# Measuring Similarity Between Mathematics Research and Its References Using Bibliographic Coupling 

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## TUMO?

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UUM:?
An analysis of the development of mathematics research overtime, with a focus on similarity between publication-reference and citation-publication pairs.

## DUTHE

In order to understand mathematics it is important to develop knowledge of how it has grown and the ways it builds upon itself.

## UFInE?

The data used is from the Clarivate Web of Science citation database, 1900-2017. All records with Web of Science category designations Mathematics; Mathematics, Applied Mathematics; and Mathematics, Interdisciplinary Applications were included in the analysis.

## HODN?

Similarity between publication pairs is measured using raw and proportional Bibliometric Coupling strength. Raw strength is the number of publications in the intersection of reference sets. The proportional strengths takes the raw counts and divide them by sizes of each publication's sotal reference set.


## 

| Category | Publication Reference Pairs | At least 1 Shared Reference (\% of total) | At least 3 (\% of total) | At least 5 (\% of total) | $\begin{aligned} & 10 \text { or more } \\ & \text { (\% of total) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mathematics | 4802134 | $\begin{aligned} & 3221604 \\ & (67.09 \%) \end{aligned}$ | $\begin{aligned} & 1443842 \\ & (30.07 \%) \end{aligned}$ | $\begin{aligned} & \hline 681683 \\ & (14.20 \%) \end{aligned}$ | $\begin{aligned} & 133506 \\ & (2.38 \%) \end{aligned}$ |
| Applied | 3765012 | $\begin{aligned} & 2579284 \\ & (68.51 \%) \end{aligned}$ | $\begin{aligned} & 1228600 \\ & (32.63 \%) \end{aligned}$ |  | $\begin{aligned} & 136962 \\ & (3.64 \%) \end{aligned}$ |
| Interdisciplinary | 918937 | $\begin{aligned} & 631977 \\ & (68.77 \%) \end{aligned}$ | $\begin{aligned} & 317735 \\ & (34.58 \%) \end{aligned}$ | $\begin{array}{\|l\|} \hline 168611 \\ (18.33 \%) \end{array}$ | $\begin{aligned} & 44386 \\ & (4.83 \%) \end{aligned}$ |
| Total | 7901392 | $\begin{gathered} 5348251 \\ (67.69 \%) \end{gathered}$ | $\begin{aligned} & 2481515 \\ & (31.41 \%) \end{aligned}$ | $\begin{aligned} & 12216547 \\ & (15.40 \%) \end{aligned}$ | $\begin{aligned} & 263331 \\ & (3.33 \%) \end{aligned}$ |



Percentage of Publication-Reference pairs sharing at least 1 reference over time


Publication


Reference


Percentage of Publication-Reference pairs sharing at least 5 references over time


Publication


Reference

Percentage of Publication-Reference Pairs with relative Percentage of Publication-Reference Pairs with relative coupling strength greater than $5 \%$ over time coupling strength greater than $20 \%$ over time

## 

| Category | Citation- <br> Publication <br> Pairs | At least I Shared <br> Reference <br> (\% of total) | At least 3 <br> (\% of total) | At least 5 <br> (\% of total) | 10 or more <br> (\% of total) |
| :--- | :--- | :--- | :--- | :--- | :---: |
| Mathematics | 4967056 | 3273539 <br> $(65.91 \%)$ | 1442886 <br> $(29.05 \%)$ | 675081 <br> $(13.59 \%)$ | 131860 <br> $(2.65 \%)$ |
| Applied | 3390481 | 2391880 <br> $(70.61 \%)$ | 1175232 <br> $(35.66 \%)$ | 599808 <br> $(17.69 \%)$ | 136182 <br> $(4.02 \%)$ |
|  | 815449 | 585437 <br> $(71.79 \%)$ | 306705 <br> $(37.61 \%)$ | 165914 <br> $(20.35 \%)$ | 44696 <br> $(5.48 \%)$ |
| Total | 7919132 | 5361943 <br> $(67.71 \%)$ | 2489505 <br> $(31.41 \%)$ | 1221186 <br> $(15.42 \%)$ | 264558 <br> $(3.34 \%)$ |



| Category | Citation- <br> Pubbication <br> Pairs | At least 1 Shared <br> Reference <br> (\% of total) | At least 3 <br> (\% of total) | At least 5 <br> (\% of total) | 10 or more <br> (\% of total) |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Mathematics | 936977 | 429699 <br> $(45.86 \%)$ | 123869 <br> $(13.22 \%)$ | 45808 <br> $(4.89 \%)$ | 6730 <br> $(0.72 \%)$ |
| Applied | 673396 | 373582 <br> $(55.48 \%)$ | 131497 <br> $(19.53 \%)$ | 53714 <br> $(7.98 \%)$ | 8788 <br> $(1.31 \%)$ |
| Interdisciplinary | 225874 | 142328 <br> $(63.01 \%)$ | 60078 <br> $(26.60 \%)$ | 26721 <br> $(11.83 \%)$ | 154 <br> $(0.80 \%)$ |
| Total | 1634021 | 838287 <br> $(51.30 \%)$ | 280299 <br> $(17.15 \%)$ | 112472 <br> $(6.88 \%)$ | 18367 <br> $(1.12 \%)$ |

## 0:5\&MURTIOMS

- While raw coupling strength for Publication-Reference pairs has increased over time, especially for higher strengths, relative coupling strength on the other hand shows a flattening for lower relative strengths and a decrease for higher one since the 1960s. This is likely related to the dramatic increase in references per publication, from a median around 7 to over 20 since 1960
- The relative coupling strength of Citation-Publication pairs shows a steady increase over time, but evidence indicates this may be caused by citing publications sharing fewer references with older publications, behavior which would drive down relative strength as a publication ages.
- There is a noticeable decrease in the raw coupling strength of Citation-Publication pairs when publications with more than 100 citations are considered. There are many possible causes of such behavior, including popular papers serving as stand-ins for the publications they reference or highly cited publications being cited due to popularity instead of applicability. - The more applied publications had higher raw coupling strength, while the more pure mathematics publications had higher relative strengths. Since applied publications by their nature will reference a broader range of publications it is logical for pure mathematics publications to be more similar relative to their reference lists.

