

## Thermodynamic properties of silicides

### II. Heat capacity at temperatures $T$ from 5.9 K to 341 K and derived thermodynamic properties to $T = 1200$ K of tungsten disilicide: $\text{WSi}_{2.06}$

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The heat capacity of tungsten disilicide  $\text{WSi}_{2.06}$  was measured over the temperature range  $5.9 < (T/\text{K}) < 341$  using adiabatic calorimetry. Our results show that neither a phase transition nor anomalies are present. A contribution from the electronic molar heat capacity is present and  $\gamma = (1.33 \pm 0.25) \text{ mJ} \cdot \text{K}^{-2} \cdot \text{mol}^{-1}$ . For the lattice, the Debye characteristic temperature  $\Theta_D^{\text{c}} = (317.8 \pm 3.3) \text{ K}$ . From our results, the standard molar entropy  $S_m^{\circ}(\text{WSi}_{2.06}, \text{cr}, 298.15 \text{ K}) = (68.43 \pm 0.17) \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$ . On the basis of this result, the standard molar Gibbs free energy of formation  $\Delta_f G_m^{\circ}(\text{WSi}_{2.06}, \text{cr}, 298.15 \text{ K}) = -(79.5 \pm 5.5) \text{ kJ} \cdot \text{mol}^{-1}$ . Heat capacities derived from drop calorimetry at  $T = 460 \text{ K}$  together with those reported in this work allowed standard molar thermodynamic functions to be presented at selected temperatures from 5 K to 1200 K.

### 1. Introduction

The transition-metal silicides, like the transition-metal dichalcogenides, possess special properties that lend themselves to applications as engineering materials. The well defined family of compounds  $\text{M}_a\text{Si}_b$  contains the metal element M within groups 13 through 18. Their stability, resistance to oxidation, low electrical resistivity, and great tensile strength at high temperatures naturally lead to their use in high-temperature furnaces and coatings, integrated circuits, and ceramic reinforcements in metal matrices and other composites.<sup>(1,2)</sup> Tungsten disilicide  $\text{WSi}_2$  is especially suitable as a refractory material.<sup>(3-5)</sup> The need to know its thermodynamic properties

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has prompted several studies to obtain key values such as the standard molar enthalpy of formation,<sup>(6, 9)</sup> enthalpy increments at high temperatures,<sup>(10, 11)</sup> and the energy of combustion.<sup>(12)</sup>

In the stable form at room temperature, tungsten disilicide is tetragonal with space group  $I4/mmm$  of No. 139  $D_{4h}^{17}$ , lattice parameters:  $a = 0.3212$  nm,  $c = 0.7880$  nm, and  $Z = 2$ .<sup>(13)</sup> The absence of low-temperature thermodynamic quantities in general, and heat capacity, enthalpy increments, and standard entropy in particular, led us to investigate these properties as part of our experimental programme on advanced materials. In this paper, we report for the first time the results of adiabatic heat-capacity measurements on  $WSi_2$  at any temperature.

## 2. Experimental

The sample of  $WSi_2$  was a gift from Dr M. Sugano, Nippon Mining Company, Japan, and is from the same batch used in the combustion studies at the National Institute of Standards and Technology (NIST).<sup>(12)</sup> The formula of the specimen is taken to be  $WSi_{2.060 \pm 0.002}$ . The  $WSi_2$  had been prepared by heating a mixture of tungsten and silicon in an evacuated tube (pressure  $p = 1$  mPa), initially at temperature  $T = 1073$  K to  $T = 1573$  K, and then at  $T = 1553$  K to  $T = 1773$  K. The details of the synthesis are presented in a patent.<sup>(14)</sup> The finely divided powder was shipped from NIST to the Royal Military College (RMC) where it was stored and handled, including the filling of the calorimeter vessel, within a glovebox filled with dry circulating nitrogen. When received at RMC, crystals were removed for X-ray study and the Guinier-de-Wolff diffraction pattern was in agreement with the standard pattern for  $WSi_2$ , No. 11-195 as determined by the Joint Committee for Powder Diffraction Standards. Its structure was found to be tetragonal at room temperature with parameters:  $a = (0.3212 \pm 0.0001)$  nm,  $c = (0.7830 \pm 0.0001)$  nm, which compare with the JCPDS 11-195:  $a = 0.3211$  nm and  $c = 0.7868$  nm, and with Zachariasen:<sup>(13)</sup>  $a = 0.3212$  nm and  $c = 0.7880$  nm.

The molar isobaric heat capacity  $C_{p,m}$  was measured at temperatures from 5.9 K to 341 K by adiabatic calorimetry in the Mark XIII adiabatic cryostat, which is an upgraded version of the Mark II cryostat described previously.<sup>(15)</sup> A guard shield was incorporated around the adiabatic shield. A capsule-type platinum resistance thermometer (laboratory designation A-5) was used for the temperature measurements. The thermometer was calibrated at the U.S. National Bureau of Standards (N.B.S., now NIST) against the IPTS-1948 (as revised in 1960)<sup>(16)</sup> for temperatures above 90 K, against the 1955 N.B.S. (NIST) provisional scale from  $T = 10$  K to  $T = 90$  K, and by the technique of McCrackin and Chang<sup>(17)</sup> at  $T < 10$  K. These calibrations are judged to reproduce thermodynamic temperatures to within 0.03 K at  $10 \leq (T/K) \leq 90$  K and within 0.04 K at  $T > 90$  K.<sup>(18)</sup> The effects of changing the temperature scale to ITS-90 vary over the range  $90 \leq (T/K) \leq 350$  from  $0.020 \leq \{(T_{90} - T_{48})/K\} \leq -0.27$ , and for the range  $14 \leq (T/K) \leq 90$  from  $-0.008 \leq \{(T_{90} - T_{55})/K\} \leq 0.018$ .<sup>(19, 20)</sup> The changes in heat capacity, enthalpy increment, and entropy resulting from the conversion from IPTS-68 to ITS-90 have been shown for a number of materials to lie within the experimental error of the

measurements over the range from  $14 \leq (T/K) \leq 2150$ .<sup>(20)</sup> Measurements of mass, current, potential difference, and time were based upon calibrations done at the U.S.N.B.S. (NIST). The heat capacities at temperatures from about 6 K to 329 K were acquired with the assistance of a computer,<sup>(21, 22)</sup> which was programmed for a series of determinations. During the drift periods, both the calorimetric temperature and the first and second derivatives of temperature with respect to time were recorded to establish the equilibrium temperature of the calorimeter before and after the energy input. While the calorimeter heater was on, the heater current and potential difference as well as the duration of the heating interval were determined. Also recorded was the apparent heat capacity of the system, which included the calorimeter, heater, thermometer, and sample.

A gold-plated copper calorimeter (laboratory designation W-139) with four internal vertical vanes and a central entrant well for (heater + thermometer) was loaded with  $\text{WSi}_2$ . Following the loading, the calorimeter was evacuated and pumping was continued for several hours to ensure that any moisture released from the sample was removed. After addition of  $p \approx 30$  kPa  $\text{He(g)}$  (at  $T = 296$  K) to facilitate thermal equilibration, the vessel was then sealed by means of an annealed gold gasket tightly pressed on to the stainless-steel knife edge of the calorimeter top using a screw closure about 5 mm in diameter.

Buoyancy corrections were calculated on the basis of a crystallographic density of  $9.805 \text{ g} \cdot \text{cm}^{-3}$ , derived from the X-ray diffraction of our sample. The mass of  $\text{WSi}_2$  was  $25.35736 \text{ g}$  ( $\approx 0.1049099$  mol, based on its molar mass of  $241.706 \text{ g} \cdot \text{mol}^{-1}$  as calculated from the 1985 IUPAC recommended atomic masses of the elements).<sup>(23)</sup>

The thermal history of the  $\text{WSi}_2$  measurements is represented by the following linear array. The arrows denote either cooling or heating, which correspond to the acquisition of heat-capacity results.

$$T = 300 \text{ K} \xrightarrow{\text{Series I}} 6 \text{ K} \xrightarrow{\text{Series II}} 77 \text{ K} \xrightarrow{\text{Series III}} 223 \text{ K} \xrightarrow{\text{Series III}} 341 \text{ K}.$$

### 3. Results

The experimental molar heat capacities  $C_{p,m}$  of our  $\text{WSi}_{2.06}$  sample are listed in table 1, where the results are presented in order of increasing temperature. The measurements were made in three series that began at  $T = 5.9$  K and ended at  $T = 341$  K. The probable errors in heat capacity decrease from about  $10^{-2} \cdot C_{p,m}$  at  $T = 10$  K to less than  $2 \cdot 10^{-3} \cdot C_{p,m}$  at temperatures above 30 K. The heat capacity of the sample varied from  $0.20 \cdot C_{p,\text{total}}$  at  $T = 15$  K to  $0.45 \cdot C_{p,\text{total}}$  at  $T = 325$  K where  $C_{p,\text{total}}$  is the total heat capacity of the sample plus the calorimeter vessel.

Shown in figure 1 is the experimental  $C_{p,m}/R$  (where  $R$  is the gas constant) against  $T$  plot for  $\text{WSi}_{2.06}$  from  $T = 5.9$  K to  $T = 341$  K. The curve appears smooth and without anomalies.

The standard molar thermodynamic functions are given at selected temperatures in table 2. The heat capacities at  $T \leq 8$  K were determined by fitting our

TABLE I. Experimental molar heat capacity of  $\text{WSi}_{2.06}$   
 ( $M = 241.706 \text{ g} \cdot \text{mol}^{-1}$ ,  $R = 8.31451 \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$ )

| $T/\text{K}$ | $C_{p,m}/R$ | $T/\text{K}$ | $C_{p,m}/R$ | $T/\text{K}$ | $C_{p,m}/R$ | $T/\text{K}$ | $C_{p,m}/R$ | $T/\text{K}$ | $C_{p,m}/R$ | $T/\text{K}$ | $C_{p,m}/R$ |
|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|
| 6.80         | 0.0035      | 28.47        | 0.169       | 67.76        | 1.720       | 127.09       | 4.578       | 188.56       | 6.570       | 263.37       | 7.879       |
| 8.01         | 0.0050      | 30.38        | 0.207       | 71.58        | 1.909       | 131.17       | 4.726       | 192.72       | 6.656       | 269.50       | 7.961       |
| 10.44        | 0.0094      | 32.30        | 0.250       | 75.42        | 2.112       | 135.24       | 4.895       | 196.86       | 6.752       | 275.71       | 8.067       |
| 11.21        | 0.011       | 34.24        | 0.299       | 79.27        | 2.310       | 139.33       | 5.029       | 200.97       | 6.834       | 281.91       | 8.146       |
| 12.25        | 0.015       | 36.21        | 0.353       | 83.07        | 2.516       | 143.41       | 5.185       | 205.12       | 6.910       | 288.16       | 8.220       |
| 13.64        | 0.020       | 38.36        | 0.422       | 87.00        | 2.695       | 147.50       | 5.313       | 209.31       | 7.009       | 294.27       | 8.300       |
| 14.78        | 0.026       | 40.58        | 0.496       | 90.96        | 2.893       | 151.59       | 5.472       | 213.40       | 7.073       | 300.53       | 8.369       |
| 15.96        | 0.032       | 42.79        | 0.577       | 94.91        | 3.073       | 155.69       | 5.609       | 217.52       | 7.161       | 306.65       | 8.430       |
| 17.30        | 0.039       | 45.36        | 0.674       | 98.90        | 3.281       | 159.79       | 5.726       | 221.65       | 7.234       | 312.90       | 8.485       |
| 18.79        | 0.049       | 48.11        | 0.785       | 102.89       | 3.499       | 163.90       | 5.849       | 226.52       | 7.318       | 319.15       | 8.522       |
| 20.29        | 0.059       | 50.87        | 0.901       | 106.89       | 3.698       | 168.00       | 5.974       | 232.38       | 7.410       | 325.40       | 8.569       |
| 21.79        | 0.072       | 53.89        | 1.039       | 110.92       | 3.864       | 172.11       | 6.125       | 238.58       | 7.509       | 331.70       | 8.596       |
| 23.32        | 0.088       | 57.15        | 1.201       | 114.96       | 4.043       | 176.23       | 6.243       | 244.77       | 7.610       | 337.99       | 8.643       |
| 24.88        | 0.108       | 60.43        | 1.363       | 119.01       | 4.216       | 180.36       | 6.344       | 250.87       | 7.701       |              |             |
| 26.60        | 0.135       | 63.97        | 1.541       | 123.05       | 4.406       | 184.47       | 6.455       | 257.14       | 7.801       |              |             |

experimental values at  $T \leq 20 \text{ K}$  to the limiting form of the Debye equation that included a term due to electronic conduction (see section 4). Plots of  $C_{p,m}/T$  against  $T^2$  and of  $(C_{p,m} - \gamma T)/T^3$  against  $T^2$ , when extrapolated to  $T \rightarrow 0$ , yielded identical results.

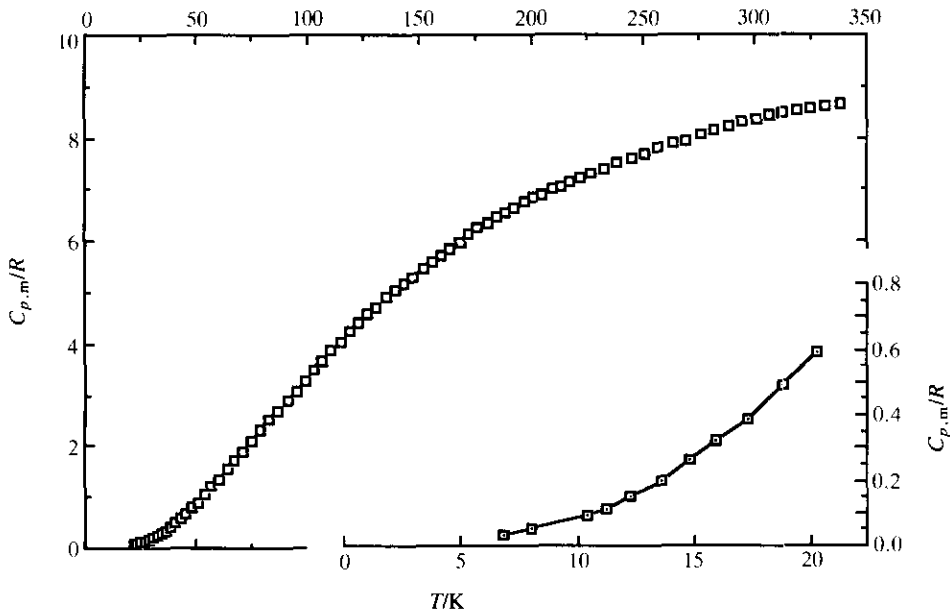

 FIGURE 1. Experimental molar heat capacities  $C_{p,m}$  at constant pressure plotted against temperature  $T$  for  $\text{WSi}_{2.06}$ . The region below  $T = 22 \text{ K}$  is enlarged in the lower right-hand corner.

TABLE 2. Standard molar thermodynamic functions for  $\text{WSi}_{2.06}$ 

$$\{M = 241.706 \text{ g} \cdot \text{mol}^{-1}; p^\circ = 101.325 \text{ kPa}; R = 8.31451 \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}; \Phi_m^\circ \stackrel{\text{def}}{=} \Delta_0^f S_m^\circ - \Delta_0^f H_m^\circ / T\}$$

| $T$<br>K | $C_{p,m}$<br>R | $\frac{\Delta_0^f S_m^\circ}{R}$ | $\frac{\Delta_0^f H_m^\circ}{R \cdot K}$ | $\frac{\Phi_m^\circ}{R}$ | $T$<br>K | $C_{p,m}$<br>R | $\frac{\Delta_0^f S_m^\circ}{R}$ | $\frac{\Delta_0^f H_m^\circ}{R \cdot K}$ | $\frac{\Phi_m^\circ}{R}$ |
|----------|----------------|----------------------------------|--|--------------------------|----------|----------------|----------------------------------|--|--------------------------|
| 5        | (0.017)        | (0.0010)                         | (0.0031)                                 | (0.0004)                 | 280      | 8.116          | 7.710                            | 1247.8                                   | 3.254                    |
| 10       | 0.0088         | 0.0039                           | 0.0261                                   | 0.0013                   | 290      | 8.245          | 7.997                            | 1329.3                                   | 3.413                    |
| 15       | 0.0260         | 0.0102                           | 0.1065                                   | 0.0031                   | 300      | 8.363          | 8.278                            | 1412.4                                   | 3.570                    |
| 20       | 0.0560         | 0.0214                           | 0.3045                                   | 0.0062                   | 310      | 8.458          | 8.554                            | 1496.5                                   | 3.727                    |
| 25       | 0.1080         | 0.0389                           | 0.7025                                   | 0.0108                   | 320      | 8.528          | 8.824                            | 1581.4                                   | 3.882                    |
| 30       | 0.1950         | 0.0659                           | 1.448                                    | 0.0176                   | 330      | 8.588          | 9.087                            | 1667.0                                   | 4.036                    |
| 35       | 0.3180         | 0.1047                           | 2.716                                    | 0.0271                   | 340      | 8.643          | 9.344                            | 1753.2                                   | 4.188                    |
| 40       | 0.4760         | 0.1570                           | 4.685                                    | 0.0399                   | 350      | 8.700          | 9.596                            | 1839.9                                   | 4.339                    |
| 45       | 0.6610         | 0.2236                           | 7.520                                    | 0.0564                   | 375      | 8.818          | 10.20                            | 2058.9                                   | 4.710                    |
| 50       | 0.8660         | 0.3052                           | 11.41                                    | 0.0771                   | 400      | 8.910          | 10.77                            | 2280.5                                   | 5.071                    |
| 55       | 1.098          | 0.3983                           | 16.30                                    | 0.1019                   | 425      | 8.983          | 11.32                            | 2504.3                                   | 5.423                    |
| 60       | 1.337          | 0.5039                           | 22.38                                    | 0.1309                   | 450      | 9.045          | 11.83                            | 2729.6                                   | 5.764                    |
| 65       | 1.586          | 0.6208                           | 29.69                                    | 0.1640                   | 475      | 9.090          | 12.32                            | 2956.4                                   | 6.097                    |
| 70       | 1.834          | 0.7473                           | 38.24                                    | 0.2011                   | 500      | 9.111          | 12.79                            | 3184.0                                   | 6.420                    |
| 75       | 2.087          | 0.8824                           | 48.04                                    | 0.2420                   | 525      | 9.140          | 13.23                            | 3412.1                                   | 6.734                    |
| 80       | 2.338          | 1.025                            | 59.10                                    | 0.2864                   | 550      | 9.162          | 13.66                            | 3640.9                                   | 7.039                    |
| 85       | 2.591          | 1.175                            | 71.43                                    | 0.3342                   | 575      | 9.184          | 14.07                            | 3870.2                                   | 7.336                    |
| 90       | 2.844          | 1.330                            | 85.02                                    | 0.3852                   | 600      | 9.218          | 14.46                            | 4100.2                                   | 7.625                    |
| 95       | 3.088          | 1.490                            | 99.85                                    | 0.4391                   | 625      | 9.240          | 14.83                            | 4331.0                                   | 7.906                    |
| 100      | 3.358          | 1.655                            | 115.9                                    | 0.4957                   | 650      | 9.263          | 15.20                            | 4562.2                                   | 8.180                    |
| 105      | 3.593          | 1.825                            | 133.3                                    | 0.5550                   | 675      | 9.293          | 15.55                            | 4794.2                                   | 8.446                    |
| 110      | 3.818          | 1.997                            | 151.8                                    | 0.6166                   | 700      | 9.321          | 15.89                            | 5026.9                                   | 8.706                    |
| 115      | 4.042          | 2.172                            | 171.5                                    | 0.6804                   | 725      | 9.355          | 16.22                            | 5260.3                                   | 8.960                    |
| 120      | 4.266          | 2.348                            | 192.3                                    | 0.7462                   | 750      | 9.382          | 16.53                            | 5494.5                                   | 9.207                    |
| 125      | 4.487          | 2.527                            | 214.1                                    | 0.8138                   | 775      | 9.408          | 17.84                            | 5729.4                                   | 9.448                    |
| 130      | 4.690          | 2.707                            | 237.1                                    | 0.8832                   | 800      | 9.432          | 17.14                            | 5964.9                                   | 9.684                    |
| 135      | 4.881          | 2.888                            | 261.0                                    | 0.9541                   | 825      | 9.462          | 17.43                            | 6201.1                                   | 9.914                    |
| 140      | 5.062          | 3.068                            | 285.9                                    | 1.026                    | 850      | 9.482          | 17.71                            | 6437.9                                   | 10.14                    |
| 145      | 5.242          | 3.249                            | 311.6                                    | 1.100                    | 875      | 9.510          | 17.99                            | 6675.3                                   | 10.36                    |
| 150      | 5.415          | 3.430                            | 338.3                                    | 1.175                    | 900      | 9.539          | 18.26                            | 6913.4                                   | 10.58                    |
| 155      | 5.576          | 3.610                            | 365.8                                    | 1.250                    | 925      | 9.561          | 18.52                            | 7152.1                                   | 10.79                    |
| 160      | 5.734          | 3.789                            | 394.0                                    | 1.327                    | 950      | 9.583          | 18.77                            | 7391.4                                   | 10.99                    |
| 165      | 5.893          | 3.968                            | 423.1                                    | 1.404                    | 975      | 9.617          | 19.02                            | 7631.4                                   | 11.20                    |
| 170      | 6.050          | 4.147                            | 453.0                                    | 1.482                    | 1000     | 9.646          | 19.27                            | 7872.2                                   | 11.40                    |
| 175      | 6.205          | 4.324                            | 483.6                                    | 1.561                    | 1025     | 9.668          | 19.51                            | 8113.7                                   | 11.59                    |
| 180      | 6.344          | 4.501                            | 515.0                                    | 1.640                    | 1050     | 9.697          | 19.74                            | 8355.7                                   | 11.78                    |
| 190      | 6.596          | 4.851                            | 579.7                                    | 1.800                    | 1075     | 9.720          | 19.98                            | 8598.4                                   | 11.97                    |
| 200      | 6.811          | 5.195                            | 646.8                                    | 1.961                    | 1100     | 9.753          | 20.19                            | 8841.8                                   | 12.15                    |
| 210      | 7.011          | 5.532                            | 715.9                                    | 2.123                    | 1125     | 9.775          | 20.41                            | 9085.9                                   | 12.33                    |
| 220      | 7.203          | 5.863                            | 787.0                                    | 2.286                    | 1150     | 9.807          | 20.63                            | 9330.7                                   | 12.51                    |
| 230      | 7.374          | 6.187                            | 859.9                                    | 2.448                    | 1175     | 9.820          | 20.63                            | 9330.7                                   | 12.51                    |
| 240      | 7.535          | 6.504                            | 934.4                                    | 2.611                    | 1200     | 9.860          | 21.04                            | 9822.1                                   | 12.86                    |
| 250      | 7.695          | 6.815                            | 1010.6                                   | 2.773                    |          |                |                                  |  |                          |
| 260      | 7.836          | 7.119                            | 1088.2                                   | 2.934                    | 298.15   | 8.344 ±        | 8.23 ±                           | 1396.9 ±                                 | 3.541 ±                  |
| 270      | 7.977          | 7.418                            | 1167.3                                   | 3.094                    |          | 0.014          | 0.02                             | 2.1                                      | 0.004                    |

Experimental  $C_{p,m}$  results over any part of the temperature range reported in this paper are unavailable in the literature for direct comparison. See section 4 below for a comparison of our results at  $T \leq 340$  K with those reported in the literature at higher temperatures.

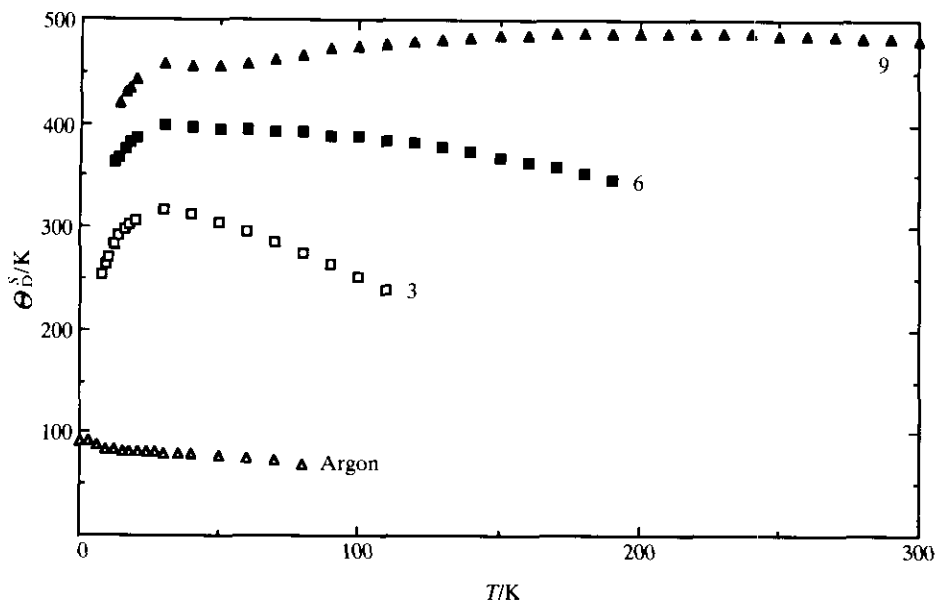


FIGURE 2. Plots of the Debye temperature  $\Theta_D^S$  against temperature  $T$  for different numbers of vibrational modes per molecule as shown for  $\text{WSi}_{2.06}$ ; that for Argon is also shown for comparison.

#### 4. Analysis and discussion

##### THE DEBYE CHARACTERISTIC TEMPERATURE $\Theta_D(T)$

When the Debye model is obeyed,  $\Theta_D(T)$  should be constant for any crystal. However, for real crystals, this model does not normally describe the experimental observations. In many diatomic lattices and metals,  $\Theta_D$  asymptotically approaches constant values at high and low temperatures and shows a minimum in  $\Theta_D$  at lower temperatures between the two extremes.<sup>(24)</sup>

The Debye temperature derived from the entropy  $\Theta_D^S(T)$  for  $\text{Ar}(\text{cr})$ <sup>(25,26)</sup> is a simple reference with which to compare  $\text{WSi}_2$  (see figure 2). The decrease in  $\Theta_D^S$  for Ar at  $T \geq 20$  K is due mainly to the expansion of the lattice. For Ar, there is no ambiguity in the choice of the number of vibrations used in the calculation of  $\Theta_D^S$ , namely three vibrations (translations) per molecule. On the other hand, when the lattice of a crystal is considered, the choice of the number of vibrations depends on which vibrations are excited in a particular range of temperature. The shape of the  $\Theta_D(T)$  against  $T$  curve for molecular crystals, when calculated on the basis of three modes per molecule, will differ from that of Ar. Advantage can be taken of this to obtain qualitative information about the form of the frequency spectrum by varying the size of the vibrating unit and then examining the curves of  $\Theta_D(T)$  against  $T$  in the different temperature regions.

The  $\Theta_D^S$  for  $\text{WSi}_2$ , calculated using the Debye model, is plotted in figure 2 based upon three conditions of vibration: three, six, and nine modes.  $\Theta_D^S$  was selected over  $\Theta_D^C$  because it is less sensitive to errors in heat-capacity, which is especially important

at higher temperatures in view of our inability to make  $(C_{p,m} - C_{v,m})$  corrections, as noted below. In figure 2,  $\Theta_D^S(T)$  for three vibrations in  $\text{WSi}_2$  rises rapidly from  $T = 3$  K and gradually flattens to a constant value over the narrow range  $29 < (T/\text{K}) < 32$ , implying that in this range the three modes of translation become fully excited in their contribution to the heat capacity. At  $T > 32$  K, the decline in the curve is due to the additional modes starting to contribute their energy to the heat capacity and to expansion of the  $\text{WSi}_2$  lattice. It is this latter feature that accounts for the drop in  $\Theta_D^S(T)$  for Ar. The  $\Theta_D^S(T)$  for the curve for six modes in  $\text{WSi}_2$  begins to flatten at  $T = 50$  K as the three librational modes become excited. At  $T \geq 75$  K, this  $\Theta_D^S(T)$  falls off as other contributions become active and the lattice expands further. Clearly, the translational and librational branches of the frequency spectrum are separated in  $\text{WSi}_2$ . At  $T \geq 170$  K, the  $\Theta_D^S(T)$  for nine modes reaches a constant value as the internal vibrational modes become fully excited. As the temperature rises above 240 K, the lattice continues to expand and the  $(C_{p,m} - C_{v,m})$  corrections become significant.

It is evident from figure 2 that the drop in  $\Theta_D^S$  at  $T < 20$  K for all the  $\text{WSi}_2$  curves makes a reliable extrapolation to obtain  $\Theta_D^S(T \rightarrow 0)$  virtually impossible. Such a drop results from the failure of the Debye model to account for our heat-capacity measurements.

#### TEMPERATURE DEPENDENCE OF $C_{p,m}$ AT TEMPERATURES BELOW 20 K

The failure of the Debye model at  $T < 20$  K noted above implies a possible contribution to the  $C_{p,m}$  from a source other than the lattice vibrations. The fact that  $\text{WTe}_2$  is known to be a conductor with interesting electrical properties<sup>(27, 28)</sup> suggests that for  $\text{WSi}_2$  an electronic term  $\gamma T$  should be incorporated along with those representing the phonons.

The quantity measured calorimetrically is  $C_{\text{sat}}$ , the heat capacity of the solid in equilibrium with the saturated vapour  $\text{Si}(\text{g})$ , where  $p(\text{Si})$  is miniscule. The background heat capacities of the vessel and helium exchange gas have been deducted from this quantity. A complete analysis of heat-capacity results over a wide temperature range requires  $C_{v,m}$ , which is related to  $C_{\text{sat},m}$  by

$$C_{\text{sat},m} - C_{p,m} = (\partial p / \partial T)_{\text{sat}} \{ (\partial H_m / \partial p)_T - V_m \}, \quad (1)$$

$$C_{p,m} - C_{v,m} = \alpha^2 V_m T / \kappa_T, \quad (2)$$

where  $\alpha = V_m^{-1} (\partial V_m / \partial T)_p$  is the isobaric expansivity,  $V_m$  is the molar volume, and  $\kappa_T = -V_m^{-1} (\partial V_m / \partial p)_T$  is the isothermal compressibility. The vapour pressure over solid  $\text{WSi}_2$  is negligible so that  $C_{\text{sat},m} = C_{p,m}$  from equation (1). It should be noted that the pressure effect of the helium exchange gas ( $p = 2.0$  kPa at  $T = 20$  K) on the heat capacity of solid  $\text{WSi}_2$ ;  $(\partial C_{p,m} / \partial p)_T$ , is also negligible. Returning to equation (2), low-temperature values of  $\alpha$ ,  $V_m$ , and  $\kappa_T$  are unavailable for  $\text{WSi}_2$  but, fortunately, at the lowest temperatures in most solids,  $(C_{p,m} - C_{v,m})$  becomes negligibly small.<sup>(29-31)</sup> Therefore, we have assumed that  $C_{p,m} = C_{v,m}$  in the low-temperature region where our analysis is focused.

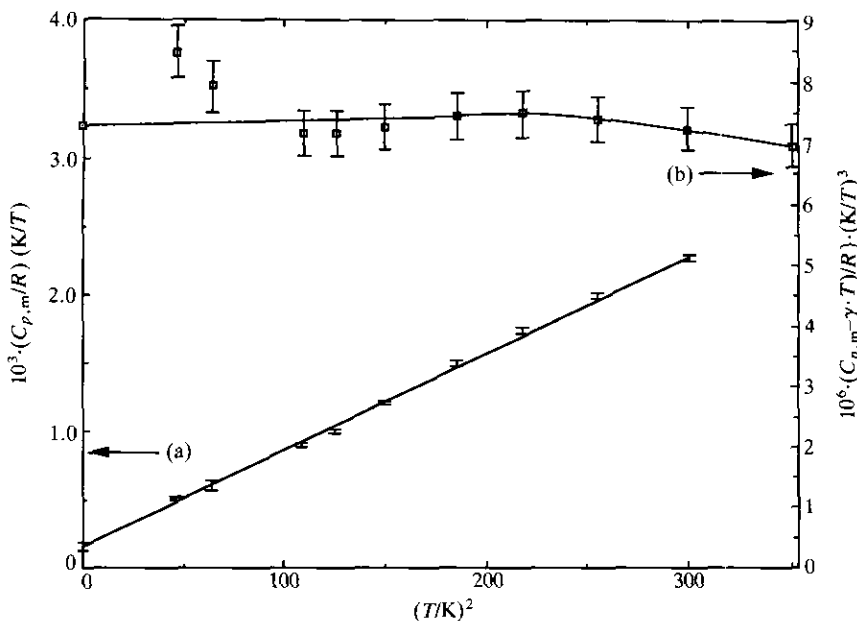


FIGURE 3. Plots of (a),  $C_{p,m}/RT$  and (b),  $(C_{p,m} - \gamma T)/RT^3$  against  $T^2$  for  $\text{WSi}_{2.06}$ . I. The vertical error bars correspond to: (a),  $20(C_{p,m}/R)(K/T)$  and (b),  $20\{(C_{p,m} - \gamma T)/R\}(K/T)^3$ .

The heat capacity at very low temperature can be described by a power series of the form:

$$C_{v,m} = \gamma T + aT^3 + bT^5 + cT^7 + \dots, \quad (3)$$

in which the coefficient  $\gamma$  arises from conduction of the electrons through the lattice<sup>(32)</sup> and the coefficients  $a$ ,  $b$ , and  $c$  are related directly to the coefficients in the corresponding power series for the frequency spectrum at low frequencies.<sup>(33)</sup> As  $T \rightarrow 0$ , the lattice heat-capacity of the solid should equal that of an elastic continuum and is described by the Debye  $T^3$  law:  $C_{v,m} = aT^3$  and  $\Theta_D^C = (12\pi^4 Nk/5a)^{1/3}$ . The  $\Theta_D^C$  is the Debye characteristic temperature derived from heat-capacity results rather than from the entropy.

A plot of  $C_{p,m}/T$  against  $T^2$  yields as  $T \rightarrow 0$  the electronic  $\gamma$  as the intercept and the coefficient  $a$  of the first lattice term as the slope. From figure 3, the resulting  $\gamma = (0.000160 \pm 0.000030) R \cdot K^{-1}$  or  $(1.33 \pm 0.25) \text{ mJ} \cdot K^{-2} \cdot \text{mol}^{-1}$  and  $a = 10^{-4} \cdot (0.606 \pm 0.018) \text{ J} \cdot K^{-4} \cdot \text{mol}^{-1}$ . As a check on the determination of  $a$ , the plot of  $(C_{p,m} - \gamma T)/T^3$  against  $T^2$  (see figure 3) yielded when  $T^2 \rightarrow 0$  an identical  $a = 10^{-4} \cdot (0.606 \pm 0.019) \text{ J} \cdot K^{-4} \cdot \text{mol}^{-1}$  as the intercept and the coefficient of the second lattice term  $b = 10^{-10} \cdot (7.85 \pm 11.57) \text{ J} \cdot K^{-6} \cdot \text{mol}^{-1}$  as the slope. Using this value of  $a$  in equation (3),  $\Theta_D^C(T \rightarrow 0) = (317.8 \pm 3.3) \text{ K}$ , which compares with 93.5 K for Ar.

Published values of the electronic molar heat capacity for related materials are scarce. For  $\text{MoSe}_2$  and  $\text{MoTe}_2$ ,  $\gamma = 0$ ,<sup>(34)</sup> but for  $\text{WTe}_2$   $\gamma = 5.99 \text{ mJ} \cdot K^{-2} \cdot \text{mol}^{-1}$ ,<sup>(35)</sup> for  $\text{WS}_2$   $\gamma = 3.6 \text{ mJ} \cdot K^{-2} \cdot \text{mol}^{-1}$ ,<sup>(36)</sup> and for  $\text{WC}_{1.01}$   $\gamma = 0.79 \text{ mJ} \cdot K^{-2} \cdot \text{mol}^{-1}$ .<sup>(37)</sup>



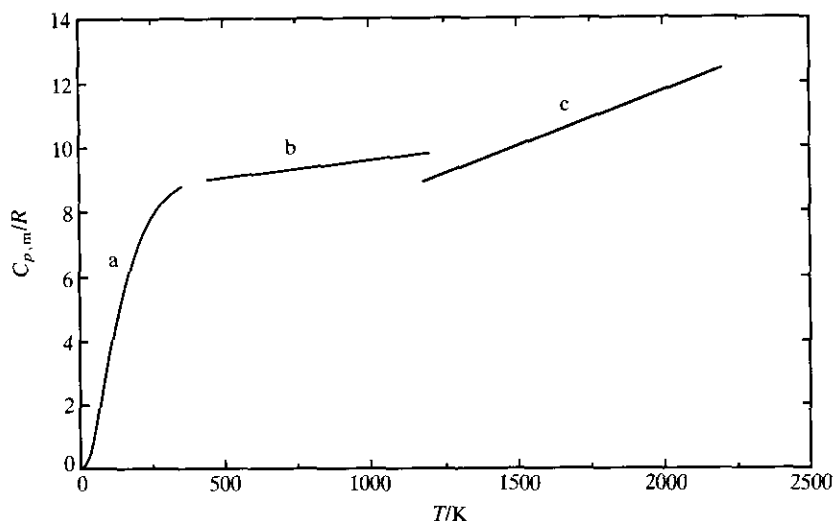


FIGURE 4. Experimental molar heat capacities  $C_{p,m}$  at constant pressure plotted against temperature  $T$  for  $\text{WSi}_{2.06}$  up to  $T = 2200$  K: a, this work; b, Mezaki *et al.*;<sup>(10)</sup> c, Bondarenko *et al.*<sup>(11)</sup>

Our value of  $1.33 \text{ mJ} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$  for  $\text{WSi}_{2.06}$  compares with  $1.3 \text{ mJ} \cdot \text{K}^{-2} \cdot \text{mol}^{-1}$  for pure tungsten.<sup>(38)</sup>

The low-temperature heat capacity of  $\text{WSi}_{2.06}$  reported in this work has led to a reliable determination of its standard molar entropy:  $S_m^\circ(\text{WSi}_{2.06}, \text{cr}, 298.15 \text{ K}) = (68.43 \pm 0.17) \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$ . Together with its standard molar enthalpy of formation at  $T = 298.15 \text{ K}$  recently reported by O'Hare<sup>(12)</sup> as  $-(80.4 \pm 4.7) \text{ kJ} \cdot \text{mol}^{-1}$ , the standard molar entropies at  $T = 298.15 \text{ K}$  for W<sup>(39,40)</sup> as  $(32.66 \pm 0.2) \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$  and for Si<sup>(41)</sup> as  $(18.820 \pm 0.2) \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$ , the standard molar Gibbs free energy of formation is calculated to be  $\Delta_f G_m^\circ(\text{WSi}_{2.06}, \text{cr}, 298.15 \text{ K}) = -(79.5 \pm 5.5) \text{ kJ} \cdot \text{mol}^{-1}$ . This compares with  $-(91.9 \pm 9) \text{ kJ} \cdot \text{mol}^{-1}$  from the Knudsen-effusion studies of Chart,<sup>(7)</sup> the uncertainty of which was criticized and revised by Chandrasekharaiah *et al.*<sup>(42)</sup> to  $-(91.9 \pm 20) \text{ kJ} \cdot \text{mol}^{-1}$ , and the estimate by O'Hare:<sup>(12)</sup>  $-(80 \pm 5) \text{ kJ} \cdot \text{mol}^{-1}$ .

#### MOLAR HEAT CAPACITY AT TEMPERATURES ABOVE 340 K

Enthalpy increments for  $\text{WSi}_2$  were determined by Mezaki *et al.*<sup>(10)</sup> using drop calorimetry over the temperature range  $461 \leq (T/\text{K}) \leq 1068$  from which  $C_{p,m}$  values were derived as

$$C_{p,m} = \{8.576 + 10.7 \cdot 10^{-4} \cdot (T/\text{K})\} \cdot R. \quad (4)$$

Their extrapolation at  $T < 461 \text{ K}$  yielded  $C_{p,m} = 8.897 \cdot R$  at  $T = 300 \text{ K}$ , which lies above the value of  $8.363 \cdot R$  of this work. A plot of their  $C_{p,m}$  results against temperature using equation (4) permitted an extrapolation at  $T < 460 \text{ K}$  to join our results smoothly at  $T = 340 \text{ K}$  as shown in figure 4. The reproducibility of the  $C_{p,m}$

results of Mezaki *et al.* is no better than  $10^{-2} \cdot C_{p,m}$  and the uncertainty may be about  $4 \cdot 10^{-2} \cdot C_{p,m}$ , since their material was of industrial grade and was used without further purification. Nevertheless, the smooth connection of their heat capacities with those of this work justify their inclusion and preparation of thermodynamic functions up to  $T = 1200$  K, which are given in table 2.

Heat-capacity results for  $\text{WSi}_2$  derived from drop calorimetry have also been reported by Bondarenko *et al.*<sup>(11)</sup> but over the temperature range  $1173 \leq (T/\text{K}) \leq 2113$ . The results from their equation:

$$C_{p,m} = \{4.125 + 37.094 \cdot 10^{-4}(T/\text{K}) + 7.0527 \cdot 10^5(\text{K}/T)^2\} \cdot R, \quad (5)$$

are also plotted in our figure 4 where it is evident that the curve defined by their  $C_{p,m}$  values does not join smoothly with either the curves defined by Mezaki *et al.*<sup>(10)</sup> at  $T < 1200$  K or with the results of this work at  $T < 350$  K. Therefore, the thermodynamic functions listed in table 2 are not extended to  $T > 1200$  K.

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