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## PRESSURE VOLUME TEMPERATURE RELATIONSHIPS AND

## PHASE EQUILIERIA IN THE SYSTEM ETHYLENE-NORMAL BUTANE

by

## BRYMER WILLIAMS

## A Dissertation Submitted in Partial

Fulfillment of the Requirements for the Degree of Doctor of Philosophy in The University of Michigen

COMMITTEE IN CHARGE
Professor G. G. Brown, Chairman Associate Professor L. 0. Case Associate Professor A. S. Foust Professor D. L. Katz
Associate Professor D. W. McCready

Department of Chemical and Metallurgical Engineerirg

## SUMMARI

This dissertation presents the results obigined in the experimental investigation of the binary hydrocarbon system, athylene-normal butane. The pressure-volume-temperature relations at the liquid-vapor phase boundaries and in the single phase regions were deterained for four mixtures of this system. The experimental results are reported as such, and in the form of generalized equilibrium constants and densities.

By comparison with other binary systems, it was found that the volatility of ethylene in butane solutions is considerably greater than that of a corresponding, but necessarily hypothetical, peraffin hydrocarbon.

The deviations from the ideal gas law of the mixtures in the geseous regions were compared with those of pure ethylene and pure butane. Jpon the bases of reduced pressures and temperatures, the compressibility factors agreed remarkably well.

The construction and operation of the apparatue, wich is suitable without modification for the study of other gaseous mixtures, is described.

## ACKNOwLEDGEMENT

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## INTRODUCTION

The need of modern technology for more extensive and more reliable data than currently exist is much too nell known to require repetition here. The petroleum industry, for example, requires more information regarding the equilibrium relationships of vapor and liquid, critical properties and the densities of hydrocarbon mixtures. As a result of many fears' effort, the behavior of mixtures of paraffin hydrocarbons has been reasonably well, but jet far from completely, explored. The behavior of mixtures which include msaturated hydrocarbons is not so familiar. It was the purpose of this study to extend this knowledge by the investigation of the vapor-liquid phase equilibria and the pressure-volume-temperature-composition relationships of the binary system, ethylene-normal butane.

Knowledge of binary systems is frequently directly applicable to an industrial problem, and is always useful in developing empirical or thermodynamic relationships which can be used to predict the behavior of the constituents of a binary system in a more complex mixture. As many of the problems in the petroleum industry involve such complex mixtures that an experimental analysis of the properties is, from a practical standpoint, impossible, it is very desirable to obtain as much information as possible regarding the properties of the verious types of hydrocarbons in simple mixtures.

At the start of this investigation, it was known that the results of similar work were soon to be published which would complete the data for the three binary paraffin systems: ethane-n-butane, ethane-n-heptane and n-butane-n-heptene ${ }^{(18,19,21)}$. The particular
system ethylene-n-butione was chosen as the subject for this investigation to further some integration of the overall problem, and to compare the behavior in butane of ethylene with that of the corresponding paraffin, ethene.

## DESCRIPTION OF THE APPARATUS

## The Piezometric Equipment

The sketch, Figure 1, shows the equipment used in observing the dew and bubble points and the densities of the samples. The apparatus is similar to that used by Sydney Young in his classical studies and to that later used by Kay ${ }^{(1,17-21)}$. A sample of known weight of the hydrocarbon mixture under study is confined over mercury in a Pyrex tube (piezometer). The open end of the tube was fastened tightly in a high pressure bomb and was under a liquid seal. The details of the stuffing box and closure are also show in Figure 1. Once installed, the tubes were never removed from the stuffing boxes.

In this investigation two glass tubes were used, one for measurements at relatively high pressures, the other used in the lower pressure ranges. The external diameter of each tube was about 15 millimeters and the internal diameters 5.0 and 1.9 millimeters, respectively. A bulb, about 15 cubic centimeters in volume, was blown in the base of each tube so that a gas sample charged at atmose pheric pressure might be large enough to result in a volume which could be measured witin sufficient accuracy at high pressures. The overall length of the tube was about 70 centimeters. The volume of the sample confined over the mercury was found by measuring with a cathetometer the position of the mercury relative to a reference point on the tube. The volume corresponding to this position was then found by reference to a calibration of the tube, wich is described elsewhere in this report.

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The tubes were enclosed, as shown, by glass jackets, forming a vapor bath and insulation. The temperature was maintained wherever desired by the choice of the proper boiling liquid and regulation of the pressure. The compounds used and their atmospheric boiling points are:

| Acetone | $133.0^{0} \mathrm{~F}$ |
| :--- | :--- |
| Benzene | 176.15 |
| Toluene | 231.1 |
| Mono-chlorobenzene | 269.0 |
| Mono-brombenzene | 312.6 |
| Acetophenone | 396.3 |
| Methylsalicylate | 432.1 |

The temperatures were measured by copper-constantan thermocouples suspended over the top of the tube, and the glass connections were shaped to prevent drops of cold condensate from falling on the thermocouples.

Agitation of the sample in the tube to ensure equilibrium between phases was accomplished by inclusion of a small steel rod in the tube. The rod was moved magnetically by the solenoid surrounding the tube.

The source of pressure which was either a cylinder of compressed nitrogen or a hydraulic jack filled with mercury, was connected to a small pressure vessel filled with mercury. This vessel served as a trap and a reservoir of mercury. The pressure in the system was measured at this point. As the bourdon tubes were filled with oil, an oil-filled trap was placed betreen the mercury reservoir and the gages. The surge volune of gas contained in these reservoirs was sufficient to prevent changes in pressure as a result of slight doviations in either room or test temperature.

The pressure in the reservoir was transmitted to either of the piezometers by the flow of mercury. A ball check vaive was inserted in this line to limit surges and loss of mercury in the event of breakage of the glass tubes. The check valve was installed with a slight tilt so that the buoyancy of the ball would prevent sealing at low rates of flow, and yet would close at high rates.

All tubing was $1 / 8$-inch O.D. steel, and the connections were of the cone and follower type fabricated by the American Instrument Company. All valves were $1 / 4$-inch metric valves.

## Pressure Control System

This system was designed to regulate the pressure in the vapor baths so that the desired limit of variation in temperature, $\pm 0.01^{\circ} \mathrm{F}$, might be attained. As, in the usable region, the slope of the vapor pressure curves of the compounds used in the vapor baths was 6-10 mm mercury per degree Fahrenheit, it was necessary that the pressure be regulated to about $\pm 0.1 \mathrm{~mm}$ mercury. The system, illustrated by the flow diagram in Figure 2, behaved admirably; with it the galvanometer frequently remained motionless for hours.

In essence, a surge volume of ten gallons was connected to the vapor baths. Air was supplied to or withdrawn from this volume continuously for operation above or below atmospheric pressure, respectively. This tendency toward a change in the pressure was offset by intermittent leakage or venting through an electrically operated flutter valve which was actuated by the pressure in the system.


To follow the operation, suppose that while the vapor bath is under vacuum, its pressure rises slightly. As a result, the mercury level rises in the small arm of the manostat, and closes the circuit of the miniature relay. This closes, in turn, the second relay and the relay flutter valve. In the latter, a soft rubber pad was attached to the moving arm of the relay, so placed that when the relay circuit was closed the pad sealed the end of the vent tube. To continue the sequence of events, the closure of the vent tube stopped the leakage of air into the system and allowed the vacum pump to reduce the pressure to the required value.

The absolute pressure of the system was roughly set by manipulation of the throttle valves in the vacuum pump or compressed air lines, and in the vent line. A fine adjustment could be made by use of the extra level of mercury attached to the manostat. Other refinements were the reversing awitch which was useful in transferring from vacuum to above atmospheric pressure and the manually operated auxiliary vent valve. The use of the miniature relay, which required only about 15 microamperes, assured rapid response without arcing to small changes in pressure at tine manostat. The system operated smoothly and without hunting at all desired pressures.

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## Preparation of the Mixtures

The apperetus used in preparing the mixtures and introducing measured samples in the tubes ie shown in Figure 3. Two glass bulbs, connected as shown each with its owa mercury leveling bottle, were used to make the gaseous mixtures. The large bulb, with a volume of approximately one and one-half liters, had about seven times the capacity of the smaller bulb.

A mixture was prepared by filling the small bulb a number of times with one gas or the other, and emptying its contents into the large bulb. For instance, one filling of ethylene and four of butane would result in a mixture of approximately 20 mol percent ethylene.

The swall bulb was filled to an etched reference mark, and the pressure above or below atmospheric determined by measurement, with a cathetometer, of the difference between the level in the sample bulb and in the leveling buib. The temperature, which was maintained by immersion in a water bath, was measured to $0.01^{\circ} \mathrm{F}$ with a thermometer. As the volume of the small bulb was taken as unity, no calibration of the volume was necessary.

The densities and deviations from the ideal ges laws are accurately laom for butane and etinylene at and near atmospheric temperatures and pressures $(3,4,5,6,3,15,16)$. With these known densities the relative weights of butane or ethylene in each of the portions of the totol mixture were easily calculated. A sample calculation of this sort is included in the appendix.

After preparation, a sample was thoroughly mixed by agitation and by etanding before the piezometric tubes were filled.

The method, used in this investigation, of determining the weight of the sample placed in the pieqometers required precise knowledge of the densities of the mixtures at room conditions. Therefore, as a prelude to loading the piezometers, the density of each mixture was messured over a range of pressures from 300 to 900 mm mercury at a temperature as close to $68^{\circ} \mathrm{F}\left(25^{\circ} \mathrm{C}\right)$ as possible. The densities were found by weighing the quantity of ethylene in a glass density bulb of known volume. The customary precautions and technique of using a second bulb as a counter balance were followed. The temperature of $68^{\circ} \mathrm{F}$ was chosen as, $\varepsilon$ t this temperature, the densities of ethylene and butane are most accurately known.

These experimental densities were used to compute the amount of materiel cherged to a piezometer. A tabulation of the dimensionless compressibility factors (PV/NRT) for verious pressures at $68^{\circ} \mathrm{F}$, and for the four mixtures made, fcllows:

## Mol Percent Ethylene

| Pressure <br> mm Hg | 12.85 |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  |  | 40.78 | 66.18 | 80.88 |
| 950 | 0.9677 | 0.9745 | 0.9827 | 0.9875 |
| 800 | 0.9716 | 0.9776 | 0.9850 | 0.9892 |
| 700 | 0.9746 | 0.9800 | 0.9866 | 0.9905 |
| 500 | 0.9815 | 0.9858 | 0.9902 | 0.9980 |
| 200 | 0.9925 | 0.9941 | 0.9961 | 0.9972 |

The measured densities and compressibility factors agree very well with densities obtained by molar interpoletion between the densities of the pure compounds. The maximum deviation between the experimental and interpolated densities was $0.044 \%$; the former was the higher density at this point. This is in accord with the reported behavior of butane-pentone mixtures ${ }^{(16)}$.

As a precaution against major errors in the computed compositions, each mixture was analyzed in an absorption gas analysis apparatus over bromine water. Naturally, the accuracy of analysis by absorption is inherently far less than that of a computed analysis, only gross errors in composition would be revealed. The anslytical and calculated compositions agreed within one percent.

## Filling the Tubes

The apparatus used to fill the tubes, which is also shown in Figure 3, consists of two essentiel parts, namely, the precision buret in which the sample is measured, and the device for placing this sample in the plezometer without loss or leakage of air.

The weight of a sample was computed from the measured valume of vapor at a knom pressure and temperature, by means of the compressibility factors previously cited. In order to combine the properties of sufficient capacity and accuracy, a buret was made by blowing a number of bulbs, as shom, in a relatively small bore glass tube. About two centimeters of straight tube were left between adjacent bulbs. The volume of the buret was calibrated with mercury by the same technique used for the piezometers. The total volume of the buret was about 35 cubic centimeters. As the measurements of height were made in the straight sections, in which the volume was one cubic centimeter per twelve centimeters of length, the accuracy of volume neasurement should have been comparable to that of a calibrated tube over 400 centimeters long.

The buret was submerged in a water bath for constancy of temperature. The pressure in the buret was found by measuring, with the cathetometer, the difference in height of the mercury columns in the buret and in the second leg which wes open to atmospheric pressure. The internal diameters of the straight portions of the buret and the external leg were the same. This eliminated errors caused by differences in the extent of capillary depression of mercury.

As for any composition, the gaseous density was known as a function of temperature and pressure, the conversion from volume confined in the buret to weight was simple and accurate. In practice, the weight of sample was verified by repeating the volume measurements at two or three pressures. No sigaificant discrepancy was ever noticed.

The known sample was transferred to the pressure tubes through a hypodermic needle in the apparatus sketched in Figure 3. A cross of large bore glass tubing was made with a cup sealed around one of the short arms. This cross was mounted securely upon a frame in the position shown, and one long arm was permanently connected to the vacuam system, i.e., a McLeod gage, a mercury diffusion pump, and a Cenco Hyvac pump.

The pressure tube to be filled was then sealed to the upper arm with a sleeve of rubber tubing and deKhotinsky cement. The buret assembly was installed with the leur of the hypodermic attachment inserted into the lower arm so that the tip of the needle extended well into the bulge in the piezometer, but was below the rim of the cup. The leur, which had been chosen with a close clearance in the lower arm, was sealed in place with a rubber sleeve and cement.

The procedure used in filling a tube was as follows:

1) The cup surrounding the top arm was filled with mercury, and the entire system was evacuated for $24-36$ hours at an absolute pressure of le:s than 0.1 micron of mercury. At intervals the tube was heated to aid the removal of adsorbed gases from the glass surface.
2) When evacuation and desorption were considered complete, the tube was flushed with some of the gaseous mixture to be studied and reevacuated.
3) After this second evacuation, mercury was admitted through the long arin until the liquid level in the piezometer was just below the top of the needle.
4) The gas sample, the weight of which had been determined, was passed from the buret through the needle into the tube.
5) By use of the leveling bulb, the pressure in the piezometer was adjusted to very slightly above one atmosphere.
6) The rubber-cement joint between the piezometer and the cross was removed. Without breaking the liquid seal, the tube was disengaged from the needle.
7) In order to transport the tube to the pressure equipment without breaking the liquid seal, a very small beaker was then fitted under the open end of the tube mader the mercury level in the cup. As the mall beaker formed a seal, it and the tube could be removed from the cup and placed under the mercury level in the high pressure bamb without air leakage or loss of sample. After this, the small beaker was removed, the bomb closed and made ready for the experiments.
8) Owing to certain unavoidable features in the construction, it was possible that small amounts of the gas sample might be trapped
in the stopcocks and connecting tubes. Before the piezometer was removed, a test was made for the presence of trapped vapor by closing the stopcock nearest the leur and reducing the pressure in the buret by lowering the mercury level. In no case was any of the measured gas sample so lost.

EXPERIMENTAL TECHNIQUE

The operation of the apparatus which has been described was basically simple. It involved the application of pressure, control of the temperature and measurement of a volume. However, various refinements, especially in determining dew and bubble points, and arbitrary conditions of equilibrium and tightness were found necessary. These are described here as a possible aid to further work, and as a clue to the accuracy of the recorded data.

## Leakage in the System

In certain portions of the two-phase region the density or quality of the sample was extremely sensitive to small changes in the pressure or temperature. This was especially true near the critical points and in the retrograde region. Owing to this sensitivity, the determination of dew or bubble points, and the volume was frequently very slow. Maintenance of pressure through elimination of leakage was, therefore, absolutely essential. Accordingly, an arbitrary standard for tightaess of the system wes set: the allowable pressure drop was one percent at 1000 1b./sq.in. in twenty-four hours. This allowed two hours for a single measurement at the maximum pressure with a loss of pressure of but one-tenth of one percent. Actually the leakage was always less than this. The maximum resulted in a loss of about 0.7 percent in twenty-four hours.

## Order of the Measurements

In general, measurements were made at successively higher temperatures within the temperature range of any one compound used in the vapor bath, and further, successively higher boiling compounds were used. However, efter the range had been explored, measurements were repeated at approximately the medium temperature and at the lowest temperature to test for eny chemical or physicel changes in the sample. In 811 cases, there was no apparent deterioration.

## Maintenence of Steady State Conditions

No data were recorded until steady state or equilibrium conditions had been maintained for at least two minutes. The indications of stability were no visible change in pressure, no change in the mercury level and agreement to $0.4^{\circ} \mathrm{F}$ between the temperature indicated by the thermocouples and that corresponding to the pressure of the vepor bath. The limit of $0.4^{\circ} \mathrm{F}$ was rather high, but it was about the limit of accuracy given by the combination of vopor pressure data, the manometer and the purity of the vapor bath. The stipulation, however, insures uniformity of temperature between the base and the top of the tube, and the attainment of equilibrium after a change in temperature.

## Determination of Bubble Points

Bubble points were determined by approaching from the single phase region. After the sample had been thoroughly stirred, and iso-
thermal conditions maintained, the pressure was slowly decreased by venting nitrogen from the system until the merest bubble of vapor appeared in the top of the tube. This was noted as the bubble point pressure, and was repeated at least once as a check. When well removed from the critical region, the compressibility of the liquid is low, and the bubble point density may be measured at pressures slightly above the bubble pressure. However, near the critical region the compressibility is much greater, and much more care was required in measuring the density.

## Determination of the Des Points

As with the bubble points, these were best determined by approach from the single phase region, either by isothermal increase or decrease (in the retrograde region) of pressure. As the volume was relatively large at the dew point, the resulting long, narrow shape of the sample made stirring more difficult. Frequently, it was necessary to augment the magnetic stirring device by alternate expansion and recompression.

When viewed by reflected light, the dew point was characterized by the appearance of small black or dark spots on the glass wall. Other indications of the dew point which were also sensitive, but which usually occurred after further penetration into the two-phase region, were the appearance of the interference colors and the glistening of the meniscus because of the presence of a thin film of liquid. These indications of the dew point were very sensitive. For instance, in the tube filling buret at the ice point, the colored film was observed to appear and disappear with a change in pressure of one millimeter at a total pressure of two atmospheres.

## Determination of the Critical Point

The experimental determination of the critical point is best described by its definition, namely, the point of intersection of the dew point and bubble point lines. In determining bubble points the meniscus first appeared at the top, for dew points it first appeared at the bottom of the sample. To fix the critical point, many dew and bubble point determinations were made at slight changes in temperature. The point at which the meniscus seemed suddenly to appear at neither the top nor at the bottom was judged the critical point. It is believed that the critical points were determined within $0.05^{\circ} \mathrm{F}$ and $\mathrm{l} \mathrm{lb} . / \mathrm{sq} . \mathrm{in}$. The region of opalescence existed over a temperature range as high as $5^{\circ} \mathrm{F}$.

## PURIFICATION OF MATERIALS

## Ethylene

A cylinder of C.P. ethylene $99 \%$ pures obtained from the Ohio Chemical Company, was used in preparing the pure material for the investigation. The raw gas was dried by phosphorus pentoxide and condensed in the reboiler of a silvered, vacuum jacketed Podbielniak distillation column. The fractionating medium was a wire helix about three feet in length. The liquefied ethylene was degassed by prolonged distillation at essentially totel reflux, and then was slowly fractionated at a high reflux ratio. A constant boiling heart cut of about $30 \%$ was condensed in a high pressure storage cylinder. The storage cylinder had been previously deaerated by evacuation while warm, and was purged several times with ethylene before the purified sample was collected. Approximately twenty cubic centimeters of liquid were purified. When tested by absorption in bromine water, the absence of any residusl gas proved the refining process to be satisfactory.

## Butane

The raw material, in this case, was a sample of C.P. n-butene produced by the Philips Petroleum Corporation, and was reported to contain 99.6\% n-butane. The pure hydrocarbon was prepared in the same fashion as was the ethylene, that is, by fractionation and collection of the middle, constant boiling fraction. However, before distillation, the raw butane Was bubbled through fuming sulfuric acid, then through concentrated
potassium hydroxide and dried by phosphorous pentoxide. As a test of the purity, a portion of the finished butane was condensed in a glass tube immersed in melting ice. As the change in pressure during the condensation process was about 0.25 mm of mercury or 1 ess than $0.05 \%$ of the total vapor pressure, the purification was considered to be satisfactory.

## Calculetion of Densities

A sample calculation in the appendix shows the use of the various corrections and calibrations in computing the density of a sample in the tube.

## CALIBRATION OF THE GXPERIMENTAL EQUTPMGNT

## Cathetometer

The measurements of s.ll levels of mercury, either in determining the density of mixtures or in calibrating the piezometer tubes, were made by a cathetometer. With this instrument distances were measured to 0.001 cm by using the vernier scale. To test the accuracy and precision of measurement, the length of a carefully machined and calipered metal bar was determined by use of the cathetometer at several locations along the meter length of the latter. The scale proved to be accurate, as readings were precise and reproducible over the entire range of the instrument. However, the scale bar was rather wavy and it was necessary to level the telescope before each reading and to focus the lens carefully to minimize the effect of parallax. With these simple precautions the measurements were absolutely dependable, and were used directly, without correction. With care, the maximum difference between check readings did not exceed 0.002 cm , and the sverage difference was less than 0.001 cm .

## Thermocoup? es

The temperatures were messured by the combination of copperconetanten thermocouples and a Leeds and Northrup type $K$ potentiometer. With this arrangement, voltages were read, by interpolation, to 0.0001 millivolts which corresponds approximately to $0.005^{\circ} \mathrm{F}$. Temperatures were recorded to the nearest, $0.01^{\circ} \mathrm{F}$. In fabricating the thermocouples, all the customery precautions were observed, such as testing for homogeneity of
the wires, using all copper leads and switches and maintaining proper cold junction conditions. The instruments were cslibrated by comparison With a platinum resistance thermometer and several precision mercury thermometers. All devices used for comparison had been calibrated by the National Bureau of Standards.

The thermocouples were tested during and after the experiments, and the calibrations were found to be unchanged.

## Pressure Gages

Three pressure gages were used; the ranges weres

| $0-200$ psi | $6^{n \prime}$ dial |
| :--- | ---: |
| $0-1000$ psi | $10^{n}$ dial |
| $0-5000$ psi | $6^{n}$ dial |

Nearly all the pressure readings were made with the first two of these gages. Pressures were estimated and recorded to 0.1 psi but are probably accurate only to $0.3-0.4$ psi. The gages were calibrated with a dead weight tester before the experiments, and thereafter were rechecked weekly.

## Piezometer Tubes

The volume of a tube was determined by incrementel filling with small weighed amounts of mercury and by measuring the height of the mercury colum after each addition. Table $X$ shows the data obtained by this procedure. The calibrations were used by plotting on a large graph, as a function
of length, the deviations from the volume of a cylinder with a diameter equal to the arithmetic average diameter of the bore. This method is extremely accurate and simple to use. It is interesting to note that the deviations seem to follow a very rough sine curve.

Before use, the mercury was triple-distilled and degassed. The portions were weighed to the nearest 0.00005 gram with calibrated weights. In measuring the length of the mercury column, two reference points were used. These were the top of the sealed end of the tube and the end of the bore. Either one of these points made a convenient and visually clear base mark. In practice four or five readings were taken of the location of each reference, and of the top and of the bottom of the mercury meniscus.

During the calibration the tube was immersed in a water columan to maintain a constant temperature; this eliminated fluctuation in the level and assured a uniform temperature, and therefore density, throughout the column of mercury.

To obtain the actual volume of the tube at any point on the length by this method, it is necessary to allow for the volume occupied by the meniscus. There are recorded some empirical relations (26) between the meniscus volume, height and diameter but which, when applied to these tubes, were obviously inaccurate. Therefore, the meniscus was assumed to be spherical and its volume calculated as a spherical segment for the given diameter and height. The relative volumes involved and the fact that the height of the meniscus in calibration was so very close to that in the system, density measurements justify this assumption.

## Stixring Rods

The small rods used as magnetic stirring devices in the piezometers were short pieces of polished iron wire, as nearly fashioned into a cylinder as possible. The volume of each rod was determined in two separate ways. It was calculated directly from micrometer measurements, and it was computed from the weight of the rod by using the handbook density. The volumes determined by these methods agreed within three parts in one thousand.

After this comparison showed such good agresment between the two methods, the rods were polished to round the ends and remove any sharp edges. The final volume was then obtained from the weight.

In use the volume was corrected for thermal expansion. As an example of the size of the rod and the correction, the following values were given for the rod used in the high pressure plezometer.

| Temperatures ${ }^{\circ} \mathrm{F}$ | Yolumenm ${ }^{3}$ |
| :---: | :---: |
|  | 0.00483 |
| $140-240$ | 0.00484 |
| $240-340$ | 0.00485 |
| $340-400$ | 0.00486 |

## EXPEFTMENTAL RESUKTS

In the course of this investigation, four mixtures of ethylene and normal butane were prepareci and their behavior studied. The compositions of these four mixtures are given in Teble I. The deasities, pressures and temperatures ot he jiquid-vapor phase boundaries were determined by the techniques previously described. The densities in the single phase region were deternined at several isotherac for each mixture. The linits of the temperature renge explowed were about $50^{\circ} \mathrm{F}$, the temperature of cooling water, and $400^{\circ} \mathrm{F}$. The reconded pressures veried from about 50 to 1100 pounds per square inch.

The experimental data ere presented graphically on the succeadIng pages by Figures 4 - 10, which show respectively, the pressure-temperature relathonshipe at the phase boundaries, the saturated dersities of the mixtures and densities at various isotheres for each of the mixtures. The experimentai points from which these plots gere constructed are shown in the plots and are also listed in Tables VII - IX, wich are to be found in the Appendix. The conditions defining the critical points, and the points of maximum temperatwe and pressure for each of the mixtures are reported in Tabie I.

The vepor pressures of pure ethylene and butane are also shown in Figure 4. Data for these two curves were selented from the literature. The references ore: ethylene $(14,25)$ and nomal butane $(1,8,11,14,20,23,25)$. In this figure, the critical locus is the envelope curve which terminates at the criticsl points of the two pure compounds and is tangent to each of the border curves as it passes through the respective eritieel point.

| TABLEI <br> OSITION AND CRITICAL CONSTANTS OF XTURES OF ETHYLENE AND n-BUTANE |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Composition |  | Critical Point |  |  | Maximum Pressure Point |  |  | Maximum Temperature Point |  |  |
| Mol \% Ethylene | 耻. \% Ethylene | Molecular $\qquad$ | $\begin{aligned} & \text { Temp. } \\ & \mathrm{o}_{\mathrm{F}} \mathrm{~F} \\ & \hline \end{aligned}$ | Press. psia | Density gms/cc | $\begin{gathered} \text { Temp. } \\ \mathrm{OF}_{\mathrm{F}} \end{gathered}$ | Press. -nsian | Density gms/cc | $\begin{gathered} \text { Temp. } \\ { }_{\mathrm{O}}^{\mathrm{F}} \end{gathered}$ | Press. psia | Density gms/ce |
| 0 | 0 | 58.12 | 306.0 | 550.1 | 0.225 |  |  |  |  |  |  |
| 19.85 | 10.68 | 52.15 | 266.51 | 752.8 | Q. 2564 | 262.95 | 756.7 | 0.2885 | 271.5 | 677 | 0.185 |
| 40.78 | 24.95 | 45.86 | 224.47 | 889.3 | 0.2617 | 214.4 | 909 | 0.3035 | 234.6 | 762 | 0.175 |
| 66.18 | 48.57 | 38.22 | 169.02 | 973.5 | 0.2541 | 170.01 | 973.5 | 0.2508 | 189.54 | 823 | 0.145 |
| 80.88 | 67.13 | 33.80 | 125.97 | 945.7 | 0.2429 | 132.5 | 951.5 | 0.2120 | 147.44 | 828 | 0.135 |
| 100 | 100 | 28.05 | 49.1 | 736.0 | 0. 220 |  |  |  |  |  |  |








## Caiculations sind Accuracy of the Reported Date

The possible errors involved in the reported data, and the accuracy of the various measurements are sumarized in the following discussion. Two sample calculations which shor the rethods of computing the anclysis of a mixture and the steps involved in converting the original data to the reported values of pressure, temperature and density are civen.

## Pressure

Ail prescures are reported as the absolute values. The two most important corrections to be made to the gage reading are the celibration of the diel and the correction for the atmospheric pressure. Only one other correction of any consequence was required. As the level of mercury in the piezoneter was frequently higher than the reservoir to which the gaces mere comected, the pressure in the tube was lower than the gage reatire by an amount ecuivalent to the head of mercury. Accordingly, this correction was elways made.

There were two other possible corrections to the gage resding. These were the effect of capillary depression and of the vepor pressure of mercury. The capillary depression of nercury hes been messured (30) and in tubes as large as those used in this study, the correction wes negligible. Also at all temperatures the vapor pressure of mercury was insignificant. The accuracy of the reported pressure reading is believed to be 0.5 percent at $200 \mathrm{lb} . / \mathrm{sc} . \mathrm{in}$. and to decrease Inearly to 0.1 percent at $1000 \mathrm{Ib} . / \mathrm{sg} . \mathrm{in}$.

## Temperature

The accuracy of the reported temperatures is believed to be $\pm 0.325^{\circ} \mathrm{F}$.

Composition

Considering the possible errors in ressuring the pressure and tempereture in mating up a indxume of gas, the anayose given is accurate withir 0.0005 mol fraction.

## Densities

The accursey of the reportec dengities depends upon the menitudeg of the errors in the weight and volume of the sample. A tabulation of the sources and possible megnitudes of errox and the effect upon the denstity follows:

## Wenet of the Garate

| Meesurement | Posstble Errosi( $\left.{ }^{( }\right)$ |
| :---: | :---: |
| Temperature | $0.05^{\circ} \mathrm{F}$ |
| Preseure | O.OE man IIg |
| Cathetoneter | 0.02 mal |
| Anclysia | 0.0005 |

Possible Totai
Erfect on Reault
$1 \times 10^{-\frac{4}{4}}$
$0.2 \times 10^{-4}$
$0.8 \times 10^{-4}$
$\frac{-}{1.22 \times 10^{-4}}$

## Volume Messurement

| Cathetometex |  |  |
| :---: | :---: | :---: |
|  | Maximum | $8.5 \times 10^{-4}$ |
|  | Mirimua | $0.2 \times 10^{-4}$ |
| Calibrestion | meximum | $2 \times 1004$ |
|  | Minimun | $0.6 \times 10^{-4}$ |
| Posaible Total | Paxigum | $8.5 \times 10^{-4}$ |
|  | Sinimurs | $0.86 \times 10^{-4}$ |

Since an error in either volume or veight is carried directiy to the density, the maximun possible error in the dersity is very nearly 0.1. percent. The Iragest source of errox Iies in the cathetometer readinge. The accurcey of this instrument for averace of severaj readings was teken es $\pm 0.01$ millineter. As the length of the piezometer occupied by the sample varied between is and 350 millimetere, it is obvious thet at hish dencities the accuracy will ke far less the st very low densities.

The calitration procecure involves the srme source of error. In view of the number of measurements mode in calizeting tise portion of the tube used at the kigher iencities and the snoothnese of the reching plot which showed the volumetric deviation fron a true crlinder, it is probekle that the scouracy of the calinration curve is bettor by one significant figure then the accuracy of the cathetometer reacirg. However, to he conservetive, it was arbitrarily assumed thot the error of the caliration wa: one-third of the possible error of the cathetometer reading. Densities are reportec to four sienificant figures. The sccuracy increases approximately liner riy from about 0.l percent at a density of 0.5 eram/ce to approximately 0.05 percent at a density of 0.01 Eram/cc. The semple calcuiation show the correction in the caljurated volume for therma expension of gless; a linea coefficient of $2.0 \times 10^{-6} /{ }^{\circ} \mathrm{F}$ has been reported (10) for Pyrex. As the measuring scale vas not a part of the heated system, the volumetric coefficient is only twice the above, or $4.0 \times 10^{-6}$.

$$
P V=Z M R T
$$

Assume $V=1$ inter
Then Weight per liter $=\frac{\mathrm{PM}}{\mathrm{ZRT}}=$ grans/Iiter
Where $\quad P=$ Pressure atmospheres
$M=$ Molecular weight
$T=A$ Asolute temperature ${ }^{\circ} \mathrm{K}$
$\mathrm{R}=\mathrm{A}$ constant - 0.0820 E Iiter atm. $/ \mathrm{O}_{\mathrm{K}} / \mathrm{Mol}$
Then Illustrating this by application to the first recorded unit volume of ethylene in the data belov:

$$
\text { grams } / 11 \text { ter }=\frac{769.38 \times 28.050}{760 \times 0.9940 \times 0.08206 \times 297.77}=2.1674
$$

| Component in Unit Volume | Pressure 1 Hm Hg | Temp. ${ }^{\circ} \mathrm{K}$ | 2 | Grame/Liter |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 297.77 | 0.9840 | 1.1674 |
| Ethyrlene | 769.32 889.08 | 297.91 | 0.9536 | 1.6576 |
| Ethylene | 829.02 |  |  | 2.4250 |
| Total |  |  |  |  |
| Butane | 754.50 | 298.00 | 0.9665 | 2.4416 2.4161 |
| Butene | 747.05 | 298.08 | 0.3668 0.9664 | 2.41857 |
| Butsne | $75 \% .85$ | 238.10 |  | 7.2934 |

Total.

Weight frection ethylene in mixture $=\frac{2.1250}{2.4550+7.2934}=0.2495$
Corresponding nol fraction
$=0.4078$

## CAMPLE CALCULATON

## DEWGTX OF BMCLE PHASE FLUSD IN THE

LIGH PILESTS TUSE

Composition of Mixture
Weight of Semple in High Precsure Tube
Tomperatiare
E.M.F. Mescureà

Corresponding Temperaturs
80.98 Hol ${ }^{[5}$ Ethylene 0.10439
3.780 volts $192.35{ }^{\circ} \mathrm{F}$
815.5 psi
12.2 psi 51.0 752.3 psi 14.4 psi 766.7 psi
Negligible corrections to Pressure
Vepor Brossarc. of hercur at $102.65^{\circ} \mathrm{F} \sim$
Cepillary Depression of Mercury
0.007 psi
0.02 pas

Volume Measurctante
Cethetoneter pendings
Feference Point

```
00.653 cm .
0.051
```

Top of meniscus
Dotlom of Menisous
Heiget of Meniscus
Volumen
Tolure in Tube to gutban of chabede
$0.102 \mathrm{~cm}^{3}$
Yess: $i) V_{0}$ wis of Starring Fod
0.00484
b) Vame of Penimeus
0.00045
net Volume of Tube at $70^{\circ} 5$
0.7 .7598

Themel Experision of Tabe
Coefficient $=4.0 \times 10^{-6} / \mathrm{F}$
Tomperature Dfference from retur $\left(70^{\circ}\right)=201.05^{\circ} \mathrm{F}$
Coryectec Volure at $193.65^{\circ} \mathrm{F}$
$\left(1+4.0 \times 10^{-6}\right)(1.1 .85)(0.17596)=0.17606 \mathrm{~cm}^{3}$
True Densiti of Somie $=\frac{0.01429}{0.37606}=0.001501$

## DTSCUSSION OF THE EXPERIMENTAL RESULTS

## Ilquid-Vapor Phase Ecuilionia

The general shape of the fhase diegrans, tinat is, the pressuretemperature plots shown Figure 4 is similar to those reported for other binkry mixtures of hydrocerbons, and the same increase of critical pressure over those of the pure components is noted. The effect of composition upon the critical constants and the points of maximum temperature and pressure which define the retrograce region are shown in Figures 11 ena 12. Upon comparison with the methane-butane system (24,27) and the ethenembutane system ${ }^{(15)}$ the eeneral relationehip of eritical properties is verified. That is, in general, the greater the difference between the normal volatilities or between the moleculax weights, the larger will be the range of retrograde condensation and the range of critical prescures. The following date mey bo cited:

## Ethane-Butane Ethylene-Butane Methane-Butene

Maximum Pressure

$$
\text { lu. } / \mathrm{sc} . \operatorname{in} .
$$

843
Maximum Range of Retrogrede Region ib. $/ \mathrm{sq}_{\mathrm{F}}$. in.

70
15

973

150
22

1800

900
75

The dote for the methane-butane system are not complete 3 they do not extend far into the methene rich region; the values given, then, mey not necessarily be exactly the maximum. It is interesting to note that each of the above respective maxime occurs at about the same concentration of ethylene as ethane.



The interpolated teraperatures, and densities at uniform intervals of pressure are listed in Tables II and III for the phase boundary curves and the locus of critical pointe, respectively.

## Vapor-I,iquid Equilibris

Another two dimensional representation of the three dimensional spaciel shape may be obtcined by cross plotting the boundary curces of Fifure 4 to show the vapor and liquic temperatures as a function of composition at a coustant pressure. Such curves, Figures 13 and 14, are also known as boiling point diagrams. These plots are extreacly usefill for interpolating between the experimentel concentrations so that equilibrium data may be obtained at any composition. Interpolated points from these curves are recorded in Table IV.

The curves in Figure 13 represent isobars up to the lowest critical pressure in the system, that of pure butene, while in Figure 14 all the curves are at pressures greater then the critical pressure of butene. The diagrans show the shrinkage of the area of co-eyisting liauid and vepor as the pressure is increased. Thet is, at pressures above the critical of one or both pure components, there are limiting compositions as mell as limiting temperatures at each isober. To illustrate, at $500 \mathrm{Ib} . / \mathrm{sq} . \mathrm{in}$. liquid and vapor may comexist at all concertrations of either component. At $800 \mathrm{It} . / \mathrm{sc}$. in. the composition of the phases must be between the limits of 24.8 and 95.7 mol percent ethylene. The trophsse racion vanishes at the point of maximum pressure, $973 \mathrm{l} . \mathrm{b} . / \mathrm{sq} .1 \mathrm{n}$.; the compasition at this point is approxinately 69 mol percent ethylene.




At pressures above the criticals of a pure component more points become svailable for establishing the curves. Those, which are show in Figure 8, represent the temperature, pressure and the composition at the criticals and the points of maximum temperature and pressure. The critical pressure of the mixtures, show as a function of composition in Figure 12, reaches a maximum value at an intermediate composition. Therefore, if the pressure of a two-phase system is greater than the critical pressures of either pure component, there must be for each isobar two critical temperatures and corresponding compositions.

Sinilarly, for each isobar there are two points at which the pressure is a maximum, each with its corresponding temperature and pressure. A third set may be derived from the other limit of retrograde condensation, the point of maximum temperature, but the pressure range does not extend as far as the two others. At pressures between the criticals of ethylene and butane, there is, of course, only one set of these three points for each isobar and it lies in the butane rich end of the boiling point curves.

In technical calculations which involve vapor-liquid equilibria, it is customary and convenient to express the $r$ lation between the composition of liquid and vapor in terms of the somalled equilibrium constant, $K=y / x$, in which $y$ and $x$ are the mol fractions of a component in vapor and in the liquid, respectively. The composition of vapor and liquid and the corresponding equilibrium constants for various isotherms are listed in Table $V$; the isothermal equilibrium constants are plotted as a function of pressure in Figure 15.

As is the case for other systems plotted in this manner, the equilibrium constant of the lighter component decreases continuously with increasing pressure to a value of unity at the critical pressure. As the
pressure is increased, the constant for heavier component decreases, passes through a minimun and converges with the constant of the lighter component at the critical pressure and unity.

The construction of these curves demonstrates the difficulty of obtaining, at low pressures, accurate equilibrium constants for the lighter component when it is present in low concentrations. For instance, at concentrations of ethylene less than, say 5 percent, the steep slope of the bubble point curve in Figure 13 can easily cause small errors in the interpolated compositions. Although the absolute value of the error is small, it becomes relatively large at low concentrations and may result in a considerable error in the equilibrium constant. This error of interpolation usually does not appear in the dew point composition as the slope of this curve is low. The relative magnitudes of the error of interpoletion and the concentration of butane are such that here the resulting inaccuracy is insignificant. As, in the ethylene rich region, the dew point line is steep and the bubble point line is relatively flat. A similar error is apt to appear in the equilibrium constant of butene. At higher pressures the curves are not so steep and, as mentioned above, there are additional points aveilable for establishing the curves.

When the concept of the equilibrium constant was proposed $(7,29)$, velues of the constants for hydrocarbons were reported and have been widely used. These constants were besed upon fugacities computed from deviations from ideal gas laws and the assumption of ideal solutions. The composition of the solution is, therefore, not $s$ variable. As the fugacities were computed from a. generalized P-V-T plot derived from ethylene, a comparison between the ideal and the experimental equilibrium constants in the binary

mixture will indicate the extent to which this binary system deviates from ideality. In the following tabulation, some values of the constants ${ }^{(28)}$ computed from fugacities are compared with the experimental constents as listed in Table $V$. The constants cited from the Iiterature are ideal below the critical pressures; at higher pressures a correction is included to allow for the phenomenon of convergence.

## Vapor-Liquid Equilibrium Constents of Ethylene

| Pressure | $120^{\circ} \mathrm{F}$ |  | $160^{\circ} \mathrm{F}$ |  | $200^{\circ} \mathrm{F}$ |  | $240^{\circ} \mathrm{F}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 300 lb ./sq.in. | 4.0 | 3.32 | 5.40 | 4.2 | 6.15 | 5.3 | 6.40 | 6.55 |
| 500 (s. | 2.18 | 2.10 | 2.83 | 2.68 | 3.40 | 3.3 | 3.48 | 4.05 |
| 700 | 1.56 | 1.61 | 1.956 | 2.0 | 2.135 | 2.5 | 1.89 | 3.05 |
| 800 | 1.315 | 1.47 | 1.615 | 1.82 | 1.79 | 2.2 | 1.38 | 2.7 |

Vapor-ILquia Equilibrium Constants for Butane

| Pressure | Exptil. Idegl | Exptil. Ideal | Exptil. IdenI | Exptil. Ideal |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $300 \mathrm{Ib} . / \mathrm{sc}$. in. | 0.307 | 0.355 | 0.47 | 0.54 | 0.742 | 0.74 | 0.994 | 0.97 |
| 500 | 0.275 | 0.3 | 0.372 | 0.44 | 0.560 | 0.61 | 0.782 | 0.76 |
| 700 | 0.301 | 0.325 | 0.389 | 0.45 | 0.547 | 0.60 | 0.734 | 0.73 |
| 800 | 0.380 | 0.34 | 0.442 | 0.45 | 0.599 | 0.60 | 0.865 | 0.71 |

The agreement between the ideal and experimental constants is not good except in a few short sections of the curves. In general, the idesl constants for the lighter component are too high at pressures greater than 500 Ib./su.in. and the deviation increases with increasing temperature or pressure. In other mords, the discrepancy of the ideal constants is grestest in the critical region. The differences, of course, are the result of departure of ethylenembutane mixtures from ideal solutions in the trom phese region. That is, assumptions such as no heat of mixing and additivity of volumes must be invalid in this case.

Except for the highest isotherm, the minimum points of the experimental butane constants are appreciably lower than those of the ideal constants. The ideal constants again fail to show the temperatures or pressures at the criticel or convergence points.

Another way in which the behavior of a compound may be shown is through comparison with the properties of adjacent hydrocarbons. The vapor-liquid equilibria of methane, of ethane and of heptane in butane heve been reportad in the literature $(19,21,24,27)$. Because of the differences in the temperature ranges of the two-phase systems, only the equilibrium constants of the light hydrocarbons in butane can be compared. In figures 16 and 17 the equilibrium constants of methane, ethylene and ethane are plotted at $160^{\circ} \mathrm{F}$ and $190^{\circ} \mathrm{F}$. In order to show the volatility of ethylene relstive to the paraffins, the equilibrium constants at constant pressure and temperature are plotted in Figure 18 against the temperatures of the boiling points at atmospheric pressurs. Upon this basis, the equilibrium constant, or volatility of etiaylene in butane, is as much as $40 \%$ greater than would have been predicted by this approximation.

## Densities of Hydrocarbon Mixtures

The densities of the saturated liquid and vapor for the four mixtures and the two pure compounds are show, in relation to the temperature, by Figure 5. As was reported for the ethane-heptane and the ethanebutane systems $(18,19)$ there is a point of inflection in the density curve at the critical density. Further, this point of inflection becomes more pronounced with increasing ethylene concentrations. A second point of



inflection at a lower density was found in the other two systems, but this point is not easily discernible in the phase diagrams of the ethylene-butane mixturez. The density curves show some irregularity at lower concentrations of elther component, this indicates, perhaps, the deviation from ideality is greatest in these regions.

In addition to the denstites at the phase boudaries, the pres-sure-wolune-tempersture relationships wera determined in the single phase region. The experinental data are reported in Tables VIII and IX. The former table covers densities of superheated vapor, wile in the latter, the reported densities refer to the liquid and the fluid in the vicinity of the critical points. The densities which were deternined isothernally, and are show in Figures 6-10, were put in a more usable or cuatomary form by cross plotting to show the density as a fuction of temperature for several uniformly spaced isobars in Figures 19 - 22.

The method of predicting or correlating densities of gaseous hydrocarbons by the law of corresponding states has been well developed and is highly succeasful $(7,9,22)$. As is now well known, according to the theorem of corresponding states, the compressibility factors, PV/NRT, of the pure hydrocarbons are approximately equal at identical values of reduced pressure and reduced temperature. Thase terms which nust be taken in consistent units are identified as:
p - Pressure
T - Tempsrature
$y$ - Volue
N - Number of mols considered
R - Gas law constant

The reduced pressure and tempersture are, of course, the ratio of the existing terpersture or pressure to the respective criticel velues.

It hes been show that the compessibility factors of mixtures of hydrocarbons can be correlated with thase of the pure compounds on a reduced basis in mhich a hypotheticel point, termed the pseudo-eritical, is used rether than the true critical point (17). It has been further shown that for mixtures of light hydrocarbons, the ccordinates of the pseudomeritical point may be taken as the molal average of the critical pressures and temperatures of the individual components.

To test the validity of this procedure with mixtures of ethylene and kutane, the compressibility factors were computed from the experimental dete, are given in Table VI and are platted on a reduced or pseudomeduced basis in Figure 23.

The densities of ethylene reported in the literature ${ }^{(1,12)}$ nere used as the basis of the work referred to above ${ }^{(7,9,22)}$ on the generalized properties of hydrocarbons, and is also used as the basis of Figure 23.

The compressibility factors for ethylene are shown in this figure as the solid line as a function of pressure for two reduced temperatures. The compressibility factors of butane and the four mixtures are shown as points for the seme reduced or pseudo-reduced temperatures. The critical or pseudo-critical constants and the temperatures corresponding to the reduced or pseudo-reduced temperatures ere given in Table VI. In making the greph, the compressibility factors were computed st pressures in multiples of $1001 \mathrm{k} . / \mathrm{sg} . \mathrm{in}$. abs.

It is not possible to use a wider range of pseudo-reduced temperatwes and show the datic for all four mixtures, for if the pseudo-reduced temperature of 1.10 is reduced by as littie as $1 \%$, it will lie within the two-phase region of the etnylene rich minture, and if incressed aver 1.20, it will fall outside the experimental mange of temperature for the butane rich mixture.

FIGURE 20
OTE MIXTURE CONTAINING 40.78 MOL PERCEST
ETHYLDE IX n-BUTNE


FIGORE 22
DKENSITY OF A MITTURE COATAIMIRG 80.88 MOL PERCEIG ETHYLENE IN n-BUTANS

However, the data do demonstrate that deviations from the theorem of corresponding states tend to increase as the two-zhase region is epproached. A visuel inspection of Figure 23 readily proves this. At the higher pseudowreduced tempersture the avergge deviation from the line which represents the compressibility factor of athylene is about one percent. The similar deviation at the lower pseudo-reduced temperature, which is nearer the liquid region, is almost three precent. Further, the largest such deviation noted, about sight percent, oceurs in the rixture richest in ethylene at $8001 b . / \mathrm{sq} . \ln .0 \mathrm{bs}$. and $254.7^{\circ} \mathrm{F}$. At this pressure the temperature is but $8^{0} \mathrm{~F}$ higher than the dew point. However, for the same mixture at the same pressure the deviation falls to less then one-half of one percent at $210.3^{\circ} \mathrm{F}$ wich is abouto $65^{\circ} \mathrm{F}$ above the dew point.

It is also to be noted that these deviations, relative to pure othylene, from the theorem of corresponding state increase with increasing pressure. This is part of the same effect, namely, that the discrepancies tend to occur near the phase boundaries.

In general, the data show that on a pseudo-reduced basis mixtures of this tope conforin to the the rem of corresponding states as well as do the two pure hydrocarbons except when near the liquid region.



CONCLUSIOX

Four mixtures, uniformly distributed in the composition range, were prepared. The pressures, temperetures and densities at the liquidvapor phase boundary were determined experimentally for each of these mixtures in addition to similer measurements in the single phase region. These data, taken with those reputed for pure ethylene and butane, enable the construction of diagrems which show the properties, such as the composition of coexisting liquid and vapor as functions of pressure and temperature throughout the entire composition range. Graphs, presented in this dissertation, show the volatility of ethylene in butane in comparison with reported data for methane and ethane in the same solvent. The experimental data, pressuremolumetemperatire relationships at the phase boundary and in the single phase region, are also shown graphically for each of the mixtures studied. The densities of the gaseous mixtures are showr to obey the theorem of corresponding states, but that slight deviations accur near the two-phase boundary.

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## APPENDIX



$\begin{array}{cc}80.38 \text { Mol \％Ethylene } \\ \text { Density } \\ \text { Rems／cc } & \text { Temp．} \\ \text { OF }\end{array}$



SUMMARY OF PRESSURE, TEMPERATURE AND DENSITY DATA
AT PHASE BOUNDARIES FOR THE ETHYLENE - -BUTANE SYSTEM

.00802
.01095
.0142
.0174
.02045
.0239
.0278
.03185
.0356
.0408
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58
5 88
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.0097
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.0219 \begin{tabular}{l}
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## TABLEIII

CRITICAL PROPERTIES OF ETHYLENE—R BUTANE MIXTURES

| Critical Pressure psia | Critical <br> Composition Mol \% Ethylene | $\begin{gathered} \text { Critical } \\ \text { Temperature } \\ \mathrm{O}_{\mathrm{F}} \end{gathered}$ | Critical Density gms/cc |
| :---: | :---: | :---: | :---: |
| 550.1 | 0 | 306.0 | 0.228 |
| 575 | 2.0 | 301.7 | 0.283 |
| 600 | 4.0 | 297.5 | 0.237 |
| 625 | 6.2 | 293.2 | 0.240 |
| 650 | 8.5 | 288.7 | 0.243 |
| 675 | 10.7 | 284.1 | 0.247 |
| 700 | 13.3 | 279.0 | 0.250 |
| 725 | 16.1 | 273.4 | 0.253 |
| 750 | 19.2 | 267.2 | 0.256 |
| 775 | 22.5 | 260.4 | 0.258 |
| 800 | 26.2 | 255.0 | 0.260 |
| 825 | 30.0 | 245.4 | 0.261 |
| 850 | 34.2 | 237.6 | 0.262 |
| 875 | 38.2 | 229.4 | 0.262 |
| 900 | 42.6 | 220.5 | 0.262 |
| 925 | 47.8 | 210.2 | 0.261 |
| 950 | 54.4 | 196.4 | 0.259 |
| 965 | 59.9 | 184.2 | 0.257 |
| 973.5 | 65.8 | 171 | 0.255 |
| 965 | 59.8 | 145.0 | 0.248 |
| 950 | 79.9 | 128.9 | 0.244 |
| 925 | 84.0 | 114.6 | 0.239 |
| 900 | 86.9 | 105.9 | 0.236 |
| 875 | 89.4 | 94.3 | 0.2315 |
| 850 | 91.6 | 85.6 | 0.227 |
| 825 | 93.5 | 77.2 | 0.223 |
| 800 | 95.3 | 69.3 | 0.219 |
| 775 | . 97.2 | 61.3 | 0.216 |
| 750 | 98.9 | 53.6 | 0.212 |
| 756 | 100 | 49.1 | 0.210 |

TABLEIV

## ETHYLFNE=R—BUTANE SYSTEM

Temperature - Composition Curves At Constant Pressures

| Mol \% <br> Ethylene | 100 psia |  | 200 psia |  | 300 peia |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Liquid | Vapor | Liquid | Vapor | Liquid | Vapor |
|  | Temp. ${ }^{\circ} \mathrm{F}$ | Temper | Temp. ${ }^{\text {P }}$ | Temp. ${ }^{\circ}$ | Temp. ${ }^{\circ} \mathrm{F}$ | Tempe ${ }^{\text {P }}$ |
| 0 | 146.0 | 146.0 | 202.7 | 202.7 | 241.2 | 241.2 |
| 5 | 101.5 | 140.3 | 151.7 | 194.2 | 196.6 | 232.6 |
| 10 | 70.0 | 134.2 | 118.2 | 186.7 | 164.4 | 224.5 |
| 15 | 47.0 | 128.4 | 94.8 | 179.9 | 137.1 | 217.0 |
| 20 | 29.5 | 122.6 | 75.2 | 173.8 | 115.3 | 209.9 |
| 30 | 7.0 | 112.1 | 46.8 | 163.6 | 86.2 | 197.8 |
| 40 | - 9.0 | 102. 8 | 26.7 | 154.0 | 65.8 | 185.7 |
| 50 | -21.5 | 94.1 | 10.6 | 145.9 | 48. ${ }^{\text {a }}$ | 172.1 |
| 60 | -34.0 | 84.7 | -2.9 | 130.1 | 32.8 | 156.2 |
| 70 | -45.5 | 70.0 | -14.5 | 109.8 | 18.7 | 134.6 |
| 80 | -57.5 | 43.5 | -25.0 | 78.4 | 5.9 | 102.4 |
| 85 | -63.5 | 24.2 | -29.7 | 57.5 | - 0.1 | 80.6 |
| 90 | -69.0 | -1.5 | -34.5 | 32.1 | -6.0 | 55.E |
| 95 | -75.5 | -35.5 | -38.5 | - 0.3 | -11.7 | 24.4 |
| 100 | -80.4 | -80.4 | -42.8 | -42.8 | -17.1 | -17.1 |


| $\begin{gathered} \text { Mol \% } \\ \text { Ethylene } \end{gathered}$ | 400 psia |  | 500 psia |  | 550.1 psia |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Liquid | Vapor | $\begin{aligned} & \text { Liquid } \\ & \text { Temn. } 0_{F} \end{aligned}$ | Vapor Tempor | $\begin{aligned} & \text { Liquia } \\ & \text { Temp. } \end{aligned}$ | $\begin{aligned} & \text { Vapor } \\ & \text { Temp. } \mathrm{OF} \end{aligned}$ |
|  |  |  |  |  |  |  |
| 0 | 270.9 | 270.9 | 295.0 | 295.0 | 306.0 | 306.0 |
| 5 | 233.6 | 261.S | 259.5 | 285.0 | 273.2 | 294.9 |
| 10 | 201.3 | 253.8 | 228.6 | 275.0 | 242.8 | 284.0 |
| 15 | 175.4 | 244.0 | 202.4 | 264.9 | 216.3 | 275.8 |
| 20 | 152.4 | 235.7 | 180.2 | 254.9 | 193.6 | 262.8 |
| 30 | 117.6 | 220.1 | 143.4 | 236.8 | 156.3 | 243.1 |
| 40 | 91.2 | 205.2 | 115.3 | 220.0 | 126.4 | 224.7 |
| 50 | 70.3 | 190.4 | 92.9 | 203.9 | 102.8 | 208.1 |
| 60 | 53.4 | 174.3 | 75.8 | 187.8 | 83.4 | 192.8 |
| 70 | 58.7 | 152.6 | 57.8 | 166.3 | 66.8 | 171.4 |
| 80 | 25.8 | 119.9 | 43.5 | 132.4 | 52.4 | 137.2 |
| 85 | 19.7 | 97.2 | 37.e | 110.5 | 45.3 | 124.9 |
| 90 | 13.6 | 70.2 | 30.8 | 84.3 | 39.0 | 89.1 |
| 95 | 7.5 | 37.5 | 24.5 | 53.1 | 32.3 | 59.0 |
| 100 | 2.5 | 2.5 | 18.6 | 18.6 | 25.7 | 25.7 |

## TABLEIV <br> (Continued) <br> ETHYLENE-n-BUTANE SYSTEM

Temperature - Composition Curves At Gonatant Pressures

| Mol \% Ethylene | 600 psia <br> Liquid <br> Temp. ${ }^{\circ}{ }^{\mathrm{F}}$ | Vapor <br> Temp. ${ }^{\circ} \mathrm{F}$ | Mol \% Ethylene | 700 psia Liquid Temp. ${ }^{\circ} \mathrm{F}$ | $\begin{gathered} \text { Vapor } \\ \text { Temp. }{ }^{\text {Fer }} \end{gathered}$ | Mol \% <br> Ethylene | 800 psia <br> Liquid <br> Temp. ${ }^{\circ} \mathrm{F}$ | $\begin{gathered} \text { Vapor } \\ \text { Temp. }{ }^{\circ} \mathrm{F} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a) 4.0 | 297.5 | 297.5 | a) 13.3 | 279.0 |  | a) 26.2 | 253.0 | 253.0 |
| b) 3.6 | 297.7 |  | b) 13.3 | 276.8 |  | b) 24.7 | 242.5 |  |
| - 5 | 286.8 | 297.7 | 15 | 264.0 | 279.2 | 80 | 219.7 | 248.1 |
| 10 | 257.? | 288.0 | 20 | 237.4 | 272.4 | 40 | 179.8 | 234.9 |
| 20 | 208.1 | 268.3 | 30 | 192.6 | 252.3 | 50 | 154.1 | 220.7 |
| 30 | 168.3 | 247.8 | 40 | 157.1 | 234.9 | 60 | 132.8 | 202.3 |
| 40 | 136.9 | 229.2 | 50 | 132.2 | 218.8 | 70 | 113.2 | 180.0 |
| 50 | 112.2 | 213.1 | 60 | 112.2 | 200.7 | 80 | 95.3 | 149.4 |
| 60 | 92.3 | 197.? | 70 | 95.1 | 179.0 | 90 | 78.1 | 105.8 |
| 70 | 75.1 | 175.3 | 80 | 78.9 | 146.9 | 95 | 69.3 | 7'5. 2 |
| 80 | 61.5 | 141.8 | 90 | 62.5 | 103.3 | a) 95.3 | 69.3 | 69.5 |
| 90 | 46.9 | 94.7 | 100 | 44.8 | 44.8 | b) 96.0 |  | 69.3 |
| 95 | 39.6 | 65.5 |  |  |  |  |  |  |
| 100 | 32.3 | 32.5 |  |  |  |  |  |  |


| Mol \% Ethylene | 00 psia <br> Liquid Temp. ${ }^{\circ} \mathrm{F}$ | $\begin{gathered} \text { Vapor } \\ \text { Temp. }{ }^{9} \mathrm{~F} \end{gathered}$ | Mol \% Ethylene | 950 psia <br> Liquid Temp. ${ }^{\circ} \mathrm{F}$ | $\begin{aligned} & \text { Vapor } \\ & \text { Tempe }{ }_{F} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| a) 42.6 | 220.5 | 220.5 | a) 54.4 | 196.4 | 196.4 |
| b) 39.2 | 218.5 |  | b) 51.2 | 196.8 |  |
| - 40 | 208.7 | 221.7 | 55 | 182.5 | 196.5 |
| 50 | 179.8 | 213.8 | 60 | 171.0 | 194.0 |
| 60 | 155.1 | 200.1 | 70 | 146.5 | 175.0 |
| 70 | 183.0 | 179.3 | 80 | 138.6 | 139.0 |
| 80 | 11.3 .8 | 148.? | a) 79.9 | 128.9 | 128.9 |
| 85 | 105.9 | 102.9 | b) 81.2 |  | 131.5 |
| a) 86.9 | 103.9 | 103.9 |  |  |  |
| b) 87.8 |  | 107.6 |  |  |  |

a) Critical Point
b) Temperature and Pressure at Point of Maximum Pressure

## ETHYLENE-n-BUTANE SXSTEM

Vapor-Liquid Compositions and Equilibrium
Constants at Constant Temperatures

|  | $\begin{gathered} \text { Presbure } \\ \text { psi } \end{gathered}$ | Mol \% Ethylene |  | Vapor-Liquid Equilibrium Constant |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | In Licuid | In Vapor | Ethrlene | n-Butane |
| $120^{\circ} \mathrm{F}$ | 740.8 | 0 | 0 | - | - |
|  | 200 | 10.8 | 65.7 | 6.8 | 0.38 |
|  | 300 | 18.7 | 75.0 | 4.0 | 0.307 |
|  | 400 | 28.7 | 80.0 | 2.8 | 0.28 |
|  | 500 | 58.2 | 83.0 | 2.18 | 0.275 |
|  | 600 | 46.6 | 85.1 | 1.82 | 0.280 |
|  | 700 | 55.8 | 86.6 | 1.56 | 0.304 |
|  | 800 | 66.3 | 87.2 | 1.315 | 0.580 |
|  | 900 | 76.6 | 85.5 | 1.1 .15 | 0.618 |
|  | 936 | 82.5 | 82.5 | 1 | 1 |
| $160^{\circ} \mathrm{F}$ | \$40120 | 0 | 0 | - | $1$ |
|  | $200$ | $3.7$ | 33.7 | 9.05 | $0.0 .63$ |
|  | 500 | 10.7 | 57.8 | 5.40 | 0.48 |
|  | 400 | 18.2 | 67.0 | 5.66 | 0.402 |
|  | 500 | 25.2 | 72.2 | 2.83 | 0.872 |
|  | 600 | 32.5 | 75.1 | 2.E4 | 0.569 |
|  | 700 | 39.1 | 76.8 | 1.956 | 0.589 |
|  | 800 | 47.5 | 76.8 | 1.615 | 0.442 |
|  | 900 | 57.9 | 76.8 | 1.828 | 0.556 |
|  | 950 | 64.4 | 74.4 | 1.15 | 0.719 |
|  | 972 | 64.7 | 64.7 | 1 | 1 |
| ; |  |  |  |  |  |
| $200^{\circ} \mathrm{F}$ | 194 | 0 | 0 | - | 1 |
|  | 200 | 0.15 | 1.45 | 11 | 0.988 |
|  | 800 | 4.6 | 28.2 | 6.15 | 0.742 |
|  | 400 | 10.2 | 45.6 | 4.28 | 0.628 |
|  | 500 | 15.5 | 52.7 | 5.40 | 0.560 |
|  | 600 | 21.8 | 58.4 | 2.68 | 0.532 |
|  | 700 | 28.8 | 60.5 | 2.135 | 0.547 |
|  | 800 | 34.2 | 61.3 | 1.79 | 0.588 |
|  | 900 | 42.4 | 60.0 | 1.415 | 0.694 |
|  | 944 | 52.7 | 52.7 | 1 | 1 |
| $240^{\circ} \mathrm{F}$ | 296 | 0 | 0 | 6.5 | 1 |
|  | 300 | 0.1 | 0.65 | 6.40 | 0.994 |
|  | 400 | 3.8 | 17.4 | 4.59 | 0.860 |
|  | 500 | 8.1 | 28.2 | 3.48 | 0.782 |
|  | 600 | 13.2 | 34.1 | 2.48 | 0.759 |
|  | 700 | 19.5 | 36.9 | 1.89 | 0.784 |
|  | 800 | 26.2 | $36 . E$ | 1.38 | 0.865 |
|  | 842 | 82.8 | 32.8 | 1 | 1 |

TABLEVI

|  | 0 Mol \% Ethylene |  |  |  | 19.85 Mol \% Ethylene |  |  |  | 40.78 Mol \% Ethylene |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Press. psia | Reduc. <br> Press. | Density Ideal | gms/cc <br> Actual | 2 | PseudoReduc. Press. | $\begin{aligned} & \text { Density } \\ & \text { Ideal } \end{aligned}$ | mms/cc Actual | Z | PseuxdoReduc. Press. | Density Ideal | gras/ec Actual | 2 |
|  |  |  |  |  |  | - $\mathbf{T r}=$ | $1.10-$ |  |  |  |  |  |
| 100 | 0.182 | 0.0105 | 0.0108 | 0.952 | 0.170 | 0.00991 | 0.0104 | 0.952 | 0.160 | 0.0094 | 0.0098 | 0.957 |
| 200 | 0.364 | 0.0208 | 0.0229 | 0.899 | 0.340 | 0.0198 | 0.0220 | 0.900 | 0.520 | 0.0188 | 0.0204 | 0.922 |
| 300 | 0.546 | 0.0509 | 0.0361 | 0.855 | 0.510 | 0.0297 | 0.0348 | 0.854 | 0.480 | 0.0282 | 0.0330 | 0.855 |
| 400 | 0.728 | 0.0412 | 0.0520 | 0.793 | 0.680 | 0.0596 | 0.0485 | 0.801 | 0.640 | 0.0578 | 0.0468 | 0.805 |
| 500 | 0.910 | 0.0515 | 0.070 | 0.735 | 0.850 | 0.0495 | 0.0675 | 0.753 | 0.800 | 0.0470 | 0.063 | 0.746 |
| 600 | 1.092 | 0.0618 | 0.092 | 0.671 | 1.020 | 0.0594 | 0.0880 | 0.674 | 0.960 | 0.0564 | 0.079 | 0.713 |
| 700 | 1.274 | 0.0721 |  |  | 1.190 | 0.0694 | 0.117 | 0.592 | 1.120 | 0.0658 | 0.100 | 0.658 |
| 800 | 1.456 | 0.0824 | 0.161 | 0.512 | 1.560 | 0.0798 | 0.151 | 0.525 | 1.280 | 0.0752 | 0.126 | 0.596 |
| 900 | 1.638 | 0.0927 |  |  | 1.530 | 0.0892 | 0.196 | 0.455 | 1.440 | 0.0846 | 0.1598 | 0.529 |
| 1000 | 1.820 | 0.103 | 0.253 | 0.406 | 1.700 | 0.0991 | 0.235 | 0.426 | 1.600 | 0.0940 |  |  |
|  |  |  |  |  |  | - $\mathbf{T r}=$ | $1.20-$ |  |  |  |  |  |
| 100 | 0.182 | 0.00936 | 0.0098 | 0.966 | 0.170 | 0.00909 | 0.00946 | 0.960 | 0.160 | 0.00875 | 0.00901 | 0.971 |
| 200 | 0.364 | 0.0187 | 0.0203 | 0.920 | 0.540 | 0.01818 | 0.0196 | 0.927 | 0.320 | 0.0175 | 0.0187 | 0.936 |
| 500 | 0.546 | 0.0281 | 0.0518 | 0.880 | 0.510 | 0.02727 | 0.0303 | 0.901 | 0.480 | 0.02625 | 0.0288 | 0.912 |
| 400 | 0.728 | 0.0574 | 0.0440 | 0.85 | 0.680 | 0.03636 | 0.0425 | 0.355 | 0.640 | 0.0350 | 0.0598 | 0.380 |
| 500 | 0.910 | 0.0468 | 0.0580 | 0.807 | 0.850 | 0.04545 | 0.0554 | 0.820 | 0.800 | 0.0458 | 0.0515 | 0.852 |
| 600 | 1.092 | 0.0561 | 0.073 | 0.768 | 1.020 | 0.05454 | 0.0714 | 0.755 | 0.960 | 0.0525 | 0.0646 | 0.812 |
| 700 | 1.274 | 0.0655 |  |  | 1.190 | 0.08363 | 0.0866 | 0.735 | 1.120 | 0.06125 | 0.0791 | 0.775 |
| 800 | 1.456 | 0.0749 | 0.108 | 0.693 | 1.560 | 0.07272 | 0.104 | 0.698 | 1.230 | 0.0700 | 0.0952 | 0.735 |
| 900 | 1.638 | 0.0942 |  |  | 1.550 | 0.08181 | 0.124 | 0.657 | 1.440 | 0.07875 | 0.113 | 0.697 |
| 1000 | 1.820 | 0.0935 | 0.251 | 0.619 | 1.70 | 0.0909 | 0.147 | 0.619 | 1.600 | 0.0875 | 0.133 | 0.656 |


| Press. |
| ---: |
| psia |
|  |
|  |
| 100 |
| 200 |
| 300 |
| 400 |
| 500 |
| 600 |
| 700 |
| 800 |
| 900 |
| 1000 |


-
$0.00870 \quad 0.00905$


0.975
0.942
0.919
0.890
0.855
0.814
0.780
0.758
0.721
0.685







욱 88888888888

## TABLEVI

PSEUDO-CRITICAL CONSTANTS

| Mol \% | PseudoCritical Pressure | $\begin{aligned} & \text { Pseudo- } \\ & \text { Critical } \\ & \text { Temp. } \end{aligned}$ | Tempe | ure at |
| :---: | :---: | :---: | :---: | :---: |
| Ethylene | psia | $\mathrm{OF}^{\mathrm{F}}$ | $T x=1.10$ | $T \mathrm{~T}=1.30$ |
| 0 | 550.1 | 506.0 | 582.6 | 459.2 |
| 19.85 | 587 | 255.4 | 326.5 | 398.1 |
| 40.78 | 625 | 201.7 | 268.2 | 334.4 |
| 66.18 | 673 | 136.z | 196.4 | 256.0 |
| 80.88 | 700 | 98.6 | 154.7 | 210.5 |
| 100 | 756 | 49.1 | 100.0 | 150.9 |

TABLTEVITI

Actual Measurements of Pressures, Temperatures and Densities at the Phase Boundaries
$19.35 \mathrm{Mol} \%$ Ethylene

| $\begin{gathered} \text { Pressure } \\ \text { psia } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Tamp. } \\ & 0_{\mathrm{F}} \\ & \hline \end{aligned}$ | Density <br> ems/cc | Pressure $\qquad$ | $\begin{gathered} \text { Temp. } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Density } \\ & \text { ems/cc } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 57.1 | 85.22 | 0.00882 | 755.5 | 265.12 | 0.2707 |
| 81.5 | 108.74 | 0.01185 | 756.1 | 264. 24 | 0.2752 |
| 87.3 | 113.70 | 0.01251 | 756.5 | 262.79 | 0.2881 |
| 124.2 | 138.57 | 0.01726 | 754.6 | 261.31 | 0.2994 |
| 163.5 | 158.62 | 0.02231 | 754.3 | 262.06 | 0.2940 |
| 221.0 | 182.65 | 0.03079 | 754.0 | 260.02 |  |
| 223.3 | 184.07 | 0.03137 | 753.5 | 260.04 | 0.3056 |
| 249.5 | 193.20 | 0.03526 | 748.5 | 258.24 | 0.3148 |
| 274.1 | 201.73 | 0.04003 | 751.4 | 257.20 | 0.3207 |
| 279.2 | 202.94 |  | 742.2 | 254.28 | 0.3339 |
| 282.5 | 202.90 |  | 741.5 | 253.42 | 0.3392 |
| 282.7 | 204.79 | 0.04243 | 741.4 | 251.02 | 0.3504 |
| 318.1 | 215.55 | 0.04936 | 738.5 | 250.25 | 0.3477 |
| 363.2 | 230.63 | 0.06142 | 720.1 | 244.22 | 0.3632 |
| 398.5 | 235.34 | 0.06603 | 701.8 | 240.26 | 0.3713 |
| 450.7 | 246.21 | 0.07795 | 690.7 | 235.68 | 0.3785 |
| 510.2 | 257.20 | 0.09442 | 658.3 | 226.62 | 0.3937 |
| 557.6 | 264.33 | 0.1102 | 635.1 | 219.27 | 0.4047 |
| 627.3 | 270.55 | 0.1437 | 609.2 | 212.04 | 0.4154 |
| 657.0 | 271.95 | 0.1619 | 578.8 | 202.53 | 0.4278 |
| 680.2 | 272.54 | 0.1782 | 545.0 | 192.78 | 0.4392 |
| 703.5 | 272.47 | 0.1905 | 518.1 | 183.71 | 0.4490 |
| 716.3 | 272.10 | 0.1967 | 513.2 | 183.07 | 0.4586 |
| 725.2 | 271.26 | 0.2120 | 505.3 | 182.35 | 0.4587 |
| 730.5 | 270.63 | 0.2168 | 412.7 | 159.17 | 0.4712 |
| 735.5 | 270.01 | 0.2258 | 416.2 | 159.32 |  |
| 740 | 269.23 | 0.2328 | 414.3 | 157.05 |  |
| 744 | 268.61 | 0.2392 | 381.4 | 146.54 | 0.4816 |
| 748.5 | 267.59 | 0.2477 | 338.7 | 131.25 | 0.4947 |
| 751.9 | 267.02 | 0.2529 | 340.9 | 131.18 |  |
| *752.8 | 266.51 | 0.2564 | 316.2 | 119.53 | 0.5046 |
| 752.6 | 266.52 | 0.2572 | 281.0 | 108.67 | 0.5132 |
| 754.5 | 266.03 | 0.2505 | 220.9 | 84.80 | 0.5301 |

> T A B L E VII
> (Continued)
> ETHYLENE $n=$ BUTANE SYSTMM

Actual Measurements of Pressures, Temperatures and Densities at the Phase Boundaries
40.78 Mol \% Ethylene

| $\begin{gathered} \text { Pressure } \\ \text { psia } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Temp. } \\ & \mathbf{o}_{\mathbf{F}} \\ & \hline \end{aligned}$ | Density gens/ce | Pressure $\qquad$ | $\begin{gathered} \text { Temp. } \\ \mathrm{O}_{\mathrm{F}} \\ \hline \end{gathered}$ | Density pms/cc |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 63.4 | 76.21 | 0.00885 | 885.2 | 225.72 | 0.2558 |
| 108.5 | 107.61 | 0.01352 | 887.2 | 225.08 | 0.2597 |
| 110.3 | 114.52 | 0.01491 | * 889.3 | 224.47 | 0.2617 |
| 144.9 | 129.05 | 0.01814 | 884.? | 222.57 |  |
| 154.1 | 130.22 | 0.01856 | 897.7 | 221.23 |  |
| 197.3 | 152.10 | 0.02487 | 881.9 | 226.39 |  |
| 217.3 | 159.67 | 0.02760 | 888.7 | 224. 57 | 0.2675 |
| 278.2 | 178.74 | 0.05602 | 891.1 | 223.49 | 0.2667 |
| 355.0 | 194.23 | 0.04490 | 895.3 | 221.72 | 0.2763 |
| 347.2 | 194.55 | 0.34507 | 896.5 | 220.78 | 0.2758 |
| 557.6 | 196.76 | 0.04680 | 898.7 | 220.71 | 0.2776 |
| 361.2 | 197.51 |  | 900.3 | 219.74 | 0.2849 |
| 366.2 | 197.41 |  | 906.2 | 218.52 | 0.2892 |
| 393.1 | 203. 19 | 0.05213 | 907.5 | 217.01 | 0.2348 |
| 396.5 | 202.27 |  | 906.8 | 215.69 | 0.3009 |
| 431.1 | 209.48 | 0.05827 | 908.4 | 214.58 | 0.3042 |
| 522.3 | 220.92 | 0.07491 | 909.5 | 212.24 | 0.3121 |
| 540.5 | 223.17 | 0.07945 | 907.5 | 210.51 | 0.3178 |
| 609.6 | 228.7 |  | 905.5 | 208.50 | 0.3243 |
| 601.2 | 228.72 | 0.09556 | 890.2 | 203.75 | 0.3345 |
| 633.8 | 230.41 | 0.1056 | 893.1 | 202.19 | 0.3426 |
| 683.5 | 233.04 | 0.1278 | 878.5 | 196.82 | 0.3567 |
| 699.1 | 233.27 | 0.1364 | 870.7 | 194.75 |  |
| 704.5 | 234.02 | 0.1408 | 856.2 | 190.62 | 0.3705 |
| 726.0 | 234.66 | 0.1551 | 825.1 | 182.21 | 0.3869 |
| 792.8 | 233.38 |  | 810.1 | 173.78 |  |
| 789.9 | 234.09 | 0.1982 | 783.8 | 172.92 | 0.4016 |
| 683.1 | 233.04 |  | 722.4 | 159.36 | 0.4197 |
| 698.8 | 233.31 |  | 686.5 | 152.? 0 | 0.4277 |
| 704.5 | 234.03 |  | 627.3 | 140.55 | 0.4401 |
| 792.8 | 233.25 |  | 547.7 | 124.24 | 0.4548 |
| 798.5 | 234.17 | 0.1982 | 504.5 | 114.46 | 0.4622 |
| 815.0 | 235.20 | 0.2079 | 500.2 | 115.51 | 0.4641 |
| 856.2 | 250.21 | 0.2315 | 472.3 | 107.51 | 0.4695 |
| 868.5 | 228.68 | 0.2412 | 412.5 | 92.03 | 0.4811 0.4910 |
| 875.5 | 227.66 | 0.2469 | 353.2 | 78.19 | 0.4910 |

# TABLEVII <br> (Continued) 

ETHYLENE-D-BUTANE SYSTM
Actual Measurements of Pressuren, Temperatures and Densities at the Phase Boundaries

| 66.18 Mol \% Ethylene |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure $\qquad$ | $\begin{aligned} & \text { Temp. } \\ & { }_{0} \\ & \hline \end{aligned}$ | Density me/ce | Pressure $\qquad$ | Temp. <br> $\mathrm{O}_{\mathrm{F}}$ | Density ams/ac |
| 101 | 77.3 | 0.01285 | 968 | 179.17 | 0.2152 |
| 121 | 88 |  | 968.4 | 177.84 | 0.2238 |
| 121 | 87 |  | 969.5 | 176.12 | 0.2275 |
| 124 | 89.0 |  | 971 | 175.27 | 0.2328 |
| 132 | 92.2 | 0.01953 | 974.5 | 172.36 | 0.2402 |
| 185 | 115.8 | 0.02162 | 973 | 172.81 | 0.2405 |
| 225 | 124.38 |  | 973 | 171.32 | 0.2446 |
| 217 | 124.38 | 0.02558 | 973 | 170.01 | 0.2508 |
| 251 | 133.86 | 0.02901 | 973 | 168.24 | 0.2517 |
| 285 | 140.72 | 0.0322 | 973.5 | 170.55 |  |
| 363 | 155.70 | 0.04081 | 973.5 | 169.04 |  |
| 413 | 164.35 | 0.04656 | * 973.5 | 169.02 | 0.2541 |
| 432 | 167.02 | 0.04926 | 973 | 168.6 |  |
| 526.3 | 179.15 | 0.06453 | 972 | 167.03 | 0.2598 |
| 589 | 184.39 | 0.07726 | 970 | 165.17 | 0.2672 |
| 680 | 188.12 | 0.09688 | 970 | 164.39 | 0.2705 |
| 699 | 188.57 | 0.1006 | 967.3 | 162.11 | 0.2777 |
| 728 | 188.43 |  | 965.5 | 160.72 | 0.2820 |
| 782 | 189.51 | 0.1187 | 963 | 158.65 | 0.2885 |
| 802.5 | 189.54 | 0.1241 | 952.1 | 155.60 | 0.2971 |
| 845 | 189.53 | 0.1335 | 941.6 | 152.48 | 0.3059 |
| 887 | 189.45 | 0.1514 | 909.2 | 142.31 | 0.3324 |
| 902 | 189.20 | 0.1557 | 862.4 | 132.75 | 0.3560 |
| 928 | 188.25 | 0.1615 | 849.1 | 129.47 | 0.3627 |
| 934.5 | 187.29 | 0.1764 | 815.2 | 123.62 | 0.3745 |
| 950 | 185.08 | 0.1890 | 732.0 | 107.34 | 0.3989 0.4108 |
| 958 | 182.51 | 0.2011 | 684.8 | 97.87 89.41 | 0.4108 0.4211 |
| 960 | 181.33 | 0.2063 | 639.1 | 89.41 | 0.4211 0.4346 |
| 964 | 178.06 | 0.2197 | 575.6 | 77.42 | 0.4346 |
| 967 | 178.31 | 0.2185 |  |  |  |

## TABLEVII <br> (Continued) <br> ETHYLENE———BUTANE SYSTEM

Actual Measurements of Pressures Temperatures and Densities at the Phase Boundaries
80.83 Mol \% Ethylene

| Pressure |
| :---: |
| psia |
| 128.3 |
| 132.2 |
| 153.9 |
| 214.0 |
| 238.1 |
| 305.8 |
| 343.7 |
| 418.5 |
| 418.9 |
| 421.3 |
|  |
| 461.8 |
| $550 . ?$ |
| 626.7 |
| 648.1 |
| 645.5 |
| 686.7 |
| 714.8 |
| 816.4 |
| 876.1 |
| 878.7 |
| 905.2 |


| Temp. <br> 0 F | Density <br> gms/cc |
| :---: | :---: |
| 51.86 | 0.01302 |
| 52.71 | - |
| 60.27 | 0.01538 |
| 79.32 | 0.02290 |
| 85.69 | 0.02516 |
| 100.81 | 0.03487 |
| 107.66 | 0.03871 |
| 119.32 | 0.04827 |
| 117.60 | 0.04743 |
| 121.85 | 0.05162 |
|  |  |
| 125.25 | 0.05488 |
| 134.15 | 0.06995 |
| 140.62 | 0.03193 |
| 141.37 | 0.09614 |
| 142.28 | 0.1008 |
| 144.25 | 0.1123 |
| 145.09 | 0.1182 |
| 147.44 | 0.1352 |
| 147.12 | 0.1587 |
| 147.09 | 0.1445 |
| 145.69 | 0.1549 |
| 145.35 | 0.1575 |
| 144.16 | 0.1620 |
| 143.30 | 0.1701 |
| 142.98 | 0.1725 |
| 140.65 | 0.1814 |
| 139.02 | 0.1862 |


| Pressure |
| :---: |
| psia |
| 947.2 |
| 9472.8 |
| 942.8 |
| 948.7 |
| 950.3 |
| 951.5 |
| 951.5 |
| 949.5 |
| 945 |
| 949.2 |
| 947.5 |
|  |
| 944 |
| 945.7 |
| 945 |
| 943.5 |
| 940.5 |
| 923.8 |
| 875.5 |
| 822 |
| 741.0 |
| 706.8 |
| 597.3 |
| 555.6 |
| 550.2 |
| 552.7 |
| 545.8 |
| 947 |
| 937 |


| Temp. |
| ---: |
| orp |
| 137.58 |
| 137.05 |
| 135.46 |
| 134.34 |
| 132.83 |
| 131.21 |
| 129.01 |
| 128.88 |
| 128.29 |
| 127.29 |
|  |
| 126.12 |
| 125.97 |
| 125.19 |
| 124.65 |
| 122.80 |
| 117.51 |
| 107.85 |
| 99.24 |
| 85.71 |
| 79.45 |
| 60.14 |
| 52.75 |
| 51.07 |
| 52.02 |
| 51.95 |
| 126.52 |
| 121.83 |

Density gexs/cc
0.1308
942.8137 .03
0.19501
8.7
134.34
0.2001
0.2047
0.2115
951.5
131.21
0.2179

45
128.88
0.2271
949.2
128.29
0.2296
0.2514
0.2359
0.2396
*
945
943.5
923.8
117.51
0.2429
$125.19 \quad 0.2468$
124.650 .2492
875.5
107.85
0.2589
144.250 .1123
145.09
0.1352
0.1445
741.0
85.71
79.45
60.14
52.75
51.07
52.02
51.95
0.4043
121.83


Density
gms/cc







of
 $188.4^{\circ} \mathrm{F}$ Press.
psia


19.25 Mol \% Ethylene
19.25 Mol \% Ethylene


for Various Isotherms in the Superheated Vapor Region

$$
\begin{array}{ccc} 
& \text { 162.10\% } \\
\text { Temp. } & \text { Press. } & \text { Density } \\
\mathrm{O}_{\mathrm{F}} & \text { psia } & \text { gns/ce } \\
\hline
\end{array}
$$




$151.6^{\circ} \mathrm{F}$ $151.6^{\circ} \mathrm{F}$

| $\begin{array}{l}\text { Temp. } \\ \text { OF }_{\mathbf{F}}\end{array}$ |
| :--- |
| 131.64 |
| 131.60 |




Density
gms/ce


会
罥
 $n$
$\stackrel{n}{0} 0$
0
0 둥 ©
0
0
0
0
0 8
8
0
0
0





517.90\%
Press.
psia.


TABLE VIII
(Continued)
EXHYLENE-BUCTANE SYSTEM
Actual Measurements of Pressures and Densities
for Various Isotherms in the Superheated Vapor Region
40.78 Mol \% Ethylene

| $\begin{aligned} & \text { Temp. } \\ & \mathbf{o}_{\mathrm{F}} \end{aligned}$ | $\begin{aligned} & 128.8^{\circ} \mathrm{F} \\ & \text { Press. } \\ & \text { psia } \end{aligned}$ | Density gms/cc | $\begin{gathered} \text { Temp. } \\ \mathrm{O}_{\mathrm{F}} \\ \hline \end{gathered}$ | $186.1^{\circ} \mathrm{F}$ Press. psis | Density <br> gms/ce | $\begin{gathered} \text { Temp. } \\ \mathrm{O}_{\mathrm{F}} \\ \hline \end{gathered}$ | $174.3^{\circ} \mathrm{F}$ <br> Press. <br> psia | Density pms/cc | $\begin{aligned} & \text { Tempe } \\ & \mathbf{o p}_{\mathbf{F}} \\ & \hline \end{aligned}$ | $189.9^{\circ} \mathrm{F}$ <br> Press. <br> pgis | Density gms/cc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 127.95 | 101.0 | 0.01198 | 136.14 | 105.8 | 0.01243 | 174.28 | 106.0 | 0.01176 | 189.92 | 104.5 | 0.01118 |
| 127.99 | 122.6 | 0.01465 | 136.14 | 139.8 | 0.01680 | 174,35 | 134.7 | 0.01588 | 189.91 | 141.2 | 0.01565 |
|  |  |  |  |  |  | 174.33 | 173.8 | 0.02059 | 189.91 | 190.3 | 0.02205 |
|  |  |  |  |  |  | 174.32 | 224.4 | 0.02741 | 189.89 | 265.6 | 0.03296 |
|  | 240. $5^{\circ} \mathrm{F}$ |  |  | $302.6{ }^{0} \mathrm{~F}$ |  |  | $357.4{ }^{\circ} \mathrm{F}$ |  |  | $396.0^{\circ} \mathrm{F}$ |  |
| $\begin{aligned} & \text { Temp } \\ & \mathbf{o}_{\mathrm{F}} \\ & \hline \end{aligned}$ | Presb. psia | $\begin{aligned} & \text { Density } \\ & \mathrm{gms} / \mathrm{cc} \end{aligned}$ | $\begin{gathered} \text { Temp. } \\ \mathrm{O}_{\mathrm{F}} \\ \hline \end{gathered}$ | Press. psia | Density $\mathrm{gms} / \mathrm{cc}$ | $\begin{gathered} \text { Temp. } \\ \hline{ }_{\mathrm{o}}^{\mathrm{F}} \end{gathered}$ | Press. psie | Density $\mathrm{gms} / \mathrm{cc}$ | $\begin{gathered} \text { Temp. } \\ \mathrm{o}_{\mathrm{F}} \end{gathered}$ | Press. nsia | Density $\mathrm{gmb} / \mathrm{cc}$ |
|  |  |  |  |  |  | 357.48 | 111.3 | 0.00966 | 395.97 | 104.5 | 0.00871 |
| 259.48 | 101.3 | 0.01015 | 302.56 | 101. ${ }^{\text {a }}$ | 0.00954 | 357.4 | 152.7 | 0.01339 | 395.97 | 153.6 | 0.01268 |
| 239.48 | 142.1 | 0.01473 | 302.57 | 142.4 | 0.01354 | 357.40 | 195.6 | 0.01746 | 395.98 | 174.3 | 0.01438 |
| 239.47 | 174.8 | 0.01844 | 302.56 | 173.0 | 0.01651 | 357.42 | 294.1 | 0.02735 | 395.99 | 207.9 | 0.01758 |
| 239.47 | 246.1 | 0.02781 | 302.60 | 200.8 | 0.01946 | 357.43 | 406.0 | 0.05946 | 395.98 | 292.5 | 0.02561 |
| 239.46 | 297.0 | 0.03436 | 502.61 | 250.5 | 0.02001 | 357.41 | 496.8 | 0.04967 | 396.02 | 347.9 | 0.03099 |
| 239.44 | 384.2 | 0.04728 | 302.58 | 306.4 | 0.05126 | $\mathbf{3 5 7 . 4 3}$ | 592.0 | 0.06078 | 396.01 | 415.5 | 0.05775 |
| 239.47 | 411.5 | 0.05148 | 302. 60 | 404.7 | 0.04372 | 357.40 | 693.7 | 0.07356 | 395.98 | 494.9 | 0.04608 |
| 289.48 | 493.5 | 0.06551 | 302.60 | 475.3 | 0.05318 | 357.43 | 752.6 | 0.08179 | 395.99 | 551.3 | 0.05204 |
| 239.49 | 602.0 | 0.08941 | 302.60 | 586.5 | 0.06867 | 357.45 | 805.5 | 0.08942 | 396.02 | 616.8 | 0.05925 |
| 289.47 | 655.8 | 0.1060 | 302.60 | 714.1 | 0.08851 | 357.43 | 906.0 | 0.1049 | 396.00 | 695.4 | 0.06847 |
| 239.46 | 706.2 | 0.1285 | 302.60 | 807.1 | 0.1063 | 357.43 | 999.1 | 0.1211 | 396.02 | 811.0 | 0.08582 |
| 239.48 | 804.0 | 0.1694 | 302.61 | 891.7 | 0.1252 |  |  |  | 396.02 | 848. 2 | 0.09816 |
| 239.48 | 905.0 | 0.2088 | 302.59 | 1002.5 | 0.1516 |  |  |  | 395.97 | 902.8 | 0.09577 |
|  |  |  |  |  |  |  |  |  | 395.01 | 978.E | 0.1056 |






|  |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  | 0 MO <br>  |  |
|  |  |  | 궂주 <br>  |


| $\begin{gathered} \text { Temp. } \\ \hline{ }_{0} \\ \hline \end{gathered}$ | $261.0^{\circ} \mathrm{F}$ |  | $342.5{ }^{\circ} \mathrm{F}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Press． psia | Density <br> gme／ce． | $\begin{aligned} & \text { Temp. } \\ & \mathrm{O}_{\mathrm{F}} \\ & \hline \end{aligned}$ | Press． $\xrightarrow{\text { psia }}$ | Density gms／cc |
|  |  |  | 342.47 | 150.3 | 0.01093 |
| 261.04 | 129.1 | 0.01096 | 342.47 | 194.4 | 0.01437 |
| 261.04 | 174.0 | 0.01432 | 342．44 | 221.6 | 0.01643 |
| 261.04 | 255.3 | 0.02165 | 342.16 | 290.2 | 0.02198 |
| 261.05 | 353.9 | 0.03113 | 342.16 | 352.4 | 0.02691 |
| 261.03 | 446.7 | 0.04081 | 342.47 | 380.5 | 0.02920 |
| 261.03 | 537.0 | 0.05075 | 352.48 | 473．2 | 0.08715 |
| 261．03 | 622.6 | 0.06101 |  |  |  |
| 261.04 | 726.2 | 0.07448 | 342.47 | 573.7 | 0.04643 |
| 261．02 | 817.1 | 0.08745 | 342．50 | 676.3 | 0.05596 |
| 261．02 | 935.8 | 0.1 .0418 | 342.51 | 700．4 | 0.05843 |
|  |  |  | 342.47 | 788.7 | 0.06706 |
|  |  |  | 342． 47 | 923.0 | 0.08105 |

s．
0
0
0
0
 $157 . \hat{0}^{\circ} \mathrm{F}$

| $\begin{aligned} & \text { Temp. } \\ & \mathrm{o}_{\mathrm{F}} \end{aligned}$ | $121.8{ }^{\circ} \mathrm{F}$ |  | 157．0 $0^{\circ} \mathrm{F}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Press． psia | Density gms／cc | $\begin{gathered} \text { Temp. } \\ \hline \end{gathered}$ | Press． psia | Density $\mathrm{mms} / \mathrm{ce}$ |
| 121.82 | 101.8 | 0.01157 | 157.62 | 109.0 | 0.01125 |
| 121.83 | 120.3 | 0.01342 | 157.62 | 122.5 | 0.01275 |
| 121.82 | 149.8 | 0.01689 | 157.63 | 163.8 | 0.01683 |
|  |  |  | 157.62 | 104.3 | 0.02139 |
|  |  |  | 157.52 | 257.3 | 0.02741 |
|  |  |  | 157.62 | 296.1 | 0.03197 | $103.4^{\circ} \mathrm{F}$

Press．



－

| Temp． <br> $0_{\mathrm{F}}$ | $103.4^{\circ} \mathrm{F}$ <br> Press． <br> psia | Density <br> gms／cc |
| :--- | :--- | :--- |
| 103.38 <br> 103.38 | 102.9 <br> 113.5 | 0.01224 |
|  |  | 0.01461 |

66．18 Mol \％Ethylene
Actual Measurements of Pressures and Densities
for Various Isotherms in the Superheated Vapor Region －

TABLEVIII
（Continued）
ETHYLENEM－BUTANE SYSTEM


















## ETHYLENE-D-BUIANE SYSTEM

Actual Measurements of Temperatures, Pressures and Densities in the Liquid and Critical Regions
19.85 Mol \% Ethylene

| $\begin{aligned} & \text { Temp. } \\ & \text { OPF }_{\mathrm{F}} \\ & \hline \end{aligned}$ | Pressure psia | Density gms/cc |
| :---: | :---: | :---: |
| 84.88 | 431. ${ }^{2}$ | 0.5321 |
| 84.88 | 605.0 | 0.5557 |
| 84.88 | 761.5 | 0.5395 |
| 84.88 | 864.1 | 0.5432 |
| 84.88 | 977 | 0.5455 |
| 118.92 | 316.z | 0.5056 |
| 118.92 | 409.2 | 0.5068 |
| 118.92 | 486.9 | 0.5097 |
| 118.92 | 656.6 | 0.5122 |
| 118.52 | 808.2 | 0.5145 |
| 118.9\% | 930.z | 0.5182 |
| 159.38 | 453.0 | 0.4728 |
| 159.38 | 512.7 | 0.4796 |
| 159.38 | 625.0 | 0.4776 |
| 159.E7 | 798.0 | 0.4823 |
| 159. ${ }^{\text {7 }}$ | 934.1 | 0.4862 |
| 202.55 | 602.4 | 0.4276 |
| 202.70 | 736.0 | 0.4407 |
| 202.70 | 840.7 | 0.4492 |
| 202.70 | 925.5 | 0.1563 |
| 266.51 | 775.8 | 0.27751 |
| 266.51 | 837.1 | 0.2965 |
| 266.51 | 930.9 | 0.3248 |
| 266.50 | 980 | 0.3682 |
| 266.51 | 1012 | 0.3774 |

40.78 Mol \% Ethylens

| $\begin{gathered} \text { Temp. } \\ \mathrm{o}_{\mathrm{F}} \end{gathered}$ | Pressure psia | Density <br> ems/ce |
| :---: | :---: | :---: |
| 72.04 | 408.2 | 0.4972 |
| 72.04 | 624.7 | 0.5008 |
| 72.04 | 755.1 | 0.5029 |
| 72.06 | 891.9 | 0.5059 |
| 72.04 | 988.4 | 0.5071 |
| 140.20 | 695.4 | 0.4431 |
| 140.21 | 780.2 | 0.4465 |
| 140.20 | 856.3 | 0.4480 |
| 140.20 | 981 | 0.4525 |
| 190.64 | 875.2 | 0.3744 |
| 190.6E | 910.7 | 0.3785 |
| 190.62 | 963 | 0.3840 |
| 190.63 | 1003 | 0.3921 |
| 202.78 | 895.5 | 0.3418 |
| 202.78 | 951 | 0.3586 |
| 202.79 | 995 | 0.3755 |
| 203.11 | 990 | 0.8742 |
| 208.55 | 957.5 | 0.3325 |
| 208.55 | 963 | 0.3897 |
| 208.55 | 1015 | 0.8595 |
| 215.87 | 945 | 0.3187 |
| 215.87 | 967 | 0.3301 |
| 215.87 | 985 | 0.3824 |
| 215.88 | 991 | 0.3345 |

# TABLEIX <br> (Continuea) 

## ETHYLENE———BUTANE SYSTEM

Actual Measurements of Temperatures, Pressures and Densities in the Liquid and Critical Regions
$66.18 \mathrm{Mol} \%$ Ethylene

| $\begin{aligned} & \text { Temp. } \\ & O_{T} \\ & \hline \end{aligned}$ | Pressure $\qquad$ | Density $\mathrm{gma} / \mathrm{cc}$ |
| :---: | :---: | :---: |
| 71.70 | 595.9 | 0.4362 |
| 71.70 | 660.9 | 0.4365 |
| 77.68 | 720.5 | 0.4386 |
| 77.58 | 813.8 | 0.4436 |
| 77.58 | 874.5 | 0.4454 |
| 123.62 | 819.3 | 0.3750 |
| 125.78 | 942.7 | 0.3750 |
| 130.86 | 892.1. | 0.3643 |
| 145.07 | 913.4 | 0.3251 |
| 145.08 | 936.7 | 0.8288 |
| 145.07 | 991 | 0.3885 |
| 163.21 | 979 | 0.2784 |
| 163.22 | 994 | 0.2863 |

80.88 Mol \% Ethylene

| $\begin{gathered} \text { Temp. } \\ \mathrm{o}_{\mathrm{F}} \\ \hline \end{gathered}$ | Pressure $\qquad$ | Density $\mathrm{gms} / \mathrm{cc}$ |
| :---: | :---: | :---: |
| 51.86 | 614.6 | 0.4142 |
| 51.86 | 698.5 | 0.4157 |
| 51.86 | 870.3 | 0.4168 |
| 51.86 | 924.6 | 0.4193 |
| 79.70 | 753.0 | 0.3728 |
| 79.66 | 800.4 | 0.3781 |
| 79.66 | 865.3 | 0.3818 |
| 79.66 | 930.9 | 0.3895 |
| 79.67 | 1007 | 0.3972 |
| 117.51 | 958 | 0.2824 |
| 117.50 | 965 | 0.2847 |
| 117.50 | 981 | 0.2875 |
| 117.50 | 998 | 0.2926 |
| 122.84 | 949 | 0.2625 |
| 122.84 | 976 | 0.2702 |
| 122.84 | 979 | 0.2751 |
| 122.84 | 996 | 0.2794 |
| 134.34 | 957.5 | 0.2098 |
| 134.35 | 969 | 0.2162 |
| 134.35 | 988 | 0.2187 |
| 134.35 | 996 | 0.2285 |

CALIBRATION OF HIGH PRESSURE TUBE
Volume of Mercury
in Thbe-cis



$$
\begin{aligned}
& \text { Distance from } \\
& \text { End of Tube to Top } \\
& \text { of Moniscus-ca }
\end{aligned}
$$


Volume of Morcury
in Tube-cm 0.03497
.04806
.06860
.0891
.09496
0.10955
.14588
.172866
.215808
.244822

Distance from | End of Tube to Top |
| :--- |
| of Meniscus-an | 1.765

2.195 2.912 $\mathbf{3 . 5 7 4}$
$\mathbf{3 .} .858$ 4.544 4.505 6.524 8.010 9.00 13.204 14.814 17.835 18.952 20.590 22.812 23.537 26.717 29.89 32.669 55.50 38.484 4
4
4
4 8
0
0
0
8 52.619


[^0]:    

