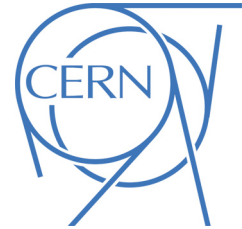




Honors Senior Thesis

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Measurement of the Higgs Spin and Parity in the Four-Lepton Channel with the ATLAS Detector

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Abstract

The Spin and Parity (J^P) of the newly discovered Higgs boson is studied in the $H \rightarrow ZZ^* \rightarrow 4l$ decay channel with the ATLAS experiment at the Large Hadron Collider. This study uses the entire proton-proton collision data set: corresponding to an integrated luminosity of 4.6 fb^{-1} at 7 TeV and 20.3 fb^{-1} at 8 TeV. Comparisons with data of the predicted Standard Model, $J^P = 0^+$, hypothesis and alternative hypotheses ($J^P = 0^-, 1^+, 1^-,$ and 2^+) are made through a multivariable analysis based on lepton kinematic, Z boson invariant masses, and angular observables. The results show that data is in favor of the Standard Model 0^+ hypothesis, while other alternative J^P states are excluded at a 83.1% to 99.8% confidence level, independent of assumptions on the coupling strengths between the Standard Model Higgs boson to other particle.

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1 Introduction

On July 4th 2012 CERN (European Organization for Nuclear Research) announced the discovery of a new boson with a mass around 125 GeV, which was observed by both the ATLAS and CMS experiments in their search for the Standard Model (SM) Higgs boson at the Large Hadron Collider (LHC). Later that year CERN published the discovery of a particle consistent with the Higgs boson [1]. The discovery of this new particle was experimentally observed in three different final states: $\gamma\gamma$, ZZ^* , and WW . Both experiments have since collected more data and studied the properties of this newly discovered particle. The measured properties (couplings, spin, and parity) of the new particle by both experiments are consistent with the predictions of the SM Higgs boson. Confirming this particle as the SM Higgs boson will help to unlock the mystery of the electroweak symmetry breaking mechanism of the SM.

The SM describes the building blocks of the universe through elementary particles and their interactions. This theory is based on two principles: (1) gauge invariance, from which all the interactions between particles are naturally introduced in a theoretical framework; (2) Higgs Mechanism, from which the electroweak symmetry is broken and all the massive elementary particles acquire their mass through this symmetry breaking mechanism. The aspects of gauge invariance (interactions) in the SM has been successfully tested by many experiments over the past half century. However, the electroweak symmetry breaking mechanism has remained a mystery for almost 50 years. The discovery the Higgs field's quanta, the Higgs boson, at the LHC in 2012 provides evidence of and a means of further studying this SM symmetry breaking process. It is therefore crucial to measure the newly discovered Higgs boson's properties to advance our understanding of electroweak symmetry breaking mechanism and search for new physics beyond the SM at the LHC. This thesis reports the current measurements of the spin (J) and parity (P) quantum numbers of the Higgs boson in the $H \rightarrow ZZ^* \rightarrow 4l$ channel from reconstructed data events collected by the ATLAS experiment. This analysis uses the full ATLAS proton-proton collision data set, with an integrated luminosity of $4.6 fb^{-1}$ at a center-of-mass energy of $\sqrt{s} = 7$ TeV, and $20.3 fb^{-1}$ at $\sqrt{s} = 8$ TeV. In this thesis the predicted Standard Model, $J^P = 0^+$, hypothesis and alternative hypotheses corresponding to other J^P states ($jcp = 0^-, 1^+, 1^-,$ and 2^+) are compared with a multivariable analysis dependent on discriminating variables constructed from lepton kinematics, Z boson invariant masses, and angular decay observables.

This thesis is organized as follows: Section 2 describes the LHC and ATLAS detector; Section 3 describes the event reconstruction and modeling of the ATLAS experiment; Section 4 briefly reports the $H \rightarrow ZZ^* \rightarrow 4l$ event selection and background estimation; Section ?? details the Spin and Parity measurement with four-lepton final state events and presents the results; the ongoing work and conclusion can be found in Section 6 and 7, respectively.

2 The Large Hadron Collider and ATLAS

2.1 The Large Hadron Collider

The LHC is the largest and highest energy particle collider in the world. The LHC is located on the France-Swiss boarder at CERN, and was built from 1998 to 2008. In 2010, the LHC physics run started with proton-proton collisions at a center of mass energy of $\sqrt{s} = 7$ TeV. In 2012, the energy was increased to $\sqrt{s} = 8$ TeV. The peak luminosity of the LHC reached $7 \times 10^{33} cm^{-2}s^{-1}$ in 2012, with a total integrated luminosity of $26 fb^{-1}$ delivered to each experiment at the LHC during its 2010 to 2012 operation. The designed LHC energy, $\sqrt{s} = 14$ TeV, is expected to be reached in 2015 after the current upgrade efforts are finished.

The LHC is a largest accelerator complex at CERN, which accelerates particles to various energies before finally being injected into the LHC ring where collisions take place. The proton beams consist

45 of many proton bunches that are taken from a tank of hydrogen atoms stripped of their electrons by an
 46 electric field. The protons first enter Linac 2, which accelerates the protons to an energy of 50 MeV. The
 47 bunch is then injected into the Proton Synchrotron Booster, which accelerates the protons to 1.4 GeV.
 48 Next, the bunch enters the Proton Synchrotron and the Super Proton Synchrotron where the particles are
 49 accelerated to 25 GeV and 450 GeV, respectively. Finally, the bunch is injected into the Large Hadron
 50 Collider where each bunch is currently accelerated to 4 TeV and collide with a total energy of 8 TeV. A
 51 schematic of the accelerator complex can be seen in Figure 1. The two beams, comprised of thousands
 52 of bunches, travel in opposite directions and circulate the LHC for hours as they are contained and
 53 collimated using superconducting magnets to keep the bunches sufficiently dense. The beams collide
 54 inside four detectors: ALICE, ATLAS, CMS, and LHCb. Each bunch consists of about 10^{11} protons
 55 with bunch collisions occurring every 50 nanoseconds.

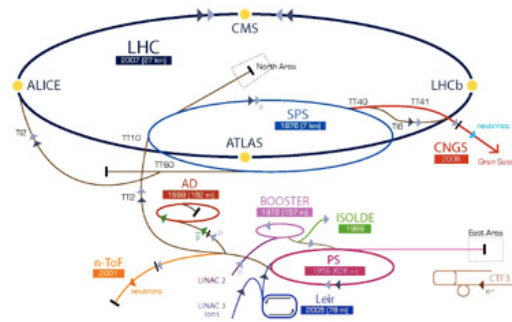


Figure 1: The CERN accelerator complex for the LHC.

56 2.2 The ATLAS Detector

57 The ATLAS detector (A Toroidal LHC Apparatus) is a multipurpose particle detector in the LHC com-
 58 plex with forward-backward symmetric cylindrical geometry as shown Figure 2. ATLAS uses a right-
 59 handed coordinate system with its origin at the interaction point (IP), where the beams collide in the
 60 center of the detector. The z-axis is along the beam line, while the x-axis points from the IP to the center
 61 of the LHC, and the y-axis extends upwards. Cylindrical coordinates (r, ϕ) are used in the transverse
 62 plane, where ϕ is the azimuthal angle around the beam line. The pseudorapidity (η) describes the final
 63 dimension analogous to the polar angle, and is defined in terms of the polar angle θ as $\eta = \ln[\tan(\theta/2)]$.
 64 Observables labeled "transverse" are projected into the x-y plane.

65 The ATLAS detector consists of a magnet system and four major specialized detectors: the inner
 66 detector, electromagnetic calorimeter, hadronic calorimeter, and the muon spectrometer. The detector
 67 components important to this study include the inner tracking detector (ID), the liquid argon (LAr) elec-
 68 tromagnetic calorimeter, and the muon spectrometer (MS). The ID is located in the center of ATLAS
 69 and consists of silicon pixel and microstrip trackers, as well as straw-tube transition-radiation trackers
 70 which in total cover the region of $|\eta| < 2.5$. The ID tracks charged particles using discrete measure-
 71 ments to produce precision measurements of the particle's trajectory, as well as its momentum. The ID is
 72 surrounded by a superconducting solenoid that produces a 2T magnetic field which bends the particle's
 73 trajectory. The LAr calorimeter surrounds the solenoidal magnetic field, and is divided into a central
 74 barrel covering $|\eta| < 1.475$ and two endcaps covering $|\eta| < 3.2$. The LAr calorimeter provides precision
 75 location and energy measurements of particles that interact electromagnetically (charged particles and
 76 photons) by absorbing the particles. The EM calorimeter is made of sheets of lead separated by layers of
 77 liquid argon. When a charged particle or a photon hits the lead it produces many more particles, creating

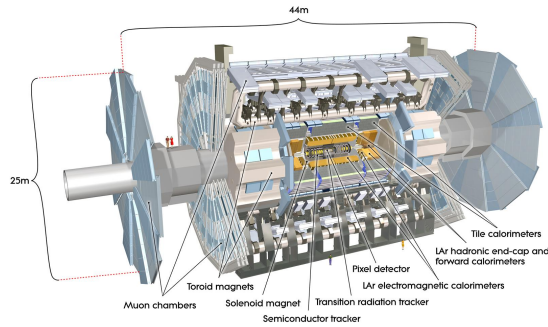


Figure 2: The ATLAS detector.

78 a shower of mostly electrons and some protons, that then ionize electrons in the liquid argon creating
 79 an avalanche effect. The shower of electrons strikes the next lead sheet and produces more particles.
 80 This process continues until the avalanched particles do not have enough energy to ionize electrons. The
 81 ionized electrons in the liquid argon are collected and used to measure the original particle's total energy.
 82 Additionally, the LAr calorimeter measures the position of the particle. When combining the momentum
 83 and tracking measurements from the inner detector with the measurements from the LAr calorimeter,
 84 and taking the magnetic field into account, one can measure the charge of the particle by the direction
 85 its track bended in the magnetic field. Additionally, one can use the curvature of the reconstructed track
 86 in the magnetic field to measure the particle's momentum. The MS surrounds the entire detector with
 87 a barrel region ($|\eta| < 1.7$), transition region ($1.7 < |\eta| < 1.9$), and endcaps which in total cover the
 88 region of $|\eta| < 2.7$. The MS contains a system of precision tracking chambers embedded in a toroidal
 89 magnetic field produced by three large air-core superconducting magnets. The MS has three measuring
 90 stations to make additional precision measurements of muons' tracks and momentum, since muons are
 91 the only particle that can penetrate through to the MS. The designed precision of the MS is to measure
 92 the momentum of a 100 GeV muon within 3% and a 1 TeV muon to within 10% accuracy.

93 In addition to the detector subsystems described above, the ATLAS experiment also contains a trigger
 94 system with three levels. Triggers are vital to the experiment and allow the experiment to decide which
 95 events should be recorded for physics analysis. The trigger system makes these decisions based upon
 96 certain event selection criteria. This procedure is critical for the experiment at the LHC since the 40
 97 MHz collision rate in the LHC proton-proton collisions would produce terabytes of data per minute if
 98 each event were recorded. The first level of triggers (LV1) is hardware based and is completely located in
 99 the calorimeter and MS. LV1 triggers have course granularity and primarily determine regions of interest
 100 based upon particle flight path in the MS or the calorimeter. LV1 triggers have low granularity because
 101 they must make a decision before the next bunch crossing to avoid a large pileup of data. If an event
 102 passes the LV1 triggers it is sent to the higher level trigger system which includes the level two trigger
 103 (LV2) and event filter (EF or LV3). LV2 is a software based trigger which partially reconstructs the
 104 event by looking at the regions of interest indicated by the LV1 trigger in the MS and calorimeter. Those
 105 events that pass the LV2 trigger are sent to the EF where the event is fully reconstructed and the final
 106 trigger decisions are made After passing the EF, events are recorded at a rate of 300 MB/s. Because of
 107 the trigger system, the event rate falls from 40 MHz in the LHC to 75 KHz after LV1, then 3 KHz after
 108 LV2, and finally 300 Hz after EF for event collection.

109 Due to the 50 ns bunch-crossing there is a large "pileup" of collisions, since each bunch-crossing
 110 produces around 20, and up to 40, proton-proton collisions. This creates the challenging problem of cor-
 111 rectly recreating events and correctly tracing particles back to the correct primary vertex of the interaction

112 point. A graph of the number of proton-proton collisions per bunch crossing, as well as a reconstructed
 113 bunch crossing with 25 collisions can be seen in Figure 3 for data collected in 2011 and 2012. This rate
 114 of collisions allows the LHC to deliver data at a record breaking rate. The amount of data delivered by
 115 the LHC, as well as the amount that is suitable for physics analyses can be seen in Figure 4 for both
 116 2011 and 2012.

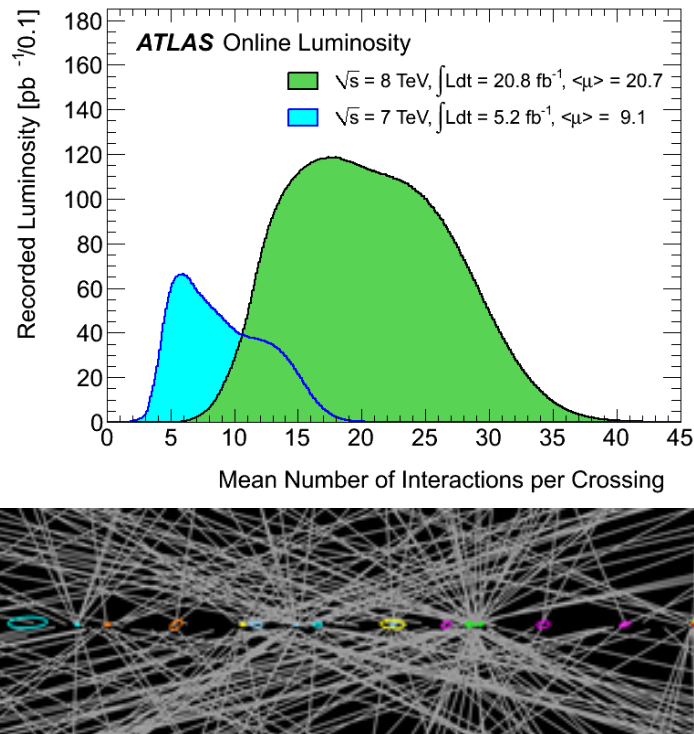


Figure 3: The mean number of proton-proton collisions per bunch crossing for 2011 and 2012 collected in ATLAS (top) [2] and a reconstruction bunch crossing with 20 interaction vertices (bottom).

117 Since protons are predominantly made of gluons with three small quarks (uud) "floating" in a sea
 118 of gluons, the vast majority of the proton-proton collisions result in the collision of two gluons. It is
 119 extremely rare to see a quark-quark collision. For this reason our predominant model is based upon
 120 gluon-gluon fusion. Additionally, since the gluons that collide do not necessarily have the same velocity
 121 along the beam pipe (z-axis), the center of mass of the collision will have velocity along the z-axis. For
 122 this reason our measurements are done in the transverse plane perpendicular to the beam pipe to avoid
 123 any center of mass velocity.

124 2.3 Grid Computing for Data Processing

125 The ATLAS data processing (data quality checks, prompt event reconstruction and calibrations, as well
 126 as Monte Carlo event productions) for physics analyses are carried out with a grid computing system [13].
 127 Data analysis for individual physics topics are done at individual institutes with local computing system.
 128 The Worldwide LHC Computing Grid (WLCG) is the world's largest computing grid and serves more
 129 than 5000 physicists around the world. The WLCG contains more than 150 computing centers (from
 130 Tier-0 to Tier-4) around the world in 40 different countries to store and analyze multi-terabytes of data.
 131 Tier computing systems are ordered depending upon their responsibilities and can be accessed from

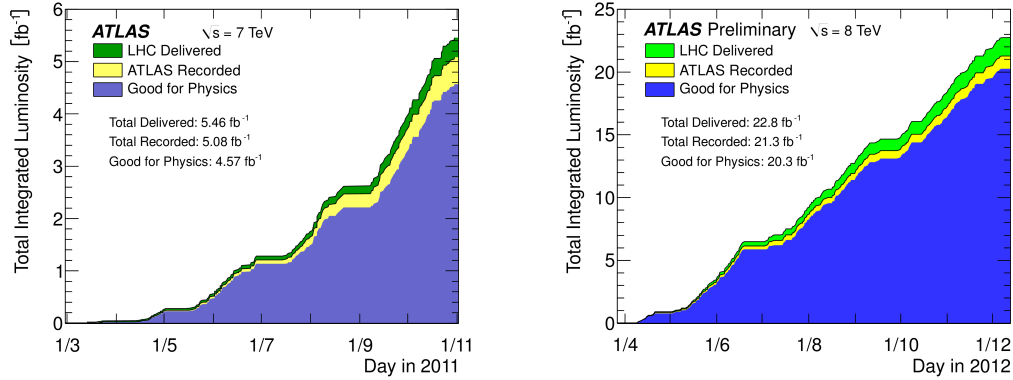


Figure 4: Total integrated luminosity from the LHC and ATLAS for 2011 at 7 TeV (left) and for 2012 at 8 TeV (right) [2].

132 around the world. CERN is Tier-0, where the data is produced, promptly reconstructed and distributed.
 133 Tier-1 centers are national centers that are responsible for holding the most updated raw data from CERN,
 134 in addition to doing data analysis. Tier-2 facilities are regional computer clusters used primarily for
 135 Monte Carlo event productions, detector calibrations, and data analyses. To run computing jobs on the
 136 the grid facility: physicists can upload the analysis code to the grid and specify which data files they
 137 wish to use. The grid sends the jobs to various tiers where the data is available and then splits the job
 138 among various computer cores at that tier according to how the splitting was specified by the maker of
 139 the code. The results of finished jobs are then sent back to the physicist. Most the computational jobs in
 140 the final stages of a physics analysis are done at local Tier-3 computing system. Michigan is responsible
 141 for a Tier-2 and Tier-3 computing system, where the Tier-3 is dedicated for Michigan physicists and the
 142 Teir-2 system stores the majority of the LHC dataset. The analysis presented in this thesis was carried
 143 out using Michigan Tier-3 computing cluster.

144 3 Event Reconstruction and Monte Carlo Simulations

145 Physics objects from the event reconstructions of raw data collected by ATLAS are the basis of data
 146 analysis, as well as physics modeling and detector simulations with Monte Carlo (MC) techniques used
 147 to simulate data. The important physics objects for this analysis are electrons and muons.

148 3.1 Lepton Reconstruction and Identification

149 Electrons are reconstructed from energy deposits in the electromagnetic calorimeter and matched to a
 150 track in the inner detector. For the 2012 data at 8 TeV, improved electron discrimination from jets is
 151 obtained using a likelihood function from parameters characterizing the electromagnetic shower shape
 152 and track association, which significantly increased electron identification efficiency and decreased mis-
 153 identification rate compared to 7 TeV data analyses. Electron candidates are required to have $p_T > 7$
 154 GeV and $|\eta| < 2.47$. The electron reconstruction and identification efficiency is greater than 75%.

155 Muons are identified by tracks (or track segments) reconstructed in the MS, which are matched to
 156 tracks reconstructed in the ID. The muon momentum is calculated by combining the information from
 157 the two subsystems and correcting for the energy lost in the calorimeter. Additionally, one muon in
 158 each event is allowed to be a stand-alone muon or a calorimeter-tagged muon, where stand-alone muon
 159 is identified by only having a muon spectrometer track in $2.5 < |\eta| < 2.7$, and the calorimeter-tagged

160 muon is identified by an inner detector track with $p_T > 15$ GeV associated with a compatible calorimeter
161 energy deposit in $|\eta| < 0.1$. All muon candidates are required to have $p_T > 4$ GeV and $|\eta| < 2.7$. The
162 muon reconstruction and identification efficiency is greater than 94%.

163 3.2 Physics Modeling

164 The Higgs production and decays at the LHC are modeled by the *Powheg* MC generator, which is used
165 to calculate the signal cross sections and includes perturbative QCD corrections to next-to-leading order
166 (NLO) [6]. The CT10 set of parton distribution functions (pdfs), QCD renormalization, factorization
167 scales, μ_R , and $\mu_F = M_{4l}$ are used in the calculations. To generate MC events with detector simulations to
168 determine the signal acceptance, *Powheg* is interfaced with the *Pythia* MC Program and *Photos*. *Pythia*
169 is used to simulate parton showering and hadronization [12], while *Photos* is responsible for simulating
170 radiated photons from charged leptons [9].

171 The *JHU* generator is used to generate Higgs events with alternative spin and parity states. These
172 calculations are done with leading order corrections for perturbative QCD corrections [8]. Each event
173 from the *JHU* generator must be reweighted to make sure the leading order Higgs p_T distribution is con-
174 sistent with the Higgs p_T distribution generated by the NLO *Powheg* generated events, which generates
175 the SM Higgs events. The *JHU* MC calculates the correlations of the leptons decay from the Higgs
176 boson that are sensitive to the Higgs Spin and Parity quantum numbers.

177 Background events are modeled and produced using the following MC Generators: *MC@NLO* (for
178 top events) [7], *Alpgen* (for $Z/W + jets$ events) [10], and *Powheg* for diboson (ZZ , Zg , and ZW) events.

179 MC generators produce events from proton-proton collisions based on theoretically predicted pro-
180 duction cross sections and kinematic distributions. These events are input for the detector simulation
181 and reconstruction programs which produce MC datasets used to simulate the data collected from the
182 proton-proton collisions at the LHC and reconstructed by ATLAS experiment.

183 3.3 Detector Simulations

184 The detector response simulation is based on the GEANT4 program [5]. Additional inelastic proton-
185 proton collisions in each bunch crossing (referred to as pile-up) are included in this simulation. Addi-
186 tionally, the MC events are reweighted to reproduce the observed pile-up distribution, the average number
187 of collisions per bunch-crossing in the data. The distribution of the number of proton-proton collisions
188 per bunch crossing for both 7 TeV and 8 TeV data can be seen in Figure 4 .

189 Furthermore, GEANT4 contains detailed descriptions of the detectors' materials and how they react
190 to particles passing through them, such as gas ionization from a particle passing through a gaseous muon
191 detector. With this information, a particle's interactions with the detector can be simulated. However,
192 the results of all these procedures follow distributions governed by the laws of physics for particles
193 interacting with matter. Therefore, Monte Carlo programs are used to generate random numbers from
194 these distributions that are based on underlying physics to simulate the detector response.

195 MC simulated events for physics analysis must be calibrated and corrected to precisely simulate real
196 detector responses and reproduce data distributions. The corrections and calibrations are done with con-
197 trol data samples that are very well understood and produce a very clean and strong signal, such as $Z \rightarrow \mu\mu$
198 and $Z \rightarrow ee$ events. In this analysis, the MC lepton identification and trigger efficiencies are corrected
199 based on studies performed in data control regions. The energy and momentum scales, as well as their
200 resolutions, of the MC events are calibrated to reproduce data from $Z \rightarrow ll$ and $J/\Psi \rightarrow ll$ decays. The
201 uncertainties of the $H \rightarrow ZZ^* \rightarrow 4l$ signal detection efficiencies are determined by varying the nominal
202 calibrations: lepton energy resolution, momentum resolutions, the lepton trigger, as well as reconstruc-
203 tion and identification efficiencies. The overall uncertainties in the Higgs signal efficiencies range from
204 2.7% to 9.8%, depending on final state lepton flavors, where the major uncertainty contributions are from

205 the lepton reconstruction and identification efficiencies. These uncertainties are considered in the final
 206 J^P analysis and will be described in Section 5.4.

207 4 Higgs Event Selection

208 The $H \rightarrow ZZ^* \rightarrow 4l$ channel is characterized by a four-lepton final state with two pairs of same flavor
 209 opposite charge leptons. This channel is referred to as the "golden channel" for the Higgs boson dis-
 210 covery since the four leptons can be measured very well and the final state signature is easy to detect.
 211 Additionally, this channel has very low background contamination due to its clean final state. Figure 5
 212 shows reconstructed Higgs candidates in the $4e$ and 4μ channel from data in ATLAS, where the tracks in
 213 the muon spectrometer and the showers in the LAr calorimeter are highlighted in the $4e$ and 4μ channel
 214 decays, respectively.

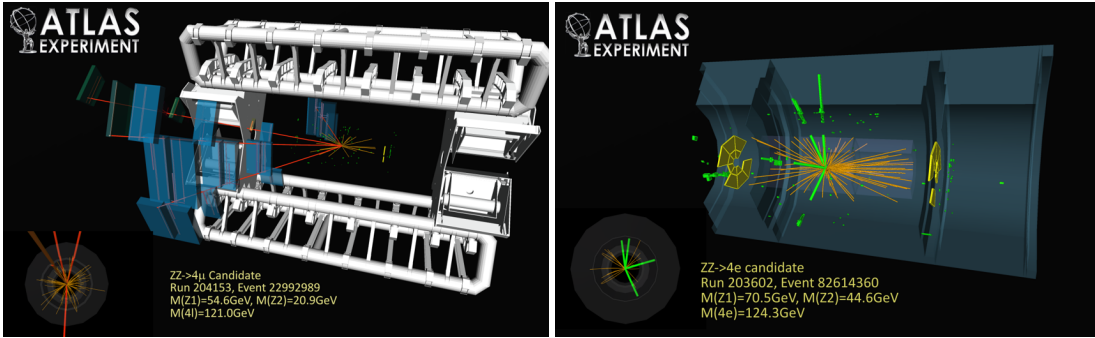


Figure 5: Higgs candidate in the 4μ channel (left) and $4e$ channel (right) in the ATLAS detector.

215 This decay channel contains one real (on-shell) Z boson and one virtual Z^* boson with a mass of 30
 216 GeV. The cross section of the Higgs boson production is dominated by the gluon-gluon fusion process
 217 ($19.5 fb$ at 8 TeV). Additionally, the Higgs can be produced through vector-boson fusion ($1.57 fb$ at 8
 218 TeV) and the association production mechanism with W and Z vector bosons ($1.08 fb$ at 8 TeV). The
 219 association production with top pair accounts for less than 1% of the Higgs production cross section
 220 ($0.13 fb$). The decay branching ratio for $H \rightarrow ZZ^* \rightarrow 4l$ is only 0.012%. For these reasons, we expect
 221 the number of four-lepton events found at the Higgs resonance to be statistically limited, which requires
 222 great effort to retain high efficiency in the event selection.

223 4.1 $H \rightarrow ZZ^* \rightarrow 4l$ Event Selection

224 Events are selected from proton-proton collisions by requiring at least one reconstructed vertex with at
 225 least three charged particle tracks with $p_T > 0.4$ GeV. If more than one vertex satisfies the selection
 226 requirement, the primary vertex is chosen as the one with the highest Σp_T^2 , where the sum runs over all
 227 tracks associated with this vertex.

228 The $H \rightarrow ZZ^* \rightarrow 4l$ events must contain at least four identified leptons, selected with criteria de-
 229 scribed in Section 3.1. In order to reject electrons and muons faked by jets, only isolated leptons are
 230 selected, requiring the scalar sum of the transverse momentum, Σp_T , of other tracks inside a cone size of
 231 $\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2} = 0.2$ around the lepton to be less than 15% of the lepton p_T . In addition, the ΣE_T
 232 deposited in calorimeter cells inside a cone of $\Delta R = 0.2$ around the lepton track, excluding the transverse
 233 energy due to the lepton and corrected for the expected pile-up contributions, is required to be less than
 234 30% of the lepton p_T for 7 TeV data, less than 2% for electrons from 8 TeV data, and less than 15%

235 for stand-alone muons. To further reject leptons from heavy-flavor jets, the impact parameter relative
 236 to the primary vertex is required to be less than 3.5 (6.0) standard deviations for all muons (electrons).
 237 This looser electron requirement allows for the tails in the electron impact parameter distribution due to
 238 bremsstrahlung radiation in the inner detector.

239 The Higgs candidate quadruplets are formed by selecting two opposite-sign, same-flavor dilepton
 240 pairs in an event. The four leptons of the quadruplets are required to be well separated, $\Delta R > 0.1$ for
 241 same-flavor lepton pairs and $\Delta R > 0.2$ for $e\mu$ pairs. The two leading leptons, determined as the two
 242 leptons with the highest p_T , must have $p_T > 20$ GeV and $p_T > 15$ GeV. The third lepton must have
 243 $p_T > 10$ (8) GeV if it is an electron (muon). The lepton pair with greatest invariant mass (denoted
 244 M_{12}) and closest to the Z pole mass is called the leading lepton pair, while the sub-leading lepton pair
 245 is chosen to have the largest invariant mass (denoted M_{34}) among the remaining possible pairs. The
 246 dilepton masses must satisfy $50 < M_{12} < 115$ GeV, and $M_{34} > 12$ GeV. In the $4e$ and 4μ channels all
 247 same-flavor, opposite-sign lepton pairs are required to have invariant masses greater than 5 GeV. This
 248 helps reject event contamination from $J/\Psi \rightarrow ll$ decays. The final cut on the quadruplet requires M_{4l}
 249 to be within the Higgs signal region of 115 GeV to 130 GeV. A total of 31 Higgs candidate events are
 250 selected from the 2011 and 2012 datasets: 13, 8, 9, and 7 events from the 4μ , $2\mu 2e$, $2e 2\mu$, and $4e$ final
 251 state, respectively, where $2\mu 2e$ ($2e 2\mu$) indicates the leading lepton pair is comprised of 2μ ($2e$).

252 From MC simulation studies, we expect to select total 15.1 Higgs signal events and 8.7 irreducible
 253 background events from the SM $qq \rightarrow ZZ^* \rightarrow 4l$ process. The reducible background from $Z + Jet$ and
 254 top events are estimated using a data-driven method to contribute 2.24 events, which will be described
 255 in the next section. Figure 6 shows the inclusive $4l$ invariant mass distribution without applying the final
 256 Higgs mass cut, from which we see that the Higgs resonance mass is around 125 GeV. This peak is
 257 clearly observed over the background. The Higgs signal significance is computed to be 6.6σ , exceeding
 258 the 5σ criteria to claim a discovery of a new particle in high energy physics.

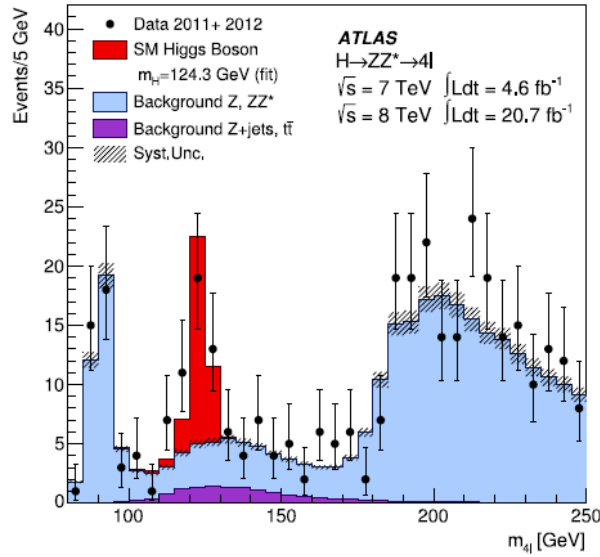


Figure 6: M_{4l} distribution with combined 7 TeV and 8 TeV data.

259 4.2 Background Estimation

260 $Z + Jet$ background consists of events that contain an on-shell Z boson, as well as a jet. This process
 261 can be confused as a $H \rightarrow ZZ^* \rightarrow 4l$ decay if the jet produces a pair of same flavor oppositely charged
 262 leptons. The leptons produced in jets will often have lower energies, which is similar to the low energy
 263 leptons produced from the decay of the virtual Z boson at 30 GeV. Therefore, since both decay processes
 264 involve an on-shell Z boson, if the jet produces a pair of same flavor oppositely charged leptons with a
 265 combined mass of 30 GeV, then a $Z + Jet$ event may be mistaken as a $H \rightarrow ZZ^* \rightarrow 4l$ event. There are
 266 however more cuts to avoid this mis-identification, such as the impact parameter cuts described above.

267 The background contamination from the $t\bar{t}$ production comes from its decay into a pair of opposite
 268 sign W bosons, as well as two b quarks. The opposite sign W bosons can in turn decay into leptons of
 269 the same flavor, producing a same flavor oppositely charged pair of leptons that could be mistaken for
 270 an on-shell Z boson. The two b quarks would produce jets that could produce another pair of leptons to
 271 mimic the virtual Z . In this manner a Higgs event could be mis-identified.

272 Both $Z + Jet$ and top background are estimated from data. As described above these background
 273 events may contain two isolated leptons from Z decays or W decays in top events, together with additional
 274 activities such as heavy flavor jets or misidentified components of jets yielding reconstructed leptons.
 275 These background estimations are done using background-enriched control data samples containing two
 276 isolated leptons (ll) and two lepton-like jets (j_l, j_l) in each event. The control samples are selected with
 277 the standard signal requirement except that the lepton-like jets are selected in place of two of the signal
 278 leptons. The total reducible background in the signal sample is estimated by scaling each event in the ll
 279 and j_l, j_l control sample by $f_1 \cdot f_2$, where the factor $f_i (i = 1, 2)$ for each of the two lepton-like jets depends
 280 on lepton flavor and p_T . The factor f is the ratio of the probability for a jet to satisfy the signal lepton
 281 selection criteria to the probability for a jet to satisfy the lepton-like jet selection criteria, and is obtained
 282 from independent jet-enriched data samples dominated by $Z + Jet$ or top pair events. The total estimated
 283 reducible background is 2.24 events in the selected Higgs signal sample.

284 4.3 Observed and Expected Number of Events at the Higgs Resonance

285 Table 4.3 gives the number of observed and expected events from the combined 7 TeV and 8 TeV datasets.
 286 The expected numbers of events include the Higgs signal, the irreducible ZZ^* background, and the
 287 reducible background from $Z + Jet$ and top events.

Channel	Higgs	ZZ^*	Reducible Background	Expected	Observed
$\mu\mu\mu\mu$	5.68	3.35	0.75	9.78	13
$\mu\mu ee$	2.94	1.58	0.52	4.04	8
$ee\mu\mu$	3.77	2.31	0.69	6.77	9
$eeee$	2.67	1.42	0.29	4.38	7
Total	15.06	8.65	2.24	25.95	31

288 These estimates for the expected number of events will be used to calculate the expected and observed
 289 significance of a specific J^P state for the spin and parity studies.

290 5 Spin-Parity Measurement

291 5.1 Multivariable Analysis

292 The discovery of the Higgs boson opened a new chapter in the history of particle physics. The measure-
 293 ments of the newly discovered boson's properties, including mass, couplings, spin, and parity quantum

294 numbers, will play a central role in confirming the SM Higgs and aid in the search for unknown physics
 295 in the Higgs sector beyond SM. This chapter will provide a detailed description of the spin and parity
 296 measurement with the four-lepton final states using events selected by the criteria described in Section
 297 4.1. The SM Higgs boson is predicted to have spin 0 and even parity, $J^P = 0^+$. However, there are other
 298 theoretical models that predict the Higgs-like boson could have different spin and parity states, or mixing
 299 states of even and odd parities. The method used to test the likelihood or find the exclusion of a specific
 300 J^P hypothesis involves a multivariable analysis which utilizes a boosted-decision-tree (BDT). This is
 301 necessary because the observed number of events is only 31, including the estimated background contri-
 302 bution of 10.9 events. The BDT output is calculated based on several sensitive variables and used to be
 303 the final discriminating variable to separate different spin and parity states. In this study, parity-even and
 304 parity-odd resonances of spin 0, 1, and 2 (denoted as $J^P = 0^+, 0^-, 1^+, 1^-, \text{and } 2^+$) are considered. In this
 305 study, spin and parity hypotheses are tested in pairs. In each individual test, a hypothesis is assumed for
 306 the spin and parity of the observed resonance, and the exclusion significance is calculated with respect
 307 to other modes. The goal is therefore to find a model for which the observed exclusion with respect to
 308 all other hypothesis is comparable to the expected sensitivity given by the observed data. To confirm the
 309 new boson is indeed the SM Higgs boson, the $J^P = 0^+$ state is compared with all other J^P states.

310 The $H \rightarrow ZZ^* \rightarrow 4l$ reconstructed events, with the decay of Z bosons, provides full information of
 311 the Z decay planes. The spin and parity sensitive variables used for this measurement include the five
 312 decay angles as shown in Figure 7, and the dilepton invariant masses: M_{12} and M_{34} . The BDT analysis
 313 will use these variables to create a final discriminate variable.

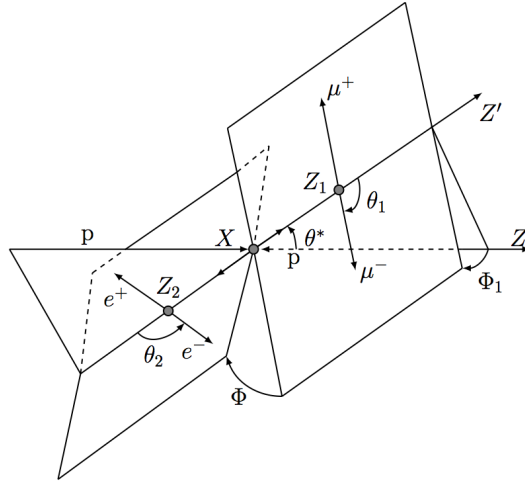


Figure 7: Illustration of the Higgs decay angular variables sensitive to the Higgs' spin and parity [4].

314 5.1.1 Boosted Decision Trees

315 The Boosted-Decision-Tree (BDT) is a multivariable analysis technique that was developed at the Uni-
 316 versity of Michigan, and is used in this analysis to separate different spin and parity states in hypothesis
 317 tests. BDTs are often used with statistically limited datasets. Since no single spin sensitive variable can
 318 be used to completely determine the spin and parity, a BDT has been employed. BDTs utilize the sep-
 319 aration power of each variable to separate two samples. Additionally, the BDT produces a single BDT
 320 output (score) for each event, which reduces the multivariable input into a single discriminating variable.
 321 Details of the BDT algorithm can be found in [11], and a brief description is given below.

322 The BDT technique involves a 'training' procedure for event pattern recognition. The BDT requires

323 two data samples to separate, such as a *signal* and *background* sample. The data is represented by a set
 324 of physics variable distributions. These physics variables are given to the BDT as input. A decision-
 325 tree splits data recursively based upon cuts on the input variables until a stopping criterion is reached
 326 (e.g. *signal* purity, minimum number of event, and designed number of decision-tree nodes). After these
 327 recursive splittings, every event ends up in a signal (score=1) or a background (score=-1) leaf of the
 328 decision-tree. Misclassified events will be given larger weights in the training of the next decision-tree
 329 (boosting). This procedure is repeated several hundreds to thousands of times until the performance is
 330 optimized. The discriminator produced by the BDT training is the sum of the weighted scores from all
 331 the decision-trees. If the total score for a given event is relatively high this event is most likely a signal
 332 event, and if the score is low it is likely a background event.

333 Applying this technique to separate different spin and parity hypotheses, the $J^P = 0^+$ hypothesis is
 334 treated as *signal* and alternative J^P state as *background* in the BDT training. The BDT output (score)
 335 distribution is used as the final discriminant. The BDT output distributions are later used as the *signal*
 336 (0^+ state) and *background* (alternative J^P state) probability density functions for toy MC experiments
 337 produced to perform the statistic analysis for final spin and parity state measurement, as described in
 338 Section 5.3.

339 The systematic uncertainties of the BDT discriminants are evaluated by varying the input variable
 340 calibration uncertainties. These uncertainties are taken into account when producing the toy MC experi-
 341 ments for hypothesis testing and are described in Section 5.4. Additionally, BDTs suffer from overtrain-
 342 ing systematics caused by insufficiently large samples. Overtraining occurs when a certain type of event
 343 is over sampled by the BDT and therefore over represented in the training, the statistical fluctuations in
 344 small samples can be large. BDTs can also be overtrained if the depth of the tree is too large. Overtrain-
 345 ing effects can be seen when comparing the BDT output distribution from the sample used for training
 346 and the BDT output distributions from a "test" sample, often these training and testing samples are each
 347 half of the original input sample.

348 5.1.2 Spin and Parity Sensitive Variables

349 The $H \rightarrow ZZ^* \rightarrow 4l$ channel, where $l = e$ or μ , benefits from the full reconstruction of four-lepton final
 350 state, which produces many spin and parity sensitive variables. The observables sensitive to the Higgs
 351 spin and parity are the reconstructed Z boson masses, M_{12} and M_{34} , as well as five decay angles that
 352 describe the decay of the Higgs boson in its rest frame (Figure 7): the production angle θ^* and the decay
 353 angles Φ , Φ_1 , θ_1 , and θ_2 .

354 The production angle θ^* defined in the four-lepton rest frame is the angle between Z_1 and the beam
 355 pipe. Φ_1 is the azimuthal angle of the Z_1 decay plane. The decay angle Φ is the azimuthal angle between
 356 the decay planes of Z_1 and Z_2 . The decay angle θ_1 (θ_2) is the angle between the decay vector of the
 357 negative reconstructed lepton and the direction of flight of Z_1 (Z_2). The expected (via MC) and observed
 358 distributions of each variable, as well as a comparison between the expected results for 0^+ and 0^- , can
 359 be seen in Figure 8, 9, and 10. From these distributions it is evident that no single variable can be used
 360 to determine if data favors 0^+ or 0^- . For this reason the BDT multivariable analysis must be used.
 361 Additionally, the BDT output distribution for 0^+ versus 0^- can be seen in Figure 11

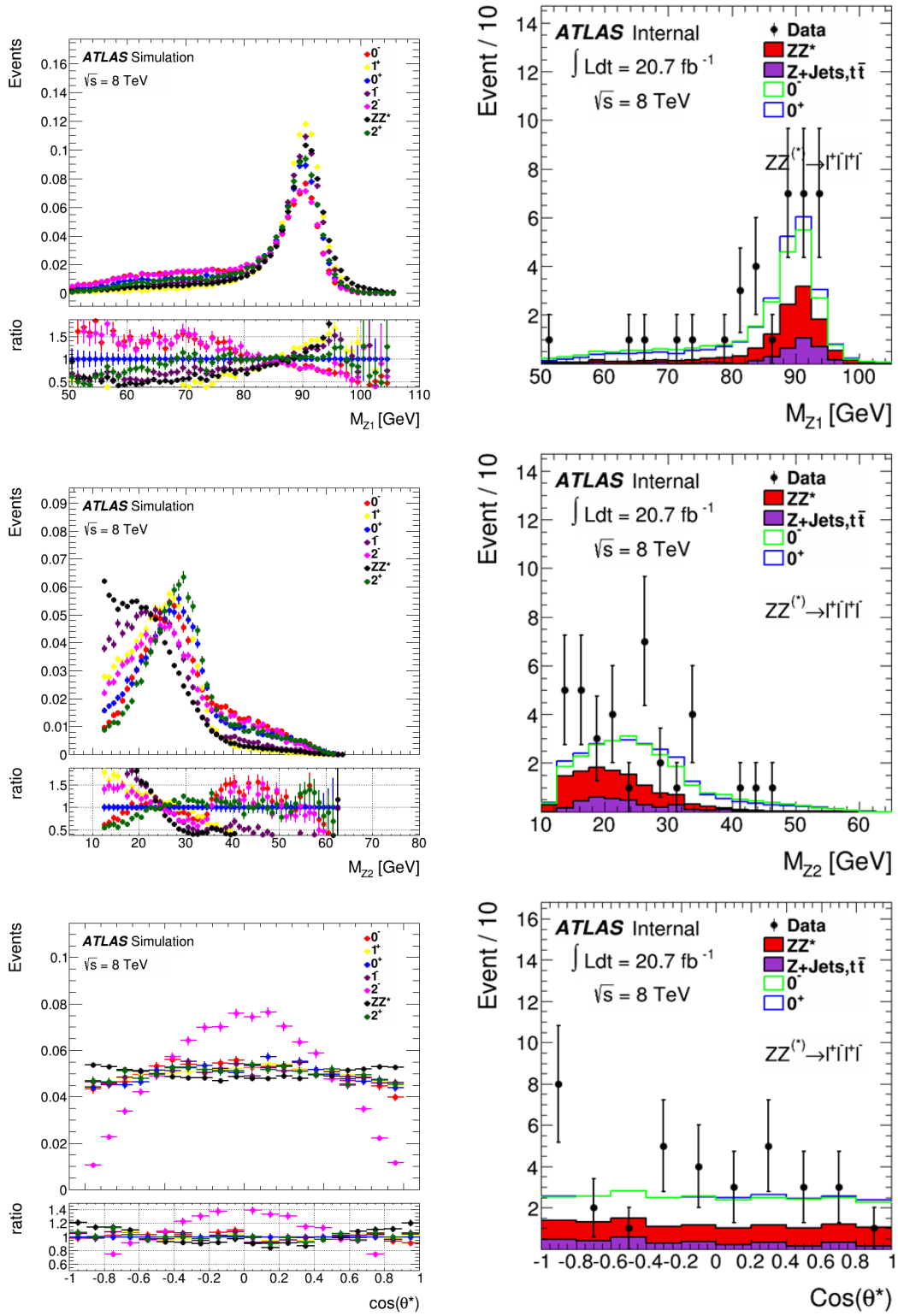


Figure 8: Comparison of kinematic J^P sensitive observables and the production angle that describes the decay of Z_1 for different J^P states and with data compared to 0^+ and 0^- .

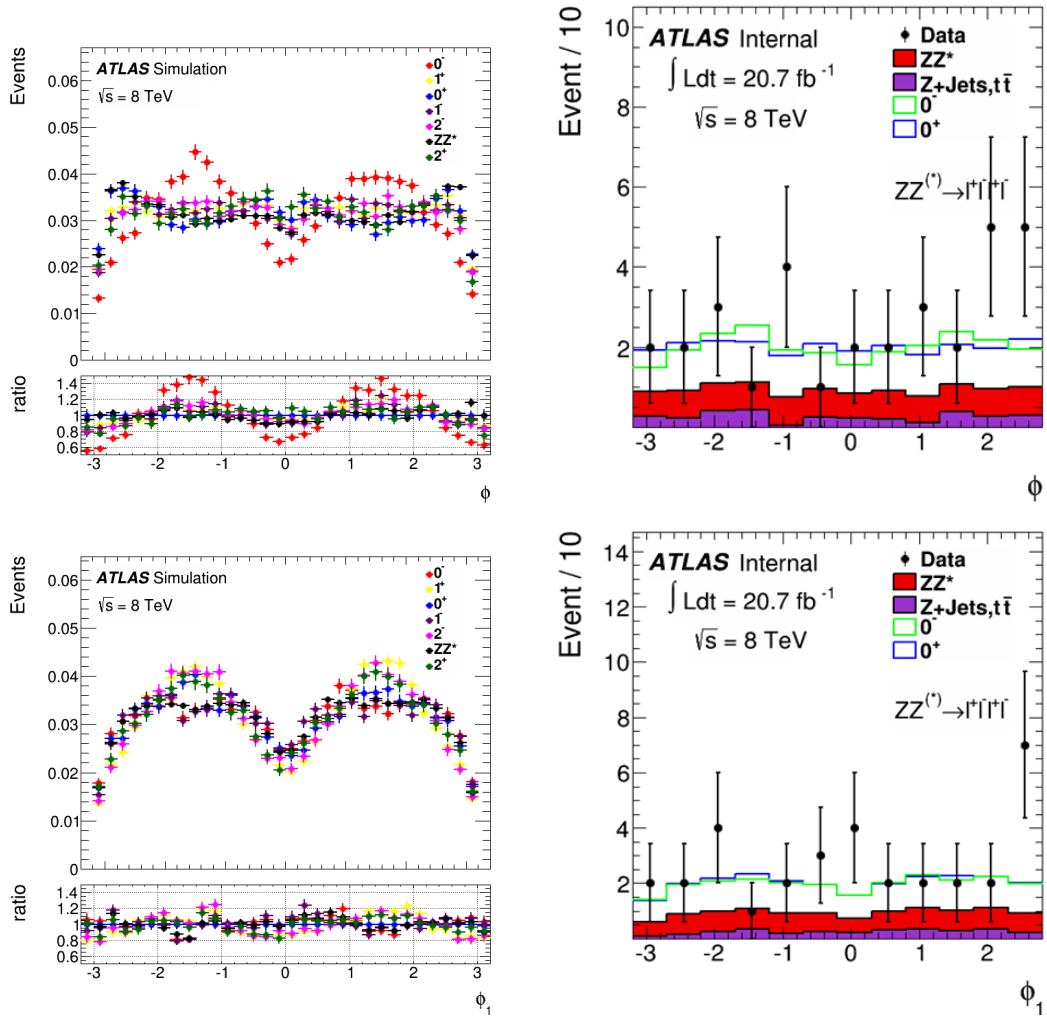


Figure 9: Comparisons of angular J^P sensitive observables which describe the Z decay planes for different J^P states and with data compared to 0^+ and 0^- .

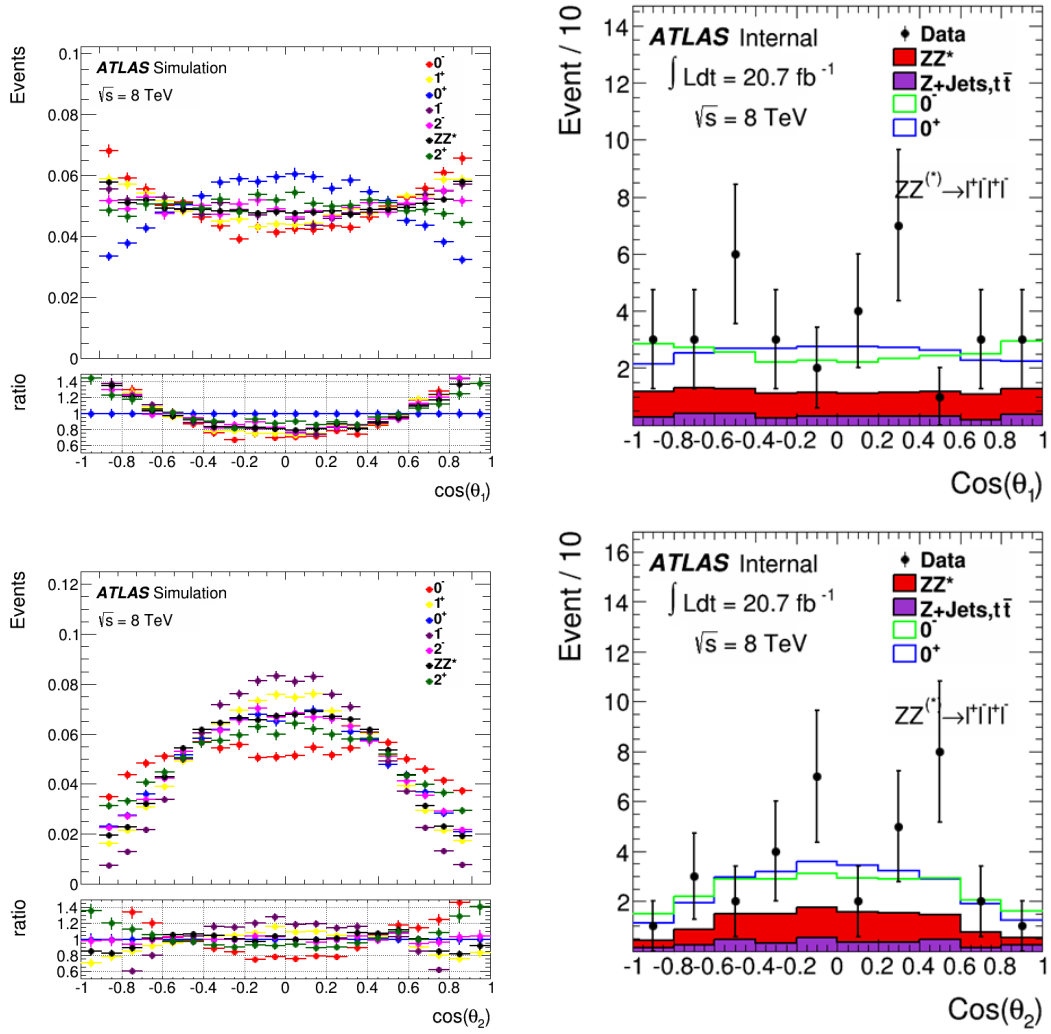


Figure 10: Comparisons of angular J^P sensitive observables which describe the Z decay products for different J^P states and with data compared to 0^+ and 0^- .

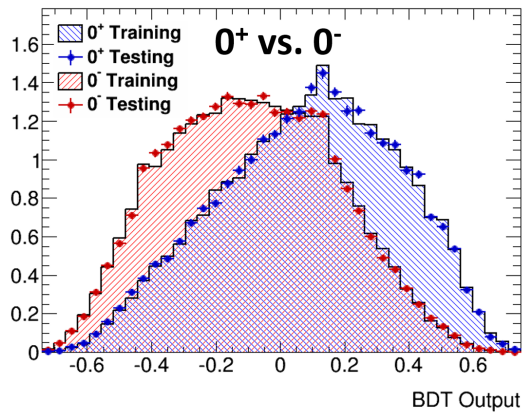


Figure 11: BDT output from training 0^+ versus 0^- .

362 5.2 Probability Density Function Creation

363 The hypothesis test used to obtain the final significance or exclusion of J^P states utilizes many conditional
 364 Poisson probabilities based upon the given and expected number of events, which is detailed in Section
 365 5.3. To model the expected number of events, 1 dimensional probability density functions (PDFs) are
 366 made from the BDT output (D_{J^P} discriminator) and normalized to the expected number of events for the
 367 corresponding PDF. Furthermore, to better separate the Higgs signal from the background, these PDFs
 368 are made in *high* and *low* pairs defined by either a high or low signal to background ratio. The high
 369 signal to background region is defined as $121 < M_{4l} < 127$ GeV, while the low signal to background
 370 region covers $M_{4l} > 127$ GeV and $M_{4l} < 121$ GeV. A PDF is made for each decay channel in the two
 371 J^P states being considered, as well as for each background. This set of plots is also made for each
 372 systematic, as will be discussed in Section 5.4. Since these PDFs will be used to calculate the expected
 373 number of events, we do not expect there to be much fluctuation between neighboring bins. Additionally,
 374 the PDFs cannot have empty bins, as they have a large negative effect on the hypothesis test results since
 375 the probability of finding an event in this region should not be 0. To account for the empty bins at the
 376 tails of the distributions and to make sure bins do not vary too much from their neighbors, each PDF is
 377 smoothed using a kernel density estimator (kde) with a Gaussian kernel of varying width. An example
 378 of a PDF can be seen in Figure 12, where the PDFs for 0^+ and 0^- are compared to each other and
 379 data. From this distribution it is evident the separation power between the two hypotheses is still small
 380 given the amount of data we currently have. However, we can still get good exclusion confidence levels
 381 utilizing a hypothesis test method that samples these PDFs, as described in 5.3.

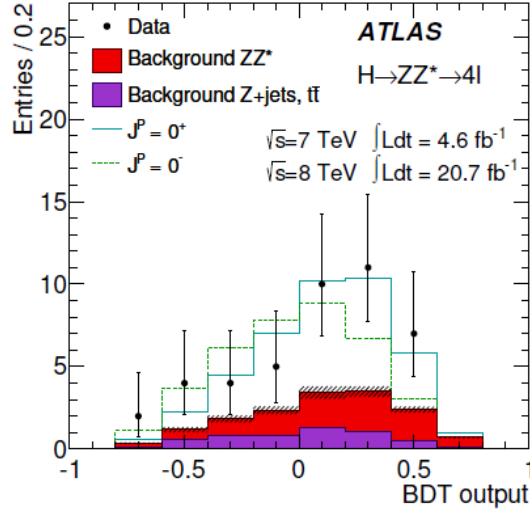


Figure 12: Distribution of the 0^+ versus 0^- BDT output for data and MC, where the $J^P=0^+$ hypothesis (solid line) and the $J^P=0^-$ hypothesis are plotted together for comparison.

382 The kde is a way to estimate the PDF of a random variable using finite data points by treating entries
 383 as a PDF themselves, instead of a single point, by placing a normalized distribution, such as a Gaussian
 384 in this case, at the point of each data entry. The final PDF is given by summing individual distributions
 385 placed at each data entry. The formal definition of a kde with a Gaussian kernel is

$$f(x) = \frac{1}{N} \sum_{i=1}^N K\left(\frac{x-x_i}{h}\right) \text{ where } K(u) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}u^2} \quad (1)$$

386 where h is referred to as the bandwidth. In the Gaussian case, h acts similar to the standard deviation.

387 The kde used in this measurement has a variable bandwidth based upon the number of events in a given
 388 region. In regions well populated by data points, the bandwidth is small so the Gaussians resemble
 389 points, while the bandwidth is increased in regions with fewer events. This process protects the original
 390 shape of the distribution from being over-smearred in areas with higher populations, while still providing
 391 a smooth distribution with no empty bins, which is expected for this analysis.

392 5.3 Statistical Method

393 To measure the separation between different J^P states, the PDFs created from BTD outputs, described
 394 above, are used to create a likelihood function $\mathcal{L}(J^P, \mu, \theta)$ that depends on the J^P assumptions. This
 395 likelihood is the production of conditional probabilities over the binned PDFs in each channel, and is
 396 calculated twice under the assumption of the signal and null hypotheses (H_0 and H_1). These two like-
 397 lihoods are then used to create a final test-statistic, q . This process of calculating the test statistic is
 398 done thousands of times using MC toy experiments, where the expected number of events for signal
 399 and background are slightly varied based upon a Poisson Distribution. These thousands of toy MCs are
 400 used to create a distribution of test statistics for the case of assuming H_0 and H_1 , which are then used to
 401 determine the corresponding p_0 value for both hypotheses.

402 As mentioned, the likelihood is the production of conditional probabilities over each bin of the PDFs:

$$\mathcal{L}(J^P, \mu, \theta) = \prod_n^{N_{\text{Chann.}}} \prod_j^{N_{\text{Bins}}} P(N_{n,j} | N_{n,j}^{\text{Exp.}}). \quad (2)$$

403 Here N is the given number of events either from data or simulated data, μ is the signal strength, and θ
 404 represents the nuisance parameters. $P(N_{n,j} | N_{n,j}^{\text{Exp.}})$ is the Poisson probability of getting N events from
 405 data, given an expected number of events $N^{\text{Exp.}}$.

406 The expected number of events, $N^{\text{Exp.}}$, is determined using the signal and background PDFs:

$$N_{n,j}^{\text{Exp.}} = \mu_n \mathcal{L} N_n^{\text{signal}} \left[\varepsilon \cdot PDF_{n,j}^{H_1} + (1 - \varepsilon) \cdot PDF_{n,j}^{H_0} \right] + \sum_b^{N_{\text{Background}}} N_{n,b}^{\text{Background}} PDF_{n,b,j}^{\text{Background}} \quad (3)$$

407 Here ε is the parameter of interest, which is either 0 or 1 when looking at hypothesis H_0 ($\varepsilon = 0$) or H_1
 408 ($\varepsilon = 1$). Additionally, $PDF_n^{\text{Background}}$ and PDF_n^{Signal} are the normalized PDFs of the n th channel created
 409 from the BDT output for background and signal, respectively, with the index j summing over the bins.
 410 $N_{n,b}^{\text{Background}}$ and N_n^{Signal} are the expected number of signal and background b events, as described in Sec-
 411 tion 4.2. \mathcal{L} is a normalized variable that accounts for the uncertainty in the total integrated luminosity.
 412 The two likelihoods, $\mathcal{L}(H_1, \mu, \theta)$ and $\mathcal{L}(H_0, \mu, \theta)$ are calculated in the same way, except ε is 1 (0) for
 413 H_1 (H_0). $N_{n,b}^{\text{Background}}$ and N_n^{Signal} represent the number of events in the b th background and signal, re-
 414 spectively, in the n th channel. The parameters \mathcal{L} , $N_{n,b}^{\text{Background}}$, N_n^{Signal} , and the signal strength (μ) are
 415 nuisance parameters whose average values and uncertainties are found from the nominal event selection.
 416 The nuisance parameters are constrained by Gaussian terms with a standard deviation of the uncertainty.
 417 The nuisance parameters in the likelihood are profiled, such that each parameter is fitted to a value that
 418 maximizes the likelihood. The final test statistic used to distinguish between the two signal J^P states is
 419 based on the ratio of the two profiled likelihoods:

$$q = \log \left(\frac{\mathcal{L}(J^P = 0^+, \hat{\mu}_{0^+}, \hat{\theta}_{0^+})}{\mathcal{L}(J_{Alt}^P, \hat{\mu}_{J_{Alt}^P}, \hat{\theta}_{J_{Alt}^P})} \right), \quad (4)$$

420 where $\mathcal{L}(J^P, \hat{\mu}_{J^P}, \hat{\theta}_{J^P})$ is the profiled maximum likelihood, and $\hat{\mu}_{J^P}$ and $\hat{\theta}_{J^P}$ represent the values of the
 421 signal strength and nuisance parameters fit to the data under each J^P hypothesis.

422 In order to create distributions of the test statistic for each hypothesis, the test statistic is calculated
 423 thousands of times using MC toy experiments. In each toy experiment the number of expected signal
 424 and background events are smeared by a Poisson random number to create a distribution of q statistics.
 425 This is done by multiplying the expected number of signal events and the expected number of events
 426 from each background by a different Poisson random number. By smearing the number of expected
 427 events in each bin by this process, the Poisson statistic $P(N_{n,j}|N_{n,j}^{Exp.})$ is changed, resulting in a different
 428 likelihood and subsequently a different test statistic. Test statistics are calculated thousands of times
 429 using this method to create PDFs that will then be compared to the test statistic calculated using data.
 430 When comparing the value of the test statistic from real data to the distributions made from the MC toy
 431 experiments, the p_0 value can be calculated by integrating the tail of the distributions that do not include
 432 the data test statistic in a simple hypothesis test fashion. The exclusion level of a specific hypothesis
 433 while assuming another J^P hypothesis can be calculated using the p_0 value.

434 5.4 Systematic Uncertainties

435 Most of the systematic uncertainties come from the event selection used to find Higgs candidates. Addi-
 436 tionally, theoretical uncertainties, background normalization uncertainties, lepton reconstruction uncer-
 437 tainties, and luminosity uncertainties are considered. These uncertainties consequently affect the shapes
 438 and normalization of the PDFs. These affects are taken into account in various ways depending on how
 439 the uncertainty affects the measurement.

440 5.4.1 PDF Shape Uncertainty Treatment

441 The systematics described below will change the total number of events, in addition to the shape of the
 442 PDF. To study the effects of a systematic, the systematic is shifted both up and down by one standard de-
 443 viation. The first sample (σ_+) is produced by shifting the systematic upwards by one standard deviation,
 444 while the second sample (σ_-) is the results of the event selection run with the systematic shifted down
 445 by one standard deviation. This is often made possible by the analysis packages used which often have
 446 a built in option to add or subtract one standard deviation to the systematic in question. The results from
 447 the event selection using these samples are then used to produce PDFs from the BDTs that were trained
 448 using the nominal sample. In the hypothesis test, each PDF from the nominal, σ_+ , and σ_- sample are
 449 fit to find the mean. The means from the σ_+ and σ_- PDFs are used to determine the standard deviation
 450 of the mean value in the PDF. These numbers are used to create a normalized distribution with standard
 451 deviations determined by the mean of the σ_+ and σ_- PDF means. During each MC pseudo-experiment
 452 a random number for each systematic is chosen from the respective distribution and then multiplied by
 453 the expected number of events, Equation 3, used in the Poisson probability to calculate the likelihood in
 454 Equation 2. The expected number of events is smeared in this way for each bin independently.

455 MC Event Modeling

456 Lepton reconstruction and identification introduces the largest systematic uncertainties. The systematic
 457 errors introduced by the electron energy corrections and momentum smearing, as well as the muon mo-
 458 mentum smearing, are considered in this analysis by producing separate samples with these corrections
 459 individually shifted up and down by 1 standard deviation. Additionally, the uncertainties introduced from
 460 the muon and electron scale factors are considered in the same manner.

461 **Mis-Pairing Effects**

462 Same flavor channels are affected by incorrectly pairing same flavor opposite sign leptons when forming
463 Z_1 and Z_2 . For the 0^+ MC sample the mis-pairing fraction is around 4.2% in the mass region of 115 and
464 130 GeV. This effect has been shown to be negligible on BDT shapes when the fraction of mis-paired
465 events is changed by 10%. For this reason the mis-pairing effects on the BDT shapes has been neglected.

466 **Mass Resolution**

467 The M_{4l} resolution has been taken into consideration in the same way as the lepton reconstruction and
468 identification uncertainties. This was done by shifting the Higgs mass both up and down by 1 GeV to
469 create a σ_+ and σ_- PDF.

470 **BDT Overtraining**

471 Limited statistics in the BDT training can result in specific types of events having more weight in the
472 training than others and result in a BDT that is not trained to a sample that adequately represents data.
473 Overtraining can lead to inefficiencies in the separation of the two samples, but does not represent a
474 source of systematic errors. To assess the magnitude of this affect, the BDT output from the training
475 sample were compared to the BDT output of the test sample. By comparing the separations J^P states
476 with the two independent samples (training and testing samples), the overtraining is seen to be negligible.
477 This comparison can be seen in Figure 11 for 0^+ versus 0^- . These comparisons illustrate there are no
478 significant differences between the testing and training sample, and thus the BDT was adequately trained
479 to correctly reflect two input samples.

480 **Theoretical Uncertainties**

481 As described in Section 3.2, events from the *JHU* generator are calculated with leading order perturbative
482 QCD corrections and must be reweighted based upon their p_T . This is done so the lepton p_T distributions
483 from the *JHU* generator agree with the lepton p_T distributions from the next to leading order SM Higgs
484 event generator: *PowHeg*. The systematics from this reweighting procedure have been considered and
485 treated in the same manner as the other reweighting systematics introduced by MC corrections.

486 **5.5 Results**

487 The results are obtained from running 100,000 pseudo-experiments to obtain a final p_0 value in order to
488 exclude or validate J^P states. The p_0 values for different J^P states compared to 0^+ can be seen in Table 1.
489 The resulting distributions of the test statistic for 0^+ and 0^- formed by the toy MC experiments, as well
490 as the test statistic of data can be seen in Figure 13. Additionally, the expected and observed p_0 values
491 and exclusion limits for 0^+ versus 2^+ with different amounts of $q\bar{q}$ production ($f_{q\bar{q}}$) can be seen in Table
492 2. The combined results from different Higgs decay channels for the expected and observed confidence
493 levels when assuming $J^P = 0^+$, as well as for 2^+ for various $f_{q\bar{q}}$, can be seen in Figure 14. These results
494 indicate that data is in favor of a $J^P = 0^+$ Standard Model Higgs [3].

Alternative J^P	$p_0(J^P = 0^+)$ for assumed J_{Alt}^P		$p_0(J^P = J_{Alt}^P)$ for assumed 0^+		Exclusion CL
	Expected	Observed	Expected	Observed	
0^-	1.5×10^{-3}	0.015	3.7×10^{-3}	0.31	97.8%
1^+	4.6×10^{-3}	0.001	1.6×10^{-3}	0.55	99.8%
1^-	0.9×10^{-3}	0.051	3.8×10^{-3}	0.15	94%
2^+	0.099	0.532	0.092	0.079	83.1%

Table 1: p_0 values and exclusion confidence levels given for various J^P states when compared to 0^+ .

$f_{q\bar{q}}$	$p_0(J^P = 0^+)$ for assumed 2^+		$p_0(J^P = 2^+)$ for assumed 0^+		Exclusion CL
	Expected	Observed	Expected	Observed	
100%	0.102	0.962	0.082	0.001	97.4%
75%	0.117	0.923	0.099	0.003	96.1%
50%	0.129	0.943	0.113	0.002	96.5%
25%	0.125	0.944	0.107	0.002	96.4%
0%	0.099	0.532	0.092	0.079	83.1%

Table 2: Expected and observed p_0 values and exclusion confidence levels for the $J^P=0^+$ and $J^P=2^+$ hypotheses with different fractions of $q\bar{q}$ production.

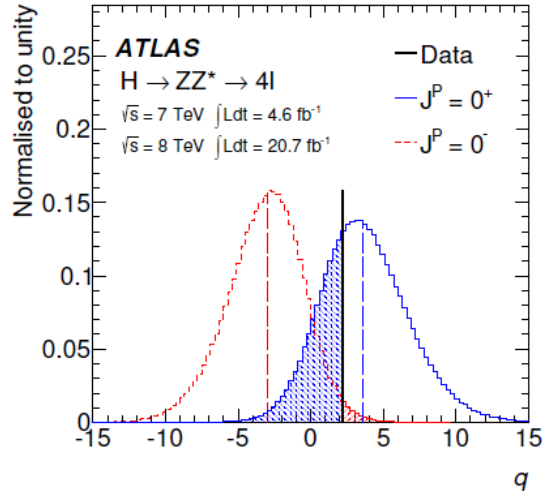


Figure 13: Hypothesis test result for 0^+ versus 0^- , with the respective p_0 values shaded in.

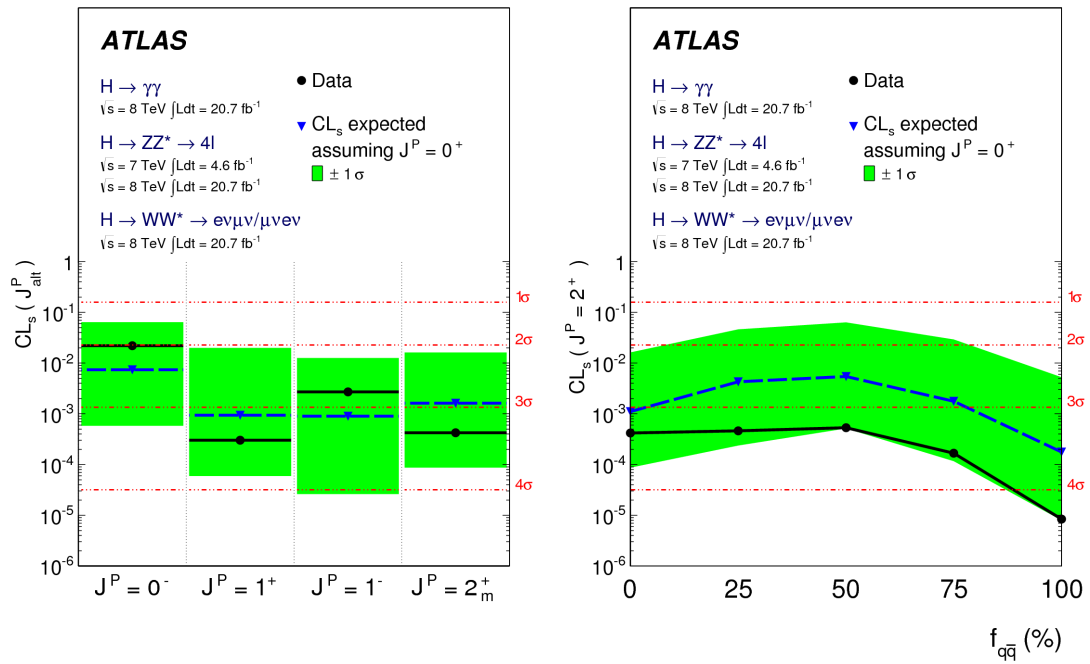


Figure 14: Combined expected (blue dashed lines) and observed (black solid lines) confidence levels, as well as Gaussian standard deviations, from other Higgs decay channels when comparing various J^P states with 0^+ (left). As well as the expected and observed results for comparing 0^+ versus 2^+ as a function of the percentage of events from $q\bar{q}$ processes (right). The green bands represent the 68% expected exclusion range for a signal with assumed $J^P=0^+$.

495 6 Ongoing Work

496 6.1 2 Dimensional PDF

497 To improve the sensitivity of this study through better separation of the Higgs signal and the background,
498 we are currently altering this measurement to include 2 dimensional PDFs made from two BDTs. The
499 second BDT will be trained with the Standard Model Higgs sample and ZZ^* sample. The BDT output
500 from training 0^+ versus ZZ^* is plotted against the the BDT output from the 0^+ versus J_{Alt}^P BDT output.
501 The two BDT discriminants used to form the 2 dimensional PDF are referred to as D_{J^P} , for separating
502 J^P states, and D_{ZZ} , for separating signal and background. The training of the D_{ZZ} variable is described
503 in Section 6.2. Again, a PDF is made for each spin state and in each individual decay channel, as well as
504 for each background. However, there are no *high* or *low* PDFs, since the D_{ZZ} variable is used to separate
505 Higgs events from background. This set of PDFs is also made for each systematic and cannot have empty
506 bins and should be smooth as well. Therefore, the 2D PDFs are smoothed through the kde method. An
507 example of 2D PDF before and after smoothing can be seen in Figure 15. These 2 dimensional PDFs can
508 be seen in Figure 16, where the 0^+ , 0^- , and ZZ^* PDF distributions are overlaid, as well as projected
509 into two 1 dimensional PDFs, to illustrate the separation power of this new PDF.

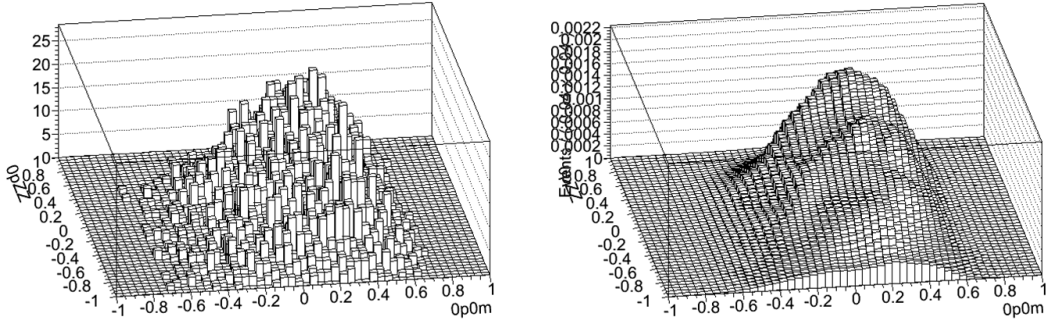


Figure 15: A 2 Dimensional PDF of the 0^+ vs. 0^- BDT output plotted against the 0^+ vs. ZZ^* BDT output both before smoothing (left) and after smoothing (right).

510 6.2 Discriminants for Higgs Signal Versus Background Separation

511 To separate the Higgs signal from the ZZ^* background after the event selection, a BDT is trained using
512 kinematic variables. Only variables that are not sensitive to the Higgs spin are chosen in order to reduce
513 biases towards a specific J^P state since this BDT is trained using a SM Higgs ($J^P = 0^+$) sample and
514 SM ZZ^* sample. The observables chosen are M_{ZZ} , η_{4l} , and p_T^{4l} . The expected distributions of each
515 observable for the SM Higgs and SM ZZ^* for using MC, and the observed distributions in data, can be
516 seen in Figure 17. The BDT output, along with the ROC curve can be seen in Figure 18. This BDT is well
517 trained, as is evident from the agreement between the testing and training samples' BDT output in Figure
518 18. Additionally, this BDT has a strong separation power between the Higgs signal and ZZ^* background,
519 as shown by the large ROC integral of 0.814.

520 6.2.1 Matrix Element Kinematic Discriminant

521 Currently we are investigating the addition of a Matrix Element Discriminating variable (MEKD) to the
522 current observables used to separate the Higgs signal from ZZ^* . MEKD is a discriminating variable for

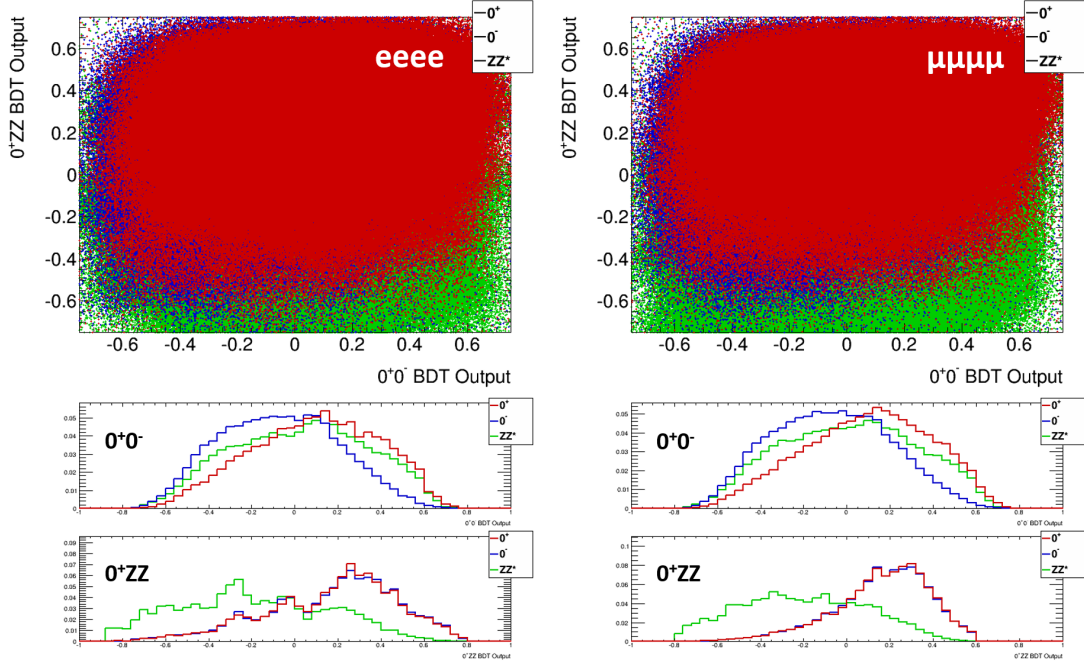


Figure 16: 2 Dimensional PDFs separating 0^+ and 0^- , as well as the Higgs signal and ZZ^* background through the D_{ZZ} and D_{J^P} discriminants built from BDTs in the $4e$ channel (left) and 4μ channel (right).

523 four lepton processes involving two Z s ($X \rightarrow ZZ \rightarrow 4l$) that is based upon lepton kinematics \mathbf{p} . The
 524 MEKD discriminates between two hypothesis (A and B) via a ratio of the probability of observing either
 525 event given the alternative production hypotheses:

$$D(A;B) = \frac{P(\mathbf{p}|A)}{P(\mathbf{p}|B)}, \quad (5)$$

526 where $P(\mathbf{p}|A)$ and $P(\mathbf{p}|B)$ are the probability density functions for observing the event in the case of either
 527 hypothesis. However, the probabilities can be represented by the matrix elements of the corresponding
 528 process (\mathcal{M}_A and \mathcal{M}_B) derived from their Feynman diagrams. The MEKD variable is thus defined as

$$KD(A;B) = \ln \left(\frac{|\mathcal{M}_A(a+b \rightarrow 4l)|^2}{|\mathcal{M}_B(a'+b' \rightarrow 4l)|^2} \right). \quad (6)$$

529 Here a and b (a' and b') stand for different types of partons that can produce a four lepton final state via
 530 process A (B). The log of the ratio is used for technical convenience due to the large dynamic range in
 531 the ratio. The addition of MEKD to the D_{ZZ} discriminator boosts its separation power, which can be seen
 532 in Figure 19, where the ROC integral increases from 0.814 to 0.873. Furthermore, the separation power
 533 of the hypothesis test is increased by 15%.

534 To reduce our biases towards a particular J^P state, the MEKD's correlation to spin sensitive variables
 535 was investigated. Density plots of the MEKD versus the spin sensitive variables can be seen in Figure
 536 20. From these plots we can see that MEKD is slightly correlated to M_{34} and has no correlation to any
 537 other spin sensitive variables.

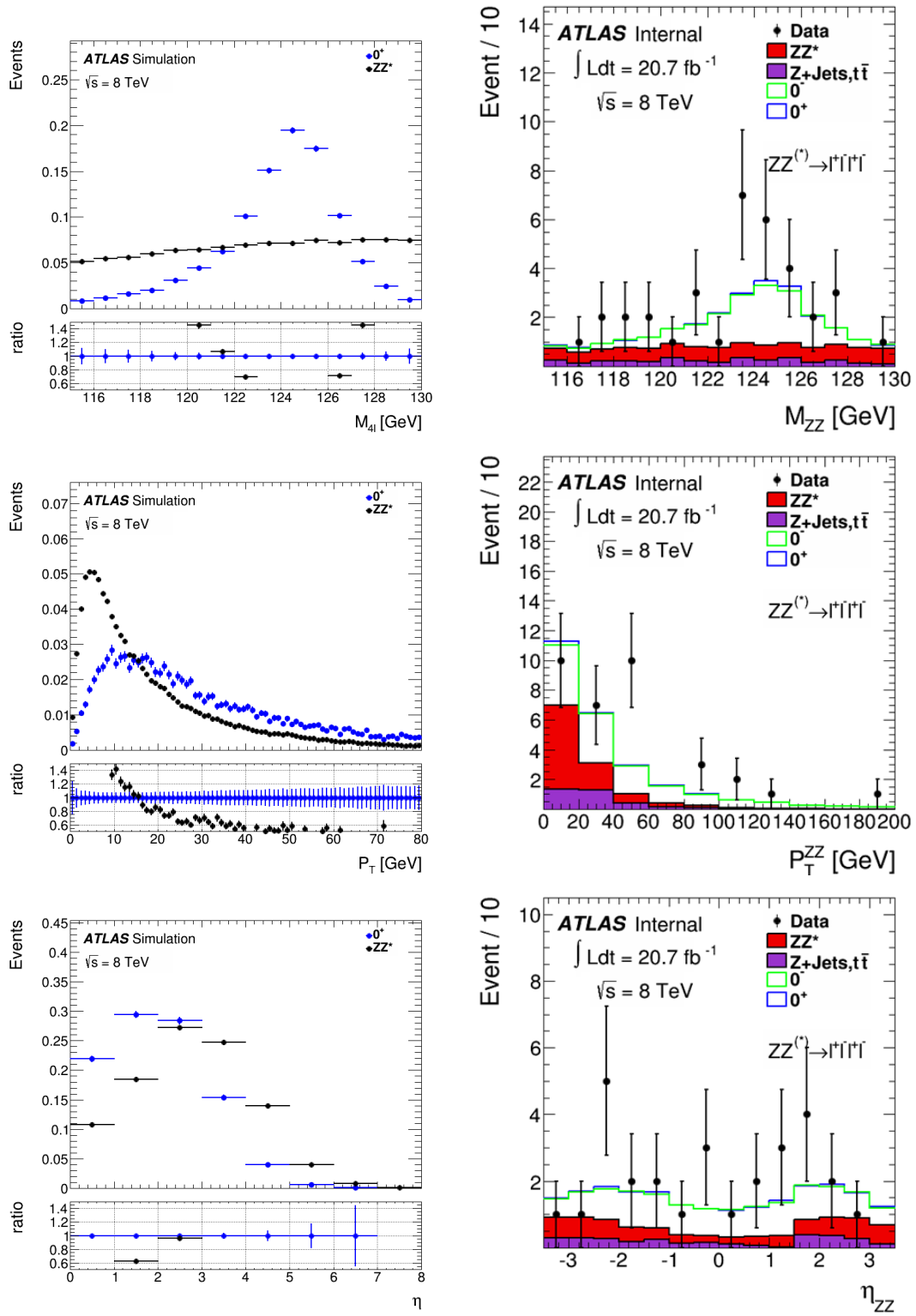


Figure 17: Discriminant variables used in the training of Higgs vs. ZZ^* BDT and the comparison of 0^+ and 0^- with data.

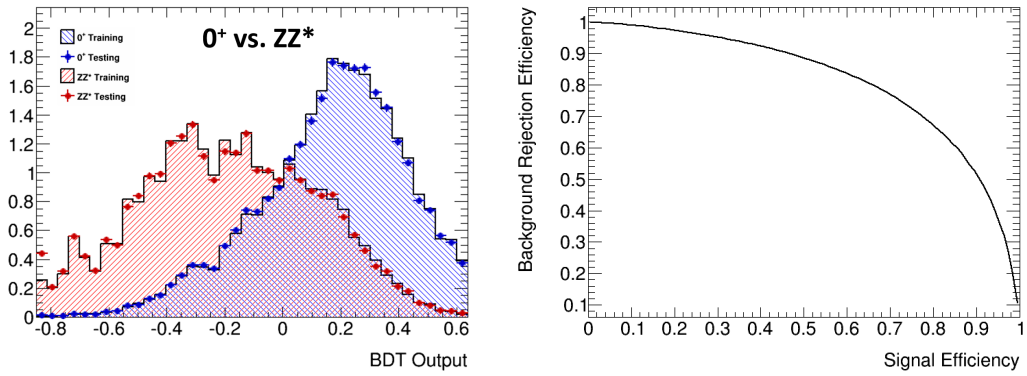


Figure 18: BDT output from both the testing and training sample for 0^+ vs. ZZ^* (left) and the ROC curve from this training (right) with an ROC integral of 0.814

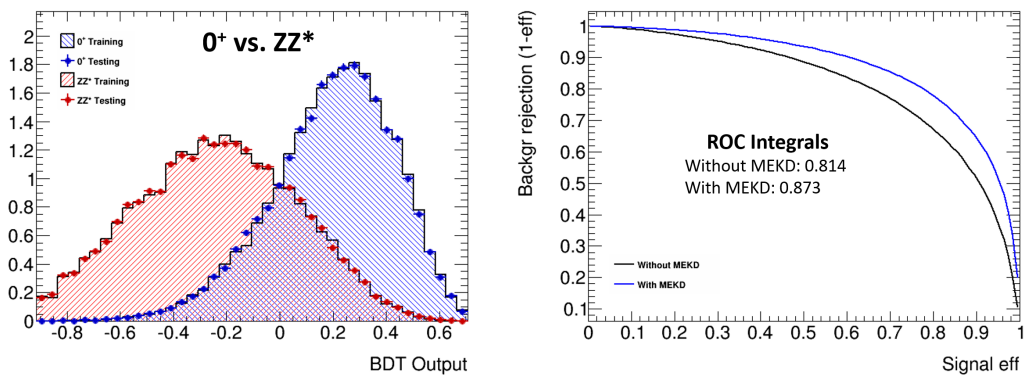


Figure 19: BDT output distribution for D_{ZZ} with MEKD (left), and the ROC curves for training D_{ZZ} with and without MEKD.

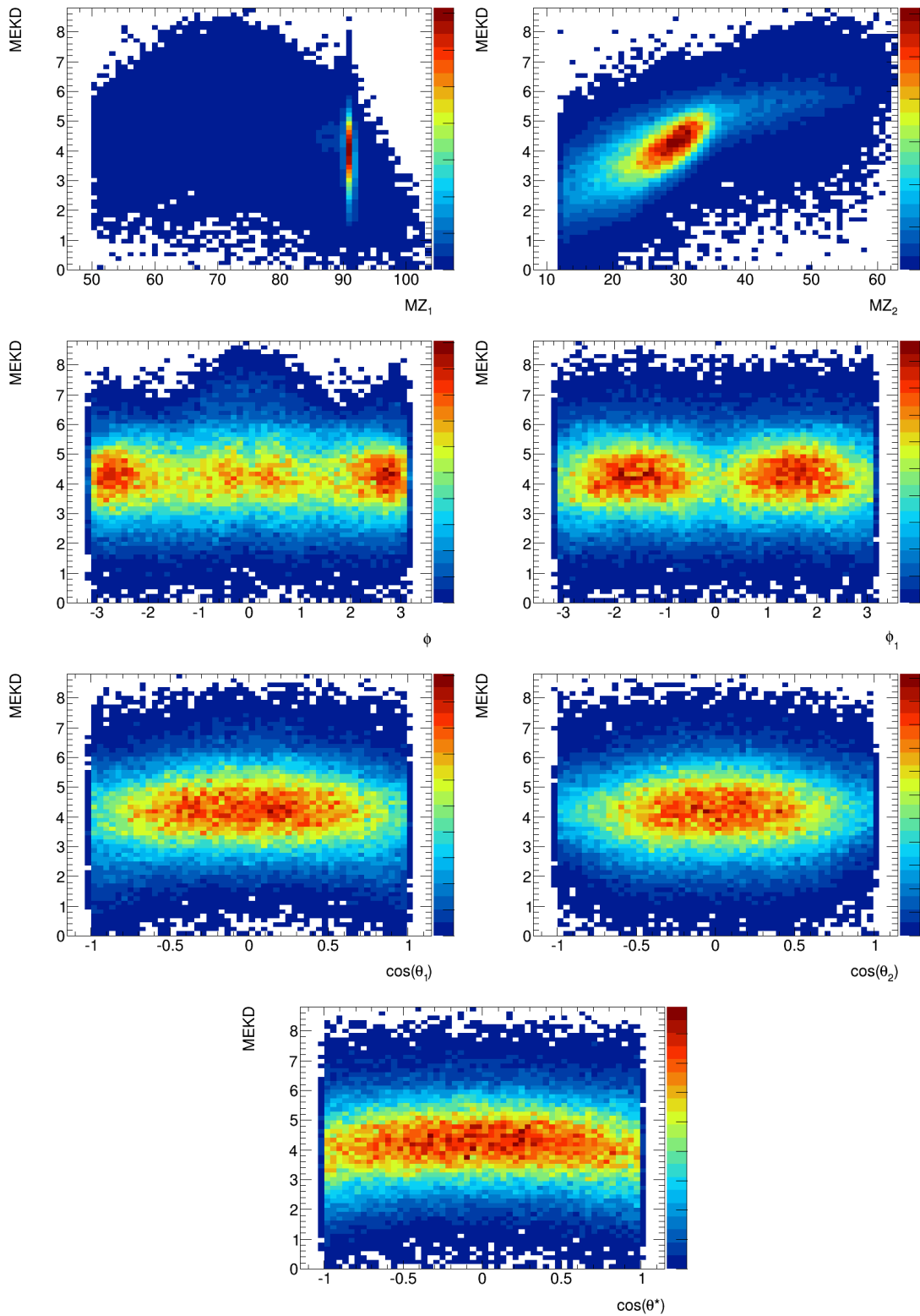


Figure 20: Correlation plots of the MEKD discriminant versus spin sensitive variables.

538 **7 Conclusion**

539 The SM Higgs spin and parity hypothesis has been compared to multiple spin and parity hypotheses
540 through the use of BDTs and toy MCs using ATLAS data collected at the LHC. The results indicate the
541 SM Higgs spin and parity ($J^P = 0^+$) is favored and 0^- , 1^+ , 1^- , and 2^+ have been excluded with 97.8%,
542 99.8%, 94%, and 83.1% confidence, respectively. Current work is being done to improve these exclu-
543 sions, including the addition of 2 dimensional PDFs where the second dimension is used to discriminate
544 against the SM ZZ^* background. Additionally, it has been shown that the addition of the MEKD variable
545 significantly improves the separation power of the D_{ZZ} discriminant. These additions are nearing their
546 final stages and will produce unblinded results along with the rest of ATLAS with a new publication in
547 2014.

References

- 548
- 549 [1] A particle consistent with the higgs boson observed with the atlas detector at the large hadron
550 collider. *Science*, 338(6114):1576–1582, Dec 2012.
- 551 [2] ATLAS Public Results, 2013.
- 552 [3] Evidence for the spin-0 nature of the higgs boson using atlas data. *Physics Letters B*, Jul 2013.
- 553 [4] Measurements of the properties of the Higgs-like boson in the four lepton decay channel with the
554 ATLAS detector using 25fb^{-1} of proton-proton collision data. Report No. ATLAS-CONF-2013-
555 013, 2013.
- 556 [5] Agostinelli S.; Allison J.; Amako K.; Apostolakis J.; et al. Geant4 - a simulation toolkit. *Nuclear*
557 *Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors,*
558 *and Associated Equipment*, 506, 2003.
- 559 [6] Alioli S.; Nason P.; Oleari C.; Re E.; et al. Nlo higgs boson production via gluon fusion matched
560 with shower in powheg. *Journal of High Energy Physics*, 904, Dec 2008.
- 561 [7] Frixione S.; Stoeckli F.; Torrielli; et al. The mc@nlo 4.0 event generator. Oct 2010.
- 562 [8] Gao Y.; Gritsan A.; Guo Z.; Melnikov K.; et al. Spin determination of single-produced resonances
563 at hadron colliders. *Physical Review D*, 81, Apr 2010.
- 564 [9] Golonka P.; Was Z.; et al. A brief introduction to pythia 8.1. *European Physical Journal*, C45:97–
565 107, 2006.
- 566 [10] Mangano M.; Piccinini F.; et al. Alpgen, a generator for hard multiparton processes in hadronic
567 collisions. 2003.
- 568 [11] Roe B.; Yang H.; Zhu J.; Liu Y.; et al. Boosted decision trees as an alternative to artificial neural
569 networks for particle identification. *Nuclear Instruments and Methods A*, Nov 2004.
- 570 [12] Sjostrand T.; Mrenna S.; et al. A brief introduction to pythia 8.1. *Computational Physics Commu-*
571 *nications*, 178:852–867, Jan 2008.
- 572 [13] Brumfiel G. Down the petabyte highway. *Nature*, 469, Dec 2011.