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**EMPIRICS OF TAXES ON DIFFERENTIATED PRODUCTS:  
THE CASE OF TARIFFS IN THE U.S.  
AUTOMOBILE INDUSTRY**

by

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Empirics of Taxes on Differentiated Products:  
The Case of Tariffs in the U.S. Automobile Industry

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## I. Introduction

Recent theoretical advances in the Industrial Organization literature have provided insight into modelling the demand for differentiated products. Lancaster (1979) introduced and developed what he termed the "Characteristics Approach" to modelling the demand for differentiated products, while Dixit and Stiglitz (1977) pioneered what has come to be known as the "Love of Variety" approach to the subject. Both of these approaches have been applied to international trade theory. The result has been a heightened awareness of the role that product differentiation plays in trade theory. This work is presented in Helpman and Krugman (1985).

There have thus far been relatively few empirical applications of the new theories of trade. In this paper, I present a new technique for econometrically estimating the demand for differentiated products. I adopt a Lancasterian approach to product differentiation and use theoretical results from this approach to solve several empirical problems. I then apply the technique to the demand for automobiles.

The estimates derived from this method allow me to analyze many trade and industrial policies for the U.S. automobile industry. For example, what would be the effect of a tariff applied only to Japanese imports on the total automobile import demand? Would domestically produced auto sales replace the Japanese imports or might German and Swedish imports rise, leaving total imports relatively constant? Some economists have argued for a tariff on all small foreign cars. Such a tax does not discriminate by country of origin and hence is viewed more kindly by GATT. As foreign small cars became more costly,

would domestic car sales rise substantially or would the U.S. just trade imports of small cars for imports of larger cars? Optimal industrial policy toward the U.S. auto industry may involve subsidies to domestic producers thereby possibly lowering the price of domestic autos.<sup>1</sup> Or perhaps government policy may involve subsidizing only one producer (e.g. Chrysler). What effects would these policies have on demand for different types of foreign and domestic automobiles?

All of these questions are, in a formal sense, quite similar. Each considers the effect of a tax placed on a subset of a group of differentiated products. Parameters needed to answer questions such as those posed above are own and appropriately-defined cross price elasticities of demand. Any analysis of the taxation of differentiated products must estimate (or use existing estimates of) these demand elasticities. The approach developed in this paper provides a utility-consistent technique for deriving these elasticities. While I apply the methodology to issues of trade and industrial policy in the U.S. automobile industry, I believe that the general approach will have wider application. The methodology could, for example, be used to estimate demand elasticities in other differentiated products industries such as microcomputers, audio-video equipment, lumber, and steel. All of these industries have been the subject of recent policy debate.

This paper is a first attempt at solving some of the empirical issues associated with the analysis of taxation of differentiated products. While the paper provides some answers, it also raises a number of microeconomic and econometric issues for future research.

In Section II, I provide a brief critical review of the literature. Section III develops the methodology that is then applied in Section IV. Using

the demand system estimated in Section IV, Section V addresses many of the policy concerns posed in this introduction. Section VI concludes the paper with a brief summary.

## II. A Brief Summary of the Literature

In theory, estimating the demand system for a set of differentiated products is no different than estimating a demand system for several homogenous products. A typical estimated equation in such a system would regress quantity of a good demanded on its own price, the prices of the other differentiated or homogenous products, and several other variables such as income and personal and demographic characteristics. Food is a good example of a set of differentiated products whose demand functions are nicely estimated by standard techniques. Recent work based on Deaton and Muellbauer's Almost Ideal Demand System provide excellent examples of this approach.<sup>2</sup>

For many sets of differentiated products, though, standard techniques are inapplicable. In the case of automobiles, there are over 100 models available and few models are available for more than four consecutive years. The standard techniques would imply a system of, say, 100 equations with 99 cross price effects. With so few years of data, the system is not estimable with any degree of accuracy. In the case of VCRs or micro-computers, technology changes so quickly that no more than two or three years of data is likely to be available.

Several approaches to these problems have been taken in the empirical literature. Almost all of them have been applied to the automobile industry-- at least partially because data is relatively plentiful. I will accordingly focus on this body of research.

The easiest way around the problems posed by product differentiation is to ignore the issue. Not surprisingly, this was the approach first adopted. Work by Suits in 1958 used time series of total quantity of autos sold, average auto price, and real disposable income to arrive at aggregate demand elasticities. While it is surely unfair to judge the econometric methods of 30 years ago by the standards permitted by today's computing technology, Suits' approach is incapable of addressing the issues raised in this paper's introduction. Surprisingly, research as recent as Toder (1978) uses elasticities imputed in part from Suit's original work, when analyzing current automobile trade and industrial policy. Tarr and Morkre (1984) and Dixit (1986) in turn use elasticities derived from Toder.

Time series techniques, even modern ones, are not applicable to investigating the effects of trade policy in the U.S. automobile industry. This is because both products and tastes have changed significantly over the period of estimation (approximately the last 20 years.) A 1965 Toyota is not the same car as a 1985 Toyota. As Toyotas change, the meaning of a single (constant) elasticity of demand for Toyotas becomes unclear. Tastes for autos and the characteristics which comprise them have also changed. While it may be theoretically possible to control for the reputation effects and network externalities that are responsible for this shift of tastes, it is not easy to do so in practice.

The most recent comprehensive study of the U.S. demand for automobiles is reported in Toder et. al.'s Trade Policy and the U.S. Automobile Industry. In that book, demand elasticities are estimated using three methodologies. As most studies of the welfare effects of trade policy in the auto industry have used elasticity estimates from Toder, it is worthwhile to take a close look at



these alternative approaches. Each will be discussed in turn.

Toder's first approach is a time-series analysis. This work is more sophisticated than earlier work in that it introduces hedonic price indices.

Toder estimates the following regression:

$$\ln \left( \frac{F}{D} \right) = \alpha_0 + \alpha_1 \ln \left( \frac{P_f}{P_d} \right) + \alpha_2 \bar{Z}$$

$\frac{F}{D}$  is the foreign to domestic auto sales ratio.

$\frac{P_f}{P_d}$  is the ratio of foreign to domestic hedonic prices.

$\bar{Z}$  is a vector of exogenous variables.

The estimation uses annual data from 1960 to 1974. Estimates of  $\alpha_1$  ranged from -0.9 to -1.7, depending on the Z vector. The coefficient  $\alpha_1$  is the elasticity of substitution in demand. Using the estimate of  $\alpha_1$  and older estimates of total market demand elasticities, conventional price elasticities of demand can be derived.

There are at least four problems with this approach. First, as mentioned above, tastes seem to have changed over time, since casual empiricism suggests that a foreign car in 1960 was viewed very differently than one in 1974. As tastes vary over time, the economic relevance of the estimates of the elasticity of substitution in demand is called into question. Second, older estimates of the total market elasticity of demand are required to convert Toder's results into standard price elasticities of demand. While Toder used hedonic price indices, the older studies did not. As cars are not homogenous products, it is unclear exactly what the results of the older studies by Suits and others mean. Also, the older studies were conducted before auto imports were an empirically relevant phenomenon. Using these older out-of-sample

market elasticities to derive the standard elasticities of demand may yield very misleading results. Third, even if the time-series would yield accurate estimates, the agglomeration of all foreign cars prevents the analysis of taxes applied to only a subset of foreign autos. Fourth, regressing relative demands on relative hedonic prices does not follow from either a Lancasterian or Dixit-Stiglitz model of product differentiation. The choice of using relative demands and relative prices of domestic and foreign goods allows Toder, like all his predecessors, to estimate a single equation instead of a complete demand system. Toder's implicit assumption that an otherwise homogenous good is differentiated only by country of origin is termed the Armington Assumption. This assumption makes little sense from a consumer theory viewpoint, unless there is some basis for supposing that goods are homogenous within countries but not across countries. Toder's first approach is, then, a utility inconsistent approach to modelling demand for differentiated products.

Toder's second method employed a cross-sectional approach to the demand-estimation problem. Toder used transport costs to introduce cross-sectional price variation. The units of observation were each of the continental United States. Here the regression estimated was:

$$\frac{F}{D} = \alpha_0 + \alpha_1 \left( \frac{P_f}{P_d} \right) + \alpha_2 PC2029 + \alpha_3 PCI + \alpha_4 PGAS$$

where:  $\frac{F}{D}$  is the ratio of foreign to domestic new car sales.

$\frac{P_f}{P_d}$  is the ratio of delivered foreign to domestic list prices.

PC2029 is the percentage of population between ages 20 and 29.

PGAS is the price of gasoline.

While the problems of time varying parameters are not present in this cross-sectional approach, this method still relies on previously derived market

elasticities to construct conventional price elasticities of demand. The cross-sectional methodology yielded generally unsatisfactory results. This is not surprising, since one might suspect that variables other than transport costs, gasoline costs, per capita income, and the percentage of population in their 20's explain why foreign cars are more predominant in New Jersey or California than they are in Michigan or Indiana.

Toder's third approach is by far the most innovative. Although computationally complex, the intuition behind this methodology--termed a hedonic market share model-- is straightforward.

The model requires only one year's data on sales, list prices and characteristics of automobiles. Let  $\{\alpha_n^i\}$  be the set of marginal rates of substitution between  $N$  characteristics and price. Toder et. al. posit a log-normal distribution of  $\{\alpha^i\}$  across consumers. Next, they estimate coefficients,  $\beta$ , which form a vector of sufficient statistics for the probability distribution of the  $\alpha$ 's. Let  $S$  be the vector of actual shares of auto sales by model. They next choose  $\beta$  to maximize the likelihood of observing  $S$ . In brief, the technique selects statistics describing a distribution of consumer's utility functions that reproduce as nearly as possible the actual market shares observed.

Toder et. al. then apply the estimated taste distribution to a new set of available models (differing from the old set by price) to generate a new market share distribution. In this sense, the model simulates the relevant elasticities. Unlike the previous two approaches, the hedonic market share model can, in principle, predict market share elasticities for any subset of models. In practice only a elasticity of substitution in demand between all foreign and all domestic cars is estimated. This yielded coefficients of -2.3

and -2.1 depending on the price increase simulated.

There are at least three major problems with this approach--the first two of which are related.

1. The model is computationally quite difficult. Toder uses five characteristic variables to estimate the taste distribution. Calculating the maximum likelihood estimates for  $\beta$  requires a fifth-order numerical integration between each iteration of the likelihood function maximization. The cost of such computational techniques is often prohibitive. Also, some experts at numerical analysis question the accuracy of such a high order integration of a complicated distribution function.

2. More importantly, this technique does not yield standard errors. For policy analysis, point estimates without standard errors are of limited use. Without the standard errors, it is impossible to know whether and how well the data fit the model.

3. The results of this technique hinge critically on the choice of the distribution function of tastes. Toder et. al. used a log-normal distribution. The choice of the distribution function is completely arbitrary yet possibly key to the results. While all non-robust estimation methods are subject to this critique, the problem is compounded here by the lack of standard errors of the estimates. Without the standard errors, it is especially difficult to ascertain whether the distribution function of tastes chosen fits the model.

Bresnahan (1981) also models the demand for automobiles. Using sophisticated econometric techniques, he accounts for product differentiation and avoids the pitfalls of time-series analysis. His goal, though, is more

ambitious than just a model of automobile demand, as he focuses on the issue of departures from marginal cost pricing in the automobile industry. Because he looks at a broader range of issues than just the demand side of the model, his results are not disaggregated enough to analyze the questions posed in the introduction of this paper. While he does not estimate elasticities, per se, estimated parameters can be manipulated to give an industry demand elasticity (a proportionate change of all prices) of .25 and an elasticity for the average product (one price changes and all others are constant) of 3.2. Bresnahan is very forthright about the quite restrictive assumptions that he requires on the demand side of his model. The most serious of these is the assumption that the density of consumer tastes is uniform (as opposed to Toder's log-normal assumption.) Bresnahan's methodology also is computationally complex and, like Toder's hedonic market-share model, it does not yield estimates of standard errors. Bresnahan, though, approximates the variances of parameter estimates in four ways. Although variances depend on the approximation used, this does give some feel for how well the data fit the model. In short, Bresnahan's method is carefully developed, but it is not suitable for addressing the types of issues raised in the introduction of this paper.

Finally, there are a number of studies of automobile demand that investigate the question of whether or not a car is purchased at all, and if so, how many are purchased. These studies are fairly common in mode-of-transportation studies. Methods used range from simple logit to multinomial logit to multinomial probit. A quite technically sophisticated example of this approach is found in Train (1986).<sup>3</sup> These studies ask a set of questions that are for the most part only tangentially related to questions about the demand effect of taxes on differentiated products. As such, their results are not very useful to the issues with which I am concerned.<sup>4</sup>

### III. Methodology.

In this section, I explain my approach to the estimation of demand for differentiated products. I do this in two steps. In step 1, I derive a demand function that I wish to estimate. I avoid many of the pitfalls of previous approaches by relying on results from Lancasterian consumer theory. In step 2, I explain how the insights offered by Lancasterian consumer theory are empirically implemented.

Step 1: I avoid the problems associated with time-series analysis by using only three years of data--1983 to 1985.<sup>5</sup> Three years of time-series data, though, leaves few degrees of freedom. I introduce the much needed additional price quantity variation by using a cross section of (the same) 100 models of automobiles for each year. The data, then are a time-series cross section, or panel, consisting of 300 observations.<sup>6</sup>

While using panel data instead of only time-series introduces additional price-quantity variation, it also poses some problems. It may be wrong to regress quantity on price since, across observations, the good is not the same. I address these problems using results from the Characteristics Approach to product differentiation.

In the Lancasterian model of product differentiation, a good is represented by its bundle of characteristics. Different models of the good contain different bundles of these characteristics. With this view of product differentiation, as tastes vary across consumers, demands for a model, given its price, will vary with the model's characteristics bundle. Because products are identified by their bundle of characteristics, it is appropriate to control for the cross sectional variation in models by including in the demand function

those characteristics which differentiate models.<sup>7</sup>

Lancaster hence posits that the quantity demanded of a model depends on its own price and characteristics and on the price and characteristics of competing models. In log-linear form, this implies:

$$\ln Q_{it} = \alpha_0 + \alpha_1 \ln P_{it} + \alpha_2 \ln \bar{P}_{jt} + \beta' X_{it} + \Gamma' X_{jt}$$

where:  $Q_{it}$  is the quantity demanded of model  $i$  in year  $t$ .

$P_{it}$  is the price of model  $i$  in year  $t$ .

$\bar{P}_{jt}$  is the vector of prices of substitutes to a model with sales  $Q_{it}$ .

$X_{it}$  is a characteristics vector of model  $i$  in year  $t$ .

$X_{jt}$  is a characteristics vector of model  $j$  in year  $t$ .

I posit that the above model may be subject to country-of-origin specific errors, and hence use a fixed effects model. Allowing also for time dependent shifts of demand gives:

$$\ln Q_{it} = \alpha_0 + \alpha_1 \ln P_{it} + \alpha_2 \ln \bar{P}_{jt} + \beta' X_{it} + \Gamma' X_{jt} + \alpha_3 \text{JAPAN}_i + \alpha_4 \text{GERMAN}_i + \alpha_5 \text{SWEDE}_i + \alpha_6' T_t \quad (1A)$$

where:  $\text{JAPAN}_i = 1$  if model  $i$  is Japanese.

$\text{GERMAN}_i = 1$  if model  $i$  is German.

$\text{SWEDE}_i = 1$  if model  $i$  is Swedish.

$T_t$  is a time dummy for year  $t$ .

Equation (1A) is consistent with a Lancasterian approach to consumer demand for autos.

Somewhat surprisingly, Lancaster's work does not discuss the hedonic price literature. This literature posits that the price of a good is a linear combination of the implicit prices of the attributes of the good. Thus in equation (1A),  $X_{it}$  would be highly collinear with  $P_{it}$ . An analogous

relationship holds for  $X_{jt}$  and  $P_{jt}$ . According to the hedonic approach, the price of a good already contains information about the qualities of the good. Hence, estimating (1A) merely introduces severe multicollinearity. Instead, the hedonic hypothesis argues in favor of estimating the following demand function.

$$\ln Q_{it} = \alpha_1 + \alpha_2 \ln P_{it} + \alpha_2 \ln \bar{P}_{jt} + \alpha_3 \text{JAPAN}_i + \alpha_4 \text{GERMAN}_i + \alpha_5 \text{SWEDE}_i + \alpha_6' T_t \quad (1B)$$

I econometrically consider equations (1A) and (1B). In both, I assume the consumer takes as given all independent variables.

The functional form of the demand function should follow from the density of consumers over characteristics space. Formally, demand for a model is given by integrating the density of consumers over the neighborhood of the model. Making the link between distribution of consumers to functional form of demand is a difficult question that I do not address. Rather, I consider equations (1A) and (1B) as convenient statistical approximations of demand.

In standard consumer theory, with 100 models, 99 models could serve as substitutes for model  $i$ , and thus 99 prices would appear in  $\bar{P}_{jt}$ . This would imply 9900 cross price terms to be estimated in the standard demand system. This is not feasible with only 3 years of data. Again, I rely on the theory of product differentiation to, in effect, place many zero restrictions on the vector  $\alpha_2$ .

The earliest work on product differentiation by Hotelling (1929) arranged products along a line. In Figure 1, model B competes for customers with models A and C, but not with any other models.

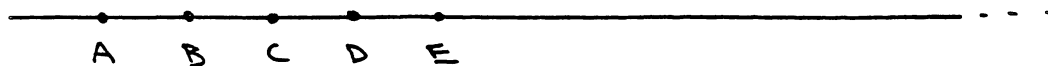


Figure 1.



Here, models A and C are termed "neighbors" of model B, whereas the other models (D, E, etc.) were not. Were there 100 models arranged along the spectrum, this set-up would imply 97 zero restrictions on the vector  $\alpha_2$  for good B. Only the price of B and the prices of its neighbors, A and C, would enter the demand function for B.

Lancaster extends the Hotelling model to allow products to differ across more than one dimension. Lancaster posits that each good is a bundle of several characteristics. In this case, if there are  $n$  products, each product may have up to  $n-1$  neighbors and all have at least one neighbor.<sup>8</sup> I rely on the Lancasterian approach to product differentiation to endogenously determine which products compete with each other for consumers. This, in turn, allows me to place zero restrictions on  $\alpha_2$  in a utility-consistent manner.

Step 2: Empirically determining the neighbors for each product is complicated by the fact that while characteristics of the goods are observed, individual consumer tastes over these characteristics are not. I adopt an approach to this problem that is based in part on a methodology developed by Feenstra (1986).<sup>9,10</sup>

The first task in any Lancasterian model is to define the metric in characteristics space that is to be used to determine how far apart any two products are. To this end, let  $x = (x_1, x_2, \dots, x_n) > 0$  be a vector of physical characteristics which differ across models and  $X^n$  be the  $n$ -dimensional space in which products are differentiated. Let  $\theta = (\theta_1, \theta_2, \dots, \theta_n)$  represent the vector of taste parameters for a particular individual.

I assume that all individuals have the same form of utility function, namely CES, but that individuals differ in their vector of tastes  $\theta$ . Then, an

individual's utility is given by:

$$U(x, \theta) = \sum_{i=1}^n \theta_i x_i^\delta \quad (2)$$

The parameter  $\delta$  is related to the elasticity of substitution between characteristics,  $\sigma$ . i.e.

$$\sigma = -\frac{1}{\delta-1}$$

The twin constraints of utility increasing in  $x$  and concavity of utility in  $x$  imply  $\sigma \in (0, -1)$ . This range of  $\sigma$  is perhaps overly restrictive for the case of substitutability of auto characteristics. In order to permit  $\sigma \in (0, -\infty)$ , I take a Box-Cox transformation of (2). This yields:

$$U(x, \theta) = \sum_{i=1}^n \theta_i \tilde{x}_i^\delta$$

$$\text{where } \tilde{x}_i^\delta = (x_i^\delta - 1) / \delta, \quad 0 \text{ not equal to } \delta < 1.$$

$$\text{and } \tilde{x}_i^\delta = \ln x_i \quad \text{if } \delta = 0.$$

As I will be working with the case of less than perfect substitutability between characteristics, I will, for notational simplicity, henceforth use the (still CES) utility function:

$$U(x, \theta) = \sum_{i=1}^n \theta_i (x_i^\delta - 1) / \delta \quad (3)$$

The price of a model depends upon its characteristics. I specify the functional form for  $P(x)$ . In particular,

$$P(x) = \exp(\alpha + \beta'x) \quad (4)$$

where  $\alpha > 0$  and  $\beta = (\beta_1, \beta_2, \dots, \beta_n) > 0$  are parameters.

Denoting the homogeneous numeraire good by  $N$  and exogenous income by  $Y$ , the consumers problem is to:

$$\begin{aligned} & \text{Max } U(x, \theta) + N \\ & x, N \end{aligned} \quad (5)$$

subject to  $P(x) + N \leq Y$ .

The additively separable form of the utility function in (5) and the linearity in  $N$  implies that the optimal choice of auto characteristics is independent of income. The first order conditions for (5) imply:

$$e_i x_i^{\delta-1} = \beta_i \exp(\beta'x + \alpha) \quad (6)$$

at an optimum  $x^*$ .

Equation (6) can be solved for the unobservable taste parameters in terms of observables. As in Feenstra (1986), it proves to be very useful to do so. I find:

$$\theta_i = (x_i^*)^{1-\delta} \beta_i \exp(\beta'x^* + \alpha) \quad (7)$$

I next define a surplus function  $S(x, x^*) = U(x, x^*) - p(x)$ . This function gives the surplus associated with a model having characteristics vector  $x$  if the consumer's optimal choice is described by  $x^*$ . Simple substitution gives:

$$S(x, x^*) = \exp(\beta'x^* + \alpha) \sum \left[ \frac{\beta_i}{\delta} \right] (x_i^*)^{1-\delta} (x_i^\delta - 1) - \exp(\beta'x + \alpha) \quad (8)$$

It is easy to verify that  $S$  is maximized when  $x = x^*$ . This surplus function will serve as the metric for measuring distance in characteristics space.

Having defined the metric, I turn now to the task of using this metric to determine which products compete with one another. (i.e. which are neighbors) While there are many models of automobiles, and hence many available bundles of characteristics, there is not a continuum of products available on the market. Thus, a consumer may find that her optimal model,  $x^*$ , does not exist in the market. In this case, the consumer receives less surplus than she would if  $x^*$  had been available. In Figure 2, I illustrate an iso-surplus contour for a typical consumer for the case of 2 characteristics. In the figure,  $S(x, x^*)$  is constant along any contour and  $S(x, x^*)$  decreases as one moves away from  $x^*$ . Thus, the consumer whose optimal characteristics bundle is  $x^*$  is indifferent

between point A which entails slightly more horsepower and less weight and point B which gives relatively much more horsepower and a heavier auto.

Two models A and B would be neighbors if there is any consumer who is indifferent between A and B who prefers these two to all other models. Graphically, in Figure 2, A and B would not be neighbors if there existed a model such as C.

Different consumers may have different ideal models. Because of this, there are many iso-surplus contours that will pass through any two models.

In Figure 3, individual 1 has an optimal choice of  $x_1^*$ , and A and B lie on the same iso-surplus contour-- $S_1$ . Another consumer, individual 2, has an optimal choice of  $x_2^*$ . For this consumer, A and B also lie on the same iso-surplus contour ( $S_2$ ). The analogous story applies to consumer 3 whose optimal choice is  $x_3^*$ .

An ideal algorithm for determining neighbors would proceed in steps. For every possible pair of models in the sample, one would conduct a detailed grid search in characteristics space. At every point in the grid search, one would pose the following question. Is the consumer whose ideal model is this point in characteristics space indifferent to the 2 potential neighbors. If the answer is no, move on to the next point on the grid and repeat the question. If the answer is yes, ask if any of the other 98 models in the sample give higher surplus than the pair being considered. If the answer here is no, the pair of potential neighbors are indeed neighbors.

This algorithm will determine which multi-dimensionally differentiated products are neighbors. Unfortunately, the algorithm is computationally infeasible for the case of automobiles. This is because I find that at least 5 characteristics are necessary to adequately account for differentiation between

autos. The algorithm described above, then, would require very many 5-dimensional grid searches entailing many calculations at each point in each search. This is too expensive on a mainframe computer and too time consuming on an advanced personal computer.

I refine the above definition of neighbors. (Two models were neighbors if there existed a consumer indifferent between them and who preferred them to all other available models.) Amending this definition allows me to derive a computationally feasible method for determining neighbors to each model in my sample. I take the smallest iso-surplus contour containing the potential neighbors as the basis for comparison. In Figure 3, this is  $S_1$ -- the surplus that consumer 1 obtains. This is akin to saying that it is the preferences of the consumer whose optimal bundle is most similar to the potential neighbors that, on the margin, matter. In diagram 3, then, when I ask if A and B are neighbors, I use the preferences of consumer 1 and then look for a point such as C that lies within  $S_1$ . If a point such as C exists, A and B are not neighbors. This method is economically sound if it will always be the case that if consumer 1 has a model preferred to A and B, so will all other consumers. There exist examples in which this will not be true, and this issue will be discussed in detail. First, though, it is convenient to state a working definition of "neighbors."

Definition: Models A and B are considered neighbors if, for the smallest iso-surplus contour containing both of them:

$$S(x_a, x^*) [=S(x_b, x^*)] > S(x_c, x^*) \text{ for all models } c.$$

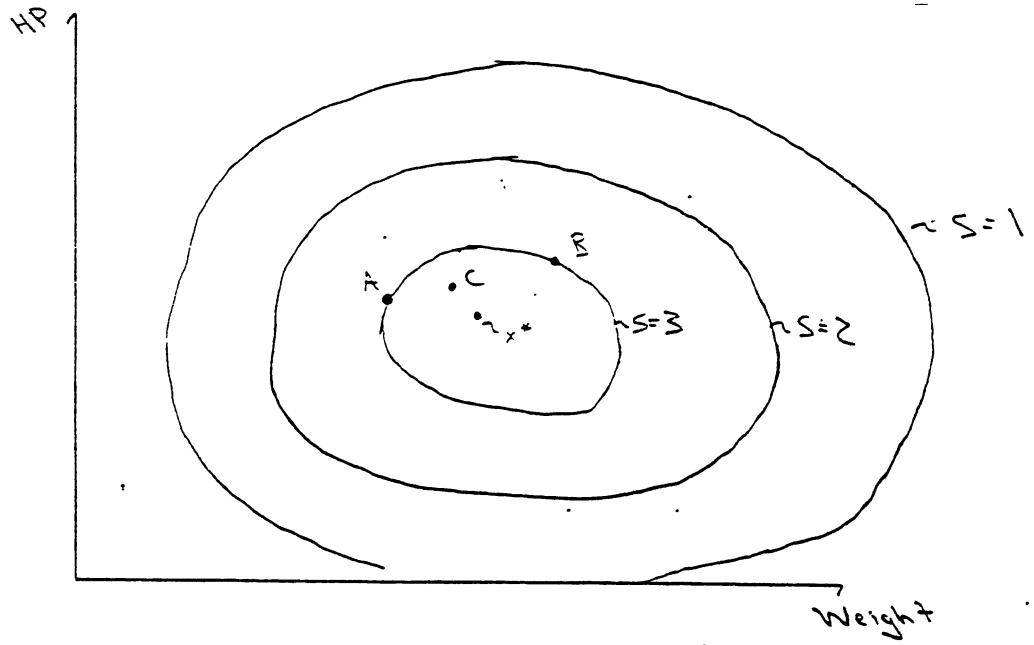


Figure 2

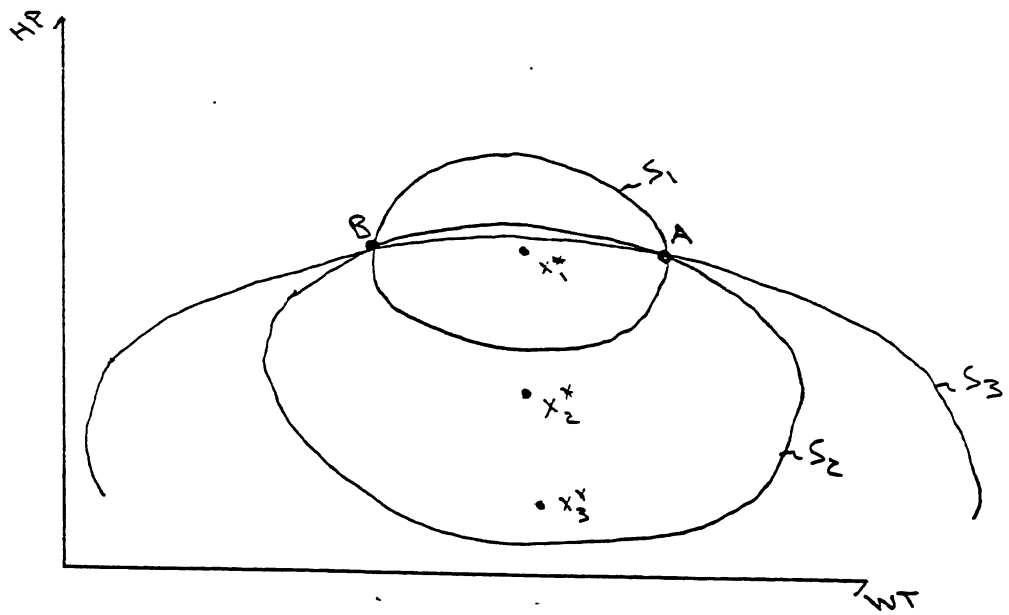


Figure 3.

This is, I believe, an economically intuitive and computationally straightforward definition of neighbors. It is not a perfect definition for at least two reasons. I discuss each in turn.

The first problem with the definition of neighbors concerns identifying the  $x^*$  which defines the highest surplus associated with indifference between models A and B. Recall that  $x^*$  is a consumer's optimal choice of characteristics and as such is not observed. I posit that  $x^*$  is the midpoint of a line drawn between two potential neighbors, A and B, where the surplus function provides the metric. Since a model is represented by a vector of its characteristics, I find  $x^*$  by varying  $\Omega$  from 0 to 1 until  $x^* = \Omega x_A + (1-\Omega)x_B$  and  $S(x_A, x^*) = S(x_B, x^*)$ . If iso-surplus contours were proper ellipsoids, the  $x^*$  defined in the above linear fashion would indeed identify the smallest iso-surplus contour containing A and B. Insofar as the iso-surplus contours defined by (8) are not proper ellipses, defining  $x^*$  as the mid-surplus point on the line between points A and B may not yield the smallest contour containing A and B.

There are two possible responses to this critique. First, the iso-surplus contours defined by (8) are, in fact, not too different from ellipses for the case of automobiles. Iso-surplus contours derived from data are drawn in weight-horsepower space in figure 4. Due to the symmetry of (8), contours are similarly shaped in the space of any two characteristics. Second, if  $x^*$  was poorly defined by drawing a line between A and B, one would expect the method to yield nonsensical sets of neighbors. I show in the next section that this is not the case.<sup>12</sup>

A second problem is that this definition of neighbors which uses the smallest iso-surplus contour as the basis for comparison may falsely reject potential neighbors. This is demonstrated in Figure 5.





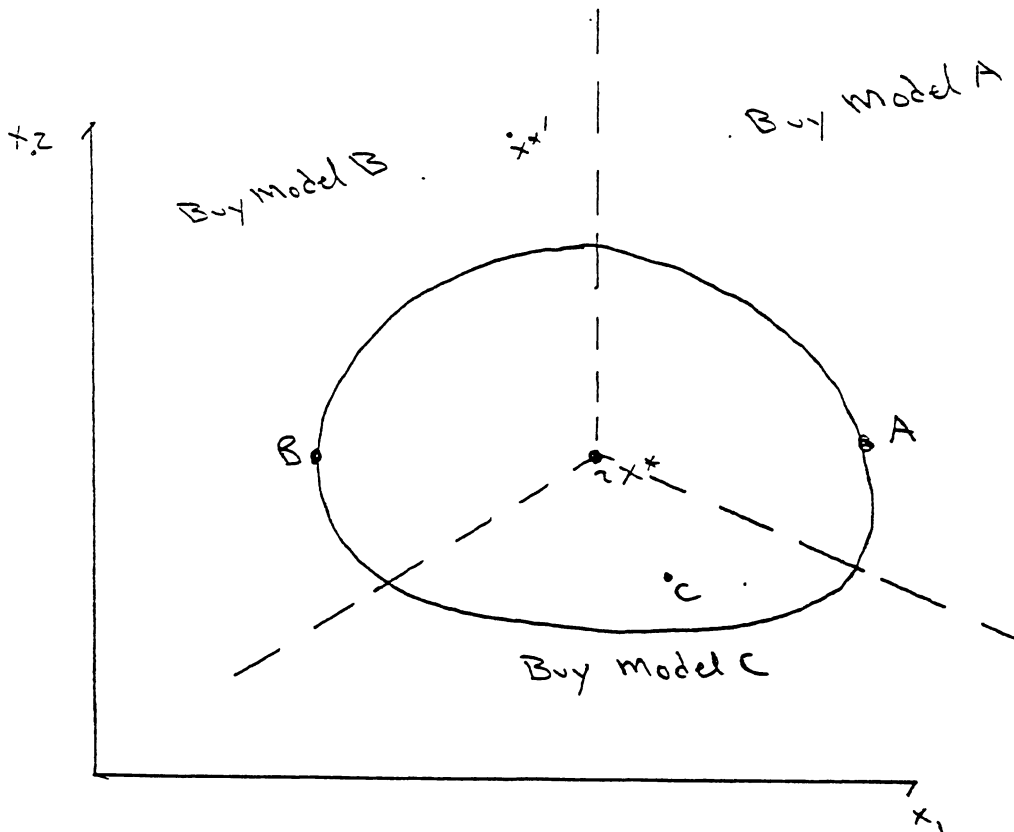


Figure 5

Suppose there are only 3 models, A, B, and C. My definition of neighbors rules out A and B as potential neighbors, since the iso-surplus contour drawn is the smallest containing A and B and C is preferred to A and B. Yet for a consumer whose optimum is  $x^*$ , A and B are neighbors. My method for determining neighbors, though, will never account for the preferences of a consumer with an optimal choice of  $x^*$  in Figure 5. Because I find the optimum

bundle by drawing a line between 2 models, and do so for all pairs in the sample, I will never account for the preferences of a consumer whose optimum bundle lies outside the outermost envelope of available models. The preferences of these consumers are ignored. In figure 5, this envelope is defined by the triangle ABC-- an area which does not include  $q^*$ .

For the automobile market, this problem is not likely to be an empirically important one. This is because, in a market with as many models as the auto market, it is unlikely that there are very many consumers whose ideal lies outside this outer envelope. Were this the case, one would expect such profitable market niches to be readily filled.

The algorithm for finding neighbors, then, is as follows.

Step 1: Find  $x^*$  such that  $S(x_1, x^*) = S(x_2, x^*)$  using the above described linear method.

Step 2: See if there exists a model  $j$  not equal to 1,2 such that  $S(x_1, x^*) < S(x_j, x^*)$ . Models 1 and 2 are neighbors if no such  $j$  exists in the sample.

Step 3: Repeat the above two steps for all possible pairs in the sample. This algorithm ensures that if 1 is a neighbor of 2, then 2 is a neighbor of 1. If 3 is a neighbor to 2, though, it need not be a neighbor to (2's neighbor) 1. The number of neighbors a model has depends on its characteristics and the characteristics of the other models in the sample. The actual number of neighbors for each model is endogenous and will differ across models.

This procedure yields the neighbor(s) to every model in the sample. I use these neighbors as the elements of  $P_{j,t}$  in the demand equation (1). Conversely, models which are not neighbors are assumed to have no cross price effect in (1).

This concludes the description of the methodology. In this section, I have explained how I use results from a Lancasterian model of product differentiation to derive an estimable demand function. The resulting demand function circumvents many of the myriad problems that plagued earlier attempts to estimate the demand for differentiated products--specifically automobiles.

#### IV. Data and Results.

The data set comprises almost all automobile models which were sold in calendar years 1983 - 1985. Specialty models with annual sales of under 4000 were excluded (e.g. Ferrari and Rolls Royce). Models which were not produced for all of each of the three years were also deleted. This allows me to avoid the problems that would be posed by a model which is introduced in October and hence has very low annual sales for the calendar (as opposed to model) year. A similar, though less severe, problem would exist for models withdrawn after October. Models included in the sample are given in Table 1. Each model/year observation consists of the following variables.

- 1) Sales by Nameplate
- 2) Suggested retail list price for the base model
- 3) Wheelbase of the base model
- 4) Length " "
- 5) Width " "
- 6) Height " "
- 7) Weight " "
- 8) Headroom " "
- 9) Legroom " "
- 10) Number of engine cylinders of the base model.
- 11) Engine displacement " "
- 12) Fuel injection or carburation " "
- 13) Manual or automatic transmission " "
- 14) Power or manual steering " "
- 15) Power or manual brakes " "
- 16) Air conditioning as standard on the base model.
- 17) Horsepower (HP) of the base model
- 18) Turning radius " "
- 19) Country of origin.

All data were collected from issues of Automotive News' annual Market Data Book Issue.

Some variables of economic significance are absent from the above list. In particular, I lack data on the incomes of consumers and on the actual transaction price. I use the suggested list price of the base model for  $P_{it}$ .<sup>13</sup> This introduces systematic bias in so far as some models consistently sell for more or less than list price. For some Japanese models, this may have been the case in my sample.<sup>14</sup>

I compute neighbors for the 1984 models. I assume that product characteristics do not change so much that neighbors change over the sample period. I will relax and test this assumption in future work. Indeed, computing neighbors for each year provides an alternative test of Feenstra's (1985) upgrading results. Here, differential upgrading would take the form of changing neighborhoods over time.

I begin by estimating the hedonic price equation  $P(x)$ . Like most researchers before me<sup>15</sup>, I find that the functional form of  $P(x)$  which best fits the data is:<sup>16</sup>

$$P(x) = \exp(\alpha + \beta'x) \quad (4)$$

I find that a linear combination of the following five characteristics accounts for almost 90 percent of the variation of  $P(x)$ --weight, horsepower, and dummies for power steering, air conditioning, and foreign. Dummy variables take the value of 2 if a car is foreign, and if air and power steering are standard and a value of 1 otherwise. This differs from the usual 1-0 convention because

Table 1

Models Used in the Sample

Toyota Tercel	American Motors Alliance	Chevrolet Camaro
Corolla	Eagle	Celebrity
Celica	Plymoth Horizon	Corvette
Camry	Turismo	MonteCarlo
Cressida	Reliant	Chevrolet
Supra	Plymoth GF	Oldsmobile Firenza
Nissan Sentra	LeBaron	Cutlass/Cie
Maxima	NewYorker/5thA	Cutlass/Sup
300zx	Dodge Omni	Olds88
200SX	Charger	Olds98
Stanza	Aries	Toronado
Pulsar	Dodge600	Pontiac 1000
Honda Accord	Diplomat	Sunbird
Civic1.5S	Ford EXP	Firebird
Mazda 626	Escort	6000
RX-7	Mustang	Bonneville
GLC	T-bird	GrandPrix
Suburu DL/GL	LTD	Volkswagon Rabbit
Chry/Ply Colt	CrownVict.	
Volvo DL	Mercury Lynx	
760 GLE	Cougar/XR7	
VW Jetta	Capri	
Quantum	Marquis	
BMW 320/318	GrandMarqui	
530/528	Continental	
733	MarkVii	
Mercedes 300D	Lincoln	
300SD	Buick Skyhawk	
190E	Skylark	
Audi 5000	Century	
4000	Regal	
Mitsubishi Tredia	LeSabre	
Cordia	Electra	
Starion	Riviera	
Saab 900 S	Cadillac Cimarron	
900 Turbo	Seville	
Porsche 944	Cadillac DV	
911	ElDorado	
Isuzu I-mark	Chevrolet Chevette	
Impulse	Cavalier	
Peugeot 505	Citation	

some dummies are raised to negative powers. The only effect of this change is to alter the constant term in the hedonic regression. Numerical experiments show that this has no effect on the determination of neighbors. I estimate the log of equation (4) to give:

$$\ln P = .215 + .209 \text{ Weight} + .0045 \text{ HP} + .1261 \text{ PS} + .4703 \text{ Air} + .161 \text{ Foreign} \quad (9)$$

(.123)
(.056)
(.0009)
(.052)
(.050)
(.044)

standard errors are in parentheses.  
 100 observations.  $R^2 = .885$

It is useful to view dummy variables here as proxies for various degrees of luxury and/or quality. Hence an optimal choice of characteristics,  $x^*$ , may involve .5 units of air conditioning. This just means that the consumer would prefer less luxury than is imposed by the all or nothing choice of air conditioning but more than is afforded by a no-air model. The coefficients in (9) are used to parameterize the surplus function of equation (8). While the coefficients are subject to measurement error, their very small standard errors argue that neglecting this error is unlikely to be an empirically relevant omission.

The only remaining unknown in the surplus function is the parameter  $\delta$  which is related to the degree of concavity of the utility function. Recall that the elasticity of substitution,  $\sigma = 1/(\delta-1)$ . This parameter is not identifiable with the data available. Following Feenstra (1986), I posit many different values for  $\delta$  and replicate the entire methodology from the beginning for each of these. I find that the choice of  $\delta$  over a wide range of plausible values does not affect the qualitative results. I consider values of  $\delta = .5, -1, -3, -6, \text{ and } -8$ . Only at values of  $-8$  and below do results change substantially. That is, the choice of neighbors is mostly unaffected until

$\delta = -8$ . At  $-8$ , neighbors become much more numerous and, to a degree, counter-intuitive.

Once  $\delta$  has been specified, I compute neighbors for every model using the 1984 data.<sup>17</sup> The results for  $\delta = -3$  are given in Table 2. Table 2, for example, tells us that the neighbors of the Honda Accord, model 13, are the Toyota Camry, Nissan Stanza, Mazda 626, Mitsubishi Tredia and Cordia, Chevrolet Cavalier, and Pontiac Sunbird. An intuitive way of interpreting Table 2 is to note that it answers the question: What other autos did the consumer consider before she decided to purchase the one actually selected?

In addition to varying  $\delta$ , another type of sensitivity test was conducted in calculating neighbors. Because iso-surplus contours are not perfect ellipses, the linear method of finding the optimal model  $x^*$  is, as noted above, only an approximation. I used another approximation and re-tested for neighbors. This other approximation was based on finding  $x^*$  such that consumers whose ideal models were A and B were equally dissatisfied with  $x^*$ . This approximation yielded the same qualitative results as the linear approximation of  $x^*$ .

The next step in the methodology is to estimate the demand functions given in (1A) and (1B). Models have, on average, about 6 neighbors. With 100 models, this implies 600 cross price terms to be estimated. While this is certainly an improvement over the previous 9900 terms, the demand functions are still not accurately estimable with only 300 observations. I take the mean price of neighbors as the observation for  $P_{j,t}$ . Similarly, I take the mean characteristics of neighbors as the observation for  $X_{j,t}$ . Because the demand functions use the log of  $P_{j,t}$ , it matters that the average of the logs is not the log of the averages. Numerical experiments show that this approximation does not affect results. There are other specifications for  $P_{j,t}$ . Recall that

Table 2

Neighbors when  $\delta = -3$ .

Model #	Model Name	Number of Neighbors	Model Numbers of Neighbors																		
1	Toyota Tercel	6	17	18	19	42	44	80													
2	Corolla	2	18	39																	
3	Celica	4	4	10	16	45															
4	Camry	8	3	11	13	15	45	52	81	82											
5	Cressida	4	6	21	37	67															
6	Supra	3	5	9	37																
7	Nissan Sentra	4	12	17	19	100															
8	Maxima	3	25	29	36																
9	300zx	3	6	26	38																
10	200SX	8	3	11	16	20	24	31	41	53											
11	Stanza	5	4	10	12	31	53														
12	Pulsar	8	7	11	17	18	22	23	31	100											
13	Honda Accord	5	4	15	32	33	81														
14	Civic1.5S	1	100																		
15	Mazda 626	9	4	13	23	32	57	69	81	82	88										
16	RX-7	4	3	10	20	34															
17	GLC	7	7	12	1	18	19	56	100												
18	Suburu DL/GL	8	2	12	17	1	22	51	61	94											
19	Chry/Ply Colt	3	7	17	1																
20	Völvo DL	10	10	16	24	30	34	35	41	54	62	98									
21	760 GLE	4	5	25	27	37															
22	VW Jetta	6	12	18	39	55	61	100													
23	Quantum	5	12	15	31	40	76														
24	BMW 320/318	6	10	20	31	35	40	76													
25	530/528	4	8	21	27	92															
26	733	5	9	28	38	68	85														
27	Mercedes 300D	8	21	25	28	74	75	79	92	93											
28	300SD	5	26	27	74	77	78														
29	190E	2	8	35																	
30	Audi 5000	3	20	35	40																
31	4000	6	10	11	12	23	24	76													
32	Mitsub Tredia	5	13	15	33	81	95														
33	Cordia	3	13	32	39																
34	Starion	6	16	20	36	54	60	62													
35	Saab 900 S	4	20	24	29	30															
36	900 Turbo	3	8	34	37																
37	Porsche 944	4	5	6	21	36															
38	911	3	9	26	85																
39	Isuzu I-mark	4	2	22	33	55															
40	Impulse	5	23	24	30	41	76														
41	Peugeot 505	7	10	20	40	43	59	83	98												
42	Alliance	2	1	80																	
43	Eagle	5	41	59	76	87	99														
44	Horizon	3	1	50	94																
45	Turismo	4	3	4	46	53															





the estimated demand equation is just a convenient statistical representation. Perhaps  $P_{j,t}$  should be the average price of neighbors weighted by their sales. This representation of  $P_{j,t}$  yields the same qualitative results, but standard errors on the parameters in the demand function are larger.

I estimate (1A) and (1B) using OLS. Because (1B) is nested within (1A), a straightforward F-test is used to test which specification should be used. That is, I test to see if own and neighbor's mean characteristics are jointly statistically significant.<sup>18,19</sup> For all values of  $\delta$  tested, the data cannot reject the hypothesis that own and neighbors' characteristics are jointly insignificant.

The existence of multicollinearity in (1A) is confirmed by collinearity diagnostics following the approach of Belsley, Kuh, and Welsch (1980). Singular Value Decomposition analysis indicates multicollinearity. The SVD analysis does not indicate that the data matrix is so ill-conditioned as to suggest numerical error in the estimates. Due to the multicollinearity in (1A), estimated standard errors are inflated. This biases the F-test toward rejecting joint statistical significance of own and neighbors' mean characteristics. I nonetheless accept the results of the F-tests and use (1B) as the demand function in the analysis that follows. Table 7 in the Appendix presents the results of instead using (1A). As the collinearity diagnostics indicated, results are very similar to those obtained using (1B) (and given in Table 4), except that standard errors are inflated.

OLS estimates of (1B) are presented in Table 3. In Table 3, equation 3.1 presents estimates of the demand function excluding any cross price effects. This equation is roughly a panel data version of the older time-series studies which neglected cross-price effects. Equation 3.1 gives a highly significant total market elasticity of demand of  $-.794$ . This estimate is in line with

existing, older estimates. Equation 3.1, though, is misspecified, as cross-price effects are omitted.

Equations 3.2 to 3.6 in Table 3 give estimates when the demand function includes the price of neighbors, hence allowing for the possibility of substitution. Varying  $\delta$  from .5 to -6 affects the significance of the parameters on own and neighbor's price but the point estimates are fairly constant. (Recall that the choice of  $\delta$  only enters the demand function via its effect on the determination of the set of neighbors.) For  $\delta = .5, -1, -3$  and  $-6$ , the coefficient on neighbor's price is highly significant. For these values of  $\delta$ , the coefficient on own price is somewhat stable across equations and is highly significant.

For values of  $\delta$  between  $-1$  and  $-6$ , the total market elasticity ( $\alpha_1 + \alpha_2$ ) varies from  $-.81$  to  $-.83$  --all of which are statistically significant at the 90% level. As theory would lead one to expect, allowing for substitutability leads to a more elastic own price elasticity. This is evidenced by own price elasticities ( $\alpha_1$ ) greater in absolute value than the coefficient of  $-.794$  in equation 3.1.

In sum, the "neighbors" approach to restricting the dimensionality of the demand function in conjunction with a short panel of data seems to fit the data remarkably well. I have completed some sensitivity analyses in the spirit of Leamer (1985). These ad hoc specification tests include using other hedonic characteristics to control for cross sectional variation. The results have been exceptionally robust to such tests.

Table 3

Estimated Demand Functions  
Standard Errors in Parentheses

## Variable Definitions:

LOGSALE	--	Log of sales in 1000's.
LOGLIST	--	Log of the list price in \$1000's
LOGPN	--	Log of the average price of the neighbors in \$000.
D84	--	1 if the year is 1984 , 0 otherwise.
D85	--	1 if the year is 1985 , 0 otherwise.
SWEDE	--	1 if the car is Swedish, 0 otherwise.
JAPAN	--	1 if the car is Japanese, 0 otherwise.
GERMAN	--	1 if the car is German, 0 otherwise.

Dependent Variable is LOGSALE

Eqn.	(3.1)	(3.2)	(3.3)	(3.4)	(3.5)	(3.6)
		$\delta = .5$	$\delta = -1.0$	$\delta = -3.0$	$\delta = -6.0$	$\delta = -8.0$
CONSTANT	6.085 (.278)	5.814 (.276)	6.087 (.277)	6.041 (.270)	6.004 (.267)	5.772 (.411)
LOGLIST	-.7942 (.119)	-1.814 (.254)	-1.333 (.319)	-2.076 (.313)	-2.271 (.311)	-.912 (.165)
LOGPN		1.112 (.246)	.522 (.287)	1.250 (.284)	1.444 (.282)	.237 (.229)
D84	.114 (.116)	.111 (.113)	.118 (.116)	.122 (.113)	.120 (.112)	.108 (.116)
D85	.1672 (.117)	.161 (.113)	.173 (.116)	.178 (.113)	.179 (.112)	.155 (.117)
SWEDE	-1.321 (.253)	-1.350 (.245)	-1.316 (.252)	-1.228 (.246)	-1.181 (.244)	-1.302 (.254)
JAPAN	-.554 (.117)	-.607 (.113)	-.570 (.116)	-.578 (.113)	-.594 (.112)	-.529 (.119)
GERMAN	-1.01 (.117)	-.615 (.183)	-.843 (.189)	-.537 (.193)	-.424 (.196)	-.928 (.183)
R <sup>2</sup>	.3954	.4349	.4022	.4330	.4450	.3976

#### V. On the Empirics of Taxation Schemes for Differentiated Products.

The methodology by which the demand functions in Table 3 were derived was based on Lancasterian consumer theory. That theory tells us that not all differentiated products need be substitutes. It also tells us to group products according to their characteristics and not only, as the Armington Assumption implies, according to their country of origin.<sup>20</sup> The elasticities that are estimated in the equations of Table 3, then, are the relevant ones from the vantage point of consumer theory.

Trade policy, though, typically taxes a good based on its country of origin. The analysis of trade policy issues requires trade elasticities. I derive these elasticities from the estimates of the demand system provided in Sections III and IV. This is accomplished by perturbing the system on whatever margin trade policy operates to simulate the elasticity relevant to the study of trade taxes. This approach is more likely to give valid elasticities than direct estimation of import demand equations (see, for example Leamer and Stern), because it is based on a utility-consistent framework for demand.

Suppose, for example, that policy makers wish to know how the demand for domestic autos changes when a tariff is applied to all auto imports. To derive this elasticity, I increase the price of all foreign cars by one percent--my proxy for a small change. This increases the demand for models of domestic autos which have as neighbors some foreign model. Summing the new demand for all domestic autos gives the information needed to construct the relevant elasticity.

This approach requires a caveat. I have nothing to say about the effect of large taxes. This is because the estimated demand system is only a local representation of demand. The system may behave quite differently at a point

far from the initial situation. This is a standard warning in the empirical tax analysis literature. Also, here, large taxes may change the neighbors of a model. I assume that the taxes I consider are small enough that neighbors do not change. Preliminary numerical experiments indicate that this is indeed the case for the one percent price changes I consider.

In Table 4, I give a wide variety of elasticities corresponding to various policy scenarios. For each elasticity, I also give its standard error. This statistic is computable given the variance-covariance matrix of the estimates of the initial demand equation. These elasticities all are simulated using the demand equation (3.4). That is,  $\delta$  from the utility function is set to -3. I take this as a central case for expositional purposes. Appendix A presents the same elasticities when the entire methodology is conducted using other values of  $\delta$ . That appendix shows that results remain qualitatively similar for a range of  $\delta$ 's.

Table 4 is easily interpreted. The table shows, for example, that the elasticity of demand for domestically produced automobiles with respect to the price of Japanese autos is .187. That is, a one percent increase in the price of all Japanese cars (via a tariff perhaps) yields a .187 percent increase in demand for domestically produced autos. Were such a price increase applied to all imported autos, demand for domestically produced autos would rise instead by .367 percent. This example illustrates an error present in earlier studies of U.S. - Japanese auto trade policy. These studies used an imputed elasticity of demand for domestic autos with respect to a foreign price change. This is because there were no estimates available of elasticities of domestic demand with respect to a change in only the Japanese price. Table 4 tells us

Table 4

Elasticities of Demand using Eq. 1B

$$\delta = -3$$

Standard errors in parentheses.

		QUANTITY CHANGE				
		Domestic Autos	All Imports	Japanese Imports	German Imports	Swedish Imports
P R I C E  C H A N G E	All Domestic	-1.187 (.146)	.225 (.051)	.213 (.048)	.258 (.058)	.076 (.017)
	All Foreign	.367 (.084)	-1.045 (.129)	-1.030 (.128)	-1.078 (.132)	-.897 (.118)
	Japanese	.187 (.042)	-.663 (.081)	-1.43 (.187)	.393 (.089)	.300 (.068)
	German	.112 (.025)	-.279 (.036)	.317 (.072)	-1.717 (.240)	.745 (.169)
	Swedish	.024 (.005)	-.064 (.011)	.071 (.016)	.247 (.056)	-1.971 (.292)
	All Foreign weighing < 2300 lbs.	.096 (.021)	-.376 (.046)	-.550 (.067)	-.199 (.025)	0.0 ---

that this error leads one to believe that demand for domestic autos is twice as responsive to a small tariff on Japanese cars than is actually the case. The difference arises due to substitution by American consumers away from Japanese cars toward other foreign cars not affected by the trade policy.

Suppose that the purpose of trade or industrial policy in the U.S. automobile industry is to increase demand for domestically produced autos. Table 4 shows that a tax on all imports has less than half the effect on domestic demand than an equal subsidy on domestic models would have (.367 v. -1.187). (Consequences for government revenue are, of course, quite different.) An increase in a tariff on Swedish autos has very little effect on domestic demand. The relevant elasticity is .034. This is because most of the neighbors to Swedish autos are also foreign.

Suppose that the purpose of trade taxes is to reduce imports from a specific country. Then Table 4 shows that a tax on only Swedish cars reduces Swedish imports by relatively less than the same tariff on German autos. Swedish cars are the most elastically demanded import, followed by German models, then Japanese models (-1.97 v. -1.71 v. -1.43). This is because Japanese models have many Japanese neighbors; while this is not the case for Swedish models. Indeed, most neighbors to Swedish models are German. This is evidenced by the relatively high cross price elasticities between German and Swedish autos.

Perhaps contrary to prior beliefs, a tax on all imports would have roughly the same relative impact on Japanese, German, and Swedish producers.

Some economists have argued for a tax on all small foreign cars instead of a tax on Japanese autos. Such a tax does not discriminate on the basis of country of origin and is viewed more kindly by GATT. I arbitrarily define small cars to be those weighing under 2300 pounds. (For purposes of comparison, a Toyota Tercel weighs 1985 lbs., a Honda Accord 2187 lbs., and a



Saab 900 2612 lbs.) While such a broadly based tax might make a Trade Representative's job more easy, the policy is only half (.096 v. .187) as effective as is a direct tax on imports at increasing demand for domestically produced autos. Swedish producers are totally unaffected by such a tax since no Swedish export to the U.S. weighs less than 2300 lbs. (there is a reason Volvos are so safe), and no Swedish car has a neighbor weighing less than 2300 lbs.

It is possible to investigate the effects of various other trade and industrial policies using Table 4. The above scenarios provide only a beginning.

#### VI. Summary

This paper has developed a new methodology for investigating empirically the effects of taxes on differentiated products. The approach adopted a Lancasterian, utility-consistent view of product differentiation. Using this approach, I calculated which multidimensionally differentiated products were neighbors. This information proved a useful basis for decreasing the dimensionality of the demand estimation problem. Using a panel of 100 automobile models over 3 years, a demand function was estimated. This yielded quite reasonable and statistically significant demand elasticities.

Recognizing that tax policy often acts on a different margin than consumer theory, the demand elasticities necessary for tax policy analyses were simulated. This provided the first estimated set of such elasticities. These elasticities provide some insight into a number of possible policy scenarios.

The methodology developed in this paper provides ample opportunities for Leamer-type ad-hoc specification tests. Many of these are presented in the Appendix. Results appear robust.

The elasticities estimated and given in Table 4 are well suited to

simulation analyses of strategic trade and industrial policies concerning the U.S. automobile industry. This is the subject of ongoing research.

## APPENDIX A

Table 5

Elasticities of Demand using Eq. 1B  
 $\delta = -1$

Standard errors in parentheses.

		QUANTITY CHANGE				
		Domestic Autos	All Imports	Japanese Imports	German Imports	Swedish Imports
P R I C E  C H A N G E	All Domestic	-.967 (.154)	.112 (.062)	.122 (.067)	.100 (.055)	.053 (.029)
	All Foreign	.162 (.089)	-.918 (.137)	-.928 (.140)	-.906 (.134)	-.859 (.124)
	Japanese	.086 (.047)	-.559 (.089)	-1.080 (.198)	.147 (.081)	.108 (.059)
	German	.042 (.023)	-.259 (.037)	.120 (.066)	-1.173 (.241)	.343 (.189)
	Swedish	.015 (.008)	-.078 (.011)	.026 (.014)	.101 (.056)	-1.326 (.318)
	All Foreign weighing < 2300 lbs.	.051 (.028)	-.338 (.052)	-.491 (.076)	-.188 (.028)	0.0 ---

Table 6

Elasticities of Demand using Eq. 1B  
 $\delta = -6$

Standard errors in parentheses.

## QUANTITY CHANGE

	Domestic Autos	All Imports	Japanese Imports	German Imports	Swedish Imports	
P R I C E  C H A N G E	All Domestic	-1.247 (.083)	.239 (.046)	.231 (.045)	.267 (.052)	.100 (.019)
	All Foreign	.426 (.145)	-1.060 (.125)	-1.052 (.125)	-1.088 (.128)	-.922 (.117)
	Japanese	.226 (.044)	-.709 (.082)	-1.568 (.190)	.466 (.091)	.361 (.070)
	German	.124 (.024)	-.243 (.035)	.427 (.083)	-1.849 (.236)	.821 (.160)
	Swedish	.026 (.005)	-.074 (.010)	.071 (.014)	.269 (.052)	-2.144 (.288)
	All Foreign weighing < 2300 lbs.	.119 (.023)	-.390 (.045)	-.581 (.067)	-.189 (.024)	0.0 ---

Table 7

Elasticities of Demand using Eq. 1A  
 $\delta = -3$

Standard errors in parentheses.

## QUANTITY CHANGE

	Domestic Autos	All Imports	Japanese Imports	German Imports	Swedish Imports	
P R I C E  C H A N G E	All Domestic	-1.412 (.533)	.201 (.103)	.191 (.584)	.230 (.118)	.067 (.034)
	All Foreign	.328 (.168)	-1.285 (.580)	-1.275 (.098)	-1.314 (.569)	-1.152 (.633)
	Japanese	.167 (.085)	-.793 (.309)	-1.636 (.046)	.352 (.180)	.268 (.137)
	German	.100 (.056)	-.358 (.195)	.284 (.145)	-1.886 (.405)	.666 (.342)
	Swedish	.021 (.011)	-.091 (.068)	.064 (.033)	.221 (.113)	-2.113 (.385)
	All Foreign weighing < 2300 lbs.	.086 (.044)	-.462 (.206)	-.672 (.293)	-.250 (.124)	0.0 ---

## Endnotes

1. See Dixit (1986) who argues this point.
2. See, for example, Deaton and Muellbauer (1980).
3. Other simpler examples of this type of methodology are Johnson (1978) and Cragg and Uhler (1970).
4. Demand for automobiles is the most prevalent example of modelling the demand differentiated products. I am unaware of any modelling approach for other differentiated products that is not mentioned in this section of the paper.
5. This is the most recent data available until April 1987.
6. Note that this differs from the usual panel in which goods are the same, but demand is across consumers and over time. Here, the consumers are assumed the same, but goods differ across models, and these models are tracked over time.
7. Actually, it is sufficient to include in the regression those characteristics of which a linear combination account for the product differentiation.
8. This differs from the Dixit-Stiglitz approach to product differentiation. There, all products are neighbors.
9. The approach I use to find neighbors when products are multidimensionally differentiated benefitted greatly from discussions with Rob Feenstra. I am very grateful for his many helpful suggestions.
10. Recent theoretical work by Caplin and Nalebuff (1986) has also addressed the issue of determining neighbors to a good when products are multidimensionally differentiated. They show that if preferences can be represented by a utility function that is Cobb-Douglas in product characteristics and income, then there exists a straightforward way of finding neighbors. Using the unit simplex in Cobb-Douglas parameter space, they show that a hyperplane divides all consumers who prefer good x to good y from those who prefer y to x. Because set of consumers who prefer one model to another (i.e. the model's neighborhood) are defined by hyperplanes, finding neighbors is a tractable problem. The tractability comes from the functional form of the utility function. While this is an elegant result, it is not applicable to the automobile market. This is because the utility function that permits the tractability of the problem also implies that all consumers purchase the same value of the most preferred model but differ in quantities purchased. For big-ticket items such as automobiles, this is just not the case.
11. This function over characteristics is sometimes referred to in the literature as a sub-utility function.

12. While I realize this line of reasoning has strong Bayesian overtones, I do not know another way of getting a feel for the validity of a new methodology. This is another reason why the auto industry is a good candidate to which to apply a new methodology. If my methodology were first applied to lumber and I found Clear Pine-2 to be a neighbor to grade 3 Birch, few economists would have any idea of how well neighbors are defined.
13. This is also the practice adopted by Feenstra (1985). In that paper, Feenstra puts forth the argument that for national welfare considerations, dealer mark-ups represent an intra-country transfer.
14. Implicit discounts due to selectively applied low financing rates have also been ignored due to lack of data.
15. The most recent examples are Feenstra (1985) and (1986). Griliches is a much earlier example.
16. I also estimate this function without logarithms. This functional form yielded a loss of about .20 in the  $R^2$ .
17. This procedure is programmed in IBM Profortran for implementation on IBM-compatible personal computers. The program is available to researchers on request.
18. Throughout this paper, "statistically significant" means statistically significant from zero at the 90% confidence level unless stated otherwise.
19. Because FOREIGN is a near linear combination of SWEDE, JAPAN, and GERMAN--the fixed effects, I do not include FOREIGN in equation (1A) as an own characteristic.
20. Indeed, demand estimation according to the Armington Assumption, using my data set, yields statistically insignificant and nonsensical demand elasticities.

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