Building Blocks for Sampling and Digitization in High-speed Communication Systems

by

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Go Blue!

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LIST OF ABBREVIATIONS

ADC Analog-to-digital converter
CMOS Complementary metal-oxide semiconductor
DAC Digital-to-analog converter
DSP Digital signal processing
dB Decibel
ENOB Effective number of bit
FFT Fast Fourier Transform
FoM Figure of merit
Gbps Giga bit per second
IC Integrated circuit
IF Intermediate frequency
LO Local oscillator
LPF Low-pass filter
LSB Least significant bit
MDAC Multiplying digital-to-analog converter

- MSB Most significant bit
- MUX Multiplexer
- NMOS N-type metal-oxide-semiconductor
- NPFRVCO N-path filter enchanced voltage-controlled ring oscillator
- PCB Printed circuit board
- PLL Phase-locked loop
- **PMOS** P-type metal-oxide-semiconductor
- **PSD** Power spectral density
- **QFN** Quad-flat no-leads
- RF Radio frequency
- **RMS** Root-Mean-Square
- SAH Sample-and-hold
- SAR Successive approximation
- SNDR Signal to noise-plus-distortion ratio
- SNR Signal to noise ratio
- TI Time-interleaved
- T/H Track-and-hold
- T-Line Transmission line
- VCO Voltage-controlled oscillator

ABSTRACT

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The performance of high speed communication systems crucially depends on the quality and precision of sampling and digitization. Low phase noise oscillators are essential in high data rate communication to ensure data accuracy. The ring VCO is gaining importance in ultra-scaled CMOS technologies because of its efficiency in silicon area. High-speed analog-to-digital converters are used as analog frontends of DSP-based receivers. Power efficient ADCs are required to reduce the energy cost per bit for GHz-rate communication systems.

This thesis first presents a novel self-filtering scheme to break the typical tradeoff between noise and power, enabling a ring oscillator to approach the phase noise performance of an LC-VCO. The new scheme only incurs a small extra cost in power consumption and does not require any extra reference or control circuitry.

The prototype N-path filter enhanced VCO (NPFRVCO) achieves a measured phase noise of -110 dBc/Hz at a 1 MHz offset frequency for an oscillation frequency of 1.0 GHz. This is more than a 10 dB improvement over a comparable fabricated prototype structure without N-path filtering.

A new traveling wave pipeline ADC is also proposed that simultaneously achieves the maximum sampling rate and high efficiency. The scheme exploits the delay of on-chip transmission lines to implement a pipeline, and thereby avoids the use of power hungry track-and-hold or MDAC stages. High sampling rates are achieved without using time interleaving, thus no interleaving calibration is needed, making the system design far simpler. This fast energy-efficient ADC architecture will facilitate and improve communication applications. The transmission line is implemented with differential symmetric inductors. This differential structure not only benefits from the mutual inductance, but is also more realistic for integration since it saves silicon area. The prototype is measured at 4.0 GS/s and 6.0 GS/s sampling clock rate. SNDR of 21.35 dB and 18.8 dB is measured, respectively. The prototype consumes 38.2 mW, and occupies 0.65 mm².

CHAPTER I

Introduction

1.1 High-speed Communication Systems

High-speed communication systems enable global interaction between people from different nations and from different places on earth. Advances in communication technology and semiconductor fabrication technology have led to exponential growth in the speed and capacity of communication systems. At the same time, many of todays applications such as remote video meeting and on-line streaming have pushed the needs for bandwidth.

1.1.1 The Growth of High-speed Communication Systems

Based on the CTIA - The Wireless Association's annual wireless industry survey [9], the number of wireless subscriber connections has increased from 207.9 million in 1995 to 377.9 million in 2015, an 82% increase over the past ten years. This rapid growth of the mobile market has made wireless communication a market



Figure 1.1 5G applications [1]

worth \$200 billion annually.

The 5th generation wireless systems (abbreviated 5G) are the proposed next generation communication systems to meet the significantly expanding connectivity needs, as shown in Figure 1.1 [1]. The higher capacity of 5G allows a higher number of mobile broadband connections per area unit. This makes it feasible for 5G to enhance existing application and enable new applications. For example, extreme mobile broadband applications, such as cloud storage and augmented reality for entertainment, are driving the requirements for 5G. People can remotely control diverse automated electronic devices with 5G equipped smart homes or buildings. Due to the higher capacity of 5G, demanding indoor and outdoor



Figure 1.2 High speed links inside a router [2]

conditions such as crowded football stadium will not be a problem. 5G also supports autonomous vehicles and object tracking, starting with Cellular Vehicle to Everything (C-V2X) technologies that satisfy the 3rd generation partnership project (3GPP) specifications. Moreover, wireless communication systems are becoming increasingly important for industrial applications. Thanks to the low latency and very low error rates, 5G technologies are useful for remote control of critical infrastructure and process automation.

The surging demand for internet-enabled data center/devices, and cloud networking has led to high-speed wireline communication systems to support data traffic at several Gbps. Figure 1.2 shows a router that uses an Ethernet cable to connect to a modem [2]. There are 8 to 16 line cards in the router to serve as input/output ports and data link processing. The switch cards execute the routing protocols and perform network management. In this system, the chip-to-chip data speed is 10 Gb/s and the laser driver link speed is 40 Gb/s to supply the four-serial



Figure 1.3 Basic components in a communication system

links in parallel. Despite the fact that router and switching technology is well developed, there is a constant need to transmit faster while consuming less power, especially when there is large amount of data. Thus, the energy cost-per-bit has to decrease to realize good power efficiency in high speed wireline communication systems.

1.1.2 Key Building Blocks in a High-speed Communication System

Selectivity and sensitivity are some of the most important characteristics of a data link. There are three basic components in a communication system: the transmitter (TX), the channel and the receiver (RX), as shown in Figure 1.3. S(t) is the source signal that is transmitted through communication channel and R(t) is received by the receiver.

Communication channels fall into two major categories: wired channels and unwired channels. A wired channel is a conductor or media that confines the energy, for examples, twisted wire, coaxial cable, and optical fiber. Wireless channels (also called unguided channels) use radio waves. These include broadcast radio, terrestrial microwave, and satellite microwave. In these wireless channels the energy spreads out and is not confined.



Figure 1.4 Superheterodyne receiver (a) and transitter (b)

Figure 1.4 shows a superheterodyne wireless receiver (a) and transmitter (b). In a receiver (Figure 1.4(a)), the RF filter selects the desired band. A low noise amplifier (LNA) amplifies the signal to be detected. A mixer and local oscillator (LO) down-convert the incoming radio frequency signal (RF) signal to a relatively lower Intermediate Frequency (IF). An IF bandpass filter further separates out the desired signal from signals that are close in frequency. After bandpass selection, an IF amplifier amplifies the signal for demodulation. The output of the demodulator is processed by the baseband digital circuitry. Converting the signal to IF has several advantages. Firstly, it is feasible to convert signals at various frequencies within a fixed frequency range by tuning the LO frequency. This can alleviate the tunability requirements of subsequent stages such as filters and amplifiers. Secondly, in general a filters bandwidth increases proportionally with its center frequency for the same frequency-response. For a lower center frequency, a narrower bandwidth can be achieved, thus more filter selectivity. Thirdly, there is upper limit on the transition frequency of transistors that are used to perform signal processing. As the speed of communication systems gets higher (several GHz), transistors cannot provide enough gain to directly process a high-speed RF signal. Besides, without converting to IF, expensive high frequency techniques such as stripines and waveguides should be employed. In a superheretodyne transmitter (Figure 1.4(b)) baseband signals are processed and then upconverted by mixer. The mixer is controlled by the tunable oscillator, LO. Before the signal reaches the antenna, it is amplified by a linear power amplifier and bandpass filtered by an RF filter.

The data rates of wireless communication systems have increased dramatically over the past twenty years. The wireless local area network (WLAN) standard 802.11b (in 1999) data rate is 11 Mb/s and the 802.11ac (in 2013) data rate is up to 866 Mb/s [10]. New modulation formats, such as OFDM and pulse position modulation, have been developed to make higher data rates feasible. The carrier frequency has increased from 2.4 GHz in 802.11b to 5 GHz in 802.11a. 802.11ad uses a 60 GHz carrier and supports data rates is up to 6.75 Gb/s.

Figure 1.5 shows the transmitter, channel and receiver in a high-speed link system. The receiver must recover both the data and timing of the incoming signal and often has two detectors: one is the slicer for data, and the other is the phase-detector (PD) for timing recovery [3].

In ultra-scaled CMOS technology, digital signal processing implements most



Figure 1.5 High speed link system [3]

of the processing in modern, high-speed communication systems. This has led to ADCs becoming the bottleneck in the scaling and performance of transceivers. High-speed, high-precision ADCs are needed for high-dynamic-range applications. However, these ADCs are too costly and power hungry. Moreover, it is difficult to generate precise sampling clocks required for high speed ADCs to have optimal performance. Random clock jitter degrades signal-to-noise ratio (SNR) and increases the noise floor. Data dependent clock jitter results frequency spurs and increases distortion in the ADCs output.

Clock signals not only serve as the sampling clock in ADCs, but also are the heartbeat of many high-speed communication systems. Given the significant processing that is dependent on a good clean clock, the phase noise performance of clocks is critical for multi-gigabit data rate transmission.

1.2 Contributions

Designing building blocks for high-speed communication systems is challenging due to the many design tradeoffs that need to be considered, including circuit complexity, power and area efficiencies, and phase noise performance. A simple block design with low complexity is critical. Complex designs result in a longer design cycle and a higher possibility of implementation flaws. Therefore, commonly employed structures in a high-speed block such as a time-interleaving structure in high-speed ADCs are unattractive because of the need for complicated calibration circuits. In addition, power and area efficiency are essential to reduce the cost of a high-speed communication system. To achieve these, power-hungry structures such as sample-and-hold and Multiplying DAC (MDAC) need to be avoided in a high-speed ADC, and area-efficient clock generation blocks such as the ring VCO (RVCO) should be considered. Last but not least, having a low phase noise high-speed clock is important for signal purity. However, low phase noise performance is usually at the cost of high power consumption in RVCO designs. Therefore, it is important to research the design of low phase noise oscillators that also have acceptable power consumption.

This thesis focuses on solving the design challenges of high-speed communication systems mentioned above. First of all, a novel self-filtering scheme is proposed for a ring oscillator to break the typical tradeoff between phase noise performance and power consumption. This newly proposed design enables the phase noise performance of a ring VCO to approach that of an LC-VCO, without any extra reference or control circuitry, and introduces only a small amount of extra power consumption. To study the performance of the proposed scheme, a prototype N-path filter enhanced VCO (NPFRVCO) is implemented in TSMC CMOS 65nm technology. This NPFRVCO achieves a measured phase noise of -110 dBc/Hz at a 1 MHz offset frequency for an oscillation frequency of 1.0 GHz. This is more than a 10 dB improvement over a comparable fabricated prototype structure without N-path filtering.

Secondly, a new traveling wave pipeline ADC is proposed to simultaneously achieve the maximum sampling rate and high power and area efficiencies. To reduce the design complexity, the maximum ADC sampling rates are achieved without using time interleaving. Also calibration circuits are avoided. In addition, the proposed ADC improves the power efficiency by leveraging the delay of on-chip transmission lines to implement a pipeline, which avoids the need for power-hungry track-and-hold or MDAC stages. The transmission lines are implemented with differential symmetric inductors that not only benefit from the mutual inductance, but also are more area efficient for integration. A prototype ADC is taped out in TSMC CMOS 40 nm technology. It is measured at sampling clock rates of 4.0 GS/s and 6.0 GS/s. The measured power consumption is 38.2 mW and the die area is 0.65 mm² area. An SNDR of 21.35 dB and 18.8 dB is measured, for 4.0 GS/s and 6.0 GS/s, respectively. With its high speed and relatively low power consumption, this proposed ADC architecture will facilitate and empower high-speed communication systems.

1.3 Organization

The rest of this dissertation is organized as follows. Chapter II gives some background on the voltage-controlled oscillators and high-speed ADCs. Chapter III describes the design of an N-path filter enhanced low phase noise ring VCO and demonstrates its power efficiency along with its low phase noise performance. Chapter IV describes a traveling-wave ADC, which leverages the delay of on-chip transmission lines and accomplishes both the maximum sampling rate and high power efficiency. Future work is proposed in Chapter V. Finally, Chapter VI concludes the dissertation.

CHAPTER II

Background

2.1 Oscillators in High-speed Communication Systems

In both wireless superheterodyne receivers and direct-conversion receivers, a local oscillator (LO) drives a mixer to down-convert the frequency of the incoming radio-frequency signal. In a wireless transmitter, an LO is often used to tune the frequency of output signal. In data link receivers, phase-locked loops (PLL) generate clock signals to capture and align data received over impaired channels. In other applications, such as a chirp generator for radar system, the oscillator is rapidly swept over a certain frequency range. In high-speed communications systems, low phase noise oscillators are critical because they directly impact the signal-to-noise ratio of high-speed ADCs and bit-error rate in high-speed data transmission applications.

One resource block (12 sub-carriers)



Figure 2.1 Resource block defination in frequency domain-LTE [4]

2.1.1 Voltage-controlled Oscillators

An oscillator produces a periodic oscillating signal that is either sine wave or square wave. There are two categories of oscillators in high speed communication systems: crystal oscillators and tuned oscillators (LC or RC oscillators). A crystal oscillator, whose oscillation frequency is determined by the piezoelectric crystal (commonly a quartz crystal), has good temperature stability and good phase noise performance because the crystal functions as a very high Q-factor mechanical resonator. However, since the frequency of crystal oscillator is mostly fixed, changing the frequency requires physical changes in the crystal. Moreover, modern wireless communication systems require tunable oscillators. For example, Long Term Evolution (LTE) is a widely adopted standard for the fourth-generation high-speed wireless communication. An LTE band consists of many small spaced frequency channels called subcarriers, and these subcarriers are spaced 15 kHz



Figure 2.2 PLL for wireless tranceiver

apart from each other, based on the 3GPP LTE specifications [11]. As shown in Figure 2.1, 12 subcarriers with bandwidth of 15 kHz are grouped together to carry signal in parallel in a resource block. To accommodate to the LTE specification, the precision of tuning of the oscillator must be compatible with the channel spacing of the desired signals.

To obtain a stable, tunable LO in a wireless receiver (shown in Figure 1.4), a PLL with voltage-controlled oscillator (VCO) is commonly employed. In the PLL (shown in Figure 2.2), a phase detector (PD) compares a divided-down fed-back frequency with the reference frequency. The PD outputs current pulses that are filtered and integrated by a loop filter to generate a control voltage. This control voltage drives the VCO, increasing or decreasing the output frequency to drive the PDs average output towards zero. Similarly, in a link receiver, it is important to recover both the data and the timing of the incoming signal. Therefore, a PLL must generate and maintain precise edge timing, as shown for example, in the high speed serial link system in Figure 1.5.

A VCO is the major component in a PLL. The performance of the VCO has significant influence on the frequency stability and tuning range of the PLL, which in turn determines the tunability and accuracy of an LO. Therefore, the performance of a receiver in wireless communication system depends on the characteristics of the VCO. Firstly, the tuning range of the VCO has to be wide enough to cover all the frequency channels. Meanwhile, since the phase noise of a VCO impacts receiver blocker and sensitivity performance, a low phase noise VCO with low harmonics is preferred. In addition, a power-efficient VCO is required for the system, while the VCO must produce enough output power to effectively drive the subsequent stages of circuitry, such as mixers or frequency multipliers.

In a wireline communication system, such as a high-speed data link, the clock and data recovery (CDR) circuitry also require VCOs. The design challenges for the VCO in a CDR circuit are similar to that in a wireless transceiver, however, the required tuning range is often narrower. Also, the required noise performance of the VCO in a CDR is often less stringent compared to wireless systems.

In a wireless receiver, a VCO with poor phase noise performance contaminates the receiving signal, reducing receiver sensitivity and degrading blocking performance. In a wireless transmitter, high VCO phase noise increases out of band spectral emission, possibly causing output spectrum to fail the mask requirement. In a wireline CDR, a VCO without fast and clean transitions will not sample data accurately.

It is important to have the VCO generate a clean clock signal with low random and periodic variations. The VCO plays a critical role not only in generating LO



Figure 2.3 The effect of timing jitter sampling error [5]

signals, but also in the sampling of the analog input signal. For example, the sample-and-hold circuit controlled by the clock signal, shown in Figure 2.3(a), is commonly used when an ADC digitizes the input. The accuracy of the sampling process is affected by clock jitter, as shown in Figure 2.3(b). Clock jitter in the sampling instant translates directly to an error in the sampled value that appears as noise [6].

Data transmission requires Analog-to-Digital (ADC) and Digital-to-analog (DAC) converters, as shown in Figure 1.4. The sampling performance of ADC highly depends on clock purity. For an ideal ADC of infinite resolution, the sampling clock jitter is the only factor limiting the signal-to-noise-ratio (SNR). Assume an input signal given by:

$$v(t) = V_0 sin2\pi ft \tag{2.1}$$

where f is the frequency of analog input signal, V_0 is the input signal amplitude.

The RMS value of dv/dt can be obtained:

$$dv/dt|_{rms} = 2\pi f V_0 / \sqrt{2}$$
 (2.2)

Let Δe = the voltage error and Δt = the timing error, solving for Δe :

$$\Delta e = 2\pi f V_0 \Delta t / \sqrt{2} \tag{2.3}$$

The SNR due to clock jitter is given by [5]:

$$SNR = 20\log\left(\frac{V_0\sqrt{2}}{\Delta e}\right) = 20\log\left(\frac{V_0\sqrt{2}}{2\pi f V_0 t_j/\sqrt{2}}\right) = 20\log\left(\frac{1}{2\pi f t_j}\right)$$
(2.4)

where t_j is the variance of the timing error, f s the frequency of analog input signal. This relationship is plotted in Figure 2.4 [6] and shows that the phase noise of the sampling clock in any sampled data system is important, especially for higher analog input frequencies.

2.1.2 Two Types of Voltage-controlled Oscillators

There are two common types of VCOs, LC-VCO and ring VCOs. Figure 2.5 shows an equivalent circuit of an LC-VCO. An inductor and capacitor are connected in parallel to form a resonator. A transconductance (gm) is connected in positive feedback to synthesize a negative resistance, Ramp. This negative resistance cancels the parasitic resistance (Rp) of the resonant tank and initiates and sustains the oscillation. LC oscillators are widely employed because of their low phase



Figure 2.4 Theoretical SNR and ENOB due to jitter vs. input frequency for different values of the RMS jitter [6]



Figure 2.5 Typical LC oscillator structure



Figure 2.6 Typical ring VCO structure

noise performance, due to on-chip high Q factor inductors. However, LC oscillators occupy large silicon area because of the need for an on-chip inductor. Integrating inductors on chip needs extra fabrication steps. The circuit also suffers from secondary effects such as eddy currents and magnetic coupling caused by integrated inductors.

The basic structure of a ring VCO is shown in Figure 2.6 an odd number of inverter cells form a positive feedback ring structure. The delay through an inverter gate with fanout of one, sets the absolute upper limit on oscillation frequency [12]. A ring VCO can cover a wide frequency tuning range and is easily integrated on chip, because it consists of only small transistors. However, the nonliearity of the inverter cell results in an imperfect sinusoidal ring VCO output, which contains frequency components other than the desired oscillator frequency. Moreover, there is little isolation between the ring VCO and power supply so that power supply noise is a major contributor of phase noise. For the same power consumption, a ring VCO has a worse phase noise performance, compared to its LC-VCO counterparts. Moreover, as supply voltages decrease with technology scaling, the achievable signal swing is lower and the VCO is more sensitive to noise.

2.2 High Speed ADCs in High-speed Communication Systems

2.2.1 High Speed ADC Applications

Higher data bandwidths demanded by metro networks and data centers have led to the deployment of very high data rates (10 Gb/s) wireless and wireline communication systems. A number of standards have been developed to support high bandwidth communication systems, including 10G Ethernet [11], over both fiber and copper media. The data channels range from short optical and electrical links within a data center, to long optical fibers connecting these data centers together. Under severe channel impairments, a flexible receiver with a DSP backend provides robust performance. DSP-based receivers incorporate sophisticated equalization and timing recovery techniques, while allowing for better power and area scaling with technology. A key block for such a receiver is the frontend ADC that digitizes the incoming signal. Running at more than the aggregate data rate, the ADC has to provide sufficient resolution under reasonable power dissipation and area constraints [13] [14].

2.2.2 High Speed ADC Techniques

High-resolution digitizion of high-speed signals requires an ADC with good sampling performance. For a Nyquist frequency ADC, the sampling clock frequency must at least be two times greater than the analog input frequency to generate a true representation of the high-speed analog input. Jitter in the highspeed sampling clock causes uncertainty in actual sampling time. This results in



Figure 2.7 Block diagram of a converntional flash ADC

additional noise in sampled value and reduces the effective number of bits (ENOB), causing the resolution of high-speed digitization to fall below the resolution predicted by quantization error alone. For oversampling ADCs, the clock sampling rate has to be many times faster than the analog input frequency. When samples are accumulated and averaged, the quantization noise power within the band of interest is reduced and thus ENOB is increased. However, oversampling ADCs trade digitization speed for resolution and therefore the analog signal bandwidth applied to the input of the oversampled converters needs to be relatively low. In addition, since high-speed communication systems tend to be power-constrained due to high throughput requirements, so that a well-designed high-speed ADC should have a low energy cost per sample.



Figure 2.8 Block diagram of a converntional SAR ADC

Flash ADCs, SAR ADCs and pipeline ADCs are the most common ways of implementing a Nyquist frequency ADC. An n-bit flash ADC has comparators and one reference ladder, as shown in Figure 2.7. Flash ADCs directly sample the anlog input and compare the input signal with references generated by the linear reference ladder. The flash ADC is the most parallel data converter structure, and completes an entire conversion within one clock cycle.

Instead of using a large number of comparators, a SAR ADC is comprised of a sample-and-hold circuit, a comparator, a DAC and a SAR logic control circuit, as shown in Figure 2.8. The front-end sample-and-hold circuit samples and holds the input signal. In each comparison cycle, the comparator compares the sampled data with the DAC voltage, then the output of the comparator triggers that SAR logic control circuit. According to the SAR logic, the DAC changes the reference voltage. The cycle repeats until all the bits are determined [15].

Unlike flash ADCs and SAR ADCs which pose stringent requirements on all circuit components, pipeline ADCs cascade several stages that are low resolution to



Figure 2.9 Block diagram of a pipeline ADC

achieve a high overall resolution, as shown in Figure 2.9. In each stage, a sub-ADC digitizes the sampled input signal, then passes this digital output to sub-DAC which converts the digital output back to an analog representation. After subtracting this analog representation from the original sampled input signal, the residue is amplified and sent to the next stage.

A delta-sigma ADC (shown in Figure 2.10), the most popular oversampling ADC, consists of the delta-sigma modulator and the digital/decimation filter. The delta-sigma modulator digitizing the inputs signal at very high frequency and produces a 1-bit stream. The delta-sigma modulator implements noise shaping so that the low frequency quantization noise is pushed up to higher frequencies, outside the band of interest. The digital/decimation filter converts the sampled 1-bit stream into a high-resolution, slower digital output [16].

The very high sample rates required for high bandwidth applications can be achieved in two ways. First, a single-channel moderate-resolution ADC with



Figure 2.10 Block diagram of a delta-sigma ADC

GHz operating frequency can be used. The widely used ADC structure for such an ADC is flash ADC. With the comparator limiting the maximum sampling speed, a significant design challenge is to increase the comparator speed and reduce the metastability rate of the comparator. Small sized transistors are usually used to increase the comparator speed. To lower comparator input offset due to random mismatch and to increase the digitization accuracy, comparator offset calibration techniques such as adding binary-scaled variable capacitors to the output nodes of the comparator input pair to shift the input threshold voltage [17], and combining trim DAC and comparator redundancy [18] are employed. For an n-bit flash ADC, comparators are used. Thus, the power and hardware costs of a flash ADC increase exponentially with resolution. Therefore, the flash ADC architecture is only commonly used for digitization at moderate resolution in high-speed communication systems.

For high resolution digitization in high speed applications, oversampling ADCs such as continuous-time (CT) delta-sigma ADCs are popular [19, 20]. The maximum sampling rate of oversampling ADCs is set by excess loop delay that relates to comparator speed and latency, feedback DAC delay and additional delay due to

parasitics.

In order to achieve very high sample-rates, an alternative solution is to use several lower sample-rate ADCs in a time-interleaved (TI) configuration. The TI approach uses several sub-ADCs that quantize the input signal at a fraction of the overall conversion speed and sample the input in a sequential manner. This approach increases the design complexity because compensation for timing misalignment and bandwidth mismatch of the sub-ADCs is often required. A further challenge is to achieve the lowest possible latency. The TI approach allows for a variety of sub-ADC architectures to be used, such as Flash ADCs, Successive approximation (SAR) ADCs and Pipeline ADCs, depending on specific requirements such as power dissipation, latency and silicon cost.

Because of their high conversion rate, flash ADCs are not only used for single channel high speed applications but are also popular in TI structures. As flash ADCs suffer from area and power penalties with increasing resolution; [13] employs a rectifying flash ADC architecture that rectifies the input signal based on the decision of a MSB comparator, thereby allowing the number of comparators to be halved. There are various digital calibration circuits to optimize the ADC path performance, including resistor calibration, offset calibration, gain adjustment and phase alignment. These calibration circuits greatly increase the design complexity.

In addition to flash ADCs, SAR ADCs are among the most popular sub-ADC structures. This SAR ADC architecture typically generates one bit per clock cycle and has the benefit of a relatively small area, which is helpful in a highly interleaved ADC. As in [14], with interleaving ratio of 8, each SAR is made of a compact
comb capacitor array, a comparator and 6-bit registers. The active area is only 0.009 mm2.

Pipeline ADCs are also commonly used as sub-ADCs, especially for high resolution applications [21, 22, 23]. Pipeline ADCs achieve a high throughput thanks to pipelining. When a stage decision is made, and the residue from this stage is passed to the next stage, the current stage can then start processing the next sample. The pipeline process is achieved with a multiplying DAC (MDAC) that combines the functions of sample-and-hold, subtraction, DAC, and gain into a single switched capacitor circuit, shown in Figure 2.9. Requirements such as timing matching and sampling accuracy are only critical when resolving the most significant bits (MSBs). Therefore, pipeline ADCs are more attractive as sub-ADCs than SAR ADCs in terms of design complexity and power efficiency, especially when high resolution and high convertion speed are demanded. The MDAC is the most power-hungry block in pipeline ADC. One approach to reduce the power consumption of pipeline ADC is to avoid using a sample-and-hold. amplifier (SHA) in the MDAC [24].

Figure 2.11 shows a summary plot of Walden FoM of state-of-art high speed (>5 GS/s) ADCs based on ADC survey [25]. It can be concluded that the TI structure is widely employed in high speed ADC designs; SAR ADCs and flash ADCs are popular sub-ADCs in TI ADCs.



Figure 2.11 Walden FoM vs. sampling clock rate of ADCs

2.3 High Speed Sampling and Digitization

This research focuses on high-speed sampling and digitization which are challenging because many design tradeoffs are critical and inevitable. The first challenge is to design an energy-efficient high-speed ADC with the least complexity. In order to reduce the power consumption, power hungry blocks such as sampleand-hold and MDAC are avoided. To reduce design complexity, time-interleaving is not used, so that complicated calibration circuits are not needed. Secondly, for a given power consumption, a challenge is to generate a low phase noise high-speed clock that is compatible with technology scaling. For area efficient oscillators such as ring VCO, there is typical tradeoff between noise and power. The target of this research is to enable a ring VCO to deliver the phase noise performance of an LC-VCO, in this way achieving both high area efficiency and low energy cost.

CHAPTER III

An N-path Filter Enhanced Low Phase Noise Ring VCO

3.1 Ring Voltage-controlled Oscillator

The reliability and the phase noise of an oscillator greatly affect system performance. CMOS ring oscillators consume significantly less silicon area than integrated LC-VCOs and do not require high quality factor inductors. They also have the advantage of a much wider tuning and can easily generate multiple phases [12]. However, LC oscillators offer better phase noise and are less sensitive to supply noise. Recent research has concentrated on reducing the phase noise of ring oscillators by modifying the delay cell to help make the ring oscillator less sensitive to supply noise, such as in [26], where a source-follower-based delay multipath ring oscillator is proposed. Others have achieved good in-band phase noise in a ring oscillator with the reference phase alignment technique, such as demonstrated in [27].



Figure 3.1 Power spectrum of RVCO and desired power spectrum of NPFRVCO

To achieve a better phase noise performance, the technique of band-pass filtering around the oscillation frequency is widely applied. If the quality factor of this filter is high enough, this helps the oscillator remove unwanted signal power away from the carrier, as shown in the power spectral plot in Figure 3.1. There have been several approaches to realize the band-pass filter based on inductors and capacitors, such as in [28], where the LC band-pass filter provides sufficient phase shift to tune to the oscillation frequency of the VCO and serves as the load to each of the ring oscillator stages. These filters, however, tend to be large and suffer from a limited tuning range. Instead, in this work, an N-path filter filters the output of each ring and, injects the filtered output into the other ring. Unlike the scheme in [28], our scheme does not require inductors and inherently tracks the oscillation



Figure 3.2 Low pass filter transformed to bandpass filter



Figure 3.3 N-path band-pass filter network

frequency of the VCO. As N-path filter characteristically has a narrow pass-band, which is determined by its RC constant from low-pass filter on each path; as shown in Figure 3.2, it suppresses the excess noise around the oscillator carrier frequency.

3.2 N-path Filter

A large bank of low-pass filters that are composed of resistors and capacitors, is sampled in frequency with switched-capacitor network, as shown in Figure 3.3 (a) and (b) [29]. The non-overlapping control signals for switches are shown in Figure 3.4 (a). If the second switches at the output are eliminated and the resistor is placed in-between input and output, the circuit in Figure 3.3 (b) will transform to



Figure 3.4 Control signals for switches (a) and simplified N-path filter (b)

the circuit in Figure 3.4 (b). The frequency response of this filter looking in from the input port is a band-pass function.

An N-path filter is comprised of N capacitors, connected in turn to the signal source through a resistor and one of N switches, and controlled by N nonoverlapping clock signals. The center frequency of the band-pass filter is at the N-path clocking frequency. The band-pass filtering mechanism of an n-path filter can be understood by considering an input test tone, exactly at the switching frequency. In that case, because the switches operate at the same frequency as the input frequency, the capacitor in each path samples the same input value every time, so there is no attenuation. On the other hand, signals away from the clock frequency are attenuated. From a spectral point of view, the N-path filter first down-converts the input frequency, and then recovers the signal while suppressing the portion of signal that is offset from the desired frequency; as a result, making the N-path filter a very high Q band-pass filter [30]. Figure 3.5 shows an N-path filter equivalent circuit. Bandwidth of this bandpass filter is decided by R_s and C_L



Figure 3.5 N-path filter equivalent structure

if:

$$|f_{in} - f_{clk}| < \frac{1}{R_s C_L} \tag{3.1}$$

3.3 NPFRVCO Circuit Implementation

The concept of the new low phase noise N-path filter assisted ring VCO is shown in a block diagram in Figure 3.6. Two identical differential three-stage ring oscillators (A and B) are cross-coupled through differential continuous time band-pass N-path filters (FA and FB). The output of each ring oscillator is injected to the other ring oscillator after it is filtered by the N-path filter and buffered. By itself without filtering, the coupling of two oscillators should lead to a 3 dB reduction in phase noise. Because coupling of two oscillators is equivalent to doubling the size of the device and power consumption in one oscillator; the



Figure 3.6 NPRVCO block diagram

signal doubles in amplitude and the noise only doubles in power. This results in a 3 dB improvement in SNR. Thus the phase noise is inversely proportional to the oscillator power consumption. There is a trade-off between phase noise and power consumption. N-path band-pass filters are added to filter the injected coupling signal to the coupled structure to further improve the overall phase noise, with only a small power penalty. Minimizing the phase noise for a given power consumption is achieved.

The N-path filter structure transfers a low-pass RC filter characteristic to a high frequency bandpass filter to achieve a high Q. Because the resulting band-pass filter has just twice the 3 dB bandwidth of the low-pass RC filter, an N-path filters achieve a high Q using only resistors, capacitors and switches.



Figure 3.7 NPFRVCO implementation

Figure 3.7 shows a block diagram of coupled, N-path filtered oscillator system. There are two three-path N-path filters for each oscillator. A differential buffer follows the two N-path filters to generate the injection signals. The three nonoverlapping switch signals are conveniently derived from the outputs of a threestage ring oscillator with the help of a non-overlap clock generator. The overall coupled oscillator is differential–a single ended version is shown for clarity.

The non-overlapping switch control signals are generated from the outputs of each oscillator so that the switching frequency is the same as the oscillator frequency, as shown in Figure 3.8. Similar to the conventional two phase nonoverlapping clock generator, this generator circuit consists of three coupled NAND



Figure 3.8 Non-overlapping clocks generator

gates. $\overline{OUTA'1}$, $\overline{OUTA'2}$ and $\overline{OUTA'3}$ are the delayed outputs of ring A.SWA'1, SWA'2 and SWA'3 are the three generated non-overlapping clock phases. The NAND gates are followed by the inverters with optimal sizing to delay the edge of the clocks.

The tunable differential delay cell, shown in Figure 3.9, has a coarse-tuning NMOS tail current cell and fine-tuning PMOS loads. The differential structure is less sensitive to power supply noise. The inputs are connected to both NMOS transistor and PMOS transistors. A latch follows the differential delay cell to speed up signal transitions and convert the outputs to rail-to-rail signals. White noise in the delay cell and flicker noise in the tuning current cell are main sources of phase noise [12].

Figure 3.10 shows phase noise simulation results for NPFRVCO with different capacitances in the N-path filters and also the phase noise simulation for a cross-coupled oscillator without N-path filters. The phase noise is at 1 MHz offset from



Figure 3.9 Differential delay cell

carrier. As shown in the figure, an NPFRVCO with large capacitor load (the red curve) in the N-path filters has better phase noise performance than the one with a small capacitor load (the blue curve). Because an N-path filter with a larger load capacitance has a larger time constant and therefore a narrower bandwidth, it enables more phase noise reduction than the one with smaller capacitance. In addition, both NPFRVCOs with N-path filters have better phase noise performance than the cross-coupled oscillators without filters (the dotted line).



Figure 3.10 Phase noise comparison of NPFRVCO with different capacitor values and cross-coupled oscillator

3.4 Measurements

The prototype N-path-assisted ring oscillator was fabricated in 65 nm CMOS technology. For comparison, we fabricated both the N-path assisted ring-VCO and an identical, coupled two-ring VCO, but without N-path filtering. The N-path filter assisted ring oscillator consumes 4.7 mW from 1.2 V power supply when operating at 1.0 GHz. At the same frequency the oscillator without N-path filtering consumes 3.8 mW. At 1 GHz, the measured phase noise (measured with an Agilent E5052B signal source analyzer) at a 1 MHz offset is -110 dBc/Hz, while the measured phase noise for the comparable coupled oscillator circuit without N-path filtering is -100 dBc/Hz, as shown in Figure 3.11. Both noise measurements are



Figure 3.11 Phase noise at 1 MHz offset from carrier at 1.0 GHz

the average of 10 successive measurements, and the variance is approximately 1 dB. This improvement in phase noise of more than 10 dB is achieved with only a 23% increase in power consumption. Figure 3.12 shows the measured variation of the phase noise at a 1 MHz offset versus VCO frequency. The phase noise difference between the NPFRVCO and the conventional coupled ring oscillator is even larger at lower VCO frequencies (i.e. >20 dB at 1 MHz offset from the carrier at 240 MHz offset). The active die area of NPFRVCO is 0.015 mm² and the die micrograph is show in Figure 3.13.



Figure 3.12 Phase noise vs. frequency at 1 MHz offset from carrier



Figure 3.13 Die micrograph

The Heterodyne (digital) discriminator method for PN (wide) and AM noise measurements

Basic theory of operation (for a single channel of the E5052B)



Figure 3.14 Digital discriminator method for PN and AM noise measurements [7]

A conventional spectrum analyzer cannot achieve accurate VCO phase-noise measurements and often results in measurement discontinuities due to frequency drift of a free-running VCO [31]. The Agilent E5052B has two phase noise measurement methods, a PLL method (i.e. reference source/PLL technique) and a discriminator method (i.e. analog delay-line technique). The wide capture mode uses the discriminator method, as shown in Figure 3.14 to offer wider phase noise measurement ranges than the PLL method [32]. The wide capture mode is used to measure phase noise of the two VCOs. The measured phase noise improvement is 9.3 dB at 0.7 GHz and 7.5 dB at 1.6 GHz, as shown in Figure 3.15.



Figure 3.15 Measured phase noise comparison between coupled-osc without N-path filters and NPFRVCO at 1MHz offset from carrier. Measurements are made with discriminator method.

CHAPTER IV

Traveling-Wave ADC

4.1 High Speed ADC with On-chip Transmission Line

This new ADC architecture is inspired by the RF traveling-wave amplifier architecture. As shown in Figure 4.1, a distributed amplifier [8] has a pair of transmission lines that are independently connected to the inputs and outputs. The delays of the input and output lines are made equal. Similarly, in this very high speed ADC, shown in Figure 4.2, an on-chip transmission line provides an alternative approach to transmit clock and input signaling without needing powerconsuming active circuitry. A significant advantage is that high tracking bandwidth sample-and-hold [33] amplifiers and MDACs are no longer needed to sample and transmit input signal.



Figure 4.1 Distributed amplifier [8]



Figure 4.2 Block diagram of the traveling wave ADC



Figure 4.3 Traveling-wave ADC

4.2 System Architecture

The new scheme exploits the delay of on-chip transmission lines to implement a pipeline and thereby avoids the use of power hungry track-and-hold or MDAC stages. As illustrated in Figure 4.3, the input signal and the clock signal propagate down a matched pair of transmission lines. The delay of the transmission line allows time for a stage decision to be made at stage n, before the signal and clock edge reach the next stage n+1. Because this scheme is intended for moderate resolution, the stages do not need to provide gain; instead the comparators zoom into the signal value.

The critical decision path in the traveling-wave pipeline is relaxed by using



Figure 4.4 DAC algorithm

two comparators in all stages after the first. Although, the delay between stages is independent of the sampling rate, the delay does need to be long enough so that the stage n decision is resolved in time to set up the comparator reference voltage of stage n + 1. To circumvent this timing constraint, we use two comparators in stage n + 1. The two comparators of stage n + 1 are setup with two pre-computed reference values corresponding to both possible decisions of stage n. When stage n decides, we select which of the two comparator outputs of stage n + 1 is appropriate. This allows the reference voltages for the comparators in stage n + 1 to be configured before a decision is made by stage n.

Figure 4.4 shows the algorithm of how the DAC values are set in each comparison stage. Assuming the proposed ADC has N-bit resolution overall and generates one bit per stage, the MSB and LSB bits are generated by the first and the *Nth* comparison stage, respectively. As mentioned above, for each comparison stage, there is a pair of DAC values that needs to be set (the first stage is the only exception as this has a single DAC value). For the stage *i*, there are totally 2^{i-2} pairs of possible DAC values for the *ith* comparison stage:

$$(-\frac{2^{i-1}-1}{2^{i-1}}, -\frac{2^{i-1}-3}{2^{i-1}}), (-\frac{2^{i-1}-5}{2^{i-1}}, -\frac{2^{i-1}-7}{2^{i-1}}), ..., (-\frac{3}{2^{i-1}}, -\frac{1}{2^{i-1}}), (\frac{1}{2^{i-1}}, \frac{3}{2^{i-1}}), ..., (\frac{2^{i-1}-7}{2^{i-1}}, \frac{2^{i-1}-5}{2^{i-1}}), (\frac{2^{i-1}-3}{2^{i-1}}, \frac{2^{i-1}-1}{2^{i-1}})$$

$$(4.1)$$

The MSB to MSB+3-i bits are used to decide which pair of DAC values listed above will be chosen. For example, assuming that the input value is $\frac{7}{16}$ and the DAC full scale is -1 to 1, the first four bits of the ADC outputs are MSB=1, MSB-1=0, MSB-2=1, MSB-3=1. For Stage 1, the DAC value is zero. For Stage 2, there is only one pair of possible DAC values $(-\frac{1}{2}, \frac{1}{2})$. For Stage 3, the possible DAC value pairs are $(-\frac{3}{4}, -\frac{1}{4})$ and $(\frac{1}{4}, \frac{3}{4})$. Since the MSB bit is 1, $(\frac{1}{4}, \frac{3}{4})$ is selected. For Stage 4, the possible DAC value pairs are $(-\frac{7}{8}, -\frac{5}{8})$, $(-\frac{3}{8}, -\frac{1}{8})$, $(\frac{1}{8}, \frac{3}{8})$ and $(\frac{5}{8}, \frac{7}{8})$. Because MSB is high and MSB-1 is low, the 3rd pair $(\frac{1}{8}, \frac{3}{8})$ is chosen. To summarize, for this example the DAC values from Stage 1 to 4 for this ADC are 0, $(-\frac{1}{2}, \frac{1}{2}), (\frac{1}{4}, \frac{3}{4})$ and $(\frac{1}{8}, \frac{3}{8})$.

4.3 System Implementation

4.3.1 On-chip Transmission Line

The on-chip transmission line must provide sufficient delay between stages. At the same time the loss and dispersion of the line must be small. The frequencydependent complex transfer function H(f) of a transmission line can be expressed as:

$$H(f) = A(f) \cdot \exp j\phi(f) \tag{4.2}$$

where A(f) denominates the magnitude and $\phi(f)$ is the phase response. Based on phase simulation results and measurement results, we can find the group delay t_{gr} of the transmission line. t_{gr} is the negative derivative of the phase ϕ (in degrees) with respect to frequency f:

$$t_{gr} = -\frac{1}{360^{\circ}} \cdot \frac{d\phi}{df} \tag{4.3}$$

For non-dispersive transmission lines, group delay is not a function of frequency at all, but constant. Therefore, phase $\phi(f)$ is a linear function of frequency:

$$\phi(f) = -360^\circ \cdot f \cdot t_d \tag{4.4}$$

Where, t_d is the delay time of the transmission line. From 4.3 and 4.4, since phase is a linear function of frequency f, the delay time t_d and the group delay t_{gr} are equivalent. To measure the delay of the non-dispersive transmission line, measurements of group delay can be performed. For accurate tracking of the phase shift versus frequency, the frequency span and the number of points for the network analyzer must be chosen so that the phase shift between each two adjacent frequency points does not exceed 180°. The delay time t_d is directly related to its physical length L_{phy} of the transmission line, the light velocity in vacuum c; and the equivalent dielectric constant around the transmission line ε_{eff} :

$$t_d = \frac{L_{phy} \cdot \sqrt{\varepsilon_{eff}}}{c} \tag{4.5}$$

The product $L_{phy} \cdot \sqrt{\varepsilon_{eff}}$ denotes the effective length of the transmission line as 'seen' by the electrical signal traveling along the line. To make the on-chip transmission line practical, we want the physical transmission line length L_{phy} to be as short as possible. Meanwhile, since the comparator must decide based on the previous decision, the delay provided by the transmission line should be long enough to avoid decision errors. As the velocity of light *c* is a constant, to keep t_d equal to the delay of comparator, a smaller L_{phy} requires an even larger ε_{eff} .

The slow-wave transmission line structure proposed in Figure 4.5 increases ε_{eff} , therefore increasing the effective length of the transmission line and slowing down the signal propagation speed in the transmission line. This can, in principle, reduce the required length by an order of magnitude. To reduce the silicon cost and make the layout more compact, we want to use the shortest possible transmission line, thus requiring an even larger ε_{eff} which furthermore increases the design difficulty of the transmission line.



Figure 4.5 Cross section of on-chip microstrip transmission line

In the first prototype, we added equally-spaced floating metal strips underneath the transmission line, as a result, artificially increasing the effective dielectric constant of the transmission line. To reduce ohmic losses, the metal conductor of the resonator is formed with the top three metal layers, connected in parallel. The floating metal shield is formed with floating strips, with each strip formed with the lower three metal layers connected in parallel. This use of parallel strips not only helps reduce the strip resistance, but also helps meet the stringent metal fill requirements of the CMOS 65 nm process. The strip structure also breaks induced eddy currents. Since the top of the floating metal shield is relatively close to the conductor, the shield deliberately loads the conductor with capacitances. Thus the equivalent dielectric constant is increased. This periodic capacitive loading introduces the slow-wave effect.

This slow-wave technique was demonstrated in both simulation and in the test of a prototype line. However, the increase of the equivalent dielectric constant



Figure 4.6 Differential transmission line

offered by this technique and the micro-strip structure is not enough for a 6-bit ADC. At least five segments of the transmission line in the 6-bit ADC design are needed. These long microstrip lines occupy a lot of silicon area, and attenuate the signal by more than the resolution of the comparator in the last stage; and so the ADC cannot resolve the signal accurately. Meanwhile, both clock signal and input signal are differential, requiring four on-chip transmission lines running in parallel. The physical size of the lines must be optimized so that the chip area is efficiently used. In addition, electromagnetic coupling between lines is a potential problem with the transmission line structure of the first prototype. There are four microstips lines in the first prototype running in parallel, and transmitting the differential input and the differential clock. Each microstrip line between stages is 1.4 mm long.

Instead, we propose the use of differential symmetric inductors that are loaded



Figure 4.7 LC ladder form

with differential symmetric capacitors (shown in Figure 4.6) [34] for each section of the delay line. Identical interconnected inductors and capacitors are connected in ladder form, as shown in Figure 4.7.

The differential inductor benefits from the mutual inductance of the two halves. Therefore, larger value inductances are achievable with the same or even smaller area. The ladder is a lumped approximation of transmission line, thus can be used as a delay line. The delay of the structure is approximately:

$$T_d = \sqrt{LC} \tag{4.6}$$

The characteristic impedance Z_0 of the LC ladder is:

$$Z_0 = \sqrt{L/C} \tag{4.7}$$

Designed for a characteristic impedance $Z_0 = 50\Omega$, $T_d = 9 ps$, we can calculate $L_{eff} = 450 \ pH$ and $C = 180 \ fF$. Thus the transmission line between stages consists of four LC ladder segments that contribute a delay of 36 ps delay. The impedance of the line versus frequency is:

$$Z_{\omega} = \sqrt{\frac{L}{C}} \cdot \sqrt{1 - \frac{LC\omega^2}{4}} = Z_0 \cdot \sqrt{1 - \frac{LC\omega^2}{4}}$$
(4.8)

From this expression, we can see that the impedance becomes imaginary for frequencies above a critical frequency given by:

$$\omega_c = \frac{2}{\sqrt{LC}} \tag{4.9}$$

The delay of one segment of LC ladder should be small enough to ensure the critical frequency is far above the LC ladder operating frequency. Therefore, 4.6 and 4.9 sets the maximum delay of one segment of LC ladder.

In contrast to the microstrip line, which is a continuous transmission line, the LC delay line does not provide a constant delay over the entire passband. Thus, the frequency dependent group delay over the desired range should be measured to fully characterize the line. Figure 4.8 shows the magnitude and phase of the transmission line. From the slope, we can see that over the operating frequency range the group delay is constant and delay is sufficient.

Another concern is the loss in the signal as it propagates along the transmission line. To counteract this loss, the DACs in each stage are calibrated according to the



Figure 4.8 Magnitude and phase of the transmission line

attenuation on the transmission line. The 3 dB bandwidth is around 10 GHz for the entire transmission line. This relatively low attenuation along the transmission line alleviates the design challenges of the clock buffer that generates a full swing CMOS clock.

4.3.2 High Speed Comparator

As illustrated in Figure 4.3, there is one comparator in the MSB stage and two comparators in other decision stages. Five segments of transmission lines are needed for a 6-bit ADC. Since the MSB-1 stage has two fixed DAC references, the MSB-1 stage is combined with the MSB stage to save one segment of transmission line. Because transmission lines occupy most of the silicon area, saving one

segment of transmission line reduces almost 20% of silicon cost. Moreover, the signal is attenuated along the transmission lines. The signal received by the last active stage will be less attenuated since the lines are shorter. This can alleviate the requirements for resolution of the comparator in the last stage. However, combining the first two stages results in only one transmission line delay for the MSB decision to set the DACs references in the MSB-2 stage. To solve this issue, instead of two comparators, four comparators with four possible DAC references are placed in MSB-2 stage. Increasing the number of comparators to compensate for lack of delay provided by the transmission line is a tradeoff between silicon cost and power consumption. In conclusion, there are two comparators per decision stage, one comparator in MSB stage and four comparators in the MSB-2 stage. The peak-to-peak input range is 640 mV, resulting in a nominal LSB value of 10 mV. To achieve a power-efficient design, dynamic comparators without any pre-amplifiers are employed in this ADC.

Figure 4.9 shows the design of the comparator, which is based on a dynamicsense amplifier latch [35] incorporating several modifications. The comparator consists of a double differential input stage and a regenerative latch at the output. The input devices are sized small to minimize input capacitance. Because the comparator input transistors are small, there are two 4-bit trim currents to calibrate the comparator offsets [36]. The offset trimming circuit generates a current which compensates the input device offset, such that the error after trimming is below 1/4 LSB. For all the comparators, offset calibration is done simultaneously during startup. Two reset switches are employed to reset the gates and sources of the



Figure 4.9 High speed comparator

regenerative output latch when clock is held low.

The comparator samples the differential input signal and compares it with the differential references generated, based on the previous stage decisions. The input device configuration accommodates the large signal range. Since the LC structure attenuates the signal, the LSB value is reduced to 7 mV. The comparator output is valid for a half clock period (when the clock is high), since the comparator is reset when the clock is low. Therefore, an SR latch follows the comparator to hold the output for an entire clock period.

4.3.3 Current-steering DAC

Current-steering DACs are normally implemented with a tail current source and a pair of switches that are controlled by digital signals. Current steering DACs produce and combine several scaled copies of a reference current. The summed current is then converted to voltage with a pair of resistor loads. Currentsteering DACs mitigate the effects of mismatch and process variations with careful arrangement of current cells while saving silicon cost by using compact devices such as MOSFETs, instead of capacitors or resistors as unit current cell. Moreover, the structure of current-steering DACs can be easily integrated with trim current calibration technique. However, even with calibration there are still dynamic nonidealities that need to be taken care of. For example, the finite settling time due to RC time constants of the resistor loads and parasitic capacitors; the coupling of control signals to the current DAC output though switch charge injection; and timing error due to control signal timing skew.

To achieve faster settling time, the resistor loads in current-steering DACs are chosen to be small. The DAC swing is set by the product of resistor load and combined currents of the array of current cells. The minimum DAC swing is set by the minimum voltage difference that the comparator can detect. For a fixed DAC swing, if the resistor loads are small, the DAC should burn more current to generate the same DAC swing. Thus, there is a tradeoff between fast settling time and lower power consumption. To make sure the DAC references are ready for comparators to make a decision, i.e. the settling time is longer than twice the RC time constant (86% accuracy), the maximum settling time t_{settle} can be calculated as:

$$t_{settl} = 2 \cdot T_{d-tline} - t_{clk-q} \tag{4.10}$$

Where $T_{d-tline}$ is the delay provided by the transmission line between two stages and t_{clk-q} is the time it takes for the high speed comparator output to be in a stable state after clock samples. Since the peak-to-peak input range is 640 mV, for a 6-bit ADC with 64 conversions, the LSB size is 10 mV. The RMS noise voltage of the high speed comparator is 2.34 mV, which is within the LSB size of current-steering DACs. For a 100-ohm resistor load, the nominal LSB current is 0.1 mA.

These current DACs allow in-DAC summing, thereby eliminating the need for high-speed digital logic in the critical path. The current-steering DAC consists of binary weighted current cells driven by decision bits from previous stages. Each current cell is composed of current source devices, cascode devices and switches. For fast settling, a small cascode device isolates the large drain capacitance of the current source device from switch devices. Figure 4.10 (a) and (b) shows the two DACs in the stage MSB-2. Each DAC generates two differential signals that are sent to the reference input nodes of the corresponding comparator. The current cell with fixed control switches (VDD and VSS) in each DAC sets the resolution of the DAC. Bit B_0 and bit $\overline{B_0}$ are the complementary decision bits from stage MSB and bit B_1 and bit $\overline{B_1}$ are from stage MSB-1. These bits directly set the DAC outputs in stage MSB-2 without extra high-speed logic. Figure 4.10 (c) shows the DACs generate -3/4 and -1/4 of full input range for comparators when both B_0 and B_1 are



Figure 4.10 DACs in stage MSB-2

low.

As the transmission line consists of inductors and capacitors and is not ideal, signal loss in inevitable along the transmission line. The LSB current I_{lsb} in the DACs of each stage is tuned according to the attenuation on the transmission line to compensate for the signal loss.

To keep the common-mode of the DAC differential outputs in all stages consistent with input common mode V_{in_cm} , a series resistor R_s is added between power supply *VDD* and the resistor load *R*. Taking one DAC in stage MSB-2 as an example, shown in Figure 4.10 (a), the binary weights of current sources in MSB-2 stage are 4, 8 and 16. The DAC common mode V_{cm} is the average of V_{refap} and V_{refam} . Assume V_{cm} equals to V_{in_cm} and the nominal DAC unit current is I_{lsb} , solve for series resistor R_s :

$$R_{s} = \frac{VDD - [V_{in_{c}m} + \frac{1}{2}R \cdot (4 \cdot I_{lsb} + 8 \cdot I_{lsb} + 16 \cdot I_{lsb})]}{4 \cdot I_{lsb} + 8 \cdot I_{lsb} + 16 \cdot I_{lsb}} = \frac{VDD - V_{in_{c}m}}{2828 \cdot I_{lsb}} - \frac{1}{2}R$$
(4.11)

If a current change ΔI is applied to the DAC unit current I_{lsb} , i.e. $I'_{lsb} = I_{lsb} \pm \frac{1}{2}R$, the common mode of the DAC differential outputs will be changed to V'_{cm} :

$$V_{cm}^{'} = VDD - (4 \cdot I_{lsb}^{'} + 8 \cdot I_{lsb}^{'} + 16 \cdot I_{lsb}^{'}) \cdot (R_{s} + \frac{1}{2}R)$$
(4.12)

Set $\Delta V_{cm} = V_{in_cm} - V'_{cm}$, ΔV_{cm} is given by:

$$\Delta V_{cm} = 28 \cdot \Delta I \cdot \left(R_s + \frac{1}{2}R\right) \tag{4.13}$$



Figure 4.11 DC characterization: DNL and INL of 5 Bit ADC

Substitute R_s with 4.11,

$$\Delta V_{cm} = \frac{\Delta I}{I_{lsb}} \cdot (VDD - V_{in_cm})$$
(4.14)

Thus, the common mode of the DAC differential outputs is independent of the binary weights of the current sources. The common mode change is only proportional to $\frac{\Delta I}{I_{lsb}}$, the change rate of unit current.

4.4 Measurements

The prototype traveling-wave ADC is fabricated in 40 nm CMOS. The measured DNL/INL plots made after foreground DAC calibration, are shown in Figure 4.11. The measured DNL and INL are within -0.62/+0.77 LSB and -0.83/+0.88


Figure 4.12 Measured normalized spectrum for 4.24 MHz input sampled at 4 GS/s

LSB, respectively.

With single tone 4.24 MHz sinewave input, the ADC achieves 21.35 dB SNDR (3.25 bit ENOB) and 30.18dB SFDR at a 4GS/s clock sampling rate, as shown in Figure 4.12. With an increased sampling clock rate of 6 GS/s, and a single tone 6.36 MHz sinewave input, the ADC achieves 19.1 dB SNDR (2.88 bit ENOB) and 28.7 dB SFDR, as shown in Figure 4.13. The power consumption is 38.2 mW (clock buffer 2.1 mW, comparator 8.7 mW, DAC 26 mW, others 1.35 mW), which corresponds to 0.86 pJ/step FoM. The power breakdown is shown in Figure 4.14. The on-chip LC transmission line is fabricated using top level thick metal M10 and M9 as intersection. The capacitors are Metal-Insulator-Metal (MIM) structures. Figure 4.15 shows one segment of transmission line between two active stages, which consists of four differential LC structures. The active die area of traveling-wave ADC is 0.65 mm² and the die micrograph is shown in Figure 4.16.



Figure 4.13 Measured spectrum for 6.36 MHz input sampled at 6 GS/s



Figure 4.14 Power breakdown



Figure 4.15 On-chip transmission line



Figure 4.16 Die micrograph



Figure 4.17 Diagram of the test setup

4.5 Test Setup

Figure 4.17 shows the test setup for the traveling-wave ADC. To test the prototype high-speed traveling-wave ADC, two high-speed signal sources generate both the high-speed input signal and the high speed clock. Since the traveling-wave ADC needs differential inputs, high bandwidth transformers or baluns are necessary to provide high speed differential signals. On the test board, there are two pairs of transmission lines with 50-ohm characteristic impedance to transmit the differential input signals and the differential clocks to the travelling-wave ADC chip. To terminate the two pairs of transmission lines, there are footprints on the testing board for impedance matching network (shown as a series resistor) that consists of resistors, inductors and capacitors. ICALIB is the bias current for calibration. IB1 to IB5 are bias currents for DACs in each active stage. A logic analyzer is used to read the decimated clock (CK) and the output data (D0 to D5).



Figure 4.18 Test setup

The output is decimated by the on-chip decimator. The read-out data is processed in MATLAB for spectrum analysis and DC characteristic analysis.

Figure 4.18 shows the test setup (on the left) and the 4-layer board (on the right). The travelling-wave ADC chip sits in the center.

CHAPTER V

Future Work

With the assistance of N-path filters, good phase noise performance is achieved in a ring VCO. The following improvements can be considered for more flexibility and better system performance:

- To support higher output frequency, the delay cell can be modified by adjusting the coarse and fine control signals.
- The non-overlapping clock generation circuitry can be optimized to further reduce power consumption, especially at higher output frequency.
- Integrate the NPFRVCO in a PLL.

The travelling wave ADC is a high speed reconfigurable resolution ADC. It can find many applications in high-speed communication systems, such as direct digitization in optical fiber system. Some potential improvements include:

• Adding redundancy to improve ENOB.

- Use of a single clock phase so that the on-chip transmission line for transmitting clock is not necessary.
- Characterization of magnetic pulling and signal coupling from transmission line to low metals.
- Layout of circuitry underneath transmission line to save area.

CHAPTER VI

Conclusion

The prototype N-path filter enhanced voltage-controlled ring oscillator (NPFRVCO) achieves a measured phase noise of -110 dBc/Hz at a 1 MHz offset frequency for an oscillation frequency of 1.0 GHz. The self-clocked N-path filter reduces the phase noise by 10 dB and 28 dB for 1.0 GHz and 300 MHz oscillation frequencies, respectively. Implemented in 65 nm CMOS, the NPFRVCO occupies a die area of 0.015 mm² and consumes 4.7 mW from 1.2 V power supply when operating at 1.0 GHz. The NPFRVCO has a measured frequency tuning range from 300 MHz to 1.6 GHz and achieves a FoM of 163 dB at 1 MHz offset.

This research developed and demonstrated new techniques that enable energy efficient, very-high-speed, moderate resolution analog-to-digital conversion. Onchip transmission lines provide sufficient delay between decision stages, avoiding the need for power hungry high-bandwidth track-and hold amplifiers. The feedforward settings of DACs further relax the timing constraints of delay between stages. Current summing of the current steering DAC requires no high speed digital logic in the critical path. The scheme combines the efficiency of the SAR technique with the throughput of flash. With a energy efficiency of 0.895 pJ per conversion bit, this very-high-speed ADC will facilitate ADC-based wireline links, optical communication system and high bandwidth wireless communication systems such as next generation cellular.

The key contributions of this research are summarized as follows:

- A novel scheme to reduce phase noise of ring VCO using N-path filter.
- A completely new ADC scheme based on a traveling wave structure.
- Compact on-chip transmission line design and characterization.
- Design of a prototype power-efficient very-high-speed ADC.

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