# Rating global magnetosphere model simulations through statistical data-model comparisons

A. J. Ridley<sup>1</sup>, D. L. De Zeeuw<sup>1</sup>, and L. Rastätter<sup>2</sup>

<sup>1</sup>Climate and Space Sciences and Engineering, University of Michigan, Ann Arbor, Michigan, USA.
<sup>2</sup>Community Coordinated Modeling Center, Goddard Space Flight Center, Maryland, USA.

Key Points:

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This is the first statistical comparison between data and magnetosphere models
Global MHD models statistically perform worse during active time periods
Including coupling to a ring current code statistically improves the MHD model

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#### 10 Abstract

The Community Coordinated Modeling Center (CCMC) was created in 2000 to allow researchers 11 to remotely run simulations and explore the results through online tools. Since that time, over 12 10,000 simulations have been conducted at CCMC through their runs-on-request service. Many 13 of those simulations have been event studies using global magnetohydrodynamic (MHD) mod-14 els of the magnetosphere. All of these simulations are available to the general public to ex-15 plore and utilize. Many of these simulations have had virtual satellites flown through the model 16 the simulation results at the satellite location as a function of time. This study used 17 62 or mese magnetospheric simulations, with a total of 2,503 satellite traces to statistically 18 compare the magnetic field simulated by models to the satellite data. Ratings for each satel-19 lite trace were created by comparing the root-mean-squared error of the trace with all of the 20 other traces for the given satellite and magnetic field component. The 1-5 ratings, with 5 be-21 he best quality run, are termed "stars". From these star ratings, a few conclusions were 22 made: (1) Simulations tend to have a lower rating for higher levels of activity; (2) there was 23 a clear bias in the  $B_z$  component of the simulations at geosynchronous orbit, implying that 24 the models were challenged in simulating the inner magnetospheric dynamics correctly; and 25 highest performing model included a coupled ring current model, which was about 0.15 (3)26 ter on average than the same model without the ring current model coupling. 27

### 28 1 Introduction

In the mid-1980s, global magnetospheric models started to be created. These models al-29 ed researchers to explore various aspects of the solar wind-magnetosphere-ionosphere sys-30 , Fedder and Lyon, 1987]. The Lyon-Fedder-Mobarry (LFM) magnetohydrodynamic tei le.g 31 (MnD) code [Fedder et al., 1998; Lyon et al., 2004] was one of the first global magnetosphere 32 models. The LFM solves the MHD equations on a distorted spherical mesh in order to align 33 the grid with the magnetic field as much as possible. This results in less numerical diffusion 34 in the code in the inner magnetosphere, where currents are calculated for the ionospheric solver. 35 A has been coupled with a thermosphere-ionosphere model [Wiltberger et al., 2004; Th 36 et al., 2004] and the Rice Convection Model [Toffoletto et al., 2004]. It is available at 37 munity Coordinated Modeling Center (CCMC) for runs-on-request, as will be described the 38 later. 39

The Open Geospace General Circulation Model (Open GGCM) is also an MHD-based code that has been used in many scientific investigations [*Raeder et al.*, 1996, 1997, 1998, 2001a].

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The Open GGCM uses a stretched Cartesian grid, concentrating high resolution grids anywhere in the magnetosphere. The OpenGGCM has been coupled to a thermosphere-ionosphere model [*Raeder et al.*, 2001b], and is also available at CCMC.

Robert Winglee's code solves the multi-fluid MHD equations [Winglee, 1995, 1998]. This 45 code was used to explore the problem of ion outflow earlier than any other global code, since 46 d oxygen, hydrogen, and helium ions in the magnetosphere before other global mod-47 code is not available at the CCMC at the time of this writing. The Mission Research The 48 Corporation (MRC) MHD code is similar to Winglee's code, but goes a step further - it mod-49 ele the magnetosphere and ionosphere as one system [White et al., 1998]. The MRC code is 50 also not available at the CCMC. The MHD code described by Tanaka [1995] is also a global 51 sphere-ionosphere code that is more widely used outside of the United States and is 52 anable at the CCMC. 53

Block Adaptive Tree Solar-wind Roe-type Upwind Scheme (BATSRUS) MHD code 54 [Powen et al., 1999; Gombosi et al., 2001, 2004] also solves for the global magnetosphere. A 55 atively simple yet effective block-based adaptive mesh refinement (AMR) technique was de-56 veloped and is used in conjunction with a finite-volume scheme [Stout et al., 1997] to solve 57 MHD equations. At the CCMC, a variety of grids are available, all of which are static in 58 to a vary significantly throughout the domain. BATSRUS has been coupled to a va-59 Inner magnetosphere models [e.g., De Zeeuw et al., 2004; Zhang et al., 2007; Glocer 60 et al., 2009; Zaharia et al., 2010]. Multispecies (multiple continuity and single momentum equa-61 tions) and multifluid (mutiple continuity and multiple momentum equations) versions of BAT-62 SRUS were developed and have been used for scientific studies [e.g., Welling and Ridley, 2010b; 63 Willing t al., 2011; Welling and Zaharia, 2012; Welling and Liemohn, 2014; Yu and Ridley, 64 by Different versions of BATSRUS are available for runs-on-request at CCMC, as it 65 described below. 66

The Grand Unified Magnetosphere-Ionosphere Coupling Simulation (GUMICS) MHD code is imilar to BATSRUS in that it uses an adaptive grid architecture and similar solvers [e.g. *panhunen*, 1996; *Palmroth et al.*, 2001, 2005]. It is different from BATSRUS in that it doesn't use blocks, but allows each cell to be split into eight sub-cells. GUMICS has a three dimensional ionosphere in order to resolve the ionospheric densities and conductivities [*Palmroth et al.*, 2004, 2006]. It is also available for runs-on-request at CCMC.

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A wide variety of studies have been conducted to validate global MHD models of the magnetosphere. For example, *Ridley et al.* [2002] explored the ionospheric drift velocities predicted by the BATSRUS magnetospheric model coupled to an ionospheric potential solver. *Raeder et al.* [1998] explored how well an MHD code matched boundaries in the ionosphere, such as the low latitude boundary layer. *Raeder et al.* [1997] investigated how the MHD code compared against measurements by the Geotail satellite.

e studies by Wang et al. [2008], Korth et al. [2011], and Kleiber et al. [2016] compared 79 field-aligned currents produced by global MHD codes projected to the ionosphere to differ-80 ert satellite measurements. Raeder et al. [2001a]; Ridley et al. [2001]; Yu et al. [2010]; Yu and 81 Ridley [2008] and Pulkkinen et al. [2010, 2011] all validated MHD codes by comparing ground-82 pagnetometer data to simulation results by computing the magnetic perturbation that 83 dle be registered on the ground using different current systems in the ionosphere, magne-84 tosphere and the gap region between the two. Global MHD codes have also been compared 85 to geosynchronous satellite measurements of magnetic fields, as shown by Taktakishvili et al. 86 [2013]; Welling and Ridley [2010a] and Honkonen et al. [2013]. 87

While the majority of the validation studies described above highlight how one code com-88 inst a single type of data, some of them have compared different models against the 89 The of data or different models against different data [Pulkkinen et al., 2010, 2011; Honko-90 al., 2013]. Because MHD models have historically needed significant computational re-91 sources to run, the comparisons have been quite limited, focusing on a small number of events. 92 Recently, the Community Coordinated Modeling Center (CCMC) has led validation studies 93 in which different models were run for the same time periods in order to compare how well 94 they performed against each other. For example, Pulkkinen et al. [2011] compared different 95 sults of ground-based magnetic field perturbations to magnetometer measurements to 96 the capabilities of the different models. *Rastätter et al.* [2016] compared different 97 models against DMSP poynting flux in the ionosphere. Rastätter et al. [2013] focused on the 98 ability d many different models in many different configurations to reproduce Dst from four 99 different events. The assessment was also completed with a variety of different metrics. They 100 unc that models that MHD models that coupled to an inner magnetospheric ring current model 101 performed better during storms than other MHD models. Both Pulkkinen et al. [2010] and Rastätter 102 et al. [2011] included geosynchronous data in a similar evaluation. 103

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Statistical comparisons between models and data have been attempted as well. *Gordeev et al.* [2015] compared different models by running nominal conditions and comparing to statistical models. The goal of that study was to determine whether the different models reproduced key parameters within the magnetosphere, such as the size. They concluded that no model was better than any other model. *Zhang et al.* [2011] compared a two-month simulation of the LEM model to a number of ionospheric electrodynamic quantities. This was one of the first long-term simulations of a global MHD model.

Even with these types of studies, a very small number of simulations were conducted to complete the comparisons. In this study, statistical comparisons are made between global MHD simulation results and satellite-based magnetic field measurements. Specifically, the general ability of global models to simulate active versus quiet conditions is explored. In additical, medifferent models are statistically compared to each other to determine whether there are models that are statistically better at modeling the magnetosphere. Finally, statistical model biases are explored.

### 2 Methodology

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The CCMC has a program in which a user can request simulations of the geospace en-119 vironment by specifying a domain to simulate, the model to use and a time period to run. The 120 mutation is then conducted at CCMC and the model results are made available through a web 121 interface to allow the user (and the entire community) to visualize the simulation results. Fur-122 the. **EEMC** has traced virtual satellites through many of the simulation results, allowing di-123 t comparisons between the model results and the satellite data. As of December 2014, when 124 the study obtained data from the Virtual Model Repository (VMR), there were 662 magne-125 pheric simulations at CCMC that had such traces through them. The satellites that were con-126 In this study were GOES-8, GOES-9, GOES-10, GOES-11, GOES-12, Geotail, THEMIS-127 THEMIS-B, THEMIS-C, THEMIS-D, THEMIS-E, and Cluster-1. A total of 2,503 satel-128 lite tracks were used. 129

At the VMR, the CCMC-produced simulation results along the satellite trajectory, along with all of the observational data, were downloaded and compared. Figures 1 and 2 show examples of comparisons between simulations conducted at CCMC and GOES-11 and GOES-12, respectively. Four simulations are shown for the December 14-15, 2006 storm. These simulations were carried out with (a) Open-GGCM [*Raeder*, 2003], (b) BATSRUS [*Powell et al.*,

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1999], (c) LFM [Lyon et al., 2004] and (d) GUMICS [Janhunen, 1996]. There are some clear 139 differences between the simulation results and the data. For example, the Open-GGCM results 140 had large perturbations in the second half of the time period, while the data does not show these 141 perturbations. On the other hand, the Open-GGCM matched the  $B_z$  component in the mid-142 dle of the time period better than the other models. BATSRUS captured the overall structure 143 quite well, but missed a large amount of the variability in the data. For GOES-12, BATSRUS 144 underestimated the magnetospheric response in all three components in the middle of the time 145 LEM also captured the overall structure, and some of the variability, but seemed to have 146 too much variability at times. GUMICS appeared to show some semi-diurnal variations dur-147 in  $\mathbf{E}$ -time period in the  $B_x$  and  $B_y$  components and looked remarkably like the BATSRUS 148 del results in the  $B_z$  component. 149

while four simulations are shown for this storm case, there were actually 15 simulations 150 at CCMC of this storm. Each of these simulations can be compared in exactly the same man-151 ner as shown in Figures 1 and 2. Indeed, all of the 662 magnetospheric simulations that have 152 litertraces through them were compared in this way. For each of the simulations and each 153 Higherent satellites and magnetic field components, the average difference, root-mean-154 squared (RMS) error, and normalized RMS error (i.e., RMS error divided by mean of the data 155 multiplied by 100%) between the simulation result and the observational data were computed 156 and saved. These average differences and RMS errors were then explored to gain a better un-157 ing of how each simulation compared against all of the other simulations that were 158 conducted. 159

Figures 3 and 4 show statistical histograms of the comparisons between the simulation 164 ults a d the GOES-11 and GOES-12 satellite measurements of the magnetic field, respec-165 For both satellites (and all the other geosynchronous satellites including GOES-8, GOES-166 **ECOES**-10), the median error in  $B_x$  and  $B_y$  were close to zero, with a roughly symmet-167 no distribution. For  $B_z$ , the distribution had a clear bias in the positive direction, with the dis-168 tribution roughly symmetric around this positively biased value. For the other satellites, the 169 three magnetic field components were roughly symmetric around zero error (not shown). This 170 au ntified in Table 2. 171

In the middle column of Figures 3 and 4, the root-mean-squared error distributions are shown from the simulations.  $B_x$  and  $B_y$  show distributions that have peaks below 5 nT and taper slowly off from there. The  $B_z$  distributions peak at higher values (close to 10-15 nT),

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ght) for  $B_x$  (top),  $B_y$  (middle) and  $B_z$  (bottom) for the GOES-11 satellite.

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ght) for  $B_x$  (top),  $B_y$  (middle) and  $B_z$  (bottom) for the GOES-12 satellite.

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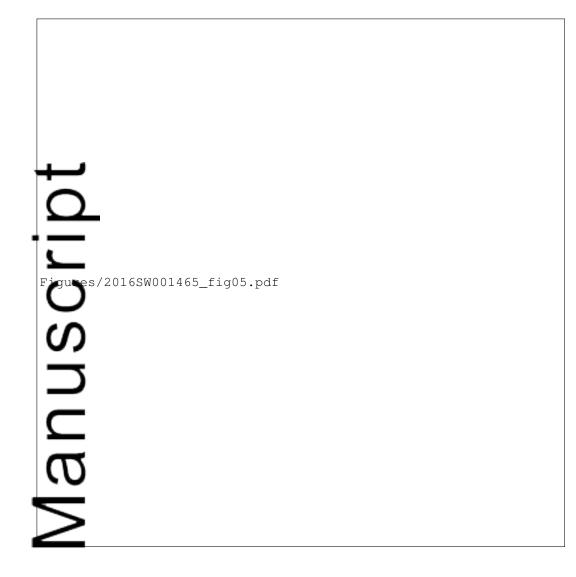
consistent with the median errors. It is asserted that a simulation that had, for example, an er-175 ror in  $B_x$  of less than 1 nT simulated  $B_x$  better than a simulation that had an error in  $B_x$  of 176 30 nT. The idea of "better" has been quantified by breaking the RMS errors into five distinct 177 regions, assigning them ratings of 5 (best), with very low RMS errors, down to 1 (worst), with 178 very high RMS errors. The demarcations between the five different ratings are indicated by 179 the vertical lines in the plots in the center column of Figures 3 and 4. The placement of these 180 demarcations are described completely below. The plots in the right column of Figures 3 and 4 181 distributions of errors in normalized RMS error, where the normalization is done with the are 182 mean of the measured data. 183

From zero RMS (or nRMS) error to the blue line were all of the runs with a rating of 184 for that particular satellite and component of the magnetic field. RMS (or nRMS) errors 185 be wenthe blue to the yellow lines were assigned a rating of four. From yellow to orange 186 indicated a rating of three, etc. Originally, the demarcations were determined by taking the mean 187 and star lard deviation and linearly combining these in a way to give roughly normal distri-188 for the ratings, but this did not work well for some satellites. For example, the GOESbut 189 Me error distributions had extremely long tails. By choosing linear combination coeffi-190 ci nt of the mean and standard deviation that worked well for other satellites, the GOES-12 191 rating distribution was skewed towards low ratings. 192

or this study, the rating distributions, as described by the vertical lines in Figures 3 and 4 193 were determined by first sorting all of the RMS errors for the particular satellite and magnetic 194 field component, and then determining the values that were 7.7%, 30.8%, 69.2%, and 92.3% 195 of the way through the list. These percentages produced distributions that were roughly 1, 3, 196 5, 8 1 i population for the 5, 4, 3, 2, 1 ranking, respectively, in most individual satellite mag-197 field component comparisons. The same ranking scheme was used for the normalized 198 **Ferr**ors. The rankings for both RMS and nRMS are indicated by the blue, yellow, orange 199 and red lines, respectively in Figures 3 and 4. The RMS and nRMS ratings were kept seper-200 ate from each other in order to determine whether conclusions made with one type of assess-201 ment are consistent with another type of assessment. 202

The 1-5 run ratings qualities are termed "stars", since they are roughly equivalent to a user-rating of the simulation. Each of the three magnetic field components for a simulationsatellite combination was given a star rating (from 1-5 as described above). So, for example, if a simulation run had the same 10 nT RMS error in all three of GOES-12  $B_x$ ,  $B_y$ , and  $B_z$ 

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- Figure 5. Star ratings for data-model comparisons between (a) GOES-8, (b) GOES-9, (c) GOES-10, (d) GOES-11, (e) GOES-12 and (f) Geotail. The mean star rating is indicated in each plot. The blue distributions show the RMS star ratings, while the red distributions show the nRMS star ratings.
- magnetic field components, the ratings for the three components would be 3, 3 and 4, respec-207 tively. These three star ratings would then be averaged together to give a star rating for the 208 simulation-satellite combination. In the example above, the average for the GOES-12-model 209 rision would be 3.33. Most of the time each run had multiple satellites traced through 210 the results, such that the star ratings for each of these satellite comparisons could be averaged 211 to provide an overall star rating for the particular simulation. Given that there were 662 sim-212 ulations and 2,503 satellite traces, an average of 3.78 satellite traces existed for each simu-213 lation. 214

Figures 5 and 6 show the distributions of the star ratings for all of the satellite-simulation 218 combinations included in this study, sorted by satellite. The top plots (blue histograms) show 219 the histograms of the RMS star ratings, while the bottom plots (red histograms) show the his-220 tograms of the nRMS star ratings. Most of the histogram shows what one would expect – the 221 most probable value is close to the mean value of around 3, with very few simulations receiv-222 ing very high or very low star ratings. In Figure 5, most of the the GOES satellite results have 223 somewhat skewed distributions, with a second peak a bit above the mean value, around 3.67 224 **COES**-9 does not have very many data points, so it is hard to determine whether this 225 Is significant at all. The GOES-10, GOES-11, and GOES-12 satellites have hundreds of com-226 parisons, so the skewed distribution is possibly meaningful, when compared to other satellites, 227 th as Geotail. While exploring why this might be the case is beyond the scope of the cur-228 dy, it is noteworthy that these types of possible differences in datasets can be observed rent stu 229 is type of statistical study. 230

Figure 6 shows the distributions of the star ratings for the five THEMIS satellites and one of the Cluster satellites. The other Cluster satellites were not included since the spacing between the Cluster satellites was typically on the same magnitude or closer than the grid spacing it most of the simulation results. This means that the RMS errors between each of the Cluster satellites and the simulation results would all be very similar to each other. There are significantly less data points for the THEMIS and Cluster satellites, since they have not been in figure as long as some of the GOES or Geotail satellites. The distributions for most of the satellites look roughly normal, with peaks close to the median value, which are all close to 3 me. There are not enough Cluster data points to determine whether the distribution is skewed.

243 3 Results

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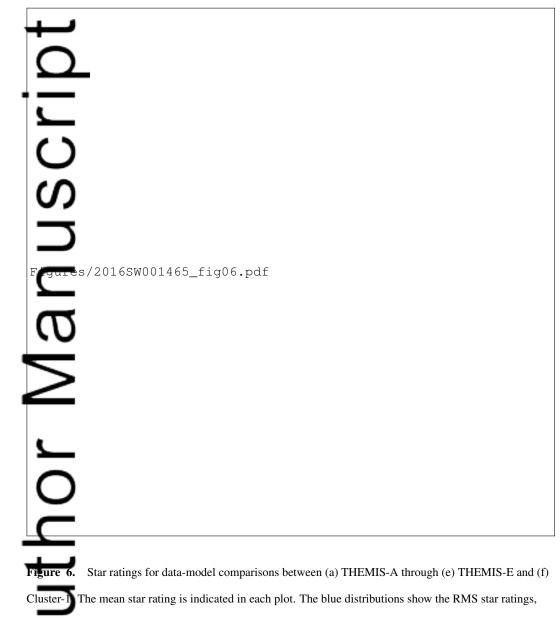
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While there are many different types of analyses that can be conducted on the simulations due are presented in this study, three are focused on here: (1) the relationship between the star rating and the activity level, as indicated by the distrubance storm time ( $D_{st}$ ) index, that has occuring during the time, (2) the mean star rating for individual models, and (3) the biases that can exist within the models that point to possibly missing physics.

Figure 7 shows the statistical relationship between the minimum  $D_{st}$  that occurred during the simulation time period and the star rating of that simulation for each of the simulations included in this study (top right). The vast majority of the simulations were conducted

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while the red distributions show the nRMS star ratings.

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n Dst and star rating for GOES-12 (c) and Geotail (d).

for non-storm time periods, while only a small number covered super-storm periods. Exam-257 ining the lower figure, it can be seen that there were multiple simulations with the exact same 258 Dst value but different star values. These were simulations of the same event but using either 259 different models, different grids or different drivers. As was described by Ridley et al. [2010], 260 running the same model with different numerical schemes or grids can provide different re-261 sults and therefore different qualities of simulation. Running the same event with different mod-262 an accentuate this, since the models may solve the MHD equations in completely differels 263 This is observed in Figures 3 and 4. 264

The general trend in the top right plot of Figure 7 is that runs with higher levels of activity (i.e., more negative Dst) tend to have lower star ratings. At lower levels of activity (i.e., Ds new zero), the star ratings tend to be higher, although there is a huge amount of variability in fun quality at lower activity levels. This trend appears to mean that global MHD codes consistently have a harder time simulating large storms, but can often simulate quiet time periods very well. There are a couple of reasons why this might be the case.

First, the perturbations in the magnetic field away from a simple dipole are significantly 271 larger during a storm than during a quiet time period, so if there is any error, it has the pos-272 of being much larger than during a quiet time. For example, if the code put the pres-273 merease from the ring current build up in a slightly incorrect location during a storm, re-274 sulting in the current distribution being shifted by a few degrees, then the difference in the mag-275 netic perturbations may be quite large. On the other hand, during a quiet time, when there are 276 no large current systems, a slight shift of the pressure in the magnetosphere will not result in 277 large differences in the magnetic perturbations, since the field would still be dominated by the 278 diolar lackground. The normalized RMS ratings back this idea up: in the largest storm events, 279 didots (nRMS stars) are consistently above the blue dots (RMS stars). While the genthe 280 **m**l of having worse results during major storms still exists, the trend appears to be weaker 281 with the normalized RMS. 282

Second, the majority of the simulations that were included in this study were with global magnetospheric MHD models that do not include the physics of the ring current. This means that ese models were not really expected to simulate storm times accurately, since the ring current dynamics dominate the inner magnetosphere during storm events. This will be discussed in more detail below, when individual models are compared.

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The conclusion that the skewing of the distribution towards worse results as the activ-288 ity level increased was due to the inner magnetospheric dynamics can be further explored by 289 comparing two satellites: one that was in the inner magnetosphere (GOES-12, left) and one 290 that was not (Geotail, right), shown in Figure 7(bottom). The GOES-12 data shows a strong 291 dependence on Dst in both the RMS and nRMS results, with simulations of strong storms hav-292 ing an average star rating 1-2 stars below the quiet times. Geotail, on the other hand, has very 293 little dependence on activity level, especially in the normalized RMS, where the values are close 204 independent of activity level. In the RMS star values, there is a small decrease for 295 moderate storms, but it is not as strong as the decrease in GOES-12. For the strongest storms 296 (D) enveen -400 and -500 nT), the statistics are very low for both the Geotail and GOES-297

These results are consistent with *Rastätter et al.* [2013], who compared the simulated Dst from many different MHD models to the measured Dst. They showed that models that included coupling to inner magnetosphere models typically had better prediction efficiencies. The result presented here show that this tendency is also true if comparing to inner magnetospheric magnetic field measurements. It also expands the *Rastätter et al.* [2013] study from four events to seven a hundred.

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Figure 8 shows distributions of star ratings for individual models that are included in CCMC runs an request. While there are more variations of individual models in the database, the models have been grouped into five categories:

BATSRUS: There have been many different versions of BATSRUS at CCMC. Each of 311 ese versions had been coupled to an ionospheric electrodynamics solver, described 312 Ridley et al. [2004] and Ridley and Liemohn [2002]. The specific versions that were 313 included in this list were: v6.07, v7.42, v7.73, v8.00, and v8.01. Some of these ver-314 sions were significant upgrades to the model, but in the standard runs at CCMC, very 315 few of the new features were implemented, so the versions were run in ways that were 316 wry similar to each other. In addition, some of the runs were tagged as being part of 317 the Space Weather Modeling Framework (SWMF), which is described by Tóth et al. 318 [2005]. SWMF, as run at the CCMC, was similar to the older BATSRUS versions, which 319 included only coupling to the ionospheric electrodynamics. 320

2. **BATSRUS with RCM**: In this version of the code, the BATSRUS model was coupled to the Rice Convection Model (RCM), as described by *De Zeeuw et al.* [2004], and the

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top to bottom, include: (B) GUMICS and (D) LFM. More detail is provided in the text.

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ionospheric electrodynamics code using the SWMF. The inner magnetospheric dynamics were described with the RCM, so, in theory, storm-time dynamics could be captured with more accuracy with this coupled model. The specific versions of BATSRUS that were run coupled to RCM at CCMC were: v7.73, v8.01, and v20101108. Updated versions of this model, which include coupling to the Comprehensive Ring Current Model [e.g., *Fok et al.*, 2008], and a newer version of the RCM, are currently available at CCMC, but were not included in this study.

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<sup>3</sup> **CUMICS**: The GUMICS MHD code was similar to BATSRUS in that it used an adapuve grid architecture [e.g., *Janhunen*, 1996] and was coupled to an ionospheric elecnodynamics solver [e.g., *Palmroth et al.*, 2005]. The specific versions of GUMICS that were run at CCMC included: 4-HC-1.11 and 4-HC-20140326.

4 JFM: The LFM MHD code was fully described by *Lyon et al.* [2004]. The specific verbions of LFM included here include: 1, 1.04, 1.05, LTR-2\_1\_1, LTR-2\_1\_4, LTR-2\_1\_5, and LTR-2\_2\_0. These versions were coupled to an ionospheric electrodynamics solver, described by *Merkin and Lyon* [2010] and a coupled ionosphere-thermosphere model, as described by *Wang et al.* [2004].

penGGCM: The OpenGGCM was described in many papers, including (for example) *Raeder et al.* [1996, 1997, 2001b]; *Raeder* [2003]. This code was coupled to an ionospheric electrodynamics solver and a global ionosphere-thermosphere model [*Fuller-Rowell and Rees*, 1983]. The specific versions included at the CCMC and in this study were: 2.1-1, 3.0, 3.1, and 4.0.

Figure 8 shows that BATSRUS was the most used model at the time of this study (286 344 ulations), with BATSRUS coupled to the RCM being the second most used (165 simula-345 and the OpenGGCM having the third most simulations (151). GUMICs had been used 346 the least of any of the models (12 simulations). LFM had a total of 49 simulations. Because 347 there were differences in the numbers of samples in each distribution, and since the distribu-348 tions all looked slightly different, a Kolmogorov-Smirnov test was used to determine the prob-349 ability that the distributions were the same. Table 1 shows the results of those tests. If the prob-350 ilit is low, it indicates that the distributions were most likely different from each other, and 351 that the differences in star ratings for the different models were statistically significant. If the 352 probability was high, it implies that the distributions were similar (or that there was not enough 353 data to determine whether the distributions were different) and that the differences in star rat-354 ing were not statistically significant. In the table, two numbers are reported in each cell: the 355

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Table 1. Kolmogorov-Smirnov statistical results showing the probability that the two distributions are from

the same sampling pool. Numbers on the left of the cell are for RMS, while numbers on the right of the cell

are for nRMS.

	Model	B/RCM		OpenGGCM		LFM		GUMICS	
	BATSRUS	0%	11%	0%	0%	3%	11%	83%	27%
Ì	B/RCM			0%	0%	0%	0%	39%	32%
<u> </u>	OpenGGCM					3%	0%	18%	3%
	LFM							69%	30%
C									

left number is using the RMS star value, while the right number is using the normalized RMS 356 es. Table 1 indicates that: (a) there was not enough data to determine if GUMICS was 357 istically different than any of the other models, meaning that any differences in star rat-358 st ing are mostly meaningless; (b) there was a small chance that LFM was similar to BATSRUS 359 ry small chance that it was similar to OpenGGCM, but almost no chance that it was ve 360 an similar to BATSRUS with RCM, meaning that star rating comparisons between LFM and BAT-361 SRUS ith RCM are valid, but comparisons with other models are questionable; (c) there was 362 sman chance that BATSRUS and BATRUS with RCM were chosen from the same distri-363 bution with the normalized RMS, but not with the RMS; and (d) there was almost no chance 364 that OpenGGCM was similar to BATSRUS or BATSRUS with RCM, implying that compar-365 is no between the star ratings for these models is valid. As more simulations are conducted 366 at CCMC with LFM and GUMICS, it will be easier to determine the actual distributions to 367 lore how the models statistically compare to the other models. 368

All of the models have very similar star ratings, with BATSRUS with RCM having the 372 highest at 3.18 (3.17 nRMS) and OpenGGCM having the lowest at 2.64 (2.59 nRMS), for a 373 mean spread of about 0.54 stars. BATSRUS, GUMICS and LFM have similar average star rat-374 ith BATSRUS having a rating of 3.03 (3.08 nRMS), LFM having a star rating of 2.84 375 (2.94 nRMS) and GUMICS having a rating of 3.0 (3.21 nRMS). These results indicate that 376 including an inner magnetosphere model makes a small, but statistically significant, difference 377 to the model results. While these results might be interesting, they most likely don't indicate 378 whether a given simulation will be better or worse with a given model, since there is so much 379

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spread around the mean rating of each model. In addition, other factors, such as model resolution, may play a large role in determining the star rating. These factors are not accounted for here, but could be explored in further studies.

Table 2 shows the average errors for each of the three components of the magnetic field 383 for each of the satellites. The mean values for the  $B_x$  and  $B_y$  components for the GOES geosyn-384 satellites were near zero, while the  $B_z$  component had a strong positive value. This 385 implies that the magnetic field in the majority of the model runs was too dipolar, as would be 386 expected if the tail current within the simulations was too weak. For each of the other satel-387 lites that were not geosynchronous (Geotail, THEMIS-X, and Cluster-1), the average of  $B_z$ 388 was close to zero, indicating that the bias does not exist in the outer magnetosphere, or at least 389 from geosynchronous orbit. With more analysis, this bias can be investigated much furxploring which models had more bias, the local time dependence of the bias, and whether 391 including a ring current model helped to reduce the bias. This analysis is beyond the scope 392 of the current study, which is simply introducing the statistical analysis that can be done with 393 medel results. 394

### 4 Sumpary

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This study used 662 magnetospheric simulations conducted at NASA's Community Coordinated Modeling Center (CCMC) that were carried out for a variety of users within the community over the last 14 years. Satellite trajectories were traced through each of these simulations to provide the magnetic field along the paths allowing direct comparisons between the satellite data and the simulation results. The Root-Mean-Squared (RMS) and Normalized RMS error for each component of the magnetic field measured by each satellite were sorted and four demonstration lines were created to separate the results into five bins, ranked from 1 (worst RMS within the distribution of events would be 1, 3, 5, 3, 1. The 1-5 ratings are termed "stars", to be consistent with other popular rating systems that exist. The ratings for each of the components for a given satellite were averaged, and then all of the ratings for each of the satellites for a system run were averaged to give an overall star rating for each of the 662 simulations.

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From these star ratings, a few conclusions can be made:

1. When evaluating individual models, the difference between RMS and nRMS error doesn't appear to matter much, since the star ratings for each model, when compared to other

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2.

 $B_y$ Satellite Traces  $B_x$  $B_z$ GOES-8 274  $0 \ nT$ 13 nT -1 nT GOES-9 23  $0 \, nT$ 1 nT 10 nT 370 GOES-10 -1 nT  $0 \ nT$ 18 nT GOES-11 204 -1 nT 0 nT 6 nT GOES-12 -3 nT 315  $2 \ \mathrm{nT}$ 13 nT Geotail 632  $0 \ \mathrm{nT}$  $0 \ nT$ -1 nT THEMIS-A 1 nT 0 nT 138 0 nT THEMIS-B 124  $0 \ \mathrm{nT}$  $0 \ nT$  $0 \ \mathrm{nT}$ THEMIS-C 128 0 nT  $0 \ \mathrm{nT}$ 0 nT THEMIS-D 127 1 nT 0 nT $2 \, \mathrm{nT}$ THEMIS-E 127  $0 \ \mathrm{nT}$ 1 nT  $0 \ \mathrm{nT}$ 41 -1 nT 0 nT Cluster-1 -1 nT

Satellites and median errors associated with each component of the magnetic field.

models, are very similar. When exploring how models work as a function of activity level, the normalized RMS reduces some of the dependence on activity, since both the errors and the background levels are larger during active time periods.

2. Runs with higher activity, as quantified by the D<sub>st</sub> index, tend to have worse star ratings. This is especially true in the data-model comparisons in the inner magnetosphere,
indicating that the ring current dynamics may play a roll in this. This finding is similar to the finding of *Rastätter et al.* [2013] who showed that coupling an MHD code
intervent model provided better results when compared to Dst during a storm. Satelintervent that were not in the inner magnetosphere tended to have higher ratings during acintervent time periods.

3. There is a clear bias in the  $B_z$  component of the geosynchronous magnetic field simplation results, indicating that the models do not have strong enough stretching of the pole. This bias was not observed in non-geosynchronous satellites.

4. The best model, as determined by the star ratings, was BATSRUS coupled to the RCM, which indicates that the presence of an inner magnetosphere model improves the model's ability to accurately reproduce the magnetic field in the magnetosphere. When the in-

Most of the models' distributions of star ratings are statistically different from each other, indicating that the models definitely have strengths and weaknesses that are unique, although GUMICS did not really have enough models runs to statistically differentiate it from other models.

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