# Rotational spectrum, structure and modeling of the SO<sub>2</sub>-CS<sub>2</sub> complex

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The rotational spectra of seven isotopomers of the  $SO_2-CS_2$  van der Waals dimer have been observed with a Fourier transform microwave spectrometer. The rotational constants for the normal species were determined to be  $A=2413.2000(3)\,\mathrm{MHz}$ ,  $B=1105.3803(3)\,\mathrm{MHz}$  and  $C=884.9885(2)\,\mathrm{MHz}$ . They are consistent with the  $SO_2$  straddling the  $CS_2$  molecule and  $C_s$  symmetry for the complex. The centers of mass of the two monomers are separated by  $3.4287(2)\,\mathrm{Å}$ . Two structures were found that are consistent with this symmetry which differ in the relative tilt of the  $CS_2$  and  $SO_2$ . In both structures, the  $C_2$  axis of the  $SO_2$  is aligned close to parallel to the  $CS_2$  molecular axis with the oxygen end of the  $SO_2$  tipped closer to the  $CS_2$ . In one structure the deviation from parallel is  $9.8(8)^\circ$  while in the other it is  $17.7(11)^\circ$ . The dipole moment components have been determined to be  $\mu_a=0.0137(5)\,\mathrm{D}$  and  $\mu_b=1.1961(9)\,\mathrm{D}$ . A semi-empirical model employing electrostatic, dispersion and repulsion interactions was employed to analyze the system and resulted in a reasonable reproduction of the angular geometry. A comparison of the results for the  $SO_2-CS_2$  complex with the closely related  $SO_2-CO_2$  and  $SO_2-OCS$  complexes is presented. ©  $1999\,\mathrm{American}\,\mathrm{Institute}\,\mathrm{of}\,\mathrm{Physics}.\,[\mathrm{S}0021-9606(99)00314-1]$ 

## I. INTRODUCTION

The recent determination of the structures of the SO<sub>2</sub>-CO<sub>2</sub> (Ref. 1) and SO<sub>2</sub>-OCS (Ref. 2) complexes by rotational spectroscopy revealed some rather significant structural changes on going from a nonpolar linear molecule to a polar one. In  $SO_2$ - $CO_2$ , the  $C_2$  axis of the  $SO_2$  was perpendicular to the  $CO_2$  axis ( $C_{2v}$  symmetry). In SO<sub>2</sub>-OCS, the SO<sub>2</sub> rotated approximately 45° away from the perpendicular ( $C_s$  symmetry). It is appropriate to further extend this series with the study of the SO<sub>2</sub>-CS<sub>2</sub> dimer, which contains another nonpolar, linear triatomic molecule. This system is particularly attractive in that CS<sub>2</sub> has a molecular quadrupole moment of opposite sign to that of CO<sub>2</sub>. For example, Watson et al. give values for the molecular quadrupole moments (obtained from electric field induced birefringence experiments) as follows:  $\Theta(CS_2) = +3.4 \times 10^{-26} \text{ esu cm}^2$  and  $\Theta(CO_2) = -4.3 \times 10^{-26} \text{ esu cm}^2$ . It is of interest to see what effect this has on the structure of the CS<sub>2</sub> complex with SO<sub>2</sub> and whether the resulting structure will resemble the SO2-CO2 or the SO2-OCS complex more closely.

In this paper we report on the analysis of the rotational spectra of seven isotopomers of the  $SO_2$ – $CS_2$  dimer. A structure in which the  $SO_2$  straddles the  $CS_2$  molecular axis, with the  $C_2$  axis of the  $SO_2$  lying close to parallel to the  $CS_2$  axis, has been determined from fitting the moments of inertia.

A semi-empirical model employing electrostatic, dispersion and repulsion interactions was also used in an attempt to reproduce the experimental structure. An analysis of the model's performance and a comparison of the structure and

bonding of the  $SO_2$ – $CS_2$  complex in light of the  $SO_2$ – $CO_2$  and  $SO_2$ –OCS results will be discussed.

## **II. EXPERIMENT**

The rotational spectra of the SO<sub>2</sub>-CS<sub>2</sub> dimer and six additional isotopomers were measured with a Balle-Flygare Fourier transform microwave spectrometer<sup>4</sup> in the frequency range 5.5 to 14.5 GHz. After an initial search of a 1.4 GHz region between 6 and 7.4 GHz in which the 3←2 transitions were predicted, mixing experiments were carried out to eliminate transitions that did not require both components. Stark effect measurements were then made on several of the strongest remaining transitions observed in the initial search region. Stark effect experiments were carried out by the application of an electric field up to  $\pm 6$  kV to a pair of parallel steel mesh plates measuring approximately 50 cm×50 cm. These plates are situated above and below the Fabry-Perot cavity and are separated by around 30 cm. The electric field was calibrated daily by the measurement of the  $J=1 \leftarrow 0$ transition of OCS at 12162.980 MHz and using a dipole moment of 0.7152D.<sup>5</sup>

The SO<sub>2</sub>-CS<sub>2</sub> dimer was generated in a supersonic expansion of a gas mixture of approximately 1.5% of each of the two components diluted in "first-run" He/Ne carrier gas (90% Ne, 10% He) at a backing pressure of *ca.* 2.8 atm. This gas mixture was expanded into the evacuated cavity through a modified Bosch fuel injection valve operating at a frequency of about 10 Hz, in a direction perpendicular to the resonator axis. Full width at half maximum of the transitions was estimated to be of the order of 30 kHz and our measured transition frequencies were reproducible to 2 kHz. Only *b*-type transitions were observed during measurement of the spectra and the most intense of the normal species transi-

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TABLE I. Rotational transition frequencies and residuals for the normal isotopomer of  $SO_2$ – $CS_2$ .

$J'_{KaKc}$	$J_{KaKc}^{\prime\prime}$	$\nu_{ m obs}$ (MHz)	$\Delta  u  ({ m kHz})^{ m a}$
$2_{21}$	110	8124.3841	-0.9
220	111	8370.4731	-2.8
313	$2_{02}$	6737.7725	-1.7
330	3 <sub>21</sub>	6981.4453	3.9
331	322	7105.4183	-1.3
322	211	9893.8176	-3.2
321	212	10 681.0938	3.9
331	220	13 050.3277	1.2
330	2 <sub>21</sub>	13 077.8185	-0.1
404	313	6856.2390	0.1
431	4 <sub>22</sub>	6820.6121	2.5
432	423	7171.0368	-0.5
4 14	3 <sub>03</sub>	8340.9527	1.3
440	431	9872.6083	-3.3
441	432	9885.5399	-1.5
4 <sub>23</sub>	3 <sub>12</sub>	11 549.7985	-2.5
4 <sub>22</sub>	313	13 234.1710	0.9
5 24	5 <sub>15</sub>	5984.6148	-1.0
532	5 <sub>23</sub>	6553.2885	-1.5
5 14	423	7163.6906	-3.6
5 <sub>33</sub>	5 <sub>24</sub>	7297.4264	1.5
5 <sub>05</sub>	4 14	8900.4499	4.0
541	5 <sub>32</sub>	9821.1646	6.6
542	5 <sub>33</sub>	9871.5112	-4.2
5 <sub>15</sub>	$4_{04}$	9922.9880	2.0
624	5 <sub>33</sub>	5982.8161	-1.3
625	616	6689.6477	-0.3
634	6 <sub>25</sub>	7505.5165	-1.1
615	5 <sub>24</sub>	9614.2489	4.0
642	633	9716.9670	-1.2
643	634	9861.8581	2.4
6 <sub>06</sub>	5 <sub>15</sub>	10 872.2081	-1.8
6 <sub>16</sub>	5 <sub>05</sub>	11 524.9847	-0.2
625	5 <sub>14</sub>	14 554.5512	0.0
744	7 <sub>35</sub>	9869.3933	-0.5
707	616	12 776.3257	-0.7
7 17	$6_{06}$	13 168.1880	-0.5

 $<sup>^{\</sup>mathrm{a}}\Delta \nu = \nu_{\mathrm{obs}} - \nu_{\mathrm{calc}}$  .

tions, the  $2_{21}\leftarrow 1_{10}$  and  $2_{20}\leftarrow 1_{11}$  transitions, had signal-to-noise ratios in excess of 30 in 100 gas pulses.

The <sup>34</sup>SO<sub>2</sub> isotopomer and the two singly substituted C<sup>32</sup>S<sup>34</sup>S isotopomers were observed in natural abundance (ca. 4%). The  $2_{20} \leftarrow 1_{11}$  transition for these species typically had a signal-to-noise ratio of ca. 7 or more in 1000 gas pulses. Some of the weaker transitions for these species required averaging for several thousand gas pulses in order to achieve a satisfactory signal to noise. The spectrum of the SO<sub>2</sub>-13CS<sub>2</sub> species was observed using an isotopically enriched sample of <sup>13</sup>CS<sub>2</sub> (Cambridge Isotope Labs., 97%– 99% <sup>13</sup>C). The S<sup>18</sup>O<sub>2</sub>-CS<sub>2</sub> isotopomer was observed using an isotopically enriched sample of S18O2 purchased from Icon (97% <sup>18</sup>O). Upon least-squares fitting of the moments of intertia for these isotopomers it became apparent that there existed two structures that were consistent with the inertial data. Another isotopomer,  ${}^{34}SO_2 - {}^{13}CS_2$  (consisting of a sample of the enriched <sup>13</sup>CS<sub>2</sub> and the <sup>34</sup>SO<sub>2</sub> in natural abundance), was therefore assigned in an attempt to clear up the ambiguity.

# III. RESULTS

# A. Spectra

Only b-type transitions were observed for this complex with searches for a- and c-type transitions being unsuccessful. Further searches for a-type transitions in light of the nonzero  $\mu_a$  dipole component obtained from analysis of the Stark data (see Sec. III B) also proved to be unsuccessful, with averaging for 50 000 gas pulses failing to reveal a transition. The lack of a  $\mu_c$  dipole component suggests an ab plane of symmetry with the SO<sub>2</sub> monomer likely straddling the CS<sub>2</sub> monomer as observed in the SO<sub>2</sub>–OCS complex.<sup>2</sup> The lack of intense a-type transitions was initially problematic since attempts at initial assignment assumed a structure in which the  $\mu_a$  component was sizable. Based on Stark effect data obtained from the transitions at 6737.7725 and 7163.6906 MHz a tentative assignment of these lines as the  $3_{13} \leftarrow 2_{02}$  and the  $5_{14} \leftarrow 4_{23}$  transitions was made since these transitions seemed to be the only likely candidates in the regions. Stark shift data from several other strong lines in the 6 to 7 GHz region were important in suggesting further assignments, and a process of trial and error in which various combinations of transitions were added to the above transitions eventually revealed the correct assignment. The fit with a rigid rotor model at this stage proved to be more than sufficient to give reasonably good agreement, even upon the inclusion of lines with  $K_a = 2$  or 3. This is in contrast to the  $SO_2$ -OCS complex in which inclusion of lines with  $K_a$ greater than 1 caused large standard deviations.<sup>2</sup> The good performance of the rigid rotor model greatly simplified the location of further transitions in the rotational spectrum. The 37 measured lines for the normal species were fit to a Watson A-reduction Hamiltonian. Transition frequencies for the normal species along with the residuals for this fit are given in Table I, while the resulting spectroscopic constants are given in Table II for the normal and the six other isotopic species. Isotopic shifts were calculated from a model based upon a structure obtained from a semi-empirical model (to be discussed later) in which the SO<sub>2</sub> straddled the CS<sub>2</sub> molecule; the tilt and separation of the SO2 molecule were adjusted so as to more closely reproduce the rotational constants and the dipole moment of the normal species. This model provided isotopic shifts which were sufficiently good to locate the isotopomers with a minimum of searching. As noted above, a least-squares fit of the transition frequencies to a rigid rotor model that included no centrifugal distortion constants gave a reasonable fit, suggesting that centrifugal distortion was much less important in this complex than in the SO<sub>2</sub>-OCS complex.<sup>2</sup> We conclude that the SO<sub>2</sub>-CS<sub>2</sub> complex likely exhibits considerably less floppiness in its structure.

Several transitions found in the initial search region still remain unassigned although they are considerably weaker and are not suitable for a Stark effect study. These lines likely belong to trimeric and higher order clusters of  $SO_2$ ,  $CS_2$ , rare gases and maybe  $H_2O$ , and further studies will attempt to identify these species.

TABLE II. Spectroscopic constants for the seven isotopomers of SO<sub>2</sub>-CS<sub>2</sub>.

Spectroscopic constant	SO <sub>2</sub> –CS <sub>2</sub>	<sup>34</sup> SO <sub>2</sub> –CS <sub>2</sub>	SO <sub>2</sub> -C <sup>34</sup> S <sup>32</sup> S	SO <sub>2</sub> -C <sup>32</sup> S <sup>34</sup> S
A (MHz)	2413.2000(3)	2411.3806(11)	2365.0998(9)	2357.1336(12)
B (MHz)	1105.3803(3)	1088.1265(11)	1091.8708(10)	1095.7358(12)
C (MHz)	884.9885(2)	873.6646(8)	869.8006(7)	871.1596(8)
$\Delta_J$ (kHz)	1.639(4)	1.624(2)	1.61(1)	1.59(2)
$\Delta_{JK}$ (kHz)	170.1(1)	164.5(6)	160.4(5)	163.5(6)
$\Delta_K$ (kHz)	-177.2(2)	-172.9(9)	-166.8(8)	-171(1)
$\delta_I$ (kHz)	0.355(2)	0.352(8)	0.345(7)	0.362(10)
$\delta_K$ (kHz)	-219.2(4)	-214.9(2)	-197(2)	-202(2)
$P_{cc}$ (amu Å <sup>2</sup> ) <sup>a</sup>	47.782	47.785	47.755	47.753
$\Delta \nu_{\rm rms} \; ({ m kHz})^{ m b}$	2.81	3.47	2.90	3.36
N°	37	22	22	21
	$S^{18}O_2 -$	$CS_2$	$SO_2$ - $^{13}CS_2$	$^{34}SO_2 - ^{13}CS_2$
A (MHz)	2337.92	06(3)	2413.2116(6)	2411.3904(9)
B (MHz)	1063.40	09(4)	1099.5262(8)	1082.2549(11)
C (MHz)	866.09	65(3)	881.2330(7)	869.8754(7)
$\Delta_{I}$ (kHz)	1.49	8(5)	1.64(2)	1.57(2)
$\Delta_{JK}$ (kHz)	169.0(2	2)	167.8(4)	162.6(7)
$\Delta_K (kHz)$	-176.9(2	2)	-174.9(3)	-167.2(7)
$\delta_I (kHz)$	0.30	4(3)	0.351(9)	0.335(10)
$\delta_K$ (kHz)	-264.2(	7)	-217(1)	-211(2)
$P_{cc}$ (amu Å <sup>2</sup> ) <sup>a</sup>	53.95	0	47.782	47.785
$\Delta \nu_{\rm rms} ({\rm kHz})^{\rm b}$	1.96		2.76	2.47
N <sup>c</sup>	29		24	21

 $<sup>{}^{</sup>a}P_{cc}$  is the out of plane second moment.

# **B.** Dipole

Thirteen M components from the  $3_{13} \leftarrow 2_{02}$ ,  $4_{31} \leftarrow 4_{22}$  and  $5_{14} \leftarrow 4_{23}$  transitions were least squares fitted to determine the dipole moment components for this complex (Table III). As was suspected from the initial failure to locate any a-type transitions, the  $\mu_a$  component of the dipole moment was found to be very small,  $\mu_a = 0.0137(5)$  D, while  $\mu_b$ 

TABLE III. Stark coefficients and dipole moment components for  $SO_2-CS_2$ .

Transition	M	$\Delta   u /  \epsilon^{2a}$	ObsCalc.a					
3 <sub>13</sub> -2 <sub>02</sub>	0	2.339	-0.003					
	1	17.623	-0.022					
	2	63.603	0.050					
4 <sub>31</sub> -4 <sub>22</sub>	1	-2.694	-0.015					
	2	-4.926	-0.006					
	3	-8.752	-0.098					
	4	-13.829	0.053					
514-423	1	-2.835	0.035					
	2	-3.983	0.045					
	3	-5.897	0.062					
	4	-8.394	0.267					
	$\mu_a =$	0.0137(5) D						
	$\mu_b = 1.1961(9) \text{ D}$							
	$\mu_c =$	$0.00(5) D^{b}$						
$\mu_{\text{tot}} = 1.1962(9) \text{ D}$								

<sup>&</sup>lt;sup>a</sup>Observed Stark coefficients and residuals in units of  $10^{-6}$  MHz/(V cm<sup>-1</sup>)<sup>2</sup>. <sup>b</sup> $\mu_c$  fixed at zero during fitting.

=1.1961(9) D. This gives  $\mu_{\text{total}}$ =1.1962(9) D, some 0.43 D less than the dipole moment of the SO<sub>2</sub> monomer.<sup>7</sup> The small  $\mu_a$  component could be accurately determined because of high sensitivity of the Q branch transition in the set to this component.

# C. Structure

The ab plane of symmetry that is suggested by the absence of c-type transitions can be verified by calculation of the out of plane second moments for the normal isotopic species. The value of the second moment  $P_{cc}[=\sum m_i c_i^2 = 0.5(I_a + I_b - I_c)]$  is calculated to be 47.782 amu Ų, in good agreement with the value of 47.8(4) amu Ų for  $P_{bb}$  in the SO<sub>2</sub>–CO<sub>2</sub> complex¹ and similar to the value of  $P_{cc}$  = 48.350 amu Ų in the SO<sub>2</sub>–OCS complex.¹ This provides convincing evidence that the oxygen atoms of SO<sub>2</sub> are indeed straddling the symmetry plane. Values of  $P_{cc}$  for all of the isotopomers studied are listed in Table II. Using litera-

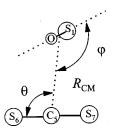


FIG. 1. Structure of the  $SO_2$ – $CS_2$  complex in the ab symmetry plane showing the fitted structural parameters. The center of mass of the  $SO_2$  is labeled  $M_4$  but is suppressed in the figure for simplicity.

 $<sup>^{</sup>b}\Delta \nu_{\rm rms} = [\Sigma (\nu_{\rm obs} - \nu_{\rm calc})^2 / N]^{1/2}.$ 

<sup>&</sup>lt;sup>c</sup>N is the number of fitted transitions.

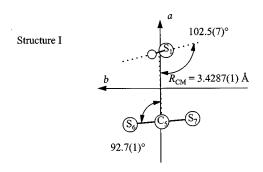
TABLE IV. Fitted structural parameters for possible structures I and II in the SO<sub>2</sub>-CS<sub>2</sub> complex.

Parameter	Literature value <sup>a</sup>	I	II	ORIENT <sup>b</sup>
R <sub>CM</sub> (Å)	3.4273(10)	3.4287(1)	3.4287(2)	3.377
$\theta$ (°)	92.6(9)	92.7(1)	87.0(2)	96.7
$\varphi$ (°)	103(4)	102.5(7)	104.1(9)	143.7
$\Delta I_{\rm rms}^{\ \ c}$ (amu Å <sup>2</sup> )	0.7281	0.1144	0.1599	•••

a "Literature value" and "Adjusted value" refer to whether the literature or adjusted values for the SO<sub>2</sub> monomer structural parameters were used in the fitting process. Refer to the text for a full discussion.

ture values for the SO<sub>2</sub> monomer structure [r(S-O) = 1.4308 Å and an OSO angle of  $119.3^{\circ},^{8}$  a  $P_{bb}$  value for the monomer of 48.77 amu Å<sup>2</sup> may be calculated compared to the ground state spectroscopic value<sup>9</sup> of 49.05 amu Å<sup>2</sup>. It is readily apparent that these values for  $P_{bb}$  of the monomer and  $P_{cc}$  for the complex  $(47.78 \text{ amu Å}^2)$  are significantly different. This arises from large amplitude vibrational effects that lead to a contamination of the effective moments of inertia.

The normal species and data from an additional six isotopic species ( $^{34}\text{SO}_2\text{-CS}_2$ ,  $\text{SO}_2\text{-C}^{32}\text{S}^{34}\text{S}$ ,  $\text{SO}_2\text{-C}^{34}\text{S}^{32}\text{S}$ ,  $\text{SO}_2\text{-C}^{34}\text{S}^{32}\text{S}$ ,  $\text{SO}_2\text{-}^{13}\text{CS}_2$ ,  $\text{S}^{18}\text{O}_2\text{-CS}_2$  and  $^{34}\text{SO}_2\text{-}^{13}\text{CS}_2$ ) allowed a least squares fitting of the moments of inertia to structural parameters. The University of Michigan implementation of the STRFTQ program of Schwendeman<sup>10</sup> was employed in the fitting of the inertial data. Three parameters are required to describe the structure of this dimer: a center of mass separation ( $R_{\text{CM}}$ ), an angle  $\theta$  (the  $\text{S}_6\text{-C}_5\cdots\text{M}_4$  angle in Fig. 1 and the angle  $\varphi$  (the  $\text{C}_5\cdots\text{M}_4\cdots\text{S}_1$  angle). Figure 1 illustrates the



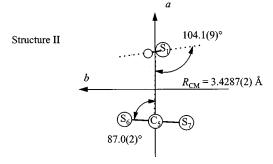


FIG. 2. The two possible fitted structures for the  $SO_2$ – $CS_2$  complex: (a) structure I,  $\Delta I_{rms}$ =0.1144 amu Å $^2$  and (b) structure II,  $\Delta I_{rms}$ =0.1599 amu Å $^2$ .

atom numbering scheme and the three fitted parameters. The parameters obtained from using the literature values for the SO<sub>2</sub> given above and the CS<sub>2</sub> monomer structure  $[r(C-S)=1.552 \text{ Å}^8]$  are given in the first column of Table IV; the  $\Delta I_{\rm rms}$  value of 0.728 amu Å<sup>2</sup> which results from this fit is relatively high. The rather poor quality of this fit arises from the difference in the values of  $P_{cc}$  for the complex calculated from the monomer structure of SO2 and those derived from the experimental data. Small adjustments to the structure of the  $SO_2$  are often found to be necessary  $^{11-13}$  in order to bring the observed and calculated  $P_{cc}$  (or equivalent) values into better agreement as a means of compensating for vibrational effects arising from large amplitude motions in the complex which affect the observed moments of inertia. In this case, the S-O bond length was decreased by 0.003 Å and the OSO angle decreased by 1.5° in order to better reproduce the experimentally observed  $P_{cc}$  value. With this adjusted structure there was a marked improvement in the quality of the inertial fit as is illustrated in the second and third columns of Table IV. It should be noted that the uncertainties in Table IV are statistical uncertainties  $(1\sigma)$  resulting from the fitting process. The structure suggested by the parameters in Table IV may therefore be considered an effective ground state structure and we expect the equilibrium values to fall within approximately 0.05 Å for the  $R_{\rm CM}$  distance and 5° or so for the angles  $\theta$  and  $\varphi$ .

During the course of the fitting with the adjusted  $SO_2$  structure, it became apparent that two structures closely fit

TABLE V. Principal axis coordinates for the two possible fitted structures (I and II) of  $SO_2$ – $CS_2$ . <sup>a</sup> All coordinates are given in Angstroms.

	ú	a		b		c	
Atom	I	II	I	II	I	II	
$S_1$	1.9531	1.9416	-0.2880	-0.4057	0.0000	0.0000	
$O_2$	1.7668	1.7796	0.4256	0.3138	1.2226	1.2226	
$O_3$	1.7668	1.7796	0.4256	0.3138	-1.2226	-1.2226	
$M_4^{b}$	1.8599	1.8606	0.0689	-0.0458	0.0000	0.0000	
$C_5$	-1.5665	-1.5670	-0.0580	0.0386	0.0000	0.0000	
$S_6$	-1.6976	-1.4467	1.4884	1.5859	0.0000	0.0000	
$S_7$	-1.4353	-1.6874	-1.6045	-1.5087	0.0000	0.0000	

<sup>&</sup>lt;sup>a</sup>Structures I and II refer to the two possible structures that result from the fitting of the inertial data. Structure I has  $\Delta I_{\rm rms}$ =0.1144 amu Å<sup>2</sup> and structure II has  $\Delta I_{\rm rms}$ =0.1599 amu Å<sup>2</sup>. See the text for a more detailed discussion and Fig. 2.

<sup>&</sup>lt;sup>b</sup>Values calculated from the structure obtained using the ORIENT model (see text).

 $<sup>^{\</sup>rm c}\Delta I_{\rm rms}$  is the standard deviation when fitting the 21 moments of inertia.

<sup>&</sup>lt;sup>b</sup>M<sub>4</sub> is the center of mass of the SO<sub>2</sub>.

TABLE VI. Absolute values of the Kraitchman substitution coordinates in  $\mathring{A}$  for  $SO_2-CS_2$  obtained from the single and double substitution isotopic data.

Atom	<i>a</i>	b	c
S <sub>1</sub>	1.9184	0.2848	0.0390
$O_{2,3}$	1.7291	0.3826	1.2818
C <sub>5</sub>	1.5632	0.0000	0.0000
$S_6$	1.6850	1.4930	0.0000
$S_7$	1.4208	1.6090	0.0000

the experimental data. The two structures, I and II (shown in Fig. 2) had values of  $\Delta I_{\rm rms} = 0.114$  and 0.160 amu Å<sup>2</sup>, respectively, and differ only in the relative tilt of the CS<sub>2</sub> molecule (corresponding to the atom  $S_7$  tilted either towards or away from the  $S_1$  atom of the  $SO_2$ , respectively, using  $R_{CM}$ as a reference axis—see Fig. 2). The structural parameters that result for structures I and II from the least-squares fitting of the 21 moments of inertia are given in Table IV. It can be seen that structure I gives a slightly better fit when using the adjusted values of the SO2 monomer structure, based on the value of  $\Delta I_{\rm rms}$  and on the slightly lower uncertainties in the derived parameters. Structures I and II are clearly almost equivalent, with  $R_{\rm CM}$  and  $\varphi$  agreeing to within experimental uncertainty. The angle  $\theta$ , however, does differ quite significantly between the two structures. In structure I this corresponds to the  $C_2$  axis of the  $SO_2$  and the  $CS_2$  axis deviating 9.8(8)° from parallel, while in structure II the deviation is  $17.7(1.1)^{\circ}$ . This may also be viewed as a sliding of the SO<sub>2</sub> moiety along an axis parallel to the CS<sub>2</sub> molecular axis with a resultant switching of the centers of mass of both species across the a axis. Also included in Table IV for comparison purposes are the parameters that result from the use of a semi-empirical model, ORIENT, which will be discussed in Sec. IV.

As was also the case with the  $SO_2$ –OCS complex,<sup>2</sup> the dipole moment components that are derived from a simple projection of the  $SO_2$  monomer moment onto the principal axis system of the fitted structures are noticeably different from the components obtained from the experimental measurement of the dipole. In structure I,  $\mu_a$  and  $\mu_b$  components of 0.41 and 1.58 D result, while for structure II we obtain values of 0.36 and 1.59 D, respectively. Both structures overestimate the *a*-component of the dipole and the *b*-component by approximately 0.4 D. Vibrational averaging effects and induced dipole moments within the monomers that reduce

TABLE VII. Comparison of the predicted rotational constants of the  $^{34}SO_2$ – $^{13}CS_2$  isotopic species for structures I and II with the experimental constants.

Rotational constant		Predicted <sup>a</sup>		
(MHz)	Experimental	Structure I	Structure II	
A	2411.390	2411.114	2409.384	
B	1082.255	1081.904	1082.087	
<i>C</i>	869.875	869.703	869.596	

<sup>&</sup>lt;sup>a</sup>Rotational constants predicted from the structure I or II that result from fitting the moment of inertia data.

the dipole components are likely explanations for this discrepancy. As a check that induction effects will reduce the projected values, a simple point polarizability model was used. The experimental values of the polarizabilities <sup>14</sup> for CS<sub>2</sub> ( $\alpha_{zz}$ =15.090 Å<sup>3</sup>,  $\alpha_{xx}$ = $\alpha_{yy}$ =5.090 Å<sup>3</sup>) and SO<sub>2</sub> ( $\alpha_{xx}$ =3.007 Å<sup>3</sup>,  $\alpha_{yy}$ =5.317 Å<sup>3</sup>,  $\alpha_{zz}$ =3.511 Å<sup>3</sup>) were placed at the center of mass of each monomer. An *ab initio* calculation using GAUSSIAN 98<sup>15</sup> for each monomer provided the electric field at the center of mass of the other monomer in the complex. Calculations were carried out at the SCF level using the AUG-cc-pVTZ basis set from the Gaussian library. This gave induced moments of  $\mu_a$ =0.36 D and  $\mu_b$ =0.74 D with the expected signs. Applying these induced dipole corrections to the projected dipole moment components from structure I reduces  $\mu_a$  to 0.05 D, close to the value in the complex but overcorrects  $\mu_b$  by about 0.4 D.

Table V contains the principal axis coordinates of the complex for both of the fitted structures and Table VI contains the coordinates that were obtained from the single and double isotopic substitution Kraitchman calculations. <sup>16</sup> Table VI shows that the coordinates for the carbon and sulfur atoms of  $CS_2$  are very close to those of either model I or II although there is a slight preference for structure I. For the  $SO_2$  coordinates there is a definite preference for structure I, particularly apparent in the b coordinates of the sulfur and oxygen atoms. This better agreement for structure I is, however, still not conclusive.

In order to attempt to resolve this ambiguity there are several approaches that may yield evidence to differentiate in favor of one structure. Occasionally, small changes in the dipole moment components on isotopic substitution may be used. The small rotations of the principal axes that are encountered upon isotopic substitution may occasionally be sufficient<sup>17</sup> to choose between possible structures. In the present case, the  $\mu_b$  component is calculated to change very little upon isotopic substitution although the changes in the  $\mu_a$  component are computed to be somewhat larger. However, given the small magnitude of the  $\mu_a$  component and the uncertainty in the measurement of that dipole, the changes are likely to be too insignificant to definitively support one structure.

Another possible approach is to use a semi-empirical model to deduce which structure is correct. In this particular case, the agreement between the calculated and experimental structures was just not good enough to enable us to use this method (see below). Careful *ab initio* calculations which could differentiate between I and II are beyond the scope of this study.

Finally, there is the possibility that a doubly substituted isotopomer may yield rotational constants that distinguish between the structures. For this purpose, the  $^{34}SO_2-^{13}CS_2$  isotopomer was chosen. Table VII compares the experimental rotational constants for the  $^{34}SO_2-^{13}CS_2$  species with the predicted constants for structures I and II. From the table it is clear that structure I gives much better agreement for the *A* rotational constant. *B* and *C* are much less clear cut with II giving slightly better agreement for *B* while I is better for the *C* rotational constant. Although there seems to be a definite preference for structure I, we cannot completely rule out

TABLE VIII. Distributed multipole moments (DMM's) for CS<sub>2</sub>. The components are given in spherical tensor notation and all quantities are in atomic units.

Atom	$z^{a}$	$Q_{00}$	$Q_{10}$	$Q_{20}$	Q <sub>30</sub>	Q <sub>40</sub>
С	0.0000	0.826 16	0.000 11	-0.442 01	0.000 05	0.829 38
S	-2.9340	0.458 20	0.646 81	1.950 15	0.487 18	0.15839
S	2.9340	0.458 20	-0.64681	1.950 15	$-0.487\ 18$	0.158 39
BC1 <sup>b</sup>	-1.4670	-0.87123	-0.13184	0.802 82	0.521 07	0.74895
BC2 <sup>b</sup>	1.4670	$-0.871\ 23$	0.131 84	0.802 82	$-0.521\ 07$	0.74895

<sup>&</sup>lt;sup>a</sup>z-coordinate of the atoms (in atomic units).

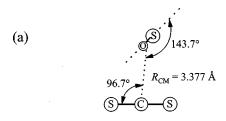
structure II. Nevertheless, since the two structures are very similar, the major feature of the interaction, namely nearly parallel units, is common to both models.

#### IV. DISCUSSION

A semi-empirical model was employed in the initial modeling of this complex in order to explore possible structures and make predictions of spectra to aid us in our assignments. The ORIENT model of Anthony Stone was used<sup>18</sup> with ab initio distributed multipole moments (DMM's) for the SO<sub>2</sub> and CS<sub>2</sub> molecules. These DMM's were calculated at the SCF level using the CADPAC suite of programs<sup>19</sup> with a TZ2P basis set taken from the CADPAC library. Multipoles up to and including hexadecapole moments were calculated on sites located at each atomic center, with additional sites placed at the bond midpoints; the DMM's employed in the calculations are listed in Tables VIII and IX. Dispersion and repulsion interactions are included in the intermolecular interaction potential by means of combined dispersionrepulsion atom-atom parameters of the familiar exp-6 form. The combined dispersion-repulsion portion of the interaction energy for an interaction between two molecules A and B may be expressed as a sum over all of the individual sites:<sup>20</sup>

TABLE IX. Distributed multipole moments (DMM's) for the SO<sub>2</sub> monomer. The coordinates of the SO<sub>2</sub> are as follows: x (S)=0.00 000, y (S)=0.00 000; x (O)=±2.33 328, y (O)=-1.36 619 and x (BC)=±1.16 962, y (BC)=-0.68 324 (all distances and multipoles are in atomic units).

	Atoms						
Component	S	О	О	BC1	BC2		
Q <sub>00</sub>	1.908 11	-0.081 98	-0.081 98	-0.872 08	-0.872 08		
$Q_{11c}$	0.00000	-0.42845	0.428 45	-0.19928	0.199 28		
$Q_{11s}$	-1.78374	0.417 97	0.417 97	0.167 83	0.167 83		
$Q_{20}$	-0.20267	-0.25003	-0.25003	-0.66404	-0.66404		
$Q_{22c}$	1.321 195	0.356 91	0.356 91	$-0.243\ 56$	$-0.243\ 56$		
$Q_{22s}$	0.00000	$-0.857\ 11$	0.857 11	-0.69849	0.698 49		
$Q_{31c}$	0.00000	0.438 57	-0.43857	-0.37498	0.374 98		
$Q_{31s}$	0.194 47	-0.32947	-0.32947	0.127 72	0.127 72		
$Q_{33c}$	0.00000	0.302 26	$-0.302\ 26$	-0.00423	0.004 23		
$Q_{33s}$	0.432 77	0.607 14	0.607 14	$-0.465\ 19$	$-0.465\ 19$		
$Q_{40}$	0.271 40	0.26853	0.268 53	0.089 71	0.089 71		
$Q_{42c}$	-0.19708	-0.08980	$-0.089\ 80$	0.093 19	0.093 19		
$Q_{42s}$	0.00000	0.385 57	$-0.385\ 57$	0.455 09	-0.45509		
$Q_{44c}$	-0.42292	-0.46765	-0.46765	-0.63153	-0.63153		
Q <sub>44s</sub>	0.000 00	-0.209 26	0.209 26	-0.122 04	0.122 04		



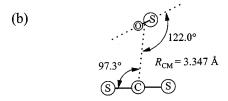


FIG. 3. Structures resulting from the use of the ORIENT model using the default parameters, with (a) no polarization and (b) polarization included.

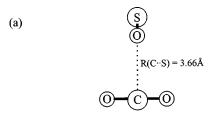
$$U_{\text{exp-6}} = \sum_{i,j} K \exp[-\alpha_{ij}(R_{ij} - \rho_{ij})] - \frac{C_6^{ij}}{R_{ij}^6}.$$
 (1)

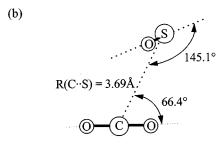
K is an energy unit and is taken to be 0.001  $E_h$  (hartree) in the present work.  $R_{ij}$  is the distance between the sites i and j on the molecules A and B, respectively.  $\alpha_{ij}$  describes the hardness of the exponential repulsion,  $\rho_{ij}$  is a sum of effective radii of the sites i and j, and  $C_6^{ij}$  is an empirical site-site dispersion term. Values for  $\alpha_{ij}$ ,  $\rho_{ij}$  and  $C_6^{ij}$  were taken from the tabulated values of Mirsky<sup>21</sup> in Table 11.2 of Ref. 18. Values for atom-atom pairs not available in Ref. 18 were generated by means of the following approximate combining rules: harmonic mean for  $\alpha$  (i.e.,  $1/\alpha_{ij} \approx 1/\alpha_i + 1/a_j$ ), geometric mean for  $C_6$  and arithmetic mean for  $\rho$ .

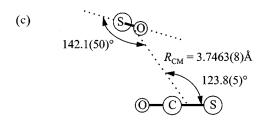
The ORIENT model was used starting with numerous possible structures for the  $SO_2$ – $CS_2$  complex. The global minimum structure that emerged from the calculations (-699.4 cm $^{-1}$ ) is pictured in Fig. 3(a) and is, at first glance, a reasonable approximation to the experimental structure, especially in the close prediction of the  $R_{\rm CM}$  distance (3.377 Å  $\nu s$ . the experimental distance of 3.429 Å). However, the last column of Table IV reveals that even though the model closely reproduces the  $R_{\rm CM}$  separation, the tilt of the  $SO_2$  monomer with respect to the  $CS_2$  molecule (the angle  $\varphi$  in Fig. 3) is markedly different from experiment (by around  $40^\circ$ ).

Neglect of errors in the distributed multipole moments are likely responsible for some of the discrepancy btween the ORIENT values and the experimental values. The values of the dipole moment recovered from the *ab initio* DMM calculation for the  $SO_2$  monomer overestimates the total dipole moment of  $SO_2(\mu=1.63~\rm D^6)$  by some 25%. The neglect of induction effects also contribute to the structural discrepancy. It is possible to include induction interactions at the simplest level in the ORIENT intermolecular potential by the introduction of a point molecular polarizability placed at the center of mass of each monomer. The tilt of the  $SO_2$  is considerably different in the structure resulting from this calculation [Fig.

<sup>&</sup>lt;sup>b</sup>BC1 and BC2 refer to the midpoints of the C-S bonds.







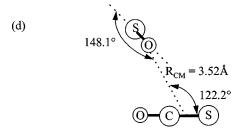


FIG. 4. Experimental and predicted structures for the  $SO_2$ –OCS and  $SO_2$ –CO $_2$  complexes. (a) and (b) show the experimental and predicted structures for the  $SO_2$ –CO $_2$  complex and (c) and (d) show the experimental and predicted structure for  $SO_2$ –OCS. Note that (b) and (d) used DMM's with additional multipole sites located at bond midpoints and that the value of the preexponential factor K was changed to improve the agreement in the prediction of the intermolecular separation.

3(b)] compared to the calculation in which induction was ignored [Fig. 3(a)], with the angle  $\varphi$  decreasing by approximately  $20^{\circ}$  to a value of  $122^{\circ}$ . Although this is a crude model, it does serve to illustrate that there are indeed appreciable polarization effects that significantly affect the calcu-

TABLE X. Relative contributions to the intermolecular interaction energy in the ORIENT model for the  $SO_2$ –OCS,  $SO_2$ – $CS_2$  and  $SO_2$ – $CO_2$  complexes. All energies are in hartrees ( $E_h$ ).

Complex	Electrostatic	Repulsion	Dispersion	Total <sup>a</sup>
SO <sub>2</sub> -CS <sub>2</sub>	-0.000 432	0.002 658	-0.005 412	-0.003 187
SO <sub>2</sub> -CO <sub>2</sub>	-0.002 838	0.002 478	-0.003 496	-0.003 856
SO <sub>2</sub> -OCS	-0.001 850	0.002 057	-0.003 409	-0.003 201

<sup>&</sup>lt;sup>a</sup>All energies exclude polarization contributions.

lated structure. Our initial efforts at introducing distributed polarizabilities into the model did not lead to significant improvement.

## V. SUMMARY

It is interesting that the  $SO_2-CS_2$  complex possesses a structure which is not readily extrapolated from a simple dipole-quadrupole interaction between the monomers or by a straightforward argument by analogy from  $SO_2-CO_2$  or  $SO_2-CCS$ . In  $SO_2-CO_2$ , the experimental structure had  $C_{2v}$  symmetry with the  $SO_2$  crossed relative to the  $CO_2$  axis [Fig. 4(a)]. In  $SO_2-CCS$ , the  $SO_2$  is shifted considerably from directly over the carbon atom compared to either  $SO_2-CCS_2$  or  $SO_2-CCS_2$ . This translation places the sulfur atom of the  $SO_2$  much more directly over the oxygen end of the  $SCS_2$  molecule [Fig. 4(c)].

The ORIENT modeling program reproduced  $R_{\rm CM}$  and came within  $6^{\circ}$  of the tilt angles in  $SO_2$ –OCS [Fig. 4(d)].<sup>2</sup> As noted above, the tilt angles are much less well reproduced for  $SO_2$ –CS<sub>2</sub> and similarly for  $SO_2$ –CO<sub>2</sub> [Fig. 4(b)]. For the latter, the  $C_{2v}$  structure was found as a transition state on the interaction potential energy surface, some 35 cm<sup>-1</sup> higher in energy than the less symmetric  $C_s$  structure in Fig. 4(b). We also have observed that the relative contributions from the electrostatic and dispersion terms in the ORIENT model vary significantly for the three  $SO_2$  complexes (Table X).

This mixed behavior in the modeling results is in contrast to the recent studies of the trimers CO<sub>2</sub>-CO<sub>2</sub>-OCS, <sup>22,23</sup> OCS-OCS-CO<sub>2</sub>, <sup>24</sup> and CO<sub>2</sub>-CO<sub>2</sub>-N<sub>2</sub>O, <sup>25</sup> where the simple ORIENT model used here (sans polarization) was remarkably successful in predicting rotational constants and assignment of the spectrum. Thus, this simple model can be very helpful to a spectroscopist in suggesting the general structural features and symmetry, and in some cases it even closely predicts the rotational constants. Additional comparisons between experiment and such models may be helpful to map out further the reliability patterns and perhaps suggest further improvements. While many essential features of the intermolecular forces are captured by the model, the simplicity of the terms included and the neglect of others such as polarization, and anisotropy in the dispersion and repulsion terms suggests that such complications are probably ultimately needed.<sup>20</sup> The quality of the distributed multipole moments from the ab initio calculation should also be systematically explored. In summary, the bent triatomic SO<sub>2</sub> is a good test case for exploring such modeling questions as it has proven to be frequently recalcitrant in both simple dimers like SO<sub>2</sub>–CS<sub>2</sub> and more complex ones.<sup>26</sup>

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