this calculation the transition state species is assumed to have equal bond lengths with the fluorine pairs on respective sides of a plane passing through the sulfur atom ( $C_{2 v}$ symmetry). In the equilibrium configurations, corresponding to the minima of the two potential wells, the fluorine atoms are all on one side of the plane. ${ }^{12,13} \quad\left(S-F_{\mathrm{ax}}=1.646 \AA\right.$ and $\left.S-F_{\text {eq }}=1.545 \AA .{ }^{12}\right)$ In order to estimate $V_{0}$, we assume that the force con$\operatorname{stant} f_{\beta}$ for the equatorial fluorine distortion is dominant in the exchange motion. A value for $f_{\beta}$ of $0.63 \mathrm{mdyn}-\AA$ is used ${ }^{7}$ in the expression for $V_{0}$. Although these considerations lead to a barrier, $V_{0}{ }^{\text {max }}$, corresponding to the intersection of the harmonic curves, it is probably more realistic to scale the barrier because of anharmonicity. ${ }^{10,11} V_{0}{ }^{\text {max }}$ was scaled by replacing the intersecting parabolas with a cosine function ${ }^{2}$ whose second derivative at each minimum is equivalent to those for the parabolas. Thus, $V_{0}{ }^{\text {final }}=\left(4 / \pi^{2}\right) V_{0}{ }^{\text {max }}=10.3 \mathrm{kcal} / \mathrm{mole}$. This close agreement with the barrier height from the eigenvalue fit of $10.0 \mathrm{kcal} / \mathrm{mole}$ is, perhaps, fortuitous, but it does add credence to the approach of fitting experimentally observed vibrationally excited transitions to a double minimum potential function. Finally, the barrier to intramolecular exchange in $\mathrm{SF}_{4}$, which we

Table I. Calculated excited vibrational levels v for $\mathrm{SF}_{4}$ from the quartic-harmonic potential function $V=14.62\left(z^{4}-31 z^{2}\right)$. (obs and calc frequencies are in $\mathrm{cm}^{-1}$.)

| obs | calc | $\Delta$ (obs-calc) | Assignment <br> $(v)^{9}$ |
| :---: | :---: | :---: | :---: |
| 227.6 | 227.6 | 0 | $0 \rightarrow 1$ |
| 224.5 | 224.6 | -0.1 | $1 \rightarrow 2$ |
| 221.0 | 221.6 | -0.6 | $2 \rightarrow 3$ |
| 219.0 | 218.6 | +0.4 | $3 \rightarrow 4$ |
| 215.5 | 215.3 | +0.2 | $4 \rightarrow 5$ |

Barrier height $V_{0}=10.0 \pm 0.5 \mathrm{kcal} / \mathrm{mole}$
calculate here from far-infrared data, is consistent with available NMR data for a series of pentacoordinated species in which the barriers occur between 6-12 $\mathrm{kcal} /$ mole. ${ }^{14}$

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# Structure and Conformation of Trimethylphosphine* 

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The structure of trimethylphosphine has been previously reported, but these investigations did not include the possibility of a small tilt of the methyl groups. ${ }^{1,2}$ Pierce et al. ${ }^{3}$ have pointed out that a methyl group attached to an atom possessing an unshared electron pair frequently is tilted toward the unshared pair. They further suggested that this effect might be associated with barriers to internal rotation.

Recent microwave studies of trimethylamine, ${ }^{4}$ monomethylphosphine, ${ }^{5}$ and dimethylphosphine ${ }^{6}$ have suggested methyl group tilts of $1^{\circ}-2^{\circ}$. Only in the case of $\mathrm{Me}_{3} \mathrm{~N}$ was this deduced from direct isotopic substitution. We report here evidence for methyl group tilts in $\mathrm{Me}_{3} \mathrm{P}$ from the analysis of the spectra of several deuterated species.

Samples of $\left(\mathrm{CH}_{2} \mathrm{D}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}(97 \%)$ and $\left(\mathrm{CD}_{3}\right)$ -

Table I. Observed ground state transitions and rotational constants for some deuterated trimethylphosphine species (megacycle/second).

| Transition | $\left(\mathrm{CD}_{3}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ | $\left(\mathrm{CH}_{2} \mathrm{D}_{a}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ | $\left(\mathrm{CH}_{2} \mathrm{D}_{5}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $2_{21}-1_{12}$ | 21804.06 | 22913.06 | 22615.71 |
| $2_{11}-1_{01}$ | 20702.50 | 22221.11 | 22333.63 |  |
| $2_{20}-1_{10}$ | 21370.70 | 22610.60 | 22482.25 |  |
| $3_{22}-2_{12}$ | 31879.61 | 33850.32 | 33711.57 |  |
| $3_{31}-2_{21}$ | 32772.98 | 34394.98 | 33928.07 |  |
| $3_{30}-2_{20}$ | 32318.45 | 34020.00 | 33742.21 |  |
| $3_{12}-2_{02}$ | 31441.18 | 33680.84 | 33680.75 |  |
| $3_{21}-2_{11}$ | 31136.49 | 33360.54 | 33505.11 |  |
| A | $5588.71 \pm 0.03$ | $5814.72 \pm 0.03$ | $5689.14 \pm 0.04$ |  |
| B | $5037.87 \pm 0.03$ | $5468.75 \pm 0.03$ | $5548.08 \pm 0.04$ |  |
| C | $3406.4 \pm 1$ | $3588 \pm 2$ | $3689 \pm 9$ |  |

$\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}(99 \%)$ were prepared by treating dimethylphosphine with the appropriate isotopic species of $\mathrm{CH}_{3} \mathrm{I} .{ }^{7}$ Their spectra were measured at approximately $-78^{\circ}$ with a conventional spectrometer ${ }^{8}$ and are accurate to $\pm 0.05 \mathrm{MHz}$.

The spectra of $\left(\mathrm{CD}_{3}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ and the two isotopic species of $\left(\mathrm{CH}_{2} \mathrm{D}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ are listed in Table I. The species possessing no symmetry element $\left(\mathrm{CH}_{2} \mathrm{D}_{a}\right)$ $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$, exhibited a spectrum which was approximately twice as intense as that of the species having a symmetry plane $\left(\mathrm{CH}_{2} \mathrm{D}_{s}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$. The assignments were confirmed from the Stark effect and rigid rotor frequency fit ( $\nu_{\text {obs }}-\nu_{\text {calc }} \leq|0.25| \mathrm{MHz}$ for all transitions). No torsional splittings were observed.

The hydrogen substitution coordinates ${ }^{9}$ calculated for the two $\left(\mathrm{CH}_{2} \mathrm{D}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ species show that each methyl group is staggered with respect to the other two PC bonds. For a symmetric top molecule, only the distance from the symmetry axis can be determined by substitution of an off-axis atom. Thus, it is impossible to calculate directly the distance between the equivalent out-of-plane H atoms in each methyl group (designated as $\mathrm{H}_{a}$ and $\left.\mathrm{H}_{a}{ }^{\prime}\right)^{4}$ from substitution coordinates alone. The distance, however, can be obtained from the expression $\quad 4\left(m_{\mathrm{D}}-m_{\mathrm{H}}\right) b_{\mathrm{H}_{a}}{ }^{2}=2 \mathrm{P}_{b}\left[\left(\mathrm{CD}_{3}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}\right]$ -

Table II. Coordinates of $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{P}$ (angstroms). ${ }^{a}$

| Atom | $a$ | $b$ | $c$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{P}$ | 0.0 | 0.0 | 0.5514 |
| C | 1.6174 | 0.0 | -0.3378 |
| $\mathrm{H}_{s}$ | 1.4771 | 0.0 | -1.4307 |
| $\mathrm{H}_{a}$ | 2.1809 | $\pm 0.8816$ | -0.0979 |

${ }^{\text {a }}$ The coordinates are expressed in the principal axis system of $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{P}$ in which the substituted atoms in those species which possess $C_{s}$ symmetry lie in the ac plane ( $b=0$ )
$\mathrm{I}_{c}\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{P}\right]$ since $r\left(\mathrm{H}_{a} \mathrm{H}_{a}{ }^{\prime}\right)=2\left|b_{\mathrm{H}_{a}}\right|$. The value of $\mathrm{I}_{c}$ for $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{P}$ was calculated from $\left(\mathrm{I}_{c}+\mathrm{I}_{a}-\mathrm{I}_{b}\right)$ of the $\left(\mathrm{CH}_{2} \mathrm{D}_{a}\right)\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}$ species since these values have the least experimental error. The value of $1.763 \AA$ obtained for $r\left(\mathrm{H}_{a} \mathrm{H}_{a}{ }^{\prime}\right)$ compared well with other $r\left(\mathrm{H}_{a} \mathrm{H}_{a}{ }^{\prime}\right)$ values. ${ }^{10,11}$

The structure was calculated three different ways by using the rotational constants from Ref. 1 along with those in Table I. In the first method, substitution coordinates were computed for the carbon and hydrogen atoms and the first moment equation was used for the phosphorous coordinate. The resulting structure was rather unsatisfactory ${ }^{10}$ because it gave $\angle \mathrm{HCH}$ values which were outside the range normally found for methyl groups. ${ }^{12}$ The primary cause was the small value for $c_{\mathrm{H}_{a}}$ since small substitution coordinates are subject to large errors from both experimental uncertainty and zero-point effects. ${ }^{13,14}$ Consequently, a first and second moment equation were solved simultaneously to determine $c_{\mathrm{P}}$ and $c_{\mathrm{H}_{a}}$ and the resulting coordinates are shown in Table II. The structure calculated from these coordinates is labeled structure A in Table III.

A third calculation was also undertaken to estimate what effect the assumption of bond shortening upon deuteration would have on the final structure. It was assumed that the average CH bond shortened by

Table III. Structural parameters of $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{P}$.

|  | Structure A | Structure B |
| :--- | :---: | :---: |
| $\mathrm{C}-\mathrm{H}_{s}(\AA)$ | 1.102 | $1.112 \pm 0.005$ |
| $\mathrm{C}-\mathrm{H}_{a}(\AA)$ | 1.073 | $1.090 \pm 0.010$ |
| $\mathrm{P}-\mathrm{C}(\AA)$ | 1.846 | $1.843 \pm 0.003$ |
| $\angle \mathrm{PCH}_{s}$ | $111.5^{\circ}$ | $111.4^{\circ} \pm 0.2^{\circ}$ |
| $\angle \mathrm{PCH}_{a}$ | $110.6^{\circ}$ | $109.8^{\circ} \pm 0.4^{\circ}$ |
| $\angle \mathrm{H}_{8} \mathrm{CH}_{a}$ | $106.8^{\circ}$ | $108.2^{\circ} \pm 0.8^{\circ}$ |
| $\angle \mathrm{H}_{a} \mathrm{CH}{ }_{a}{ }^{\circ}$ | $110.4^{\circ}$ | $109.4^{\circ} \pm 0.4^{\circ}$ |
| $\angle \mathrm{CPC}^{\circ}$ | $98.7^{\circ}$ | $98.9^{\circ} \pm 0.2^{\circ}$ |

$0.005 \AA$ upon deuteration. The resulting structure is referred to as B in Table III

Structures A and B compare well with the electron diffraction results: $r(\mathrm{PC})=1.846 \pm 0.003 \AA, r(\mathrm{CH})=$ $1.091 \pm 0.006 \AA, \angle \mathrm{CPC}=98.6^{\circ} \pm 0.3^{\circ}$ and $\angle \mathrm{PCH}=$ $110.7^{\circ} \pm 0.5^{\circ} .^{2}$ The differences between structures A and $B$ should be useful estimates of the uncertainties in the structural parameters caused by zero-point effects. The actual structure is probably closer to B. The error limits in structure B are those arising from experimental uncertainty alone.

It is interesting to compare structure B with the results for $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}$. ${ }^{4}$ The parameters involving the hydrogens are remarkably similar. For example, in $\mathrm{Me}_{3} \mathrm{~N}$ the $r\left(\mathrm{CH}_{s}\right)$ value ( $1.109 \pm 0.008 \AA$ ) is also found to be longer than the $r\left(\mathrm{CH}_{a}\right)$ value $(1.088 \pm 0.008 \AA)$. The calculation of $\left(\angle \mathrm{NCH}_{s}-\angle \mathrm{NCH}_{a}\right)$ for $\mathrm{Me}_{3} \mathrm{~N}$ and $\left(\angle \mathrm{PCH}_{8}-\angle \mathrm{PCH}_{a}\right)$ for $\mathrm{Me}_{3} \mathrm{P}$ both give $1.6^{\circ}$, which indicates that the methyl groups appear to be tilted slightly toward the unshared electron pair in both cases.

In conclusion, it appears that there are small methyl group tilts in $\mathrm{Me}_{3} \mathrm{P}$ and that $r\left(\mathrm{CH}_{8}\right)$ is slightly longer than $r\left(\mathrm{CH}_{a}\right)$. The effect is assuredly small, but the
repeated observation of the effect in this and similar molecules suggests that it is probably real.

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# Effect of Molecular Shape on the Dielectric Second Virial Coefficients of Polar Gases 

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Recently, a modified Stockmayer potential of the form

$$
\begin{aligned}
& U\left(R, \theta_{1}, \theta_{2}, \phi\right)=4 \epsilon\left[(\sigma / R)^{12}-(\sigma / R)^{6}\right] \\
& +C_{\alpha} R^{-14}-C_{\alpha}^{\prime} R^{-8}+C_{\beta} R^{-13}\left(\cos \theta_{1}+\cos \theta_{2}\right) \\
& +C_{\gamma} R^{-14}\left(3 \cos ^{2} \theta_{1}+3 \cos ^{2} \theta_{2}-2\right) \\
& +C_{\delta} R^{-14}\left(\sin \theta_{1} \sin \theta_{2} \cos \phi+13 \cos \theta_{1} \cos \theta_{2}\right) \\
& -C_{\beta}^{\prime} R^{-7}\left(\cos \theta_{1}+\cos \theta_{2}\right)-C_{\gamma}{ }^{\prime} R^{-8}\left(3 \cos ^{2} \theta_{1}+3 \cos ^{2} \theta_{2}-2\right) \\
& -C_{\delta}{ }^{\prime} R^{-8}\left(\sin \theta_{1} \sin \theta_{2} \cos \phi+7 \cos \theta_{1} \cos \theta_{2}\right) \\
& +\mu_{0}^{2} R^{-3}\left(2 \cos \theta_{1} \cos \theta_{2}+\sin \theta_{1} \sin \theta_{2} \cos \phi\right) \\
& \quad-\left(\alpha_{e} \mu_{0}^{2} / 2\right) R^{-6}\left(3 \cos ^{2} \theta_{1}+3 \cos ^{2} \theta_{2}-2\right)
\end{aligned}
$$

has been used to account for the effect of molecular shape on the dielectric second virial coefficients of simple gases of axially symmetric polar molecules. ${ }^{1,2}$ Estimating the coefficients $C_{\alpha}, C_{\beta}, C_{\gamma} \cdots$ from the knowledge of the pairwise interactions among the constituent atomic groups of the molecules, ${ }^{1,3}$ it was reduced to a function of only two adjustable parameters, $\epsilon$ and $\sigma$, that were determined from the experimental
ordinary second virial coefficient, $B$. The model then predicted the correct sign of the dielectric second virial coefficient, $\mathfrak{B}$, for $\mathrm{CH}_{3} \mathrm{~F}$ and $\mathrm{CHF}_{3}$. The lack of reliable experimental data made it difficult to further test the model in the previous papers. Recently, Sutter and Cole ${ }^{4}$ have reported experimental measurements of $B$ and $B$ at several temperatures for two additional gases, $\mathrm{CClF}_{3}$ and $\mathrm{CH}_{3} \mathrm{Cl}$, as well as more extensive measurements for $\mathrm{CH}_{3} \mathrm{~F}$ and $\mathrm{CHF}_{3}$. Their results show that $\mathcal{B}$ values of the halogenated methanes are very sensitive to differences in molecular shape. In this note, the foregoing molecular model is applied to calculate $\mathbb{B}$ for

Table I. Molceular and potential-energy parameters.

|  | $L$ <br> $(\AA)$ | $l$ <br> $(\AA)$ | $\mu_{0}$ <br> $(\mathrm{D})$ | $\alpha_{e} \times 10^{24}$ <br> $\left(\mathrm{~cm}^{3}\right)$ | $\epsilon / k$ <br> $\left({ }^{\circ} \mathrm{K}\right)$ | $\sigma$ <br> $(\AA)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Molecule |  |  |  |  |  |  |
| $\mathrm{CHF}_{3}$ | 0.021 | 1.444 | 1.649 | 3.57 | 190 | 4.60 |
| $\mathrm{CClF}_{3}$ | 0.724 | 1.408 | 0.51 | 5.59 | 150 | 5.40 |
| $\mathrm{CH}_{3} \mathrm{~F}$ | 0.612 | 0.773 | 1.81 | 3.55 | 270 | 4.058 |
| $\mathrm{CH}_{8} \mathrm{Cl}$ | 0.553 | 1.304 | 1.895 | 4.72 | 265 | 4.455 |


[^0]:    ${ }^{1}$ R. S. Berry, J. Chem. Phys. 32, 933 (1960).
    ${ }^{2}$ R. S. Berry, Rev. Mod. Phys. 32, 447 (1960).
    ${ }^{3}$ E. L. Mutterties and W. D. Phillips, J. Am. Chem. Soc. 81, 1084 (1959).
    ${ }^{4}$ R. A. Frey, R. L. Redington and A. L. K. Aljibury, J. Chem. Phys. 54, 344 (1971).
    ${ }^{5}$ R. L. Redington on C. V. Berney, J. Chem. Phys. 43, 2020 (1965).
    ${ }^{6}$ E. L. Muetterties, Inorg. Chem. 5, 769 (1965).
    ${ }^{7}$ I. W. Levin, "Calculation of Infrared Spectra Using CNDO/2 Techniques: An Application to $\mathrm{SF}_{4}$." (unpublished) Although Frey et al. ${ }^{4}$ assign the $\nu_{4}\left(a_{1}\right)$ mode at $228 \mathrm{~cm}^{-1}$ to the axial bending mode, reassignment of this mode to the equatorial bending motion of $\mathrm{SF}_{4}$ correlates better with the equatorial (in-plane) bend of $\mathrm{PF}_{\mathrm{j}}$ at $179 \mathrm{~cm}^{-1}$. (Note that $\mathrm{SF}_{4}$ can be considered a quasipentacoordinated system if the lone pair is viewed as a ligand.) For $\mathrm{PF}_{5}$, the 533 - and $179-\mathrm{cm}^{-1} e^{\prime}$ modes, primarily the axial and in-plane modes, respectively [I. Levin, J. Mol. Spectry. 33, 61 (1970) ; W. J. Adams and L. S. Bartell, J. Mol. Struct. 8, 23 (1971)] correlate with two of the $a_{1}$ and one of the $b_{2}$ modes of $\mathrm{SF}_{4}$. Thus, for the $\mathrm{SF}_{4} a_{1}$ bending modes, the lower vibration is expected to be the equatorial bend and would probably appear at a slightly higher frequency than that of the $\mathrm{PF}_{5} 179-\mathrm{cm}^{-1}$ transition. The weak infrared intensity for this motion in $\mathrm{SF}_{4}$ also follows from the virtually zero infrared intensity that arises for the in-plane $e^{\prime}$ bending mode of $\mathrm{PF}_{5}$. Finally, an approximate force field for $\mathrm{SF}_{4}$ supports this reassignment.
    ${ }^{8}$ J. Laane, Appl. Specty. 24, 73 (1970).
    ${ }^{9}$ We note that in this high barrier case, the eigenvalues $n$ for 0 and 1, 1 and 2, etc., are degenerate; thus, in the tables ${ }^{8}$ the degenerate 0 and 1 levels correspond to $v=0$, the degenerate 1 and 2 levels correspond to $v=1$, etc.)
    ${ }^{10}$ L. C. Hoskins and R. C. Lord, J. Chem. Phys. 46, 2402 (1967).
    ${ }^{11}$ R. R. Holmes and Sr. R. M. Dieters, Inorg. Chem. 7, 2229 (1968).
    ${ }^{12}$ W. M. Tolles and W. D. Gwinn, J. Chem. Phys. 36, 1119 (1962).
    ${ }^{13}$ K. Kimura and S. H. Bauer, J. Chem. Phys. 39, 3172 (1963).
    ${ }^{14}$ E. I. Muetterties, W. Mahler, K. J. Packer and R. Schmutzler, Inorg. Chem. 3, 1298 (1964).

[^1]:    * This work was supported by a grant from the National Science Foundation, Washington, D.C.
    ${ }^{1}$ D. R. Lide, Jr. and D. E. Mann, J. Chem. Phys. 29, 914 (1958).
    ${ }^{2}$ L. S. Bartell and L. O. Brockway, J. Chem. Phys. 32, 512 (1960).
    ${ }^{3}$ L. Pierce, R. G. Hayes, and J. F. Beecher, J. Chem. Phys. 46, 4352 (1967).
    ${ }^{4}$ J. E. Wollrab and V. W. Laurie, J. Chem. Phys. 51, 1580 (1969).
    ${ }^{5}$ T. Kojima, E. L. Breig, and C. C. Lin, J. Chem. Phys. 35, 2139 (1961).
    ${ }^{6}$ R. Nelson, J. Chem. Phys. 39, 2382 (1963).
    ${ }^{7}$ W. L. Jolly, Inorganic Syntheses, edited by W. L. Jolly (McGraw-Hill, New York, 1968), Vol. 11, p. 126.
    ${ }^{8}$ R. L. Kuczkowski, J. Am. Chem. Soc. 90, 1705 (1968).
    ${ }^{9}$ J. Kraitchman, Am. J. Phys. 21, 17 (1953).
    ${ }^{10}$ P. S. Bryan, Ph.D. thesis, University of Michigan, Ann Arbor, Mich., 1970.
    ${ }^{11}$ J. E. Wollrab and V. W. Laurie, J. Chem. Phys. 48, 5058 (1968).
    ${ }^{12}$ L. E. Sutton (Editor), Chem. Soc. (London), Spec. Publ. 11 (1958).
    ${ }^{13}$ C. C. Costain, J. Chem. Phys. 29, 864 (1958).
    ${ }^{14}$ D. R. Herschbach and V. W. Laurie, J. Chem. Phys. 37, 1668 (1962).

