

$$\rho c^s(r) = \frac{1}{2\pi} \int_0^\infty dq q J_0(qr) \left[ \frac{4}{q^2} - \frac{1}{\exp(q^2/4) - 1} \right] \quad (4)$$

[this is equivalent to Eq. (14) of Ref. 3, by an integration by parts]. The asymptotic behavior of  $c^s(r)$  is governed by the four poles of its Fourier transform [defined by Eq. (4)] which are closest to the real axis, i.e., at  $q^2 = \pm 8i\pi$ . Keeping only the contributions of these poles gives

$$\rho c^s(r) \underset{r \rightarrow \infty}{\sim} -\frac{1}{2\pi} \int_0^\infty dq q J_0(qr) \left[ \frac{4}{q^2 + 8i\pi} - \frac{4}{q^2 - 8i\pi} \right] \\ = -(4/\pi) \ker(8^{1/2}\pi^{1/2}r), \quad (5)$$

where  $\ker$  is a Bessel function<sup>4</sup> of known asymptotic behavior:

$$\rho c^s(r) \underset{r \rightarrow \infty}{\sim} -(2/\pi)^{3/4} r^{-1/2} \\ \times \exp(-2\pi^{1/2}r) \cos[2\pi^{1/2}r + (\pi/8)]. \quad (6)$$

Thus, it is seen, on this model, that  $c(r)$  behaves asymptotically as  $-\beta v(r)$  and that the remainder  $c^s(r)$  is indeed short ranged and, more explicitly, has the exponential decay [Eq. (6)].

A second remark is about the asymptotic behavior of the "bridge function"  $B(r)$ , which is defined by

$$B(r) = \ln[1 + h(r)] - h(r) + c^s(r). \quad (7)$$

Since, here  $h(r)$  is the Gaussian  $-\exp(-r^2)$ , the bridge function  $B(r)$  has the same asymptotic behavior [Eq. (6)]

as  $c^s(r)$ . Therefore,  $B(r)$  has an exponential decay, which is slower than the Gaussian decay of  $h(r)$ . This is in contradiction with a common belief that  $B(r)$  has a faster decay. Of course, our observation might be a pathology of the present model at the special value  $\Gamma = 2$ .

It is amusing to note that, if we express  $B(r)$  as an infinite sum of graphs built with  $h$  bonds,<sup>5</sup> since  $h$  is a Gaussian, every given graph can be explicitly computed and gives a Gaussian result.<sup>6</sup> For instance,

$$\begin{aligned} \text{◇} &\sim \exp(-r^2), \\ \text{◇} \text{---} \text{◇} &\sim \exp[-(7/8)r^2], \\ \text{◇} \text{---} \text{◇} \text{---} \text{◇} &\sim \exp[-(2/3)r^2]. \end{aligned}$$

Therefore, the exponential decay of  $B(r)$  results from the infinite summation of Gaussians of increasing ranges.

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<sup>1</sup> B. Jancovici, Phys. Rev. Lett. **46**, 386 (1981).

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<sup>4</sup> I. S. Gradshteyn and I. M. Ryzhik, *Tables of Integrals, Series, and Products* (Academic, New York, 1980).

<sup>5</sup> K. Hiroike and T. Morita, Prog. Theor. Phys. **25**, 537 (1961).

<sup>6</sup> G. E. Uhlenbeck and G. W. Ford, in *Studies in Statistical Mechanics*, edited by J. de Boer and G. E. Uhlenbeck (North-Holland, Amsterdam, 1962), Vol. 1.

## ERRATA

### Erratum: The thermodynamics of ammonium scheelites. III. An analysis of the heat capacity and related data of deuterated ammonium perrhenate $\text{ND}_4\text{ReO}_4$ [J. Chem. Phys. **85**, 5963 (1986)]

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Equation (3) contains a misplaced bracket at  $C_{11}$  plus an incorrect  $2C_{13}\alpha_1\alpha_3$  term. It should read  $c_p - c_e = VT\{2(c_{11} + c_{12})\alpha_1^2 + 4c_{13}\alpha_1\alpha_3 + c_{33}\alpha_3^2\}$ .