How Would 401(k) ‘Rothification’ Alter Saving, Retirement Security, and Inequality?

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Abstract
The U.S. has long incentivized retirement saving in 401(k) and similar retirement accounts by permitting workers to defer taxes on contributions, levying them instead when retirees withdraw funds in retirement. This paper develops a dynamic life-cycle model to show how and whether “Rothification” — that is, taxing 401(k) contributions rather than payouts — would alter household saving, investment, and Social Security claiming patterns. We show that these changes differ importantly for low- versus higher-paid workers. We conclude that moving to a system that taxes pension contributions instead of withdrawals will lead to later retirement ages, particularly for the better-educated. It also would reduce work hours and lifetime tax payments and increase wealth and consumption inequality. In addition, we show how these behaviors would differ in a persistently low interest rate environment versus a more “normal” historical return world.

Citation

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The United States has long incentivized retirement saving by deferring taxes on workers’ pension contributions until the assets are withdrawn in old age, at which point the withdrawn funds become subject to income tax. In this way, most 401(k) retirement accounts are taxed according to an “EET” regime: Workers contribute out of pretax earnings, recognize pretax investment earnings in their accounts, and pay income tax on withdrawals during retirement. This policy has a large current budgetary cost: the U.S. Treasury foregoes over $100 billion per year due to tax-deferred contributions to 401(k) and similar plans (Thornton 2017). Partly because of projected federal budget shortfalls, some policymakers have recently proposed eliminating or capping tax-qualified retirement plan contributions, a practice termed “Rothification,” named after Senator William Roth who successfully passed legislation allowing this in 1997. Specifically, the idea would be to treat all future retirement contributions to a “TEE” regime, in which workers would contribute to their pensions out of after-tax income, and then no additional tax would be levied thereafter (Schoeff 2017).

The Rothification idea has been a topic of considerable recent discussion, with former President Obama recommending a pretax pension contribution cap in 2015, and related proposals offered by the Trump Administration during the 2017 tax-reform debate. Though those proposals were not enacted, the topic is certain to be revisited given the amount of revenue involved. In an economy with a single tax rate and a flat benefit system, taxing benefits now versus later is unlikely to change behavior. Yet in the

1 The Federal Government does receive some of the deferred tax revenue later when benefits are paid out, but retirees are often in a lower tax bracket than when working. Moreover the deferral of taxes tends to mean that the revenue is not ‘captured’ in the traditional 10-year accounting window used for revenue neutrality calculations. Hence moving the tax capture forward is politically appealing to some; see Sibaie (2017).
U.S. economy, there are numerous nonlinearities in the tax and Social Security systems that render less obvious the ways in which such a reform might alter household behavior. Accordingly, if such a reform were to be passed in the future, it could have important implications for household behavior. Moreover, effects are likely to vary across different population subgroups.

To date, however, there has been no coherent microeconomic analysis of how Rothification could alter household consumption, saving, retirement patterns, and tax-payments. Our paper fills this gap by developing a richly detailed and state-of-the-art life-cycle stochastic dynamic model with endogenous work effort, portfolio choice, consumption, saving, and Social Security claiming patterns, to evaluate such a policy's potential effects for the population overall and for different population subgroups. Of key importance is heterogeneity: That is, how outcomes will differ for workers with different lifetime earnings profiles. For instance, some have argued that “Roths may not, in fact, work out to be a better deal” for low-income people (Tergesen 2017), while others argue the opposite.\(^2\) We therefore assess how key outcomes change for a variety of worker-types differentiated by sex and education.

Additionally, it is important to recognize that converting retirement plans to Roth plans would take place against the backdrop of the new income tax structure implemented in 2018, which reduced the tax burden for most earners.\(^3\) The tax reform, therefore, also changed the relative attractiveness of saving for retirement in an EET

\(^2\) Hallez (2017) reports that some predict that low-wage workers would save less in a TEE regime, whereas Statman (2017) concluded the opposite.

\(^3\) This tax reform doubled the standard deduction to calculate taxable income, cut marginal tax rates, and raised tax brackets, especially for high earners. (IRS 2018)
environment, since lower marginal tax rates on workers’ earnings decreased the attractiveness of saving in 401(k) accounts. Our research also compares how work, saving, benefit claiming behavior, and tax payments would respond in an EET versus TEE setting for a heterogeneous set of workers.

Finally, we analyze how our results would differ if the economy were to move out of the very low interest rate environment of the last decade, and return to a more “normal” regime. We know that persistent low returns spur workers to save and invest differently and can also drive different decisions about how long to work and when to claim Social Security benefits (Horneff, Maurer, and Mitchell 2018). The quantitative easing policies of the U.S. Federal Reserve Bank after the financial crisis have resulted in extraordinarily low real U.S. Treasury yields over the past decade, compared to the normal historical real return of 3% (1989-2008). We seek to study how appealing Rothification might be in this new low interest rate environment, compared to the traditional EET framework, for the $5 trillion invested in 401(k) assets.

In what follows, we first build and calibrate a structural life-cycle model, assuming an EET framework calibrated to U.S. federal/state income tax and Social Security/Medicare premium structures, and realistic Social Security benefit formulas, including adjustments for early and delayed claiming. Importantly, the baseline model also incorporates real-world rules characterizing EET tax-qualified 401(k) accounts including the current caps on 401(k) pretax contributions, employer matches, penalties and taxes on early withdrawals, and Required minimum distribution withdrawals. We show that our results agree closely with observed consumption, saving, and Social Security.

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4Based on our analysis using DataStream of U.S. Treasury rates deflated by the Consumer Price Index (CPI).
Security claiming age behavior of U.S. households, while matching the current distribution of 401(k) wealth rather nicely.

Next, we develop results under an alternative environment where 401(k) contributions are taxed according to a TEE structure. This permits U.S. to identify changes in behavior for the heterogeneous workers described above, under the two tax regimes (EET versus TEE).

Next, we compare results with those obtained in a higher real return environment. In particular, we assess whether the lower-paid behave differently from the higher-paid in terms of savings inside and outside the tax-qualified accounts, as well as in nonpension savings accounts, and whether they would change their claiming behavior for Social Security benefits. In addition, we are interested in how Rothification would alter the distribution of retirement incomes relative to the current EET-system. For example, the gap between high- and low-wage workers' take home pay is not diminished by income taxes under an EET system, whereas it is under a TEE program. Moreover, the Social Security replacement rate formula is progressive, as it provides relatively higher benefits for low-wage workers than for the higher paid. Given this, an EET scheme enhances the progressivity of overall old age income (pension account withdrawals plus Social Security benefits), whereas a TEE structure treats retirement benefits more neutrally. Accordingly, it is theoretically unclear how Rothification will alter household behavior without modeling the rich institutional details confronting real-world consumers, along with the economic environment, capital and labor market risk, and uncertain lifetimes. The paper also compares expected household tax payments over the life cycle under both the EET and TEE regimes. We conclude that taxing pension contributions instead of withdrawals leads to delayed retirement, lower lifetime tax
payments, reductions in consumption, and higher wealth and consumption inequality. Retirement asset accumulation is also lower under the Rothification regime.

**Related literature**

This research builds on prior work (Horneff, Maurer, and Mitchell 2018, 2019) by exploring the impact of a Rothification reform for 401(k) plans. Here we add to the literature by delving into the distributional impacts of such a reform in both a “normal” and a low return environment, while accounting for the income tax regime recently adopted. Our work is informed by a number of studies using a life-cycle framework to model and evaluate how individuals respond to a range of environmental shocks. For example, the workhorse model of Cocco, Gomes, and Maenhout (2005) and Gomes and Michaelides (2005) was subsequently extended by Love (2010) and Hubener, Maurer and Mitchell (2016), who showed how family shocks due to changes in marital status and children alter optimal consumption, insurance, asset allocation, and retirement patterns. Horneff, Maurer, Mitchell, and Rogalla (2015) demonstrated how capital market surprises can influence saving and portfolio allocation patterns, and Chai, Horneff, Maurer, and Mitchell (2011) shows how flexible work patterns can help people hedge both earnings and capital market risk. In the present paper, we evaluate how people might optimally respond to a TEE versus the current EET tax regime for retirement accounts by adjusting their consumption, saving, investment, and retirement patterns. In addition, we analyze these possible changes in optimal behavior if the capital market were to move away from a persistently low return environment to what used to be perceived as the “normal” return environment. In contrast to our life-cycle model in
Horneff, Maurer, and Mitchell (2016), we do not include annuity purchases, but we do allow flexible work effort and endogenous claiming of Social Security benefits.\(^5\)

**The consumer’s life-cycle problem: model and calibration**

In what follows, we build and calibrate a structural dynamic consumption and portfolio choice model for an individual maximizing his utility over his life cycle using a richly specified, sophisticated formulation of lifetime behavior calibrated to U.S. federal/state income tax and Social Security/Medicare premium structures, along with realistic Social Security benefit formulas.\(^6\) Just as importantly, the baseline model also incorporates real-world rules characterizing EET tax-qualified 401(k) accounts including the current U.S. caps on 401(k) pretax contributions, employer matches, penalties and taxes on early withdrawals, and required minimum distribution withdrawal amounts. Results using calibrated baseline parameters agree closely with observed consumption, saving, and Social Security claiming age patterns of U.S. households. Specifically, our model generates a large peak at the earliest claiming age at 62, along with a second peak at the (system-defined) Full Retirement Age. The model also matches the current distribution of 401(k) wealth rather nicely (Horneff et al. 2018).

**Preferences**

We work in discrete time and assume that the worker’s decision period starts at \(t = 1\) (age 25) and ends at \(T = 76\) (age 100). Accordingly, each period corresponds to

\(^5\) We also provide a theoretical backing for the empirical claiming age patterns identified by Shoven and Slavov (2012, 2014).

\(^6\) In particular, we take account of Social Security PIA and AIME formulas, as well as early and delayed retirement adjustments, and full retirement ages.
one year. The household has an uncertain lifetime, such that the probability to survive from \( t \) until the next year \( t + 1 \) is denoted by \( p_t \). Survival rates entering into the utility function are taken from the U.S. Population Life Table (Arias 2010). Preferences are represented by a Cobb Douglas function 
\[ u_t(C_t, l_t) = \frac{(C_t l_t^{\alpha})^{1-\rho}}{1-\rho} \]
based on current consumption \( C_t \) and leisure time \( l_t \) (normalized as a fraction of total available time). The parameter \( \alpha \) measures leisure preferences; \( \rho \) is the coefficient of relative risk aversion; and \( \beta \) is the time preference factor. The recursive definition of the value function is given by:
\[ J_t = \frac{(C_t l_t^{\alpha})^{1-\rho}}{1-\rho} + \beta E_t(p_t J_{t+1}) , \]  
with terminal utility 
\[ J_T = \frac{(C_T l_T^{\alpha})^{1-\rho}}{1-\rho} \]
and \( l_t = 1 \) after retirement. We calibrate the preference parameters so our results match empirical claiming rates reported by the U.S. Social Security Administration and average assets in tax-qualified retirement plans. This matching procedure produces preference parameters of \( \alpha = 1.2, \rho = 5 \) and \( \beta = 0.96 \) (for details, see below).

**Time budget, labor income, and Social Security retirement benefits**

As in Horneff et al. (2016), our model allows for flexible work effort and retirement ages. The worker has the opportunity to allocate up to \( (1 - l_t) = 0.6 \) of his available time budget to paid work (assuming 100 waking hours per week and 52 weeks per year).

Depending on his work effort, the uncertain yearly before-tax labor income is given by:
\[ Y_{t+1} = (1 - l_t) \cdot w_t \cdot P_{t+1} \cdot U_{t+1} . \]  

Here $w_t$ is a deterministic wage rate component which depends on age, education, sex, and an indicator for whether the individual works full time, part time, or overtime. The variable $P_{t+1} = P_t \cdot N_{t+1}$ is the permanent component of wage rates with independent lognormal distributed shocks $N_t \sim LN(-0.5\sigma_P^2, \sigma_P^2)$, having a mean of one and volatility of $\sigma_P^2$. In addition, $U_t \sim LN(-0.5\sigma_U^2, \sigma_U^2)$ is a transitory shock with volatility $\sigma_U^2$ and assumed uncorrelated with $N_t$.

The calibration of the deterministic component of the wage rate process $w_t^i$ and the variances of the permanent and transitory wage shocks $N_t^i$ and $U_t^i$ is based on 1975 to 2015 waves of the Panel Study of Income Dynamics (PSID). We estimate these separately by sex and educational level, where the latter groupings are less than high school, high school graduate, and at least some college (<HS, HS, Coll+); see Appendix A, Table A1.

Between ages 62 and 70, a worker may retire from work and claim Social Security benefits. The benefit formula is an overall concave piece-wise linear function of the worker’s average indexed lifetime earnings. Accordingly, this provides an annual unreduced Social Security benefit — also named Primary Insurance Amount (PIA) — equal (in 2015) to 90 percent of (12 times) the first $826 of average indexed monthly earnings, plus 32 percent of average indexed monthly earnings over $826 and through $4,980, plus 15 percent of average indexed monthly earnings over $4,980 and through the cap $9,875.\textsuperscript{7} This value is called the Primary Insurance Amount (PIA). Should an individual claim benefits before (after) his system-defined Normal Retirement Age of 66, \textsuperscript{7} Following Chai et al. 2011 in the optimization the PIA is approximated using the permanent income; in the simulation of optimal life cycle we use the 35 best years of earnings to specify the PIA and adjust the corresponding permanent income state.
his lifelong Social Security benefits will be permanently reduced (increased) according to prespecified factors. If the individual were to work beyond age 62, the model stipulates that he devote at least one hour per week; also, our model rules out overtime work in retirement (i.e., \(0.01 \leq (1 - l_t) \leq 0.4\)).

**Wealth dynamics during the work life**

During the work life, an individual has the opportunity to use current cash on hand for consumption \(C_t\) and investments. Some portion \(A_t\) of the worker’s pretax salary \(Y_t\) (up to a limit of $18,000 per year) can be invested into a tax-qualified 401(k)-retirement plan of the EET or TEE type. Also, from age 50 onward, he is permitted an additional $6,000 of ‘catch-up’ contributions. In addition, a worker can invest outside his retirement plan in risky stocks \(S_t\) and riskless bonds \(B_t\). Hence, cash on hand \(X_t\) in each year can is given by:

\[
X_t = C_t + S_t + B_t + A_t.
\]  

(3)

In addition to the usual constraints, \(C_t, A_t, S_t, B_t \geq 0\), the worker may not contribute more than \(A_t \leq $18,000\) in the 401(k) plan (as per U.S. law). One year later, his cash on hand is given by the value of stocks (bonds) having earned an uncertain (riskless) gross return of \(R_{t+1} (R_f)\), plus income from work (after housing costs \(h_t\)), plus withdrawals \((W_t)\) from the 401(k) plan, minus any federal/state/city taxes and Social Security contributions, \(Tax_{t+1}\), and health insurance \(HI_t\) costs:

\[
X_{t+1} = S_t R_{t+1} + B_t R_f + Y_{t+1}(1 - h_t) + W_t - Tax_{t+1} - HI_t.
\]

(4)

We model housing costs \(h_t\) as in Love (2010). Our “baseline” financial market parameterizations assume a risk-free interest rate of 1%, and an equity risk premium of
4% with a return volatility of 18%. In subsequent simulations, we work with a higher interest rate of 3%, reflective of the more historically normal capital market returns. The annual cost of health insurance $H_{t}$ is set at $1,200. As in Lusardi, Michaud, and Mitchell (2017), if a worker’s cash on hand were to fall below $X_{t+1} \leq 5,879$ p.a., the model posits that he receives a minimum welfare benefit of $5,879 the next year.

**Taxation and evolution of retirement plans**

During the work life and retirement, households must pay various taxes ($Tax_{t+1}$) which reduce cash on hand available for consumption and investment. The amount and timing of these tax payments over the life cycle differ significantly in the case of an EET versus TEE system.

First, workers must pay payroll taxes $PT_{t+1}^{tax}$ amounting to 11.65%, which is the sum of 1.45% Medicare, 4% city and state tax, and 6.2% Social Security tax (up to a cap of $118,500 per year). Payroll taxes are not directly affected by retirement accounts.

Second, the individual must also pay a progressive federal income tax $IT_{t+1}^{tax}$ based on his taxable income $Y_{t+1}^{tax}$, seven income tax brackets, and the corresponding marginal tax rates for each tax bracket (for details, see Appendix B). Taxable income is a complex function of labor earnings, income from investments, and contributions into as well as withdrawals from 401(k) plans. Under both regimes for tax-qualified retirement accounts that we consider, investment earnings on assets are not counted as part of taxable earnings, yet the treatment of contributions (including employer matching contributions) and withdrawals differs between the two tax regimes. In the EET setup, contributions to the retirement account are tax-exempt (E) up to a limit, while withdrawals are part of taxable income (T). Technically, this means that employer matching contributions are
not part of taxable income, while own contributions can be subtracted from taxable income. In the TEE case, contributions (including matching employer contributions) are taxed, but withdrawal are tax exempt. Technically, this means that own contributions cannot be deducted from taxable income, and employer matching contributions are added to taxable income. To sidestep liquidity problems due to back tax payments, we assume that employer contributions are taxed directly at the source, based on the worker’s personal income tax rate. This generates a tax burden of $M_{t}^{tax}$, which reduces the contribution into the TEE account as well as the income tax amount.\footnote{Actual Roth-401(k) regulation requires that employer contributions are taxed according to the EET regime, which requires a separate account for own versus employer contributions. This would require an additional state variable in our models, greatly increasing the computational burden required to solve the models, so we do not follow that approach here.}

Finally, in line with U.S. regulation, the individual must also pay penalty tax of 10\% on early withdrawals from 401(k) accounts prior to age 59 \( \frac{1}{2} \) \((t = 36)\). This rule applies for both the TEE and EET regime:

EET

\[
Tax_{t} = P_{t}^{tax} + I_{t}^{tax} + penalty_{t}
\]  

(5)

TEE

\[
Tax_{t} = P_{t}^{tax} + (I_{t}^{tax} - M_{t}^{tax}) + penalty_{t}
\]

Next, we describe the development of the tax-qualified retirement account in the life-cycle model. Prior to the endogenous retirement age \( t = K \), the worker’s assets in his tax-qualified retirement plan are invested in bonds earning a risk-free gross (pretax) return of $R_f$, as well as risky stocks paying an uncertain gross return of $R_t$. The total value ($F_{t+1}^{401(k)}$) of the 401(k) assets at time \( t + 1 \) is, therefore, determined by the previous period’s value minus any withdrawals ($W_t \leq F_t^{401(k)}$), plus additional own

\[
F_{t+1}^{401(k)} = F_t^{401(k)} - W_t + (R_f + R_t) \]
contributions \((A_t)\), plus any employer match \((M_t)\), and returns on stocks and bonds. To avoid substantial tax penalties from age 70.5 onward, retirees must take required minimum distributions from 401(k) plans, which are based on life expectancy data from the IRS Uniform Lifetime Table (IRS 2015b). In the TEE regime, the employer match is reduced by the tax prepayment \(M^\text{tax}_t\). The variable \(\omega_t^S\) denotes the relative exposure of overall assets allocated to stocks. Overall, the wealth dynamics of the EET or TEE retirement account evolves as follows:

\[
\begin{align*}
\text{EET} \quad & F'_{t+1}^{401(k)} = \omega_t^S \left( F_t^{401(k)} - W_t + A_t + M_t \right) R_{t+1} + \left(1 - \omega_t^S\right) \left( F_t^{401(k)} - W_t + A_t + M_t \right) R_f \\
\text{TEE} \quad & F'_{t+1}^{401(k)} = \omega_t^S \left( F_t^{401(k)} - W_t + A_t + M_t - M^\text{tax}_t \right) R_{t+1} + \left(1 - \omega_t^S\right) \left( F_t^{401(k)} - W_t + A_t + M_t - M^\text{tax}_t \right) R_f.
\end{align*}
\]

To be considered as a safe harbor 401(k) plan and, therefore, avoid complex nondiscrimination testing, we assume that the employers match 100% of employee contributions up to 5% of yearly labor income.\(^9\) Due to regulation, the matching rate can only apply to a maximum compensation of $265,000, so the maximum employer contribution is $13,250. The matching contribution is then given by:

\[
M_t = \min(A_t, 0.05Y_t, 13,250).
\]

**Wealth dynamics during retirement**

The worker can retire and claim Social Security benefits between age 62 and 70. After selecting his endogenous retirement age, \(K\), the individual may still elect to save outside the tax-qualified retirement plan in stocks and bonds, as follows:

\[ X_t = C_t + S_t + B_t. \]  

(8)

His cash on hand for the next period evolves as follows:

\[ X_{t+1} = S_t R_{t+1} + B_t R_f + Y_{t+1}(1 - h_t) + W_t - Tax_{t+1}. \]  

(9)

Old-age retirement benefits provided by Social Security are determined by the worker’s Primary Insurance Amount (PIA), which in turn depend on his average lifetime earnings as described above. Social Security payments \( Y_{t+1} \) in retirement \( (t \geq K) \) are given by:

\[ Y_{t+1} = PIA_K \cdot \lambda_K \cdot \varepsilon_{t+1}. \]  

(10)

Here, \( \lambda_K \) is the mandated adjustment factor for claiming before or after the system-defined Full Retirement Age, which in our model is assumed to be age 66.\(^{10}\) The variable \( \varepsilon_t \) is a transitory shock \( \varepsilon_t \sim LN(-0.5\sigma^2, \sigma^2) \), which reflects out-of-pocket medical and other expenditure shocks in retirement (as in Love 2010). During retirement, benefit payments from Social Security are partially taxed by the individual federal income tax rate, as well as the 4% city and state and 1.45% Medicare taxes.\(^{11}\)

We model the 401(k) plan payouts as follows:

\(^{10}\) The factors we use are 0.75 (claiming age 62), 0.8 (claiming age 63), 0.867 (claiming age 64), 0.933 (claiming age 65), 1.00 (claiming age 66), 1.08 (claiming age 67), 1.16 (claiming age 68), 1.24 (claiming age 69), and 1.32 (claiming age 70); see U.S. SSA (nd_c).

\(^{11}\) For Social Security tax rules see U.S. SSA (nd_d). Up to 85% of Social Security benefits may be subject to income tax for higher-income households, yet due to generous exemptions, most households receive their Social Security benefits tax-free (see Horneff, Maurer, and Mitchell 2016). From age 65 onward, benefits are not taxed by Social Security or Medicare Part A (hospital insurance). Nevertheless, most elderly enroll in Medicare Part B (medical insurance), Part C (advantage plans), and Part D (drug prescription), and pay premiums. To simplify calculations, we assume that these premiums equal 1.45% of benefits.
\[ F_{t+1}^{401(k)} = \omega_t \left( F_t^{401(k)} - W_t \right) R_{t+1} \]
\[ + (1 - \omega_t) \left( F_t^{401(k)} - W_t \right) R_f, \quad \text{for } t < K. \]  

Under U.S. law, plan participants must take retirement account payouts from age 70 onward, according to the Required minimum distribution rules \((m)\) specified by the Internal Revenue Service (IRS 2015b). Accordingly, withdrawals from the retirement account must take into account the following constraints: \(F_t^{401(k)} m \leq W_t < F_t^{401(k)}.\)

**Calibration of preference parameters and model solution**

We posit that households maximize the value function (1) subject to the constraints and calibrations set out above, by optimally selecting their consumption, work effort, claiming age for Social Security benefits, investments and withdrawals from tax-qualified 401(k)-plans, and investments in, as well as redemptions of, stocks and bonds. As this optimization problem cannot be solved analytically, it requires a numerical procedure using dynamic stochastic programming. Accordingly, to generate optimal policy functions, in each period \(t\) we discretize the space in four dimensions \(30(X) \times 20(F^{401(k)}) \times 8(P) \times 9(K)\), with \(X\) being cash on hand, \(F^{401(k)}\) assets held in the 401(k) retirement plan, \(P\) permanent income, and \(K\) the claiming age. Next, we simulate 100,000 independent life cycles based on optimal feedback controls for each of the six population subgroups of interest (men/women with <HS, HS, and Coll+). We then aggregate the subgroups to obtain national mean values using weights from the National Center on Education Statistics (2016). Specifically, the weights are 50.7% women (61% with Coll+, 28% with HS, and 11% with <HS), and 49.3% men (57% with Coll+, 30% HS, and 13% <HS).
We calibrate preference parameters (assumed to be unique for the six subgroup) in such a way that our model results match empirical claiming rates reported by the U.S. Social Security Administration and average assets in 401(k) plans. Our baseline calibration assumes a risk-free interest rate of 1%, and also that people have access to tax qualified 401(k) retirement accounts under the EET regime. Specifically, we calibrate our model to data from the Employee Benefit Research Institute (2017) which reports 401(k) account balances for 7.3 million plan participants in five age groups (20 to 29, 30 to 39, 40 to 49, 50 to 59, and 60 to 69) in 2015. To generate 401(k) simulated balances and claiming rates, we first solve the life-cycle model where the individual has access to traditional EET 401(k) plans under the tax-regime in 2015 (i.e., before the reform in 2018). We then generate 100,000 life cycles using optimal feedback controls for each of the six subgroups (men/women with <HS, HS, and Coll+). These six subgroups are aggregated to obtain national median values, using National Center on Education Statistics (2016) weights. Finally, to compare our results to the EBRI (2017) data, we construct average account levels for each of five age subgroups. Repeating this procedure for alternative preference parameter sets, we find that a coefficient of relative risk aversion $\rho$ of 5, a time discount rate $\beta$ of 0.96, and a leisure parameter $\alpha$ of 1.2 are the parameters that most closely match simulated model outcomes and empirical evidence on both 401(k) balances and claiming rates of Social Security Benefits.\(^{12}\)

Figure 1 (top) presents claiming rates generated by our life-cycle model (dark bars) versus empirical claiming rates (light bars) reported by the U.S. Social Security Administration for the year 2015 for nondisabled men and women. Here we see that our

\(^{12}\) Interestingly, these parameters are also in line with those used in prior work on life-cycle portfolio choice; see for instance Brown (2001).
model closely tracks the empirically-observed early claiming age peak at age 62, as well as the second peak at the Full Retirement Age (66). The lower panel of Figure 1 displays simulated versus empirical evidence on 401(k) assets by age groups. Again, our simulated outcomes are remarkably close to the empirically-observed 401(k) account values, implying that our model accords well with real-world data.
Figure 1: Social Security Claiming Patterns for Women and Men, and 401(k) Asset Values (model versus data)

A: Women

B: Men

Notes: The top two panels compare claiming rates generated by our life-cycle models and empirical claiming rates reported by the US Social Security Administration for the year 2015 (excluding disability). Expected values are calculated from 100,000 simulated life cycles based on optimal feedback controls. Results for the entire female (male) population are computed using income profile for three education levels: 61% Coll+; 28% HS; 11% <HS (57% Coll+; 30% HS; 13%<HS). Parameters used for the baseline calibration are as follows: risk aversion $\rho=5$; time preference $\beta=0.96$; leisure preference $\alpha = 1.2$; endogenous retirement ages 62 to 70. Social Security benefits are based on average permanent income and the bend points in place in 2015; minimum required withdrawals from 401(k) plans are based on life expectancy using the IRS-Uniform Lifetime Table in 2015; tax rules for 401(k) plans are as of 2015 and described in Appendix B. The risk premium for stock returns is 5% and return volatility 18%; the risk-free rate in the baseline case is 1%. The lower panel compares empirical 401(k) account balances across the U.S. population. Empirical account balance data are taken from the Employee Benefit Research Institute (2017); age groups referred to as 20s, 30s, 40s, 50s, and 60s denote average values for persons ages 20 to 29, 30 to 39, 40 to 49, 50 to 59, and 60 to 69. Source: Authors’ calculations
What would Rothification do?

We next illustrate how switching from traditional EET to a TEE tax regime for retirement savings would affect claiming ages, assets held inside and outside tax-qualified retirement plans, consumption, hours of work, asset and consumption inequality, and tax payments over the life cycle. In addition, we study how the results would differ, if the very low interest rate environment of the last decade \((r = 1\%)\) were to be replaced by a more historically “normal” return regime \((r = 3\%)\).

Asset accumulation patterns

Table 1 offers an accounting of how the tax regime change alters asset allocation patterns in the 401(k) accounts versus nontax-qualified assets. Here we focus on life-cycle asset accumulation patterns under the EET/TEE regimes, as well as the low/high expected return scenarios. Most strikingly, we see that assets in 401(k) plans (Panel A) are lower under the Rothification regime, particularly in later life, compared to the higher levels under the EET regime. This shortfall is greater in the higher return regime, such that tax qualified assets are always larger in the EET environment. By contrast, nonqualified assets are markedly lower in the EET world from age 60 onward, by about half as of the Full Retirement Age (i.e., the mid-60s). Yet in terms of consumption opportunities, the value of retirement plan assets in the EET regime is not directly comparable with that in the TEE regime. This is because withdrawals of EET assets must be taxed before they can used for consumption, while withdrawals from TEE assets are tax free.
Table 1: Life-cycle Asset Accumulation Patterns under EET versus TEE Tax Regimes, and Low versus High Expected Return Scenarios

<table>
<thead>
<tr>
<th></th>
<th>r=1%</th>
<th></th>
<th>r=3%</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>EET</td>
<td>TEE</td>
<td>EET</td>
<td>TEE</td>
</tr>
<tr>
<td>Panel A: 401(k) Assets ($000)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Age 30-39</td>
<td>54.8</td>
<td>46.6</td>
<td>61.5</td>
<td>51.5</td>
</tr>
<tr>
<td>Age 40-49</td>
<td>130.6</td>
<td>110.2</td>
<td>149.5</td>
<td>114</td>
</tr>
<tr>
<td>Age 50-59</td>
<td>174.7</td>
<td>147.3</td>
<td>201.7</td>
<td>148.8</td>
</tr>
<tr>
<td>Age 60-69</td>
<td>127.1</td>
<td>91.1</td>
<td>162.9</td>
<td>105.3</td>
</tr>
<tr>
<td>Age 70-79</td>
<td>87.6</td>
<td>67.1</td>
<td>128.6</td>
<td>94.9</td>
</tr>
<tr>
<td>Age 80-89</td>
<td>43.6</td>
<td>34.3</td>
<td>75.5</td>
<td>58</td>
</tr>
<tr>
<td>Age 90-99</td>
<td>8.8</td>
<td>6.6</td>
<td>18.9</td>
<td>14.7</td>
</tr>
<tr>
<td>Panel B: Nonqualified Assets ($000)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Age 30-39</td>
<td>6.3</td>
<td>5.6</td>
<td>7.2</td>
<td>5.7</td>
</tr>
<tr>
<td>Age 40-49</td>
<td>8.9</td>
<td>8.2</td>
<td>7.9</td>
<td>6.9</td>
</tr>
<tr>
<td>Age 50-59</td>
<td>8.1</td>
<td>8.6</td>
<td>6.4</td>
<td>7.9</td>
</tr>
<tr>
<td>Age 60-69</td>
<td>16.7</td>
<td>31.5</td>
<td>16.6</td>
<td>30.5</td>
</tr>
<tr>
<td>Age 70-79</td>
<td>10.9</td>
<td>16.2</td>
<td>11.9</td>
<td>11.7</td>
</tr>
<tr>
<td>Age 80-89</td>
<td>7.7</td>
<td>8.7</td>
<td>8.5</td>
<td>6.8</td>
</tr>
<tr>
<td>Age 90-99</td>
<td>5.4</td>
<td>6</td>
<td>5.7</td>
<td>5.4</td>
</tr>
</tbody>
</table>

Notes: The two panels show expected assets by age in tax-qualified 401(k) plans and nonqualified assets for low- and high-interest rate (1% and 3%), and different tax regimes. Expected values are based on 100,000 simulated life cycles using optimal feedback controls from the life-cycle model. The assumed risk premium for stock returns is 5% and return volatility 18%. For other parameters, see Figure 1. Source: Authors’ calculations.

Impacts on consumption and work hours

Table 2 evaluates the effects of moving from an EET to a TEE regime on consumption patterns and work hours, for low- and high interest rates (r = 1% and 3%). In the low-interest rate regime, EET lifetime consumption is below that in the TEE world from age 40 onward. Panel B also reveals that people work about three more hours per week in the TEE scenario during the Social Security claiming window (ages 62 to 69). If
the real return were instead $r = 3\%$, average consumption under TEE would be lower for all age groups, compared to the EET case. In addition, during the work life, work effort would be about two hours per week lower under TEE. Nevertheless, in the Social Security benefit claiming window, people work about three hours more per week under the TEE regime. Overall, Rothification reduces work over the lifetime but pushes out retirement claiming, compared to the EET tax environment.

Table 2: Life-Cycle Consumption and Working Hours under EET versus TEE Tax Regimes, and Low versus High Expected Return Scenarios

<table>
<thead>
<tr>
<th>Age Group</th>
<th>Consumption ($000)</th>
<th>$r=1%$</th>
<th>$r=3%$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age 30-39</td>
<td>EET 24.0 TEE 23.7</td>
<td>24.3</td>
<td>21.3</td>
</tr>
<tr>
<td>Age 40-49</td>
<td>EET 27.8 TEE 28.0</td>
<td>28.5</td>
<td>24.9</td>
</tr>
<tr>
<td>Age 50-59</td>
<td>EET 29.5 TEE 30.2</td>
<td>30.2</td>
<td>27.0</td>
</tr>
<tr>
<td>Age 60-69</td>
<td>EET 27.9 TEE 29.1</td>
<td>29.5</td>
<td>26.6</td>
</tr>
<tr>
<td>Age 70-79</td>
<td>EET 24.8 TEE 25.2</td>
<td>27.3</td>
<td>24.0</td>
</tr>
<tr>
<td>Age 80-89</td>
<td>EET 23.4 TEE 23.9</td>
<td>26.4</td>
<td>23.9</td>
</tr>
<tr>
<td>Age 90-99</td>
<td>EET 20.8 TEE 21.8</td>
<td>22.9</td>
<td>22.1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Age Groups</th>
<th>Av. Work Hours per Week</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age 25-61</td>
<td>EET 33.8 TEE 33.9</td>
</tr>
<tr>
<td>Age 62-69</td>
<td>EET 8.8 TEE 11.6</td>
</tr>
<tr>
<td>Age 25-69</td>
<td>EET 29.4 TEE 29.9</td>
</tr>
</tbody>
</table>

Notes: The two panels report average consumption and weekly work hours for low and high $r$ (1% and 3%), and different tax regimes. Expected values are based on 100,000 simulated life cycles using optimal feedback controls from the life-cycle model. The assumed risk premium for stock returns is 5% and return volatility 18%. For other parameters, see Figure 1. Source: Authors’ calculations.
Impact on claiming ages

Table 3 shows how Social Security benefit claiming ages would change by sex across tax regimes and under the low-versus high-interest rate scenarios. In both tax regimes, men’s and women’s average retirement ages are later when interest rates are low ($f = 1\%$). This is because delaying Social Security is similar to buying a deferred annuity.\(^{13}\) Therefore, it is more attractive to draw down one’s 401(k) account to delay Social Security claiming, compared to keeping the money in the retirement account and earning (uncertain) investment returns.

Overall, the TEE regime’s lower marginal tax rate on 401(k) payouts induces workers to defer Social Security claiming more than under the EET regime. This may be explained as follows: Some workers with sufficient retirement plan assets want to retire, but they find it attractive to wait to claim Social Security so as to boost those benefits via the delayed claiming factors (6% to 8% increase per year of delayed claiming).

Meanwhile, financing consumption during this no-work phase requires them to withdraw from their 401(k) assets. Under an EET regime, workers must pay income taxes on their pension withdrawals. Thus, the attraction of earning higher Social Security benefits by delaying claiming must be weighed against the disadvantage of paying high income taxes on withdrawals. If the tax burden on withdrawals is heavier than the advantage of receiving higher Social Security benefits, it is rational to claim earlier. This tradeoff must also take into account the fact that only a portion of Social Security benefits are included in taxable income (up to 50% could be tax-free). Accordingly, the net-of-tax gain from

\(^{13}\) Naturally, the price of the annuity varies with the market return. For instance, the implied interest rate to price an annuity comparable to Social Security in the private market would range between 2 and 5%, depending on the retiree’s age and sex. See Hubener et al. (2016), Shoven and Slavov (2014), and Maurer et al 2017.
delaying Social Security claiming is relatively small in the EET scenario. The effect is stronger when interest rates are high, because workers build more assets in their 401(k) accounts.

Such complex tax considerations are irrelevant under the TEE regime, because pension withdrawals are not counted as part of taxable income. Therefore, given their financial resources to finance consumption until claiming, in the TEE scenario workers base their decisions to delay claiming only on delayed retirement credit earned by deferring Social Security. Moreover, this effect is stronger under a high- versus a low-interest rate regime.
Table 3: Social Security Claiming Patterns (in %) for Women and Men under EET versus TEE Tax Regimes, and Low versus High Expected Return Scenarios

<table>
<thead>
<tr>
<th>Age</th>
<th>Women</th>
<th></th>
<th></th>
<th></th>
<th>Men</th>
<th></th>
<th></th>
<th></th>
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<tbody>
<tr>
<td></td>
<td>r=1 %</td>
<td>r=3 %</td>
<td>r=1 %</td>
<td>r=3 %</td>
<td>r=1 %</td>
<td>r=3 %</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>EET</td>
<td>TEE</td>
<td>EET</td>
<td>TEE</td>
<td>EET</td>
<td>TEE</td>
<td></td>
<td></td>
</tr>
<tr>
<td>62</td>
<td>42.5</td>
<td>37.8</td>
<td>49.1</td>
<td>37.3</td>
<td>34.6</td>
<td>29.4</td>
<td>36.9</td>
<td>28.6</td>
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<tr>
<td>63</td>
<td>3.1</td>
<td>3.1</td>
<td>4.9</td>
<td>4.4</td>
<td>4.3</td>
<td>4</td>
<td>6.2</td>
<td>4.1</td>
</tr>
<tr>
<td>64</td>
<td>3.9</td>
<td>2.8</td>
<td>5.6</td>
<td>4.3</td>
<td>4.6</td>
<td>3</td>
<td>7.8</td>
<td>3.1</td>
</tr>
<tr>
<td>65</td>
<td>6.7</td>
<td>4</td>
<td>7.7</td>
<td>6.0</td>
<td>7.9</td>
<td>3.8</td>
<td>10.4</td>
<td>7.1</td>
</tr>
<tr>
<td>66</td>
<td>16</td>
<td>7.3</td>
<td>13.6</td>
<td>8.0</td>
<td>19.8</td>
<td>14.1</td>
<td>17.3</td>
<td>15.5</td>
</tr>
<tr>
<td>67</td>
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<td>5.5</td>
<td>11.4</td>
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<td>10</td>
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<td>68</td>
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<tr>
<td>69</td>
<td>7.2</td>
<td>11</td>
<td>4.2</td>
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<td>8.3</td>
</tr>
<tr>
<td>70</td>
<td>4.9</td>
<td>15.1</td>
<td>2.3</td>
<td>9.3</td>
<td>5.3</td>
<td>12.3</td>
<td>3.2</td>
<td>8.3</td>
</tr>
<tr>
<td>Av. Claim Age (years)</td>
<td>64.7</td>
<td>65.5</td>
<td>64.1</td>
<td>65.2</td>
<td>65.0</td>
<td>65.8</td>
<td>64.5</td>
<td>65.6</td>
</tr>
</tbody>
</table>

Notes: We report the average claiming age for low and high $r$ (1% and 3%) by sex, for the two different tax regimes (EET versus TEE) derived from 100,000 simulated life cycles based on optimal feedback controls from the life-cycle model. The assumed risk premium for stock returns is 5% and return volatility 18%. For other parameters, see Figure 1. Source: Authors’ calculations.

The average claiming-age changes do obscure some interesting differences across population subgroups, as can be seen in Figure 2. Specifically, claiming behavior of the least-educated high school dropouts is relatively similar in the EET and TEE regimes, primarily because this group saves and accumulates fewer assets than the better-educated. Moreover, the changes in claiming ages for this group are small under both interest rate environments. For example, women (men) without a high school degree work only 0.5 (3) month more under the TEE regime in a low-interest rate
environment, while Coll+ men and women defer claiming benefits by more than a year under both interest rate environments. The impact is strongest for college-educated women who work 16 months longer given a high real rate in the TEE versus EET setup. Accordingly, more educated and wealthier workers are predicted to work substantially longer under Rothification, with a much smaller impact on the less-educated.

**Figure 2: Average Claiming Age Differences by Education: TEE (Roth) versus EET Tax Regimes, and Low- versus High-Return Scenarios**

**A: Women**

**B: Men**

**Notes:** We report the average claiming age difference for EET versus TEE for r=1% and 3% by sex and education groups <HS, HS, Coll+, derived from 100,000 simulated life cycles based on optimal feedback controls from the life-cycle model. Preference parameters are as follows: risk aversion \( \rho=5 \); time preference \( \beta=0.96 \); leisure preference \( \alpha = 1.2 \). The endogenous retirement age is between ages 62 to 70. The assumed risk premium for stock returns is 5% and return volatility 18%. Tax bracket are based on 2018 regulations (as described in Appendix B).

**Source:** Authors' calculations.

**Impacts on tax payments over the life cycle**

Next, in Figure 3 we plot the average tax payments per individual over the life cycle under the EET and TEE regimes. The figure includes payroll taxes, income taxes,
and penalty taxes for early withdrawals for the overall population comprised by our six subgroups. Both scenarios assume a low and persistent interest rate of 1%. As anticipated, tax payments under EET are lower during the first 25 years of the worklife, since 401(k) contributions are not part of taxable income; by contrast, under the TEE regime, workers must pay taxes on both own and employer matching contributions. Yet the situation changes around age 50 when tax payments rise in the EET regime, and the difference is particularly marked between ages 62 and 70. Thereafter, tax payments in both the EET and TEE scenarios are relatively low.

The explanation is that, in both tax regimes, workers begin curtailing their work hours after age 50 and finance their consumption by 401(k) withdrawals. From age 60 onward, 401(k) withdrawals are not subject to the 10% penalty tax in both tax regimes, but withdrawals from EET accounts are part of taxable income which results in higher tax payments — in contrast to the TEE world. The difference in tax payment is particularly large between ages 62 and 70. For example, at age 65, the annual EET tax payment averages $8,000, or about twice as large as in the Roth regime. This result is driven by individuals who have relatively large accumulations in their 401(k) plans and use these assets to (partially) retire from work, delay claiming Social Security benefits, and spend retirement assets to cover consumption until claiming. From age 70 onward, most of the 401(k) assets are spent so people withdraw only small amounts from their retirement plans. Hence, retirees in the EET world pay only slightly more taxes than those in the TEE world.
**Figure 3: Average Annual Tax Payments per Individual: EET versus TEE (Roth)**

Tax Regimes

![Graph showing average annual tax payments per individual for EET versus TEE taxation based on low interest rates (1%)](image)

**Notes:** The figure shows average annual tax payments (sum of income taxes, payroll taxes, and penalty tax for early withdrawals) over the life cycle per individual for EET versus TEE taxation based on low interest rates (1%). Values are based on 100,000 simulated life cycles for each of the six subgroups (men/women and three education groups) using optimal feedback controls from the life-cycle model. Results for the entire population are computed using the following weights for the three education levels: women (61% Coll+; 28% HS; 11% <HS) and men (57% Coll+; 30% HS; 13%<HS); the weights for women is 51% and for men 49%. Further notes on parameters see Figure 2.

Table 4 shows numerical values of average lifetime tax payments per individual for the two tax regimes and interest rate scenarios under consideration. In all scenarios, we find that average tax payments are higher under the EET system until workers attain age 49. For example, assuming \( r = 1\% \), workers pay about $11,000 more in taxes under the TEE system up to that age. Yet between ages 50 and 69, workers in the EET regime pay $26,000 more than in the TEE world. Over the complete life cycle,
tax payments average 6% ($24,000) more in the EET world when the interest rate is low; the difference increases to about 10% ($42,000) if the real rate is 3%. Overall, we conclude that tax payments are higher in the short run in the TEE regime, but lower in the long run.

**Table 4: Sum of Average Lifetime Tax Payments per Individual: EET versus TEE (Roth) Tax Regimes, and Low versus High Expected Return Scenarios**

<table>
<thead>
<tr>
<th>Age</th>
<th>r = 1 %</th>
<th></th>
<th>r = 3 %</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>EET</td>
<td>TEE</td>
<td>EET</td>
<td>TEE</td>
</tr>
<tr>
<td>Age 25-49</td>
<td>214.6</td>
<td>225.4</td>
<td>213.9</td>
<td>222.7</td>
</tr>
<tr>
<td>Age 50-69</td>
<td>167.4</td>
<td>141.2</td>
<td>165.8</td>
<td>133.4</td>
</tr>
<tr>
<td>Age 70-100</td>
<td>43.4</td>
<td>35.2</td>
<td>54.5</td>
<td>36.3</td>
</tr>
<tr>
<td>Age 25-100</td>
<td>425.4</td>
<td>401.8</td>
<td>434.2</td>
<td>392.4</td>
</tr>
</tbody>
</table>

**Notes:** The table reports average lifetime tax payments (sum of income taxes, payroll taxes, and penalty tax for early withdrawals) per individual for EET versus TEE taxation and for low and high interest rates (1% and 3%). Values are based on 100,000 simulated life cycles for each of the six subgroups (men/ women and three education groups) using optimal feedback controls from the life-cycle model. Results for the entire population are computed using the following weights for the three education levels: women (61% Coll+; 28% HS; 11% <HS) and men (57% Coll+; 30% HS; 13%<HS); the weights for women is 51% and for men, 49%. For further notes on parameters see Figure 2.

**Impact on Inequality**

Last, we evaluate how a TEE versus an EET tax regime for retirement savings affects asset and consumption inequality. For the three population subgroups and the ETT versus TEE tax regimes, Table 5 reports average wealth inside and outside tax-qualified accounts as of age 62, as well as average income and average consumption between ages 25-62. Panel A depicts results for the low- and Panel B for the high-interest rate scenario.
**Table 5: Asset and Consumption Inequality by Education under EET versus TEE Tax Regimes, and Low versus High Expected Return Scenarios**

<table>
<thead>
<tr>
<th></th>
<th>EET</th>
<th>TEE</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Ave. Cash on Hand @62</td>
<td>Ave. Cash on Hand @62</td>
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<tr>
<td></td>
<td>Pre-tax Ave. 401(k) Assets @62</td>
<td>Pre-tax Ave. 401(k) Assets @62</td>
</tr>
<tr>
<td></td>
<td>Pre-tax Ave. Income Age 25-62</td>
<td>Pre-tax Ave. Income Age 25-62</td>
</tr>
<tr>
<td></td>
<td>Ave. Cash on Hand @62</td>
<td>Ave. Cash on Hand @62</td>
</tr>
<tr>
<td></td>
<td>Ave. 401(k) Assets @62</td>
<td>Ave. 401(k) Assets @62</td>
</tr>
<tr>
<td></td>
<td>Pre-tax Ave. Income Age 25-62</td>
<td>Pre-tax Ave. Income Age 25-62</td>
</tr>
</tbody>
</table>

**Panel A: r= 1%**

<table>
<thead>
<tr>
<th></th>
<th>Low</th>
<th>High</th>
<th>Coll+</th>
<th>Ratio (Coll+/&lt;HS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;HS</td>
<td>$19,291</td>
<td>$16,677</td>
<td>$13,940</td>
<td>301%</td>
</tr>
<tr>
<td>HS</td>
<td>$35,027</td>
<td>$67,193</td>
<td>$28,913</td>
<td>1,261%</td>
</tr>
<tr>
<td>Coll+</td>
<td>$58,061</td>
<td>$210,349</td>
<td>$52,016</td>
<td>373%</td>
</tr>
<tr>
<td></td>
<td>$21,021</td>
<td>$13,039</td>
<td>$13,856</td>
<td>271%</td>
</tr>
</tbody>
</table>

**Panel B: r=3%**

<table>
<thead>
<tr>
<th></th>
<th>Low</th>
<th>High</th>
<th>Coll+</th>
<th>Ratio (Coll+/&lt;HS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;HS</td>
<td>$21,075</td>
<td>$28,443</td>
<td>$15,177</td>
<td>273%</td>
</tr>
<tr>
<td>HS</td>
<td>$35,849</td>
<td>$90,032</td>
<td>$28,364</td>
<td>882%</td>
</tr>
<tr>
<td>Coll+</td>
<td>$57,616</td>
<td>$250,887</td>
<td>$49,173</td>
<td>324%</td>
</tr>
<tr>
<td></td>
<td>$23,536</td>
<td>$21,969</td>
<td>$15,118</td>
<td>255%</td>
</tr>
</tbody>
</table>

**Notes:** The table reports average cash on hand, 401(k) plan assets, and average annual pretax earnings by educational group, for low and high r (1% and 3%) and different tax regimes. Expected values are based on 100,000 simulated life cycles using optimal feedback controls from the life-cycle model. The assumed risk premium for stock returns is 5% and return volatility 18%. For other parameters, see Figure 1. **Source:** Authors' calculations.
Following Lusardi, Michaud, and Mitchell (2017), we measure relative wealth, income, and consumption inequality in terms of the ratio of college graduates to high school dropouts as of age 62. The higher is this ratio, the greater the inequality along this dimension. Regardless of the interest rate environment, we see that inequality measured in this way is greater under the TEE regime for all four metrics. For example, under the EET regime, for \( r = 1\% \), workers with Coll+ education have three times the assets in nonqualified accounts compared to high school dropouts; this rises to four times under the TEE regime. Due to the different tax regimes, income inequality also rises by 8 percentage points under the TEE regime when interest rates are low, and by 11 percentage points for the higher interest rate. Absolute asset levels in 401(k) accounts are not directly comparable across the two tax regimes, but the inequality measure is comparable and it is 6 percentage points higher in the TEE case. Finally, consumption inequality is greater under TEE taxation of retirement savings.

**Conclusions**

This paper evaluates whether adopting a different tax treatment of retirement plan contributions would materially change Social Security benefit claiming ages and work hours, consumption, and asset allocation of workers looking ahead to retirement. We also assess whether the lower-paid would behave differently from the higher-paid, in terms of change in claiming, saving inside and outside the Roth accounts, and nonpension saving. Rothification also alters the distribution of retirement incomes relative to the current EET-system. For example, the gap between high and low-wage workers' take home pay is not diminished by income taxes under an EET system, whereas it is under a TEE program. Moreover, the Social Security replacement rate formula is progressive, as it provides relatively
higher benefits for low-wage workers than for the higher paid. Given these realities, an EET scheme enhances the progressivity of overall old-age income (pension account withdrawals plus Social Security benefits), whereas a TEE structure treats pension benefits more neutrally. Accordingly, it is theoretically impossible to predict how Rothification will alter household behavior without taking into account the rich institutional details confronting real-world consumers, along with the economic environment, capital and labor market risk, and uncertain lifetimes.

Our structural model is a richly specified, sophisticated formulation of lifetime behavior calibrated to U.S. federal/state income tax and Social Security/Medicare premium structures, along with realistic Social Security benefit formulas. We account for PIA and AIME formulas, early and delayed retirement adjustments under Social Security, and real-world rules characterizing tax-qualified DC accounts, including the current caps on pretax contributions, employer matches, penalties and taxes on early withdrawals, and required minimum distribution withdrawals. This life-cycle model of work, saving, consumption, and retirement behavior provides several lessons for those interested in an alternative tax regime for pension plans. Overall, we show that taxing pension contributions instead of withdrawals leads to later retirement ages, especially for the better-educated. It also reduces lifetime work hours, and increases wealth and consumption inequality. While there is some sensitivity to market returns, our overall conclusions remain robust to the alternative assumptions explored here. Finally, lifetime tax payments are lower by 6-10% under the Rothification tax regime.
References


U.S. National Center for Health Statistics: Hyattsville, Maryland.


Appendix A: Wage rate estimation

We calibrated the wage rate process using the Panel Study of Income Dynamics (PSID) 1975 to 2015, from ages 25 to 69. During the work life, each individual's labor income profile has deterministic, permanent, and transitory components with uncorrelated and normally distributed shocks according to $\ln(N_t) \sim N(-0.5\sigma_n^2, \sigma_n^2)$ and $\ln(U_t) \sim N(-0.5\sigma_u^2, \sigma_u^2)$. The wage rate values are expressed in $2015. These are estimated separately by sex and by educational level. The educational groupings are: less than high school (<HS), high school graduate (HS), and those with at least some college (Coll+). Extreme observations below $5 per hour and above the 99th percentile are dropped.

We use a second order polynomial in age and dummies for employment status. The regression function is:

$$\ln(w_{i,y}) = \beta_1 \cdot \text{age}_{i,y} + \beta_2 \cdot \text{age}_{i,y}^2 + \beta_5 \cdot ES_{i,y} + \beta_{waves} \cdot \text{wave dummies}, \quad (A1)$$

where $\log(w_{i,y})$ is the natural log of wage at time $y$ for individual $i$, age is the age of the individual divided by 100, ES is the individual's employment status, and wave dummies control for year-specific shocks. For employment status, we include three groups depending on work hours per week as follows: part-time worker ($\leq 20$ hours), full-time worker ($< 20 \& \leq 40$ hours) and overtime worker ($< 40$ hours). OLS regression results for the wage rate process equations are provided in Table A1.

To estimate the variances of the permanent and transitory components, we follow Carroll and Samwick (1997) and Hubener at al. (2016). We calculate the difference of the observed log wage and the regression result, and we take the difference of these differences across different lengths of time $d$. For individual $i$, the residual is:
\[ r_{i,d} = \sum_{s=0}^{d-1}(N_{t+s}) + U_{i,t+d} - U_{i,t}. \]  

(A2)

We then regress the \( v_{id} = \frac{r_{i,d}^2}{r_{i,d}^2} \) on the lengths of time \( d \) between waves and a constant:

\[ v_{id} = \beta_1 \cdot d + \beta_2 \cdot 2 + e_{id}, \]  

(A3)

where the variance of the permanent factor \( \sigma_N^2 = \beta_1 \) and the \( \sigma_U^2 = \beta_2 \) represents the variance of the transitory shocks.
**Table A1: Regression results for wage rates**

<table>
<thead>
<tr>
<th>Age/100</th>
<th>Men &lt;HS</th>
<th>Men HS</th>
<th>Men Coll+</th>
<th>Women &lt;HS</th>
<th>Women HS</th>
<th>Women Coll+</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>3.161***</td>
<td>5.972***</td>
<td>9.092***</td>
<td>1.256***</td>
<td>2.767***</td>
<td>4.731***</td>
</tr>
<tr>
<td></td>
<td>(0.108)</td>
<td>(0.049)</td>
<td>(0.070)</td>
<td>(0.110)</td>
<td>(0.046)</td>
<td>(0.072)</td>
</tr>
<tr>
<td></td>
<td>(0.130)</td>
<td>(0.062)</td>
<td>(0.089)</td>
<td>(0.131)</td>
<td>(0.059)</td>
<td>(0.094)</td>
</tr>
<tr>
<td>Part-time work</td>
<td>-0.109***</td>
<td>-0.153***</td>
<td>-0.0826***</td>
<td>-0.0858***</td>
<td>-0.129***</td>
<td>-0.0847***</td>
</tr>
<tr>
<td></td>
<td>(0.020)</td>
<td>(0.009)</td>
<td>(0.011)</td>
<td>(0.006)</td>
<td>(0.003)</td>
<td>(0.004)</td>
</tr>
<tr>
<td>Over-time work</td>
<td>0.00412</td>
<td>0.0506***</td>
<td>0.0949***</td>
<td>0.0158***</td>
<td>0.0748***</td>
<td>0.106***</td>
</tr>
<tr>
<td></td>
<td>(0.004)</td>
<td>(0.002)</td>
<td>(0.002)</td>
<td>(0.006)</td>
<td>(0.002)</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Constant</td>
<td>1.807***</td>
<td>1.435***</td>
<td>1.151***</td>
<td>2.051***</td>
<td>2.015***</td>
<td>1.938***</td>
</tr>
<tr>
<td></td>
<td>(0.042)</td>
<td>(0.012)</td>
<td>(0.015)</td>
<td>(0.037)</td>
<td>(0.011)</td>
<td>(0.017)</td>
</tr>
<tr>
<td>Observations</td>
<td>48,762</td>
<td>327,305</td>
<td>293,386</td>
<td>31,788</td>
<td>290,597</td>
<td>225,211</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.069</td>
<td>0.102</td>
<td>0.147</td>
<td>0.032</td>
<td>0.044</td>
<td>0.092</td>
</tr>
<tr>
<td>Permanent</td>
<td>0.009***</td>
<td>0.013***</td>
<td>0.019***</td>
<td>0.008***</td>
<td>0.013***</td>
<td>0.019***</td>
</tr>
<tr>
<td></td>
<td>(0.001)</td>
<td>(0.0002)</td>
<td>(0.0003)</td>
<td>(0.0001)</td>
<td>(0.0002)</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Transitory</td>
<td>0.028***</td>
<td>0.031**</td>
<td>0.041***</td>
<td>0.023***</td>
<td>0.028***</td>
<td>0.038***</td>
</tr>
<tr>
<td></td>
<td>(0.001)</td>
<td>(0.001)</td>
<td>(0.001)</td>
<td>(0.002)</td>
<td>(0.001)</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Observations</td>
<td>28,359</td>
<td>175,247</td>
<td>140,984</td>
<td>20,863</td>
<td>176,304</td>
<td>123,145</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.214</td>
<td>0.283</td>
<td>0.307</td>
<td>0.146</td>
<td>0.255</td>
<td>0.264</td>
</tr>
</tbody>
</table>

**Notes:** Regression results for the natural logarithm of wage rates (in $2015) are based on information in the Panel Study of Income Dynamics (PSID) for persons ages 25 to 69 in waves 1975 to 2015. Independent variables include age and age-squared, and dummies for part-time work (≤20 hours per week) and overtime work (≥ 40 hours per week). Robust standard errors in parentheses. **Source:** Authors’ calculations.
Appendix B: Modeling retirement accounts

We embed a U.S.-type progressive tax system in our model to explore the impact of having access to a qualified (tax-sheltered) pension account of the EET versus the TEE (Roth) type.\(^\text{14}\) (All values are in $2015 and relevant amounts are inflation adjusted yearly). Here the worker must pay taxes on labor income and on capital gains from investments in bonds and stocks. During the working life, he invests \(A_t\) in a tax-qualified pension account which reduces his taxable income; contributions can be made to an annual maximum amount \(D_t=18,000\) (and from age 50 an additional $6,000 catch up is feasible). Correspondingly, withdrawals \(W_t\) from the tax-qualified account increase taxable income. Finally, the worker’s taxable income is reduced by a general standardized deduction \(GD\). For a single person, this deduction was in 2015 $6,300 (in 2018 $12,000) per year. Consequently, taxable income during the working age is given by:

\[
\begin{align*}
\text{EET} \quad Y_{t+1}^{\text{tax}} & = \max \left[ \max \left( S_t \cdot (R_{t+1} - 1) + B_t \cdot (R_f - 1); 0 \right) + Y_t + (1 - h_t) - GD; 0 \right], \\
\text{TEE} \quad Y_{t+1}^{\text{tax}} & = \max \left[ \max \left( S_t \cdot (R_{t+1} - 1) + B_t \cdot (R_f - 1); 0 \right) + M_t + Y_{t+1} (1 - h_t) - GD; 0 \right].
\end{align*}
\]

For Social Security \((Y_{t+1})\) taxation, we use the following rules: when the retiree’s combined income\(^\text{15}\) is between $25,000 and $34,000 (more than $34,000), 50% (85%) of benefits are taxed. After retirement, we set \(A_t=0\), i.e. no further contributions in 401(k) retirement plans are possible.

\(^{14}\) That is, contributions and investment earnings in the account are tax exempt (E), while payouts are taxed (T).

\(^{15}\) Combined income is sum of adjusted gross income, nontaxable interest, and half of his Social Security benefits (US SSA nd_c).
In line with U.S. rules for federal income taxes, our progressive tax system has seven income tax brackets (IRS 2015a). These brackets \( i = 1, \ldots, 7 \) are defined by a lower and an upper bound of taxable income \( Y_{t+1}^{\text{tax}} \in [l_b_i, u_b_i] \) and determine a marginal tax rate \( r_i^{\text{tax}} \). In 2018, the marginal tax rates for a single household were 10% from $0 to $9,225, 12% from $9,225 to $38,700, 22% from $38,701 to $82,500, 24% from $82,501 to $157,500, 32% from $157,500 to $200,000, 35% from $200,001 to $500,000 and 37% greater than $500,000 (see IRS 2018). Based on these tax brackets, the dollar amount of taxes payable is given by:

\[
IT_{t+1}^{\text{tax}} = (Y_{t+1}^{\text{tax}} - l_b_7) \cdot 1_{\{Y_{t+1}^{\text{tax}} \geq l_b_7\}} \cdot r_7^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_6) \cdot 1_{\{l_b_7 > Y_{t+1}^{\text{tax}} \geq l_b_7\}} + (u_b_6 - l_b_6) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_7\}} \right) \cdot r_6^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_5) \cdot 1_{\{l_b_6 > Y_{t+1}^{\text{tax}} \geq l_b_6\}} + (u_b_5 - l_b_6) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_6\}} \right) \cdot r_5^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_4) \cdot 1_{\{l_b_5 > Y_{t+1}^{\text{tax}} \geq l_b_5\}} + (u_b_4 - l_b_5) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_5\}} \right) \cdot r_4^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_3) \cdot 1_{\{l_b_4 > Y_{t+1}^{\text{tax}} \geq l_b_4\}} + (u_b_3 - l_b_4) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_4\}} \right) \cdot r_3^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_2) \cdot 1_{\{l_b_3 > Y_{t+1}^{\text{tax}} \geq l_b_3\}} + (u_b_2 - l_b_3) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_3\}} \right) \cdot r_2^{\text{tax}}
\]

\[
+ \left( (Y_{t+1}^{\text{tax}} - l_b_1) \cdot 1_{\{l_b_2 > Y_{t+1}^{\text{tax}} \geq l_b_2\}} + (u_b_1 - l_b_1) \cdot 1_{\{Y_{t+1}^{\text{tax}} > l_b_2\}} \right) \cdot r_1^{\text{tax}}
\]

where, for \( A \subseteq X \), the indicator function \( 1_A \rightarrow \{0, 1\} \) is defined as:

\[
1_A(x) = \begin{cases} 
1 & x \in A \\
0 & x \notin A 
\end{cases}
\]

\[\text{(B2)}\]

\[\text{(B3)}\]

---

\[\text{16} \text{ Here we assume that capital gains are taxed at the same rate as labor income, so we abstract from the possibility that long-term investments may be taxed at a lower rate.}\]