Filling the Gaps: Spatial Interpolation of Residential Survey Data in the Estimation of Neighborhood Characteristics

Amy H. Auchincloss,* Ana V. Diez Roux,* Daniel G. Brown,† Trivellore E. Raghunathan,‡ and Christine A. Erdmann*

Abstract: The measurement of area-level attributes remains a major challenge in studies of neighborhood health effects. Even when neighborhood survey data are collected, they necessarily have incomplete spatial coverage. We investigated whether interpolation of neighborhood survey data was aided by information on spatial dependencies and supplementary data. Neighborhood "availability of healthy foods" was measured in a population-based survey of 5186 persons in Baltimore, New York, and Forsyth County (North Carolina). The following supplementary data were compiled from Census 2000 and InfoUSA, Inc.: distance to supermarkets, density of supermarkets and fruit and vegetable stores, housing density, distance to a high-income area, and percent of households that do not own a vehicle. We compared 4 interpolation models (ordinary least squares, residual kriging, spatial error regression, and thin-plate splines) using error statistics and Pearson correlation coefficients (r) from repeated replications of cross-validations. There was positive spatial autocorrelation in neighborhood availability of healthy foods (by site, Moran coefficient range = 0.10-0.28; all P < 0.0001). Prediction performances were generally similar for the evaluated models (r ≈ 0.35 for Baltimore and Forsyth; r ≈ 0.54 for New York). Supplementary data accounted for much of the spatial autocorrelation and, thus, spatial modeling was only advantageous when spatial correlation was at least moderate. A variety of interpolation techniques will likely need to be utilized in order to increase the data available for examining health effects of residential environments. The most appropriate method will vary depending on the construct

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- From the *Department of Epidemiology, School of Public Health; †School of Natural Resources and Environment; and ‡Department of Biostatistics, School of Public Health, University of Michigan, Ann Arbor, Michigan.
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- Correspondence: Amy H. Auchincloss, Department of Epidemiology, School of Public Health, University of Michigan, 1214 South University 2nd floor, Ann Arbor, MI 48104. E-mail: aauchinc@umich.edu.
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of interest, availability of relevant supplementary data, and types of observed spatial patterns.

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G rowing evidence supports the concept that residential neighborhoods play a role in determining individual behaviors that are linked to health outcomes.^{1–3} However, there is a scarcity of relevant data for characterizing neighborhoods that continues to challenge researchers. One option for obtaining information on neighborhoods is to conduct surveys of residents who can provide information about their residential environment. However, survey data necessarily have incomplete spatial coverage. Routinely collected data such as census data have complete coverage but may not provide direct measures of the construct of interest.

Geologists and other natural scientists have used geostatistical methods to interpolate when there is incomplete spatial sampling^{4–7} and have used supplementary data at colocated sites to try to improve predictions at the unsampled locations.^{8,9} While spatial modeling in itself may predict reasonably well, supplementary data that are well-correlated with the primary data should improve prediction over and above models of spatial variation alone.

We investigated the utility of spatial interpolation methods to obtain estimates of neighborhood characteristics (specifically "availability of healthy foods") at unsampled locations. We also explored the extent to which spatially complete (and colocated) supplementary data improved the prediction of neighborhood characteristics at unsampled locations. Our hypotheses were: there is positive spatial autocorrelation in the availability of healthy foods in our study sites; supplementary data yield a superior prediction compared with models that do not use these data; and use of spatial information (ie, spatial correlation or conditioning on location) will improve prediction over models that do not incorporate spatial information. Finally, we compared prediction results to determine the best model for predicting the neighborhood characteristic (availability of healthy foods) for our 3 study sites.

METHODS

Data

Sources of data used in these analyses are listed in Table 1. The primary survey data came from the Community

TABLE 1. Distribution of "Availability of Healthy Foods" Scale and Area Characteristics by Study Site Using Data From the Community Survey (n = 5186), 2004, InfoUSA 2003, and Census 2000

			Baltimore	Forsyth Co.	New York	
	Ν	Study area dimensions: o. of Community Survey respondents:	36 km × 20 km 1587	42 km × 32 km 1493	28 km × 11 km 2106	
Original Data Source	Type of Data	Computed Variables	Distribution of Variables for Community Survey Respondents Median (25th–75th percentile)			
Community Survey, 2004	Survey scale	"Availability of healthy foods"*	3.52 (2.56-4.06)	3.40 (2.43–4.03)	3.76 (3.03–4.24)	
InfoUSA, Inc., 2003	Food stores	Distance to supermarkets (km) [†]	0.95 (0.58-1.46)	1.68 (1.04-2.51)	0.30 (0.18-0.48)	
		Number of supermarkets and fruit/ vegetable stores combined within a 1.6 km [‡]	2 (1–4)	0 (0–1)	18 (12–25)	
Census, 2000	Other area	Housing density within 1.6 km [§]	9200 (5000-14,300)	1800 (1000-2900)	72,300 (57,500–94,800)	
	characteristics	Distance to high-income area (km) [¶]	1.69 (0.59–3.35)	2.14 (0.41-5.84)	0.32 (0-1.1)	
		Average percent of households within a 1.6 km area that do not own a vehicle	20% (8%-35%)	5% (3%-8%)	73% (69%-76%)	

*"Availability of healthy foods" scale was based on the mean for: (1) "A large selection of fresh fruits and vegetables is available in my neighborhood;" (2) "The fresh fruits and vegetables in my neighborhood are of high quality;" and (3) "A large selection of low-fat foods is available in my neighborhood." Survey estimates were weighted to account for differential probabilities of selection into the sample; estimates were also adjusted for age and sex.

[†]Euclidean distance from the survey respondent's residence to the nearest supermarket. There were 85 supermarkets in Baltimore, 38 in Forsyth Co., and 87 in New York. [‡]There were 116 supermarkets plus fruit/vegetable stores in Baltimore, 43 in Forsyth, and 186 in New York.

[§]Census block group housing units were apportioned over the area of the block group and then summed across a 1.6-km buffer.

¹Euclidean distance to a high-income area defined as a block group in the top 10th percentile of US per capita incomes (\$33,000).

Survey, a population based random-digit-dialing telephone survey.¹⁰ Data were collected in 2004 from 5988 residents in Baltimore City/County, Maryland; Forsyth County, North Carolina; Northern Manhattan and Bronx, New York. While the Forsyth site was the most rural of the 3 sites, it did include the cities of Winston-Salem and Kernersville. The Community Survey collected information on a number of neighborhood-level domains potentially related to cardiovascular disease, including neighborhood "availability of healthy foods" which was a scale derived from the mean participant score on 3 items (Table 1 footnote). Participants were asked to report on the area within 1 mile (1.6 km) from their home and to choose from Likert-responses that ranged from 1 = strongly disagree (unfavorable) to 5 = strongly agree (favorable). Both scale internal consistency and test-retest reliability (2 weeks postsurvey) were acceptably high (Cronbach's alpha = 0.78; test-retest = 0.69).¹⁰ Survey estimates were weighted to account for the differential probabilities of selection into the sample. Survey estimates also were adjusted for age and sex to account for reporting differences by age or sex. We used the adjusted healthy food scale in all analyses. Among 5988 participants, 325 were excluded because of missing data, and 477 survey scores for respondents living within 29 m of each other were averaged together (because geostatistical procedures require that distances between observations not approximate zero and because raster cell size was 20 m²), thus, leaving 5186 observations for these analyses.

Potential predictors of availability of healthy foods included 2003 food store data extracted from InfoUSA, Inc.,¹¹ and 2000 US Census block group data.¹² We selected supplementary data a priori based on theory and empirical

relations found in prior work. Food stores were identified based on Standard Industrial Classifications in the InfoUSA data.¹³ Because supermarket proximity has been related to availability of healthy foods,^{14,15} supermarket location was used in 2 measures: distance to supermarkets and density of supermarkets. Supermarket density also included retail fruit and vegetable stores because these stores also may contribute to the availability of healthy foods. Census-derived data included housing density, percent of households without a vehicle, and distance to a high income area. We included housing density because it may be positively related to availability of food resources. Vehicle data were included because automobile transport may influence perceived availability of healthy foods.^{16,17} In addition, both vehicle and housing variables capture city and suburban differences in food availability. High income areas were included because they have been associated with greater availability of healthy foods.¹⁸ Estimated grids (using a 20 m² cell size) were computed from the supplementary data, and grid values were extracted for survey respondents' residential addresses (latitude, longitude).

Statistical Analysis

Analyses were done separately for each study site. Models fit to the healthy food scale at surveyed points were used to predict availability of healthy foods at unobserved locations. We used model-fit statistics and estimates of regression coefficients from ordinary least squares to evaluate the importance of supplementary data (also referred to as "covariate" information) in predicting food availability.

Semivariograms (described below) and the Moran coefficient¹⁹⁻²¹ were used to describe/quantify spatial auto-

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correlation among original survey values and among ordinary least squares residuals. Four types of prediction models were fit in order to assess the impact of different ways of modeling the spatial correlation in the data. Each of the 4 models is briefly described below. Models were fit both with and without covariates to contrast prediction performance when supplementary data were added to spatial information.

Model 1 Parametric Mean and Independent Covariance—Fitted With Ordinary Least Squares

We selected ordinary least squares, a widely-used method for aspatial prediction, to assess whether covariate information applied in a global aspatial regression model would be sufficient for prediction. Ordinary least squares was the benchmark to which all other models were compared. Using k covariates (X) at locations not sampled (j), unbiased predicted values for unobserved Y were derived by applying mean Y (intercept, μ) plus the regression coefficients (β) obtained when Y was observed. This is illustrated by:

$$\hat{Y}_{j} = \hat{\mu} + \sum_{k=1}^{n} \hat{\beta}_{k} X_{jk}.$$
(1)

Model 2 Spatial Covariance—Fitted With Residual Kriging

If "availability of healthy foods" is spatially autocorrelated and covariate information does not fully account for that pattern, then using spatial dependencies in the data could benefit prediction. We applied residual kriging to assess whether global aspatial prediction by ordinary least squares would be improved by local spatial information remaining in the residuals. Kriging is a spatial interpolation method widely used by geologists and natural scientists, though relatively infrequently used in epidemiology.^{22–24} Kriging utilizes a weighted linear combination of the available data to obtain an exact best linear unbiased predictor.^{4,7} In model 2, predictions for unsampled locations were obtained by adding together predicted values from ordinary least squares regression and predicted values obtained from ordinary kriging of the regression residuals, illustrated in simple form as:

$$\hat{Y}_j + \hat{\varepsilon}_j$$
 where $\hat{\varepsilon}_j = \sum_{i=1}^n w_i \varepsilon_i$. (2)

 $\hat{\varepsilon}_j$ is the ordinary least squares residual predicted at unsampled location *j*; *n* is the number of sampled (nearby) residuals (ε_i) that participate in the estimation; and w_i are their weights with the constraint that all weights sum to 1 (so as to be unbiased and minimize the mean square prediction error). In order to obtain the weights, ordinary kriging requires prespecification of both a functional form for spatial dependence and the associated parameters for spatial continuity. We used semivariograms (regular and robust),^{5,25} which plot the covariation of the healthy foods scale as a function of geographic distance between sampled pairs, to

investigate the most appropriate functional form for these data. To derive a smoothed plot, semivariogram values were binned into intervals (lag-size). To ensure that bins had sufficient data, in each bin $\geq 80\%$ of surveyed participants were paired with at least one other participant. Model parameters for spatial continuity were derived by noting the distance at which samples ceased to be positively correlated (the spatial "range"), the maximum covariation between samples (the "sill"), and semivariogram values at the origin (measurement error/microscale covariation, the "nugget"). The model parametric functional form was selected by visually comparing plots fit using spherical, exponential, and Gaussian functions, and then subsequently fitting and refitting at least 3 candidate spatial parameterizations with the goal of minimizing root mean square error. Results are presented for the best fitting model. Because patterns in covariation may vary by direction, anisotropic variograms also were examined. All models were specified with a nugget parameter.

The spatial dependence function for ordinary kriging of residuals can be written as:

$$Cov\{\varepsilon_{i},\varepsilon_{i}\} = \sigma^{2} f(d_{ii},\theta), \qquad (3)$$

where σ^2 is the sill, f() is the parametric functional form that uses the distance (d) between locations i and j and the spatial range (θ). Ordinary kriging of the sampled values also was used to derive predicted values without covariate information.

Model 3 Spatial Covariance—Fitted as Spatial Error

Spatial error regression was used to assess whether global ordinary least squares prediction would be improved by simultaneously modeling spatial dependence while estimating the relationship between observed *Y* and covariates. Predicted values were derived from the following equation:

$$Y_{i} = \mu + \sum_{k=1}^{k} \beta_{k} X_{ik} + \varepsilon_{i}, \text{ where } Cov\{\varepsilon_{i}, \varepsilon_{j}\} = \sigma^{2} f(d_{ij}, \theta).$$
(4)

The spatial dependency function (illustrated in equation 4 as the covariance between locations i and j) and its parameters were the same as those determined for model 2, with 2 principal differences between model 3 and model 2. First, model 2 used a 2-step approach: supplementary data were fit in ordinary least squares; spatial interpolation (kriging) was performed on residuals; and resultant predicted values were subsequently added to ordinary least squares predictions. In model 3, spatial interpolation was performed by simultaneously modeling supplementary data and the spatial autocorrelation. In model 3, the spatial dependency function was applied such that predicted values were spatially weighted averages of both observed Y and the observed relationship between Y and covariates (X). Second, restricted/residual maximum likelihood was used to estimate simultaneously the mean (μ and β) and covariance parameters.^{26,27}

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Model 4 Nonparametric Mean—Fitted With Spline

Spline regression was selected to assess whether global ordinary least squares prediction would be improved by modeling spatial trend using a deterministic distribution-free approach. In contrast to the 2 previous models, the functional relationship between spatial location (geographic coordinates: z_1, z_2) and the dependent variable *Y* was assumed to be unknown and so was modeled using thin-plate splines (without tension).²⁸ Penalized least squares was used to fit the model while simultaneously using generalized cross-validation to select the optimal smoothing (degrees of freedom or "knots") for the splines.²⁶ Predicted values for this model were obtained using:

$$\hat{Y}_{j} = f(z_{1j}, z_{2j}) + \sum_{k=1}^{k} \hat{\beta}_{k} X_{jk}$$
(5)

Model Diagnostics

Multivariable regression variance inflation factors were examined to determine if multicollinearity barred interpretation of coefficients derived using ordinary least squares. An inflation factor of 10 was used to define high multicollinearity.²⁹ We also examined whether the mean and variance were approximately constant throughout each region (first-order spatial stationarity).⁴ This was broadly investigated by first examining maps and scatter plots of residuals against predicted values. Second, model 1 fit statistics (Akaike information criterion) were examined before and after adding x, y coordinates (polynomial trend analyses using first and second-order polynomials and interactions³⁰). Finally, maps of predicted values were compared with maps of the original data to assess if predicted values appeared to be reasonable.

Validation

The predictive performance of the models was evaluated using repeated replications of cross-validations.^{31,32} One-third of the observed data at each site was selected randomly and set aside as the validation data. Models fitted to the remaining two-thirds of the data were used to predict values for the validation data and then predicted values were compared with the validation data using root mean square error (RMSE), mean error (ME), mean absolute error (MAE), and Pearson linear correlation coefficients.^{4,8}

RMSE =
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2};$$

ME = $\frac{1}{n} \sum_{i=1}^{n} y_i - \hat{y}_i;$
MAE = $\frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|$ (6)

To examine how much variability remained in the predicted values, we also examined standard deviations of the predicted values relative to the standard deviation of the original survey scale. Cross-validations were repeated 100 times to obtain the distribution of the sampling error.

All analyses were conducted using SAS v. 8.0 (SAS Institute, Cary, NC) except for the Moran coefficient, which was estimated using S+ SpatialStats v. 1.5 Supplement (MathSoft, Needham, MA).

RESULTS

The mean values of the "availability of healthy foods" scale were highest in New York City and lowest in Forsyth County (Table 1). Other area characteristics differed considerably across the sites. The Forsyth site had the lowest population density, relatively poor proximity to food stores, and a relatively high level of vehicle ownership. The New York site was the most urban with relatively high proximity to food stores and high percent of households that did not own a vehicle. Area characteristics in Baltimore were intermediate to these two.

There was high bivariate collinearity between 2 covariates in Baltimore and in New York, although multivariable collinearity was only moderate for those same variables/sites [housing unit density and vehicle ownership in Baltimore (bivariate Pearson r = 0.90, regression inflation factor \leq 7), and housing density and food store density in New York (bivariate Pearson r = 0.80 and regression inflation factor \leq 5)]. Multicollinearity was low for all other variables/sites (inflation factor <3.0), thus, broad interpretation of the ordinary least squares beta coefficients was possible. In the ordinary least squares models, the relationship between supplementary data and the availability of healthy foods scale was generally in the expected direction at all sites (Table 2): ie, negative for distances to supermarkets, distance to a high-income area, and percent of households that did not own a vehicle; and positive for density of food stores (except for NY) and high housing density. Covariates provided the strongest predictive power in New York (adjusted R^2 : NY = 25%; Baltimore = 11%; Forsyth = 12%). New York variables with the strongest predictive capacity were distance to a high-income area (partial R^2 = 0.22, not shown); in Baltimore the strongest variables were percent of households that did not own a vehicle and distance to a supermarket (partial R^2 0.05 and 0.03, respectively); and in Forsyth County the strongest variable was distance to a supermarket (partial R^2 0.10).

Diagnostics suggested that there was nonstationarity in New York (not shown): directional semivariograms of the original survey scale revealed periodicity and zonal anisotropy and there was evidence of a trend. Covariate information reduced nonstationarity; therefore, directional spatial dependence was modeled only in New York when covariates were absent in models 2 and 3. In contrast, the Baltimore and Forsyth sites generally had acceptable stationarity. In general, model variograms fit the data reasonably well (Fig. 1) and maps of predicted values and observed residuals appeared reasonable for all the study sites.

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		Baltimore $(n = 1587)$			Forsyth Co. (n = 1493)			New York (n = 2106)	
Model Fit Akaike's information criterion: Adjusted R ² :		4322 0.11			4140 0.12			5034 0.25	
	Linear Spline Cut-Points*	Estimate (Standard Error)	Ρ	Linear Spline Cut-Points*	Estimate (Standard Error)	Ρ	Linear Spline Cut-Points*	Estimate (Standard Error)	Ρ
Intercept parameters		3.8903 (0.1267)			3.7844 (0.1150)			4.3909 (0.1501)	
Food stores	ĩ		10000			000000			
Distance to supermarkets, km	≤1.5km >1.5km	-0.280/(0.0711) -0.0032(0.0823)	0.9690		0.1883 (0.02/7)	0.000	≤0.3km >0.3km	-0.1264(0.1029) -0.3686(0.1029)	0.0003
Number of supermarkets plus fruit/vegetable stores [†]		$0.1834\ (0.0610)$	0.0027		0.0953 (0.0305)	0.0018		-0.0134 (0.0031)	0.0000
Other area characteristics									
Housing density (per 10,000 households) [‡]		0.0680 (0.1100)	0.5364		-0.1238 (0.4016)	0.7579		0.0888 (0.0144)	0.0000
Distance to high-income area, km [§]		-0.0635(0.0159)	0.0001	≤3km	-0.0662 (0.0312)	0.0342	≤0.6 km	-1.5864 (0.1102)	0.0000
Dourset of households that do	/03C/	1 5172 (0 5150)	10000	>3km	-0.0089 (0.0137)	2010.0	>0.6 km	0.3099 (0.04/3)	0.000.0
referent of nousenotids that do not own a vehicle ¹	≥25% >25%	-3.0394 (0.4280) - 3.0394 - 3.0394	9.0000		(6/70.0) 7064.1	conn.n		(6167.0) 6/11.1	0000.0
*Plots and tests for nonlinearity from , covariates. In subsequent prediction models for distance to supermarkets (knot 1.5 km, area (knot 3 km, 58% of the data were bel were below).	generalized additive , nonlinearity was mo 64% of the data are b ow). New York splin	models were used to visu deled using linear splines below the knot), and hous tes were created for distan	ally and s or log tran eholds with	atistically examine poten formations. In Baltimore, tout a vehicle (knot at 25' stores (knot 0.3 km, 50'	tial nonlinear relations bet density of supermarkets an %, 45% of the data are below the 6 of the data are below th	ween indep ad fruit/vege ow the knot), knot), and	andent variables and the table stores was log trans. I. Forsyth Co. splines ve distance to a high-income	te outcome variable while adju nsformed and linear splines wer vere created for distance to hig ome area (knot 0.6 km, 57% of	tsting for e created h-income
[†] Number of supermarkets plus fruit/ve [‡] Sum of occupied housing units within [§] Distance in kilometers to highest 10th [¶] Aversoe perioortion of households with	sgetable stores within a 1.6-km area, per a percentile of US di thout a vehicle within	1.6 km, log. 10,000 households. stribution of per capita b n 1.6 km.	lock group	incomes.					

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FIGURE 1. Empirical and model semivariograms for "availability of healthy foods" scale before ("original value") and after adjustment for supplementary data using ordinary least squares ("residual value"), by study site; Community Survey, 2004. Supplementary data were distance to supermarkets, density of supermarkets and fruit and vegetable stores, housing density, distance to a high-income area, and percent of households that do not own a vehicle. All semivariograms are omnidirectional except for New York's original value semivariogram which is in the north/south direction.

TABLE 3. Moran Coefficients* for the Original "Availability of Healthy Foods" Scale and Residuals From Ordinary Least Squares Using Supplementary Data[†], by Study Site, Community Survey, 2004

	Original	Survey Value	Residual Value		
Study Site	Moran Coefficient*	Permutation <i>P</i> Value*	Moran Coefficient*	Permutation P*	
Baltimore	0.10	< 0.0000	0.01	0.0060	
Forsyth Co.	0.12	< 0.0000	0.02	0.0020	
New York	0.28	< 0.0000	0.01	< 0.0000	

*Moran coefficient (MC) quantifies spatial autocorrelation and typically ranges from -1 to 1; -1 indicates clustering of dissimilar values, 0 indicates a random scatter, and 1 indicates clustering of similar values. The MC was calculated using a 2-km binary weight matrix. An extension of the MC to regression residuals^{19,21} produced identical results to those using the regular MC. Permutation *P* values were based on 999 random permutations.

[†]Supplementary data were distance to supermarkets, density of supermarkets and fruit and vegetable stores, housing density, distance to a high-income area, and percent of households that do not own a vehicle.

Variograms (Fig. 1; "original value") and Moran coefficients (Table 3) of the availability of healthy foods showed moderate/strong spatial autocorrelation in New York and weaker spatial autocorrelation in both Baltimore and Forsyth County. Variograms showed that scale values were roughly spatially independent for distances >4 km; nugget effect represented a moderate (40%) percent of the total variance of the healthy-foods scale for New York but a much higher percentage for Baltimore and Forsyth County (85% and 80%, respectively). After accounting for supplementary data, spatial dependence was further attenuated at all study sites though spatial autocorrelation was still apparent in New York (Fig. 1; "residual value").

Within each study site, prediction performances were similar for the models compared—95% confidence intervals of the estimated root mean square error overlapped (Table 4).

Thus, in general, spatial models with or without covariates (models 2–4) provided little or no prediction benefit over an aspatial ordinary least squares model with covariates (model 1) (Table 4). The only exception to this was the New York site—the site with strong spatial autocorrelation—where all spatial models (both with and without covariates) reduced errors by 3% compared with the aspatial least squares model including covariates.

A comparison of spatial information alone (models 2a, 3a, 4a) (Table 4) versus spatial information with supplementary data (models 2b, 3b, 4b) found that including covariates consistently improved spatial prediction only in Forsyth County—the site with relatively sparse sampling. Comparisons among spatial models with covariates (models 2b, 3b, 4b), found the spatial error model performed very slightly better than the krige and spline models in Baltimore and

TABLE 4. Distribution of Errors, Standard Deviations, and the Correlation Comparing Observed Values to Predicted Values of "Availability of Health Foods" Obtained in Cross-Validation (Number of Replications = 100), by Study Site, Community Survey, 2004

Model No.	Fitted	Covariate Information*	Root Mean Square Error (RMSE) Median (5th and 95th Percentile)	% RMSE Changed From OLS Model With Covariates	Mean Absolute Error (Median) as % of Original Mean	Standard Deviation (SD, Median) of Predicted Values as % of Original SD	Correlation Coefficient (Pearson) for Predicted and Observed Values
			Baltimor	e			
Model 1	Ordinary least squares	With covariates	0.933 (0.898–0.961)		23%	35%	0.33
Model 2	Krige	(a) No covariates	0.933 (0.899-0.960)	0%	23%	35%	0.33
	-	(b) With covariates [†]	0.933 (0.896-0.959)	0%	23%	41%	0.34
Model 3	Spatial error	(a) No covariates	0.932 (0.894-0.956)	0%	23%	33%	0.33
		(b) With covariates	0.928 (0.895-0.960)	-1%	23%	37%	0.35
Model 4	Spline	(a) No covariates	0.937 (0.902-0.962)	0%	23%	36%	0.32
		(b) With covariates	0.933 (0.900-0.968)	0%	23%	38%	0.33
			Forsyth C	Co.			
Model 1	Ordinary least squares	With covariates	0.953 (0.923–0.990)		24%	37%	0.35
Model 2	Krige	(a) No covariates	0.957 (0.925-0.994)	0%	24%	37%	0.34
	-	(b) With covariates [†]	0.953 (0.920-0.992)	0%	24%	42%	0.36
Model 3	Spatial error	(a) No covariates	0.955 (0.924-0.991)	0%	24%	34%	0.35
	-	(b) With covariates	0.949 (0.918-0.986)	0%	24%	39%	0.37
Model 4	Spline	(a) No covariates	0.964 (0.930-1.001)	1%	24%	40%	0.33
	-	(b) With covariates	0.957 (0.925-0.995)	0%	24%	38%	0.34
			New Yor	k			
Model 1	Ordinary least squares	With covariates	0.796 (0.766-0.828)		18%	50%	0.50
Model 2	Krige	(a) No covariates	0.775 (0.745-0.810)	-3%	17%	56%	0.54
		(b) With covariates [†]	0.776 (0.742-0.810)	-3%	17%	57%	0.54
Model 3	Spatial error	(a) No covariates	0.773 (0.745-0.808)	-3%	17%	54%	0.54
		(b) With covariates	0.774 (0.742-0.807)	-3%	17%	55%	0.54
Model 4	Spline	(a) No covariates	0.775 (0.742-0.811)	-3%	17%	56%	0.54
		(b) With covariates	0.773 (0.742-0.810)	-3%	17%	56%	0.54

*Covariates used for prediction were: distance to supermarkets, density of supermarkets and fruit and vegetable stores, housing density, distance to a high-income area, and percent of households that do not own a vehicle.

*Residuals from the ordinary least squares model with covariates were used for kriging.

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Forsyth though differences were indistinguishable in New York. When detrended residuals were used to execute models 2b and 3b in New York, prediction was only very slightly improved (root mean square error 0.774 and 0.773, respectively, not shown in tables).

Residual kriging preserved the most variability (as a percent of that present in the observed value), and the ordinary least squares model preserved the least. Overall, among the 3 study sites, the models for New York had the most favorable statistics—highest linear correlation coefficient (0.54), lowest root mean square error (≤ 0.800), and lowest mean absolute error (≤ 0.635 , not shown).

DISCUSSION

We found evidence of positive spatial autocorrelation in the reported availability of healthy foods, though the strength of spatial autocorrelation varied by study site. In general, when covariate information was available, spatial modeling approaches improved prediction only when spatial autocorrelation was at least moderate—as it was in New York (original survey value Moran coefficient for New York was 0.28; for Baltimore 0.10; for Forsyth County 0.12). However, in the absence of covariate information but with quite dense sampling, spatial modeling approaches performed as well or even better than ordinary least squares with covariates in the presence of weak (Baltimore) or moderate (New York) spatial autocorrelation.

Three key lessons can be gleaned from our results. First, analysts can be quite confident that geostatistical interpolation will not perform substantially better than covariateadjusted ordinary least squares when Moran coefficients and semivariogram plots show weak spatial autocorrelation among original survey values and among covariate-adjusted ordinary least squares residuals (ie, Baltimore and Forsyth County residual variograms showed almost no patterning and there was $\leq 1\%$ reduction in prediction error compared with using covariate information alone). Second, spatial modeling may be advantageous if spatial autocorrelation among original survey values is at least moderate, and covariate information exists but ordinary least squares does not fully capture the autocorrelation (ie, in New York spatial autocorrelation of the original survey value was moderate, some spatial patterning remained in the residual variogram, and spatial models showed a 3% reduction in prediction error compared with using covariate information alone). Third, provided the survey is guite densely sampled, spatial modeling may be advantageous in the absence of supplementary data even if spatial autocorrelation is somewhat weak (ie, in Baltimore and New York, spatial models without covariates had lower prediction errors compared with ordinary least squares models).

In our application, true contrasts between spatial modeling approaches may have been obscured by measurement error in our survey scale. Measurement error could have been due to the scale being comprised of only 3 items and thus only partly capturing overall availability of healthy foods. Denser sampling can reduce measurement error noise and thereby strengthen spatial autocorrelation—as evidenced by the New York site, which had the densest sampling and strongest spatial autocorrelation.

In this empirical analysis, differences in prediction performances were not large, but several contrasts between spatial modeling approaches are worth noting. Among spatial models, the spatial error model with covariates generally had the lowest errors—likely due to its ability simultaneously to optimize the spatial covariance parameters while fitting supplementary variables. Drawbacks of modeling using a spatial error or a kriging approach are stationarity assumptions and having to prespecify spatial continuity parameters. In contrast, spline models conditioning on location do not assume stationarity or prior knowledge regarding the structure of spatial dependence. Relatively good prediction performance for spline models in New York illustrated the advantage of using spline interpolation when spatial continuity is varied and complex and thus prone to misspecification. However, splines may be out-performed by other spatial interpolation methods when there is wide variation in sample distances (which is often the case when sampling is sparse) and when the regional trend is weak.³³ The relatively poor performance for spline models in Forsyth County illustrated this, as sampling there was relatively sparse and irregularly spaced, and there was no strong spatial trend. Another consideration in selecting an appropriate model is the extent to which informative variability is removed.³⁴ Most interpolation techniques smooth variability from the data, which is desirable if noise is obfuscating the signal. If, however, variability is believed to be informative, a benefit of ordinary least squares combined with kriging is that kriging adds back local variability removed in the least squares prediction. This was illustrated by results that showed a relatively high loss of variability in the ordinary least squares model and low loss of variability in the residual kriging model.

When interpolating, supplementary data can partly compensate for sparse sampling. In the site with the sparsest sampling (Forsyth County), most of the supplementary data models performed better than models without those data. Supplementary data can also stabilize nonstationarity in the mean, as revealed by the reduction of directional influences in New York after including covariate information. An obvious substantive advantage of using covariates is their ability to examine what factors (at least in part) determine the spatial patterns that are observed.³⁵ In our analysis, results from least squares regression provided insights into which factors may be influencing healthy food availability. In 2 of the study sites, Baltimore and Forsyth County, distance to a supermarket and percent of households that did not own a vehicle were the strongest predictors of availability of healthy foods. Spatial distributions of supermarkets has been identified as being correlated with healthy food availability in other research.^{13,14,36} Recent trends in increasing the size of food stores and locating them in areas distant from residential neighborhoods has increased the importance of vehicular transport for accessing healthy foods.¹⁶ Our results suggest the need to locate supermarkets closer to residential areas and to improve transportation to those markets. In New York, the most urban site with high proximity to food stores, distance to

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a high-income area was the strongest predictor of availability of healthy foods. One recent study found that higher quality fresh fruits and vegetables (regardless of type of food store) are more commonly available in areas with higher socioeconomic indicators³⁷—thus, food quality may partly explain the strong association found between distance to a high-income area and neighborhood availability of healthy foods.

We chose to interpolate using spatial surfaces derived from point data. Instead, interpolation could have been achieved by aggregating survey responses to areal units such as census tracts. If survey data are being used to assign environmental attributes to a separate sample of persons, then concordance is required between census tracts where survey respondents reside and those where the separate sample resides. Interpolation methods used in this study can easily fill in a complete spatial surface, as well as integrate covariate information from diverse sources or units. In addition, simple aggregations of survey responses to census tracts predefines scale and creates boundary discontinuities, thus, may not accurately reflect actual spatial patterns present in the data. In contrast, spatial covariance models (models 2–3) smooth over and aggregate responses by spatially weighting responses based on observed spatial continuities. Disadvantages of geostatistical models are their complexity in determining the spatial structure (models 2-3) and the computer resources needed to execute them (models 2-4).

In summary, we illustrated methodologies that can be applied when selecting interpolation methods for data that are spatially structured. In this application, we found positive spatial autocorrelation in neighborhood availability of healthy foods, which suggested that some residential environments are more supportive of healthy eating than others and may partly explain differences found in diets across neighborhoods.^{38,39} Use of sophisticated spatial interpolation methods was advantageous when availability of healthy foods was at least moderately spatially autocorrelated (in 1 study area). However, little was gained by using sophisticated spatial interpolation at study sites where spatial autocorrelation was weak. In order to increase the data available for examining health effects from residential environments, a variety of interpolation techniques will likely need to be used. The most appropriate method will vary depending on the construct of interest, availability of relevant supplementary data, and types of observed spatial patterns.

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