

1 **Improving the wind-induced human comfort of the Beijing Olympic Tower by a**
2 **double-stage pendulum tuned mass damper**

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4 **Abstract:** With five sub towers and a maximum height of 246.8 m, the Beijing Olympic Tower
5 (BOT) is a landmark of Beijing. The complex structural properties and slenderness of the BOT
6 render it prone to wind loading. As far as the wind-induced performance of this structure is
7 concerned, this paper thus aims at a tuned mass damper-based mitigation system for controlling the
8 wind-induced acceleration response of the BOT. To this end, the three-dimensional wind loading of
9 various wind directions are simulated based on the fluctuating wind force obtained by the wind
10 tunnel test, by which the wind-induced vibration is evaluated in the time domain by using the finite
11 element model (FEM). A double-stage pendulum tuned mass damper (DPTMD), which is capable of
12 controlling the long period dynamic response and requires only a limited space of installation, is
13 optimally designed at the upper part of the tower. Finally, the wind-induced response of the structure
14 with and without DPTMD is compared with respect to various wind directions and in both the time

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15 and frequency domain. The comparative results show that the wind-induced accelerations atop the
16 tower with the wind directions of 45° , 135° , 225° , and 315° are larger than those with the other
17 directions. The DPTMD significantly reduces the wind-induced response by the maximum
18 acceleration reduction ratio of 30.05%. Moreover, it is revealed that the control effect varies
19 noticeably for the five sub towers, depending on the connection rigidity between Tower1 and each
20 sub tower.

21 **Keyword:** Multi-tower structure; Wind-induced responses; Human comfort; Double-stage pendulum
22 tuned mass damper; Vibration mitigation; High-rise building

24 1. Introduction

25 With the increasing use of high-strength materials, light-weight floors, and curtain wall systems,
26 the mass and stiffness of modern high-rise buildings and towers are decreasing (Ghorbani-Tanha et
27 al. 2009; Kim et al. 2008). Thus, they suffer from excessive wind-induced oscillations (Chen et al.
28 2018; Li et al. 2011). The undesirably excessive vibration may cause not only the structural damage
29 or failure but also the discomfort of occupants. Hence, very often those structures may need specific
30 measures to mitigate the wind-induced responses (Kareem et al. 1999). Generally, increasing the
31 structural stiffness is effective in reducing dynamic response, but it is often economically inefficient.
32 Structural control technology, which aims to enhance structural safety and serviceability against
33 dynamic excitations, is now a widely-used alternative (Basu et al. 2014; Spencer&Nagarajaiah 2003;
34 Housner et al. 1997; Soong&Spencer 2002; Ikeda 2009).

35 Tuned mass damper (TMD) is one of the simplest and practical control devices and especially
36 useful in mitigating dynamic response within the narrow frequency range. Generally, a typical TMD

37 can be modeled as a device consisting of a mass element, a stiffness element, and a damping element.
38 The frequency of the TMD is tuned to a particular vibration frequency so that when the structural
39 vibration at that frequency is excited, the damper will resonate out of phase and mitigate the induced
40 vibration. A portion of vibration energy input to the structure may be imparted to the TMD and
41 dissipated by the damping element. Due to the convenient implementation procedure, low cost and
42 no requirement of external energy, TMD has attracted many researches, most of which are focused
43 on the configuration, design, and application of the TMD. A proper configuration is essential to
44 realize the TMD in engineering practice. Options of the effective stiffness may include the springs
45 (Ohtake et al. 1992; Chen et al. 2012), the suspended pendulum (Roffel et al. 2013;
46 Nagase&Hisatoku 1992), and the laminated rubber bearings (Saito et al. 2001). Although the oil
47 dampers are typical, there are still others such as the friction (Chung et al. 2013), the eddy current
48 (Lu et al. 2018), the sub tuned absorbers (Sarkar&Gudmestad 2013), and the pounding (Song et al.
49 2016; Zhang et al. 2013). Moreover, the analysis and design methods of TMD are under active
50 investigation, including the design formulas of the TMD's parameters. These researches may date
51 back to (Den Hartog 1956), such as simplified expressions for optimum TMD parameters of
52 undamped/damped systems considering various combinations of responses (e.g., displacement,
53 velocity, acceleration and force) and excitations (e.g., harmonic and white noise random excitations)
54 (Chang&Qu 1998; Sadek et al. 1997; Warburton 1982; Chung et al. 2013; Hoang et al. 2008;
55 Fujino&Abe 1993). On the other hand, the metaheuristic optimization methods have been utilized in
56 the design of TMD (Farshidianfar&Soheili 2013; Leung et al. 2008; Bekdaş&Nigdeli 2011; Bekdaş
57 et al. 2018; Carlo Marano et al. 2010; Jin et al. 2018).

58 With the development in the past four decades, the TMD has been successfully installed on

59 practical buildings to mitigate dynamic responses including pedestrian-induced vibration (An et al.
60 2015; Chen et al. 2012), wind-induced vibration (Ghorbani-Tanha et al. 2009; Nagase&Hisatoku
61 1992) and earthquake-induced vibration (Chen et al. 2018; Hoang et al. 2008). Researches and
62 applications show that the TMD in the high-rise tower can suppress the wind-induced vibration
63 significantly, such as John Hancock Tower in Boston (1975), Taipei 101 Tower (Kao et al. 2011),
64 Shanghai Tower (Zhou et al. 2018), and many others (Ghorbani-Tanha et al. 2009; Ohtake et al.
65 1992; Kang et al. 2012; Li et al. 2011; McNamara 1977; Nagase&Hisatoku 1992). Most of these
66 cases are a TMD on a single-tower building, but most recently some complicated buildings with two
67 or more towers have been constructed out of their architecture benefits. However, the researches of
68 TMD on these irregular buildings are rare. Hence, further investigations on the wind-induced
69 vibration and mitigation are still needed for multi-tower buildings.

70 With a height of 246.8m, Beijing Olympic Tower (BOT) in the northern of Beijing, China, is a
71 new landmark. The BOT consists of five towers, each of which has an atop large mass. Preliminary
72 studies demonstrate that the upper part of the tower suffers from excessive wind-induced acceleration
73 beyond the human comfortability limit. This paper presents a study on the TMD installed on the BOT.
74 The remainder of this paper is organized as follows. Section 2 introduces the structural system of the
75 BOT. Section 3 presents the finite element model (FEM) of the structure and discusses its dynamic
76 characteristics. The following section introduces the results of the wind tunnel test for this structure
77 and the simulation of the wind loading in the time domain. Section 5 designs a double-stage
78 pendulum tuned mass damper (DPTMD) for this tower and assesses the mitigation effect of the
79 tower by comparing the acceleration response with and without the DPTMD. Finally, the main
80 conclusions of the numerical study are summarized in Section 6.

81 **2. Description of the Beijing Olympic Tower**

82 Beijing Olympic Tower (BOT), shown in Fig.1, is adjacent to the landscape avenue on the axis
83 line of the Beijing Olympic Forest Park. It boasts one of the two buildings around the world
84 officially with Olympic rings permanently on the top (BeijingInternational 2016; OlympicNews
85 2016). This tower consists of five sub towers with different heights: one central tower (Tower1)
86 locates in the middle and four lower towers (Tower2, Tower3, Tower4, and Tower5) stands around
87 the Tower1. The geometry of these sub towers is shown in Table.1. Towers 2-5 are connected to
88 Tower1 by the corridors which are spatial steel girders with a height of 3.0m and a width of 2.7m.
89 The sections of these sub towers are regular hexagon or circular, the dimension of which increases
90 with the height. The structure of Tower1 is a tube-in-tube system; its outer tube is composed of 16
91 concrete-filled steel tube (CFST) circular columns stiffened by I-shape steel beams and H-shape steel
92 braces. Towers 2-5 has the structure of tube systems composed of 6 CFST circular columns
93 connected by steel beams and braces.

94 **3. Dynamic characteristics of the structure**

95 *3.1 Finite element model*

96 As shown in Fig.2, a three-dimensional (3D) finite element model (FEM) of the BOT was
97 established by using CSI SAP2000 based on the structural design drawings. Two kinds of elements
98 were employed in the FEM: the beam elements for the beams, columns, and braces, and the shell
99 elements for the floors and walls. The nonstructural components were modeled as the dead loads,
100 while the mass was transformed from the dead loads and live loads. The connections between the
101 braces and other components were hinged constraints, and the connections between the beams and
102 columns and between the structure and its foundation were fixed constraints.

103 3.2 Natural frequencies and modal shapes

104 The structural dynamic characteristics of the BOT were analyzed and shown in Table.2 and
105 Fig.3. Here, 45° and 135° denotes the angles between the vibration directions and the x -axis in the
106 x - y plane. It can be observed that the first natural period can be as long as 5.687s and the
107 torsional-translation period ratio is 0.775. The first two modes of the tower are overall bending in the
108 direction of 45° and 135° , respectively, where the third mode is torsional. The first six modes are
109 overall vibration modes, indicating that the corridors in this tower are stiff enough to combine the
110 five sub towers. The modes from the sixth to ninth are all 2nd order torsional modes with different
111 vibration shapes of the sub towers with dense-distributed frequencies, which may influence the
112 vibration of the tower.

113 4. Wind loads simulation

114 4.1 Introduction of the wind tunnel test

115 Wind tunnel testing is an effective tool to evaluate the wind effects on buildings, especially
116 those with complex silhouettes. In this study, wind tunnel tests of wind pressure on the BOT were
117 carried out in the atmospheric boundary layer wind tunnel TJ-2 at the Tongji University using a
118 synchronous multi-pressure sensing system (Ming et al. 2010). The dimension of the working section
119 of the wind tunnel is 3.0m wide \times 2.5m high. In order to reproduce the building shape more detailed,
120 the rigid sectional models are used. The whole building is divided into four sections vertically. The
121 sectional models are made of plexiglass and ABS. These four scaled segments are shown in Fig.4(a),
122 and the tower bodies and the tower crowns are 1:70 and 1:100 scaled, respectively. The wind
123 direction is defined as an angle from the tower south along a clockwise direction (see Fig.4(b)), and
124 the measurements were made with the wind direction varying from 0° to 360° with the increment of

125 15°. 1944 pressure taps were installed on these four sectional models. Due to the lack of instruments,
126 the scaled are divided into eight synchronous pressure measuring segments, and not all of them use
127 the same sampling rate. Hence, the pressure data were acquired at five sampling rates with a
128 sampling length of 6000 steps. The sectional model testing was conducted in a turbulent wind field
129 with the turbulence intensity in Table.3, but the mean wind speed was 12.0 m/s and constant along
130 the height. In this experiment, significant mutual aerodynamic interference effects among the sub
131 towers existed, and complicated wind pressure and force distributions were found. Therefore, the
132 wind loads for the BOT is undoubtedly different from the conventional high-rise towers.

133 *4.2 Simulation of the three-dimensional wind loads*

134 In this paper, because of the nonlinearity of the damping devices, the time-domain method is
135 introduced to compute the wind-induced vibration of the BOT. To this end, one should simulate a
136 three-dimensional wind loading field that is applicable to the FEM of the BOT firstly. In this study,
137 the fluctuating wind pressure coefficients given by the wind tunnel tests are used to model the
138 three-dimensional wind field. However, there are some difficulties to utilize these data directly: (1)
139 As mentioned above, the data were acquired at five different sampling rates, including 6.0391Hz,
140 8.1145 Hz, 7.3379 Hz, 6.8065 Hz, and 6.2723 Hz. (2) The directions of the tested wind pressure
141 coefficients are perpendicular to the model surfaces. (3) There are 1944 pressure taps and 6000 steps
142 per testing wind direction, and locations of the pressure taps do not strictly one-to-one coincide with
143 the structural nodes in the FEM. These difficulties may lead to unsynchronized time steps, difficulty
144 in the loads' assignment and extensive computing time in the FEM time history analysis. Therefore, a
145 method for the three-dimensional wind loading field simulation is proposed as depicted by Fig.5
146 including four steps:

147 (1) In order to unify the sampling rates of all data into 6.0391Hz, the nearest interpolation
 148 method is used. Fig.6 shows the comparison of the data from a pressure tap with and without
 149 interpolation and illustrates a good agreement not only in the time domain but also in the frequency
 150 domain.

151 (2) The wind pressure coefficients are decomposed into three orthogonal directions based on the
 152 global coordinate system of the FEM. Hence, the wind pressure coefficients in the x , y , and
 153 z -direction of global coordinate can be obtained as follows:

$$154 \quad \mu_{si,x}(t) = \mu_{si}(t) \cdot \cos \varphi \cdot \sin \theta \quad (1)$$

$$155 \quad \mu_{si,y}(t) = \mu_{si}(t) \cdot \cos \varphi \cdot \cos \theta \quad (2)$$

$$156 \quad \mu_{si,z}(t) = \mu_{si}(t) \cdot \sin \varphi \quad (3)$$

157 where μ_{si} is the wind pressure coefficient of the i th pressure tap; $\mu_{si,x}$, $\mu_{si,y}$ and $\mu_{si,z}$ are the
 158 decomposed wind pressure coefficients in the x , y , and z -direction of the i th pressure tap; φ and θ ,
 159 shown in Fig.5, are the angles between the normal direction of the surface and the horizontal and
 160 vertical axis direction respectively.

161 (3) The surface of the tower is divided into 1367 sub-areas in which the values of the wind
 162 pressure coefficients of the embodied pressure taps are regarded as the same. In each subarea, the
 163 nominal wind pressure coefficients can be calculated as:

$$164 \quad \mu_{sk} = \frac{\sum_{i=1}^n A_i \mu_{si}}{\sum_{i=1}^n A_i} \quad (4)$$

165 where μ_{sk} is the wind pressure coefficient of the k th subarea, A_i is the influence area of i th pressure
 166 tap, n is the total number of the pressure taps included in the k th area. Then the wind pressure of the
 167 k th subarea can be written as:

$$168 \quad w_k(t) = \mu_{sk}(t) \mu_{zk} w_0 \quad (5)$$

169 where w_k is the wind pressure of the k th subarea, μ_{zk} is the height coefficients of the wind pressure,
170 w_0 is the basic wind pressure, in this study $w_0=0.30$ kPa according to 10-year return period (2012).
171 Both the Eqs. (4) and (5) applies to x , y , and z -direction.

172 (4) Lastly, the loading nodes in the FEM are selected for the subareas in Step (3), and the wind
173 loading time histories can be calculated as:

$$174 \quad F_m(t) = w_k(t)A_m \quad (6)$$

175 where F_m is the m th loading nodes, A_m is the influence area of the m th loading nodes. Finally, 4101
176 time histories in FEM global coordinate system are obtained.

177 **5. Vibration control using DPTMD**

178 *5.1 Design of the Double-stage Pendulum Tuned Mass Damper*

179 A TMD system is installed in the BOT in order to mitigate the excessive wind-induced vibration.
180 Constrained by the architectural requirements, the space available for the mitigation service in this
181 building is quite limited: only a room of 4.80m×4.20m×5.80m can be utilized. In order to take full
182 advantage of the space without a significant increase in the total weight, the fire water tank is utilized
183 as the mass element of the absorber, because the volume of the tank excludes the possibility as a
184 sloshing-based mitigation. In consideration of all these factors, a Double-stage Pendulum Tuned
185 Mass Damper (DPTMD) was designed and installed on the floor of the Tower1 at the height of
186 232.5m(Fig.7).

187 There are some requirements, including long period, limit space and all motion directions, for
188 the TMD used in this tower. If a conventional pendulum TMD scheme was used in this project, at
189 least a space with more than 7.90m in height should be needed. However, the height of the available
190 space for the TMD is only 5.80m. Therefore, this DPTMD system utilizes the fire water tank as the

191 mass element and hangs the tank by a double-stage suspension system. As shown in Fig.8, this
192 system is composed of the fire water tank, outer cables, inner cables, suspension frame, tank support,
193 viscous dampers, limiters, structure connections, and support connections. The tank support supports
194 the fire water tank, which has a total mass of 50t. They together are hung by the double-stage
195 suspension system consisting of the outer cables, inner cables, and suspension frame. Four viscous
196 dampers are installed between the floor and the tank support to suppress the motion between the tank
197 and its support. Moreover, four limiters are used to restrict the maximum displacement of the tank.
198 The parameters of the DPTMD are shown in Table.4, determined by the limitations of the total mass,
199 maximum stroke and installation space of the DPTMD. The mass ratio of the DPTMD to the
200 structure is only 0.058%. The frequency ratio of the DPTMD in the directions of the first two modes
201 are 1.055 and 1.025, while the corresponding damping ratios are 0.120 and 0.116 respectively.
202 Considering the uncertainty in the construction, one can adjust the length of the cables after the field
203 testing.

204 5.2 Numerical simulation of the wind-induced vibration

205 5.2.1 Spatial distribution

206 The wind-induced vibrations of the BOT with and without TMD are analyzed by inputting the
207 three-dimensional wind field simulated in Section 4.2 to the FEM model. Fig.9 shows the spatial
208 distribution of the maximum node acceleration over time under the wind directions of 45° and 135°.
209 The combination of the horizontal accelerations and of all the three acceleration components are
210 $\sqrt{a_x^2 + a_y^2}$ and $\sqrt{a_x^2 + a_y^2 + a_z^2}$, in which a_x , a_y , and a_z are the maximum node accelerations over time in
211 the directions of X, Y and Z. It can be observed that: (1) The acceleration distributions of the BOT
212 with and without TMD are similar. After the installation of the TMD, the total horizontal

213 accelerations are all reduced. However, the TMD does not affect the vertical acceleration responses.

214 (2) In general, the acceleration increases from the bottom to the top and from the inner part to the

215 outer part. The accelerations of the tower crown are larger than those of the body, especially in the

216 vertical direction. The maximum accelerations the main bodies of the Tower 2 and 4 are larger than

217 those of the other sub towers, while those of the crowns of the Tower 3 and 5 are larger than the other

218 towers.

219 5.2.2 Response variation with wind directions

220 There are two main public scenic sites in each sub tower: one is the viewing platform at the top

221 of each tower, and the other is the viewing hall, which is the floor immediately below the platform.

222 As there will be many people on these sites to watch the scenery of Beijing city, the issue of human

223 comfort is of concern. Therefore, by considering eight typical wind directions, the mean and

224 maximum horizontal accelerations of the viewing platform and hall are assessed and shown in Fig.10

225 and Fig.11. It can be concluded from the Fig.10 that: (1) In general, the maximum acceleration

226 occurs at the edge nodes of the viewing platform. The structural constraint on these nodes is much

227 weaker than those at the middle. Thus the reduction effect of the TMD on the mean accelerations is

228 better than on the maximum accelerations. (2) The wind-induced accelerations of the tower subjected

229 to the wind loads with the directions of 45° , 135° , 225° , and 315° are larger than those subjected to

230 the wind loads with the other directions. This phenomenon is mainly due to the first two modal

231 shapes of the BOT. (3) The best reduction effect is with the wind direction of 270° , when the

232 reduction ratio of Tower1, Tower2, and Tower3 are 16.44%, 30.05%, and 22.63%, respectively. (4)

233 Because the DPTMD was installed only on Tower1, it has a slight effect on some of the sub towers,

234 among which reduction effect on Tower5 is limited. The reduction effect in the viewing hall as

235 shown in Fig.11 is similar to the effect in the viewing platform. Moreover, the maximum reduction
236 ratio of the viewing hall is 24.56%, which also occurs in the wind direction of 270°. As the
237 connections between Tower1 and Tower5 are weaker than those between Tower1 and the other sub
238 towers, the acceleration reduction effect, both in the viewing platform and in the viewing hall of
239 Tower5, is the weakest among these sub towers. Moreover, the reduction effect in the viewing hall is
240 much better than in the viewing platform.

241 5.2.3 Response time history and PSD

242 The time history responses and the corresponding power spectral densities of two nodes on the
243 viewing platform of the Tower1 and Tower5 in the x -direction are shown in Fig.12 and Fig.13 with
244 the wind direction of 45°. Meanwhile, these responses in the y -direction are shown in Fig.14 and
245 Fig.15. In the time domain, the reduction of the displacements is better than the accelerations at both
246 x and y directions. In the frequency domain, the DPTMD has a considerable reduction effect on both
247 the accelerations and displacements at the first bending mode but does not affect the higher modes.
248 However, the higher modes do have some influences on the wind-induced responses, and the
249 accelerations are affected much more than the displacements. Comparing with the node in Tower 5,
250 the reduction effect of the node in Tower1 is much better, and this confirms the conclusions from the
251 analysis in the section above.

252 6. Concluding remarks

253 The wind-induced response of the BOT and the performance of its vibration control are
254 presented in this paper. The three-dimensional wind loading for the FEM analysis of the BOT is
255 established based on the wind tunnel test results. Moreover, based on the dynamic characteristics and
256 responses of the BOT, a DPTMD was designed and installed on the tower. Then, the wind-induced

257 responses of the tower with and without DPTMD are compared with respect to various wind
258 directions and both in the time and frequency domain. Based on the results and discussions presented,
259 the following remarks can be obtained:

- 260 (1) Mostly, the wind-induced accelerations of the tower subjected to the wind loads with the
261 directions of 45° , 135° , 225° , and 315° are larger than those with the other directions.
- 262 (2) The DPTMD design utilizes a shorter pendulum length to achieve a long period, thus a lot of
263 spatial space can be saved given the excellent control performance on the BOT can be ensured.
264 The design serves as a reference for other slender high-rise towers.
- 265 (3) Only with 0.058% structural mass does the DPTMD mitigate the wind-induced vibration of the
266 tower effectively. The maximum acceleration reduction ratio for the mean accelerations of each
267 floor, which occurs in Tower2 with the wind direction of 270° , reaches 30.05%. Because of the
268 relatively weak connections between sub towers, the reduction effect of the Tower5 is lower than
269 the other sub towers.
- 270 (4) Because of the limitation of the physical space, only one TMD with a small mass can be installed
271 in this tower. Only the response induced by the first two modes can be suppressed, although
272 higher modes can affect the towers' wind-induced accelerations as well.

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Table.1 Structural geometry of the BOT

Tower	Tower1	Tower 2	Tower 3	Tower 4	Tower 5
Architectural diameter/ m	16.20	9.60	9.60	8.30	8.30
Structural diameter/ m	14.00	7.30	7.30	6.00	6.00
Structural height/ m	244.35	228.00	210.00	198.00	186.00
Slenderness ratio	17.45	31.23	28.77	33.00	31.00
Diameter of the top/ m	51.20	33.60	32.40	30.00	26.40
Distance to Tower1/ m	-	19.17	15.75	15.10	16.90

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Table.2 Natural frequencies of the tower

Modes	Frequency/ Hz	Description
1	0.176	1st overall bending (45°)
2	0.181	1st overall bending (135°)
3	0.227	1st overall torsional (anti-symmetric bending of the Tower2 and 4 (45°) + anti-symmetric bending of the Tower3 and 5 (135°))
4	0.512	2nd overall bending (45°)
5	0.559	2nd overall bending (135°)
6	0.598	2nd overall torsional (symmetric bending of the Tower2 and 4 (45°) + anti-symmetric bending of the Tower3 and 5 (135°))
7	0.703	2nd overall torsional (symmetric bending of the Tower2 and 4 (45°) + symmetric bending of the Tower3 and 5 (135°))
8	0.721	2nd overall torsional (anti-symmetric bending of the Tower2 and 4 (45°) + symmetric bending of the Tower3 and 5 (135°))
9	0.790	2nd overall torsional (local vibration of the Tower4 crown + anti-symmetric bending of the Tower3 and 5 (135°))
10	1.019	3rd overall bending (45°)
11	1.088	3rd overall bending (135°)

Table.3 Simulated turbulence intensity in the model tests

Segment model	Elevation/ m	Reference height/ m	Reference turbulence intensity/ %	Simulated turbulence intensity/ %
1	0-49.2	30-40	18-20	18
2	49.2-109.2	70-90	15-16	15
3	109.2-169.2	130-150	13-14	14
4	145.8-244.35	180-200	12	11.5

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Table 4. Parameters of the DPTMD system

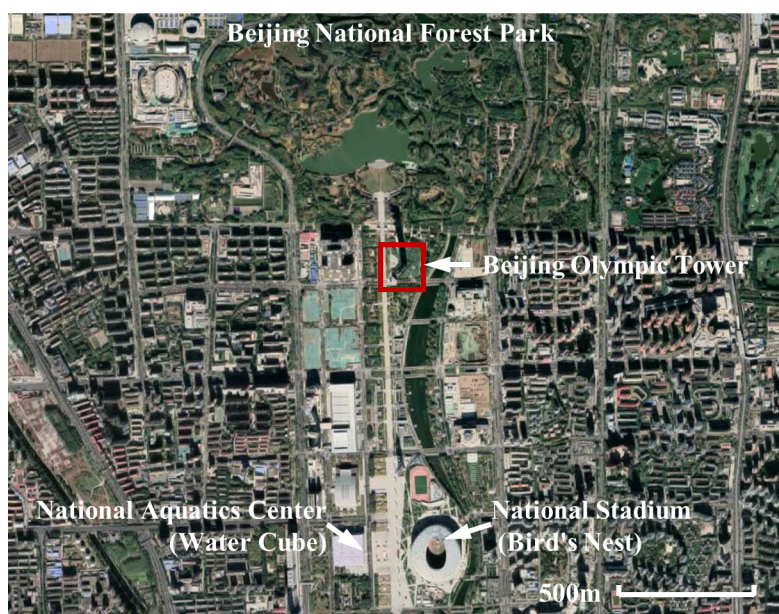
Direction	x	y
Effective length of cable/ m	7.90	7.90
Mass/ t	50	50
Damping exponent of the damper	1	1
Damping coefficient of the damper/ N·s/m	6997	6788

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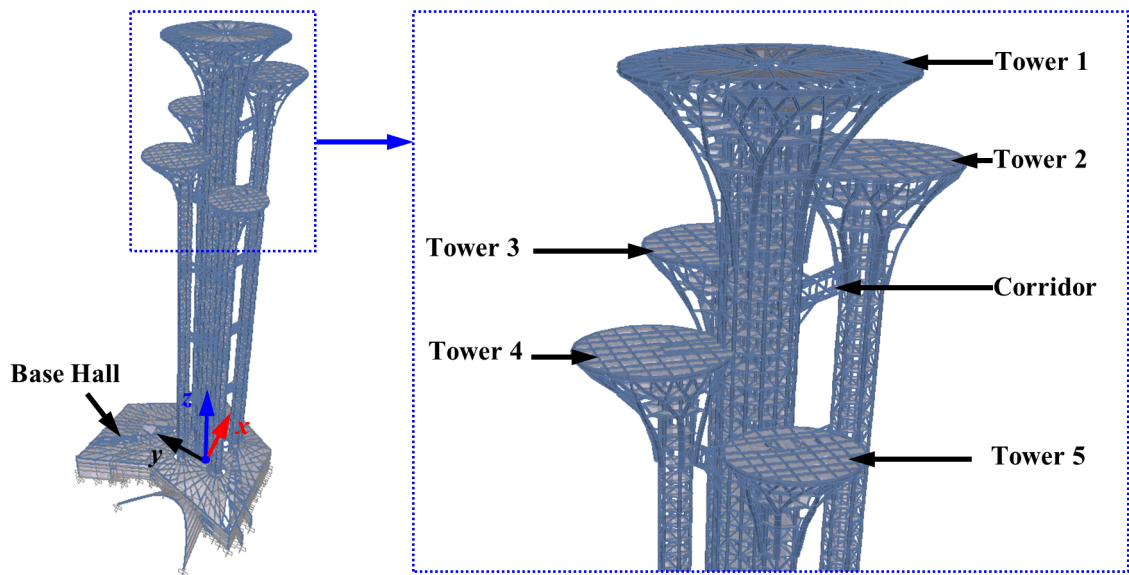
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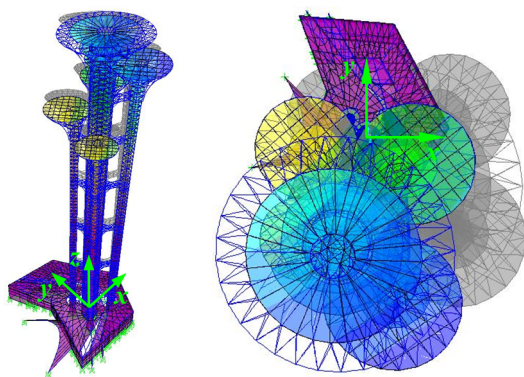
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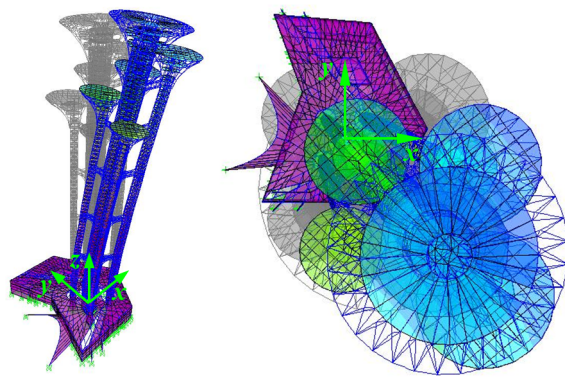
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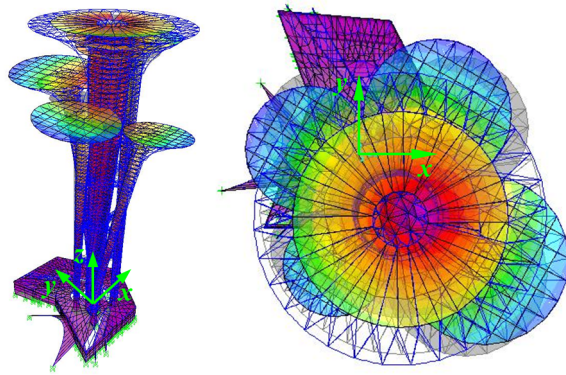
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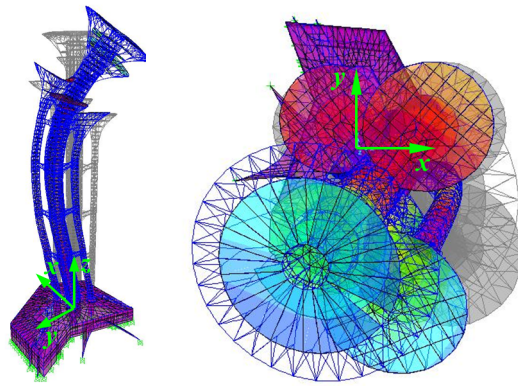
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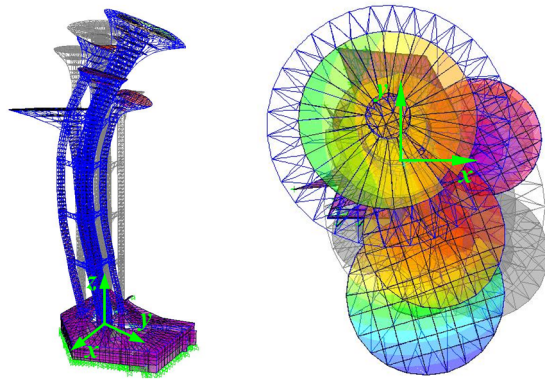
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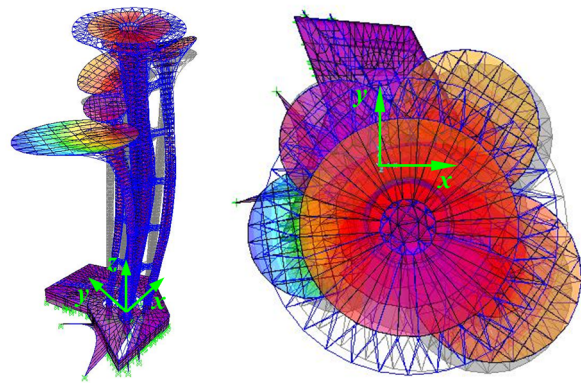
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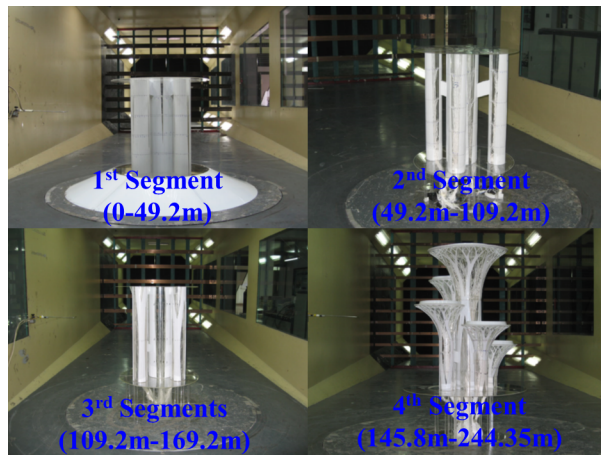
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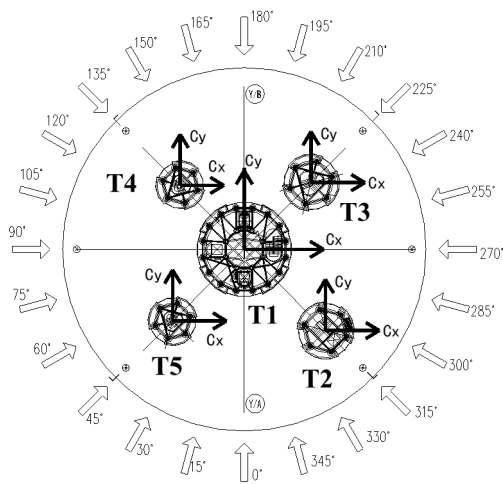
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TAL_1704_Fig.3f.tif

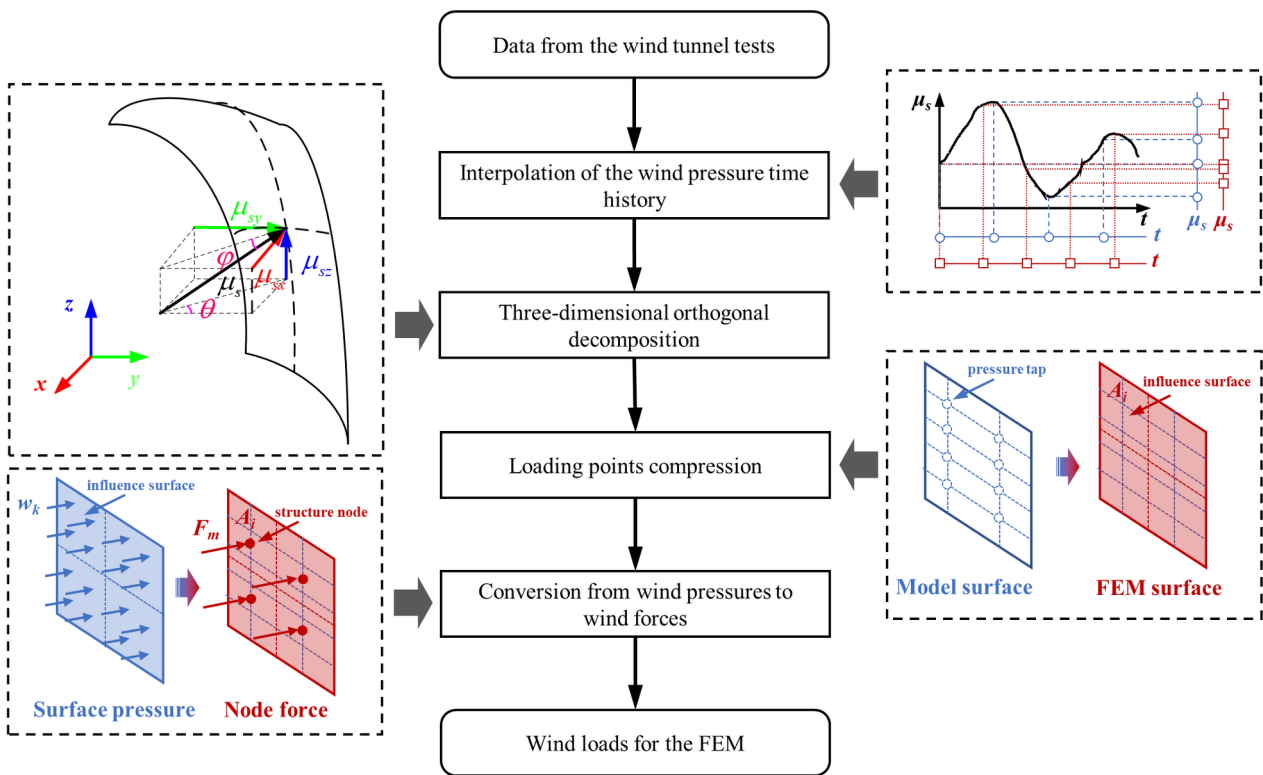


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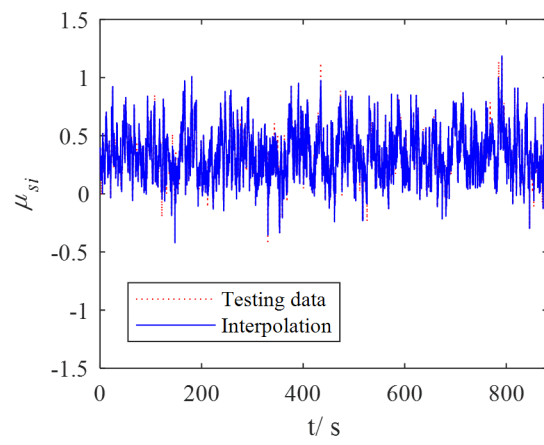


Note: T is short for Tower.

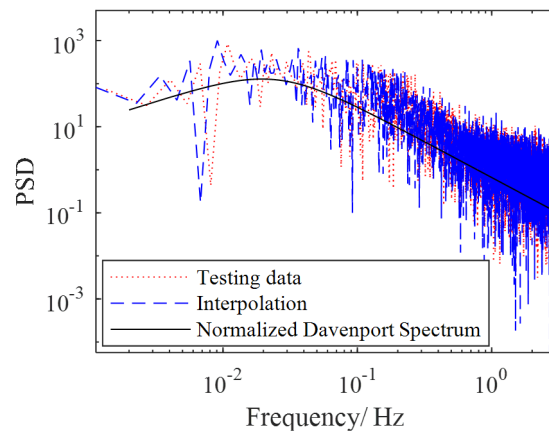
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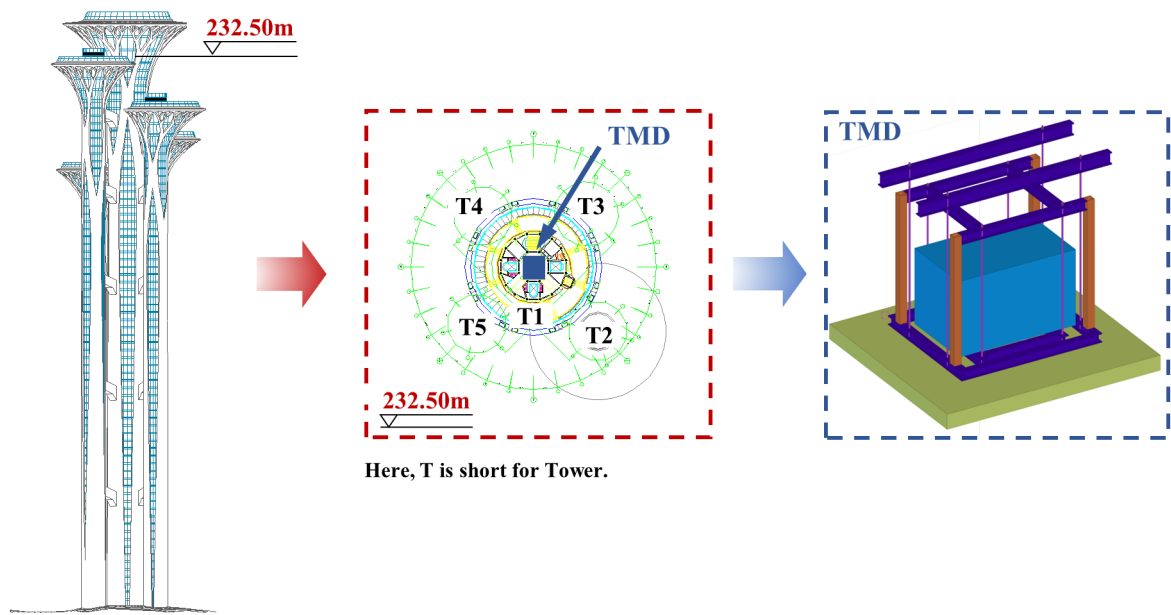
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TAL_1704_Fig.6a.tif

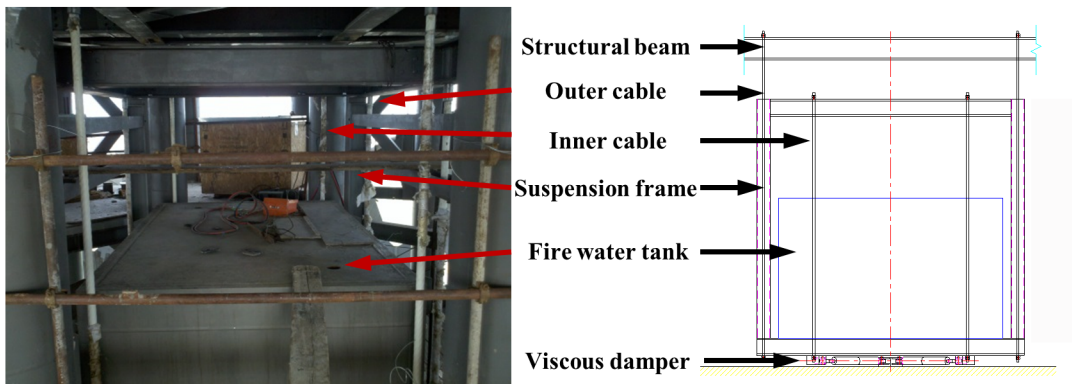


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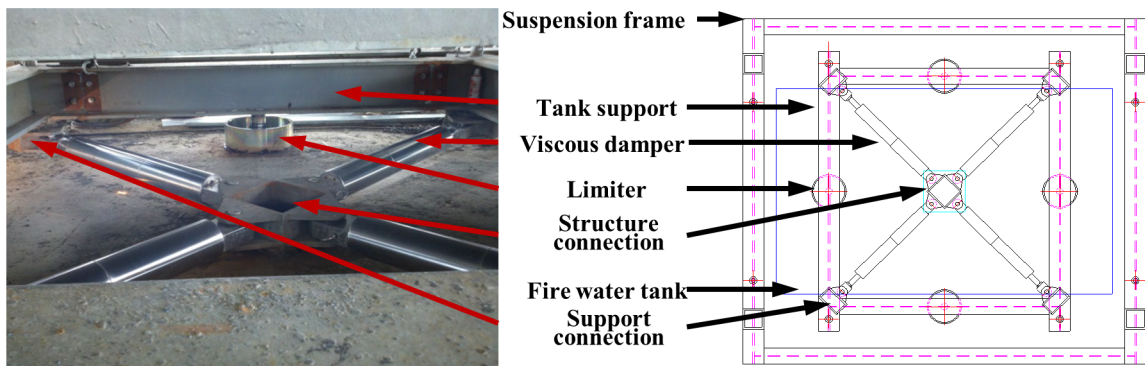


Here, T is short for Tower.

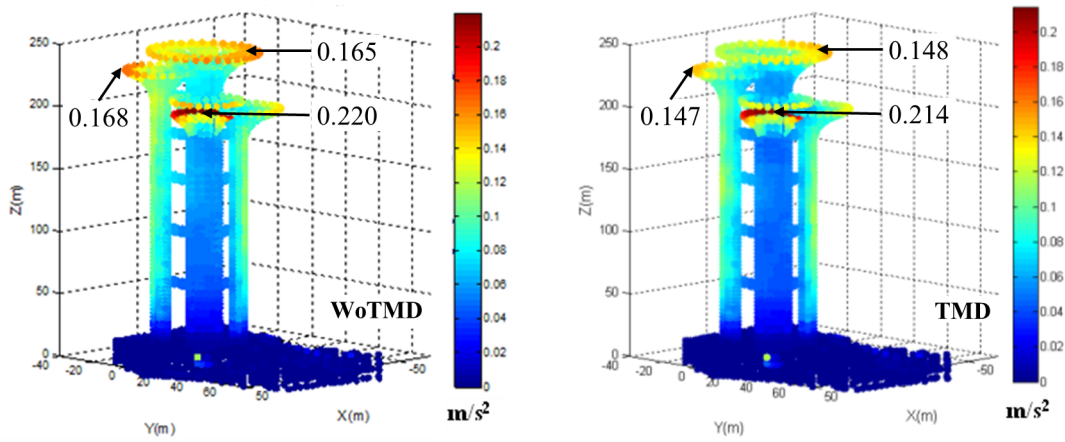
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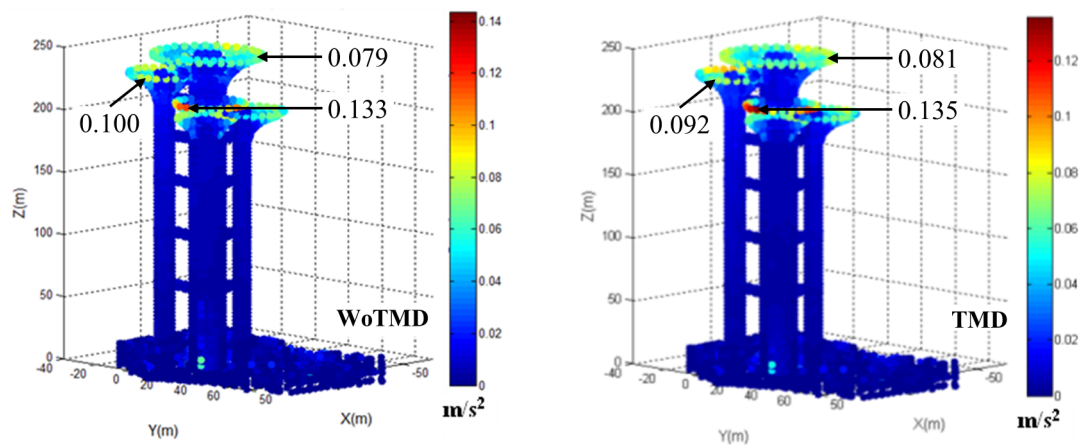
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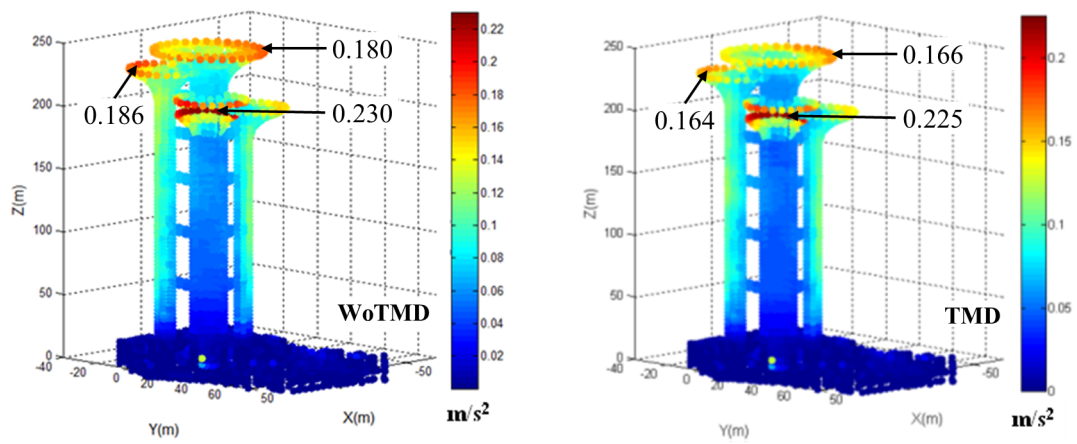
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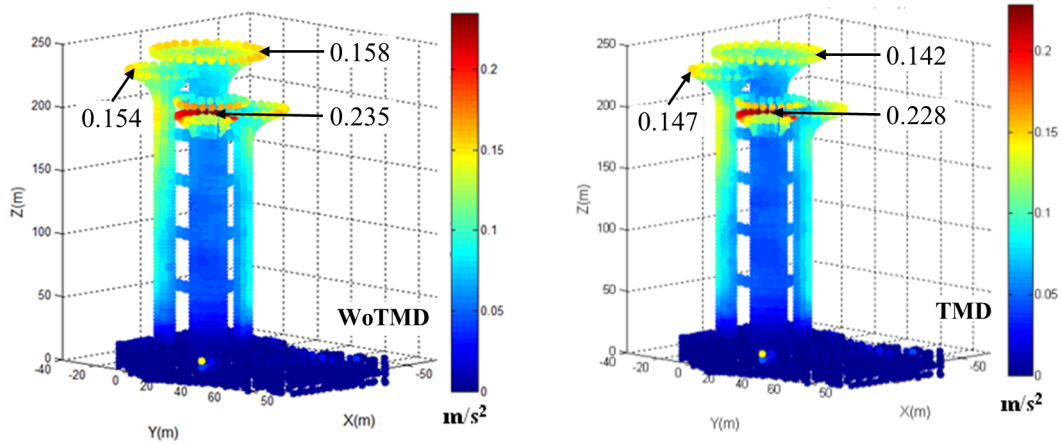
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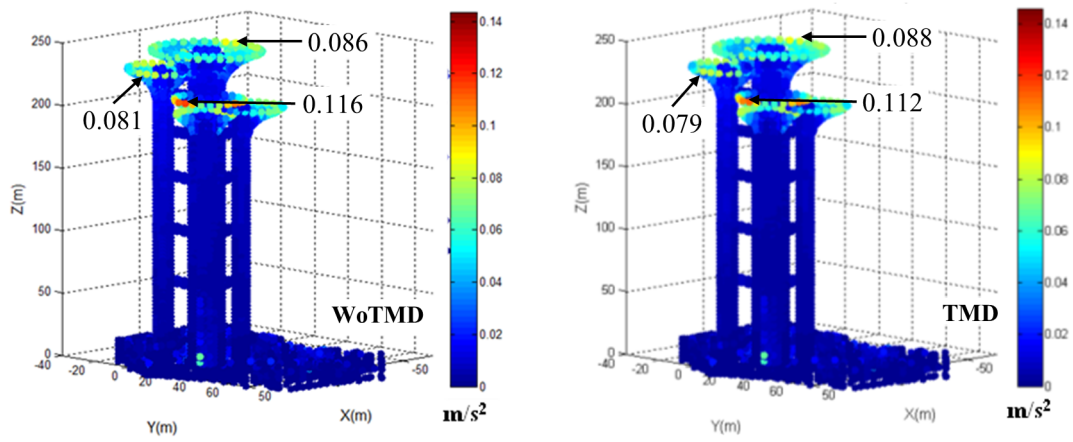
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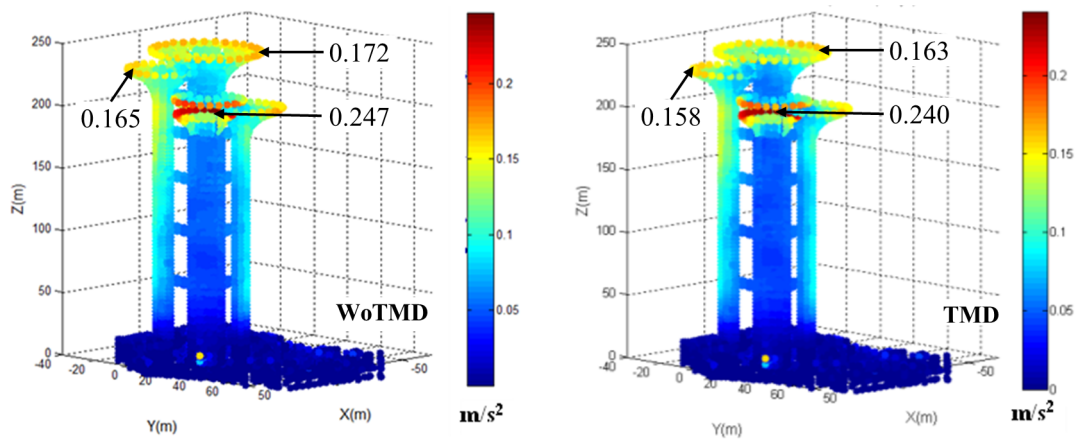
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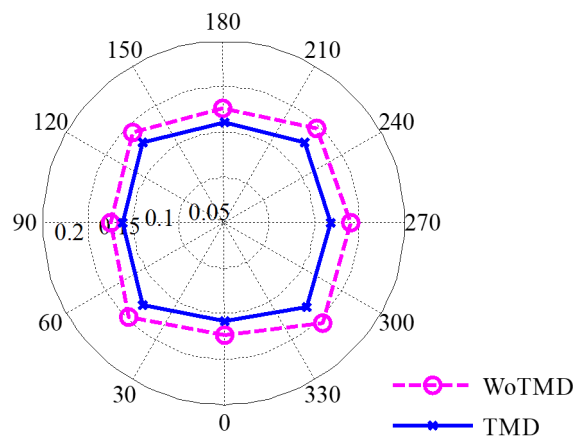
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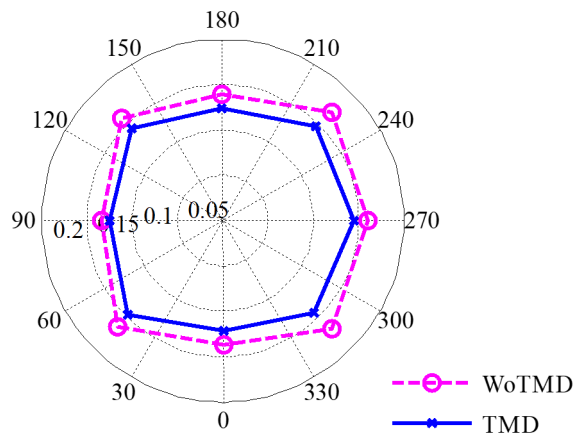
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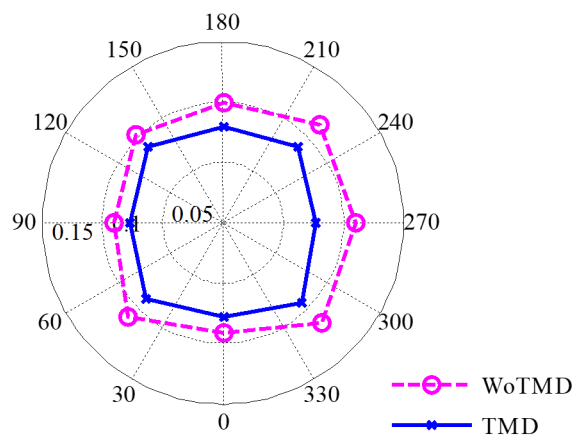
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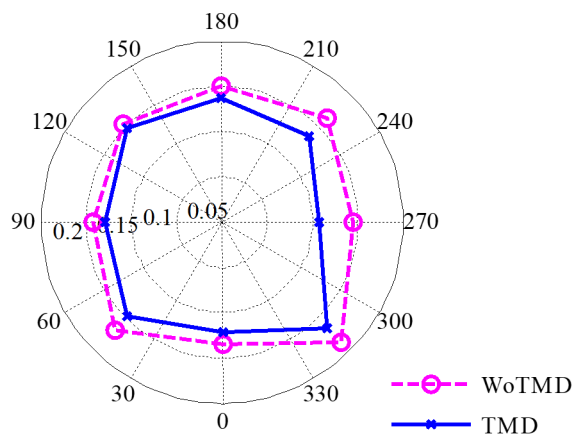
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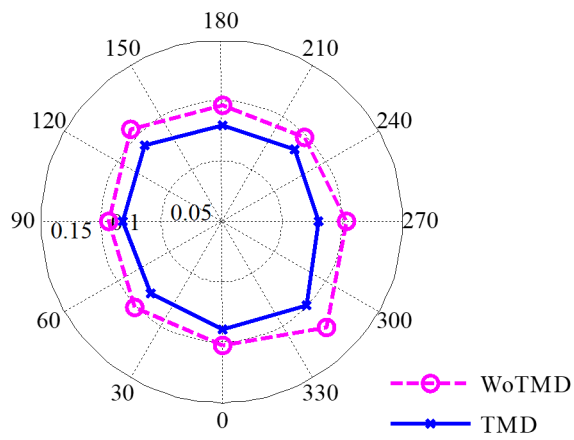
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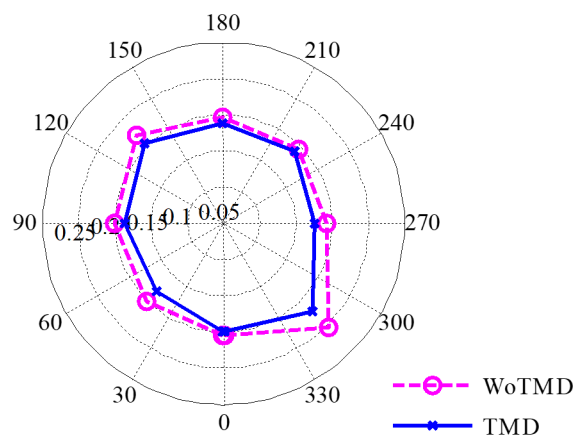
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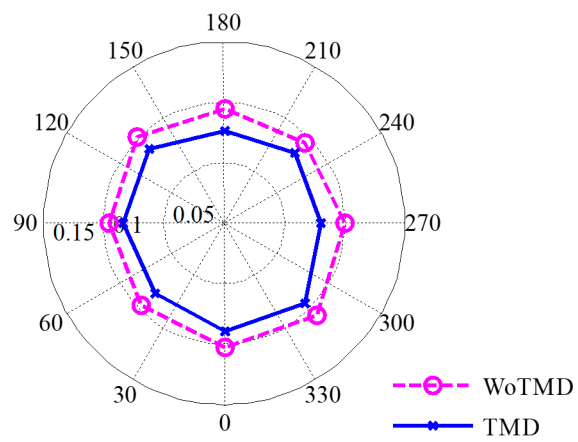
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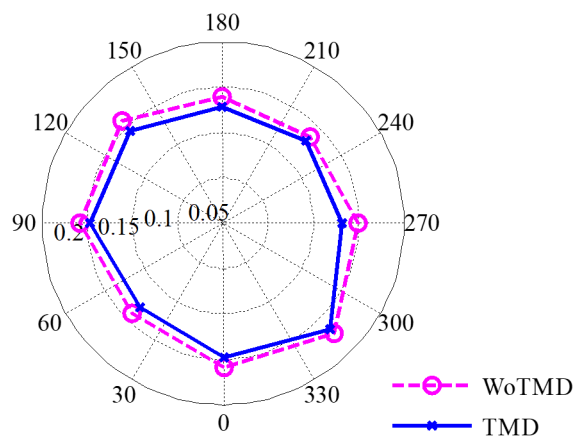
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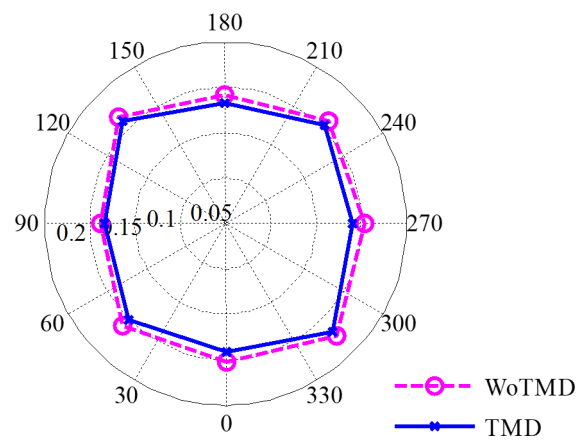
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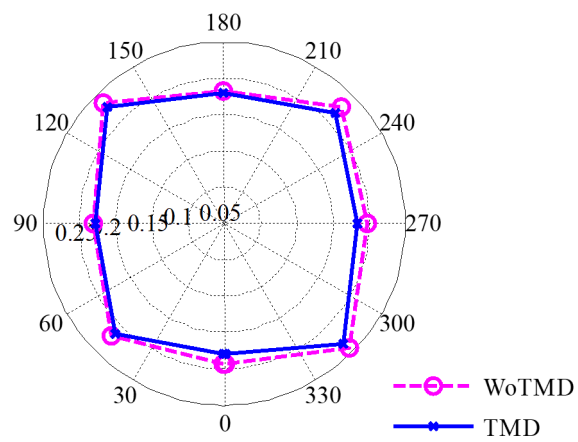
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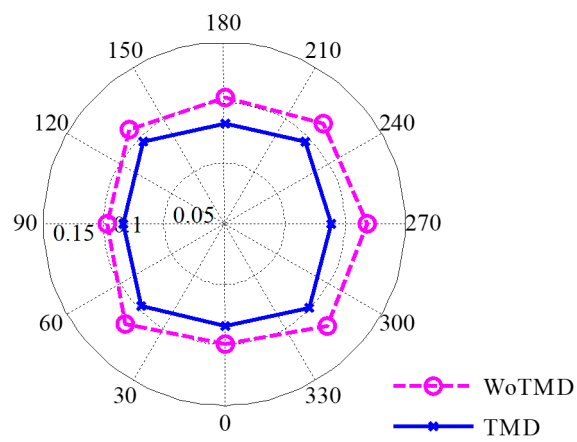
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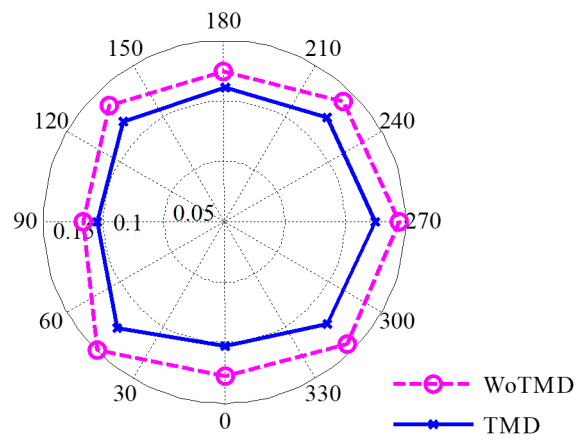
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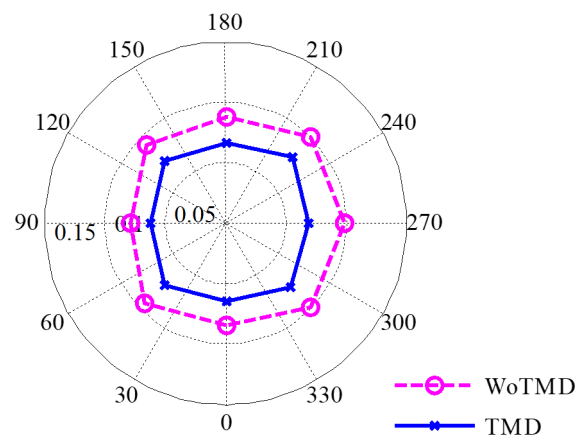
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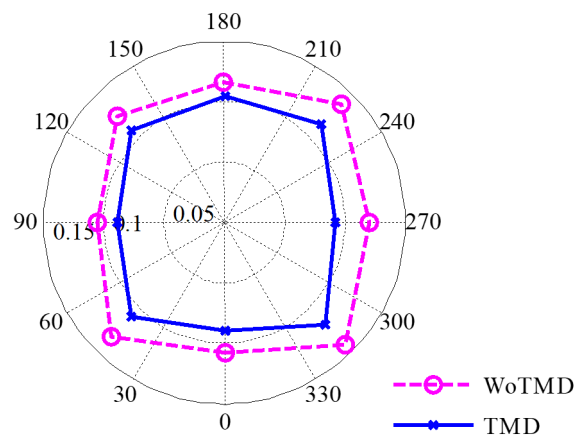
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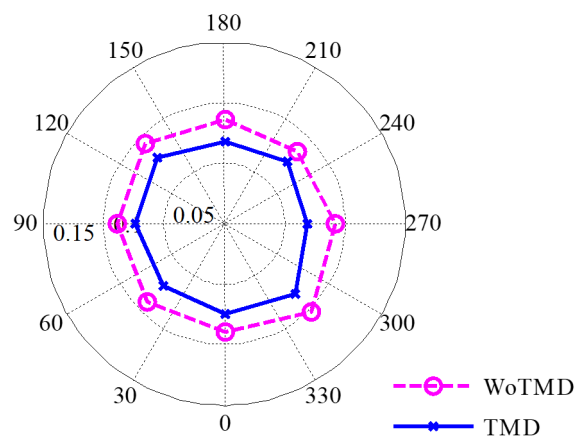
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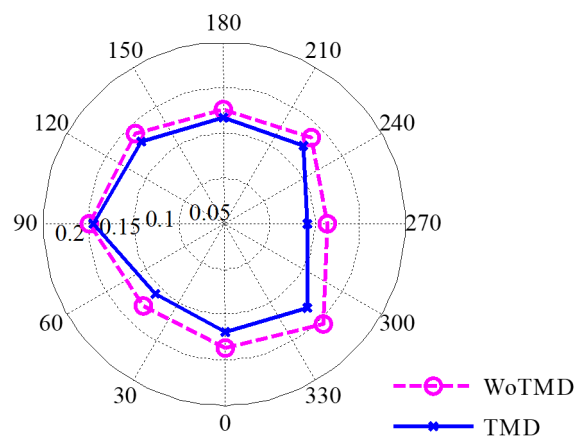
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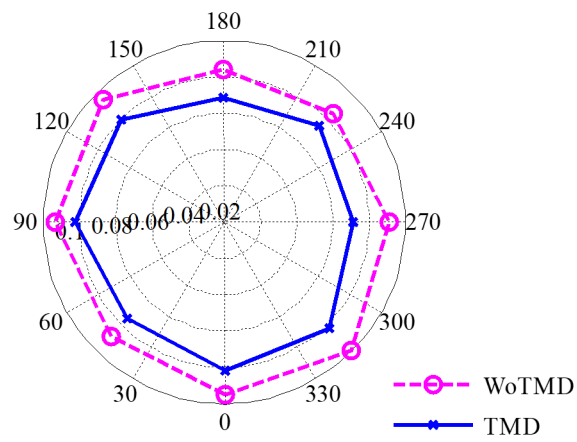
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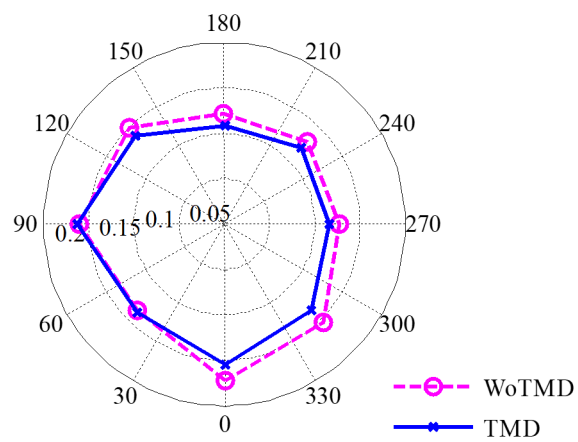
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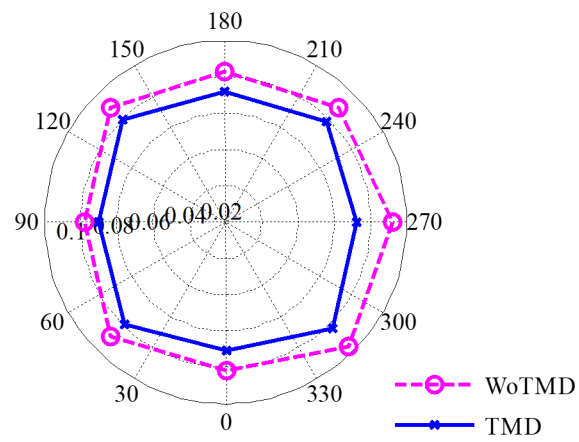
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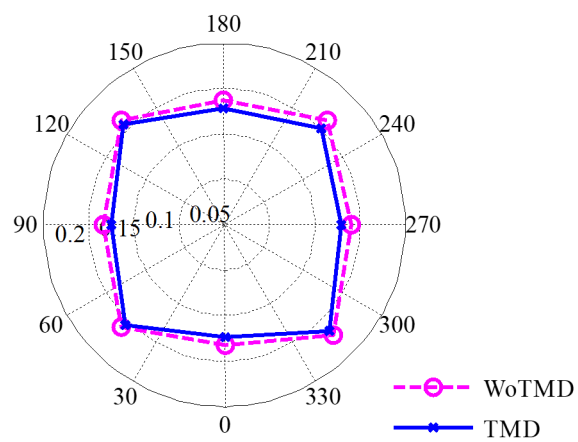
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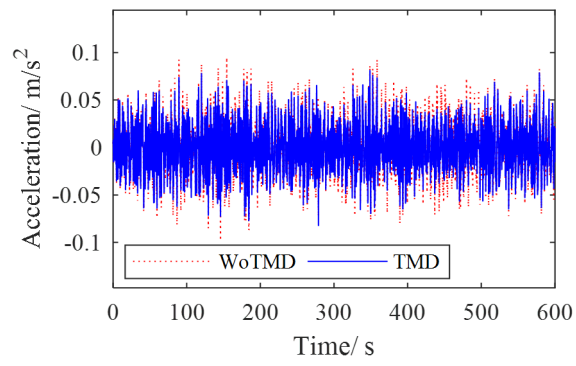
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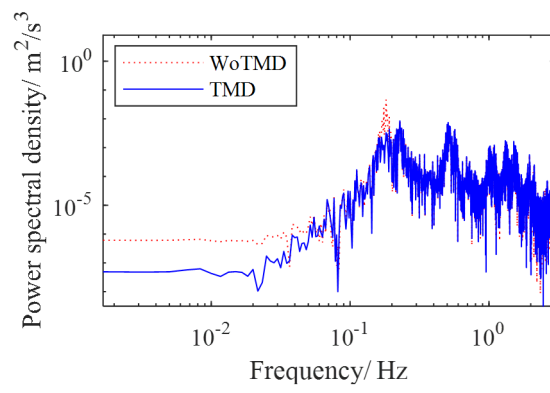
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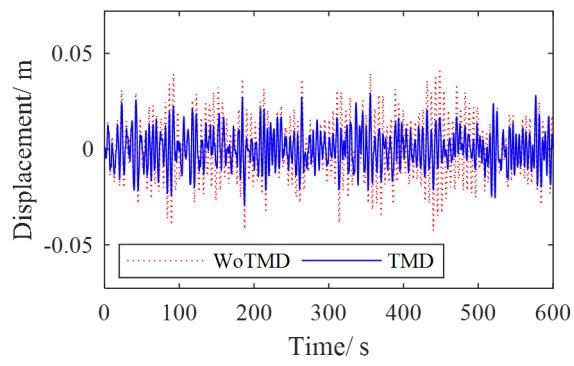
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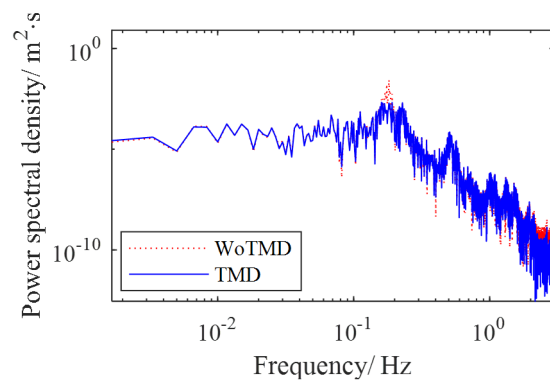
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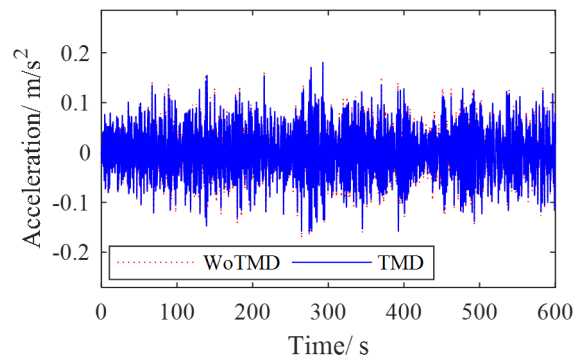
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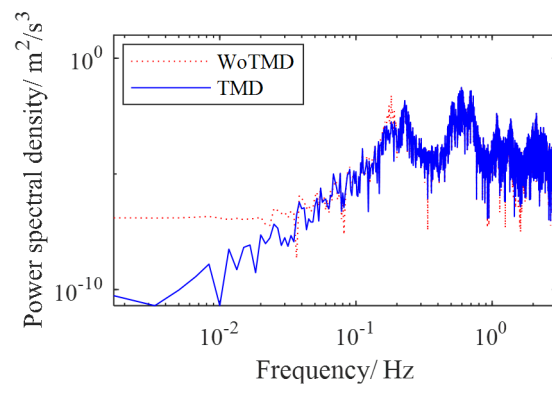
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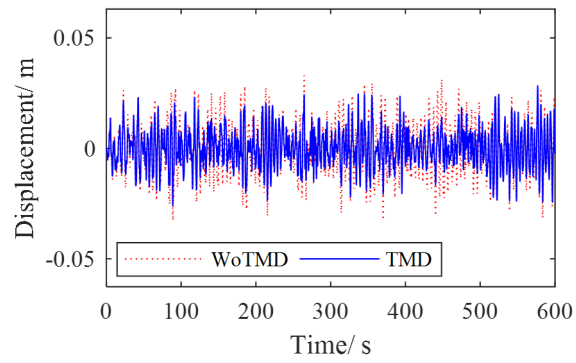
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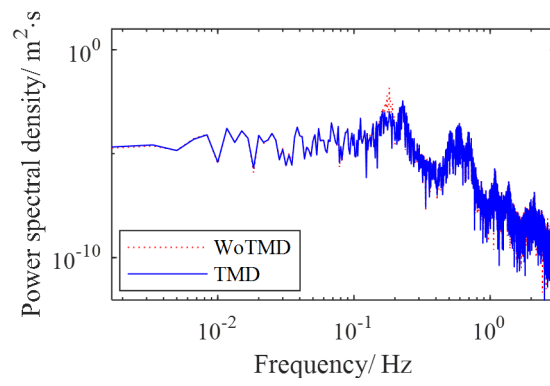
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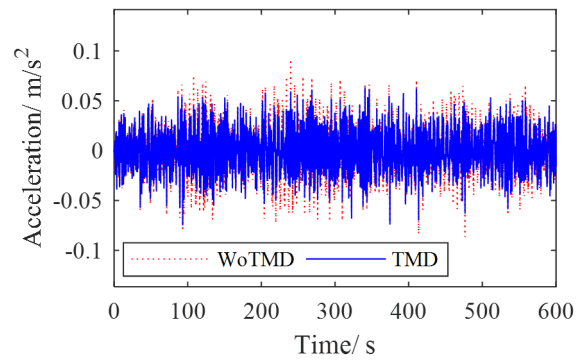
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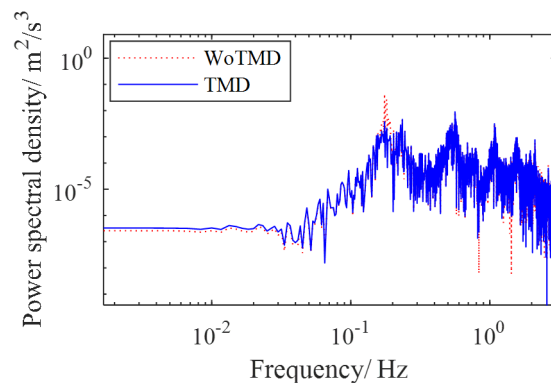
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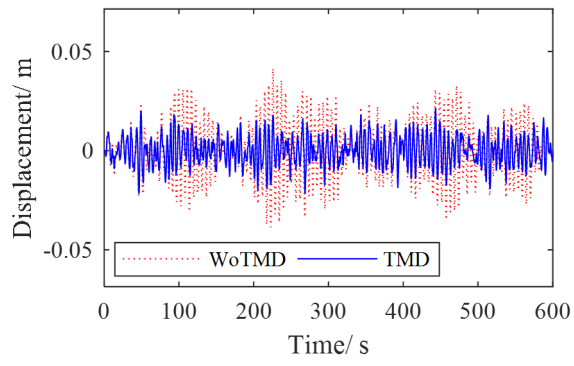
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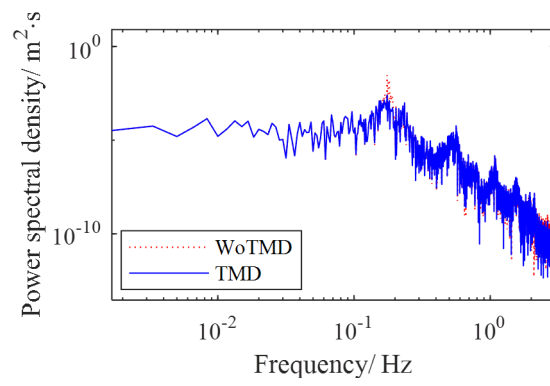
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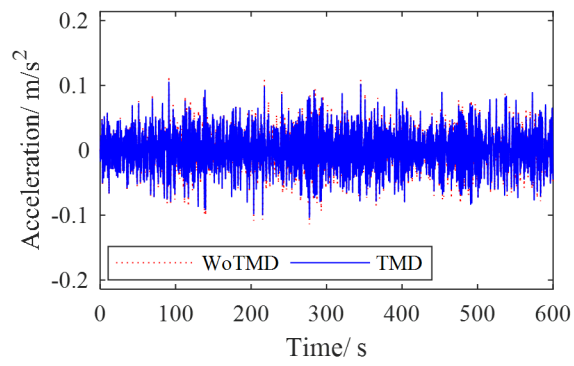
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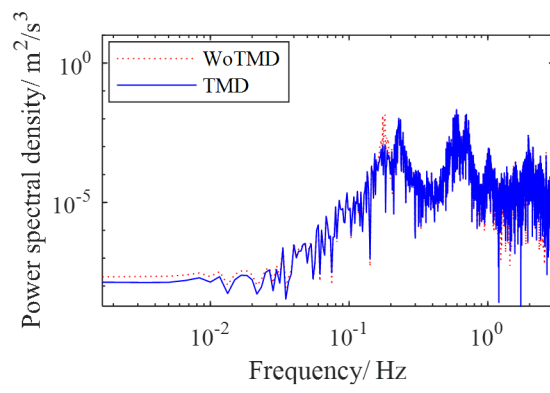
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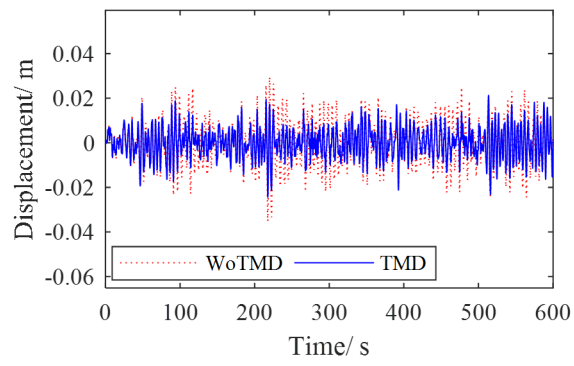
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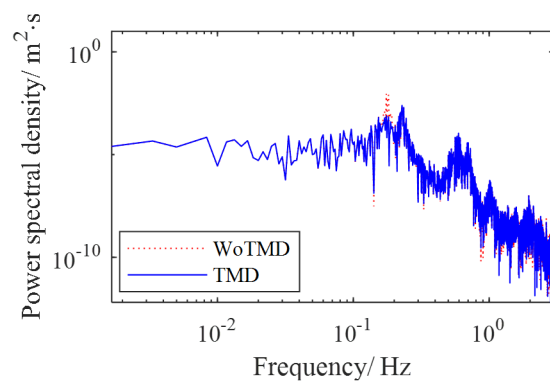
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TAL_1704_Fig.15c.tif



TAL_1704_Fig.15d.tif