

RESEARCH ARTICLE

Inflation expectations and nonlinearities in the Phillips curve

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Summary

This paper examines the presence of nonlinearities in the Phillips curve. We allow for a flexible form of nonlinearity and estimate a threshold regression model with the number and location of thresholds determined directly from the data. Over the estimation period starting in the late 1960s, we document that the linear model cannot be rejected if we properly control for inflation expectations. More precisely, not controlling for *consumer* expectations may lead the econometrician to overestimate the degree of nonlinearity. Our results hold with aggregate data, regional data, and controlling for cost-push shocks directly or using instrumental variables.

KEYWORDS

consumer expectations, missing disinflation, nonlinearities, Volcker disinflation

1 | INTRODUCTION

Inflation dynamics have long been a subject of prolific economic research. In the 1970s and 1980s, much research in this area was dedicated to understanding the causes and costs of high inflation and how to disinflate effectively. Afterward, the focus shifted to understanding the Phillips curve in the context of low or moderate inflation. Despite important new developments in the study of the Phillips curve, its exact functional form depends on specific modeling assumptions and remains heavily debated empirically (e.g., Ball & Mazumder, 2011, 2019, 2020; Clark & McCracken, 2006; Mavroeidis et al., 2014; Nason & Smith, 2008; Stock & Watson, 2020).

In this paper, we explore whether nonlinearity can reconcile the Phillips curve with evidence from several prominent episodes of extreme fluctuations in inflation and/or economic activity: the Great Inflation of the 1970s, the Volcker disinflation, the missing disinflation following the Great Recession, and the missing inflation of the late 2010s. It turns out that the answer to this question depends crucially on the measurement of inflation expectations. In our preferred model, which, following Coibion and Gorodnichenko (2015), emphasizes the survey measures of households' expectations, nonlinearity plays a negligible role. Nonlinearity marginally helps to improve the fit of the model during the missing disinflation but not at all during the other episodes. In the full sample, the linear model cannot be rejected in favor of a nonlinear model. But if the expectations process does not include households' expectations, the estimated nonlinearity appears more important, because the linear model with mismeasured expectations has less bearing in the data.

The novelty of our paper is threefold. First, we estimate a Phillips curve without assuming a particular form of nonlinearity, by approximating an arbitrary function with a piecewise-linear function for which the number of segments is estimated directly from the data. The previous empirical literature on nonlinear Phillips curves typically imposes a particular functional form and therefore provides limited evidence on nonlinearity in general. Second, by revisiting nonlinearity

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of the Phillips curve with the 2010s data, we significantly extend the high-unemployment sample and shed more light on inflation dynamics during such episodes. The post-World War II data prior to the Great Recession, on which much of the existing results are based, contain limited observations of high unemployment.¹ Moreover, understanding inflation dynamics in the high-unemployment environment is especially relevant for pandemic recessions, which are characterized by particularly high levels of unemployment. Third, our paper considers possibly spurious nonlinearity of the Phillips curve that may result from measurement error in inflation expectations. Such measurement issues have been brought to the forefront by the recent literature but had not been considered in the context of nonlinear models prior to this paper. Hence, we provide a framework to merge two strands of the literature on the inability of Phillips curves to explain inflation dynamics during high-volatility episodes.

Studying whether the empirical Phillips curve is nonlinear can also shed light on the relevant mechanism in workhorse aggregate models, especially those that emphasize state dependence. For instance, downward nominal wage rigidity could break the link between economic activity and prices during deep recessions, making the Phillips curve flatter. If, instead, prices change more frequently during a deep recession (e.g., due to state dependence or rational inattention, whereby firms easily observe a deep recession but not a mild one), the Phillips curve should become steeper.² Because different mechanisms can push the slope of the Phillips curve in opposite directions—and can also create several regions with different slopes—this paper takes an empirical approach that has the advantage of detecting any type of nonlinearity stemming from any structural parameter.

We estimate the Phillips curve using single-equation methods. To properly identify this structural relationship and examine the robustness of the results, we consider several different identification strategies. First, we control for an extensive list of supply-side shifters considered in the literature. Second, similar to Barnichon and Mesters (2020), we isolate exogenous variation in demand, using monetary policy shocks identified in the literature (Romer & Romer, 2004) to instrument for the unemployment gap. Finally, we exploit regional variation in inflation and unemployment, thereby removing the effects of aggregate shocks (Hazell et al., 2022). Because controlling for supply-side shifters allows us to explore the longest time period, we use this method as a baseline.³

To estimate nonlinearity without imposing any particular functional form, we combine these identification strategies with threshold regression methods (Hansen, 2000, 2017). The threshold regression allows us to determine the number and location of thresholds directly from the data, and therefore can be used to approximate any arbitrary form of nonlinearity. A one-threshold model (i.e., two regions with different slopes) could detect changes in the slope due to downward nominal wage rigidity and kinked demand, among other reasons. A two-threshold model could provide an even better fit to a nonlinear relationship, and could also detect an inaction (flat) region surrounded by two steep regions, as one would expect from a state-dependent pricing perspective.

We estimate our model for a range of measures of inflation, inflation expectations, and labor market slack. Our preferred inflation measure is headline CPI inflation, because consumer inflation expectations correspond most closely to this measure. We discuss other headline measures such as PCE and GDP deflator inflation as well as core inflation. Because the methodology that the BLS uses to construct the CPI has significantly evolved during our sample period, we also consider a current-method CPI series. We measure inflation expectations using surveys of consumers and professional forecasters as well as backward-looking adaptive expectations. Our preferred measure of labor market slack is the unemployment gap, which accounts for changes in the natural rate of unemployment. The results based on the labor share are similar.

We document several findings. First, over the estimation period, we find no evidence, or at best weak one, for nonlinearity. Depending on the inflation measure and identification strategy, we either cannot reject a linear model in favor of a nonlinear model or, when we do, the preferred nonlinear model has a high-unemployment threshold, with a “flat” regime that is rarely operational. Second, the measurement of inflation expectations plays a pivotal role. When consumer expectations are included in the model and the inflation measure corresponds to those expectations, estimated nonlinearities are not statistically significant. But when inflation expectations are not measured properly, nonlinearities may appear to

¹If the Phillips curve becomes flatter during recessions, the high levels of unemployment would not lead to a sharp decrease in inflation. In fact, the empirical relationship between wage inflation and unemployment originally documented by Phillips (1958) is represented by a convex curve, not a linear relationship. Hooper et al. (2020) also show interesting evidence along these lines.

²We discuss these effects in more detail in Appendix S1 Section A. In the workhorse New Keynesian models, the slope of the Phillips curve depends on the Calvo probability of resetting prices, the intertemporal elasticity of substitution, the Frisch elasticity of labor supply, and the elasticity of substitution across product varieties. In addition, nonlinearities in the microfoundations (e.g., a kink in individual demand curves) may result in nonlinear aggregate relationships.

³The Romer and Romer shocks are obtained with a five-year lag, while regional data are not available during the early period. Hence, we would not be able to study jointly the Great Inflation of the 1970s, the Volcker disinflation of the 1980s, and the recent missing-inflation episode with either method.

have a role. Third, not only are nonlinearities negligible over the full sample period but also they help improve the fit of the model and its out-of-sample forecasts only marginally during the early 2010s and not at all during other episodes considered.

This paper contributes to a broad literature examining nonlinearities in macroeconomic relationships in general (e.g., Auerbach & Gorodnichenko, 2012; Barnichon et al., 2022; Berge et al., 2021; Kilian & Vigfusson, 2011; Santoro et al., 2014; Tenreyro & Thwaites, 2016) and specifically in the Phillips curve (e.g., Ascari et al., 2022; Barnes & Olivei, 2003; Debelle & Laxton, 1997; Hooper et al., 2020; Kumar & Orrenius, 2016). Our paper is related to the recent studies examining whether nonlinearities can explain the missing disinflation (e.g., Beaudry & Portier, 2018; Harding et al., 2022; Kumhof & Wang, 2021).⁴ We contribute to this literature by adopting a flexible estimation approach and by examining jointly nonlinearities and consumer expectations.⁵ Finally, our paper contributes to the literature analyzing the economic environments of the 1970s and 1980s, characterized by an inflation runup followed by a drastic disinflation.⁶

The paper proceeds as follows. Section 2 describes the empirical methodology, including identification strategies. Section 3 briefly summarizes our data and sources. In Section 4, we present our main results. We discuss our baseline estimates for measures of labor market slack, inflation, inflation expectations, and a number of estimation approaches. Section 5 uses our baseline estimates to better understand inflation dynamics during the historical episodes. We examine in-sample model fit during each episode and discuss some out-of-sample forecasting performance of the nonlinear models during the recent period. Section 6 examines robustness of the results. Section 7 concludes.

2 | METHODOLOGY

We estimate the structural Phillips curve using single-equation methods. We consider multiple approaches to identify this structural relationship. Our baseline approach follows a long list of papers that estimated the Phillips curve by controlling for an extensive list of supply-side shifters. In addition, we consider two other approaches. First, in order to isolate demand-driven variation, we instrument the slack variable with the monetary policy shocks separately identified in the literature. Following Barnichon and Mesters (2020), we focus on Romer and Romer (2004) shocks. Second, we focus on regional variation, thereby removing aggregate effects such as oil shocks and endogenous monetary policy responses using time fixed effects. Despite some natural quantitative discrepancy between these approaches, all of them qualitatively paint a similar picture. While this estimation approach focuses on a single equation, our empirical specification can be derived from standard New Keynesian models. Hence, by isolating variation specific to demand shifters, our estimates have structural interpretation relevant for the New Keynesian Phillips curve.

We begin with a linear version of the expectations-augmented Phillips curve:

$$\pi_t = \mu + \mathbb{E}_t \pi_{t+1} + \kappa u_t + \boldsymbol{\varphi} \mathbf{z}_t + \varepsilon_t, \quad (1)$$

where π_t is the rate of inflation, $\mathbb{E}_t \pi_{t+1}$ is expected inflation, u_t is a measure of real economic activity (e.g., the unemployment gap), \mathbf{z}_t is a vector of controls observed in period t , ε_t is the error term, and μ , κ , and $\boldsymbol{\varphi}$ are estimated parameters.⁷ The coefficient κ measures the slope of the linear Phillips curve. When κ is large in absolute value, inflation is sensitive

⁴Nonlinearities can arise due to interest-rate bounds (Beaudry & Portier, 2018; Brunnermeier & Koby, 2018; Kumhof & Wang, 2021), a kinked demand curve (Harding et al., 2022; Kimball, 1995), downward nominal wage rigidity (Daly & Hobijn, 2014), and state dependence in structural parameters such as the Calvo rate (Alvarez et al., 2018; Gagnon, 2009; Petrella et al., 2018). Asymmetries in the transmission of monetary policy and their consequences are examined in Schaling (2004) and Santoro et al. (2014).

⁵The literature emphasizing survey measures of inflation expectations includes Leduc et al. (2007), Adam and Padula (2011), Chan et al. (2018), Coibion et al. (2018), and Pfajfar and Roberts (2022), among many others, with some papers emphasizing robust deviations from rationality (e.g., Andrade & Le Bihan, 2013; Binder, 2017; Bordalo et al., 2020; Ehrmann et al., 2017; Fuhrer, 2018; Pfajfar & Santoro, 2013). On the theoretical side, a closely related literature focuses on beliefs in macro models (e.g., Gerko, 2018; Mertens, 2016).

⁶Popular explanations of the macroeconomic dynamics of that time include, among many others, a policy-regime change (Blanchard, 1984; Clarida et al., 2000), changes in NAIRU and real-time measurement issues (Ball, 1997; Orphanides, 2001), supply-side shifters (Barsky & Kilian, 2002; Blinder & Rudd, 2013), rising disagreement in inflation forecasts (Mankiw et al., 2004), and the evolution of policymakers' beliefs (Primiceri, 2006). Erceg and Levin (2003), Goodfriend and King (2005), Bordo et al. (2007), and Nunes (2009) also examine these issues.

⁷We do not impose the constraint that $\mu = 0$, because our focus is on the empirical relationship between inflation and unemployment. If the models that give rise to this constraint are correct, the econometric cost of including the intercept is negligible. But if they are wrong, omitting the intercept would bias our estimates of the slope. Moreover, the constant controls for the mismatch between the levels of expectations and actual inflation in surveys. For instance, consumers in the Michigan survey expect on average higher inflation than observed in the data.

to changes in economic activity. Before we proceed to nonlinearities, we discuss a few modeling choices in the context of the linear model: the choice of the slack variable u_t , the control variables z_t , and the treatment of expectations $\mathbb{E}_t \pi_{t+1}$.

As a baseline measure of slack, we use the unemployment gap. By using the gap—rather than the unemployment rate—we focus on nonlinearities that occur over the business cycle and separate them from possible secular trends in the labor market dynamics. In the New Keynesian tradition, one can use a microfounded model (e.g., Rotemberg & Woodford, 1997) to derive a relationship between inflation and marginal cost. Therefore, an empirical analog of this model calls for a direct measure of marginal cost such as the labor share of income (Galí 1999). However, the downward trend in the labor share observed since the early 2000s makes this measure problematic. For this reason, we use the unemployment gap as a benchmark measure, but we also report estimates of the model using the unemployment rate, the labor share, and an adjusted measure that accounts for the downward trend in the raw labor share by setting the labor fraction of proprietors' income to its historical average (Armenter, 2015).⁸

In a very interesting analysis, McLeay and Tenreyro (2019) discuss the pitfalls of estimating the Phillips curve due to optimal monetary policy and the presence of cost-push shocks. One of the solutions they propose is to include a set of variables that control for cost-push shocks. We follow that approach and include in our set of controls, z_t , two lags of the growth of the relative price of food and energy, two lags of the change in the nominal exchange rate, and the Gordon (1982) price- and wage-control variable. McLeay and Tenreyro (2019) also mention the importance to control for inflation expectations—as we do in our baseline specification—as well as financial frictions, which we analyze more carefully in a later section. As discussed before, we also present results when marginal costs are the driving force of inflation because, as McLeay and Tenreyro discuss, the econometric identification is improved when the central bank's stabilization variable differs from the one driving the inflation process.

We estimate our model using single-equation methods.⁹ The advantage of our approach is that its econometric implementation is straightforward and can be easily combined with available techniques to estimate nonlinearity. Despite the well-known identification challenges of this approach, we make significant inroads by considering a variety of different strategies and conducting extensive sensitivity analyses. Adopting single-equation estimation also facilitates comparison with extensive previous literature.

2.1 | Expectations process

Following the literature, we model inflation expectations as a combination of backward-looking and forward-looking terms (e.g., Fuhrer, 2010; Nunes, 2018). We employ the University of Michigan's Surveys of Consumers (UMSC), which asks consumers about their expectation of inflation over the following year,¹⁰ as well as the Survey of Professional Forecasters (SPF), which collects forecasts from expert forecasters for various inflation variables, including at a one-quarter horizon.¹¹ The SPF may best capture how large firms set prices, while the UMSC reflects consumers' expectations and may best capture expectations of small businesses.

In addition, a large body of literature emphasizes inflation persistence (e.g., Fuhrer, 2006; Fuhrer & Moore, 1995), which can be reconciled with backward-looking expectations wherein a firm's forecast of future inflation is a weighted average of past inflation. Hence, we also include lags of actual inflation. To cover a full year of observations and to minimize the Akaike information criterion for both the labor-share and unemployment-gap specifications, we choose five lags, but our results are not sensitive to this choice.¹²

⁸We extend the original variable through 2019:Q4.

⁹Alternatively, the Phillips curve could be estimated using full information from a DSGE model, as in Smets and Wouters (2007), among many others. This method relies on cross-equation restrictions and priors (e.g., Del Negro & Schorfheide, 2008). Our approach complements that strand of literature.

¹⁰While the New Keynesian Phillips curve mandates the use of one-period-ahead expectations, the Michigan survey does not ask about one-quarter-ahead expectations. The strong performance of this measure, however, suggests that this measurement error is likely immaterial for our analysis.

¹¹While we focus on short-term inflation expectations, as motivated by workhorse models, practitioners have recently turned their attention to long-term expectations (e.g., Yellen, 2015). We note that long-term expectations are persistent and thus have less potential to explain the puzzling inflation dynamics that we study in this paper. We verify that our estimates are not affected in a material way by controlling for the 10-year inflation expectations used in the Federal Reserve Board's FRB/US model.

¹²By controlling for inflation lags, we also focus on inflation innovations over the business cycle and remove the lower frequency fluctuations in inflation.

To summarize, the expectations process is modeled as follows:

$$\mathbb{E}_t \pi_{t+1} = \sum_{i=1}^5 \delta_i \pi_{t-i} + \alpha_1 \mathbb{E}_t^{\text{SPF}} \pi_{t+1} + \alpha_2 \mathbb{E}_t^{\text{UMSC}} \pi_{t+1}, \tag{2}$$

where $\mathbb{E}_t^{\text{SPF}} \pi_{t+1}$ is one-quarter-ahead expected inflation in the SFP, $\mathbb{E}_t^{\text{UMSC}}$ is the expected inflation from the UMSC, and $\delta_i, \alpha_1, \alpha_2$ are estimated parameters. Denoting $\sum_{i=1}^5 \delta_i$ by α_0 , we constrain the coefficients on the expectation terms to sum to one (i.e., $\alpha_0 + \alpha_1 + \alpha_2 = 1$); thus, $\hat{\alpha}_0, \hat{\alpha}_1$, and $\hat{\alpha}_2$ represent the relative weights of the backward-looking and forward-looking components in the expectations process.¹³

Because we focus directly on the Phillips curve equation, we can allow the expectations process to deviate from the full information rational expectations benchmark. That is, instead of treating $\mathbb{E}_t \pi_{t+1}$ as the mathematical expectation of next-period inflation, as would be the case in FIRE DSGE models, we can think of it as a separate—though possibly endogenous—process, which may depend both on the underlying inflationary trend and subjective beliefs. This approach is consistent with recent evidence on nonrationality of expectations obtained, in particular, from the survey data that we use (e.g., Andrade & Le Bihan, 2013; Bordalo et al., 2020; Coibion et al., 2018; Fuhrer, 2018). One can loosely think of aggregate expectations in Equation (2) as a weighted average of expectations of backward-looking agents; large firms, approximated by professional forecasters; and small firms, approximated by households, with the corresponding weights α_i .

2.2 | Nonlinear specification

To estimate nonlinearities, we employ the Hansen (1996, 2000) threshold regressions. This method approximates a nonlinear curvature by a piecewise-linear function in which the number of kinks (thresholds) is determined endogenously. Relative to other nonlinear estimation methods, the threshold regression has several advantages. Each linear segment can be estimated by ordinary least squares, and therefore, estimation and inference are straightforward. There is no need to assume any specific form of nonlinearity: The data decide how much nonlinearity (i.e., how many thresholds) there is. Further, this method has been used before and therefore allows for comparison with previous studies (e.g., Barnes & Olivei, 2003). Its major shortcoming is the tendency to produce wide confidence intervals for thresholds. That is, even though we can improve the fit of the model and test explicitly for nonlinearities, we may not be able to determine the thresholds' location with certainty.

We estimate the model with a continuity constraint.¹⁴ Without it, even in the absence of shocks, infinitesimal changes in unemployment would lead to jumps in the inflation rate. Discontinuity could also result in a lack of equilibrium, which would be difficult to reconcile with the US time series and most standard economic models. Hansen (2017) describes in detail the econometric apparatus for the linear constraint case that we analyze here.

A piecewise-linear Phillips curve with a vector $\gamma = (\gamma_1, \dots, \gamma_m)$ containing m thresholds can be written as follows:

$$\begin{aligned} \pi_t &= \underline{\mu}(\gamma) + \mathbb{E}_t \pi_{t+1} + \underline{\kappa}(\gamma) u_t + \varphi z_t + \varepsilon_t, \\ \underline{\mu}(\gamma) &= \sum_{j=1}^{m+1} \mu_j \mathbb{I}(\gamma_{j-1} \leq u_t < \gamma_j), \\ \underline{\kappa}(\gamma) &= \sum_{j=1}^{m+1} \kappa_j \mathbb{I}(\gamma_{j-1} \leq u_t < \gamma_j), \end{aligned} \tag{3}$$

where $\mathbb{I}(\gamma_{j-1} \leq u_t < \gamma_j)$ is an indicator function of a condition $\gamma_{j-1} \leq u_t < \gamma_j$, assuming $\gamma_0 = -\infty$ and $\gamma_{m+1} = +\infty$. In a one-threshold case, this definition results in two regimes: $u_t < \gamma$ (regime “L”) and $u_t \geq \gamma$ (regime “R”). This threshold

¹³In a standard New Keynesian model, $\alpha_0 + \alpha_1 + \alpha_2 = \beta$, the discount factor. At a quarterly frequency, $\beta \approx 1$. The unconstrained regressions support this restriction in the vast majority of cases. See Appendix S1 Section A for additional details.

¹⁴Note that continuity imposes a constraint on the intercept across the regimes. With one threshold (two regimes), we have one free intercept parameter, while the other one is pinned down by the constraint.

allows for shifts in the Phillips curve over the range of u_t . To compute the optimal thresholds γ^* , an OLS regression is estimated sequentially for all possible values of γ . We then choose γ^* that minimizes the residual sum of squares.¹⁵

We then test the null hypothesis of the linear model against the alternative of a one-threshold model. Let S_0 and S_1 be the residual sums of squares under the null hypothesis and under the alternative, respectively. For a sample of n observations, the F -statistic of this test is of the form:

$$F = n \frac{S_0 - S_1}{S_1},$$

with a distribution that can be approximated through a bootstrap procedure.¹⁶ Because the critical values of this test depend on parameters of the model, it is more informative to report its p -values. This test can be extended for the null of an arbitrary number of thresholds $\ell \geq 0$ against the alternative of $\ell + k$ thresholds, $k \geq 1$. The optimal number of thresholds can be determined by running the test sequentially, starting from $\ell = 0$ and $k = 1$ and then increasing ℓ by one if the null is rejected. The optimal number of thresholds ℓ^* is the lowest ℓ for which the null is not rejected.

3 | DATA

We use aggregate data, obtained from public sources, from 1968 through 2019 at a quarterly frequency. The start date is motivated by availability of data on consumer expectations. Our baseline inflation measure is the seasonally adjusted, annualized quarterly growth rate of the CPI. We focus on the headline CPI, because surveys of consumer expectations ask their respondents about the cost of living, which corresponds to headline consumer prices, as food and energy expenses take a significant share in US households' budgets. Because our paper emphasizes expectations as a key factor of inflation dynamics, it is important to avoid a mismatch between the measure of inflation and the corresponding expectations. We also study in detail the specifications based on the growth rates of the PCE price index and the GDP deflator as well as the core measures of consumer prices (i.e., net of food and energy prices).

We measure unemployment with the total civilian population (over 16 years old) unemployment rate. To construct the gap, we subtract from this measure the natural unemployment rate, produced by the CBO. As an alternative slack variable, we consider the seasonally adjusted labor share for the nonfarm business sector. We also use the Armenter (2015) procedure to account for the secular downward trend in labor's share.

To measure expectations, we rely on two major sources: the SPF and the UMSC. Both surveys have been widely used in the literature. From the SPF, we take the one-quarter-ahead median expectations of the GDP deflator, because the corresponding series for the CPI is available starting only in the 1980s. From the UMSC, we take the mean expectations of the cost-of-living increase over the following 12 months period.¹⁷ For controls and robustness checks, we use a plethora of other variables summarized in Table B.1 of Appendix S1 Section B.

4 | EMPIRICAL RESULTS

4.1 | Baseline estimates for a range of slack and regime measures

Table 1 presents estimates of the Phillips curve for a range of slack and regime measures. In Panel A, we show estimates of a standard linear model. Our baseline estimates are based on the unemployment gap as a slack and regime measure (Column (1)). In the linear case, the slope of the Phillips curve is -0.30 , which is consistent with the previous literature. The slope is also negative and significant when we use the unemployment rate as a slack and regime variable (Column (2)). We estimate a significant slope also when we focus on the labor-share measures. In Column (3), we use the raw measure because it relates directly to the unobserved output gap, while in Column (4), we use the adjusted measure based on the historical average of proprietors' income allocated to labor. Because the labor share moves in the opposite direction from unemployment, the slope in this case is positive, as expected. In all these cases, consumer expectations,

¹⁵To maintain statistical power of the test, we constrain the grid for γ to ensure that each regime contains no less than 10% of the sample size.

¹⁶Confidence intervals for the threshold are computed using a similar bootstrap procedure; see Hansen (2017) for more details.

¹⁷It is well known that the SPF mean and median inflation expectations are similar, but the UMSC mean and median expectations are not. We use the mean for the UMSC because it is available in the earlier period. The main results are similar if we use the median UMSC expectations for a shorter period with available data.

TABLE 1 Linear versus nonlinear Phillips curve: Various slack/regime measures.

	Unemployment		Labor share	
	Gap (1)	Rate (2)	Raw (3)	Adjusted (4)
Panel A: Linear model				
Slope, $\hat{\kappa}$	-0.30*** (0.08)	-0.14* (0.07)	0.20*** (0.04)	0.32*** (0.05)
Expected inflation				
UMSC, $\hat{\alpha}_2$	0.79*** (0.17)	0.77*** (0.16)	1.06*** (0.18)	0.93*** (0.16)
SPF, $\hat{\alpha}_1$	-0.12 (0.27)	-0.14 (0.27)	-0.14 (0.22)	0.02 (0.23)
Sum of lags, $\hat{\alpha}_0$	0.33*** (0.11)	0.38*** (0.12)	0.08 (0.12)	0.05 (0.12)
Panel B: Threshold model				
Slopes				
Left, $\hat{\kappa}_L$	-0.50*** (0.18)	-0.04 (0.21)	0.08 (0.07)	0.62*** (0.16)
Right, $\hat{\kappa}_R$	0.08 (0.19)	-0.19** (0.09)	0.33*** (0.10)	0.26*** (0.07)
Expected inflation				
UMSC, $\hat{\alpha}_2$	0.73*** (0.15)	0.77*** (0.16)	1.04*** (0.18)	0.99*** (0.16)
SPF, $\hat{\alpha}_1$	-0.07 (0.27)	-0.14 (0.27)	-0.05 (0.24)	-0.07 (0.24)
Sum of lags, $\hat{\alpha}_0$	0.34** (0.17)	0.38** (0.16)	0.02 (0.19)	0.08 (0.17)
Threshold, $\hat{\gamma}$				
Point estimate	1.95	5.87	-1.95	-3.11
95% confidence interval	[-0.82, 2.93]	[4.23, 8.47]	[-7.63, 3.21]	[-4.27, 2.54]
No. of thresholds, p -value				
0 vs. 1, $H_0: 0$	0.20	0.95	0.18	0.41
1 vs. 2, $H_0: 1$	0.92	0.38	0.41	0.34
R^2	0.77	0.75	0.79	0.79
N	205	205	205	205

Note: The estimation sample is 1968:Q4 through 2019:Q4. The dependent variable is the seasonally adjusted, annualized CPI inflation rate. Alternative threshold variables are in Columns (1)–(4). Inflation expectations include consumer expectations from the University of Michigan's Surveys of Consumers, SPF forecasts of one-quarter-ahead GDP inflation, and five lags of inflation. (The SPF forecasts of CPI inflation are not available for the early sample.) Control variables (estimates not reported) are two lags of the growth rate of the relative price of food and energy, two lags of the change in the nominal exchange rate, and the price- and wage-control measure. The adjusted labor share (Column (4)) is obtained by setting the labor fraction of proprietors' income to its historical average. The threshold point is estimated using the Hansen regression-kink method. Newey–West standard errors, allowing for autocorrelation of up to five lags, are in parentheses.

* $p < 0.1$.

** $p < 0.05$.

*** $p < 0.01$.

measured by the University of Michigan survey, are a dominant component of the inflation expectations process. Across these specifications, the UMSC coefficient is at least 0.73, whereas the sum of coefficients on inflation lags is at most 0.38. The SPF carries almost no weight. Consumer inflation expectations are particularly important in the labor-share specifications, with a corresponding weight close to one.

Next, we compare the linear model with a one-threshold model, whose estimates are shown in Panel B. We estimate the threshold value of the unemployment gap at 1.95%.¹⁸ The 95% confidence interval is rather wide, corresponding to unemployment rates between 4.7% and 8.4%. The curve is relatively steep left of the threshold (with a slope of -0.50) and essentially flat right of the threshold. Note that, even for the left portion of the curve (low unemployment), we cannot rule out estimates of a small response of inflation to unemployment, suggesting that the piecewise-linear Phillips curve may still be overall flat, and it is especially so when unemployment is high. Overall, we cannot reject the linear model in favor of the threshold model, suggesting that nonlinearities played a limited role in the full sample. The p -value of the test for the linear model (null hypothesis) versus the one-threshold model ranges 0.18–0.95, depending on the slack and regime variable.¹⁹ The results are qualitatively similar for the unemployment-rate and labor-share specifications. Similar to the linear case, consumer expectations of inflation play a prominent role. The baseline UMSC coefficient is 0.73, whereas

¹⁸According to Congressional Budget Office (CBO) data, the natural rate of unemployment averages at 5.47% during our baseline estimation period. Hence, the estimated unemployment-gap threshold corresponds to an unemployment rate of 7.42%.

¹⁹In the table, we also report a test for one versus two thresholds. This test suggests an even smaller likelihood of the second thresholds.

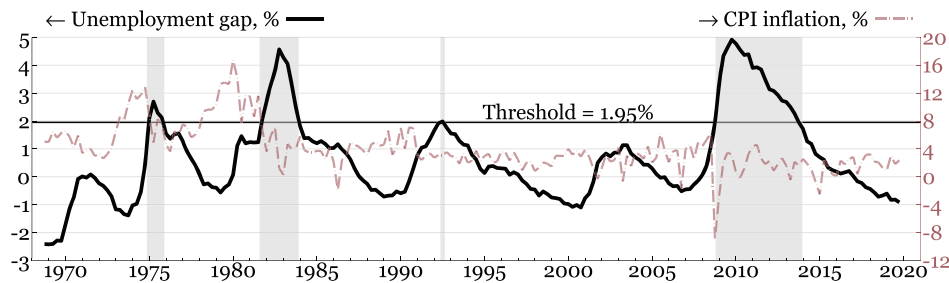


FIGURE 1 Regimes in the nonlinear model. *Note:* The shaded areas correspond to the periods when the unemployment gap is above the estimated threshold (a flatter segment of the Phillips curve). The unemployment gap (solid line, left axis) is constructed as the difference between the unemployment rate and the CBO measure of the natural rate. Inflation (broken line, right axis) is measured as the annualized quarterly growth rate of the headline CPI.

the sum of coefficients on inflation lags is 0.34. The SPF expectations remain irrelevant once consumer expectations are controlled for.

To better understand why nonlinearities play only a limited role in the full sample, Figure 1 highlights the episodes when the unemployment gap was high and the Phillips curve was flatter than usual. The longest episode of the high-unemployment regime corresponds to the Great Recession and its aftermath. In addition, our procedure identifies three other, shorter episodes, which are spread in time and are each associated with an economic downturn. The timing of our unemployment regimes, however, differs from the timing of recessions defined as two consecutive quarters of a GDP decline or by a more comprehensive procedure employed by the NBER. Typically, a high-unemployment regime also contains early recovery periods, when output is on an upward trend but the unemployment gap remains high. Hence, such regimes better capture the state of labor markets than output dynamics. Importantly, our model puts thresholds in different noncontiguous time periods and therefore provides a mechanism different from a structural break resulting in a flattening of the Phillips curve (e.g., Luengo-Prado et al., 2018; Roberts, 2006; Simon et al., 2013).

Overall, our baseline estimates provide a compelling case that, as a whole, nonlinearities do not matter much. The “best” case for nonlinearities favors one threshold that gives rise to two regimes: a dominant regime that prevails in the sample and an infrequent regime driven by a few deep recessions. While this asymmetry makes it difficult to estimate the difference between the regimes precisely, we note that, en route to the best model, our grid-search procedure considers cases where the threshold values give rise to regimes occurring with similar frequencies. However, such symmetric models are rejected by the data in favor of linear models. Hence, to the extent nonlinearities matter at all, they do so only rarely.

4.2 | The role of inflation and inflation expectations measures

In this section, we discuss how the measurement of inflation and inflation expectations affects estimated nonlinearity. We show that overall the mismatch between the measures of inflation and inflation expectations puts nonlinearities in a more prominent light. We begin by excluding consumer expectations from the baseline specification based on headline CPI inflation. These results are shown in Column (1) of Table 2.²⁰ In this case, we still identify the threshold at 1.95, and the left regime is steeper than the right regime. However, the linear model is rejected at the 5% significance level and the coefficient of SPF expectations becomes large and highly significant. Hence, not accounting for consumer expectation leads the econometrician to overestimate the role of nonlinearities and the importance of professional forecasters' expectations.

While we use headline CPI inflation as a baseline measure, there are several good reasons to consider other inflation measures as well. First, the Federal Reserve's preferred measure changed in 2000 from CPI to PCE inflation; hence, significant media coverage relates to this measure. Second, the GDP deflator has the advantage of having the longest forecast series in the SPF. Third, headline inflation tends to be volatile due to energy and food prices, which are not directly accounted for by DSGE models. While our controls partially address this issue, using core inflation measures is a more straightforward way to remove these components. This of course comes at a cost that survey measures of consumer expectations ask the respondents about prices in general, and food and energy prices can have disproportionate effects on

²⁰To save space, in Panel A, we report only the slopes of the linear models, as in this section, we focus mainly on the threshold model. Similarly to the baseline, the coefficients on inflation expectations are not materially affected by allowing for nonlinearity in the effect of the slack variable.

TABLE 2 Nonlinearity and inflation measurement.

	CPI (1)	PCE (2)	GDP deflator (3)	Core CPI (4)	Core PCE (5)	CPI-U-RS (6)
Panel A: Linear model						
Slope, $\hat{\kappa}$	-0.31*** (0.10)	-0.15** (0.06)	-0.15*** (0.05)	-0.22*** (0.05)	-0.15*** (0.05)	-0.16* (0.09)
Panel B: Threshold model						
Slopes						
Left, $\hat{\kappa}_L$	-0.63*** (0.19)	-0.36*** (0.13)	-0.60*** (0.16)	-0.59** (0.24)	-0.60*** (0.16)	-0.46** (0.20)
Right, $\hat{\kappa}_R$	0.31 (0.27)	0.24* (0.14)	-0.08 (0.05)	-0.19*** (0.05)	-0.08 (0.05)	0.28 (0.18)
Expected inflation						
UMSC, $\hat{\alpha}_2$		0.57*** (0.08)	0.29*** (0.07)	0.35*** (0.13)	0.29*** (0.07)	0.66*** (0.19)
SPF, $\hat{\alpha}_1$	0.73*** (0.16)	0.13 (0.16)	0.24* (0.12)	0.16 (0.23)	0.24* (0.12)	0.38** (0.19)
Sum of lags, $\hat{\alpha}_0$	0.27 (0.16)	0.30** (0.12)	0.47*** (0.08)	0.49*** (0.13)	0.51*** (0.09)	-0.05 (0.18)
Threshold, $\hat{\gamma}$						
Point estimate	1.95	1.95	-0.32	-0.82	2.47	1.95
95% CI	[-0.67, 2.93]	[-0.82, 2.93]	[-0.82, 1.27]	[-0.82, 2.93]	[-0.80, 2.93]	[-0.38, 3.31]
Test p -value						
0 vs. 1, $H_0: 0$	0.03	0.01	0.04	0.69	0.04	0.05
1 vs. 2, $H_0: 1$	0.94	0.72	0.77	0.34	0.36	0.56
R^2	0.74	0.83	0.90	0.87	0.91	0.71
N	205	205	205	205	205	163

Note: See notes to Table 1. The estimation sample in Columns (1)–(5) is 1968:Q4 through 2019:Q4. The SPF expectations are based on the GDP deflator because it is the only available series that dates back to the 1960s. CPI-U-RS refers to the CPI research series that uses current methods. This sample (Column (6)) is truncated at 1978 due to data availability.

* $p < 0.1$.

** $p < 0.05$.

*** $p < 0.01$.

expectations due to their salience. Finally, the methods used to construct the CPI have evolved during the sample period. The BLS publishes a research series based on current methods (CPI-U-RS). We consider these alternative measures of inflation next.

Column (2) of Table 2 presents our baseline-specification estimates when inflation is measured using the PCE price index. In this specification, the estimated threshold equals the baseline value, and the linear model is rejected at a 1% level. The relative weight of the consumer expectations decreases from 0.73 to 0.57, whereas the weight of the professional forecasters' expectations increases relative to the baseline in Table 1, but overall remains small. Despite the stronger statistical case for nonlinearities, the economic interpretation is similar to the baseline. That is, even if nonlinearities matter, they do so at rather high levels of unemployment, thereby giving rise to a regime that occurs relatively infrequently.

Column (3) of Table 2 focuses on the GDP deflator. This inflation measure has been often preferred in the DSGE literature (e.g., Smets & Wouters, 2007). The threshold is again significant, at a 5% level. Importantly, the estimated threshold is -0.32 , giving relatively more prominence to the high-slope regime than in the baseline.²¹ As before, the curve appears relatively steep when the unemployment gap is high and nearly flat when it is low. The UMSC weight in this model is 0.29, even lower than in the PCE model, while the SPF weight is 0.24. The more prominent role of the SPF expectations can be explained by the fact that both actual inflation and predicted inflation are measured with the GDP deflator.

Our conclusions remain qualitatively the same when we consider the core measures of consumer prices, but there are some quantitative differences. For the core CPI (Column (4)), the threshold moves to the left. However, the threshold estimate is insignificant (p -value at 0.69), and the slopes on both sides of the threshold are strongly negative and statistically indistinguishable from each other. Simply put, with the core CPI, the threshold disappears completely. This result supports our general conclusion that nonlinearities do not provide a consistent explanation of inflation dynamics in our study. For the core PCE price index (Column (5)), the high-unemployment regime occurs even less frequently than in the baseline, as the estimated threshold is about 0.5 percentage points larger than our benchmark estimate.²²

²¹This point is visualized by Figure B.1 in Appendix S1 Section B.

²²In Appendix S1 Section B, Tables B.2–B.7 present a set of results for other measures of slack (the unemployment rate and labor's share). They are consistent with our main conclusions.

Finally, in Column (6), we show estimates obtained using constant methods CPI inflation (CPI-U-RS).²³ Starting in 1978, this series is shorter than the baseline. Nonetheless, the overall conclusions remain intact. The threshold value is the same as in our baseline based on the longer sample. The left portion of the curve is flatter than the right portion. Consumer expectations have the largest weight in the inflation expectations process. As in some other exercises, and unlike in our baseline, the formal test rejects linearity in favor of one threshold. But, as before, the baseline threshold gives rise to asymmetric regimes, with the high-unemployment regime being relatively infrequent.

To summarize, this section establishes two main points. First, despite the mismatch, consumers' inflation expectations are important not only for CPI inflation but for a wide range of inflation measures. Second, while nonlinearities are either marginally significant or insignificant in specifications with CPI inflation and consumer expectations (of CPI inflation), nonlinearities may regain significance when consumer expectations are absent or when the measures of inflation and consumer expectations no longer coincide, most notably for GDP inflation.

4.3 | Evidence from other identification strategies

4.3.1 | External shocks as instruments

In our baseline specification, we trace the Phillips curve by controlling for cost-push shocks. Including these controls addresses various issues with identification of the Phillips curve.²⁴ A complementary approach is to use instrumental variables. In recent work, Barnichon and Mesters (2020) estimate the Phillips curve using monetary policy shocks as instruments.²⁵ Combining the Hansen (2017) threshold regression with the Barnichon and Mesters (2020) approach is a very interesting but challenging endeavor, as the econometric tools to do so are currently unavailable.

Instead, we make an inroad as follows. We estimate the model using two-stage least squares with grid search over potential threshold values. And then, we assess nonlinearities by testing for equality of the estimated regimes' slopes in the nonlinear case. However, we are unable to formally test the linear model versus nonlinear models or to compute confidence intervals for the threshold. To implement two-stage least squares, we follow the literature and instrument the unemployment gap with separately identified monetary policy shocks. We use the Romer and Romer (2004) shocks updated by Wieland and Yang (2020). These shocks are constructed using the Federal Reserve's confidential forecasts, which are released to the public with a five-year lag. Therefore, our sample period ends in 2015. We consider two version of these shocks: One is based on the federal funds rate, as in the original paper. The other is based on the Wu and Xia (2016) shadow rate, which we use to account for unconventional monetary policies during the period when the federal funds rate was constrained by the zero lower bound.

Results in Columns (1) and (2) of Table 3 show that our qualitative conclusions remain mostly unchanged. The slope parameter in the linear regression (-0.30 for the shadow rate specification in Panel A, Column (2)) is similar to the OLS linear slope, thereby indicating that cost-push shocks can address endogeneity issues. In the nonlinear case (Panel B), the threshold is estimated at 1.13, with a left slope (-0.59) higher in absolute value than the right slope (-0.06). However, we cannot reject the null hypothesis that the slopes in the two-threshold regions are equal (p -value is 0.51).²⁶

4.3.2 | Exploiting regional variation

Yet another approach to identify the Phillips curve exploits regional variation. Kumar and Orrenius (2016), Babb and Detmeister (2017), Hooper et al. (2020), and Hazell et al. (2022), among others, provide very interesting analyses along this dimension. A particular advantage of this approach is that, by focusing on deviations of regional inflation and unemployment from their corresponding aggregate rates, one can remove variation due to aggregate supply shocks (e.g., oil price shocks), monetary policy, and other factors determined at the national level.

²³For a description and a recent application of this series, see Stewart and Reed (2000) and Bolhuis et al. (2022).

²⁴In Section 6.1, as a robustness exercise, we also control for financial frictions, because they could simultaneously affect the left-hand-side and right-hand-side variables.

²⁵See also Del Negro et al. (2020) for an estimation approach conditional on demand shocks.

²⁶We provide additional results in Appendix S1 Section D. In particular, we consider the case where we fix the threshold at the level estimated using our baseline method. We find qualitatively similar results. However, we note that the slopes in all these exercises are not statistically different from zero, indicating limited power of this method.

TABLE 3 Alternative identification strategies.

Method Slack/regime Romer and Romer shocks based on Fixed effects	Two-stage least squares Unemployment gap		MSA panel Unemployment rate
	Federal funds rate	Wu and Xia shadow rate	—
	(1)	(2)	MSA, time (3)
Panel A: Linear model			
Slope, $\hat{\kappa}$	-0.27 (0.18)	-0.30 (0.19)	-0.41*** (0.06)
Panel B: Threshold model			
Slopes			
Left, $\hat{\kappa}_L$	-0.65 (0.64)	-0.59 (0.54)	-0.45*** (0.07)
Right, $\hat{\kappa}_R$	-0.10 (0.32)	-0.06 (0.31)	-0.34*** (0.08)
Expected inflation			
UMSC, $\hat{\alpha}_2$	0.84*** (0.20)	0.84*** (0.19)	0.00 (0.11)
SPF, $\hat{\alpha}_1$	-0.27 (0.36)	-0.27 (0.35)	
Sum of lags, $\hat{\alpha}_0$	0.43** (0.15)	0.43** (0.15)	0.07** (0.04)
Threshold, $\hat{\gamma}$	1.08	1.13	6.8
Test p -value (H_0 : linear model)	0.55	0.51	0.94
N	168	168	1248

Note: Estimates obtained using two-stage least squares with grid search and aggregate data are shown in Columns (1) and (2). The estimation sample is 1969:Q1 through 2015:Q4 at a quarterly frequency. The dependent variable is CPI inflation. The slack and regime variable is the unemployment gap. The Romer and Romer (2004) shocks, extended by Wieland and Yang (2020), are used to instrument the gap. In Column (1), the shocks are based on the federal funds rate. In Column (2), the shocks are based on the Wu and Xia (2016) shadow rate. The 2SLS regressions include 20 lags of the shocks. The threshold estimates in Panel B are obtained by minimizing the residual sum of squares. Estimates of the panel regression in Equation (4) applied to metropolitan-level data are shown in Column (3). The estimation sample includes 24 MSAs during the period 1991:H1 through 2017:H2 at a semiannual frequency. The dependent variable is the core CPI inflation rate. The slack and regime variable is the unemployment rate. The threshold is estimated following Kremer et al. (2013). The threshold p -value is computed using a residual wild bootstrap clustered at the MSA level (Cameron et al., 2008). Both MSA and time fixed effects are included. Standard errors are clustered at the MSA level.

* $p < 0.1$.

** $p < 0.05$.

*** $p < 0.01$.

Building on McLeay and Tenreyro (2019), we introduce a threshold into a Phillips curve estimated at the metropolitan area level. Following their approach, we approximate consumer inflation expectations in a given MSA by the UMSC expectations for the broad geographical region in which the metro area is located.²⁷ In our preferred specification, we include the unemployment rate as a slack and regime variable, metropolitan area fixed effects (to partially account for regional variation in the natural unemployment rates), and time fixed effects to account for aggregate shocks. The threshold is estimated as in Kremer et al. (2013). Due to the requirement of a balanced panel and general data availability, we estimate the model for 24 MSAs during the period 1991:H1–2017:H2 at a semiannual frequency.²⁸

Specifically, we estimate the following specification:

$$\pi_{i,t} = \mu_i + \zeta_t + \delta \pi_{i,t-1} + \alpha \mathbb{E}_{j(i),t}^{\text{UMSC}} \pi_{j(i),t+1} + \kappa_L u_{i,t} \times \mathbb{I}(u_{i,t} < \gamma) + \kappa_R u_{i,t} \times \mathbb{I}(u_{i,t} \geq \gamma) + \varepsilon_{i,t}, \tag{4}$$

where $\pi_{i,t}$ is the inflation rate at MSA i and semester t , $\mathbb{E}_{j(i),t}^{\text{UMSC}} \pi_{j(i),t+1}$ is the expected next year inflation in geographical region j containing MSA i , $u_{i,t}$ is the unemployment rate, $\varepsilon_{i,t}$ is the error term, and $\mu_i, \zeta_t, \delta, \alpha, \kappa_L, \kappa_R, \gamma$ are estimated parameters. In this specification, location fixed effects, μ_i , help account for variation in the natural unemployment rates across metropolitan areas, and time fixed effects, ζ_t , for aggregate effects, including endogenous monetary policy responses.

We show estimates of the regional specification in Column (3) of Table 3. Overall, they are consistent with those based on aggregate data. The linear slope, at -0.41 , is slightly higher than in the aggregate case. In the nonlinear model, we

²⁷The four broad regions for which the UMSC measure is available are North Central, North East, South, and West. We note that metropolitan inflation varies substantially within these regions and likely so do the corresponding expectations. Alternative measures with more detailed regional variation are available only for a short period.

²⁸To enhance comparability with McLeay and Tenreyro (2019), we focus on core CPI inflation.

Inflation	Great Inflation		Volcker disinflation	
	Peak-to-trough		Peak-to-trough	
	change (ppt)	RMSE	change (ppt)	RMSE
	(1)	(2)	(3)	(4)
CPI inflation	13.1		-16.5	
Linear model	6.6	1.90	-9.9	2.70
Threshold model	6.6	1.98	-9.0	2.85

TABLE 4 Model in-sample fit.

Note: The Great Inflation episode is defined as the period 1976:Q2 through 1980:Q1, based on the lowest and highest CPI inflation values around the crisis. The Volcker disinflation episode is 1980:Q1 through 1983:Q1.

again find that the Phillips curve is steeper in the left region (with a slope of -0.45) than in the right region (-0.34). The difference between the slopes is smaller in magnitude than in the aggregate case. We estimate the threshold at an unemployment rate of 6.8%, with a 95% confidence interval from 5.4% to 7.5%. However, the linear model cannot be rejected in favor of a one-threshold model, with a corresponding p -value of 0.94. The coefficient on consumer inflation expectations is virtually zero, likely due to mismeasured expectations.²⁹ We note that, due to data limitations, these results call for further research, as more detailed data on regional variation in consumer expectations and longer time series become available.

To sum up, whether we identify the Phillips curve using supply-side control variables, exogenous demand shocks, or regional variation, the case for nonlinearities is weak. In contrast, we find that consumer expectations of aggregate inflation play an important role in inflation dynamics, which cannot be fully captured by professional forecasters' expectations or inflation inertia.

5 | ANALYSES OF HISTORICAL EPISODES

We now examine the merits of nonlinearities during four different periods of large deviations of inflation and/or unemployment from their trends. During the early episodes (1970s–1980s) inflation surged, making the policymakers focus on potentially costly disinflation strategies. During the recent episodes (2010s), the unemployment surged and then dropped to very low levels, whereas inflation remained relatively stable. Hence, these two periods allow us to focus on significant deviations from the steady state on both sides of the Phillips curve equation.

5.1 | The Great Inflation and the Volcker disinflation

We now look at the performance of the model during the Great Inflation of the 1970s and the subsequent Volcker disinflation. We define the former period as 1976:Q2 through 1980:Q1 and the latter period as 1980:Q1 through 1983:Q1. While we would like to focus on out-of-sample forecasts, the sample period preceding these episodes is too short to reliably estimate a threshold model. Therefore, in this section we focus on in-sample performance.³⁰ We use two criteria: (1) the change in inflation from the beginning to the end of the period and (2) the models' fit during the entire episode measured by the root mean squared error (RMSE).³¹ Table 4 shows the results.

During the Great Inflation, the runup in inflation was 13.1 percentage points (Column (1)). We show that nonlinearities do not help explaining this runup. Switching from the linear model to the nonlinear one does not result in a larger fraction of explained inflation, as both models produce an increase of 6.6 percentage points. Similar conclusions follow from the RMSE analysis (Column (2)). In this case, nonlinearities even harm the model's fit, resulting in a larger RMSE.

The Volcker period is characterized by a disinflation of 16.5 percentage points (Column (3)). The linear model explains more of the disinflation (9.9 ppt) than the nonlinear model (9.0 ppt). During this episode, the Phillips curve can explain

²⁹We present additional results in Appendix S1 Section E. When we do not include time fixed effects, which absorb aggregate inflation expectations, the coefficient on regional consumer expectations is positive and significantly different from zero. Thus, consumer inflation expectations are likely still important at the regional level. See Appendix S1 Section E, Table E.1 for more details. Note also that time fixed effects fully absorb our measure of professional forecasters' expectations, as these data are available only at the aggregate level.

³⁰In the next section, where we study the missing disinflation and the missing inflation of the 2010s, we focus mainly on out-of-sample forecasts, with in-sample results relegated to the Appendix S1.

³¹Figure B.2 in Appendix S1 Section B shows the models' fit during the full estimation period. Figures B.3 and B.4 provide additional evidence on the two episodes.

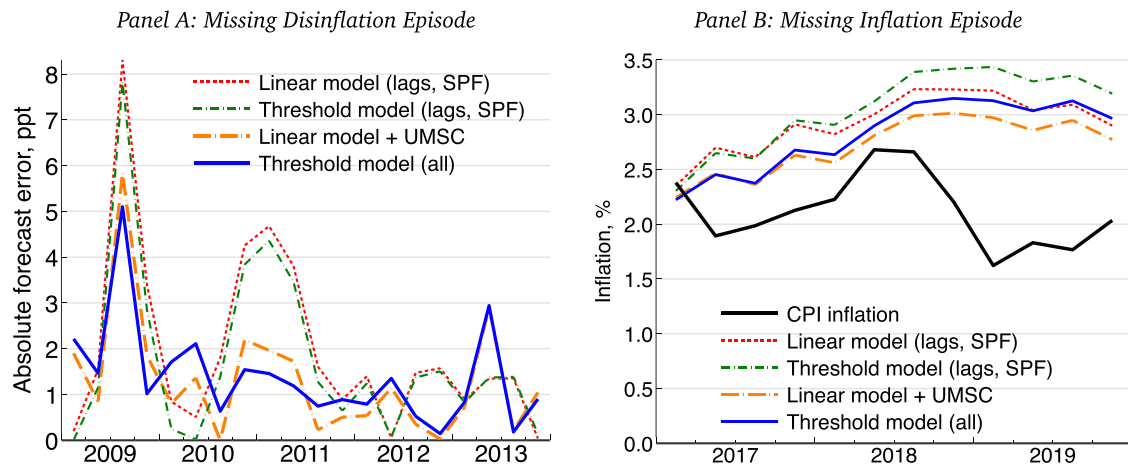


FIGURE 2 Out-of-sample forecasts. *Note:* The left panel focuses on the missing-disinflation episode and shows absolute out-of-sample forecast errors for the linear model with inflation lags and SPF (red dashed line); for the corresponding threshold model (green short dash-dot line); for the linear model with the lags, SPF, and UMSC inflation expectations (orange long dash-dot line); and for the threshold model with all expectations based on estimates in Column (1) of Table 1 (blue thin line). The right panel shows actual out-of-sample forecasts and the actual, seasonally adjusted, annualized CPI inflation rates (thick black line). As quarterly changes in the headline CPI were volatile during the missing-inflation period, for better visibility in Panel B, we show averages of the annualized quarterly rates over the preceding four-quarter period.

a larger share of the peak-to-trough change in inflation than during the Great Inflation. Again, the linear model has a smaller RMSE than the nonlinear model (Column (4)). Overall, during this early episode, nonlinearities make the Phillips curve dynamics too slow relative to the data.

5.2 | The missing disinflation and the missing inflation of the 2010s

In contrast, during the early 2010s, nonlinearities play a somewhat more positive role, but such improvements become weaker when consumer expectations are included.³² One key piece of evidence comes from one-step-ahead out-of-sample forecasts of inflation. Panel A of Figure 2 compares the absolute forecast errors obtained from the linear model with backward-looking and SPF expectations (red dashed line) and the corresponding threshold model (green thin dash-dot line). It is well known that inflation forecasts of different models are usually similar. Still, during the missing-disinflation period, the threshold model's forecast improves upon the linear model's forecast. For 2009:Q3, the linear model's forecast is improved by about half a percentage point. For the period 2010:Q4 through 2011:Q2, the threshold model produces quarterly forecasts that are again significantly closer to actual inflation. In 2012 and 2013, as the missing-disinflation episode is near its end, the two forecasts converge to each other.

Panel A of Figure 2 also plots forecasts from the linear model with consumer expectations (orange dash-dot line) and from the baseline model with one threshold and consumer expectations (blue solid line). Adding consumer expectations to the model clearly has a larger quantitative effect than allowing for nonlinearities. For example, in 2009:Q3 and 2010:Q4 through 2011:Q2 consumer expectations reduce absolute forecast error by up to 2.5 percentage points. But while adding nonlinearities to the model with consumer expectations improves the forecast further, the gain is relatively small and short-lived (compare the blue solid line with the orange thick dash-dot line). Hence, even though nonlinearities occasionally improve the fit of the model during this episode, their role is muted when expectations are properly measured.³³

In the late 2010s, a *missing-inflation* puzzle emerged, providing yet another evidence on nonlinearities and expectations. This episode featured very low-unemployment rates and gaps, indicating possible overheating (CBO, (2019); Crump et al., (2019)). In 2017:Q1, for example, the unemployment gap fell below zero and continued to decline until it reached its

³²Figures B.5 and B.6 in Appendix S1 Section B show that nonlinearities help explain the missing-disinflation episode for the case of naive, backward-looking expectations and evaluate the role of the continuity constraint.

³³In Appendix S1 Section B, we also show in-sample fit (Tables B.8 and B.9 and Figure B.7) and out-of-sample dynamic forecasts (Figure B.8). These results support our conclusions.

trough of nearly -1% in the second half of 2019. According to both the linear and nonlinear models, inflation should have picked up during this period. Instead, inflation remained stable and even declined by some measures. At the same time, consumers expected low inflation, which could bridge the gap between the models and the data. We find that consumer expectations improve the fit during this period; however, the effects are not large.

Panel B of Figure 2 shows the forecasts obtained from the four versions of the Phillips curve we considered earlier, as well as actual CPI inflation, during the period 2017–2019. All four models produce inflation dynamics similar to one another: that is, they forecast rising inflation. However, the threshold models diverge from the data more than the corresponding linear models, because the Phillips curve is relatively steeper in the low-unemployment regime. In contrast, the models with consumer expectations are closer to the observed inflation than the corresponding models that allow for only SPF and backward-looking expectations. The best forecasts are obtained from the linear model with consumer expectations (orange thick dash-dot line). Yet the differences between the models' forecasts are small relative to the corresponding forecast errors. For instance, consumer expectations account for a 0.1 percentage point improvement in forecast accuracy, while the thresholds harm the forecasts by up to 0.2 percentage points. However, even the best forecasting model misses the data by 0.75–1.5 percentage point by 2019. Hence, from a Phillips curve prospective, the missing inflation remains a puzzle even when nonlinearities and various measures of expectations are considered.³⁴

Thus, while allowing for a high-unemployment regime somewhat helps the Phillips curve match the data in the early 2010s (during the missing disinflation), it does not help at all or even harms the model in the 1970s (during the Great Inflation), in the 1980s (during the Volcker disinflation), and in the late 2010s (during the missing inflation).³⁵ These results are consistent with the observation that in the full sample nonlinearities are not significant.

6 | ROBUSTNESS

6.1 | Financial frictions

The recent global financial crisis brought to the forefront financial frictions as a factor affecting economic fluctuations. Gilchrist et al. (2009), Philippon (2009), and others emphasize the predictive content of corporate bond spreads for consumption, output, and inflation. Moreover, in a structural model, Christiano et al. (2015) and Del Negro et al. (2015), among others, propose financial frictions as yet another explanation for the missing disinflation.³⁶ If financial frictions correlate with expectations or the sources of nonlinearities, controlling for them may affect our baseline estimates. Therefore, we test whether the state of financial markets overturns our results on nonlinearities and expectations.

In Column (1) of Table 5, we control for the Baa–Aaa corporate bond spread, a popular measure used in the literature.³⁷ We find that this measure does not change the results qualitatively. In fact, the results strengthen (see Table 1, Column (1)). The coefficient on consumer expectations increases and remains statistically significant. Thresholds remain insignificant and now even more so.

In Column (2) of Table 5, we control for the Gilchrist and Zakrajšek (2012) credit spread, a measure based on corporate bonds traded in the secondary market and shown to be highly informative about economic activity. In addition to the component measuring countercyclical movements in expected defaults—which is similar to the Baa–Aaa corporate bond spread—this variable captures the excess bond premium, measuring changes in the relationship between default risk and credit spreads. In Column (3), we estimate the specification with the excess bond premium.

Similar to the results with the Baa–Aaa spread, these financial variables strengthen our findings. This can be seen by comparing the results in Columns (2) and (3) with those in Column (4), which presents estimates of our baseline specification for the same sample period.³⁸ Consumer expectations remain significant and their relative weight increases.

³⁴For explanations of the missing inflation favoring changing trends in competition, see Heise et al. (2022).

³⁵We also confirm this evidence formally, by testing nonlinearities in each of these episodes. The F -test is borderline for the missing-disinflation period (the p -value is 0.05) but favors the linear model for the other episodes (Appendix S1 Section C).

³⁶The two papers, however, provide alternative explanations. Christiano et al. (2015) emphasize a decrease in TFP growth and an increase in the cost of working capital, whereas Del Negro et al. (2015) focus on the economic slack during the Great Recession.

³⁷To reflect firms' financial costs, we add the federal funds rate to all spread measures. The qualitative results are unchanged if we employ the spread measures directly. The results for other measures of inflation are also qualitatively similar to the baseline and are reported in Table B.10 in Appendix S1 Section B.

³⁸The credit-spread data are available starting in 1973. Relative to the baseline sample, therefore, we lose more than 4 years of observations with high inflation. The results in Column (1) can be directly compared with the baseline (Table 1, Column (1)).

TABLE 5 Controlling for credit spreads.

	Baa–Aaa spread (1)	GZ credit spread (2)	Excess bond premium (3)	Fixed sample (4)
Panel A: Linear model				
Slope, $\hat{\kappa}$	−0.21*** (0.08)	−0.18** (0.08)	−0.16** (0.07)	−0.29*** (0.09)
Panel B: Threshold model				
Slopes				
Left, $\hat{\kappa}_L$	−0.34** (0.15)	−2.01 (1.41)	−1.82 (1.24)	−3.57** (1.45)
Right, $\hat{\kappa}_R$	0.04 (0.23)	−0.15* (0.08)	−0.13* (0.08)	−0.22** (0.09)
Expected inflation				
UMSC, $\hat{\alpha}_2$	1.08*** (0.20)	1.09*** (0.21)	1.15*** (0.22)	0.83*** (0.20)
SPF, $\hat{\alpha}_1$	−0.10 (0.17)	−0.17 (0.24)	−0.20 (0.23)	−0.21 (0.36)
Sum of lags, $\hat{\alpha}_0$	0.03 (0.18)	0.08 (0.21)	0.05 (0.22)	0.38* (0.21)
Spread coefficient	0.22*** (0.05)	0.21*** (0.06)	0.22*** (0.06)	
Threshold, $\hat{\gamma}$				
Point estimate	1.95	−0.71	−0.71	−0.71
95% confidence interval	[−0.82, 2.93]	[−0.71, 3.14]	[−0.71, 3.14]	[−0.71, 2.30]
No. of thresholds, p -value				
0 vs. 1, $H_0: 0$	0.38	0.62	0.68	0.21
R^2	0.81	0.81	0.81	0.78
N	205	188	188	188

Note: The slack variable is the unemployment gap. Inflation is measured with the CPI inflation. The baseline estimation sample (Column (1)) is 1968:Q4 through 2019:Q4; the sample in Columns (2)–(4) is 1973:Q1 through 2019:Q4. For estimation details, see the notes to Table 1.

* $p < 0.1$.

** $p < 0.05$.

*** $p < 0.01$.

The linear model statistically dominates the nonlinear one. The presence of thresholds was statistically insignificant, and now becomes even more so. In addition, the presence of nonlinearities would still have to be confronted with other popular explanations of the missing inflation, such as smaller movements in short-term unemployment (Ball & Mazumder, 2019) or in expected future marginal costs (Del Negro et al., 2015).

6.2 | Structural break

To provide more evidence that the regimes identified in the threshold model are not due to a structural break in the linear model, we estimate our baseline specification when the sample is split about a possible break period considered in the literature. While the exact reasons for the flattening of the Phillips curve are debated, inflation overall was more stable and less responsive to unemployment starting in the early 1990s than in the previous decades. We therefore split our sample about 1990:Q1.³⁹

Table 6 shows estimates of the threshold model in the post-1990 period.⁴⁰ They are overall consistent with the baseline estimates. The threshold is estimated at an unemployment gap of 2.5% (Column (1)), a little higher than the baseline. The threshold is (marginally) insignificant at the 10% level, as in the baseline case. The Phillips curve appears relatively steep in the low-unemployment regime and flat in the high-unemployment regime. As in the baseline, consumer expectations dominate other expectation components. The results are also similar to the baseline for other measures of slack (Columns (2)–(4)). Thus, we conclude that our findings are not driven by a structural change in the Phillips curve slope and they remain materially unchanged when we focus on the recent period.

³⁹This choice is consistent with procedures based on optimization over possible break points.

⁴⁰We focus on the later subsample because it is more relevant for the contemporaneous Phillips curve. Table B.11 in Appendix S1 Section B shows estimates for the pre-1990 period.

	Unemployment		Labor share	
	Gap (1)	Rate (2)	Raw (3)	Adjusted (4)
Slopes				
Left, $\hat{\kappa}_L$	-0.64** (0.25)	-0.37** (0.17)	0.17** (0.07)	0.72*** (0.17)
Right, $\hat{\kappa}_R$	0.24 (0.33)	0.14 (0.46)	0.59*** (0.21)	0.22* (0.12)
Expected inflation				
UMSC, $\hat{\alpha}_2$	1.35*** (0.34)	1.24*** (0.34)	1.46*** (0.34)	1.59*** (0.23)
SPF, $\hat{\alpha}_1$	-0.51 (0.33)	-0.52 (0.33)	0.77** (0.37)	-0.08 (0.35)
Sum of lags, $\hat{\alpha}_0$	0.16 (0.36)	0.28 (0.36)	-1.23** (0.49)	-0.51 (0.42)
Threshold, $\hat{\gamma}$				
Point estimate	2.50	8.03	-0.80	-2.77
95% confidence interval	[-0.59, 3.14]	[4.07, 8.27]	[-7.75, 1.46]	[-4.95, 0.32]
No. of thresholds, p -value				
0 vs. 1, $H_0: 0$	0.12	0.65	0.13	0.22
R^2	0.47	0.43	0.51	0.49
N	120	120	120	120

TABLE 6 Robustness to structural break: Post-1990 period.

Note: The estimation sample is 1990:Q1 through 2019:Q4. For estimation details, see the notes to Table 1.

* $p < 0.1$.

** $p < 0.05$.

*** $p < 0.01$.

7 | CONCLUSION

In this paper, we examine the presence of nonlinearities in the Phillips curve. It turns out that it is important to properly control for inflation expectations in order to assess the role of nonlinearities in inflation dynamics. Once inflation expectations are measured so as to account for consumer expectations, nonlinearities are muted overall and marginally important only in some specific cases.

Our paper examines in detail several episodes wherein inflation was especially hard to predict: the Great Inflation of the 1970s, the Volcker disinflation, the missing disinflation following the 2008–2009 financial crisis, and the missing inflation of the late 2010s. The missing disinflation can be explained by consumer expectations; once the expectations are controlled for, nonlinearities become far less important. The stability of consumer expectations in this period provided an anchor for inflation, and a flatter Phillips curve helped stabilize inflation only marginally.

In contrast, the Volcker disinflation provides key evidence against nonlinearities. This period was characterized by high unemployment and a recession similar to the missing-disinflation episode. During the Volcker disinflation, however, inflation was reduced; therefore, the nonlinearity operating through a flatter Phillips curve makes the Volcker disinflation too slow. The Great Inflation in the 1970s is yet another episode that sheds light on this important issue. This episode brings additional evidence because in the 1970s, unlike in the other two episodes, economic activity was not subdued. In this episode, too, nonlinearities are detrimental for the model's fit. A more recent episode of the *missing inflation*, which emerged around 2017–2019, also points against nonlinearities.

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This article has been awarded Open Data Badge for making publicly available the digitally-shareable data necessary to reproduce the reported results. Data is available at Open Science Framework.

DATA AVAILABILITY STATEMENT

The data and code used to generate the results in this paper are available on: <https://journaldata.zbw.eu/dataset/inflation-expectations-and-nonlinearities-in-the-phillips-curve-journal-of-applied-econometrics>.

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