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# Modeling of Heat Transfer Attenuation by Ablative Gases **During the Stardust Reentry**

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Modern space vehicles designed for planetary exploration use ablative materials to protect the payload against the high heating environment experienced during reentry. To properly model and predict the aerothermal environment of the vehicle, it is imperative to account for the gases produced by ablation processes. The present study aims to examine the effects of the blowing of ablation gas in the outer flow field. Using six points on the Stardust entry trajectory at the beginning of the continuum regime, from 81 to 69 km, the various components of the heat flux are compared to air-only solutions. Although an additional component of the heat flux is introduced by mass diffusion, this additional term is mainly balanced by the fact that the translational-rotational component of the heat flux, the main contributor, is greatly reduced. Although a displacement of the shock is observed, it is believed that the most prominent effects are caused by a modification of the chemical composition of the boundary layer, which reduces the gas-phase thermal conductivity.

#### Nomenclature

- nondimensional ablation rate =
- vector of source terms =
- = mass diffusion coefficient, m<sup>2</sup>/s
- = energy, J/m<sup>3</sup>
- energy, J/kg =
- = inviscid flux matrix
- =
- diffusive flux matrix
- species enthalpy vector, J/kg =
- = identity matrix
- = directional species diffusion,  $kg/(m^2 \cdot s)$
- = Knudsen number
- thermal conductivity,  $W/(m\cdot K)$ =
- $\dot{m}^{\prime\prime}$ = mass flow rate,  $kg/(m^2 \cdot s)$ 
  - = pressure, Pa
  - = vector of conserved variables
  - = heat flux, W/m<sup>2</sup>
  - = temperature, K
- U, v= velocity, m/s ŵ
  - mass source term,  $kg/(m^3 \cdot s)$ =
- = vibrational energy relaxation source term,  $J/(m^3 \cdot s)$  $\dot{w}_v$ Y
  - = mass fraction, kg/kg
  - = distance normal to the wall, m
- ρ = mass density, kg/m<sup>3</sup>
  - = viscous tensor, Pa

## Subscripts

С	=	char

- gas blown = g
- next to the wall nc =

5	=	species
t	=	time
tr	=	translational-rotational
ve	=	vibrational-electron-electronic
w	=	wall
$\infty$	=	freestream

#### I. Introduction

**O** NE of the most important components of a reentry vehicle is its thermal protection system (TPS). Depending on the reentry trajectory and atmospheric conditions, two types of materials may be used for TPS design: ablative materials, such as the ones used on the Apollo missions, and non-ablative materials, such as the ceramic tiles used on the Space Shuttle. For most planetary exploration missions, a multi-component ablative material is most frequently used. In this type of material, an inner resin is first chemically and thermally decomposed before the surface begins to react. This type of ablator, called charring or pyrolysing ablator, offers multiple advantages, like generating a relatively cold pyrolysis gas that travels through the char layer or expelling that gas at the surface, which modifies the transport properties, thus the heat flux transmitted to the vehicle.

To properly model the heating rates at the surface of the vehicle, the ablating boundary condition must take into account many phenomena: surface recession, wall temperature, blowing rates, gas composition, surface chemistry, etc. However, to account for the effects of the pyrolysis gas on the vehicle, the chemistry model of the flow field must include the reactions associated with the presence of this gas. Because ablation coupling is becoming an increasingly important research topic [1-7], the development of an accurate, yet usable, chemistry model is of great importance. Models have been proposed in the past [8-10], but important reactions were not included, and some of the reaction rates were inappropriate or simply outdated.

Recently, a more complete model was proposed [11,12], which includes an extensive set of kinetic rates taken from the combustion community. The model was reduced using zero-dimensional sensitivity analysis over a parameter space relevant to the reentry conditions that such a material would be exposed to. It was established that such a model was necessary to study carbon-phenolic TPS through a review of past models, which gave a wide range of results, especially when radiative heat transfer calculations were performed [13]. The reduced model was later integrated into the hypersonic computational fluid dynamics (CFD) code LeMANS. As a test case, results were obtained at various trajectory points of the Stardust reentry vehicle, and the importance of accounting for ablation in flow field

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Fig. 1 Geometry and mesh of the Stardust reentry capsule, used for the chemistry model comparison. The mesh has 165 points along the wall and 238 points along the axis.

chemistry was highlighted [12,14]. A later paper [15] focused on the 71 km trajectory point, for which spectrally resolved radiative emission measurements were obtained. The experimental data were compared to the computed results, which were processed using the NEQAIR (version 7) radiation code [16]. The agreement was surprisingly good, considering the high level of assumptions and uncertainties of both the experimental data and the computations.

The current paper further analyzes the Stardust trajectory between 81 and 69 km. Six trajectory points are analyzed, and an attempt is made to identify the key aspects of the heat flux reduction caused by pyrolysis gas injection.

Finally, for validation purposes, a comparison is made with the experimental data obtained with the echelle spectrometer at altitudes of 71 and 81 km. A good agreement is noted at 71 km, as previously published [15], and an even better one is obtained at 81 km. These results show the validity of the chemistry model used in the CFD code and demonstrate that the assumptions made for calculating blowing rates and pyrolysis gas composition are reasonable.

The results presented here are unique as they provide a detailed analysis of how the ablation species are transported in the flow field and subsequently affect the surface heat fluxes. Moreover, the results use actual trajectory data to perform the calculation and are compared to experimental measurements.

#### II. Chemistry Model

The chemistry model used in this analysis has been developed and optimized for vehicles equipped with ablative heat shields composed of Carbon-Phenolic that reenter in a  $N_2$ - $O_2$  atmosphere [11,12,14]. The species and reaction mechanisms used in the model were carefully selected using a material response analysis. The corresponding kinetic chemistry rates were taken from the GRI-Mech model and then reduced using a sensitivity analysis [11–14]. The reduced model contains 38 species and 158 reaction rates. The selected species can be grouped into three categories, as follows.

1) The air species:

$$N_2, O_2, NO, N, O, N_2^+, O_2^+, NO^+, N^+, O^+, e$$

2) The boundary-layer and surface species:

3) And the reacting species:

## H, NH, HO<sub>2</sub>, H<sub>2</sub>O<sub>2</sub>, HCO, C, C<sub>2</sub>, CH, CH<sub>2</sub>, CH<sub>3</sub>, NCO, HNO CO<sup>+</sup>, CN<sup>+</sup>, C<sup>+</sup>, H<sup>+</sup>

The reaction mechanisms and forward kinetics rates are listed in Refs. [11,12]. Gibb's free energy is used to calculate the equilibrium constants needed for the backward reaction rates. The model has been validated with multiple zero-dimensional simulations performed using the CHEMKIN [17] package and compared to available experimental data that are representative of an ablative boundary layer during hypersonic reentry [13].

#### III. LeMANS: Unstructured Three-Dimensional Navier–Stokes Solver for Hypersonic Non-Equilibrium Aerothermodynamics

The hypersonic aerothermodynamic CFD code used in the present analysis is LeMANS, a finite-volume Navier–Stokes solver [18]. The code assumes that the rotational and translational energy modes of all species can be described by a single temperature T and that the vibrational energy mode and electronic energy mode of all species, as well as the free electron kinetic energy, can be described by another single temperature  $T_{ve}$ . The following equations are therefore solved:

$$\frac{\partial \boldsymbol{Q}}{\partial t} + \nabla \cdot (\boldsymbol{F} - \boldsymbol{F}_d) = \boldsymbol{C} \tag{1}$$

where

$$\boldsymbol{Q} = \begin{pmatrix} \rho \boldsymbol{Y}^T \\ \rho \boldsymbol{u}^T \\ \boldsymbol{E} \\ \boldsymbol{E}_{ve} \end{pmatrix} \quad \text{and} \quad \boldsymbol{C} = \begin{pmatrix} \dot{\boldsymbol{w}}^T \\ \boldsymbol{0}^T \\ \boldsymbol{0} \\ \dot{\boldsymbol{w}}_v \end{pmatrix} \tag{2}$$

are the vector of conserved variables and the vector of source terms, respectively. In these equations,  $\mathbf{Y} = (Y_1, \ldots, Y_{ns})$  is the species densities vector,  $\mathbf{u}$  is the bulk velocity components, and E and  $E_{ve}$  are the total and the vibrational–electron–electronic excitation energy per unit volume of mixture, respectively.

The inviscid and diffusive flux matrices are given by

$$F = \begin{pmatrix} \rho Y^T u \\ \rho u^T u + I p \\ (E + p) u \\ E_{ve} u \end{pmatrix} \text{ and } F_d = \begin{pmatrix} -J \\ \tau \\ u\tau - (q_{tr} + q_{ve}) - (h^T J) \\ -q_{ve} - (e_{ve}^T J) \end{pmatrix}$$
(3)

Table 1 Freestream conditions used for the Stardust trajectory

Altitude, km	Time, s	$U_{\infty}, \mathrm{km/s}$	$T_{\infty}, K$	$\rho_{\infty}$ , kg/m <sup>3</sup>	$Y_{N_2}$	$Y_{O_2}$	Kn
81.0	34	12.4	218.	$1.27 \times 10^{-4}$	0.763	0.237	0.00645
78.5	36	12.3	218.	$1.87 \times 10^{-4}$	0.763	0.237	0.00432
76.0	38	12.3	219.	$2.72 \times 10^{-4}$	0.763	0.237	0.00292
73.5	40	12.2	220.	$3.92 \times 10^{-4}$	0.763	0.237	0.00203
71.2	42	12.1	222.	$5.55 \times 10^{-4}$	0.763	0.237	0.00145
68.9	44	11.9	224.	$7.72\times10^{-4}$	0.763	0.237	0.00105

Table 2 Wall conditions at the stagnation point for the Stardust trajectory

Altitude,	$T_w$ ,	$\dot{m}_w^{\prime\prime},$				$Y_{\rm H_2O},$			$Y_{\rm CO_2}$ ,			
km	Κ	kg/m <sup>2</sup> /s	$Y_{\rm N_2}$ , kg/kg	$Y_{\rm CO}$ , kg/kg	$Y_{\rm H_2},  \rm kg/kg$	kg/̃kg	$Y_{\rm OH},  \rm kg/kg$	$Y_{\rm O},  \mathrm{kg/kg}$	kg/k̃g	$Y_{\rm NO}$ , kg/kg	$Y_{O_2}$ , kg/kg	$Y_{\rm N}$ , kg/kg
81.0	2670.	0.0214	$6.16\times10^{-1}$	$2.32\times10^{-1}$	$1.52\times10^{-2}$	$6.85\times10^{-2}$	$1.94 \times 10^{-2}$	$1.24\times10^{-2}$	$2.72\times10^{-2}$	$4.93\times10^{-3}$	$5.05\times10^{-3}$	0.00
78.5	2750.	0.0264	$6.14 \times 10^{-1}$	$2.34 \times 10^{-1}$	$1.52 \times 10^{-2}$	$7.32 \times 10^{-2}$	$1.72 \times 10^{-2}$	$9.18 \times 10^{-3}$	$2.94 \times 10^{-2}$	$4.38 \times 10^{-3}$	$4.02 \times 10^{-3}$	0.00
76.0	3070.	0.0299	$6.49 \times 10^{-1}$	$1.75 \times 10^{-1}$	$1.08 \times 10^{-2}$	$4.88 \times 10^{-2}$	$3.21 \times 10^{-2}$	$3.75 \times 10^{-2}$	$1.92 \times 10^{-2}$	$1.22 \times 10^{-3}$	$1.52 \times 10^{-2}$	0.00
73.5	3150.	0.0378	$6.54 \times 10^{-1}$	$1.65 \times 10^{-1}$	$9.38 \times 10^{-3}$	$5.41 \times 10^{-2}$	$3.19 \times 10^{-2}$	$3.33 \times 10^{-2}$	$2.30 \times 10^{-2}$	$1.30 \times 10^{-2}$	$1.72 \times 10^{-2}$	0.00
71.2	3240.	0.0453	$6.75 \times 10^{-1}$	$1.23 \times 10^{-1}$	$5.76 \times 10^{-3}$	$5.23 \times 10^{-2}$	$3.30 \times 10^{-2}$	$3.68\times10^{-2}$	$2.70 \times 10^{-2}$	$1.74 \times 10^{-2}$	$2.99 \times 10^{-2}$	0.00
68.9	3310.	0.0549	$6.78\times10^{-1}$	$1.25\times10^{-1}$	$7.21\times10^{-3}$	$3.08\times10^{-2}$	$3.71\times10^{-2}$	$6.46\times10^{-2}$	$1.22\times10^{-2}$	$2.08\times10^{-2}$	$2.44\times10^{-2}$	$7.84 \times 10^{-5}$

where p is the pressure,  $\tau$  is the viscous tensor, and  $q_{\rm tr}$  and  $q_{\rm ve}$  are the directional translational–rotational and vibrational–electron–electronic excitation heat flux vectors, respectively, calculated using Fourier's law of conduction:

$$q_i = k_i \nabla T_i \tag{4}$$

where  $k_i$  is the thermal conductivity, and index *i* represents the various energy modes (in the present case, either tr or ve). Moreover, *h* is the species enthalpy vector, and *J* is the directional species diffusion flux tensor. The details of these equations and models are found in [19].

The viscous stresses in  $\tau$  are modeled assuming a Newtonian fluid using Stokes's hypothesis, and the species mass diffusion fluxes are modeled using a modified version of Fick's law, which forces the sum of all diffusion velocity to be zero.

The species transport properties are calculated from Lennard– Jones potentials, using CHEMKIN [17], to produce individual species temperature dependent viscosity curve fits (Blotter's model [20]). Mixture transport properties are calculated using Wilke's semiempirical mixing rule [21], and species thermal conductivities are determined using Eucken's relation [22]. According to the constant Lewis number assumption, the diffusion coefficient of each species is assumed to be equal. Heat fluxes are modeled according to Fourier's law for all temperatures. Finally, the source terms of the species conservation equations are modeled using a standard finite-rate chemistry model for reacting air in conjunction with Park's twotemperature model [23] to account for thermal non-equilibrium effects on the reaction rates.

The code has the capability to handle meshes containing any mix of hexahedra, tetrahedra, prisms, and pyramids in three dimensions or triangles and quadrilaterals in two dimensions. Numerical fluxes between the cells are discretized using a modified Steger–Warming flux vector splitting scheme, which has low dissipation and is appropriate to calculate boundary layers. A point or line implicit method is used to perform the time integration. The code has been extensively validated against experimental data [19,24–33] and has also been compared to other similar codes such as NASA Ames's DPLR [34] and NASA Langley's LAURA [35].

To account for the coupling between the flow field and the material response, the effects of ablation are added to the CFD code; therefore, a modification to the surface boundary condition is necessary. The physical values at the wall are obtained by solving the surface momentum balance equation:

$$p_{\rm nc} + \rho_{\rm nc} v_{\rm nc}^2 = p_w(\rho_w, T_w) + \rho_w v_w^2 \tag{5}$$

It is to be noted that the diffusive fluxes are neglected in this relation. Using perfect gas relation, the density, pressure, and velocity at the wall can be calculated:

$$\rho_w = \frac{p_\eta + \sqrt{p_\eta^2 - 4RT_w \dot{m}_w'^2}}{2RT_w}$$
(6)

$$v_w = \frac{2RT_w \dot{m}_w''}{p_\eta + \sqrt{p_\eta^2 - 4RT_w \dot{m}_w'^2}}$$
(7)



a) Surface temperature



b) Surface blowing rate

Fig. 2 Imposed surface temperature and blowing rates for the echelle part of the trajectory of Stardust.

$$_{w} = \frac{p_{\eta} + \sqrt{p_{\eta}^{2} - 4RT_{w}\dot{m}_{w}^{\prime 2})}}{2}$$
(8)

The mass fractions of the species leaving the wall  $(Y_{ws})$  are calculated using a surface mass balance equation:

p

$$\rho_w D_{ws} \frac{\partial Y_{ws}}{\partial \eta} + \dot{m}_w^{\prime\prime} Y_{ws} = \dot{m}_w^{\prime\prime} Y_{gs} \tag{9}$$

The left side of the equation represents the diffusive and convective flux approaching the wall, from the flow field domain, and the right side represents the convective flux approaching the wall from the the TPS domain. In all these equations, the blowing rate  $\dot{m}''_{w'}$ , temperature *T*, and ablating species  $Y_{gs}$  are imposed. The surface energy balance equation does not need to be solved in the present analysis.

Once values are computed for the primitive variables, the conservative quantities in the ghost cells of the boundary are set such that the flux across the wall is the required blowing flux. This blowing boundary condition has been tested over a wide range of blowing rates, assuring the robustness of the implementation. Following the same methodology for the verification and validation of NASA Ames's DPLR code [36] and NASA Langley's LAURA code



e) High concentration species

f) Low concentration species

Fig. 3 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 81 km (34 s into reentry).

[37], the blowing boundary of LeMANS has also been verified and validated [7,38]. More details on these relations are provided in Ref. [39].

### IV. Test Case: Stardust Return Capsule Reentry Trajectory

#### A. Problem Description

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To evaluate and validate the model in LeMANS, the forebody of the Stardust Return Capsule is modeled during the first 10 s of its reentry in the continuum regime [40]. These reentry points are chosen because they also correspond to the period where spectral emission data were measured by the echelle instrument [41]. The echelle instrument is a miniature echelle spectrograph that operates at very high resolution of 0.14–0.9 nm, over the range of 360 to 880 nm. The instrument was installed onboard [41] a NASA observation airplane and was used to record emission spectroscopy of the reentry of the Stardust Return Capsule.

The geometry and mesh are presented in Fig. 1, and the flow and surface parameters in Tables 1 and 2, respectively. The flow field is computed with the previously defined 38 species chemistry model, with reaction rates listed in Ref. [13].



e) High concentration species

f) Low concentration species

Fig. 4 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 78.5 km (36 s into reentry).

The values used for the surface temperature, blowing rates, and gas composition are listed in Table 2. The data were obtained through an uncoupled approach, using a combination of NASA codes, and are explained in great detail in Refs. [11,12]. In this approach, the surface balance equations are solved from the material response side and provide the temperature at the wall and gas composition at the wall.

The values obtained through this procedure are only calculated at the stagnation point and are expected to be significantly lower elsewhere on the forebody of the vehicle. To reflect this, a temperature profile is obtained using a fully radiative equilibrium boundary condition at the wall, without ablation. The surface temperature profile is then normalized and reapplied for the ablating wall simulation via multiplication by the surface temperature at the stagnation point that is listed in Table 2. This method has been proven to give a good estimate of the surface conditions [40]. For the blowing rate, a linear relation between the temperature and the mass flux is derived using the second and third columns of Table 2 and applied proportionally



e) High concentration species

f) Low concentration species

Fig. 5 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 76 km (38 s into reentry).

using the normalized surface temperature profile. For stability reason, when solving the momentum and mass balance equations, the mass flux goes to zero when the surface temperature goes below 2650 K. The values for those two parameters are presented in Fig. 2.

#### B. Results

The stagnation line temperatures and gas composition as well as the heat flux components are presented in Figs. 3–8. Overall, for this particular trajectory, condition, and material, the various species behave in the same manners and are present along the same distance proportionally to the location of the shock. Most of the blowing species are destroyed almost immediately once they enter the flow, although CO and OH remain in relatively high concentration. These two species are important because they are strong radiators. Atomic species H and C are created in high concentration near the boundary, as are CN and CN<sup>+</sup>, which are also quite important due to their



e) High concentration species

f) Low concentration species

Fig. 6 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 73.5 km (40 s into reentry).

radiative properties. As noted previously [12,14,15], the concentration of HNO, a species neglected in other models, is relatively high.

The 71 km trajectory point is examined more closely. The Mach number over the whole computational is plotted on Fig. 9. On this figure, the shock can be clearly seen. The number density of the species identified as important in Fig. 7 are plotted over the domain in Figs. 10–12. In Fig. 10, it is interesting to notice that H and C remain at a fairly high concentration throughout the entire shock layer. As for HNO and NH, they are both essentially created in the shock region and are present in substantial concentration. Both of these species were previously neglected in other carbon-phenolic-in-air chemistry models. The distribution of the CO and CN species are presented in Fig. 11. As can be seen, both CO and CN do not ionize near the stagnation region but do inonize farther along the body of the vehicle. This is an important observation because this ionization translates to a reduction of the CN/CO concentration along the body, which is likely to affect the comparison to the echelle measurements (as seen in the next subsection). Finally, Fig. 12 presents the electron distribution as well as the C<sup>+</sup> distribution. As with the other species, ionized C



e) High concentration species

f) Low concentration species

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Fig. 7 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 71 km (42 s into reentry).

reaches its greatest concentration along the body, but not in the stagnation region, as is the case with  $O^+$  and  $N^+$ . The overall ion distribution can be evaluated by looking at the distribution of electrons. It is noted that  $H^+$ , the only ion not presented in these graphs, only exists with a negligible concentration.

#### 1. Heat Flux Reduction

To evaluate the heat flux reduction caused by the blowing of pyrolysis species from the surface, two additional series of test cases are run for the echelle trajectory points. The first series uses a noncatalytic boundary condition, and the second uses a super catalytic one. Because a non-catalytic wall is known to underestimate the heat flux, and the super catalytic wall is known to overestimate, those two models provide a good starting point for comparisons. In both cases, an 11-species air chemistry model is used. The imposed surface temperature is the one listed in Table 2.

First, the blowing effect on the total surface heat flux is assessed by comparing the blowing boundary results to the super catalytic



Fig. 8 Stagnation line temperature, surface heat fluxes, and species concentrations along the stagnation line for the Stardust reentry vehicle at an altitude of 68.9 km (44 s into reentry).



Fig. 9 Mach-number isolines for the Stardust vehicle at 71 km into reentry (42 s).



Fig. 10 Mole fraction isolines for some the species for the Stardust vehicle at 71 km into reentry (42 s).

and non-catalytic ones for three of the trajectory points (81, 76, and 68.9 km). The total heat flux is defined as the sum of translational–rotational heat flux, vibrational–electronic–electron heat flux, and diffusion heat flux:  $q_{tr}$ ,  $q_{ve}$ , and  $h^T J$ , respectively, from Eq. (3). The comparison is presented in Fig. 13; as expected, the heat flux for the blowing boundary condition is smaller than the non-catalytic heat flux, which is usually regarded as the lower bound when no ablation is present.

To understand the effects of the heat flux reduction, it is more suitable to look at the individual components of the heat flux one by one. Figure 14 presents the translational–rotational heat flux at the wall. Although the super-catalytic boundary condition provides a larger total heat flux (Fig. 13), the changes in composition of the boundary layer result in a significant reduction of the translational–rotational component. The same analysis can be performed on the vibrational–electron–electronic component of the heat fluxes (Fig. 15). As with  $T_{\rm tr}$ , the changes in the chemical composition of the boundary layer result in a generalized reduction in the heat flux. However, the effects are not as straightforward as for the other conductive heat flux because the amount of species with vibrational (and electronic) degrees of freedom has a direct impact on the energy distribution.

The heat fluxes due to mass diffusion are shown in Fig. 16. As expected, the super-catalytic wall results in an artificially high heat flux, and those values are significantly reduced when a blowing boundary condition is applied. That figure also shows that the reduction in the translational–rotational heat fluxes is directly proportional



Fig. 11 Mole fraction isolines for some the species for the Stardust vehicle at 71 km into reentry (42 s).



Fig. 12 Mole fraction isolines for some the species for the Stardust vehicle at 71 km into reentry (42 s).











to the mass diffusion heat flux. By also comparing with Fig. 2b, it can be seen that the mass diffusion heat flux is directly proportional to the pyrolysis gas mass flow.

Finally, in Fig. 17, the relative contributions of each component of the heat flux are plotted for all trajectory points. It can be seen that, for the trajectory points chosen for this analysis, the translationalrotational component contributes the most. We can also observe that the amount of blowing has a direct and linear influence on the translational-rotational heat flux. This result clearly shows that an increase in blowing rates has a major impact on the overall heat flux and that, although it translates into an increase in mass diffusion heat flux, it does not become the dominant component.

Next, the effects of ablation blowing on translational-rotational energy are examined. Figures 18-20 present the translationalrotational temperature, the vibrational-electronic-electron temperature, and the pressure on the stagnation line, respectively. As can be seen in Fig. 20, the first notable effect of blowing is the displacement of the shock. Even at low blowing rates (81 km), the shock is significantly moved away from the surface of the vehicle. This has, of course, a direct repercussion on the shape of the temperature curves and therefore affects the gradient of temperature at the wall, as can be seen in Fig. 18 and 19. However, even if the heat flux is directly linked to the gradient of temperature at the wall [see Eq. (4)], the gas-phase thermal conductivity also plays an important role. It is for that reason that the results show no direct correlation with the steepness of the gradient and the heat flux. The steepest curves shown in Fig. 18 are the ones associated with super-catalytic boundary condition; however, as can be seen in Fig. 14, the higher translational-rotational heat fluxes are the ones associated with the non-catalytic boundary condition. It therefore appears that, regardless of the altitude, blowing rate, and chemical species, the most important effect that contributes to heat flux reduction is most likely the composition of the gas in the boundary layer.

#### 2. Radiative Emission

Certain species present in the boundary layer are strong radiative emitters and are expected to significantly contribute to the overall radiative heat flux at the surface. For the Stardust reentry vehicle, the contribution of the radiative heat flux to the overall heat flux has been evaluated, at maximum intensity, to be approximately 10% [40].







b) Reentry altitude of 76 km













A radiative emission calculation is performed using the flow field solution of the 42 s trajectory point (71 km), with the NEQAIR 12 (version 7) [16] non-equilibrium radiation code. Apart from the usual air species, radiative emission from the CN violet and CN red systems is included (see Table 3).

The temperatures and species concentrations used as inputs to NEQAIR are presented in Figs. 21 and 22. Because the echelle data have no spatial resolution, the computed spectra need to be spatially averaged over the front surface using multiple lines parallel to the symmetry line. The lines used are located at r = 0, 0.20, 0.30, and0.42 m. The last line does not intersect with the surface, which explains why the temperatures are not at equilibrium on the righthand side of Fig. 22c and why Fig. 22d does not have the same general behavior as the other density plots.

From the density plots presented in Figs. 21 and 22, it is interesting to note that CN<sup>+</sup> plays a more significant role in the determination of the species concentrations than was previously thought. It is created at the cost of CN and therefore reduces the CN concentration by up to



Fig. 20 Blowing effects on stagnation line pressure.

two orders of magnitude in a region where the vibrational–electron– electronic temperature is high. The same cannot be said about CO<sup>+</sup> because nowhere in the flow is that molecule present in quantities that approach the concentration of CO.

A comparison of the spectral emission from CN is presented in Fig. 23. To assess the importance of kinetic rates on radiation modeling, three different flow field simulations are used. The first one (labeled "Andersson") is considered the baseline and uses the

Table 3 Emission mechanisms considered for the radiative heat flux, excluding the air species

Species	Mechanism (electronic state transition)	Spectral range, nm
CN	Violet $(B^1\Sigma - X^1\Sigma)$	230-462
CO	$4 + (A^1\Pi - X^1\Sigma)$	110-385
C <sub>2</sub>	Swan $(d^3\Pi - a^4\Pi)$	319-806

462



a) Temperatures (r = 0.00 m)



c) Temperatures (r = 0.20 m)



0.05

0.06

0.07

0.08

0.03

Fig. 21 Temperatures and radiating species concentrations along the first two of four parallel lines for the Stardust vehicle at 42 s into reentry (71 km). Park's rate is used for the CN/CO exchange reaction.

10<sup>22</sup>

10<sup>21</sup> 10<sup>20</sup>

10<sup>19</sup>

10<sup>18</sup>

10<sup>17</sup>

10<sup>16</sup>

10<sup>15</sup> 10<sup>14</sup>

0.02

Number density [m<sup>-3</sup>]

CN CN⁺ CO



c) Temperatures (r = 0.42 m)

d) Radiating species from ablation (r = 0.42 m)

Fig. 22 Temperatures and radiating species concentrations along the last two of four parallel lines for the Stardust vehicle at 42 s into reentry (71 km). Park's rate is used for the CN/CO exchange reaction.



b) Radiating species from ablation (r = 0.0 m)





Fig. 23 Comparison of the CN spectral line for the Stardust reentry vehicle at 42 s (71 km).

chemistry model detailed in Refs. [12,14]. The second one (labeled "Park") uses the kinetic rates of Ref. [42] that were devised for Mars reentry and therefore tailored for high temperature. The last one, labeled "All Andersson" uses all of the kinetics rates of the CN/ NO reduced model presented in Ref. [43].

It can be seen in that figure that the spectral computations match the echelle data remarkably well because the values are all within the same order of magnitude. Considering all the assumptions that are made throughout the modeling process and the uncertainties related to the conditions of the acquisition of the experimental data, an agreement such as this one exceeds expectations. The Park kinetic model appears to give better results than both of the Andersson models. However, all results are relatively close to the experimental data, and when one factors in all the assumptions that are made during the entire modeling process, no definitive recommendation can be made as to which rates to use. The interesting part, however, is that there are some noticeable differences in the predicted CN spectral intensity when the CN/CO exchange reaction is modified.

Finally, the radiative heat flux was computed for the three cases. For all three sets of reaction rates, the total radiative flux is approximately 1% of the convective heat flux, making it negligible at this trajectory point. What is more important to acknowledge, however, is that a large portion (30-40%) of the radiative heat flux is generated by CN over the wavelength range of the echelle instrument (about 360 to 890 nm).

As additional results, and in an attempt to validate the current methodology, the spectral line emissions for CN are compared to the experimental data obtained by the echelle instrument [41] at high altitude (81 km) and lower altitude (71 km). The radiative emission calculation is again performed along the stagnation line of a converged flow field solution using NEQAIR. The temperatures and species concentrations used as inputs NEQAIR are presented in Figs. 3 and 7, and the spectral emissions are presented in Fig. 24. As was previously reported, the lower-altitude trajectory point reasonably matches the experimental data because the discrepancy remains within one order of magnitude. As seen in [15], the difference would be even less if a spatially resolved input was used in NEOAIR instead of simply the stagnation line. The high-altitude trajectory point (81 km) gives an even better comparison. For those two results, the CN calculation was run independently of the air calculations.

#### V. Conclusions

To evaluate the mechanism of heat flux reduction caused by pyrolysis gas blowing, a comprehensive chemistry model for computing the flow around a reentry vehicle using an ablative heat shield has been used in a CFD code. The species used in the model have been selected with careful consideration of the flow physics, and the reactions have been evaluated and chosen from various sources in the literature. The model has been reduced to a more manageable number of species and reactions, using a zero-dimensional sensitivity analysis, and was validated using various experimental results.

The CFD software used to model the flow field is the hypersonic non-equilibrium code LeMANS, which was adequately modified to allow flow through the surface of the vehicle. As a test case, the Stardust reentry vehicle was used. This vehicle has been extensively studied in the past and is relatively simple to model. The first six trajectory points corresponding to the continuum regime were chosen because experimental data is available in the form of spectral radiative emission gathered by the echelle instrument [41].

As expected, the convective heat flux predicted using the carbonphenolic-in-air chemistry model was significantly reduced relative to the prediction obtained using a non-blowing air chemistry model. The species concentrations along the stagnation line were also presented, and it was shown that, at chemical equilibrium conditions, most species blown from the surface immediately react in the flow field and are transformed. These results clearly indicate the need to use an appropriate chemistry model in the flow field and that the chemistry model should be significantly different from that used to model pyrolysis gas behavior inside the TPS. Also, it was observed that the blowing rates were directly proportional to the mass diffusion



a) 81 km: 34s into reentry

Fig. 24 Spectral emission for the Startdust reentry vehicle at 81 and 71 km.

heat flux, which in turn was directly proportional to the reduction of the translational–rotational conduction heat flux component. It was also noted that the main source of heat flux reduction for all trajectory points is the translational–rotational conduction component. This clearly indicates that the chemical composition of the boundary layer is of great importance and that the diffusion coefficients of each species, as well as the mixing rules, must be calculated with great care.

Finally, the flow field solution was used to perform analysis of the CN radiative spectral emission using NEQAIR. The result was compared to the experimental data obtained by the echelle instrument [41] at the 81 and 71 km trajectory points. The computed results were very close to the observed values, which provides increased confidence in the carbon-phenolic-in-air chemistry model and the overall approach.

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