The role of current sheet scattering in the proton isotropic boundary formation during geomagnetic storms

John D. Haiducek¹, Natalia Y. Ganushkina²,³, Stepan Dubyagin³, Daniel T. Welling²,⁴

¹U.S. Naval Research Laboratory, Washington, DC, USA
²Climate and Space Sciences, University of Michigan, Ann Arbor, MI, USA
³Finnish Meteorological Institute, Helsinki, Finland
⁴University of Texas at Arlington, Arlington, TX, USA

Key Points:

• We corrected estimates of the adiabaticity parameter $K$ using in situ data, obtaining consistent results between empirical and MHD models
• A significant fraction of the $K$ estimates was below the threshold for current sheet scattering
• Corrected $K$ estimates are independent of Symh-$H^*$ and MLT, even for high values of $K$

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Corresponding author: John Haiducek, jhaiduce@umich.edu

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Abstract

There is considerable evidence that current sheet scattering (CSS) plays an important role in isotropic boundary (IB) formation during quiet time. However, IB formation can also result from scattering by electromagnetic ion cyclotron (EMIC) waves, which are much more prevalent during storm time. The effectiveness of CSS can be estimated by the parameter $K = \frac{R_c}{R_g}$, the ratio of the field line radius of curvature to the particle gyroradius. Using magnetohydrodynamic (MHD) and empirical models, we estimated the parameter $K$ associated with storm-time IB observations on the night side. We used magnetic field observations from spacecraft in the magnetotail to estimate and correct for errors in the $K$ values computed by the models. We find that the MHD and empirical models produce fairly similar results without correction, and that correction increases this similarity. Accounting for uncertainty in both the latitude of the IB and the threshold value of $K$ required for CSS, we found that 29–54% of the IB observations satisfied the criteria for CSS. We found no correlation between the corrected $K$ and magnetic local time, which further supports the hypothesis that CSS played a significant role in forming the observed IBs.

1 Introduction

During geomagnetic storms, the shape and structure of the magnetotail can change rapidly and dramatically. This includes changes in the orientation of the current sheet, as well as rapid stretchings and dipolarizations. Although storms are driven by the solar wind, the ionosphere plays an important role in regulating the geomagnetic response to these solar wind inputs (e.g. Brambles et al., 2013, 2011; Daglis, 1997; Gloer, Tóth, Gombosi, & Welling, 2009; Welling & Liemohn, 2016). As such, characterizing the connections and interaction between the ionosphere and the magnetotail during storms is necessary in order to fully understand the behavior of the magnetosphere during storm conditions.

Most interaction between the magnetosphere and the ionosphere occurs through the flow of particles and currents along magnetic field lines. Characterizing the structure of these field lines can help us to determine the origins and destinations of plasma flows between the magnetosphere and ionosphere, and thus to better understand how the two regions interact with each other. Unfortunately, our ability to determine field line structure is limited by the very sparse distribution of satellite observations through-
out much of the magnetosphere. As a result, models of field line structure are often poorly constrained, particularly during storm conditions when rapid changes in field line shape pose an added challenge in determining the global system state at any given time.

To supplement the sparse magnetospheric observations, ionospheric observations can be used to help better determine the state of the magnetotail. Ionospheric observations have the advantage of being at a low altitude where relatively large numbers of satellites with fairly short orbital periods provide much better data coverage than is available in most of the magnetosphere. For instance, at present three National Oceanic and Atmospheric Administration (NOAA) Polar Orbiting Environmental Satellites (POES) satellites are in operation at altitudes of 800-900 km and with orbital periods around 100 minutes (https://www.ospo.noaa.gov/Operations/POES/status.html). Similarly, two METOP satellites are in orbit at an 817 km altitude (https://www.eumetsat.int/website/home/Satellites/CurrentSatellites/Metop/index.html), and several Defense Meteorological Satellite Program (DMSP) spacecraft orbit at a nominal 850 km orbit (http://www.au.af.mil/au/awc/space/factsheets/dmsp.htm).

In order to leverage ionospheric observations to help determine magnetotail structure, we must identify a feature in the ionosphere that maps to a known location in the magnetosphere (or at least, to a location with known characteristics). This is the case for the isotropic boundary (IB), which is a feature in the auroral zone of the ionosphere characterized by a substantial change in the flux of downwelling particles. Poleward of the IB, comparable fluxes are observed in directions parallel to and perpendicular to the local magnetic field, while equatorward of the IB the flux in directions perpendicular to the local magnetic field is much greater than the flux in the parallel direction. This tendency has been observed by a number of satellites, including Injun 1 and 3, ESRO IA and IB, NOAA, and DMSP (Imhof, Reagan, & Gaines, 1977; Newell, Sergeev, Bikkuzinina, & Wing, 1998; V. Sergeev, Sazhina, Tsyganenko, Lundblad, & Søraas, 1983; Søraas, 1972). The proton isotropic boundary is observed at all activity levels and in all magnetic local time (MLT) sectors (V. A. Sergeev, Malkov, & Mursula, 1993).

The change in loss-cone filling observed as a spacecraft transits the IB indicates that the IB maps to a transitional region in the magnetosphere, which is characterized by a substantial change in the rate of pitch angle scattering. Two mechanisms for this have been proposed. Current sheet scattering (CSS) refers to a process in which parti-
particles undergo chaotic motion upon crossing the current sheet, resulting in changes to the particles’ pitch angles (Büchner & Zelenyi, 1987; V. A. Sergeev et al., 1993; West, Buck, & Kivelson, 1978). This occurs when the radius of curvature, \( R_c \), and the effective particle gyroradius, \( r_g \), become comparable to each other, resulting in a violation of the first adiabatic invariant (Alfvén & Fälthammar, 1963; Büchner & Zelenyi, 1987; Delcourt, Sauvaud, Martin, & Moore, 1996; Tsyganenko, 1982). The second mechanism that has been proposed for IB formation is the scattering of particles by electromagnetic ion-cyclotron (EMIC) waves, in which plasma waves having oscillations near the particle gyrofrequency result in a violation of the first adiabatic invariant (Kennel & Petschek, 1966; Liang et al., 2014; V. A. Sergeev, Chernyaev, Angelopoulos, & Gamushkina, 2015; V. A. Sergeev, Chernyaeva, Apatenkov, Gamushkina, & Dubyagin, 2015).

Of the two mechanisms, the CSS process operates at all times and in all MLT sectors. A number of papers have identified CSS as the main (though not necessarily exclusive) mechanism for IB formation during quiet time (Gamushkina et al., 2005; Haiducek, Gamushkina, Dubyagin, & Welling, 2019 accepted; V. Sergeev & Tsyganenko, 1982; V. A. Sergeev et al., 1993). However, at times EMIC scattering may cause the IB to be observed at a lower latitude than would occur if CSS were the operative mechanism. This occurs primarily during storms and substorms (Dubyagin, Gamushkina, & Sergeev, 2018; Gvozdevsky, Sergeev, & Mursula, 1997; V. A. Sergeev et al., 2010; Søraas, Lundblad, Maltseva, Troitskaya, & Selivanov, 1980; Yahnin & Yahnina, 2007), though there is evidence that it occurs during quiet times as well (e.g. Popova, Yahnin, Demekhov, & Chernyaeva, 2018; V. A. Sergeev, Chernyaev, et al., 2015).

Distinguishing whether CSS or EMIC is the responsible mechanism for a particular IB observation is necessary for the application of IB observations to estimating magnetotail field geometry. When CSS is the responsible mechanism, the IB latitude can be used to estimate the amount of field line stretching in the magnetotail (Meurant et al., 2007; V. A. Sergeev & Gvozdevsky, 1995; V. A. Sergeev et al., 1993). This approach is likely to work well during quiet periods, but during storms it is expected that EMIC scattering will play a more significant role than it does in quiet time, because EMIC waves are more prevalent during storms. For instance, Erlandson and Ukhorskiy (2001) found that the EMIC wave occurrence rate increases by a factor of 5 during storm conditions over 10 years of observations, and Halford, Fraser, and Morley (2010) also found an increased EMIC occurrence rate during storm conditions. Determining whether EMIC or
CSS is responsible for IB formation at a given time and longitude requires estimating the value $K = \frac{R_c}{r_g}$ associated with a given IB observation. $K$ parameterizes the effectiveness of the CSS process. V. Sergeev et al. (1983) proposed $K \leq 8$ as a threshold condition for CSS scattering, while Delcourt, Malova, and Zelenyi (2006); Delcourt, Moore, Giles, and Fok (2000); Delcourt et al. (1996) showed that CSS operates when $K \lesssim 1–10$, and V. A. Sergeev, Chernyaev, et al. (2015) suggested that CSS could be responsible for IB formation with $K$ as high as 12. In the present work, recognizing that no single value of $K$ can be regarded as the definitive threshold, we adopt the range $K = 8–13$ as a nominal uncertainty range for the CSS scattering threshold, where the commonly used $K \leq 8$ threshold serves as the lower end of the uncertainty range and the $K \leq 13$ value as the upper end of the uncertainty range, following the recent study by Dubyagin et al. (2018).

Computing $K$ values associated with an IB observation requires tracing a magnetic field line from the location of the observation to the point where it crosses the current sheet. Both steps require a magnetic field model that can provide field vectors at arbitrary points within the magnetosphere. Most previous studies to do this have employed empirical models such as the Tsyganenko models (e.g. Dubyagin et al., 2018; Ganushkina et al., 2005; V. A. Sergeev, Chernyaev, et al., 2015; V. A. Sergeev et al., 1993), but two have done so using magnetohydrodynamic (MHD) models (e.g Haiducek et al., 2019 accepted; Ilie, Ganushkina, Toth, Dubyagin, & Liemohn, 2015). Ilie et al. (2015) obtained $K$ values for IB observations during a quiet period, and obtained unrealistically high $K$ values for conditions in which CSS was expected to be the dominant mechanism. Haiducek et al. (2019 accepted) simulated the same quiet period using different model settings. Haiducek et al. (2019 accepted) obtained lower $K$ values than those of Ilie et al. (2015), and demonstrated that these values could be corrected using in situ magnetic field observations, concluding that the quiet time IB observations were likely the result of CSS and not EMIC.

The work of Haiducek et al. (2019 accepted) demonstrated the use of MHD to estimate $K$ during quiet conditions, and obtained results that were consistent with those derived from empirical models for the same time period. However, the circumstances in which MHD is likely to be most advantageous for studying the IB are during storm conditions. Through simulations of storms, the physics incorporated into an MHD model can be used to shed light on the causes of storm-time dynamics. Several previous papers have presented $K$ estimates during storm conditions, but all have used empirical
models which were constructed from fits to historical satellite observations (e.g. Dubya-
gin et al., 2018; Ganushkina et al., 2005; V. A. Sergeev et al., 1993). Since MHD mod-
els simulate the physics of the magnetosphere rather than presenting a fit to historical
observations, it has the potential to reproduce features and dynamics of storm events
that may be missed by empirical models, as well as provide additional information that
can shed light on the causes of any dynamics that are reproduced by the model. The use
of MHD to explore IB properties during disturbed conditions (specifically, during a sub-
storm) was previously demonstrated by Gilson, Raeder, Donovan, Ge, and Kepko (2012),
but no comparison of $K$ estimates with IB observations was performed. To date, no pub-
lished work has used MHD to explore IB properties during a geomagnetic storm.

The goal of the present work is to estimate what fraction of IB observations might
be the result of CSS during storm conditions, and to test whether MHD and empirical
models produce consistent values of $K$ during storm conditions. We estimate $K$ using
multiple MHD simulations and multiple empirical models, in order to obtain a better
representation of the range of variability for $K$ than would be possible using any single
model alone. Next we compare our $K$ values with the $K = 8$ and $K = 13$ threshold
conditions to estimate what fraction of the IB observations may have been the result of
CSS (as opposed to EMIC wave scattering). We estimate errors in the model output by
comparing with in situ magnetic field observations, and apply procedures from Dubya-
gin et al. (2018) and Haiducek et al. (2019 accepted) to correct for these errors. The present
work is the first to use MHD to explore IB properties during a geomagnetic storm, and
the first to estimate $K$ using MHD during disturbed conditions.

The paper is organized as follows. Section 2 provides a description of the time pe-
riod chosen and the observational data used. Section 3 describes the procedures used to
estimate $K$, and the details of the MHD simulations. Section 4 presents a validation of
the MHD magnetic fields against in situ observations. Sections 5 and 6 present results
from the MHD and empirical models, respectively. Section 7 outlines the procedure for
correcting the $K$ values and presents the overall results for $K$ and the corrections, and
the paper concludes with section 8.
Figure 1. Solar wind driving parameters used in the study, along with geomagnetic indices parameterizing the magnetospheric response. (a) $u_x$ component of bulk velocity, in GSM coordinates, (b) proton density $\rho$, (c) temperature, (d) IMF $B_z$, (e) Symh-$H$, (f) $Kp$, (g) $AL$. The beginning of the storm is marked with a vertical line.

2 Event and observations

We chose the time period of 2100 UT on 4 April, 2010 to 1400 UT on 6 April, 2010 for our analysis. The major feature of this time period is a moderate storm with a minimum Symh-$H$ of -90 nT and a maximum $Kp$ of 7.7. This storm was the result of a coronal mass ejection observed at 0954 UT 3 April. The northern flank of the CME reached the Sun-Earth L1 Lagrange point around 0755 UT on 4 April, and was followed by the passage of a magnetic cloud from around 1200 UT on 5 April until 1320 UT on 6 April (Liu, Luhmann, Bale, & Lin, 2011; Möstl et al., 2010). Solar wind parameters from this time period are shown in Figures 1a–1d. The beginning of the storm is marked with a vertical line. Observational data shown in Figure 1 come from the 1-minute OMNI data set provided by the National Aeronautics and Space Administration (NASA) Goddard Spaceflight Center (GSFC). The beginning of the storm is marked by a sudden increase in solar wind speed between 0800 and 0900 UT on 5 April (see the $u_x$ velocity component in Figure 1a), accompanied by sharp increases in solar wind density $\rho$ (Figure 1b) and temperature (Figure 1c). The $B_z$ component of the interplanetary magnetic field (IMF, Figure 1d) abruptly became more negative at the same time, and oscillated rapidly for the next few hours.

To quantify the magnetospheric response to the storm, we use the Symh-$H$, $Kp$, and $AL$ indices. The latitude of the IB has been found to be sensitive to all three of Symh-$H$ (e.g. Asikainen, Maliniemi, & Mursula, 2010; Dubyagin et al., 2013, 2018; Ganushkina et al., 2005; Hauge & Søraas, 1975; Lvova, Sergeev, & Bagautdinova, 2005; Søraas, 1972; Søraas, Aarsnes, Oksavik, & Evans, 2002), $Kp$ (e.g. V. A. Sergeev et al., 1993; Søraas, 1972; Yue et al., 2014), and $AL$ (e.g. Dubyagin et al., 2013; Lvova et al., 2005; Søraas, 1972).

The Symh-$H$, $Kp$, and $AL$ indices during 4–6 April 2010 are shown in Figures 1e, 1f, and 1g. From the Symh-$H$ index (Figure 1e), a storm sudden commencement can
be seen just after 0800 UT on 5 April, followed by a sharp decrease in $Symh-H$. The minimum $Symh-H$ of -90 nT does not occur until almost 24 hours later. The maximum $Kp$ of 7.7 occurred around 0900 UT on 5 April (Figure 1f), and $Kp$ remained at or above 3 throughout the event. The $AL$ index (Figure 1g) dropped rapidly after the storm commencement, reaching a minimum of -2,152 nT but quickly recovering.

Observations of isotropic boundaries were obtained using the Medium Energy Proton and Electron Detector (MEPED) instruments (Evans & Greer, 2000) onboard five NOAA/POES and one METOP spacecraft. This instrument consists of two telescopes which detect proton fluxes in four energy bands between 30 and 6900 keV. The telescopes are referred to as the 0° and 90° telescope, after their approximate directions relative to the spacecraft’s zenith. The 0° telescope points away from the Earth, while the 90° telescope is roughly perpendicular to the 0° telescope and points along the spacecraft’s velocity vector. When the spacecraft is at relatively high latitudes, this configuration results in the 0° telescope mainly detecting precipitating particles, while the 90° telescope mainly detects locally trapped particles.

IB locations were identified from the MEPED P1 energy channel. The nominal energy range of this channel is 30–80 keV, but in reality the lower energy limit is somewhat higher than 30 keV and varies among the satellites due to degradation of the detectors over time. We used the low energy limits given by Asikainen, Mursula, and Maliniemi (2012), and these are reproduced in Table S1 in the supporting information. In addition to variance between the spacecraft, the 90° telescope degrades more rapidly than the 0°.

We recalibrate the 90° flux to correspond to the 0° cutoff energy using the procedure given in the Appendix of Dubyagin et al. (2018). Using these corrected fluxes, we found IB crossings with the procedure described in Dubyagin et al. (2018). It should be noted that there can be significant uncertainty associated with the determination of IB locations from MEPED data during storm periods. To address this, the Dubyagin et al. (2018) procedure defines a high latitude (HL) and low latitude (LL) limit of the IB based on the MEPED data, which we use to estimate the uncertainty range for the IB latitude.

Rather than using all available IB observations, we limit our analysis to those for which in situ magnetic field observations were available in the magnetotail from one or more spacecraft that were conjugate with the location of the IB observation in the ionosphere. To consider a spacecraft as conjugate with the IB observation, we require it be
Figure 2. (a) Locations of THEMIS A and GOES 11 at the times of all the IB observations. (b) and (c) Relative positions of THEMIS A, D, and E at 0700 UT on 5 April.

within one hour MLT of the location of the IB observation. In addition, we require the conjugate spacecraft to be located near the equatorial plane between 4 and 12 \( R_E \) from the Earth. Only IB observations from the night side were used. The spacecraft meeting these criteria were Time History of Events and Macroscale Interactions during Substorms (THEMIS, Auster et al., 2008; McFadden, Carlson, Larson, Bonnell, et al., 2008; McFadden, Carlson, Larson, Ludlam, et al., 2008) A, D, and E, and Geostationary Operational Environmental Satellite (GOES Singer, Matheson, Grubb, Newman, & Bouwer, 1996) 11–15. Representative locations for these spacecraft are shown in Figure 2. In total, 127 HL IB observations and 127 LL IB observations were found on the night side for which at least one of the GOES or THEMIS satellites was conjugate with the IB observation. Exact times and locations of each IB observation are provided in the supporting information.

Figure 2a shows examples of conjugate satellite positions in the \( x-y \) geocentric solar magnetospheric (GSM) plane, with THEMIS A locations marked with turquoise pentagons and GOES 11 locations with purple triangles. THEMIS D and E, not shown, had orbits somewhat similar to that of THEMIS A, while GOES 12–15 were in geosynchronous orbits similar to that of GOES 11. Satellite locations were obtained using orbital data from the Satellite Situation Center Web (https://sscweb.gsfc.nasa.gov). The markers in Figure 2a show satellite positions for all the times at which the respective satellite was conjugate with an IB observation.

Figures 2b and 2c show the relative positions of THEMIS A, D, and E at 0700 UT on 5 April, when all three were near apogee. Figure 2b shows the \( x-y \) (GSM) plane, while Figure 2c shows the \( y-z \) plane. THEMIS E is depicted as a purple hexagon, and THEMIS D as an orange diamond. Note that the spacecraft are spaced relatively closely in \( x \) and \( y \), but THEMIS A is separated significantly in the \( z \) direction from THEMIS D and E. This configuration allows the estimation of gradients in the \( z \) direction by computing a difference between THEMIS A and E. Configurations like this existed a significant part of the time interval under study, and we used such satellite configurations to estimate \( R_c \) and its influence on \( K \).
3 Methodology

For each of the 227 IB crossings identified as described in the previous section, we trace a magnetic field line from the location of the IB observation, and compute \( K = \frac{R_c}{r_g} \) at the point along the field line that is farthest from the Earth. Both the field line tracing and the computation of \( K \) require a model to estimate the magnetic fields. For this purpose we use MHD simulations executed using the Space Weather Modeling Framework (SWMF) (Tóth et al., 2005) and the T01 (Tsyganenko, 2002), TS05 (Tsyganenko & Sitnov, 2005), and TA16 (Tsyganenko & Andreeva, 2016) empirical magnetic field models. The set-up for the SWMF simulations is described in detail later in this section, and the empirical models are described in section 6.

The point of maximum distance from the Earth was chosen as an estimate of where the field line crosses the current sheet. Although intuitively the point of minimum \( |B| \) would indicate the current sheet, we found that in some cases the field line is “pinched” around the current sheet, producing an additional pair of local minima in \( |B| \) which are sometimes lower than the minimum that occurs when the field line crosses the current sheet. As a result the maximum distance proved to be a more robust indicator of where the field line crossed the current sheet. In a few cases the field line traced from the IB location was found to be open (extending outside the MHD domain), and such cases were excluded from further analysis.

At the point of maximum distance from the Earth along the field line, we compute \( R_c \), the field line radius of curvature, given by

\[
R_c = \frac{1}{|\mathbf{b} \cdot \nabla \mathbf{b}|},
\]

where \( \mathbf{b} \) is the unit vector in the direction of the local magnetic field. The gradient \( \nabla \mathbf{b} \) is computed using a two-point centered difference scheme on the MHD grid. The effective gyroradius \( r_g \) is computed for protons whose energy is equal to the low energy limit of the respective detector, as given in Table S1 in the supporting information. We then use these estimates of \( R_c \) and \( r_g \) to compute \( K \). We rejected any \( K \) estimates below 0.01.

Our SWMF simulations use the Block Adaptive Tree Solar-Wind, Roe-type Upwind Scheme (BATS-R-US) MHD code (DeZeeuw, Gombosi, Groth, Powell, & Stout,

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2000; Powell, Roe, Linde, Gombosi, & De Zeeuw, 1999). This is coupled with the Rice
Convection Model (RCM) (Sazykin, 2000; Toffoletto, Sazykin, Spiro, & Wolf, 2003; Wolf
et al., 1982) and the Ridley Ionosphere Model (RIM) (Ridley, Gombosi, & De Zeeuw,
2004; Ridley & Liemohn, 2002). The inputs to the model are solar wind parameters (ve-
clocity, density, temperature, and magnetic field) and F10.7 solar radio flux, as shown in
Figure 1. Solar wind parameters were obtained from the 1-minute OMNI data set. F10.7
flux was obtained from the noontime flux observed at Penticton, British Columbia and
published online at ftp://ftp.geolab.nrcan.gc.ca/data/solar_flux/daily_flux_values/
fluxtable.txt (Tapping, 2013).

We ran three SWMF simulations, with the same inputs but with different grid res-
olutions and differences in numerical schemes and coupling parameters. By comparing
the results obtained with the three simulations we are able to assess qualitatively how
sensitive the model-derived $K$ values are to the model settings. The three simulations
are the same as those in Haiducek et al. (2019 accepted), and details on the settings can
be found there and in Haiducek, Welling, Ganushkina, Morley, and Ozturk (2017) which
shares some of the settings in common. We describe them briefly here:

- **SWMFa**: Same settings as Ilie et al. (2015), but with modifications to improve
  stability (details in Haiducek et al. (2019 accepted)). 4 million cell grid, with 0.25
  $R_E$ cell size in the expected region of IB formation.
- **SWMFb**: A 2 million cell grid, with a finer resolution the mid tail (48–120 $R_E$)
  compared with SWMFa, but courser resolution farther down-tail (beyond 120 $R_E$).
  0.25 $R_E$ cell size in the expected region of IB formation. Settings described in de-
  tail in Haiducek et al. (2017) where this model configuration is referred to as the
  “Hi-res” configuration.
- **SWMFc**: A 1 million cell grid with settings based on those used operationally
  by the NOAA Space Weather Prediction Center. 0.5 $R_E$ cell size in the expected
  region of IB formation. Settings are described in detail in Haiducek et al. (2017),
  where this model configuration is referred to as the “SWPC” configuration.

During execution of the simulations, magnetic field lines were traced from the lo-
cations of each IB observation once every minute of simulation time. Within the MHD
domain, the field lines were traced using a third order Runge-Kutta scheme with a sec-
ond order error estimation and adaptive step size. Since the inner boundary of the MHD

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domain was set to 2.5 $R_E$, well above the altitude of the IB observations, the IB locations were mapped to 2.5 $R_E$ prior to tracing through the MHD domain. This was done by transforming the IB locations into altitude adjusted corrected geomagnetic coordinates (AACGM, Baker & Wing, 1989) with the reference height set to 0 km, and then mapping to 2.5 $R_E$ using a dipole field. The use of AACGM coordinates minimizes the influence of non-dipole harmonics on the mapping.

4 Comparison of MHD magnetic fields with in situ observations

Before analyzing the IB observations using MHD, we made a comparison of the MHD magnetic fields with in situ observations. This provides a means to verify that the simulation accurately reproduces the magnetic field in the magnetotail. An example of this comparison is shown in Figure 3, which contains plots of simulated and observed magnetic fields along the orbit of the THEMIS A satellite. (Similar plots for THEMIS D and E and GOES 11–15 are included in the supporting information.) Figures 3a, 3c, and 3e show the $x$, $y$, and $z$ (GSM) components of the total magnetic field, while Figures 3b, 3d, and 3f show the same for the external field. In all of these plots, the observed field is depicted as a light blue curve, and the SWMFa, SWMFb, and SWMFc simulations are shown as thinner curves colored in medium blue, orange, and green, respectively. THEMIS data were downloaded and calibrated using the THEMIS Data Analysis Software (TDAS, http://themis.ssl.berkeley.edu/software.shtml). Magnetic field data are shown only for times when the satellite was at least 4 $R_E$ away from the Earth, since closer locations do not satisfy our selection criteria for analysis. The time period shown is 0009 UT on 4 April to 1400 UT on 6 April 2010, an interval which includes the times of all the IB observations used in this study.

The external magnetic field shown in Figures 3b, 3d, and 3f was obtained by removing dipole component of the Earth’s intrinsic field, evaluated using Geopack (http://geo.phys.spbu.ru/~tsyganenko/modeling.html). We remove only the dipole component because that is how the intrinsic field is represented within SWMF. As mentioned in the previous section, the influence of non-dipole harmonics on the $K$ estimations is minimized by converting the IB locations to AACGM coordinates prior to tracing the fields in SWMF. Points where the spacecraft is closer than 4 $R_E$ to the Earth have been excluded from the plot, since such points do not meet the criteria for selection of conjugate points with IB observations.
Multiple sign changes in $B_x$ can be seen in Figure 3a, which are indicative of current sheet crossings. This occurs most noticeably between 0900 and 1600 UT on 5 April during the initial phases of the storm, and a few additional current sheet crossings occur between 2100 and 0200 UT on 5–6 April and around 1200 on 6 April.

From Figure 3, it can be seen that the SWMF simulations reproduce many of the major variations in the observed field. During the quiet period before the storm, the error generally remains within 25 nT in all three components (Figures 3b, 3d, and 3f).

Figure 3. Magnetic field components of the total field in GSM coordinates at the THEMIS A satellite, observed and simulated, from 0009 UT on 5 April to 1400 UT on 6 April, 2010.

At the storm sudden commencement around 0900 UT on 5 April, a sharp increase in observed $B_z$ occurs, and is accompanied by an increase in $B_x$ and oscillations in $B_y$. Similar behavior occurs in the simulations, but the timing is slightly different and the variation in $B_x$ and $B_y$ is weaker than observed. After the storm sudden commencement, all three simulations reproduce the general trend in the observations, in which $B_x$ and $B_y$ become more negative, and $B_z$ increases sharply and then decreases. Like the observations, rapid fluctuations in $B_x$ and $B_y$ are apparent, though the magnitude of these fluctuations is weaker and the timing is not exactly the same as the observations. In some cases this results in particularly large magnetic field errors such as the spike in $B_x$ around 1200 UT on 5 April which was not reproduced by any of the simulations. The somewhat weaker magnitude of oscillations in the model output may indicate a thicker or weaker current sheet compared with reality. From about 1300 to 1800 UT on 5 April the simulations produce more negative $B_x$ than observed, which suggests that the model current sheet is more northerly than actual during that time, or that the current in the model is stronger than actual. During the next orbit of the spacecraft (2100 UT on 5 April to 1400 UT on 6 April) the conditions are somewhat quieter, with the largest disturbance being a brief but substantial ($\approx 60$ nT) oscillation in $B_x$ and $B_y$ around 2400 UT and a weaker one around 0300 UT, neither of which is reproduced by the simulations. Some fairly large ($\approx 50$ nT) errors occur in SWMFb between 2200 and 2400. Aside from the aforementioned periods, the simulation fields during the second orbit remained generally within 20 nT of the observations.
5 MHD results

Figure 4 shows the behavior of the $Kp$ and $Symh-H$ indices and the IB mapping parameters over the course of the storm. Figures 4a and 4b show $Kp$ and $Symh-H^*$, respectively, with the observations drawn with thick light-blue lines and the SWMF simulations with thinner lines (SWMFa in blue, SWMFb in orange, and SWMFc in green). $Symh-H^*$ is computed from the $Symh-H$ index by applying a correction for solar wind dynamic pressure $p_{\text{dyn}}$ using the same formula as the Dst* index given in Burton, McPherron, and Russell (1975). This correction removes the contribution of the magnetopause current to $Symh-H$. Figure 4c shows the absolute value of the AACGM magnetic latitude at which each IB was observed. Observations from the equatorward boundary of the IB (abbreviated as LL for low latitude) are shown in blue, while observations from the poleward boundary of the IB (abbreviated as HL for high latitude) are shown in red. The two boundaries are identified according to the procedure from Dubyagin et al. (2018), as discussed in the previous section. Figure 4d shows the MLT of each IB observation, with red and blue markers identifying the HL and LL IB observations as in Figure 4c. Figure 4e shows the maximum distance from the Earth along the field line traced from each of these IB observations, which as discussed earlier is used to estimate the current sheet crossing location. The points in Figure 4e include both the HL and the LL sets. The results for each SWMF simulation are shown, with SWMFa depicted as blue circles, SWMFb as orange squares, and SWMFc as green triangles. Figure 4f shows the values of $K$ obtained from the MHD solution at the locations depicted in Figure 4e.

Figure 4. IB parameters and geomagnetic indices as a function of time. (a) $Kp$ index, observed and simulated, (b) $Symh-H^*$ index, observed and simulated, (c) Absolute value of magnetic latitude of the IB observations, (d) MLT of the IB observations, (e) Maximum down-tail distance of the field lines mapped from the IB locations, for each of the three MHD simulations, (f) $K$ computed from the MHD solution at the farthest point of each field line.

From Figure 4a it is apparent that the simulated $Kp$ is generally within 1 $Kp$ unit of the observations, except for a $Kp$ of zero computed at the beginning of the simulations, an early increase in $Kp$ three hours before the storm begins and a decrease in $Kp$ reported by SWMFc near the end of the storm. Figure 4b shows that the simulated $Symh$-
$H^*$ values are generally within 20 nT of the observed $Symh-H^*$, with exceptions being an overestimation (in magnitude) of $Symh-H^*$ during some of the stronger periods of the storm, and an underestimation (in magnitude) of $Symh-H^*$ by SWMFc near the end of the storm.

From Figure 4c it is apparent that the IB latitude varies over time during the storm. The few quiet time IB observations are spaced fairly close together in latitude, and their latitude gradually increases from around 63 to 66 degrees between 0300 and 0800 UT. When the storm commences around 0900 UT, the IB latitude sharply decreases to around 62 degrees. 62 degrees remains the most common latitude for the next several hours, but outlier IB observations occur as high as 73 degrees. After 2000 UT, the number and severity of high-latitude outliers decreases somewhat, and the lower latitude limit of IB observations initially decreases to 60 degrees around 2400 UT on 5 April, then increases gradually until reaching 64 degrees around 1200 UT on 6 April.

Figure 4d shows that there are distinct trends in MLT over time as well. These trends are due mainly to the orbital motion of the conjugate satellites over time. Since IB latitude is known to vary with MLT (e.g. Asikainen et al., 2010; Dubyagin et al., 2018; Ganushkina et al., 2005; Lvova et al., 2005), these variations in MLT are probably responsible for some of the variations in IB latitude seen in Figure 4c.

The distances in Figure 4e reflect the latitudes shown in Figure 4c: The distances tend to increase when the IB latitudes increases, and decrease when the IB latitudes decrease. This correspondence between latitude and mapping distance is expected. For a dipole field, distance increases monotonically with increasing latitude of field line footpoints, and the stretched geometry of the night side magnetosphere results in an even faster increase. A similar correspondence with latitude can be seen in Figure 4f, but the behavior is reversed, with the $K$ estimates tending to decrease with increasing IB latitude.

The overall range of $K$ estimations from the SWMF simulations is shown in the first two rows of Table 1, which shows the total number of usable $K$ estimations in each row, 25th percentile, median, and 75th percentile of the $K$ estimations. Results from all three SWMF simulations are combined together in Table 1, and only usable $K$ estimates are included (those for which the traced field line was closed, and $K$ was greater than 0.01). The percentiles for $K = 8$ and $K = 13$ (i.e., the percentage of $K$ values falling...
below $K = 8$ and $K = 13$) are also shown. The number of $K$ estimates falling below these thresholds provides an estimate for what percentage of the IB’s might have been formed by CSS. By using two different thresholds we are able to provide a rough estimate of the uncertainty range for this percentage. The $K_{\text{crit}} = 8$ threshold, as discussed in the Introduction, was originally introduced by V. Sergeev et al. (1983) as a rough estimate of the threshold condition for CSS, and has been widely adopted by other researchers. In the present work, we adopt $K = 8$ as a probable low end of the uncertainty range for $K_{\text{crit}}$. For the upper end, we note that V. A. Sergeev, Chernyaev, et al. (2015) found differences in the properties of IB’s above and below $K = 13$, while Dubyagin et al. (2018) found that $4.5 < K < 13$ fell within $1 R_E$ of where $K = 8$ for 90% of field configurations produced by the TS05 model, and Haiducek et al. (2019 accepted) obtained corrected $K$ values falling mostly below $K = 11$ for carefully chosen IB observations in quiet conditions. Based on these results, we have adopted $K = 13$ as an approximate upper end of the uncertainty range for $K_{\text{crit}}$. The results in Table 1 are separated according to whether they were obtained from observations of the high-latitude (HL) or low-latitude (LL) boundary of the IB. Both the medians and the interquartile ranges of $K$ are somewhat higher for the LL set, consistent with the tendency noted in the previous paragraph that increases in IB latitude are associated with decreases in $K$ and vice versa. The remaining rows of Table 1 will be discussed later in the paper.

The negative correlation between the estimated $K$ in the IB formation region and IB latitude can be explained by both the EMIC wave and the CSS mechanisms, noting that the value of $K$ can be approximated as

$$K = \frac{R_e}{T_k} \approx \frac{q B_z^2}{\sqrt{2} m E d B_r/dz},$$  \hspace{1cm} (2)$$

where $q$ denotes the particle charge, $m$ the particle mass, and $E$ the particle energy. $B_r$ is the radial component of magnetic field in GSM coordinates, given by

$$B_r = \frac{x B_x + y B_y}{\sqrt{x^2 + y^2}}.$$  \hspace{1cm} (3)$$

$B_z$ near the equatorial plane decreases as $1/r^2$ in a dipole field, and the stretched field lines in the night side magnetosphere result in even faster decrease. This tends to result in an inverse relationship where $K$ decreases with increasing distance. If the IB forma-
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**Uncorrected $K$**

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**$K^*$ correction**

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Table 1. Values summarizing the distribution of $K$ and $K^*$.
tion process is independent of \( K \) (as is the case for EMIC wave scattering), the IB latitude roughly corresponds to the distance of the IB field line in the equatorial plane, resulting in a negative correlation between IB latitude and \( K \). For CSS-driven IB formation, this relationship between \( K \) and distance from the Earth should be absent since we are computing \( K \) at points mapped from the IB, and IB formation through CSS is directly controlled by \( K \). However, if the simulation fails to respond to fast variations in the magnetosphere, the IB will be projected to (and \( K \) estimated at) points distributed around the true IB formation region, and the deviation of the model \( K \) estimates from reality will reflect the average radial profile of \( K \), with associated negative correlation between \( K \) and IB latitude. Thus, the approximately inverse relationship between \( K \) and distance seen in Figures 4e and 4f could indicate a failure of the model to reproduce the true magnetic field geometry, or it could indicate that some of the observed IB’s were formed by EMIC scattering.

Noting the quadratic dependence of \( K \) on \( B_z \) in equation (2), we estimate the error in \( B_z \) at the locations were \( K \) was estimated by computing the \( B_z \) errors at the spacecraft that are conjugate with each IB location. The conjugate spacecraft include at least one and in some cases several of the GOES and THEMIS satellites. We denote the averaged error as \( \Delta B_z \). Figure 5 shows \( K \) as a function of \( \Delta B_z \) for the points from Figure 4. Figure 5a shows the HL points, while 5b shows the LL points. Results from each model run are depicted using the same color and marker scheme as Figure 4. Fit lines are drawn in black on top of the points. Note that a logarithmic scale is used for the y axis and a linear fit has been performed on the transformed data; the reason for this will be explained later. Points that mapped to within 8 \( R_E \) of the MHD domain boundaries have been excluded.

**Figure 5.** \( K \) as a function of \( \Delta B_z \) for all three MHD simulations, computed for locations mapped from IB observations in the HL data set (a) and the LL data set (b). Black lines show linear fits (in log space) to the data.

Figure 5 shows that \( K \) increases with increasing \( \Delta B_z \). Noting the quadratic dependence of \( K \) on \( B_z \) in equation (2), \( K \) at the IB location will be overestimated if the model overestimates \( B_z \). In addition, this effect is strengthened by the mapping error;
because understretched model fields map the IB field line closer to the Earth, in the region of higher $K$.

From Figure 5 it appears that the SWMF has a tendency to over-predict $B_z$, with a substantial fraction of the $\Delta B_z$ values falling between 0 and 20 nT. Indeed, we found that the SWMF simulations overestimated $\Delta B_z$ about 65–70% of the time (more detailed statistics for $\Delta B_z$ are given in Table S2 in the supporting information). Most of the $K$ values corresponding to $\Delta B_z > 0$ fall within the interquartile ranges shown in the first two rows of Table 1. Anomalously low $K$ values ($K \lesssim 4$) appear only when $\Delta B_z \lesssim 12$. Despite the correlation between $K$ and $\Delta B_z$, $K$ values seem to be constrained to $K \lesssim 100$, with $K$ remaining below that threshold even for the largest overestimations of $B_z$.

6 Empirical results

In this work we use the empirical magnetic field models T01, TS05, and TA16. All three are available at http://geo.phys.spbu.ru/~tsyganenko/modeling.html. These models operate by computing a sum of analytical functions of a set of solar wind and geomagnetic activity parameters. In the case of T01 and TS05 these functions represent specific current systems, while in TA16 they are radial basis functions with no correspondence among the known current systems in the magnetosphere.

We now describe some of the features of these models that are relevant to estimating $K$. In the T01 model, the current sheet thickness is constant, but the inner edge of the tail current moves Earthward with increasing activity, and the tail current radial profile is controlled by two independent sub-modules.

The TS05 model was designed specifically to model storm-time conditions, and it was constructed by fitting to data from storm periods. The position and thickness of the TS05 tail current vary with activity, and are parameterized by a complex integral functions of the time history of solar wind parameters.

While the T01 and TS05 models used pre-determined functions to define the magnetospheric current systems, the TA16 model replaces these ad hoc functions with a sum of radial basis functions controlled by driving parameters (Newell, Sotirelis, Liou, Meng, & Rich, 2007). This avoids imposing assumptions about the form of the current systems through the choice of fitting functions. However, the limited number of observations available for fitting precludes resolving fine spatial structures by this method.

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We traced field lines from the IB locations (in AACGM coordinates) using each of these models, and with a dipole representation for intrinsic field of the Earth. Geopack was used to perform the actual tracing of the field lines. As with the SWMF simulations, \( K = \frac{r_g}{r} \) was estimated at the point of maximum distance from the Earth along each field line, using the detector cutoff energies (Table S1 in the supporting information) to estimate \( r_g \) and equation (1) to estimate \( R_c \). The output from the models was also computed at the locations of the THEMIS spacecraft for comparison with observations.

Figure 6 shows the \( K \) values obtained from the empirical models as a function of \( \Delta B_z \), which as with the SWMF simulations represents the model error in \( B_z \), averaged over the THEMIS spacecraft that were conjugate with each IB observation. Points from T01 are shown as red diamonds, TS05 as purple right-pointing triangles, and TA16 as brown left-pointing triangles. Figure 6a shows the HL data, and Figure 6b shows the LL data. A least-squares fit (in log-space) through all the points is shown in black. It appears that the three models performed similarly, and a general similarity with the SWMF simulations is also apparent, although the \( K \) values are somewhat lower and the tendency to overestimate \( B_z \) is less pronounced.

From Figure 6 it is also apparent that the T01 model has a tendency toward underestimation of \( \Delta B_z \), while the TS05 and TA16 models tend toward overestimation of \( \Delta B_z \). This is further supported by the metrics for \( \Delta B_z \) given in Table S2 of the supporting information.

The third and fourth rows of Table 1 summarize the range of \( K \) obtained from the empirical models. As with the SWMF results, the empirical model results in the table were obtained by combining the results from all the empirical models together. \( K \) estimates below 0.01 were excluded from the results. Like the SWMF estimates of \( K \), the median, 25th, and 75th percentiles are all higher for the LL data set than for the HL data set. \( K \) values at all three quartiles are lower than they are for SWMF, indicating a sys-
tematic tendency toward lower $K$ values with the empirical models. On the other hand, the interquartile ranges overlap substantially between the two classes of models.

7 $K$ correction

We have seen that both the SWMF simulations and the empirical models have tendencies to over- or under-estimate $B_z$ relative to in situ observations in the magnetotail. However, both the SWMF simulations and the empirical models exhibit a positive correlation between $K$ and $\Delta B_z$, which is consistent with the quadratic relationship between $K$ and $B_z$ seen in equation (2). This relationship enables us to correct the model-derived $K$ values for the known errors in $B_z$, using the correction procedure previously described in Dubyagin et al. (2018) and Haiducek et al. (2019 accepted). The procedure consists of taking the logarithm of both sides of equation (2), then linearizing to obtain a linear equation of the form

$$\log K = A_1 + A_2 \Delta B_z,$$

where $A_1$ and $A_2$ are obtained from the fit line shown in Figures 5 and 6. From this we obtain a corrected value $K^*$, which estimates the value $K$ would have in the absence of $B_z$ errors, and is given by

$$K^* = K \exp(-A_2 \Delta B_z).$$

The lower half of Table 1 shows statistics for $K^*$. As with the $K$ results, data are shown for the SWMF simulations, empirical models, and both together. Each is further broken down into results for the HL and LL IB observations. For $K^*$, the $y$ axis intercept from the fit of equation (4) is also given, along with its 95% confidence interval. The intercepts provide an estimation of what the average value of $K$ would be in the case of zero magnetic field error.

From the values in Table 1, it is apparent that the SWMF tends to produce higher values of $K$ (as indicated by the higher median and interquartile ranges) compared with the empirical models. The $K^*$ correction tends to produce smaller values compared with the uncorrected $K$ values, while also reducing the amount of difference between the SWMF and the empirical model results compared with $K$. 

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The values in Table 1 also show that the LL IB observations tended to be associated with larger values of $K$ and $K^*$ compared with the HL observations. Each of the rows of the table showing data from the LL set has a higher median than the corresponding row from the HL set. For instance, the SWMF $K$ estimations for the HL set have a median of 10.7, while those from the LL set have a median of 11.0. Similarly, the empirical model estimations for the HL set have a median of 10.8, while those for the LL set have a median of 14.3. This is consistent with the expected relationship between $K$ and latitude discussed earlier.

The $K = 8$ and $K = 13$ percentiles in Table 1 provide an estimate of what fraction of the IB observations might have been produced by current sheet scattering (for which $K \lesssim 8–13$ is expected). The remaining IB observations (those for which $K \gtrsim 8–13$) could potentially be the result of EMIC wave interactions. For SWMF, 23.6% of the uncorrected HL $K$ values fall below $K = 8$, and 38.6% fall below $K = 13$; for the LL set it is 20.1% and 35.1%. For the empirical models 40.2% of the values from the HL set are below $K = 8$ and 61.4% are below $K = 13$, while for the LL set it is 31.5% and 52.7%. The $K^*$ correction increases the number of SWMF estimates that fall below the $K = 8$ and $K = 13$ thresholds, to 29.1% and 51.6%, respectively, for the HL set, and 23.3% and 42.2%, respectively, for the LL set. The $K^*$ correction has a somewhat less significant effect on the empirical model results, with the percentages below the $K = 8$ and $K = 13$ falling within 5% compared with the uncorrected $K$.

Figure 7 shows the distributions of $K$ before and after correction, represented using kernel density estimation (KDE, Parzen, 1962). A KDE approximates a PDF by convolving a set of discrete points with a Gaussian kernel. The resulting plot can be interpreted in much the same way as a normalized histogram. The high-latitude (HL) IB data is shown in blue, and low-latitude (LL) IB data is shown in orange. Figure 7a shows the distribution of $K$ values estimated by SWMF, while Figure 7b shows the corresponding distribution of $K^*$. Figures 7c and 7d show $K$ and $K^*$ for the empirical models, while Figures 7e and 7f show the results of combining the SWMF and empirical results into a single data set and computing $K^*$ for the combined data set.

The empirical models (Figure 7c) produce slightly narrower distributions of $K$ compared with SWMF (Figure 7a), but after correction the distributions become more comparable, and the SWMF distribution of $K^*$ for the HL set (Figure 7b) is slightly nar-
Figure 7. Distributions of (a) $K$ and (b) $K^*$ for all three MHD simulations, and distributions of (c) $K$ and (d) $K^*$ for all empirical models. (e) and (f) show SWMF and empirical models together. The distributions have been separated according to whether the observations came from the high-latitude (HL) or the low-latitude (LL) edge of the IB.

rower than that of the empirical models (Figure 7d). For both classes of models, the $K^*$ correction (Figures 7b, 7d, and 7f) produces a narrower distribution for the HL set compared with the uncorrected $K$ values (Figures 7a, 7c, and 7e). However, for the LL set the opposite is true, with the SWMF distribution being relatively unaffected and the empirical distribution being widened appreciably. In all the distributions of Figure 7, a noticeable difference can be seen between the LL and HL data. For values of $K$ and $K^*$ greater than about 20, the probability density is higher for the LL set than for the HL set, while for values less than this, the probability density is higher for the HL set than for the LL set. This means that the LL points tend to be associated with higher values of $K$. This is consistent with the tendency previously noted in Table 1. When the $K^*$ correction (Figures 7b, 7d, and 7f) is applied, the same pattern is seen that LL observations are associated with higher values, and the effect is more pronounced for the corrected values.

8 Discussion

The goal of this study is to test what fraction of observed IB’s during the storm on 4–6 April 2010 may have been the result of CSS. To accomplish this, we estimated $K = \frac{R_c}{r_g}$ associated with ion isotropic boundary observations. $K$ provides a measure of the effectiveness of the CSS process at a particular location. We used MHD and empirical models to trace field lines from the IB observation locations to the magnetotail, and to estimate $K$ where those field lines cross the current sheet. We then corrected our $K$ estimations for errors in the model magnetic fields that could be quantified with in situ observations from spacecraft in the magnetotail. By correcting for these errors, and by using of multiple models to estimate $K$, we are able to constrain the possible range of $K$. This is the first study to explore IB properties using an MHD model during storm conditions.
A number of previous studies have noted a tendency for SWMF to produce understretched magnetic fields on the night side. As discussed in section 5, this is expected to result in overestimation of $K$. Glocer et al. (2009) found that SWMF overestimated $B_z$ at GOES spacecraft during storms on 4 May 1998 and 31 March 2001, though they also found that this could be improved by coupling a wind model to BATS-R-US. Gamushkina, Liemohn, Kubyshkina, Ilie, and Singer (2010) showed that SWMF overestimated $B_z$ at GOES spacecraft during storms on 6–7 November, 1997 and 21–23 October, 1998. Ilie et al. (2015) reported over-prediction at GOES, Geotail, and THEMIS spacecraft during a quiet interval on 13 February, 2009, and Haiducek et al. (2019 accepted) reported this for different simulations of the same event. In the present study we find this tendency as well, with all three simulations overestimating $B_z$ for about 65–70% of the IB observations.

The amount of tail stretching in TA16 was previously reported to be similar to the older T89 model (Tsyganenko & Andreeva, 2016), which in turn has been reported as producing overstretched fields in the magnetotail (Peredo, Stern, & Tsyganenko, 1993; Tsyganenko, 1989). Haiducek et al. (2019 accepted) reported understretched fields for T01 and overstretched fields in TS05 and TA16. Results in the present work show a slight tendency toward over-stretching in T01, but a slight tendency toward under-stretching in TS05 and TA16, based on errors in $B_z$ relative to in situ observations.

Compared with SWMF, the empirical models tend to produce smaller values of $K$, consistent with the tendency noted above of understretched fields in SWMF and overstretched fields in the empirical models. However, the distributions of $K$ overlap significantly between the two classes of models even before correction. The median $K$ values and percentiles in Table 1 demonstrate that, after correction, the difference between the distributions of $K$ obtained using MHD and those obtained using the empirical models is less than the difference between the $K$ distributions found by using different criteria of IB selection (HL or LL data sets). This is different from the quiet time results of Haiducek et al. (2019 accepted), which included non-overlapping distributions of uncorrected $K$, with the empirical models tending toward quite small values of $K$ and the SWMF $K$ values uniformly above 10. The overlapping distributions reflect the presence of much higher $K$ estimates (on average) coming from the empirical models compared with Haiducek et al. (2019 accepted), along with marginally lower $K$ estimates from SWMF and broader distributions for both classes of models. The broader distributions are probably the re-
result of using less restrictive selection criteria for the IB observations, as well as storm-time variability. Storm conditions likely increase the range of $K$ estimates both by causing the true value of $K$ to vary more broadly (due to EMIC scattering, as well as producing CSS under a wider variety of conditions). Storm conditions also create rapidly varying dynamics which the models are not always able to reproduce, contributing to errors in magnetic field configuration and causing randomly varying errors in $K$.

The results of our study are somewhat different from those obtained by Dubyagin et al. (2018) using the TS05 model in the 21–03 MLT sector for larger statistics (nine storms, > 200 IB observations). Dubyagin et al. (2018) found that 68% of the events in their HL data set had $K^* < 13$, which is reasonably close to the 66.1% obtained from the HL data set using empirical models in our study. However, 63% of their LL IB’s had $K^* < 13$, which is significantly higher than the 51.3% in our LL data set (see Table 1). In both cases the percentages are lower. When the SWMF results are added, the percentages decrease further since SWMF tends to produce higher values for $K$ and $K^*$. Finally using a $K^* < 8$ threshold condition reduces the percentages further. The lower percentages we obtained compared to Dubyagin et al. (2018) can be attributed to several factors including

- A different methodology for estimating the uncertainty (the use of two $K$ thresholds versus a single one)
- The use of multiple models (three empirical models, plus three MHD simulations) in the present work, compared with a single empirical model in Dubyagin et al. (2018)
- The application of additional restrictions on MLT and $\Delta B_z$ by Dubyagin et al. (2018)
- Differences in the magnetospheric state between the storm we analyzed and those analyzed in Dubyagin et al. (2018)

Given the differences in the analysis, and in the events included in the two studies, our paper and Dubyagin et al. (2018) should be considered complementary, but some caution should be applied when making quantitative comparisons between the two.

The results in Haiducek et al. (2019 accepted) made it clear that errors in the magnetic field models can affect $K$ values significantly, but also that such errors, if quanti-
fied, can be corrected for effectively. However, it should be noted that the corrections provide only a rough estimate of the true value of $K$. These corrections are subject to a number of sources of uncertainty, including errors due to the linearization of the expression for $K$, the position of satellites relative to where $K$ is actually estimated, and the fact that our correction procedure involves a fit to numerous $K$ estimates from numerous IB observations, each of which came from a different time, with a different magnetospheric state and different satellite positions for each. By fitting all of these points together we find the average relationship between the magnetic field errors and $K$ estimates. The true relationship between the two probably varies with the magnetospheric state and the satellite positions, which our correction procedure does not account for. With the $\Delta B_z$ estimates there is a potential issue with the GOES magnetometer data in that it may contain offsets of unknown magnitude (Singer et al., 1996).

Despite these sources of uncertainty, there are indications that the correction procedure is successful in removing much of the difference between the two classes of models. The distributions of $K$ become narrower and substantially more similar to each other after correction. While we have no ground-truth measurement with which to test our $K$ estimations, we interpret the similarity between the distributions of $K$ obtained by very different types of models as a sign that both are likely reproducing the major characteristics of the true $K$ distribution. On the other hand, we also noted in section 7 that the correction procedure seems to amplify the differences between the HL and LL data sets. This is largely due to the correction procedure narrowing the distribution of $K$ obtained from the HL IB observations, while the distribution of $K$ derived from the LL data is relatively unchanged. This could indicate that the LL data are subject to greater inaccuracies in the $\Delta B_z$ estimates used in the correction, or that the LL data are more sensitive to additional error terms not included in the correction procedure. Another possibility is that variance in the incident particle population prior to scattering plays a greater role for the particles observed at the LL latitudes. Finally, it is possible that the procedure used to identify the HL and LL locations is somehow more precise for the HL latitudes.

In addition to checking the $K$ values to determine whether they are below a given threshold value, we can also check for a dependence on MLT as an indication of whether CSS is the mechanism responsible for IB formation. EMIC scattering has been noted to contribute significantly to proton precipitation in the dusk sector (e.g. Fuselier, 2004; Yah-
A number of previous studies have found a noon-midnight asymmetry in IB latitude, characterized by a night side minimum latitude and a day side maximum latitude (e.g. Asikainen et al., 2010; Ganushkina et al., 2005; V. A. Sergeev et al., 1993; Yue et al., 2014). In addition, many studies have found a tendency for IB latitude to decrease as Symh-H becomes more negative (e.g. Asikainen et al., 2010; Dubyagin et al., 2018; Ganushkina et al., 2005; Hauge & Søraas, 1975; Lvova et al., 2005; Søraas et al., 2002). In most cases the noon-midnight asymmetry in latitude is accompanied by a weaker dawn-dusk asymmetry, with the minimum IB latitude occurring around 23 MLT (e.g. Asikainen et al., 2010; Ganushkina et al., 2005; Lvova et al., 2005; Newell et al., 1998; V. A. Sergeev, Bikkuzina, & Newell, 1997; Yue et al., 2014). Figures 8a and 8b show the latitude of our IB observations as a function of MLT, with the HL data set shown in Figure 8a and the LL data set in 8b. As has been seen by previous authors, the minimum IB latitude occurs in the pre-midnight sector, and a dawn-dusk asymmetry is clearly visible. A correlation with Symh-H is also apparent. Figures 8c and 8d show $K^*$ as a function of MLT, with the HL data in Figure 8c and the LL data in Figure 8d. All plots of Figure 8 are colored by Symh-H*, and SWMF results are plotted with triangles while empirical models are plotted with squares. Figure 8 shows that $K^*$ exhibits none of the trends found in the IB latitude, which is consistent with CSS playing a significant role in IB formation since it suggests that $K$ is controlling the pitch angle scattering rather than some other process. Note however that the MLT dependence shown in Figure 8 is affected by the motions of the GOES and THEMIS satellites since we use only IB observations that are conjugate with those spacecraft. It should be noted that independence of the K parameter on MLT was also found by Dubyagin et al. (2018) using only empirical models. However, that study concentrated on a narrower MLT sector (21–03 MLT), and there were serious doubts that this dependence would not emerge if 18–21 MLT sector was included. Indeed, the plasmaspheric plume is often seen at $\approx$ 18 MLT and the EMIC wave related precipitations have also been detected in this sector (Yahnin & Yahnina, 2007).
The independence of $K^*$ on MLT, despite a dependence of IB latitude on MLT, was interpreted by Dubyagin et al. (2018) as an indication that the CSS was the operative scattering mechanism for a majority of their data. Our results also find $K^*$ to be independent of MLT, even though a lower percentage of our $K^*$ values were within the expected range for CSS. We conducted additional tests in which we plotted $K^*$ as a function of MLT while limiting the data set to IB observations for which $K^*$ exceeded a specified threshold. By doing so we found that $K^*$ is independent of MLT even when $K^* > 30$. This could indicate that the lack of dependence of $K^*$ is not due to $K$ controlling the scattering process, but is simply the result of random variations in the estimated $K$ values due to mapping errors which are large enough to obscure the MLT dependence. If this is the case, then the mapping accuracy must be increased before the dependence of $K$ on MLT can be used reliably as an indicator of CSS, and comparison of $K$ with a threshold value is probably the better criterion.

The conclusions of the paper can be summarized as follows:

1. By correcting each $K$ estimate using in situ observations from 2–3 conjugate satellites in the current sheet, we were able to produce consistent results, with similar distributions of $K$ obtained using both empirical and MHD models.
2. Accounting for uncertainty in the IB latitude and in the threshold condition for $K$, we find that between 29% and 54% of the IB observations may be the result of CSS.
3. We find that $K^*$ is independent of both $Symh-H^*$ and MLT during this storm interval, and this independence persists even for high $K$ values.

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THEMIS data were retrieved using the THEMIS Data Analysis Software (TDAS; http://themis.igpp.ucla.edu/software.shtml). We acknowledge NASA contract NAS5-02099 and V. Angelopoulos for use of data from the THEMIS Mission. Specifically: K. H. Glassmeier, U. Auster and W. Baumjohann for the use of FGM data provided under the lead of the Technical University of Braunschweig and with financial support through the German Ministry for Economy and Technology and the German Center for Aviation and Space (DLR) under contract 50 OC 0302, and C. W. Carlson and J. P. McFadden for use of ESA data.

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The Spacepy python library (Burrell et al., 2018; Morley, Koller, Welling, Larsen, & Niehof, 2014; Morley et al., 2011) was used for a number of tasks related to reading and analyzing data in this paper.

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Tsyganenko, N. A. (2002, aug). A model of the near magnetosphere with a dawn-


Figure 1.
a) $u_x$ (km/s)  
b) Density ($\rho$) (cm$^{-3}$)  
c) Temperature (K)  
d) $B_z$ (nT)  
e) $S_{Sym-H}$ (nT)  
f) Kp  
g) AL (nT)

Universal time, 4-6 April 2010

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Figure 4.
\[ \Delta B_z = B_{z,\text{model}} - B_{z,\text{obs}} \text{ (nT)} \]
\[ \Delta B_z = B_{z_{\text{model}}} - B_{z_{\text{obs}}} \text{ (nT)} \]
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\[ \Delta B_z = B_{z\text{model}} - B_{z\text{obs}} \text{ (nT)} \]