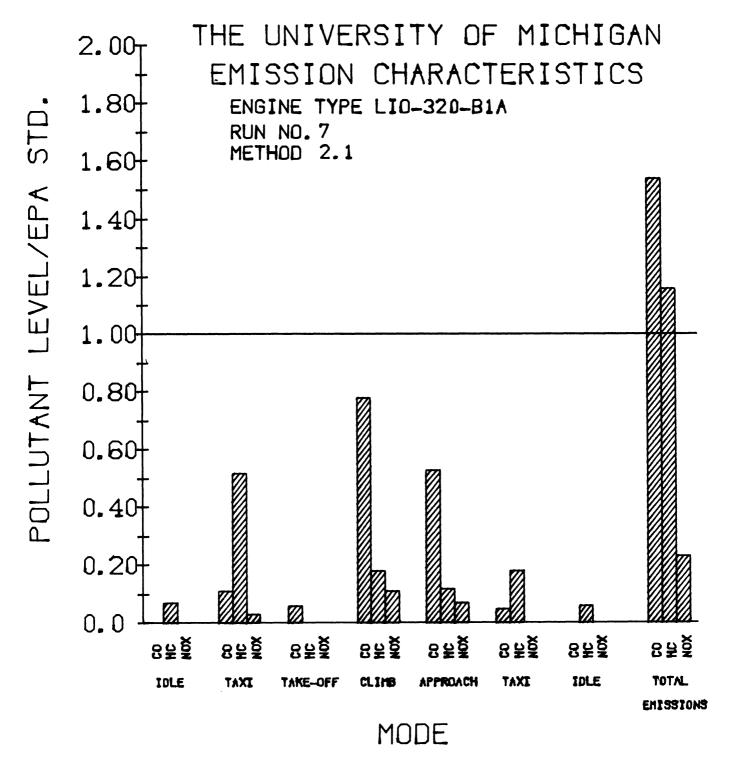


Figure 5.2.B. LIO-320 Baseline Results: Run 7, Method 2.1.

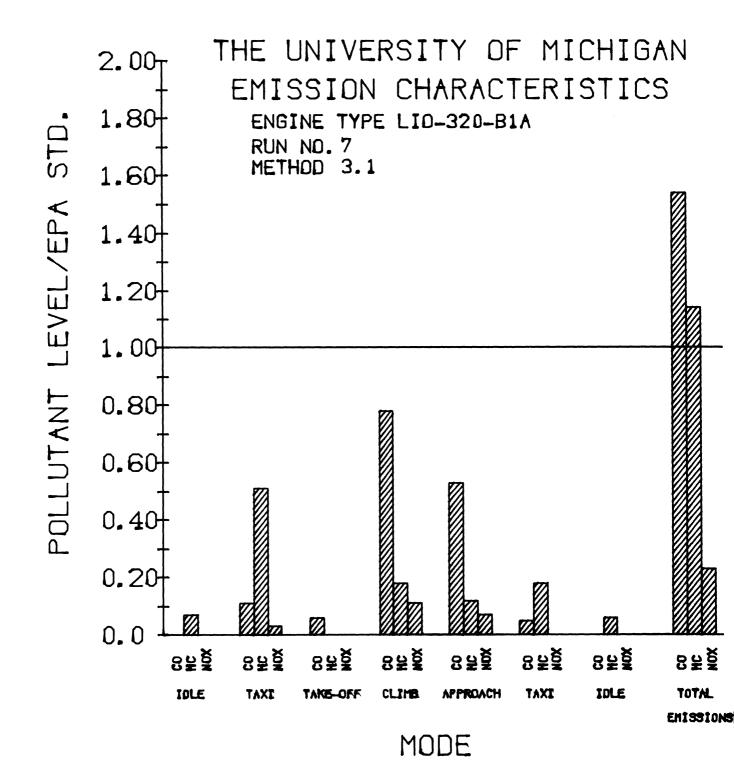


Figure 5.2.C. LIO-320 Baseline Results: Run 7, Method 3.1.

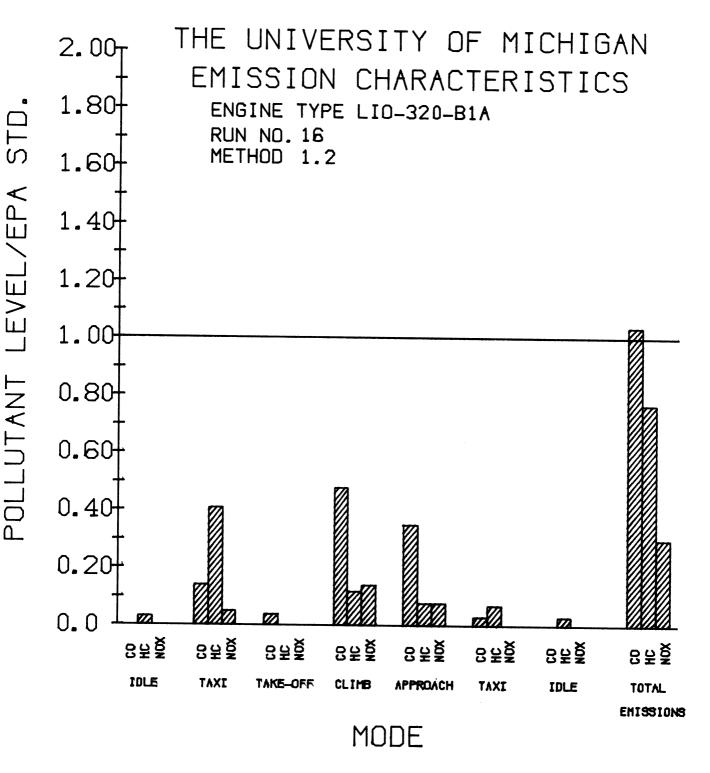


Figure 5.3.A. LIO-320 Baseline Results: Run 16, Method 1.2.

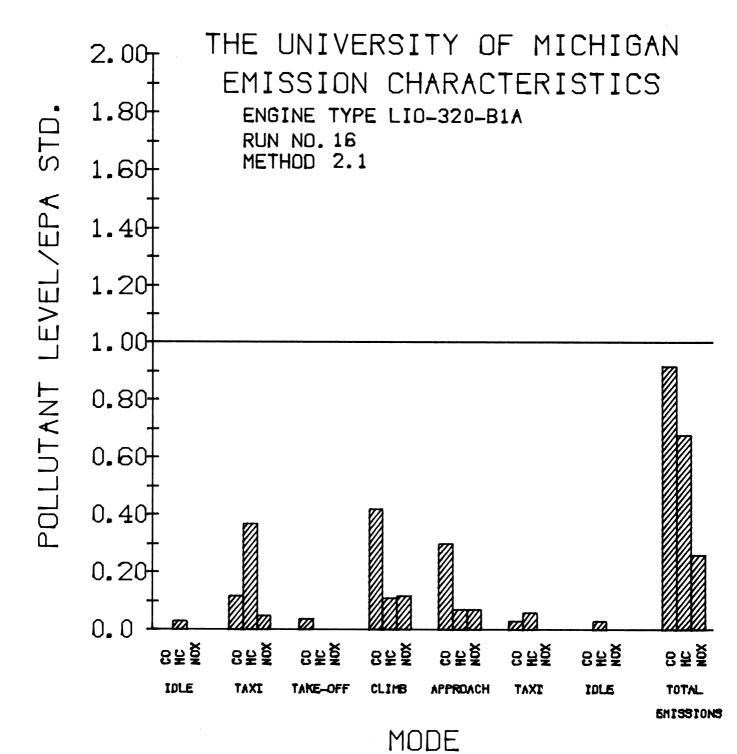


Figure 5.3.B LIO-320 Baseline Results: Run 16, Method 2.1.

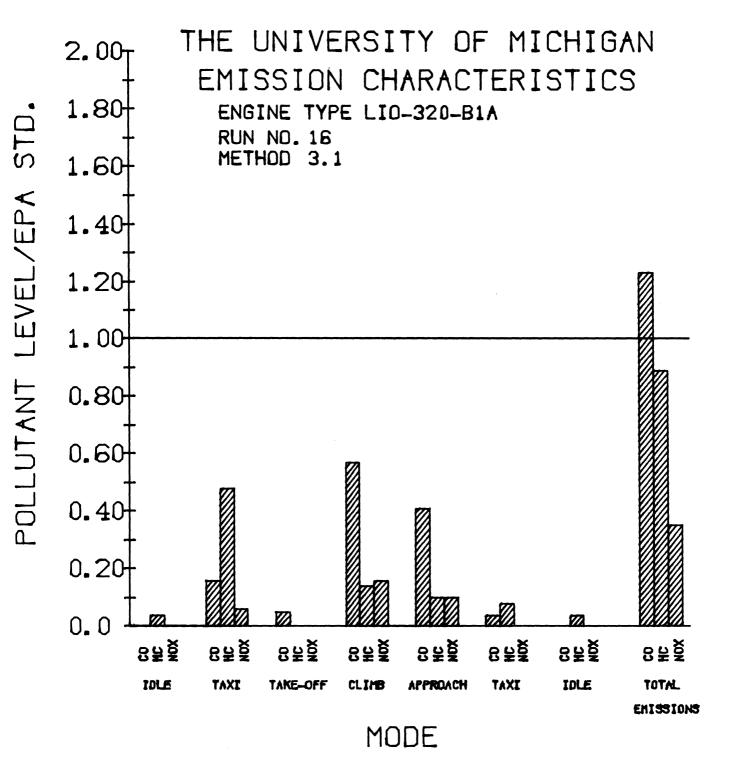


Figure 5.3.C. LIO-320 Baseline Results: Run 16, Method 3.1.

TABLE 5.2. COMPUTER PRINTOUT: RUN 4

DATE: 8-11-75 ENGINE TYPE: LIO-320-B1A FUEL H/C RATIO = 2.190 LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG OPERATORS: PACE, PERRY, PONSONBY, LEO RUN NO 1 COMMENTS: BASELINE DATA RUN4. 1 TEMP(DB) = 96.06F FUEL RATE= 4. 2595#/HR ENGINE RPM(NOM)= 700 RPM FUEL RATE = 4.2595#/HR ENGINE RPM(NON AIR RATE = 70.0810#/HR ENGINE RPM(ACT F/A RATIO= 0.0608#/# BHP(0BS) TEMP(DP) = 67,00F ENGINE RPM(ACT) = 744. RPM TEMP(BAR) = 85, 00F = 2. OHP = 0. OHP PHIM = 0.9144BAR PRESS(OB)= 29.11"HG BHP (CORR) MAN VAC(OBS) =17,00"HG BAR PRESS(CR)= 28.96"HG MAN PRESS(CORR)= 0.00"HG SPEC HUMIDITY=0.0146#/# NOX 002 02 UHCC CO NO 27388. 69080. 192. 27735. CONC (PPM) 68368. KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 1. 2 0.89356 0.96902 27.55150 1040.114 0.06515 0.06078 7 204 FAM ERROR MASS/MODE(LBM) 0.13535 0.09939 0.01704 0.03491 0.00026 0.00045 MASS/RATED HP(#/HP) 0.00084 0.00062 0.00011 0.00022 0.00000 0.00000 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0.86278 1.00000 28.07666 1020.660 0.06004 0.06078 -1 214 FAM ERROR METHOD 2.1 MASS/MODE(LBM) 0. 13282 0. 09753 MASS/RATED HP(#/HP) 0. 00083 0. 00061 0. 03425 0. 00025 0. 00044 0. **0167**ଞ 0. 00021 0. 00000 0.00010 0.00000 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 3.1 0.87942 1.01530 27.13356 1056.135 0.07131 0.06078 17.332 0.01731 MASS/MODE(LBM) 0.13743 0.10092 MASS/RATED HP(#/HP) 0.00085 0.00063 0.00046 0. 00000 0.00000 0.00063 0 00011 0. 00022 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 3. 2 0 89298 0 24116 27 50000 1042 062 0 06289 0 06078 3 473 FACAL MASS/MODE(LBM) 0.13560 0.09958 MASS/RATED HP(#/HP) 0.00084 0.00062 0.00011 0.00022 0.00000 0.00000 RUN NO COMMENTS: BASELINE DATA RUN4. 2 TEMP(DB) = 96. 27F FUEL RATE= 7. 9051#/HR ENGINE RPM(NOM)=1200 RPM = 66,00F AIR RATE = 101.5497#/HRENGINE RPM(ACT)=1201. RPM TEMP (DP) TEMP(BAR) = 85.00FBHP(OBS) = 6.2HP BHP(CORR) = 0.0HPF/A RATIO= 0.0778#/# BAR PRESS(OB)= 29 11"HG PHIM = 1.1712MAN VAC(OBS) =19.00"HG BAR PRESS(CR)= 28.96"HG MAN PRESS(CORR)= 0.00"HG SPEC HUMIDITY=0 0141#/# 002 02 UHCC CO NO NOX 214. 21854. CONC (PPM) 92875. 9600. 48817. 237 48817. 214. FACAL FAM ERROR KWD XTC MWEXH EXH FLOW METHOD 1 2 0.86498 0.98035 27.45172 1536.971 0.07621 0.07784 -2.099 MASS/MODE(LBM) 2.98862 0.51112 0.09711 0.99864 0.00470 0.00794 MASS/RATED HP(#/HP) 0.01868 0.00319 0.00061 0.00624 0.00003 0.00005 MWEXH FACAL KWD XTC EXH FLOW FAM ERROR METHOD 2. 1 0.84542 1.00000 27.80904 1517.223 0.07191 0.07784 -7.619 MASS/MODE(LBM) 2, 95022 0, 50455 0, 09586 0, 98581 0, 00464 0 00784 MASS/RATED HP(#/HP) 0.01844 0.00315 0.00060 0.00616 0.00003 0.00005 FACAL FAM ERROR 0.07995 0.07784 2.707 KWD XTC MWEXH EXH FLOW 0.85634 1.01002 27.17859 1552, 417 METHOD 3. 1 1.00868 0.00475 0.00802 MASS/MODE(LBM) 3.01865 0.51626 MASS/RATED HP(#/HP) 0.01887 0.00323 0. 09808

0.00323

KWD XTC MWEXH

0. 86466 0. 29629 27. 50000

MASS/MODE(LBM) 2. 98337 0. 51022 MASS/RATED HP(#/HP) 0 01865 0. 00319

METHOD 3. 2

0.00061

EXH FLOW

1534, 273

0. 09694

0.00061

0.00630

FACAL

0.00623

0.00003

0. 99689 0. 00469 0. 00793

0.00003 0.00005

FACAL FAM ERROR 0.07450 0.07784 -4.296

0.00005

TABLE 5.2. Continued

```
RUN NO. 4
MODE
              3
COMMENTS: BASELINE DATA RUN4. 3
TEMP(DB) = 89.27F FUEL RATE = 75.1880#/HR ENGINE RPM(NOM)=2700 RPM
TEMP(DP) = 61.00F AIR RATE = 859.1758#/HR ENGINE RPM(ACT)=2695. RPM
TEMP(BAR) = 86.00F F/A RATIO = 0.0875#/# BHP(OBS) = 138.4HP
BAR PRESS(OB) = 29.11"HG PHIM = 1.3166 BHP(CORR) = 153.4HP
                                                                                             MAN VAC(OBS) = 0.70"HG
BAR PRESS(CR)= 28.96"HG
                                                                                           MAN PRESS(CORR)=29.00"HG
SPEC HUMIDITY=0.0118#/#
CO2 O2 UHCC CO NO N

CONC(PPM) 87484. 1758. 1746. 85456. 201.

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

METHOD 1. 2 0. 85993 0. 99461 26. 87442 13402. 240 0. 08810 0. 08751 0. 678
                                                                                         CO NO NOX
                                                                                                                            205
MASS/MODE(LBM) 0.66949 0.00978 0.00420 0.41574 0.00105 0.00164 MASS/RATED HP(#/HP) 0.00418 0.00006 0.00003 0.00260 0.00000 0.00001 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 2.1 0.85449 1.00000 26.98341 13348.100 0.08661 0.08751 -1.031
MASS/MODE(LBM) 0.66678 0.00974 0.00418 0.41406 0.00104 0.00163 MASS/RATED HP(#/HP) 0.00417 0.00006 0.00003 0.00259 0.00000 0.00001
MASS/MODE(LBM) 0.65426 0.00955 0.00410 0.40629 0.00102 0.00160 MASS/RATED HP(#/HP) 0.00409 0.00006 0.00003 0.00254 0.00000 0.00001
RUN NO
             4
COMMENTS: BASELINE DATA RUN4. 4
BHP(CORR) = 0.0HP
MAN VAC(OBS) = 3.50"HG
BAR PRESS(CR)= 28.97"HG
                                                                                            MAN PRESS(CORR)= 0.00"HG
SPEC HUMIDITY=0.0127#/#
                                                     02 UHCC
1758. 1742
                                                                                        CO NO
                                                                                                                          NOX
                                      002
                             91052. 1758. 1742 81134.
KWD XTC MWEXH EXH FLOW FACAL
                                                                                                           245
CONC (PPM)
                                                                                                      FAM ERROR
METHOD 1, 2 0 85711 0,99969 26,96886 10188,110 0,08665 0,08770 -1,198
MASS/MODE(LBM) 8.82815 0.12391 0.05308 5.00097 0.01617 0.02559
MASS/RATED HP(#/HP) 0.05518 0.00077 0.00033 0.03126 0.00010 0.00016
KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
                      KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
0.85680 1.00000 26.97507 10185.770 0.08656 0.08770 -1 294
METHOD 2.1
MASS/MODE(LBM) 8.82612 0.12388 0.05307 4.99982 0.01617 0.02558 MASS/RATED HP(#/HP) 0.05516 0.00077 0.00033 0.03125 0.00010 0.00016
MASS/RATED HP(#/HP) 0.05516 0.00077 0.00033 0.03125 0.00010 0.0 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 3 1 0.85698 1.00017 26.96439 10189.800 0.08671 0.08770 -1 128
MASS/MODE(LBM) 8.82962 0.12393 0.05309 5.00180 0.01617 0.02559 MASS/RATED HP(#/HP) 0.05519 0.00077 0.00033 0.03126 0.00010 0.00016

        KWD
        XTC
        MWEXH
        EXH
        FLOW
        FACAL
        FAM
        ERROR

        METHOD 3, 2
        0.85711
        0.33685
        27.50000
        9991
        336
        0.08661
        0.08770
        -1.233

        MASS/MODE(LBM)
        8.65764
        0.12152
        0.05206
        4.90438
        0.01586
        0.02509

        MASS/RATED HP(#/HP)
        0.05411
        0.00075
        0.00033
        0.03065
        0.00009
        0.00016
```

TABLE 5.2. Continued

```
RUN NO. 4
MODE:
         5
COMMENTS: BASELINE DATA RUN4, 5
TEMP(DB) = 98.79F FUEL RATE= 34.8432#/HR
                                                           ENGINE RPM(NOM)=2350 RPM
                           FUEL RATE= 34.8432#/HR
AIR RATE = 396.3127#/HR
             = 65.00F
TEMP(DP)
                                                           ENGINE RPM(ACT)=2358. RPM
TEMP(BAR)
            = 88,00F
                           F/A RATIO= 0.0879#/#
PHIM = 1.3227
                                                           BHP(OBS) = 53. OHP

BHP(CORR) = 0. OHP
BAR PRESS(OB) = 29.12"HG
                                         1. 3227
                                                           MAN VAC(OBS)
BAR PRESS(CR)= 28.96"HG
                                                                           =11.50"HG
SPEC HUMIDITY=0.0136#/#
                                                           MAN PRESS(CORR) = 0.00"HG
                        002
                                             UHCC
                                                        CO NO NOX
                   92861. 1758. 1768.
KWD XTC MWEXH EXH FLOW
CONC (PPM)
                                                                    207.
                                                        78852.
                                                     FACAL FAM ERROR
METHOD 1, 2 0, 85528 1, 00164 27, 00743 6153, 914
                                                     0. 03905
MASS/MODE(LBM) 6. 52609 0. 08981
MASS/RATED HP(#/HP) 0. 04079 0. 00056
                                                                            0.01561
                                            0.00024
                                                                            0.00009
                  KWD XTC MWEXH EXH FLOW FACAL
                                                                  FAM ERROR
METHOD 2, 1
              0. 85696 1. 00000 26. 97456 6161. 414 0. 08643 0. 08791 -1. 692
                                                     3. 52722 0. 00993
0. 02205 0. 00006
FACAL FAM ERR
MASS/MODE(LBM) 6.53405 0.08992 0.03910
MASS/RATED HP(#/HP) 0.04084 0.00056 0.00024
                                                                            0.01563
                                                                            0.00009
                 KWD XTC MWEXH EXH FLOW
                                                                 FAM ERROR
METHOD 3. 1
             0. 85597 0. 99912 27. 03120 6148. 504
                                                      0.08565 0.08791 -2 572
MASS/MODE(LBM) 6.52036 0.08973 0.03902
MASS/RATED HP(#/HP) 0.04075 0.00056 0.00024
                                                     3, 51983 0, 00991
                                                                            0.01560
                                                      0. 02200
                                                                  0.00006
                                                                            0 00009
                :/HP) 0.04075 0.00056 0.00024
KWD XTC MWEXH EXH FLOW
                                                      FACAL FAM ERROR
0.08614 0.08791 -2.014
                                                                 FAM ERROR
             0.85531 0.33670 27.50000 6043.687
(M) 6.40920 0.08820 0.03835
METHOD 3, 2
                                                     3 45982 0.00974 0 01534
MASS/MODE(LBM)
MASS/RATED HP(#/HP) 0.04006 0.00055 0.00024
                                                      0. 02162 0. 00006 0. 00009
RUN NO.
MODE:
         6
COMMENTS: BASELINE DATA RUN4. 6
TEMP(DB) =100.35F FUEL RATE= 7.7963#/HR
TEMP(DP) = 66.00F AIR RATE = 99.5044#/HR
                                                           ENGINE RPM(NOM)=1200 RPM
                                                           ENGINE RPM(ACT)=1222, RPM
            BHP(OBS) = 4.3HP

BHP(CORR) = 0.0HP
TEMP(BAR)
BAR PRESS(OB)= 29.12"HG
                            PHIM =
                                                           BHP(CORR)
                                           1. 1788
                                                           MAN VAC(OBS) =19.10"HG
BAR PRESS(CR) = 28.96"HG
SPEC HUMIDITY=0.0141#/#
                                                           MAN PRESS(CORR)= 0.00"HG
                                                        C0 N0
49025. 204
                        002
                         02
                                             UHCC
                                                                              NOX
                                                        49025.
CONC (PPM)
                                            12300.
                        92260.
                                                                               229
KWD XTC MWEXH EXH FLOW METHOD 1. 2 0.86504 0.98720 27.40898 1509.072
                                                     FACAL FAM ERROR
0.07722 0.07835 -1 443
MASS/MODE(LBM) 0.79499 0.14630 0.03332
MASS/RATED HP(#/HP) 0.00497 0.00091 0.00021
                                                     0. 26855 0 00120 0. 00206
                                                      0.00168 0.00000
                                                                             0.00001
                                                      FACAL
                 KWD XTC
                                MWEXH EXH FLOW
                                                                 FAM ERROR
                                                      0. 07436 0. 07835 -5. 083
METHOD 2.1
              0. 85223 1. 00000 27. 64326 1496. 282
                                                     0. 26628 0. 00119
MASS/MODE(LBM) 0. 78825
MASS/RATED HP(#/HP) 0. 00493
                                 0. 14506
                                                                             0.00204
                                                      0. 00166
                                                                 0.00000
                                                                            0.00001
                                                     FACAL
                                                                  FAM ERROR
                KWD XTC
                                  MWEXH EXH FLOW
METHOD 3. 1 0.85940 1.00654 27 23067 1518.953 0.07966 0.07835 1.671
MASS/MODE(LBM) 0.80019 0.14726 0.03354
MASS/RATED HP(#/HP) 0.00500 0.00092 0.00021
                                                     0. 27031 0. 00121 0. 00207
                VHP) 0.00500 0.00092 0.00021
KWD XTC MWEXH EXH FLOW
                                                      0. 00169 0. 00000
                                                                            0.00001
                                                                  FAM ERROR
                                                      FACAL
              0. 86482 0. 29866 27. 50000 1504. 077
                                                      0.07608 0 07835 -2.889
METHOD 3, 2
MASS/MODE(LBM) 0.79236 0.14582 0.03321
MASS/RATED HP(#/HP) 0.00495 0.00091 0.00021
                                                     0, 26766 0, 00120 0, 00205
                                                      0.00167
                                                                 0. 00000
                                                                           0.00001
```

TABLE 5.2. Continued

RUN NO. 4					
MODE: 7					
COMMENTS: BASELINE DATA RUN					
TEMP(DB) = 98.40F	FUEL RATE=	3. 9002#/HF		E RPM(NOM)	= 680 RPM
TEMP(DP) = 66.00F	AIR RATE =	68. 6606#/HF	R ENGINE	E RPM(ACT)	
TEMP(BAR) = 88.00F	F/A RATIO=	0. 0568#/#	BHP (OI	BS)	= 1.9HP
BAR PRESS(OB)= 29.12"HG	PHIM =	0. 8546	BHP (C)		= 0. OHP
BAR PRESS(CR)= 28.96"HG			MAN V	AC(OBS)	=16.80"HG
SPEC HUMIDITY=0. 0141#/#				RESS(CORR)	= 0.00"HG
C02		UHCC	CO	NO	NOX
CONC(PPM) 8062		12700.	30954.	258.	300.
	XTC MWEXH	EXH FLOW	FACAL	FAM ER	
METHOD 1. 2 0. 88312 0. 97		1007, 845		05680 11.	
MASS/MODE(LBM) 0. 154		0. 00765	0. 03775	0. 00034	0 00060
MASS/RATED HP(#/HP) 0.000		0. 00005	0. 00024	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.125		0.00157	0.06424	0. 00021	0. 00034
	XTC MWEXH	EXH FLOW	FACAL	FAM ER	
METHOD 2. 1 0. 85348 1. 000		989. 670			566
MASS/MODE(LBM) 0.151: MASS/RATED HP(#/HP) 0.000:		0. 00752	0. 03707	0. 00033	0. 00059
	· · · · · · · · · · · · · · · · · · ·	0. 00005	0.00023	0. 00000	0. 00000
	31 0.00652 XTC MWEXH	0.00156 EXH FLOW	0. 06415	0. 00021	0.00034
METHOD 3. 1 0. 86963 1. 01			FACAL		ROR
MASS/MODE(LBM) 0. 156		1022. 943 0. 00777	0.06914 0. 0.03831	05680 21 0. 00034	
MASS/RATED HP(#/HP) 0.000		0.00005	0. 00024	0. 00000	0.00061
MASS/HP/CYC(#/HP/C) 0.125		0.00003	0.00024	0.00000	0. 00000 0. 00034
	XTC MWEXH	EXH FLOW	FACAL		0. 00034 ROR
METHOD 3. 2 0. 88259 0. 25		1017, 114			797
MASS/MODE(LBM) 0. 156		0.00772	0.03809	0.00034	0.00061
MASS/RATED HP(#/HP) 0.000		0.00005	0. 00024	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.123		0. 00156	0.06317	0.00021	0.00033
	U. UUUUU	0.00100	Q. QUULF	0.00021	0. 00003

TABLE 5.3. COMPUTER PRINTOUT: RUN 7

ENGINE TYPE: LIO-320-BIA DATE: 8-14-75 FUEL H/C RATIO = 2.190LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG

OPERATORS: PACE, PONSONBY, LEO, CARLOS RUN NO. MODE: COMMENTS: 4TH BASELINE RUN TEMP(DB) =102.08F FUEL RATE= 3. 7585#/HR ENGINE RPM(NOM) = 650 RPM AIR RATE = 64. 5482#/HR = 54.00F TEMP(DP) ENGINE RPM(ACT)= 650. RPM F/A RATIO= 0.0582#/# = 82.00F BHP(OBS) = 0.4HPTEMP(BAR) = 0.0HP BAR PRESS(OB) = 29.32"HG PHIM = 0.8760BHP (CORR) BAR PRESS(CR)= 29.18"HG MAN VAC(OBS) =17, 50"HG SPEC HUMIDITY=0, 0090#/# MAN PRESS(CORR) = 0.00"HG 002 02 UHCC CO NO CONC (PPM) 98219. 40787. 13423. 120. 66000. KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 90611 1. 03925 27. 78641 0. 05932 0. 05823 1. 884 METHOD 1.2 947. 613 MASS/MODE(LBM) 0.11904 MASS/RATED HP(#/HP) 0.00074 0. 02313 0. 12875 0. 01539 0. 00015 0. 00022 0.00080 0.00014 0. 00009 0. 00000 0.00000 MWEXH EXH FLOW FACAL KWD XTC FAM ERROR 0.06544 0.05823 12.393 METHOD 2.1 0. 94739 1. 00000 27. 09962 971. 628 MASS/MODE(LBM) 0. 12206 MASS/RATED HP(#/HP) 0. 00076 0. 13201 0. 02371 0. 01578 0. 00015 0.00023 0.00082 0. 00009 0.00015 0 00000 KWD XTC FACAL MWEXH EXH FLOW 0. 92503 0. 98058 28. 33650 METHOD 3. 1 929. 217

0.00000 FAM ERROR 0. 05149 0. 05823-11. 579 MASS/MODE(LBM) 0.11673 0. 12625 0. 02268 0. 01509 0. 00014 0.00022 MASS/RATED HP(#/HP) 0.00073 0.00078 0.00014 0.00009 0.00000 0.00000 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 90659 0. 22023 27. 50000 957, 482 0.06192 0.05823 6.339 METHOD 3 2 MASS/MODE(LBM) 0. 01555 0. 00015 0. 00023 0. 12028 0. 13009 0.02337 MASS/RATED HP(#/HP) 0.00075 0. 00000 0.00015 0.00009 0. 00000 0.00081

2 MODE: COMMENTS 4TH BASELINE RUN =101. 73F TEMP(DB) TEMP(DP) = 56,00F = 81.00F TEMP(BAR)

BAR PRESS(OB)= 29.30"HG

BAR PRESS(CR)= 29.16"HG

SPEC HUMIDITY=0.0097#/#

FUEL RATE= 8. 1544#/HR ENGINE RPM(NOM)=1200 RPM AIR RATE = 114, 4802#/HR ENGINE RPM(ACT)=1200 RPM BHP(OBS) = 5 4HP BHP(CORR) = 0 OHPF/A RATIO= 0.0712#/# PHIM = 1.0716 MAN VAC(OBS) = 18. 90"HG MAN PRESS(CORR) = 0.00"HG

NOX

120.

NOX 00202 THEC CO NO CONC (PPM) 35921. 32589. 152. 98093. 13902. 180 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL . 0. 87097 1. 01283 27. 81004 1699, 855 0. 06967 - 0. 07123 -2. 180 METHOD 1 2 MASS/MODE(LBM) 3 49107 MASS/RATED HP(#/HP) 0. 02182 0. 00368 0. 92915 0.15553 0. 73733 0 00668 0.00581 0.00002 0.00097 0.00461 0.00004 FACAL FAM ERROR 0.07229 0.07123 1 499 MWEXH EXH FLOW KWD XTC METHOD 2. 1 0.88404 1.00000 27.57799 1714.158 MASS/MODE(LBM) 3.52044 0.93697 MASS/RATED HP(#/HP) 0.02200 0.00586 0, 74353 0, 00372 0, 00674 0. 15684 0. 00465 0.00098 0.00002 0.00004 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 87681 0. 99352 27 99283 0. 06726 | 0. 07123 | -5. 565 1688. 755 METHOD 3 1 MASS/MODE(LBM) 3. 46828 0. 92308 MASS/RATED HP(#/HP) 0. 02168 0. 00577 0. 15452 0. 73251 0. 00366 0. 00664 0.00458 0.00002 0.00096 0.00004 KWD XTC MWEXH EXH FLOW

FACAL FAM ERROR 0.07068 0.07123 -0.769 0 87112 0 27754 27 50000 1719.020 METHOD 3, 2 MASS/MODE(LBM) 3.53043 0. 93962 0 15728 0. 74564 0.00373 0.00676 MASS/RATED HP(#/HP) 0 02207 0.00587 0.00098 0.00466 0.00002 0.00004

TABLE 5.3. Continued

```
RUN NO. 7
               3
MODE:
COMMENTS: 4TH BASELINE RUN
                                               FUEL RATE= 76. 0456#/HR
TEMP(DB) = 92.75F
                                                                                                 ENGINE RPM(NOM)=2700 RPM
                                               AIR RATE = 875. 0493#/HR
TEMP(DP)
                      = 52.00F
                                                                                                 ENGINE RPM(ACT)=2700 RPM
TEMP(BAR) = 82.00F
                                              F/A RATIO= 0.0869#/#
PHIM = 1.3074
                                                                                                 BHP(OBS) =140.4HP
BHP(CORR) =154.3HP
BAR PRESS(OB) = 29.30"HG
BAR PRESS(CR)= 29.16"HG
                                                                                                 MAN VAC(OBS) = 0.60"HG
SPEC HUMIDITY=0. 0084#/#
                                                                                                MAN PRESS(CORR)=29. 10"HG
                                                                       UHCC
1635.
                                        C02
                                                          02
                                                                                             CO NO NOX
                                      86102.
                              86102. 1758. 1635.
KWD XTC MWEXH EXH FLOW
                                                                                                              216.
CONC (PPM)
                                                                                       86374. 216. 211.

FACAL FAM ERROR

0. 08824 0. 08690 1. 537

0. 42730 0. 00115 0. 00171

0. 00267 0. 00000 0. 00001
                                                                                           86374.
                                                                                                                                 211.
METHOD 1. 2 0. 86403 0. 99042 26. 90207 13628. 200
MASS/MODE(LBM) 0.67002 0.00994 0.00400
MASS/RATED HP(#/HP) 0.00419 0.00006 0.00002

        MASS/RATED HP(#/HP)
        0.00419 KWD
        0.00006 MWEXH
        0.00002 EXH FLOW EXH FLOW FACAL FAM ERROR

        METHOD 2.1
        0.85449 1.00000 27.09535 13530.990
        0.08561 0.08690 -1.485

        MASS/MODE(LBM)
        0.66524 0.00987 0.00397 0.42425 0.00114 0.00170

        MASS/RATED HP(#/HP)
        0.00416 0.00006 0.00002 0.00265 0.00000 0.00001

        KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

        METHOD 3.1 0.86014 1.00517 26.76370 13698.660 0.09016 0.08690 3.746

        MASS/MODE(LBM) 0.67349 0.00999 0.00402 0.42950 0.00115 0.00172

        MASS/RATED HP(#/HP) 0.00421 0.00006 0.00003 0.00268 0.00000 0.00001

        KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

        METHOD 3.2 0.86395 0.33392 27.50000 13331.890 0.08724 0.08690 0.395

        MASS/MODE(LBM) 0.65546 0.00972 0.00391 0.41800 0.00112 0.00168

        MASS/RATED HP(#/HP) 0.00410 0.00410 0.00006 0.00002 0.00261 0.00000 0.00001

RUN NO
MODE:
               4
COMMENTS: 4TH BASELINE RUN
TEMP(DB) = 94.75F FUEL RATE= 58.9970#/HR ENGINE RFM(NOM)=2440 RPM
TEMP(DP) = 52.00F AIR RATE = 679.1985#/HR ENGINE RPM(ACT)=2440. RPM
TEMP(BAR) = 82.00F F/A RATIO= 0.0868#/# BHP(OBS) =108.5HP
                                                                                                 BHP(0BS) =108.5HP
BAR PRESS(OB)= 29.30"HG
                                             PHIM =
                                                                   1. 3068
                                                                                                  BHP (CORR)
                                                                                                                          = 0. OHP
                                                                                               MAN VAC(OBS) = 3.30"HG
BAR PRESS(CR)= 29.16"HG
 SPEC HUMIDITY=0. 0084#/#
                                                                                                MAN PRESS(CORR)= 0.00"HG
                                                          02 UHCC
2010. 1752.
                                                                                            CO NO NOX
                                       002
CONC (PPM)
                                       90052.
                                                                                            81991.
                                                                                                               251.
5, 22730 0, 01717 0, 02617
                                                                                                                              0.00016
                                                                                        MASS/MODE(LBM) 8.86786 0.14383 0.05424
MASS/RATED HP(#/HP) 0.05542 0.00089 0.00034
```

TABLE 5.3. Continued

```
RUN NO. 7
MODE:
         5
COMMENTS: 4TH BASELINE RUN
                               FUEL RATE= 35. 1288#/HR
TEMP(DB) =101.08F
                                                                ENGINE RPM(NOM)=2350 RPM
                               FUEL RATE = 35.1288#/HR
AIR RATE = 404.5498#/HR
TEMP(DP)
            = 54 00F
                                                                ENGINE RPM(ACT) =2350, RPM
            = 84.00F
                               F/A RATIO= 0.0868#/#
PHIM = 1.3064
                                                                BHP(OBS) = 55.6HP
BHP(CORR) = 0.0HP
MAN VAC(OBS) =11.50"HG
TEMP (BAR)
BAR PRESS(OB)= 29 30"HG
BAR PRESS(CR)= 29. 15"HG
SPEC HUMIDITY=0. 0090#/#
                                                                MAN PRESS(CORR)= 0.00"HG
                                                             CO NO NOX
                          CO2
                                      02
                                                  UHCC
CONC (PPM)
                         92065.
                                      1758.
                                                 1674.
                                                             78783.
                                                                          252.
                                                                                      248
                                                                        FAM ERROR
                                                          FACAL
                    KWD
                           XTC MWEXH EXH FLOW
METHOD 1. 2 0. 86035 0. 99762 27. 07744 6259. 336 0. 08575 0. 08683 -1. 249
MASS/MODE(LBM) 6.58094 0.09135
MASS/RATED HP(#/HP) 0.04113 0.00057
                                                          3. 58011 0. 01228 0. 01848
0. 02238 0. 00007 0. 00012
                                              0. 03761
0. 00024
                  KWD XTC MWEXH EXH FLOW
                                                            FACAL
                                                                       FAM ERROR
             KWD XTC MWEXH EXH FLUW FHEHE FRI LINGS ON 85796 1,00000 27,12497 6248,367 0,08511 0,08683 -1,986 BM) 6,56941 0,09119 0,03754 3,57383 0,01226 0,01845 BP(#/HP) 0,04106 0,00057 0,00023 0,02234 0,00007 0,00012
METHOD 2. 1
MASS/MODE(LBM) 6. 56941
MASS/RATED HP(#/HP) 0. 04106
                                     MWEXH EXH FLOW FACAL
                 KWD XTC
                                                                        FAM ERROR
METHOD 3. 1 0.85936 1.00127 27.04303 6267.301 0.08621 0.08683 -0.711
MASS/MODE(LBM) 6.58932 0.09146 0.03766 3.58466 0.01229
MASS/RATED HP(#/HP) 0.04118 0.00057 0.00024 0.02240 0.00007
                                                                                    0.01850
                                                                                    0.00012
                  KWD XTC
                                   MWEXH EXH FLOW
                                                            FACAL
                                                                        FAM ERROR
METHOD 3. 2 0. 86032 0. 33079 27. 50000 6163 156 0. 08551 0. 08683 -1. 524
MASS/MODE(LBM) 6. 47982
MASS/RATED HP(#/HP) 0. 04050
                                   0. 08994
0. 00056
                                              0. 03703 3. 52510 0. 01209 0. 01820
0. 00023 0 02203 0. 00007 0. 00011
RUN NO
MODE:
          6
COMMENTS: 4TH BASELINE RUN
TEMP(DB) =107, 22F
                               FUEL RATE= 8. 7566#/HR
                                                                ENGINE RPM(NOM)=1200 RPM
TEMP(DP) = 53.00F
TEMP(BAR) = 83.00F
                               AIR RATE = 109. 4959#/HR
                                                                ENGINE RPM(ACT)=1200. RPM
                               F/A RATIO= 0.0799#/#
PHIM = 1.2031
                                                                BHP(OBS) = 5.4HP
BHP(CORR) = 0.0HP
MAN VAC(OBS) =19 30"HG
BAR PRESS(OB) = 29.30"HG
BAR PRESS(CR)= 29.16"HG
SPEC HUMIDITY=0. 0087#/#
                                                                MAN PRESS(CORR)= 0.00"HG
                           002
                                      02
                                                  UHCC
                                                              CO NO NOX
                                              18375.
                         88252.
                                     30897.
CONC (PPM)
                                                             54301.
                                                          54301. 135.
FACAL FAM ERROR
0. 07888 0. 07997 -1. 354
                                                                         135.
                                                                                      139
                    KWD XTC MWEXH EXH FLOW
METHOD 1. 2 0. 87100 1. 02314 27. 33202 1667. 781
                                   0. 21385
                                                          MASS/MODE(LBM) 0.84043
MASS/RATED HP(#/HP) 0.00525
                                    KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
0.89465 1.00000 26.88763 1695.345 0.08442 0.07997 5.572
1) 0.85432 0.21738 0.05592 0.33417 0.00088 0.00140
0(#/HP) 0.00534 0.00136 0.00035 0.00209 0.00001 0.00000
METHOD 2, 1
MASS/MODE(LBM) 0 85432 0.21738
MASS/RATED HP(#/HP) 0.00534 0.00136
                   KWD XTC MWEXH EXH FLOW
                                                            FACAL
                                                                        FAM ERROR
METHOD 3. 1 0. 88112 0. 98790 27. 66672 1647. 605
                                                           0.07438 0.07997 -6.991
                                    0. 00136
MASS/MODE(LBM) 0.83026
MASS/RATED HP(#/HP) 0.00519
                                   0. 21126
                                                          0 00001
                                                                                   0.00000
                                                         FACAL
                KWD XTC MWEXH EXH FLOW
                                                                       FAM ERROR
METHOD 3. 2
               0. 87124 0. 30238 27. 50000 1657. 593 0. 08099 0. 07997 1. 279
MASS/MODE(LBM) 0.83529 0.21254 0.05467
MASS/RATED HP(#/HP) 0.00522 0.00133 0.00034
```

TABLE 5.3. Continued

RUN NO. 7					
MODE: 7					
COMMENTS: 4TH BASELINE RUN					
TEMP(DB) =105, 49F	FUEL RATE=	4. 1557#/HF	R ENGIN	NE RPM(NOM)= 650 RPM
TEMP(DP) = 54.00F	AIR RATE =	65. 0877#/HF	R ENGIN	NE RPM(ACT) = 650. RPM
TEMP(BAR) = 83.00F	F/A RATIO=	0.0638#/#	BHP (C	OBS)	= 1.7HP
BAR PRESS(OB)= 29.30"HG	PHIM =	0. 9606	BHP (C	CORR)	= 0. OHP
BAR PRESS(CR)= 29.16"HG			MAN V	/AC(OBS)	=17.00"HG
SPEC HUMIDITY=0.0090#/#			MAN F	PRESS (CORR)= 0.00"HG
C02	2 02	UHCC	CO	NO	NOX
CONC(PPM) 7757	' 9. 75862 .	33092.	19262.	93.	105
KWD	XTC MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 1. 2 0. 89368 1. 02	850 27. 78122	960. 788	0.06391 0	0. 06384° 0	. 107
MASS/MODE(LBM) 0.141	.87 0. 10083	0.01902	0. 02239	0.00012	0. 00020
MASS/RATED HP(#/HP) 0.000	0.00063	0.00012	0.00014	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.130	0. 01013	0.00218	0. 06459	0.00022	0. 00034
KWD	XTC MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 2. 1 0. 92318 1. 00		978. 491	0.06887	0. 06384 7	. 877
MASS/MODE(LBM) 0. 144	148 0. 10269	0. 01937	0. 02281	0.00012	0.00020
MASS/RATED HP(#/HP) 0.000		0.00012	0.00014	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.130		0. 00220	0. 06459	0.00022	0. 00034
KWD	XTC MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 3. 1 0. 90711 0. 98		947. 145		D. 06384 - 8	. 582
MASS/MODE(LBM) 0. 139		0. 01875	0. 02208	0. 00011	0. 00020
MASS/RATED HP(#/HP) 0.000		0.00012	0. 00014	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.130		0. 00217	0. 06459	0. 00022	0. 00034
KWD	XTC MWEXH	EXH FLOW	FACAL		RROR
METHOD 3, 2 0, 89402 0, 24		970. 613			. 299
MASS/MODE(LBM) 0.143		0. 01922	0. 02262	0.00012	0. 00020
MASS/RATED HP(#/HP) 0.000		0.00012	0. 00014	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C) 0.128	395 0. 01017	0. 00219	0. 06366	0.00022	0.00034

TABLE 5.4. COMPUTER PRINTOUT: RUN 16

ENGINE TYPE: LIO-320-B1A DATE: 10/2/75 FUEL H/C RATIO = 2.190LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG OPERATORS: PACE, PONSONBY, GRIFFIN **RUN NO. 016** MODE 1 COMMENTS: BASELINE DATA RUN#16 FUEL RATE= TEMP(DB) = 81.40F 3. 3925#/HR ENGINE RPM(NOM) = 640 RPM = 29.00F AIR RATE = 56. 9457#/HR ENGINE RPM(ACT) = 633. RPM TEMP(DP) TEMP (BAR) = 75.00F F/A RATIO= 0.0596#/# BHP (OBS) = 0.5HP BAR PRESS(OB) = 29.53"HG 0. 8963 BHP (CORR) = 0. OHP PHIM BAR PRESS(CR)= 29. 41"HG MAN VAC(OBS) =17.00"HG MAN PRESS(CORR) = 0.00"HG SPEC HUMIDITY=0. 0033#/# C02 02 UHCC CO NO NOX CONC (PPM) 72373. 19556 118. 151 12661 44726. KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 93159 0. 76304 28. 20909 824, 525 0. 05084 0. 05957-14. 658 METHOD 1, 2 MASS/MODE(LBM) 0. 07019 MASS/RATED HP(#/HP) 0. 00044 0.08254 0.00964 0.01263 0.00013 0.00025 0.00052 0.00006 0.00007 0.00000 0.00000 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 73639 1. 00000 31. 40211 0. 02882 0. 05957-51. 626 740. 686 METHOD 2.1 0.00866 0.00011 0.01135 0.00022 MASS/MODE(LBM) 0.06305 0.07415 0.00005 MASS/RATED HP(#/HP) 0, 00039 0.00046 0.00007 0.00000 0.00000 FAM ERROR KWD FACAL MWEXH EXH FLOW XTC METHOD 3. 1 0. 83071 1. 10457 25. 45438 913, 756 0. 09542 0. 05957 60. 171 MASS/MODE(LBM) 0.07778 MASS/RATED HP(#/HP) 0.00049 0. 01400 0. 00014 0.01069 0.09148 0.00027 0.00008 0.00000 0.00057 0.00006 0.00000 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL 0. 93055 0. 14801 27. 50000 845, 785 0. 03803 0. 05957-36. 158 METHOD 3, 2 0. 07200 MASS/MODE(LBM) 0.08467 0.00989 0.01296 0.00013 0.00025 MASS/RATED HP(#/HP) 0.00045 0.00053 0.00006 0.00008 0.00000 0.00000 **RUN NO. 016** MODE: COMMENTS: 1 TEMP(DB) = 69.47FFUEL RATE= 8. 9153#/HR ENGINE RPM(NOM)=1201 RPM ENGINE RPM(ACT)=1201 RPM TEMP(DP) = 28,00F AIR RATE = 113.8139#/HR = 8.7HP TEMP(BAR) = 74.00F F/A RATIO= 0.0783#/# BHP (OBS) - = 0 OHP BAR PRESS(OB) = 29.53"HG PHIM BHP (CORR) 1.1785 MAN VAC(OBS) =18.80"HG BAR PRESS(CR)= 29.41"HG SPEC HUMIDITY=0.0032#/# MAN PRESS(CORR) = 0.00"HG NOX C02 02 UHCC coNO 41059. 320. CONC (PPM) 69065. 16506. 11111. 326 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL 0. 89862 0. 78428 27. 56613 0. 07836 0. 07833 0. 043 1716, 218 METHOD 1 2 MASS/MODE(LBM) 2. 48164 MASS/RATED HP(#/HP) 0. 01551 0.00783 0.43106 0.12551 0. 93790 0.01221 0.00269 0.00078 0.00586 0.00005 0.00007 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL 0 72254 1.00000 30.82196 METHOD 2.1 1534, 928 0. 04377 0. 07833-44, 125 MASS/MODE(LBM) 2. 21949 MASS/RATED HP(#/HP) 0. 01387 0. 00700 0.38552 0.11225 0. 83883 0.01092 0.00004 0.00241 0.00070 0.00524 0.00006 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0. 11635 0. 07833 48. 539 0. 81257 1. 10074 25. 02763 1890, 291 METHOD 3.1 MASS/MODE(LBM) 2. 73335 MASS/RATED HP(#/HP) 0. 01708 0.00862 0 47478 0.13824 1.03303 0.01345 0.00005 0.00086 0.00645 0.00008 0.00297 KWD MWEXH EXH FLOW FACAL FAM ERROR XTC 0. 89782 0. 23312 27. 50000 1720. 346 0. 05969 0. 07833-23. 797 METHOD 3. 2 0. 12581 0. 94016 0. 00785 0.01224MASS/MODE(LBM) 2. 48761 0.43209 MASS/RATED HP(#/HP) 0.01555 0.00270 0.00078 0.00588 0.00005 0.00007

TABLE 5.4. Continued

```
RUN NO. 016
MODE: 3
COMMENTS: 1
TEMP(DB) = 64.38F FUEL RATE = 77.2798#/HR
TEMP(DP) = 32.00F AIR RATE = 932.1025#/HR
TEMP(BAR) = 74.00F F/A RATIO = 0.0020#/"
                                                                                                                                         ENGINE RPM(NOM)=2688 RPM
                                                                                                                                         ENGINE RPM(ACT)=2689, RPM
                                                                                                                                                                     =151.5HP
                                                                                                                                           BHP(OBS)
BAR PRESS(OB) = 29.52"HG
                                                                   PHIM = 1.2473
                                                                                                                                         BHP(CORR)
                                                                                                                                                                                =156. 2HP
BAR PRESS(CR)= 29.40"HG
                                                                                                                                        MAN VAC(OBS) = 0.70"HG
SPEC HUMIDITY=0.0038#/#
                                                                                                                                         MAN PRESS(CORR)=29.09"HG
                                                         C02
                                                                                   02
                                                                                                            UHCC
                                                                                                                                     CO NO NOX
                                                                                   635.
                                                                                                                                   56747.
CONC (PPM)
                                                        67432.
                                                                                                          1047.
                                                                                                                                                               238.
                                                                                                                                                                                        231.

        CONC (PPM)
        67432.
        635.
        1047.
        56747.
        238.
        231.

        KWD
        XTC
        MWEXH
        EXH
        FLOW
        FACAL
        FAM
        ERROR

        METHOD 1. 2
        0. 89779
        0. 75240
        27. 19536
        14307. 420
        0. 08524
        0. 08290
        2. 815

        MASS/MODE(LBM)
        0. 55089
        0. 00377
        0. 00269
        0. 29472
        0. 00133
        0. 00197

        MASS/RATED HP(#/HP)
        0. 00344
        0. 00002
        0. 00002
        0. 00184
        0. 00000
        0. 00001

        METHOD 2. 1
        0. 69915
        1. 00000
        31. 04938
        12531. 500
        0. 04205
        0. 08290-49. 285

        MASS/MODE(LBM)
        0. 48251
        0. 00300
        0. 00236
        0. 25814
        0. 00116
        0. 00172

        MASS/RATED HP(#/HP)
        0. 00302
        0. 00002
        0. 00001
        0. 00161
        0. 00000
        0. 00001

        KWD
        XTC
        MWEXH
        EXH
        FLOW
        FACAL
        FAM
        ERROR

        METHOD 3. 2
        0. 89676
        0. 24859
        27. 50000
        14148. 930
        0. 06169
        0. 08290-25. 598

        MASS/MODE(LBM)
        0. 54479
        0. 00373
        0. 00266
        0. 29145
        0. 00131
        0. 0

        MASS/RATED HP(#/HP)
        0. 00340
        0. 00002
        0. 00002
        0. 00182
        0. 00000
        0. 0

                                                                                                                                                                                  0.00194
                                                                                                                                                                                0. 00001
 RUN NO. 016
 MODE: 4
 COMMENTS: 1
 TEMP(DB)
                                = 65. 90F
                                                                   FUEL RATE= 56, 4972#/HR
                                                                                                                                        ENGINE RPM(NOM)=2434 RPM
 TEMP(DP)
                                = 30,00F
                                                                   AIR RATE = 683.9753#/HR
                                                                                                                                          ENGINE RPM(ACT)=2434 RPM
                           = 74.00F
                                                                   F/A RATIO= 0.0826#/#
PHIM = 1.2427
                                                                                                                                          BHP(OBS) =111.0HP
BHP(CORR) = 0.0HP
 TEMP(BAR)
 BAR PRESS(OB) = 29.52"HG
                                                                                                                                           BHP (CORR)
                                                                                                                                                                               = 0. OHP
                                                                                                                                           MAN VAC(OBS) = 3 60"HG
 BAR PRESS(CR)= 29.40"HG
 SPEC HUMIDITY=0.0035#/#
                                                                                                                                          MAN PRESS(CORR)= 0.00"HG
                                                                                 02
                                                                                                                                     CO
                                                                                                           HHCC
                                                                                                                                                           NO NOX
                                                          C02
                                                       68709.
                                                             3709. 1270. 1182.
XTC MWEXH EXH FLOW
 CONC (PPM)
                                                                                                                                    50737.
                                                                                                                                                                 326.

        KWD
        XTC
        MWEXH
        EXH FLOW
        FACAL
        FAM
        ERROR

        METHOD 1. 2
        0. 89923
        0. 73928
        27. 34589
        10438.000
        0. 08307
        0. 08260
        0. 570

        MASS/MODE(LBM)
        6. 82518
        0. 09166
        0. 03691
        3. 20402
        0. 07207
        0. 03311

        MASS/RATED HP(#/HP)
        0. 04266
        0. 00057
        0. 00023
        0. 02003
        0. 00014
        0. 00021

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
METHOD 2. 1 0. 69241 1. 00000 31. 29414 9121. 082 0. 03973 0. 08260-51 906
MASS/MODE(LBM) 5. 96408 0. 08010 0. 03225 2. 79978 0. 01929 0. 02894
MASS/RATED HP(#/HP) 0. 03728 0. 00050 0. 00020 0. 01750 0. 00012 0. 00018
 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
METHOD 3. 1 0. 79867 1. 12233 24. 36182 11716. 550 0. 12894 0. 08260 56. 095
                                                                                                                                                          FAM ERROR
MASS/MODE(LBM) 7. 66120 0. 10290 0. 04143 3. 59648 0. 02478 0. 03717
MASS/RATED HP(#/HP) 0. 04788 0. 00064 0. 00026 0. 02248 0. 00015 0. 00023

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR
METHOD 3. 2 0. 89821 0. 23986 27 50000 10379, 510 0. 05907 0. 08260-28, 482
MASS/MODE(LBM) 6. 78693 0. 09115 0. 03670 3. 18606 0. 02195 0. 03293
 MASS/RATED HP(#/HP) 0.04242 0.00057
                                                                                                        0. 00023 0. 01991
                                                                                                                                                           0.00014
                                                                                                                                                                                    0.00021
```

TABLE 5.4. Continued

```
RUN NO. 016
 MODE: 5
 COMMENTS: 1
 TEMP(DB)
                                                    FUEL RATE= 34. 6021#/HR
                         = 69.07F
                                                                                                          ENGINE RPM(NOM)=2353 RPM
                     = 32.00F
= 74.00F
  TEMP(DP)
                                                    AIR RATE = 413. 1118#/HR
                                                                                                       ENGINE RPM(ACT)=2354, RPM
                                                   F/A RATIO= 0. 0837#/#
PHIM = 1. 2601
  TEMP(BAR)
                                                                                                          BHP(OBS) = 58.5HP
 BAR PRESS(OB) = 29.52"HG
                                                                                                                                      = 0. OHP
                                                                                                         BHP (CORR)
                                                                                                         MAN VAC(OBS) =11.50"HG
 BAR PRESS(CR) = 29.40"HG
 SPEC HUMIDITY=0.0038#/#
                                                                                                         MAN PRESS(CORR) = 0.00"HG
CONC (PPM) 70433. 1270. 1155. 50870. 279. 276.

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

METHOD 1. 2 0. 89723 0. 75093 27. 36317 6307. 168 0. 08279 0. 08376 -1. 157

MASS/MODE (LBM) 5. 07313 0. 06646 0. 02615 2. 32934 0. 01367 0. 02072

MASS/RATED HP(#/HP) 0. 03171 0. 00042 0. 00016 0. 01456 0. 00008 0. 00013

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

METHOD 2. 1 0. 69783 1. 00000 31. 16397 5537 941 0. 04087 0. 08376-51. 210

MASS/MODE (LBM) 4. 45441 0. 05836 0. 02296 2. 04525 0. 01200 0. 01819

MASS/RATED HP(#/HP) 0. 02784 0. 00036 0. 00014 0. 01278 0. 00007 0. 00011

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

METHOD 3. 1 0. 80060 1. 11724 24. 48836 7047. 602 0. 12663 0. 08376 51 188

MASS/MODE (LBM) 5. 66869 0. 07427 0. 02922 2. 60280 0. 01527 0. 02315

MASS/RATED HP(#/HP) 0. 03543 0. 00046 0. 00018 0. 01627 0. 00009 0. 00014
                                  CO2 O2 UHCC
70433. 1270. 1155.
KWD XTC MWEXH EXH FLOW
                                                                                                      CO NO
                                                                                                                                         NOX
                      HP(#/HP) 0.03543 0.00046 0.00018 0.01627
KWD XTC MWEXH EXH FLOW FACAL
                                                                                                                    FAM ERROR
 METHOD 3. 2
                            0. 89616 0. 24327 27. 50000 6275. 789 0. 05992 0. 08376-28. 467
 MASS/MODE(LBM) 5.04789 0.06613 0.02602 2.31775 0.01360 0.02061
MASS/RATED HP(#/HP) 0.03155 0.00041 0.00016 0.01449 0.00008 0.00013
 RUN NO. 016
 MODE 6
 COMMENTS: 1
 TEMP(DB)
                         = 69.73F FUEL RATE= 8.4986#/HR
= 26.00F AIR RATE = 110.4127#/HR
                                                                                                         ENGINE RPM(NOM)=1194 RPM
                      = 26.00F
  TEMP(DP)
                                                                                                      ENGINE RPM(ACT)=1202. RPM
  TEMP(BAR)
                      = 74.00F
                                                    F/A RATIO= 0.0769#/#
                                                                                                         BHP(OBS) = 7.9HP
BHP(CORR) = 0.0HP
 BAR PRESS(OB) = 29.52"HG
                                                    PHIM = 1.1580
                                                                                                          BHP (CORR)
 BAR PRESS(CR)= 29.40"HG
                                                                                                         MAN VAC(OBS) =18.80"HG
 SPEC HUMIDITY=0.0029#/#
                                                                                                         MAN PRESS(CORR) = 0 00"HG
                                                             02 UHCC
21585. 7500.
                                                                                                      CO NO NOX
35862. 271. 276.
                                          002
 CONC (PPM)
                                                                                                     35862.
                                          67856.
                                  KWD XTC MWEXH EXH FLOW FACAL
                                                                                                                    FAM ERROR
 METHOD 1. 2 0. 90406 0. 77050 27. 73962 1652 429 0. 07251 0. 07697 -5. 785

MASS/MODE(LBM) 0. 64025 0. 14802 0. 02225 0. 21511 0 00174 0 00271

MASS/RATED HP(#/HP) 0 00400 0. 00092 0. 00014 0. 00134 0 00001 0 00002

KWD XTC MWEXH EXH FLOW FACAL FAM ERROR

METHOD 2 1 0 71739 1. 00000 31 12189 1472. 846 0 03895 0. 07697-49 392
 MASS/MODE(LBM) 0.57067 0.13193 0.01983 0.19174 0.00155 0.00742 MASS/RATED HP(#/HP) 0.00357 0.00082 0.00012 0.00120 0.00001 0.00002
                              /HP) 0.00357 0.00082 0.00012 0.00120 KWD XTC MWEXH EXH FLOW FACAL
                                                                                                                    FAM ERROR
  METHOD 3.1 0.81176 1.10596 25.04637 1830.116 0.11325 0.07697 47.140
 MASS/MODE(LBM) 0.70909 0.16394 0.02464 0.23825 0.00193 0.00301 MASS/RATED HP(#/HP) 0.00443 0.00102 0.00015 0.00149 0.00001 0.00002
                                                                                                 0.00149

        KWD
        XTC
        MWEXH
        EXH FLOW
        FACAL
        FAM
        ERROR

        METHOD 3. 2
        0 90328 0. 21786 27. 50000
        1666. 828
        0. 05432 0. 07697-29 424

        MASS/MODE(LBM)
        0. 64583 0 14931 0. 02244 0. 21699 0. 00176 0. 00274

        MASS/RATED HP(#/HP)
        0. 00404 0. 00097 0. 00014 0. 00136 0. 00001 0. 00002
```

TABLE 5.4. Continued

RUN NO. 016						
MODE: 7						
COMMENTS: 1						
TEMP(DB) = 70.		EL RATE=	3. 4463#/H		INE RPM(NOM)= 662 RPM
TEMP(DP) = 34.	OOF AIF	RATE =	55. 9467#/HF	R ENGI	INE RPM(ACT)= 663. RPM
TEMP(BAR) = 74.	00F F/F	A RATIO=	0.0616#/#	BHP ((OBS)	= 0.7HP
BAR PRESS(OB)= 29.	52"HG PHI	[M =	0. 9267	BHP ((CORR)	= 0. QHP
BAR PRESS(CR)= 29.	40"HG			MAN	VAC(OBS)	=17. 50"HG
SPEC HUMIDITY=0.00	42#/#			MAN	PRESS(CORR)= 0.00"HG
	,C02	02	UHCC	CO	NO	NOX
CONC(PPM)	48153.	69833.	19405.	13124.	138.	138.
	KWD XTC	MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 1. 2 0. 92	714 0. 77648	28. 19276	812, 079	0. 05230	0.06160-15	. 091
MASS/MODE(LBM)	0. 07442	0. 07844	0.00942	0. 01290	0.00015	0.00022
MASS/RATED HP(#/HP) 0. 00047	0. 00049	0. 00006	0. 00008	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C	0. 09822	0. 00564	0.00145	0. 04379	0. 00029	0. 00044
	KWD XTC	MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 2. 1 0. 74	120 1.00000	31, 23962	732. 875	0. 03046	0.06160-50	. 549
MASS/MODE(LBM)	0.06716	0. 07079	0.00850	0. 01164	0.00013	0.00020
MASS/RATED HP(#/HP	0.00042	0. 00044	0. 00005	0. 00007	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C	0.08638	0.00503	0.00129	0. 03848	0. 00026	0. 00039
	KWD XTC	MWEXH	EXH FLOW	FACAL	FAM E	RROR
	146 1. 09909	25, 57610	895. 162	0. 09409	0.06160 52	. 759
MASS/MODE(LBM)	0. 08204	0. 08647	0.01039	0.01422	0.00016	0.00025
MASS/RATED HP(#/HF	0. 00051	0. 00054	0. 00006	0. 00008	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C	0.10968	0.00624	0.00161	0. 04893	0 00033	0. 00050
	KWD XTC	MWEXH	EXH FLOW	FACAL	FAM E	RROR
METHOD 3, 2 0, 92	591 0.15601	27. 50000	832, 536	0. 03984	0.06160-35	. 325
MASS/MODE(LBM)	0. 07630	0. 08042	0. 00966	0.01322	0.00015	0.00023
MASS/RATED HP(#/HF		0. 00050	0. 00006	0. 00008	0. 00000	0. 00000
MASS/HP/CYC(#/HP/C	0 09788	0. 00567	0. 00146	0. 04362	0. 00029	0. 00044

5.2 AVCO-LYCOMING LIO-320 LEAN-OUT RUNS

The purpose of this test was to observe the effect of fuelair ratio on emission levels. The standard test setup was used for this series of measurements except for the addition of a knock sensor to detect the onset of detonation.

The test procedure consisted of operating the engine at the five modes of the seven mode test cycle. The fuel-air ratio was varied within each mode. The first data point taken for each mode was with the mixture set full-rich. This data point was used to establish the baseline emission levels and to establish the cooling air requirements necessary to hold the cylinder heads at the maximum continuous operating temperature. This cooling air flow rate was held constant throughout the leaning process.

Other values held constant throughout leaning were engine RPM and engine power output.

There were three criteria used to judge the lean limit for this engine. They were engine cylinder head temperature exceeding the maximum continuous operating temperature, the onset of detonation (either audible or by means of the knock sensor), and severe power and RPM drops. During testing, large power and RPM drops were encountered before the knock or cylinder head temperature limits were exceeded.

The results from these tests are plotted in figures 5.4 to 5.8, which are taken from reference 10. CO and CO2 concentrations are shown to be dependent on fuel-air ratio only and independent of operating mode. This is also true for O2 concentrations at mixture ratios leaner than stoichiometric. However, NOX levels are strongly dependent upon both operating mode and mixture ratio, the peak levels for all modes occurring at about a fuel-air ratio of 0.065. The strong dependence of NOX concentration on mixture ratio is clearly illustrated.

[&]quot;Computer print-outs from these tests are given in tables 5.5-5.8."

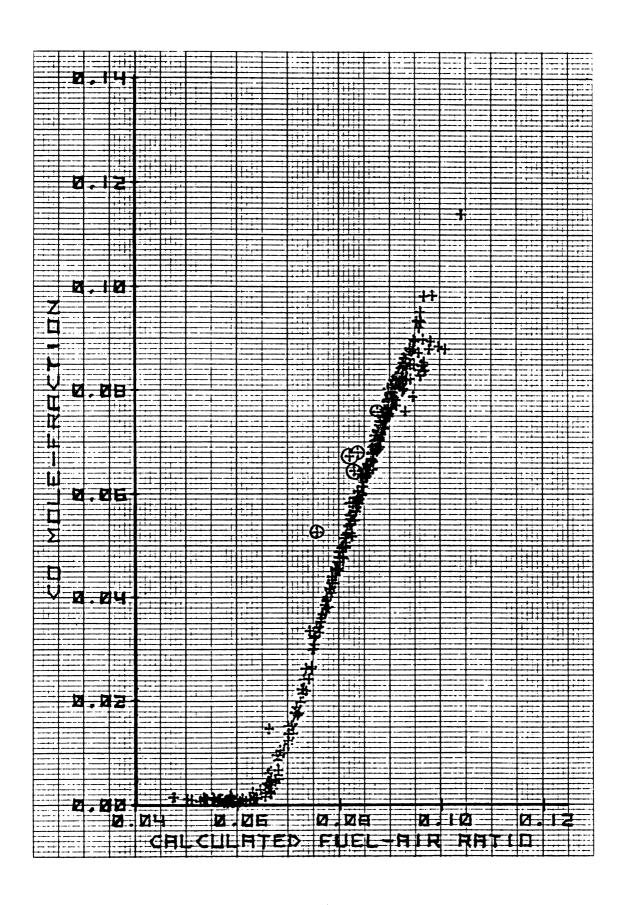


Figure 5.4. LIO-320 Lean-Out Results for CO (Reference 10)

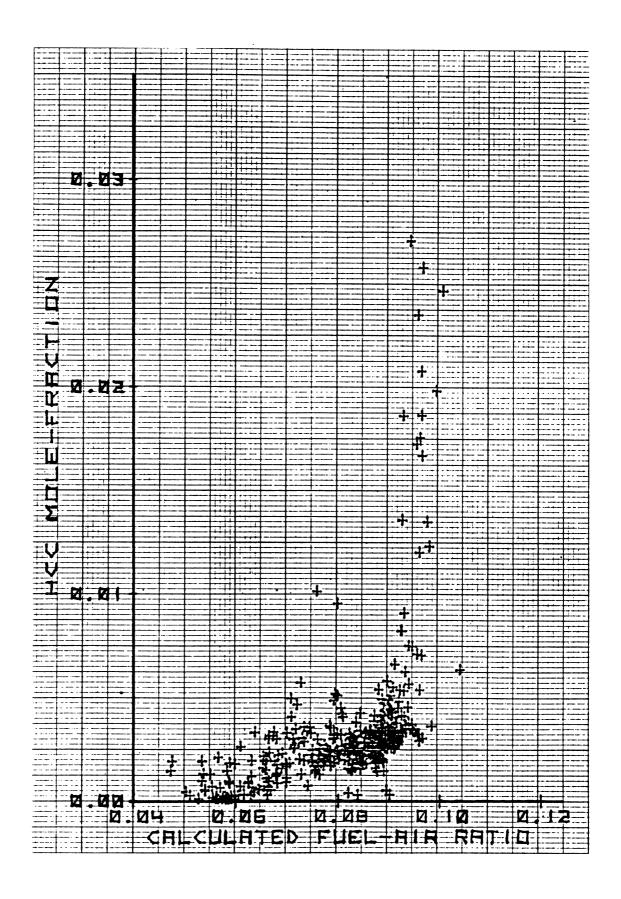


Figure 5.5. LIO-320 Lean-Out Results for UHCC (Reference 10)

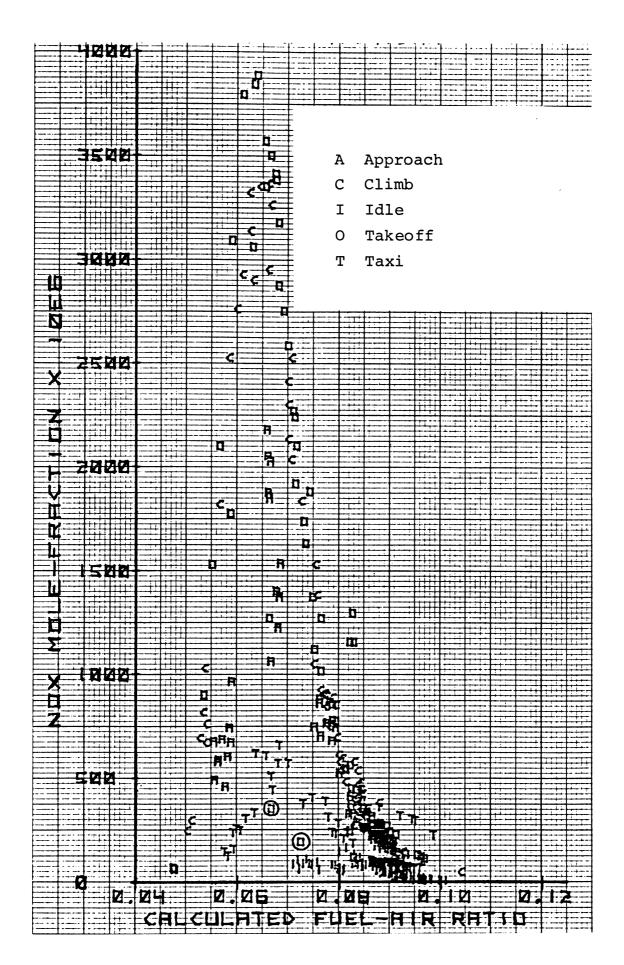


Figure 5.6. LIO-320 Lean-Out Results for: NOX (Reference 10)

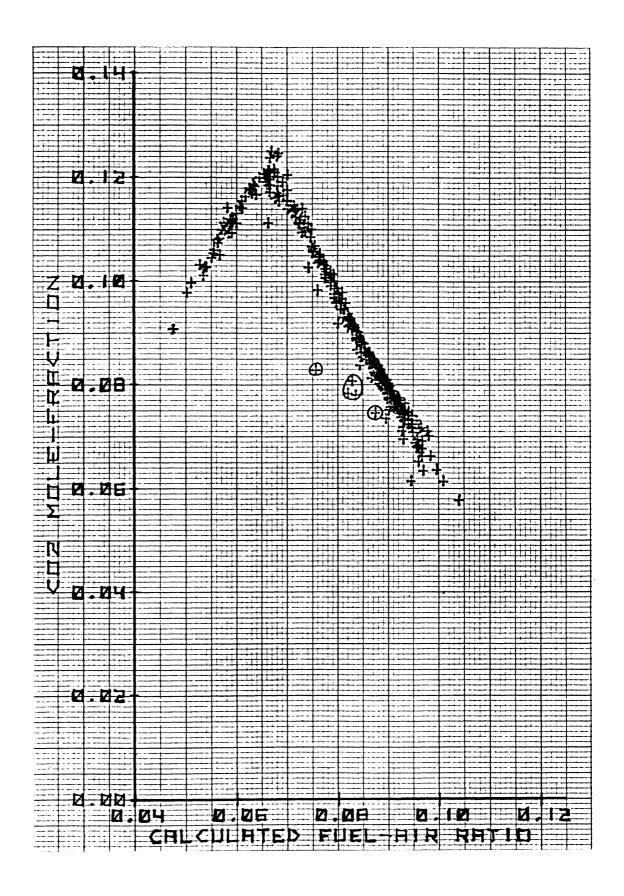


Figure 5.7. LIO-320 Lean-Out Results for CO2 (Reference 10)

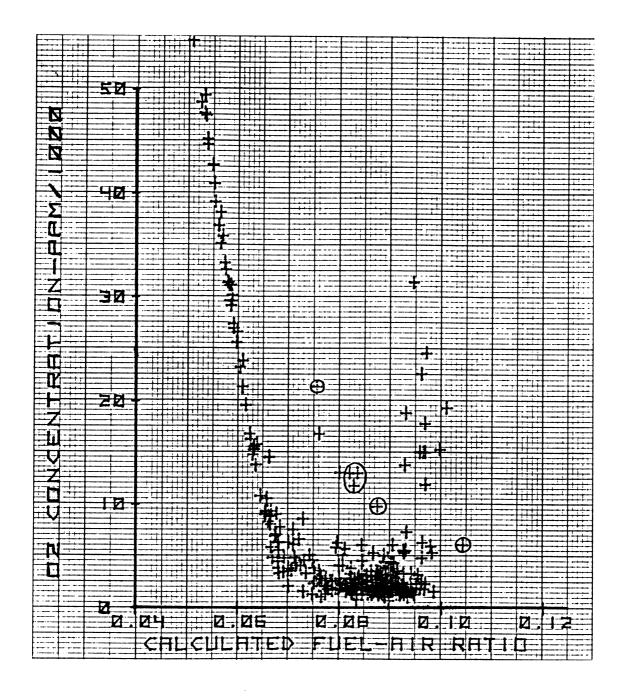


Figure 5.8. LIO-320 Lean-Out Results for O2 (Reference 10)

TABLE 5.5. COMPUTER PRINTOUT: LEAN-OUT RESULTS, MODE 2.

DATE: 12/11/75 ENGINE TYPE: LIO-320-B1A FUEL H/C RATIO = 2.180 LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG OPERATORS: PACE, GRIFFIN, DRAXLER

```
RUN NO. 24
       22
MODE:
COMMENTS: LEAN OUT TESTS-TAXI MODE
TEMP(DB) = 95.93F
                         FUEL RATE=
                                         8. 9847#/HR
                                                        ENGINE RPM(NOM)=1207 RPM
             = 36.00F
TEMP(DP)
                           AIR RATE = 112.0691#/HR
                                                        ENGINE RPM(ACT)=1206, RPM
TEMP(BAR)
             = 76.00F
                           F/A RATIO= 0.0801#/#
                                                                     = 8. OHP
= 0. OHP
                                                         BHP (OBS)
BAR PRESS(OB) = 29.34"HG
                           PHIM
                                   =
                                         1. 2051
                                                         BHP (CORR)
BAR PRESS(CR)= 29. 21"HG
                                                        MAN VAC(OBS) =18, 20"HG
SPEC HUMIDITY=0.0045#/#
                                                        MAN PRESS(CORR) = 0.00"HG
                                            UHCC
                      002
                                 02
                                                      CO
                                                                NO
                                                                           NOX
CONC (PPM)
                     102873...
                                 16986.
                                           6000.
                                                      55262.
                                                                 387
                                                                            387.
                  KWD XTC
                                 MWEXH EXH FLOW
                                                     FACAL
                                                                 FAM ERROR
METHOD 1. 2 0. 86407 1. 04070 27. 63261 1688. 718 0. 07625 0. 08017 -4. 882
MASS/MODE(LBM) 3.63719 0.43650
MASS/RATED HP(#/HP) 0.02273 0.00273
                                         0. 06668
                                                   1. 24210
                                                               0.00933 0.01428
                                         0. 00042
                                                    0.00776
                                                               0. 00006
                                                                         0.00008
                                         EXH FLOW FACAL FAM ERROR 1739.169 0.08637 0.08017 7.731
                KWD XTC
                               MWEXH EXH FLOW
                                                               FAM ERROR
            0. 90621 1. 00000 26. 83102
METHOD 2, 1
                                                   1. 27921 0. 00961
MASS/MODE(LBM)
MASS/MODE(LBM) 3. 74585
MASS/RATED HP(#/HP) 0. 02341
                                         0. 06868
                               0. 44954
                                                                         0.01470
                                0.00281
                                         0.00043
                                                    0.00799
                                                               0.00006
                                                                         0.00009
                                         EXH FLOW FACAL FAM ERROR 1652.189 0.06847 0.08017-14.595
                  KWD
                       XTC:
                                MWEXH
                                                               FAM ERROR
METHOD 3.1
              0. 88191 0. 97848 28. 24356
                                                   1. 21523
MASS/MODE(LBM) 3. 55851 0. 42705
MASS/RATED HP(#/HP) 0. 02224 0. 00267
                                          0.06524
                                                               0.00913
                                                                         0.01397
                                                   0. 00759
FACAL
                               0.00267
                                                               0.00006
                                          0.00041
                                                                         0.00008
                 KWD XTC
                                MWEXH
                                         EXH FLOW
                                                                FAM ERROR
                                                   0. 07979 0. 08017 -0. 473
METHOD 3. 2
              0. 86428 0. 30780 27. 50000
                                         1696, 862
                                                   1. 24809 0. 00937
MASS/MODE(LBM)
                   3, 65473 0, 43860
                                          0. 06700
                                                                         0.01435
MASS/RATED HP(#/HP) 0.02284
                               0.00274
                                          0.00042
                                                               0.00006
                                                    0.00780
                                                                         0.00009
RUN NO. 24
MODE:
COMMENTS: TAXI MODE-, 5 IN. LEANED
TEMP(DB) = 96.62F FUEL RATE=
                                         8.8679#/HR
                                                         ENGINE RPM(NOM)=1204 RPM
TEMP(DP)
             = 36,00F
                                                         ENGINE RPM(ACT)=1197. RPM
                           AIR RATE = 108.7265#/HR
                                                                  . = 8. OHP
            = 76.00F
                           F/A RATIO= 0.0815#/#
TEMP (BAR)
                                                         BHP(OBS)
                                                                        = 0. OHP
BAR PRESS(OB)= 29.34"HG
                                                         BHP (CORR)
                            PHIM =
                                         1, 2259
                                                         MAN VAC(OBS) =18.30"HG
BAR PRESS(CR)= 29, 21"HG
SPEC HUMIDITY=0.0045#/#
                                                         MAN PRESS(CORR) = 0.00"HG
                       002
                                 02
                                            UHCC
                                                      CO
                                                                 NO NOX
                                                      54562.
CONC (PPM)
                                 16357.
                     101772
                                            5700.
                                                                 412.
                                                                            412
                  KWD XTC
                                 MWEXH EXH FLOW
                                                     FACAL
                                                                 FAM ERROR
METHOD 1. 2 0. 86542 1. 02855 27. 63574
                                         1640, 272
                                                   0. 07626 | 0. 08156 | -6. 499
```

TABLE 5.5. Continued

```
RUN NO. 24
                22
MODE:
COMMENTS: TAXI MODE-1 IN. LEANED
                                                                                                               ENGINE RPM(NOM)=1195 RPM
TEMP(DB) = 97.40F FUEL RATE= 8.5837#/HR
TEMP(DP)
                         = 36, 00F
                                                      AIR RATE = 105 8810#/HR
                                                                                                                ENGINE RPM(ACT)=1188. RPM
                     = 76.00F
                                                                                                               BHP(OBS) = 7.9HP

BHP(CORR) = 0.0HP
TEMP(BAR)
                                                    F/A RATIO= 0.0810#/#
                                                                  =
BAR PRESS(OB)= 29.34"HG
                                                    PHIM
                                                                                 1. 2186
BAR PRESS(CR)= 29, 21"HG
                                                                                                               MAN VAC(OBS)
                                                                                                                                           =18.40"HG
SPEC HUMIDITY=0. 0045#/#
                                                                                                               MAN PRESS(CORR)= 0.00"HG
                                                                                                                                                 NOX
                                            002
                                                                  02
                                                                                      UHCC
                                                                                                           CO NO
| 10243. | 6300. | 54911. | 375. | 375. | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. | | 375. |
                              MP) 0.02149 0.00277 0.00041 0.00729 0.00005 0.0 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0.91088 1.00000 26.75163 1649.384 0.08710 0.08106 7.443
KWD XTC MWEXH
METHOD 2. 1 0. 91088 1. 00000 26. 75163
                                                                                 0. 06839 1. 20548 0. 00882 0 01349
0. 00043 0. 00753 0. 00006 0. 00008
MASS/MODE(LBM) 3.55247 0.45791
MASS/RATED HP(#/HP) 0.02220 0.00286
                                                             0. 00286
                                                              MWEXH EXH FLOW FACAL FAM ERROR
28.31651 1558.233 0.06729 0.08106-16.987
                                 KWD XTC
                                                                                                                           FAM ERROR
METHOD 3. 1
                            0. 88390 0. 97621 28. 31651
MASS/MODE(LBM) 3.35615 0.43260
MASS/RATED HP(#/HP) 0.02098 0.00270
                                                                                 0, 06461 1, 13886 0, 00833 0, 01275
                                                                                 0.00040 0.00711 0.00005 0.0
EXH FLOW FACAL FAM ERROR
1604.499 0.07979 0.08106 -1 571
                              HP) 0.02098 0.00270
KWD XTC MWEXH
                                                                                                                                            0. 00008
                                                                                                                            FAM ERROR
METHOD 3. 2 0. 86439 0. 30756 27. 50000
MASS/MODE(LBM) 3.45580 0.44545
MASS/RATED HP(#/HP) 0.02160 0.00278
                                                                                 0. 06653
                                                                                                     1, 17268 0, 00858 0, 01313
                                                                                                                            0.00005 0.00008
                                                                                0.00042
                                                                                                     0. 00732
RUN NO. 24
MODE: #2
COMMENTS: TAXI MODE-1, 5 IN. LEANED
                                                                                                               ENGINE RPM(NOM)=1207 RPM
 TEMP(DB) = 98.05F FUEL RATE= 8.4364#/HR
                                                                                                             ENGINE RPM(ACT)=1188. RPM
                         = 36, 00F
                                                      AIR RATE = 107.0497#/HR
 TEMP(DP)
                     = 76. OOF
                                                     F/A RATIO= 0.0788#/#
 TEMP(BAR)
                                                                                                                BHP(OBS) = 8.2HP
                                                                                                                BHP(CORR) = 0.0HP
MAN VAC(OBS) = 18.50"HG
 BAR PRESS(OB) = 29.34"HG
                                                    PHIM = 1.1846
 BAR PRESS(CR)= 29, 21"HG
                                                                                                                MAN PRESS(CORR) = 0.00"HG
 SPEC HUMIDITY=0.0045#/#
                                                                                  UHCC
6750.
                                                                                                            CO NO NOX
                                              002
                                                                  02
 CONC (PPM)
                                                                20132.
                                                                                                          53868.
                                                                                                                                 375.
                                                                                                                                                     387
                                           102322.
                                                                                 EXH FLOW FACAL FAM ERROR
1609, 869 0, 07532 0, 07880 -4, 416
0, 07152 1, 15426 0, 00861 0, 01361
0, 00045 0, 00721 0, 00005 0, 00008
                                    KWD
                                                                  MWEXH EXH FLOW
                                                XTC
 METHOD 1, 2 0, 86502 1, 04606 27, 65285
MASS/MODE(LBM) 3.44878 0.49317
MASS/RATED HP(#/HP) 0.02155 0.00308
                                                               MWEXH EXH FLOW FACAL FAM ERROR
26.74348 1664.610 0.08671 0.07880 10.027
0.50994 0.07395 1.19351 0.00890 0.01407
                     KWD XTC
                           0. 91302 1. 00000 26. 74348
 METHOD 2. 1
MASS/MODE(LBM) 3.56605 0.50994
MASS/RATED HP(#/HP) 0.02229 0.00319
                                                                                 /HP) 0.02229 0.00319
KWD XTC MWEXH
                                                                                                                                                0.00008
                                                                                EXH FLOW
 METHOD 3 1 0.88531 0.97561 28.34837
                                                                                 0. 06976 1. 12594 0. 00840 0. 01328
0. 00044 -0. 00703 0. 00005 0. 00008
 MASS/MODE(LBM) 3.36417 0.48107
MASS/RATED HP(#/HP) 0.02103 0.00301
                                                                                 EXH FLOW FACAL FAM ERROR 1618, 817 0.07927 0.07880 0.594
                                  KWD XTC MWEXH
                           0.86526 0.30551 27.50000
 METHOD 3, 2
                                                                                 0.07191
                                                                                                     1, 16067 0 00865 0, 01369
 MASS/MODE(LBM) 3. 46795 0. 49591
                                                                                                                            0.00005
                                                                                                      0.00725
                                                                                                                                                0.00008
 MASS/RATED HP(#/HP) 0.02167
                                                             0.00310
                                                                                 0.00045
```

TABLE 5.5. Continued

	7. 8575#/HR ENGINE RPM(NOM)=1203 RPM 108. 6463#/HR ENGINE RPM(ACT)=1171. RPM 0. 0723#/# BHP(OBS) = 7. 7HP 1. 0871 BHP(CORR) = 0. 0HP MAN VAC(OBS) =18. 30"HG MAN PRESS(CORR)= 0. 00"HG
CO2 O2	UHCC CO NO NOX
CONC(PPM) 102873. 33973.	8250. 38085. 412. 450.
KWD XTC MWEXH	EXH FLOW FACAL FAM ERROR
METHOD 1, 2 0, 87134 1, 04769 27, 92587	1608, 177 O. 06837 O. 07232 ~5, 45 5
MASS/MODE(LBM) 3. 46372 - 0. 83136	0. 08732 0. 81520 0. 00946 0. 01579
MASS/RATED HP(#/HP) 0.02165 0.00520	0. 00055 0. 00509 0. 00006 0. 00009
MASS/HP/CYC(#/HP/C) 0.10927 0.01633	0, 00221 0, 03481 0, 00028 0, 00045
KWD XTC MWEXH	EXH FLOW FACAL FAM ERROR
METHOD 2. 1 0. 92138 1. 00000 27. 01570	1662, 357 0, 07881 0, 07232 8, 983
MASS/MODE(LBM) 3, 58041 0, 85936	0, 09026 0, 84266 0, 00978 0, 01632
MASS/RATED HP(#/HP) 0.02238 0.00537	0, 00056 0, 00527 0, 00006 0, 00010
MASS/HP/CYC(#/HP/C) 0.11257 0.01683	
KWD XTC MWEXH	EXH FLOW FACAL FAM ERROR
METHOD 3, 1 0, 89300 0, 97519 28, 64545	1567, 779 0, 05924 0, 07232-18, 088
MASS/MODE(LBM) 3. 37671 0. 81047	0. 08512
MASS/RATED HP(#/HP) 0.02110 0.00507	0, 00053
MASS/HP/CYC(#/HP/C) 0.10686 0.01596	
KWD XTC MWEXH	
METHOD 3, 2 0, 87160 0, 28186 27, 50000	
MASS/MODE(LBM) 3.51736 0.84423	
MASS/RATED HP(#/HP) 0.02198 0.00528	
MASS/HP/CYC(#/HP/C) 0.11005 0.01647	0. 00222 0. 03504 0. 00029 0. 00045

```
TABLE 5.6. COMPUTER PRINTOUT: LEAN-OUT RESULTS, MODE 3.

12/22/75 ENGINE TYPE: LIO-320-B1A FUEL H/C RATIO = 2.180
```

IGNITION TIMING= 25DEG

LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A

OPERATORS: PACE, GRIFFIN, PONSONBY **RUN NO. 28** MODE: COMMENTS: LEAN OUT, TAKEOFF, FULL RICH = 89.84F FUEL RATE= 75.8533#/HR ENGINE RPM(NOM)=2700 RPM TEMP(DB) AIR RATE = 868. 2720#/HR ENGINE RPM(ACT)=2702. RPM = 15.00F TEMP(DP) F/A RATIO= 0.0873#/# =140. 7HP = 76. 00F BHP(OBS) TEMP(BAR) BAR PRESS(OB)= 29.31"HG = 1. 3131 BHP (CORR) =156, 2HP PHIM = 1. 20"HG MAN VAC(OBS) BAR PRESS(CR)= 29.18"HG MAN PRESS(CORR)=29, 22"HG SPEC HUMIDITY=0. 0015#/# NO NOX CO UHCC C02 02 88666. 93400. 1507. 1169. 255. CONC (PPM) MWEXH EXH FLOW FAM ERROR FACAL XTC KWD 0. 08675 0. 08736 -0. 690 METHOD 1, 2 0, 86331 1, 04202 27, 10544 13426, 840 MASS/MODE(LBM) 0. 71607 MASS/RATED HP(#/HP) 0. 00448 0.00839 0.00282 0. 43215 0.00133 0.00204 0.00005 0.00002 0.00270 0.00000 0.00001FACAL XTC MWEXH EXH FLOW FAM ERROR KWD 0. 90663 1. 00000 26. 21115 13884. 940 0. 09929 0. 08736 13. 663 MASS/MODE(LBM) 0. 74050 0. 00868 0. 00291 MASS/RATED HP(#/HP) 0. 00463 0. 00005 0. 00002 0.44690 0.00138 0.00211 0. 00279 0.00000 0.00001 MWEXH EXH FLOW FACAL FAM ERROR KWD XTC 0.07835 0.08736-10 307 METHOD 3. 1 0. 88056 0. 97680 27. 74921 13115. 340 MASS/MODE(LBM) 0.69946 0.00820 MASS/RATED HP(#/HP) 0.00437 0.00005 0.00130 0.00199 0.00275 0.42213 0.00000 0.00264 0.00001 0.00002 FACAL FAM ERROR 0.09103 0.08736 4 201 KWD XTC MWEXH EXH FLOW 0. 86337 0. 34037 27. 50000 13234 190 METHOD 3 2 MASS/MODE(LBM) 0.70580 0.00827 MASS/RATED HP(#/HP) 0.00441 0.00005 0 42595 0.00278 0.00131 0 00201 0.00266 0 00000 0.00001 0.00002 RUN NO. 28 MODE: COMMENTS: TAKEOFF, . 75 IN. LEAN ENGINE RPM(NOM)=2700 RPM FUEL RATE= 65. 6455#/HR TEMP(DB) = 90.71FENGINE RPM(ACT)=2695, RPM TEMP(DP) = 15.00F AIR RATE = 860. 6604#/HR F/A RATIO= 0.0762#/# =140. 7HP BHP(OBS) = 76.00F TEMP (BAR) = BAR PRESS(OB) = 29.31"HG PHIM 1.1465 BHP (CORR) =155. 7HP BAR PRESS(CR)= 29.18"HG MAN VAC(OBS) = 1.30"HGMAN PRESS(CORR)=28.99"HG SPEC HUMIDITY=0.0015#/# UHCC CO NO C02 02705. 49810. 705 1884. 874. CONC (PPM) KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0.85606 1.05295 27.88744 12804.020 0.07637 0.07627 0.33 METHOD 1 2 MASS/MODE(LBM) 0.87716 0.01001 0.00201 0. 23151 0. 00351 0 00537 0. 00002 0.00145 0 00003 MASS/RATED HP(#/HP) 0.00548 MASS/HP/CYC(#/HP/C) 0.00995 0. 00006 0.00001 0995 0.00012 0.00003 XTC MWEXH EXH FLOW 0.00415 0.00003 0.00005 FACAL FAM ERROR KWD 0. 91085 1 00000 26, 84024 13303, 580 0. 09002 | 0. 07627 | 18. 030 METHOD 2.1 .0. 24054 0. 00365 0. 00558 0: 00209 MASS/MODE(LBM) 0.91138 MASS/RATED HP(#/HP) 0.00570 MASS/HP/CYC(#/HP/C) 0.01032 0. 01040 0.00001 0.00006 0.00150 0.00002 0.00003 0.00430 0 00003 0.00005 0.00012 0.00003 FACAL FAM ERROR 0.06668 0.07627-12.572 KWD MWEXH EXH FLOW XTC 0. 87941 0. 97212 28. 69218 12444 890 METHOD 3. 1 0. 22501 0 00341 0.00195 0 00522 0. 85255 MASS/MODE(LBM) 0.00973 0.00003 0.00001 0. 00533 0.00141 0.00002 MASS/RATED HP(#/HP) 0. 00006 0.00003 MASS/HP/CYC(#/HP/C) 0.00970 0. 00404 0.00003 0.00005 0.00011 FACAL FAM ERROR 0.08093 0.07627 6.115 MWEXH EXH FLOW KWD XTC 0. 85614 0. 31590 27 50000 12984. 410 METHOD 3 2 0. 00356 0.00544 0. 23477 MASS/MODE(LBM) 0.88951 0.01015 0.00204 0.00001 0.00147 0.00002 0.00003 MASS/RATED HP(#/HP) 0.00556 0.00006 0.00005 MASS/HP/CYC(#/HP/C) 0.00997 0 00012 0.00003 0.00413 0.00003

TABLE 5.7. COMPUTER PRINTOUT: LEAN-OUT RESULTS, MODE 4.

ENGINE TYPE LI0-320-B1A FUEL H/C RATIO = 2.18012/19/75 LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG OPERATORS: PACE, PONSONBY, GRIFFIN

```
MODE:
COMMENTS: LEAN OUT, CLIMBOUT, FULL RICH
                           FUEL RATE= 56. 0224#/HR
                                                           ENGINE RPM(NOM)=2419 RPM
TEMP(DB)
            = 82.80F
              = 23.00F
                             AIR RATE = 672. 9324#/HR
                                                           ENGINE RPM(ACT)=2451. RPM
TEMP(DP)
                                                           BHP(OBS)
                                                                           =110.8HP
TEMP(BAR)
             = 72.00F
                             F/A RATIO=
                                           0.0832#/#
                             PHIM
                                           1. 2513
                                                           BHP (CORR)
                                                                           = 0. OHP
BAR PRESS(OB) = 29.32"HG
                                                                          = 3.50"HG
BAR PRESS(CR)= 29. 21"HG
                                                           MAN VAC(OBS)
                                                           MAN PRESS(CORR)= 0.00"HG
SPEC HUMIDITY=0.0025#/#
                        C02
                                              UHCC
                                                         CO
                                                                   NO
                                                                              NOX
                                   02
                                                                    386.
CONC (PPM)
                       97445.
                                   3140.
                                              1121.
                                                        76223.
                                                                                386
                                                                    FAM ERROR
                          XTC
                                   MWEXH EXH FLOW
                                                        FACAL
                   KWD
                                                      0. 08324 0. 08325 -0. 004
             0, 86325 1, 02568 27, 31596 10286, 900
METHOD 1.2
                                                                             0. 03937
MASS/MODE(LBM) 9. 53961
MASS/RATED HP(#/HP) 0. 05962
                                            0.03451
                                                       4. 74380
                                                                  0. 02574
                                 0. 22341
                                 0 00140
                                            0.00022
                                                       0. 02965
                                                                  0.00016
                                                                             0.00025
                                                      FACAL FAM ERROR
0. 09025 0. 08325 8. 407
4. 83639 0. 02624 0. 04014
                   KWD
                          XTC
                                   MWEXH EXH FLOW
               0.88931 1.00000 26 79305 10487.670
METHOD 2.1
MASS/MODE(LBM) 9. 72579
MASS/RATED HP(#/HP) 0. 06079
                                            0.03518
                                 0. 22777
                                            0.00022
                                                       0. 03023
                                                                  0.00016
                                                                             0.00025
                                 0.00142
                                                      FACAL FAM ERROR
0. 07825 0. 08325 -6. 000
                                                       FACAL
                                  MWEXH EXH FLOW
                  KWD XTC
               0.87398 0.98615 27.70000 10144.280
METHOD 3 1
                                                      4 67803 0. 02538
                                 0. 22032
                                                                             0.03882
                     9 40735
                                            0. 03403
MASS/MODE(LBM)
                                                                  0.00016
MASS/RATED HP(#/HP) 0.05880
                                            0.00021
                                                       0.02924
                                                                             0 00024
                                 0.00138
                                                      FACAL FAM ERROR
0.08571 0.08325 2.965
                  KWD
                                  MWEXH EXH FLOW
                          XTC
METHOD 3 2
               0, 86332 0, 32672 27, 50000 10218, 060
                     9. 47577
                                            0. 03428 4. 71206 0. 02557
                                                                             0 03910
                                 0 22192
MASS/MODE(LBM)
                                                                             0.00024
MASS/RATED HP(#/HP) 0.05922
                                 0.00139
                                            0.00021
                                                       0. 02945
                                                                  0.00016
RUN NO. 27
MODE:
COMMENTS: LEAN OUT, CLIMBOUT, 1 IN. LEAN
TEMP(DB)
           = 87.83F
                          FUEL RATE= 46.8018#/HR
                                                           ENGINE RPM(NOM)=2423 RPM
                                                           ENGINE RPM(ACT)=2378 RPM
             = 23, 00F
                             AIR RATE = 663.4822#/HR
TEMP(DP)
                                                                        =106 2HP
                             F/A RATIO= 0 0705#/#
                                                           BHP (OBS)
TEMP(BAR)
             = 72, 00F
                                                           BHP (CORR)
                                                                            = 0. OHP
BAR PRESS(OB)= 29.32"HG
                                      =
                                           1 0603
                             PHIM
                                                           MAN VAC(OBS) = 3 30"HG
BAR PRESS(CR)= 29, 21"HG
                                                           MAN PRESS(CORR) = 0 00"HG
SPEC HUMIDITY=0 0025#/#
                                              UHCC
                                                         CO
                                                                    NO
                                                                               NOX
                        C02
                                    02
CONC (PPM)
                       132928.
                                    3768.
                                               728.
                                                        19990.
                                                                    1565.
                                                                               1565
                                                                    FAM ERROR
                                           EXH FLOW
                                                        FACAL
                   KWD
                           XTC
                                    MWEXH
                                           9647, 734
                                                      0.06946 0.07054 -1 519
METHOD 1, 2
              0 85878 1 02230 28 37965
                                 0. 25144
                                                                 0.09791
                                            0.02101
                                                                             0.14976
MASS/MODE(LBM) 12. 20466
MASS/RATED HP(#/HP) 0. 07627
MASS/MODE(LBM)
                                                       1. 16680
                                            0.00013
                                                       0.00729
                                                                  0.00061
                                                                             0.00090
                                 0 00157
                                                      FACAL FAM ERROR
0.07423 0.07054 5.238
                   KWD
                            XTC
                                    MWEXH
                                           EXH FLOW
               0 88114 1 00000 27 98036
                                           9785, 414
MASS/MODE(LBM) 12.37883
MASS/RATED HP(#/HP) 0.07736
                                 0. 25503
                                            0 02131
                                                       1. 18345
                                                                 0. 09931
                                                                             0 15190
                                 0.00159
                                            0.00013
                                                       0.00739
                                                                  0.00062
                                                                             0.00094
                                                       FACAL
                                                                   FAM ERROR
                                           EXH FLOW
                   KWD XTC
                                    MWEXH
               0 86891 0.98881 28 70715
                                           9507 672
                                                      0.06559 0.07054 -7.009
METHOD 3 1
MASS/MODE(LBM) 12 06543
MASS/RATED HP(#/HP) 0.07540
                                            0. 02077
                                                       1. 15349
                                                                             0.14806
                                 0. 24857
                                                                  0. 09679
                                                                  0.00060
```

0 00155

0. 25948

0.00162

MWEXH

KWD XTC

12 59506

METHOD 3, 2

MASS/MODE(LBM)

MASS/RATED HP(#/HP) 0.07871

0.85885 0.28830 27.50000

0.00013

0.02168

0 00014

EXH FLOW 9956 344 0.00720

FACAL

1. 20412

0.00752

0.00092

0. 15455

0 00096

FAM ERROR

0.10105

0.00063

0.07116 0.07054 0.892

TABLE 5.7. Continued

RUN NO. 27 MODE: 4 COMMENTS: LEAN OUT, CLMBOUT, 1, 25 IM. LEAN = 89. **4**9F TEMP(DB) TEMP(DP) = 23.00F F/A RATIO= 0.0660#/# = 72.00F TEMP(BAR) BHP(OBS) =105.1HP PHIM = 0.9928 BHP(CORR) = 0.0HP MAN VAC(OBS) = 2.50"HGBAR PRESS(OB) = 29.32"HG BAR PRESS(CR)= 29, 21"HG SPEC HUMIDITY=0. 0025#/# MAN PRESS(CORR) = 0.00"HG CO 002 LIHCC 02NΩ NOX CONC (PPM) 13816. 331. 4752. 2307. KWU XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 1.2 0.86382 1.02799 28.65352 3877.184 0.06320 0.06605 -4.301 MASS/MODE(LBM) 12.86614 0.94387 0.00976 0.28396 0.14772 0.2 MASS/RATED HP(#/HP) 0.08041 0.00500 0. 28396 0. 14772 0. 23028 MASS/RATED HP(#/HP) 0. 08041 MASS/HP/CYC(#/HP/C) 0. 21631 0. 00590 0 00006 0. 00177 0.00092 0.00144 0. 03872 0.00170 /C) 0.21631 0.00886 0.00041 KWD XTC MWEXH EXH FLOW 0.00262 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 2. 1 0 89220 1.00000 28.16641 10048.000 0.06862 0.06605 3 901 MASS/MODE(LBM) 13.08864 0.96019 0.00993 MASS/RATED HP(#/HP) 0.08180 0.00600 0.00006 MASS/HP/CYC(#/HP/C) 0.21996 0.00901 0.00042 KWD XTC MWEXH EXH FLOW 0. 28887 0. 15028 0. 2342¢ 0.00181 0.00093 0 00146 0. 03943 0. 00172 0. 00266 FACAL FAM ERROR 0. 87687 0. 98613 29. 06889 9736, 043 0, 05834 0, 06605-11 675 METHOD 3, 1 0. 27991 0. 14561 0 22639 0. 00175 0. 00091 0. 00142

 MASS/MODE(LBM)
 12.68229
 0.93038

 MASS/RATED HP(#/HP)
 0.07926
 0.00581

 MASS/HP/CYC(#/HP/C)
 0.21347
 0.00874

 0. 00962 0. 00581 0. 00006 0. 00874 0. 00167 0. 00259 0. 00040 0. 03820 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0.86391 0.26934 27.50000 10291.490 0.06512 0.06605 -1 404 METHOD 3 2 0. 29587 0. 15392 0 23994 MASS/MODE (I.BM) 13. 40582 0. 98346 0. 01018 0. 00150 0. 00096 MASS/RATED HP(#/HP) 0.08378 0 00615 0. 00006 0. 00185 0 00041 0. 03883 0.00175 0 00271 MASS/HP/CYC(#/HP/C) 0. 22173 0.00915

TABLE 5.8. COMPUTER PRINTOUT: LEAN-OUT RESULTS, MODE 5.

DATE 12/17/75 ENGINE TYPE: LIO-320-B1A FUEL H/C RATIO = 2.180 LOCATION: UNIV OF MICH SERIAL NUMBER. L-287-66A IGNITION TIMING= 25DEG IGNITION TIMING= 25DEG OPERATORS: PACE, PONSONBY, GRIFFIN, DRAXLER COMMENTS: LEAN OUT RUN, APPROACH MODE, FULL RICH ENGINE RPM(NOM)=2350 RPM FUEL RATE = 34.4827#/HR AIR RATE = 417.0754#/HR TEMP(DP) = 13.00F TEMP(BAR) = 74.00F ENGINE RPM(ACT)=2349, RPM F/A RATIO= 0.0826#/# PHIM = 1.2427 BHP(OBS) = 58 7HPBAR PRESS(OB) = 29.28"HG BHP(CORR) = 0.0HP MAN VAC(OBS) =11.10"HG BAR PRESS(CR)= 29, 16"HG SPEC HUMIDITY=0.0012#/# MAN PRESS(CORR) = 0.00"HG 0.02 02 UHCC CO NO NOX CONC (PPM) 102873. 2768. 828. 71083 425. 425 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0.87737 0.98020 28.02197 6211.770 0.07447 0.08267 -9.925 METHOD 3 1 MASS/MODE(LBM) 7. 29764 0. 14272 0. 01846 3. 20567 0. 02056 0. 03145 MASS/RATED HP(#/HP) 0. 04561 0. 00089 0. 00012 0. 02004 0. 00013 0. 00020 MASS/RATED HP(#/HP) 0.04561 0.00089 0.00012 0.02004 0.00013 0.0 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR METHOD 3.2 0.86183 0.32472 27.50000 6329,676 0.08497 0.08267 2.776 0.00013 FAM ERROR MASS/MODE(LBM) 7. 43616 0. 14543 0. 01881 MASS/RATED HP(#/HP) 0. 04648 0. 00090 0. 00012 3. 26651 0 02095 0 03205 0. 02042 0. 00013 0. 00020 MODE: 5 COMMENTS: LEAN OUT RUN, APPROACH, 1 IN. LEAN TEMP(DB) = 87 74F FUEL RATE= 29.6296#/HR ENGINE RPM(NOM)=2350 RPM
TEMP(DP) = 13.00F AIR RATE = 414.9094#/HR ENGINE RPM(ACT)=2370. RPM
TEMP(BAR) = 74.00F F/A RATIO= 0.0714#/# BHP(OBS) = 59.2HP F/A RATIO= 0.0714#/# PHIM = 1.0734 BHP(OBS) = 59. 2HP BAR PRESS(OB) = 29, 28"HG BHP(CORR) = 0.0HP MAN VAC(OBS) =10.90"HG BAR PRESS(CR)= 29.16"HG SPEC_HUMIDITY=0.0012#/# MAN PRESS(CORR)= 0 00"HG CO NO NOX 16253. 1042 1071 002 02 UHCC CONC(PPM) 3775. 1042 132928 730. 16253. FAM ERROR KWD XTC MWEXH EXH FLOW FACAL METHOD 1 ? 0.86235 1 00651 28.45932 6021.238 0.06881 0.07141 -3 634 MASS/MODE(LBM) 9 14044 0. 18865 MASS/RATED HP(#/HP) 0. 05713 0. 00118 0.01578 0 71048 0 04883 0 07673 0 00444 0 00031 0 00048 0 00009 0.00118 KWD XTC FACAL FAM ERROR 0.07014 0.07141 1 770 MWEXH EXH FLOW METHOD 2. 1 0. 86876 1. 00000 28 34541 6045. 434 MASS/MODE(LBM) 9. 17717 0. 18941 0 01584 MASS/RATED HP(#/HP) 0. 0573/ 0. 00118 0. 00009 0. 71334 0. 04909 0. 07704 0. 00446 0. 00031 0. 00048 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0 86529 0.99677 28.55357 6001.363 0.06770 0.07141 -5.198 KWD XTC MWEXH EXH FLOW METHOD 3. 1 MASS/MODE(LBM) 9.11027 0.18803 MASS RATED HP(#/HP) 0.05694 0.00118 0 01573 0. 70814 0. 04867 0. 07648 ‡/ḤP) 0.05694 0.00118 KWD XTC MWEXH 0.00009 0.00443 0 00030 0.00048 FACAL FAM ERROR 0.06930 0.07141 -2.949 EXH FLOW METHOD 3, 2 0. 86235 0. 28093 27. 50000 6231. 285 MASS/MODE(LBM) 9.45930 0.19523 0.01633 MAS- RATED HP(#/HP) 0.05912 0.00122 0.00010 0. 73527 0 05053 0. 07941 0. 00460 0. 00032 0. 00050

TABLE 5.8. Continued

RUN_NO. 26_	
MODE: 5	- 0.61
COMMENTS: LEAN OUT, APPROACH, 1, 25 IN. LE	
TEMP(DB) = 88.27F FUEL RATE=	28. 1955#/HR ENGINE RPM(NOM)=2355 RPM
	451. 8899#/HR
TEMP(BAR) = $74.00F$ F/A RATIO=	0. 0624#/# BHP(OBS) = 59. 1HP
BAR PRESS(OB)= 29. 28"HG PHIM =	0. 9379 BHP(CORR) = 0. OHP
BAR PRESS(CR)= 29.16"HG	MAN VAC(OBS) = 9.60"HG
SPEC HUMIDITY=0.0012#/#	MAN PRESS(CORR)= 0.00"HG
CO2 O2	UHCC CO NO NOX
CONC(PPM) 134208. 20132.	
KWD XTC MWEXI	
METHOD 1, 2 0, 86914 1, 02540 28, 7236	
MASS/MODE(LBM) 9.87467 1.0765	
MASS/RATED HP(#/HP) 0.06172 0.0067	·
MASS/HP/CYC(#/HP/C) 0.16538 0.0088	
KWD XTC MWEX	
METHOD 2. 1 0. 89494 1. 00000 28. 2835	
MASS/MODE(LBM) 10.02832 1.0933	
MASS/RATED HP(#/HP) 0.06267 0.0068	
MASS/HP/CYC(#/HP/C) 0.16787 0.0089	
KWD XTC MWEX	
METHOD 3 1 0.88103 0.98744 29 1012	
MASS/MODE(LBM) 9, 74655 1, 0626	
MASS/RATED HP(#/HP) 0.06092 0.0066	
MASS/HP/CYC(#/HP/C) 0.16347 0.0087	
KWD XTC MWEX	
METHOD 3, 2 0 86917 0, 25933 27, 5000	
MASS/MODE(LBM) 10.31405 1.1244	
MASS/RATED HP(#/HP) 0.06446 0.0070	
MASS/HP/CYC(#/HP/C) 0.17006 0 0091	5 0,00022 0,02571 0,00084 0,00131

Unburned hydrocarbon levels are low and almost independent of fuel-air ratio at lean mixtures but increase rapidly with fuel enrichment beyond stoichiometric. The primary reason for the latter is, of course, the lack of sufficient oxygen for combustion. However, at quite high fuel-air ratio, there is poor mixing of the unburned hydrocarbons with the available oxygen and, in general, quite poor combustion. Figure 5.8 shows this effect through the high oxygen levels.

Some data points in these figures were found to be in error and are shown circled.

5.3 EFFECT OF PROBE LOCATION ON AIR-DILUTION OF EXHAUST SAMPLE

Experience in automotive emission measurement practice has shown that air dilution of the exhaust gases can extend some distance upstream from the open end of the tail pipe. Therefore, when using short, open-ended exhaust pipes during engine emission testing, care must be taken to select a probe location that will avoid sample dilution. Tests were run to determine the extent of dilution at various probe locations at the different operating modes. This was accomplished with a sliding probe which was inserted into the end of the exhaust pipe and centered in the pipe with fin guides. Any axial position could be selected by sliding the probe to the desired location.

A test was first made to compare the results from both the variable and standard fixed probes at the fixed probe position. No significant differences in results were found. Tests were then run at five probe locations, equally spaced from 2 to 32 inches from the open end of the exhaust pipe, and at each of the seven operating modes. The results are plotted in figures 5.9 and 5.10 showing both O2 concentration and calculated fuel-air ratio as a function of probe position.

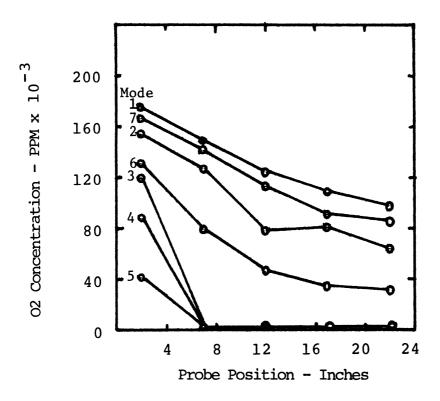


Figure 5.9. Effect of Probe Location on O2 Concentration

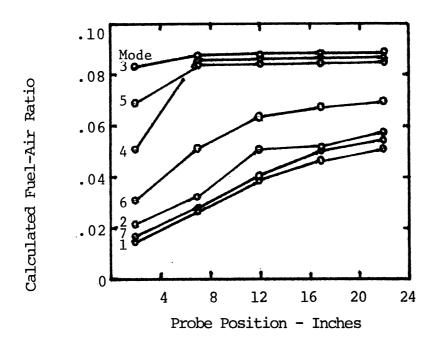


Figure 5.10. Effect of Probe Location on Calculated Fuel-Air Ratio

These results indicate that dilution is not a problem for the high power modes for probes located seven or more inches from the open end of the exhaust pipe. However, when operating at idle and taxi modes, dilution effects are detectable at distances up to and possibly beyond 22 in. The reliability of the data is indicated by the fact that the 35 data points show low values of the error parameters ΔE and XTC, as indicated below.

Number of Points	ΔE Range (Percent)	XTC Range	
31	-4.0 to 6.7	0.980 to 1.016	
4	-7.7 to 13.0	0.967 to 1.030	

The usefulness of the error parameters as indicators of data reliability should be pointed out, since the attempted use of the Spindt error would be completely useless in this test. Values of Spindt errors for the above runs ranged from -75 to 2.9%, the negative values resulting from the leaning of the mixture due to air dilution.

5.4 CHECK FOR AIR LEAKS

Two tests were run to check the gas analysis and exhaust systems for possible air leaks. This was done when the data analysis indicated consistently low values of calculated fuelair ratio from all four computational methods.

5.4.1 Leak Check of Gas Analysis System

Both the gas sampling inlet system and lines to the O2 analyzer were checked for possible air leaks. This was accomplished by first determining the normal pressure at the sampling probe during engine testing. Since this pressure is below atmospheric, any leaks in the line would cause air dilution of the sample rather than leak exhaust gas to the atmosphere. Then the line normally connected to the probe was connected to a bottle of nitrogen gas, which was then used as the sample gas while operating the instrumentation in the normal engine—test modes. A measure—ment for O2 was then recorded.

If air leaks into the system were present, some level of oxygen would be measured. A leak-tight system would be free of oxygen and a zero reading would be recorded. (Possible oxygen impurities in the nitrogen gas could give rise to very small oxygen readings.) Our tests showed practically zero values of oxygen, indicating a leak-tight system.

5.4.2 Leak Check of Engine Exhaust System

Air leaks into the exhaust system are possible because of the existence of transient negative pressures in the exhaust pipe (reference 11), especially at idle and taxi modes. Since the data analysis indicated air leakage (large negative fuel-air errors) and because the instrument check in section 5.4.1 proved negative, tests were run to check the exhaust system for leaks.

Two reference runs, one at idle and one at taxi, were made to determine the extent of exhaust gas dilution as indicated by the negative fuel/air errors. The exhaust system was then sealed at the flanges and slip joints using a high temperature exhuast system sealer. When the sealant had dried, the runs were repeated and the fuel-air errors checked (run A). Since the results showed a large decrease in errors, a complete baseline was then run (run B). The results are given in table 5.9.

TABLE 5.9. ERROR ANALYSIS OF EXHAUST SYSTEM LEAK TESTS

	<u>P</u>		
Mode	E(3.1)	E(1.2)	$\Delta \mathbf{E}$
1	-56.55	-41.78	-14.77
2	-27.28	-10.93	-16.35

	Post Seal							
Run A				Run B				
Mode	E(3.1)	E(1.2)	ΔΕ	E(3.1) E(1.2)	ΔE			
1	-12.10	-6.64	-5.46	-21.44 -10.05 -	-11.39			
2	-16.20	-4.86	-11.34	-15.98 -3.08 -	-12.90			
3			-	-3.19 1.43	-4.62			
4	_	_	_	-3.60 0.04	-3.64			
5	-		_	-7.09 -1.71	-5.38			
6	-	_	-	-15.91 -5.79	-10.12			
7	-	_	-	-26.41 -30.72	4.31			

The decrease in negative values of both E(1.2) and E(3.1) from the pre-seal to post-seal tests indicate a substantial reduction, but possibly not elimination, of air leakage into the exhaust system. The substantial increase in E(1.2) for Mode 7 was due to a sealant failure at one of the joints.

6. INTER-FACILITY DATA ANALYSIS

An analysis and correlation study of inter-facility data on the Lycoming 320 engine was run. These efforts show promise that an effective method for determining data validity has been developed.

It is obvious that before any correlations of data from the various facilities are made, the validity of the data should be established. Otherwise, wrong conclusions can be reached. For this reason, a considerable effort was undertaken at Michigan to develop a method to evaluate data validity, based on the use of fuel-air error E(1.2), ΔE and XTC. In the following section, plots of ΔE vs XTC are shown and their significance is discussed.

6.1 DATA ANALYSIS CHARTS - AE vs XTC

Preliminary data on the Lycoming 320 engine from Lycoming and Michigan and one set of 13 runs on an automotive V-8 engine from Eltinge (reference 7) are plotted to show ΔE vs XTC in figures 6.1-6.3. These charts show that the data from various sources and for different engines give straight line plots with negative slopes.

These results suggest that the best data should lie at the intersection of the $\Delta E = 0$ and XTC = 1 axes, and that the extent of departure from this point gives an indication of the errors involved. The method suggests that imposed limits on ΔE or XTC would provide one of the criteria for good data, together with a limit on E(1.2).

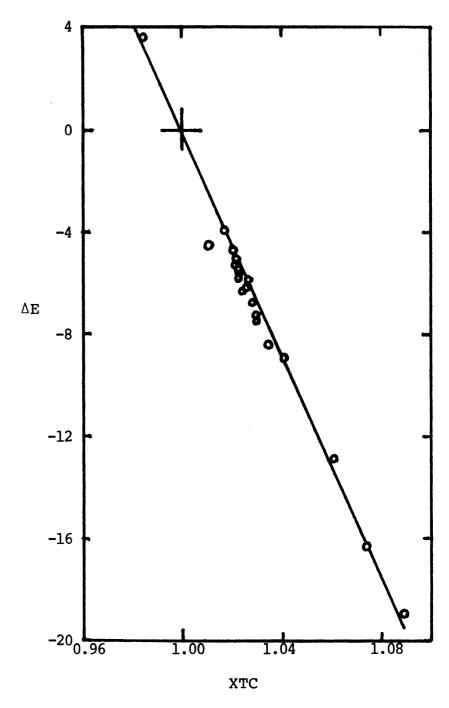
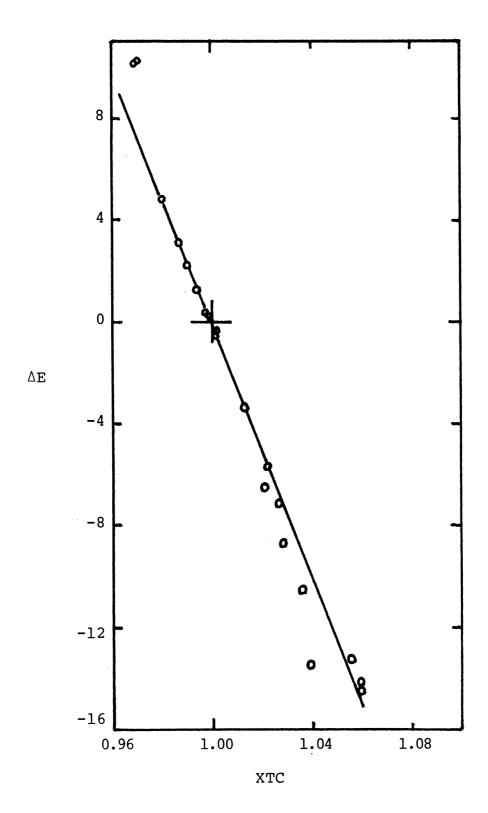


Figure 6.1. ΔE vs XTC: Lycoming Data (Reference 12)



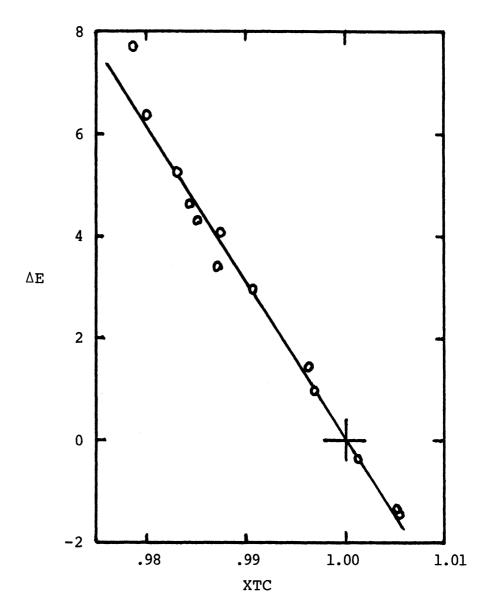


Figure 6.3. ΔE vs XTC: Eltinge Data (Reference 7)

6.2 DATA ANALYSIS CHARTS - E(1.2) vs XTC

The use of either ΔE or XTC as an indicator of data reliability appears to be optional since close correlations were found to exist as shown in section 6.1. However, ΔE requires the use of two computational methods, Method 3.1 and Method 1.2, while XTC is computed using Method 1.2. Therefore, if one selects E(1.2) and XTC as indicators of data reliability, only one computational method need be used. The use of either indicator by itself was shown in section 2.3 to be insufficient.

An examination of plots of E(1.2) vs XTC in figures 6.4 to 6.8 shows that data can be expected to fall in a band of \pm 5% for XTC and a somewhat larger band for E(1.2). Data for these plots were taken from Michigan Runs 4 and 7, given at the end of Section 5, and Run 5, given at the end of this section, together with AVCO-Lycoming data from reference 12.

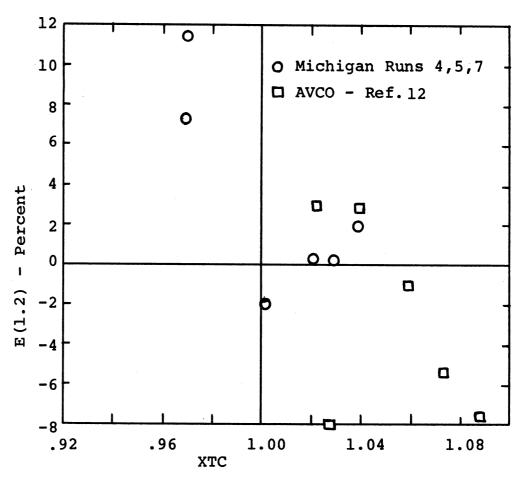


Figure 6.4. E(1.2) vs XTC: Idle Mode

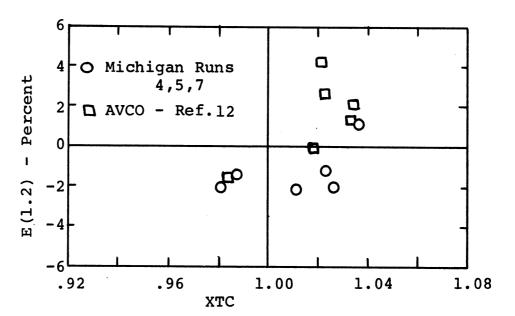


Figure 6.5. E(1.2) vs XTC: Taxi Mode

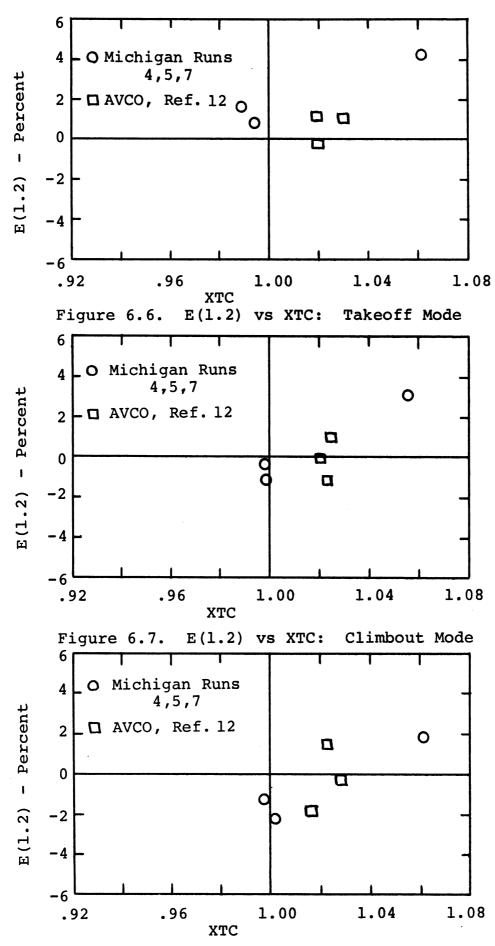


Figure 6.8 E(1.2) vs XTC: Approach Mode

TABLE 6.1 COMPUTER PRINTOUT: RUN 5

DATE: ENGINE TYPE: LIO-320-BIA FUEL H/C RATIO = 2.1908-12-75 LOCATION: UNIV OF MICH SERIAL NUMBER: L-287-66A IGNITION TIMING= 25DEG OPERATORS: PERRY, PACE, PONSONBY, LEO (UN NO. MODE: 1 COMMENTS: BASELINE DATA RUN5. 1 TEMP(DB) = 94.71FFUEL RATE= 3. 3681#/HR ENGINE RPM(NOM)= 720 RPM = 51.00F ENGINE RPM(ACT)= 712. RPM AIR RATE = 64. 1414#/HR TEMP(DP) = 81.00F 0. 0525#/# BHP (OBS) = 0.2HP TEMP(BAR) F/A RATIO= = 0. OHP BHP (CORR) BAR PRESS(OB) = 29. 24"HG MAN VAC(OBS) =17. 50"HG BAR PRESS(CR)= 29.10"HG SPEC HUMIDITY=0 0081#/# MAN PRESS(CORR) = 0.00"HG 02 UHCC CO NO NOX 00251214. CONC (PPM) 109523. 31808. 17656. 173. 223 FACAL FAM ERROR 0.05146 0.05251 -1 995 MWEXH EXH FLOW KWN XTC 0. 92108 1. 00125 27 83681 METHOD 1, 2 934, 859 MASS/MODE(LBM) 0. 09112 MASS/RATED HP(#/HP) 0. 00057 0.01997 0.14164 0.01779 0.00021 0.00041 0 00000 0.00012 0 00000 0.09088 0.00011 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL 0.05162 0 05251 -1.690 0. 92237 1. 00000 27. 81548 935, 576 METHOD 2. 1 0. 09119 0. 01999 MASS/MODE(LBM) 0.14175 0.01781 0.00021 0.00041 0.00012 0.00000 MASS/RATED HP(#/HP) 0.00057 0.00088 0.00011 0.00000 FAM ERROR EXH FLOW KWD XTC MWEXH FACAL 0 05120 0.05251 -2.495 934. 268 0, 92166 0, 99938 27, 85442 METHOD 3. 1 MASS/MODE(LBM) 0. 09106 MASS/RATED HP(#/HP) 0. 00057 0.14155 0 01996 0 00021 0.01778 0.00041 0.00088 0.00011 0 00012 0.00000 0.00000 KWD XTC MWEXH EXH FLOW FACAL FAM ERROR 0 05153 0 05251 -1 861 0. 92109 0. 19063 27. 50000 946, 308 METHOD 3. 2 0.00042 MASS/MODE(LBM) 0. 09224 0.14337 0.01801 0. 02022 0.00021 ASS/RATED HP(#/HP) 0. 00058 0.00089 0.00011 0.00013 0 00000 0.00000 RUN NO. MODE: 2 COMMENTS: BASELINE DATA RUN5. 2 FUEL RATE= ENGINE RPM(NOM)=1200 RPM = 96.53F 7. 0805#/HR TEMP(DB) ENGINE RPM(ACT)=1189. RPM = 52.00F AIR RATE = 104. 9433#/HR TEMP(DP) = 5.8HP = 0.0HP BHP(OBS) = 81.00F F/A RATIO= 0.0674#/# TEMP (BAR) BHP (CORR) BAR PRESS(OB) = 29.23"HG MAN VAC (OBS) =18.80"HG BAR PRESS(CR)= 29.09"HG MAN PRESS(CORR) = 0.00"HG SPEC HUMIDITY=0 0084#/# UHCC CO NO NOX 0.0202 CONC (PPM) 93691 42201. 12006. 39227. 226 267 MWEXH EXH FLOW FACAL FAM ERROR XTC KWD 0.06821 0 06747 1.106 0, 87335 1, 03655 27, 75891 1555, 637 METHOD 1 2 MASS/MODE(LBM) 3.05150 MASS/RATED HP(#/HP) 0.01907 0 00501 0.00907 0 99898 0.12293 0.81222 0. 00003 0.00076 0.00006 0.00624 0.00508 FAM ERROR KWD XTC MWEXH EXH FLOW FACAL 0. 91167 1. 00000 27. 06935 1595, 266 0. 07595 0. 06747 12 574 METHOD 2. 1 MASS/MODE(LBM) 3. 12924 MASS/RATED HP(#/HP) 0. 01956 0.00930 0. 83291 0 00514 1. 02442 0.12606 0.00521 0 00003 0.00006 0.00078 0.00640 FAM ERROR KWD MWEXH EXH FLOW FACAL XTC 0 06747 -9 454 0.88997 0.98110 28.30031 1525, 877 0.06109 METHOD 3. 1 0.00492 0.00890 MASS/MODE(LBM) 2. 99312 MASS/RATED HP(#/HP) 0. 01871 0. 79669 0. 97987 0.12057 0.00075 0.00612 0.00498 0.00003 0.00006 FACAL FAM ERROR 0.07102 0.06747 5.271 KWD XTC MWEXH EXH FLOW 0.87372 0.27819 27.50000 1570. 284 METHOD 3. 2 0.12408 0.81987 0 00506 1.00838 0.00916 MASS/MODE(LBM) 3. 08023 0.00006 MASS/RATED HP(#/HP) 0.01925 0.00630 0.00077 0.00512 0.00003

TABLE 6.1. Continued

```
RUN NO. 5
MODE:
COMMENTS: BASELINE DATA RUN5. 3
TEMP(DB) = 89.18F
                            FUEL RATE= 75. 7576#/HR
                                                           ENGINE RPM(NOM)=2700 RPM
                             AIR RATE = 864, 6914#/HR
TEMP(DP)
             = 58, 00F
                                                           ENGINE RPM(ACT)=2694. RPM
            = 82. 00F
TEMP(BAR)
                            F/A RATIO= 0.0876#/#
                                                           BHP (OBS)
                                                                           =139.8HP
BAR PRESS(OB) = 29, 23"HG
                                                           BHP (CORR)
                                                                           =153 7HP
BAR PRESS(CR)= 29. 09"HG
                                                           MAN VAC(OBS) = 0.70"HG
SPEC HUMIDITY=0. 0105#/#
                                                           MAN PRESS(CORR)=29.00"HG
                        C02
                                   02
                                              UHCC
                                                         CO
                                                                   NO NOX
CONC (PPM)
                       88079.
                                   1256.
                                                       102717.
                                                                    213.
                                              1607.
                                                                               185
                                                     FACAL FAM ERROR
0.09128 0.08761 4.196
                                                       FACAL
                   KWD
                                   MWEXH EXH FLOW
                          XTC
METHOD 1. 2
              0. 85456 1. 06022 26. 66957 13593. 140
MASS/MODE(LBM) 0. 68364
MASS/RATED HP(#/HP) 0. 00427
                                 0. 00708 0. 00392
                                                      0. 50684 0. 00113
                                                                            0.00150
                                 0.00004
                                           0. 00002
                                                      0.00317
                                                                 0. 00000
                                                                            0.00000
                                                     FACAL FAM ERROR
0. 11171 0. 08761 27. 501
0. 53387 0. 00119 0. 00158
                  KWD XTC
                                  MWEXH EXH FLOW
METHOD 2. 1
               0. 91968 1. 00000 25. 31911 14318. 160
                   0. 72010 0. 00746 0. 00413
MASS/MODE(LBM)
MASS/RATED HP(#/HP) 0.00450
                                 0.00005
                                           0.00003
                                                      0. 00334
                                                                 0. 00000
                                                                            0.00001
                                                     FACAL FAM ERROR
0.07858 0.08761-10.304
                                 MWEXH EXH FLOW
                 KWD XTC
                                                                  FAM ERROR
              0. 87924 0. 96585 27. 61258 13128. 910
METHOD 3. 1
MASS/MODE(LBM) 0.66029 0.00684 0.00379
MASS/RATED HP(#/HP) 0.00413 0.00004 0.00002
                                                     0. 48953 0. 00109
                                                                            0.00145
                                 0. 00004
                                                                 0. 00000
                                           0. 00002
                                                       0.00306
                                                                            0.00000
                                                     FACAL FAM ERROR
0.09791 0.08761 11.754
                  KWD XTC
                                  MWEXH EXH FLOW
                                                                   FAM ERROR
METHOD 3.2
              0. 85519 0. 36584 27. 50000 13182. 660
MASS/MODE(LBM)
                  0. 66300 0. 00687
                                            0.00380
                                                     0. 49153 0. 00109 0 00145
MASS/RATED HP(#/HP) 0.00414
                                 0.00004
                                            0. 00002
                                                      0.00307
                                                                 0.00000
                                                                            0 00000
10DE :
         4
COMMENTS BASELINE DATA RUN5. 4
TEMP(DB) = 92.75F FUEL RATE= 57.8592#/HR
                                                           ENGINE RPM(NOM)=2450 RPM
             = 58.00F
                             AIR RATE = 669. 1042#/HR
                                                           ENGINE RPM(ACT)=2430, RPM
TEMP(DP)
            = 82. 00F
TEMP(BAR)
                             F/A RATIO= 0.0864#/#
                                                           BHP (OBS)
                                                                           =107. 3HP
BAR PRESS(OB)= 29. 24"HG
                                                           BHP (CORR)
                                                                           = 0 OHP
BAR PRESS(CR)= 29 10"HG
                                                           MAN VAC(OBS)
                                                                         = 3 50"HG
SPEC HUMIDITY=0 0105#/#
                                                           MAN PRESS(CORR)= 0.00"HG
                                                                   NO
                        002
                                              UHCC
                                                         CO
                                                                              NOX
                                   02
CONC (PPM)
                       91453
                                   1758.
                                              1676.
                                                        95383.
                                                                    269
                                                                               244
                                   MWEXH EXH FLOW
                                                      FACAL FAM ERROR
0.08908 0 08647 3.025
                          XTC
                   KWD
METHOD 1, 2
             0, 85357 1, 05545 26, 81676 10449, 770
                                           0. 05239
MASS/MODE(LBM) 9 09468
MASS/RATED HP(#/HP) 0 05684
                                 0. 12709
                                                      6. 03019 0. 01823
                                                                            0.02531
                                                       0. 0376°
                                 0.00079
                                           0.00033
                                                                 0.00011
                                                                            0.00016
                   KWD XTC
                                   MWEXH EXH FLOW
                                                       FACAL
                                                                  FAM ERROR
              0. 91309 1. 00000 25 60011 10946. 390
                                                      0 10704 0 08647 23 788
METHOD 2, 1
MASS/MODE(LBM) 9 52691 0.13313
MASS/RATED HP(#/HP) 0.05954 0.00083
                                           0. 05488
                                                      6, 31678 0, 01910 0, 02651
                                            0.00034
                                                      0 03948
                                                                  0.00012
                                                                            0.00017
                  KWD
                          XTC
                                  MWEXH EXH FLOW
                                                       FACAL
                                                                   FAM ERROR
              0, 87661 0, 96896 27, 67520 10125, 630
                                                      0.07763 0 08647-10.222
METHOD 3 1
MASS/MODE(LBM) 8 81258
MASS/RATED HP(#/HP) 0.05508
                                                       5. 84315
                                0. 12315
                                            0.05076
                                                                 0.01767
                                                                            0.02453
                                0.00077
                                            0.00032
                                                      0. 03652
                                                                  0.00011
                                                                            0.00015
                                                      FACAL FAM ERROR
0 09498 0 08647 9 849
5 88037 0 01778 0 02468
                   KWD XTC
                                   MWEXH EXH FLOW
METHOD 3. 2
               0. 85418 0. 35864 27. 50000 10190. 140
MASS/MODE(LBM) 8.86872 0.12393 0.05109
 1ASS/RATED HP(#/HP) 0. 05543
                                 0. 00077
                                            0.00032
                                                       0 03675
                                                                  0 00011
                                                                           0.00015
```

TABLE 6.1. Continued

```
RUN NO.
          5
MODE:
COMMENTS: BASELINE DATA RUN5. 5
[EMP(DB) = 97.83F
                          FUEL RATE= 34.3840#/HR
                                                             ENGINE RPM(NOM)=2360 RPM
                              AIR RATE = 393, 1924#/HR
TEMP(DP)
             = 60.00F
                                                             ENGINE RPM(ACT)=2363, RPM
            = 82.00F
TEMP(BAR)
                             F/A RATIO= 0.0874#/#
                                                             BHP (OBS)
                                                                             = 53. 6HP
                                                             BHP (CORR)
BAR PRESS(OB) = 29. 23"HG
                                                                              = 0. OHP
BAR PRESS(CR)= 29. 09"HG
                                                                            =11. 70"HG
                                                             MAN VAC(OBS)
SPEC HUMIDITY=0. 0113#/#
                                                             MAN PRESS(CORR) = 0.00"HG
                         002
                                    02
                                               UHCC
                                                          CO
                                                                      NΩ
                                                                                NOX
                      • 92056.
                                    1758.
CONC (PPM)
                                               1600.
                                                         95696.
                                                                      232.
                                                       rHUAL FAM ERROR
0.08905 0.08744 1.841
4.27147 0.01110
                                                                                  217
                    KWD
                          XTC
                                    MWEXH
                                            EXH FLOW
METHOD 1. 2
              0. 85213 1. 05975 26. 80812
                                            6148, 195
MASS/MODE(LBM). 6.46348 0.08973
MASS/RATED HP(#/HP) 0.04040 0.00056
                                            0. 03532
                                                                   0. 01110 0. 01590
                                            0.00022
                                                        0.02670
                                                                    0. 00006
                                                                               0.00009
                                                       FACAL FAM ERROR
0.10864 0.08744 24 230
                   KWD XTC
                                   MWEXH
                                            EXH FLOW
               0. 91670 1. 00000 25. 49028
METHOD 2.1
                                            6466, 055
MASS/MODE(LBM) 6.79764 0.09437
MASS/RATED HP(#/HP) 0.04249 0.00059
                                            0.03714
                                                       4. 49230
                                                                   0. 01167
                                                                               0.01672
                                            0.00023
                                                      0. 02808
                                                                   0. 00007
                                                                               0.00010
                                            EXH FLOW FACAL FAM ERROR 5942. 293 0. 07668 0. 08744-12. 307
                   KWD
                            XTC
                                    MWEXH
                                                                     FAM ERROR
               0. 87703 0. 96648 27. 73703
METHOD 3. 1
MASS/MODE(LBM) 6. 24702 0. 08672
MASS/RATED HP(#/HP) 0. 03904 0. 00054
                                            0.03413
                                                       4. 12842
                                                                   0.01073 0.01536
                                                        0. 02580
                                             0.00021
                                                                   0.00006
                                                                               0.00009
                          XTC
                  KWD
                                    MWEXH
                                            EXH FLOW
                                                        FACAL
                                                                     FAM ERROR
               0. 85282 0. 36071 27. 50000
                                                       0. 09542 0. 08744 9 119
METHOD 3.2
                                            5993, 512
                      6. 30086
                                  0. 08747
MASS/MODE(LBM)
                                             0.03443
                                                        4. 16400
                                                                   0. 01082 0. 01550
MASS/RATED HP(#/HP) 0.03938
                                  0.00055
                                             0.00022
                                                        0.02603
                                                                   0. 00006
                                                                              0 00009
RUN NO
          5
10DE:
         6
COMMENTS: BASELINE DATA RUNS. 6
TEMP(DB)
            =102. 29F FUEL RATE=
                                            7. 2604#/HR
                                                             ENGINE RPM(NOM)=1220 RPM
TEMP(DP)
              = 64.00F
                              AIR RATE = 100.4240 \# / HR
                                                             ENGINE RPM(ACT)=1203. RPM
                                                                            = 2.4HP
= 0.0HP
TEMP(BAR)
             = 82.00F
                             F/A RATIO= 0.0723#/#
                                                             BHP(OBS)
BAR PRESS(OB) = 29, 23"HG
                                                             BHP (CORR)
                                                                                 O. OHP
BAR PRESS(CR)= 29.09"HG
                                                             MAN VAC(OBS) =19 70"HG
SPEC HUMIDITY=0.0131#/#
                                                             MAN PRESS(CORR) = 0.00"HG
                         C02
                                    02
                                               UHCC
                                                          CO
                                                                     NO
                                                                                 NOX
CONC (PPM)
                        89063.
                                   47728.
                                              21791.
                                                         34916.
                                                                      107
                                                                                 127
                                                                      FAM ERROR
                    KWD
                           XTC
                                    MWEXH
                                            EXH FLOW
                                                         FACAL
                                            1504. 354
METHOD 1.2
              0. 87295 1. 02668 27. 59329
                                                       0. 07079 0 07229 -2. 085
MASS/MODE(LBM) 0. 76504
MASS/RATED HP(#/HP) 0. 00478
                                             0.05884
                                 0. 29797
                                                       0. 19067
                                                                   0.00062 0.00114
                                  0.00186
                                             0.00037
                                                        0.00119
                                                                   0.00000
                                                                              0.00000
                  KWD XTC
                                   MWEXH
                                            EXH FLOW
                                                        FACAL
                                                                     FAM ERROR
METHOD 2. 1
               0. 90069 1. 00000 27. 10353
                                            1531, 537
                                                       0. 07635 0 07229 5, 608
MASS/MODE(LBM) 0. 77886
MASS/RATED HP(#/HP) 0. 00487
                                  0.30335
                                             0.05991
                                                        0. 19412
                                                                   0.00063
                                                                               0.00116
                                  0.00190
                                             0.00037
                                                        0.00121
                                                                   0 00000
                                                                               0.00000
                   KWD XTC
                                                        FACAL
                                    MWEXH
                                            EXH FLOW
                                                                    FAM ERROR
                                                      0. 06561 0. 07229 -9 241
0. 18807 0. 00062 0. 0
               0. 88520 0. 98640 27. 97520
METHOD 3. 1
                                            1483.816
MASS/MODE(LBM) 0. 75459
MASS/RATED HP(#/HP) 0. 00472
                                  0. 29390
                                             0.05804
                                                                              0.00112
                                  0.00184
                                             0.00036
                                                        0.00118
                                                                   0.00000
                                                                              0.00000
                                                        FACAL
                  KWD XTC
                                    MWEXH
                                            EXH FLOW
                                                                    FAM ERROR
METHOD 3. 2
                                            1509, 457
                                                       0. 07293 0. 07229 0. 885
               0. 87338 0. 27941 27. 50000
                                             0.05904
MASS/MODE(LBM)
                     0. 76763
                                  0. 29898
                                                        0.19132
                                                                   0.00062 0.00114
1ASS/RATED HP(#/HP) 0.00480
                                                                              0.00000
                                                                   0. 00000
                                  0.00187
                                             0.00037
                                                        0.00120
```

TABLE 6.1. Continued

RUN NO. 5					
MODE: 7					
COMMENTS: BASELINE DA					g4.
7EMP(DB) = 101.60F					OM)= 700 RPM
TEMP(DP) = 66.008				NE RPM(A	CT) = 712. RPM
TEMP(BAR) = 82.00F		0.0631#/#	BHP(OBS)	= 3.3HP
BAR PRESS(OB) = 29. 23			BHP (CORR)	= 0. OHP
BAR PRESS(CR) = 29.09			MAN	VAC(OBS)	=16.00"HG
SPEC HUMIDITY=0. 0140			MAN	PRESS(COR	RR) = 0.00"HG
	CO2 O2	UHCC	CO	NO	NOX
CONC(PPM)	83260. 66 5 6		21292.	156.	194
KWI			FACAL	FAM	ERROR
	8 1. 02108 27. 788			0. 06317	0 202
MASS/MODE(LBM)	0. 18446 0. 107	- · · · · · · · · · · · · · · · · · · ·	0. 02999	0. 00024	0. 00045
MASS/RATED HP(#/HP)	0. 00115 0. 000		0. 00019	0. 00000	
MASS/HP/CYC(#/HP/C)	0. 12709 0. 011		0. 07413	0. 00023	
KWI			FACAL	FAM	ERROR
	8 1.00000 27.417			0. 06317	6. 118
MASS/MODE(LBM)	0 18696 0.108		0. 03039	0. 00024	
MASS/RATED HP(#/HP)	0. 00117 0. 000		0. 00019	0. 00000	
MASS/HP/CYC(#/HP/C)	0. 13269 0. 011		0. 07762	0. 00024	
KWI			FACAL	FAM	ERROR
	7 0. 98948 28. 086			0.06317 -	
MASS/MODE(LBM)	0. 18250 0. 106		0. 02967	0. 00023	
MASS/RATED HP(#/HP)	0. 00114 0. 000		0. 00019	0. 00000	
MASS/HP/CYC(#/HP/C)	0. 12338 0. 010		0. 07184	0. 00022	2 0.00033
KWI			FACAL	FAM	ERROR
	7 0. 25133 27. 500	00 1176. 214	0.06479	0. 06317	2. 570
MASS/MODE(LBM)	0. 18640 0. 108		0. 03030	0. 00024	0 00045
MASS/RATED HP(#/HP)	0. 00116 0. 000		0.00019	0.00000	
MASS/HP/CYC(#/HP/C)	0. 12474 0. 011	11 0.00192	0. 07248	0. 00022	0.00033

7. SUMMARY

Four methods have been developed for computing fuel-air ratios from exhaust gas analyses. These methods are based on atom balances, partial sums of mole-fractions, defined wet, dry and dried measurements and the water-gas reaction equilibrium constant equation. For an ideal case, all methods give the same calculated fuel-air ratio. However, when measurement errors occur, each method gives a different result. This occurs because of differences in specific errors among the different methods.

In addition to providing a check on fuel-air and concentration errors, the Michigan method calculates exhaust molecular weight from the calculated mole-fractions of ten gaseous exhaust products. Calculated results indicate that poor fuel-air mixtures, and the resulting poor combustion, lead to low exhaust molecular weights. As the mixture and combustion improve, the molecular weights increase and approach the values obtained from equilibrium calculations. The Michigan method also eliminates the need for dryto-wet water correction factors, since the method can use wet, dry or dried concentration measurements directly.

The rationale behind selecting a particular procedure for determining data validity is developed in this report. It leads to the conclusion that no single variable can be used alone to determine data validity. E(1.2) is a good measure of fuel-air ratio error, but a low error can come about because of compensating errors in concentration measurements. On the other hand, XTC is a good measure of the accuracy of concentration measurements. When coupled together, they indicate those runs which have low fuel-air errors together with low concentration measurement errors. Use of Method 1.2, together with E(1.2) and XTC as indicators of data validity, is suggested.

3. REFERENCES

- 1. Sheehy, J.P., Achinger, W.C., and Simon, R.A., "Handbook of Air Pollution," Robert A. Taft Sanitary Engineering Center, Dept. of Health, Education and Welfare.
- 2. Handbook of Chemistry and Physics, CRC Press, 53rd Ed., 1972-1973.
- 3. Stern, A.C., Air Pollution, Academic Press, Vol. I, 2nd Ed., 1968.
- 4. Spindt, R.S., "Air-Fuel Ratios from Exhaust Gas Analysis," SAE Paper No. 650507, 1965.
- 5. Stivender, D.L., "Development of a Fuel-Based Mass Emission Measurement Procedure," SAE Paper No. 710604, 1971.
- 6. Federal Register, Vol. 38, No. 136, Part II, July 17, 1971.
- 7. Eltinge, L., "Fuel-Air Ratio and Distribution from Exhaust Gas Composition," Ethyl Corporation, January 1968; also SAE Paper No. 680114, 1968.
- 8. Rezy, B.J., "Exhaust Emissions Calculations," Teledyne-Continental Engineering Report A-81-1, 14 March 1975.
- 9. AVCO-Lycoming Report to FAA, April 21, 1975.
- 10. Mirsky, W. and Nicholls, J.A., "The Influence of Mixture Distribution on Emissions from an Aircraft Piston Engine," FAA report: FAA-RD-78-70.
- 11. Yun, H.J. and Mirsky, W., "Schlieren-Streak Measurements of Instantaneous Exhaust Gas Velocities from a Spark-Ignition Engine," SAE Paper No. 741015, October 1974.
- 12. AVCO-Lycoming Communication Report 311-20 to FAA, March 18, 1976.

Appendix A

Computer Program FAA

```
THE UNIVERSITY OF MICHIGAN
      FAA. FR
                       (5-19-76 VERSION)
      FAA ENGINE EMISSIONS DATA REDUCTION PROGRAM
      USE WITH SUBROUTINES CRT12 CRT15, CRT16
      REAL K1, K2, K3, NO, NOX, NOSP, NOXSP, NOSPR, NOXSPR, NOR, NOXR, NOMPC,
     INOXMPC, MUINA, MWEXH, NOMFR, NOXMFR, NOMPM,
    2NOXMPM, NOMMP, NOXMMP, NO2SP, KWD, KWDD, N2O2, N2A, MWAIR, MET
      INTEGER RPMN, CO2RNG, CORNG, HCRNG, WOT, DIA, DIAM
      DIMENSION A2(15,16), A3(16,17), A4(12,13) B(16,17), X(16), IDATE(4),
     1IOPERS(24), IENGT(6), IENGSN(6), IRUN(3)
      DIMENSION INFO(34), DATAF(10), YP(24,4), HCMPC(4), NOXMPC(4),
     1COMPC(4), CO2MPC(4), O2MPC(4), NOMPC(4)
      COMMON/INIT/B/X
      COMMON/INIT2/A2
      COMMON/INITS/AS
      COMMON/INIT4/A4
      COMMON/STOR1/C1, C2, C3, C4, C5, C6, C7, C11, C12, C13, C15, C16, C17, C27U,
    (1028U) 029U) 018, 019, 020, 021, 022, 023, 024, 025, 026, 027, 028, 029, 030, 031,
     2032, 033, 034, 035, 036, 037, 038, 040, 041, 042, 043, 044, 045, 068, 069, 070
     3071, 072, 073, 074, 075, 076, 077, 078, 079, 0770, 0780, 0790, 080, 081, 083
     4083, 084, 085, 086, 087, 088, 089, 090, 091, 093, 094, 095
      COMMON/STORE/CO2RNG, CO2SP, CO2SPR, CO2R, CO2, CO2SPC, CO2RK, CO2MFF
     1002MPM, CO2MMP, CO2MPC, CORNG, COSP, COSPR, COR, CO,
     2COSPC, CORK, COMFR, COMPM, COMMP, COMPC, O2SP, O2SPR, O2R,
     302, 02MFR, 02MPM, 02MMP, 02MPC, HCRNG, HCSP, HCCSP, HCSPR,
     4HCR, HCC, HCSPC, HCRK, HCMFR, HCMPM, HCMPC, NOSP, NOSPR,
     5NOR, NO, NOMER, NOMEM, NOMME, NOMEC, NOXSE, NOXSER, NOXR,
     6NOX, NOXMER, NOXMPM, NOXMMP, NOXMPC, NO2SP
       COMMON/STOR TRIMB, KWDD, AA, FF, XCO2, XCO, XHC, XO2, XNO, XNO2, XH2C, XN2
     1XAR, XH2/XC
       COMMON ISTOR4/YP
       DATA A2/2*1 0,14*0,0,-1,0,31*0,0,-1,0,13*0,0,2,0,2*1 0/
     112*0 0 2*1 0 0 0,1, 0,15*0, 0,1, 0,10*0, 0,2, 0,4*0, 0,1, 0,9*0, 0
     21. 0, 5*0 0, 1, 0, 3*0, 0, 1, 0, 4*0, 0, 2, 0, 6*0 0, 1, 0, 2*0, 0, 1, 0, 2*0, 0
     31: 0 (-0.1, 0.7*0, 0.2 0.5*0, 0.1, 0.9*0, 0.1, 0.15*0, 0.2, 0.
     415*0 0, 1, 0, 11*0, 0, 2, 0, 4*0, 0, 1, 0, 14*0, 0/
       DATA A3/2*1, 0, 15*0, 0, -1 0, 45*0, 0, -1 0, 2*0, 0, 2, 0, 0, 0, 1, 0, 5*0 0, 1 0
      (4*0 0 ) 0.2*0, 0, 1, 0, 2*0, 0, 1 0, 4*0 0, 1, 0 4*0, 0, 1, 0, 6*0, 0, 1
     21 0, 7*6, 0, 2 0, 4*0 0, 1 0, 2*0 0, 1 0 7*0, 0, 1, 0, 5*0, 0, 1, 0, 0 0
     30 0.1.0,5*0.0,2 0,6*0.0,2*1 0.0 0.1 0,3*0 0,1 0,0 0.1 0,0 0.
     46*0 0, 1, 0, 3*0 0 +1 0 2*0, 0, 1 0 9*0 0, 1, 0, 14*0, 0, 1, 0, 0, 0, 2, 0
     513*0 0,1 0 2*0 0,1 0,5*0 0,2 0 6*0 0,1 0,20*0 0,2*1 0,15*0 0
     DATA A4/1 0, 11 0, 11*0 0, 1, 0, 20 0, 0, 1 0, 11*0, 0, -1, 0, 1 0, 19*0, 0, 0 5, 1 0, 0 0, 1, 0, 8*0, 0 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1, 0 7*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, 1 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, :*0, 0, 
     2-0 5, 4*0, 0, 1 0, 4*0, 0, 1 0, 0, 0, 0, 5, 5*0, 0, -2, 0
     32*0. 0, -1. 0, 0. 0, -1. 0, 7*0. 0, 1. 0, 4*0. 0, 1. 0, 7*0. 0,
     4 1 0:3*0.0,1 0:5*0.0;-2.0:5*0.0,1 0:9*0.0/
 79 FORMAT(" DATAFILE NAME
 80 FORMAT($19)
 81 FORMAT(II)
 82 FORMAT(I2
 83 FORMAT(3A2)
 84 FORMAT: 14)
 85 FORMAT(I5)
 86 FORMAT(G8 5)
 .90 FORMAT(4A.
  91 FORMAT(6A1)
 92 FORMAT(24A2)
 .93 FORMAT(34A2)
99 FORMAT(1H = "COMMENTS.", 34A2)
100 FORMAT(1H : 7/" | DATE ",5X,4A2,T07 "ENGINE TYPE: ",3X,6A2,T54 "FUEL H/C
     1 RATIO =", F6 3)
101 FORMAT(1H ," LOCATION: UNIV OF MICH", T27. "SERIAL NUMBER: ", 1X, 6A2, T56, "IGN
      1ITION TIMING= ".IZ, "DEG")
```

C

C

```
102 FORMAT(1H , " OPERATORS: ", 24A2)
103 FORMAT(1HO, "RUN NO. ", 3A2/" MODE: ", I5)
                               =", F6. 2, "F", T29, "FUEL RATE=", F9. 4, "#/HR", T57, "EN
104 FORMAT(1H , "TEMP(DB)
   1GINE RPM(NOM)=", I4, " RPM")
105 FORMAT(1H _ "TEMP(DP)
                              =",F6. 2, "F", T29, "AIR RATE =",F9. 4, "#/HR", T57, "EN
   1GINE RPM(ACT)=",F5.0,"RPM")
                               =",F6. 2, "F",T29, "F/A RATIO=",F9. 4, "#/#", T57, "BHP
106 FORMAT(1H , "TEMP(BAR)
   1(OBS)
                 =", F5. 1, "HP")
107 FORMAT(1H , "BAR PRESS(OB)=",F6.2, ("HG', T29, "PHIM"
                                                               =", F9, 4, T57, "BHP
                =", F5. 1, "HP")
   1 (CORR)
108 FORMAT(1H , "BAR PRESS(CR)=",F6.2, "HG", T57, "MAN VAC(OBS)
                                                                     ="7F5, 27 "HG1)
109 FORMAT(1H , "SPEC HUMIDITY=", F6. 4, "#/#", T57, "MAN PRESS(CORR)=", F5. 2, " "HG )
110 FORMAT(1H , T25, "CO2", T35, "O2", T45, "UHCC", T55, "CO", T65, "NO", T75, "NOX ')
114 FORMAT(1H - "CONC(PPM)", T23, F7, O, T33, F7, O, T43, F7, O, T53, F7, O, T63, F7, O, T73,
   1F7. 0)
115 FORMAT(1H > "MASS/MODE(LBM)", T22, F8. 5, T32, F8. 5, T42, F8. 5, T52, F8. 5, T62, F8. 5,
   1772, F8. 5)
116 FORMAT(1H , "MASS/RATED HP(#/HP)", T23, F7, 5, T33, F7, 5, T43, F7, 5, T53, F7, 5, T63,
   1F7. 5, T73, F7. 5)
117 FORMAT(1H , T20, "KWD", T28, "XTC", T35, "MWEXH", T42, "EXH FLOW", T54,
   1"FACAL", T65, "FAM", T70, "ERROR")
118 FORMAT(1H , "METHOD", F4. 1, 3X, 2F8. 5, F9. 5, F10. 3, 2F9. 5, F7. 3)
119 FORMAT(1H , "MASS/HP/CYC(#/HP/C)", T23, F7, 5, T33, F7, 5, T43, F7, 5, T53, F7, 5, T63,
   1F7. 5, T73, F7. 5)
120 FORMAT(1H1,/)
122 FORMAT(1H . " (2F5 2)"/" 24")
123 FORMAT(1H , (2F5. 2))
    FITT(K1, K2, K3, VAR)=K1*VAR+K2*VAR*VAR+K3*VAR**3
    C1=1 81792E-4
    C2=1, 75E-10
    C3=3. 5116E-11
    C4=4. 71177E1
    05=-2.00984
    C6=3 28746E-1
    07=.01934
    C11=-1, 26635E-2
    C12=5, 36797E-3
    C13=4. 91015E-8
    C15=-3. 0205E-3
    C16=5, 66919E-6
    C17=-4, 59596E-10
    C18=6 70727E-2
    C19=4. 07332E-4
    C20=4 35863E-6
    C21=3. 09387E-2
    622=1.88357E-4
    C23=5, 76719E-8
    C24=1, 80806E-2
    C25=6 37274E-5
    026=8 39907E-9
    C27=6, 08450E-2
    C28=3, 28671E-4
    C29=3 96270E-6
    C27U=4 92230E-1
    C28U=-1. 00439E÷2
    C29U=6, 62162E-5
    C30=2. 60958E-2
    C31=7. 83471E-5
    C32=1, 86948E-7
    C33=6, 10711
    C34=1, 44451E-2
    C35=2, 44838E-4
    036=1.62481
    C37=5, 33428E-3
    C38=-1. 58241E-5
    040=164, 581
```

```
041 = .245
 C42=992, E-7
 C43=3, 89549E2
 C44=1, 27588
 C45=-6, 23371E-3
 C68=1, 38694E1
 C69= 8.38889E-1
 C70=2. 37654E-2
 C71=3 07229E1
 072=-3, 4629
 073=2 59663E-1
 C74=5, 44677E1
 075=-8, 05437
 C76=1, 01355
 C77=1, 62951E!
 078=-1 35417
 C79=5, 90278E-2
 077U=1. 32639E1
 C78U=-5 55556E-1
 C79U=7 71605E-3
 080=3 78735E1
 081=-3 71806
 082=2 62956E-1
 083=1.66345E-1
 C84= -9, 70595E-5
 085=3 07143E-8
 086=6. 07292E-1
 087=-8, 75E-4
 C88=1 69271E-6
 089=2 59±27E6
 C90=-2 59517E4
 091=3 48605E2
 092≈2, 52202E-3
 C94=-1 41714E-8
 C95=1 55315E-13
 GENERAL INPUT DATA
 WRITE(10, 79)
 READ(11/80)DATAF(1)
  CALL OPEN(13 DATAF(1), 2, IER)
  IF (IER. NE. 1) GO TO 38
  ACCEPT "OUTPUT?LPT=1, PTP=2, BOTH=3", IOUT
 READ(13 @0:(IDATE(1), I=1,4)
 READ(13.92'(IOPERS(I), I=1, 24)
 READ(13,91) (IENGT(I), I=1,6)
 READ(13,91)(TENGSN(I), I=1,6)
 READ(13, 8/-) HPR, HTCR, EHCR, EHCC
  READ(13, 92) IGNT
 READ(13 01)DIAM
 GO TO (2.3,2), IOUT
Z WRITE (12, 100) IDATE | IENGT, HTCR
 WRITE (12, 101) IENGSN, IGNT
  WRITE(12 102) IOPERS
3 READ(13/31)MMAX
  DO 4 I=1 4
 HCMPC(1)
  NOXMPO(1 #0.0
  COMPC(I)=0 0
  002MPC(I) = 0.0
 02MPC(I)=0.0
 NOMPC(I)=0 0
4 CONTINUE
  DO 5 I=1,24
  DO 5 J=1.4
5 YP(I,J)=0.0
```

```
IPAGE=0
     DO 37 MODE=1, MMAX
      IF (IOUT, EQ. 2) GO TO 6
      IPAGE=IPAGE+1
      IF (IPAGE, LT. 3) GO TO 6
      WRITE(12,120)
      IPAGE=1
     INPUT DATA PER RUN
    6 READ(13,93)(INFO(I), I=1,34)
      READ(13,83)(IRUN(I), I=1,3)
     READ(13-81)M
    1 READ(13,81)WOT
     READ(13,84)RPMN
      READ(13,81)CO2RNG, CORNG
     READ(13, 85) HCRNG
     READ(13.86) TIM, PBAR, TBAR, TWB, TDP, REV: TIME, DYNL, PMANV,
     1TINAV, DPINA, PINAS, WFUEL, CO2SP, COSP, O2SP, HCSP, NOSP,
     2NO2SP, CO2SPR, COSPR, O2SPR, HCSPR, NOSPR, CO2R, COR,
     302R, HCR, NOR, NOXR, DPINJ
      START OF COMPUTATION
      TBARC=(TBAR-32, )*5, 79,
      TINA=FITT(C4, C5, C6, TINAV)+32.
      TDB=TINA
      PBARK=PBAR*(1, +1, 84E-5*(TBARC-16, 667))/(1, +FITT(C1, C2, C3, TBARC))
      PBARE=PBARK+7, 33623E-2*DPINJ
      PSAT=C11+C12*TDP+C13*TDP**3, 73
      W=. 622*PSAT/(PBARK-PSAT)
      PVAP=W*PBARK/(W+. 62197)
      RPM=REV/(6. *TIME)
      CORRECTED BRAKE HORSEPOWER
      HPB=DYNL*RPM/3000.
      HPBK=0, 0-
      PMANK=0. 0
      IF (WOT, EQ. 1) GO TO 10
      CEVAP=PBARK/(PBARK-PVAP)
      PMANK=29.53-.555*SIN((RPM-2000.)/8.333)+.038*SIN((RPM-2000.)/3 889)
      CFMP=PMANK/(PBARK-PMANV)
      CFTEMP=((TINA+460,)/520,)**,8
      CFTOT=CFVAP*CFMP*CFTEMP
      HPF=FITT(C15, C16, C17, RPM)
      HPBK=(HPB+HPF)*CFTOT-HPF
   10 MUINA=C40+C41*TINA+C42*TINA*TINA
      DIA=DIAM/2
      GO TO (11,12,13), DIA
   11 FVINA=FITT(C89, C90, C91, DPINA)*(PBARK+, 0733623*PINAS-PVAP)/
     1((460, +TINA)*MUINA)
   12 60 TO 14
   13 FVINA=2.5177E7*DPINA*(PBARK-.0733623*PINAS-PVAP)/((460.+TINA)*MUINA)
   14 FMINA= 07486*FVINA
      FMFUEL=WFUEL*60. /TIME
      BSFC=FMFUEL/HPB
      FAM=FMFUEL/FMINA
C
      CORRECTED CONCENTRATION
      HCCSP=HCSP*3.
      HCRNG=HCRNG/15000+1
      GO TO (17,18), HCRNG
   17 HCC=HCCSP*HCR/HCSPR
```

C

C

C

GO TO 19

- 18 HCSPC=FITT(C93,C94,C95,HCCSP) HCRK=HCR*HCSPC/HCSPR HCC=FITT(C43,C44,C45,HCRK)
- 19 NO=NOSP*NOR/NOSPR
 O2=(02SP*02R/02SPR)*1E4
 NOXSP=NOSP+NO2SP
 NOXSPR=NOXSP*NOSPR/NOSP
 NOX=NOXSP*NOXR/NOXSPR
 GO TO (20,24,25,26), CORNG
- 20 IF (COSP.GE.9.0) GO TO 21 COSPC=FITT(C77,C78,C79,COSP) GO TO 22
- 21 COSPC=FITT(C77U,C78U,C79U,COSP)
- 22 CORK=COR*COSPC/COSPR
 1F \CORK GE 80.0) GO TO 23
 CO=FITT(C27,C28,C29,CORK)*1E4
 GO TO 27
- 23 CO≃FITT(C27U, C28U, C29U, CORK)*1E4 GO TO 27
- 24 COSPC=FITT(C80,C81,C82,COSP) CORK=COR*COSPC/COSPR CO=FITT(C30,C31,C32,CORK)*1E4 GO TO 27
- 25 COSPC=FITT(C83,C84,C85,COSP) CORK=COR*COSPC/COSPR CO=FITT(C33,C34 C35,CORK) GO TO 27
- 26 COSPC=FITT(C86,C87,C88,COSP)
 CORK=COR*COSPC/COSPR
 CO=FITT(C36,C37,C38,CORK)
- 27 CONTINUE GO TO (28,29,30),CO2RNG
- 28 CO2SPC=FITT(C68,C69,C70,C02SP)
 CO2RK=L02R*C02SPC/C02SPR
 C02=FITT(C18,C19,C20,C02RK)*1E4
 G0 TC 31
- 29 CO2SPC=FITT(C71,C72,C73,C02SP) CO2RK=CO2R*CO2SPC/CO2SPR U2=FITT(C21,C22,C23,C02RK)*1E4 G0 TO 31
- 30 CO2SPC=FITT(C74,C75,C76,C02SF) C02RF=C02R*C02SPC/C02SPR C02=FITT(C24,C25,C26,C02RK)*1E4
- 31 CONTINUE 30 TO 44
- C EMISSION FLOW RATES (LBM/HR)
 - 40 HCMFR=FVEXH*, 0359*HCC/1E6 NOXMFR=FVEXH*, 119*NOX/1E6 COMFR=FVEXH*, 0726*C0/1E6 C02MFR=FVEXH*, 1142*C02/1E6 02MFR=FVEXH*, 083*02/1E6 NOMFR=FVEXH*, 0778*NO/1E6
- C EMISSION MASS PER MODE (LBM)

HCMFM=HCMFR*TIM/60.
NOXMPM=NOXMFR*TIM/60.
COMPM=COMFR*TIM/60.
CO2MPM=CO2MFR*TIM/60.
02MPM=02MFR*TIM/60.
NOMPM=NOMFR*TIM/60.

C MASS PER MODE PER RATED HORSEPOWER

HCMMP=HCMPM/HPR NOXMMP=NOXMPM/HPR COMMP=COMPM/HPR CO2MMP=CO2MPM/HPR 02MMP=02MPM/HPR NOMMP=NOMPM/HPR

YP(3*MODE-2, METH)=COMMP/0.042 YP(3*MODE-1, METH)=HCMMP/0.0019 YP(3*MODE, METH)=NOXMMP/0.0015

MASS PER RATED HORSEPOWER PER CYCLE

HCMPC(METH)=HCMPC(METH)+HCMMP
NOXMPC(METH)=NOXMPC(METH)+NOXMMP
COMPC(METH)=COMPC(METH)+COMMP
CO2MPC(METH)=CO2MPC(METH)+CO2MMP
02MPC(METH)=O2MPC(METH)+O2MMP
NOMPC(METH)=NOMPC(METH)+NOMMP

IF(MODE.LT. MMAX) GO TO 41 YP(22, METH)=COMPC(METH)/O. 042 YP(23, METH)=HCMPC(METH)/O. 0019. YP(24, METH)=NOXMPC(METH)/O. 0015

41 GO TO (65,32,32,32), METH

COMPUTED AIR-FUEL RATIO
METHOD 1.2(EXP K); METHOD 2.1(EXF XGW); METHOD 3.1(K & XGW);
METHOD 3.2(K, XGW & NO 02)

44 N202=78.09/20.95 AR02=.93/20.95 C0202=.03/20.95 AIR02=1.0+N202+AR02+C0202 N2A=(100.-C02A)/(1.0+20.95/78.09+.93/78.09) 02A=20.95*N2A/78.09 ARA=.93*N2A/78.09 MWAIR=.39948*ARA+.4400995*C02A+.280134*N2A+.319988*02A

MWAIR=.39948*ARA+.4400995*CUZA+ 780134*NZA+.319988*UZA H2002=W*AIRO2*MWAIR/18.01534

WTR=. 08866/19

A2(3,3)=-(2.0+2 0*C0202+H2002) A2(4,3)=-C0202 A2(4,7)=EHCC

A2(5,2) = -002/1E6A2(6,1) = -00/1E6

A2(7,16) = HCC/(1E6*EHCC)

A2(8,2)=-02/1E6 A2(9,16)=N0/1E6

A2(10, 16) = (NOX-NO)/1E6

A2(11/?)=-2.0*H200?

A2(11, 4) = -HTCR

A2(11,7)=EHCC*EHCR

A2(12,2)=-WTR

A2(13/3)= 7 0*N202

A2(14,3) = -AR02

METH=1 2 METH=1 A2(15.5)

A2(15/5)=0.0

A2(15,6)=0.0

A2(15,7)=0 0

A2(15,8)=0 0

A7(15,9)=0.0

```
A2(15,10)=0.0
   A2(15,11)=-1.0
   A2(15,13)=0.0
   A2(15,14)=0.0
   A2(15,15)=3.5*C02/C0
   A2(15, 16)=0.0
   GO TO 48
46 MET=2. 1
   METH=2
   A2(15,5)=1.0
   A2(15,6)=10
   A2(15,7)=1.0
   A2(15,8)=1.0
   A2(15, 9)=1 0
   A2(15,10)=1.0
   A2(15,11)=1.0
   A2(15,13)=1.0
   A2(15, 14)=1.0
   A2(15/15)=1.0
   A2(15,16)=1 0
48 CALL CRT15
   KWD=X(1)
   KWDD=X(2)
   AA=X(3)
   FF=X(4)
   XCO2=X(5)
   XCO=X(6)
   XHC =X(7)
   X02=X(8)
   XNO=X(9)
   XN02=X(10)
   XH20=X(11)
   XN2=X(13)
   XAR=X(14)
   XH2=X(15)
   XC=0. O
   GO TO 60
50 MET 3. 1
   METH=3
   AS(3,3)=-(2 0+2.0*00202+H2002)
   A3(4,3) = -2.0 * H2002
   43(4,4)=-HTCR
   A3(4,7)=EHCC*EHCR
   A3(5,2) = -002/1E6
   A3(6,1) = -C0/1E6
   A$(7.17)≈HCC (1E6*EHCC)
   AS(8 2:=-02/1E6
   A3(%, 17)=N0/1E6
   A3(10, 17) = (NOX-NU)/1E6
   A3(11:17)=1 0
   A3(12,2)=-WTR
   A3(13, 3) = -2.0*N202
   A3(14-3)=-AR02
   A3(15,15)=3.5*c02/00
   A3(16,3)=-00202
   A3(16,7)=EHCC
   CALL ORT16
   KWD=X(1)
   KWDD=X(2)
```

AA=X(3)

```
FF≈X(4)
   XC02=X(5)
   XC0=X(6)
  XHC=X(7)
  X02=X(8)
   XNO=X(9)
   XN02=X(10)
   XH20=X(11)
   XN2=X(13)
  XAR=X(14)
   XH2=X(15)
   XC=X(16)
   GO TO 60
55 MET=3. 2
  METH=4
   A4(1, 13)=1.0
   A4(3,3)=1.0+C0202+H2002/2.0+N202
   A4(4,3)=00202
  A4(4,7) = -EHCC
   A4(5,2) = -C02/1E6
   A4(6,1) = -C0/1E6
   A4(7,13)=HCC/(1E6*EHCC)
   A4(8,13) = (NOX-NO)/1E6
   A4(9,3)=2.0*H2002
   A4(9 4)=HTCR
   A4(9,7)=-EHCC*EHCR
   A4(10,2)=-WTR
   A4(11.3)≈AR02
   A4(12,12)=3.5*C02/C0
   CALL ORT12
   KWD=X(1)
  EWDD=X(2)
   AA=X(3)
   FF=X(4)
   XCO2=X(5)
   XCO=X(6)
   XHC≔X(7)
   X02=0. 0
   XNO=0 0
   XN02=X(8)
   XH20=X(9)
   XN2=0. 0
   XAR=X(11)
   XH2=X(12)
   XC=0. 0
60 XTC=XCO2+XCO+XHC+XO2+XNO+XNO2+XH2O+XN2+XAR+XH2+XC
   FACAL=FF*(12.01115+1.00797*HTCR)/(AIR02*MWAIR*AA)
   ERROR=(FACAL-FAM)*100. /FAM
   PHIM=FAM*(HTCR/4.+1.)*AIRO2*MWAIR/(12 01115+1.0079 **HTCR)
   IF (METH NE 4) GO TO 61
   MWEXH=27, 5
   GO TO 62
61 MWEXH=(44.00995*XC02+28.01055*XC0+(12.01115*EHCC+1.00797*EHCC*EHCR)
  1*XHC+31, 9988*X02+18, 01534*XH20+2, 01594*XH2+28, 0134*XN2+
  200,0061*YN0+46.0055*XN02+39.948*XAR+12.01115*XC)/XTC
6. FVFXH=385 479*(FMINA+FMFUEL)/MWEXH
   60 10 40
65 GO TO (67,68,67), IOUT
67 WRITE(12, 103) IRUN, M
   WRITE(12,99)INFO
   WRITE(12, 104) TDB, FMFUEL, RPMN
```

```
WRITE(12, 105) TDP, FMINA, RPM
   WRITE(12, 106) TBAR, FAM, HPB
   WRITE(12, 107)PBAR, PHIM, HPBK
   WRITE(12, 108) PBARK, PMANV
   WRITE(12, 109)W, PMANK
   WRITE(12, 110)
   WRITE(12, 111) 002, 02, HCC, CO, NO, NOX
32 IF(10UT, EQ. 2) GO TO 68
   WRITE(12, 117)
   WRITE(12, 118) MET, KWD, XTC, MWEXH, FVEXH, FACAL, FAM, ERROR
   WRITE(12, 115)CO2MPM, O2MPM, HCMPM, COMPM, NOMPM, NOXMPM
   WRITE(12, 116)CO2MMP, O2MMP, HCMMP, COMMP, NOMMP, NOXMMP
68 IF (MODE. LT. MMAX) GO TO 36
   IF(IOUT. EQ. 1) GO TO 70
   WRITE(14,122)
  DO 69 I=1,24
   XP=0.25+0.25*(I-1)+0.5*((I-1)/3)+0.25*((I-1)/21)
89 WRITE(14, 123) XP, YP(I, METH)
   IF(IOUT, EQ. 2) GO TO 36
70 WRITE(12,119)CO2MPC(METH),O2MPC(METH),HCMPC(METH),COMPC(METH),
  1NOMPC(METH), NOXMPC(METH)
36 CONTINUE
   GO TO (46,50,55,37), METH
37 CONTINUE
   READ(13,81)MORE
   IF (MORE, EQ. 0) GO TO 39
   GO TO 3
38 TYPE "FILE NOT OPENED"
39 CONTINUE
   CALL RESET
   STOP
   END
```

Appendix B

Computer Program FARAT

```
THE UNIVERSITY OF MICHIGAN
             C
      FARAT, FR
C.
                   (5/20/76 VERSION)
      FUEL-AIR RATIO CALCULATION
      USE WITH CRT4, CRT12, CRT15, CRT16
      REAL N202, N2A, N2AS, MWAIR, MWEXH, NO, NOW, NOD, NODD, NOX, NOXW, NOXD, NOXDD
      REAL KWDD, KWD, MET, INCR, K, KR
       INTEGER GT, FMAT, VAR, DISP1, DISP2, DISP3, DISP4, DISPS, FLAG
       DIMENSION A1(4,5), A2(15, 16), A3(16, 17), A4(12, 13), B(16, 17), X(16)
       COMMON/INIT/B, X
       COMMON/INITI/A1
       COMMON/INIT2/A2
       COMMON/INITS/AS
       COMMON/INIT4/A4
       COMMON/STOR/JCO2W, JCO2D, JCO2DD, JCOW, JCOD, JCODD, JO2W, JO2D, JO2DD,
     1JHCCW, JHCCD, JHCCDD, JNOW, JNOD, JNODD, JNOXW, JNOXD, JNOXDD
  100 FORMAT(1H : T7: "HTCR": T17: "EHCC": T27: "EHCR": T37: "C02A": T47:
     1"PSAT", T57, "PTRP", T70, "W", T77, "N202")
  110 FORMAT (1H , T4, F5, 3, T16, F5, 3, T25, F6, 3, T36, F5, 3, T44, F7, 5, T55, F6, 3,
      1T65, F6. 4, T74, F7 4)
  120 FORMAT(1H , //T5, "RUN: ", F5, 1, T27, "C02", T38, "C0", T48, "02", T57,
     1"HCC", T68, "NO", T77, "NOX")
  130 FORMAT(1H , T5, "DRY MEASUREMENTS", T24, F7 0, T34, F7. 0, T44, F7 0,
     1T54, F7 (0: T64, F7, 0, T74, F7, 0)
  131 FORMAT(1H , T5, "DRIED MEASUREMENTS", T24, F7, 0, T34, F7, 0, T44, F7 0,
      1T54, F7. 0, T64 F7. 0, T74, F7. 0)
  132 FORMATCIH , T5, "WEI MEASUREMENTS", T24, F7 0, T34, F7. 0, T44, F7. 0,
      1T54, F.7. O. T64, F7. O. T74, F7. O.
  135 FORMAT(1H // T5, "ONLY WET MEASUREMENTS ALLOWED USE METHOD 2")
  140 FORMAT(1H ) 75, "XCO2", T13, "XCO", T20, "XHC", T27 "XO2", T33, "XH20",
      1T41, "XH2", T48, "XN2", T55, "XN0", T61, "XN02", T69, "XAR", T77, "XC")
  150 FORMAT(1H / 11F7, 4)
   160 FORMAT(1H ) T6, "MTD", T13, "XTC", T22, "K", T26, "KWDD", T34, "KWD", T40,
      1"PHIM", T47, "MWEXH", T53, "PHICAL", T62, "FACAL", T72, "F/M", T77, "ERROR")
   16: SORMAT(1H , T4, "N202", T10, "C02A" T20, "W", T22, "HTCR', T27, "EHCC",
      1T33) "EHCR", T40, "XGW"/T47, "K", T50, "MTD", T56, "KWD".
      2T62, "FACAL", T72, "FAM", T77, "ERROR")
   164 FORMAT (1H , 2F6, 3, F7, 4, F6, 3, F4, 1, 2F6, 3, F5, 2, F5, 1, F6, 3, 2F8, 5, F7, 3)
   165 FORMAT(1H . T6, "CO2" . T14, "CO", T21, "O2", T26, "HCC", T32, "NO",
      1T% "NOX", T40, "FCHC" T44, "FDA", T50, "MTD" T56, "XTC", T62, "FACAL",
      2T7 : 'FAM" T '7, "ERROR")
   166 FORMAT(1H : F8 0, 2F7 0, F6, 0, 2F5, 0, F4, 2, F5 2, F4 1, F6, 3, 2F8, 5, F7, 3)
   170 FORMAT(1H > T7, 1 SE7 4, F8, 4, F7, 4, 2F8 5, F7, 3)
   180 FORMAT (1H1)
   181 FORMATCIH
        (=()
       7≠0 ↔
       ACCEPT "HTCR " HTCR.
               ",RUN "CL2 ",CO2I,"CO ",COI,
",HCCI,"NO ",NOI,"NOX ",NOXI
                                               ", COI, "02
                                                             7,021,
      1 "RUN
               ">HOGI>"NO
      2"HCC
      3"MEASURED FUEL/AIR "FAM,
      4"METHOD 1 1(1),1 2(2),2 1(3),3:1(4),3:2(5)  ",METHR,
      5" IMETH, METHMX " IMETH, METHMX,
      6"DISP1.DISP2.DISP3.DISP4 ", DISP1.DISP2.DISP3.DISP4
       METHMX=METHMX+1
       METH=METHR
       DISPS=DISP1+DISP2+DISP3+DISP4
    28 EHCC=1 0
       EHCR=1, 85
       CO2A=0, 03
       W=0.01
       PSAT=0 08866
       PTRP=19. 0
```

```
XGW=1. O
  K=3. 5
  FCHC=0. 0
  FDA=0. 0
   N2AS=78. 09
   02AS=20. 95
   ARAS=0. 93
   NNEG=0
   NPOS=1
   INCR=0. 0
   VAR=18
   JC02W=0
   JC02D=0
   JC02DD=1
   JCOW=0
   JCOD=1
   JCODD=0
   J02W=0
   J02D=0
   J02DD=1
   JHCCW=1
   JHCCD=0
   JHCCDD=0
   JNOW=1
   JNOD=0
   JNODD=0
   JN0XW=1
   JN0XD=0
   JNOXDD=0
29 CO2W=CO2I*JCO2W
   CO2D=CO2I*JCO2D
   CO2DD=CO2I*JCO2DD
   COW=COI*JCOW
   COD=COI*JCOD
   CODD=COI*JCODD
   02W=02I*J02W
   02D=02I*J02D
   02DD=02I*J02DD
   HCCW=HCCI*JHCCW
   HCCD=HCCI*JHCCD
   HCCDD=HCCI*JHCCDD
   WOW=NOI*JNOW
   NOD=NOI*JNOD
   NODD=NOI*JNODD
   WXONL*IXON=WXON
   NOXD=NOXI*JNOXD
   NOXDD=NOXI*JNOXDD
 O ACCEPT "GT ", GT
   GO TO (1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24
  125, 26, 37, 28), GT
 1 ACCEPT "HTCR, EHCC, EHCR ", HTCR, EHCC, EHCR
   GO TO 0
 2 ACCEPT "CO2A, W ", CO2A, W
   GO TO 0
 3 ACCEPT "JCO2W, JCO2D, JCO2DD, JCOW, JCOD, JCODD "", JCO2W, JCO2D, JCO2DD.
  1JCOW, JCOD JCODD
   GO TO 29
 4 ACCEPT "JOSW, JOSD, JOSDD, JHCCW, JHCCDD, JHCCDD ", JOSW, JOSD, JOSDD.
  тиносм, инсор, инсорв
   GO TO 29
 5 ACCEPT "UNOW, UNOD, UNODD, UNOXW, UNOXD, UNOXDD "", UNOW, UNOD, UNODD,
  1UNOXW, UNOXD, UNOXDD
GO TO 29
```

```
6 ACCEPT "RUN ", RUN
    GO TO O
  7 ACCEPT "CO2 ", CO2I
    GO TO 29
  8 ACCEPT "CO ", COI
    GO TO 29
  9 ACCEPT "02 ",02I
    GÖ TO 29
 10 ACCEPT "HCC ", HCCI
    GO TO 29
 11 ACCEPT "NO ", NOI
    GO TO 29
 12 ACCEPT "NOX ", NOXI
    60 TO 29
 13 ACCEPT "MEASURED FUEL/AIR ", FAM
    GO TO O
 14 ACCEPT "XGW, K ", XGW, K
    GO TO O
 15 ACCEPT "FCHC, FDA ", FCHC, FDA
    GO TO 0
 16 ACCEPT "PSAT, PTRP ", PSAT, PTRP
     GO TO O
  17 ACCEPT "N2AS, 02AS, ARAS ", N2AS, 02AS, ARAS
    GO TO 0
  18 ACCEPT "METHOD: 1, 1(1), 1, 2(2), 2, 1(3), 3, 1(4), 3, 2(5) ", METHR
    METH=METHR
     60 TO 0
 19 ACCEPT" IMETH, METHMX ", IMETH, METHMX
     METHMX=METHMX+1
     GO TO O
 20 ACCEPT "DISP1, DISP2, DISP3, DISP4 ", DISP1, DISP2, DISP3, DISP4
     DISPS=DISP1+DISP2+DISP3+DISP4
     GO TO 0
 21 J=0
     GO TO 0
 22 WRITE(12, 181)
     GO TO 0
 23 WRITE(12, 180)
     GO TO 0
  25 ACCEPT "NNEG, NPOS, INCR ", NNEG, NPOS, INCR
     NNEG=-NNEG
     GO TO O
  26 ACCEPT "VAR=HTCR(1), EHCC(2), EHCR(3), CO2A(4), W(5), PSAT(6), PTRP(7),
    1002(8), C0(9), 02(10), HCC(11), NO(12), NOX(13), XGW(14), K(15), FCHC(16),
    2FDA(17), NONE(18) ", VAR
     GO TO 0
  27 DO 90 NN=NNEG, NPOS
     FLAG=0
     GO TO (1010, 1020, 1030, 1040, 1050, 1060, 1070, 1080, 1090, 1100, 1110, 1120,
    11130, 1140, 1150, 1160, 1170, 1300), VAR
1010 IF (NN. GT. NNEG) GO TO 1011
     HTCRR=HTCR
1011 IF (NN. EQ. NPOS) GO TO 1012
     HTCR=HTCRR*(1.0+INCR*NN)
     GO TO 1300
1012 HTCR≃HTCRR
     GO TO 90
1020 IF (NN. GT. NNEG) GO TO 1021
     EHCCR=EHCC
1021 IF (NN. EQ. NPOS) GO TO 1022
     EHCC=EHCCR*(1 O+INCR*NN)
     GO TO 1300
1022 EHCC=EHCCR
```

GO TO 90

- 1030 IF (NN. GT. NNEG) GO TO 1031 EHCRR=EHCR
- 1031 IF (NN.EQ.NPOS) GO TO 1032 EHCR=EHCRR*(1.0+INCR*NN) GO TO 1300
- 1032 EHCR=EHCRR GO TO 90
- 1040 IF (NN. GT. NNEG) GO TO 1041 CO2AR=CO2A
- 1041 IF (NN.EQ.NPOS) GO TO 1042 CO2A=CO2AR*(1.O+INCR*NN) GO TO 1300
- 1042 CO2A≒CO2AR GO, TO 90
- 1050 IF (NN GT NNEG) GO TO 1051 WR=W
- 1051 IF (NN EQ NPOS) GO TO 1052 W=WR*(1 O+INCR*NN) GO TO 1300
- 1052 W=WR GO TO 90
- 1060 IF (NN. GT. NNEG) GO TO 1061 PSATR=PSAT
- 1061 IF (NN.EQ.NPOS) GO TO 1062 PSAT=PSATR*(1 O+INCR*NN) GO TO 1300
- 1062 PSAT=PSATR GO TO 90
- 1070 IF (NN GT NNEG) GO TO 1071 PTRPR=PTRP
- 1071 IF (NN.EQ.NPOS) GO TO 1072 PTRP=PTRPR*(! O+INCR*NN) GO TO 1300
- 1072 PTRP=PTRPR GO TO 90
- 1080 IF (NN.EQ NPOS) GO TO 1081 CO2W=CO2I*(1.O+INCR*NN)*JCO2W CO2D=CO2I*(1 O+INCR*NN)*JCO2D CO2DD=CO2I*(1.O+INCR*NN)*JCO2DD GO TO 1300
- 1081 CO2W=CO2I*JCO2W CO2D=CO2I*JCO2D CO2DD=CO2I*JCO2DD GO TO 90
- 1090 IF (NN EQ.NPOS) GO TO 1091 COW=COI*(1.0+INCR*NN)*JCOW COD=COI*(1.0+INCR*NN)*JCOD CODD=COI*(1.0+INCR*NN)*JCODD GO TO 1300
- 1091 COW=COI*JCOW
 COD=COI*JCOD
 CODD=COI*JCODD
 GO TO 90
- 1100 IF (NN.E0 NPOS) GC TO 1101 02W=02I*(1.O+INCR*NN)*JO2W 02D=02I*(1.O+INCR*NN)*JO2D 02DD=02I*(1.O+INCR*NN)*JO2DD

GO TO 1300 1101 02W=02I*J02W 02D=02I*J02D 02DD=02I*J02DD GO TO 90

- 1110 IF (NN.EQ.NPOS) GO TO 1111
 HCCW=HCCI*(1.O+INCR*NN)*JHCCW
 HCCD=HCCI*(1.O+INCR*NN)*JHCCD
 HCCDD=HCCI*(1.O+INCR*NN)*JHCCDD
 GO TO 1300
- 1111 HCCW=HCCI*JHCCW HCCD=HCCI*JHCCD HCCDD=HCCI*JHCCDD GO TO 90
- 1120 IF (NN.EQ.NPOS) GO TO 1121 NOW=NOI*(1.O+INCR*NN)*JNOW NOD=NOI*(1.O+INCR*NN)*JNOD NODD=NOI*(1.O+INCR*NN)*JNODD GO TO 1300
- 1121 NOW=NOI*JNOW NOD=NOI*JNOD NODD=NOI*JNODD GO TO 90
- 1130 IF (NN.EQ.NPOS) GO TO 1131
 NOXW=NOXI*(1 O+INCR*NN)*JNOXW
 NOXD=NOXI*(1 O+INCR*NN)*JNOXD
 NOXDD=NOXI*(1 O+INCR*NN)*JNOXDD
 GO TO 1300
- 1131 NOXW=NOXI*JNOXW
 NOXD=NOXI*JNOXD
 NOXDD=NOXI*JNOXDD
 GO TO 90
- 1140 IF (NN GT NNEG) GO TO 1141 XGWR=XGW
- 1141 IF (NN.EG.NPOS) GO TO 1142 XGW=XGWR*(1 O+INCR*NN) GO TO 1300
- 1142 XGW=XGWR GO TO 90
- 1150 IF (NN.GT NNEG) GO TO 1151 KR=K
- 1151 IF (NN.EQ.NPOS) GO TO 1152 K=KR*(1 O+INCR*NN) GO TO 1300
- 1152 K=KR
- 1160 IF (NN.GT.NNEG) GO TO 1161 FCHCR=FCHC
- 1161 IF (NN.EQ NPOS) GO TO 1162 FCHC=FCHCR*(1 O+INCR*NN) GO TO 1300
- 1162 FCHC=FCHCR GO TO 90
- 1170 IF (NN.GT.NNEG) GO TO 1171 FDAR=FDA
- 1171 IF (NN.EQ.NPOS) GO TO 1172 FDA=FDAR*(1.O+INCR*NN) GO TO 1300
- 1172 FDA=FDAR C02W=C02I*JC02W

```
CO2D=CO2I*JCO2D
     CO2DD=CO2I*JCO2DD
     COW=COI*JCOW
     COD=COI*JCOD
     CODD=COI*JCODD
     02W=02I*J02W
     02D=02I*J02D
     02DD=02I*J02DD
     HCCW=HCCI*JHCCW
     HCCD=HCCI*JHCCD
     HCCDD=HCCI*JHCCDD
     WOW=WOI*JNOW
     NOD=NOI*JNOD
     NODD=NOI*JNODD
     WXONC*IXON=WXON
     NOXD=NOXI*JNOXD
     NOXDD=NOXI*JNOXDD
     GO TO 90
1300 CONTINUE
     IF (NN. EQ. NPOS) GO TO 90
     CO2=CO2W+CO2D+CO2DD
     CO=COW+COD+CODD
     02=02W+02D+02DD
     HCC=HCCW+HCCD+HCCDD
     NO=NOW+NOD+NODD
     NOX=NOXW+NOXD+NOXDD
     GO TO (30,40,40,40,40), METH
     METHOD 1.1 (SIMPLE K, WET MEASUREMENTS ONLY) ********
  30 MET=1.1
     IF (CO2W.LT 1.) GO TO 32
IF (COW.LT.1.) GO TO 32
     GO TO 34
  32 WRITE (12,135)
     GO TO 0
  34 CONTINUE
     N202=79, 01/20, 99
     AR02=0. 0
     0.0202 = 0.0
     AIR02=4.764
     N2A=79, 01
     02A=20, 99
     ARA=0. 0
     MWAIR=28.97
     H2002=0 0
     DATA A1/2. 0, 4*0 0, 1. 0, 2*0 0, -1 0, 0. 0, -2. 0, 1. 0, 2*0. 0, -2. 0, 5*0. 0/
     A1(1,5)=(COW+2,*(CO2W+O2W))/1E6
     A1(2.5) = (C02W + C0W + HCCW)/1E6
     A1(3,2)=HTCR
     A1(3/5)=EHCR*HCCW/1E6
     A1(4,4) = -K*C02W/C0W
     CALL CRT4
     KWD=1.0-X(3)
     AA=X(1)
     FF=X(2)
     XCO2=CO2W/1E6
     XC0=C0W/1E6
     XHC=HCCW/(EHCC*1E6)
     X02=02W/1E6
```

```
XH20=X(3)
     XH2=X(4)
     XN2=N2O2*X(1)
     XN0=0. 0
     XN02=0. 0
     XAR=0. 0
     XC=0. O
     GO TO 75
     METHOD 1.2 (EXP K); METHOD 2.1 (EXP XGW); METHOD 3.1 (K & XGW) *******
     METHOD 3. 2 (K, XGW & NOT 02) ************
  40 N202=N2AS/02AS
     ARO2=ARAS/02AS
     C0202=C02A/02AS
     AIR02=1. +N202+AR02+C0202
     N2A=(100. -C02A)/(1. +02AS/N2AS+ARAS/N2AS)
     02A=02AS*N2A/N2AS
     ARA=ARAS*N2A/N2AS
     MWAIR=, 39948*ARA+, 4400995*C02A+, 280134*N2A+, 319988*02A
     H2002=W*AIR02*MWAIR/18.01534
     WTR=PSAT/PTRP
     GO TO (30,50,50,60,70), METH
     DATA A2/1, 0, 1, 0, 14*0, 0, -1, 0, 31*0, 0, -1, 0, 13*0, 0, 2, 0, 2*1, 0,
    112*0. 0, 2*1. 0, 0, 0, 1, 0, 15*0. 0, 1, 0, 10*0. 0, 2, 0, 4*0. 0, 1, 0, 9*0. 0, 1, 0,
    25*0. 0 1. 0, 3*0. 0, 1. 0, 4*0. 0, 2. 0, 6*0. 0, 1. 0, 2*0. 0, 1. 0, 2*0. 0, 1. 0,
    30, 0, 1 0, 7*0, 0, 2, 0, 5*0, 0, 1, 0, 9*0, 0, 1, 0, 15*0, 0, 2, 0,
    415*0. 0, 1, 0, 11*0. 0, 2, 0, 4*0. 0, 1, 0, 14*0. 0/
  50 A2(1,7)=FCHC
      A2(3,3)=-(2.0+2.0*00202+H2002)
      A2(4.3) = -00202
      A2(4,7)=EHCC
      A2(5,1) = -002D/1E6
      A2(5 2) = -C02DD/1E6
      A2(5,16)=C02W/1E6
      A2(6,1) = -COD/1E6
      A2(6,2) = -CODD/1E6
      A2(6,16) = COW/1E6
      A2(7,1) = -HCCD/(1E6*EHCC)
      A2(7,2) = -HCCDD/(1E6*EHCC)
      A2(7,16) = HCCW/(1E6*EHCC)
      A2(8,1) = -02D/1E6
      A2(8,2) = -02DD/1E6
      A2(8,16)=02W/1E6
      A2(9,1) = -NOD/1E6
      A2(9,2) = -NODD/1E6
      A2(9 16)=NOW/1E6
      A2(10,1) = -(NOXD-NOD)/1E6
      A2(10 2) = -(NOXDD - NODD)/1E6
      A2(10, 16) = (NOXW-NOW)/1E6
      A2(11,3)=-2.0*H2002
      A2(11, 4) = -HTCR
      A2(11,7)=EHCR*EHCC
      A2(12,2)=-WTR
      A2(13/3) = -2.0*N202
      A2(14,3) = -AR02
      GO TO (30,51,52), METH
Ċ
      METHOD 1 2 (EXPANDED K) ********
   51 MET=1 2
      A2(15,5)=0.0
```

A2(15,6)=0.0

```
A2(15,7)=0.0
      A2(15,8)=0.0
      A2(15,9)=0.0
      A2(15, 10)=0.0
      A2(15,11)=-1.0
      A2(15, 13)=0.0
      A2(15, 14)=0.0
      A2(15,15)=K*C02/C0
       A2(15, 16)=0.0
       GO TO 55
     METHOD 2.1 (EXPANDED XGW) ********
C
   52 MET=2. 1
       A2(15,5)=1.0
       A2(15,6)=1.0
       A2(15,7)=1.0
       A2(15,8)=10
       A2(15, 9)=1.0
       A2(15, 10)=1.0
       A2(15,11)=1.0
       A2(15, 13)=1.0
       A2(15,14)=1.0
       A2(15, 15)=1.0
       A2(15,16)=XGW
       GO TO 55
    55 CALL CRT15
       KWD=X(1)
       KWDD=X(2)
       AA=X(3)
       FF=X(4)
       XCO2=X(5)
       XCO=X(6)
       XHC=X(7)
       X02=X(8)
       XNO=X(9)
       XN02=X(10)
       XH20=X(11)
       XN2=X(13)
       XAR=X(14)
       XH2=X(15)
       XC=0. 0
       GO TO 75
       METHOD 3.1 (K & XGW) ***********
 C
       DATA A3/2*1. 0, 15*0. 0, -1. 0, 45*0. 0, -1. 0, 2*0 0, 2. 0, 0. 0, 1. 0, 5*0 0, 1. 0,
       14*0. 0, 1. 0. 2*0. 0, 1 0, 2*0. 0, 1. 0, 4*0. 0, 1 0, 4*0. 0, 1. 0, 6*0. 0, 1. 0, 3*0. 0,
      21 0, 7*0, 0, 2 0, 4*0, 0, 1, 0, 2*0, 0, 1, 0, 7*0, 0, 1, 0, 5*0, 0, 1, 0, 0, 0, 1 0,
       30. 0, 1, 0, 5*0. 0, 2, 0, 6*0. 0, 2*1. 0, 0, 0, 1, 0, 3*0. 0, 1, 0, 0, 0, 1, 0, 2, 0,
       46*0 0, 1, 0, 3*0, 0, -1, 0, 2*0, 0, 1, 0, 9*0, 0, 1, 0, 14*0 0, 1, 0, 0, 0, 2, 0,
       513*0 0, 1, 0, 2*0 0, 1 0, 5*0, 0, 2, 0, 6*0, 0, 1, 0, 20*0, 0, 2*1, 0, 15*0, 0/
    60 MET=3. 1
        A3(1,7)=FCHC
        A3(3,3)=-(2.0+2.0*C0202+H2002)
        A3(4,3)=-2.0*H2002
        A3(4,4)=-HTCR
        A3(4,7)=EHCR*EHCC
        A3(5,1) = -C02D/1E6
        A3(5,2) = -002DD/1E6
        A3(5,17)=C02W/1E6
        A3(6,1)=-COD/1E6
        A3(6,2) = -CODD/1E6
        A3(6,17)=COW/1E6
```

```
A3(7,1) = -HCCD/(1E6*EHCC)
      A3(7,2) = -HCCDD/(1E6*EHCC)
      A3(7,17) = HCCW/(1E6*EHCC)
      A3(8,1)=-02D/1E6
      A3(8,2) = -02DD/1E6
      A3(8,17)=02W/1E6
      A3(9,1) = -NOD/1E6
      A3(9,2)=-NODD/1E6
      A3(9,17)=NOW/1E6
      A3(10,1)=-(NOXD-NOD)/1E6
      A3(10,2)=-(NOXDD-NODD)/1E6
      A3(10,17) = (NOXW-NOW)/1E6
      A3(11,17)=XGW
      A3(12,2)=-WTR
      A3(13,3)=-2.0*N202
      A3(14,3) = -AR02
      A3(15,15)=K*C02/C0
      A3(16,3) = -00202
      A3(16,7)=EHCC
      CALL CRT16
      KWD=X(1)
      KWDD=X(2)
      AA=X(3)
      FF=X(4)
      XCO2=X(5)
       XCO=X(3)
       XHC=X(7)
       XO2=X(8)
       XNO=X(9)
       XNO2=X(10)
       XH20=X(11)
       XN2=X(13)
       XAR=X(14)
       XH2=X(15)
       XC = X(16)
       GO TO 75
      METHOD 3 2 (K, XGW, BUT 02 NOT REQ/D) ************
C
      DATA A4/1 0,-1, 0, 11*0, 0, 1, 0, 25*0, 0, 1, 0, 11*0, 0, -1, 0, 1, 0,
     19*0 0, 0, 5, -1, 0, 0, 0, 1, 0, 8*0 0, 1, 0, 3*0, 0, 1, 0, 7*0, 0,
     2\text{--}0,\ 5,\ 4\text{+}0,\ 0,\ 1,\ 0,\ 4\text{+}0,\ 0,\ 1,\ 0,\ 0,\ 0,\ 0,\ 5,\ 5\text{+}0,\ 0,\ -2,\ 0,
     32*0, 0, -1 0, 0 0, -1, 0, 7*0, 0, 1, 0, 4*0, 0, 1, 0, 7*0, 0,
     4-1 0,3*0.0,1.0,5*0.0,-2.0,5*0.0,1.0,9*0.0/
   70 MET=3, 2
       A4(1,7)=FCHC
       A4(1,13) = XGW
       A4(3,3)=1.0+C0202+H2002/2.0+N202
       A4(4.3)=00202
       A4(4,7) = -EHCC
       A4(5,1) = -C02D/1E6
       A4(5,2)=-C02DD/1E6
       A4(5,13)=C02W/1E6
       A4(6.1) = -COD/1E6
       A4(6,2) = -CODD/1E6
       A4(6,13)=COW/1E6
       A4(7,1) = -HCCD/(1E6*EHCC)
       A4(7,2) = -HCCDD/(1E6*EHCC)
       A4(7,13)=HCCW/(1E6*EHCC)
       A4(8,1) = -(NOXD-NOD)/1E6
       A4(8,2)=-(NOXDD-NODD)/1E6
       A4(8,13) = (NOXW-NGW)/1E6
       A4(9,3)=2.0*H2002
```

```
A4(9,4)=HTCR
  A4(9,7) = -EHCR*EHCC
  A4(10,2)=-WTR
  A4(11,3)=ARO2
  A4(12,12)=K*C02/C0
  CALL CRT12
  KWD=X(1)
  KWDD=X(2)
  AA=X(3)
  FF=X(4)
  XCO2=X(5)
  XCO=X(6)
  XHC=X(7)
  X02=0.-0
  XN0=0. 0
  XN02=X(8)
  XH20=X(9)
  XN2=0. 0
  XAR=X(11)
  XH2=X(12)
  XC=0. 0
75 IF (FLAG. EQ. 1) GO TO 80
  IF (FDA. EQ. 0) GO TO 80
  FLAG=1
  DA02=AIR02+H2002
   V1=FDA/DA02
   V2=AIR02*V1
   CO2W=((CO2I+V1*CO2O2)*JCO2W)/(1.O+FDA)
   CO2D=((CO2I*KWD+V1*CO2O2)*JCO2D)/(KWD+V2)
   CO2DD=((CO2I*KWDD+V1*CO2O2)*JCO2DD)/(KWDD+V4)
   COW=(COI*JCOW)/(1.0+FDA)
   COD=(COI*KWD*JCOD)/(KWD+V2)
   CODD=(COI*KWDD*JCODD)/(KWDD+V2)
   02W=((02I+V1)*J02W)/(1.0+FDA)
   02D=((02I*KWD+V1)*J02D)/(KWD+V2)
   02DD=((02I*KWDD+V1)*J02DD)/(KWDD+V2)
   HOCW=(HCCI*JHCCW/EHCC)/(1.0+FDA)
   HCCD=(HCCI*KWD*JHCCD/EHCC)/(KWD+V2)
   HCCDD=(HCCI*KWDD*JHCCDD/EHCC)/(KWDD+V2)
   NOW=(NOI*JNOW)/(1.0+FDA)
   NOD=(NOI*KWD*JNOD)/(KWD+V2)
   NODD=(NOI*KWDD*JNODD)/(KWDD+V2)
   NOXW≃(NOXI*JNOXW)/(1. O+FDA)
   NOXD=(NOXI*KWD*JNOXD)/(KWD+V2)
   NOXDD=(NOXI*KWDD*JNOXDD)/(KWDD+V2)
   GO TO 1300
80 XTC=XCO2+XCO+XHC+XO2+XNO+XNO2+XH2O+XN2+XAR+XH2+XC
   FACAL=FF*(12.01115+1.00797*HTCR)/(AIRO2*MWAIR*AA)
   ERROR=(FACAL-FAM)*100. /FAM
   PHIM=FAM*(HTCR/4, +1, )*AIRO2*MWAIR/(12, 01115+1, 00797*HTCR)
   PHICAL=PHIM*FACAL/FAM
   MWEXH=(44 00995*XC02+28.01055*XC0+(12.01115+1.00797*EHCR)*EHCC
  1*XHC+31 9988*X02+18.01534*XH20+2.01594*XH2+28.0134*XN2+
  230 0061*XN0+46, 0055*XN02+39, 948*XAR+12, 01115*XC)/XTC
```

```
IF (J. GT. O) GO TO 81
    WRITE(12, 120) RUN
    WRITE(12, 130) CO2D, COD, O2D, HCCD, NOD, NOXD
    WRITE(12, 131)CO2DD, CODD, O2DD, HCCDD, NODD, NOXDD
    WRITE(12, 132)CO2W, COW, O2W, HCCW, NOW, NOXW
    WRITE(12, 100)
    WRITE(12, 110) HTCR, EHCC, EHCR, CO2A, PSAT, PTRP, W, N2O2
    WRITE(12, 181).
 81 J=J+1
    IF (DISP1.EQ.O) GO TO 83
    IF (DISPS. GT. 1) GO TO 811
    IF (J. GT. 1) GO TO 82
811 WRITE(12, 165)
 82 WRITE(12, 166)CO2, CO, O2, HCC, NO, NOX, FCHC, FDA, MET, XTC, FACAL, FAM, ERROR
 83 IF (DISP2 EQ. 0) GO TO 85
    IF (DISPS.GT.1) GO TO 831
    IF (J. GT. 1) GO TO 84
831 WRITE(12,160)
 84 GO TO (841,841,842,841,841), METH
841 WRITE(12, 170) MET, XTC, K, KWDD, KWD, PHIM, MWEXH, PHICAL, FACAL, FAM, ERROR
    GO TO 85
842 WRITE(12, 170) MET, XTC, Z, KWDD, KWD, PHIM, MWEXH, PHICAL, FACAL, FAM, ERROR
 85 IF (DISP3.EQ.O) GO TO 87
    IF (DISPS. GT 1) GO TO 851
    IF (J. GT. 1) GO TO 86
851 WRITE(12,140)
 86 WRITE(12, 150)XCO2, XCO, XHC, XO2, XH2O, XH2, XN2, XN0, XN02, XAR, XC
 87 IF (DISP4.EQ.O) GO TO 89
    IF (DISPS GT 1) GO TO 871
    IF (J. GT. 1) GO TO 88
871 WRITE(12/163)
 88 WRITE(12, 164)N202, CO2A, W, HTCR, EHCC, EHCR, XGW, K, MET, KWD, FACAL,
   1FAM, ERROR
 89 IF (DISPS. EQ. 1) GO TO 891
    WRITE(12, 181)
891 IF (IMETH. EQ. 0) GO TO 0
    METH=METH+IMETH
    IF (METH LT METHMX) GO TO 27
    METH=METHR
    GO TO 0
 90 CONTINUE
 24 CONTINUE
```

24 CONTINUE STOP END Appendix C

```
SUBROUTINE CRT4
    INTEGER C
    DIMENSION A1(4,5), B(16,17), X(16)
    COMMON/INIT/B, X
    COMMON/INIT1/A1
    DO 1 I=1,16
    DO 1 J=1,17
    B(I,J)=0
 1 CONTINUE
    DO 2 I=1,16
    X(I)=0
 2 CONTINUE
    DO 3 I=1,4
    B(I,1)=A1(I,1)
 3 CONTINUE
    DO 4 J=2,5
    B(1,J)=A1(1,J)/A1(1,1)
 4 CONTINUE
    DO 8 C=2,4
    J=C
    DO 6 I=J,4
    SUM=0
    J1=J-1
    DO 5 K=1, J1
    \mathsf{SUM=SUM+B(I,K)*B(K,J)}
 5 CONTINUE
    B(I,J)=A1(I,J) SUM
 6 CONTINUE
    ل=I
    I1=I+1
    DO 8 J=I1,5
    SUM=0
    J1 = J - 1
    DO 7 K=1, J1
    \mathsf{SUM} = \mathsf{SUM} + \mathsf{B}(\mathsf{I}_{\mathsf{F}}\mathsf{K}) * \mathsf{B}(\mathsf{k}_{\mathsf{F}}\mathsf{J})
 7 CONTINUE
    B(I, J) = (A1(I, J) - SUM)/B(I, I)
 8 CONTINUE
    X(4)=B(4/5)
    DO 10 L=2,4
    I=4+1-L
    SUM=0
    I1=I+1
    DO 9 K=I1,4
    SUM=SUM+B(I.K)*X(K)
9 CONTINUE
    X(I)=B(I,5)-SUM
10 CONTINUE
    RETURN
```

END

Appendix D

```
SUBROUTINE CRT12
   INTEGER C
   DIMENSION A4(12,13), B(16,17), X(16)
   COMMON/INIT/B, X
   COMMON/INIT4/A4
   DO 1 I=1,16
   DO 1 J=1,17
B(I,J)=0
1 CONTINUE
   DO 2 I=1,16
   X(I)=0
2 CONTINUE
   DO 3 I=1,12
   B(I,1)=A4(I,1)
3 CONTINUE
   DO 4 J=2,13
   B(1,J)=A4(1,J)/A4(1,1)
4 CONTINUE
   DO 8 C=2,12
   J=C
   DO 6 I=J, 12
   SUM=0
   J1=J-1
   DO 5 K=1, J1
   SUM=SUM+B(I,K)*B(K,J)
5 CONTINUE
   B(I,J)=A4(I,J)-SUM
6 CONTINUE
   I=J
   I1 = I + 1
   DO 8 J=I1,13
   SUM=0
   Ji=J-1
   DO 7 K=1, U1
   SUM=SUM+B(I,K)*B(K,J)
  CONTINUE
   B(I, J) = (A4(I, J) - SUM)/B(I, I)
8 CONTINUE
   X(12)=B(12,13)
   DC 10 L=2,12
    I=12+1-L
   SUM=0
    I1=I+1
   DO 9 K=I1,12
    SUM=SUM+B(I,K)*X(K)
9 CONTINUE
   X(I)=B(I,13)-SUM
10 CONTINUE
    RETURN
    END
```

Appendix E

```
SUBROUTINE CRT15
   INTEGER C
   DIMENSION A2(15,16), B(16,17), X(16)
   COMMON/INIT/B, X
   COMMON/INIT2/A2
   DO 1 I=1,16
   DO 1 J=1,17
   B(I,J)=0
1 CONTINUE
   DO 2 I=1,16
   X(I)=0
2 CONTINUE
   DO 3 I≃1,15
   B(I, 1) = A2(I, 1)
3 CONTINUE
   DO 4 J≈2,16
   B(1,J)=A2(1,J)/A2(1,1)
4 CONTINUE
   DO 8 0-2 15
   J=C
   DO 6 1≈J,15
   SUM=0
   1 -ل=1ل
   DO 5 K≈1.J1
   SUM=SUM+B(I,K)*B(K,J)
5 CONTINUE
   B(I,J)=A2(I,J)-SUM
 6 CONTINUE
   I=J
   I1=I+1
   DO 8 J=I1,16
   $UM≃0
    J1=J-1
   DO 7 K=1, J1
   SUM=SUM+B(I,K)*B(K,J)
 7 CONTINUE
   B(I,J) = (A2(I,J) - SUM)/B(I,I)
 8 CONTINUE
    X(15)=B(15,16)
   DO 10 L=2,15
    I=15+1-L
   SUM=0
    I1=I+1
   DO 9 K=I1,15
    SUM=SUM+B(I,K)*X(K)
9 CONTINUE
    X(I)=B(I,16)-SUM
10 CONTINUE
   RETURN
   END
```

Appendix F

SUBROUTINE CRT16 INTEGER C DIMENSION A3(16,17), B(16,17) X(16) COMMON/INIT/B, X COMMON/INIT3/A3 DO 1 I=1,16 DO 1 J=1,17 B(I,J)=01 CONTINUE DO 2 I=1,16 X(I)=0CONTINUE DO 3 I=1,16 B(I,1)=A3(I,1)3 CONTINUE DO 4 J=2,17 B(1,J)=A3(1,J)/A3(1,1)4 CONTINUE DO 8 C=2,1∪ J=C DO 6 I=J, 16 SUM=0 J1=J-1 DO 5 K=1, J1 SUM=SUM+B(I,K)*B(K,J)5 CONTINUE B(I,J)=A3(I,J)-SUM6 CONTINUE I=J I1=I+1 DO 8 J=I1,17 SUM=0 J1 =J−1 DO 7 K=1, J1 SUM=SUM+B(I,K)*B(K,J) 7 CONTINUE $B(I,J) = (A \otimes (I \cup i) - SUM) / B(I,I)$ 8 CONTINUE X(16)=B(16 17) DO 10 L=2,16 I=16+1-L SUM=0 I1 = I + 1DC 9 K=I1,16 SUM=SUM+B(I, K)*X(K) 9 CONTINUE X(I)=E(I,17)-SUM 10 CONTINUE RETURN

END