

Improving surface tidal accuracy through two-way nesting in a global ocean model

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ABSTRACT

In global ocean simulations, forward (non-data-assimilative) tide models generally feature large sea-surface-height errors near Hudson Strait in the North Atlantic Ocean with respect to altimetry-constrained tidal solutions. These errors may be associated with tidal resonances that are not well resolved by the complex coastal-shelf bathymetry in low-resolution simulations. An online two-way nesting framework has been implemented to improve global surface tides in the HYbrid Coordinate Ocean Model (HYCOM). In this framework, a high-resolution child domain, covering Hudson Strait, is coupled with a relatively low-resolution parent domain for computational efficiency. Data such as barotropic pressure and velocity are exchanged between the child and parent domains with the external coupler OASIS3-MCT. The developed nesting framework is validated with semi-idealized basin-scale model simulations. The M_2 sea-surface heights show very good accuracy in the one-way and two-way nesting simulations in Hudson Strait, where large tidal elevations are observed. In addition, the mass and tidal energy flux are not adversely impacted at the nesting boundaries in the semi-idealized simulations. In a next step, the nesting framework is applied to a realistic global tide simulation. In this simulation, the resolution of the child domain ($1/75^\circ$) is three times as fine as that of the parent domain ($1/25^\circ$). The M_2 sea-surface-height root-mean-square errors with tide gauge data and the altimetry-constrained global FES2014 and TPX09-atlas tidal solutions are evaluated for the nesting and no-nesting solutions. The better resolved coastal bathymetry and the finer grid in the child domain improve the local tides in Hudson Strait and Bay, and the back-effect of the coastal tides induces an improvement of the barotropic tides in the open ocean of the Atlantic.

1. Introduction

Global surface tides have been studied in barotropic (two-dimensional) and baroclinic (three-dimensional) forward and data-assimilative simulations (Arbic et al., 2004; Arbic et al., 2009; Buijsman et al., 2015; Egbert and Ray, 2001; Egbert et al., 2004; Green and Nycander, 2013; Ngodock et al., 2016; Shriver et al., 2012; Stammer et al., 2014). Despite recent progress in reducing tidal sea-surface-height root-mean-square errors (RMSE) in the global HYbrid Coordinate Ocean Model (HYCOM), the model used in this paper, the errors in the North Atlantic near Hudson Strait, and near coastal-shelf areas in general, are still relatively large (Buijsman et al., 2015; Ngodock et al., 2016; Shriver et al., 2012). Coastal-shelf bathymetry is imperfectly known and represented in models, and may be a likely

cause of tidal model errors (Egbert et al., 2004). Moreover, the large errors in the North Atlantic may be attributed to the inability of the model to correctly simulate the known semidiurnal tidal resonances in the North Atlantic (Wünsch, 1972).

Both analytical models of coastal tides (e.g. the classic quarter-wavelength resonance model, see for instance Defant, 1961) and more realistic numerical models of coastal tides have long treated the open ocean as representing an unchanging boundary condition acting on a coastal region that may or may not achieve resonance depending on its geometry. However, in analytical and numerical studies, Arbic et al. (2009), Arbic et al. (2007), and Arbic and Garrett (2010) have shown that there is a substantial “back-effect” of coastal tides upon the open-ocean tides. They showed that if both the shelf sea and ocean basin are near resonance, small geometry changes to the shelf sea can have a

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large impact on the open-ocean tides. This suggests that if we better resolve the coastal geometry by increasing the model resolution, we may not only improve the coastal tides, but also the open-ocean tides through the back-effect, in particular if the shelf and ocean basins are near resonance, as is the case in the North Atlantic near Hudson Strait.

In general, higher resolution yields more accurate tides in forward models (Egbert et al., 2004). However, high-resolution model simulations are computationally expensive and require large data storage. To achieve higher resolution in regions of interest without dramatically increasing the cost of a basin- or global-scale model, one can use two-way nesting, as introduced in Spall and Holland (1991). The basic idea of two-way nesting is to apply a high-resolution (fine) grid only to a small area of interest, i.e., the ‘child’ domain, and a low-resolution (coarse) grid to the entire ‘parent’ domain. In two-way nesting, information is allowed to propagate from the coarse grid to the fine grid and vice versa. In this way, the improved solution on the child grid may also improve the solution on the parent grid. In this paper, we implement a two-way nesting framework for barotropic HYCOM simulations to better simulate the local surface tides, e.g. on Hudson shelf, as well as the remote tides in the open ocean.

In the two-way nesting framework, the data exchange between the child and parent domains occurs in two opposing directions. In the first ‘coarse-to-fine’ direction, the information of the parent domain is transferred to the child domain via the lateral boundaries of the child domain. Data exchange in this direction is also referred to as ‘one-way nesting’. In one-way nesting, the parent domain is not updated with the child grid solution. One-way nesting has been extensively used for basin-scale modeling (Chassignet et al., 2007; Hogan and Hurlburt, 2006; Mason et al., 2010; Penven et al., 2006). In the second ‘fine-to-coarse’ direction, the coupling variables in the high-resolution child domain are transferred to the relatively low-resolution parent grid. The two-way nesting approach has been widely applied in atmospheric modeling (Bowden et al., 2012; Lorenz and Jacob, 2005), and in coupling of multiple climate models (Lam et al., 2009; Ličer et al., 2016; Wahle et al., 2017) as well as ocean modeling (Barth et al., 2005; Debreu et al., 2012; Ginis et al., 1998). To make the updated variables continuous across the nesting boundaries of the parent and child domains in the second direction, smoothing filters were sometimes applied to physical variables, and/or the bottom topography of the child domain was relaxed with that of the parent domain (Debreu et al., 2012; Fox and Maskell, 1995; Ginis et al., 1998; Mason et al., 2010). The artifacts at the nesting boundary are amplified when the grid-resolution ratio of the child and parent domains increases (Spall and Holland, 1991). In this study, barotropic pressure, velocity, and bottom topography are linearly relaxed near the boundary of the child domain to allow for a smooth transition of these data between the child and parent domains, which the grid-resolution ratio is three.

The two-way nesting approaches can be classified into two categories: (i) internal, and (ii) external coupling. In internal coupling, a nesting framework is included in the source code of ocean models (Barth et al., 2005; Debreu and Blayo, 2008; Haley Jr. and Lermusiaux, 2010; Herrnstein et al., 2005; Santilli and Scotti, 2015; Tang et al., 2014). This approach requires more complicated nesting algorithms than a single resolution (no-nesting) case. In external coupling, a separate coupler facilitates the communication between numerical models. The main advantage of using such a coupler is that the modification of the source code of these models is minimal. It is only necessary that the Application Programming Interface (API) of the coupler be built into the existing source codes. In addition, external couplers provide a wide variety of interpolation schemes and efficient search algorithms that can be used to calculate interpolation (remapping) coefficients. The data that are transferred between coupled models need to be interpolated for use in the destination domain because the grid cells in the destination domain may not be located at the same coordinates as the grid cells in the source domain. Several external couplers have been developed and applied (Valcke et al., 2012). The Earth

System Modeling Framework (ESMF) can be used to couple multiple domains with different resolutions (Qi et al., 2018). In recent research, the AGRIF and OASIS3-MCT coupling toolkits have been widely applied. The AGRIF (Adaptive Grid Refinement In Fortran) coupler has been used to couple ocean circulation models (Debreu et al., 2012; Penven et al., 2006; Urrego-Blanco et al., 2016). The OASIS3-MCT coupler (Valcke et al., 2015) has been used to couple climate models (Juricke et al., 2014; Ličer et al., 2016; Wahle et al., 2017; Will et al., 2017). OASIS3-MCT is an integrated version of OASIS3 (Ocean Atmosphere Sea Ice and Soil) by CERFACS in France and MCT (Model Coupling Toolkit) by the Argonne National laboratory in USA. We utilize OASIS3-MCT as a coupler for the HYCOM to HYCOM two-way nesting because its partition option, grid and mask, and parallel computing by Message Passing Interface (MPI) are more compatible with HYCOM as compared to AGRIF. Scientists at the Service Hydrographique et Océanographique de la Marine (SHOM; Brest, France) applied AGRIF to facilitate the HYCOM to HYCOM coupling, but found it hard to maintain as the HYCOM code was updated (personal communication with Remy Baraille, 2015).

HYCOM provides reliable results as a multi-layer global ocean circulation model and contributes to the United States Navy’s operation (Arbic et al., 2010; Chassignet et al., 2007; Metzger et al., 2010; Ngodock et al., 2016; Shriver et al., 2012). The forward barotropic tide simulations (single layer), used in this paper, employ astronomical tidal forcing, a spatially-varying self-attraction and loading (SAL) term, a linear topographic wave drag (Buijsman et al., 2015), and an atmospheric mean sea level pressure forcing, which modulates the S_2 tide and is obtained from the atmospheric NAVGEM (NAVY Global Environmental Model; Hogan et al., 2014). HYCOM is also capable of improving basin-scale modeling with offline one-way nesting (Chassignet et al., 2007; Hogan and Hurlburt, 2006). However, the offline one-way nesting in HYCOM has some drawbacks. First, it requires additional data storage for nesting data, whose size increases proportionally to the resolution of the computational domain. Second, global-scale modeling on the parent grid must be performed in advance of regional/basin-scale modeling on the child grid to provide boundary conditions for the child domain. Third, offline one-way nesting is useful only for improving the solution in the child domain, while the parent domain does not receive any feedback from the child domain. An *online* two-way nesting framework is able to resolve these issues and improve the accuracy in HYCOM for both regional/basin- and global-scale modeling. The most complicated issue in applying OASIS3-MCT to HYCOM is how to deal with barotropic time stepping in conjunction with the baroclinic time steps that are based on the second-order leapfrog scheme. This study synchronizes nesting variables at the barotropic time steps of the parent domain without any other treatments (Santilli and Scotti, 2015; Urrego-Blanco et al., 2016), and stores them so that they can be used at the next baroclinic time level.

In this study, the improvement through two-way nesting is evaluated and validated by comparing the nesting results to tide gauge data and the TPXO9-atlas and FES2014 global tidal solutions. TPXO9-atlas (volkov.oce.orst.edu/tides/tpxo9_atlas.html) is an altimetry-constrained tidal solution (Egbert and Erofeeva, 2002). FES2014 (<https://www.avisio.altimetry.fr/>) is the latest global solution of the FES (Finite Element Solutions) model, which is constrained with altimetry and tide gauge data (Carrère et al., 2015). Stammer et al. (2014) compared the numerical results of forward and data-assimilative tide models to the tide gauge data separately in the deep ocean, shelf sea, and coastal regions. According to Stammer et al. (2014), TPXO8-atlas (the previous version of TPXO9-atlas) is more accurate in the deep ocean than FES2012 (the previous version of FES2014), whereas TPXO8-atlas has larger root-mean-square errors with the tide gauge data in the shelf seas than FES2012. The FES2014 tidal solution has improved its tidal accuracy compared to its previous versions (Cancet et al., 2018), and so has TPXO9-atlas. Hence, we compare the two-way nesting results to both the TPXO9-atlas and FES2014 solutions, as well as to the tide gauge data of

Stammer et al. (2014).

This paper is organized as follows. The online two-way nesting framework in HYCOM is described in Section 2. The developed nesting framework is validated with semi-idealized basin-scale simulations in Section 3. The framework is then applied to a realistic global-scale simulation and validated against tide gauge data, FES2014, and TPXO9-atlas in Section 4. Finally, we end with a discussion and conclusions in Section 5.

2. Methodology: OASIS3-MCT in HYCOM

2.1. Data exchange in HYCOM

In solving the layer-integrated nonlinear momentum equations, HYCOM uses a split-explicit time-stepping scheme that separates the fast barotropic mode (single layer) from the slow baroclinic modes (multiple layers) for numerical efficiency (Bleck and Smith, 1990). In barotropic HYCOM simulations, as in this paper, this split-explicit time-stepping scheme is still used. In this case, HYCOM performs the calculations over two layers: a surface layer with a varying thickness and a bottom layer with a zero thickness. Hence, we need to prescribe a barotropic time step (Δt_T) and a baroclinic time step (Δt_C). Since barotropic waves have larger phase speeds than baroclinic waves, the barotropic time step is much smaller than the baroclinic time step. The split-explicit scheme is computationally efficient because the two-dimensional calculations occur on the fast time step and the more elaborate three-dimensional calculations occur on the longer time step. An example of the barotropic and baroclinic time stepping is shown in Fig. 1 for both the parent and child domains. Time is integrated with the second-order leapfrog scheme for the baroclinic mode, and with a combination of the first-order forward and backward Euler schemes for the barotropic mode (Bleck and Smith, 1990). The leapfrog scheme is a two-step method that uses two baroclinic time steps of $(t - \Delta t_C)$ and t to evaluate the values at $(t + \Delta t_C)$ where t denotes a certain simulation time. This means that one of two baroclinic time steps is overlapped every baroclinic calculation (Fig. 1). In this study, the data of the second baroclinic time step of the previous simulation time (t) are stored in memory, and the saved data are used in the first baroclinic time step of the next simulation time ($t + \Delta t_C$). This method, in which the stored data for one baroclinic time step is used, is more efficient than exchanging data from $(t - \Delta t_C)$ and $(t + \Delta t_C)$ every simulation time.

In general, the baroclinic and the barotropic time steps of a parent

domain ($\Delta t_{C,1}$ and $\Delta t_{T,1}$) are different from those of a child domain ($\Delta t_{C,2}$ and $\Delta t_{T,2}$) because the stable time step for a fine grid is smaller than that for a coarse grid based on the CFL (Courant-Friedrichs-Lewy) condition (Figs. 1 and 2). As shown in Fig. 2, the barotropic longitudinal and latitudinal velocities, and the barotropic pressure are transferred in the first *coarse-to-fine* direction before solving the continuity equation, and in the second *fine-to-coarse* direction after computing the momentum equations. In HYCOM, two barotropic time steps are calculated in a pair to improve the numerical stability in calculating the momentum equations with the Coriolis force (Bleck and Smith, 1990). The child domain can receive data every barotropic time step from the parent domain ($\Delta t_{T,2}$), but no data are sent from the parent domain in the case that the barotropic time steps of the parent and the child domains do not coincide. In Figs. 1 and 2, for example, the barotropic ($\Delta t_{T,1}$) and the baroclinic ($\Delta t_{C,1}$) time steps of the parent domain are twice as large as those ($\Delta t_{C,2}$ and $\Delta t_{T,2}$) of the child domain. In this case, data are exchanged in both directions every other barotropic time step of the child domain as the nesting time step (Δt_{NT}). This means that the nesting variables are synchronized at the end of the barotropic time step of the parent domain ($\Delta t_{NT} = \Delta t_{T,1} = 2\Delta t_{T,2}$).

The data from the parent domain are used as a lateral boundary condition for the child domain in the first direction. However, the difference in grid resolution between the two domains may create discontinuities in the topography along the domain boundaries. To prevent this, it is necessary to match the topography of the parent domain with that of the child domain along the boundary of the child domain. As shown in Fig. 3a, the bottom topography of the child domain is divided into three zones. The outermost zone (width: N_B) uses the low-resolution bottom topography that is the same as that of the parent domain while the innermost zone uses the high-resolution bottom topography. The smoothing zone in the middle merges the low- and high-resolution topographies as

$$\phi = \gamma_R \cdot \phi_{\text{child}} + (1.0 - \gamma_R) \cdot \phi_{\text{parent}} \quad (1)$$

where ϕ is the bottom topography, and γ_R is the relaxation factor that is linearly evaluated by

$$\gamma_R = \min \left(\frac{x_{R,l}}{N_{R,l}} \right), \quad l = \{N, S, E, \text{ or } W\} \quad (2)$$

where $N_{R,l}$ is the number of cells in the width of the smoothing zone, and $x_{R,l}$ is the cell number as counted from the outer north, south, east,

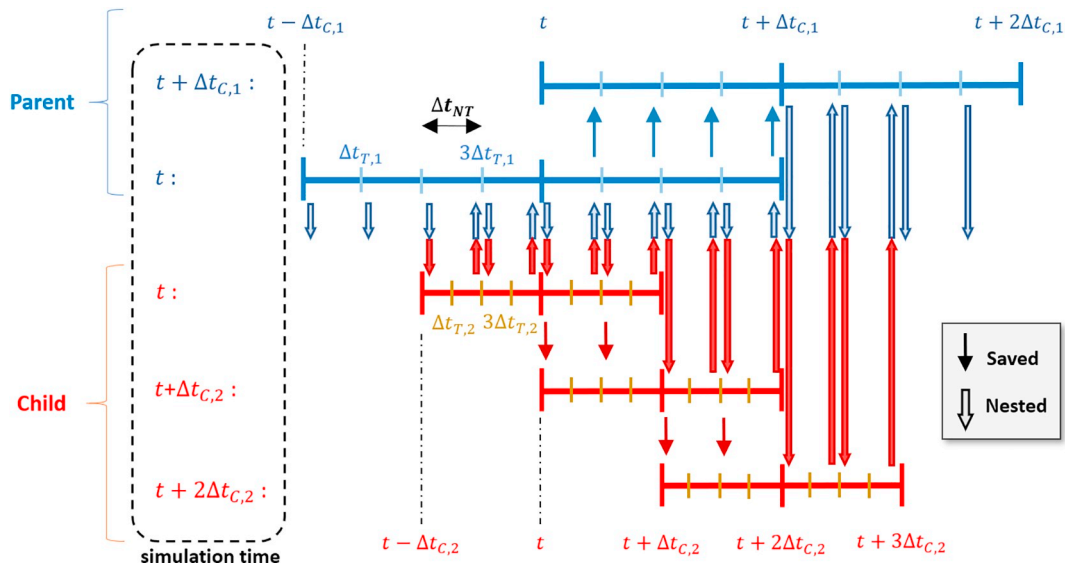


Fig. 1. The split-explicit time stepping scheme for both the parent and child domains. The barotropic and baroclinic time steps are Δt_T and Δt_C , respectively. Data are exchanged at the nesting time step (Δt_{NT}).

Table 1
Base grids of data exchange on the HYCOM C-grid for OASIS3-MCT remapping files (\mathcal{P} : p -grid, \mathcal{U} : u -grid, and \mathcal{V} : v -grid).

No.	Variable name	Parent	Direction	Child
First direction: parent (coarse) → child (fine)				
1	Barotropic pressure	\mathcal{P}	→	\mathcal{P}
2	Barotropic u -velocity	\mathcal{U}	→	\mathcal{U}
3	Barotropic v -velocity	\mathcal{V}	→	\mathcal{V}
Second direction: child (fine) → parent (coarse)				
1	Barotropic pressure	\mathcal{P}	←	\mathcal{P}
2	Barotropic u -velocity	\mathcal{U}	←	\mathcal{U}
3	Barotropic v -velocity	\mathcal{V}	←	\mathcal{V}

In computing the remapping coefficients, OASIS3-MCT searches the entire parent grid, which may take a long time. Will et al. (2017) suggested that the masks of the ocean cells located outside the child domain be modified into land in the second direction. If the target point is a land cell, this calculation is skipped in OASIS3-MCT, reducing the computing time for the remapping coefficients. In this study, the approach by Will et al. (2017) is applied to both the first and the second directions. In the first direction, we not only modify most of the child domain into land cells except for the boundary cells, but also set limits to the search algorithm. Since the data coming from the parent domain are used as the boundary condition for the child domain, only boundary ocean cells in the child domain require data in the first direction. As shown in Fig. 4a, a specific number of boundary cells (green, 5 cells from the boundary) are active while the other inner ocean cells in the child domain (white) are changed to land cells. In order to calculate remapping coefficients for a target point in the destination (child) domain, OASIS3-MCT searches for four surrounding points of each target point in the source (parent) domain. Instead of including all the parent grid points in the search, we limit the search to a small area (light blue box) around the ocean cell in the parent domain corresponding to the target point in the child domain (Fig. 4a). In this study, the search box has 20 grid points in the parent domain in both longitudinal and latitudinal directions. This box follows the target point in the child domain as it moves eastward or northward. The efficiency of this approach is shown in Table 2. Three regions (ARC, HUD, and GLB), which are used in Sections 3 and 4, are involved in the calculation. The modified approach significantly reduces the computing time by at least an order of magnitude as compared to the original method.

In the second direction, only ocean cells that are located inside the child region are updated in the parent domain. As illustrated in Fig. 4b, the remapping coefficients for the target points that are located outside the child region are not necessary in two-way nesting. By modifying the masks of the ocean cells outside the child area into land cells, the computing time of creating the remapping files for the second direction

Table 2
Wall-clock time for the one-time calculation of remapping files for the first direction for the ARC, HUD, and GLB configurations.

Number of cells		Computing time	
Parent	Child	Original	Modified
3200 × 5040 (ARC)	658 × 1015 (HUDa)	4.07 h	12.12 min
3200 × 5040 (ARC)	1975 × 3046 (HUDb)	2.06 d	1.62 h
9000 × 7055 (GLB)	1975 × 3046 (HUDb)	10.02 d	1.82 h

Table 3
Wall-clock time for computing remapping files for the second direction for the ARC, HUD, and GLB configurations.

Number of cells		Computing time	
Parent	Child	Original	Modified
3200 × 5040 (ARC)	658 × 1015 (HUDa)	7.76 d	12.59 min
3200 × 5040 (ARC)	1975 × 3046 (HUDb)	75.3 d	1.72 h
9000 × 7055 (GLB)	1975 × 3046 (HUDb)	> 200 d	2.23 h

significantly decreases by several orders of magnitude as shown in Table 3.

3. Validation of the nesting framework

The developed nesting framework is validated with six semi-idealized model simulations. Experiments 1–2 concern one-way nesting and Experiments 3–6 concern two-way nesting. The parent and child grid resolutions are the same in Experiments 1–4, while they differ in Experiments 5–6. Experiment pairs 1–2, 3–4, and 5–6 concern the sensitivity to equal and different time steps on the parent and child grids. The grid resolutions and time steps of the parent and child domains in Experiment 6 are the same as those of the global experiment, discussed in the next section. The specifications of Experiments 1–6 are presented in Tables 4 and 5.

The HUD child domain, covering Hudson Strait, and the ARC parent domain are shown in Fig. 5. The parent domain covers the Arctic and the North Atlantic Oceans rather than the entire global ocean for computational efficiency. For Experiments 1–4, the grid resolution of both the child and parent domains is $1/25^\circ$. To ensure the child grid is identical to the parent grid in Experiments 1–4, the child domain is extracted from the parent domain (Fig. 6a). For Experiments 5 and 6, the child grid has a resolution of $1/75^\circ$, which is three times as fine as the parent grid (Fig. 6b). In case that the refinement ratio between parent and child domains is odd, the interpolation error is reduced because the grid points on the p -, u -, and v -grids of the parent domain

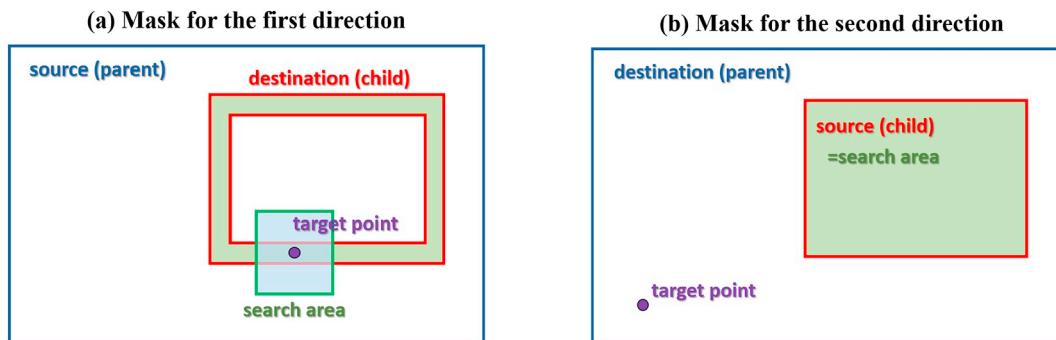


Fig. 4. Masks for computing remapping coefficients. (a) In the first direction, the calculation in the child domain (destination) is limited to a small green area along its boundary, and the search for four neighboring points of a target point in the parent domain (source) is limited to the blue box. (b) In the second direction, the computation is limited to parent grid cells located inside the child region (green), and all parent grid cells outside the child domain are masked as land (white). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 4
Specifications of the child and parent domains for the semi-idealized model experiments.

	Child (HUD)		Parent (ARC)
Experiment number	1–4	5–6	1–6
Grid resolution (°)	1/25	1/75	1/25
Number of cells	658 × 1015	1975 × 3046	3200 × 5040
Number of MPI Processes	128	128	320
OASIS3-MCT interpolation	Bi-linear	Bi-linear	Bi-linear

Table 5
Time steps and excluding zones for the six semi-idealized experiments.

		Experiments					
		Exp. 1	Exp. 2	Exp. 3	Exp. 4	Exp. 5	Exp. 6
		Nesting					
		One way		Two way			
Parent	$\Delta t_T, 1(s)$	3.0		3.0	3.0	1.0	3.0
	$\Delta t_C, 1(s)$	60.0		60.0	60.0	20.0	60.0
	$\Delta t_{NT}(s)$	3.0		3.0	3.0	1.0	3.0
Child	$\Delta t_T, 2(s)$	3.0	1.0	3.0	1.0	1.0	1.0
	$\Delta t_C, 2(s)$	60.0	20.0	60.0	20.0	20.0	20.0
	N_n (cells)	5	5	10	10	10	10
	N_s (cells)	5	10	10	10	10	10
	N_e (cells)	5	10	10	10	10	10
	N_w (cells)	5	5	10	10	10	10
	N_R (cells)	N/A	N/A	10	10	10	10
	N_B (cells)	N/A	N/A	10	10	10	10

are located at the same grid points of the child domain. In Experiments 1–4, the child domain has 658 cells in the longitudinal direction and 1015 cells in the latitudinal direction, while in Experiments 5 and 6 the child domain has 1975 cells in the longitudinal direction and 3046 cells in the latitudinal direction (Table 4). The number of computational cells in the parent domain is 3200 × 5040 for all the experiments. The child domain runs on 128 MPI processes, and the parent domain is partitioned in 320 MPI processes.

The barotropic and baroclinic time steps of the parent domain are

$\Delta t_T = 3.0$ s and $\Delta t_C = 60.0$ s in all experiments, except in Experiment 5, which features $\Delta t_T = 1.0$ s and $\Delta t_C = 20.0$ s (Table 5). The nesting time step (Δt_{NT}) is the same as the barotropic time step of the parent domain in all experiments. In Experiments 1, 3, and 5, the barotropic and baroclinic time steps of the child domain are the same as those of the parent domain. In Experiments 2, 4, and 6, the barotropic and baroclinic time steps of the child domain are a third of those of the parent domain, i.e., $\Delta t_T = 1.0$ s and $\Delta t_C = 20.0$ s.

In Experiments 1–6, the number of cells excluded in the second direction ($N_{n, s, e, w}$) is 5 to 10 cells to prevent errors at the boundary of the child domain from propagating into the parent domain. In all two-way nesting experiments, the width of the zone with the low-resolution parent bathymetry is $N_B = 10$ cells and the width of the smoothing (relaxation) zone is $N_R = 10$ cells.

The simulations start from rest in all the experiments. The M_2 barotropic tide is forced at the southern boundary of the parent domain. The only forcing of the child domain comes from the parent domain through the lateral boundary. No atmospheric forcing is applied in all the simulations. The boundary forcing and the identical grids in Experiments 1–4 provide two advantages as a validation case. First, the result of the parent domain without any nesting can be used as the ‘true’ reference solution. In the experiments with identical grid-resolution and two-way nesting (Experiments 3 and 4), the two-way nesting result computed in the parent domain should be the same as the reference solution because the parent domain does not obtain any improvement from the same-resolution child domain. This means that the difference between the nesting and the no-nesting solutions represents the numerical error caused by the nesting communication. The resolution of the child domain is not the same as that of the parent domain in Experiments 5 and 6. Since the higher-resolution child domain generally returns more accurate results to the parent domain, the no-nesting solution is not valid as the true solution. Hence, we focus on discontinuities and errors near the updated boundaries in the parent domain in Experiments 5 and 6. Second, the performance of the lateral boundary condition of the child domain can be validated with one-way nesting (Experiments 1 and 2). The child domain receives forcing only through the lateral boundary in the first *coarse-to-fine* direction but does not send back any data to the parent domain in the second *fine-to-coarse* direction. The difference between the numerical results in the child domain and the no-nesting solution informs us about the accuracy of

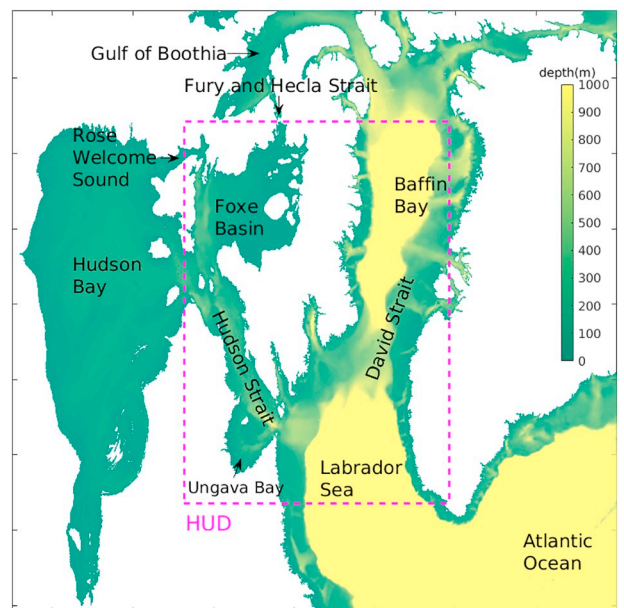
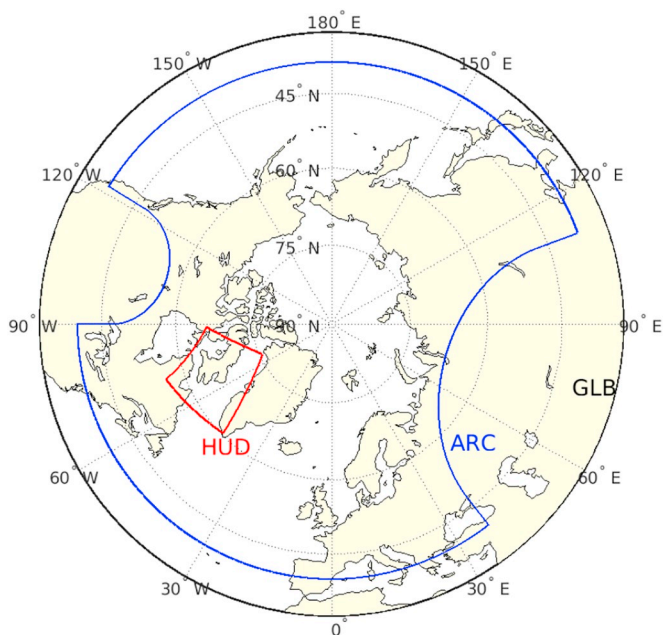


Fig. 5. (a) Geographical location of the parent (ARC) and child (HUD) domains at 1/25°, and (b) geography of the child domain and the surrounding area.

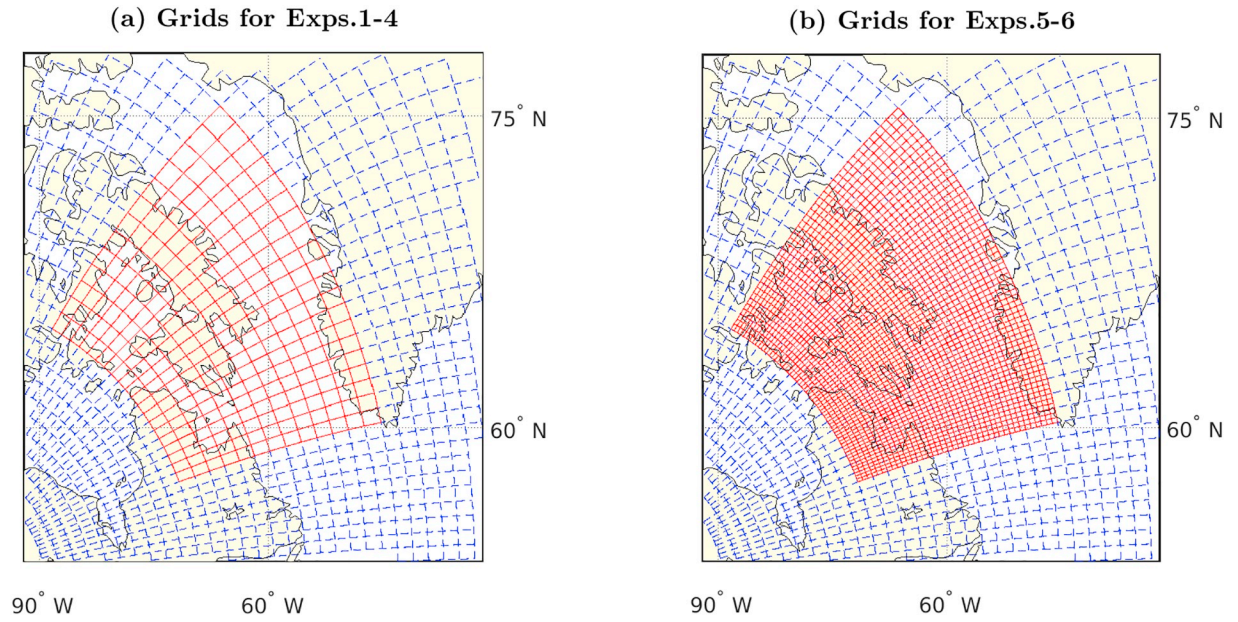


Fig. 6. Grid resolution of the parent domain (blue dashed lines) and the child domain (red solid lines) for (a) Experiments 1–4, in which the parent and child grids have the same resolution, and (b) Experiments 5 and 6, in which the parent and child grids have a resolution of $1/25^\circ$ and $1/75^\circ$, respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the lateral boundary conditions in HYCOM.

In Experiments 1–4, the accuracy over the parent domain is evaluated with the sea-surface-height root-mean-square error between the nesting result and the no-nesting reference solution at each computational cell

$$\text{RMSE}_{i,j} = \sqrt{\frac{\sum_{n=1}^N (\eta_{i,j}^n - \hat{\eta}_{i,j}^n)^2}{N}} \quad (3)$$

where η is the sea-surface height (SSH) of the nesting solution, $\hat{\eta}$ is the SSH of the reference solution, n is the temporal order of the hourly saved data, N is the total number of output data, and i and j are the computational cell indexes along the longitudinal and latitudinal directions, respectively. To exclude a spin-up error, only data between days 3 and 5 are used in the calculation. Eq. (3) represents the time-averaged absolute error with the reference solution. The relative error can be estimated with the normalized root-mean-square error

$$\text{NRMS}_{i,j} = \frac{\text{RMSE}_{i,j}}{\sigma_{i,j}} \quad (4)$$

where

$$\sigma_{i,j} = \sqrt{\frac{\sum_{n=1}^N (\eta_{i,j}^n)^2}{N}} \quad (5)$$

is the standard deviation of the sea-surface heights.

The sea-surface-height root-mean-square errors (RMSE) and the normalized errors (NRMS) with the reference solution for Experiments 1–4 are shown in Fig. 7. In these experiments, the resolutions of the parent and child grids are identical. The standard deviation of the sea-surface heights in the parent domain for the no-nesting reference solution is illustrated in Fig. 8. The NRMS values in Fig. 7 are plotted only in the Hudson Strait region where relatively large sea-surface heights are observed. In Fig. 7a and b, the RMSE values for Experiment 1 are mostly < 2.0 mm over the child domain (HUD), and the NRMS values are $< 0.1\%$ in the Hudson Strait region. This result indicates that the lateral boundary condition of the child domain works accurately. Fig. 7c and d shows RMSE and NRMS for Experiment 2, in which the parent and child-grid time steps differ. Even though these RMSE and NRMS values are larger than those of Experiment 1, the accuracy is still

quite good with errors $< 0.5\%$ in the Hudson Strait region. The errors of Experiment 2 are larger than those of Experiment 1 because the data are exchanged between the parent and child domains only at the nesting time steps ($\Delta t_{NT} = 3.0$ s), and errors are accumulated at the other two barotropic time steps ($\Delta t_{T, 2}$) in the child domain. The numerical errors of the two-way nesting experiments are expected to be larger than those of the one-way nesting experiments because the two-way nesting performs one more communication for the second direction, and there should be no accuracy improvement in the child domain with identical grid resolution. The RMSE and NRMS values for Experiment 3 in Fig. 7e and f are < 5.0 mm and 0.2% in the Hudson Strait region, respectively. As expected, these errors are slightly larger than those of the one-way nesting Experiment 1. However, for Experiment 4, with different parent- and child-grid time steps (Fig. 7g and h), the errors are reduced compared to Experiment 2 (< 7.0 mm and 0.35%) due to unknown causes. We do not observe significant error accumulations along the boundaries of the child domain in Experiments 3 and 4 (Fig. 7e and g).

To study how the two-way nesting affects the propagation of physical variables, in particular near the nesting boundaries and smoothing zones, we calculate for Experiments 3–6 the mass flow rate

$$\dot{m} = \rho(\eta + H)\mathbf{u}, \quad (6)$$

the residual of the continuity

$$R = \frac{\partial \eta}{\partial t} + \nabla \cdot (\eta + H)\mathbf{u}, \quad (7)$$

and the barotropic energy fluxes (Egbert and Ray, 2001)

$$\mathbf{F} = (\rho g H \eta)\mathbf{u} \quad (8)$$

where ρ is the water density ($= 1036.31$ kg/m³), \mathbf{u} is the barotropic velocity vector, η is the sea-surface height, H is the water depth, $\mathbf{F} = (F_x, F_y)$ is the energy flux vector, F_x and F_y are the longitudinal and latitudinal components, and g is the gravitational coefficient ($= 9.81$ m/s²). The magnitude of the time-mean and the standard deviation of the mass flow rate vectors and energy flux vectors, and the time-mean and the standard deviation of the continuity residual for Experiment 6 are presented in Fig. 9. The results for Experiments 3–6 are nearly identical, and similar figures for Experiments 3–5 are not shown. The difference

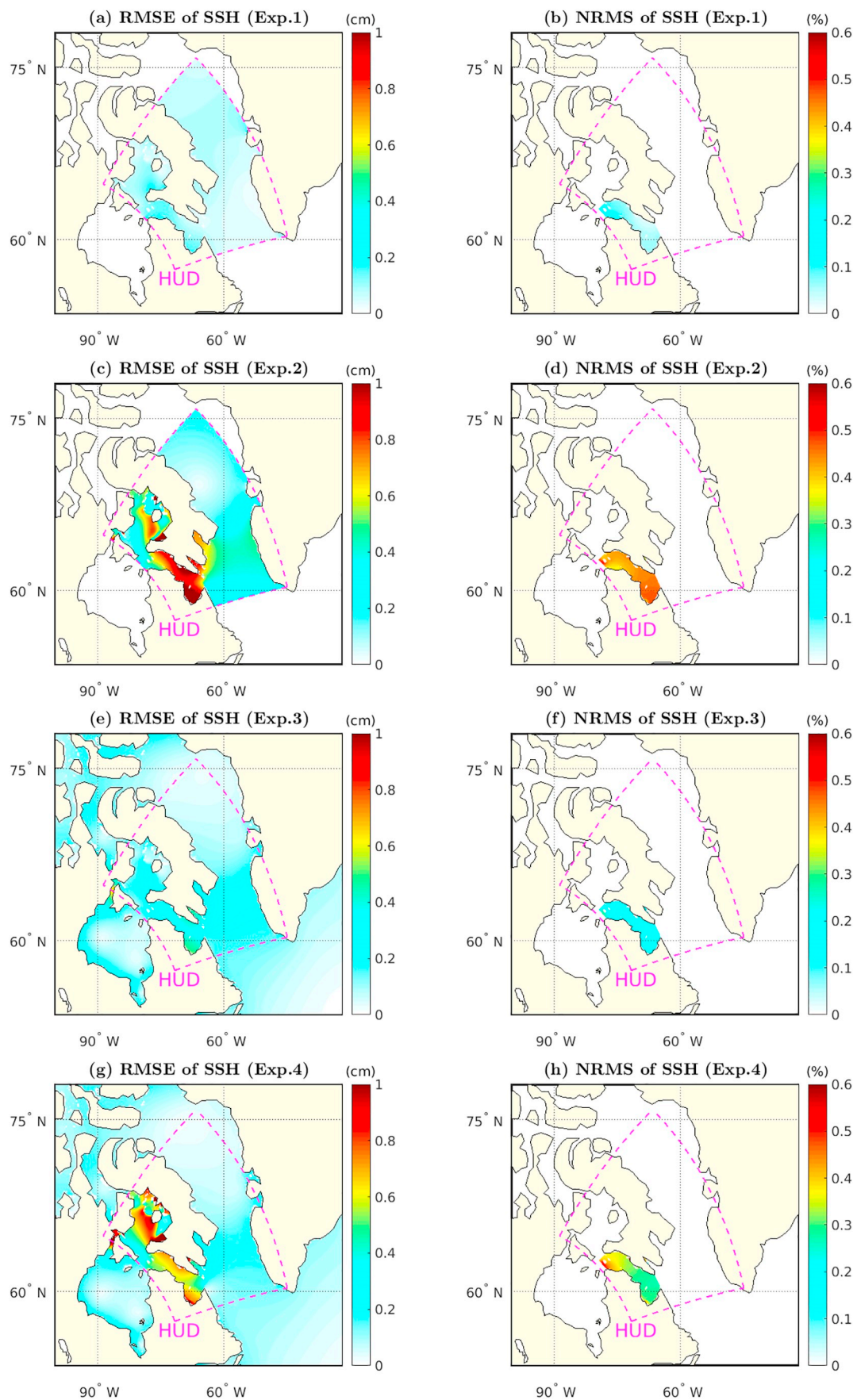


Fig. 7. Sea-surface-height root-mean-square errors (RMSE) with the reference solution and normalized root-mean-square errors (NRMS): (a) and (b) for Experiment 1, (c) and (d) for Experiment 2, (e) and (f) for Experiment 3, and (g) and (h) for Experiment 4. The NRMS values are shown only in the Hudson Strait region where the maximum SSH is observed.

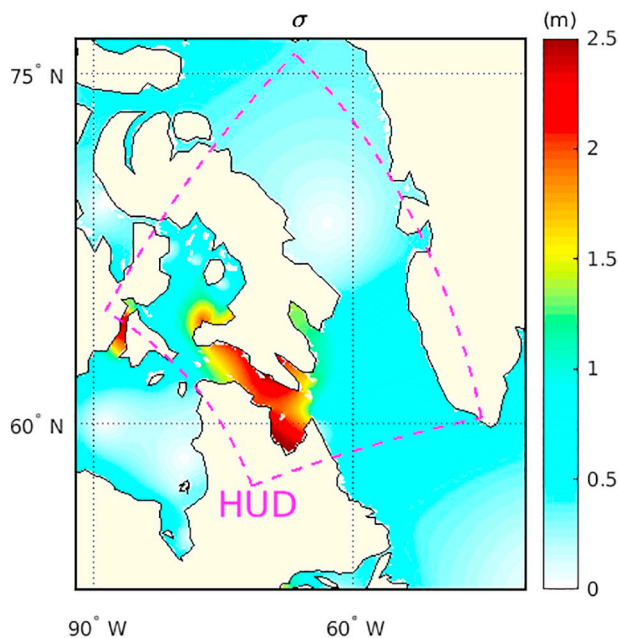


Fig. 8. Standard deviation of the sea-surface height of the reference solution on the parent grid, in the Hudson Strait region.

in time steps between Experiments 3 and 4 and Experiments 5 and 6 causes relative differences in the mass flow rate, continuity, and energy fluxes in the parent solution updated with the child solution that are generally smaller than 1%. The mean and the standard deviation of the residual in Fig. 9c and d have larger values near topographic gradients, as opposed to the nesting boundaries. In all two-way nesting experiments, mass is conserved across the south, west, north, and east boundaries. There are no obvious indications that the nesting boundaries trap, reflect, and diffract the tidal waves. This is further illustrated in Fig. 10, which shows the time-averaged tidal energy flux in the parent domain integrated along the cells parallel to the boundaries for Experiments 3–6. Compared to the reference (no-nesting) solution, the tidal energy flux is conserved in all experiments. Since the comparisons for the mass flow rate and the continuity residual show the same smooth transition as that of the tidal energy flux, they are not shown here.

In this section, we have tested the performance of the developed two-way nesting framework with six semi-idealized experiments for various time steps and grid resolutions. We conclude that the two-way nesting framework works with a high accuracy, and the tidal energy and mass are conserved quite well.

4. Global barotropic tides

To improve the tidal accuracy in the global HYCOM simulations, we apply the two-way nesting framework to a high-resolution child domain (1/75°) and a relatively low-resolution global parent domain (1/25°). The child domain, referred to as HBF, and its surroundings are shown in Fig. 11. Since the southeast entrance of Fury and Hecla Strait is blocked as land in the relatively low-resolution (1/25°) domain, and Hudson Bay plays an important role in the resonance of the M_2 barotropic tide in Hudson Strait (Arbic et al., 2007), the child domain in this realistic experiment is moved westward and extended to Hudson Bay, Rose Welcome Sound, and Fury and Hecla Strait. Moreover, the child domain is expanded southward to include the Bay of Fundy and Gulf of St. Lawrence regions that feature large tides and sea-surface-height root-mean-square errors. The southward expansion ensures that additional tide gauge stations, used for validation, are included in the child domain. The bathymetries of the parent and child domains are based on

the 1/120° GEBCO (General Bathymetric Chart of the Oceans) bathymetry. It is interpolated onto the 1/75° and 1/25° HYCOM grids for the child and parent domains.

Both the child and parent domains are forced by the five leading tidal constituents (M_2 , S_2 , N_2 , K_1 , and O_1) and a mean sea level pressure (MSLP). The simulation period is 29 days between November 27 and December 26 in 2013, and the numerical results of the sea-surface heights are stored every hour. The child domain receives additional forcing from the parent domain through its lateral boundaries. The simulation specifications of the realistic global-scale case are summarized in Table 6. To balance the number of computational cells for each process of the child and parent domains, the child domain is parallelized with 1408 MPI processes and the parent domain is parallelized with 1296 MPI processes. The simulation results for 29 days are decomposed into five tidal constituents with a least-squares harmonic analysis. The amplitudes and phases of the M_2 barotropic tide are compared to the global FES2014 and TPXO9-atlas solutions in addition to the tide gauge data.

Fig. 12 displays the locations of the tide gauge stations in (a) the deep oceans and (b) shallow water (coastal-shelf) regions. For the deep oceans, the tidal data from 132 stations are used for comparison, and 44 out of 132 stations are located in the North Atlantic Ocean (cyan triangles). For the shallow water regions, 75 stations of the total 128 sites are located in the North Atlantic Ocean. To check the effect of the two-way nesting on local and remote tides, these stations are divided into two groups: 38 tide gauges along the East Coast of North America (blue squares), and 37 gauges along the European Shelf (cyan triangles). The root-mean-square error between the tide gauge measurements and the HYCOM, TPXO9-atlas, and FES2014 tidal solutions, averaged over all gauges, is evaluated as

$$\text{RMS}_{TG} = \sqrt{\frac{1}{N} \sum_{k=1}^N \frac{1}{2} |a_k e^{i\phi_k} - \hat{a}_k e^{i\hat{\phi}_k}|^2} \quad (9)$$

where $i = \sqrt{-1}$, k is the tide gauge station number, N is the number of the tide gauge stations, \hat{a} and $\hat{\phi}$ are the amplitude and phase of the tide gauge data, a and ϕ are the amplitude and phase of the tidal solutions of HYCOM, TPXO9-atlas, or FES2014, respectively. The tidal solutions are interpolated onto the locations of the tide gauge stations with a bi-cubic interpolation method. Table 7 shows the gauge-averaged root-mean-square error of the tidal solutions from the tide gauge data in the North Atlantic Ocean (NATL) and the global ocean (GLB) for the TPXO9-atlas and FES2014 tidal solutions, and for the stand-alone 1/25° HYCOM (GLB25) and the two-way nesting results.

The overall surface tidal accuracy is improved through two-way nesting in both the deep oceans and the shallow shelf seas. The improvement generally decreases farther away from the child domain. The reduction in RMS_{TG} of ~ 3 cm is the largest for the North American East Coast tide gauges, which are located closest to the child domain. For these gauges, the relative improvement of tidal predictability $(\text{RMS}_{TG, \text{GLB25}} - \text{RMS}_{TG, \text{two-way}}) / \text{RMS}_{TG, \text{GLB25}}$ is 15.89%. However, the two-way nesting reduces the tidal accuracy for the gauges on the European Shelf by 2.22%. The relative improvement of predictability is 8.94% for all the gauges in the deep North Atlantic Ocean, which is larger than the improvement of 6.24% for all the gauges in the deep global ocean. The FES2014 and the TPXO9-atlas solutions have a better tidal accuracy than the HYCOM results. Small differences exist between the FES and TPXO solutions, although FES2014 is generally more accurate than TPXO9-atlas in both the deep and shallow oceans, except on the European shelf where the TPXO solution is more accurate.

The tide gauge data set is limited in spatial coverage. Hence, we also validate the global HYCOM simulations with the FES2014 and TPXO9-atlas tidal solutions. At each computational cell (i, j) of HYCOM, we calculate the M_2 sea-surface-height root-mean-square error between the HYCOM simulations and the FES/TPXO solutions as (Shriver et al., 2012)

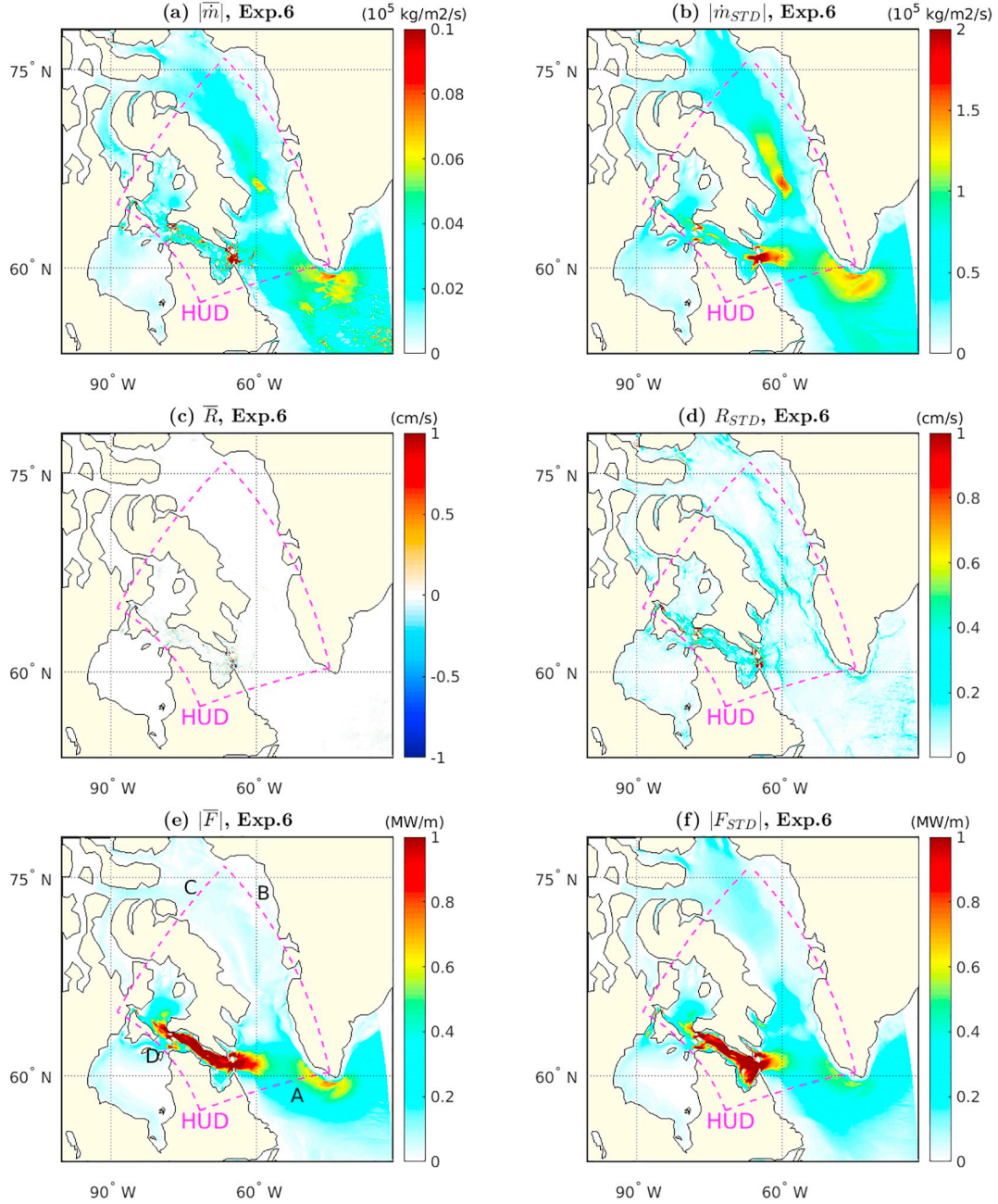


Fig. 9. Mean and standard deviation of the mass flow rate (a & b), the residual (c & d), and the tidal energy flux (e & f) in the parent domain for Experiment 6, in the vicinity of the child domain.

$$\text{RMSE}_{i,j} = \sqrt{\frac{1}{2} |a_{i,j} e^{i\phi_{i,j}} - \hat{a}_{i,j} e^{i\hat{\phi}_{i,j}}|^2} \quad (10)$$

where a and ϕ are the amplitude and phase of the M_2 barotropic tide in HYCOM, and \hat{a} and $\hat{\phi}$ are the amplitude and phase of the global tidal solutions of TPX09-atlas or FES2014, respectively. Since the HYCOM grid differs from the FES and TPX0 grids, the FES2014 and TPX09-atlas solutions are interpolated onto the HYCOM grid with a bi-cubic interpolation. Fig. 13a shows the amplitudes and phases of the M_2 barotropic tide for the two-way nesting simulation. The RMSE between FES2014 and the two-way nesting simulation is depicted in Fig. 13b. Fig. 13c shows the improvement of predictability of the global M_2 barotropic tide through two-way nesting, $\Delta\text{RMSE} = \text{RMSE}_{\text{GLB25}} - \text{RMSE}_{\text{two-way}}$. An increase in ΔRMSE through two-way nesting corresponds to a reduction in RMSE relative to the reference solution without nesting. The RMSE values of the two-way nesting experiment

and ΔRMSE in the region of the child domain are also plotted in Fig. 14. In Figs. 13c and 14b, the warm (cool) colors indicate an improvement (reduction) of the predictability through two-way nesting. Figs. 13c and 14b show that the predictability is not only improved in the child domain, but also in the parent domain outside the child area as far as the South Atlantic Ocean. This clearly illustrates that the improved accuracy in the coastal-shelf region of the child domain is allowed to propagate to the open ocean through the two-way nesting.

In addition, the spatially averaged root-mean-square error over several ocean domains (RMS_{avg}) is evaluated as (Arbic et al., 2004)

$$\text{RMS}_{\text{avg}} = \sqrt{\frac{\sum_{j=1}^{N_j} \sum_{i=1}^{N_i} (\text{RMSE}_{i,j})^2 \mathcal{A}_{i,j}}{\sum_{j=1}^{N_j} \sum_{i=1}^{N_i} \mathcal{A}_{i,j}}} \quad (11)$$

where \mathcal{A} is the area of the computational cell (i,j) , and N_i and N_j are the

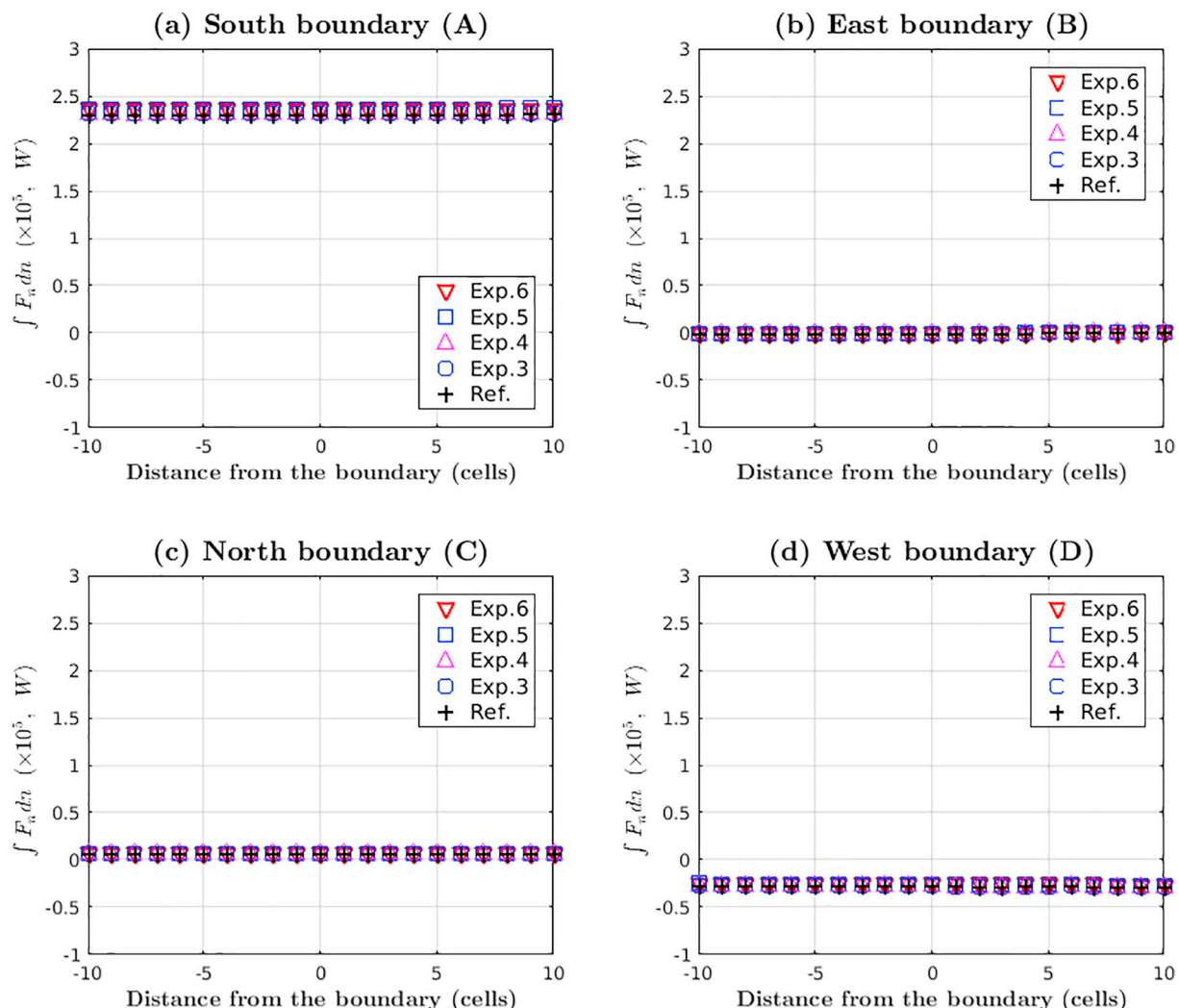


Fig. 10. Time-averaged tidal energy flux integrated along the cells parallel to the updated boundary: (a) south, (b) east, (c) north, and (d) west.

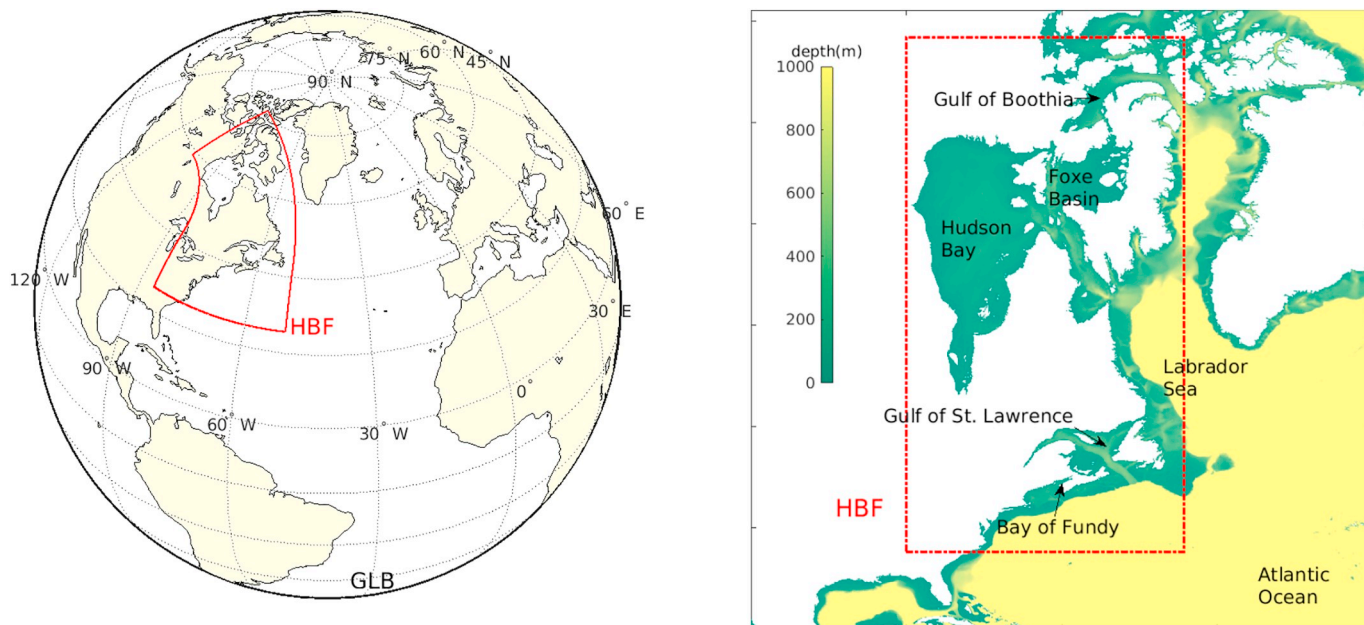


Fig. 11. (a) Geographical location of the child domain (HBF) in the parent domain (GLB), and (b) geography of the child domain and the surrounding area.

Table 6
Specifications for the realistic global-scale case.

	Child (HBF)	Parent (GLB)
Grid resolution (°)	1/75	1/25
Number of cells	2682 × 7614	9000 × 7055
Number of MPI processes	1408	1296
OASIS3-MCT interpolation	Bi-linear	Bi-linear
Barotropic time step, Δt_T (s)	1.0	3.0
Baroclinic time step, Δt_C (s)	16.0	48.0
Nesting time step, Δt_{NVT} (s)	3.0	3.0
Excluding zones, $N_{n, s, e, w}$ (cells)	10	N/A
Smoothing zones, N_R (cells)	10	N/A
Low-resolution zones, N_B (cells)	10	N/A

Table 7
Gauge-averaged M_2 sea-surface-height root-mean-square error between the tide gauge data and the tidal solutions (RMS_{TG} , cm). The relative improvement of tidal predictability is abbreviated with RIOP.

Case	NATL		GLB		
	Deep	Shallow	Deep	Shallow	
					North Am. East Coast
TPXO	0.55	2.23	2.78	0.52	6.18
FES	0.32	1.73	3.30	0.30	3.59
GLB25	8.39	18.06	16.22	5.77	18.94
Two-way	7.64	15.19	16.58	5.41	18.38
RIOP	8.94%	15.89%	-2.22%	6.24%	2.96%

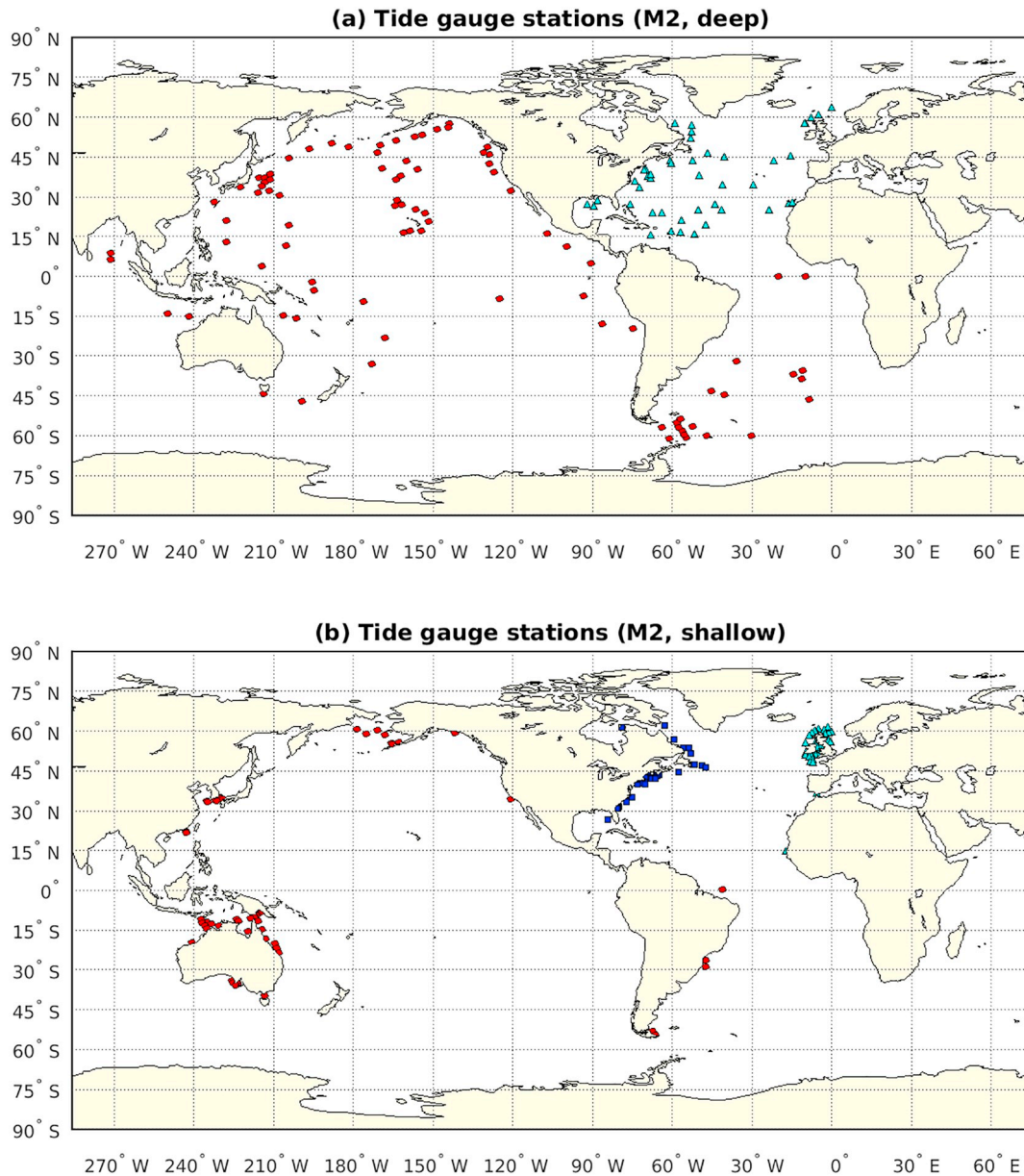


Fig. 12. Location of tide gauge stations in the global ocean (GLB) in (a) deep ocean and (b) shallow water. The deep-ocean stations in the North Atlantic Ocean (NATL) are represented by cyan triangles, and the shallow-water stations in NATL are grouped into the western stations (blue squares) and the eastern stations (cyan triangles). The stations in other oceans are shown in red circles for both deep ocean and shallow water. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

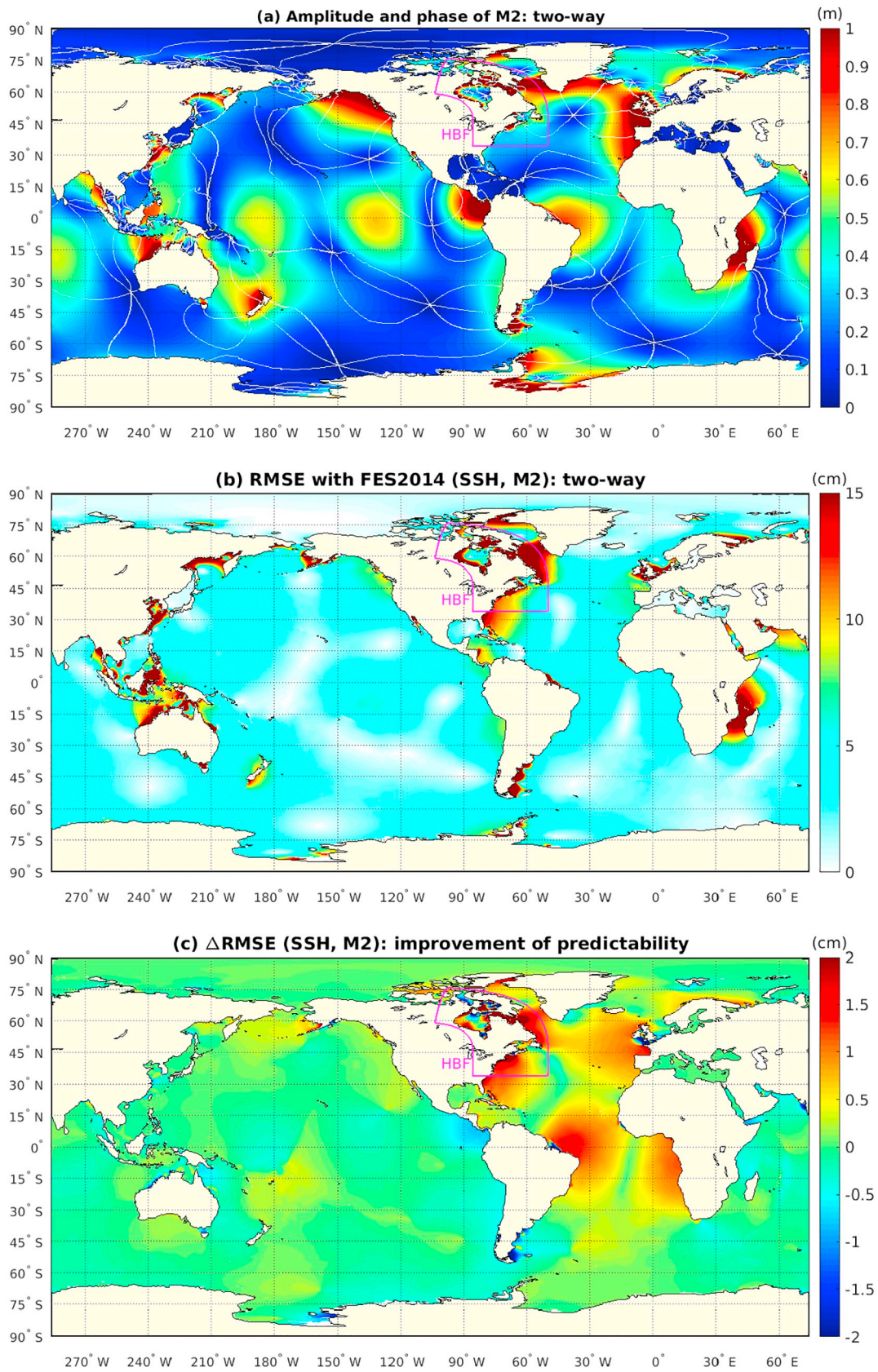


Fig. 13. (a) Amplitudes and phases of the M₂ barotropic tide for the two-way nesting solution, (b) M₂ sea-surface-height RMSE between FES2014 and the two-way nesting solution, and (c) the improvement of predictability ΔRMSE. Warm (cool) colors indicate an improvement (reduction) of the predictability. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

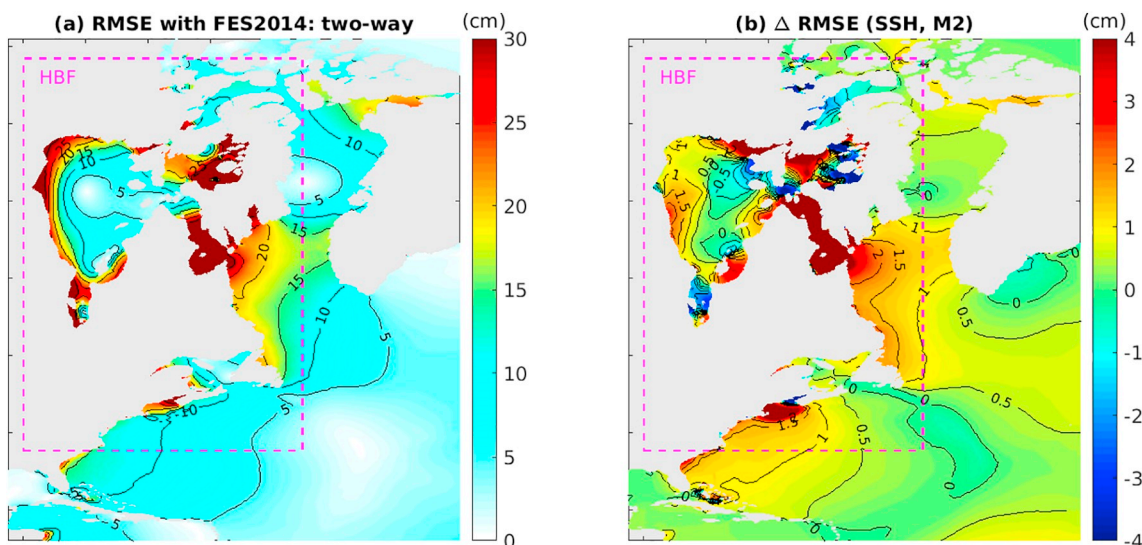


Fig. 14. (a) M_2 sea-surface-height RMSE between FES2014 and the two-way nesting solution and (b) the improvement of predictability in the vicinity of the child domain. In the figure, the x and y axes represent the computational indexes i and j , respectively, for a clear view. The corresponding longitudes and latitudes can be found in Fig. 11. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.)

Table 8

Area-averaged root-mean-square error (RMS_{avg}) with TPXO9-atlas (TPXO) and FES2014 (FES) for four areas of GLB25 ($1/25^\circ$ simulation without nesting) and two-way nesting solutions (cm). The relative improvement of tidal predictability is abbreviated with RIOP.

Case	HBF		NATL		GLB		GLB ₆₆	
	TPXO	FES	TPXO	FES	TPXO	FES	TPXO	FES
GLB25	20.57	18.45	9.61	8.68	6.67	5.93	4.13	4.12
2-way	19.18	17.11	9.08	8.07	6.60	5.85	4.05	4.03
RIOP	6.76%	7.26%	5.52%	7.03%	1.05%	1.35%	1.94%	2.18%

number of ocean cells in the longitudinal and latitudinal directions, respectively. Table 8 represents the root-mean-square error averaged over the child area in the parent domain (HBF), the North Atlantic Ocean (NATL), and the global parent domain (GLB), respectively, for water depths > 5.0 m. In addition, RMS_{avg} is computed over water depths > 1000 m and latitudes equatorward of 66° (GLB₆₆) for comparison with previous studies. The differences in RMS_{avg} computed with either FES2014 or TPXO9-atlas are small. The improvement of predictability is largest in the child domain (7.26%) when TPXO is used. This relative improvement is smaller than the 15.89% improvement computed for the tide gauges on the shelf of the North American East Coast (Table 7). As can be seen in Figs. 12b and 14b, these tide gauges are located in areas where $\Delta RMSE$ is both large and positive. The relative improvement of 7.26% averaged over the child domain is lower due to localized reductions in the predictability in Hudson Bay and Foxe Basin (blue areas in Fig. 14b). The improvement in predictability decreases as the size of the averaging area increases. However, this reduction in predictability is minimal for the North Atlantic (NATL), where the relative improvement in predictability is 7.03% when FES is used. This relatively large value can be attributed to $\Delta RMSE$ being positive over a large area (Fig. 13c). However, beyond the Atlantic Ocean, the improvement in tidal accuracy is minimal. As a consequence, the reduction in RMS_{avg} for the GLB₆₆ case is small, i.e., only 2.18%.

While the reduction in RMSE may not seem very large, the surface area where the predictability is improved is generally much larger than the area where it is reduced (Table 9). In the HBF domain, $\Delta RMSE > 5.0$ mm occurs in 64.44% of the domain, while $\Delta RMSE < -5.0$ mm occurs only in 5.84% of the domain. The largest reduction in

Table 9

Area integral over ocean surface where $\Delta RMSE > 5$ mm (improved predictability) and $\Delta RMSE < -5$ mm (reduced predictability) with FES2014 for the child domain (HBF), the North Atlantic (NATL), and the global ocean (GLB). The fraction of the total area is between parentheses.

RMSE reduction ($\times 10^4$ km ²)	HBF	NATL	GLB
$\Delta RMSE > 5$ mm (improvement)	321.95 (64.44%)	2271.62 (49.83%)	3456.01 (9.69%)
$\Delta RMSE < -5$ mm (reduction)	29.20 (5.84%)	49.93 (1.10%)	550.03 (1.54%)

predictability (increase in RMSE) is observed in Foxe Basin (Fig. 14b). In about 1.10% of the North Atlantic Ocean (NATL), the predictability in the two-way nesting solution is reduced. This reduction mostly occurs in other shelf regions such as the English Channel, the Patagonian Shelf, and the Amazon Shelf, as shown in Fig. 13c. Only 9.69% of the global ocean (GLB) features an improved predictability because the Pacific and Indian Oceans are minimally affected by the two-way nesting in the North Atlantic Ocean.

5. Discussion and conclusions

We have implemented an online two-way nesting framework in a global ocean circulation model (HYCOM) to improve global surface tides. The barotropic pressure and velocity are exchanged between a parent and a child domain with an external coupler, OASIS3-MCT. We modified the masks in both the first *coarse-to-fine* and the second *fine-to-coarse* directions, and set the limits of the search area in the first direction to reduce the computing time of the remapping coefficients in OASIS3-MCT.

In the global HYCOM simulations, Hudson Strait and the adjacent North Atlantic Ocean feature relatively large M_2 sea-surface-height root-mean-square errors with the tide gauges and the altimetry constrained tide models. These errors may be associated with the inability of low-resolution simulations to resolve the semi-diurnal tidal resonances on and off the shelf in the North Atlantic Ocean. These errors can be reduced by two-way nesting a high-resolution child domain in a low-resolution parent domain. Hence, we selected the Hudson Strait region as the child domain in our nesting experiments.

The developed two-way nesting framework is validated with six semi-idealized one- and two-way nesting experiments. In these

experiments, the child domain covers the Hudson Strait region, while the parent domain covers the Arctic, North Pacific, and North Atlantic Oceans. The M_2 barotropic tide is forced at the southern boundary of the parent domain. The accuracy of the nesting framework is tested for time steps and grid resolutions that are the same and/or differ between the parent and child domains. The parent and child grids have the same resolution in Experiments 1–4. The tidal solution on the parent grid without nesting is used as the ‘true’ reference solution. The semi-idealized experiments have a good agreement with the reference solution. The errors of the sea-surface height in the four experiments are generally much $< 1\%$. In addition, two experiments are performed in which the grid resolution of the child domain is three times as fine ($1/75^\circ$) as that of the parent domain ($1/25^\circ$) to check for discontinuities along the nesting boundaries. It is shown that mass and energy are conserved across the boundaries through all the experiments.

Next, the developed two-way nesting framework is applied to a realistic global-scale experiment. The resolution of the child domain ($1/75^\circ$) is three times as high as that of the parent domain ($1/25^\circ$). Realistic tidal forcing (M_2 , S_2 , N_2 , K_1 , and O_1) and atmospheric pressure (MSLP) are applied over the child domain (HBF) as well as the parent domain (GLB). Compared to the child domain of the semi-idealized experiments, the HBF domain is extended to Hudson Bay and the Bay of Fundy to improve the tidal accuracy in these areas. The no-nesting and two-way nesting results are compared to tide gauge data and the FES2014 and TPXO9-atlas tidal solutions. The application of the two-way nesting reduces the M_2 sea-surface-height root-mean-square errors with the tide gauge data and the tidal solutions, in particular in the Northwest Atlantic Ocean. The largest improvement of predictability (i.e., reduction of the root-mean-square error) of about 16% occurs at the tide gauges located along the East Coast of North America. The M_2 root-mean-square errors between the two-way nesting simulation and the TPXO/FES tidal solutions are not only reduced in the vicinity of the child domain, but they are reduced as far as the South Atlantic Ocean (red areas in Figs. 13c and 14b). The improvement of the tidal predictability in the North Atlantic Ocean averages about 6.28%. The two-way nesting simulation shows that a higher horizontal grid resolution and a better resolved coastal bathymetry in the regions of Hudson Strait and the Bay of Fundy not only improves the tidal prediction in the child domain, but also in the coastal and abyssal ocean away from the nesting boundaries through the back-effect (Arbic and Garrett, 2010; Arbic et al., 2009; Arbic et al., 2007).

In recent years, the global-mean M_2 sea-surface-height root-mean-square error between $1/12.5^\circ$ HYCOM and TPXO tidal solutions has been reduced from 7.48 cm in Shriver et al. (2012) to 4.43 cm in Buijsman et al. (2015) to 2.60 cm in Ngodock et al. (2016). The reduction from 7.48 cm to 4.43 cm is due to the inclusion of bathymetry under the ice shelves, the application of a spatially varying and iterated SAL, and the tuning of the linear wave drag. The reduction from 4.43 cm to 2.60 cm is due to the application of an augmented state ensemble Kalman Filter (ASEnKF) to correct for errors in the tide model associated with imperfectly known topography and damping terms. In this paper, we do not apply the ASEnKF technique. The reduction in RMSE from 4.43 cm to 4.13 cm for the no-nesting solution is due to an increase in model resolution from $1/12.5^\circ$ to $1/25^\circ$. The application of the two-way nesting framework to one area, i.e. the Hudson Shelf, reduces this global-mean error to 4.03 cm, which is a modest improvement.

This paper mainly describes the development of a two-way nesting framework in a non-data-assimilative version of HYCOM and its validation with the tide gauge data and the global FES2014 and TPXO9-atlas tidal solutions. To reduce the large M_2 surface tide errors in the North Atlantic, a high resolution child grid is applied to the Hudson Shelf. This improves the accuracy of the tides not only in the Hudson Shelf region, but also in the Atlantic Ocean as far south as South Africa. However, the European Shelf, the Patagonian Shelf, and the Northwest Australian Shelf, among others, still feature large sea-surface-height root-mean-square errors in HYCOM (Fig. 13b). To further reduce these

errors, we plan to apply the two-way nesting technique to multiple shelf areas in different ocean basins and find the break-even point where two-way nesting is computationally efficient compared to the stand-alone high-resolution global simulation in a subsequent paper.

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