

Supporting Information

**Concerted Rattling in CsAg<sub>5</sub>Te<sub>3</sub> Leading to Ultralow Thermal Conductivity and High Thermoelectric Performance**

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### Calculations details:

DFT calculations were carried out using the VASP<sup>[1]</sup> code with GGA-PBE<sup>[2]</sup> for the electronic exchange-correlation functional. The lattice thermal conductivity was calculated by using the Debye-Callaway formalism.<sup>[3-5]</sup> [ENREF 17](#) This method has recently been shown to produce accurate values of lattice thermal conductivity, compared to experiment, for low-conductivity thermoelectric compounds.<sup>[4,6]</sup> The total lattice thermal conductivity could be written as a sum over one longitudinal  $\kappa_{LA}$  and two transverse  $\kappa_{TA}$  and  $\kappa_{TA'}$  acoustic phonon branches:  $\kappa_{Latt} = \kappa_{LA} + \kappa_{TA} + \kappa_{TA'}$ . The partial conductivities  $\kappa_i$  ( $i$  corresponds to  $TA$ ,  $TA'$  and  $LA$  modes) was given by

$$\kappa_i = \frac{1}{3} C_i T^3 \left\{ \int_0^{\Theta_i/T} \frac{\tau_c^i(x) x^4 e^x}{(e^x - 1)^2} dx + \frac{\left[ \int_0^{\Theta_i/T} \frac{\tau_c^i(x) x^4 e^x}{\tau_N^i (e^x - 1)^2} dx \right]^2}{\int_0^{\Theta_i/T} \frac{\tau_c^i(x) x^4 e^x}{\tau_N^i \tau_U^i (e^x - 1)^2} dx} \right\}$$

In this expression,  $\Theta_i$  was the longitudinal (transverse) Debye temperature,  $1/\tau_N^i$  was the scattering rate for normal phonon processes,  $1/\tau_R^i$  was the sum of all resistive scattering processes, and  $1/\tau_c^i = 1/\tau_N^i + 1/\tau_R^i$ ,  $x = \hbar\omega/k_B T$ , and  $C_i = k_B^4/2\pi^2 \hbar^3 v_i$ , here,  $\hbar$  was the Planck constant,  $k_B$  is the Boltzmann constant,  $\omega$  was the phonon frequency, and  $v_i$  was the longitudinal or transverse acoustic phonon velocity.

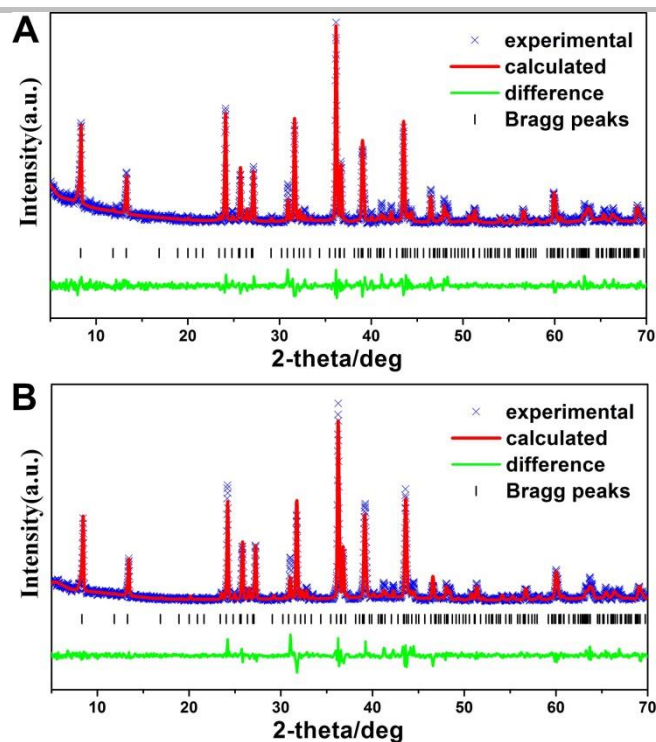
The resistive scattering rate was the sum of scattering rates due to Umklapp phonon-phonon scattering ( $1/\tau_U^i$ ), mass-difference impurity scattering ( $1/\tau_m^i$ ), boundary scattering ( $1/\tau_B^i$ ), and electron-phonon scattering ( $1/\tau_{e-ph}^i$ ). In the pure single crystallize compound considered here, we ignored the effect of impurity scattering, and we assumed that boundary and electron-phonon scattering contributions could be ignored at temperatures above approximately 100 K. Thus the resistive scattering rate was mainly determined by the Umklapp phonon-phonon processes ( $1/\tau_R^i \cong 1/\tau_U^i$ ). The normal phonon scattering and Umklapp could be written as,

$$\begin{aligned} \frac{1}{\tau_N^{LA}(x)} &= \frac{k_B^5 \gamma_{LA}^2 V}{M \hbar^4 v_{LA}^5} x^2 T^5 \\ \frac{1}{\tau_N^{TA/TA'}(x)} &= \frac{k_B^5 \gamma_{TA/TA'}^2 V}{M \hbar^4 v_{TA/TA'}^5} x T^5 \\ \frac{1}{\tau_U^i(x)} &= \frac{k_B^2 \gamma_i^2}{M \hbar v_i^2 \Theta_i} x^2 T^3 e^{-\theta_i/3T} \end{aligned}$$

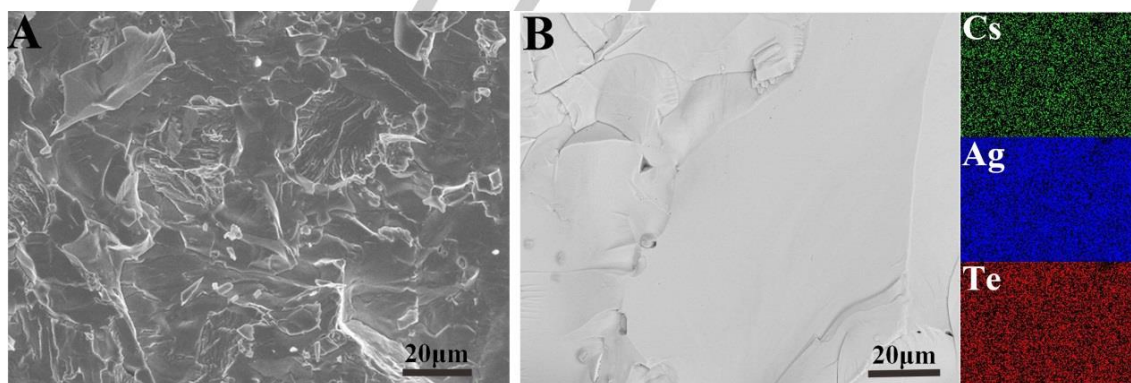
where  $\gamma$ ,  $V$ , and  $M$  were the Grüneisen parameter, the volume per atom, and the average mass of an atom in the crystal, respectively. The Grüneisen parameter could be defined as,  $\gamma_i = -\frac{V \partial \omega_i}{\omega_i \partial V}$ , characterizing the relationship between phonon frequency and volume change.

**Low temperature thermal conductivity measurements:**

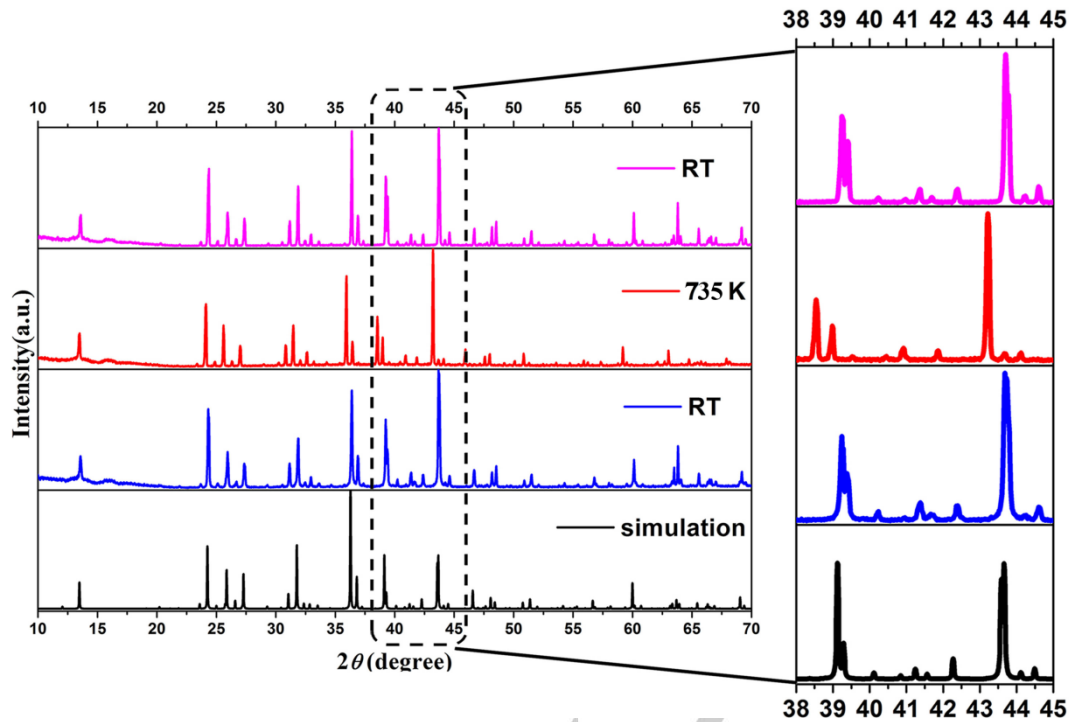
Low temperature thermal conductivity measurements were carried out over the temperature range of 5–300 K using a longitudinal steady-state technique in a homemade cryostat. One end of a uniform bar-shaped sample was thermally anchored to the cold tip of a cryostat, which served as a heat sink. The other end was provided with a miniature strain gauge which served as the heat source. The power supplied to the heater is the product of the constant current passed through the resistive element of the strain gauge and the voltage developed across it. The thermal gradient set up along the length of the sample by the passage of heat from the heater was measured by a pair of fine calibrated copper-constantan thermocouples that were attached to the body of the sample with indium at two points along its length. Thermocouple leads were thermally anchored to the cold tip of the cryostat, the temperature of which was monitored by a calibrated Cernox thermometer establishing the absolute temperature. The Cu legs of the thermocouples also served to measure the potential difference. The sample is surrounded by two radiation shield to minimize radiation losses. The actual radiation loss measured at a room temperature is obtained by detaching the sample from the cold tip, letting the sample “hang” on its connecting leads and determining the heater power resulting in the identical average temperature of the sample as that during the normal thermal conductivity measurement. Thus specified radiation loss at 300 K was scaled to lower temperatures using the Stefan-Boltzmann law. <sup>[10,11]</sup>



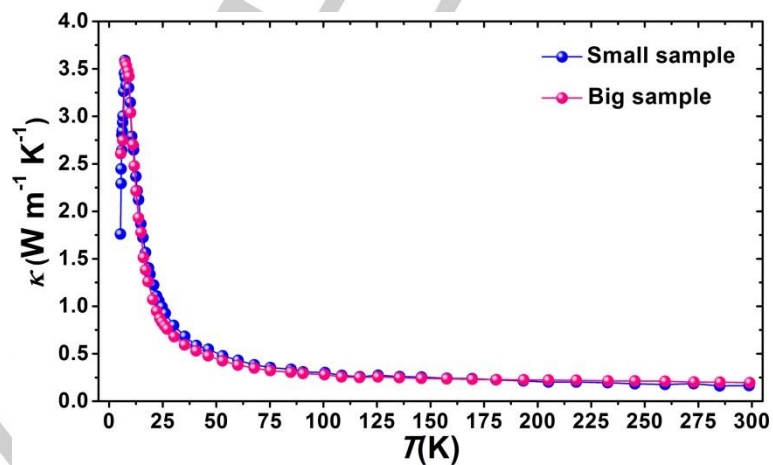
**Figure S1.** Experimental (black cross), calculated (red solid line), positions of the Bragg peaks (vertical bars) and difference (green) results of powder XRD refined by General Structure Analysis System (GSAS) for (A) as-synthesized and (B) SPSed polycrystalline  $\text{CsAg}_5\text{Te}_3$ .



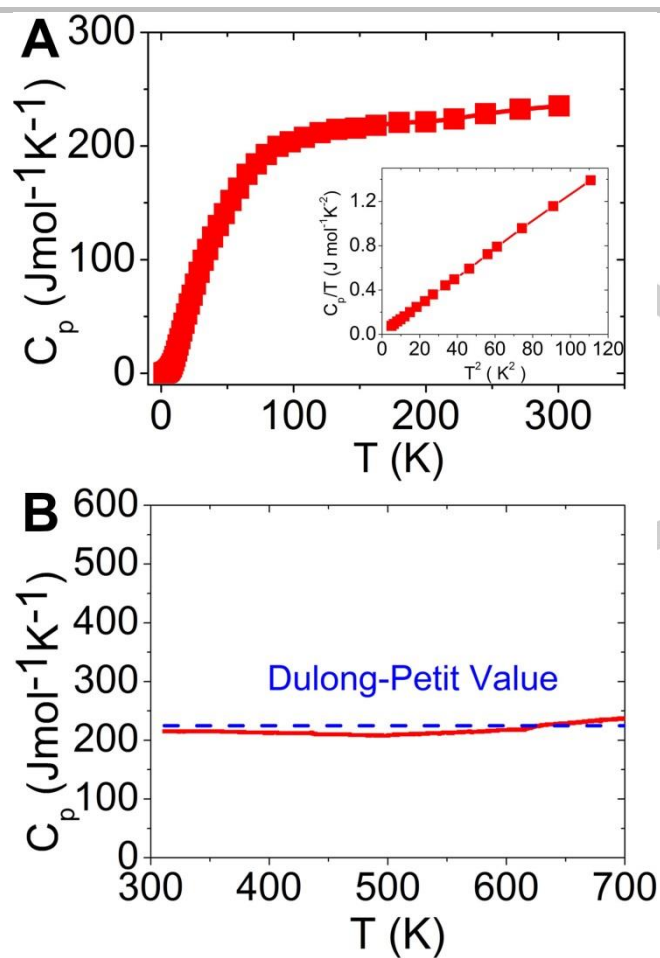
**Figure S2.** (A) The SEM image, and (B) the BSE image and the X-ray elemental mapping of Cs, Ag and Te elements of the freshly fractured surface obtained from the SPSed pellet of  $\text{CsAg}_5\text{Te}_3$ .



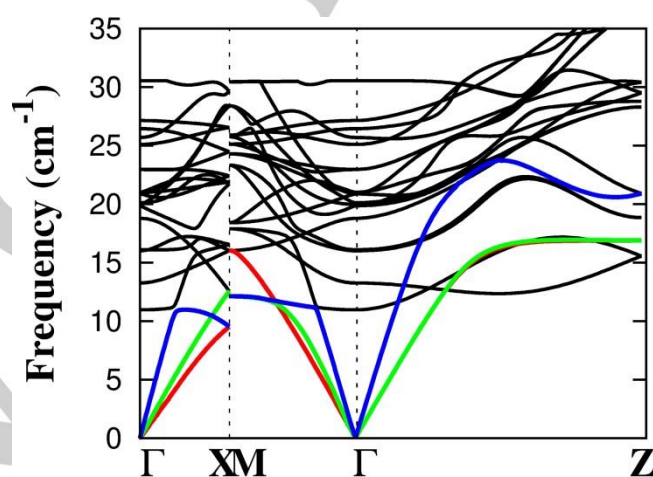
**Figure S3.** Temperature-dependent powder XRD patterns of the as-synthesized  $\text{CsAg}_5\text{Te}_3$  collected between 300 and 735 K indicating the phase transition at  $\sim 730$  K. The magnified part shows the variation of the major diffraction peaks indicating the phase transition.



**Figure S4.** Low temperature thermal conductivities of  $\text{CsAg}_5\text{Te}_3$  from 5 to 300 K.

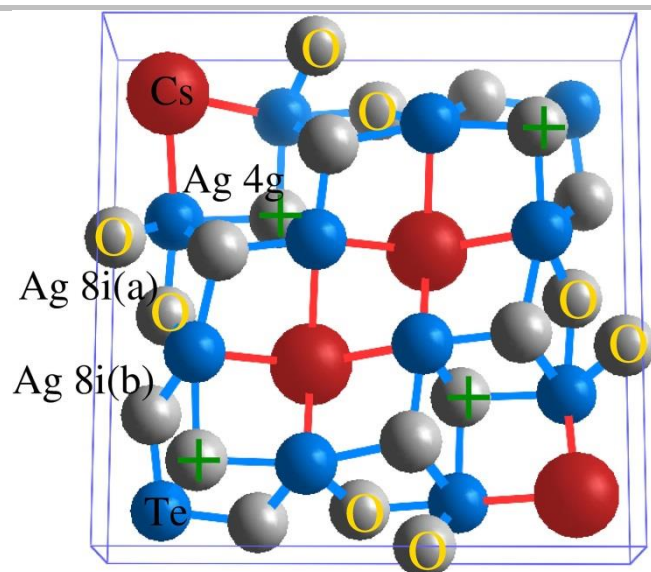


**Figure S5.** (A) The curve of  $C_p$  – Temperature (low temperature). Inset: The curve of  $C_p/T - T^2$  at low temperature. (B) The curve of  $C_p$ -Temperature (RT to 700K).

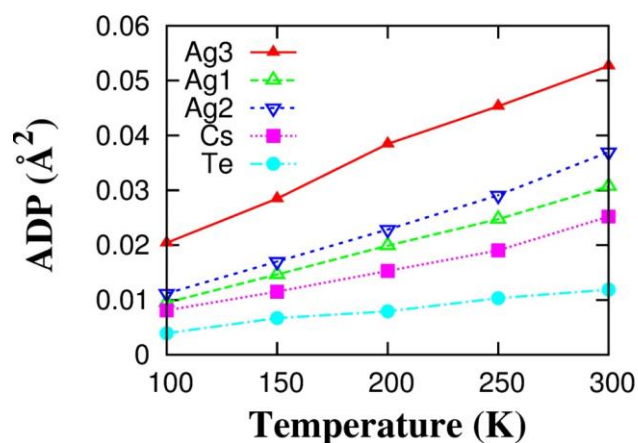


**Figure S6.** Phonon dispersion of  $\text{CsAg}_5\text{Te}_3$  at the isotropically expanded volume  $1.015V_0$ .

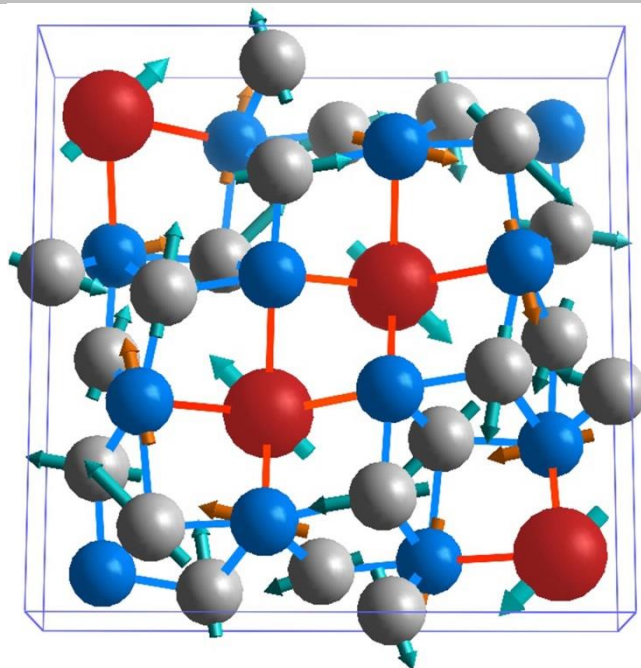




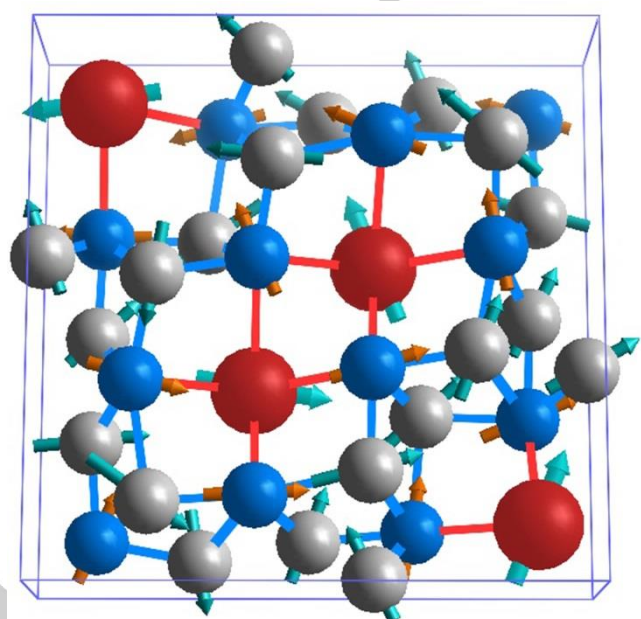
**Figure S7.** Atomic structure of  $\text{CsAg}_5\text{Te}_3$  with Wyckoff sites. Ag3 atoms at the 4g site are silver balls labeled with green cross, Ag2 atoms at the 8i(a) site are silver balls marked with yellow circles, Ag1 atoms at the 8i(b) site are bare silver balls, big red spheres are Cs atoms and Te atoms are blue balls.



**Figure S8.** Temperature dependence of the ADP values from 100 to 300K.

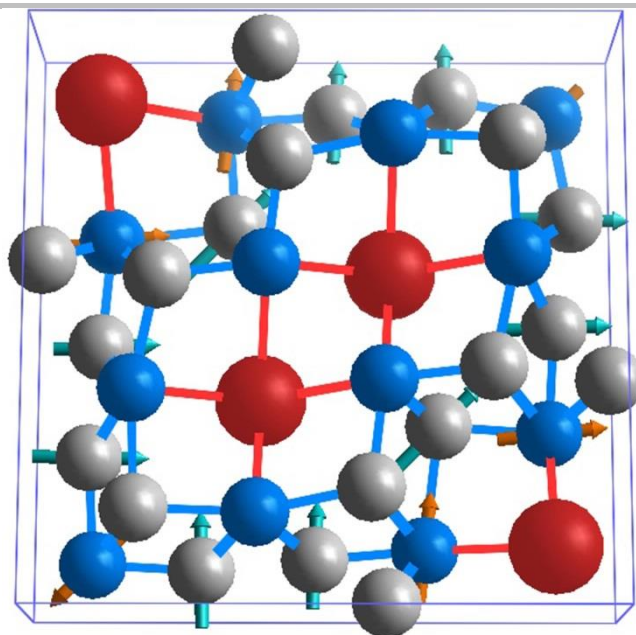


**Figure S9.** A snapshot of concerted rattling vibrational mode at  $\Gamma$   $14.6\text{ cm}^{-1}$ . The details of vibration mode can be seen from corresponding movie.

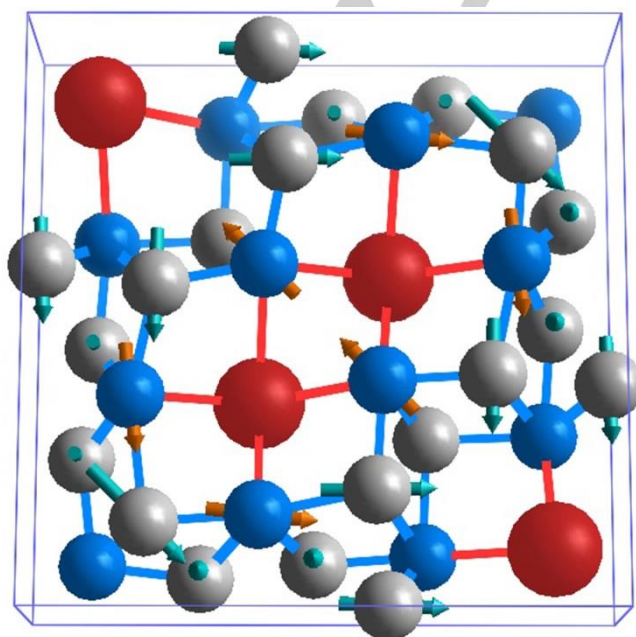


**Figure S10.** A snapshot of concerted rattling mode at  $0.5(\Gamma+X)$   $13.2\text{ cm}^{-1}$ . The details of vibration mode can be seen from corresponding movie.

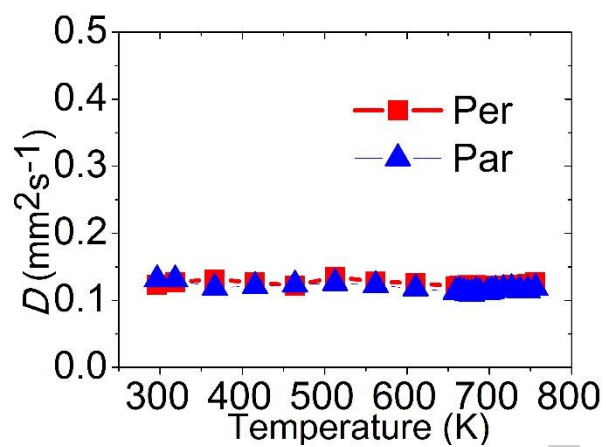




**Figure S11.** A snapshot of concerted rattling mode at  $Z$   $20.2\text{ cm}^{-1}$ . The details of vibration mode can be seen from corresponding movie.



**Figure S12.** A snapshot of concerted rattling mode at  $Z$   $20.2\text{ cm}^{-1}$ . The details of vibration mode can be seen from corresponding movie.



**Figure S13.** Thermal diffusivities of the SPSed polycrystalline  $\text{CsAg}_5\text{Te}_3$  (Per: the perpendicular direction of SPS pressure, Par: the parallel direction of SPS pressure).

**Table S1.** Crystallographic Data and Refinement Details for CsAg<sub>5</sub>Te<sub>3</sub> at room temperature (RT) and 100 K

Empirical formula	CsAg <sub>5</sub> Te <sub>3</sub> (RT)	CsAg <sub>5</sub> Te <sub>3</sub> (100 K)
Formula weight	1055.05	1055.05
Temperature(K)	293(2)	100(2)
Crystal system	Tetragonal	Tetragonal
Space group	<i>P4<sub>2</sub>/mnm</i> (No.136)	<i>P4<sub>2</sub>/mnm</i> (No.136)
Pearson code	<i>tP36</i>	<i>tP36</i>
<i>a</i> (Å)	14.645(2)	14.567(2)
<i>c</i> (Å)	4.5907(9)	4.5501(9)
<i>V</i> (Å <sup>3</sup> )	984.6(3)	965.6(3)
<i>Z</i>	4	4
<i>D<sub>c</sub></i> (g·cm <sup>-3</sup> )	7.117	7.258
$\mu$ (mm <sup>-1</sup> )	22.043	22.478
Reflections	14475/1233	14142/1206
collected/unique	[ <i>R</i> (int) = 0.0893]	[ <i>R</i> (int) = 0.1334]
GOOF on <i>F</i> <sup>2</sup>	1.154	1.277
<i>R</i> <sub>1</sub> , <i>wR</i> <sub>2</sub> ( <i>I</i> > 2σ( <i>I</i> )) <sup>a</sup>	0.0508, 0.1111	0.0450, 0.1092
<i>R</i> <sub>1</sub> , <i>wR</i> <sub>2</sub> (all data)	0.0555, 0.1135	0.0462, 0.1100
Largest diff. peak and hole (e·Å <sup>-3</sup> )	3.172, -2.823	2.606, -3.233

$$^a: R_1 = \frac{\sum ||F_o| - |F_c||}{\sum |F_o|}, wR_2 = \left[ \frac{\sum w(F_o^2 - F_c^2)^2}{\sum w(F_o^2)^2} \right]^{1/2}$$

**Table S2.** Atomic Coordinates and Equivalent Isotropic Displacement Parameters of CsAg<sub>5</sub>Te<sub>3</sub> at room temperature (RT) and 100 K.

RT					
Atom	Wyckoff site	<i>x</i>	<i>y</i>	<i>z</i>	$U_{iso}(\text{Å}^2)$
Te1	8 <i>i</i>	0.61584(4)	0.17220(4)	0.0000	0.02079(17)
Te2	4 <i>f</i>	0.40029(4)	0.40029(4)	0.0000	0.01979(18)
Cs1	4 <i>f</i>	0.38666(5)	0.61334(5)	0.5000	0.0275(2)
Ag1	8 <i>i</i>	0.41798(8)	0.21389(6)	0.0000	0.0402(2)
Ag2	8 <i>i</i>	0.51770(6)	0.10450(6)	0.5000	0.0309(2)
Ag3	4 <i>g</i>	0.32285(8)	0.32285(8)	0.5000	0.0445(4)
100 K					
Atom	Wyckoff site	<i>x</i>	<i>y</i>	<i>z</i>	$U_{iso}(\text{Å}^2)$
Te1	8 <i>i</i>	0.61596(4)	0.17383(4)	0.0000	0.00998(15)
Te2	4 <i>f</i>	0.40085(4)	0.40085(4)	0.0000	0.00975(18)
Cs1	4 <i>f</i>	0.38733(4)	0.61267(4)	0.5000	0.01223(18)
Ag1	8 <i>i</i>	0.41736(6)	0.21319(5)	0.0000	0.01562(18)
Ag2	8 <i>i</i>	0.51670(5)	0.10401(5)	0.5000	0.01293(17)
Ag3	4 <i>g</i>	0.32191(6)	0.32191(6)	0.5000	0.0169(2)

$U_{eq}$  is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S3.** Anisotropic Displacement Parameters of CsAg<sub>5</sub>Te<sub>3</sub> at room temperature (RT) and 100 K.

RT						
Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Te1	0.0227(3)	0.0205(3)	0.0192(3)	0.00125(19)	0.00000	0.00000
Te2	0.0190(2)	0.0190(2)	0.0215(4)	0.0002(3)	0.00000	0.00000
Cs1	0.0280(3)	0.0280(3)	0.0266(4)	-0.0003(3)	0.00000	0.00000
Ag1	0.0496(6)	0.0226(4)	0.0483(6)	0.0023(3)	0.00000	0.00000
Ag2	0.0218(3)	0.0410(5)	0.0301(4)	-0.0035(3)	0.00000	0.00000
Ag3	0.0546(6)	0.0546(6)	0.0243(6)	-0.0120(7)	0.00000	0.00000
100K						
Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Te1	0.0096(2)	0.0091(2)	0.0112(3)	0.00008(18)	0.00000	0.00000
Te2	0.0086(2)	0.0086(2)	0.0120(4)	0.0000(3)	0.00000	0.00000
Cs1	0.0115(2)	0.0115(2)	0.0137(4)	0.0000(2)	0.00000	0.00000
Ag1	0.0174(3)	0.0101(3)	0.0194(4)	0.0002(2)	0.00000	0.00000
Ag2	0.0094(3)	0.0151(3)	0.0143(3)	-0.0011(2)	0.00000	0.00000
Ag3	0.0187(3)	0.0187(3)	0.0133(4)	-0.0037(4)	0.00000	0.00000

**Table S4.** Effective band mass of CsAg<sub>5</sub>Te<sub>3</sub> calculated for the top valence band (VBM) and the bottom conduction band (CBM) at the  $\Gamma$ -point.

	$m^*/m_0$ ( $m_0 = 9.11 \times 10^{-31}$ kg)	
	VBM	CBM
$\Gamma \rightarrow X$ ( $a$ or $b$ direction)	-3.53	0.30
$\Gamma \rightarrow Z$ ( $c$ direction)	-0.50	0.75

**Table S5.** Detailed calculated parameters in CsAg<sub>5</sub>Te<sub>3</sub>.

Parameters	$\Gamma$ -X	M- $\Gamma$	$\Gamma$ -Z
$\theta_{TA}$ (K)	14.8	24.5	29.3
$\theta_{TA'}$ (K)	19.1	22.1	29.4
$\theta_{LA}$ (K)	19.1	30.6	35.9
$v_{TA}$ (m/s)	985.2	1243.6	1244.7
$v_{TA'}$ (m/s)	1271.6	1491.4	1244.7
$v_{LA}$ (m/s)	2487.2	2301.1	2296.8
$\gamma_{TA}$	2.4	2.9	5.6
$\gamma_{TA'}$	2.9	4.2	5.6
$\gamma_{LA}$	5.9	5.8	3.8

**Table S6.** Percent weight and atomic composition of CsAg<sub>5</sub>Te<sub>3</sub> at 10 randomly selected locations for EPMA analysis.

Location-1				Location-2			
Element	Weight%*	Atomic%*	Formula	Element	Weight%	Atomic%	Formula
Ag L	51.82	56.24	5.09	Ag L	51.18	55.61	4.97
Te L	36.16	33.17	3	Te L	36.54	33.56	3
Cs L	12.02	10.59	0.96	Cs L	12.28	10.83	0.97
Matrix	Correction	ZAF		Matrix	Correction	ZAF	
Location-3				Location-4			
Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
Ag L	51.78	56.2	5.08	Ag L	51.77	56.19	5.06
Te L	36.17	33.19	3	Te L	36.33	33.33	3
Cs L	12.05	10.61	0.96	Cs L	11.9	10.48	0.94
Matrix	Correction	ZAF		Matrix	Correction	ZAF	
Location-5				Location-6			
Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
Ag L	51.48	55.9	5.00	Ag L	51.61	56.03	5.06
Te L	36.53	33.53	3	Te L	36.18	33.2	3
Cs L	11.99	10.57	0.95	Cs L	12.22	10.77	0.97
Matrix	Correction	ZAF		Matrix	Correction	ZAF	
Location-7				Location-8			
Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
Ag L	51.15	55.58	5.00	Ag L	51.02	55.46	4.99
Te L	36.28	33.33	3	Te L	36.31	33.36	3
Cs L	12.57	11.09	1.00	Cs L	12.67	11.18	1.01
Matrix	Correction	ZAF		Matrix	Correction	ZAF	
Location-9				Location-10			
Element	Weight%	Atomic%	Formula	Element	Weight%	Atomic%	Formula
Ag L	51.66	56.08	5.06	Ag L	51.19	55.62	5.02
Te L	36.25	33.27	3	Te L	36.22	33.27	3
Cs L	12.09	10.65	0.96	Cs L	12.59	11.1	1.00
Matrix	Correction	ZAF		Matrix	Correction	ZAF	
Average formula: Cs <sub>0.98(2)</sub> Ag <sub>5.03(3)</sub> Te <sub>3</sub>							
*All the numbers are normalized to 100%.							



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