

An Instant Change of Elastic Lattice Strain during Cu₂Se Phase Transition: Origin of Abnormal Thermoelectric Properties

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The superionic conductor Cu₂Se is a promising thermoelectric material due to its low thermal conductivity. An abnormal but clear change in the thermoelectric parameters has been observed during the phase transformation from the ordered and non-cubic α -Cu₂Se to the disordered and cubic β -Cu₂Se. However, the microstructural origin of the abnormal change and its implications for thermoelectric applications remain largely unknown. Herein, by mimicking the real working conditions of thermoelectrics, the phase transition from α - to β -Cu₂Se induced by the rising temperature has been carefully investigated by in situ transmission electron microscopy. It is observed that an abrupt and anisotropic volume-change in the Se-sublattice occurs when the temperature is raised to the phase transition point. The abnormal change in the crystalline volume versus temperature, which is caused by the local migration of Cu-ions, induces an instant and uncommon strain-field, which reduces the carrier's mobility and increases the electrical resistance. Local migration of Cu-ions is responsible for a quite low thermal conductivity. Such effects exist only at the instance of the phase transition. Observing the thermoelectric response of the structure during the phase transition may provide insights into the development of high performance thermoelectric materials, which fall beyond the traditional approaches.

1. Introduction

Thermoelectric technology is a promising approach of generating clean energy from waste heat, including the heat from


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automobile's exhaust systems, solar energy, and geothermal energy.^[1] Advances in the thermoelectric technology rely on the discovery of highly efficient thermoelectric materials. The efficiency of a thermoelectric (TE) material is gauged by its dimensionless thermoelectric figure of merit ZT , defined as $ZT = \alpha^2 \sigma T / (\kappa_l + \kappa_e)$, where α , σ , κ_l , κ_e , and T are the Seebeck coefficient, electrical conductivity, lattice thermal conductivity, electronic thermal conductivity, and the absolute temperature, respectively.^[2]

Cu₂Se is one of the so-called "liquid-like" thermoelectric materials, often referred to as "phonon-liquid electron-crystal" structure.^[3] In the crystal lattice, Se-anions constitute a rigid cubic sublattice while Cu cations form a liquid-like sublattice, and thus have a rather high mobility.^[3a,4] Due to its "liquid-like" structure, Cu₂Se has an intrinsically ultralow lattice thermal conductivity, an important aspect for an efficient thermoelectric.^[5] Moreover, Cu₂Se (and other liquid-like

materials) show an exceptionally good electronic transport property, which are believed to be associated with the rigid Se sub-lattice. Therefore, high ZT values above 2 were attained in Cu₂Se, which shows great perspective for commercial applications in power generation recycling the waste heat at high temperature.^[6] However, noted that this "half-solid half-liquid" nature of the structure gives rise to the "abnormal" transport properties. A striking feature of Cu₂Se is its abnormal transport behavior observed in the temperature range between 340 and 400 K, where a phase transition from the ordered α -Cu₂Se phase to the disordered β -Cu₂Se phase takes place.^[7] Within the narrow range of the α to β phase transition, the so-called critical scattering regime for phonons and electrons, ingenious experimental designs were developed to make transport measurements under precisely controlled temperature.^[8] Under an unusual transport measurement, an extremely high Seebeck coefficient and ZT (as high as 400) have been reported.^[9] Under the usual conditions of transport measurements, it was also shown that the ZT has increased by a factor of about ≈ 3 – 7 times at the phase transition temperature.^[4c,8] However, the underlying mechanism of the abnormal behavior

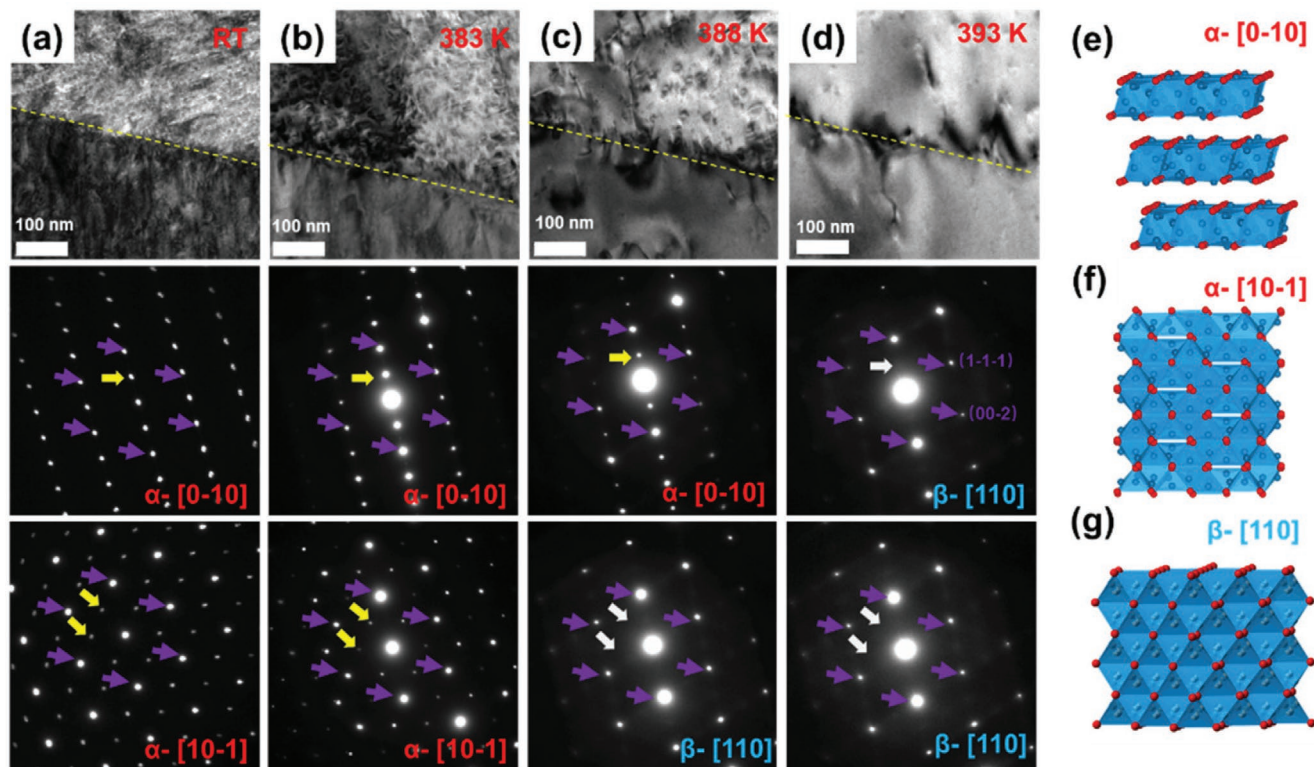


Figure 1. Change in the diffraction patterns and TEM images during heating of Cu_2Se . a–d) TEM images and selected area electron diffraction (SAED) on both sides of the grain boundary (yellow dotted line) at RT, 383, 388, and 393 K, respectively. The second row is the SAED of area 1, and the third row is the SAED of area 2. e–g) Simulated structure of the α - Cu_2Se phase along the [0-10], [10-1], and of the β - Cu_2Se phase along the [110] directions, respectively.

remains largely unclear and thus its potential impact on the development of high performance thermoelectric materials, by utilizing the above extraordinary properties, has not yet materialized.

In this paper, the dynamical microstructural evolution of Cu_2Se during the α to β phase transition has been carefully studied to reveal the microstructural mechanism of the critical scattering and the origin of the abnormal thermoelectric properties. When a thermoelectric material operates as a power generator or as an electronic cooler, it is exposed to a temperature gradient. With the development of in situ transmission electron microscopy (TEM),^[10] microstructural evolutions can be monitored by both imaging and diffraction while the temperature is varied. Adopting the latest technical advances, we have observed an abrupt change in the lattice strain in Cu_2Se during the phase transition. We believe this provides a novel insight into the cause of the observed critical scattering.

2. Results and Discussion

Microstructural changes and crystalline evolution in the Cu_2Se sample prepared by the method of self-propagating high-temperature synthesis (SHS) were studied by in situ TEM. The temperature was gradually increased to induce the α - Cu_2Se to β - Cu_2Se phase transition (please refer to Video S1, Supporting Information). While the high temperature β - Cu_2Se has

a face-centered cubic structure ($a = 5.84 \text{ \AA}$), at room temperature Cu_2Se is in its monoclinic α - Cu_2Se phase^[7b] ($a = 7.148 \text{ \AA}$, $b = 12.349 \text{ \AA}$, $c = 13.833 \text{ \AA}$, $\beta = 100^\circ$, space group of $C2/C$). According to the previous studies of the α - Cu_2Se structure,^[7a–7d] although there are many α - Cu_2Se variants, we found that all observed electron diffraction patterns could be indexed using this structure. As shown in Figure 1a and Figure S1, Supporting Information (with spots being indexed), two α - Cu_2Se crystals separated by a grain boundary can be identified, one oriented along the [0-10] direction and the other along the [10-1] direction. When heated up to 383 K, the two crystals remained in the α - Cu_2Se phase, while based on the observed image contrast, the density of dislocations and stacking faults created due to the fast non-equilibrium SHS process was greatly reduced in the two crystals (Figure 1b). At the temperature of 388 K, based on the disappearance of the superlattice spots (as marked by white arrowheads in Figure 1c), a phase transition from α - Cu_2Se [10-1] to β - Cu_2Se [110] has commenced. However, the α - Cu_2Se [0-10]-oriented crystal has not transformed into the β - Cu_2Se [110] phase until the temperature reached 393 K. This is shown in Figure 1d, where the superlattice spots identifying the α - Cu_2Se [0-10] crystal have disappeared. The atomic structure of the two α - Cu_2Se crystals and of β - Cu_2Se is shown in Figures 1e–g, respectively. Their experimental selected area electron diffraction (SAED) patterns are compared to the simulated patterns to confirm the correctness of the crystalline indexes in Figure S2, Supporting Information.

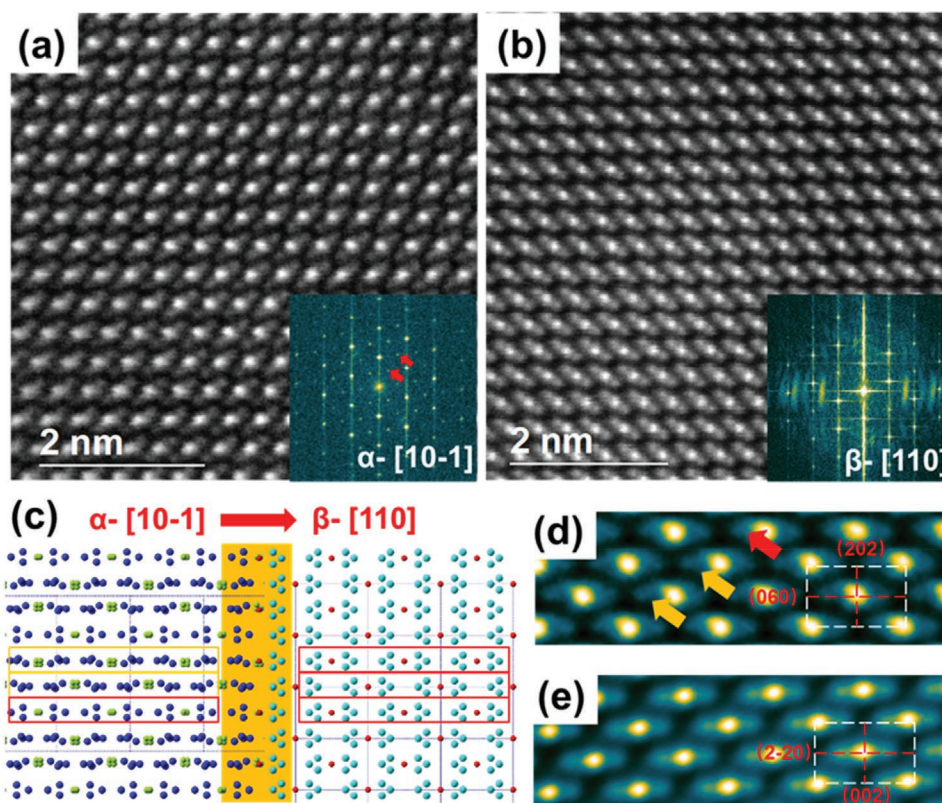


Figure 2. Structural contrast between the α -phase of Cu_2Se along the $[10\bar{1}]$ direction and the β -phase along the $[110]$ direction. a,b) Atomic resolution HAADF-STEM images in the α - $[10\bar{1}]$ and β - $[110]$ directions. The insets are the corresponding FFT images. The red arrow points out the difference between the two phases. c) Schematic diagram of atomic structure of the two phases. d) Atomic images of the α - Cu_2Se along $[10\bar{1}]$ directions at high magnifications. e) Atomic images of the β - Cu_2Se along $[110]$ directions at high magnifications.

It is a surprising observation that the critical phase transition temperature depends on the orientation of the α - Cu_2Se domains. In our in situ TEM experiment, we kept the temperature at 388 K for more than an hour (≈ 68 min) and the α - Cu_2Se $[0\bar{1}0]$ - oriented crystal remained stable (Figure S3, Supporting Information). At the moment the temperature was increased to 393 K, we observed instantly the formation of β - Cu_2Se . This suggests that the phase transformation is not related to the Cu-ions' gradual (or thermal) diffusion, but is closely correlated to a sudden Cu-ion's hopping among sites with quantized energy levels.

Along with the hopping of Cu-ions from ordered sites to disordered ones, there is also an elastic contraction and/or expansion of the Se-sublattice due to the phase transformation, which induces a large elastic strain in the system with mixed α and β - Cu_2Se phases. The Se-sublattice has a *fcc* structure and can be identified by the strong diffraction spots as marked by purple arrowheads in Figure 1a–d. An overlap of the diffraction patterns of the α - Cu_2Se $[10\bar{1}]$ domain, α - Cu_2Se $[0\bar{1}0]$ domain, and β - Cu_2Se $[110]$ is shown in Figure S4, Supporting Information, in which the mismatch among the domains can be clearly seen. As shown in Figure S4b, Supporting Information, when the lattice parameter of β - Cu_2Se is used as the reference, the pseudocubic parameter *a* of the α - Cu_2Se $[10\bar{1}]$ domain and $[0\bar{1}0]$ domain is different. This is especially so in the phase transformation from the α - Cu_2Se $[0\bar{1}0]$ domain to β - Cu_2Se $[110]$, where

the *d*-spacing of the $(\bar{2}02)$ plane becomes large, while that of the (004) plane is reduced. This induces an anisotropic elastic strain in the Se-sublattice.

The resemblance of the α - Cu_2Se $[10\bar{1}]$ domain to the β - Cu_2Se $[110]$ structure leads to a lower transition temperature (compared to that between the α - Cu_2Se $[0\bar{1}0]$ domain and β - Cu_2Se $[110]$), implying that the strain mismatch in the domains does change the critical energy needed for the phase transformation. In other words, under a small mismatch, hopping of Cu-ions and contraction/expansion of the Se-sublattice are more energetically favorable and the phase transformation is easier to occur. Indeed, the atomic structure of the α - Cu_2Se $[10\bar{1}]$ crystal looks very similar to that of β - Cu_2Se $[110]$, as shown in Figure 2. Although the high-angle annular dark field scanning transmission electron microscopy (HAADF STEM) image collected from the α - Cu_2Se $[10\bar{1}]$ crystal (Figure 2a) is very alike to that of the β - Cu_2Se $[10\bar{1}]$ crystal (Figure 2b), the two phases can be distinguished by their fast Fourier transform (FFT) patterns. While the superlattice spots can be found in the FFT pattern of the α -phase (insert in Figure 2a), they are not present in the β phase. There is a closed crystalline orientation relationship between the two phases during the phase transformation: for example, α - $[10\bar{1}] \parallel \beta$ - $[110]$, α - $(202) \parallel \beta$ - (002) , and α - $(060) \parallel \beta$ - $(2\bar{2}0)$, as illustrated in Figure 2c. The subtle difference in the Cu-ions clusters between the two phases can also be seen by carefully examining the STEM images (Figure 2d,e), where

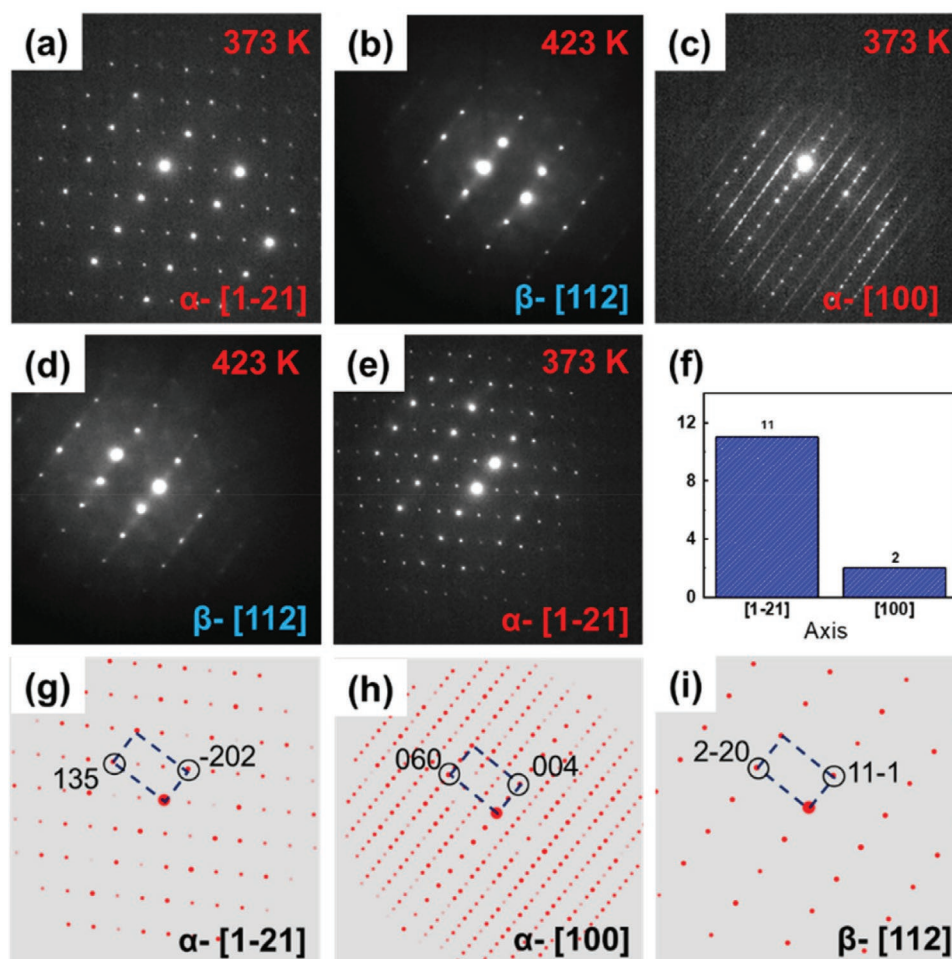


Figure 3. Phase changes during heating and cooling of Cu₂Se. a–e) Selected area electron diffraction of the sample at 373, 423, 373, 423, and 373 K during the heating and cooling process, respectively. f) Distribution histogram of the sample's low temperature phase after cooling. g–i) Simulated electron diffraction patterns of the α -phase of Cu₂Se along [1-21], [100] and of the β -phase of Cu₂Se along [112] directions, respectively.

a symmetric distribution of Cu-ions around Se was found in β -Cu₂Se. This could be the reason why the α -Cu₂Se [10-1]-oriented crystal showed a slightly lower thermal stability than the α -Cu₂Se [0-10] crystal. From the morphological changes along with the temperature rise (Figure S5, Supporting Information), it could be surmised that the defect density has gradually decreased at higher and higher temperatures. When both α -Cu₂Se crystals transformed into β -Cu₂Se at 393 K, the major defects present were dislocations located at the boundary of the two α -Cu₂Se crystals (Figure S6, Supporting Information).

The phase transformation between β -Cu₂Se and various α -Cu₂Se domains is in general reversible. While there is only one high temperature cubic β -Cu₂Se structure, there are many α -Cu₂Se domains forming at low-temperatures. We then explored whether the phase transformation was reversible and found that, in general, the original α -Cu₂Se domain structure was recovered upon lowering the temperature. However, there were also exceptions. As shown in Figure 3 and Videos S2–S5, Supporting Information, the phase transformation between the α -Cu₂Se [1-21] domain (the original domain) and the β -Cu₂Se crystal along the [112] direction was observed repeatedly by TEM via in situ heating. Every time the temperature was higher

than the phase transformation temperature, the [112] β -Cu₂Se crystal forms. When the temperature was kept below the phase transformation temperature (e.g., at 373 K), the α -Cu₂Se [1-21] domain was observed 11 times out of 13 cycles. In the other 2 cycles, the α -Cu₂Se [100] domain formed (as shown in Figure 3c). During the phase transformation, one set of the parallel lattice planes among the three domains is β -Cu₂Se (11-1) // α -Cu₂Se_{[-1-21]}}(-202) // α -Cu₂Se_{[100]}}(004). The d -spacing of the lattice planes are $d_{\beta\text{-Cu}_2\text{Se}(11-1)} = 3.389 \text{ \AA}$, $d_{\alpha\text{-Cu}_2\text{Se}(-202)} = 3.375 \text{ \AA}$ (with 0.4% mismatch to that of β phase) and $d_{\alpha\text{-Cu}_2\text{Se}(004)} = 3.406 \text{ \AA}$ (with 0.5% mismatch to that of β phase), respectively. In another crystal orientation the d -spacing of the lattice planes are $d_{\beta\text{-Cu}_2\text{Se}(2-20)} = 2.076 \text{ \AA}$, $d_{\alpha\text{-Cu}_2\text{Se}(060)} = 2.058 \text{ \AA}$ (with 0.9% mismatch to that of β phase) and $d_{\alpha\text{-Cu}_2\text{Se}(135)} = 2.076 \text{ \AA}$ (no mismatch), respectively. Here, the phase transformation proceeds preferentially through a route with the least mismatch (and thus minimal mismatch strain).

An instant buildup and release of the elastic strain at the moment the phase transformation has been observed by in situ high resolution STEM. The buildup of the elastic strain is mainly due to large volumetric changes (between α and β phases), while the release of the strain is through

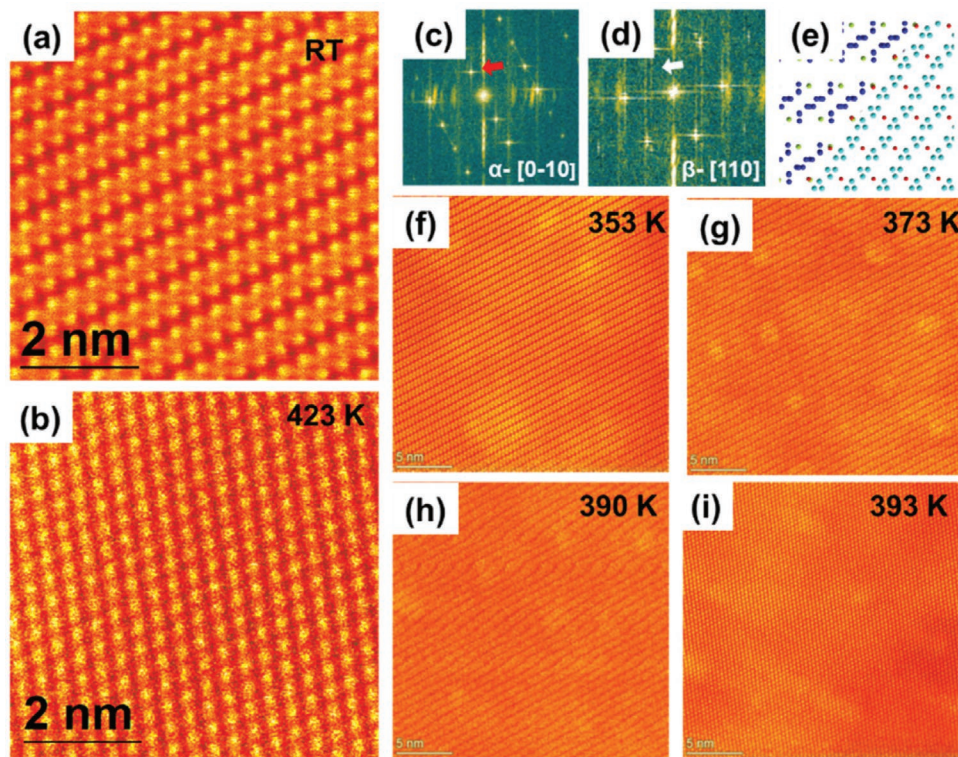


Figure 4. Changes in STEM images upon heating of Cu_2Se . a,b) STEM images of Cu_2Se at RT and 423 K, respectively. c,d) FFT image of (a) and (b), respectively. e) Schematic diagram of the α -phase of Cu_2Se along [0-10] and the β -phase of Cu_2Se along [110] directions. f,g) STEM images of Cu_2Se at 353, 373, 390, and 393 K, respectively.

lattice vibrations. One example is the vibration with the frequency of ≈ 10 Hz. As shown in **Figure 4** and Video S6, Supporting Information, the STEM images of both the α -phase at room temperature (Figure 4a) and β -phase at 423 K (Figure 4b) clearly show that the sample under observation is quite stable with no vibrational motion. However, the STEM image (Figure 4h) recorded at 390 K (when the phase transformation was taking place) depicts the obvious nearly-periodic interference fringes. Such fringes are generated by specimen vibrations (since the other possible interfering factors, such as magnetic/electric field etc., can be excluded). The frequency of vibrations was calculated by analyzing the FFT of the image as 10 Hz, meaning there are about 10 vibrations in a second observed in the experiment.

The variation of several key thermoelectric parameters of the prepared Cu_2Se samples with the rising temperature was measured across the α - Cu_2Se to β - Cu_2Se phase transformation, as shown in Figure S7, Supporting Information. The major abnormal changes during the phase transformation are: 1) the resistivity has suddenly increased; 2) the thermal conductivity dramatically decreased; and 3) the carrier concentration and the mobility precipitously decreased.^[8]

According to our investigations, the microstructural origin of the abnormal thermoelectric behavior can be better understood in terms of a sudden developed strain during the α to β - Cu_2Se phase transformation. The electrical conductivity is mainly influenced by the Se-sublattice, which is the backbone for the charge carrier transport. Elastic deformations of the

Se-sublattice during the phase transformation make it difficult for the charge carriers to go through smoothly and the electrical resistivity thus tends to increase. The dominant charge carrier in α - Cu_2Se is the electron-hole pairs formed in the crystal, which are influenced by the elastic strain (as the strain is correlated with the distribution of Cu-ion vacancies). Thus, along with the order-to-disorder transition in the Cu-ions occupancy during the phase transformation, the electronic structure has also changed suddenly.^[11] As such, the phase transformation causes sudden changes in most of the thermoelectric parameters:

- 1) The appearance of localized strain fields reduces the carrier mobility and thus increases the resistivity, which could be one of the origins of the critical scattering of electrons.^[4c,8b]
- 2) The strain induced by the phase transformation (lattice contraction or expansion happens when α - Cu_2Se is transformed into β - Cu_2Se), modifies not only the electronic structure, but also the carrier concentration, which is consistent with previous observations.^[4c,11]
- 3) The collective and sudden migration of Cu-ions (from the ordered sites to the disordered sites), enhances scattering of phonons, leading to a large decrease in the thermal conductivity.

From the experimental results (where different α -domains have different transformation temperatures), it is obvious that elastic strains play an important role in modulating the thermodynamic properties during the Cu_2Se phase transformation.

Consequently, there are large and rapid changes in the elastic strain within the Se-sublattice during the phase transformation. While the elastic strain will not destroy the integrity of the Se-lattice, it greatly reduces the electrical conductivity as the strain has a huge impact on the electronic structure. However, the effects will quickly disappear as soon as the strain is released. Thus, the abnormal thermoelectric behavior appears usually only within a very short time period. Proper design of materials with appropriate attentions to a stable strain distribution (strain engineering) might be an effective way in the development of novel high-performing thermoelectrics.

3. Conclusion

By applying in situ TEM, a dynamic evolution of the crystalline structure as well as the strain fields accompanying the elastic deformation of the Se-sublattice during the α -Cu₂Se to β -Cu₂Se phase transformation have been carefully studied. α -Cu₂Se domains with different orientations show different critical transformation temperatures, which implies that strain plays an important role in the transformation process. The smaller the mismatch between the α -Cu₂Se domain and the β -Cu₂Se domain, the lower the transformation temperature. The generation and release of a large elastic strain at an instant the phase transformation takes place has been observed and found as one of the main origins of the abnormal thermoelectric behavior of Cu₂Se.

4. Experimental Section

Polycrystalline Cu₂Se samples were prepared by the method of SHS.^[5a] High purity powders of Cu (99.95%) and Se (99.99%) were weighed out according to the stoichiometric ratio of 2:1 and mixed homogeneously in an agate mortar. A pellet with a diameter of 10 mm was prepared from the mixed powders by uniaxial cold pressing under 10 MPa for 5 min. The pellets were ignited in vacuum to obtain polycrystalline ingots containing solely the Cu₂Se α -phase. The ingots were then ground into powder using again the agate mortar to attain a homogeneous powder of Cu₂Se. The obtained powder was sintered by plasma activated sintering (PAS) (PAS-III-Ed, Elenix, Japan) using a carbon mold under 40 MPa in vacuum at 973 K for 3 min.

The as-prepared ingot was sectioned by focused ion beam (FIB) milling (Helios Nanolab G3 UC, FEI) for the structural characterization. Ex situ and in situ TEM characterizations of the samples were carried out by TEM (Talos F200s, FEI) and double C_s-corrected TEM (Titan Themis G2 60–300, FEI). In situ experiments using a nano-chip electrical and thermal holder (Dens solutions) were performed. For all of the in situ heating TEM experiments, the heating rate is 1 °C s⁻¹ and the samples been heated are hold for 1 min before the TEM images and diffraction patterns are collected (to ensure a stable temperature has reached).

The high temperature resistance and the Hall coefficient (R_H) from RT to 475 K were measured using the van der Pauw technique under a reversible magnetic field of 1.5 T. The effective carrier concentration (n_H) was calculated from $n_H = 1/eR_H$, where e is the electron charge. The Hall mobility followed from $\mu_H = \sigma R_H$.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Data Availability Statement

The data that support the findings of this study are available from the corresponding authors upon reasonable request.

Keywords

Cu₂Se ionic conductors, elastic lattice strain, in situ TEM, phase transformations, thermoelectric materials

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