Intermittent bonding for high toughness/high strength composites

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High strength and high toughness are usually mutually exclusive in brittle filament/brittle matrix composites. The high tensile strength characteristic of strong interfacial filament/matrix bonding can, however, be combined with the high fracture toughness of weak interfacial bonding, when the filaments are arranged to have alternate sections of high and low shear stress (and low and high toughness). Such weak and strong areas can be achieved by appropriate intermittent coating of the fibres. The strong regions ensure that the filament strength is picked up; weak areas randomly in the path of running cracks serve to blunt them by the Cook/Gordon mechanism which, in turn, produces long pull-out lengths with an associated large contribution to toughness. Boron-epoxy composites of volume fraction 0.20 to 0.25 have been made in this way which have fracture toughnesses of over 200 kJ m⁻², whilst retaining rule of mixtures tensile strengths (~ 650 MN m⁻²). At the volume fractions used, this apparently represents $K_{IC}$ values greater than 100 MN m⁻³/².

An analysis is presented for toughness and strength which demonstrates, in broad terms, the effects of varying the coating parameters of concern. Results show that the “toughness” of interfaces is an important parameter, differences in which may not be shown up in terms of interfacial “strength”. The choice of coating material is crucial in getting the desired effect.

Some observations are made upon methods of measuring the components of toughness in composites.

1. Introduction
Fracture in brittle matrix/brittle filament composites where the interfacial bond between fibre and matrix is strong often results in a fast matrix crack perpendicular to the filaments. Usually such an energetic crack breaks through all filaments in the path of the crack and complete fracture ensues. Even though shear debonding, of average length $l_{crit}/4$, may occur during fracture since the filaments will not necessarily break in the plane of a matrix crack, the associated “surfaces” contribution to toughness will be relatively limited because $l_{crit}$ is itself small [1]. Similarly, the contribution to toughness from Piggott/FitzRandolph stress redistribution [2, 3] is limited by the critical length, as is that from Cottrell/Kelly pull-out [4].

A general increase of $l_{crit}$ by lowering the filament/matrix shear bond will increase toughness, as discussed by Marston et al. [1]. In that paper, it was shown that a relationship between strength ($\sigma$) and total composite toughness ($R$) could be developed by recognizing that in general terms $R = \sigma l_{crit}/\tau$ where $\tau$ is the shear strength of the interfacial bond. In the case of the boron/epoxy system for which data were presented in [1], the surface condition of the as-received B/W filaments was such that when made up into composites with EPON-828 epoxy, strengths in the region of the rule of mixtures (RoM) value were attained. When the surface condition was altered by continuously coating the filaments with various substances, the strengths fell off and the toughness decreased (with strong interfaces), or increased (with weak interfaces). In the latter case, if the interfaces were sufficiently weak, there could be the possibility of introducing an additional contribution to toughness, namely Cook/Gordon tensile debonding ahead of the crack [5]. Such a mechanism, which is usually absent in conventional strongly bonded com-
posites, may blunt and slow down cracks or arrest them completely.

However, weak interfaces throughout the composite can reduce the tensile strength quite significantly. Depending on the circumstances, perhaps 1 MN m\(^{-2}\) in tensile strength is “lost” for every 1 kJ m\(^{-2}\) “added” to toughness in laboratory testpieces; this follows from Equation 16 of [1] applied to boron/epoxy. The question that presents itself is whether there are any means by which the RoM tensile strength can be maintained along with high toughness values.

Marston [6] suggested that providing there were “enough” regions of high interracial shear stress to ensure that the rule of mixtures strength was picked up, the rest of the composite could have quite weak interracial bonds. Were such a composite to be laid up randomly with respect to weak and strong regions, both high strength and high toughness should be produced simultaneously. For if the lengths of the strongly bonded regions are greater than the critical length associated with that strong interracial \(\tau\), the filament strength would be attained, whilst at the same time, those weak interfaces situated randomly ahead of any running cracks would serve to blunt the cracks by debonding. The concept is shown schematically in Fig. 1.

![Figure 1](image)

**Figure 1** The intermittent bond and Cook/Gordon debonding.

Weakly and strongly bonded interfaces can be achieved by intermittently coating the filaments with some suitable substance before composite lay up.

How interfacial properties other than shear strength are affected by the coating procedure is an interesting and vital question, because it is probably the “toughness” of the interface that is of ultimate concern rather than the “strength”. The tensile debonding envisaged by Cook and Gordon is fracture in mode I of fracture mechanics nomenclature*; the shear debonding implicit in the Outwater/Murphy analysis for toughness is fracture in the “forward sliding” mode II. The difference in modes was not clearly brought out in [1]. Each mode has its own toughness, \(R_I\) and \(R_{II}\), the explicit relationships of which to interfacial tensile and shear strengths are not obvious. Results for silicone vacuum grease (SVG) and polyurethane varnish (PUV) coatings are reported later in this paper. The uncoated regions have high interracial shear stress and the coated regions are “weak”, (being reflected in the relative transfer lengths). However, the SVG increased the toughness only modestly, whereas the PUV increases the toughness markedly; respectable tensile strengths were maintained with both coating materials. This emphasizes that the coating material is crucial, and revolves around the ill-understood Interracial toughness properties of the coatings.

An analysis for the strength and toughness of intermittently bonded brittle filament/brittle matrix composites is presented in the next section. The experimental results show quite strikingly that when appropriate coating materials are employed, strong, high toughness composites can be manufactured in the manner suggested [8].

### 2. Mathematical model

The following analysis is a modification of the treatment presented in [1]. Details of the derivations are given in the Appendix. The broad assumptions are that in a randomly laid up, intermittently bonded composite, the coated and uncoated regions of interracial shear strengths \(\tau_c\) and \(\tau_{uc}\), may be represented by a rule of mixtures average shear strength \(\tau_{av}\) given by

\[
\tau_{av} = (1 - C)\tau_{uc} + C\tau_c
\]

*The Roman mode types are used here in the fracture mechanics Volterra dislocation sense, not in the nomenclature suggested by Mullin et al. [7], for different types of fracture observed in boron/epoxy systems.*

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where $C = l_c/l_r$, i.e. the ratio of coated length to repeat distance (see Fig. 2) and $T = \tau_c/\tau_{uc}$.

Figure 2 Intermittent bond geometry.

The “fictitious” critical length of the intermittently coated filaments is then given by

$$l_{crit}(\tau_{av}) = \frac{\sigma_f d}{2\tau_{av}}$$

$$= \frac{l_{crit}(\tau_{uc})}{1 - C(1 - T)}$$

$$= \frac{1}{1 - C(1 - T)} \frac{\psi \lambda d}{\psi (1 - C(1 - T))}$$ (2)

where $\sigma_f$ is the filament tensile strength, and $d$ the filament diameter. The useful non-dimensional parameters are $\psi = l_{crit}(\tau_{uc})/l_r$, $\lambda = l_r/d$.

In the same manner, we postulate the use of an average interfacial mode II toughness, to represent the behaviour of adjacent regions of low and high toughness, given by

$$(R_{II})_{av} = (1 - C)(R_{II})_{uc} + C(R_{II})_{c}$$

$$= (1 - C)(1 - \rho_{II})$$ (3)

where $(R_{II})_{uc}$ and $(R_{II})_{c}$ are the uncoated and coated interfacial toughnesses, and $\rho_{II}$ is the ratio $(R_{II})_{c}/(R_{II})_{uc}$. It is arguable that this average should be weighted to take into account the instance of a crack growing in a non-bonded region, for example, and then propagating some distance into the well-bonded region before being arrested. The RoM approach has been taken for simplicity.

The foregoing type of toughness average is not used for mode I debonding, since cracking will not take place in the strong regions according to the Cook/Gordon model. The symbol $\rho$ for $(R_{II})_{c}/(R_{II})_{uc}$ is, however, used later.

2.1. Tensile strength

For intermittently bonded filaments, the fibre load build-up may take place at low or high interfaces, or indeed over both types of interface, as shown schematically in Fig. 3. With the use of $\tau_{av}$ to account for the different interfacial shear strengths, we can write for the RoM tensile strength

$$\sigma = (1 - \psi)\sigma_m + \psi \sigma_f \left[ 1 - \frac{\sigma_f d}{4\tau_{av} L} \right]$$

$$= (1 - \psi)\sigma_m$$

$$+ \psi \sigma_f \left[ 1 - \frac{\psi}{2n \{1 - C(1 - T)\}} \right]$$ (4)

where $\psi$ is the filament volume fraction, $\sigma_m$ the matrix tensile strength and $L$ the finite size of the testpiece or length of the filament. The non-dimensional parameter $n$ is given by $L/l_r$.

For $C = 0$, Equation 4 degenerates to the expression for continuously coated filaments [1]. At $C = 1$ (and therefore $T = 1$), the (lower) RoM tensile strength appropriate to the (lower) $\tau_c$ is given. Note that at large $C$, the uncoated length is shorter than its own uncoated critical length, thus reducing its shear transfer potential, and thus contributing to the fall in $\sigma$ with $C$. It may be shown from Equation 1 that the value of $C$ at which this occurs is given by

$$C > \frac{2 - \psi}{2(1 - T)}$$

at which time more than one repeat distance is required to get the filament stress up to $\sigma_f$ (Fig. 3). The upper bound to $\sigma$ is the uncoated RoM value itself, when load transfer happens to occur over regions of (large) $\tau_{uc}$, providing that they are as long as their own critical length.

2.2. Fracture toughness

According to [1] the total toughness, for continuously coated filaments, is given by

$$R_{total} = R_{surfaces} + R_{redist} + R_{pull-out}$$ (6)

where $R_{surfaces}$ related to debonding (mode II), $R_{redist}$ relates to Piggott/Fitz-Randolph stress redistribution (or relaxation), and $R_{pull-out}$ relates to Cottrell/Kelly pull-out.

An additional component, $R_{Cook/Gordon}$, must be added to Equation 6 if tensile debonding ahead of the running crack takes place. It turns out that the Cook/Gordon mechanism itself is a comparatively small toughness sink; however, the associated additional debond lengths in the presence of Cook/Gordon debonding significantly increase the pull-out lengths and hence the total toughness. Using Equations 1 and 2, and other assumptions detailed in the Appendix, expressions may be obtained for the total
toughness of intermittently bonded composites, by adding the various contributions from "surfaces", Piggott/Fitz-Randolph stress redistribution, Cottrell/Kelly pull-out and Cook/Gordon mode I debonding (when acting). The final expression is rather cumbersome and is left to the Appendix. A physical picture of what governs each contribution is forthcoming in Section 4.

3. Testpieces and experimental results

Tensile and toughness specimens were made from layers of intermittently bonded epoxy composite tape manufactured on a drum apparatus with a device for coating the filaments before lay-up (Fig. 4). The tape is similar to Avco proprietary the repeat distances are not multiples of the drum circumference, alternate coated and uncoated regions are presented to a running crack; additionally test specimens consisted of many layers of tape, again helping the random lay-up concept. Tapes are stored in a refrigerator with the epoxy in the half-cured B-stage, complete curing (12 h at 120°C followed by oven cooling) taking place after specimens consisting of various layers have been made.

To investigate the intermittent bond analysis, tapes were manufactured for a range of values of $\psi$, $\lambda$ and $C$. The principal coating materials were silicone vacuum grease (as used by Marston [6] in his preliminary experiments) and polyurethane varnish. The repeat distances ($l_f$) were variously 19, 25.4 and 51 mm which gave 0.05 $\sim \psi$ $\sim$ 0.13, and 135 $\sim \lambda$ $\sim$ 360. Independent tensile tests of 100% coated specimens suggested that $T = 0.06$ (silicone vacuum grease) and $T = 0.05$ (polyurethane). The toughness ratios $\rho$ were not known independently, but values can be inferred from the experimental data, as discussed later.

Tensile and toughness specimens were made from the same tape for a given combination of parameters. The tensile specimens consisted of 2 layers of the tape, in 100 mm $\times$ 6 mm strips, with end tabs reinforced by additional layers of tape. Marston et al. [1] measured composite

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toughnesses using Tattersall and Tappin three-
point bending "roof" specimens [9]. To make
comparison with the earlier data, some 5 mm ×
5 mm × 35 mm Tattersall and Tappin specimens
were made up from the tapes, but for reasons
explained later, most toughness measurements
in the present series were made on flat sheet
dge-crack specimens, akin to ASTM "compact
tension" specimens in profile [10]. These
consisted of ten layers of tape in 76 mm × 76
mm panels as shown in Fig. 5. Originally it was

intended to load the specimens at section AA,
but bearing failures occurred at the holes and the
crack velocities did not allow easy visual tracking
in the less tough testpieces. Steel outriggers were
added to the specimens, which reduced both the
crack load and the crack velocity. To prevent the
composite arms above the crack from shearing
off under load, two outside layers of tape on
each side of the specimens were arranged with the
filaments parallel to the crack. The central core
of the specimen thus consisted of six unidirec-
tional filaments perpendicular to the starter
crack, where, within the limitations of the
specimen and tape preparation method, the
coated and uncoated layers occurred randomly
relative to each filament.

Fracture toughness in the edge crack specimens
was measured for increments of crack area,
using Gurney’s sector area technique [11] shown
in Fig. 6 (the crack length being monitored
during every test and the testing machine load
extension trace “pipped” accordingly. Since
Gurney’s method does not involve a “compliance
calibration”, the alteration of specimen com-
pliance, caused by the out-riggers, is incon-
sequential. Separate tests showed that the

matrix work of fracture in the outside layers of
tape did not contribute significantly to the
toughness. The load/extension plots showed
some curvature before crack propagation
especially in the high percentage coated samples.
Upon unloading, after some crack propagation,
the tougher testpieces showed marked “displace-
ment irreversibility”, i.e. the specimen cracks
remained “open”. Although geometric inter-
ference of filaments still bridging the crack
obviously contributed to this effect, the question
arises as to whether generalized yielding has
occurred. Irreversibility at regions remote from
the crack faces is a bane of fracture toughness
testing of high toughness/low strength solids. If
specimens are saw-cut along the crack into
virgin material beyond the crack tip “plastic
zone” and they subsequently close up, it may be
assumed that all irreversible work has been
confined to areas contiguous with the crack
faces. Then the whole area under the load/
extension plot may be attributed to work of
fracture. Most of our specimens did close up.
However, in the highest percentage PUV coated
specimens, it was difficult to propagate cracks at
all, and buckling delamination at the back face
of the testpiece, or shear deformation along
planes perpendicular to the crack in the specimen
“arms”, terminated the experiments. Hence the

\[ R(A_3 - A_2) \]

Figure 5 Edge-crack fracture toughness specimen.

Figure 6 Gurney’s sector area method for \( R \). Radial lines
from the origin represent constant crack areas (or lengths).
During propagation, the fracture work required to
advance the crack from area \( A_2 \) to \( A_3 \), for example, is
given by the hatched area, of magnitude \( R(A_3 - A_2) \),
where \( R \) is the fracture toughness.
toughness values at the highest percentage coatings in PUV edge-crack specimens are not known with confidence, but the quoted values if anything are perhaps low.

The toughness data from the Tattersall and Tappin PUV testpieces did not show these effects. They did, however, display a curious behaviour, with the toughness values levelling off after about $C = 0.5$, rather than carrying on rising at large $C$. These effects are discussed later.

Tensile and edge-crack fracture toughness results for both silicone vacuum grease and polyurethane coatings are plotted against $C$ in Figs. 7 and 8. The tensile data remains at or about the RoM value until $C$ becomes greater than 0.8. The fall in $\sigma$ at very large $C$ is anticipated from the analysis in Section 3.

The toughness results with silicone vacuum grease coating fall slightly with increase of $C$, but beyond $C = 0.4$, $R$ becomes modestly greater than the “completely uncoated” (i.e. $C = 0$) case. The edge crack and Tattersall and Tappin data all essentially agree: for $v_l = 0.25$, and $C = 0$, $R = 45$ to 50 kJ m$^{-2}$; for $C = 1.0$, $R = 60$ to 65 kJ m$^{-2}$.

In contrast, the polyurethane coatings gave marked improvements in toughness for increased percentage coating. In the edge-crack specimens, with $v_l = 0.25$, toughnesses about 100 kJ m$^{-2}$ are produced for $C = 0.5$, and values around 250 to 300 kJ m$^{-2}$ occur at large $C$. As previously mentioned, these latter toughness values may not be precise. The Tattersall and Tappin data levelled out at some 110 kJ m$^{-2}$ for all $C > 0.5$, which suggests that one or more components of the toughness in the edge-crack specimens at large $C$, failed to contribute to cracking in the three-point beam bending situation.

To have some feel for the interfacial shear stresses active during pull-out, some of the “used” edge-crack specimens that were partially cracked through were regripped above the original uncracked portion and pulled in tension. After the crack had propagated across the relatively narrow section, and the crack faces had separated, the work subsequently performed in pulling the fibres out was measured from the testing machine chart. Some of the fibres had already been broken in the original edge-crack tests, and the remainder were broken when the crack faces were separated in these pull-out measurements. Inspection of the pull-out lengths enabled estimates for $\tau'$ to be obtained from the expression for work in pulling out one filament over length $h$, namely

$$\tau' \pi dh.$$
PUV pull-out lengths were quite long, which helped experimentation.

During pull-out, the interfacial frictional stress for the uncoated samples was about 10 MN m\(^{-2}\), which should be contrasted with the matrix shear stress of some 70 MN m\(^{-2}\). For most of the PUV coated samples, however, the interfacial shear stress during pull-out seemed to be independent of \(C\), having the approximate value of 2 MN m\(^{-2}\). This is perhaps surprising, as one might have expected a frictional stress decreasing with increasing \(C\). The SVG data were rather inaccurate, since the pull-out lengths were considerably shorter. Later in this paper, we will see that to obtain agreement between theory and experiment for the toughness data, we would like to have \(\tau'\) constant for PUV, but varying for SVG.

Finally, to see “how tough” a testpiece could be made, some \(v_f = 0.5, C = 0.8\) tapes were manufactured and laid up into a twelve-layer 4 mm thick edge-crack specimen, with eight layers perpendicular to the crack line and four layers parallel to the crack. Instead of cracking, the testpiece “yielded” in the arms, giving the warped shape shown in Fig. 9 on unloading. No estimate for fracture toughness is thus available. We can find a bound on it, however, in the following way: Gurney and Hunt [11] and Hahn et al. [12] have shown that generalized yielding in the testpiece, rather than crack propagation, should be expected when

\[
H < \frac{(1.5 \sim 3.0) E R}{\sigma_y^2}
\]

where \(H\) is the height of the testpiece “arms”, and \(\sigma_y\) the yield strength. Using the following values with \(v_f = 0.5\), namely \(E = (0.5) (380)\) GN m\(^{-2}\), \(\sigma_y = (0.5) (3.45)\) GN m\(^{-2}\), and inserting \(H = 38\) mm, we have

\[
R > 200 \text{ to } 400 \text{ kJ m}^{-2}
\]

For reference, uncoated specimens with \(v_f = 0.5\) (such as testpieces made up from as-received Avco Prepreg tape) give \(R \sim 100 \text{ to } 120 \text{ kJ m}^{-2}\).

4. Discussion

The tensile strengths of 0.2 \(v_f\) composites with filaments fully coated with silicone vacuum grease and polyurethane varnish were about 500 and 450 MN m\(^{-2}\) respectively. The “as-received” strength with no coating was some 650 to 700 MN m\(^{-2}\). For the size of tensile testpieces used, \(\psi/n \approx 0.03 \text{ to } 0.05\). Applying Equation 4 to the fully coated samples, with \(\sigma_f = 3.45\) GN m\(^{-2}\), \(\sigma_m = 81\) MN m\(^{-2}\) and \(d = 140\) \(\mu m\), it would appear that \(T\) was about 0.06 for SVG and about 0.05 for PUV. Using these values, Equation 4 has been plotted out versus \(C\) in Fig. 7. The general agreement with experimental tensile results at various percentage coatings is reasonable.

The longest pull-out lengths that were observed after completion of the experiments to measure \(\tau'\) (the interfacial shear stress during pull-out) agreed reasonably well with \((l_{crit})_{\tau'/2}\) given by Equation 2 for SVG using \(T = 0.06\). In the case of PUV, the longest pull-out lengths were consistently greater than \((l_{crit})_{\tau'/2}\) with \(T = 0.05\). If Cook/Gordon debonding were taking place in the intermittently bonded composites, we should expect the pull-out lengths to be longer. At \(C = 0.25\), \((l_{crit})_{\tau'/2} \approx 2\) mm; with a 25 mm repeat distance, the Cook/Gordon debond length is some 6 mm so that the longest pull-out length may be expected to be about 8 mm. This was what we observed, and at the largest percentage coatings, many filaments pulled out the complete “half height” of the specimen (Fig. 10), since the pull-out lengths (incorporating Cook/Gordon debonding) should be greater than 38 mm. Although general agreement for the longest pull-out lengths was obtained, the average pull-out lengths seemed...
smaller than \((l_{crit})_{\tau_e}/4\) for SVG and smaller than \([(l_{crit})_{\tau_e}/4] + [C_{\tau_e}/2]\) for PUV. Nevertheless, the trend of pull-out lengths seemed to indicate that Cook/Gordon debonding was taking place with PUV coatings, but that it was absent with SVG. The marked difference in toughness values (although \(T\) was not very different between SVG and PUV), confirms this contention.

Comparison with the equations in the Appendix for the composite toughness is not easy to make without some handwaving about the interfacial toughness values. The matrix toughness itself, \(R_m\), may be independently determined from edge-crack or Tattersall and Tappin testpieces: for the epoxy cure cycle that was employed, \(R_m \approx 2.5\) to 3.0 kJ m\(^{-2}\). The presence of the nylon scrim cloth, in thin edge-crack specimens made up from tapes containing no filaments, had an insignificant effect. In principle, interfacial toughness in mode II can be measured by pulling on embedded filaments, but in practice the experiments are difficult to perform (the pull-out experiments described earlier for the “frictional” \(\tau'\) are, of course, different in nature since the filaments have already broken). Interfacial toughness in mode I does not seem easy to measure. It was argued in [1] that substitution of the matrix toughness for the interfacial toughness was a reasonable approximation in continuously coated composites, because if \(R_{II}(R_{II}u_e)\) in the intermittent bond context) were greater than \(R_m\), matrix material would adhere to the filaments and this was not observed experimentally. A similar postulate is used for intermittently bonded composites where, in addition, the following is suggested for \(\rho_{II}\): let us assume that the interfacial shear stress is proportional to the mode II stress intensity factor. Then the ratio of coated and uncoated shear stresses \((T)\) becomes

\[
T \approx \frac{(K_{II})_e}{(K_{II})_{u_e}} \approx \sqrt{\frac{(R_{II}u_e)}{(R_{II}u)\_e}} \approx \sqrt{\rho_{II}}.
\]

For \(T = 0.06\), \(\rho_{II} \rightarrow 36 \times 10^{-4}\) (SVG); for \(T = 0.05\), \(\rho_{II} \rightarrow 25 \times 10^{-4}\) (PUV). Equation (A2) is not sensitive to such small values of \(\rho_{II}\) over the applicable range of variables, so that it is adequate to consider \(\rho_{II} = 0\) in the toughness expressions, or cancel out the \([1 - C(1 - \rho_{II})]\) term with the \([1 - C(1 - T)]\) term (see later).

With that assumption, and with the values of \(\tau'\) obtained from the pull-out experiments for SVG and PUV, the equations in the Appendix may be plotted and compared with the toughness data. In general terms, it is readily shown that the equations, which incorporate Cook/Gordon debonding, overestimate the observed SVG results, but are in reasonable agreement with the PUV data. There are, however, some questions regarding the precise algebraic formulations of some of the components of the total toughness.

The form of the pull-out contribution relates back to the behaviour of \(\tau'\) in the pull-out experiments. In the case of PUV, a constant \(\tau'\) of some 2 MN m\(^{-2}\) seems to be required to describe the toughness results, whereas for SVG a \(\tau'\) which diminishes with increasing \(C\) is required. Such differences in \(\tau'\) behaviour were broadly observed in the pull-out tests, but the reasons are unclear. Perhaps the interfacial friction stress of the Cook/Gordon debond lengths “biases” the average \(\tau'\) down to an approximately constant value.

The magnitude of the Piggott/Fitz-Randolph contribution could be one-half of the usually quoted expression, for the following reason. The energy dissipating mechanism is irreversible relative slip between filament and matrix in the
presence of "full" interfacial bonding. In [2], the situation was modelled where the matrix fracture strain was less than the filament fracture strain, so that filaments were stretched relative to the matrix interface before they fractured (a matrix crack perpendicular to a filament having passed ahead of the filament). Irreversible work is thus performed, and when the filament "sprang back" after fracture, more work was dissipated at the interface. The distance over which slip occurs was shown to be \((l_{\text{crit}}/2)\) [2]; the "forward slip" and "back slip" contributions to toughness were the same, and equal to \(\nu_f \sigma^2 (l_{\text{crit}})/6E_f\), i.e. one-half of Equation A6 as previously quoted. If the filament fracture strain is less than the matrix fracture strain, as is the case for boron/epoxy, presumably the "forward slip" contribution is absent. The curves superimposed on Fig. 8 show both possibilities; the data favour irreversible slip only in one direction.

Thirdly, there is also a question about the magnitude of the Cook/Gordon contribution to toughness. Equation A4 gives values differing by a factor of ten, depending on the magnitude of \(p_\text{G}\), which in turn depends upon the choice of 1/5 or 1/50 for the critical tensile strength ratio (see Appendix). However, the Cook/Gordon component to total toughness itself is comparatively small, so that it is not possible, from the experimental results, to establish which value of \(p_\text{G}\) is appropriate.

It is instructive to present the magnitudes of the relative contributions to \(R\) from the various mechanisms, taking into account the foregoing questions. For PUV, with \(R_m \approx 2.6\) kJ m\(^{-2}\) \(\approx (R_{\text{II}})_{\text{m0}}, T \approx 0.045, \psi = 0.14, \lambda = 181, d = 140\) \(\mu\)m, \(\tau' = 2\) MN m\(^{-2}\) and measuring all toughness values at a crack opening of \(h = 0.5\) mm and cancelling \([1 - C(1 - \rho_{\text{II}})] \approx [1 - C(1 - T)]\), we have from Equations A2, A4, A6 and A11 for \(\nu_f = 0.25\),

\[
R = 2 + 16 + \frac{6.3(0.7 \text{ or } 1.4)}{1 - 0.955C} + (1.9 \text{ or } 19)C^2 + 45 \left(\frac{0.14}{1 - 0.955C} + 2C\right)
\]

where \(R\) is in kJ m\(^{-2}\). We see that the contribution from matrix fracture surfaces remains constant at 2 kJ m\(^{-2}\); the surfaces contribution from filament debonding also remains constant at about 16 kJ m\(^{-2}\), (after the cancelling assumption), the increase in debond area with \(C\) being counteracted by a reduction in average \((R_{\text{II}})_{\text{m0}}\).

Piggott/Fitz-Randolph stress redistribution increases with \(C\), the longer \(l_{\text{crit}}\) of higher \(C\) giving longer relative slip distances. The Cook/Gordon contribution increases as \(C^2\), (i.e. 1.9\(C^2\) or 19\(C^2\)) but in total terms is a small contributor to composite toughness. However, the increased debond lengths that accompany the Cook/Gordon mechanism produce a significant effect on the pull-out contribution, and the latter is an important part of the total toughness.

At \(C = 1\), we have

\[
R = 2 + 16 + (100 \text{ or } 200) + (2 \text{ or } 19) + (141 + 90) = 351 \text{ or } 468
\]

taking the lower and higher values of the debatable terms. Superimposed in Fig. 8 are two curves given by the foregoing treatment with high and low values as in the example for \(C = 1\). We see that in this fully coated case, the Piggott/Fitz-Randolph contribution is 100 to 200 kJ m\(^{-2}\) and the pull-out contribution is about 231 kJ m\(^{-2}\). These should be contrasted with 2 kJ m\(^{-2}\) for the matrix surfaces, 16 kJ m\(^{-2}\) from filament debonding, and 2 to 19 kJ m\(^{-2}\) from the Cook/Gordon mechanism.

For SVG, with \(T = 0.06, \tau' = 3\) MN m\(^{-2}\) (varying) and the previous values for the other parameters in Equations A2, A6 and A10 we have

\[
R = 2 + 16 + \frac{4.5}{(1 - 0.94C)} + 10
\]

where half the Piggott/Fitz-Randolph expression is used. The resulting curve for \(R\) versus \(C\) is superimposed in Fig. 8.

The Tattersall and Tappin toughness results are interesting. In some ways, this testpiece design is not completely satisfactory since there is a transition from plane stress behaviour at the apex of the triangle to plane strain at the base, so that the area under the load/extension curve indicates some ill-defined average toughness. Also, if the triangular section is made by cutting, damaged filaments near the apex also give easy crack initiation. Moreover, the testpiece is strictly unstable, (as may be demonstrated by application of Gurney's crack stability criteria [e.g. 13] to experimental compliance data),

*If the existence of Cook/Gordon debonding is doubted, it might be asked whether Equations A2, A6 and A9 with no Cook/Gordon debonding but with the full Equation A6 for the Piggot/Fitz-Randolph contribution, could satisfy the data. Such an analysis fails to agree with the experiments.*

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although with composites those broken filaments 
bridging the crack faces, after passage of the 
crack, do introduce a measure of stability 
through the pull-out contribution to toughness. 
In the present series of experiments with very 
tough composites, another effect in such small 
three-point bending situations came to light. 

In the case of SVG, the data essentially agree 
with the edge-crack results, except that the 
$C = 1$ results are low. For PUV, however, the 
results are in reasonable agreement with the 
edge-crack results only up to $C = 0.5$; after 
that, the Tattersall and Tappin data level out 
at some 110 kJ m$^{-2}$, as opposed to the edge- 

crack results which continue to increase sig- 

nificantly. It seems as if the pull-out contribution 
was being limited in some way. Very tough 
composites have large crack opening displace-
ments before and during crack propagation; 
some of our beam specimens “bottomed-out” 
in our three-point bending rig before cracking 
through, for example. This means that the 
long pull-out lengths which bridge the crack 
faces in such circumstances are bent to severe 
“exposed” radii. Engineers’ bending theory 
suggests that the top fibres in one of our 
Tattersall and Tappin testpieces, bent to a 5 mm 
radius, suffer a stress of some 5 GN m$^{-2}$. This is 
greater than the tensile fracture strength of the 
boron-on-tungsten filaments ($\sim 3.5$ GN m$^{-2}$). It 
would appear that in very tough composites a 
proportion of fibres break by bending in small 
beam specimens, thus preventing a full pull-out 
contribution to toughness. Certainly the pull-out 
lengths of high $C$ beam specimens seemed short 
in comparison with those of equivalent tensile 
or edge-crack specimens. Also, “double filament 
fractures” have been observed in the high $C$ 
PUV beam specimens, i.e. where filaments break 
inside the beam initially, but also break subse-
quently across the crack faces. Such short 
filaments may be removed with tweezers after 
completion of a Tattersall and Tappin test.

It has been pointed out earlier that filaments, 
which bridge the crack faces for some time after 
passage of the crack front, stabilize cracking. If 
some of the pull-out contribution to toughness 
is lost at large beam deflections by those 
filaments fracturing in bending, the load/ 
deflection $R$ locus plots should revert to the 
natural shape of unstabilized cracks. Fig. 11 
shows that the shape of the Tattersall and 
Tappin load/deflection plots at large displace-
ments in high $C$ PUV specimens are different 
from the corresponding shape at low $C$.

Since the diameters of typical graphite 
filaments are much smaller than boron-on-
tungsten filaments ($\sim 8$ µm versus 140 µm), the 
bending stresses induced at large deflections in 
Tattersall and Tappin testpieces made of 
carbon-polyester composites would be much 
smaller than the filament fracture stress, so that 
valid toughness data would seem to be obtain-
able.

The foregoing observations emphasise the care 
with which the pull-out contribution to tough-
ness must be treated. Although rarely acknow-
ledged in such terms, “strict” fracture mechanics 
toughness implies displacement reversibility, i.e. 
crack testpieces return to the origin of load/ 
displacement plots upon unloading. Pull-out is a 
frictional contribution to toughness, and un-
loading the specimen involves additional 
irreversible work in pushing back “down the 
holes” those filaments that bridge the crack 
faces. It can be compared with “reversed 
plasticity”. Pull-out thus has the effect of 
stabilizing cracking situations that would be 
otherwise unstable, e.g. in the Tattersall and 
Tappin testpiece.

It may be a moot point whether pull-out 
should be included in the basic description of 
toughness, since the load bearing capacity of a 
cracked structure could be reduced to negligible 
values before the full contribution of pull-out 
were realized. At the same time, pull-out does 

improve crack stability, which is important. Also, 
like it or not, pull-out will usually be part of the 
experimentally measured toughness in typical 
testpieces, although the actual contribution will 
vary with testpiece geometry and condition of 
test. Of importance to experimentalists and 
designers in the composites field must be the 
realization that the effective contribution to 
toughness from pull-out depends markedly on 
the circumstances, and each case has to be 
viewed separately.

Further questions regarding valid toughness 
testing, and associated problems of generalized 
yielding etc are discussed in a report to NASA 
[14].

5. Conclusions

The intention of this study was to produce high 
toughness composites without significant loss of 
tensile strength. This was to be achieved by 
intermittent coating of the filaments. In brittle 
 fibre/brittle matrix composites as conventionally
made with filaments of uniform interfacial properties, high strengths and high toughnesses are usually mutually exclusive.

Some success has been achieved. For example, unidirectional boron/epoxy composites have been manufactured with toughnesses of over 200 kJ m\(^{-2}\) while retaining rule of mixtures tensile strengths of some 650 MN m\(^{-2}\). The "as-received" toughness is some 50 kJ m\(^{-2}\) so at least a four-fold increase has been realized. For the volume fractions employed, this seems to represent fracture mechanics stress intensity factors of over 100 MN m\(^{-3/2}\) (Young’s modulus for boron filaments being about 380 GN m\(^{-2}\)).

The new concept which has allowed these results is the “intermittent bond”, where the special coating process produces alternate regions along the filaments of high and low interfacial shear stresses, and low and high interfacial toughnesses. Then the high tensile strength characteristic of strong interfacial bonding may be combined with the high total fracture toughness of weak interfacial bonding.

Experiments are under way to investigate the mechanical behaviour of cross-ply lay ups as practical structural materials.

Details of the microscopic mechanisms involved in the toughening process are ill-understood at present. Marston [6] used a variety of coating materials in his early experiments on intermittently bonded composites; at the time, silicone vacuum grease looked promising. Later, we were prompted to try polyurethane varnish as an intermittent coating material following the “continuously coated” paper by Mullin and Mazzio [15]. The analysis for intermittently bonded composite strength and toughness presented in this paper indicates that interfacial toughness is as significant a property in the overall behaviour as the commonly considered shear strength. The SVG and PUV results seem to indicate that similar interfacial shear strengths may not mean similar interfacial toughnesses, so that the Cook/Gordon mechanism occurs in one system but not the other. Why this should be so is not known.

Appendix. Derivations of toughness components

(1) \(R_{\text{surface}}\)

\(R_{\text{surface}}\) consists of components from filament fracture cross-sections, matrix fracture cross-sections and surfaces created by interfacial fractures. The filament cross-sectional contribution is negligible in the boron system, and we have, for random filament fracture in

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**Figure 11** Differences in unstable and stabilized Tattersall and Tappin testpiece toughness loci. Full lines represent theoretical \(R\)-loci.
untreated" composites [1],

\[ R_{\text{surfaces}} = (1 - \nu_f)R_m + \nu_f \cdot \frac{l_{\text{cr}}}{d} \cdot R_{\text{IF}} \]  

(A1)

where \( l_{\text{cr}} \) is the critical length appropriate to the (constant) \( \tau \) and \( R_{\text{IF}} \) is the fracture toughness of the interface between filament and matrix.

For intermittently coated filaments, we may use the fictitious \( l_{\text{cr}} \) of Equation 2 in Equation A1, together with the \( (R_{\text{IF}})_{\text{av}} \) of Equation 3 to give for mode II debonding,

\[ R_{\text{surfaces}} = (1 - \nu_f)R_m + \nu_f \psi \lambda \left\{ \frac{1 - c(1 - \rho)}{1 - C(l - 1)} \right\} (R_{\text{IF}})_{\text{uc}}. \]  

(A2)

Equation A2 is given as Equation 7 in the main body of text.

It should be mentioned that when the coated length is less than its own critical length, as is often the case in the experiments reported in this paper, the average debond length of coated regions is likely to be the coated length itself and not \( l_{\text{cr}}/4 \) which the derivation of Equation A1 strictly assumes; this introduces an error in the use of Equation A2.

(2) \( R_{\text{Cook/Gordon}} \)

Cook and Gordon [5] suggested that if the tensile strength of an interface ahead of a running crack were about 1/5 of the tensile strength of the matrix material, tensile debonding (mode I) would occur at the interface before the crack reached that interface. Gilliland (quoted in [16]) revised the factor to 1/50 on account of anisotropy.

Since "tensile strength" in brittle solids is a reflection of inherent flaw propagation, we may argue that

\[ \frac{(\sigma_{\text{tensile interface}})_{\text{ec}}}{(\sigma_{\text{tensile interface}})_{\text{uc}}} \approx \frac{(K_{\text{I,interface}})_{\text{ec}}}{(K_{\text{I,interface}})_{\text{uc}}} \approx \sqrt{\frac{(R_{\text{IF}})_{\text{ec}}}{(R_{\text{IF}})_{\text{uc}}}} = \sqrt{\rho_I} \]  

(A3)

where \( K_I \) is the stress intensity factor. For the \( \sigma \) ratio to be 1/5, \( \rho_I \rightarrow 4 \times 10^{-2} \); for the ratio of 1/50, \( \rho_I \rightarrow 4 \times 10^{-3} \).

If the filament coating procedure reduces the mode I interfacial toughness by such amounts, Cook/Gordon debonding should occur in "weak" regions ahead of a crack.

If there are \( N \) filaments in the plane of the crack, \( CN \) will be coated. If Cook/Gordon debonding occurs, the debond length will be about the coated length, in the sense that the mode I crack probably arrests in the adjacent uncoated regions where, presumably, the resistance to cracking in mode I is greater than for the coated region. Then, the debond area is some \( \pi d l_{\text{cr}} \) (assuming complete cylindrical debonding, i.e. "behind" filaments in the path of the advancing crack).

The work absorbed by the \( CN \) coated filaments is

\[ CN \cdot \pi d \cdot Cl_I(R_{\text{IF}})_{\text{c}} = N \cdot \pi d^2 \cdot C^2 \cdot l_{\tau} \cdot \rho(I)_{\text{uc}}. \]

But

\[ N = \nu_f \cdot \frac{4A_{\text{nom}}}{\pi d^2} \]

where \( A_{\text{nom}} \) is the total cross-sectional area in the plane of the crack.

Whence, the Cook/Gordon contribution to toughness is

\[ R_{\text{Cook/Gordon}} = \nu_f \cdot 4C^2 \cdot l_{\tau} \cdot \rho(I)_{\text{uc}}. \]  

(A4)

Equation A4 is Equation 8 in the main text. This contribution is appropriate only when

\[ \rho_I \lesssim 4 \times 10^{-2} \text{ or } 4 \times 10^{-3} \]

For such values of \( \rho_I \), Equation A4 gives a comparatively small contribution to toughness; Cook/Gordon debonding does, however, significantly increase the pull-out lengths, and hence the pull-out contribution to toughness.

(3) \( R_{\text{redist}} \)

Piggott [2] and Fitz-Randolph [3] gave essentially the following expression for \( R_{\text{redist}} \)

\[ R_{\text{redist}} = \frac{\nu_f \sigma^2}{3E_I} (l_{\text{cr}}) = \frac{\nu_f \sigma^2 d}{6E_I} \]  

(A5)

which was the form used in [1] for continuously coated filaments.

For intermittently coated systems, fracture may take place in the coated or uncoated regions. Clearly \( R_{\text{redist}} \) is enhanced by the long load retransfer lengths that follow fracture in a coated region.

If we use the average interfacial shear stress given by Equation 1 to represent the overall average behaviour, we obtain from Equation A5,

\[ R_{\text{redist}} = \frac{\nu_f \sigma^2 \psi \lambda d}{3E_I [1 - C(l - T)]}. \]  

(A6)

Equation A6 is Equation 9 in the text. For \( C = 0 \), we regain Equation A5; for \( T = 1 \), \( R_{\text{redist}} \) appropriate to \( (l_{\text{cr}})_{\text{c}} \) is given.
The energy dissipating mechanism is irreversible relative slip between filament and matrix in the presence of “full” interfacial bonding, with some occurring before filament fracture and some occurring upon filament “spring back” after fracture. Cook/Gordon debonding should not affect Equation A6, except in so far that the relative slip after debonding would probably be taking place in uncoated regions possessing \( \tau_{u0} \), rather than in some “mixed” coated and uncoated region possessing \( \tau_{av} \). A question is raised in the text about the magnitude of the Piggot/Fitz-Randolph term in those cases where the filament fracture strain is less than the matrix fracture strain.

(4) \( R_{\text{pull-out}} \)

It was thought by Marston et al. [1] that \( R_{\text{pull-out}} \) was not significant in the boron-epoxy system. A toughness contribution of some 450 kJ m\(^{-2}\) was given by the Cottrell/Kelly equation, which was considerably greater than the total measured toughness of \( \sim 35 \) kJ m\(^{-2}\). This suggested that the original interracial shear strength was not maintained during pull-out. Moreover, electron micrography of fractured boron-epoxy specimens seemed to show that matrix material had relaxed away from the filaments after debonding.

The toughness data for the intermittently bonded composites reported in this paper consistently exceeded the contributions of “surfaces” and “stress redistribution” by significant amounts (although not by the amount that would be given by direct application of the Cottrell/Kelly expression). It must be remembered that the pull-out formula as normally quoted, i.e.

\[
R_{\text{pull-out}} = \frac{2\nu \sigma d}{24\tau} \tag{A7}
\]

implies complete separation of the severed parts, with the filaments pulling right out. If the crack faces in a toughness test are bridged by filaments upon completion of the measurements, (as is often the case), “full” pull-out is not achieved, and the measured toughness will fall short of predictions. In most experiments the actual pulled-out distance of relative slip between filament and matrix is less than the “average” \( l_{\text{crit}}/4 \) for random fracture. Rather, it is of the order of the “crack opening displacement”. A modified version of the Cottrell/Kelly formula should be employed in such cases, based on the actual relative slip between filament and matrix. Although the usual formula was not appropriate, we were wrong to dismiss it completely in [1].

It may be shown that

\[
R_{\text{pull-out}} \approx \frac{2\nu \sigma'}{d} [2Dh - h^2] \tag{A8}
\]

where \( D \) is the average distance from the end of the fractured filament to the plane of gross fracture (Fig. 12) and \( h \) is the pulled-out relative slip distance. \( \sigma' \) has been written in place of the interfacial shear stress \( \tau \) alone, as experiments seem to indicate that a lower “frictional” interfacial traction acts after filament fracture. Putting \( D = h = l_{\text{crit}}/4 \) in Equation A8 will not give the usual expression as in Equation A7 because of the integration averaging method used for pull-out [4].

In intermittently coated composites, different \( D \) are appropriate for filament fractures in coated or uncoated regions, and also for those cases where Cook/Gordon debonding additionally takes place. Also, the value for the interfacial friction stress \( \sigma' \) has to be known. It was thought that \( \sigma' \) would vary with \( C \), in the sense that if the frictional traction during pull-out was perhaps some constant fraction of the interfacial shear stress before debonding, then \( \sigma' \) should decrease with \( C \), as \( \tau_{av} \) decreases with \( C \) (Equation 1). However, pull-out experiments which attempted to measure \( \sigma' \) suggested that \( \sigma' \) was constant with one of the coatings, but perhaps varied with the other. Thus, two possibilities are presented in what follows.

In the absence of Cook/Gordon debonding,
we may use \((l_{crk})_{crit}/4\) for \(D\). Noting that for typical crack opening displacements, (a few mm), the \(2h^2/d\) term may be neglected, we have from Equation A8

\[
R_{\text{pull-out}} = \frac{\nu_\tau \tau \psi h}{[1 - C(1 - T)]}. \quad (A9)
\]

If \(\tau\) varies according to \(\tau_0'[1 - C(1 - T)]\), we obtain the simple result that the pull-out contribution to total toughness, measured at the same crack face opening \(h\), is constant and equal to

\[
R_{\text{pull-out}} = \nu_\tau \tau_0' \psi h. \quad (A10)
\]

When Cook/Gordon debonding occurs, \(D\) given by \(l_{crit}/4\) is augmented by an approximate debond length \(Cl_\tau/2\), (half the total debond length on one side of the plane of gross fracture). So, neglecting the \(2h^2/d\) term,

\[
R_{\text{pull-out}} = \nu_\tau \tau_0' \psi h \left(1 - C(1 - T)\right) + 2C \quad (A11)
\]

and if \(\tau = \tau_0'[1 - C(1 - T)]\)

\[
R_{\text{pull-out}} = \nu_\tau \tau_0' \psi h [\psi + 2C(1 - C(1 - T))]. \quad (A12)
\]

(5) Total toughness

The total toughness of intermittently bonded composites is obtained by adding up the separate appropriate contributions given by the various Equations A2, A4, A6, A9 to 12. For all expressions, with \(C = 0\), we obtain the formula for total \(R\) for continuously coated or uncoated filaments given in [1], with the addition of a pull-out term. This is, of course, the consequence of using the average \(\tau\) given by Equation 1 in the uncoated formula of Marston et al. [1].

Note that questions are raised in Section 4 regarding the magnitudes of the different contributions to total toughness.

It should also be noted that Equations A2 and A4 seem to indicate paradoxically that the greatest \(R\) would come from the largest values of \(\rho\) (i.e. increased interfacial coated toughness). The Cook/Gordon expression however only applies when \(\rho\) is very small, and in the case of Equation A2 the implication of large toughness comes about from the fact that, on average, every filament fracture is accompanied by a debond length of \(l_{crit}/4\), so that if the coated critical lengths are long (because of low \(\tau_0\), the tougher the interface the better. But some filament fractures will have zero debond length, and these are the ones that set up energetic matrix cracks which clearly will not be arrested by tough interfaces in their path.

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