

Modeling Viewer and Influencer Behavior on Streaming Platforms

by

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A dissertation submitted in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy
(Business Administration)
in The University of Michigan
2021

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DEDICATION

This dissertation is dedicated to my wife, Ankita Deepkumar,
for her continuous support, encouragement and love.

ACKNOWLEDGMENTS

I am very grateful to the wonderful people at the University of Michigan who I have had the fortune of meeting during the PhD Program which has truly been a transformative experience. I am grateful to the selection committee responsible for making me an offer to join the program and giving me the opportunity to learn and grow in a wonderful academic environment. I would like to extend my sincere gratitude to Puneet Manchanda, for taking me on as his PhD student, and mentoring me over the course of six years. His mentorship approach of “tough love” has served me well, pushed me to achieve more and helped me experience joy in research. He has always encouraged constructive debates and has always been willing to explore new ideas. Meetings spent discussing and debating about research aspects with him for three hours straight have been some of the highlights of my PhD experience! They have taught me how to think logically and analytically, and have shaped me as a researcher. His genuine care and concern about my well-being in the program have always been an added source of comfort. Puneet’s mentorship approach has been complemented well by that of Eric Schwartz, to whom I am also very grateful. His hands-on and patient approach to mentorship, and his help in breaking down complex ideas into simple parts helped me learn so much. Moreover, his frequent words of encouragement have always instilled confidence in me. One of the main reasons I joined the program was for the opportunity to work with Eric on the topic of binge-watching, and I am grateful to him for helping make that dream come true.

I am very grateful to David Jurgens for offering valuable insights and suggestions on my research and for his support during the job market. I would also like to thank Jun Li for being generous with her time and for her helpful feedback on my research. I am very grateful to S. Sriram for being a reassuring voice in the Marketing PhD committee, for always providing constructive feedback on my progress, for providing valuable feedback on my research, and for his support during the job market. I am also grateful to Anocha Aribarg, Rajeev Batra, Fred Feinberg, Aradhna Krishna, Yesim Orhun, Scott Rick, David Wooten, Katherine Burson, Carolyn Yoon, Justin Huang, and Jessica Fong for offering valuable feedback on my research at various stages of the program. I would also like to thank Fred Feinberg for teaching a fantastic PhD course by leading all paper discussions, and I would also like to thank Carolyn Yoon and Scott Rick for being very kind and supportive PhD Coordinators. My time in the program has been enriched by several interactions I have had with faculty from departments outside Marketing, and I would

like to thank them all. I would like to especially thank Brisa Sanchez for being a fantastic teacher and engaging in several discussions after class.

I am very grateful to the wonderful students I met from 2015 to 2021 across various schools and departments including the Marketing PhD program at Ross. I would like to especially thank Mike Palazollo and Linda Hagen for making me feel very welcomed when I joined the program, Kanzheng Zhu and Huanyu Zheng for their generous help and support with coursework, Longxiu Tian for his very kind and generous mentorship, Dan Zhao and Aseem Sinha for their kindness and support, Xu Zhang for always helping me with my questions, Tong Guo for providing valuable feedback on my research, Rebecca Chae for her generous help with teaching, and Gwen Ahn for engaging in helpful conversations about research. In addition, I would also like to thank Tim Doering, Dana Turjeman, Tiffany Vu, Steve Shaw, Yiqi Li, Yu Song, Hayoung Cheon, Adithya Pattabhiramaiah, Harsh Ketkar, Jihoon Cho, Giacomo Meille, Mengzhenyu Zhang, Jiawei Li, Jangwon Choi, Varad Deolankar, Frank Li and Zoey Jiang for providing helpful advice and feedback at various stages during the program. I would also like to sincerely thank the administrative team at Ross – Brian Jones, Kelsey Belzak, Ashley Stauffer, Clea Davis and Lindsay Apperson – for being very supportive and helpful.

Finally, I would like to express my gratitude to the amazing people who inspired me and supported me in my decision to pursue a PhD – Bori Csillag for her engaging conversations that provided the spark that research could be the way forward, Markus Giesler for his generous and kind mentorship, for helping me realize my potential and for showing me the path ahead, and Russ Belk for being a role model for how warm, generous, and efficient a researcher can be. While the PhD journey has generally been filled with moments of joy and happiness, there have also been moments of challenge and doubt, wherein I have realized that having self-belief and keeping a positive attitude always helps. I am also very grateful to my friends Rishabh Srivastava and Neil Sheth for their consistent support, my parents, N. Rajaram and Shyama Rajaram, for always standing with me, to my wife, Ankita Deepkumar, for her continuous support, encouragement and love, and to my unborn child for being patient! To anyone I may have inadvertently missed thanking, please accept my apologies, and know that you have my gratitude for your support.

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ABSTRACT

The video streaming industry is growing rapidly, and consumers are increasingly using ad-supported streaming services (Graham, 2020). There are important questions related to the effect of ad schedules and video elements on viewer behavior that have not been adequately studied in the marketing literature. In my dissertation, I study these topics by applying causal and/or interpretable machine learning methods on behavioral data.

In the first essay, “Finding the Sweet Spot: Ad Scheduling on Streaming Media”, I design an “optimal” ad schedule that balances the interest of the viewer (watching content) with that of the streaming platform (ad exposure). This is accomplished using a three-stage approach applied on a dataset of Hulu customers. In the first stage, I develop two metrics – Bingeability and Ad Tolerance – to capture the interplay between content consumption and ad exposure in a viewing session. Bingeability represents the number of completely viewed unique episodes of a show, while Ad Tolerance represents the willingness of a viewer to watch ads and subsequent content. In the second stage, I predict the value of the metrics for the next viewing session using the tree-based machine learning method – Extreme Gradient Boosting – while controlling for the non-randomness in ad delivery to a focal viewer using “instrumental variables” based on ad delivery patterns to other viewers. Using “feature importance analyses” and “partial dependence plots” I shed light on the importance and nature of the non-linear relationship with various feature sets, going beyond a purely black-box approach. Finally, in the third stage, I implement a novel constrained optimization procedure built around the causal predictions to provide an “optimal” ad-schedule for a viewer, while ensuring the level of ad exposure does not exceed her predicted Ad Tolerance. Under the optimized schedule, I find that “win-win” schedules are possible that allow for both an increase in content consumption and ad exposure.

In the second essay, “Video Influencers: Unboxing the Mystique”, I study the relationship between advertising content in YouTube influencer videos (across text, audio and images) and marketing outcomes (views, interaction rates and sentiment). This is accomplished with the help of novel interpretable deep-learning architectures that avoid making a trade-off between predictive ability and interpretability. Specifically, I achieve high predictive performance by avoiding ex-ante feature engineering and achieve better interpretability by eliminating spurious relationships confounded by factors unassociated with “attention” paid to video elements. The attention mechanism in the Text and

Audio models along with gradient maps in the Image model allow identification of video elements on which attention is paid while forming an association with an outcome. Such an ex-post analysis allows me to find statistically significant relationships between video elements and marketing outcomes that are supplemented by a significant increase in attention to video elements. By eliminating spurious relationships, I generate hypotheses that are more likely to have causal effects when tested in a field setting. For example, I find that mentioning a brand in the first 30 seconds of a video is on average associated with a significant increase in attention to the brand but a significant decrease in sentiment expressed towards the video.

Overall, my dissertation provides solutions and identifies strategies that can improve the welfare of viewers, platform owners, influencers and brand partners. Policy makers also stand to gain from understanding the power exerted by different stakeholders over viewer behavior.

CHAPTER I - Introduction

The video streaming industry is growing rapidly, and consumers are increasingly using ad-supported streaming services (Graham, 2020). The on-demand aspect of streaming media allows viewers to have increased control over the consumption experience which is different from traditional consumption experiences on linear TV. There are important questions related to the effect of ad schedules and video elements on viewer behavior on streaming media that have not been adequately studied in the marketing literature. In my dissertation, I study these topics by applying causal and/or interpretable machine learning methods on behavioral data. Specifically, in my first essay, “Finding the Sweet Spot: Ad Scheduling on Streaming Media”, I design an “optimal” ad schedule that balances the interest of the viewer (watching content) with that of the streaming platform (ad exposure). This is accomplished with the help of causal and interpretable tree-based learning methods applied on a dataset of Hulu customers. In my second essay, “Video Influencers: Unboxing the Mystique”, I study the relationship between advertising content in YouTube influencer videos (across text, audio and images) and marketing outcomes. This is accomplished with the help of novel interpretable deep-learning architectures that avoid making a trade-off between predictive ability and interpretability. My approach not only predicts well out-of-sample but also allows for interpretation of the attention paid on video elements. Next, I summarize my two essays.

Ad-scheduling on Streaming Media. Viewers consume content on streaming platforms in a self-directed manner since these platforms, in contrast to live TV, are primarily on-demand services. On the platform side, the tracking of individual-level viewer “eyeballs” on streaming services represents an attractive opportunity for advertisers, especially as these services allow for ad personalization due to the availability of rich data. However, interruptions to the viewing experience via advertising can detract from the viewers’ feeling of being in control, potentially leading to decreased content consumption. The challenge therefore is to balance the interests of the viewer and that of the platform while delivering advertising in these settings. I use four months of actual viewership data from the streaming platform Hulu to propose ad-schedules that maximize advertising exposure without compromising the content consumption experience for individual viewers. This is accomplished using a three-stage approach.

In the first stage, I develop two metrics – Bingeability and Ad Tolerance – to capture the interplay between content consumption and ad exposure in a viewing session. Bingeability represents the number

of completely viewed unique episodes of a show, while Ad Tolerance represents the willingness of a viewer to watch ads and subsequent content. Then, I predict the value of the metrics for the next viewing session using the tree-based machine learning method – Extreme Gradient Boosting – while controlling for the non-randomness in ad delivery to a focal viewer using “instrumental variables” based on ad delivery patterns to other viewers. Using “feature importance analyses” and “partial dependence plots” I am able to shed light on the importance and nature of the non-linear relationship with various feature sets, going beyond a purely black-box approach. Finally, I implement a novel constrained optimization procedure built around the causal predictions to provide an “optimal” ad-schedule for a viewer, while ensuring the level of ad exposure does not exceed her predicted Ad Tolerance. Under the optimized schedule, I find that “win-win” schedules are possible that allow for both an increase in content consumption and ad exposure.

Substantively, the contribution lies in using a combination of metrics, relevant data, and optimization, to develop an advertising schedule that benefits both the viewer and the platform. Methodologically, I demonstrate a novel implementation of tree-based machine learning in conjunction with instrumental variables to make causal predictions. In addition, I also present an interpretable machine learning approach that makes complex relationships between consumer behavior and managerial actions more transparent and easier to understand.

Influencer Advertising Videos. The increasing popularity of social media influencers has resulted in an exponential growth of the influencer marketing industry which allows brands to partner with influencers to promote their products. The videos made by influencers differ from conventional advertising videos in at least three ways. First, they can contain information that is unrelated to the sponsoring brand(s). Second, they are longer in duration on average, especially on platforms such as YouTube and Instagram. Finally, the platform often inserts conventional advertising videos into the influencer video. While there has been ample research to study the characteristics of conventional advertising videos and their impact on marketing outcomes, there has been little research on the design and effectiveness of influencer videos. Using publicly available data on YouTube, I study the relationship between advertising content in influencer videos (across text, audio, and images) and video views, interaction rates and sentiment. This is accomplished with the help of novel interpretable deep-learning architectures that not only offer high predictive performance by avoiding ex-ante feature engineering, but also allow interpretation of the attention paid on unstructured influencer video elements. By supplementing the deep-learning analysis with the benefits of transfer learning, I achieve high performance at a low computational cost.

The deep learning architectures used for analyzing each component of unstructured data in videos are state-of-the-art transfer learning methods customized for this setting. They comprise Bidirectional

Encoder Representation from Transformers (BERT) for textual data (title, description, and captions), YAMNet (MobileNet) with Bidirectional Long Short-Term Memory Cells (LSTMs) appended with an attention mechanism for audio data, and EfficientNet-B7 with Bidirectional LSTMs for image data. The attention mechanism in the Text and Audio models along with gradient maps in the Image model allow interpretation of the elements of videos on which attention is paid while forming an association with an outcome. Such an ex-post analysis allows me to find statistically significant relationships between advertising content and marketing outcomes that are supplemented by a significant increase in attention to advertising content. I filter out relationships that are affected by confounding factors unassociated with an increase in attention, thus generating hypotheses that are more likely to have causal effects when tested in a field setting. For example, interpreting the results from the Text model reveals that brand mentions in the first 30 seconds of a video are associated with a significant increase in attention to the brand but a significant decrease in sentiment expressed towards the video. In addition, I uncover significant relationships between sounds (e.g., speech, music, animal sounds, etc.) in audio as well as objects (e.g., persons, clothes, brand logos, etc.) in images with marketing outcomes that are also supplemented by an increase in attention.

This essay uncovers novel relationships between unstructured video elements and marketing outcomes. Influencers and brands can test these relationships for causal effects via field experiments and build better integrated content that engenders higher viewer satisfaction with the consumption experience. Methodologically, I introduce novel interpretable deep learning approaches to the marketing literature that allow interpretation of the captured relationships without trading off predictive ability.

Overall, my dissertation provides solutions and identifies strategies that can improve the welfare of viewers, platform owners, influencers and brand partners. Policy makers also stand to gain from understanding the power exerted by different stakeholders over viewer behavior. The areas I study in my dissertation (streaming media and influencer marketing) are growing, and the methods I use are state-of-the-art and novel in their application to studying agent behavior in these areas.

CHAPTER II - Finding the Sweet Spot: Ad Scheduling on Streaming Media

2.1 Introduction

Streaming video content is becoming increasingly popular. 55% of US households subscribed to at least one video streaming service in 2018, up from 10% in 2009 (Deloitte, 2018). In contrast to linear TV, on-demand streaming services give viewers agency, allowing them to consume content in a self-directed manner. As a result, viewers consume media content in a “non-linear” manner by not adhering to any set temporal schedules. For example, a common behavior viewers exhibit in such settings is that of rapid consumption of multiple episodes of a TV show, usually referred to as “binge-watching” (Cakebread, 2017; Oxford Dictionary 2018). The presence of consumer “eyeballs” on streaming media represents an attractive opportunity for advertisers, especially as these services allow for ad personalization due to the availability of rich data. As a result, advertising spending on streaming media services is expected to grow to \$20 billion in 2020 from \$4.7 billion in 2017 (eMarketer, 2018).¹ However, streaming media represents new challenges, especially as interruptions to the viewing experience via advertising detract from the viewers’ feeling of being in control and can lead to decreased content consumption (Schweidel & Moe, 2016). In addition, platforms that provide these services need to balance the viewers’ control of the consumption experience while delivering advertising commensurate with advertiser objectives. Advertiser objectives entail delivering a fixed number of ad exposures over a set of TV shows or movies within a given time frame (Johnson, 2019).² In general, there is little work that focuses on the interplay of (consumer directed) content consumption and ad exposures. While extant research in marketing has developed recommendations for ad scheduling, e.g., Dubé et al. (2005), the viewer does not have significant control in the settings considered. In addition, the focus of past ad scheduling work has been on several ad-related outcomes but not on studying *content consumption*.³ There is limited research that

¹ Streaming media providers monetize their services through three distinct mechanisms (including offering combinations of these): subscriptions, advertising and product sales (e.g., sale of a movie). It is hard to assess which is the dominant mechanism. However, the number of ad-supported platforms (with or without a free service) is growing rapidly with providers such as Hulu, CBS, Dailymotion, Ora TV, YouTube, Sony (Crackle), The Roku Channel, TubiTV, Popcornflix, Amazon (IMDb TV) and NBC (Armental, 2019; Patel, 2018; Sherman, 2019). There is also industry research suggesting that consumers prefer a platform’s lower cost ad-supported streaming service to its premium no-ad version, when both options are offered (Liyakasa, 2018; Sommerlad, 2018). In this essay, I focus on free streaming services with an ad supported mechanism.

² My focus is on the platform’s ad scheduling problem. I do not know how the advertiser arrives at exposure targets (quantity, ad location within show, customer segment etc.) specified to the platform. I also do not have access to all the downstream data e.g., browsing, purchasing etc.

³ Recent work on ad scheduling has focused on maximizing ad-related outcomes such as profits from sales (Dubé et al., 2005), campaign reach (Danaher et al., 2010), purchase (Sahni, 2015), site visits (Chae et al., 2019) or ad viewing completion rates (Krishnan & Sitaraman, 2013).

has focused on content consumption patterns in settings where viewers have control, e.g., Schweidel and Moe (2016), which does not address the ad scheduling issue.

In this essay, I propose a comprehensive approach that best combines the interests of the viewer and that of the free ad-supported platform. Specifically, I use actual viewership data from a streaming media platform to propose ad schedules that maximize advertising exposure without compromising the content consumption experience for individual viewers. In order to do this, I need to surmount a few challenges. First, the control that viewers have can manifest itself in multiple and diverse behaviors, both in relationship to content consumption and the reaction to advertising. However, there is little standardization on how consumer behavior on streaming media can be captured and described. Second, there is plethora of content on streaming media platforms, varying in terms of genre, show type and show duration (episode length, number of episodes per season and number of seasons). It becomes very important therefore to capture the impact of these variables and their interactions in a tractable manner. Third, in real settings, platforms do not deliver advertising randomly. Thus, any approach that is proposed needs to address the non-random delivery of such advertising. Finally, in order for ad scheduling recommendations to have practical value, simplicity and speed are very important.

I address these challenges using a three-stage approach (Figure 2.1). Given the lack of standardization around the measurement of content consumption and ad exposure in streaming media settings, I begin by using theory from consumer psychology to develop summary measures or metrics that capture viewer's control over the consumption experience in streaming media settings. These metrics are deterministic transforms of the data primitives (minutes watched, ads see, etc.) that are available to streaming media platforms. The two aspects of viewer behavior that I am interested in are non-linear content consumption and the response to advertising exposure. In order to do this, I first need to specify a temporal unit of consumption for a given viewer. I denote this unit as a viewer-session (in future, I use the term "session" to denote this unit) which is defined as a period of time spent by a viewer watching one TV show separated by 60 minutes or more of inactivity as in Schweidel and Moe (2016).

The first metric, which I label "Bingeability," is based on the theory of "flow" (Ghani & Deshpande, 1994; Schweidel & Moe, 2016) as well as industry norms and captures the extent of viewer immersion in the content. In essence, this metric is based on a stylized count of complete and unique episodes of a TV show watched in a session. The second metric, which I label "Ad Tolerance," is based on the theory of hedonic adaptation (Frederick & Loewenstein, 1999; Nelson et al., 2009) and captures the viewer's reaction to advertising. Specifically, the metric captures the willingness of a viewer to watch ads and to watch content after being exposed to ads in a session. I explain the theoretical motivation, construction and validation for both metrics in more detail in the section "Stage I".

In the second stage, I construct a model to predict the value of the above metrics for a session using an extensive set of current and historic descriptors, both specific to the content and to the viewer. I use the process of “feature generation” to generate the entire set of descriptors (cf. Yoganasimhan (2019)). In order to deal with the large number of descriptors (in the thousands), I use a tree-based machine learning method (Extreme Gradient Boosting or XGBoost) that is known to capture non-linear relationships well (Chen & Guestrin, 2016; Rafieian & Yoganasimhan, 2019). As noted above, the viewer behavior captured in my data is a function of the delivered advertising schedule. I therefore control for the non-randomness in ad delivery to a focal viewer using “instrumental variables” based on ad delivery patterns to other viewers. After predicting these metrics for each session in holdout samples, I use feature importance analyses and partial dependence plots to shed light on the importance and nature of the non-linear relationship with various feature sets (J. Friedman, 2002) – this allows me to go beyond a purely black-box approach.

In the third stage, I develop my ad scheduling recommendation. I begin by passing the predictions obtained from the previous stage through an “Ad Decision Tree” that helps identify sessions where ad exposure enhances, or at least does not detract from, content consumption. For these sessions, I apply a novel constrained optimization procedure built around my predictions to provide an “optimal” advertising schedule for the platform that maximizes ad exposure, subject to (predicted) Ad Tolerance.

I calibrate my approach on a novel data set that captures the viewing behavior of individuals on Hulu (when it had only a free ad-supported streaming service). I find that my proposed metrics, Bingeability and Ad Tolerance, perform well in terms of capturing viewer behavior with respect to content consumption and ad exposure. I also find strong evidence of state-dependence for these two metrics. In other words, TV shows that have a high Bingeability for a viewer in the past (week) result in a high Bingeability for the current session. Similarly, past Ad Tolerance is predictive of current Ad Tolerance. I also find that variations in ad spacing and ad exposure have a non-linear effect on content consumption. Based on these findings, my optimization module provides individual session level recommendations vis-à-vis pod (a block of ads) frequency and spacing. For example, I suggest that, on average, Hulu should decrease pod frequency (increase pod spacing) when a viewer is expected to have lower Ad Tolerance or higher Bingeability, holding the other constant. The optimization module can in general be used as a decision support system by the platform. Specifically, the platform can define critical thresholds of predicted Bingeability to decide to show ads and obtain the recommended ad delivery schedules to explore the inherent tradeoffs between content consumption and ad exposure for its viewers. I find that under the optimized ad schedule, the decision to show ads in *all* future sessions for existing viewers, i.e., when *predicted Bingeability is greater than 0*, benefits the platform *and* the viewer the most with content consumption increasing by 5% and ad exposure increasing by 71% (on average).

In sum, my essay makes four main contributions. First, it is one of the early works that examines viewer behavior spanning content consumption *and* ad exposure in streaming media environments. Second, using a combination of metrics, data and optimization, the essay makes explicit the tradeoffs between ad delivery and content consumption, thus balancing the interests of both parties. Third, it illustrates how the use of instrumental variables and partial dependence analyses help to address concerns around the purely predictive and black-box nature of machine learning methods. Finally, it provides a scalable and interpretable approach to ad scheduling at the individual session level.

2.2 Data

My data come from the streaming platform Hulu, spanning the period Feb 28, 2009 to June 29, 2009. At this time, the platform only offered a free ad-supported streaming service.⁴ I have data on the viewing behavior of a random sample of over 10,000 accounts for this period. Each account could potentially be shared by household members or friends, but as all accounts were free, I do not expect account sharing to be prevalent. Hence, I assume that each account represents a unique viewer. In addition, during this period, viewers could only access Hulu via a browser as the mobile and tablet app was not launched until 2011 (Ogasawara, 2011). Thus, I am able to capture all Hulu viewing behavior for an account.

I restrict my data to TV show viewing behavior and not movie watching behavior for two reasons. First, TV show viewing behavior has more potential to build engagement with the platform because content length of a TV show (for all episodes) is typically longer than that of a movie. Second, given multiple episodes, TV shows lend themselves more to non-linear consumption (Deloitte, 2018). TV shows make up 55.5% of total titles⁵ in the dataset, with the remaining being movies. Among the viewers who watch TV shows, I further select only those viewers who visit the platform at least twice to watch TV shows during my sample period to ensure that I can include viewer fixed effects in my model. Screening on this leaves me with a sample of 6,228 viewers who watch 568 TV shows spanning 18 genres.

⁴ Hulu offered an additional subscription plan with limited ads in 2010, and an additional premium plan with no ads in 2015 and phased out its free plan in 2016 (Ramachandran & Seetharaman 2016). However, as noted earlier, multiple streaming services such as YouTube, Dailymotion, Ora TV, The Roku Channel, TubiTV, Crackle, Popcornflix and IMDb TV continue to offer free ad-supported streaming plans.

⁵ A title is classified as a movie if there is only one video (episode) for that title *and* the duration of this video is greater than 60 minutes. For the few cases where a TV show and a movie share a name (this typically occurs when one is a spin-off of the other), I classify the movie as a TV show. Note that my results are invariant to the inclusion or exclusion of these movies.

2.2.1 Sessions

A ‘session’ (or sitting) is defined as time spent by a viewer watching show content or ads from exactly one TV show separated by 60 minutes or more of inactivity (Schweidel & Moe, 2016).⁶ A session can be split into the following parts:

$$\overbrace{\text{Session Time}}^{\text{Measured}} = \overbrace{\text{Content Time} + \text{Ad Time} + \text{Filler Content Time}}^{\text{Measured}} + \overbrace{\text{Pauses} - \text{Fast Forward} + \text{Rewind}}^{\text{Unmeasured}} \quad (2.1)$$

where *Session Time* represents the calendar time spent in the session, *Content Time* is time spent viewing show content (including minutes of content skipped in fast-forwards but excluding minutes of content seen again in rewinds), *Ad Time* is time of ad exposure, and *Filler Content Time* is time spent viewing filler content which are interjected between the main episodes. I classify all episodes less than 15 minutes e.g., short videos such as interviews, recaps, previews, trailers etc., as filler content. It is important to note that ads cannot be fast-forwarded, rewind or skipped unlike show content or filler content. All the previously mentioned variables are measured in my panel data. In addition, there are unmeasured variables that complete the above equation—*Pauses* is the time spent in a break, *Fast Forward* is the duration of content fast-forwarded, and *Rewind* is the duration of content rewind. A statistical summary of the sessions is shown in Table 2.1. The 2.5th to 97.5th percentile of the time spent in a session ranges from 1.82 minutes to 236.51 minutes (about 4 hours) with a median time spent of 42.70 minutes.

In Table 2.2, I show a representative example of typical viewing behavior in a session. More examples are detailed in Appendix A.1. In the first row of the example, ‘light gray shaded boxes’ denote *Ad Time*, ‘white shaded boxes’ denote *Content Time* and the ‘dark gray shaded box’ denotes *Filler Content Time*. In the second row of each example, the ‘white shaded dashed line boxes’ denote *Session Time*, and the ‘black shaded boxes’ indicate the beginning of the next episode. All values are in minutes. A block is a period of time from the beginning of a pod (or beginning of session) till the beginning of the next pod (or end of episode/session).

The example shows the behavior of a viewer watching two 24-minute episodes of ‘Aquarion’. The viewer’s viewing experience was interrupted by 5 ads (light gray shaded box) and 2 minutes of filler content (dark gray shaded box). The black shaded box denotes the beginning of the next episode. I can see evidence of fast-forwarding behavior in block 5 because the session time of 17.66 minutes is less than the

⁶ As noted earlier, I need to define a viewing session in order to summarize/predict viewer behavior and decide on ad delivery. Note that my approach is general as it can be applied to *any* time separation used in the definition of a session. If no time unit is defined, then a continuous time model of content consumption and ad delivery needs to be specified along with continuous time ad scheduling recommendations. I believe that such a model is likely to be intractable, if not infeasible.

sum of ad time (0.66 min) and content time (21 mins). There is evidence of pauses in block 6 because the session time of 1 min is greater than the ad time of 0.5 min. There is no evidence of rewinds in block 6 because no content was viewed and ads cannot be rewound. By substituting the values of the example in equation (2.1), I get,

$$\overbrace{44.82 \text{ minutes}}^{\text{Session Time}} = \overbrace{43 \text{ minutes}}^{\text{Content Time}} + \overbrace{2.83 \text{ minutes}}^{\text{Ad Time}} + \overbrace{2 \text{ minutes}}^{\text{Filler Content Time}} + \overbrace{\text{Unmeasured}}^{\text{Pauses - Fast Forward + Rewind}}$$

On solving the above equation, I find that the sum of the unmeasured variables is -3.01 minutes. This indicates that more time was spent in fast-forwards than in pauses or rewinds in this session.

2.2.2 Ad Delivery

It is important to understand what the platform was doing in terms of ad delivery at the time of my data. As I do not have access to institutional practices at Hulu, I examine the realized data patterns to infer the rules governing ad delivery (technical details on how Hulu collected the viewing data are described in Appendix A.2). I focus on four aspects of ad delivery – the duration of pod (block of ads) exposure, frequency of ad delivery (by examining mean spacing between pods), diversity of ad exposure (based on the industry of the advertiser) and degree of non-conformity to equal spacing (by examining “clumpiness” of pod exposure).

I first plot the distribution of the length of commercial pods, conditional on non-zero seconds of ad exposure, viewed across all sessions in Figure 2.2a. The median length of time viewed is 30 seconds with range of 6.6 to 55.2 seconds (2.5th to 97.5th percentile). Note that more than 99% of the pods have only one ad. A viewer may not watch a pod completely if she ends the session before the pod ends or refreshes the browser or skips the episode. Hence, the amount of pod duration viewed is less than or equal to the pod length. As the figure shows, the most common pod durations (lengths) are 15 seconds and 30 seconds. In other words, pod durations follow a non-uniform distribution which indicates that Hulu uses a set of rules to set duration – I label this as Hulu’s “Length Rule.” Next, I plot the density of the spacing (content time viewed including filler content) between pods in an episode across all sessions (Figure 2.2b). I find that this spacing is also not uniformly distributed. The peak at 0 minutes corresponds to pre-roll ads (ads at the beginning of an episode), and there is also a peak at 6.3 minutes. This bi-modal distribution indicates non-random spacing and I label it as Hulu’s “Spacing Rule.”

I then examine whether there is any systematic pattern in ad delivery across the type of advertiser and length of ad. Using the empirical distribution of ad lengths, I classify all ads into three types: 0-26

seconds, 26-52 seconds, and > 52 seconds. Each ad in my dataset belongs to one of 16 product categories such as CPG, Telecom, etc., resulting in 48 (= 3 X 16) unique combinations.⁷ Figure 2.2c shows the distribution of the percentage of diverse ads viewed in an episode across all sessions. It is not perfectly uniform, suggesting that certain advertisers have preferences over TV shows that they want to show ads on – I label this as Hulu’s “Diversity Rule.” Finally, I examine the degree to which pods are not equally spaced in an episode using the measure of clumpiness proposed by Y. Zhang et al. (2015) as below:

$$1 + \sum_{i=1}^n \frac{\left(\frac{x_i + 0.01}{N + 0.01}\right) \log\left(\frac{x_i + 0.01}{N + 0.01}\right)}{\log(n + 1)} \quad (2.2)$$

where n is number of pods in an episode, x_i is content time viewed till pod i , N is total content time viewed in the episode till the last pod. I add 0.01 to avoid errors because of $\log(0)$ and division by 0. Figure 2.2d shows the distribution of clumpiness of pods in an episode across all sessions. It is not perfectly uniform – I label this Hulu’s “Clumpiness Rule.”

The above suggests that Hulu’s ad delivery exhibited specific patterns i.e., ads were not delivered randomly. In subsequent analysis, I summarize this non-randomness using the four dimensions above via the Length Rule (LR), Spacing Rule (SR), Diversity Rule (DR) and Clumpiness Rule (CR). I then account for it using instrumental variables (see section “Stage II”).⁸

2.3 Stage I

My research comprises of three stages as illustrated in Figure 2.1. In the first stage, I construct parsimonious metrics to capture and summarize viewer’s control of the consumption experience, thus allowing me to systematically track viewer behavior over time.

2.3.1 Metric Development

(1) Bingeability. As noted earlier, the first metric I develop captures the extent of viewer immersion in the content, potentially leading to non-linear consumption. Immersion in the viewing experience can be likened to experiencing a “flow” state characterized by a combination of focused concentration, intrinsic enjoyment and time distortion (Ghani & Deshpande, 1994; Schweidel & Moe, 2016). Thus, the stronger the flow state that the viewer is in, the more episodes she is likely to consume within a session. My metric therefore takes the common industry metric of the raw number of episodes watched in a session (West, 2013) and adjusts it for all activities that indicate that the viewer has fallen out of the flow state e.g.,

⁷ Less than 0.15% of total ads are “ad selectors” where a viewer can choose an ad to view from a few options. Hence, I do not use an additional rule to differentiate between “ad selectors” and “non ad-selectors”.

⁸ While it is possible that there are other forms of non-randomness in ad delivery, my analysis suggested that these four aspects accounted for most of the variation in ad delivery. Any aspect of advertising that is systematic, including relating ad delivery to the story arc (e.g., delivering more ads before a cliffhanger ending), is captured in the large number of fixed effects (viewer, show, genre etc.) I use as features in Stage II.

skipping and/or fast-forwarding.⁹ In other words, this metric represents the count of episodes in which viewers are immersed in the viewing experience by using the count of “complete unique episodes” watched in a session. Specifically, “complete” refers to episodes that are watched in full i.e., no content is missed, while “unique” refers to the number of distinct episodes watched in the session.¹⁰

In effect, my metric represents the count of episodes (which are positive integer values) that characterize binge-watching behavior, and hence I name it “Bingeability.” It is important to note that I do not define binge-watching, but instead qualify the kind of episodes which should be counted in the industry definition of binge-watching. For example, Netflix conducted a poll and found that its viewers perceive watching 2 to 6 episodes of a TV show in one sitting as binge-watching (West, 2013). I argue that such a count should not be a raw episode count of 2 to 6 episodes but a count that includes only the number of complete and unique episodes watched. Thus, Bingeability is more conservative than a raw episode count, and the product of Bingeability and average episode length is more conservative than a measure of content minutes watched. In order to show that the proposed metric is not identical to a simple count of episodes, I discuss its information content and validity in the subsection on “Metric Validity.”

The Bingeability metric is defined as

$$Bingeability = \sum_{i=1}^{n_e} \mathbb{1} \left\{ \begin{array}{l} Content\ Length_i - 5\ mins \leq Content\ Time_i \leq \\ Session\ Time_i - Ad\ Time_i \end{array} \right\} \quad (2.3)$$

where, $\mathbb{1}$ is an indicator function, i denotes a unique episode, n_e is the number of unique episodes watched, $Content\ Time_i$ is the time spent watching content for episode i , $Content\ Length_i$ is the length of episode i including opening and end credits, 5 mins is an upper bound on the combined duration of opening and end credits in an episode, $Session\ Time_i$ is the calendar time spent and $Ad\ Time_i$ is the time of ad exposure. The presence of the indicator function ensures that the metric is integer valued. I explain the two conditions in the indicator function below.

i. No skipping:

$$Content\ Length_i - 5\ min \leq Content\ Time_i \quad (2.3a)$$

Skipping means moving ahead to the next episode or ending the session without completely watching the present episode. Skipping content (excluding credits) is indicative of a break in the

⁹ Recent academic work e.g., Ameri et al. (2019) and T. Lu et al. (2017) also study binge-watching of content without looking at the ad scheduling issue. Both studies customize their binge-watching definitions to their idiosyncratic settings – an anime website for the former and Coursera for the latter. In contrast, my objective is to develop a measure of non-linear consumption that can be used by the platform for its decision making, not to define binge-watching.

¹⁰ I ignore repeat viewing behavior (same episode, same Viewer ID, same session) as it is present in only 0.6% of observations.

immersive experience or the ‘flow’ state of a viewer. Hence, I exclude episodes displaying skipping behavior from the count of Bingeability.

The sum of opening and end credits for TV shows are typically less than 5 minutes which can be considered a lenient upper bound (ABC, 2014; Ingram, 2016). This is subtracted from $Content Length_i$ as viewers are less likely to watch credits when they are binge-watching the show (Miller, 2017; Nededog, 2017). After subtracting the maximum possible time involved in opening and end credits, 5 mins, from $Content Length_i$, if the difference remains less than or equal to $Content Time_i$, then I can conclude that the viewer has not skipped watching content.

ii. No excessive fast-forwarding:

$$Content Time_i \leq Session Time_i - Ad Time_i \quad (2.3b)$$

Fast-forwarding means moving ahead faster than normal pace to view future content from the same episode. There may be occasions when the viewer chooses to excessively fast-forward certain portions of an episode. This would result in a greater increase in $Content Time_i$ than a difference of $Session Time_i$ and $Ad Time_i$. Excessive fast-forwarding is indicative of a break in the ‘flow’ state of a viewer. Hence, I avoid counting episodes in which a viewer carries out excessive fast-forwards. Substituting equation (2.1) in equation (2.3b), I can rewrite equation (2.3b) as follows:

$$Fast Forward_i \leq Filler Content Time_i + Rewind_i + Pauses_i \quad (2.3c)$$

The above equation ensures that the amount of time spent in fast-forwards is less than the sum of the time spent watching filler content, in rewinding content and in pauses.¹¹

Next, I apply the Bingeability metric to the illustrative example discussed earlier in Table 2.2, and this computation is shown in Table 2.3. In this example, the value of content length for each episode is 24 minutes. Time spent watching content in Episode 1 is [**10 + 10 + 2 = 22**] minutes and in Episode 2 is **21** minutes. There is no evidence of skipping behavior in either Episode 1 or Episode 2 because the first condition is satisfied. The total time spent in the session for Episode 1 is [**10.66 + 11 + 2.5 = 24.16**] minutes and for Episode 2 is [**2 + 17.66 + 1 = 20.66**] minutes. The total ad time for Episode 1 is 1.66 min and for Episode 2 is 1.16 min. I find evidence of excessive fast-forwarding in Episode 2 because the

¹¹ I allow viewers to fast-forward filler content because viewers are less likely to be interested in viewing content that has been inserted into their viewing experience by the streaming platform. I also allow viewers to fast-forward content that has been rewound e.g., when a viewer wishes to rewind and go back to a certain section of the episode to get more clarity, and having re-watched that section, now fast-forwards ahead to the point from where the rewind had begun. Such an action need not imply a break in the flow state of a viewer, and hence I do not penalize such behavior. I am also forced to allow the minutes of content fast-forwarded to be less than the time spent in pauses. As the time spent in pauses is an unmeasured variable, I am unable to eliminate all occasions of fast-forwarding behavior. Theoretically, I end up allowing those occasions when a viewer takes frequent breaks but also keeps fast-forwarding content. Such behavioral patterns are unlikely but I cannot rule them out. Hence, I only eliminate occasions of “excessive” fast-forwarding as originally stated in the condition.

second condition is not satisfied. Thus, the value of Bingeability is 1 as my metric only counts Episode 1 which was viewed completely. The fast-forwarding behavior within Episode 2 (in block 5 – see earlier subsection “Sessions”) represents incomplete viewing and hence disqualifies the episode from being used in the Bingeability count.

(2) Ad Tolerance. Previous research has shown that interruptive stimuli e.g., ads, can influence the enjoyment level of a viewer while watching video content on certain occasions. If the viewer is watching content and adapting to that hedonic experience, then an ad interruption breaks the adaptation pattern preventing enjoyment levels from falling (Nelson et al., 2009). On the other hand, if the viewer is not adapting (to content), then (ad) interruptions can break the flow state by irritating the viewer (Frederick & Loewenstein, 1999). In the first case, the viewer can be expected to watch *more* content after the ad ends. In contrast, in the second case, the viewer can be expected to watch *less* content after the ads ends. Unfortunately, I cannot measure adaptation directly but I use these results as motivation to develop a metric – Ad Tolerance – that captures the willingness of a viewer to watch ads and to watch content after being exposed to ads in a session. Note that the tacit assumption I am making is that consumers are myopic in their viewing behavior i.e., they do not base their current viewing decision on future (expected) ad exposure.¹²

Based on the above, I develop the Ad Tolerance metric by looking at three components of the viewing experience: (i) duration of pod exposure, (ii) amount of content viewed after pod exposure till the end of session and (iii) calendar time elapsed since previous pod exposure. The first component just looks at the viewer’s propensity to watch ads – the longer she watches, the more ad tolerant she is. The second component focuses on the content watching behavior after pod exposure. The longer the viewer watches content after pod exposure, the higher her ad tolerance. Finally, the third component is a correction for the time available to adapt to the content and the absence of ad exposure (described in detail below). The Ad Tolerance metric is constructed as follows:

$$Ad\ Tolerance = \sum_{j=1}^{n_p} (w_1 PodDuration_j + w_2 ContentEnd_j - w_3 (CalendarPod_j - PodDuration_{j-1})) \quad (2.4)$$

where j is a pod in the session and n_p is number of pods watched in the session. $PodDuration_j$ is the duration of commercial pod j , $ContentEnd_j$ is content watched (including filler content) till the end of

¹² The only objective mechanism by which a viewer could obtain future ad exposure information is via hovering her cursor at the bottom of the video to bring up the progress bar (which fades out quickly) as this bar shows markers denoting pod locations. I checked online forums (reddit.com, slate.com, anandtech.com) and carried out online searches for keywords such as “ad location,” “ad position,” “future ads” and “ads coming up” for the 2008-09 period. I found a lot of discussion around viewer irritation with ad repetition and video buffering at Hulu, but none around the ability to see future ad locations. This, along with the fact that obtaining this information while viewing is costly, is supportive of my assumption regarding myopic behavior.

the session after watching commercial pod j , $CalendarPod_j$ is calendar time elapsed from the beginning of the previous pod in the same session till the beginning of pod j , $PodDuration_{j-1}$ is the duration of commercial pod $j-1$ and w_1, w_2, w_3 are the weights associated with the three components in the equation. Initially, I set the value of each of the weights to one (and in Appendix A.3, I show that the optimization outcomes are not sensitive to these weights). Note that though the unit of Ad Tolerance is minutes and its range is the real number line, it cannot be directly interpreted as a temporal measure. Its magnitude represents the willingness of the viewer in a session to watch ads and to watch content after being exposed to ads. A negative value of Ad Tolerance suggests that the viewer stopped watching content immediately after being exposed to a pod which was preceded (at some point) by a long period of no ad exposure. I now explain the importance of each component of the Ad Tolerance metric in equation (2.4).

i. *PodDuration_j*: Duration of a pod

When a viewer is exposed to a commercial pod, each passing second of the pod contributes to the viewer's willingness to be exposed to the pod. This is captured by *PodDuration_j*, the duration of the j^{th} pod that is watched in the session. While a viewer does not have the option to fast-forward, rewind or skip ads, a viewer can partially watch a pod by exiting the session in the middle of the pod, refreshing the browser or skipping to the next episode in sequence. Hence, *PodDuration_j* captures the willingness of the viewer to be exposed to the pod.

ii. *ContentEnd_j*: Content time watched till end of the session

ContentEnd_j measures the time spent watching content till the end of the session after being exposed to pod j . Longer durations suggest higher tolerance for the previous interruption (with Schweidel and Moe (2016) finding empirical evidence that content viewership decreases on average as ad exposure increases). To reduce potential bias in my estimates of *ContentEnd_j*, I operationalize the measure of *ContentEnd_j* as the minimum of (a) *Content Time* in a block and (b) the difference between *Session Time* and *Ad Time* in a block. As mentioned earlier, a block is a period of time from the beginning of a pod (or beginning of session) till the beginning of the next pod (or end of episode/session). If a viewer keeps excessively fast-forwarding content, *Content Time* would increase without a corresponding increase in *Session Time* (calendar time). As a result, using *Content Time* will positively bias the measure of *ContentEnd_j* as the viewer is not actually watching content but is only fast-forwarding content. In such situations, the metric adds option (b) which is smaller than option (a), thereby eliminating the above bias. This correction is termed as 'Caveat 1' in the rest of the essay.

iii. $CalendarPod_j - PodDuration_{j-1}$: Inter-pod calendar time

In my setting, when a viewer is not watching ads, she is either watching content, fast-forwarding/rewinding content or engaged in a break/pause. During this period, the viewer can be expected to simultaneously adapt to both the content and the absence of ad exposure. The third term captures this period because it is a measure of the calendar time elapsed since the previous pod exposure. This is the time during which the level of potentially unfavorable affective intensity resulting from ad exposure can go down.

$CalendarPod_j$ measures the calendar time from the beginning of the previous pod, $j-1$, in the same session till the beginning of pod j . For the first pod in the session, $CalendarPod_j$ measures the time from the beginning of the session as there is no previous pod watched in the session. $PodDuration_{j-1}$ is the duration of the $j-1$ pod that is watched in the session. The difference between $CalendarPod_j$ and $PodDuration_{j-1}$ is the measure of the ad-free time before the beginning of $PodDuration_j$. This measure of ad-free time is subtracted from $ContentEnd_j$ in equation (2.4) to get the net effect of the affective influence of an interruption on the viewer.

Next, I apply the Ad Tolerance metric to the illustrative example discussed earlier in Table 2.2, and this computation is shown in Table 2.4. More illustrative examples are shown in Appendix A.1. In this example, I begin by adding the duration of the first pod which is 0.66 minutes to the amount of content viewed in the remainder of the session (after the end of the pod), which is [10 + 10 + 2 + 2 + 17 + 0 = 41] minutes. It is important to note the use of ‘Caveat 1’ in block 5 (see Table 2.2) where there is evidence of fast-forwarding behavior. $ContentEnd_j$ is chosen as $Session Time - Ad Time$, [17.66 - 0.66 = 17] minutes, because it is less than $Content Time$ of 21 minutes. Then I subtract the difference between the time elapsed since the beginning of the session and duration of the previous pod, which are both 0 minutes in this case. Thus, the total value of the metric for the first pod is 41.66 minutes. Then, I repeat this process for the second pod. The second pod is 0.50 minutes long, to which I add the amount of content viewed in the remainder of the session which is [10 + 2 + 2 + 17 + 0 = 31] minutes. Then I subtract the difference between the time elapsed since the beginning of the previous pod and duration of the previous pod, which is [10.66 - 0.66 = 10] minutes. Thus, the total value of the metric for the second pod is 21.5 minutes. The same process is repeated for each of the remaining pods. On summing up the values corresponding to each pod, I get a total Ad Tolerance value of 67.98 minutes.

2.3.2 Data Summary via Metrics

For my sample comprising 110,500 sessions,¹³ Bingeability ranges from 0 to 57 (median is 1 episode) while Ad Tolerance ranges from -412.17 to $63,449.10$ minutes (median is 23.62 minutes) (see Table 2.5). The frequency distribution of Bingeability and Ad Tolerance is shown in Figure 2.3a and 2.3b. The most common value of Bingeability is one (complete episode) in a session. Thus, most of the sessions are not spent watching multiple episodes of the same TV show in my data. The distribution of Ad Tolerance is very right skewed. There is large peak between 0 and 3 minutes for more than 10,500 sessions. More than 16% of these sessions are those in which viewers end the session in less than a minute of calendar time. This suggests that there are many occasions when viewers are averse to seeing ads at the beginning of a session (pre-roll ads).

The relationship between the two metrics is shown in the jitter plots (around the values of Bingeability) in Figure 2.3c, where the darker areas indicate regions of high overlap. The correlation between Ad Tolerance and Bingeability is 0.68 over the full range of the two metrics and is 0.60 over the 2.5th to 97.5th percentile range of the two metrics. This provides some model free evidence that both metrics are complementary in terms of describing viewer behavior.

2.3.4 Metric Validity

Given that the two proposed metrics are deterministic transforms of the raw data, it is important for me to establish that they are valid and informative in terms of capturing viewer behavior. In the interest of brevity, I provide a summary of this analysis – full details are reported in Appendix A.4. I first compare the Bingeability metric to the commonly used industry metric for binge-watching – the raw count of episodes, typically unique, watched of the same TV show in one session (West, 2013). Unlike the raw count of episodes, the Bingeability metric considers whether viewers watch each episode completely by explicitly accounting for skipping or excessive fast-forwarding behavior. This allows for a much more precise measure of content consumption. The correlation between Bingeability and raw episode count is 0.85 over the full range and 0.70 over the 2.5th to 97.5th percentile range of Bingeability. The lack of perfect (or close to perfect) correlation suggests that the Bingeability metric captures information distinct from that in episode count. There are no comparable metrics to Ad Tolerance in practice or academic research to the best of my knowledge. In order to test the validity of my metric, I check for evidence of correlation between the metric and other “intuitive” measures of ad tolerance: number of pods shown, minutes of ad exposure and minutes of content viewed. The correlations are 0.78, 0.77 and 0.78 respectively, pointing to the fact that the metric captures distinctive information. Moreover, as shown in

¹³ The Ad Tolerance metric is undefined for the 12,117 sessions where there is no ad exposure and so I exclude them.

Appendix A.4, I find that this metric captures differences in behavioral consumption patterns better than intuitive measures. Overall, for both metrics, the distinctive information captured suggests face validity (cf. Ailawadi et al. (2003)).

2.4 Stage II

In this stage, I use the available information to predict the viewing behavior (summarized by the two metrics) of a new session, for either a current or a new viewer watching an existing or new TV show. In the first step, I lay out the information that is used (Feature Generation) and in the second, I lay out the predictive methods (Model).

2.4.1 Feature Generation

The high granularity of my data allows me to include a rich set of features to help predict viewer behavior during a session. I use current and past viewing activity on Hulu to choose these features. In order to include both weekdays and weekends, I use a seven-day moving window to capture past viewing activity. The features I use fall into four types.

(1). Current Behavior

These features (listed in Table 2.6a) characterize the current behavior of viewers in the session. They include fixed effects for viewer (6157), show (558), genre¹⁴ (18), month (5), week (5), day (2) and time of day (5) as well as continuous variables for episode length of the first episode viewed (1), number of episodes of the TV show ahead in sequence (1) and number of unwatched episodes of the TV show during my sample period (1). These features do not depend on a viewer’s historical activity. As my model (in subsection “Model”) can handle multicollinearity among the features to make predictions, I include fixed effects for both show and genre, and then later determine the relative importance of the predictors in the section “Results”. Since an individual viewer’s content consumption and ad response may vary as a function of where a current episode of a TV show is in the show’s entire chronology, I include two related measures to capture this. First, I measure the number of episodes of the TV show ahead in sequence (N_1) after the first episode viewed in the current session. Second, I measure the number of potentially unwatched episodes of the TV show (N_2) by subtracting the number of episodes viewed till date (during my sample period) from the total episodes available in my dataset.¹⁵ In total, I have 6,753 features in this type.

¹⁴ If a TV show is labelled with multiple genres (0.08% of the sessions), I use the first genre label assigned to it in the data.

¹⁵ Though N_1 and N_2 are correlated ($\rho=0.73$), I use both to capture behavior in the most comprehensive manner, given that I am inferring the inventory at Hulu at any given time (as I do not have access to the actual episode supply). In spite of these measures, I could still miss episodes if they are not viewed by anyone in my dataset at the time of the session and/or if they were available only for a limited time.

(2) Ad Targeting Rules

The four ad targeting rules (discussed in the earlier subsection “Ad Delivery”) can be summarized using features as follows:

- Spacing Rule (SR) is the “mean time between pods in an episode” averaged across all episodes viewed in a session.¹⁶
- Length Rule (LR) is the “mean pod length in an episode” averaged across all episodes viewed in a session.
- Diversity Rule (DR) is the mean of ad diversity per episode across all episodes viewed in a session.
- Clumpiness Rule (CR) is the mean of clumpiness in pod locations per episode across all episodes viewed in a session.¹⁷

The absolute value of the correlation between every pair of the rules ranges from 0.16 to 0.51 which shows that the rules are not too strongly correlated, thus providing evidence that each one is capturing a distinct underlying decision rule.

(3) Past Behavior: Watching TV Shows Only

I construct 9 functions to systematically generate 68 features (listed in Table 2.6b) that characterize many aspects of viewers’ TV-viewing behavior at the level of show, day of week, and time of day (cf. Yoganasimhan (2019)). The features are computed using all TV-show-viewing activity for a user during the one-week window before their current session. For instance, if a viewer decides to watch some TV show on Sunday at 5 pm, I consider all of her sessions watching TV shows that began in the 168 (7*24) hours before Sunday at 5 pm. This moving window of one week is chosen so that I have adequate information of a viewer’s recent historical viewing activity that includes both weekdays and weekends. I generate functions that vary with day and time of day to explore whether experiences that occur at specific times in the past are significant predictors of Bingeability and Ad Tolerance.

I explain one function in detail and show how its features are generated. The features for the other functions are generated similarly.

- a) *Bingeability Sum (Show, Day, Time of Day)*: This function calculates the past one-week sum of Bingeability of the viewer for the **Show** she is about to watch over that **Day** at that **Time of Day**. I consider **Day** as a Weekend or a Weekday and **Time of Day** as one of the five: Early Morning:

¹⁶ I do not consider time from the last pod shown in an episode till the end of an episode because a viewer could have stopped watching an episode at any time and not have waited till the end of the episode.

¹⁷ For 2.5% of sessions where a viewer switches between the same episodes, (e.g., watches episode 1 - episode 2 - episode 1 - episode 2), an episode’s ad targeting rule is found by averaging the rule value over each individual occurrence of the episode.

7–10am, Day Time: 10am–5pm, Early Fringe: 5pm – 8pm; Prime Time: 8pm – 11pm, Late Fringe: 11pm – 7am (Schweidel & Moe, 2016). For example, if a viewer decides to start watching the TV show *House* on a *Weekend* during *Day Time*, then the function will calculate the sum of Bingeability over all the sessions in the past week when the viewer viewed *House* on the *Weekend* during *Day Time*. More features can be generated by the function when the three variables – *Show*, *Day or Time of Day*, are dropped in turn from the function using a 2^3 design. Thus, a total of 8 features corresponding to *Bingeability Sum* (BS) can be generated for each session in my sample, and these are shown in Table 2.6c.

I note that for the first session of each viewer in the panel data, the value of features based on past behavior is 0 because past observations are censored. This is true for 5.6% of the sessions in my sample corresponding to 6,157 viewers. I do not drop these as they help me replicate situations when a new viewer joins the platform.

(4) Past Behavior: Watching TV Shows or Movies

Even though the target behavior that I study is viewing of TV show content and ads, I still consider past movie-viewing behavior. This allows me to measure how ad exposure in the past week while watching a movie or a TV show influences the decision to see a TV show in the current session. I construct 11 distinct functions that generate 136 features (listed in Table 2.6d) which consider historical one-week sessions in which *either* TV shows or movies were seen. I replace ‘Show’ with ‘Title’ in the name of these functions to indicate that when ‘Title’ is absent, the viewer could have watched either a TV show or a movie in the past week.

I explain two functions in detail and show how their features are generated. The features for the other functions are generated similarly.

- a) *Pod Count (Pod Length, Title, Day, Time of Day)*: This function calculates the past one-week sum of the number of pods of length equal to some **Pod Length**, shown to the viewer for that **Title** over that **Day** at that **Time of day**. Based on the histogram of Pod Length shown earlier in Figure 2.3a, I divide Pod Length into 3 categories: 1 (1 – 26 sec), 2 (26 – 52 sec) and 3 (>52 sec). I use the same breakdown for the categories as that used for Ad Length in the subsection “Ad Delivery” because more than 99% of the pods in my data have only 1 ad. This function generates a total of 32 features from this $4 \times 2 \times 2 \times 2$ design: Pod Length (4: 1, 2, 3, __) x Title (2: Title, __) x Day (2: Day, __) x Time of Day (2: Time of day, __), where ‘__’ corresponds to ‘any value’ as shown in Table 2.6c.
- b) *Ad Diversity (Title, Day, Time of Day)*: This function finds the past one-week average of the percentage of diverse ads shown in each session (in which there was ad exposure) for the viewer

watching that **Title** over that **Day** at that **Time of day**. As I do not have a unique Ad ID for each ad in my dataset, I use a combination of Ad Industry (16 categories such as CPG, Telecom, etc.) and Ad Length (3 categories) to generate 48 unique ad combinations.

2.4.2 Model

Model Setup. Given the set of chosen features (above), I need to develop a methodology to predict my key summaries of viewing behavior – Bingeability and Ad Tolerance – for a future session. The total number of features generated in the previous subsection “Feature Generation” is large (6,961). In order to capture the effects of this large set of features in the most flexible way, including non-linearities and interactions, I use machine learning methods (Lemmens & Croux, 2006; Neslin et al., 2006; Rafieian & Yoganarasimhan, 2019; Yoganarasimhan, 2019). These predictive methods also have the additional advantage of being scalable, handling many features for many users, and computationally efficient. Since I want to understand importance of different features and interpret those features’ relationships with the outcomes, I use tree-based machine learning models. I express my model as follows:

$$Y_t = f_1(X_{1t}, X_{2t}, X_{3t}, X_{4t}, W_{1t}, W_{2t}) + u_t \quad (2.5)$$

where Y is the metric of interest (Ad Tolerance or Bingeability),¹⁸ the subscript t denotes a session and f_1 is a non-linear function of all the features. X_1, X_2, X_3 and X_4 , are the Spacing Rule (SR), Length Rule (LR), Diversity Rule (DR) and Clumpiness Rule (CR), respectively (as detailed earlier); W_1 is the matrix of features describing current behavior listed in Table 2.6a; W_2 is the matrix of features describing past behavior listed in Table 2.6c and 2.6d; and u is the error, which is assumed to be additively separable.

I assume W_1 and W_2 to be exogenous as they are determined before the session begins, and I assume there is no autocorrelation between the errors u_t . However, as noted earlier, the data patterns suggest that the X variables, which represent the ad targeting rules, are not set exogenously to the behavior of interest. In other words, they could be endogenous due (primarily) to simultaneity, i.e., X 's could be set depending on the value of Y . For example, as Bingeability or Ad Tolerance (Y) increases, the mean spacing between pods (X_1) could increase because the streaming provider may only have a limited inventory of ads to deliver for that show at that time, leading to an average decrease in the frequency of pod spacing (if no other ads are available to compensate). The trade press has noted that low ad inventory was a frequent occurrence at Hulu around the time of my data (Sloane, 2019).

If this potential endogeneity is not corrected for, then my predicted outcomes will be biased, leading to non-optimal ad scheduling recommendations. I correct for this using instrumental variables.

¹⁸ In Appendix A.5, I show how my approach can be modified to model the two Y 's jointly. Given that there isn't a meaningful difference in the final recommendations, the additional benefit of doing so seems to be less than the additional methodological complexity required.

These instruments should affect Y only through their effect on X_i , $i = \{1,2,3,4\}$, i.e., be uncorrelated with unobservables u . I leverage the institutional detail that Hulu has been known to match sponsors with specific TV shows (Dubner, 2009). Therefore, ad schedules in an episode of a TV show for a focal viewer are likely to be correlated with ad schedules in the same episode for another viewer (while not depending on the focal viewer's viewing behavior). I construct episode-level instruments Z_i , for each X_i , $i = \{1,2,3,4\}$, in the same spirit as the instruments in Nevo (2000). I define Z_{it} to be the mean of v_i for all other viewer-episode pairs (involving any of the episodes viewed in session t) that began *before* the start of session t , where v_1 = time between pods, v_2 = pod length, v_3 = ad diversity and v_4 = clumpiness. Note that Z_{it} can affect Y_t only through its effect on X_{it} , because the focal viewer is unaware about the value of Z_{it} that was experienced by other viewers. This is a reasonable assumption for two reasons. First, my sample is a random draw from all Hulu viewers, lowering the chance that any two viewers would know each other at all. Second, at the time of my data, there is no discussion around ad delivery on Hulu's Facebook page, which was the brand's major online social media site at the time. In terms of the empirical relationship between X_i and Z_i , I find that the raw correlation between them for $i = \{1,2,3,4\}$ is reasonable at 0.35, 0.25, 0.27 and 0.33.¹⁹

Estimation Approach. The first stage of the estimation process can be expressed using a model of X_i as a function of Z_i ($i = \{1,2,3,4\}$), W_1 and W_2 as shown below:

$$X_{it} = g_i(Z_{1t}, Z_{2t}, Z_{3t}, Z_{4t}, W_{1t}, W_{2t}) + e_{it} \quad (2.6)$$

where, g_i is a non-linear function and e_i is the error term assumed to be additively separable with an expected value of 0. The estimates of the outcome variables from the above first-stage model can then be plugged as inputs to the second-stage model. The second stage of the estimation process can be expressed using a model of Y on \hat{X}_{it} (estimates of X_i from the first-stage) as well as on W_1 and W_2 :

$$Y_t = f_2(\hat{X}_{1t}, \hat{X}_{2t}, \hat{X}_{3t}, \hat{X}_{4t}, W_{1t}, W_{2t}) + u_t \quad (2.7)$$

¹⁹ The correlation between the instrument and the endogenous variables does not increase if the instruments are calculated over respective geographical states or regions of the focal viewer's permanent address, which indicates that the ad targeting rules are unlikely to vary by geographical location of the viewer (assuming the viewer primarily watches content in the state/region of her permanent address which is the only address that is recorded in the data). I also find that show-level instruments (in comparison to episode-level instruments) have a lower correlation with the endogenous variables which suggests that ad characteristics are determined by the platform at the granular episode level and not the show level. Hence, I use episode-level instruments and not show-level instruments.

where f_2 is a non-linear function, u is the error term of the second-stage, which is assumed to be additively separable with an expected value of 0, and Y_t represents the values of Bingeability and Ad Tolerance.²⁰

The use of instrumental variables along with machine learning methods is nascent, with no prior research in marketing using it, to the best of my knowledge. The machine learning literature has just begun to explore the use of instrumental variable approaches to infer causality. Two notable examples are Hartford et al. (2017), which uses a deep learning framework with instrumental variables to make counterfactual predictions of the outcome, and Athey et al. (2019), which uses random forests with instrumental variables to find asymptotic marginal effects.

To decide which tree-based method to use,²¹ I compare the performance of different methods using simulated data, so that I know the ground truth which is unlike the case with my observed dataset where I do not know the true explanatory power of the features (cf. Hartford et al. (2017)). I consider two popular tree-based machine learning methods known for their ability to get close to the ground truth – Extreme Gradient Boosting (XGBoost) and Random Forests (Breiman, 2001; Chen & Guestrin, 2016). Their performance is also compared with the traditional linear two-stage least squares (2SLS) approach. My goal is to choose the better performing method for both the first and second stage of the model. Appendix A.6 describes the two methods, the simulation, and the results, which show XGBoost gets closest to the ground truth. My findings are consistent with past literature and the results of prediction competitions that have found gradient boosting methods, and especially XGBoost, to predict better on average than Random Forests (Olson et al., 2017; Oughali et al., 2019; Synced, 2017). Thus, my results are all based on the XGBoost method (implemented on a 4 core CPU with two threads per core at 3.6 GHz) that takes about 2 minutes to run.

2.5 Results

2.5.1 Model Estimation

To estimate the model on the dataset, containing a total of 5,760 viewers, 508 unique shows, and 105,610 sessions (see Table 2.7), I construct a training dataset for calibration and two separate holdout datasets for estimation. I estimate my model on both future observations of the same set of viewers (Holdout 1) and observations of a completely new group of viewers (Holdout 2). First, I randomly hold out 500 viewers and select the remaining 5,260 viewers for training. Then, among these selected viewers, I select approximately 80% of their initial sessions to form the training sample (74,996 sessions), and 20% of

²⁰ In order to implement the instrumental variables approach, I can only use observations (sessions) for which I have complete information about $Z_i, i = \{1,2,3,4\}$. I remove 4,536 sessions where no other viewer had viewed those episodes before. Next, I drop 354 viewers who visited the platform exactly once (as their single sessions cannot be randomly assigned to both the training and holdout data).

²¹ I also explored other linear models such as LASSO, Ridge Regression and Elastic Net but found that non-linear models fit the data better.

their future sessions (21,497 sessions) to form the first holdout sample (Holdout 1). The remaining 500 viewers, with their 9,117 sessions form the second holdout sample (Holdout 2). As one of my objectives is to allow the streaming platform to build ad schedules for new TV shows that have not yet been viewed but could be viewed by current viewers or new viewers, I estimate the model on this task too. I allow both holdout samples to include sessions with 13 (Holdout 1) and 16 (Holdout 2) new TV shows not in the training data.

Next, I estimate the first-stage model (6) using the training sample and get the estimates \hat{X}_i , $i = \{1,2,3,4\}$ for both the training and holdout samples. The estimates \hat{X}_i are then plugged into the second stage of the model (2.7). I estimate the second-stage model using the training sample and obtain predictions for the outcomes in the holdout samples. The parameters of the XGBoost model are selected using 5-fold cross-validation repeated 10 times (Appendix A.7 provides details on the cross-validation process and parameter tuning). The estimates of the outcome variables will be used as inputs to the ad scheduling process (detailed in section “Stage III”).

A frequent critique of machine learning methods is that they operate as a “black-box” and yield results that are not interpretable. I try to address this via the use of two descriptive methods – “feature importance” and “partial dependence” below. The former can be seen as analogous to the “average effect” of a covariate (coefficient times mean covariate) in a traditional regression setting while the latter can be seen as analogous to the “marginal effect” of a covariate (coefficient).

2.5.2 Feature Importance

As the name denotes, this method allows me to identify the features in equation (2.7) that are most predictive of the outcomes. A commonly used metric to do this is “Variance Reduction” (Hastie et al., 2009). This is the “gain” achieved when the tree is split on a feature, defined as the maximum reduction in RMSE (for continuous outcomes, like Ad Tolerance) or Negative Log Likelihood (for discrete outcomes, like Bingeability). I identify the features that are most frequently split during model training. Then I compute the gain of a set of multiple related features by summing up the gain for each individual feature in that set. The percentage gain for each set of features used to split the tree is reported in Tables 2.8a and 2.8b for the top 10 sets of predictive features for Bingeability and Ad Tolerance respectively.

The most important predictors of Bingeability are past predictors of ‘Bingeability Sum’, and ‘Number of episodes ahead in sequence, N_1 ’ and viewer fixed effects. The most important predictors of Ad Tolerance are viewer fixed effects, past predictors of ‘Ad Tolerance Sum’ and the past predictors of ‘Pod End’. The fact that individual fixed effects and the sums of past outcomes are important in predicting the outcomes for a new session is not itself surprising, but this process quantifies their relative importance and identifies the other important features. The total gain contribution of the four estimated ad

targeting rules, \widehat{SR} , \widehat{LR} , \widehat{DR} & \widehat{CR} , is 9.0% for Bingeability and 8.2% for Ad Tolerance. This indicates that the four ad targeting rules have an important role to play in predicting the value of the metrics. The clumpiness of ads (\widehat{CR}) is the most important advertising pattern for predicting Bingeability (with a 4.8% gain) while the frequency of pod delivery (\widehat{SR}) is the most important advertising pattern for predicting Ad Tolerance (with a 4.3% gain) (Table 2.8c).

2.5.3 Partial Dependence

I use *partial dependence plots* (J. Friedman, 2001) to examine the (partial) relationship between the features and the outcomes, and to the best of my knowledge I am introducing this practice to marketing. Let $X = \{X_1, \dots, X_d\}$ be the set of all features in the training sample, and $f(X)$ be the corresponding prediction function. If X can be partitioned into a set of features of interest X_S and its complement set X_C , then the partial dependence of the outcome on X_S is defined as follows:

$$f_S(X_S) = E_{X_C}[\hat{f}(X_S, X_C)] = \int f(X_S, X_C) p_C(X_C) dX_C$$

where, $p_C(X_C)$ is the marginal probability density function of X_C . The above equation can be estimated from a set of training data by averaging out the effects of all the other features X_C in the model, while taking into account any correlations among features in X_S (J. Friedman, 2001; Greenwell, 2017).

Empirically, for a single feature of interest, consider an observation's value of that feature, and create an otherwise identical copy of the dataset except substitute that value in for all other observations' values of that feature. For the newly edited data, obtain the model's predictions for each observation and average the predictions across all observations. Then repeat this for each observation of that feature, plotting feature values versus average prediction values. This can be better understood as a two-step process:

- i. For $i = \{1, \dots, n\}$, where n is the number of observations in the training data,
 - a) Replace each value in X_S (n-dimensional vector) with X_{S_i} (constant)
 - b) Compute predicted values of the n outcome variables
 - c) Find average of the n predicted values = $\bar{f}_S(X_{S_i})$
- ii. Plot $\{X_{S_i}, \bar{f}_S(X_{S_i})\}$ for $i = \{1, \dots, n\}$ to get the partial dependence plot.

To ease the computational burden, I compute the partial dependence over the deciles of the feature in addition to its 2.5th and 97.5th percentile. Figure 2.4a shows the relationship between Bingeability and its most important feature, *Bingeability Sum (same Show, any Day, any Time of day)*. This feature represents the sum of Bingeability across all sessions shown to the viewer in the past week for the same

Show (as the current session) viewed on any Day at any Time of day. The figure shows that an increase in Bingeability for a show from 0 episodes to 15 episodes over the past week predicts an average increase in Bingeability for the same show in the current session by 0.6 episodes. The relationship between Ad Tolerance and its most important feature (other than viewer fixed effects), *Ad Tolerance Sum (same Title, any Day, any Time of day)*, is shown in Figure 2.4b. This feature calculates the sum of Ad Tolerance across all sessions shown to the viewer in the past week for the same Title (as the current session) viewed on any Day at any Time of day. The figure shows that an increase in Ad Tolerance for a title from -16 minutes to 3,513 minutes over the past week predicts an average increase in Ad Tolerance for the same title in the current session by 710 minutes. Both relationships (in Figures 2.4a and 2.4b) provide evidence of state dependence between the past and current sessions of a viewer for the same TV show.

As my goal is to make ad scheduling recommendations, I need to understand the relationships between the ad targeting rules and my two outcome variables. The partial relationships between the ad targeting rules that are most predictive, clumpiness (\widehat{CR}) and spacing (\widehat{SR}), and the predicted values of Bingeability and Ad Tolerance respectively, are shown in Figures 2.4c and 2.4d. Lower clumpiness values, i.e., more equally spaced pods, predict higher Bingeability (Figure 2.4c). Moreover, the extent of the influence of \widehat{CR} (over its 2.5th to 97.5th percentile range) on Bingeability is ± 0.44 episodes. The extent of the influence of \widehat{SR} (over its 2.5th to 97.5th percentile range) on Ad Tolerance is ± 18.95 minutes (Figure 2.4d), with most of the change occurring from the 90th percentile (7.7 minutes) to 97.5th percentile (8.6 minutes) of spacing. This suggests that, on average, spacings longer than 7.7 minutes can overly adapt viewers to the content and/or absence of ads and increase their aversion to ads.

It is also possible that the ad targeting rules may interact, so I examine the partial dependence of two predictors jointly. I consider my first pair of predictors of interest to be $X_{s1} = \{\widehat{X}_1, \widehat{X}_4\} = \{\widehat{SR}, \widehat{CR}\}$, the predicted ad targeting rules that are most important in predicting Bingeability and then the second pair of predictors $X_{s2} = \{\widehat{X}_1, \widehat{X}_2\} = \{\widehat{SR}, \widehat{LR}\}$, since these two rules are most important in predicting Ad Tolerance. The partial dependences of the estimated values of Bingeability and Ad Tolerance on each pair of their important predictors are shown in Figure 2.4e and 2.4f. Figure 2.4e shows that the magnitude of the influence of the top two ad targeting rules (over their 2.5th to 97.5th percentile range) on Bingeability is ± 0.24 episodes. Furthermore, Figure 2.4e shows that higher values of \widehat{SR} and lower values of \widehat{CR} predict higher Bingeability. Similarly, Figure 2.4f shows that the magnitude of the influence of the top two ad targeting rules (over their 2.5th to 97.5th percentile range) on Ad Tolerance is ± 15.94 minutes, which is less than the size of the partial dependence on \widehat{SR} alone, ± 18.95 minutes, found in Figure 2.4d. Furthermore, Figure 2.4d also shows that lower values of \widehat{SR} and higher values of \widehat{LR} predict higher Ad Tolerance.

Finally, I look at the effect of the pairwise interactions (six) across all the four estimated ad targeting rules $X_{s3} = \{\hat{X}_1, \hat{X}_2, \hat{X}_3, \hat{X}_4\} = \{\widehat{SR}, \widehat{LR}, \widehat{DR}, \widehat{CR}\}$. The partial dependences of the estimated values of Bingeability and Ad Tolerance on X_{s3} are calculated over the quintiles of each variable in addition to their 2.5th and 97.5th percentile to ease computational burden. The extent of the influence of the four ad targeting rules (over their 2.5th to 97.5th percentile range) on Bingeability is ± 0.25 episodes, which is about the same as ± 0.24 episodes found in Figure 2.4e. Thus, there is almost no additional impact on Bingeability. Similarly, the extent of the influence of the four ad targeting rules (over their 2.5th to 97.5th percentile range) on Ad Tolerance is ± 33.08 minutes, which is more than the extent of ± 15.94 minutes found in Figure 2.4f.

From Table 2.7, the median value of Bingeability in the data is 1 episode and that of Ad Tolerance is 23.69 minutes. The partial dependence analysis is useful in that it tells me the impact of different variables (or sets of variables) on the outcome variables. For example, based on the above, I know that the Ad Targeting rules, in combination can effect a maximum change of 25% (0.25/1.00) on median Bingeability and a maximum change of 140% (33.08/23.69) on median Ad Tolerance. Overall, these analyses show that the ad targeting rules, individually and together, have a material impact on viewer behavior as captured via the two outcomes.

2.6 Stage III

With summaries of behavior predicted and the importance of the features that predict those summaries understood, in the third stage I use the predicted values of the behavioral summary metrics to make ad scheduling recommendations. I do this in two steps. First, I provide a guide to the streaming provider on how to use these predictions with a decision tree, and then I use an optimization procedure to recommend a better ad schedule in any given session. In order to illustrate the properties of my generated ad schedule for each session in the holdout samples, I contrast it with the current ad schedule (observed in the data) and an alternative ad schedule based on a naïve heuristic.

2.6.1 Ad Decision Tree

I propose an “Ad Decision Tree” (Figure 2.5) to identify the types of sessions where ads may enhance – or at least not detract from – content consumption. The Ad Decision Tree takes in the predictions of Bingeability and Ad Tolerance obtained from the model and recommends action. The first decision split in the Ad Decision Tree is to check whether the predicted value of Bingeability is greater than a threshold, T . If the predicted value of Bingeability for the session is less than the threshold, then the streaming platform is advised to not show any ads in the session. This is because there is not much incentive for a free ad-supported only streaming platform to show ads in a session if the ads are predicted to prevent the viewer from completing a desired number of episodes (represented by the chosen threshold

value for Bingeability). By ensuring that a viewer is predicted to watch at least beyond that threshold, the streaming platform will be able to provide a minimum level of engagement with the content on its platform. I examine the impact of increasing the threshold in the subsection “Decision Support System,” but for now, I start by choosing the lowest Bingeability threshold of 0 episodes i.e., show ads for all sessions.

If the predicted value of Bingeability is greater than or equal to the threshold, I move to another part of the tree and check the sign of the predicted value of Ad Tolerance. Negative values of Ad Tolerance capture occasions where viewers stopped watching content after being exposed to a pod, which itself was preceded (at some point) by a longer period of no ad exposure. On the other hand, a positive value of Ad Tolerance indicates occasions where ads were shown more frequently to a viewer and the viewer continued to watch content.

If the predicted value of Ad Tolerance is > 0 , then I solve a novel optimization procedure discussed in subsection “Optimization”. If the predicted value of Ad Tolerance is ≤ 0 , then it is unclear how tolerant a viewer is towards seeing a pod of ads, so my proposed decision tree recommends testing and then adapting to what is learned. To test whether the viewer can have both Ad Tolerance > 0 and Bingeability ≥ 1 , the streaming platform is advised to show pods within the first half of each episode to resemble occasions of frequent ad exposure. To ensure an overall minimum ad exposure within the first half of an episode, it would be best to show pods at an interval of a quarter of the episode length with “regular interruptions” (discussed further in subsection “Optimization”). Based on the viewer’s response to the ad exposure in the first half of the episode, if the viewer continues to have Bingeability ≥ 1 , then the viewer’s Ad Tolerance is updated to > 0 and the rest of the optimization procedure can be implemented.

The recommendations made by the Ad Decision Tree for the observations in the two holdout samples are summarized in Table 2.9. I find that for most of the sessions in both holdout samples (94% of observations in Holdout 1 and 97% of observations in Holdout 2 – see Set C, Table 2.9), the recommendation to the streaming provider is to use the proposed optimization procedure.

2.6.2 Optimization

In this research, I have set the objective of a streaming provider to maximize ad exposure (to earn more ad revenue) subject to the constraint of not detracting from the consumption experience. I can express the maximization of the objective function for a given session as follows:

$$\max f(n, d) = \sum_{j=1}^n d_j \quad \text{where} \quad \sum_{j=1}^n s_j + s' = \overset{\text{expected content watched}}{\widehat{be}} \quad (2.8)$$

where, n is the number of pods shown in a session, d_j is the duration (length) of pod j , s_j is the spacing (content time shown) between pod $j-1$ (or beginning of session if $j=1$) and pod j , s' is the duration of content time shown after the end of pod n , \hat{b} is the estimated Bingeability from the model, and e is the average episode length of all episodes of the TV show watched in that session in my dataset.

My findings in subsection ‘‘Partial Dependence’’ showed that lower values of clumpiness (i.e., more equal spacings between pods) result in higher values of Bingeability. In addition, past literature has shown that viewers are less likely to adapt to irregular sources of interruptions, such as dormitory noise or aircraft noise (Frederick & Loewenstein, 1999). Hence, it is likely that having regularity in interruptions would assist the adaptation process and increase Bingeability. Unequal spacing s_j between pods and unequal duration d_j for each pod are sources of irregularity. To remove irregularities within a session, I let the duration of each pod d_j be equal to d and let the duration of each spacing s_j and s' be equal to s . Consequently, I rewrite the optimization as follows:

$$\max f(n, d) = nd \quad \text{where } s(n + 1) = \hat{b}e \quad (2.9)$$

where the product of spacing between pods, s , and number of pods plus one, $n + 1$, should equal the product of predicted Bingeability, \hat{b} , and average episode length, e . The constraint $s(n + 1) = \hat{b}e$ allows only mid-roll ads (i.e., no pre-roll ads or post-roll ads). This is because prior work has found that viewers are more likely to completely view mid-roll ads, followed by pre-roll ads and finally post-roll ads (Krishnan & Sitaraman, 2013). Note that the subsection on ‘‘Decision Support System’’ relaxes this constraint to allow for pre-roll ads.

My objective function is subject to the constraint of not detracting from the content consumption experience i.e., not exceeding the predicted Ad Tolerance for a session. Using equation (2.4) and a series of stepwise substitutions shown in Appendix A.8 (Part 1), this constraint can be expressed as follows:

$$\hat{a} = w_1 nd + w_2 \left(n\hat{b}e - \frac{n(n+1)}{2}s \right) - w_3 ns \quad (2.10)$$

where w_1, w_2, w_3 are the three weights, originally present in equation (2.4), and \hat{a} is the predicted value of Ad Tolerance. I also have additional constraints that there must be at least one pod, and the duration of a pod must be non-zero. Therefore, the constrained optimization problem in equation (2.9) can be expressed as follows along with all its constraints:

$$\max f(n, d) = nd \quad \text{where } s(n + 1) = \hat{b}e$$

$$\text{such that } \hat{a} = w_1 nd + w_2 \left(n\hat{b}e - \frac{n(n+1)}{2}s \right) - w_3 ns, \quad n \geq 1, \text{ and } d > 0$$

Since I am setting spacing to be a constant function of expected total episode content viewed, I replace s with $\frac{\hat{b}e}{n+1}$ in the constraints, and then I can re-express my constrained optimization problem as

$$\max f(s, d) = nd \quad (2.11)$$

$$\text{such that } \hat{a} = w_1 nd + w_2 \left(\frac{n\hat{b}e}{2}\right) - w_3 \left(\frac{n\hat{b}e}{n+1}\right), n \geq 1, \text{ and } d > 0$$

By applying the Lagrange function to the optimization problem, I get the following expression:

$$L(n, d, \lambda_1, \lambda_2, \lambda_3) = nd - \lambda_1 \left(\hat{a} - w_1 nd - w_2 \left(\frac{n\hat{b}e}{2}\right) + w_3 \left(\frac{n\hat{b}e}{n+1}\right) \right) + \lambda_2(n-1) + \lambda_3 d$$

with the following six constraints: (1) $\frac{\partial L}{\partial n} = 0$ (2) $\frac{\partial L}{\partial d} = 0$, (3) $\lambda_2(n-1) = 0$, $\lambda_3 d = 0$ (4) $n \geq 1$, $d > 0$
(5) $\hat{a} = w_1 nd + w_2 \left(\frac{n\hat{b}e}{2}\right) - w_3 \left(\frac{n\hat{b}e}{n+1}\right)$ (6) $\lambda_1, \lambda_2, \lambda_3 \geq 0$

I use the fifth constraint to solve for n , so I get a quadratic equation in n :

$$n^2(w_1 2d + w_2 \hat{b}e) + n(w_1 2d - (2w_3 - w_2)\hat{b}e - 2\hat{a}) - 2\hat{a} = 0 \quad (2.12)$$

As $d > 0$, and $\hat{a} > 0$, $\hat{b} \geq 1$ (from the Ad Decision Tree), the above equation has one positive root and one negative root of n . Solving the other constraints of the Lagrange Function does not give solutions within the acceptable parameter space. Next, I set the weights, w_1, w_2, w_3 , to 1, as originally done in subsection ‘‘Metric Development,’’ although these can be set differently, which I consider in Appendix A.3. The two unknown parameters in equation (2.12) are d and n . I fix d at 30 seconds,²² the median pod duration in my dataset, and then solve equation (2.12) for the optimal \tilde{n} , and use its positive root which can be expressed as follows:

$$\tilde{n} = \frac{-(1-\hat{b}e-2\hat{a})+\sqrt{\Delta}}{2(1+\hat{b}e)}, \text{ where } \Delta = (\hat{b}^2 e^2 + 12\hat{a}\hat{b}e - 2\hat{b}e + 4\hat{a}^2 + 4\hat{a} + 1) \text{ and } \sqrt{\Delta} > 0 \quad (2.13)$$

²² I also run the optimization using a fixed pod duration of 15 seconds instead of 30 seconds as the distribution of pod length (Figure 2a) shows a second peak at 15 seconds. The recommended spacing using 15 seconds and that using 30 seconds is almost identical (and the difference on average is less than 6 seconds).

Therefore, I have found the recommended number of pods \tilde{n} from the optimization routine, and this implies that the recommended spacing $\tilde{s} = \frac{\hat{b}e}{\tilde{n}+1}$. Hence, my optimization procedure recommends the pod frequency \tilde{s} for a viewer's session holding pod duration d constant.^{23,24}

In order to understand the effect of the estimates of Bingeability, \hat{b} , and Ad Tolerance, \hat{a} , on the recommended number of pods \tilde{n} and pod spacing, \tilde{s} (which is proportional to $\frac{1}{\tilde{n}}$), I take the partial derivatives of \tilde{n} in (12) with respect to \hat{b} and then with respect to \hat{a} . The expressions of the partial derivatives are shown in Appendix A.8 (Part 2). The partial derivatives suggest that the streaming provider should on average increase pod spacing (decrease pod frequency) when a viewer is expected to have lower Ad Tolerance or higher Bingeability, holding the other constant. Similarly, the streaming provider should on average decrease pod spacing (increase pod frequency) when a viewer is expected to have higher Ad Tolerance or lower Bingeability, holding the other constant.

To summarize all of these session-by-session ad spacing recommendations, I consider their full distribution. The density of the recommended spacing for the two holdout samples helps illustrate the range of recommendations made by the optimization routine (Figures 2.6a and 2.6b). The median value of the recommended spacing for Holdout 1 (future sessions of the viewers in the training sample) is 4.33 minutes, and its 2.5th to 97.5th percentile range is from 0.61 to 9.80 minutes. The median value of the recommended spacing for Holdout 2 (new viewers) is 4.43 minutes, and its 2.5th to 97.5th percentile range is from 0.71 to 9.43 minutes.²⁵ While this may seem like very frequent ad exposure, it is not very different from that in the data (below). In addition, Nelson et al. (2009) show ads every 2 minutes in their experiments and current industry practice is experimenting with comparable or even shorter ad spacing (Gessenhues, 2018). Note that the optimization procedure takes about 10 seconds.

2.6.3 Recommended Schedule: Comparison with Data

In this section, I compare the recommended spacing \tilde{s} for a session with the average observed spacing \bar{s} in the session. The average observed spacing for a session is calculated across each of its observed spacings, s_j , which is the content time shown between pod $j-1$ (or beginning of session if $j=1$) and pod j . I do not consider the content viewed from the end of the last pod till the end of the session, s' , as a viewer could have ended the session before the end of an episode thus biasing the value of s' .

²³ I express the constraint as a quadratic equation in \tilde{n} , and not \tilde{s} , because the product of the roots in the quadratic equation of \tilde{n} is always negative, giving us one positive and one negative root, and helping us choose the positive root. The product of the roots in the quadratic equation of \tilde{s} is always positive, making it harder to choose the appropriate positive root.

²⁴ I do not directly recommend number of pods, \tilde{n} , because the number of pods to be shown is not under direct control of the streaming provider. The streaming provider can only set the spacing (content time) after which a pod must be shown. The total number of pods that the viewer will end up viewing depends on the endogenous decision of the viewer to stop viewing content.

²⁵ I also examined recommendations by show length and genre. For show episodes < 30 mins, the spacing was 4.44 mins (4.26 mins) for Holdout 1 (Holdout 2), while for show episodes > 30 mins, it was 4.22 mins (4.57 mins). For Comedy shows, it was 4.60 mins (4.49 mins), for Drama 4.40 mins (4.76 mins) and for Science Fiction 4.95 mins (5.11 mins).

The density of the average observed spacing, \bar{s} , for these sessions in both holdout samples is shown in Figure 2.7a and 2.7b. The median value of the average observed spacing for Holdout 1 (future sessions of current viewers) is 6.43 minutes and its 2.5th to 97.5th percentile range is from 0 to 13.30 minutes. The median value of the average observed spacing for Holdout 2 (new viewers) is 6.96 minutes and its 2.5th to 97.5th percentile range is from 0 to 14.40 minutes. The peak at 0 minutes corresponds to sessions where there was only a pre-roll ad (ads at beginning of a session) and hence the spacing is 0 minutes.

I use the ratio of my recommended spacing to the average observed spacing in the data to highlight the difference of my approach. The distribution of the ratio of recommended spacing and average observed spacing for these sessions in the two holdout samples is shown in Figure 2.8a and 2.8b (and sessions with pre-roll ads only are dropped to avoid division by 0). The median value of the recommended ratio is 0.66 and 0.61 for Holdout 1 and 2, respectively. The optimization recommends a shorter spacing than observed (when the ratio is less than 1) in 81% and 86% of the sessions (Figure 2.8a, 2.8b). In these sessions, the streaming provider is recommended to show ads more frequently than current practice to maximize ad exposure, thus increasing revenue. On those occasions when the ratio is greater than 1, the streaming provider is recommended to show ads less frequently (with a longer spacing) than current practice to avoid compromising the content consumption experience and promote viewer engagement with the content on the platform.

2.6.4 Decision Support System

The ad decision tree can be used as a decision support system by the platform. Specifically, the platform can define critical thresholds of Bingeability and obtain the recommended ad delivery schedules to explore the inherent tradeoffs between content consumption and ad exposure for its viewers. The threshold is set so that for sessions with predicted Bingeability below the threshold, T , there should be no ads served. The recommended number of ads, \tilde{n} , is compared with the observed ad exposure, n , in Table 2.10a and Figure 2.9a for different values of the threshold, T .

Using \tilde{s} , \hat{b} and e , I can derive the recommended spacing rule \tilde{X}_1 which is the “mean recommended spacing between pod exposures in an episode” averaged across all episodes predicted to be viewed in a session. Similarly, using \tilde{s} , \hat{b} and e , I can also derive the recommended clumpiness rule \tilde{X}_4 , which is the recommended clumpiness of pods throughout an episode, averaged across all episodes predicted to be viewed in a session. In the Bingeability model (equation (2.7)), I then replace \hat{X}_1 (Spacing Rule) and replace \hat{X}_4 (Clumpiness Rule) with their newly recommended values \tilde{X}_1 and \tilde{X}_4 , respectively. I also replace \hat{X}_2 (Length Rule) with 0.5 (median pod duration) and keep \hat{X}_3 (Diversity Rule) as it is. Then I find the optimized predictions of Bingeability based on my recommended ad schedule, which I denote as, \tilde{b}_{withad} . Next, for those observations which had initial predictions of Bingeability, \hat{b} , below the threshold

T (where the platform is advised to not show ads²⁶) I train the Bingeability model *without* the four ad targeting rules ($\hat{X}_1, \hat{X}_2, \hat{X}_3, \hat{X}_4$), and then make revised predictions, \tilde{b}_{woad} . I report the net incremental change in $\tilde{b}_{withad} + \tilde{b}_{woad}$ ($= \tilde{b}$) as compared to observed Bingeability b , and initial predicted Bingeability \hat{b} , in Table 2.10b and 2.10c respectively, for different values of the threshold. These comparisons are also shown in Figure 2.9b and 2.9c for Holdout 1 and Holdout 2 respectively.

The results for Holdout 1 (future sessions of current viewers) and Holdout 2 (new viewers) show the tradeoff between content consumption (measured through Bingeability) and ad exposure. From Table 2.10a and Figure 2.9a, I see that there is a net increase in ad exposure for thresholds (of predicted Bingeability) ≤ 0.8 for observations in Holdout 1 and for thresholds ≤ 0.9 for observations in Holdout 2. A threshold of 0 results in the maximum increase in ad exposure for both Holdout 1 and Holdout 2. From Table 2.10b & 2.10c and Figure 2.9b & 2.9c, I see that the maximum increase in content consumption for Holdout 1 is for a threshold of 0, and the maximum increase (or lowest decrease) in content consumption for Holdout 2 is for a threshold of 1.6.

Overall, for future sessions of current viewers, if the platform uses a threshold of 0 to show ads, the platform gets more ad exposures and viewers see more content. This results in a 71.2% increase in ad exposure, as compared to what was observed, and a 5.17% increase in Bingeability as compared to the initially predicted Bingeability before optimization (or a 5.33% increase in Bingeability as compared to observed Bingeability).²⁷ On the other hand, for new viewers, there is a tension: the platform is better off in terms of ads shown if it uses a threshold of 0 to show ads which results in a 79.1% increase in ad exposure; whereas viewers are better off in terms of content viewed if the platform uses a threshold of 1.6 to show ads which results in a 1.03% increase in Bingeability as compared to the initially predicted Bingeability (or a decrease of 0.80% in Bingeability as compared to observed Bingeability). This indicates that for new viewers for whom preferences are unknown, there is no single threshold T that can lead to the best outcome for both the platform and the viewer. The best that can be done in this case is to compare the optimized Bingeability with initial predicted Bingeability using the same set of features, giving a 1% increase in content consumption.

It is important to note that for Holdout 1, the best threshold of 0 corresponds to *showing ads* for most sessions which results in a net increase in content consumption by 5.2%. This is higher than the net increase in content consumption of 2.1% for a threshold of 9 that corresponds to *not showing ads* for most sessions. This indicates that the decision to show ads for future sessions of current viewers (Holdout 1) under the optimized ad schedule can make viewers better off as compared to a decision to not show ads.

²⁶ It is important to note that I also do not show ads for those sessions for which $\hat{b} > T$ and $\hat{b} < \bar{s}$, i.e., if predicted value of Bingeability is greater than the threshold but less than the recommended spacing, I am unable to show ads.

²⁷ While a 71% increase seems large, it is within the range of the observed data - for Holdout 1, the recommended range of ad exposure is once every 0.01-61.01 minutes (data is 0.00-108.43 minutes) and for Holdout 2 is 0.01-28.94 minutes (data is 0.00-103.38 minutes).

I also consider the impact specifically of allowing pre-roll ads. Casual observation suggests that that it may increase ad exposure but lower content consumption. To test this, I allow for pre-roll ads by modifying the constraint in equation (2.9) to $sn = \hat{b}e$, and then I run the optimization routine followed by the steps outlined in the Decision Support System for a threshold of 0. I find that ad exposure increases substantially (23%) as compared to ad exposure under my recommendation. However, content consumption decreases as compared to my recommendation by about 0.7% across both holdout samples. The decrease in content consumption is driven by the average decrease in mean spacing between pods that results from allowing pre-rolls ads (in addition to mid-roll ads) for the same level of predicted Ad Tolerance. Thus, allowing pre-roll ads results in much higher ad exposure but comes at a cost of a very small reduction in content consumption, a trade-off that a platform may be willing to make.

I also test the performance of a naive heuristic that computes pod spacing as a ratio of the total content time to the total number of pods for a viewer in a given week (see Appendix A.9 for details). The best this heuristic can do is to increase content consumption at the expense of decreasing ad exposure (compared to observed practice) i.e., not delivering a win-win recommendation for the platform and its viewers.

2.7 Conclusion

This essay adds to the small but growing body of work that investigates the implications of increase in consumer control vis-à-vis content consumption on streaming media. To the best of my knowledge, this essay is the first attempt at providing a solution for advertising scheduling in such settings. Specifically, it provides an approach for streaming providers to explore the tradeoff between content consumption and ad exposure in order to provide a balanced viewing experience. The recommendations from this approach are available at the granular level of an individual viewer-session. The approach also uses state-of-the-art methods such as machine learning, but more importantly allows for causal inference via the use of instrumental variables and provides increased interpretability of the estimates.

In the first stage of the three-stage approach, I develop two new metrics – Bingeability and Ad Tolerance – to capture the interplay between content consumption and ad exposure for each session. I need to do this as there is little standardization around the measurement of content consumption and ad exposure in streaming media settings. My metrics are motivated by the consumer psychology literature on flow states and hedonic adaptation as well as observed consumer behavior (in these settings). In the second stage, I first use feature generation to summarize the current and past viewing environment of each consumer over a moving one-week window. I then use a novel tree-based instrumental variable approach to predict the value of the metrics. Using feature importance and partial dependence analyses, I provide insights into the relative importance of various features in predicting viewer consumption

patterns. In the third stage, I pass the predictions from the previous stage through a decision tree and an optimization routine. This is followed by the construction of a decision support system which allows the platform to explore the tradeoff between content consumption and ad delivery for both current and new viewers. The platform can then make choices around its ad schedule for each session given its objective function. It is important to note that “win-win” ad schedules are possible e.g., for current viewers, I am able to find schedules that simultaneously allow for higher content consumption (a 5.2% increase in Bingeability) at higher levels of ad exposure (a 71.2% increase).

My approach could potentially be applied to other ad supported environments, especially where consumers have control over content consumption e.g., news media consumption. My decision support system can also be integrated into an online experimentation platform, where recommendations can be tested in live settings and where the results from experiments can be used to improve the performance of predictive models.

My work does suffer from some limitations. First, while I believe that my approach is general, it is calibrated on data from just one streaming provider. Second, my optimization algorithm simplifies ad scheduling. While it provides conservative results, it can be improved (at the cost of complexity). Third, even though free ad-supported streaming platforms continue to grow, there are now combinations of free/paid ad-supported and paid ad-free models available within the same platform. Figuring out ad scheduling in these settings would necessitate modifications to my approach. Fourth, I cannot link my optimal ad exposure to final purchase due to lack of data. Finally, given the increasing availability of different online streaming options on multiple devices, newer patterns of non-linear consumption could emerge, perhaps requiring the development of other metrics. I hope that future work can address these limitations.

2.8 Tables

Table 2.1: Summary of Sessions

Session (minutes)						
N	Min	2.5%	Median	Mean	97.5%	Max
122,617	0.02	1.82	42.70	56.06	236.51	1573.03

Table 2.2: Example timeline (in minutes) of viewing behavior in a session

24 min episode of Aquarion	0.66	10	0.50	10	0.50	2	2	0.66	21	0.50	0
	10.66		11		2.5		2	17.66		1	
	-----Block 1-----		-----Block 2-----		--Block 3----		B4	-----Block 5-----		---Block 6--	

In the first row, 'light gray shaded boxes' denote *Ad Time*, 'white shaded boxes' denote *Content Time*, and the 'dark gray shaded box' denotes *Filler Content Time*. In the second row, 'white shaded dashed line boxes' denote *Session Time*, and the 'black shaded boxes' indicate the beginning of the next episode. All values are in minutes.

Table 2.3: Computation of the Bingeability Metric

Example	Expression: $\sum_{i=1}^{n_e} \mathbb{1} \left\{ \begin{array}{l} Content Length_i - 5 mins \leq Content Time_i \leq \\ Session Time_i - Ad Time_i \end{array} \right\}$		Bingeability
	No Skipping: $Content Length_i - 5 min \leq Content Time_i$	No Excessive Fast-forwarding: $Content Time_i \leq Session Time_i - Ad Time_i$	
24 min episode of Aquarion	Episode 1: $24 - 5 \leq 22$ Episode 2: $24 - 5 \leq 21$	Episode 1: $22 \leq 24.16 - 1.66$ Episode 2: $21 \not\leq 20.66 - 1.16$	1

Table 2.4: Computation of the Ad Tolerance Metric

Example	Expression: $\sum_{j=1}^{n_p} (PodDuration_j + ConEnd_j - (CalPod_j - PodDuration_{j-1}))$	Ad Tolerance (minutes)
24 min episode of Aquarion	<ul style="list-style-type: none"> Pod 1: $0.66 + (10 + 10 + 2 + 2 + 17 + 0) - (0 - 0) = 41.66$ Pod 2: $0.50 + (10 + 2 + 2 + 17 + 0) - (10.66 - 0.66) = 21.5$ Pod 3: $0.50 + (2 + 2 + 17 + 0) - (11 - 0.50) = 11$ Pod 4: $0.66 + (17 + 0) - (4.50 - 0.50) = 13.66$ Pod 5: $0.50 + 0 - (21 - 0.66) = -19.84$ 	67.98

Table 2.5: Metric Summary Statistics

Viewers	6,157	
TV shows	558	
Sessions	110,500	
	Bingeability (count)	Ad Tolerance (minutes)
Min	0	-412.17
2.5%	0	-24.27
Median	1	23.62
97.5%	5	1178.22
Max	57	63,449.10

Table 2.6a: Current Predictors

Current Variables	No. of features	Description
Viewer ID	6157	Viewer Fixed Effects
Show name	558	Show Fixed Effects
Genre	18	Genre Fixed Effects
Month	5	Month Fixed Effects (Feb, Mar, Apr, May, Jun)
Week	5	Week Fixed Effects {1 (Day 1 to 7), 2 (Day 8 to 14), 3 (Day 15 to 21), 4 (Day 22 to 28), 5 (Day 29 to 31)}
Day	2	Day Fixed Effects (Weekend and Weekday)
Time of Day (cf. Schweidel & Moe, 2016)	5	Time of Day Fixed Effects (Early morning: 7–10am, Day Time: 10am–5pm, Early Fringe: 5pm – 8pm; Prime Time: 8pm – 11pm, Late Fringe: 11pm – 7am)
First Episode Length	1	Episode length of the first episode seen in the session
Number of episodes of the TV show ahead (remaining) in sequence (N_1)	1	Season Number and Episode Number of all the episodes of a TV show establish a chronological order
Number of potentially unwatched episodes of the TV show during my sample period (N_2)	1	Subtracting the number of episodes viewed till date (during the sample period) from the total episodes available in the dataset

Table 2.6b: Functions for watching only TV shows

Functions	No. of features	Description
Bingeability Sum (Show, Day, Time of Day)	8	Sum of (historical) Bingeability of the viewer for that Show over that Day at that Time of day
Bingeability Indicator (Show, Day, Time of Day)	8	Indicator of whether the viewer has <i>Bingeability Sum</i> > 0 for that Show over that Day at that Time of day
Bingeability Session Count (Show, Day, Time of Day)	8	Sum of the number of sessions of the viewer over which Bingeability > 0 for that Show over that Day at that Time of day
Episode Count Sum (Show, Day, Time of Day)	8	Sum of the number of episodes viewed (even partially) by the viewer for that Show over that Day at that Time of day
Episode Session Count (Show, Day, Time of Day)	8	Sum of the number of sessions of the viewer over which Episode Count > 0 for that Show over that Day at that Time of day
Genre Session Count (Day, Time of Day)	4	Sum of the number of sessions over which the viewer has seen that genre over that Day at that Time of day
Episode Revert ²⁸ Count (Show, Day, Time of Day)	8	Sum of the number of times the viewer reverts to an episode that has been watched in the same session for that Show over that Day at that Time of day
Filler Content Count (Show, Day, Time of Day)	8	Sum of the number of filler content episodes (<15 mins in length) viewed (even partially) by the viewer while watching that Show over that Day at that Time of day
Episode Length (Show, Day, Time of Day)	8	Average episode length of the Show viewed by a viewer over that Day at that Time of day

Table 2.6c: Eight features of Bingeability Sum (BS)

Function	Description
<i>Bingeability Sum (Show, Day, Time of Day)</i>	<i>BS</i> for ‘House’ over ‘Weekend’ at ‘Day Time’
<i>Bingeability Sum (__, Day, Time of Day)</i>	<i>BS</i> for any Show over ‘Weekend’ at ‘Day Time’
<i>Bingeability Sum (Show, __, Time of Day)</i>	<i>BS</i> for ‘House’ over any Day at ‘Day Time’
<i>Bingeability Sum (Show, Day, __)</i>	<i>BS</i> for ‘House’ over ‘Weekend’ at any Time of Day
<i>Bingeability Sum (__, __, Time of Day)</i>	<i>BS</i> for any Show over any Day at ‘Day Time’
<i>Bingeability Sum (Show, __, __)</i>	<i>BS</i> for ‘House’ over any Day at any Time of Day
<i>Bingeability Sum (__, Day, __)</i>	<i>BS</i> for any Show over ‘Weekend’ at any Time of Day
<i>Bingeability Sum (__, __, __)</i>	<i>BS</i> for any Show over any Day at any Time of Day

²⁸ Episode Reversion is when, after finishing a few episodes, a viewer starts watching the next episode, but decides to go back and see an episode already seen while staying in the same session. This is different from the more common behavior of rewinding content while watching an episode.

Table 2.6d: Functions for watching TV shows or Movies

Functions	No. of features	Description
Clicks (Title, Day, Time of Day)	8	Sum of ad clicks by the viewer for that Title over that Day at that Time of day
Ad Proportion ²⁹ (Title, Day, Time of Day)	8	Average ad proportion (over all sessions) for the viewer for that Title over that Day at that Time of day
Pod Count (Pod Length, Title, Day, Time of Day)	32	Sum of number of pods of length Pod Length shown to the viewer for that Title over that Day at that Time of day
Pod Session Count (Pod Length, Title, Day, Time of Day)	32	Sum of number of sessions where the viewer was exposed to a given Pod Length for that Title over that Day at that Time of day
Ad Diversity (Title, Day, Time of Day)	8	Average % of unique ads per session (in which ads are shown) for the viewer for that Title over that Day at that Time of day
Pod End ³⁰ (Title, Day, Time of Day)	8	Sum of the number of times a viewer ends a pod before it is finished for that Title over that Day at that Time of Day
Calendar Time Spent (Title, Day, Time of Day)	8	Sum of calendar time (session time) spent watching that Title over that Day at that Time of day
Time Between Sessions (Title, Day, Time of Day)	8	Average time between sessions for the viewer for that Title over that Day at that Time of day
Ad Tolerance Sum (Show, Day, Time of Day)	8	Sum of (historical) Ad Tolerance of the viewer for that Show over that Day at that Time of day
Positive Ad Tolerance Indicator (Show, Day, Time of Day)	8	Indicator of whether the viewer has <i>Ad Tolerance Sum</i> > 0 for that Show over that Day at that Time of day
Positive Ad Tolerance Session Count (Show, Day, Time of Day)	8	Sum of the number of sessions of the viewer over which Ad Tolerance > 0 for that Show over that Day at that Time of day

²⁹ Ad Proportion = Ad Time / (Ad Time + Content Time)

³⁰ A viewer can end a pod (not completely watch it) under a few situations by either ending the session or refreshing the browser or skipping the episode. For a pod to be classified as “ended,” I consider all cases where the viewer watches less than 5 seconds of the Pod Length as a case of Pod End.

Table 2.7: Summary statistics for dataset used in the model

Viewers	5,760	
TV shows	508	
Sessions	105,610	
	Bingeability (count)	Ad Tolerance (minutes)
Min	0	-412.17
2.5%	0	-24.39
Median	1	23.69
97.5%	5	1182.34
Max	57	63,449.10

Table 2.8a: Top 10 sets of predictors of Bingeability

Rank	Predictor / Function	Type	No. of Features	Gain%
1	Bingeability Sum	Past Predictor	8	18.01
2	Number of episodes ahead in sequence (N_1)	Current Predictor	1	17.64
3	Viewer ID	Current Predictor	300	13.09
4	$\widehat{SR}, \widehat{DR}, \widehat{LR}, \widehat{CR}$	Ad Targeting Rules	4	9.04
5	Show name	Current Predictor	102	7.13
6	First Episode Length	Current Predictor	1	6.16
7	Ad Tolerance Sum	Past Predictor	8	5.44
8	Episode Session Count	Past Predictor	6	3.29
9	Genre	Current Predictor	8	3.22
10	Ad Diversity	Past Predictor	7	2.99

Table 2.8b: Top 10 sets of predictors for Ad Tolerance

Rank	Predictor / Function	Type	No. of Features	Gain%
1	Viewer ID	Current Predictor	107	31.03
2	Ad Tolerance Sum	Past Predictor	8	10.26
3	Pod End	Past Predictor	8	9.24
4	$\widehat{SR}, \widehat{DR}, \widehat{LR}, \widehat{CR}$	Ad Targeting Rules	4	8.18
5	Bingeability Sum	Past Predictor	8	6.93
6	Number of episodes ahead in sequence (N_1)	Current Predictor	1	6.91
7	Ad Diversity	Past Predictor	8	4.48
8	Episode Count	Past Predictor	8	3.64
9	Ad Proportion	Past Predictor	8	2.87
10	Pod Count	Past Predictor	25	2.59

Table 2.8c: Gain % of the Ad Targeting Rules

	Bingeability	Ad Tolerance
Spacing Rule \widehat{SR}	2.04	4.26
Length Rule \widehat{LR}	1.43	1.47
Diversity Rule \widehat{DR}	0.77	1.38
Clumpiness Rule \widehat{CR}	4.79	1.06

Table 2.9: Recommendation Summary for Threshold, T=0

Set	Prediction	Holdout 1 % of predictions	Holdout 2 % of predictions	Recommendation
A	Bingeability $< T$	0%	0%	Do not show ads
B	Bingeability $\geq T$ & Ad Tolerance ≤ 0	6.3%	3.3%	Show pods at an interval of a quarter of the episode length
C	Bingeability $\geq T$ & Ad Tolerance > 0	93.7%	96.7%	Solve Optimization

Table 2.10a: Percent change in optimized ad exposure compared to observed ad exposure

Bingeability Threshold (T)	Holdout 1 Future sessions	Holdout 2 New Viewers
9	-99.7%	-99.9%
5	-98.9%	-99.6%
2	-82.3%	-82.8%
1.6	-71.2%	-67.2%
1	-27.4%	-11.7%
0.9	-13.8%	3.6%
0.8	1.3%	19.3%
0	71.2%	79.1%

Table 2.10b: Percent change in optimized Bingeability compared to observed Bingeability

Bingeability Threshold (T)	Holdout 1 Future sessions			Holdout 2 New Viewers		
	Sessions with ads ($\hat{b} \geq T \ \& \ \hat{b} \geq \bar{s}$)	Sessions without ads ($\hat{b} < T \ \ \hat{b} < \bar{s}$)	Net effect	Sessions with ads ($\hat{b} \geq T \ \& \ \hat{b} \geq \bar{s}$)	Sessions without ads ($\hat{b} < T \ \ \hat{b} < \bar{s}$)	Net effect
9	-11.75%	2.31%	2.23%	42.92%	-1.65%	-1.58%
5	3.18%	2.50%	2.51%	-7.93%	-1.35%	-1.41%
2	5.76%	3.26%	3.64%	-5.66%	0.07%	-0.87%
1.6	6.85%	3.07%	3.97%	-5.93%	1.16%	-0.80%
1	2.07%	3.54%	2.72%	-7.71%	5.11%	-3.19%
0.9	2.42%	4.29%	3.05%	-5.82%	3.97%	-3.33%
0.8	2.93%	5.60%	3.55%	-5.37%	6.93%	-3.43%
0	5.31%	222.85%	5.33%	-2.86%	-59.91%	-2.88%

Table 2.10c: Percent change in optimized Bingeability compared to initial predicted Bingeability

Bingeability Threshold (T)	Holdout 1 Future sessions			Holdout 2 New Viewers		
	Sessions with ads ($\hat{b} \geq T \ \& \ \hat{b} \geq \bar{s}$)	Sessions without ads ($\hat{b} < T \ \ \hat{b} < \bar{s}$)	Net effect	Sessions with ads ($\hat{b} \geq T \ \& \ \hat{b} \geq \bar{s}$)	Sessions without ads ($\hat{b} < T \ \ \hat{b} < \bar{s}$)	Net effect
9	-17.35%	2.19%	2.07%	-14.24	0.26%	0.23%
5	-6.21%	2.54%	2.35%	-12.08%	0.52%	0.40%
2	1.06%	3.94%	3.48%	-3.13%	1.74%	0.95%
1.6	2.29%	4.30%	3.80%	-2.32%	2.27%	1.03%
1	0.02%	5.92%	2.56%	-4.89%	4.76%	-1.41%
0.9	0.62%	7.57%	2.89%	-4.24%	6.37%	-1.55%
0.8	1.25%	11.03%	3.38%	-3.68%	9.22%	-1.66%
0	5.16%	61.19%	5.17%	-1.10%	32.76%	-1.09%

2.9 Figures

Figure 2.1: Three-Stage Architecture

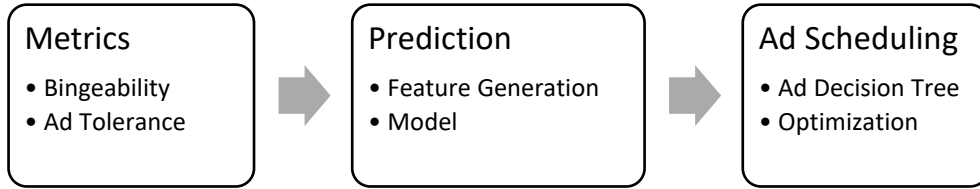


Figure 2.2a: Histogram of Pod Length
(0th to 97.5th percentile)

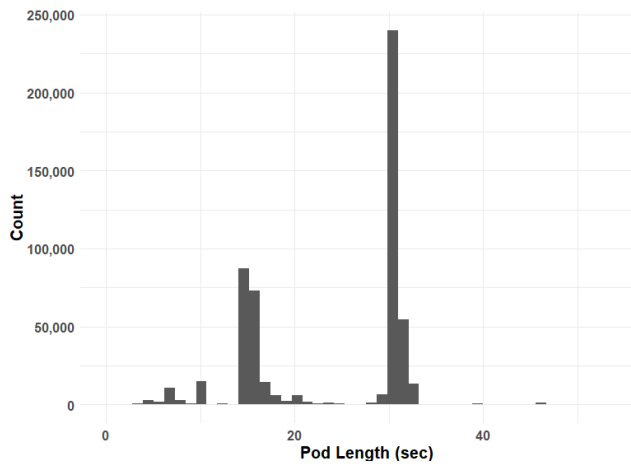


Figure 2.2b: Histogram of Pod Spacing (min)
(0th to 97.5th percentile)

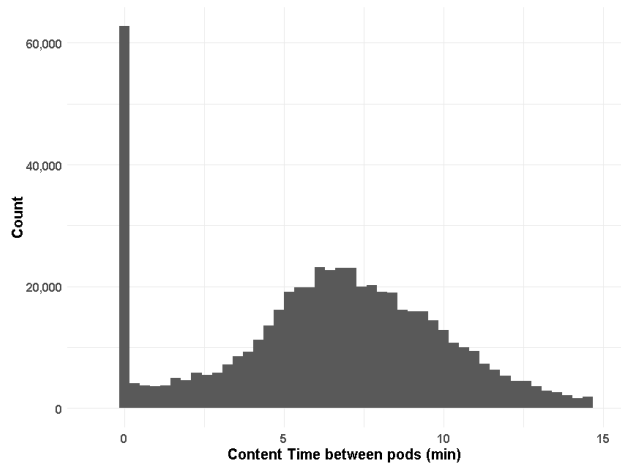


Figure 2.2c: Histogram of Ad Diversity (%)
(0th to 100th percentile)

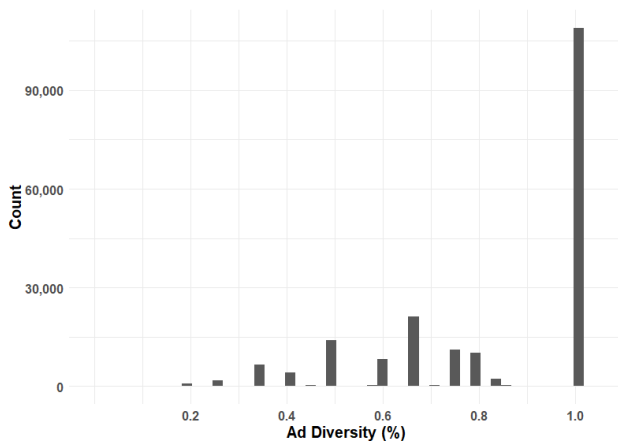


Figure 2.2d: Histogram of Pod Clumpiness
(0th to 100th percentile)

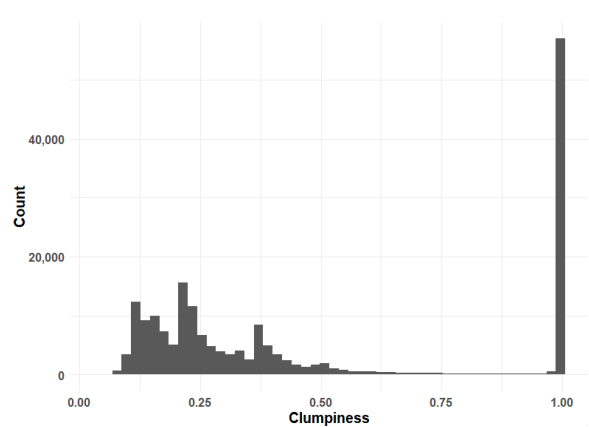


Figure 2.3a: Histogram of Bingeability

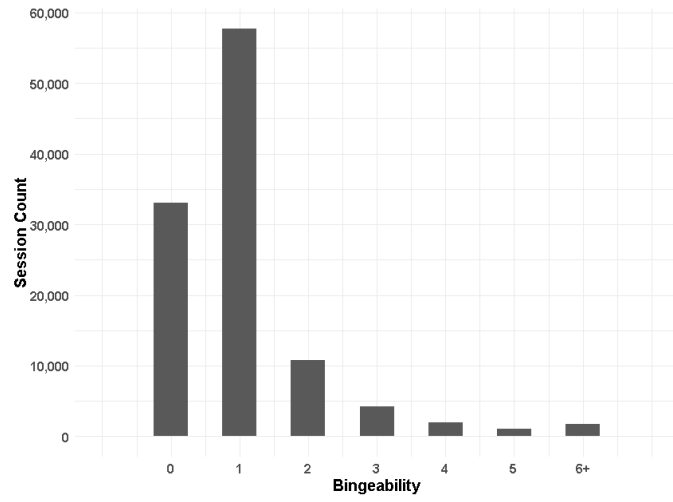


Figure 2.3b: Histogram of Ad Tolerance

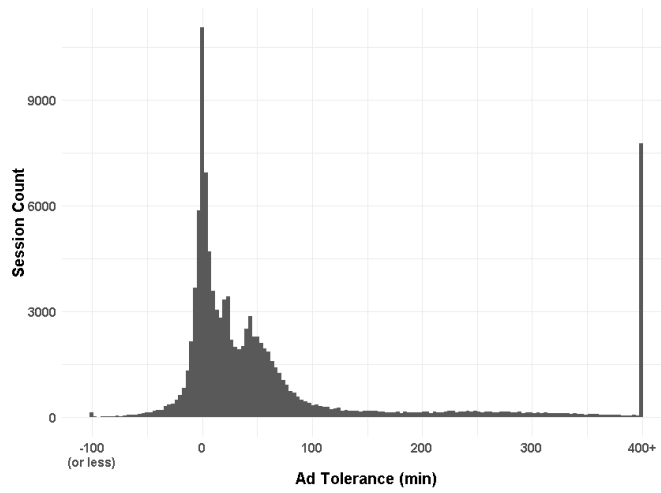


Figure 2.3c: Ad Tolerance vs Bingeability
(0.5th to 99.5th percentile)

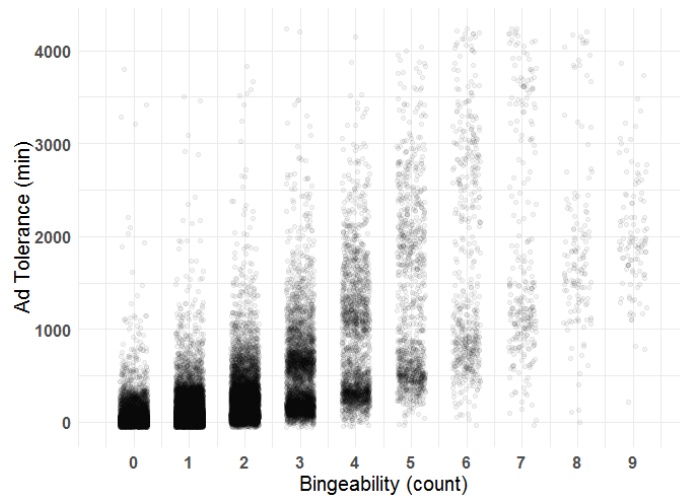


Figure 2.4a: Partial Dependence of Bingeability on Bingeability Sum (same Show, any Day, any TOD)
 (2.5th to 97.5th percentile)

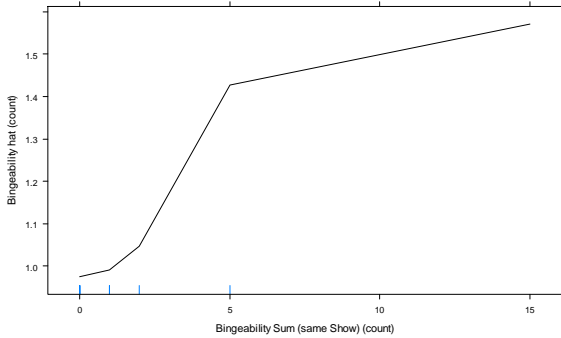


Figure 2.4b: Partial Dependence of Ad Tolerance on Ad Tolerance Sum (same Title, any Day, any TOD)
 (2.5th to 97.5th percentile)

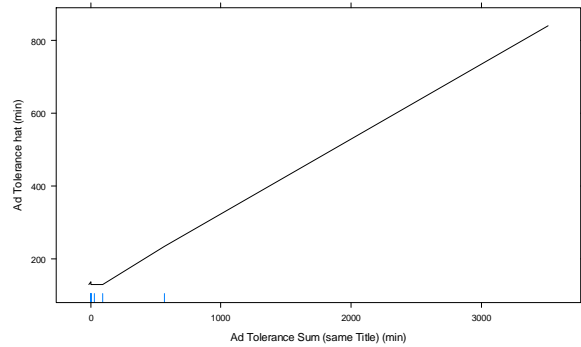


Figure 2.4c: Partial Dependence of \widehat{CR} on Bingeability
 (2.5th to 97.5th percentile)

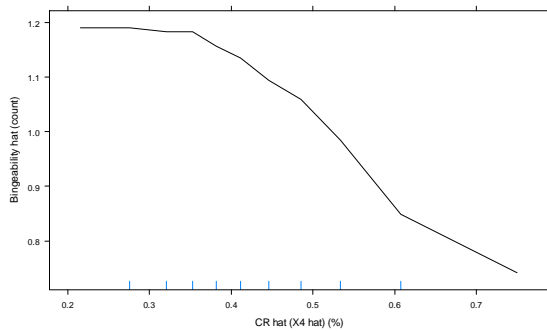


Figure 2.4d: Partial Dependence of \widehat{SR} on Ad Tolerance
 (2.5th to 97.5th percentile)

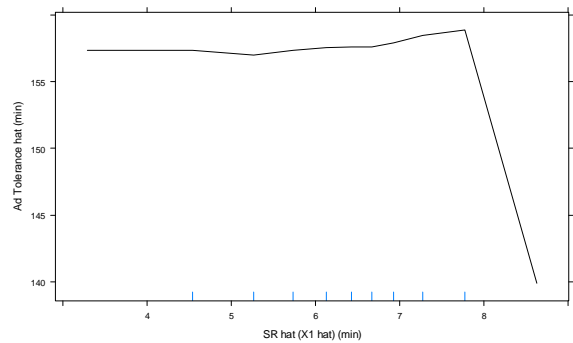


Figure 2.4e: Partial Dependence of Bingeability on its two most important Ad Targeting Rules
 (2.5th to 97.5th percentile)

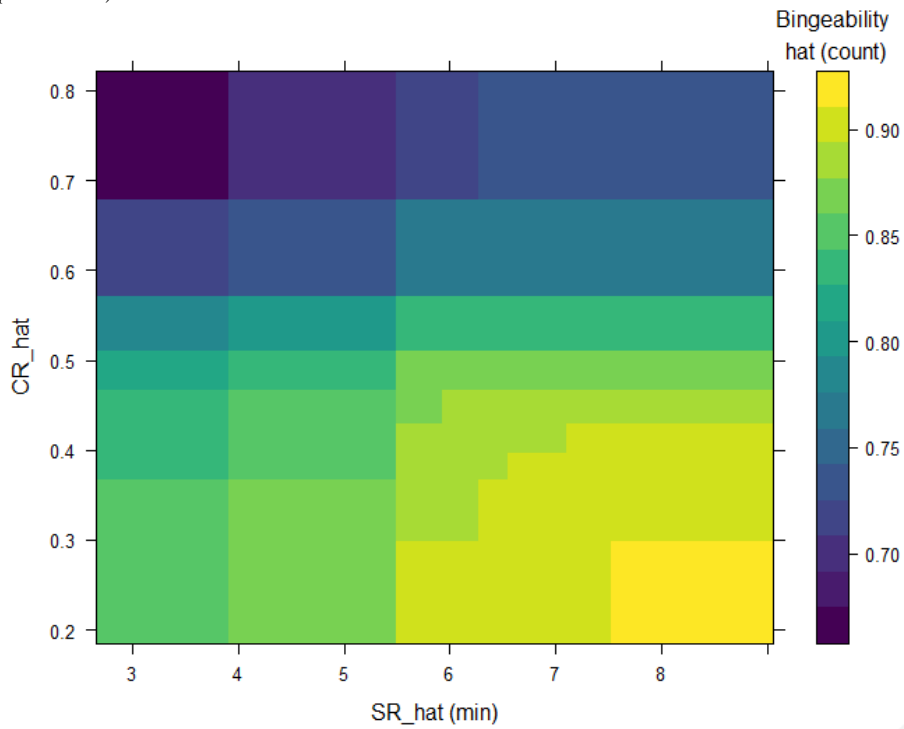


Figure 2.4f: Partial Dependence of Ad Tolerance on its two most important Ad Targeting Rules
 (2.5th to 97.5th percentile)

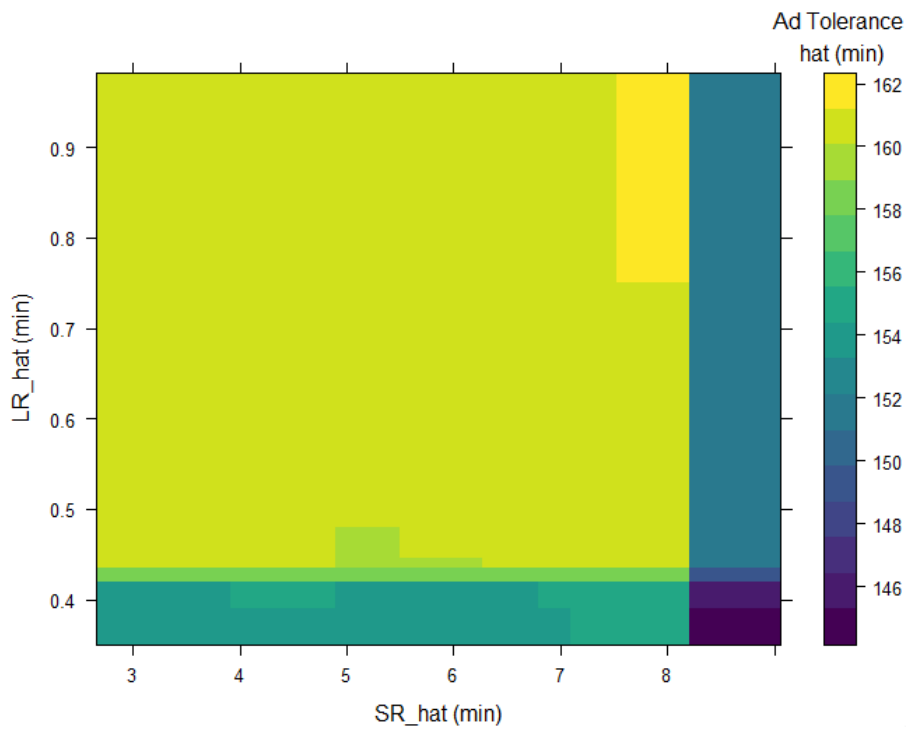


Figure 2.5: Ad Decision Tree

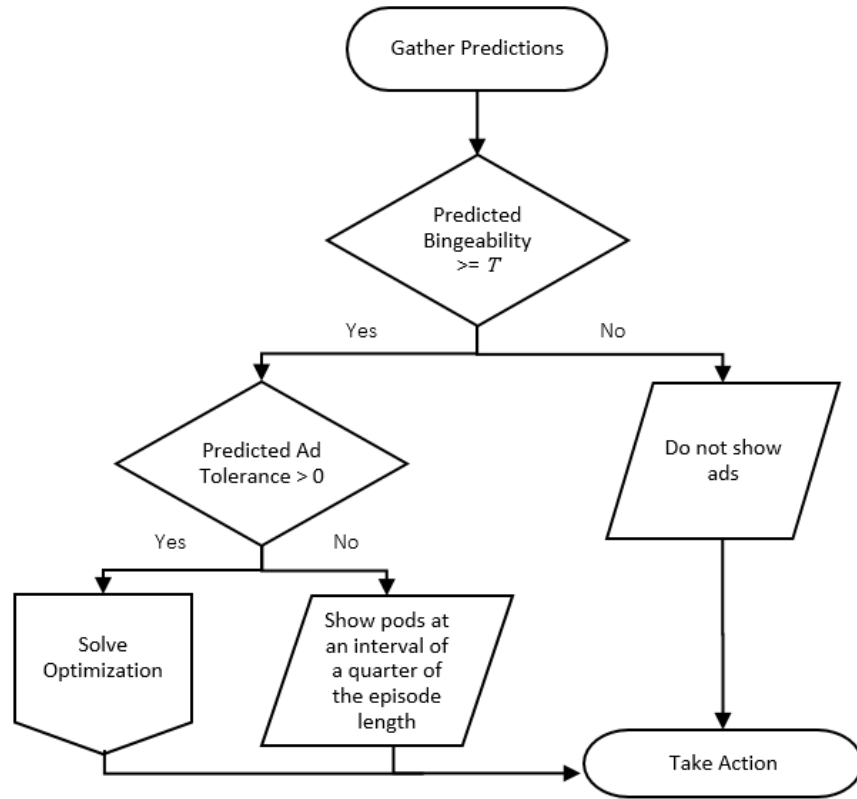


Figure 2.6a: Density of Recommended Spacing in Holdout 1
(2.5th to 97.5th percentile)

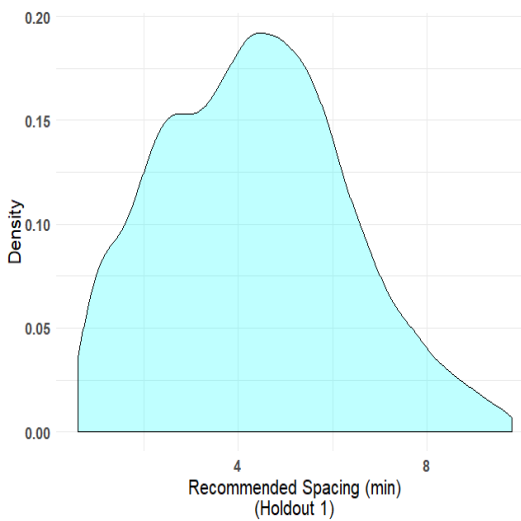


Figure 2.6b: Density of Recommended Spacing in Holdout 2
(2.5th to 97.5th percentile)

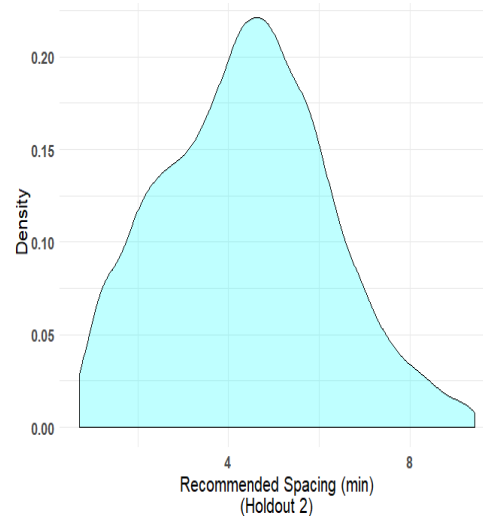


Figure 2.7a: Density of Average Observed Spacing in Holdout 1
(2.5th to 97.5th percentile)

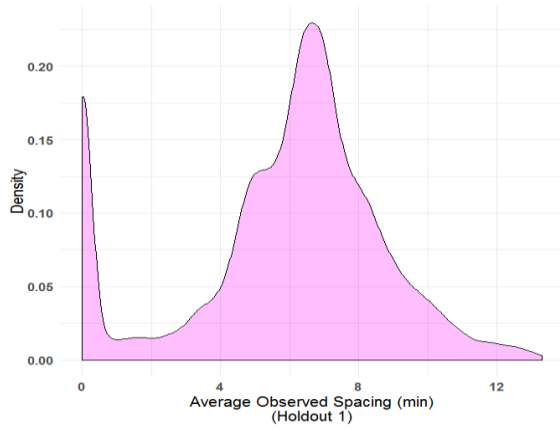


Figure 2.7b: Density of Average Observed Spacing in Holdout 2
(2.5th to 97.5th percentile)

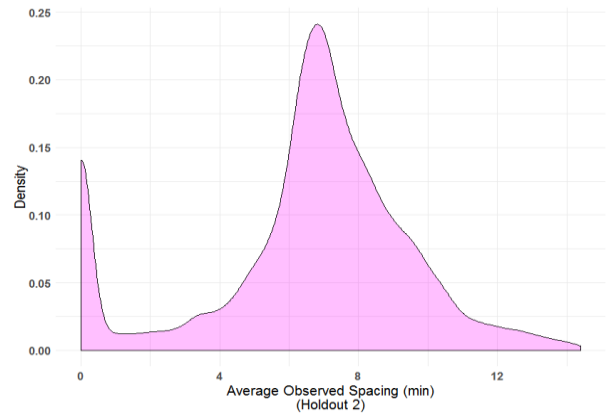


Figure 2.8a: Density of the Ratio of Recommended Spacing and Average Observed Spacing in Holdout 1
(2.5th to 97.5th percentile)

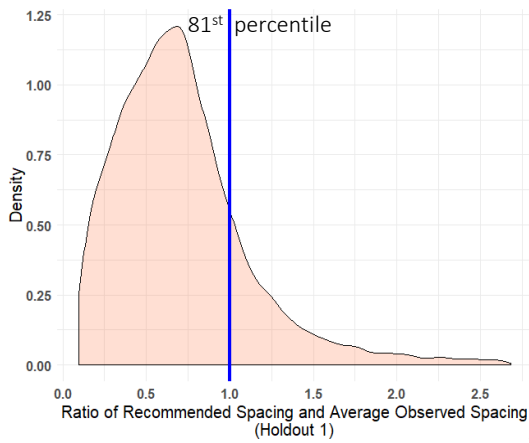


Figure 2.8b: Density of the Ratio of Recommended Spacing and Average Observed Spacing in Holdout 2
(2.5th to 97.5th percentile)

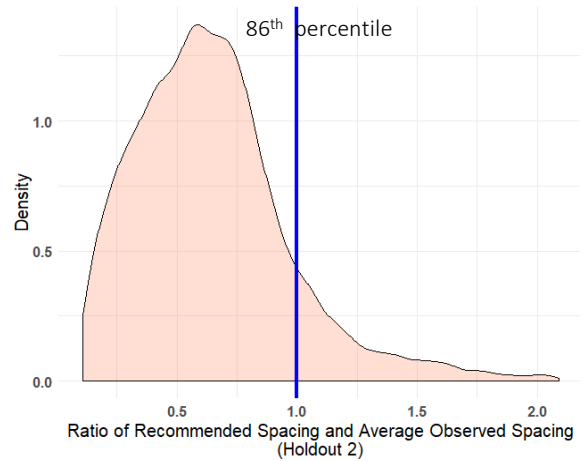


Figure 2.9a: Percentage change in optimized ad exposure (\tilde{n}) as compared to observed ad exposure (n)

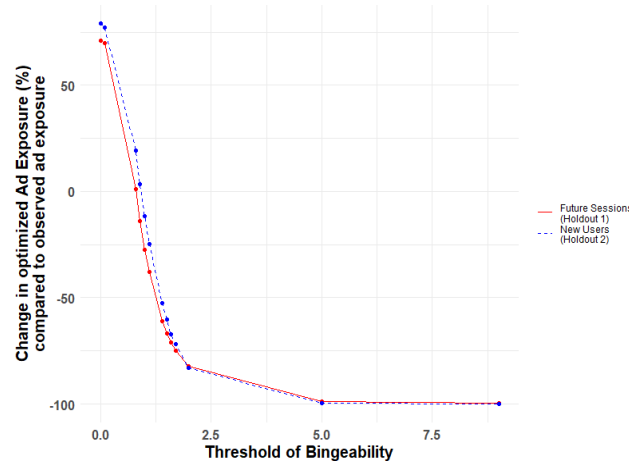


Figure 2.9b: Percentage change in optimized Bingeability (\tilde{b}) for Holdout 1

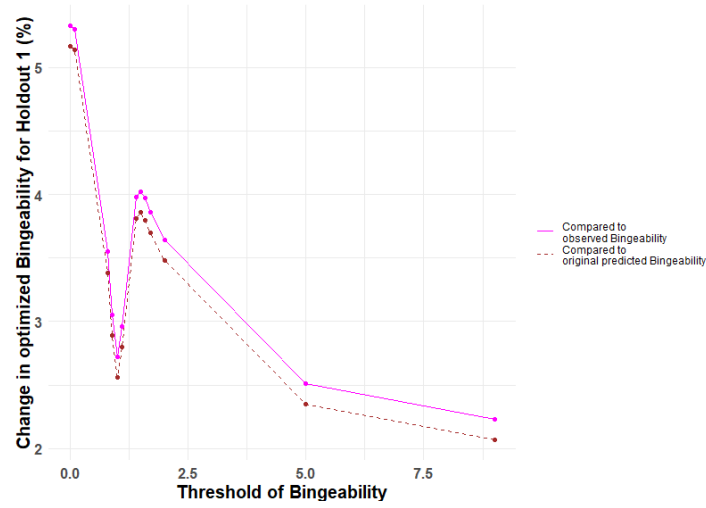
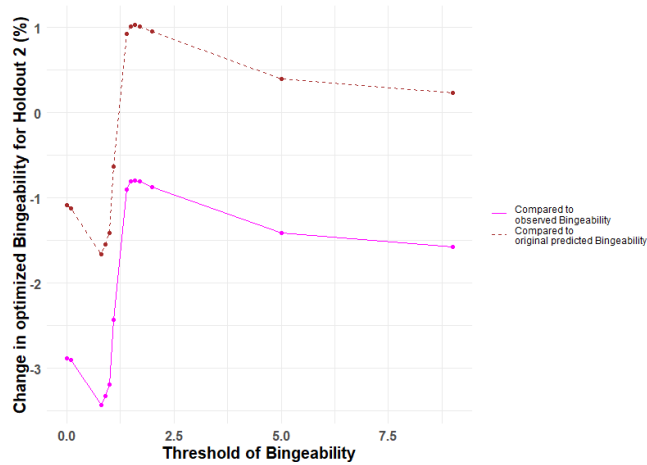


Figure 2.9c: Percentage change in optimized Bingeability (\tilde{b}) for Holdout 2



CHAPTER III - Video Influencers: Unboxing the Mystique

3.1 Introduction

Influencers have the capacity to shape the opinion of others in their network (Oxford Reference, 2020). They were traditionally celebrities (e.g., movie stars and athletes) who leveraged their expertise, fame and following in their activity domain to other domains. However, 95% of the influencers today, or “social media stars,” are individuals who have cultivated an audience over time by making professional content that demonstrates authority and credibility (Creusy, 2016; O'Connor, 2017b). The growth in their audience(s) has been in part attributed to the fact that influencer videos are seen as “authentic” based on a perception of high source credibility. The increasing popularity of social media stars has resulted in an exponential growth of the influencer marketing industry which is expected to reach a global valuation of \$10B in 2020 from \$2B in 2017 (Contestabile, 2018). There are now more than 1100 influencer marketing agencies in the world that allow brands to partner with influencers to promote their products (Influencer Marketing Hub and CreatorIQ, 2020). These influencers primarily reach their audience(s) via custom videos that are available on a variety of social media platforms (e.g., YouTube, Instagram, Twitter and TikTok) (Brooks, 2020). In contrast to conventional advertising videos, influencer videos have emerged as a distinct medium (see Section 3.3.1 for details explaining why). Despite the rapid emergence and growth of influencer videos, there is limited research on their design and effectiveness (or indeed influencer marketing in general). Specifically, little is known about the relationship between video content and viewer reactions as well as the evolution of these videos over time.³¹

In this essay, I investigate whether the presence and nature of advertising content in videos is associated with relevant outcomes (views, interaction rates, and sentiment). There are three main challenges in carrying out these tasks. First, most data in influencer videos are unstructured. In addition, these data span different modalities – text, audio and images. This necessitates the use of state-of-the-art machine learning methods commonly referred to as deep learning. The second challenge arises from the fact that past approaches in marketing using such methods have typically made a tradeoff between predictive ability and interpretability. Specifically, such deep learning models predict marketing outcomes well out-of-sample but traditionally suffer from poor interpretability. On the other hand, deep learning

³¹ The literature on influencer marketing has primarily looked at the effect of textual content in sponsored blog posts on engagement with the post (Hughes et al., 2019) and the effect of outbound activities to other users on increasing follower base (Lanz et al., 2019).

models that use ex-ante handcrafted features obtain high interpretability of the captured relationships but suffer from poor predictive ability. My “interpretable deep learning” approach handles unstructured data across multiple modalities (text, audio and images) while avoiding the need to make this trade-off. Finally, the analysis of unstructured data is computationally very demanding, leading me to use “transfer learning.” I apply my approach to publicly available influencer videos on YouTube (the platform where influencers charge the most per post³² (Klear, 2019)).

My approach helps me identify statistically significant relationships between marketing (brand) relevant outcomes and video elements. The significance of these relationships is supported by a significant change in attention (importance) paid by the model to these video elements. For the outcomes, I use publicly available data to develop metrics based on industry practice (Influencer Marketing Hub and CreatorIQ, 2020) and past research on visual and verbal components of conventional advertising (Mitchell, 1986). These metrics are # views, engagement (#comments / # views), popularity (# likes / # views), likeability (# likes / # dislikes) and sentiment (details are in Section 3.3.3). The influencer video elements I consider are text (e.g., brand names in title, captions/transcript and description), audio (e.g., speech, music, etc.), and images (e.g., brand logos, persons, clothes, etc. in thumbnails and video frames).

As noted earlier, the analysis of videos is computationally demanding, so I use a random sample of 1650 videos in order to interpret the relationship between the video elements and marketing outcomes. These videos are scraped from 33 YouTube influencers who span 11 product categories and obtain revenue from brand endorsements.³³ A concern with the use of my sample size is the possibility of “overfitting.” In order to prevent that, I implement transfer learning approaches (which also have the added benefit of aiding interpretation). Transfer learning approaches, which are applied across all modalities of text, audio and image data, involve using models pre-trained (at a high monetary and computational cost) on a separate task with large amounts of data which are then fine-tuned for my different but related task. This is followed up with an ex-post interpretation step that allows identification of salient word pieces in text, moments in audio and pixels in images.

The focus on interpretation allows me to document some interesting relationships (based on a holdout sample) across all three modalities (while controlling for other variables including influencer fixed effects). First, I find that brand name inclusion, especially in the consumer electronics and video game categories, in the first 30 seconds of captions/transcript is associated with a *significant increase* in attention paid to the brand but a *significant decrease* in predicted sentiment. Second, human sounds, mainly speech (without simultaneous music), within the first 30 seconds are associated with a *significant*

³² An influencer with 1M–3M followers on YouTube can on average earn \$125,000 per post - this is more than twice the earnings from a post on Facebook, Instagram or Twitter (O'Connor, 2017a).

³³ My usage of this data falls within the ambit of YouTube’s fair use policy (YouTube, 2020).

increase in attention, and their longer duration is associated with a *significant increase* in predicted views and likeability. Similarly, music (without simultaneous human sound) within the first 30 seconds is associated with a *significant increase* in attention. However, longer music duration is associated with a *significant decrease* in predicted engagement, popularity and likeability but a *significant increase* in predicted sentiment. Third, larger pictures (of persons as well as clothes & accessories) in five equally spaced video frames (within the first 30 seconds) are associated with a *significant increase* in attention and predicted engagement. Fourth, more animal sounds in the first 30 sec of a video is associated with a *significant increase* in attention and a *significant increase* in predicted likeability. Finally, I also demonstrate that the focus on interpretability does not compromise the predictive ability of my model.

These results are relevant for multiple audiences. For academics, who may be interested in testing causal effects, my approach is able to identify a smaller subset of relationships for formal causal testing. This is done by filtering out more than 50% of relationships that are affected by confounding factors unassociated with attention (importance) paid to video elements. For practitioners, I provide a general approach to the analysis of videos used in marketing that does not rely on primary data collection. For brands, influencers and influencer agencies, my results provide an understanding of the association between video features and relevant outcomes. Influencers can iteratively refine their videos using my model and results to improve performance on an outcome of interest. Brands, on the other hand, can evaluate influencer videos to determine their impact and effectiveness at various levels of granularity (individual video elements, interactions of elements or holistic influence).

Overall, this essay makes four main contributions. First, to the best of my knowledge, it is the first essay that rigorously documents the association between advertising content in influencer videos and marketing outcomes. Second, it presents an interpretable deep learning approach that avoids making a tradeoff between interpretability and predictive ability. It not only predicts well out-of-sample but also allows interpretation and visualization of salient regions in videos across multiple data modalities – text, audio, and images. Third, it generates novel hypotheses between advertising content and a change in the outcome of interest for formal causal testing as noted above. Finally, it provides a comprehensive, data-based approach for marketers (and influencers) to assess and evaluate the quality of videos.

The remainder of the chapter is organized as follows. Section 3.2 discusses the related literature while Section 3.3 describes the institutional setting and data used for analysis. Section 3.4 details the models for analyzing structured and unstructured data. The results are described in Section 3.5 while the implications of my approach and findings for practitioners (influencers and marketers) are described in Section 3.6. Section 3.7 concludes with a discussion of the limitations and directions for future research.

3.2. Related Literature

3.2.1 Influencer Marketing

The nascent literature on influencer marketing has so far focused only on textual data (written text, transcripts, etc.). Hughes et al. (2019) find that high influencer expertise on sponsored blog posts is more effective in increasing comments below the blog if the advertising intent is to raise awareness versus increasing trial. However, influencer expertise does not drive an increase in likes of the sponsored post on Facebook, showing that the type of platform has a role to play in driving engagement. Zhao et al. (2019) study the audio transcript of live streamers on the gaming platform Twitch, and find that lower values of conscientiousness, openness and extraversion but higher values of neuroticism are associated with higher views. Other research, such as Lanz et al. (2019), studies network effects on a leading music platform, and finds that unknown music creators can increase their follower base by seeding other creators with less followers than creators who are influencers (with more followers). My focus is to add to this literature by helping marketers better understand the role of text, audio and image elements in influencer videos.

3.2.2 Unstructured Data Analysis in Marketing via Deep Learning

The use of deep learning methods to analyze unstructured data in the marketing literature has gained increasing prominence in recent years due to its ability to capture complex non-linear relationships that help make better predictions on outcomes of interest to marketers. Marketing research on textual data has used combinations of Convolutional Neural Nets (CNNs) and Long Short-Term Memory Cells (LSTMs) to predict various outcomes including sales conversion at an online retailer (X. Liu et al., 2019), whether Amazon reviews are informative (Timoshenko & Hauser, 2019) and sentiment in restaurant reviews (Chakraborty et al., 2019). Research on image data has also used CNNs but within more complex architectures such as VGG-16 to predict image quality (S. Zhang et al., 2017) or classify brand images (Hartmann et al., 2020), Caffe framework to predict brand personality (Liu et al., 2018) and ResNet152 to predict product return rates (Dzyabura et al., 2018). Past research on both text and image data has found that deep-learning models that self-generate features have better predictive ability than those that use ex-ante hand-crafted features (Dzyabura et al., 2018; Liu et al., 2018; X. Liu et al., 2019). While hand-crafted features suffer from poor predictive ability, they allow interpretability of their effect on the outcome variable. I avoid ex-ante feature engineering of unstructured data, and instead use ex-post interpretation, so that I do not need to make a trade-off between predictive ability and interpretability.

Marketing literature has also worked with video data. Pre-trained facial expression classifiers have been used on images from video frames to infer product preference while shopping (S. Lu et al., 2016). Similarly, hand-crafted video features have been automatically extracted from images, audio and text of projects on the crowd funding platform Kickstarter to study their relationship with project success

(Li et al., 2019). More recently, there has been research that embeds information from different data modalities using deep learning methods to create unified multi-view representations. Combinations of structured data and text have been used to predict business outcomes (Lee et al., 2018); brand logo images and textual descriptions have been combined to suggest logo features for a new brand (Dew et al., 2019); and car designs have been combined with ratings data to suggest new designs (Burnap et al., 2019). In my essay, I do not generate a modality given the other modalities, but instead focus on providing tools to improve each modality and interpreting the association between multiple modalities (text, images and audio) and my outcomes of interest.

3.3 Data

3.3.1 Institutional Setting

As noted earlier, influencer videos have emerged as a distinct marketing medium. They are quite different from conventional advertising videos³⁴ in at least three ways. First, these videos can (and almost always do) contain information that is unrelated to the sponsoring brand(s). This amount of information varies by type of video. On the one extreme are “integrated-advertising” videos (e.g., unboxing videos, hauls, product reviews, etc.) that feature the brand prominently throughout the video; at the other extreme are the “non-integrated-advertising” videos that feature the name of the sponsored brand only in a part of the video in the form of mini-reviews, audio shout outs, product placements or brand image displays (Mediakix, 2020). The latter type of videos includes vlogs, educational videos, gaming videos, etc. that are not directly related to the sponsoring brand(s).

Second, influencer videos are typically much longer than a standard TV commercial especially on platforms such as Instagram and YouTube.³⁵ By making longer videos, influencers stand to gain higher revenue from more mid-roll ad exposures. Furthermore, videos with higher expected watch time are more likely to be recommended to viewers by the YouTube recommendation algorithm (Covington et al., 2016). Hence, influencer video content needs to hold viewer attention for a longer duration so that the video can reach a larger audience, potentially leading to higher word of mouth and content sharing.

Third, influencer videos can be interrupted by traditional ads on YouTube. While YouTube only allows videos that are eight minutes or longer to have mid-roll ads, pre-roll ads can be a part of all influencer videos (Google, 2020c). As advertising is the primary source of revenue for influencers (Zimmerman, 2016), it is common for influencers to enable advertising on their videos, making it likely

³⁴ Past work on characteristics of conventional advertising videos has studied their effect on ad viewing time (McGranaghan et al., 2019; Olney et al., 1991), ad attention (McGranaghan et al., 2019; Teixeira et al., 2010, 2012), ad liking / irritation (Aaker & Stayman, 1990; Pelsmacker & Van den Bergh, 1999) and purchase intent (Teixeira et al., 2014).

³⁵ The median duration of videos across my sample of 1650 videos is 5.3 min which is 10 times longer than the commonly used commercial duration of 30 seconds (W. Friedman, 2017).

for viewers to see traditional-ad-interrupted influencer videos. Given that viewers are exposed to both influencer conveyed advertising and brand conveyed (traditional) advertising during the same viewing experience, the cognitive processing of information conveyed from each source can be quite different.

In addition to the above differences, influencer videos are also perceived to have higher source credibility (Tabor, 2020). Information about the brand is conveyed by an individual with high credibility and expertise in a related subject area, e.g., review of a beauty product coming from an influencer who has demonstrated expertise in the beauty industry.

3.3.2 Video Sample

I focus on 120 influencers identified by Forbes in February 2017³⁶ (O'Connor, 2017b). These influencers obtain revenue from brand endorsements and post mostly in English across Facebook, YouTube, Instagram and Twitter. They span 12 product categories³⁷ (10 influencers in each). I exclude the influencers in the Kids category as YouTube has disabled comments on most videos featuring children. Out of the remaining 110 influencers, I exclude influencers who do not have a YouTube channel. I also use the industry threshold of 1000 followers for a person to be classified an influencer (Maheshwari, 2018) and also exclude one atypical influencer with more than 100M followers. Furthermore, I short-list those influencers who have at least 50 videos so that I can capture sufficient variation in their activity, which leaves me with a pool of 73 influencers. From this pool, I randomly choose 3 influencers per category, which gives a total of 33 influencers³⁸ and a master list of 32,246 videos, whose title and posting time were scraped using the YouTube Data API v3 in October 2019. In addition, I also record the subscriber count for each channel at the time of scraping. From this pool of 33 influencers, I randomly choose 50 public videos for each influencer so that I have a balanced sample of 1650 videos that is feasible to analyze. Excluding videos in which either likes, dislikes or comments were disabled by the influencer(s) leaves me with 1620 videos (all scraped in November 2019). Table 3.1 shows the specific data scraped.

3.3.3 Outcome Variables

The top three ways of measuring influencer marketing success in the industry are conversions, interaction rates and impressions (Influencer Marketing Hub and CreatorIQ, 2020). Unfortunately, conversion data are not publicly available. I capture the remaining two (sets of) variables and in addition also capture sentiment.

³⁶ The criteria used by Forbes to identify these influencers include total reach, propensity for virality, level of engagement, endorsements, and related offline business.

³⁷ The 12 product categories are Beauty, Entertainment, Fashion, Fitness, Food, Gaming, Home, Kids, Parenting, Pets, Tech & Business, and Travel.

³⁸ Three of the randomly chosen influencers had comments disabled on more than 95% of their videos, and hence three other random influencers were chosen in their place from the respective category.

(1) Impressions (Views)

Views are important not only to brands, but also to influencers. Higher views help brands increase exposure levels of their influencer marketing campaign, and help influencers earn more revenue equal to a 55% share of ad CPM³⁹ on YouTube (Rosenberg, 2018). Furthermore, an increase in views is correlated with an increase in channel subscribers,⁴⁰ and higher subscriber count allows the influencer to earn higher CPM rates (Influencer Marketing Hub, 2018) as well as to ex-ante charge higher for a brand collaboration (Klear, 2019; O'Connor, 2017a).

There are a few different ways in which public view counts are incremented on YouTube. First, watching a complete pre-roll ad that is 11 to 30 seconds long OR watching at least 30 seconds of a pre-roll ad that is longer than 30 seconds OR interacting with a pre-roll ad (Google, 2020b). Second, if a pre-roll ad is skipped OR there is no pre-roll ad OR the complete pre-roll ad is smaller than 11 seconds, then watching at least 30 seconds of the video (or the full video if it has a shorter duration) has been historically documented to be the minimum requirement for public view counts to increase (Parsons, 2017).

On average, only 15% of viewers have been typically found to watch 30 seconds of a YouTube pre-roll ad (Influencer Marketing Hub, 2018). Hence, it is likely that most view counts are incremented because of viewing the first 30 seconds of video content. As views are exponentially distributed, I show the distribution of the log of views across my sample of 1620 videos in Figure 3.1. The distribution is approximately normal and ranges from 3.71 to 17.57 with a median of 11.85 (or 140,000 views).

(2) Interaction Rates

Brands care more about interaction rates than views to not only ex-ante decide on a collaboration but also to ex-post measure campaign success (Influencer Marketing Hub and CreatorIQ, 2020). Hence, in addition to using impressions (views) as an outcome of interest, I develop three measures of interaction rates that are captured in publicly available data: (a) engagement = (# comments / # views), (b) popularity = (# likes / # views), and (c) likeability = (# likes / # dislikes). While measuring number of comments and likes is common practice in industry and academia (Dawley, 2017; Hughes et al., 2019), I scale each measure by (number of) views to develop unique measures that are not highly correlated with views,⁴¹ and hence can be used to compare interaction rates for videos with different levels of views. The third metric, (# likes / # dislikes), is unique to YouTube because YouTube is the only major influencer platform in the

³⁹ Median ad CPM rates on YouTube are \$9.88, and form the primary source of revenue for YouTube influencers (Lambert, 2018; Zimmerman, 2016)

⁴⁰ Total views for all videos of an influencer channel are highly correlated with subscriber count for the channel across the 33 influencers in my sample, $\rho = 0.91$.

⁴¹ Across 1620 videos spanning 33 influencers, there is a high correlation between log views and log (comments+1) at 0.91, between log views and log (likes+1) at 0.95 and between log views and log (dislikes+1) at 0.92 (I add 1 to avoid computation of log(0)).

US which publicly displays number of dislikes to the content.⁴² As the three interaction rates are also exponentially distributed, I take their natural log, and add 1 to avoid computation of $\log(0)$ or $\log(\infty)$: (a) $\log \text{ engagement} = \log \left(\frac{\text{comments}+1}{\text{views}} \right)$, (b) $\log \text{ popularity} = \log \left(\frac{\text{likes}+1}{\text{views}} \right)$, and (c) $\log \text{ likeability} = \log \left(\frac{\text{likes}+1}{\text{dislikes}+1} \right)$. The distribution of the log of the interaction rates for the 1620 videos is shown in Figure 3.2a, 3.2b and 3.2c. The distribution of all three interaction rates is approximately normal. Log engagement has a median of -6.21 (or 19 comments per 10K views), log popularity has a median of -3.81 (or 220 likes per 10K views) while log likeability has a median of 3.99 (or approximately 107 likes per dislike).

(3) Sentiment

Past work has found that the visual and verbal components of advertising can have an effect on attitude towards the ad which in turn can have a direct effect on overall brand attitude, including attitude towards purchasing and using the product (Mitchell, 1986). Hence, it is likely that brands would benefit from understanding viewer attitude towards the video as it acts as a proxy for sales. I capture attitude towards a video by measuring the average sentiment expressed in the Top 25 comments below a video using Google’s Natural Language API. Comments below a YouTube video are by default sorted as ‘Top comments’ and not ‘Newest first,’ using YouTube’s proprietary ranking algorithm.⁴³ Note that I do not measure the sentiment in the replies to each of the Top 25 comments because sentiment expressed in the reply is likely to be sentiment towards the comment and not sentiment towards the video.

The Natural Language API by Google is pre-trained on a large document corpus, supports 10 languages, and is known to perform well in sentiment analysis on textual data (including emojis) in general use cases (Hopf, 2020). For comments made in a language not supported by the API, I use the Google Translation API to first translate the comment to English, and then find its sentiment. The sentiment provided is a score from -1 to $+1$ (with increments of 0.1), where -1 is very negative, 0 is neutral and $+1$ is very positive. I calculate the sentiment of each comment below a video for a maximum of Top 25 comments, and then find the average sentiment score.⁴⁴

The distribution of sentiment scores for the 1620 videos is shown in Figure 3.3. It ranges from -0.9 to 0.9 with a median of 0.34 , which I use as a cut-off to divide sentiment in the videos into two buckets – “positive” and “not positive (neutral or negative).” The large peak at 0 is because of 71 videos

⁴² Other influencer platforms either do not allow dislikes to content or only allow content to be marked as ‘not interesting’ which is not publicly displayed.

⁴³ Higher ranked comments (lower magnitude) have been empirically observed to be positively correlated with like/dislike ratio of comment, like/dislike ratio of commenter, number of replies to the comment and time since comment was posted (Dixon & Baig, 2019). Moreover, a tabulation shows that 99% of comments are made by viewers and not the influencer (who owns the channel) and hence I do not separate the two.

⁴⁴ As a robustness check, I use Top 50 and Top 100 comments for a random sample of 66 videos (2 videos per influencer) and also explore use of progressively decreasing weights instead of a simple average. I find that the sentiment calculated using any of these measures is highly correlated with a simple average of Top 25 comments ($\rho \geq 0.88$).

where viewers do not post any comments (even though comment posting has not been disabled by the influencer). I assume that if viewers choose to not post comments below a video, then the sentiment towards the video is neutral (0).

Hence, I have a total of four continuous outcomes and one binary outcome. I find that the Pearson correlation coefficient between all outcomes ranges from 0.02 to 0.66 with a median of 0.20 (absolute value) as shown in Table 3.2, indicating that each measure potentially captures different underlying constructs.

3.3.4 Features

Next, I generate features from the data scraped in Table 3.1 and list them in Table 3.3. As can be seen from the table, I have 33 fixed effects for channel, 11 fixed effects for category, features for video length, tags and playlist information, six time-based-covariates and an indicator variable for whether captions are available for the video. For the video description, a maximum of 160 characters are visible in Google Search and even fewer characters are visible below a YouTube video before the ‘Show More’ link (Cournoyer, 2014). Hence, I truncate each description to the first 160 characters as it is more likely to contribute to any potential association with my outcome variables. Captions are only present in 74% of videos, and for those videos without a caption, I use Google’s Cloud Speech-to-Text Video Transcribing API to transcribe the first 30 seconds of the audio file to English.⁴⁵

I begin by focusing on the first 30 seconds for two reasons.⁴⁶ First, the minimum duration of video content that needs to be viewed for an impression to be registered is 30 seconds, and second, higher computational costs associated with more data in my deep learning models require me to restrict data size to a feasible amount. Similarly, I restrict the duration of the audio file to the first 30 seconds. I use audio data in addition to captions/transcript to analyze the presence of other sound elements such as music and animal sounds. Image data comprise high-resolution images that are 270 pixels high and 480 pixels wide. These images comprise the thumbnail and video frames at 0 sec (first frame), 7.5 sec, 15 sec, 22.5 sec and 30 sec.⁴⁷ I restrict my analysis to the first 30 seconds of the video to be consistent with my analysis of text and audio data, and I consider a maximum of five frames in the first 30 seconds because of computational constraints of GPU memory that can be achieved at a low cost.

I create two additional structured features from the complete description to use for analysis as the complete description is not supplied to the Text model. These features are included as they can lead the

⁴⁵ While most videos have English speech, if the first 30 seconds of audio have only non-English speech or there is only background music/sound, the transcription process results in an empty file. 65% of the 26% of videos that are transcribed result in an empty file.

⁴⁶ Note that as part of my robustness checks, I contrast my approach with the use of data from the middle 30 sec and last 30 sec of the video (see Section 2.5.4).

⁴⁷ As each video can be recorded at a different frame rate or with variable framing rates, I capture the frame equal to or exactly after the specified time point. For example, a video recorded at a fixed rate of 15 frames/sec will have a frame at 7.46 sec and 7.53 sec but not 7.50 sec - so I record the frame at 7.53 sec in place of 7.50 sec.

viewer away from the video. They comprise total number of URLs in description and an indicator for hashtag in description. The first three hashtags used in the description appear above the title of the video (if there are no hashtags in the title), and clicking on it can lead the viewer away from the video to another page that shows similar videos (Google, 2020e).⁴⁸

3.3.5 Brand Usage

I compile a list of popular global brands and a comprehensive list of brands with offices in USA. Three lists of Top 100 Global brands in 2019 are obtained from BrandZ, Fortune100 and Interbrand. To this, I add a list of more than 32,000 brands (with US offices) from the Winmo database. This is further combined with brand names identified by applying Google's Vision API - Brand Logo Detection on thumbnails and video frames (0s, 7.5s, 15s, 22.5s & 30s) in my sample of 1620 videos. From this combined list, I remove more than 800 generic brand names such as 'slices,' 'basic,' 'promise,' etc. that are likely to be used in non-brand related contexts. Using *regular expressions*, I identify a list of 250 unique brands that are used in different text elements of a video: video title, video description (first 160 characters) and video captions/transcript (first 30 sec). The Logo detection API provides a list of 51 unique brands that are used in image elements of the video – thumbnails and video frames. The percentage of videos that have a brand used in each video element is as follows: title – 11.2%, description (first 160 characters) – 36.8%, captions/transcript (first 30 sec) – 17.2%, thumbnails – 1.1% and video frames (across five frames in first 30sec) – 2.6%.⁴⁹ The distribution of the number of brand mentions in each text element is shown in Figure 3.4a, and the number of brand logos in each image element is shown in Figure 3.4b.

I find that brand mentions are most common in the description (first 160 characters), followed by captions/transcript (first 30 sec), and then video title. Moreover, all text elements typically have only one brand mentioned once; the observations where two or more brands are mentioned include cases of the same or a different brand being mentioned again. Similarly, thumbnails and video frames (five equally spaced frames in the first 30 sec) typically have only one brand logo, but they comprise a very small percentage of the total videos in my sample. Overall, I find that my sample of influencers allows me to capture sufficient advertising information in textual data.

Furthermore, the US Federal Trade Commission (FTC) has three main guidelines for influencers. First, influencers need to disclose information about brand sponsorship in the video itself and not just in the description of the video. Second, they are advised to use words such as “ad,” “advertisement,”

⁴⁸ I do not have information on how often a video was recommended to viewers by the YouTube recommendation algorithm. I discuss the potential impact of not observing this feature in Section 2.5.2.4.

⁴⁹ I do not study brand usage in the Top 25 comments below a video as an *outcome variable* because only about 5% of the comments across all 1620 videos have a brand mentioned.

“sponsored” or “thanks to ‘Acme’ brand for the free product” to indicate a brand partnership. Third, it is recommended that they disclose brand partnerships at the beginning than at the end of a video (FTC, 2020). Hence, I check for presence of the words “ad/s,” “advertisement/s,” “sponsor/s” or “sponsored” in the captions/transcript (first 30 sec).⁵⁰ I find that less than 1% of videos make such a disclosure in the first 30 seconds.⁵¹ While it is known that these influencers obtain revenue from brand endorsements (based on Forbes’ selection criteria), the lack of disclosure in every sponsored video prevents me from verifying sponsorship in each video⁵².

3.4. Model

Deep learning models are especially suited to analyze unstructured data (text, audio and images) as they can efficiently capture complex non-linear relationships and perform well in prediction tasks (Dzyabura & Yoganarasimhan, 2018). Figure 3.5a shows the traditional deep learning approach that uses unstructured data (e.g., images from videos) to predict an outcome variable. Features self-generated by deep learning models are known to have better predictive ability than ex-ante hand-crafted features passed to deep learning models (Dzyabura et al., 2018; Liu et al., 2018; X. Liu et al., 2019). This is because ex-ante feature engineering is unable to neither identify a comprehensive set of important features nor capture all the underlying latent constructs. However, hand-crafted features allow interpretability of the captured relationships which is not possible with self-generated features created by traditional deep learning models.

In Figure 3.5b, I show my “interpretable deep learning” approach that avoids ex-ante feature engineering and instead uses ex-post interpretation to allow for both good predictive ability of outcomes and interpretation of the captured relationships. To prevent the model from overfitting when analyzing a moderate sized dataset, I use transfer learning approaches where a model that is pre-trained on a separate task with large amounts of data (at a high cost) can be fine-tuned for my different but related task. This not only helps prevent overfitting but also aids in interpretation of the captured relationships. I use state-of-the-art model architectures with novel customizations that allow visualization of the captured relationships. Next, I describe each of the deep (transfer) learning models in more detail.

⁵⁰ I do not check for the presence of words such as “free” because they are often used in other contexts such as “feel free,” “gluten free,” etc.

⁵¹ YouTube also has guidelines for influencers. It requires all channel owners to check a box in video settings that says ‘video contains paid promotion’ if their video is sponsored (Google, 2020d). If this box is checked, a tag – “Includes Paid Promotion” is overlaid on a corner of the video for the first few seconds when the video is played on YouTube. While information about the presence of this “tag” cannot be scraped or downloaded with the video to the best of my knowledge, manually checking different videos on YouTube in my sample reveals that there is little compliance to this requirement.

⁵² While I do not expect my inability to verify sponsorship in each video to affect my analysis (because the influencers in my sample are known to receive brand sponsorship), this is still a limitation of using publicly available data on YouTube.

3.4.1 Text Model

Text data are analyzed using Bidirectional Encoder Representation from Transformers (BERT) (Devlin et al., 2018), a state-of-the-art NLP model that borrows the Encoder representation from the Transformer framework (Vaswani et al., 2017). The model is pre-trained using Book Corpus data (800M words) and English Wikipedia (2,500M words) to predict masked words in text and the next sentence following a sentence. Devlin et al. (2018) complete the pre-training procedure in four days using four cloud Tensor Processing Units (TPUs). The BERT model is fine-tuned to capture the association with my five outcomes using the framework shown in Figure 3.6.

The model converts a sentence into word-piece tokens⁵³ as done by state-of-the-art machine translation models (Wu et al., 2016). Furthermore, the beginning of each sentence is appended by the ‘CLS’ (classification) token and the end of each sentence is appended by the ‘SEP’ (separation token). For example, the sentence ‘Good Morning! I am a YouTuber.’ will be converted into the tokens [‘[CLS]’, ‘good’, ‘morning’, ‘!’, ‘i’, ‘am’, ‘a’, ‘youtube’, ‘##r’, ‘.’, ‘[SEP]’]. A 768-dimensional initial embedding learnt for each token during the pre-training phase is passed as input to the model, and is represented by the vector x_m in Figure 3.6, where m is the number of tokens in the longest sentence⁵⁴. The token embedding is combined with a positional encoder t_m that codes the position of the token in the sentence using sine and cosine functions (see Devlin et al. (2018) for details). This is passed through a set of 12 encoders arranged sequentially. The output of the ‘CLS’ token is passed through a feed forward layer that is initialized with pre-trained weights from the next sentence prediction task, and has a tanh activation function, i.e. $\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$. This is followed by the output layer, which has a linear activation function, i.e. $linear(x) = x$, for the four continuous outcomes and a sigmoid activation function, i.e. $sigmoid(x) = \frac{e^x}{1 + e^x}$, for the binary outcome sentiment.

In Appendix B.1, I explain the architecture of the Encoders which also contain the self-attention heads. The self-attention heads help the model capture the relative importance between word-pieces while forming an association with the outcome of interest. The three main advantages of BERT over conventional deep learning frameworks such as (Bidirectional) LSTM, CNN and CNN-LSTM that use word embeddings such as Glove and word2vec are as follows: (1) BERT learns contextual token embeddings (e.g., the embedding for the word ‘bark’ will change based on the context in which it used, such that the model can understand whether the word is referring to a dog’s bark or a tree’s outer layer) (2) The entire BERT model with hierarchical representations is pre-trained on masked words and a next

⁵³ I use the BERT-base-uncased model (that converts all words to lower case and removes accent markers) as compared to the cased model, because the uncased model is known to typically perform better unless the goal is to study case specific contexts such as ‘named entity recognition’ and ‘part-of-speech tagging’.

⁵⁴ Rare characters including emojis are assigned an ‘UNK’ (unknown) token and sentences shorter than the longest sentence are padded to the maximum length by a common vector.

sentence prediction task, thus making it suitable for transfer learning; whereas the conventional models only initialize the first layer with a word embedding (3) BERT uses a self-attention mechanism that allows the model to simultaneously (non-directionally) focus on all words in a text instead of using a sequential process that can lead to loss of information. These advantages are reflected in model performance when I compare it with conventional models (combinations of CNN and LSTM) in Section 3.5.1.

3.4.2 Audio Model

Audio data are analyzed using the state-of-the-art YAMNet model followed by a Bidirectional LSTM (Bi-LSTM) model with an attention mechanism, as shown in Figure 3.7. YAMNet takes the Mel-frequency spectrogram of the audio signal as input and passes it through a MobileNet v1 (version 1) model that is pre-trained on the AudioSet data released by Google (Gemmeke et al., 2017; Pilakal & Ellis, 2020). YAMNet predicts sound labels from 521 audio classes⁵⁵ such as speech, music, animal, etc. corresponding to each 960ms segment of the audio file. The features from the last layer of the model, corresponding to the predicted audio classes, are passed through a Bi-LSTM layer with an attention mechanism to capture the sequential structure of sound. The model is then fine-tuned to capture associations with my five outcomes.

Next, I explain the model framework in more detail. As mentioned earlier in Section 3.2, I analyze the first 30 seconds of audio in each video file. Each 30 second audio clip is resampled at 16,000 Hz and mono sound, which results in 480,000 data points for each clip. To summarize the large number of data points, I generate a spectrogram that spans the frequency range of 125 to 7500Hz (note that the 2000-5000 Hz range is most sensitive to human hearing (Widex, 2016)) over which the YAMNet model has been pre-trained. This frequency range is then divided into 64 equally spaced Mel bins on the log scale, such that the sounds of equal distance on the scale also sound equally spaced to the human ear.⁵⁶ Each segment of 960ms from the spectrogram output, i.e., 96 frames of 10ms each with overlapping patches (that have a hop size of 490ms) to avoid losing information at the edges of each patch is passed as input to the MobileNet v1 architecture. The MobileNet v1 (explained in more detail in Appendix B.2) processes the spectrogram through multiple mobile convolutions which results in 521 audio class predictions across 60 moments (time steps) in the clip. The $\langle 521 \times 60 \rangle$ dimensional vector is then passed as input to the Bi-Directional LSTM layer with an attention mechanism (explained in more detail in Appendix B.2). This layer is made Bidirectional to allow it to capture the interdependence between

⁵⁵ The AudioSet data has more than 2 million human-labelled 10 sec YouTube video soundtracks (Gemmeke et al., 2017). Pilakal and Ellis (2020) remove 6 audio classes (viz. gendered versions of *speech* and *singing*; *battle cry*; and *funny music*) from the original set of 527 audio classes to avoid potentially offensive mislabeling. YAMNet has a mean average precision of 0.306.

⁵⁶ The spectrogram uses the pre-trained Short-Term Fourier Transform window length of 25ms with a hop size of 10ms that results in a 2998 x 64 (time steps x frequency) vector corresponding to 30 seconds of each audio clip.

sequential audio segments from both directions. For example, the interdependence between the sound of a musical instrument at 5 seconds and the beginning of human speech at 15 seconds can be captured by the model bidirectionally. I adopt the attention mechanism used for neural machine translation by Bahdanau et al. (2014) to help the Bi-LSTM model capture the relative importance between sound moments in order to form an association with an outcome of interest. The output of the Bi-LSTM with attention mechanism is passed through an output layer which has linear activations for the continuous outcome and sigmoid activation for the binary outcome. I compare the performance of this model framework (Model 3) with a model devoid of the attention mechanism (Model 2) and a model devoid of both the attention mechanism and MobileNet v1 (Model 1), in Section 3.5.1⁵⁷.

3.4.3 Image Model

Individual images are analyzed using the state-of-the-art image model – EfficientNet-B7 (Tan & Le, 2019) that has been pre-trained with “noisy student weights”⁵⁸ (Xie et al., 2019). This model not only has a high Top-5 accuracy on ImageNet (98.1%) but is also known to better capture salient regions of images as it uses compound scaling. It is also a relatively efficient model that uses only 66M parameters (and hence the name EfficientNet) as compared to other high performing models that use 8x times the number of parameters (Atlas ML, 2020). All my images (frames) are at a high resolution of 270 by 480 pixels which is the largest common resolution size available across all thumbnails and video frames in the dataset. Thumbnail images are passed as input to one EfficientNet-B7, and its final layers are fine-tuned to capture relationships with an outcome. The architecture of the EfficientNet-B7, whose main building block is the Mobile Inverted Bottleneck Convolution, is explained in detail in Appendix B.3. I compare the performance of the (pre-trained) EfficientNet-B7 with a 4-layer CNN model in Section 3.5.1.

As mentioned in Section 3.3, I analyze a maximum of five video frames in the first 30 seconds of each video, i.e., frames at 0s (first frame), 7.5s, 15s, 22.5s and 30s. Each image frame $i = 1$ to m , where m has a maximum value of 5, is passed through an EfficientNet-B7 model, and then the outputs from all the models are combined before passing it through an output layer. This is illustrated using the diagram in Figure 3.8.

⁵⁷ New methods to recognize speech from unlabeled audio data (using unsupervised learning) such as wav2vec have also been recently developed which can be used in applications where labelled data is not available (Schneider et al., 2019).

⁵⁸ Xie et al. (2019) learn these weights by first pre-training the model on more than 1.2M labelled images from the ImageNet dataset (Russakovsky et al., 2015), and then use this trained model as a teacher to predict labels for a student model with 300M unlabeled images from the JFT Dataset (Xie et al., 2019). The two models are then combined to train a larger student model which is injected with noise (e.g., dropout, stochastic depth and data augmentation), and is then used as a teacher to predict labels for the original student model. This process is then iterated a few times to produce the EfficientNet-B7 model with pre-trained weights.

I compare the performance of four different ‘combination architectures’ that combine the outputs from each EfficientNet-B7. Two of the architectures are the best performing ones in Yue-Hei Ng et al. (2015), namely *Bi-LSTM*⁵⁹ and Max Pooling followed by Global Average Pooling (*Max-GAP*). The remaining two architectures are variants not tested by Yue-Hei Ng et al. (2015), namely Global Average Pooling followed by Max Pooling (*GAP-Max*) and Concatenation of Global Average Pooling (*C-GAP*). The Bi-LSTM architecture captures sequential information across the video frames, while the remaining three architectures preserve the spatial information across the video frames. The output of the combination architecture is passed through an output layer which has linear activations for the continuous outcome and softmax activation for the binary outcome. I explain the combination architectures in more detail in Appendix B.3.

3.4.4 Combined Model

I use the framework shown in Figure 3.9 to combine information from each of the unstructured models with the structured features, X_{it} , listed earlier in Table 3.3. The predicted outcome values, \hat{Y}_{it} for video t by influencer i , from the best performing model for each unstructured feature, are fed into the combined model in addition to the structured features, X_{it} . This can also be represented by the following equation:

$$Y_{it} = g\left(X_{it}, \hat{Y}_{it}^{Title}, \hat{Y}_{it}^{Description}, \hat{Y}_{it}^{Caption/Transcript}, \hat{Y}_{it}^{Audio}, \hat{Y}_{it}^{Thumbnail}, \hat{Y}_{it}^{Video\ Frames}\right) + \epsilon_{it} \quad (3.1)$$

where Y_{it} is the observed outcome for video t by influencer i , g is the combined model used and ϵ_{it} is the error term. I test the performance of seven different combined models in Section 3.5.1. The combined models comprise four commonly used linear models – OLS⁶⁰, Ridge Regression, LASSO and Elastic Net, and three non-linear models – Deep Neural Net, Random Forests and Extreme Gradient Boosting (XGBoost) – that are known to capture non-linear relationships well.

3.5 Results

In this section, I first detail the results on prediction and then on interpretation. I then dig deeper to see if I find patterns consistent with influencers “learning” about what makes their videos more engaging. I also carry out a robustness check where I estimate my model on video slices from the middle and end of videos as opposed to the beginning.

⁵⁹ While Yue-Hei Ng et al. (2015) use the LSTM approach, I use the Bidirectional LSTM (Bi-LSTM) as it can only perform better than LSTM.

⁶⁰ I drop the multicollinear category fixed effects in OLS. I retain these fixed effects in the other models so that I can capture their relative importance with influencer fixed effects.

3.5.1 Prediction Results

I divide my random sample of 1620 videos into a 60% training sample (972 videos), 20% validation sample (324 videos) and 20% holdout sample (324 videos). I train the model on the training sample, tune the number of steps of Adam gradient descent on the validation sample, and then compute model performance on the holdout sample.⁶¹ First, I compare the predictive performance of each model with benchmarks models for the continuous outcome (views) and binary outcome (sentiment), and then apply the best performing model on the other three continuous outcomes (interaction rates).⁶² In Appendix B.4, I compare my models with various benchmarks used in marketing literature. The Text model (BERT) performs better than benchmarks such as LSTM, CNN (X. Liu et al., 2019), CNN-LSTM (Chakraborty et al., 2019) and CNN-Bi-LSTM. The Audio model (YAMNet+Bi-LSTM+Attention) performs better than benchmark models devoid of the attention mechanism, thus demonstrating the benefit of capturing relative attention weights. The Image model (EfficientNet-B7) performs better than a conventional 4-layer CNN. Furthermore, the Bi-LSTM architecture which captures the sequential information from video frames performs better than other models that capture only spatial information.⁶³ Overall, I demonstrate that my models perform better than benchmark predictive models in the marketing literature and thus I do not compromise on predictive ability.

I also compared the performance of BERT with RoBERTa (Robustly Optimized BERT Pretraining Approach) (Y. Liu et al., 2019). RoBERTa is pre-trained for a longer duration, on bigger batches, with more data, on longer sequences, and with dynamic masking. I find that the change in out-of-sample predictive performance between RoBERTa and BERT ranges from -5% to +8% for all five outcomes using Title or Transcript. Overall, as performance change can be either negative or positive, RoBERTa does not always perform better than BERT in this setting. Furthermore, as the percentage differences are small, this suggests that the performance of both models is comparable in my setting and are not significantly different from each other. I was unable to analyze description (first 160c) with the RoBERTa model using a 16GB GPU because of increase in computational complexity. The number of tokens required to represent the longest first 160 characters of description increased to 314 in RoBERTa from 124 in BERT. This is primarily due to increase in tokens used to represent emojis – while BERT assigned an “unknown token” to each emoji, RoBERTa assigns two or more tokens for each emoji.

⁶¹ I carry out my analysis using one NVIDIA Tesla P100 GPU (with 16GB RAM) from Google. The predictions results are found by averaging the results over three run times of the model. It is important to note that the results are very close to each other during each run time which demonstrates robustness of the results to the random starting weights chosen by the model during each run time. Other parameters – learning rate and batch size – are chosen such that the model results are obtained in a reasonable run time of less than 30 minutes.

⁶² I do not use a Multi-Task Learning (MTL) approach to simultaneously predict all five outcomes for two reasons. First, my final goal is to interpret the relationship between each individual outcome and video data (detailed in Section 5.2), which will not be possible with a MTL approach. Second, there is low to moderate correlation between all five outcomes as shown earlier in Table 2.2, which suggests that each outcome is capturing different underlying constructs.

⁶³ I also find that using five frames results in slightly improved performance than a model that uses only three or two frames.

However, given the results obtained with Title (which has emojis) does not substantially change between RoBERTa and BERT, I do not expect the results with Description (160c) to substantially change between the two models as well. As the predictive results of RoBERTa are not always better than BERT, I do not analyze the results from RoBERTa for interpretation in Section 3.5.2.

Table 3.4 summarizes the results from the best performing models for each component of unstructured data, which are now applied to all five outcomes. The Text model (BERT) predicts all the continuous outcomes with a low RMSE, (e.g., Title can be used to predict views within an average RMSE range of $\pm e^{1.66} = \pm 5.26$ views) and the binary outcome with moderately high accuracy (e.g., Title can predict sentiment with an accuracy of 72%). The Audio model can make predictions at a slightly poorer level of performance than the Text model. The Thumbnail model is unable to predict the continuous outcomes as well as the Text and Audio Model but performs better than the Audio model in predicting sentiment. The Video Frames model performs better than the Thumbnail model but poorer than Audio and Text models in predicting the continuous outcomes but performs comparably with the Thumbnail model in predicting sentiment. Overall, the prediction results show low RMSE that ranges from 0.71 to 3.09 when predicting the (log transformed) continuous outcomes (views, engagement, popularity and likeability) and moderately high accuracies ranging from 65% to 72% when predicting sentiment.

The results of the Combined Model used in Section 3.4.4 demonstrate that Ridge Regression has the best performance on the holdout sample for all the continuous outcomes (lowest RMSE) and also the binary outcome (highest accuracy) (see Appendix B.4 for details). This suggests that structured features do not have substantial non-linear interactions with each other or with the predictions from the Text, Audio and Image models⁶⁴.

Moreover, I find that the combined model of Ridge Regression has lower RMSE or higher accuracy than the results of the individual models in Table 3.4, suggesting that the holistic influence of all features is better than the individual influence of each unstructured feature. Next, I take the magnitude of each estimated coefficient from the Ridge Regression model applied on the training sample and scale it by the sum of the magnitude of all coefficient values which gives me the percentage contribution of each feature. I thus capture the relative importance or predictive power of a feature for each of the outcomes of interest while controlling for the presence of other features. The importance of each feature set is shown in Table 3.5.⁶⁵

⁶⁴ Note that the features used in Ridge Regression do not include interactions. An alternative reason for Ridge Regression performing better than non-linear models could be the limited number of structured features used in the model (as shown in Tab 3.3). Addition of more structure features (if available) may result in non-linear models performing better at prediction.

⁶⁵ Note that I scale all the features by their $L2$ norm before running the model so that I can make relative comparisons. Also, I sum up the coefficient values that lie within a class (e.g. sum up the coefficient values of influencer fixed effects, sum up the coefficient values of features of playlist information, etc.) to get an overall picture of the contribution of a class of features in predicting an outcome of interest.

I highlight the unstructured features in gray. Title, description (first 160 characters) and captions/transcript (first 30 sec) contribute relatively more than the other unstructured features in predicting all five outcomes. The ordering of relative influence, where I control for the presence of other structured and unstructured features, is the same as my finding in Table 3.4 where I do not control for the presence of other features. However, the results of the combined model especially allow me to make relative comparisons between outcomes. I find that title and description (first 160 characters) contribute most towards predicting engagement; captions/transcript (first 30s) contribute most towards predicting popularity, whereas thumbnail, audio (first 30s) and video frames (0s,7.5s,15s,22.5s,30s) contribute most towards predicting sentiment.

3.5.2 Interpretation Results

In this section, I interpret the best performing transfer learned deep learning models in order to identify important video elements that can potentially have a causal impact on marketing outcomes. I interpret results using predictions on the holdout sample, and not the training sample, so that the identified relationships are more likely to generalize out-of-sample. On the holdout sample, I focus on the following video elements in unstructured data. First, I focus on brand presence in text as it is of interest to brand sponsors and because past literature on influencer videos has not studied this (as mentioned earlier in Section 3.2.1). Second, I study audio elements such as duration of speech, music, and animal sounds. As past advertising literature has found that ads featuring animals and those using voice-over and music reduce irritation towards the ad (Pelsmacker & Van den Bergh, 1999), I study the role of these audio elements in influencer videos. Similarly, I study image elements such as size of brand logos, clothes and accessories and persons as it is of interest to brand sponsors and has not been studied in past influencer marketing literature.

I divide my interpretation strategy into two steps to eliminate spurious relationships and visually illustrate this in Figure 3.10. In Step 1 (Attention or Importance), I first capture the attention weights (gradients) attributed to the video elements in each deep learning model while making predictions on a holdout sample. For example, the predicted attention weight for token j in the captions in video t capture the relative weight attributed to that token in video t while predicting an outcome. These weights for video t sum up to one, and hence capture the relative importance for each token. A higher attention weight can be thought of in econometrics terms as capturing the strength of the marginal effect. Hence, a token with higher attention weight would capture more of the variance in the outcome. I regress these attention weights on the video elements to determine whether the presence of a video element has a significant positive relationship (significant relationship for gradients) with the predicted attention weight. This allows me to identify important elements. However, finding important elements here need not

indicate that they have a causal impact on the outcome because of potential spurious relationships captured by the model (Vashishth et al., 2019). Hence, the captured associations need not always be intrinsically valid.

In Step 2 (Correlation), I regress the predicted outcome from each deep learning model on the video elements. I use predicted outcomes and not observed outcomes in the holdout sample because the predicted outcomes have been influenced by the attention weights (gradients) and hence are comparable with the analysis in Step 1⁶⁶. However, finding significant relationships here need not mean that the elements are important in order to predict the outcome because of confounds unassociated with attention paid to video elements. Hence, I find relationships that fall at the intersection of Step 1 and Step 2. Doing so allows me to identify relationships between video elements and outcomes that are also supported by a significant change in attention to video elements. Thus, I am able to generate a smaller set of hypotheses for formal causal testing⁶⁷. Next, I detail my interpretation strategy using the results from the Text, Audio and Image models.

3.5.2.1 Interpretation: Text Model

I average the output across all the attention heads in the last encoder of the BERT model, which results in an attention vector of dimension $\langle 324, k, k \rangle$ where 324 is the number of observations in the holdout sample, and $\langle k, k \rangle$ corresponds to k weights for k tokens, where k equals the maximum number of tokens for a covariate type – title, description (first 160 characters) or captions/transcript (first 30s). As mentioned in Section 3.4.1, the first token for each example is the ‘CLS’ or classification token. I am interested in the attention weights corresponding to this token because the output from this token goes to the output layer (as shown earlier in Figure 3.6). Thus, I get at an attention weight vector of dimension $\langle 324, k \rangle$, where each observation has k weights corresponding to the ‘CLS’ token. Note that the sum of the relative attention weights for each observation is one.

After finding the predicted attention weights in the holdout sample, I implement Step 1 where I run a regression of the predicted attention weights on brand presence to answer the following question:

1) Brand Attention: Do brand names receive more attention?

$$\log(\text{AttentionWeight}_{itj}) = \alpha_i + \gamma X_{it} + \beta_1(\text{BIT}_{itj}) + \beta_2(\text{LOTX}_{it}) + \beta_3(\text{TP}_{itj}) + \epsilon_{itj} \quad (3.2)$$

where, $\text{AttentionWeight}_{itj}$ is the weight for token j (excluding ‘CLS’, ‘SEP’ and padding tokens) in video t made by influencer i , α_i is influencer fixed effect, X_{it} is the same vector of structured features

⁶⁶. Furthermore, the low RMSE values and moderately high accuracies (found in Section 2.5.1) do not preclude the use of predicted outcomes for analysis.

⁶⁷ Alternative approaches for interpretation such as LIME (Local Interpretable Model Agnostic Explanations) can be used when engineered features are supplied ex-ante to a deep learning model. However, as I am carrying out ex-post interpretation, LIME cannot be applied in this case.

used earlier in equation (3.1)⁶⁸, and ϵ_{itj} is the error term. BIT_{itj} is a ‘Brand Indicator in Token’ variable denoting whether token j used by influencer i in video t is a part of a brand name, $LOTX_{it}$ is the Length Of Text in video t made by influencer i , and TP_{itj} is the Token Position of token j used by influencer i in video t . In addition to studying main effects in equation (3.2), I also study interaction effects in Appendix B.5.

While equation (3.2) helps study the effect of brand presence on attention to the token, I also want to study the association between brand presence and the five outcomes of interest. Now, the predicted outcomes from the BERT model would have been influenced by the relative attention weights between words. Hence, in Step 2, I run a regression to answer the following question:

2) Brand Presence: Is brand presence associated with the predicted outcome?

$$PredictedOutcome_{it} = \alpha_i + \gamma X_{it} + \beta_1(BITX_{it}) + \beta_2(LOTX_{it}) + \epsilon_{it} \quad (3.3)$$

where, $BITX_{it}$ is a ‘Brand Indicator in Text’ variable denoting whether the text in video t by influencer i has a brand, and ϵ_{it} is the error term. I study interaction effects in Step 2 in Appendix B.5. The values of the coefficients of interest in each of the above equations are shown in Table 3.6.

The table reflects results corresponding to each type of unstructured text data – Title, Desc (first 160 characters of description) and Tran (first 30 sec of captions/transcript), and the model for each of the five outcomes – views, sentiment, engagement, popularity and likeability. The values in the table reflect a percent change in the non-log-transformed outcome (e.g., views and not $\log(\text{views})$) when a covariate is present.⁶⁹ Significant results are suffixed by * ($p < 0.05$) and weakly significant results ($0.05 \leq p < 0.1$) are suffixed by W.

I highlight the cells in gray that correspond to both (a) a positive and significant effect on attention weights and (b) a significant effect associated with the predicted outcome. Such a two-step comparison allows me to filter out significant relationships confounded by factors unrelated to brand attention. Doing so allows me to identify relationships that are more likely to have causal effects when tested in the field. I find two main effects that are significant in both steps. First, brand mention in description (first 160 characters) is associated with an increase in attention and an increase in predicted views. Second, brand mention in captions/transcript (first 30s) is associated with an increase in attention but negatively associated with predicted sentiment. However, I do not find any significant evidence to show that the effect of brand mentions can vary based on length of text or its position in the text (see Appendix B.5).

⁶⁸ Note that I do not include category fixed effects in the linear regression to avoid multicollinearity with influencer fixed effects.

⁶⁹ Note that I run a logistic regression for sentiment instead of a linear regression (in Section 2.5.2.1, 2.5.2.2 and 2.5.2.3).

Next, I illustrate an example of how text data in a video in the holdout sample can be visually interpreted. In Figure 3.11, I show the attentions weights on the captions/transcript (first 30s) from a video of a tech & business influencer. The words are tokenized into word-pieces in the figure as done by the model, and a darker background color indicates relatively higher attention weights. As can be seen in Figure 3.11, on average more attention is paid to the brand ‘iphone’ than other tokens in the text.⁷⁰ The model predicts a ‘not positive’ sentiment for this clip, and this matches the observed sentiment as well. These findings can help influencers design content and test it to obtain causal effects in a field setting. Similarly, brands can evaluate content using these findings to determine sentiment.

3.5.2.2 Interpretation: Audio Model

The YAMNet model (Mel Spectrogram + MobileNet v1) finds the predicted probability of each moment of the 30 second audio clip belonging to 521 sound classes. A 30 second audio clip has 60 moments, where each moment is 960ms long, and the subsequent moment begins after a hop of 490ms. I divide the 521 sound classes into 8 categories based on the AudioSet ontology (Gemmeke et al., 2017) – Human (58.1%), Music (29.1%), Silence (3.5%), Things (0.7%), Animal (0.6%), Source Ambiguous (0.1%), Background (0.1%) and Natural (0.1%), where the percentage in brackets indicate the percentage of moments across my sample of 97,200 moments (1620 videos x 60 moments) that contain a sound of that category with probability greater than half. Note that 10.9% of moments are unclassified by the model; in addition, the same moment can be classified into multiple categories if sounds from two or more categories occur at the same moment (e.g., human speech while music is playing). The Audio Model – YAMNet + Bi-LSTM with attention, gives me 60 attention weights corresponding to each moment. Note that the sum of the relative attention weights for each observation is one. In Step 1, I run a regression of the predicted attention weights in the holdout sample to answer the following question:

1) Do certain moments of sound receive more attention?

$$\log(\text{AttentionWeight}_{itj}) = \alpha_i + \gamma X_{it} + \sum_{z=1}^8 \beta_{1z} (CI(z)_{itj}) + \beta_2 (CI(\text{Human})_{itj} \times CI(\text{Music})_{itj}) + \beta_3 (\text{Location}_{itj}) + \epsilon_{itj} \quad (3.4)$$

where, $\text{AttentionWeight}_{itj}$ is the weight for moment j in video t made by influencer i , α_i is influencer fixed effect, X_{it} is the same vector of structured features used earlier in equation (3.2), $z = 1$ to 8 corresponds to the 8 sound categories, $CI(z)$ is the Category Indicator for category z in moment j , and $CI(\text{Human}) \times CI(\text{Music})$ corresponds to moments when both Human and Music sounds occur together,

⁷⁰ Note that the model pays different attention to the word ‘the’ based on the context in which it is used.

and *Location* corresponds to location of the moment within the 60 moments of the audio clip, and ϵ_{itj} is the error term.

Next in Step 2, I examine whether these moments of sound have a significant effect on each outcome. I use the predicted outcomes from the Audio model as they would have been influenced by the relative attention weights between moments. I run a regression to answer the following question:

2) Are sound durations of certain sound categories associated with the predicted outcome?

$$\text{PredictedOutcome}_{it} = \alpha_i + \gamma X_{it} + \sum_{z=1}^8 \beta_{1z} (\text{Sum of CI}(z)_{it}) + \beta_2 (\text{Sum of CI}(\text{Human}) \times \text{CI}(\text{Music})_{it}) + \beta_3 (\text{Brand Indicator in Audio}_{it}) + \epsilon_{it} \quad (3.5)$$

where, $\text{Sum of CI}(z)_{it}$ corresponds to the sum of the Category Indicator for z across the first 60 moments in video t made by influencer i , and $\text{Sum of CI}(\text{Human}) \times \text{CI}(\text{Music})_{it}$ finds the total duration when human and music sounds occur together, $\text{Brand Indicator in Audio}_{it}$ borrows the textual information in captions/transcript (first 30 sec) and acts as an indicator for whether a brand was mentioned in the audio clip, and ϵ_{it} is the error term. The results for the coefficients in each of the above equations are shown in Table 3.7. As three sound classes – Source Ambiguous, Background and Natural are present in only 0.1% of moments, I only use them as controls and hence their coefficients are not reported in the table. The values in the table reflect a percent change in the non-log-transformed outcome when a covariate is present (equation (3.4)) or increases by one unit (equation (3.5)).

As done in Section 3.5.2.1, I highlight the cells in gray that correspond to both (a) a positive and significant effect on attention weights and (b) a significant effect on predicted outcome. This allows me to filter out significant relationships affected by confounds unassociated with an increase in attention to audio moments. I find nine significant results. First, human sounds (without simultaneous music) are associated with an increase in attention, and their longer durations are associated with higher predicted views and likeability. Second, music (without simultaneous human sounds) is associated with an increase in attention, and its longer duration is associated with lower predicted engagement, popularity and likeability but higher predicted sentiment. Last, animal sounds are associated with an increase in attention, and their longer durations are associated with higher predicted sentiment and likeability. In addition, I also find that brand presence (in first 30 seconds of audio) is associated with lower predicted sentiment (while controlling for duration of each class of sound), thus complementing my similar finding with the Text Model. Thus, I identify significant relationships between sounds and outcomes that are supported by significant increase in attention paid to audio moments.

Next, I illustrate an example of how attention paid to audio moments in a video in the holdout sample can be visually interpreted. I focus on the relationship between speech and music. In Figure 3.12, I show the first 30 seconds of the audio clip of a travel influencer using four sub plots. The first plot shows the variations in the amplitude of the 30 second audio wave (sampled at 16 KHz) followed by the spectrogram of the wave where brighter regions correspond to stronger (or louder) amplitudes. Next, I show the interim output of the Audio model with the top 10 sound classes at each moment in the audio, where the darker squares indicate higher probability of observing a sound of that class at that moment (Pilakal & Ellis, 2020). The last plot displays the attention weights corresponding to each moment in the audio clip, where the darker squares indicate higher relative attention placed on that moment while forming an association with the outcome sentiment. As can be seen in the figure, relatively more attention is directed to moments where there is music but no simultaneous speech. The model predicts a positive sentiment for this clip, and this matches the observed sentiment as well.

3.5.2.3 Interpretation: Image Model

The salient parts of the images that are associated with an outcome of interest are visualized through gradient based activation maps (cf. Selvaraju et al., 2017). Gradients are found by taking the derivative between the continuous outcome (or class of predicted outcome for sentiment) and the output of the activation layer after the last convolution layer in the EfficientNet-B7 model. However, unlike Selvaraju et al. (2017), I do not apply the ReLU (Rectified Linear Unit) activation on the gradient values as I would like to retain negative gradient values for interpretation. In the Video Frame model, this process is carried out in each EfficientNet-B7 model corresponding to each video frame. Areas of the image with positive gradients correspond to regions that are positively associated with continuous outcomes and the predicted class of sentiment. To systematically identify and summarize the salient regions in thumbnails and video frames, I use Google's Cloud Vision API to detect objects and brand logos⁷¹ in the images in the holdout sample. The API returns the vertices of the identified item which allows me to create a rectangular bounding box to define its area. Next, I divide the identified objects into six categories – Persons (44.2%), Clothes & Accessories (30.9%), Home & Kitchen (11.0%), Animal (6.0%), Other Objects (3.7%) and Packaged Goods (1.9%); I let Brand Logos (2.3%) be the seventh category. The percentage in brackets indicates the percentage of items in that category out of a total of 4066 items (3973 objects + 93 brand logos) identified across 1944 frames in the holdout sample (324 videos x (1 thumbnail frame + 5 video frames)). In Step 1, I run a regression of the predicted gradient values in the holdout sample to answer the following question:

⁷¹ I use a 70% confidence level of the Vision API to detect objects and a 90% confidence level to detect brand logos to be conservative in my estimates.

1) Is size of objects/brand logos associated with mean gradient over its area?

$$MeanGradientValues_{itz} = \alpha_i + \gamma X_{it} + \beta ItemSize_{itz} + \epsilon_{itz} \quad (3.6)$$

where, $MeanGradientValues_{itz}$ is the mean gradient values across the area (pixels) occupied by all items of category z in video t made by influencer i , α_i is influencer fixed effect, X_{it} is the same vector of structured features used earlier in equation (3.2), $z = 1$ to 7 corresponds to each item category, $ItemSize_{itz}$ is the percentage of full image size occupied by all items of category z in video t made by influencer i , and ϵ_{itz} is the error term.

Now, an increase in gradients is directly correlated with an increase in predicted values of continuous outcomes or the predicted class of binary outcome by design. However, I would like to eliminate spurious relationships due to model artifacts or confounds associated with the presence of other items in the image. Hence in Step 2, I run a regression to answer the question:

2) Is size of an object/brand logo associated with the predicted outcome?

$$PredictedOutcome_{it} = \alpha_i + \gamma X_{it} + \sum_{z=1}^7 \beta_{1z} ItemSize(z)_{it} + \epsilon_{it} \quad (3.7)$$

where, $ItemSize(z)_{it}$ is the percentage of the full image size occupied by all items of category z in video t made by influencer i , and ϵ_{it} is the error term. I run this regression for thumbnails and for the average of five video frames (in the first 30 sec) for each of the five outcomes. The results for the coefficients in the above equations are shown in Table 3.8. The values in the table reflect a percent change in the non-log-transformed outcome when size of an item increases by one percent.

I highlight the cells in gray that correspond to a significant effect for both equations in the same direction. These cells show evidence of not only a significant effect on mean attention weights but also a significant effect in the same direction on predicted outcome while controlling for the presence of other items. I find that larger pictures of persons or clothes & accessories in video frames (first 30 sec) are associated with an increase in mean attention and an increase in predicted engagement. Influencers and brands promoting clothes & accessories are likely to benefit from testing this relationship for causal effects in a field setting.

Next, I illustrate how attention paid to image pixels on the video frames of a video in the holdout sample can be visually interpreted. I focus on the first three frames at 0 sec, 7.5 sec and 15 sec for a video of a gaming influencer in Figure 3.13. The first row shows the original frames which are overlaid with bounding boxes for items identified by the Vision API. The second row shows the heat map (positive gradient values) while forming an association with engagement. Brighter heat maps correspond to values that are more positively correlated with engagement. I find that pixels associated with images of persons have brighter heat maps (as compared to other parts of the image), and as the area occupied by the person

decreases, the percentage of the area of the person that is salient also decreases. This conforms with the significant findings from Table 3.8. Furthermore, the predicted engagement for this example is 15 comments per 10,000 views which is less than the median engagement of 19 comments per 10,000 views, which can be expected given that the size of the person is progressively decreasing in subsequent frames.

3.5.2.4 Summarizing Insights

I filter out 16 significant relationships affected by confounds unassociated with an increase in attention (change in gradients) to video elements (i.e., significant in Step 2 but not in Step 1). Next, I carry out a check to ensure that the results in Step 2 remain significant while controlling for the presence of other unstructured elements, using the following equation:

$$PredictedOutcome_{it} = \alpha_i + \gamma X_{it} + \beta_1(BITX_{it}) + \beta_2(LOTX_{it}) + \sum_{z=1}^8 \beta_{3z} (Sum\ of\ CI(z)_{it}) + \beta_4(Sum\ of\ CI(Human)\ x\ CI(Music)_{it}) + \sum_{z=1}^7 \beta_{5z} ItemSize(z)_{it} + \epsilon_{it} \quad (3.8)$$

Using the above equation, I eliminate one relationship that is no longer significant. Overall, I eliminate more than 50% of the relationships (out of 29 significant relationships in Step 2) and identify a smaller subset of 12 relationships (or hypotheses) that can be plausibly causal and tested in the field. I find the greatest number of significant results from the Audio model (8), followed by the Text model (2), and then the Image model (2) which are all summarized in Table 3.9. Across these 12 results, the decision to choose video elements can be based on either conscious or sub-conscious decisions. The decision that is likely made consciously by influencers is whether to mention a brand in the video description or during speech (captions/transcript). Hence, knowing the implications of brand mentions at various locations in the video will allow influencers to make conscious changes to video design.

These significant associations between elements of one of the three modalities (text, audio or images) and marketing outcomes (views, interaction rates or sentiment) are likely not confounded by the presence of other modalities as I control for them. The effect sizes in Table 3.9 reflect a percent change in the non-log-transformed outcome when a covariate is present (brand mentions in Step 1 & 2, audio moments in Step 1), increases by one unit (audio moments in Step 2) or increases by one percent (image sizes in Step 1 & 2). The effect sizes corresponding to the outcome in Table 3.9 reflect the coefficient sizes from equation (3.8).

Finally, I highlight how the unobserved YouTube recommendation algorithm could potentially impact my findings. The algorithm analyzes watch history and video content to recommend videos with higher expected watch time for a viewer (Covington et al., 2016). In my analysis, if the ex-post elements that I study are correlated with unobserved features that cause higher expected watch time then my results corresponding to the outcome views need not be causal (because views can be expected to be highly

correlated with watch time). However, the remaining four outcomes (sentiment, engagement, popularity and likeability) are unlikely to be highly correlated with watch time because of their low correlation with views (shown earlier in Table 3.2). Hence, the algorithm is unlikely to be a confounder for the significant relationships that I find for these four outcomes.

3.5.3 Learning Patterns

In this section I take a deeper dive to examine if influencer videos exhibit informal patterns suggesting that influencers are learning and acting on these relationships over time. To do this, I select three product categories that include influencers at both ends of the follower range (“micro” with < 100K subscribers and “mega” with $\geq 1M$ subscribers as per industry classification (Ismail, 2018)) and that have at least 100 videos in each group. These are Travel (2 micro and 1 mega), Parenting (1 micro and 1 mega) and Home (2 micro and 1 mega). I then choose a smaller sample of videos from each mega influencer corresponding to the total number of videos of the micro influencers in each category so that I have a balanced sample within each category. As before, I exclude those videos in which either likes, dislikes or comments were disabled by the influencer(s), leaving me with a total of 947 videos for Travel, 900 videos for Parenting and 322 videos for Home (all scraped in January 2020).

My goal is to study whether influencers are changing their videos over time on the video elements that were found to have significant relationships with the outcomes in Table 3.9. My identification strategy is a test of the change in the coefficient of “Video Number \times Indicator of Influencer group” estimated separately for the first half and the second half of all videos uploaded by each influencer. These coefficients are obtained (for each of the three product categories) via the regression below.

$$\begin{aligned}
 V_{tih} = & \gamma_h Z_{tih} + \beta_{(h)1}(\text{Indicator for Microinfluencer}_{itp}) + \\
 & \beta_{(h)2}(\text{Indicator for Megainfluencer}_{itp}) + \\
 & \beta_{(h)3}(\text{Video Number}_{tip} \times \text{Indicator for Microinfluencer}_{tip}) + \\
 & \beta_{(h)4}(\text{Video Number}_{tip} \times \text{Indicator for Megainfluencer}_{tip}) + \epsilon_{tip}
 \end{aligned} \tag{3.9}$$

where V is the video element for video t by influencer i in half h , $h = \{1,2\}$. The video elements V were identified and listed in Table 3.9. Z includes controls for video length, number of tags, features from playlist, time between uploads, day and time of day fixed effects, captions indicator, number of URLs in description, and indicator of hashtag in description. *Video Number* is the serial number of the video uploaded by the influencer, where a *Video Number* of 0 corresponds to the first video uploaded by the influencer. To document whether there are patterns consistent with learning, I compare and contrast the coefficients $\beta_{(1)3}$ and $\beta_{(2)3}$ as well as $\beta_{(1)4}$ and $\beta_{(2)4}$ for micro and mega-influencers respectively. I find

that only 3% of the relationships exhibit significant coefficient values for both $\beta_{(1)k}$ and $\beta_{(2)k}$, $k = \{3, 4\}$, suggesting that majority of micro and mega influencers across Travel, Parenting and Home categories do not exhibit patterns consistent with learning these relationships over time. While this analysis is fairly simple, I do not find any evidence of systematic changes. I leave a more detailed analysis of this topic for future research.

3.5.4 Analysis Using Other Slices of Influencer Videos

In this section, I analyze content in the middle 30 sec and last 30 sec of each video across transcript/captions, audio and images as a robustness check. Specifically, I compare my findings with the results for the first 30 sec of the video presented in Section 3.5.1. As shown in Table 3.10, using information from the middle or end of the video does not perform better than using information from the beginning for predicting all five outcomes on the holdout sample (using any of the three modalities - transcript/captions, audio or image frames). This suggests that the information in the beginning of the video is most important for predicting all outcomes. Furthermore, I also combine information from the beginning, middle and end of video for each modality of unstructured data using a Ridge Regression model (found as best performing in Section 3.5.1) to predict each of the five outcomes. I find that prediction results improve in only 5 out of the 15 cases (3 modalities x 5 outcomes) which demonstrates that information in the beginning of the video often captures variation in data explained by the middle and end of videos. Given that the predictions using these two sets of information do not dominate, and in the interest of parsimony and computational efficiency, I keep the focus of my analysis on the initial 30 sec of the videos.⁷²

3.6 Implications for Influencers and Marketers

In this section, I illustrate how my approach and findings can be useful for practitioners (influencers and marketers) in three possible ways. First, brands that sponsor influencers can benefit from a clear understanding of how mentions across different types of brands affect outcomes. In order to do this, I focus on one of the significant relationships identified from the Text model. Using a Ridge Regression model where each brand has a unique coefficient, I run the regressions in Step 1 and 2 again and display the results of the coefficients in Figure 3.14. As can be seen from the figure, the x-axis captures the attention weight directed to brand mentions and the y-axis reflects the sentiment. The brands driving the main effect are in the bottom right quadrant (positive attention weight and negative sentiment). Based on the brands in the quadrant, it appears that this relationship mainly exists for consumer electronics and video-gaming categories (about 70% of the brands in that quadrant). Thus, brands in these categories may

⁷² I refer the interested reader to Appendix B.6 for details on the interpretable results from the middle and end slices of videos.

find it useful to suggest influencers to drop brand mentions in the first 30 seconds and then test this more rigorously. They may be better off focusing on brand mentions in other parts of the video.

Another possibility in terms of evaluating the effectiveness of influencer videos is to focus on the interaction between video elements (text, audio and images). However, this is non-trivial as the potential number of combinations is very large. One possible way to reduce this number and focus on relevant interactions is to draw on the findings from the literature, especially that on conventional advertising. For example, this literature has found that use of voice-over, animal images and music can reduce irritation towards the ad (Pelsmacker & Van den Bergh, 1999). Hence, I study whether interactions such as brand mention with background music, brand mention with size of person image, and brand mention with size of animal images (within first 30 seconds of video) are significantly associated with sentiment towards the video. I run corresponding regressions as done in Section 3.5.2 and find null effects for each of these interactions.

Second, besides evaluating specific elements or specific interactions between elements (as above), marketers may also be interested in evaluating influencer videos in a holistic manner. I develop a scoring mechanism to help them determine the impact and effectiveness of influencer videos. A video can be scored out of 100% on each of its unstructured elements when predicting any of the five outcomes. I do this with the help of the equation of the combined Ridge Regression model detailed in Section 3.4.4 which is reproduced below:

$$Y_{it} = g \left(X_{it}, \hat{Y}_{it\text{Title}}, \hat{Y}_{it\text{Description}}, \hat{Y}_{it\text{Caption/Transcript}}, \hat{Y}_{it\text{Audio}}, \hat{Y}_{it\text{Thumbnail}}, \hat{Y}_{it\text{Video Frames}} \right) + \epsilon_{it}$$

I begin by creating a linear Partial Dependence Plot (PDP) (J. Friedman, 2001) between $\hat{Y}_{it\langle\text{unstructured element}\rangle}$ and Y_{it} in the training sample. I note the minimum and maximum values of $\hat{Y}_{it\langle\text{unstructured element}\rangle}$ while predicting each of the five outcomes. I then note the values of $\hat{Y}_{it\langle\text{unstructured element}\rangle}$ for a random video in the holdout sample. I scale it using min-max scaling to get a score out of 100% for each unstructured element while predicting each outcome. Finally, I get an overall score by weighing the score for each unstructured element with its relative importance score (based on Table 3.5).

As an illustration, let me take the point of view of a brand that is evaluating a particular influencer as a potential partner. As a sample, they pick this video (https://www.youtube.com/watch?v=3-oWqeA_hc4) and score it as above. From Table 3.11, I can see that the video's weakest performance area based on its overall score is on the engagement and popularity outcomes, with the weakest elements being captions and video frames respectively. The brands can use these scores to (a) suggest areas of improvement to the influencers, (b) compare this video to other videos from the same influencer and (c) compare this video to videos from other influencers. Similarly, the influencer can use these scores to

progressively refine their videos for the relevant outcome. Note that these summary scores are based on correlations between video elements and outcomes, so their value lies in providing directions along which improvements are most likely. In contrast, without these scores, the number of directions on which influencers and brands can work is very large.

Third, a bigger question for marketers is to understand the overall importance of branded content in these influencer videos. One way to quantify this is to look at the important elements that go into outcome predictions (as in Table 3.9) and decompose the variance explained by brand related content e.g., brand mentions versus other content in captions/transcript. This is illustrated in Table 3.12, where I show the variance explained by the presence of brand mentions in the video description to predict views, and the presence of brand mentions in captions/transcript to predict sentiment. I use the Ridge Regression model (found as best performing in Section 3.5.1) to measure the ability of brand mentions to predict the outcome variable and compare its performance with the Text model (BERT) that was originally used (in Section 3.4.1) to measure the ability of the whole text to predict the outcome variable. I find that brand mentions in description explain 7.8% of the variation in views, whereas brand mentions in captions/transcript explain 39.7% of the variation in sentiment, thus demonstrating the relatively more important role played by brand mentions in predicting sentiment towards the video.

3.7 Conclusion

This essay adds to the small body of work on an important and growing marketing mechanism, influencer marketing. The main vehicle used in influencer marketing is influencer videos, with brands sponsoring and/or inserting advertising during these videos. There is virtually no research on how the elements of these videos (across text, audio and images) are related to outcomes that both influencers and marketers care about. This essay takes the first step at documenting and interpreting these relationships.

Methodologically, the essay uses novel transfer learning/deep learning approaches that avoid making a tradeoff between interpretability and predictive ability. After carrying out predictions using unstructured data, interpretation is carried out ex-post by quantifying the attention paid on word-pieces in text, moments in audio and items in images while forming an association with an outcome. This information is used to find significant positive (significant) relationships between video elements and attention (gradients), followed by the determination of significant relationships between video elements and the predicted outcome of interest. An added benefit of this approach is that it allows filtering out relationships that are affected by confounding factors unassociated with an increase in attention. This significantly reduces the effort required for further causal work.

The proposed approach not only allows quantifying the relative importance of data modalities (text, audio, and images), but also allows visualization of salient regions across these modalities. This

allows to provide a holistic perspective about the role of each component in predicting outcomes of interest to both influencers and brand partners. In terms of practical applications, key findings such as a brand mention (especially from consumer electronics and video game categories) in the first 30 seconds results in a *significant increase* in attention to the brand but a *significant decrease* in sentiment towards the video, can help influencers refine their videos. Brands can also use these findings to evaluate the attractiveness of a given influencer's video by either focusing on specific elements and their interactions or analyzing them in a holistic manner for their marketing campaigns. A broader view suggests that my approach can be adapted to the analysis of (non-traditional) videos in multiple domains e.g., education and politics.

Given that the essay represents early work on this topic, it suffers from some limitations. First, as I have no access to sales data from influencer campaigns, I use proxy metrics that, while relevant to marketers, may not be perfectly correlated to business metrics. Interestingly, however, brands find it very difficult to assess the ROI of influencer marketing campaigns, suggesting that measurement of sales data is non-trivial (Bailis, 2020; Kramer, 2018). Second, as my sample includes only influencers who use brand endorsements, I cannot offer any insights about the quality of videos from those influencers who never receive such endorsements. Third, the uncovered relationships between advertising content and outcomes, while based on an increase in attention to advertising content, do not guarantee causality, and need to be validated e.g., via field experiments. Fourth, while YouTube is one of the most important influencer marketing platforms, there may be systematic differences in how influencer videos work on other channels such as Instagram or TikTok. Finally, given that different devices (e.g., mobile, desktop and tablet) can be used to access content from the same platform, identified relationships could vary by device, but my findings only capture the average effect. I hope that future work can address these limitations.

3.8 Tables

Table 3.1: Scraped data for videos

Structured Data	Metrics	Number of views (from time of posting to time of scraping)
		Number of comments (from time of posting to time of scraping)
		Number of likes (from time of posting to time of scraping)
		Number of dislikes (from time of posting to time of scraping)
	Length	Video Length (min)
	Tags	Tags associated with each video (see Google (2020a) for details)
	Playlist	Number of playlists the video is a part of
		Position of video in each playlist
Number of videos on all the playlists the video is a part of		
Time	Time of posting video	
Unstructured Data	Text	Title
		Description
		Captions (if present)
		Comments (Top 25 as per YouTube’s proprietary algorithm) with replies
	Audio	Audio file
	Images	Thumbnail
		Video file

Table 3.2: Correlation between outcomes

	Log views	Log engagement	Log popularity	Log likeability	Binary Sentiment
Log views	1				
Log engagement	0.04	1			
Log popularity	0.20	0.66	1		
Log likeability	0.43	0.14	0.57	1	
Sentiment (binary)	-0.21	-0.15	0.02	0.15	1

Table 3.3: Video features - structured and unstructured

Type	Class	Features	
Structured Features	Fixed Effects	Influencer Fixed Effects (33)	
	Fixed Effects	Category Fixed Effects (11)	
	Length	Video Length (min)	
	Tags	Number of video tags	
	Playlist Information		Number of playlists the video is a part of
			Average position in playlist
			Average number of videos on all the playlists the video is a part of
	Time based covariates		Time between upload: Upload time and scrape time
			Year of upload (2006 to 2019)
			Time between upload: Given video and preceding video in master list
			Time between upload: Given video and succeeding video in master list
			Rank of video in master list
			Day fixed effects in EST (7) and Time of day fixed effects in intervals of 4 hours from 00:00 hours EST (6)
Captions Indicator		Indicator of whether video has closed captions	
Unstructured features	Text	Title	
		Description (first 160 characters)	
		Captions or Transcript (first 30 sec)	
	Audio	Audio file (first 30 sec)	
	Images	Thumbnail	
		Image frame at 0 sec (first frame), 7.5 sec, 15 sec, 22.5 sec, 30 sec	
Structured features	Complete Description	Total number of URLs in description	
		Indicator of Hashtag in description	

Table 3.4: Best performing model for each component of unstructured data in holdout sample
(RMSE for Views, Engagement, Popularity and Likeability; Accuracy for Sentiment)

Model	Data	Views	Sentiment	Engagement	Popularity	Likeability
BERT	Title	1.66	0.72	0.82	0.71	0.85
	Description (first 160c)	1.57	0.69	0.88	0.72	0.93
	Captions/transcript (first 30s)	1.75	0.70	0.92	0.76	0.99
YAMNet + Bi-LSTM + Attention	Audio (first 30s)	1.97	0.65	0.93	0.80	1.02
EfficientNet-B7	Thumbnail	3.09	0.68	1.75	1.34	1.43
EfficientNet-B7 + Bi-LSTM	Video Frames (0s,7.5s,15s,22.5s,30s)	2.23	0.68	0.97	0.80	1.03

Table 3.5: Importance of features based on the Ridge Regression Model

Sr No.	Name	Views	Sentiment	Engagement	Popularity	Likeability
1	Influencer Fixed Effects	21.33%	18.74%	2.65%	12.71%	49.06%
2	Title	15.85%	15.07%	43.25%	22.97%	11.21%
3	Description (first 160c)	13.82%	14.39%	34.53%	17.88%	11.14%
4	Time based covariates	12.33%	7.98%	1.18%	11.20%	5.70%
5	Playlist Information	9.87%	0.32%	2.53%	5.72%	3.60%
6	Captions/transcript (first 30s)	9.77%	12.67%	7.49%	17.34%	2.91%
7	Total URLs in description	5.32%	0.06%	0.22%	3.84%	2.10%
8	Category Fixed Effects	4.92%	12.21%	0.48%	3.29%	10.42%
9	Thumbnail	2.53%	4.98%	2.04%	0.54%	1.53%
10	Video Length	2.15%	0.09%	0.38%	0.72%	0.61%
11	Audio (first 30s)	1.23%	5.21%	4.76%	2.76%	0.06%
12	Tags Count	0.68%	0.07%	0.18%	0.59%	0.21%
13	Captions Indicator	0.11%	2.34%	0.02%	0.04%	0.51%
14	Hashtag Indicator in Description	0.08%	0.14%	0.04%	0.29%	0.92%
15	Video Frames (0s,7.5s,15s,22.5s,30s)	0.001%	5.73%	0.27%	0.09%	0.02%

Table 3.6: Results of the Text Regression Models

(* – Significant ($p < 0.05$); W – Weakly Significant ($0.05 \leq p < 0.1$))

Model for	Data Type	Step 1 - Eq(2)	Step 2 - Eq(3)
		BIT	BITX
Views	Title	27.60*	-5.26
	Desc	24.14*	61.21*
	Tran	7.25	7.72
Sentiment	Title	-25.35*	-6.27
	Desc	-16.75W	-46.04
	Tran	36.70*	-80.81*
Engagement	Title	32.10*	-6.36
	Desc	6.29	4.57
	Tran	626.23*	5.01
Popularity	Title	15.32*	-9.96
	Desc	18.88*	5.47
	Tran	156.72*	9.94
Likeability	Title	39.83*	-11.69
	Desc	82.65*	16.36W
	Tran	127.48*	5.78

Table 3.7: Results of the Audio Regression Models

	Model for	Category Indicator					Human x Music	Location	Brand Indicator
		Human	Music	Silence	Things	Animal			
Step 1	Views	23.22*	18.48*	-17.61*	-31.36*	10.15W	-7.22*	-2.34*	NA
	Sentiment	-17.82*	36.47*	35.36*	0.97	21.82*	-19.07*	0.04*	NA
	Engagement	-0.54N	5.20*	-9.79*	6.58	-6.38	-15.29*	-1.65*	NA
	Popularity	-6.29*	36.66*	-22.03*	-2.74	1.89	-4.98*	-1.35*	NA
	Likeability	6.62*	5.10*	-6.63*	-2.58	11.81*	0.33	0.26*	NA
Step 2	Views	2.82*	-0.4	-1.66*	8.45*	0.30	-1.13*	NA	5.74
	Sentiment ⁷³	-1.43*	0.13*	0.08*	1.07*	0.14*	1.03	NA	-9.82*
	Engagement	-0.43W	-2.28*	-2.11*	-6.27*	-0.16	-0.13	NA	3.29
	Popularity	-0.62*	-1.66*	-1.24*	-6.33*	0.58	0.16	NA	2.84
	Likeability	0.17*	-0.26*	-0.02W	0.13W	0.25*	0.12*	NA	-0.19

(* – Significant ($p < 0.05$); W – Weakly Significant ($0.05 \leq p < 0.1$))

Table 3.8: Results of the Image Regression Models

(* – Significant ($p < 0.05$); W – Weakly Significant ($0.05 \leq p < 0.1$))

	Model for	Data Type	Sub Covariate						
			Person	Clothes & Acc	Home & Kitchen	Animal	Other Objects	Packaged Goods	Brand Logos
Step 1	Views	Thumbnail	0.03	0.06	0.18*	-0.00	0.05	0.02	1.01
		Avg frames	0.57*	1.04*	0.85*	0.86*	0.60*	-0.93*	-2.56
	Sentiment	Thumbnail	-0.05*	-0.09*	-0.24*	-0.04	-0.07	0.01	-0.72
		Avg frames	-0.03W	-0.07	-0.17*	0.09	-0.19W	-0.31	-4.6
	Engagement	Thumbnail	-0.08*	-0.06	-0.18W	-0.05	-0.02	-0.08	0.77
		Avg frames	0.36*	0.75*	0.41*	0.89*	0.12	0.20	-1.45
	Popularity	Thumbnail	-0.11*	-0.19*	-0.14	-0.05	-0.11	-0.15	1.53*
		Avg frames	0.51*	0.92*	0.71*	0.50*	0.41W	0.35	3.05
	Likeability	Thumbnail	-0.01	-0.02	0.06	-0.03	-0.02	0.05	1.19*
		Avg frames	0.49*	0.80*	0.56*	0.61*	0.48*	-0.08*	1.60
Step 2	Views	Thumbnail	1.06W	-0.74	2.56	1.55	0.97	-0.37	6.44
		Avg frames	-0.00	0.01	-0.11*	0.00	-0.04	0.03	4.86W
	Sentiment	Thumbnail	-0.25	0.50	5.94	2.02	-7.00*	3.19	-100
		Avg frames	-0.46	-4.66*	-2.72	23.97*	-6.73	5.95	40.27
	Engagement	Thumbnail	0.20	1.03*	-1.22	0.57	0.77	-1.34	-7.46
		Avg frames	0.40*	0.66*	0.26	0.20	0.33	0.45	-1.54
	Popularity	Thumbnail	0.18	-0.21	1.02	0.32	0.84W	0.04	6.96
		Avg frames	0.02	0.00	0.03	0.01	0.09W	0.07	0.64
	Likeability	Thumbnail	-0.01	-0.53	0.82	-0.65	-0.12	0.56	8.12
		Avg frames	0.01	-0.03	0.02	-0.02	-0.03	0.15W	0.21

⁷³ p values (confidence intervals) are calculated using penalized log likelihood instead of maximum log likelihood due to 'complete separation' in logistic regression.

Table 3.9: Results from interpreting Regression Models

Outcome	Significant <i>increase</i> in attention (A) and significant <i>increase</i> in outcome (O)			Significant <i>increase</i> in attention (A) but significant <i>decrease</i> in outcome (O)	
	Text Model	Audio Model	Image Model	Text Model	Audio Model
Views	brand mentions in description (first 160 char) A: 25.14% O: 64.63%	more speech (without simultaneous music) in first 30 sec of audio A: 23.22% O: 2.75%			
Sentiment		more music (without simultaneous speech) A: 36.47% O: 0.09% or more silence A: 35.36% O: 0.08% in first 30 sec of audio		brand mentions in first 30 sec of captions/transcript A: 36.70% O: - 89.10%	
Engagement			Larger pictures of persons A: 0.36% O: 0.38% or clothes & accessories A: 0.75% O: 0.62% in first 30 sec of video frames		more music (without simultaneous speech) in first 30 sec of audio A: 5.20% O: - 2.28%
Popularity					more music (without simultaneous speech) in first 30 sec of audio A: 36.66% O: - 1.67%
Likeability		more speech (without simultaneous music) A: 6.62% O: 0.17% or more animal sounds A: 11.82% O: 0.24% in first 30 sec of audio			more music (without simultaneous speech) A: 5.10% O: - 0.26% in first 30 sec of audio

Table 3.10: Predictive accuracy in holdout sample using unstructured data from beginning, middle and end of videos
(RMSE for Views, Engagement, Popularity and Likeability; Accuracy for Sentiment)

Model	Data	Data Location	Views	Sentiment	Engagement	Popularity	Likeability
BERT	Captions/ transcript (30s)	Beginning	1.75	0.70	0.92	0.76	0.99
		Middle	1.92	0.67	0.98	0.80	1.03
		End	1.88	0.68	0.98	0.79	1.05
YAMNet + Bi-LSTM + Attention	Audio (30s)	Beginning	1.97	0.65	0.93	0.80	1.02
		Middle	2.26	0.62	0.96	0.80	1.02
		End	2.27	0.63	0.96	0.81	1.02
EfficientNet-B7 + Bi-LSTM	Video Frames (five equally spaced in 30s)	Beginning	2.23	0.68	0.97	0.80	1.03
		Middle	2.31	0.65	1.01	0.83	1.03
		End	2.31	0.68	0.99	0.82	1.06

Table 3.11: Score for a video outside the training sample

	Views	Sentiment	Engagement	Popularity	Likeability
Title Score	83.45%	100.00%	36.60%	57.98%	75.63%
Description Score	74.76%	100.00%	34.56%	59.97%	61.16%
Captions/Transcript Score	84.17%	100.00%	6.79%	45.45%	90.60%
Audio Score	88.34%	100.00%	28.43%	47.76%	58.74%
Thumbnail Score	25.62%	100.00%	43.50%	40.33%	50.00%
Video Frame Score	90.97%	0.00%	65.17%	29.75%	43.30%
Overall Score	77.58%	90.12%	33.24%	54.37%	69.74%
Observed value for this YouTube video	368,796	POSITIVE	5 comments / 10K views	179 likes / 10K views	118 (likes+1)/ (dislikes+1)
Median value in dataset across 1620 videos	140,000	NA	19 comments / 10K views	220 likes / 10K views	54 (likes+1)/ (dislikes+1)

Table 3.12: Variance explained by brand mentions

Model	Outcome	Covariate	Holdout $\sqrt{SSE} =$ $\sqrt{(y - \hat{y})^2}$ or accuracy	Baseline $\sqrt{SST} =$ $\sqrt{(y - \bar{y})^2}$ or accuracy	Improve- ment over baseline	Variance explained by branded content
Ridge Regression	Views	Two indicators for brand mention in first and second half of description (first 160c)	2.2	2.3	2.4%	7.8%
BERT	Views	Description (first 160c)	1.6	2.3	30.5%	
Ridge Regression	Sentiment	Two indicators for brand mention in first and second half of captions/transcript (first 30s)	58.0%	50.0%	16.0%	39.7%
BERT	Sentiment	Captions/Transcript (first 30s)	70.2%	50.0%	40.4%	

3.9 Figures

Figure 3.1: Distribution of log view count

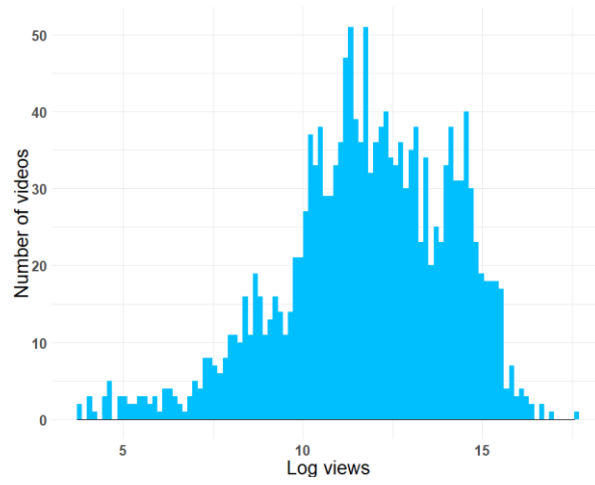


Figure 3.2a: Distribution of Log Engagement

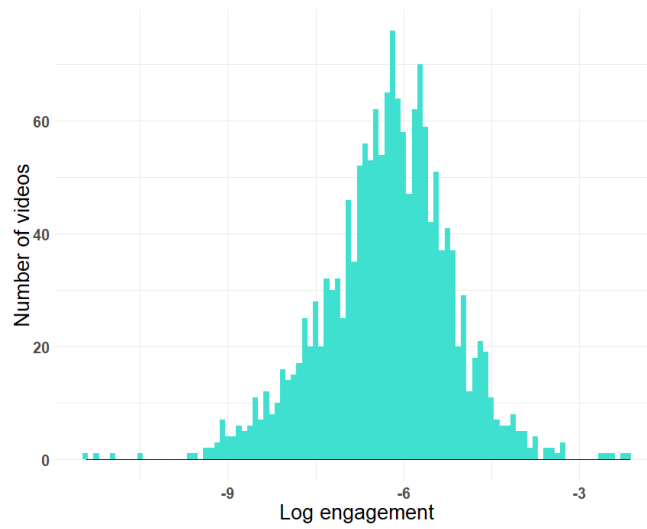
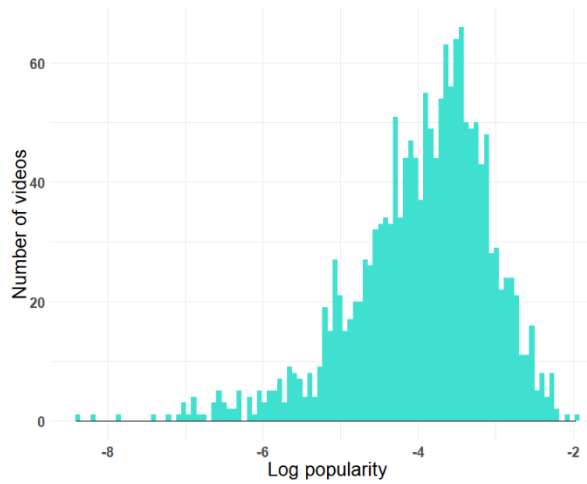


Figure 3.2b: Distribution of Log Popularity



Figures 3.2c: Distribution of Log Likeability

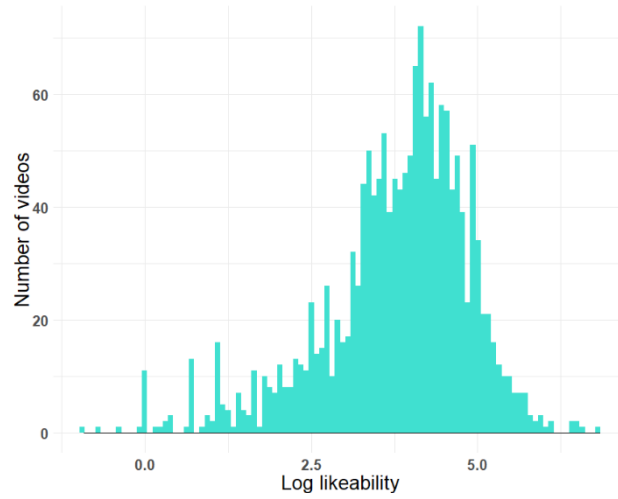


Figure 3.3: Distribution of average sentiment score across Top 25 comments

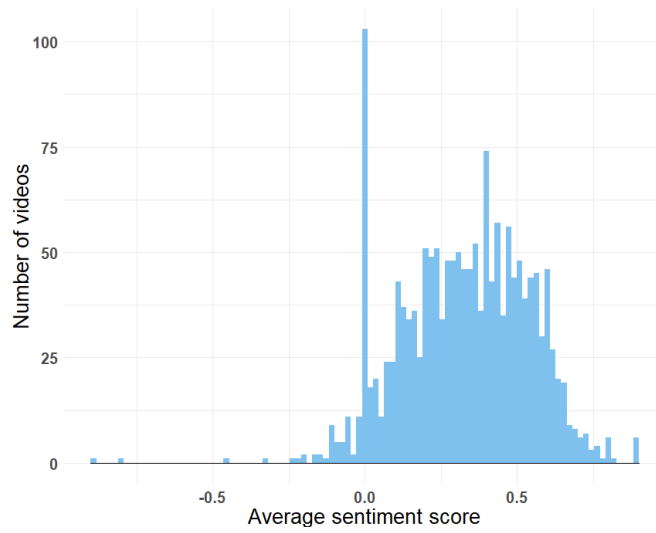


Figure 3.4a: Distribution of number of brand mentions in text

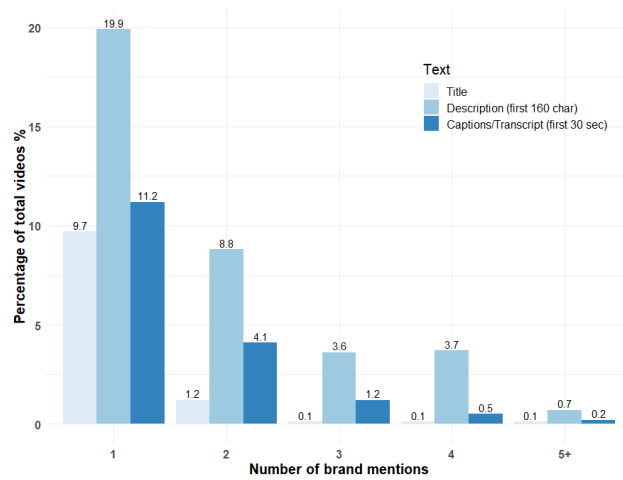


Figure 3.4b: Distribution of number of brand logos in images

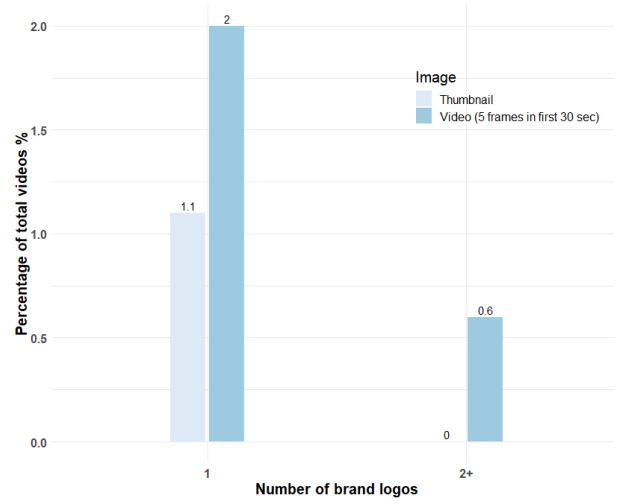


Figure 3.5a Traditional Deep Learning Approach

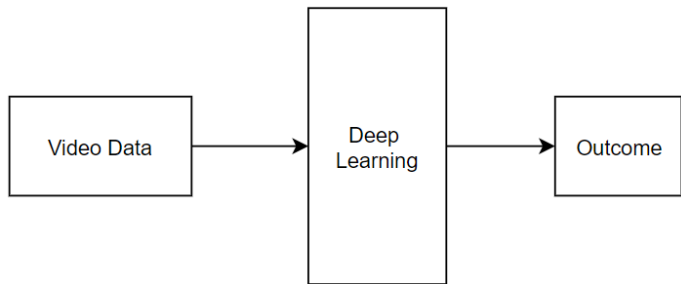


Figure 3.5b: Interpretable Deep Learning Approach

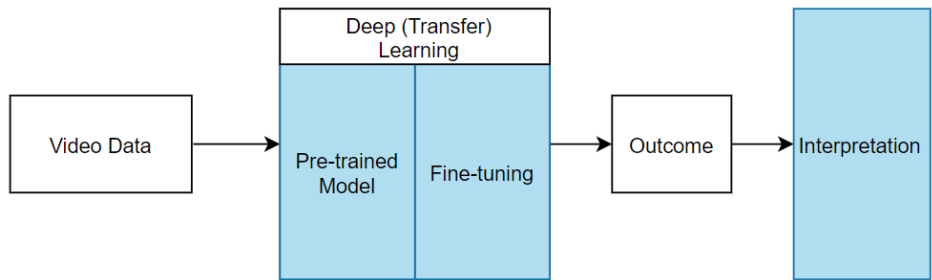


Figure 3.6: BERT Model Framework

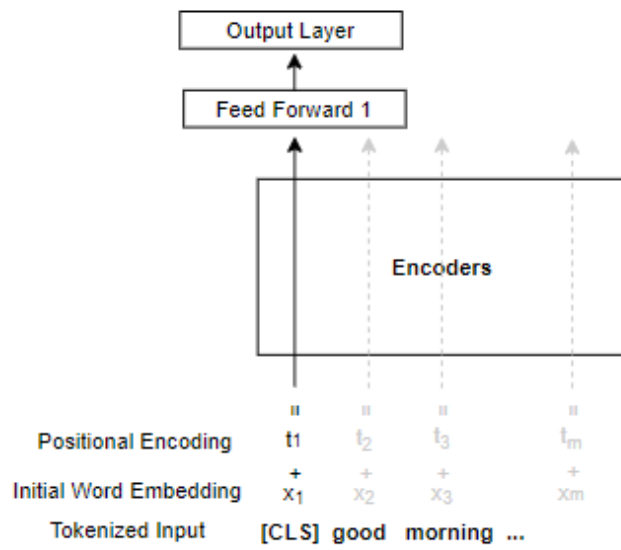


Figure 3.7: Audio Model

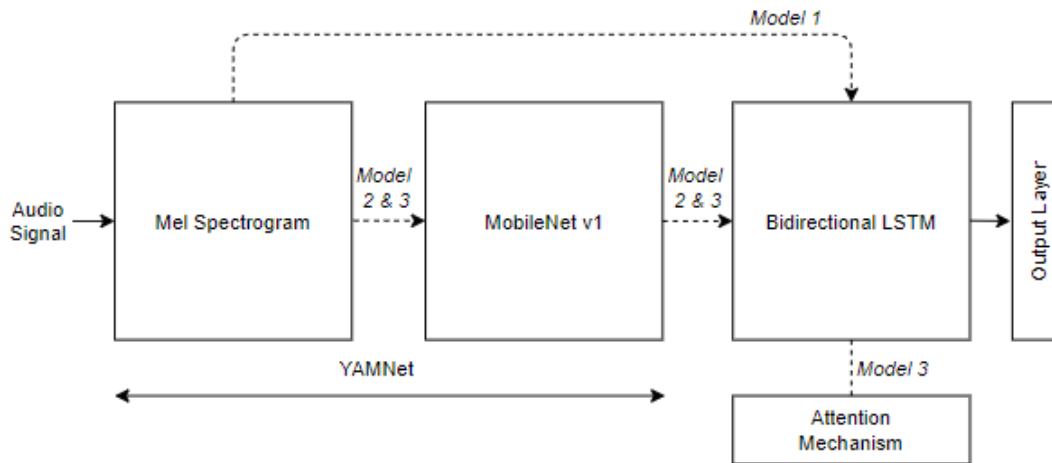


Figure 3.8: Image Model (Video Frames)

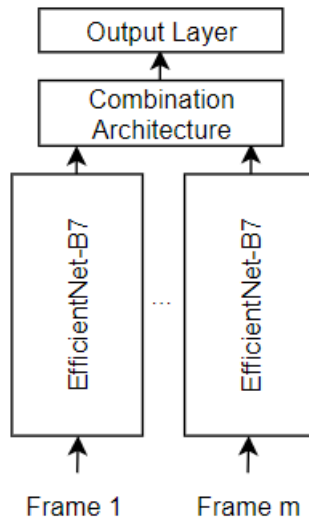


Figure 3.9: Combined Model

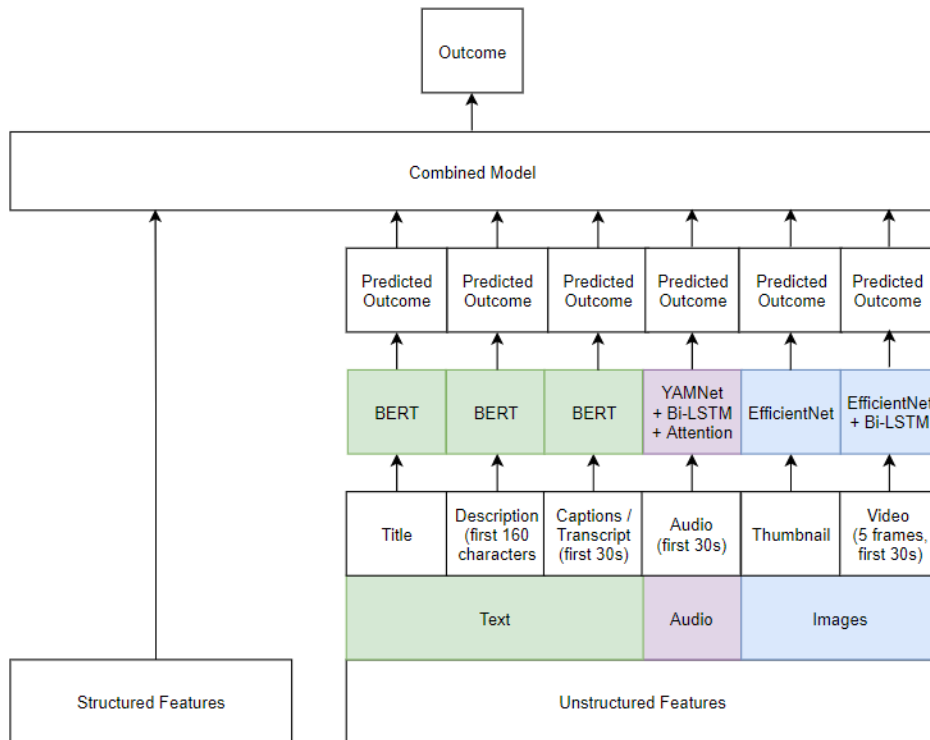


Figure 3.10: Interpretation strategy on holdout sample

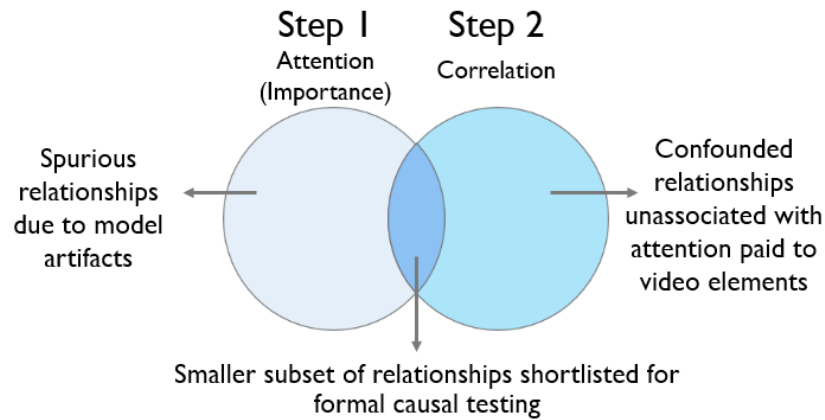


Figure 3.11: Attention Weights in captions/transcript (first 30s) of a video

Predicted sentiment: Not Positive

Observed sentiment: Not Positive

what is up guys lew here and this is the iphone 5 camera test if you haven't subscribed yet definitely click that button right now so you don't miss out on any of my iphone 5 coverage or tests there is a button around you find it click it anyway this video here we're going to be looking at the rear facing camera as well as the newly improved forward facing camera which now shoot 720p making it a viable option for shooting vlogs and things like that stick around till the end of the video to get all

Figure 3.12: Attention weights in an audio clip (first 30s) of a video

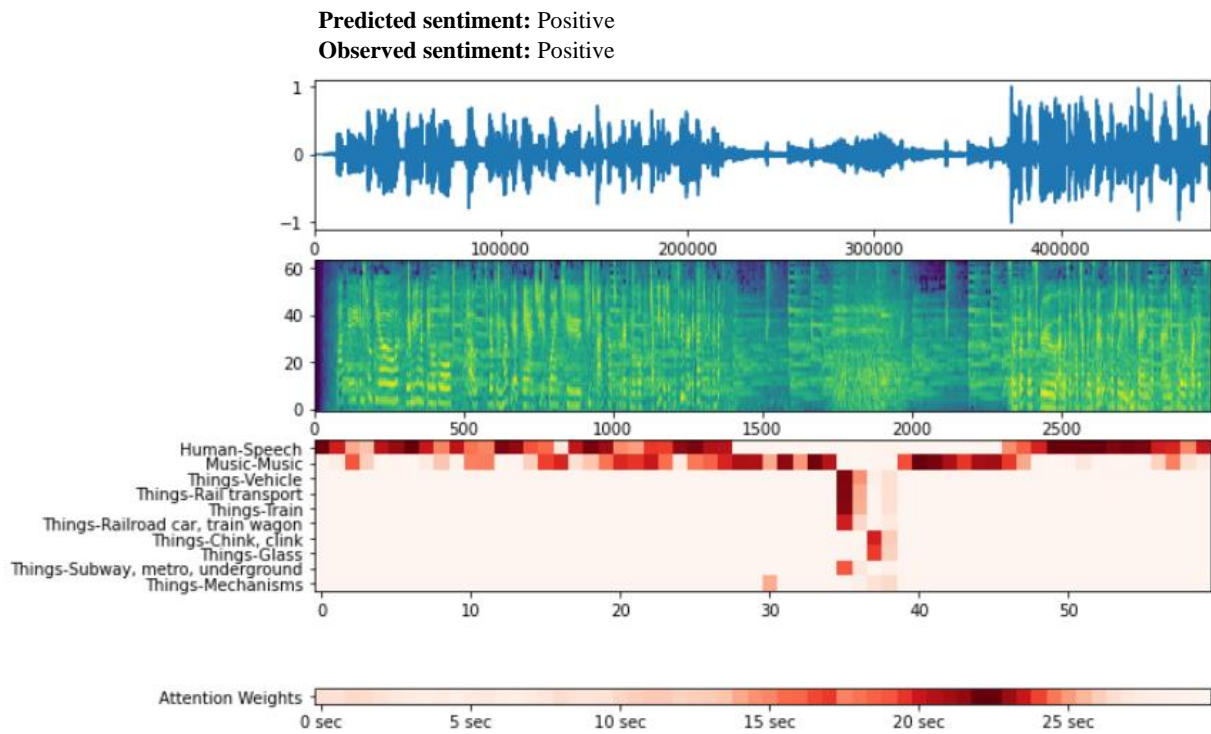


Figure 3.13: Gradient heat map (associated with engagement) in frames of a video

Predicted Engagement: 15 comments per 10K views

Median Engagement: 19 comments per 10K views

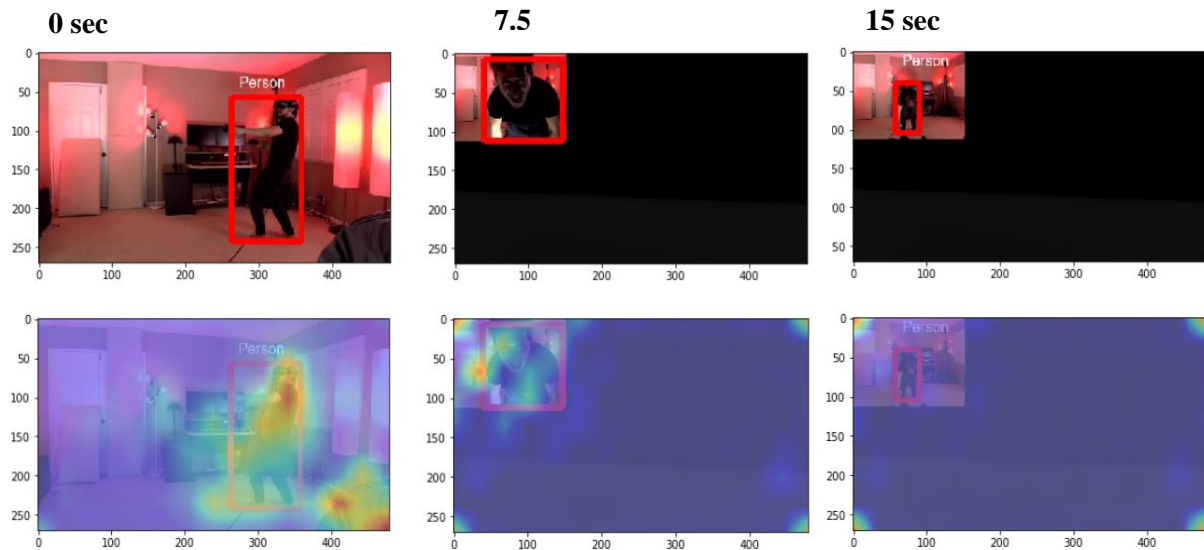
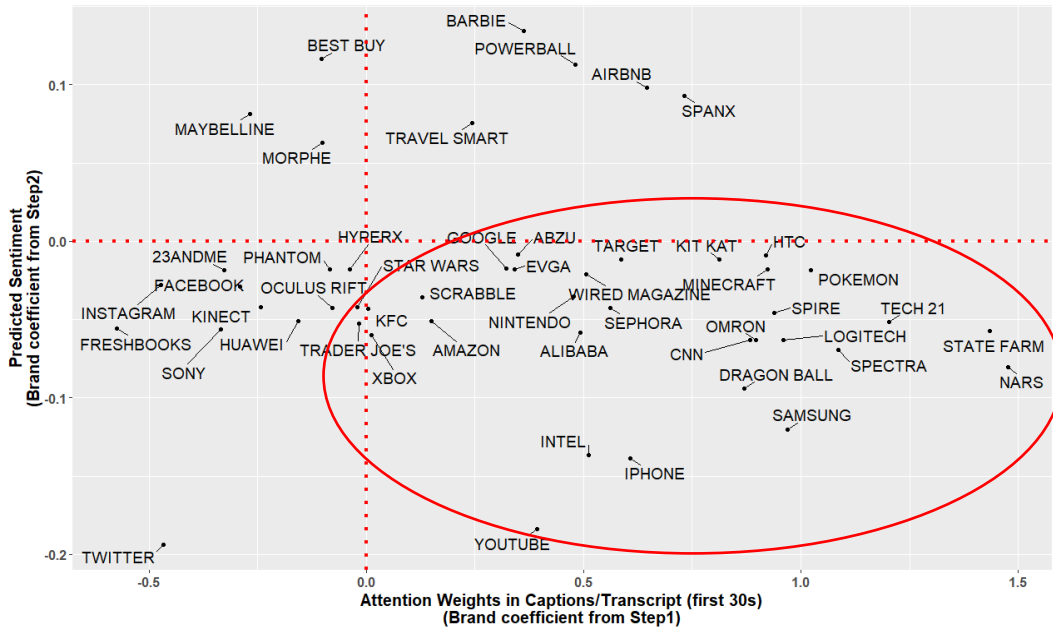


Figure 3.14: Brand Heterogeneity (brand mention in captions/transcript in first 30s vs sentiment)



CHAPTER IV – Summary & Outlook

Overall, my dissertation adds to the small but growing body of work on modeling viewer behavior on streaming platforms. It provides solutions and identifies strategies that can improve the welfare of viewers, platform owners, influencers and brand partners. Specifically, the first essay investigates the implications of increase in consumer control vis-à-vis content consumption on streaming media. To the best of my knowledge, this essay is the first attempt at providing a solution for advertising scheduling in such settings. Specifically, it provides an approach for streaming providers to explore the tradeoff between content consumption and ad exposure in order to provide a balanced viewing experience. The recommendations from this approach are available at the granular level of an individual viewer-session. The approach also uses state-of-the-art methods such as machine learning, but more importantly allows for causal inference via the use of instrumental variables and provides increased interpretability of the estimates.

The second essay focuses on an important and growing marketing mechanism, influencer marketing. This essay investigates how the elements of influencer videos (across text, audio and images) are related to outcomes that both influencers and marketers care about. Methodologically, the essay develops a novel deep learning strategy that avoids making a tradeoff between interpretability and predictive ability. After carrying out predictions using unstructured data, interpretation is carried out ex-post by quantifying the attention paid on word-pieces in text, moments in audio and items in images while forming an association with an outcome. This information is used to find significant positive (significant) relationships between video elements and attention (gradients), followed by the determination of significant relationships between video elements and the predicted outcome of interest. An added benefit of this approach is that it allows filtering out relationships that are affected by confounding factors unassociated with an increase in attention. This significantly reduces the effort required for further causal work.

Overall, both essays use state-of-the-art machine learning techniques – causal tree-based learning and interpretable deep learning to answer substantive questions in the domain of ad-supported streaming media. While the first essay investigates the implications of ad scheduling in streaming environments, the second essay focuses on the implications of the choice of video features. Together, they provide a comprehensive perspective on the role of advertising and video design in streaming media. The approach

used in both essays can be also applied to other video streaming platforms or platforms where consumers have control over content consumption, e.g., news media consumption.

Going forward there are some important research questions in this domain that can be investigated further. First, a comprehensive ad scheduling framework that allows the simultaneous optimization of different parameters of ad targeting can be developed. Second, it would be important to examine the evolution of brand usage in influencer videos over time and how this systematically differs between micro and mega-influencers. Third, understanding how “model” attention correlates with “visual” or eye-tracking attention in the context of streaming videos can help marketers develop more cost-effective solutions for their clients. Fourth, understanding the differences between video/ad characteristics in live-streamed videos and recorded videos can help quantify the advantage or disadvantage of going live. Last, research that examines the evolving relationship between AI influencers and viewers could shed light on how consumer needs and desires are going to evolve with the increasing omnipresence of AI.

APPENDICES

APPENDIX A – Appendix to Chapter II

Appendix A.1: Details on Bingeability and Ad Tolerance

I present three more illustrative examples of session viewing behavior and application of the Bingeability and Ad Tolerance metric. In the first row of each illustration, ‘light gray shaded boxes’ denote *Ad Time*, and ‘white shaded boxes’ denote *Content Time*. In the second row of each illustration, ‘white shaded dashed line boxes’ denote *Session Time*, and the ‘black shaded boxes’ (in Example C) indicate the beginning of the next episode. All values are in minutes.

Example A

A 23 min episode of Family Guy	<table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td style="width: 33%; text-align: center;">13</td> <td style="width: 33%; text-align: center;">0.50</td> <td style="width: 33%; text-align: center;">6</td> <td style="width: 33%; text-align: center;">0.50</td> <td style="width: 33%; text-align: center;">2</td> </tr> <tr> <td style="text-align: center;">13</td> <td colspan="2" style="text-align: center;">6.5</td> <td colspan="2" style="text-align: center;">2.50</td> </tr> </table> -----Block 1----- -----Block 2 ----- -----Block 3-----		13	0.50	6	0.50	2	13	6.5		2.50	
13	0.50	6	0.50	2								
13	6.5		2.50									
Bingeability: 1	No Skipping: $Content\ Length_i - 5\ min \leq Content\ Time_i$ Episode 1: $23 - 5 \leq 21$	No Excessive Fast-forwarding: $Content\ Time_i \leq Session\ Time_i - Ad\ Time_i$ Episode 1: $21 \leq 22 - 1$										
Ad Tolerance: - 8 min	$\sum_{j=1}^{n_p} (PodDuration_j + ConEnd_j - (CalPod_j - PodDuration_{j-1}))$	Pod 1: $0.5 + (6 + 2) - (13 - 0) = -4.5$ Pod 2: $0.5 + 2 - (6.5 - 0.5) = -3.5$										

Example A shows the behavior of a viewer watching one 23-minute episode of ‘Family Guy’. The first row shows blocks of time spent watching content (in white) and ads (in light gray). The viewer’s

viewing experience was interrupted by two ads that were 0.50 minutes long. The first ad was shown after the viewer viewed 13 minutes of content, and the second ad was shown after the viewer viewed 6 additional minutes of content. After the last ad, the viewer viewed 2 more minutes of content and the session ended. The second row denotes the calendar time spent corresponding to the blocks of time in the first row. In Example A, the calendar time spent in each block is equal to the sum of content time and ad time in the corresponding block. By substituting the values of Example A in equation (2.1), I get,

$$\overbrace{22 \text{ minutes}}^{\text{Session Time}} = \overbrace{21 \text{ minutes}}^{\text{Content Time}} + \overbrace{1 \text{ minute}}^{\text{Ad Time}} + \overbrace{0 \text{ minutes}}^{\text{Filler Content Time}} + \overbrace{\text{Unmeasured}}^{\text{Pauses - Fast Forward + Rewind}}$$

As the value of the measured variable on the Left-Hand-Side of the above equation is the same as sum of the measured variables on the Right-Hand-Side of the equation, the sum of the unmeasured variables is 0 minutes.

Second, both the conditions of the Bingeability metric are satisfied. As I see no evidence of skipping or excessive fast-forwarding behavior, the value of Bingeability is 1. Third, I discuss the construction of the Ad Tolerance metric in detail for Example A. I begin by adding the duration of the first pod which is 0.5 minutes to the amount of content viewed in the remainder of the session (after the end of the pod), which is $6 + 2 = 8$ minutes. I then subtract the calendar time that has elapsed since the beginning of the session, $CalPod_j$, which is 13 minutes. As there was no pod before this, I have a null value for $PodDuration_{j-1}$. Thus, the total value of the metric for the first pod is -4.5 minutes. Now, I repeat the same process for the second pod which is also 0.5 minutes in duration. To this I add the content time viewed in the remainder of the session which is 2 minutes. I then subtract the difference between the calendar time elapsed since the beginning of the previous pod and the duration of the previous pod, which is $6.5 - 0.5 = 6$. Thus, the total value of the metric for the second pod is -3.5 minutes. On summing up the values corresponding to each pod, I get a total Ad Tolerance value of $-4.5 - 3.5 = -8$ minutes. A negative value of Ad Tolerance suggests that the viewer ended a session after exposure to a commercial pod which was preceded (at some point) by a long period of no ad exposure. This is true in Example A where content time between pods (or the period of no ad exposure) was initially large at 13 minutes, and then reduced to 6 minutes, followed by 2 minutes.

Example B

B 43 min episode of Chuck	<table border="1" style="width:100%; text-align:center;"> <tr> <td style="width:5%;">3</td><td style="width:5%;">0.5</td><td style="width:5%;">6</td><td style="width:5%;">0.25</td><td style="width:5%;">8</td><td style="width:5%;">0.25</td><td style="width:5%;">9</td><td style="width:5%;">0.25</td><td style="width:5%;">6</td><td style="width:5%;">0.25</td><td style="width:5%;">7</td><td style="width:5%;">0.25</td><td style="width:5%;">2</td><td style="width:5%;">2</td> </tr> <tr> <td>7</td><td>6.5</td><td>8.25</td><td>10</td><td>5</td><td>7.25</td><td>10</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td> </tr> </table>														3	0.5	6	0.25	8	0.25	9	0.25	6	0.25	7	0.25	2	2	7	6.5	8.25	10	5	7.25	10							
	3	0.5	6	0.25	8	0.25	9	0.25	6	0.25	7	0.25	2	2																												
	7	6.5	8.25	10	5	7.25	10																																			
B1 -----Block 2----- -----Block 3----- -----Block 4----- -----Block 5----- -----Block 6----- -----Block 7-----																																										
Bingeability: 1	No Skipping: $Content\ Length_i - 5\ min \leq Content\ Time_i$							No Excessive Fast-forwarding: $Content\ Time_i \leq Session\ Time_i - Ad\ Time_i$																																		
	Episode 1: $43 - 5 \leq 41$							Episode 1: $41 \leq 54 - 1.75$																																		
Ad Tolerance: 74.25 min	$\sum_{j=1}^{n_p} (PodDuration_j + ConEnd_j - (CalPod_j - PodDuration_{j-1}))$							Pod 1: $0.5 + (6 + 8 + 9 + 4.75 + 7 + 2) - (7 - 0) = 30.25$ Pod 2: $0.25 + (8 + 9 + 4.75 + 7 + 2) - (6.5 - 0.5) = 25$ Pod 3: $0.25 + (9 + 4.75 + 7 + 2) - (8.25 - 0.25) = 15$ Pod 4: $0.25 + (4.75 + 7 + 2) - (10 - 0.25) = 4.25$ Pod 5: $0.25 + (7 + 2) - (5 - 0.25) = 4.5$ Pod 6: $0.25 + 2 - (7.25 - .25) = -4.75$																																		

Example B shows the behavior of a viewer watching one 43-minute episode of ‘Chuck’. The viewer’s viewing experience was interrupted by 6 ads shown in the light gray shaded boxes. The content time spent in the first block is 3 minutes, but the calendar time is 7 minutes. A higher value of calendar time suggests that time was spent in pauses or rewinds in this block. This is similarly observed in block 4 and block 7. In block 5, the calendar time spent is 5 minutes, which is less than the sum of ad time and content time (totaling 6.25 minutes) in the corresponding block. A lower value of calendar time suggests that time was spent in fast-forwards in this block. By substituting the values of Example B in equation (2.1), I get,

$$\overbrace{41\ \text{minutes}}^{\text{Content Time}} + \overbrace{1.75\ \text{minutes}}^{\text{Ad Time}} + \overbrace{0\ \text{minutes}}^{\text{Filler Content Time}} + \overbrace{\text{Unmeasured}}^{\text{Pauses - Fast Forward + Rewind}} = \overbrace{54\ \text{minutes}}^{\text{Session Time}}$$

On solving the above equation, I find that the sum of the unmeasured variables is 11.25 minutes. This indicates that more time was spent in pauses or rewinds than in fast-forwards in this session. Second, both the conditions of the Bingeability metric are satisfied. As I see no evidence of skipping or excessive fast-forwarding behavior, the value of Bingeability is 1. Third, I adopt a similar process to calculate Ad Tolerance as done in Example A. It is important to note the use of ‘Caveat 1’ in block 5 of Example B where there is evidence of fast-forwarding behavior: $ConEnd_j$ is chosen as $Session\ Time - Ad\ Time$, $5 - 0.25 = 4.75$ minutes, because it is less than $Content\ Time$ of 6 minutes. I get a total Ad Tolerance value of 74.25 minutes.

Example C

C 45 min episode of Rescue Me	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 10%;">0.30</td> <td style="width: 20%;">11.5</td> <td style="width: 10%; background-color: black;"></td> <td style="width: 10%;">7</td> <td style="width: 10%;">0.50</td> <td style="width: 20%;">20</td> <td style="width: 10%;">0.50</td> <td style="width: 10%;">2.5</td> </tr> <tr> <td colspan="3">11.80</td> <td>7</td> <td colspan="2">22.5</td> <td colspan="2">1</td> </tr> </table>								0.30	11.5		7	0.50	20	0.50	2.5	11.80			7	22.5		1	
	0.30	11.5		7	0.50	20	0.50	2.5																
11.80			7	22.5		1																		
	<p style="text-align: center;"> -----Block 1----- --Block 2-- -----Block 3----- ----Block 4---- </p>																							
Bingeability: 1	No Skipping: $Content Length_i - 5 \text{ min} \leq Content Time_i$				No Excessive Fast-forwarding: $Content Time_i \leq Session Time_i - Ad Time_i$																			
	Episode 1: $45 - 5 \not\leq 11.5$ Episode 2: $45 - 5 \not\leq 29.5$				Episode 1: $11.5 \leq 11.80 - 0.30$ Episode 2: $29.5 \leq 30.5 - 1$																			
Ad Tolerance: 20.80 min	$\sum_{j=1}^{n_p} (PodDuration_j + ConEnd_j - (CalPod_j - PodDuration_{j-1}))$				Pod 1: $0.30 + (11.5 + 7 + 20 + 0.5) - (0 - 0) = 39.30$ Pod 2: $0.50 + (20 + 0.50) - (18.80 - 0.30) = 2.5$ Pod 3: $0.50 + 0.50 - (22.50 - 0.50) = -21$																			

Example C shows the behavior of a viewer watching two 45-minute episodes of ‘Rescue Me’. However, the viewer watches only 11.5 minutes of the first episode and 29.5 minutes of the second episode. There is also evidence of pauses or rewind in block 3 and fast-forwarding in block 4 because there is mismatch between the calendar time spent and the sum of content time and ad time in those blocks. It is important to note that evidence of fast-forwarding behavior in block 4 could be for the content that was rewound in block 3. This is because each block in the illustration does not denote unique content being viewed due to possible rewinds and fast-forwards by the viewer. By substituting the values of Example C in equation (2.1), I get,

$$\underbrace{42.3 \text{ minutes}}_{\text{Session Time}} = \underbrace{41 \text{ minutes}}_{\text{Content Time}} + \underbrace{1.30 \text{ minutes}}_{\text{Ad Time}} + \underbrace{0 \text{ minutes}}_{\text{Filler Content Time}} + \underbrace{\text{Unmeasured}}_{\text{Pauses - Fast Forward + Rewind}}$$

On solving the above equation, I find that the sum of the unmeasured variables is 0 minutes, but as mentioned earlier I find definite evidence of fast-forwards, and pauses or rewinds. Second, the first condition (no skipping) of the Bingeability metric is not satisfied in both Episode 1 and 2. As none of the episodes in the session were viewed completely, the value of Bingeability is 0. Third, I adopt a similar process to calculate Ad Tolerance as done in Example A. I also use ‘Caveat 1’ in block 4 where there is evidence of fast-forwarding behavior. I get a total Ad Tolerance value of 20.80 minutes.

Appendix A.2: Hulu Data Collection Methodology

In the raw data, a ‘playback ping’ from the Hulu server records the amount of content viewed since the previous ‘playback ping.’ Similarly, the ‘revenue ping’ records the amount of ad viewed since the previous ‘revenue ping.’ ‘Playback ping’ and ‘revenue ping’ occur at periodic brief intervals and need not be in chronological order with respect to the other. For example, a ‘playback ping’ could fall in between successive ‘revenue pings.’ As content cannot be viewed in between an ad, I record the content viewed till this ‘playback ping’ as occurring before the commencement of that respective block of ‘revenue pings.’ In situations when the ‘playback ping’ occurs after the last ‘revenue ping’ (in a block of consecutive revenue pings), I carry out the following data manipulation: “Calculate the calendar time and content time captured between these two pings, and then take the difference between the two. If the difference is negative, I add the absolute value of the difference to the amount of content viewed before the commencement of the ad.” Thus, for these brief instances (where the difference is negative) right after the end of an ad, I assume no presence of fast-forwarding behavior because it is less likely. In addition, on 6.7% of the occasions, the amount of ad (pod) watched is registered as greater than the ad (pod) length due to potential errors in the recording of data by the streaming provider. In these cases, I increase the ad (pod) length to match the ad (pod) watched.

Appendix A.3: Using Different Weights in the Ad Tolerance Metric

As mentioned in subsection “Metric Development”, I had set each of the weights of the three components of the Ad Tolerance metric to 1. I test a few different scenarios using other combinations of weights and analyze their effect on the optimized frequency of ad exposure. This is shown in Table A3. The first scenario assumes that viewers weigh the time spent watching a pod twice as much as the other two components of the metric. The second scenario assumes that viewers weigh the time spent watching content after the end of a pod, half as much as the other two components. The third scenario assumes that viewers weigh the difference between the calendar time elapsed since the beginning of the previous pod and the duration of the previous pod, twice as much as the other two components of the metric. For each scenario, I calculate new values of the Ad Tolerance metric, and update the past predictors in Table 2.6d that correspond to functions for Ad Tolerance Sum, Positive Ad Tolerance Indicator and Ad Tolerance Session Count. Next, I run the first-stage and second-stage of the model, follow the steps of the Ad Decision Tree and then run the optimization procedure. The recommended spacing for the set of observations in each scenario is compared with the recommend spacing for the corresponding set of observations in the original scenario that had all weights set to 1. The mean absolute difference (MAD) for these comparisons are also shown in Table A1. The low value of MAD (≤ 1 minute) indicates that my optimization process is robust to the choice of values of the weights (in the range considered).

Table A1: Different weight combinations of the components of the Ad Tolerance Metric
(MAD (min) on comparing recommended spacing in each scenario with the original recommended spacing)

Scenario	Description	w_1	w_2	w_3	MAD (minutes) Holdout 1	MAD (minutes) Holdout 2
1	$PodDuration_j$ is weighed 2 times the other components	2	1	1	0.88	0.73
2	$ConEnd_j$ is weighed 0.5 times the other components	2	1	2	0.96	0.89
3	$CalPod_j - PodDuration_{j-1}$ is weighed 2 times the other components	1	1	2	1.00	0.91

Appendix A.4: Metric Validity

A.4.1 Bingeability

I apply both the Episode Count metric and the Bingeability metric to my sample and examine the cases of mismatch between them in Table A2. Bingeability is different from Episode Count for 45.4% of the sessions, 89.8% of viewers, 96.2% of TV shows and 94.4% of genres. While the mismatch seems to be frequent, it is mainly a consequence of skipping behavior and not excessive fast-forwarding behavior. Skipping behavior is 26 times more likely than excessive fast-forwarding behavior across all sessions.

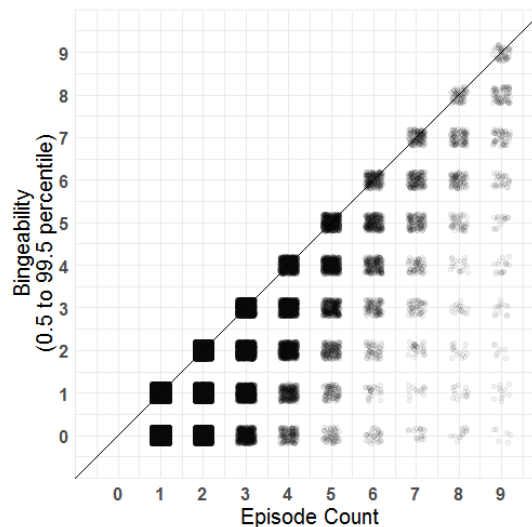
Table A2: Evidence of Skipping and Excessive Fast-Forwarding

	N (Total count)	Skipping (S)	Excessive Fast-Forwarding (FF)	Both ($S \cap FF$)	Total ($S \cup FF$)
Sessions	110,500	45.0%	1.7%	1.3%	45.4%
Viewers	6,157	89.7%	13.6%	13.4%	89.8%
TV shows	558	96.2%	46.0%	46.0%	96.2%
Genre	18	94.4%	88.8%	88.8%	94.4%

I show the relationship between the 0.05th and 99.5th percentile range of Bingeability and Episode Count in Figure A1. The darker the color of the square, more are the number of points located there. For example, when Episode Count is 7, there are more instances when Bingeability is 7 than 1.

Figure A1: Bingeability versus Episode Count

(0.5th to 99.5th percentile of Bingeability)



Now, I compare the trend in viewership of episodes across all 558 TV shows on a weekly (and monthly) basis using both Episode Count and Bingeability. Trends for both the metrics are compared to check whether they are both increasing, decreasing or constant. I find that the weekly (and monthly) trends in viewership popularity are mismatched 21.1% (and 14.7%) of the time across 72.8% (and 26.3%) of TV shows viewed in my sample. This tells me that inferences about the trend in viewership can change based on the metric one decides to use. By counting episodes which are not completely watched, Episode Count typically overstates the popularity of a TV show. Bingeability quantifies the immersive experience and presents a more conservative estimate of the popularity level. The Bingeability metric by itself can be useful to various streaming platforms, production studios, advertisers and data measurement companies who would like to measure the trend in popularity of TV shows streamed on platforms.

A.4.2 Ad Tolerance

I check whether the Ad Tolerance metric can capture differences in behavioral consumption patterns. For illustration, consider six sessions of six different viewers in Table A3 where each session is spent viewing 15 minutes of content in addition to ad exposure that is assumed to be randomly delivered. For ease of exposition, I assume there are no instances of fast-forwards, rewinds or pauses in each session.

Table A3: Examples of viewing behavior in a session

Session	Illustration	Ad Tolerance (min)	Ad Exposure (min)	Number of Pods							
Viewer 1	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 33.33%; text-align: center;">2.5</td> <td style="width: 33.33%; text-align: center;">0.50</td> <td style="width: 33.33%; text-align: center;">12.5</td> </tr> </table> --B1- -----Block 2-----	2.5	0.50	12.5	10.5	0.50	1				
2.5	0.50	12.5									
Viewer 2	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 33.33%; text-align: center;">7.5</td> <td style="width: 33.33%; text-align: center;">0.50</td> <td style="width: 33.33%; text-align: center;">7.5</td> </tr> </table> -----Block 1----- -----Block 2-----	7.5	0.50	7.5	0.5	0.50	1				
7.5	0.50	7.5									
Viewer 3	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 66.66%; text-align: center;">12.5</td> <td style="width: 16.66%; text-align: center;">0.50</td> <td style="width: 16.66%; text-align: center;">2.5</td> </tr> </table> -----Block 1----- -----Block 2-----	12.5	0.50	2.5	-9.5	0.50	1				
12.5	0.50	2.5									
Viewer 4	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 16.66%; text-align: center;">2.5</td> <td style="width: 16.66%; text-align: center;">0.50</td> <td style="width: 16.66%; text-align: center;">2.5</td> <td style="width: 16.66%; text-align: center;">0.50</td> <td style="width: 16.66%; text-align: center;">2.5</td> <td style="width: 16.66%; text-align: center;">0.50</td> <td style="width: 16.66%; text-align: center;">7.5</td> </tr> </table> B 1-- ----Block 2---- ----Block 3---- -----Block 4-----	2.5	0.50	2.5	0.50	2.5	0.50	7.5	26.5	1.50	3
2.5	0.50	2.5	0.50	2.5	0.50	7.5					

Viewer 5	<table border="1"> <tr> <td>3.75</td> <td>0.50</td> <td>3.75</td> <td>0.50</td> <td>3.75</td> <td>0.50</td> <td>3.75</td> </tr> </table>	3.75	0.50	3.75	0.50	3.75	0.50	3.75	12.75	1.50	3
	3.75	0.50	3.75	0.50	3.75	0.50	3.75				
---B 1--- -----Block 2----- -----Block 3----- -----Block 4-----											
Viewer 6	<table border="1"> <tr> <td>7.5</td> <td>0.50</td> <td>2.5</td> <td>0.50</td> <td>2.5</td> <td>0.50</td> <td>2.5</td> </tr> </table>	7.5	0.50	2.5	0.50	2.5	0.50	2.5	4	1.50	3
	7.5	0.50	2.5	0.50	2.5	0.50	2.5				
-----Block 1----- ---Block 2--- ---Block 3--- ---Block 4---											

Viewer 1 is exposed to an ad of length 0.5 minutes after viewing 2.5 minutes of content. After the end of the ad, the viewer views 12.5 more minutes of content and the session ends. Viewer 2 is exposed to an ad in the middle of her session while Viewer 3 is exposed to an ad after viewing 12.5 minutes of content. Across the first three sessions, I observe that Viewer 3 had the most time (12.5 min) to adapt to the absence of ads and viewed the least amount of content (2.5 min) after the final ad. Hence, Viewer 3 can be expected to have the lowest Ad Tolerance. Similarly, across the first three sessions, Viewer 1 had the least time (2.5 min) to adapt to the absence of ads and viewed the most content (12.5 min) after it, and hence can be expected to have the highest Ad Tolerance.

In the last three sessions, Viewer 4 is exposed to 3 ads in small intervals in the first half of her session, Viewer 5 is exposed to 3 ads at equally spaced intervals and Viewer 6 is exposed to 3 ads in small intervals in the second half of the session. Across all the six sessions, I observe that Viewer 3 had the most time (12.5 min) to adapt to the absence of ads and was exposed to only one ad in total. Hence, Viewer 3 can be expected to have the lowest Ad Tolerance overall. While both Viewer 1 and Viewer 4 had the least amount of time (2.5 min) to adapt until the first ad, Viewer 4 was exposed to two additional ads and still ended up watching 15 minutes of content in total. Hence Viewer 4 can be expected to be have the highest Ad Tolerance. Overall, I can observe that if ads are bunched together in the beginning of a session, Ad Tolerance is the highest, whereas if the session ends shortly after viewing an ad which was preceded by a long period of no ad exposure, then the Ad Tolerance is the lowest.

I can compare the Ad Tolerance metric for the six sessions with the simple measures of ‘minutes of ad exposure’ and ‘number of pods’ in Table A4. I observe that the simple measures are unable to distinguish between the first three cases or between the last three cases, whereas the Ad Tolerance metric gives me a unique value for each of the six cases. Thus, I showed that Ad Tolerance is able to capture differences in behavioral consumption patterns (assuming randomness in ad delivery) in an intuitive manner, thereby lending further validity to the construction of the metric. Non-randomness in ad delivery

is controlled with the help of instrumental variables in my model, which is detailed in the subsection “Model”.

Lastly, using my dataset, I conduct a principal component analysis (with varimax rotation) on the two metrics and the ‘number of pods’, ‘minutes of ad exposure’ and ‘minutes of content viewed’. I choose three factors and present their loadings for each variable in Table A4. I find that the factor loadings for ‘number of pods’, ‘minutes of ad exposure’ and ‘minutes of content viewed’ are very similar and are dominated by the first factor. On the other hand, Bingeability and Ad Tolerance are dominated by the third and second factor respectively. This analysis further demonstrates that the two metrics are capturing different latent constructs.

Table A4: Factor Loadings from a Principal Component Analysis

	Factor 1	Factor 2	Factor 3
Bingeability	0.44	0.30	0.85
Ad Tolerance	0.41	0.87	0.29
Number of pods shown	0.82	0.37	0.38
Minutes of ad exposure	0.81	0.40	0.38
Minutes of content viewed	0.76	0.40	0.43

Appendix A.5: Modelling Correlation Between Outcomes

I model correlation between the two outcomes—Bingeability and Ad Tolerance—using the regressor chain approach (Melki et al., 2017). It involves incorporating the predicted value of an outcome as a covariate to predict another outcome which results in the formation of a chain. This can be formalized by modifying equation (2.7) in subsection “Model” as follows:

$$Y_{1t} = f_2(\hat{Y}_{2t}, \hat{X}_{1t}, \hat{X}_{2t}, \hat{X}_{3t}, \hat{X}_{4t}, W_{1t}, W_{2t}) + u_t$$

$$Y_{2t} = f_1(\hat{Y}_{1t}, \hat{X}_{1t}, \hat{X}_{2t}, \hat{X}_{3t}, \hat{X}_{4t}, W_{1t}, W_{2t}) + u_t$$

where \hat{Y}_{1t} and \hat{Y}_{2t} are the predictions from the original model that are added as covariates to predict Y_{2t} and Y_{1t} respectively. Such an approach allows me to capture the correlational influence of one outcome on the other. The final predictions of the outcomes from the regressor chain approach are then used as inputs to the Ad Decision Tree, which is followed by running the optimization procedure. Subsequently I construct a corresponding Decision Support System whose results are shown in Figures A2.1, A2.2 and A2.3 which are analogous to Figures 2.9a, 2.9b and 2.9c.

The graphs show that for future sessions of current viewers (Holdout 1), the platform and its viewers are better-off if the platform uses a threshold of 0 to show ads. This results in a 47.5% increase in ad exposure as compared to observed ad exposure and a 7.19% increase in Bingeability as compared to initial predicted Bingeability (or a 9.77% increase in Bingeability as compared to observed Bingeability). Similarly, for new viewers (Holdout 2), the platform and its viewers are better-off if the platform uses a threshold of 0 to show ads. This results in a 51.0% increase in ad exposure as compared to observed ad exposure and a 0.93% increase in Bingeability as compared to initial predicted Bingeability (or a 1.14% decrease in Bingeability as compared to observed Bingeability). This indicates that by capturing correlation between outcomes for new viewers for whom viewer fixed effects are not known, a best threshold of 0 to show ads can be achieved. In addition, the presence of an increase of 0.93% in comparison with initial predicted Bingeability but a decrease of 1.14% in comparison with observed Bingeability suggests that there are unobserved covariates that influence observed Bingeability, whose effect cannot be completely captured by modelling correlation between outcomes.

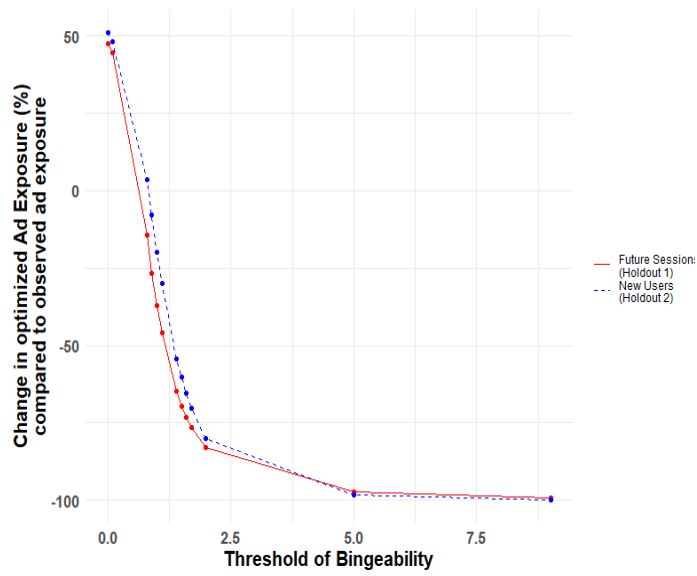


Figure A2.1: Percentage change in optimized ad exposure (\tilde{n}) as compared to observed ad exposure (n)

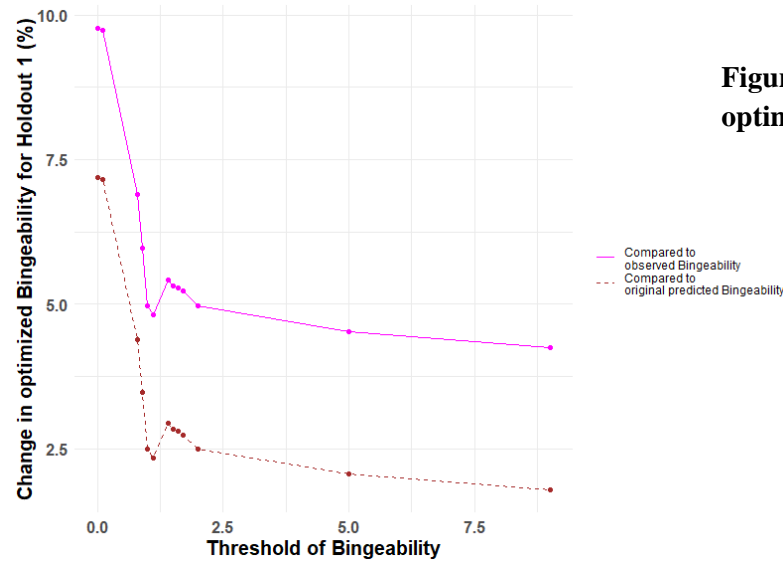


Figure A2.2: Percentage change in optimized Bingeability (\tilde{b}) for Holdout 1

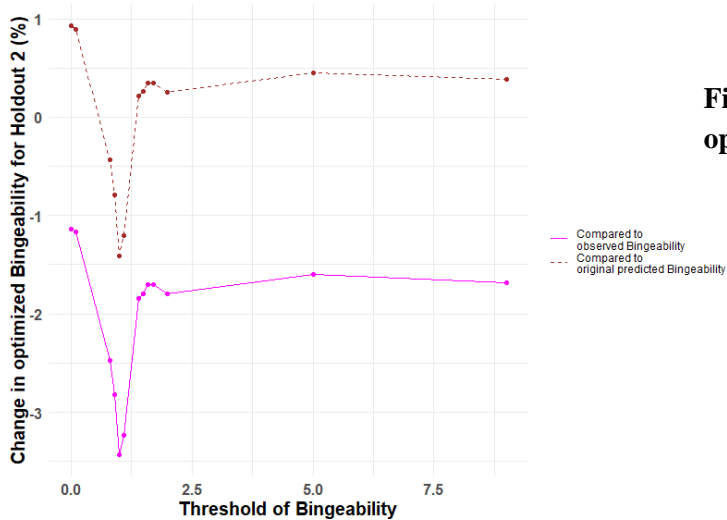


Figure A2.3: Percentage change in optimized Bingeability (\tilde{b}) for Holdout 2

Appendix A.6: Tree Based Methods And Simulated Data

A6.1 Boosting and Random Forests

Boosting or Boosted Regression Trees refer to a weighted linear combination of regression trees, with each tree trained greedily in sequence to improve the final output (J. Friedman, 2002). This output can be presented as follows:

$$F_N(x) = \sum_{k=1}^N \alpha_k f_k(x)$$

where, $f_k(x)$ is the function modelled by the k^{th} regression tree, and α_k is the weight associated with it. The value of f_k and α_k are learnt during model training. I adopt a recent extension of gradient boosting called Extreme Gradient Boosting (XGBoost) because it is a powerful method for making predictions with structured data (Chen & Guestrin, 2016). For the set of points (x_i, y_i) , and a loss function $l(y_i, \hat{y}_i)$, the XGBoost model minimizes an objective function \mathcal{L} to find the step-wise value of $f_k(x)$. For my application, the loss function $l(y_i, \hat{y}_i)$ is the least squares error when the outcome is Ad Tolerance which is continuous, and negative log likelihood when the outcome is Bingeability which is a count. The objective function \mathcal{L} can be represented as follows:

$$\mathcal{L} = \sum_i l(y_i, \hat{y}_i) + \sum_k \Omega(f_k)$$

where Ω is the regularization parameter that penalizes the complexity of the model (see Chen and Guestrin (2016) for details on the objective function). If I set the regularization parameter to 0, I would get the traditional gradient boosting model. At each step, Newton's method computes the new value of f_k that minimizes the average value of the objective function. The step-wise iterations can be shown as follows:

$$F_k(x) = F_{k-1}(x) - \eta(H_k)^{-1} \cdot g_k$$

where η is the learning rate, g_k with components $g_{ik} = \left[\frac{d\mathcal{L}(y_i, F(x_i))}{dF(x_i)} \right]_{F(x_i)=F_{k-1}(x_i)}$ is the gradient of the objective function and H_k is the second order gradient of the objective function. XGBoost has a faster computation time than conventional gradient boosting because it employs parallel processing using all the cores of the computer.

Random Forests refer to the average of thousands of distinct regression trees (Breiman, 2001). Unlike gradient boosting which uses weak learners or shallow trees at each step, Random Forests average

multiple deep trees. Each regression tree is different because it is constructed on a different training sample by sub-sampling on both observations and covariates. The output of Random Forests can be represented as follows:

$$F_{avg}(x) = \frac{1}{N} \sum_{k=1}^N f_k(x)$$

where, $f_k(x)$ is the function modelled by the k^{th} regression tree, which is learnt during model training.

A6.2 Simulation

I simulate data to match the distribution of my real data. Using simulated data, I can create the ground truth, i.e. I know the extent to which the outcome variable is influenced by the observed covariates in the model. Hence, I can compare performance of different models in terms of their ability to make predictions that are closest to the ground truth. I adopt an approach similar to Hartford et al. (2017) to create my simulated data. I let the source of endogeneity be represented by $v \sim N(1,0.1)$ and the four instruments be represented by $z_1 \sim N(1, 0.1)$, $z_2 \sim N(1, 0.1)$, $z_3 \sim N(1, 0.1)$ and $z_4 \sim N(1, 0.1)$. The spacing rule (sr) is represented as follows:

$$sr \sim \max(W_1 + 2v + 13z_1 - 17, 0)$$

$$W_1 \sim \alpha_1 N(9.1, 1.5) + (1 - \alpha_1)U(0,0)$$

$$\alpha_1 \sim \text{Bern}(0.85)$$

The correlation between sr and z_1 is 0.34 which is close to the correlation of 0.35 in the real data. The median value of the simulated and real distribution of sr is the same at 6.6 min. The length rule (lr) is represented as follows:

$$lr \sim W_2 - \frac{v}{4} + \frac{z_2}{4}$$

$$W_2 \sim \gamma_2 N(0.38, 0.01) + (1 - \gamma_2)(\alpha_2 N(0.25, 0.002) + (1 - \alpha_2)N(0.5, 0.002))$$

$$\alpha_2 \sim \text{Bern}(0.4)$$

$$\gamma_2 \sim \text{Bern}(0.2)$$

The correlation between lr and z_2 is 0.22 which is close to the correlation of 0.25 in the real data. The median value of the simulated and real distribution of lr is the same at 0.42 min. The diversity rule (dr) is represented as follows:

$$dr \sim W_3 - v + z_3$$

$$W_3 \sim \alpha_3 U(0.15, 1) + (1 - \alpha_3) U(1, 1)$$

$$\alpha_3 \sim Bern(0.5)$$

$$dr = \begin{cases} 0.05, & dr \leq 0.05 \\ 1, & dr \geq 1 \end{cases}$$

The correlation between sr and z_3 is 0.25 which is close to the correlation of 0.27 in the real data. The median value of the simulated and real distribution of dr is 0.86 and 0.87 respectively. The clumpiness rule (cr) is represented as follows:

$$cr \sim W_4 - 1.1v + 1.3z_4$$

$$W_4 \sim \gamma_4 (\alpha_4 N(0.05, 0.02) + (1 - \alpha_4) U(0.3, 0.99)) + (1 - \gamma_4) U(1, 1)$$

$$\alpha_4 \sim Bern(0.9)$$

$$\gamma_4 \sim Bern(0.8)$$

$$cr = \begin{cases} 0, & dr \leq 0 \\ 1, & dr \geq 1 \end{cases}$$

The correlation between cr and z_4 is 0.29 which is close to the correlation of 0.33 in the real data. The median value of the simulated and real distribution of cr is 0.33 and 0.30 respectively.

The outcome variable Bingeability (y_1) is simulated to have a complex non-linear relationship with the covariates. It is represented as follows:

$$y_1 \sim Poisson(\lambda)$$

$$\lambda = \max\left(\frac{\alpha_{it}}{50} + 0.2sr_t - 0.8lr_t - 1.5dr_t + 0.5W_{1t}^{W_{2t}} - 2W_{2t}^2 + \exp(W_{3t}) - W_{4t} - 0.2 + u_t, 0\right)$$

$$u \sim N(\rho v, 1 - \rho^2)$$

u is the error term that is correlated with sr , lr , dr and cr ; and ρ is the level of endogeneity which I set at 0.9. W_1, W_2, W_3 and W_4 are exogenous covariates which were defined earlier in the equation of each ad targeting rule. α_i corresponds to viewer fixed effects and I simulate 500 viewer fixed effects as follows:

$$\alpha_i = N\left(\frac{i}{10}, 0.01\right), i = \{1, \dots, 500\}$$

I ensure that the sign of the correlation between the outcome variable and the four endogenous variables in the simulated data is the same as that in the observed data.

The outcome variable Ad Tolerance (y_2) is also simulated to have a complex non-linear relationship with the covariates. It is represented as follows:

$$y_2 = \frac{\alpha_{it}}{10} - 0.05(sr - 0.9)^2 + 4000(lr - 0.4)^2 + 300e^{-4(dr+0.5)^2} - 25 +$$

$$10W_1^{W_2} - 20W_2^2 + 10 \exp(W_3) - 50W_{4t} + u$$

$$u \sim N(\rho v, 1 - \rho^2)$$

The level of endogeneity ρ is set at 0.9 as before. I again ensure that the sign of the correlation between the outcome variable and the four endogenous variables in the simulated data is the same as that in the observed data.

The first stage of the model can be represented as follows:

$$X_{1t} = sr_t = g_1(z_{1t}, z_{2t}, z_{3t}, z_{4t}, W_{1t}, W_{2t}, W_{3t}, W_{4t}, \alpha_{it}) + e_{1t}$$

$$X_{2t} = lr_t = g_2(z_{1t}, z_{2t}, z_{3t}, z_{4t}, W_{1t}, W_{2t}, W_{3t}, W_{4t}, \alpha_{it}) + e_{2t}$$

$$X_{3t} = dr_t = g_3(z_{1t}, z_{2t}, z_{3t}, z_{4t}, W_{1t}, W_{2t}, W_{3t}, W_{4t}, \alpha_{it}) + e_{3t}$$

$$X_{4t} = cr_t = g_4(z_{1t}, z_{2t}, z_{3t}, z_{4t}, W_{1t}, W_{2t}, W_{3t}, W_{4t}, \alpha_{it}) + e_{4t}$$

where, the subscript t denotes a session; e_{1t}, e_{2t}, e_{3t} , and e_{4t} are the error terms which are all equal to v_t in my simulation. The second stage of the model can be represented as follows:

$$y_{jt} = f_2(\hat{X}_{1t}, \hat{X}_{2t}, \hat{X}_{3t}, \hat{X}_{4t}, W_{1t}, W_{2t}, W_{3t}, W_{4t}, \alpha_{it}) + u_t$$

where y_j is either Bingeability (y_1) or Ad Tolerance (y_2), and $\hat{X}_{1t}, \hat{X}_{2t}, \hat{X}_{3t}, \hat{X}_{4t}$ are the fitted values from the first stage. Next, I need to determine the counterfactual function or ground truth against which the performance of different models can be compared. Let me represent this counterfactual function as h , and for each outcome variable the counterfactual function can be represented as follows:

$$h_1 \sim \text{Poisson}(\lambda_h)$$

$$\lambda_h = \max\left(\frac{\alpha_i}{50} + 0.2sr - 0.8lr - 1.5dr + 0.5W_1^{W_2} - 2W_2^2 + \exp(W_3) - W_4, 0\right)$$

$$h_2 = \frac{\alpha_i}{10} - 0.05(sr - 0.9)^2 + 4000(lr - 0.4)^2 + 300e^{-4(dr+0.5)^2} + 10W_1^{W_2} - 20W_2^2 + 10 \exp(W_3) - 50W_4$$

Note, I removed the intercept terms and the endogenous error to get the equations of the ground truth h_1 and h_2 . Next, I simulate different sizes of the data, as represented in Table A5.1, and split it into an 80% training sample and 20% holdout sample. I test the performance of three different models: XGBoost, Random Forests and Linear Regression (2SLS), in terms of their ability to get close to the ground truth, h . Note that the same model is applied on both the first and second stage. Model performance on the holdout sample is compared in terms of the RMSE between \hat{y}_1 and h_1 , and \hat{y}_2 and h_2 which is shown in Table A5. I find that XGBoost performs better than Random Forests and Linear Regression (2SLS) in getting close to the ground truth for both small and large data sizes. Hence, I use the XGBoost model to analyze my observed data.

Table A5: Comparison of Model Performance (RMSE) on holdout sample

Data Size	Bingeability			Ad Tolerance		
	Linear Regression	Random Forests	XGBoost	Linear Regression	Random Forests	XGBoost
5,000	2.12	1.93	1.90	50.48	34.75	25.97
25,000	1.90	1.88	1.84	48.81	31.74	24.72
50,000	1.89	1.88	1.82	48.04	29.55	24.82
75,000	1.88	1.88	1.82	48.43	28.97	24.61
100,000	1.87	1.87	1.81	48.64	29.50	24.66

Appendix A.7: Cross-Validation for XGBoost

The parameters of the XGBoost model for the observed data are set by cross-validation. I carry out 5-fold cross validation on the training sample by dividing viewers into five different folds. This process is repeated 10 different times with random splits made on the training data to determine the 5 folds. The parameters that are tuned are as follows:

- Maximum depth of a tree: {4,6}
- Minimum threshold for loss reduction, γ : {0,5}
- Regularization parameter on weights of a leaf: {0,1}
- Row subsampling fraction: {0.8,1}
- Column subsampling fraction at the node level: {0.8,1}

The minimum number of observations on each node of a leaf is set to 1, and the value of the learning rate η is set by judgement to ensure that the cross-validation process does not take unduly long to finish. I have $2^5 = 32$ distinct parameter combinations and 10 iterations for each parameter combination. As an exhaustive grid search for a total of 320 iterations over 74,996 observations (in the training sample) will take unduly long to finish, I use an efficient three step process to decide the final parameter combination to be used to tune the training sample.

- Step 1: I use a “fractional factorial design” to design $2^{5-2} = 8$ combinations of the parameters that are balanced and orthogonal. Then I run the cross-validation routine 10 times for these 8 combinations for a total of 80 iterations. Then I average the performance measure (e.g. RMSE or Negative Log Likelihood) across the 10 iterations for each of the 8 combinations and rank the combinations in order of best to worst performance.
- Step 2: Next, I analyze the performance across the 8 orthogonal combinations and identify other potential parameter combinations that could result in an improved cross-validation performance. I run the cross-validation routine 10 times for each of these newly identified parameter combinations. Then I average the performance measure across the 10 iterations for each of the newly identified combinations.
- Step 3: The parameter combination that leads to the lowest average value of the performance measure across the 10 repetitions for the parameter combinations in Step 1 and Step 2 is chosen to train the model.

Appendix A.8: Optimization Procedure

Part 1

My objective function is subject to the constraint of not detracting from the content consumption experience. This constraint corresponds to the equation of the Ad Tolerance metric, originally shown in equation (2.4), which is reproduced below.

$$Ad\ Tolerance = \sum_{j=1}^{n_p} (w_1 PodDuration_j + w_2 ContentEnd_j - w_3 (CalendarPod_j - PodDuration_{j-1}))$$

This constraint ensures that the optimization routine (of ad maximization) takes cognizance of the predicted values of Ad Tolerance and Bingeability, thus preventing the routine from making scheduling recommendations that can cause a reduction in the amount of content viewed. Now, I substitute the variables from equation (2.9) in the above equation, i.e. $n_p = n$; $PodDuration_j = d$; $ContentEnd_j = \hat{b}e - js$ where j is pod number; and $PodDuration_{j-1} = d$. Hence, I can rewrite the constraint corresponding to the Ad Tolerance metric as follows:

$$Ad\ Tolerance = \sum_{j=1}^n (w_1 d + w_2 (\hat{b}e - js) - w_3 (CalendarPod_j - d))$$

To substitute values into $CalendarPod_j$, I use equation (2.1) which is reproduced below:

$$\begin{aligned} & \overbrace{Session\ Time}^{\text{Measured}} \\ &= \overbrace{Content\ Time + Ad\ Time + Filler\ Content\ Time}^{\text{Measured}} + \overbrace{Pauses - Fast\ Forward + Rewind}^{\text{Unmeasured}} \end{aligned}$$

Using the variables in equation (2.9), the above equation can be rewritten as follows:

$$CalendarPod_j = \overbrace{s + d + f_j}^{\text{Measured}} + \overbrace{u_j}^{\text{Unmeasured}}$$

where, f_j is duration of filler content viewed from the beginning of the pod $j-1$ till the beginning of pod j and $u_j = (pauses - fast\ forward + rewind)_j$ is the sum of the unmeasured variables from the beginning of pod $j-1$ till the beginning of pod j . A viewer is not expected to be immersed in the viewing experience while watching filler content; hence I allow the viewer to skip it or fast forward it by setting f_j to 0. As the unmeasured variables—Pauses, Fast Forward and Rewind—are directly under viewer control

and cannot be controlled by the streaming provider, I set u_j to 0. Hence, I can rewrite the constraint (equation (2.10)) as follows:

$$\hat{a} = \sum_{j=1}^n (w_1 d + w_2 (\hat{b}e - js) - w_3 (s + d - d))$$

where the predicted value of Ad Tolerance is shown as \hat{a} . After summing over the variables, I get

$$\hat{a} = w_1 nd + w_2 \left(n\hat{b}e - \frac{n(n+1)}{2}s \right) - w_3 ns$$

Part 2

The partial derivative of \tilde{n} with respect to \hat{a} is shown below:

$$\frac{\partial \tilde{n}}{\partial \hat{a}} = \frac{1 + 2\hat{a} + 3\hat{b}e + \sqrt{\Delta}}{(1 + \hat{b}e)\sqrt{\Delta}} > 0$$

The above equation is always > 0 because $\hat{b} \geq 1$, $\hat{a} > 0$, $\sqrt{\Delta} > 0$ and $e > 0$. Thus, controlling for \hat{b} and e , an increase in Ad Tolerance results in an increase (decrease) in the number of ads \tilde{n} (spacing \tilde{s}) ($\because \tilde{s} \propto \frac{1}{\tilde{n}}$). The partial derivative of \tilde{n} with respect to \hat{b} is shown below:

$$\frac{\partial \tilde{n}}{\partial \hat{b}} = \frac{e(\hat{b}e - 3\hat{a}\hat{b}e + \sqrt{\Delta}(1 - \hat{a}) + \hat{a} - 2\hat{a}^2 - 1)}{(1 + \hat{b}e)^2 \sqrt{\Delta}}$$

On substituting the values of \hat{b} , \hat{a} and e from the observations in Set C (from Table 2.9) into the above equation, I find that the partial derivative is almost always negative. For the few instances when $\hat{a} \in (0, 0.5 \text{ min})$, the value of the partial derivative is positive. Thus, controlling for \hat{a} and e , an increase in Bingeability almost always results in a decrease (increase) in the number of ads \tilde{n} (spacing \tilde{s}). The interpretation of the partial derivative for the few instances when $\hat{a} \in (0, 0.5 \text{ min})$ can be understood as the effect of the algorithm to ensure a minimum level of Ad Tolerance before recommending a decrease (increase) in the number of ads \tilde{n} (spacing \tilde{s}) for an increase in Bingeability, \hat{b} .

Overall, the partial derivatives help illustrate the direction of the influence of the metrics on the recommended spacing \tilde{s} .

Appendix A.9: Recommended Schedule Versus A Naïve Heuristic

I develop a naïve heuristic based on viewer response to ad delivery that could be used to recommend ad spacing. As mentioned in the “Introduction” section, viewer response to ad delivery has been studied in past work by Schweidel and Moe (2016) who find that ad exposure is negatively correlated with content consumption. Hence, one naïve heuristic for a session (i) is the ratio of total time spent watching TV shows in the past week by the viewer (before the commencement of the session) to the total number of pods shown to that viewer while watching TV shows in the past week. It can be represented as follows:

$$Naive\ Spacing_i = \frac{Total\ Content\ Time_i}{Total\ Number\ of\ Pods_i}$$

The heuristic is naïve for mainly the following reasons (1) it does not incorporate the frequency (or spacing) of pod exposure in the viewing experience, as done by the Ad Tolerance metric (2) it does not account for fast-forwarding or skipping behavior, as done by the Bingeability metric, and (3) it does not control for the non-randomness in ad delivery, as done in my model using instrumental variables.

A density distribution of the naïve spacing for those sessions in Set C (from Table 2.9) is shown in Figures A3.1a and A3.1b for Holdout 1 and Holdout 2 respectively. I ignore those sessions which are the first sessions of the viewers, because the value of the naïve spacing metric will result in a ‘divide by 0’ error. The median value of the naïve spacing for Holdout 1 (future sessions of the viewers in the training sample) is 8.30 minutes and its 2.5th to 97.5th percentile range is from 4.19 to 17.96 minutes. The median value of the naïve spacing for Holdout 2 (new viewers) is 9.16 minutes and its 2.5th to 97.5th percentile range is from 5.01 to 18.11 minutes.

The distribution of the ratio of (optimized) recommended spacing and naïve spacing is shown in Figures A3.2a and A3.2b. I ignore those sessions where the naïve spacing is 0 minutes to avoid a ‘divide by 0’ error and also because they suggest showings ads continuously without any show content in between which is not meaningful. The median value of the ratio is 0.50 in Figure A3.2a and 0.47 in Figure A3.2b. As the median is a lot less than 1 (which is the 90th percentile in Figure A3.2a and 95th percentile in Figure A3.2b), I can conclude that the naïve heuristic suggests a lower frequency (longer spacing) a lot more often than the (optimized) recommendation, thus losing out on opportunities to maximize ad exposure.

Finding the ratio of the naïve spacing with the average observed spacing reveals that the median of the distribution is 1.25 for each holdout sample. This demonstrates that on average the naïve schedule recommends showing ads less frequently (with a longer spacing) as compared to observed practice. I quantify the decrease in ad exposure by using the naïve heuristic as done in the subsection “Decision

Support System” for a Bingeability threshold of 0. Ad exposure increases by -35% for Holdout 1 and by -40% for Holdout 2 as compared to observed practice. On the other hand, content consumption increases by 11.56% as compared to initial predicted Bingeability (and by 12.47% compared to observed Bingeability) for Holdout 1 and by 4.62% compared to initial predicted Bingeability (and 1.44% compared to observed Bingeability) for Holdout 2. As the naïve heuristic is unable to make both the platform and the viewers better off, it is inferior to the optimized ad schedule.

Figure A3.1a: Density of Naïve Spacing in Holdout 1

(2.5th to 97.5th percentile)

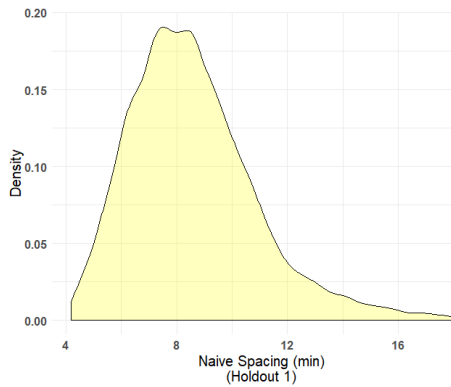


Figure A3.1b: Density of Naïve Spacing in Holdout 2

(2.5th to 97.5th percentile)

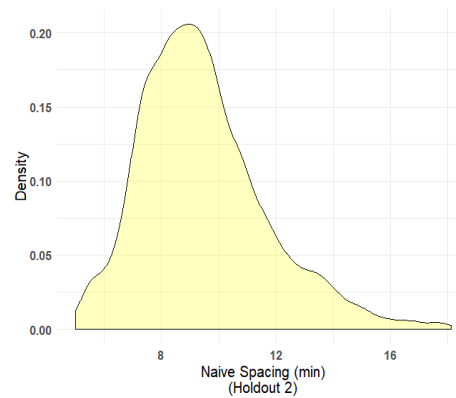


Figure A3.2a: Density of the Ratio of Recommended Spacing and Naïve Spacing in Holdout 1

(2.5th to 97.5th percentile)

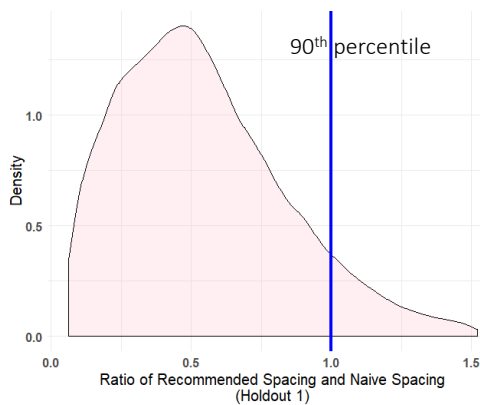
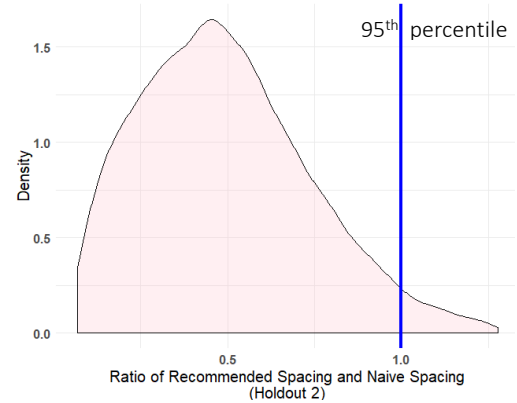


Figure A3.2b: Density of the Ratio of Recommended Spacing and Naïve Spacing in Holdout 2

(2.5th to 97.5th percentile)



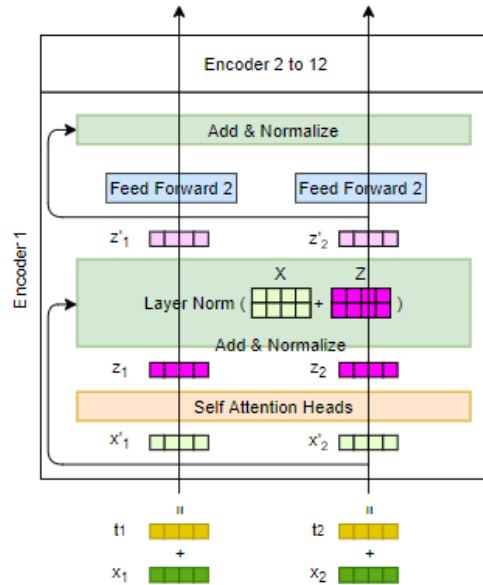
APPENDIX B – Appendix to Chapter III

Appendix B.1: BERT Encoders (in Text Model)

BERT Encoders comprise a set of 12 sequentially arranged identical encoders, and I illustrate the architecture of one encoder in Figure B1.⁷⁴ I explain an example with a sentence that has only two tokens, and this can be extended to any example that has a maximum of 512 tokens, which is the maximum limit of the pre-trained BERT model. The combined vector of the initial token embedding (x_1, x_2) and positional encoding (t_1, t_2) results in the vectors (x'_1, x'_2) that are passed through self-attention heads which incorporate information of other relevant tokens into the focal tokens. The architecture of the self-attention head is explained further ahead. The outputs of the self-attention head (z_1, z_2) are then added with the original input (x'_1, x'_2) using a residual connection (shown with a curved arrow) and normalized (using mean and variance). The outputs (z'_1, z'_2) are passed through identical feed forward networks that have a GELU (Gaussian Error Linear Unit) activation function, i.e. $gelu(x) = 0.5x \left(1 + erf \left(\frac{x}{\sqrt{2}} \right) \right)$. The gelu activation combines the advantages of the ReLU (Rectified Linear Unit) non-linearity (i.e., $relu(x) = max(0, x)$) with dropout regularization. The outputs of the feed forward network are added with the inputs (z'_1, z'_2) using a residual connection and normalized again before being fed to the next encoder in sequence. In addition, each sub-layer is first followed by a dropout probability of 0.1 before being added and normalized.

⁷⁴ My figures are inspired from the work of Jay Alammar.(see Alammar (2018) for more details)

Figure B1: Encoders



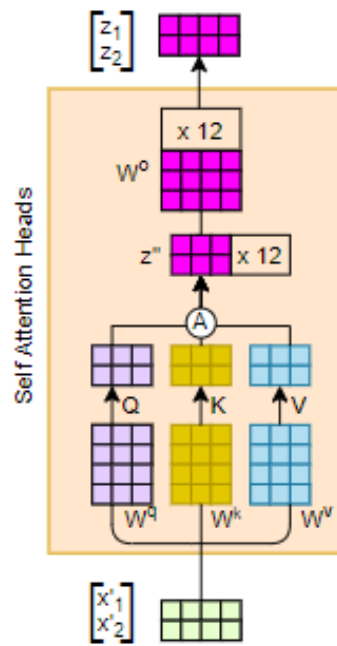
Next, I explain the self-attention heads using the framework shown in Figure B2. There are 12 self-attention heads that capture the contextual information of each token in relation to all other tokens used in the text. In other words, this allows the model to identify and weigh all other tokens in the text that are important when learning the vector representation of the focal token. I use this to visualize the strength of association between the tokens in the text and the outcome of interest in Section 3.5.2.

The inputs (x'_1, x'_2) are concatenated and multiplied with three weight matrices, W^q , W^k and W^v (that are fine-tuned during model training) to get three vectors – Q (Query), K (Key) and V (Value). These three vectors are combined using an attention function (A):

$$A(Q, K, V) = z'_0 = \text{softmax}\left(\frac{Q \cdot K^T}{\sqrt{d_k}}\right) \cdot V$$

where, d_k , the dimension of the Key vector, is chosen to be 64 and is equal to the dimensions of the other two vectors d_q and d_v ; and $\text{softmax}(x) = \frac{e^{x_i}}{\sum_{i=1}^m e^{x_i}}$. The division by $\sqrt{d_k}$ is performed to ensure stable gradients. The computation of z'_0 is for one attention head, and this is carried out in parallel for 11 additional attention heads to give me 12 vectors, $z'_0 \dots z'_{12}$, which are concatenated to produce z'' . This is multiplied with a weight vector W^o (which is fine-tuned during model training) to produce output (z_1, z_2) . The use of 11 additional attention heads allows the model to capture more complex contextual information.

Figure B2: Self-Attention Heads



Appendix B.2: MobileNet V1 followed by Bi-LSTM with Attention (in Audio Model)

The MobileNet v1 architecture is illustrated in detail in Table B1. Each row describes Stage i with input dimension $[\hat{H}_i, \hat{W}_i]$ (resolution), output channels \hat{C}_i (width) and \hat{L}_i layers (depth).

Table B1: MobileNet-v1 architecture

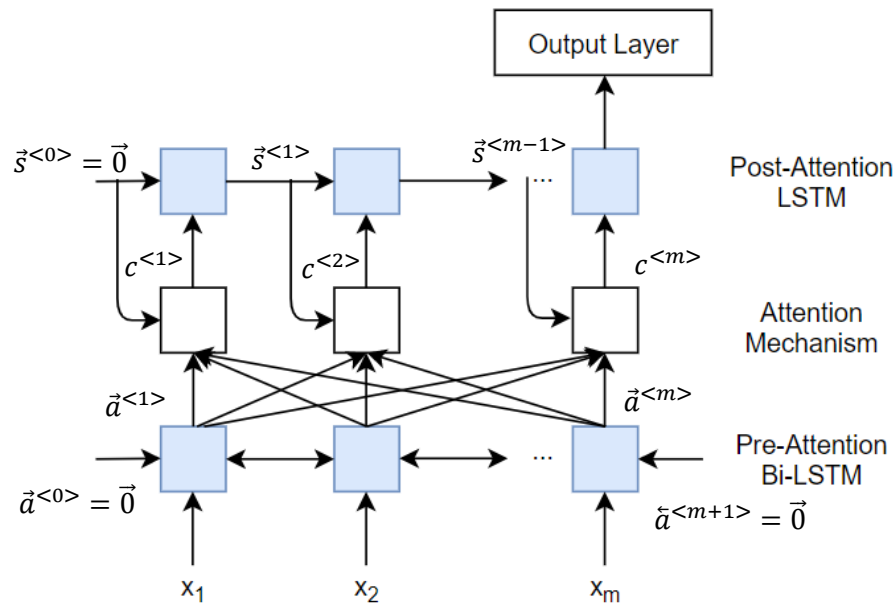
Stage i	Operator \hat{F}_i	Resolution $(\hat{H}_i \times \hat{W}_i)$ (Height x Width)	Width \hat{C}_i (Channels)	Depth \hat{L}_i (Layers)	Pre-trained Weights
1	Conv, k3x3, s2	96 x 64	32	1	Yes
2	MConv, k3x3, s1	48 x 32	64	1	
3	MConv, k3x3, s2	48 x 32	64	1	
4	MConv, k3x3, s1	24 x 16	128	1	
5	MConv, k3x3, s2	24 x 16	128	1	
6	MConv, k3x3, s1	12 x 8	256	1	
7	MConv, k3x3, s2	12 x 8	256	1	
8	MConv, k3x3, s1	6 x 4	512	5	
9	MConv, k3x3, s2	6 x 4	512	1	
10	MConv, k3x3, s2	3 x 2	1024	1	
11	Global Average Pooling	3 x 2	1024	1	
12	Dense	1 x 1	521	1	

Stage 1 has a regular convolution operation, whereas Stage 2 to 10 have the Mobile Convolution which is the main building block of the architecture. It is represented as “MConv, $k \times k$, s ” where $k \times k = 3 \times 3$ is the size of the kernel and $s = \{1,2\}$ is the stride. MConv divides the regular convolution operation into two steps – depth wise separable convolutions and point wise convolution, thus increasing the speed of computation (see Howard et al. (2017) for details). Stage 11 has a Global Average Pooling Layer that averages the inputs along its height and width and passes its output to Stage 10 which is a Dense output layer with 521 logistic functions that gives the per class probability score corresponding to the 960 ms input segment. I use a hop size of 490 ms so that I get an even number of 60 time step predictions corresponding to the 30 seconds of input. The resulting output vector has a dimension of 521x60 (audio classes x time steps) for each 30 second clip.

The output from MobileNet v1 is passed as input to the Bi-LSTM with attention mechanism, shown in Figure B3. I use two layers of LSTM cells – the first layer is a 32 unit Bidirectional LSTM layer and the second layer is a 64 unit (unidirectional) LSTM layer. They are separated by an attention mechanism as shown in Figure B3. Each audio segment $x_m \langle 521,1 \rangle$, where m is the total number of moments (time steps), is passed as input to each cell of the Bidirectional LSTM layer. This layer is made bidirectional to allow it to capture the interdependence between sequential audio segments from both directions. The sequential nature of LSTM cells in a layer allow the model to capture dependencies

between audio segments that are separated from each other (see the LSTM paper by Gers et al. (1999) for more details). I adopt the attention mechanism used for neural machine translation by Bahdanau et al. (2014) to help the Bi-LSTM model focus on more important parts of the input. The mechanism weighs the output activations ($a^{<t>} = [\vec{a}^{<t>}, \tilde{a}^{<t>}]$, $t = 1$ to m) from each cell of the pre-attention Bi-LSTM layer before passing the contextual output, $c^{<t>}$, to the post-attention LSTM layer above it. In addition, each cell of the attention mechanism takes as input the output activation $s(t - 1)$ from each preceding cell of the post-attention LSTM layer which allows it to factor in the cumulative information learnt by the model till that time step (see Bahdanau et al. (2014) for more details on the attention mechanism). The output of the last cell in the post-attention LSTM layer is passed to an output layer which has a linear activation function for the four continuous outcomes and a sigmoid activation function for sentiment. The context vector $c^{<m>}$ from the last cell of the attention mechanism allows visualization of the relative weights placed by the model along the time dimension of the input in order to form an association with the outcome of interest. Audio moments that have higher weight are more important while forming an association between the audio clip and the outcome of interest.

Figure B3: Bi-LSTM with Attention



Appendix B.3: EfficientNet-B7 Architecture and Combination Architectures (in Image Model)

The architecture of EfficientNet-B7 customized to my input dimension of 270x480x3 (where 3 corresponds to the pixel intensities for Red, Green and Blue channels) is shown in Table B2. Each row describes Stage i with input dimension $[\hat{H}_i, \hat{W}_i]$ (resolution), output channels \hat{C}_i (width) and \hat{L}_i layers (depth). B7 is the model with the highest uniform increase in resolution, width and depth of the model as compared to a baseline model B0 used by Tan and Le (2019). Scaling uniformly across the three dimensions (i.e. compound scaling) allows the model to better capture salient regions in images (see Tan and Le (2019) for details).

Table B2: EfficientNet-B7 architecture

Stage i	Operator \hat{F}_i	Resolution $(\hat{H}_i \times \hat{W}_i)$ (Height x Width)	Width \hat{C}_i (Channels)	Depth \hat{L}_i (Layers)	Pre-trained Weights
1	Conv k3x3, s2	270 x 480	64	1	Yes
2	MIBConv, e1, k3x3, s1	135 x 240	32	4	
3	MIBConv, e6, k5x5, s2	135 x 240	48	7	
4	MIBConv, e6, k5x5, s2	68 x 120	80	7	
5	MIBConv, e6, k3x3, s2	34 x 60	160	10	
6	MIBConv, e6, k5x5, s1	17 x 30	224	10	
7	MIBConv, e6, k5x5, s2	17 x 30	384	13	
8	MIBConv, e6, k3x3, s1	9 x 15	640	4	
9	Global Average Pooling	9 x 15	2560	1	No
10	Dense	1 x 1	1	1	

Stage 1 has the regular convolution operation, whereas Stages 2 to 8 comprise the main building block of the architecture which is the Mobile Inverted Bottleneck Convolution, “MIBConv, $e, k \times k, s$ ” where $e = \{1,6\}$ is the expansion factor, $k \times k = \{3 \times 3, 5 \times 5\}$ is the size of the kernel and $s = \{1,2\}$ is the stride. The strength of MIBConv lies in its ability to identify important features that are encoded in lower dimensional subspaces of images (see Sandler et al. (2018) for details). Furthermore, each MIBConv block is followed by a squeeze-and-excitation network that provides a weighted average to each channel output instead of a simple average, thus improving model performance (see Hu et al. (2018) for details).

To analyze thumbnails, I use the pre-trained weights from Stage 1 to 8, and tune the weights of Stage 9 and 10. Stage 9 has a Global Average Pooling Layer that averages the inputs along its height and width and passes its output to Stage 10 which is a Dense output layer. The output layer has a linear activation function for the four continuous outcomes and a softmax activation function for sentiment.

To analyze video frames, I compare the performance of four ‘combination architectures’ shown in Figure B4. Figure B4.1 shows the Bi-LSTM approach that captures sequential information from

different video frames. Each EfficientNet-B7 model takes a different video frame as input and provides the output from Stage 8 to the Global Average Pooling (GAP) Layer. This is followed by Dense Middle Layers (that use ReLU activation for continuous outcomes and sigmoid activation for the binary outcome), which is followed by a single Bi-LSTM layer with 256 memory cells, and finally a Dense output layer (that uses linear activation for continuous outcomes and softmax activation for the binary outcome). Figures B4.2, B4.3 and B4.4 show three approaches that preserve the spatial information across different video frames. The Max-GAP approach finds the maximum value across the $[9 \times 15 \times 2560]$ Stage 8 output from each EfficientNet-B7 model, which is followed by a GAP layer that reduces the dimensions to $[1 \times 1 \times 2560]$. The GAP-Max approach first finds the global average across each Stage 8 output, which is then followed by the Max operation, while the C-GAP approach concatenates the GAP outputs. Across all four approaches, I use the pre-trained weights from Stage 1 to 8 for each EfficientNet-B7 model and tune the weights of the final layers.

Figure B4.1: Bi-LSTM

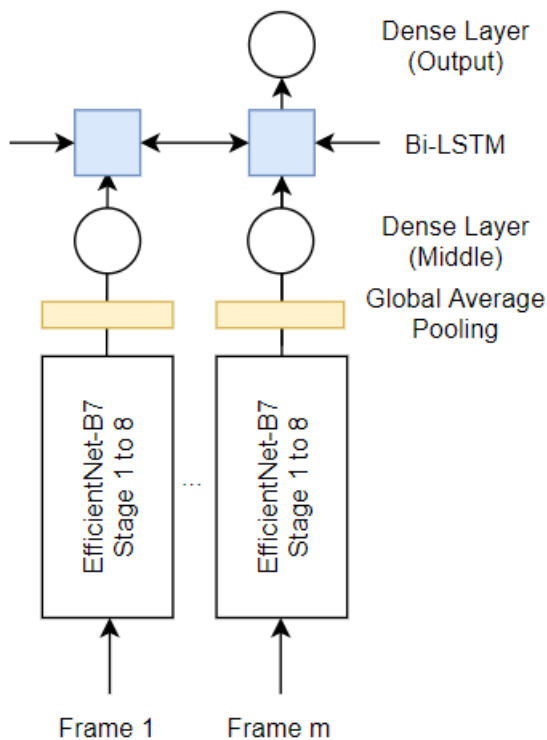


Figure B4.2: Max-GAP

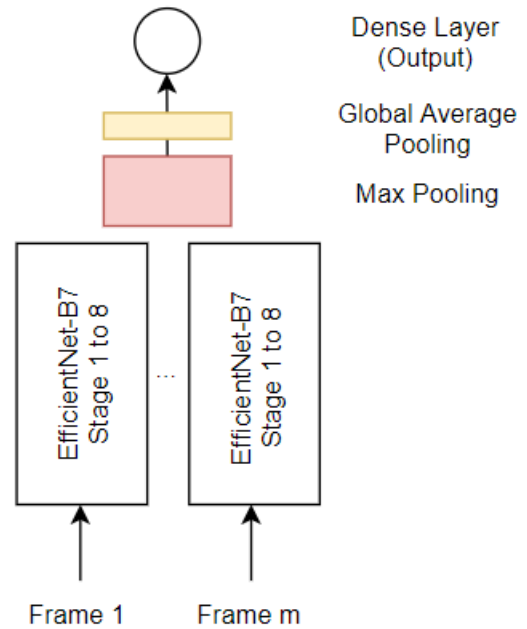


Figure B4.3: GAP-Max

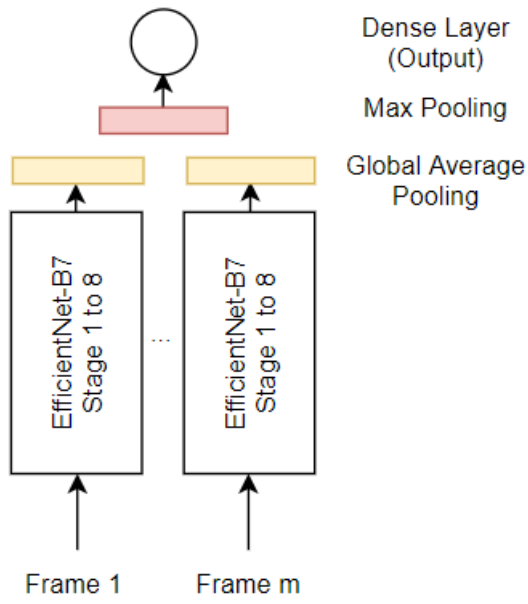
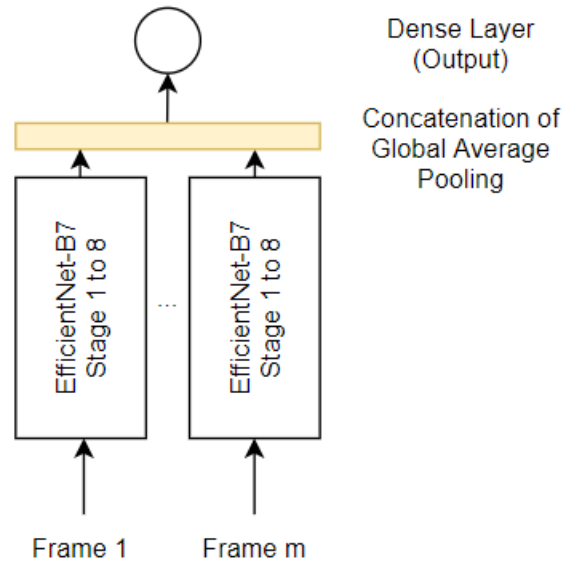


Figure B4.4: C-GAP



Appendix B.4: Comparison of Model Performance with Benchmarks

I first compare the predictive performance from the BERT Text Model with four benchmarks in Table B3.1. The benchmark models include an LSTM (with a 300 dimensional Glove word vector embedding), CNN model (X. Liu et al., 2019), CNN-LSTM (Chakraborty et al., 2019) and CNN-Bi-LSTM.

Table B3.1: Comparison of Text Model performance in holdout sample
(RMSE for Views; Accuracy for Sentiment)

Outcome	Covariate	LSTM	CNN	CNN-LSTM	CNN-Bi-LSTM	BERT
Views	Title	2.11	1.73	1.75	1.68	1.66
	Description (first 160c)	2.27	1.69	1.68	1.67	1.57
	Captions/transcript (first 30s)	2.28	1.82	1.80	1.76	1.75
Sentiment	Title	0.67	0.70	0.70	0.70	0.72
	Description (first 160c)	0.50	0.69	0.69	0.69	0.69
	Captions/transcript (first 30s)	0.67	0.70	0.70	0.70	0.70

As can be seen in Table B3.1, BERT has the best performance for both views (lowest RMSE) and sentiment (highest accuracy), with a maximum performance improvement of 6% for ‘views-description’ as compared to CNN Bi-LSTM.

I then compare the model performance of the Audio model as per the benchmarks discussed in Section 3.4.2 and present the results in Table B3.2. I find that the addition of MobileNet v1 (Model 2) helps improve accuracy when predicting sentiment, but there is no performance improvement when predicting views. Addition of the attention mechanism (Model 3) results in an improvement in both RMSE (by 10%) when predicting views and accuracy (by 1.5%) when predicting sentiment, thus demonstrating the benefit of capturing relative attention weights in the model.

Table B3.2: Comparison of Audio Model performance in holdout sample
(RMSE for Views; Accuracy for Sentiment)

Outcome	Model 1: Mel Spectrogram + Bi-LSTM	Model 2: Mel Spectrogram + MobileNet v1 + Bi-LSTM	Model 3: Mel Spectrogram + MobileNet v1 + Bi-LSTM + Attention
Views	2.19	2.19	1.97
Sentiment	0.59	0.64	0.65

Next, I compare the performance of the (pre-trained) EfficientNet-B7 with a 4-layer CNN model using thumbnails in Table B3.3. I see a substantial improvement in both RMSE (by 41%) and accuracy (by 26%) when using EfficientNet-B7, thus demonstrating the benefits of both deeper architecture and transfer learning with image data.⁷⁵

Table B3.3: Comparison of Thumbnail Model performance in holdout sample
(RMSE for Views; Accuracy for Sentiment)

Outcome	CNN	EfficientNet-B7
Views	5.20	3.09
Sentiment	0.54	0.68

Next, I compare the performance of the four Video Frame Models in Table B3.4 using two frames in each video clip – 0 sec and 30 sec.

Table B3.4: Comparison of Video Frame Model (0s,30s) performance in holdout sample
(RMSE for Views; Accuracy for Sentiment)

Outcome	Bi-LSTM	Max-GAP	GAP-Max	C-GAP
Views	2.28	3.16	2.88	5.53
Sentiment	0.66	0.66	0.66	0.66

I find that the Bi-directional LSTM architecture which captures the sequential information from two video frames performs better than the other three models that capture only spatial information while predicting views. However, all four models perform equally well in predicting sentiment. This demonstrates that capturing sequential information is more important for predicting views but not as important for predicting sentiment. As the Bi-LSTM model is the best overall, I use it to predict all the outcomes. Furthermore, I demonstrate sequential improvement in predictive performance when I add additional video frames to the model by reducing the time interval by half at each step, in Table B3.5.

Table B3.5: Bi-LSTM Video Frame Model (with different time intervals)
(RMSE for Views; Accuracy for Sentiment)

Time Interval	Covariate	Views	Sentiment
30 s	Video Frames (0s, 30s)	2.28	0.66
15 s	Video Frames (0s, 15s, 30s)	2.23	0.67
7.5 s	Video Frames (0s, 7.5s, 15s, 22.5s, 30s)	2.23	0.68

⁷⁵ Note that I am unable to tune an entire EfficientNet-B7 (without transfer learning) to demonstrate only the incremental benefit of transfer learning because of computational constraints that can be achieved at a low cost.

I find that using an additional frame at 15 sec helps improve prediction of views and sentiment. Adding two more frames at 7.5 sec and 22.5 sec improves prediction of sentiment but does not result in improved prediction of views.⁷⁶ The use of five frames results in overall best performance for both outcomes.

Last, I show the performance of the Combined Model from Section 3.4.4 on the holdout sample in Table B3.6. I use four linear models – OLS, Ridge Regression (L2 penalization), LASSO (L1 penalization), Elastic Net (0.5L1 and 0.5L2 penalization), and three non-linear models – Deep Neural Net (with three hidden layers), Random Forests and Extreme Gradient Boosting (XGBoost). I find that Ridge Regression has the best performance on the holdout sample for all the continuous outcomes (lowest RMSE) and also the binary outcome (highest accuracy).

Table B3.6: Performance of different Combined Models on holdout sample
(RMSE for Views, Engagement, Popularity and Likeability; Accuracy for Sentiment)

	Views	Sentiment	Engagement	Popularity	Likeability
OLS	1.46	0.74	0.80	0.64	0.78
Ridge Regression	1.11	0.75	0.73	0.56	0.72
LASSO	2.26	0.73	0.97	0.80	1.02
Elastic Net	2.26	0.74	0.97	0.80	1.02
Deep Neural Net	1.13	0.75	0.76	0.59	0.73
Random Forests	1.23	0.74	0.74	0.58	0.75
XGBoost	1.44	0.72	0.81	0.64	0.78

⁷⁶ I am unable to test performance with smaller time intervals due to limitations on computational performance that can be achieved at a low cost.

Appendix B.5: Interpreting Interaction Effects in Text Model

I study interaction effects in Step 1 to answer the following question:

1) Brand Attention – Brand Proportion and Brand Position: Does attention change based on whether the brand is part of a longer text (proportion) and the brand position in text?

$$\log(\text{AttentionWeight}_{itj}) = \alpha_i + \gamma X_{it} + \beta_1(\text{BIT}_{itj}) + \beta_2(\text{TP}_{itj}) + \beta_3(\text{LOTX}_{itj}) + \beta_4(\text{BIT}_{itj} * \text{LOTX}_{it}) + \beta_5(\text{BIT}_{itj} * \text{TP}_{itj}) + \epsilon_{itj} \quad \text{B5.1}$$

In Step 2, I answer the following questions related to interaction:

2a) Brand Presence - Brand Proportion: Is there an interaction effect between brand presence in text and overall length of text?

$$\text{PredictedOutcome}_{it} = \alpha_i + \gamma X_{it} + \beta_1(\text{BITX}_{it}) + \beta_2(\text{LOTX}_{it}) + \beta_{3it}(\text{BITX}_{it} * \text{LOTX}_{it}) + \epsilon_{it} \quad \text{B5.2}$$

2b) Brand Presence - Lead or End with Brand: Is brand presence in first or second half of each text associated with predicted outcome?

$$\text{PredictedOutcome}_{it} = \alpha_i + \gamma X_{it} + \beta_1(\text{BIFTX}_{it}) + \beta_2(\text{BISTX}_{it}) + \beta_3(\text{LOTX}_{it}) + \epsilon_{it} \quad \text{B5.3}$$

where, *BIFTX* & *BISTX* are Brand Indicators in First half of each Text and Second half of each Text, respectively.

The values of the coefficients of interest in each of the above equations are shown in Table B4. The values in the table reflect a percent change in the non-log-transformed outcome (e.g., views and not log(views)) when a covariate is present or increases by one unit.⁷⁷ I do not find significant evidence at the intersection of Step 1 and Step 2 to show that the effect of brand mentions can vary based on length of text or its position in the text.

⁷⁷ LOTX (Length of Text) has been mean centered to allow for interpretability of the coefficient.

Table B4: Results of the Text Regression Models with interactions(* – Significant ($p < 0.05$); W – Weakly Significant ($0.05 \leq p < 0.1$))

Model for	Data Type	Step 1 - Eq(B5.1)			Step 2 - Eq(B5.2)		Step 2 - Eq(B5.3)	
		Covariate						
		BIT	BIT x LOTX	BIT x TP	BITX	BITX x LOTX	BIFTX	BISTX
Views	Title	29.92*	2.84*	-2.84W	0.34	-2.22	3.21	-19.60
	Desc	8.77	1.35*	-0.02	54.13*	1.28	29.86W	46.89*
	Tran	4.29	0.41*	-0.23	6.26	0.05	25.31	-7.32
Sentiment	Title	-18.37	-1.8	-0.5	-12.13	2.32	-44.25	104.53
	Desc	26.02	1.52*	-2.42*	-72.34W	11.40*	-18.95	-41.99
	Tran	40.08W	0.22	-0.20	-51.98	-4.49W	-50.78	-74.99
Engagement	Title	27.87*	-0.24	0.98	-4.62	-0.71	-12.09	1.50
	Desc	-9.64	1.95*	-0.19	4.03	0.15	7.00	-0.64
	Tran	461.32*	0.81*	-0.05	15.86W	-0.34W	-0.32	6.57
Popularity	Title	22.32W	0.76	-2.03	-9.33	-0.27	-11.40	-13.8
	Desc	85.75*	-0.76	-1.53*	2.36	0.85	11.40	-1.29
	Tran	107.04*	0.76*	-0.11	-2.41	0.42*	8.75	8.79
Likeability	Title	42.59*	0.53	-0.92	-17.27	2.57	-9.20	-4.40
	Desc	130.50*	-0.61	-0.7W	10.35	1.52*	15.58	2.50
	Tran	87.47*	1.19*	-0.44	0.87	0.17	9.37	5.15

Appendix B.6: Interpreting Results for Middle and End of Videos

I interpret the results of the deep learning models on the middle 30 sec and last 30 sec of videos as done in Section 3.5.2. I focus on all the outcomes except views because, as mentioned in Section 3.3.3, view count is determined by viewing 30 seconds of a video. This is more likely to be the first 30 seconds unless viewers immediately skip to other locations in the video for which I have no demonstrated evidence of it happening on YouTube. I find eight significant results for the Audio model, but no significant results for the Image and Text model. The results are shown in Table B5.

Table B5: Results from interpreting Regression Models on middle and end of video

	Significant <i>increase</i> in attention (A) and significant <i>increase</i> in outcome (O)	Significant <i>increase</i> in attention (A) but significant <i>decrease</i> in outcome (O)
Outcome	Audio Model	Audio Model
Sentiment	more speech (without simultaneous music) in <i>middle</i> 30 sec of audio A: 2.88% O: 10.80% or more music (without simultaneous speech) in <i>middle</i> 30 sec of audio A: 3.10% O: 24.65%	
Engagement		more music (without simultaneous speech) in <i>last</i> 30 sec of audio A: 2.95% O: - 1.05%
Popularity	more speech (without simultaneous music) in <i>last</i> 30 sec of audio A: 5.60% O: 0.07%	more speech (without simultaneous music) in <i>middle</i> 30 sec of audio A: 0.98% O: - 0.21% or more music (without simultaneous speech) in <i>middle</i> 30 sec of audio A: 1.05% O: - 0.77%
Likeability	more speech (without simultaneous music) in <i>last</i> 30 sec of audio A: 3.63% O: 0.26% or more animal sounds in <i>last</i> 30 sec of audio A: 6.60% O: 1.02%	

Overall, the results for the middle and end of audio are qualitatively similar with the results for the beginning of audio with some differences (e.g., more speech without simultaneous music in the last 30 sec of audio is associated with an increase in popularity which was not found to be true for the first 30 sec of audio).

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