

Optimizing Building Envelopes' Performance by Using Photovoltaic Cells

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This study seeks the integrity and the optimality of building envelopes' performance. It focuses on the transparent parts of buildings' façades; specifically, the windows and their shading devices. It suggests a new system of utilizing solar energy while keeping optimal solutions for indoor daylighting. It employs the shading devices on windows for producing electrical power by using photovoltaic cells. To achieve the optimality for lighting and energy production, blinds with angles from zero to ninety degrees were tested in an actual physical model. This model was used to find the correlation between the blinds' angles and the illuminance level at different distances from the window. Computational methods were used to examine the photovoltaic performance for each blinds' angle.

The mathematical equations resulted from the optimization process were coded using Java programming language to enable the future users to deal with generic locations of buildings. Furthermore, the results of the study's experiments were employed to create a blinds' control system. This system controls the blinds' movements according to the sun position and workplane illuminance level.

Nomenclature

Pow	=	generated power from photovoltaic cells
I_d	=	diffused solar insolation from the sky
I_0	=	direct solar insolation, W/m^2
Φ	=	the angle between solar altitude and the normal of the cells' surface
A_{meff}	=	air mass effect at a certain solar altitude
A	=	area of photovoltaic cell.
X	=	the distance between the blinds' slats after angling the blinds
H	=	the original distance between the blinds' slats
w	=	width of the blinds slats
θ	=	angle of blinds
lat	=	latitude
long	=	longitude
β	=	solar altitude.
E	=	total energy production in a period of time
t	=	the time difference from 7 am (7am=0, 8am =1)
t_1	=	beginning time of the day
t_2	=	end time of the day.
ln	=	the natural logarithm function with base e .
EW	=	the illuminance level at workplane at distance d
E_A	=	outside illuminance at vertical surfaces
d	=	the distance from window
Fc	=	foot-candle
OBA	=	optimal blinds' angle
W	=	Watt

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I. Introduction

Building envelopes are normally designed for many physical purposes; in this study, the major concern is to enhance the performance of building facades in terms of solar energy and indoor daylight. The most active parts of building skins are the windows; a good window design is not an easy task if we consider the integrity between daylighting and energy consumption in buildings. It is essential that the solar energy projected on windows be controlled and utilized effectively.

As the illuminance level on the workplane should not exceed the standard limits, and only a small portion of the solar energy is needed for indoor daylighting, there should be some effective ways to utilize the entire solar energy projected on windows.

This study proposes placing moveable blinds on windows to act as shading devices and installing photovoltaic cells on the slats of these blinds to absorb the remainder solar energy and convert it into electrical power.

To achieve this goal, this study seeks optimal blinds' angles that 1) maintain the indoor illuminance level within the acceptable range for human visual comfort; 2) maximize the energy production from the photovoltaic cells placed on the blinds; 3) minimize the heat gain in summer and maximizing it in winter.

To trap all the solar energy falling on windows, this study suggests that the blinds be located between two glass layers. This solution helps control the amount of heat gain in summer and winter.

II. The influential treatments

The previous studies about solar energy and blinds explored the strong mathematical relation between the blinds' angle and the illuminance level inside the space¹. Likewise, most building envelopes' parameters have been studied to find out their effect on the heat gain in buildings. Glass conductivity, window size, glass absorbance, wall thickness, are examples of variables that have been studied so far². Furthermore, new methods for self-responsive thermo tropic glass have been presented to reduce the solar radiation in summer³.

In this study, the focus is on the integrity between solar energy and daylight; therefore only the interdependent variables are tested to find the correlation between daylight and energy production. The blinds' angle is the most important treatment that affects simultaneously the three major dependent variables, the heat gain, the daylight, and the energy production from the photovoltaic cells placed on the blinds.

III. The theme of measuring blinds' angles

The radiation of lighting and heat happens among surfaces; in buildings, the main source of radiation is the windows. Using blinds as shading devices on windows changes the conditions of radiation and creates a new geometrical situation. This section explores the importance of blinds' angles measurements for lighting, heat gain, and energy production from photovoltaic cells placed on the blinds.

A. Blinds' angles and photovoltaic cells

Refer to Fig. 1, the angle of the blinds θ and the incident angle Φ have a sum of 90, $\theta + \Phi = 90$ and $\Phi = 90 - \theta$. The generated energy from the photovoltaic cells placed on the blinds is fully related to the angle between the solar altitude and the normal of the blinds' surface based on the following equation:

$$Pow (W/m^2) = 0.18 [Id + A_{meff} I_0 A \cos (\Phi)] \quad (1)$$

As $\Phi = 90 - \theta$, then any change in the blinds' angle θ changes the value of Φ and eventually affects the generated power from the photovoltaic cells. In addition, blinds' angles affect the areas of photovoltaic cells that might be obstructed by the upper slats of the blinds. Figure 2 shows the relation between the blinds' angles and the maximum solar profile angle that keeps the photocells uncovered by the upper slats.

¹Kwang-Wook Park , Andreas K.Athienitis, "Workplane Illuminance Prediction Method for Daylighting Control Systems," *Solar Energy*, Vol. 75, 2003, pp. 277 –284.

² Cheol-Soo Park, Godfried Augenbroe, Tahar Messadi, "Daylighting Optimization in Smart Façade Systems," *Eighth International IBPSA Conference*, Eindhoven, Netherlands August 11-14, 2003, pp. 1001-1008.

³ Takashi Inoue, "Solar Shading and Daylighting by Means of Autonomous Responsive Dimming Glass: practical applications," *Energy and buildings*, Vol. 35, 2003, pp. 463-471

B. Blinds' angles and heat gain

Figure 3 shows the distance X that is wholly dependent on the blinds' angle θ . If this angle is zero then the value of X will be the highest and equal to the original distance between the blinds' slats. When the blinds' angle approaches 90° the value of X approaches zero. The relation between the blinds' angle θ and the value of x is given by:

$$X = H - 2w \sin(\theta) \quad (2)$$

The radiating heat through the blinds depends on the distance between the slats and the reflection of solar radiation from the slats going into the space. When the blinds' angle gets changed, the value of X gets changed as well. This gives specific thermal conditions for every blind's angle and eventually affects the amount of heat gain for each angle.

In this study, heat gain is not the only concern; rather, the study focuses on the interconnectivity among heat gain, energy production from the photovoltaic cells, and the indoor light level. Changing blinds' angles to reduce the heat gain should take into account the effect on daylighting and the energy production. Therefore, the effect blinds' angles is studied to reach an integrated and optimal situation.

C. Blinds' angles and workplane illuminance

Using the traditional methods to measure light flux among surfaces needs calculating the angular and geometrical factors among all radiating surfaces in the space. When the blinds are used with a high number of slats on windows, a great number of reflecting surfaces with a high number of angular factors among these surfaces and the work plane need to be calculated. Practically speaking, it is hard to divide the blinds into small pixels and estimate the angular factor for every pixel. In reality, a point at workplane receives light from the blinds' slats with different angular factors. Changing blinds' angles creates a new situation with new angular and geometrical factors; this eventually affects the illuminance level on the workplane.

The sum of all reflected light from the blinds' surfaces on the workplane is a function of blinds' angle change; at the same time this light comes from the blinds in different directions and is impractical to be calculated accurately (Fig. 4). Therefore, it was necessary to conduct lighting experiments to estimate the total illumination reflected from the blinds on the workplane.

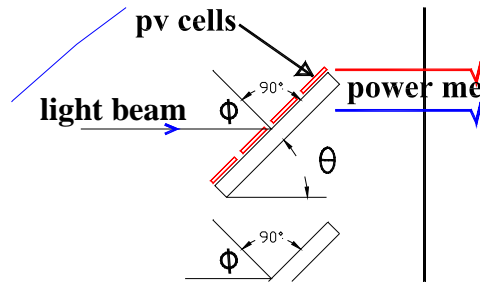


Figure 1. An explanation for all angles affecting the generated energy from the photocells.

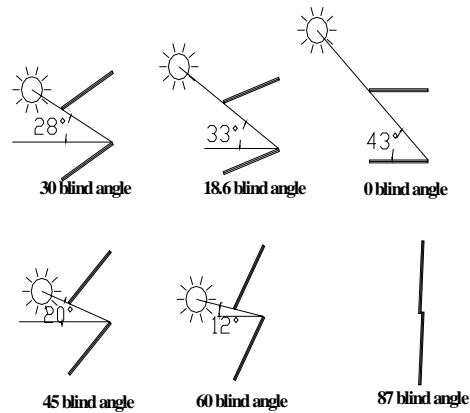


Figure 2. The minimum solar profile that covers the entire photocell for different blind angles.

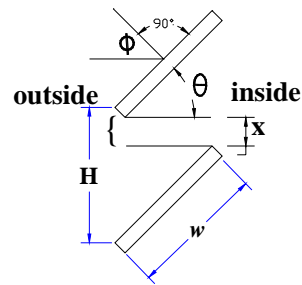


Figure 3. The relation between blind angles and the area between blinds' slats.

IV. Research methods

The study adopted two research approaches; for lighting measurements, an experimental strategy was used in a full-scale physical model. For photovoltaic cells' performance, a computational approach was used and compared with a number of actual measurements for electrical currents and voltages.

A. Experimentation

The main objectives of the lighting experiments were as follows:

- 1 Estimate the effect of blinds on horizontal workplane illuminance level;
- 2 Measure the effect of blinds on illuminance level at different distances from the window;
- 3 Estimate the relation between the vertical illuminance level outside the blinds and the vertical illuminance level inside the blinds;
- 4 Measure the change in illuminance level on vertical surfaces with blinds' angle change;
- 5 Measure the effect of wall reflections on the workplane illuminance level; and
- 6 Estimate the effect of the outside illuminance level change on workplane illuminance level.

To achieve the aforementioned objectives, a full-scale model was built in the city of Dexter, Michigan (lat. = 42, long. = 83). The model was 12 ft x 9 ft x 8 ft and had one window, 3.5 ft x 3.5 ft, located in the southern side. The blinds were placed on the window outside the glass and the transmittance factor of the glass was 0.90. The walls and the ceiling had the same finishing material. The blinds were made of white wood with a reflection of 60%; they consisted of 2-inch-wide slats with 2 inches of space between every two slats (Fig. 5).

The workplane reference point was located 7 ft from the window and 4.5 ft from the two sidewalls of the office. Other reference points were located 20 inches apart at the midline from the window to the opposite wall (Fig. 6 and Fig. 7).

The measurements were taken at all reference points (Fig. 8) by light sensors. The purpose of these measurements was to find the mathematical relation between the illuminance level at ref. point A and the other ref. points at B, C, D, E, and W (Fig. 9).

B. Computation

A computational method was used to estimate the generated power from the photovoltaic cells. In this method it was assumed that the photovoltaic efficiency is 18 percent⁴.

As the generated power depends on the amount of solar insolation, the air mass effect on the solar energy attenuation was estimated by the following equation:

$$A_{meff} = -0.334 \ln(1/\sin\beta) + 1.0 \quad (3)$$

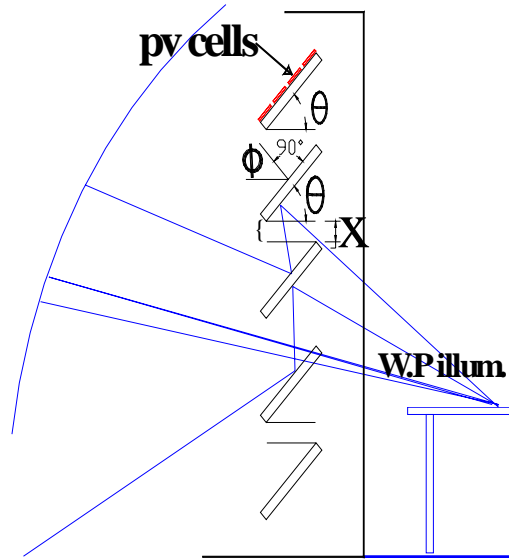


Figure 4. The effect of blind angles on light flux on the workplane illuminance level.

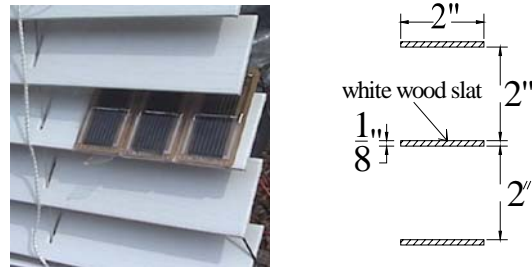


Figure 5. Details of the blind's type used in the lighting experiment.

⁴ M.A. Green, "Recent Developments in Photovoltaic", *Solar Energy* Vol. 76, 2004, pp. 3–8

The above equation was derived from the solar data in ASHRAE handbooks⁵. This equation gives the amount of solar attenuation relative to solar insolation when the solar altitude is 90. The direct solar radiation on the ground was assumed to be 1000 W/m². [Harries, 1985]⁶. The generated power and the total energy production from the photovoltaic cells were calculated by the following equations:

$$Pow(t) = 0.18 \times I_o \times A \times \cos(\Phi) \times A_{meff} \quad (4)$$

$$E(t) = \int_{t_2}^{t_1} 0.18 \times I_o \times A \times \cos(\Phi) \times A_{meff} .dt \quad (5)$$

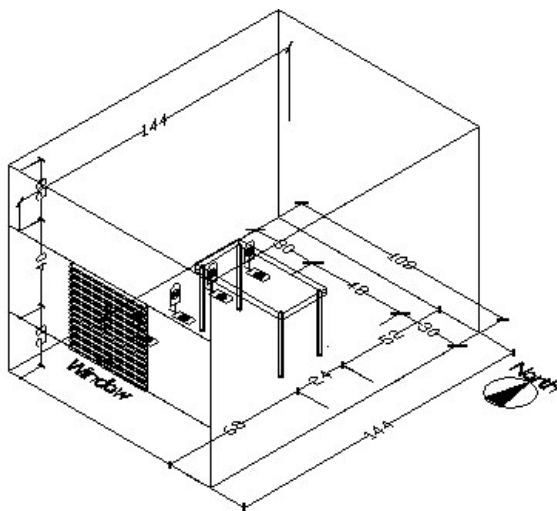


Figure 7. A general view for the experimental setting used for lighting measurements.

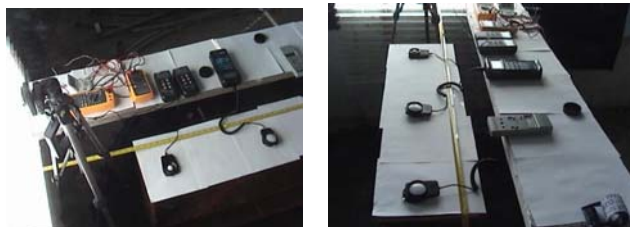


Figure 9. Light meters and sensors used to measure light level in the experiment full-scale mock-up.

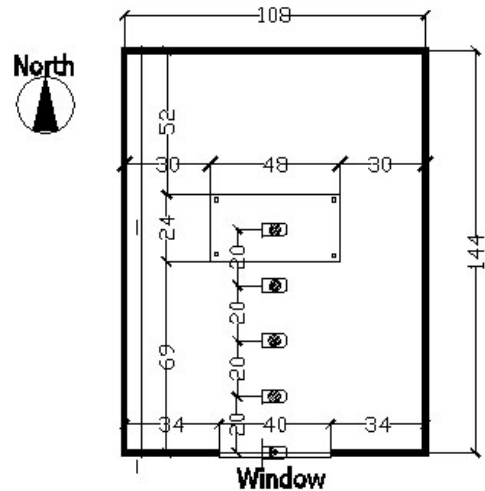


Figure 6. A plan for the experimental setting and locations of reference points and sensors.

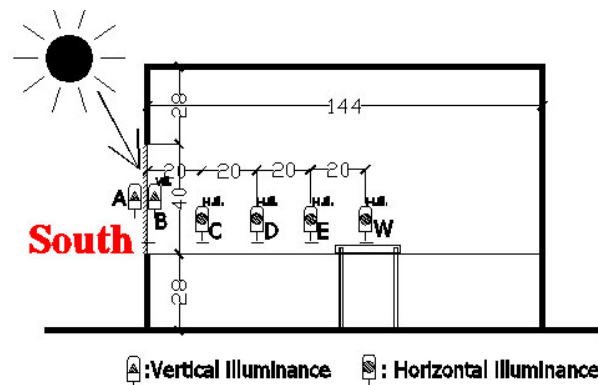


Figure 8. The reference points in the experimental setting,

- A: Outside vertical illuminance level,
- B: Average illuminance level 2 inches inside blinds,
- C: Horizontal Illuminance at 20 inches from window,
- D: Horizontal Illuminance at 40 inches from window,
- E: Horizontal Illuminance at 60 inches from window
- W: Horizontal Illuminance at workplane 80 inches from window.

⁵ ASHRAE, Faye C. McQuiston, P.E. and Jeffrey D. Spitler, P.E., *Cooling and Heating Load Calculation Manual*, second edition, Atlanta, 1992.

⁶ Harris, Miller Thomas, *Solar Energy Systems Design*, John Wiley and Sons, New York, 1985, pp. 137.

V. The experimental results and analyses

The following section discusses the experimental results for lighting and photovoltaic energy computation

A. Lighting results

The experiments showed a strong mathematical correlation between the blinds' angle changes (see Fig. 10 and Fig. 11). The results included the vertical outside illuminance level with the blinds' angles and different distances from the window as in the following equation:

$$EW=0.95e^{-0.038\theta} 0.17 (-3 \times 10^{-5} E_A^2 + 0.58 E_A) 0.97e^{-1.1829d-0.5} \quad (6)$$

To find the value of blinds' angle when the workplane is known, Eq. (6) is rewritten as follows:

$$\theta = -26.3 \ln \left[\frac{EW}{0.157(-3 \times 10^{-5} E_A^2 + 0.58 E_A) e^{-1.1829d-0.5}} \right] \quad (7)$$

B. Photovoltaic results

The energy production from the photovoltaic cells placed on the blinds was estimated for each blinds' angle as a function of time during the day.

As the solar altitude is different from season to another, the blinds' angles performances were estimated for the summer and winter seasons.

When the solar altitude is higher, the percentage of obstructed areas of the PV cells on the slats becomes greater. This caused different results between the energy production in June 21st and that in December 21st (Fig. 12 and Fig. 13).

The power from the photovoltaic cells for one slat was estimated as a function of time for winter and summer as follows:

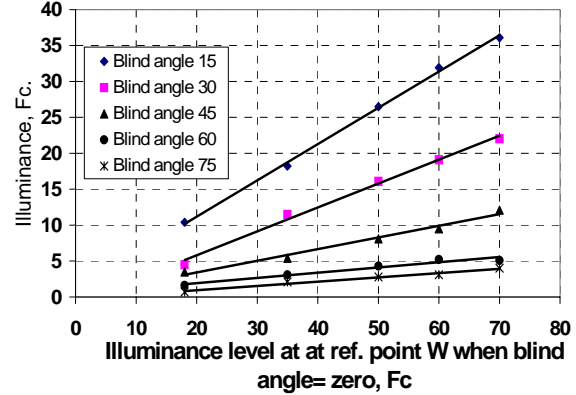


Figure 10. The relation between the illuminance at ref. point W, when the blind angle is zero, and the illuminance at the same ref. point with different blind angles.

1. The power in June 21st

$$\text{Blinds' angle } 0, \quad Pow = 0.05t^4 - 0.4t^3 + 0.75t^2 + 1.4t + 2.7 \quad (8)$$

$$\text{Blinds' angle } 18.6, \quad Pow = .04t^3 - 0.67t^2 + 2.6t + 2 \quad (9)$$

$$\text{Blinds' angle } 30, \quad Pow = 0.03t^3 - 0.56t^2 + 2.3t + 1.8 \quad (10)$$

$$\text{Blinds' angle } 45, \quad Pow = 0.02t^3 - 0.4t^2 + 1.9t + 1.1 \quad (11)$$

$$\text{Blinds' angle } 60, \quad Pow = 0.01t^3 - 0.3t^2 + 1.5t + 0.54 \quad (12)$$

2. The power in December 21st

$$\text{Blinds' angle } 0, \quad Pow = -0.06t^3 + 0.5t^2 - 0.6t + 0.7 \quad (13)$$

$$\text{Blinds' angle } 18.6, \quad Pow = -0.1t^3 + 0.8t^2 - 0.74t + 0.6 \quad (14)$$

$$\text{Blinds' angle } 30, \quad Pow = -0.15t^3 + 1.1t^2 - 0.8t + 0.6 \quad (15)$$

$$\text{Blinds' angle } 45, \quad Pow = -0.15t^3 + 1.18t^2 - 0.9t + 0.6 \quad (16)$$

$$\text{Blinds' angle } 60, \quad Pow = -0.15t^3 + 1.1t^2 - 0.67t + 0.6 \quad (17)$$

VI. Optimization

The above-mentioned equations were employed to find the optimal blinds' angles. The optimization process took into account many conditions that should exist in any indoor environment as follows:

- 1-No direct sunlight strikes the workplane.
- 2- Energy production maximized
- 3-Illuminance level maintained between 50 and 250 Fc.

Given these three conditions, the daytime hours from 9 am to 5 pm was divided into five periods in order to estimate the optimal angles.

For every time period, a minimum and maximum blinds' angle was estimated. The minimum blinds' angle maintains the illuminance level above 50 Fc, whereas the maximum blinds' angle maintains the indoor level below 250 Fc.

The blinds' angles that produce maximum energy were also estimated for each time period and checked to ensure that they lie within the acceptable range of optimal blinds' angles for lighting (Fig. 14).

For the visual criteria, an office drawing similar to the experimental setting was tested using blinds with angles 0 to 15, 30, 45, and 60. The simulation was performed by *RADIANCE* software for lighting analyses. The major concern in this simulation was to make sure that the sunlight does not go through the blinds and causes discomfort glare (Fig. 15).

The optimal angles were estimated based upon the above criteria for the 21st day of each month in the year (Fig. 16). For practical handling of the optimality curves, the mathematical relations were developed for each month as follows:

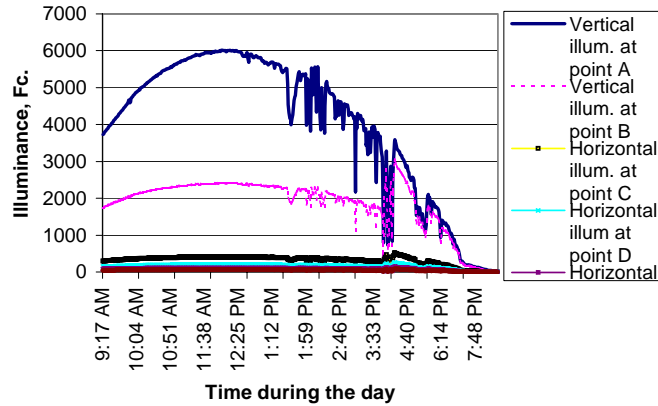


Fig. 11 Lighting readings at the reference points of lighting experiments on August 1st, 2004.

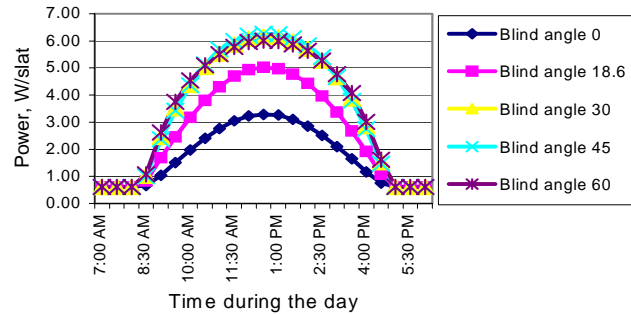


Fig. 12 The generated power from the PV cells for one slat of blinds on December 21st.

$$\text{OBA (Dec 21)} = -0.075t^4 + 1.6t^3 - 14t^2 + 54t - 57 \quad (18)$$

$$\text{OBA (Jan 21)} = -0.062t^4 + 1.3t^3 - 10t^2 + 39t - 32 \quad (19)$$

$$\text{OBA (Feb 21)} = -0.037t^4 + 0.78t^3 - 6.5t^2 + 25t - 13 \quad (20)$$

$$\text{OBA (Mar21)} = -0.0088t^5 + 0.21t^4 - 1.8t^3 + 5.4t^2 + 2.3t - 1.2 \quad (21)$$

$$\text{OBA (April 21)} = 0.0 t \quad (22)$$

$$\text{OBA (May 21)} = 0.0 t \quad (23)$$

$$\text{OBA (June 21)} = 0.0 t \quad (24)$$

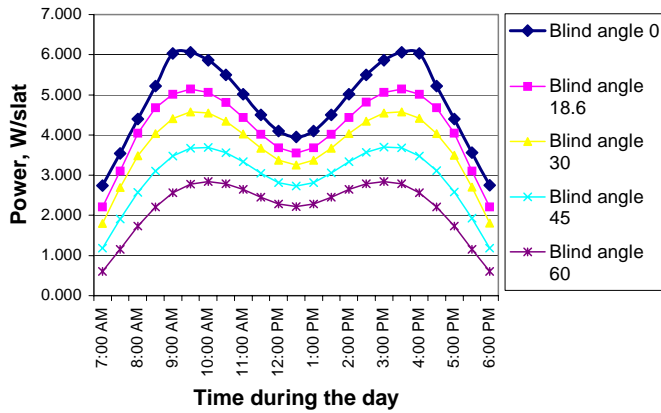


Fig. 13 The generated energy by photovoltaic cells placed on a slat one meter in length on June 21st.

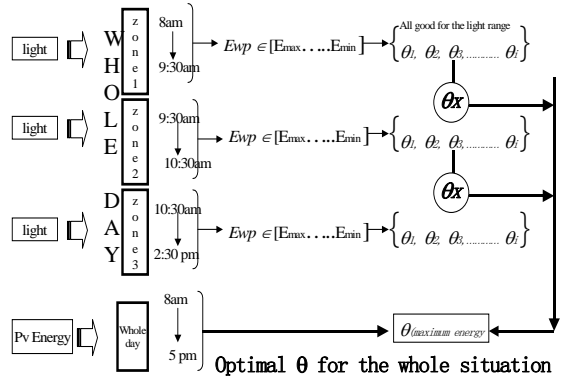
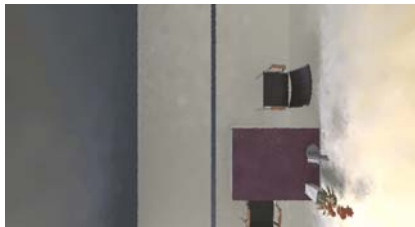


Fig.14 The optimizing process among lighting, heat gain, and generated energy from PV cells.



A



B

Fig. 15 The effect of blind angles on human visual comfort, A: light distribution in an office with discomfort glare resulted from non-optimal blind, B: light distribution in an office without glare resulted from optimal blind angle, simulated by RADIANCE software.

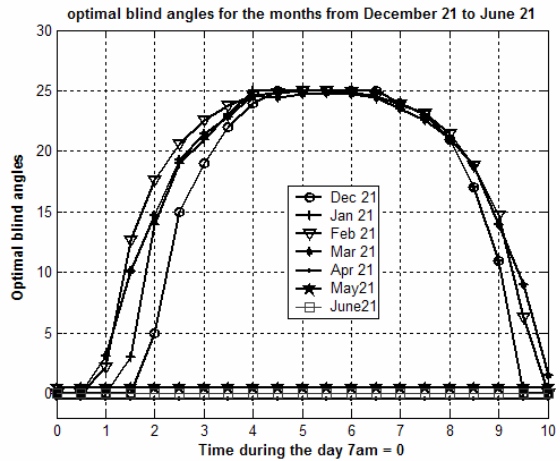


Fig. 16 Optimal blind angles estimated based on the parameters of the experimental setting.

VII. Coding

For the purpose of general applicability, the results of optimization and energy production were coded using Java programming language. The code was written to deal with generic locations and different weather conditions.

The users of this code need to input the weather data, geographical data, and space geometry. The output of this program is the optimal angles that maintain the indoor lighting within the acceptable range and maximize the energy production from the photovoltaic cells.

The logic of this code acts within the requirement of the optimality giving first priority to the indoor light level. It works with *nested loops* and *if statements* logic. The outer loop of the whole cycle is for indoor lighting that is bounded by minimum and maximum values of 50 and 250 Fc respectively. If the lighting conditions in the space are fulfilled, the second loop starts searching optimal blinds' angles for energy production from the photovoltaic cells (Fig. 17).

The output of this code takes graphical and textual format; the text format could be saved in Excel, WinWord, or txt format (Fig. 18, Fig. 19, Fig. 20, and Fig. 21).

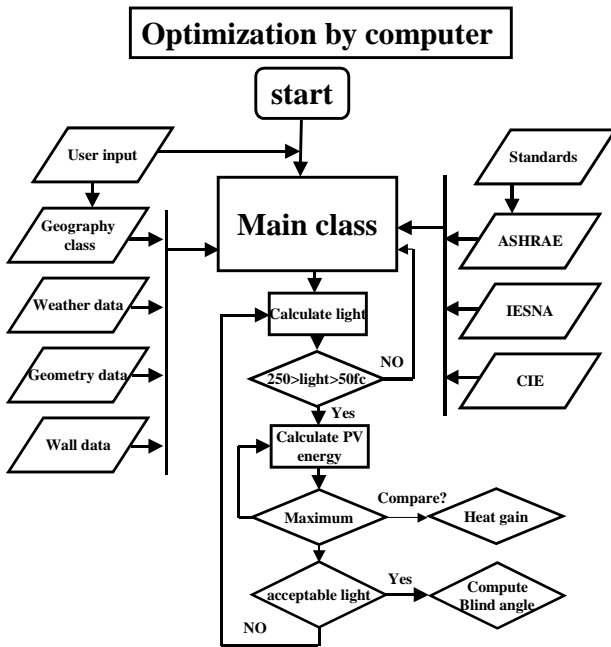


Fig. 17 Optimization method used in writing the computer code.

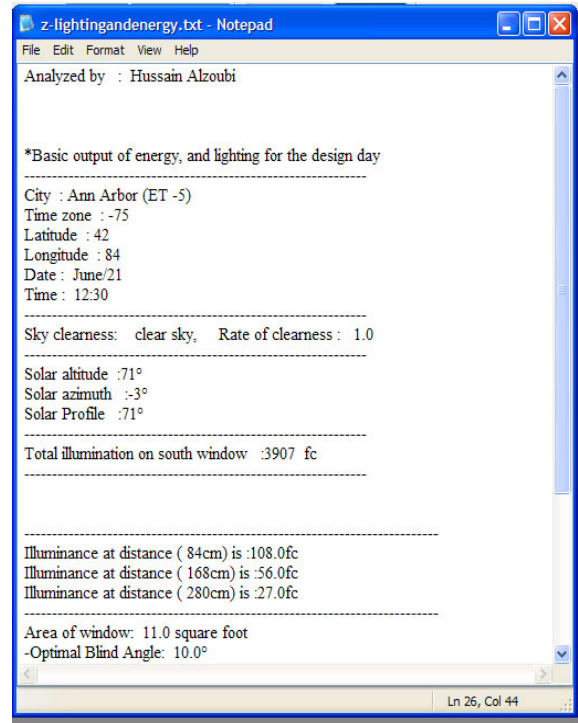


Fig. 18 A sample of output text file produced by the computer code designed for optimization.

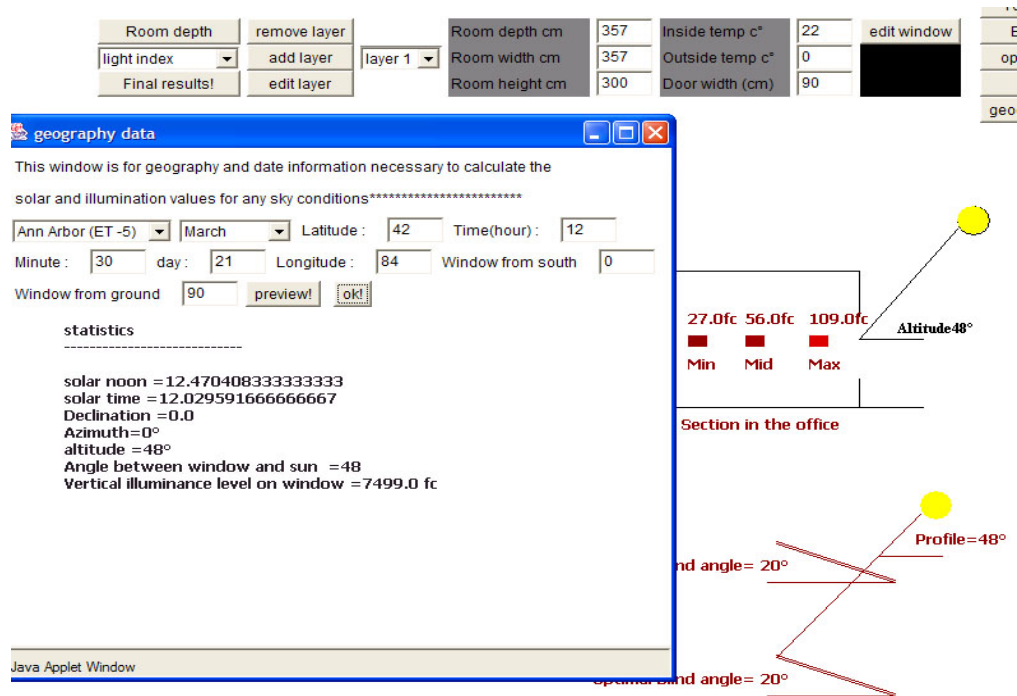


Fig. 19 An example of calling the geometry class through the main class in the optimization code.

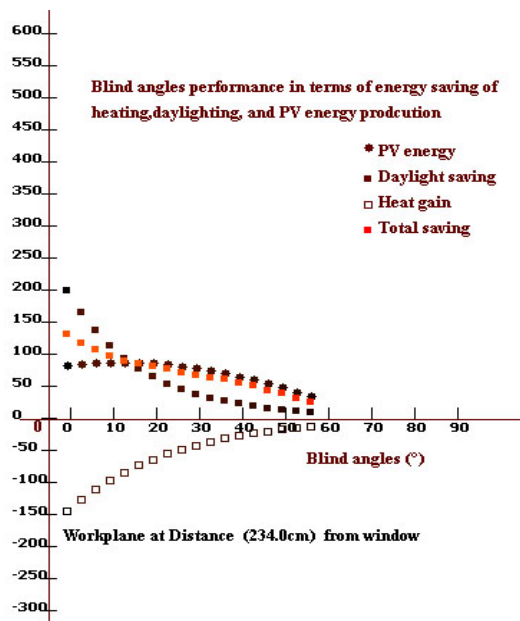


Fig. 20 Total energy saving calculated and drawn by the written computer code.

Full data analyses for blind angles at date of : 6/21
Time is : 12:30

Blind Angle	illu.level	heat gain	daylight saving	PV power
0°	80.0fc	-146W	200W	69W
5°	66.0fc	-128W	200W	71W
10°	55.0fc	-112W	200W	72W
15°	45.0fc	-99W	180W	73W
20°	37.0fc	-87W	149W	73W
25°	31.0fc	-76W	123W	72W
30°	26.0fc	-67W	102W	71W
35°	21.0fc	-58W	84W	70W
40°	17.0fc	-51W	69W	68W
45°	14.0fc	-45W	57W	65W
50°	12.0fc	-39W	47W	62W
55°	10.0fc	-35W	39W	59W
60°	8.0fc	-30W	32W	55W
65°	7.0fc	-27W	26W	50W
70°	6.0fc	-23W	22W	45W
75°	5.0fc	-20W	18W	40W
80°	4.0fc	-18W	15W	35W
85°	3.0fc	-16W	12W	29W

Optimal Blind Angle: 10.0°
Minimum incident angle : 2°
Optimum generated Power from PV : 72.0 Watt
Optimal workplane illum: 55.0fc
Distance from window: 192.0cm

Fig. 21 Computed optimal angles and related generated power estimated by the written computer code.

VIII. Control system and automation

A. Description

The algorithm used in the mentioned java code has been utilized in creating a control system programmed by C language. The system used the lighting formulas developed and derived from the experimental results to motorize the blind automatically.

The system consists of Ezio electrical board with suitable type of microchips, five major sensors for lighting, temperature, and photovoltaic cells. The system with all its components is attached with a pc to record the system data and save it in text or Excel format (Fig. 22). In this system, the blinds are sandwiched between two glass layers. The photovoltaic cells are placed on the slats of the blinds (Fig. 23). Two fans are placed on an outlet and inlet at the designed glass box containing the blinds. A 12-volt DC motor is geared with the blinds at one end; at the other end of the blind a potentiometer is attached to indicate the angle of the blinds.

B. The system's behavior

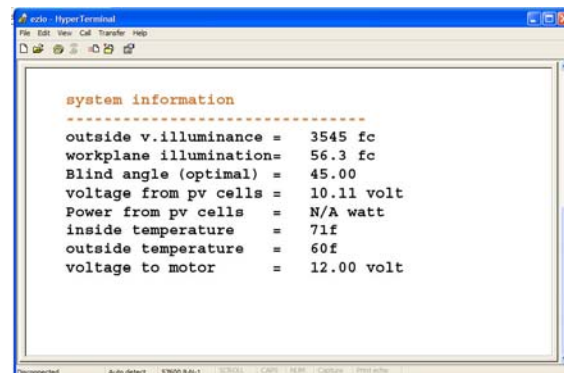
As mentioned above, the system uses five major sensors as input to the main Ezio board that controls the motor movement based upon the signals from the sensors. The lighting sensors send the light readings to the main controller in the Ezio board. If the light is below 50 Fc, the blinds stay at zero angle to allow as much light as possible getting into the space. As long as the internal light is between 50 and 250 Fc, the system starts finding the most optimal angle that maximizes the energy generated from the photovoltaic cells placed on the blinds.

The thermal sensor sends the temperature reading to the main Ezio board to determine the direction of the fans on the glass box. If the building is in the heating mode, the warm air trapped in the glass box will be blown into the space. Otherwise, if the building is in cooling mode, the warm air is kicked out of the glass box.

C. The system's performance

The system was tested in an actual office to validate the experimental results under similar conditions. The performance of this system was very similar to the predicted results. The optimal blinds' angles calibrated by the system were very close to the computed blinds' angles from the experimental results (Fig. 24). The system was also tested to measure the generated voltage from the photovoltaic cells placed on the blinds under two different conditions: the first case was estimated with fixed blinds and the other was estimated with automated blinds. The generated power by the automated blinds is higher than that generated by fixed blinds by 20 to 40 percent depending on the time during the day.

Theoretically, this system makes the angle between the normal of the photovoltaic cells and the solar altitude as small as possible. The movement of the blinds happens only if the internal light is enough and within the acceptable range. A theoretical comparison between the control system and fixed blinds at angle zero was conducted to estimate the difference in power production from the photovoltaic cells (see Fig. 25)



```
ezio - Hyperterminal
File Edit View Goto Transfer Help
-----
system information
-----
outside v.illuminance = 3545 fc
workplane illumination= 56.3 fc
Blind angle (optimal) = 45.00
voltage from pv cells = 10.11 volt
Power from pv cells = N/A watt
inside temperature = 71f
outside temperature = 60f
voltage to motor = 12.00 volt
-----
Disconnected Auto detect 57600 84+1 CTRL CAPS NUM Capture Print Info
```

Fig. 22 System's output on a monitor with hyper terminal screen.

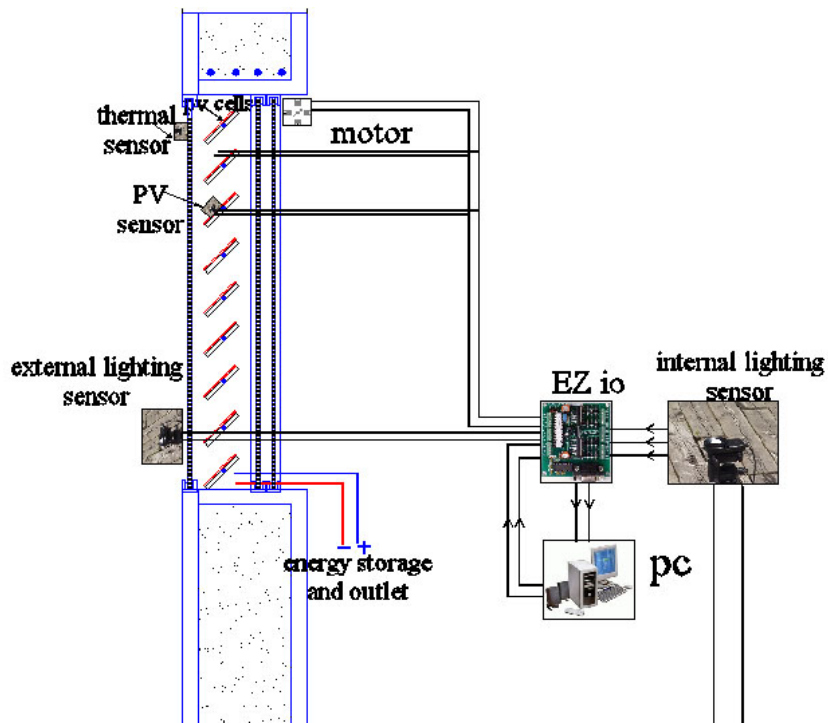


Fig. 23 A section in the control system with its major components.

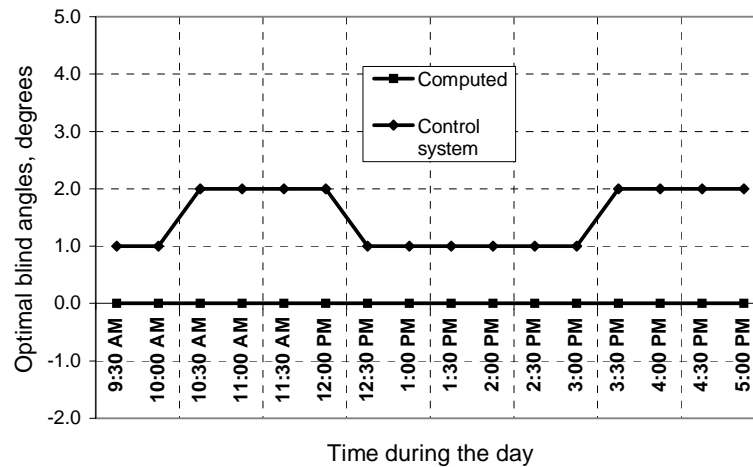


Fig. 24 A comparison between the optimal blind angles determined by the control system and computer on May 28th, 2005.

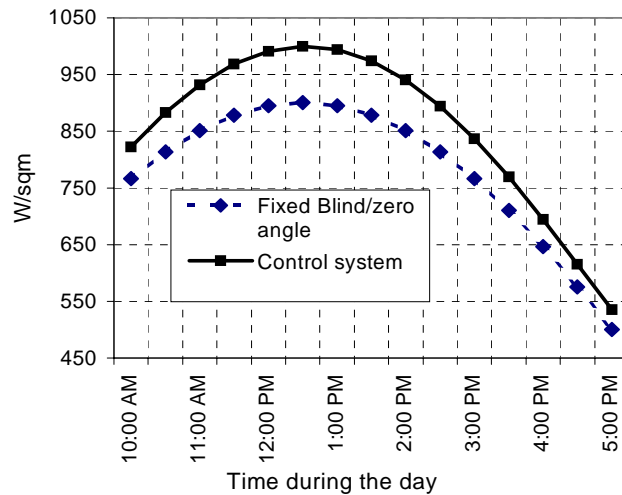


Fig. 25 Theoretical comparisons between the generated power by the computer and the control system.

IX. Conclusions

The study explored the idea of integrity in building facades' performance. It showed that optimization for lighting and energy production is possible if the blinds' angles are well adjusted to meet this goal. Automated blinds can substitute the manual solutions for blinds' adjustments.

The designed control system can adjust the blinds' angle within accuracy of ± 2 degrees compared to the manual solutions. As the experiments of this study were conducted under specific conditions, the control system presents a more flexible method to deal with generic locations in the world; it can handle any instantaneous situation as it reads the light every 0.5 second.

The power generated at noon by the control system exceeds that generated by fixed blinds' angles at angle zero degrees by almost 100 W/m^2 . This difference reaches 400 W/m^2 when the blinds tilted at angle 45° .

It should be known that the energy produced by the optimal angles is affected by keeping the indoor light within the acceptable range. The energy production becomes higher if it is not integrated with the indoor light level.

Acknowledgments

I would like to thank the Doctoral Program in Architectural at the University of Michigan for the great support and assistance. Special thanks to the chair of the doctoral program, Professor Jean Wineman, for the great support during the time of this research. I would also like to acknowledge the generous financial support from *Rackham*, the graduate school at the University of Michigan.

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