The three-dimensional cephalogram: Theory, technique, and clinical application

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The Broadbent-Bolton cephalostat produces intrinsically three-dimensional information about cranial form. Yet in the clinical setting, this information has been used primarily two dimensions at a time in the separate study of lateral or posteroanterior cephalograms. In this article we demonstrate an expedient use of existing cephalostat-based data sets to derive certain analyses of three-dimensional form. The technique is essentially the same as that of the Broadbent-Bolton "Orientator," an exploitation of the geometry of the cephalostat to simulate stereophotogrammetry. The three-dimensional method supports the usual biometrics of landmark locations, and takes advantage of a normative data base that is suited for semiautomatic analysis of syndromic data. The principal drawback of the method is its inability to represent curving form in three dimensions. However, in comparison with computed tomography (CT), it involves low radiation dose, is simpler to obtain, has an available normative data base, and is more practical for quantitative or long-term serial analysis. (Am J Orthod Dentofacial Orthop 1988;94:327-37.)

Cephalometrics is a three-dimensional enterprise. From the very first introduction of the cephalostat, Broadbent and Bolton¹ stressed the importance of coordinating the lateral (LAT) with the posteroanterior (PA) films to arrive at a distortion-free definition of craniofacial form. For this purpose they described the Orientator, an acetate overlay to be placed over both standardized cephalograms (LAT and PA) after they were oriented jointly along their common Frankfort horizontal plane. One can imagine that in the exposure of a pair of cephalograms it is not the patient's head that is turned, but instead the cephalostat itself. The LAT and PA films would in this case occupy positions at 90° to each other, approximately 150 cm above the floor of the cephalostat room. By keeping the films in register with respect to the head, one can draw the rays connecting the x-ray source to each landmark of either film as threads in space. The result (Fig. 1, A) is a pair of pyramidal sprays of thread, intersecting at approximately 90° throughout the interior of the space occupied in reality by the patient's head. The pair of films can be flattened into one plane by unfolding them along the "corner" at which they approach each other, with each bundle of threads (x-ray paths) flattened to the side of the other film at the appropriate distance. The result is the modified scene in Fig. 1, B. The Orientator is the diagram of the flattened threads. When it is superimposed over the abutted pair of films, the points in each film that correspond to any particular locus in the other can be visualized.

Broadbent and Bolton² used the Orientator to correct for the distortion inherent in the spread of the cephalostatic x-ray beam. We may imagine that, freed of the conventions of x-ray projection, we are instead truly reconstructing the locations of landmarks in space. The principle of the Orientator then becomes identical with that of one standard photogrammetric tool for this purpose, the ray intersection method (see below).

The orthodontic community paid little attention to the PA cephalogram shortly after its introduction by Broadbent. Because the clinical problems encountered by most orthodontists were symmetric, they appeared to be adequately recorded by the lateral view alone; whatever the distortion was between left and right sides in this conventionalized representation, it was nearly invariant from case to case and could be ignored. In recent years, as orthodontists have become "craniofacial orthopedists" treating more severe, often asymmetric craniofacial anomalies, the limitations of the lateral cephalogram have become obvious. For example, the lateral cephalogram (LAT) by itself is of little clinical value in the evaluation of a patient with unilateral craniofacial microsomia.³⁴

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Fig. 1. The Bolton Orientator is a two-dimensional representation of the correspondence between points in the posteroanterior and lateral views. A, The two pyramidal sprays of threads representing the lines from x-ray source to film when the patient's head is held fixed and the cephalostat is rotated 90°. B, When frame (A) is flattened into a plane, each point in one film can be restricted to lie on one particular thread in the other film. (From Broadbent BH, Broadbent BH, Golden WH. Bolton standards of dentofacial developmental growth. St. Louis: The CV Mosby Company, 1975.)

In returning to the original goal of Broadbent and Bolton, however, most methodologists have not used the original source of data, the calibrated pair of cephalograms. (However, see Wylie and Elsasser for an earlier biplane photogrammetric analysis.) Rather, modern workers have pursued new sources of data that in various ways supplant or replace the lateral cephalogram by a different type of lateral information. For example, Baumrind, Moffitt, and Curry obtained true three-dimensional cephalograms from coplanar cephalometric stereo pairs. Grayson and colleagues produced standardized tracings of the PA and basilar films keyed to depth information as recorded from a standardized LAT; Rune and associates used implants to study changes in the relative position of various bony components of the skull. The positions of these implants are reconstructed from sets of two cephalometric views.

The new methods have diverse advantages and disadvantages. They require invasion of the subject's body (by metal implants, radiation) and expensive machinery (CT scan or stereophotogrammetric reconstruction) (Baumrind et al. Berkowitz and Cuzzi, Savara et al.) for visualizing the reconstructed form. There is one further disadvantage that all share in common: the absence of normative data. It is unlikely that there will ever be a collection of CT scans from a "representative" population sample of growing children considered "normal." Normal children are not scanned, at least not with a view toward establishing normative data. Instead, they form a clinical residual category, having demonstrated negative findings in scans for the investigation of suspected diagnoses. Similarly, normal children are not implanted with metallic markers about the maxilla or frontal bones. In fact, in the United States, normal or unaffected children are no longer permitted to undergo even cephalogrammetric examination for any reason.

Thus in biometric analysis we are restricted to the normative series that have already been gathered, those associated with the larger orthodontic research groups in large and small cities in the 1950s and 1960s: the Ann Arbor sample, the Burlington sample, the Denver sample, and the Oregon sample. As heterogeneous as these groups are in ethnicity, criteria for selection, and
mode of serial follow-up, they share at least a common geometry of measurement: the Broadbent-Bolton cephalostat.

This article is divided into two parts. First, we shall explain in detail how two landmark locations, one derived from a lateral (LAT) cephalogram and one from a posteroanterior (PA) cephalogram, are combined into a three-dimensional point. Second, we shall demonstrate the biometric use of the three-dimensional cephalogram in two applications: the description of normative growth and the surgical planning of a single case of hemifacial microsomia.

THE THREE-DIMENSIONAL CEPHALOGRAM
The raw data: Pairs of points

For a radiographic landmark to be locatable in the space of the head, it must be connected to the x-ray source in two different projections: the LAT and the PA views. The best landmark candidates for such points are structures defined by means of the vertical coordinate, which is shared between the two views. For example, many landmarks are conventionally defined as the "top" or "bottom" points of structures: menton, one version of condylions left and right, superior and inferior orbital rims left and right, and cusp tips of upper and lower molar mesial cusps and canine cusps. Of course, points uppermost or lowermost on the edge of a structure in the PA cephalogram may not represent precisely the same points in space uppermost or lowermost in the lateral cephalogram (Fig. 2.).

Other points may be paired between the images by virtue of being extremities in directions oblique to both central beams and thus represented, however approximately, as extremities in each image. For example, the medial and lateral orbital points left and right are extremities in the PA view and lie where the orbital rim recedes somewhat from the x-ray source; thus they may be identified in the lateral film also, where they appear as most posterior points on the two halves of the tracing of the same rim.

The typical lateral tracing (LAT) includes eight landmarks conventionally taken to lie on the midsagittal plane: sella, nasion, anterior nasal spine, supradentale, averaged upper incisal edge, averaged lower incisal edge, menton, and pogonion. Of these, supradentale is visible in the PA film, as are the averaged incisal edges and menton (Fig. 3). Sella, nasion, anterior nasal spine, and pogonion have little visibility, if any, in the posteroanterior film. With two of their coordinates supplied by the lateral film, the third may be taken to correspond to the apparent position of the midsagittal plane at the appropriate depth (Grayson et al.3) in the frontal film.

Any three-dimensional reconstruction will proceed more accurately if the bilateral landmarks on the lateral film have not been averaged. Instead they should be identified individually by a careful consideration of study models, dental landmarks, and auxiliary cephalometric films (panoramic, basilar, or submental vertex view) whenever necessary. Existing sets of normative data for the lateral view, not collected with three-dimensional procedures in mind, generally have suffered bilateral averaging. This is satisfactory insofar as normal asymmetry is fluctuating; but the normal PA film also shows a directional asymmetry— asymmetry that cannot be corroborated by lateral data after averaging. Such landmarks will be reconstructed at different distances from the midsagittal plane (corresponding to having been digitized separately on the PA film) but
Fig. 4. Geometry of an idealized three-dimensional landmark reconstruction: intersection of two approximately perpendicular threads in space.

will have identical values for the other two coordinates, those averaged in the lateral landmarks. This is arranged by a variant of the ray-intersection algorithm. First, a true three-dimensional location for the averaged lateral landmark is computed by intersection with the midsagittal plane of the line from x-ray source to this average as located on the lateral film. Second, a line perpendicular to the midsagittal plane through this projected location is intersected with a suitable representation for each appearance on the PA film—generally, a plane through the x-ray source.

The three-dimensional cephalometric landmarks located in the PA and LAT films are listed in Table I. The operational definitions of these points will be the subject of a subsequent publication. They are available from the senior author on request.

### Registration of the pair of films

The theory of the cephalostat treats projections of the same head in a pair of views precisely to the Frankfort horizontal plane and separated by a 90° rotation about the vertical plane. The real data are more or less divergent from the ideal: heads cannot be placed precisely in the Frankfort horizontal plane, nor does the subject hold a fixed orientation while rotated 90° within the cephalostat. (In a true Bolton system, the images at 90° are generated almost simultaneously by the use of different x-ray systems that are themselves at 90°. Modern cephalostats have lost this crucial capability. We are grateful to Sheldon Baummard for pointing this out to us and for directing us to Wylie and Elsasser.

In particular, there is usually some element of rotation about the ear rods, away from the Frankfort horizontal plane in one or both images. Modest amounts of such positioning error may be routinely corrected by simple computations before one proceeds to actual three-dimensional reconstructions.

The correction procedure we invoke on all film pairs, whether or not there is reason to suspect any malpositioning, applies after the landmarks have been "digitized," assigned coordinates in any convenient Cartesian system. The films corresponding to LAT and PA projections of the same head are digitized separately. The following computations apply to the digitized data—that is, the configurations of discrete landmark points.

The LAT cephalogram is rotated so that the point midway between the two porions (which should overlap precisely, but in reality fail to do so) lies on a horizontal line with the midpoint of the two orbitales (inferior orbital rim points). The PA film is rotated so that the line between the two porions is precisely horizontal. This film is then subjected to a computed shear correcting for failure of the midorbitale point to lie precisely on the horizontal line between the two porions. Every landmark locatable on both films is sheared upward or downward by an amount corresponding to its anteroposterior separation from porion as scaled by the anteroposterior separation of midorbitale from midporion in the lateral film. This is a satisfactory approxi-

### Table I. Three-dimensional cephalometric landmarks (x, y, and z coordinates found in the lateral and posteroanterior cephalograms)

<table>
<thead>
<tr>
<th>Three-dimensional landmarks</th>
<th>Lateral cephalogram</th>
<th>Posteroanterior cephalogram</th>
</tr>
</thead>
<tbody>
<tr>
<td>Porion left and right (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Superior orbital point (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Lateral orbital point (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Medial orbital point (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Orbitale (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Nasion</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Pterion aperture lateral inner table (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Anterior nasal spine</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>A point</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Supradentale</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Upper incisal edge</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Upper molar cusp tip (L,R)</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Lower incisal edge</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Infradentale</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>B point</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Pogonion</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Menton</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Condylion (L,R)</td>
<td>z</td>
<td>x-y</td>
</tr>
<tr>
<td>Gonion (L,R)</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Lower molar cusp tip (L,R)</td>
<td>y-z</td>
<td>x</td>
</tr>
<tr>
<td>Sella</td>
<td>y-z</td>
<td>x</td>
</tr>
</tbody>
</table>
Fig. 5. A set of reconstructed three-dimensional landmarks is represented by a wire frame, the various structures rotating in a computer-graphic display. These are seven still frames from such a moving display. This patient is discussed further in connection with Figs. 14 and 15.

Fig. 6. In practice, the threads of the ray-intersection method will fail to intersect exactly. We take the three-dimensional landmark location to be the midpoint of the shortest chord joining the lines.

configuration of discrete landmarks extracted from the cephalogram by digitizing.

The ray intersection method

After this calibration step, we may imagine that the landmark locations correspond precisely to the nominal geometry of the cephalostat (Fig. 4). Each lies on one of a pair of film planes in precisely known spatial relation at 90° to each other (corresponding to the presumed 90° rotation of the head between LAT and PA films). The landmark images are at a known distance from an x-ray source whose central beams are at 90° to each of the films and which intersect in space, again at an angle of 90°, exactly halfway between the pair of portions of the subject.

As in the previous discussion of the Orientator, one may imagine each landmark location on film now replaced by the path in space that the x ray must have followed to arrive there: a thread connecting that digitized location to the source approximately 2 m away (Fig. 4). In principle, the pair of threads corresponding to a pair of landmarks visible in both films should intersect “in space” (that is, inside the region occupied by the patient’s head) at the three-dimensional location occupied by that point. In this way the distortion inherent in each cephalometric projection alone is corrected by the combination of points from both films in a distortion-free three-dimensional landmark set (Fig. 5). This three-dimensional constellation of landmarks may be joined by straight lines and rotated for viewing in all directions.

In practice, the threads going to “the same” point in both views do not intersect precisely. Although they lie at nearly 90° to each other, because of the nominal geometry of the cephalostat, they invariably miss each other by a lesser or greater extent. We have chosen to represent the “true” position of the landmark by the midpoint of the chord of shortest separation between
the two threads in space (Fig. 6). For threads so nearly perpendicular to each other as these, this midpoint is approximately the same as the point arrived at by (1) accepting the mediolateral (X) coordinate from the PA film after correction for beam spreading with information from the lateral film, (2) accepting the anteroposterior (Z) coordinate from the lateral film after correction for beam spreading with information from the PA film, and (3) averaging the two vertical coordinates (Y), one from each film, each after correction for beam spreading.

This type of three-dimensional reconstruction is susceptible to several inherent errors and limitations. One fundamental difficulty is associated with the assumption that "corresponding" landmarks in LAT and PA films actually pertain to the same three-dimensional point on the skull. For the landmarks that are defined as "bottoms" of structures (for example, orbitale), it is clear that this correspondence is guaranteed only for points lying precisely in the plane formed by the pair of central beams, the Frankfort horizontal plane. At other sites, the quality of the "three-dimensional correspondence" between points traced from the LAT and PA projections depends on the relationship of the central beam to the curved surface on which we search for a landmark. For instance, when a coordinate system is assigned in a two-dimensional film, menton can be defined unambiguously as a single point; but on a dry skull, one can see that the PA film's "menton" is slightly posterior to the lateral "menton," resulting purely from considerations of beam geometry, and that neither point is precisely at the bottom of the mandible (Fig. 2).

For landmarks other than "tops" and "bottoms," beam geometry generates discrepancy by a different mechanism: it determines which outlines of curving surfaces we see when looking at a three-dimensional object. The mesial-incisal edge of the maxillary central incisor, for example, is curved sharply in all directions. Thus the spatial location of this landmark seen in the lateral film is not far from the spatial location of the point seen in the PA film. But when landmarks are taken from surfaces that are broadly curved in one or both directions, such as the gonial region, then the bony points seen in the LAT and PA films are distinctly different, and the pair of reconstructed lines in space can fail to intersect by a considerable amount. (For gonion the problem is made worse by the fact that there is no such point on the solid skull—that is, we are combining a pair of artifacts, one from each of a pair of projections. There is no point of "sharpest curvature" on the solid skull in this region of the mandibular border.)

Whenever points on the solid skull corresponding to landmarks found in the LAT and PA film lie in systematically different locations, the reconstructed three-dimensional point will not actually lie on the skeleton, but instead will be close to it in a consistent fashion. This phenomenon is analogous to the use of the gonial intersect landmark, intersection of two double tangents to the mandibular border in two-dimensional cephalometrics. Although the three-dimensional gonion lies consistently lateral to the bony skull, this does not preclude its use in an analytic manner.

As mentioned previously, certain landmarks—for example, anterior nasal spine—are not in fact visible in both films; rather, the position in one film is imputed with information from the other. This is equivalent to assigning two coordinates (Y and Z) of the point from one of the films (in this case the lateral) and obtaining the third (X) from the PA film. Such a computation is a generalization of the ray-intersection method. When the geometry of the cephalostat is taken into account, this computation is equivalent to the intersection of a plane in space (corresponding to the X coordinate of ANS observed in the PA film) with a line (the thread through the LAT film at the Y-Z location of ANS).

Some inherent flaws and errors of this scheme include tracing and digitizing errors, failure of the portions to superimpose in the lateral film, and the finite size of the x-ray source.

**Norms**

In the clinical examples to be presented in this article, reference is made to two different sources of normative data: the Bolton standards and the University of Michigan School Study. Both are deficient in the lateral view in that they present only averages of the two sides, tracings or landmark locations, rather than true paired landmarks or curves as they embody different degrees of beam spreading. Consequently the reported ray-intersection algorithm has been modified so that bilateral points from the lateral view are represented by threads through a midsagittal location and perpendicular to the film plane, rather than joining the actually digitized film point (which we do not have) to the actual x-ray source in the nominal cephalostat geometry.

The two normative data bases suit different purposes. The Bolton norms are tracings from which one can extract subsets of landmarks ad lib. The Michigan norms comprise landmark locations only, in a list not necessarily suited to our current needs. The lateral data set incorporates all 59 of the landmarks biometrically summarized by Riolo and associates. The data base of digitized tracings underlying these coordinate data...
CLINICAL EXAMPLES

The three-dimensional data set can serve the clinician and investigator in various ways: description of normal and abnormal anatomies, documentation of normal and abnormal patterns of growth, study of growth after surgical intervention, description of relapse after surgery, and presurgical simulation and planning. The cephalometric analysis of these data permits study of normal and abnormal populations and syndrome identification and description.

A. Normative growth

The Michigan data base includes 20 paired films for boys at 8 years of age and another 20 at 12 years of age; of these, 12 correspond to serial studies. By means of the tensor biometrics of Bookstein, we describe the mean changes in configurations of a mandibular landmark configuration (menton, left and right condylions, left and right gonions) for this small sample of boys. The descriptions of mean change provided by such an analysis are equivalent to any other full-information description of the same mean change, such as the finite-element methods of Cheverud and associates or Moss and associates. Use of the tensor biometrics has the advantage of an associated multivariate statistical theory, permitting various forms of hypothesis testing. In this configuration of five landmarks, the finite-element analysis of solid form is ambiguous. The analysis to follow incorporates a sufficient number of triangles to exhaust the findings of any other biometric analysis dealing with the same five points. A complete explanation of the tensor diagrams may be found in Bookstein.

The tensor findings are summarized in Fig. 7. They represent three-dimensional descriptions of mandibular size and shape change free of the perspective distortion seen in two-dimensional cephalometrics. For example, the summary of change in the triangle menton-
Fig. 9. The two-dimensional PA view suggests too large a rate of growth of menton away from the condylar axis (3.07% per year), resulting from a decrease in foreshortening.

Fig. 10. The basilar view suggests too small a rate of growth of menton away from the condylar axis, resulting from an increase in foreshortening. In this projection, the mandibular triangle appears to grow at the same rate in all directions (approximately 1.60% per year), that is, not to change in mean shape during these 4 years.

Fig. 11. Geometry of mandibular growth as viewed in the lateral film. A, Growth of the triangle gonion-gonion-menton. B, As the bigonial distance increases at a greater rate than the bicondylar distance, the ramus uprights and becomes more parallel to the film plane. In a two-dimensional, lateral-view cephalogram, ramal height appears to increase because of both growth and reduction in foreshortening of ramus image.

Fig. 12. The true rate of growth of the mandible is biased upward in the lateral view (see text).

Fig. 13. Three-dimensional Bolton standards for the 16-year-old male patient, to be compared to the patient with hemifacial microsomia.

condylion-condylion (Fig. 8) indicates that the distance between the condyles has increased by an average of 1.53% per year, and that this is the smallest specific rate of growth of any distance definable with these three landmarks; whereas the true (three-dimensional) distance from menton to the line between the condyles (Fig. 8) has increased by an average of 2.48% per year during this interval, and this rate of increase is the largest of any distance defined by means of the same three landmarks. The standard deviation of rate of increase of this latter distance is 0.40%; for the distance between the condyles, it is twice as great (0.77% per year), corresponding to greater uncertainty in location of the condyles along this direction in the PA film.

In the two-dimensional PA view (Fig. 9), this same triangle shows a rate of increase of the (projected) distance of menton from the line between the condyles of 3.0% per year. This number is too large and thus indicates a decrease in foreshortening of this triangle (in the PA view) at the same time that growth is occurring. By contrast, in the basilar view (Fig. 10) the same distance shows a rate of increase of only 1.60% per year, considerably less than seen in the three-dimensional cephalogram (and corresponding to a considerable increase in foreshortening).
Turning now to the triangle menton-gonion-gonion (Fig. 11, A), we see that the distance between the gonions grows most slowly (about 1.95% per year), while the distance of menton from the bigonial line grows at more than 3% per year. The rate of change is exaggerated in the PA view by a decrease of foreshortening as the menton grows downward. The change in projected distance appears to be at a rate of more than 4.5% per year in the PA; a basilar view, in which foreshortening is increasing, indicates a rate of growth of about 2.8% per year, which is less than the true rate.

As the bigonial distance is growing relatively faster than the bicondylar distance, the observed changes of distance in the lateral view of the mandible are likewise altered by foreshortening (Fig. 11, B). The rate of increase of mandibular "width," as measured along the bisector of the gonial angle, is nearly the largest of any distance involving menton, gonion, and condyion (Fig. 12). The tensor analysis of the lateral cephalogram overstates both this rate and the rate of growth in the perpendicular direction. During the course of normal growth, the whole lateral view of the mandible "rotates to face the camera." While the lateral view increases in apparent area by about 5.9% per year, the triangle of landmarks in space increases in area by only about 5.2% per year.

B. A surgical simulation

The authors have previously published\textsuperscript{14,15} an application of these three-dimensional landmark configurations to the semiautomated planning of craniofacial surgery. For the simulation of the surgical procedure, the landmarks of a data set are divided into skeletal units that are left unseparated by the particular osteotomies to be performed. For example, a LeFort III
osteotomy moves the landmarks of the maxilla together with both inferior orbital rims and zygomas as one rigid unit. An "operation" is specified as a rigid motion for each of these subsets of landmarks with respect to one in particular to be taken as "fixed."

The first step in computing such an "operation" is the automatic estimation of a set of rigid motions that, when simultaneously executed, result in a set of landmarks most closely approximating a "normative" form. The landmarks derived from the age- and sex-matched Bolton templates were used three-dimensionally according to the method described previously (Fig. 13). The "optimal" computed surgery is the set of displacements and reorientations of all fragments that together minimize the mean-squared distance between the corresponding landmarks in the normal Bolton form and the patient's postoperative form. The optimization strategy used is of the coordinate search type. Once this computation is completed, the clinician is encouraged to specify further rigid motions to adjust the prescription to the subtler, more subjective requirements of clinical reality. When the clinician is satisfied, the project generates a summary report of the ultimate displacements and reorientations for each skeletal fragment.

For a patient with unilateral craniofacial microsomia, Fig. 14 illustrates the three-dimensional cephalometric image of the starting form. The plan for surgical correction includes a LeFort I osteotomy, sagittal split of the mandible, and a horizontal osteotomy (genioplasty) of the chin (Fig. 15). The optimal surgical change in landmark positions is set forth in Table II.

This form of interactive surgical planning, but without the possibility of optimization, may also be carried out with three-dimensional CT scan reconstructions of the patient's facial skeleton. Fusion of the cephalometric and CT-based models of surgery should give the clinician the advantages of both forms of three-dimensional visualization. The cephalometric computation provides access to a large normative data base necessary for the optimization and measurement operations; the CT-based model provides superior visualization of curving structures for interaction with the simulation.

**DISCUSSION**

The reported three-dimensional cephalometric technique requires a great deal of work in diverse aspects. Considerable effort must be directed to error studies. For example, intratracer and intertracer variance in the location of landmarks on separate films "propagates" into anisotropic error variance of landmark locations in three dimensions. We should not exaggerate the confidence we have in our declarations that it is "the same point" in the two views, for all the geometric and technical reasons reviewed previously. Additional effort is indicated to investigate the correspondence of pairs of landmarks between films, experimenting with pairs of operational definitions so as to have the greatest covariance of the two versions of that crucial, shared vertical coordinate. The manner in which the three-dimensional cephalogram systematically overestimates or underestimates distances as measured with calipers on the solid skull must be studied either at postmortem or during the surgical procedure.

Although we acknowledge these difficulties and unknown factors, we expect the method of three-dimensional analysis to hold its own against the three-dimensional CT scan, and so serve as one member of a family of complementary methods for the study of craniofacial form. Normative data exist for the three-
dimensional cephalogram, whereas such data are unlikely ever to exist for the more extensive visualizations of the CT scan. A pair of cephalograms involves approximately 26 mrad skin dose to the subject; by comparison, a closely spaced series of CT slices totals about 6.5 rad. Hence it is much more practical to anticipate a three-dimensional cephalogram to be repeated, as for longitudinal studies of growth and relapse after surgical treatment. Moreover, the cost of a pair of cephalograms is a negligible fraction of the cost of a CT scan. The young patient does not need to be sedated in the course of this procedure.

Archives of cephalogram pairs have been collected over decades of orthodontic treatment and research. With these data one could proceed immediately with three-dimensional study of large populations of treated cases. As we noted in our first example, changes in the geometry of the face may not be well detected in projected images; three-dimensionalization improves the precision of cephalometric analysis in the study of craniofacial treatment. In the same example, we demonstrated that morphometric methods already exist for the analysis of three-dimensional landmark data, whereas they are emerging very slowly for analyses of the comparable CT data.

Mock surgery, originally introduced as a two-dimensional technique, gains in accuracy when it has access to the three-dimensional record; its tie is likewise enhanced to the corresponding computation carried out with data from the CT scan. Because of the existence of normative data, a first step in surgical planning with the three-dimensional cephalogram can be computed automatically. The three-dimensional cephalogram serves as the link between the CT scan and the norms for this computation.

In all these applications, three-dimensional cephalometric data may be recorded and manipulated by the use of equipment no more sophisticated than the now ubiquitous personal computer. The only requirements are simple algebra and simple graphics.

For all these reasons, our preliminary studies encourage us to expand and explore this system for studying pairs of cephalograms in three dimensions.

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