Transformation of Quartz to Tridymite in the Presence of Binary Silicate Liquids

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The isothermal transformation rates for quartz to tridymite were studied in the presence of binary silicate liquids between the eutectic temperature and 1470°C. Oxide pairs included Na₂O-SiO₂, PbO-SiO₂, Fe₂O₃-SiO₂, and CuO-SiO₂. Micrographic and X-ray analytical procedures were used. Transformation was most rapid at intermediate temperatures, thus providing typical TTT curves. The rates increased as the liquid contents of the binary pairs were increased. Transformation was more rapid for the pairs which had higher SiO₂ contents in their equilibrated liquids. Transformation proceeded as a solution-reprecipitation reaction. Initially, metastable cristobalite precipitated more rapidly than the tridymite; however, it redissolved and eventually disappeared, leaving only tridymite as the solid phase. An empirical equation was adapted to the transformation.

I. Introduction and Previous Work

The reconstructive silica transformations, in contrast to the low-to-high displaceative transformations, have been qualitatively described as sluggish.¹ This investigation was undertaken to determine the effect of temperature and composition on the rate of the reconstructive transformation of quartz to tridymite in the presence of a liquid phase containing SiO₂ and another oxide. The systems studied were: Na₂O-SiO₂, PbO-SiO₂, Fe₂O₃-SiO₂, and CuO-SiO₂.

In a study of the influence of iron oxide on the rate of quartz inversion in lime and lime-clay bonded silica brick, Hugill and Rees² found that the transformation of quartz to tridymite was promoted by the presence of iron oxide, but obtained no quantitative information to describe the reaction rates. In addition, they observed that the presence of tridymite increased the cross-breaking strength, the modulus of rupture, and the crushing strength of brick.

Grimshaw et al.³ studied the kinetics of quartz transformation in the presence of various additives (Fe₂O₃, CaO, MgO, Al₂O₃, and TiO₂). The important factors in the transformation process were the presence of liquid, subdivision of the solid catalysts, and the type of oxide added.

A study of the effects of the addition of alkali oxides to quartz on the formation of tridymite was reported by De Keyser and Cypres,⁴ who found that tridymite forms more rapidly in the presence of Na₂O and K₂O than in the presence of Li₂O at the same molar concentrations and temperatures. The


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rate of the transformation was related to the amount of liquid formed in the respective systems. Furthermore, as the liquid phase became more viscous, the rate was reduced.

A study of the reaction rates of silica in the presence of other oxides at various temperatures has also been reported by Abou-El-Azm and Moore. The purpose of their investigation was to determine the rate at which glass is formed when silica is heated in the presence of another oxide. In both the binary and the ternary systems, the rate of reaction was dependent on the amount and type of oxides formed when silica is heated in the presence of another oxide. CaO, MgO (least effect). They also found that the rate is inversely influenced by the amount of liquid formed in the various systems studied.

Quartz does not transform directly to tridymite in the upper temperature range of tridymite stability. Instead, cristobalite forms as an intermediate metastable phase. Thus, the reaction is usually considered to be:

quartz → cristobalite → tridymite

Although this reaction has been assigned as appropriate by most previous investigators, it is shown later that most probably quartz forms cristobalite and tridymite concurrently but at different rates; the metastable cristobalite subsequently transforms to the stable tridymite.

II. Experimental Procedure

(1) Specimen Preparation

The raw materials included 140-mesh reagent grade powders of quartz, PbO, FeO, and Na2O-SiO2. These materials were mixed in the desired amounts and then pressed into pellets and placed on a sheet of platinum which, in turn, was placed on an aluminum combustion boat and fired in a resistive furnace heated by silicon carbide heating elements transverse to two combustion tubes. The furnace temperature was automatically controlled by a Pt-Pt10Rh thermocouple placed between the two furnace tubes. The specimen temperature was measured separately by a second thermocouple within the furnaces that had been checked against a thermocouple calibrated by the National Bureau of Standards. The temperature readings were accurate to ±0.5°C, including the ±2°C variation possible in the NBS thermocouple. After firing, the specimens were water-quenched to preserve the phases present at the firing temperature.

(2) Specimen Analysis

Two methods of analysis were used: (1) point-counting on reflected-light specimens for the CuO-SiO2 system, and (2) X-ray analyses for the PbO-SiO2, FeO-SiO2, and Na2O-SiO2 systems.

(A) Point-Count Analyses: In the CuO-SiO2 system, the difference in morphology of the solid phases and the differences in reflectivity between the solid and liquid phases made it possible to analyze the specimens by a reflected-light ceramographic technique. Specimens were mounted in either a Bakelite or polyester resin and then impregnated with a thermosetting resin to prevent pulling out any of the phases during polishing. The specimens were polished with 400 and 600 grit papers, followed by 8 and 1μ diamond polishing wheels. In the point-counting procedure approximately 250 points were used on each specimen.

(B) X-Ray Analyses: In the PbO-SiO2, FeO-SiO2, and Na2O-SiO2 systems, where the optical procedure of point-counting was less satisfactory, we used a quantitative X-ray technique based on the 4.31 and 4.04 A peaks of tridymite and cristobalite, respectively. The method of Holmquist et al. was modified to be similar to the technique described by Khug and Alexander. The specimen was ground to a uniform powder, and the powder was exposed to X-rays in a recording diffractometer. The areas under the 4.31 and 4.04 A peaks for tridymite and cristobalite were measured and compared with standard curves of known mixtures of tridymite and cristobalite. The standard deviation with this method was about 3%. The standard curves had been prepared by mixing known ratios of cristobalite and tridymite which had been ground to approximately —325 mesh. (The ratios included 0/100, 25/75, 50/50, 75/25, and 100/0 weight ratios of the two phases.) The cristobalite had previously been prepared by firing quartz in the presence of the added oxides at 1500°C for 5 hr. The tridymite was prepared by firing quartz in the presence of the added oxide at 1250°C for approximately two weeks to remove all remnants of quartz and cristobalite. In preparing standard materials, account was taken of the effect of the temperature and total composition on the amount of the crystalline silica phases within the system.

These mixtures were then analyzed in a rotating sample holder on a Norelco diffractometer operated at 37 kV and 12 ma, using copper radiation. The beam slit and the detector slit were both 1°. The unit was equipped with a Geiger-Mueller detector and a recording apparatus made by Norelco. The areas were measured with a compensating polar planimeter. The resulting standard curves are presented in Fig. 1. There was no evidence of change in lattice dimensions.

A semilogarithmic plot of time versus percent tridymite (Fig. 2) shows the time to 50% transformation to tridymite. This time was chosen to describe the reaction kinetics and was plotted as a function of temperature at a constant liquid content to illustrate the effect of the various parameters on the reaction.

III. Results and Discussion

As referred to in the foregoing, the transformation of quartz to tridymite in the presence of a liquid does not occur directly. Cristobalite forms as an intermediate metastable phase that subsequently transforms to the stable tridymite in the upper range of tridymite stability. The initial step in the transformation, the dissolution of quartz and formation of cristobalite, occurs rapidly compared to the subsequent
Fig. 3. Isothermal transformation diagrams for the systems: (A) Cu$_2$O-SiO$_2$, (B) Na$_2$O-SiO$_2$, (C) FeO-SiO$_2$, and (D) PbO-SiO$_2$.

steps that involve the final precipitation of stable tridymite. This transformation sequence was observed in all four systems studied.*

The results gave the isothermal transformation diagrams (variously called time-temperature-transformation diagrams, TTT diagrams, and C curves) shown in Figs. 3 (A) through (D). These semilogarithmic plots show that the reaction is slow near the upper temperature range for tridymite stability (1470°C), but as the temperature is decreased, the reaction rate increases until a maximum is reached. Below this temperature, the time for transformation is lengthened. In each case, the lower limit for study was the eutectic temperature. This behavior is similar to that observed in studies of the kinetics of devitrification and crystal growth in glass and parallels many of the metallic isothermal transformations typified by the eutectoid decomposition of Fe-C alloys.

(1) **Amount of Liquid**

Increasing the amount of liquid increased the rate of transformation at a given transformation temperature (Figs. 3 (A) through (D)). For a given size of the individual solid grains, increasing the amount of liquid also increases the solid-liquid boundary area per unit volume. The solid-liquid boundary area is the area of the solid grains exposed to the liquid phase and can be measured by

\[ S_t = 2P_L \]

where \( S_t \) is the solid-liquid boundary area per unit volume of the specimen and \( P_L \) is the number of solid-liquid phase boundaries traversed by a random line. Table I summarizes the data obtained in the Cu$_2$O-SiO$_2$ system on polished sections of specimens having different liquid contents. The amount of liquid in the specimens was varied by varying the amounts of Cu$_2$O and SiO$_2$ raw materials. The results show that increasing the area of the solids exposed to the liquid phase increases the time necessary to reach 50% transformation to tridymite. With more solid area exposed to the liquid phase the possibilities for solution and reprecipitation of the transforming phases are increased.

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*Subsequent work has shown that the cristobalite-quartz metastable equilibrium temperature is 880±5°C in the Na$_2$O-SiO$_2$ system, and that cristobalite does not form as a metastable phase below that temperature. All data in this paper, however, are for 900°C and above where cristobalite does form.
Transformation Rates at FeO-SiO₂, CuO-SiO₂, and PbO-SiO₂

<table>
<thead>
<tr>
<th>System</th>
<th>Silica in liquid phase (mole %)</th>
<th>Time for 50% transformation to tridymite (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Na₂O·SiO₂</td>
<td>83</td>
<td>1000</td>
</tr>
<tr>
<td>PbO·SiO₂</td>
<td>70</td>
<td>1400</td>
</tr>
<tr>
<td>FeO·SiO₂</td>
<td>44</td>
<td>2000</td>
</tr>
<tr>
<td>CuO·SiO₂</td>
<td>29</td>
<td>9000</td>
</tr>
</tbody>
</table>

(2) Liquid Composition

The curves presented in Figs. 3 (A) through (D) also show that, with a constant amount of liquid, the rate of transformation decreases as a function of the added oxide in the following order: Na₂O (fastest), PbO, FeO, CuO (slowest).

When the liquid phase contained a higher concentration of SiO₂, the maximum rate of transformation to tridymite increased (Table II). Since the concentration of the accompanying oxide was lower in the liquid, there was less solute to diffuse from the interface between the liquid and solid phases, permitting a more rapid crystallization of the tridymite from the liquid.

(3) Transformation Reactions

This study, as well as previous studies, indicates that the transformation of quartz to tridymite occurs much more rapidly in the presence of an oxide-liquid than in a completely solid system. Furthermore, the reaction is completed more rapidly as the amount of liquid is increased. Thus, it may be concluded that the most rapid transformation occurs by a solution-reprecipitation process.

On the basis of the observation that a liquid exists as an intermediate phase between succeeding solid phases, it is necessary to revise the tacit assumption that all the quartz transforms to cristobalite with the cristobalite then transforming to tridymite. Such an assumption would require that the sequence be quartz → liquid → cristobalite → liquid → tridymite, with each step achieving somewhat lower free energy (with the consequence that the same liquid appears at two energy levels).

A somewhat more plausible mechanism may be illustrated by the following equation showing a solution of the quartz and a concurrent precipitation of both cristobalite and tridymite from the liquid:

\[
\text{quartz} \rightarrow \text{liquid} \rightarrow \text{cristobalite} \downarrow \uparrow \text{tridymite}
\]

On this basis, reaction kinetics favor an initial accumulation of metastable cristobalite from the liquid (Fig. 4 (A)); however, as the more stable tridymite slowly precipitates (Fig. 4 (B)), there is a gradual resolution of the cristobalite into the same liquid until the final cristobalite disappears (Fig. 4 (C)). This analysis indicates that of the possible mechanisms involved in the transformation of quartz to tridymite the one of primary importance is solution and precipitation. However, the extent of the roles of cristobalite solution and tridymite precipitation as rate-limiting steps was not determined in this study.

(4) Empirical Relations

Inasmuch as the time requirements for transformation are similar to those observed in studies of the kinetics of the devitrification and crystal growth of glass, it was considered advantageous to use previously developed empirical relations in this study. The rate of crystal growth in glass increases as the difference between the growth temperature and the liquidus temperature is increased. The growth rate reaches a maximum and then decreases in proportion to the reciprocal of the melt viscosity. This process has been described by Swift using the following relation:

\[
U = \frac{(\text{constant}) (T_s - T_{liq})}{\eta}
\]

where \(U\) is the crystal growth rate, \(T_s\) is the liquidus temperature, \(T_{liq}\) is the temperature at the growing interface, and \(\eta\) is the melt viscosity which varies extensively with temperature. Equation (1) is based on an empirical relation between crystal growth rate and the temperature for viscous liquids originally presented by Preston:

\[
U = K(T_s - T_i)e^{-C/T_i}
\]

where \(K\) and \(C\) are constants, and temperatures are expressed in absolute degrees. Preston found that two assumptions were experimentally justifiable for the temperature regions above and below \(T_{max}\), the temperature at which the rate of crystal growth is at a maximum. In the temperature interval between \(T_{max}\) and the eutectic temperature, the rate of crystal growth was proportional to the difference between the liquidus temperature and the temperature at the growing interface. Preston considered this temperature difference to be the degree of supercooling and a measure of the force causing crystallization. Below \(T_{max}\), the viscosity of the liquid, which increases rapidly as the temperature is decreased, is assumed to be responsible for the decrease in crystal growth rate despite the continual increase in the degree of supercooling.

Fig. 4. Specimens containing 50SiO₂-50CuO (wt%) fired at 1400°C. (A) Fired 1 hr, 10% tridymite; (B) fired 4 hr, 37% tridymite; and (C) fired 72 hr, 100% tridymite. T = tridymite, C = cristobalite, L = liquid, P = impregnating plastic, and H = hole. (X250.)
To determine the applicability of the type of analysis described above to the present investigation, the following empirical relation was used:

$$ R = K(T - T_1)e^{-C/T_1} $$

where $R$ is the rate of transformation of quartz to tridymite at temperature $T$, $T_1$ is the tridymite-cristobalite equilibrium temperature ($1470^\circ C, 1743^\circ K$), $C$ is a constant that can be determined from the slope of the linear semilogarithmic plot of $R$ versus the reciprocal of the absolute temperature, and $K$ is a constant. Semilogarithmic plots of $R$ versus $1/T_1$ gave two possible values for $C$ because of a break in the curve, as shown in Fig. 5. The value of $C$ was obtained from the lower temperature portion of the curve because this part of the curve best described the process taking place below $T_{\text{max}}$. Figure 5 was obtained from data in the Na$_2$O-SiO$_2$ system at 40% liquid concentration; the value for $C$ obtained from this figure was used in Eq. (3) to calculate $(1743^\circ K - T_1)e^{-C/T_1}$. These values were then plotted versus temperature as shown in Fig. 6. This figure agrees with the experimental curve obtained for this composition and system, both in the shape of the curve and the temperature at which the rate becomes a maximum. Calculations were also made at the 20% liquid level in the Na$_2$O-SiO$_2$ system and the 30% liquid level in the PbO-SiO$_2$ system. These results are also in agreement with the experimental findings. In the CuO-SiO$_2$ and PbO-SiO$_2$ systems, the semilogarithmic plots of temperature versus the calculated value for $(1743^\circ K - T_1)e^{-C/T_1}$ did not show the full $C$ curve because $T_{\text{max}}$ occurs near the eutectic temperature and a less accurate value of $C$ was obtained.

IV. Conclusions

1. The rate of transformation of quartz to tridymite in the presence of other oxides is affected by the amount of liquid present at the transformation temperature, the type of oxide present in the silicate liquid, and the temperature at which the transformation occurs. The kinetics of the transformation show the characteristics of a $C$ curve. The transformation proceeds slowly near the upper temperature limit of tridymite stability ($1470^\circ C$) and at temperatures near the eutectic and passes through a maximum in an intermediate range.

2. The transformation rate increases as the liquid content is increased because the amount of solid/liquid boundary area increases with the amount of crystallite silica present. Admittedly, there are several atomic mechanisms that are probably important in the transformation of silica from one polymorphic phase to another. The relation just cited, however, indicates that the solution-precipitation steps are very important and possibly are the rate-controlling steps.

3. The rate of transformation of quartz to tridymite is related to the solubility of silica in the liquid phase. The transformation rate decreased in the following order: Na$_2$O (fastest), PbO, FeO, CuO (slowest). The extent of solubility of silica in the liquid phase decreases in the same order, suggesting that higher silica contents give more rapid precipitation on the surface.

4. The following empirical equation has been formulated to describe the rate of transformation $R$:

$$ R = K(1743^\circ K - T_1)e^{-C/T_1} $$

In this equation $C$ and $K$ are constants, and $T_1$ is the specific temperature of interest. The validity of this relation is dependent on the accuracy of the value obtained for the constant $C$. The part of the isothermal curve below $T_{\text{max}}$ (the temperature at which the rate is at a maximum) is taken into account by the factor $e^{-C/T_1}$. The part of the curve above $T_{\text{max}}$ is related to the term $(1743^\circ K - T_1)$, where $1743^\circ K$ is the tridymite-cristobalite equilibrium temperature of $1470^\circ C$.

The relation developed is similar to that Preston used to describe crystal growth rates from viscous liquids.

References