THE UNIVERSITY OF MICHIGAN
COLLEGE OF ENGINEERING
High Altitude Engineering Laboratory
Departments of
Aerospace Engineering
Meteorology and Oceanography

Technical Report

THE EFFECT OF SEVERAL INFRARED TRANSPARENT
BROADENING GASES ON THE ABSORPTION OF INFRARED
RADIATION IN THE 15µm BAND OF CARBON DIOXIDE

ORA Project 05863

under contract with:
NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
CONTRACT NO. NASr-54(03)
WASHINGTON, D. C.

administered through
OFFICE OF RESEARCH ADMINISTRATION  ANN ARBOR

May 1969
This report was also a dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in The University of Michigan, 1969.
THE EFFECT OF SEVERAL INFRARED TRANSPARENT BROADENING GASES ON THE
ABSORPTION OF INFRARED RADIATION IN THE 15 $\mu$m BAND OF CARBON DIOXIDE

by
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A dissertation submitted in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy in
The University of Michigan
1969

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ACKNOWLEDGMENTS

As is the case in most investigations of this type, the work reported here is the result of the efforts of many people. The author would like to thank all of those who contributed. The advice and help of Professor Frederick Bartman, Chairman of the Doctoral Committee and Professor Charles Young of the University of New Brunswick, whose advice during the early part of the investigation and during the data analysis was most helpful, are particularly appreciated. The author is also grateful to Professors Edward Boettner, Leslie Jones, and William Kuhn for serving as members of the Committee and for their help and suggestions during the course of the work.

The help of the staff of the High Altitude Engineering Laboratory is appreciated. Among them the author would most like to thank Mr. Charles Hubler, whose assistance in all phases of this investigation was of great value.

The financial support received from the Goddard Space Flight Center of the National Aeronautics and Space Administration under contract NASR-54(03) and the loan of the spectrophotometer by the Langley Research Center of the National Aeronautics and Space Administration is acknowledged.

Finally the author would like to thank his wife for her patience, encouragement, and financial support and the other members of his family (including Mrs. Donald Reichle, who typed this paper) for their encouragement and help.
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a
A
A_v
B
B'
B_{avg}
B_i
B_A
B_{He}
B_{N_2}
B_{O_2}
c
C
C_{aa}
C_{ab}
D_{aa}
D_{ab}
D_{aN_2}
D_{CO_2CO_2}
a constant
equivalent width
wavenumber dependent absorptivity
broadening coefficient
mean value of the wavenumber dependent broadening
coefficient
average value of the broadening coefficient
broadening coefficient for gas i
broadening coefficient for argon
broadening coefficient for helium
broadening coefficient for nitrogen
broadening coefficient for oxygen
speed of light
absorber concentration
constant involving collision diameter and molecular
weight of an absorber
constant involving collision diameter and molecular
weights of an absorber and a broadener
optical collision diameter for collisions of the
absorber with itself
optical collision diameter for collisions of the
absorber with a broadening gas
optical collision diameter for collisions of the
absorber with nitrogen
optical collision diameter for collisions between
carbon dioxide molecules
$D_{\text{CO}_2}$ b optical collision diameter for collisions between carbon dioxide molecules and a broadening gas

E extinction coefficient

E energy

f frequency

$f_0$ frequency of the line center

F broadening factor

$F'$ broadening factor calculated from the mean value of the wavelength dependent broadening coefficients

$F_i$ broadening factor for gas $i$

$F_A$ broadening factor for argon

$F_{\text{He}}$ broadening factor for helium

$F_{\text{N}_2}$ broadening factor for nitrogen

$F_{\text{O}_2}$ broadening factor for oxygen

h Planck's constant

I intensity of the transmitted radiation

$I_0$ intensity of the incident radiation

k Boltzmann's constant

$k_f$ absorption coefficient at frequency $f$

$k_o$ absorption coefficient at the line center

$k_\nu$ absorption coefficient at wavenumber $\nu$

l path length

l cell length

m mass
\( M_a \) molecular weight of the absorbing molecule

\( M_b \) molecular weight of the broadening molecule

\( N_a \) number density of the absorbing gas

\( N_b \) number density of the broadening gas

\( P_a \) partial pressure of the absorbing gas

\( P_b \) partial pressure of the broadening gas

\( P_e \) effective pressure

\( P_i \) partial pressure of gas i

\( P_x \) calibration pressure

\( P_A \) argon partial pressure

\( P_{CO_2} \) carbon dioxide partial pressure

\( P_{He} \) helium partial pressure

\( P_{N_2} \) nitrogen partial pressure

\( P_{O_2} \) oxygen partial pressure

\( P^L_e \) effective pressure in the long cell

\( P^S_e \) effective pressure in the short cell

\( P^L_{CO_2} \) carbon dioxide partial pressure in the long cell

\( P^S_{CO_2} \) carbon dioxide partial pressure in the short cell

\( S \) a constant generally called the line strength

\( t \) time

\( T \) temperature
$T_{\text{cell}}$ transmissivity of the sample cell relative to the transmissivity of the reference cell

$T_{\text{ind}}$ transmissivity as indicated by the spectrophotometer

$T_{\text{reference cell}}$ transmissivity of the cell in the reference beam

$T_{\text{sample cell}}$ transmissivity of the cell in the sample beam

$T_\nu$ wavenumber dependent transmissivity

$V$ particle velocity

$w$ optical mass

$Z_{\text{off}}$ zero offset

$\alpha$ line half width at half maximum

$\alpha_D$ Doppler halfwidth

$\alpha_L$ Lorentz halfwidth

$\alpha_N$ natural halfwidth

$\lambda$ wavelength

$\mu$ Dipole moment

$\nu$ wavenumber

$\nu_{\text{min}}$ minimum wavenumber

$\nu_{\text{max}}$ maximum wavenumber

$\tau$ mean time between molecular collisions
ABSTRACT

The objective of this investigation is to determine the effects of argon, helium, nitrogen and oxygen on the absorption of radiation by carbon dioxide in the 15μm (667 cm⁻¹) region. The investigation is carried out at medium resolution (approximately 3 to 5 cm⁻¹) and at gas pressures that are less than one atmosphere. After a review of previous experimental and theoretical work pertinent to the investigation the expressions defining the broadening coefficient and the broadening factor are given. The experimental apparatus used to measure the effects of the various broadening gases is described and the experimental procedure is discussed. The results of the investigation are presented in the form of a band averaged broadening coefficient for nitrogen, band averaged broadening factors for argon, helium and oxygen, and wavelength dependent broadening coefficients for argon, helium, nitrogen and oxygen. It is found that the band averaged broadening coefficient for nitrogen and the band averaged broadening factors for argon and oxygen are in good agreement with previous experimental results in other carbon dioxide absorption bands. The band averaged value of the broadening factor for helium, however, is found to be significantly higher than values previously obtained in the 2350cm⁻¹ band.

The wavelength dependent broadening coefficients are found to be more complex in structure than previous determinations have
indicated. It is noted that the broadening coefficients for argon, nitrogen and oxygen are qualitatively similar to each other but are quite different from the broadening coefficient for helium. It is shown that the fine structure of the wavelength dependent broadening coefficient is correlated with the presence of several absorption bands having strong Q branches in the 15μm region. Comparisons of the mean values of the wavelength dependent broadening coefficients are used to substantiate the previously determined values of the band averaged broadening factors.

The wavelength dependent broadening coefficient for nitrogen is compared to previously calculated theoretical predictions of this quantity. It is shown that, although Anderson's theory successfully predicts the mean value and general features of the wavelength dependent broadening coefficient, it fails to predict the sharp peaks in the broadening coefficient that are observed in the vicinity of the frequencies of the main Q branches. On the basis of a qualitative argument it is shown that the peaking of the broadening coefficient in the vicinity of Q branches and the unusual behavior of the broadening coefficient for helium could be explained by deviations of the line shape from the theoretical line profile similar to those that have been observed in other carbon dioxide absorption bands or by a variation of the line half width with rotational quantum number.
CHAPTER 1

INTRODUCTION

The advent of the sounding rocket, the earth orbiting satellite and the interplanetary spacecraft has placed in the hands of meteorologists and atmospheric scientists powerful new tools for measuring the characteristics of planetary atmospheres. The effective use of these devices often involves inferring the desired information from remotely sensed data. At the present time, one very widely used technique involves scanning a planetary atmosphere using radiometers, spectrometers or interferometers operating in the infrared region (1-50 $\mu m$). This spectral region is of great interest because the black body emission of the planetary surface peaks at these wavelengths, and because some important gases present in planetary atmospheres e.g., water vapor, carbon dioxide and ozone, have strong absorption bands in this spectral region. Furthermore, the distribution of these gases, with their strong absorption bands, influences the temperature structure of the atmosphere. Before the properties of the planetary atmosphere can be properly inferred from the remotely sensed data or the atmospheric structure can be properly understood, it is necessary to have a complete understanding of the radiative transfer problem for the atmosphere. This involves an accurate knowledge of the transmission properties of the infrared optically active gases.

In the past the transmission properties of the atmospheric gases have generally been obtained using idealized mathematical models, called band models. A band model, for example, assumes some distri-
bution of absorption lines which enables the transmission to be readily obtained analytically and is primarily used to facilitate hand solution of the radiative transfer problem. The models have become inadequate because of their basic limitations and fundamental inaccuracies, particularly, as the problem of translating measurements taken at satellite altitudes into knowledge of the atmospheric structure has become better known. The high speed digital computer with large information storage capability has, however, made it possible to calculate the transmission properties of a gas directly from knowledge of the positions, shapes, strengths and widths of the absorption lines comprising an absorption band. Unfortunately, much of the very accurate information required for calculations of this type is not available at the present time. Most of the existing theoretical and experimental work has been done for highly polar molecules such as hydrogen chloride. Generally, the data have been obtained for samples of pure gas or for samples using nitrogen as a broadening gas, the data for broadening by other transparent gases being very limited. Since the gases that are active in the infrared region are trace constituents in the atmosphere of the earth, it is important that the effects of the other atmospheric gases on the absorption properties of the optically active gas be known.

This paper discusses the results of a medium resolution spectroscopic investigation of the effects of several broadening gases on the absorption properties of carbon dioxide in the 15 μm band. The broadening gases used (argon, helium, nitrogen and oxygen) were selected because of their possible importance in the atmosphere of the earth or other planets (argon, nitrogen, and oxygen) or because
of some unusual property (the low mass of helium).

The introduction will be concluded with a review of the literature concerning previous experimental work on foreign gas broadening for carbon dioxide. Chapter 2 is devoted to a summary of the theory of line broadening and the development of a set of semi-empirical relations that will define experimentally measurable parameters related to the widths of the absorption lines. The experimental apparatus is described in detail in Chapter 3. In Chapter 4 spectra for nitrogen broadened carbon dioxide samples are presented. These are compared with spectra obtained by other experimenters under similar test conditions and with absorption spectra obtained by the direct computational technique described by Drayson and Young (1966) and Drayson et al., (1968). Chapters 5 and 6 are devoted to a study of the band averaged broadening abilities of the gases. Chapter 7 discusses the wavelength dependence of the broadening ability of the various gases. Comparisons with the predictions of Anderson's Theory (Anderson, 1949) for nitrogen as the broadening gas obtained by Yamamoto et al., (1968) are presented and possible reasons for the differences between theory and experiment are discussed. The wavelength dependence of the broadening abilities for the various gases is compared and possible mechanisms to explain the differences are offered. The report concludes with Chapter 8 which summarizes the principal findings of the work and suggests possible areas for future research efforts.

Although absorption line broadening as a result of the Doppler effect had been studied earlier, the effects of other perturbing molecules was begun by Michelson (1895). It was his conclusion that the
nature of the perturbing gas would be of secondary importance. The work on foreign gas broadening was continued primarily in Europe until approximately 1940. It was during this interval that it became possible to resolve the structure of the bands and to examine the transmission properties of the gas for more or less monochromatic radiation. A review of the work in the field performed prior to 1944 is given by Nielsen et al., (1944). Coggeshall and Saier (1947) reported the effects of several broadening gases on the absorption of radiation by methane at 7.65 \( \mu \text{m} \) and carbon dioxide at 4.3 \( \mu \text{m} \) and 14.8 \( \mu \text{m} \). On the basis of their experiments at a single wavelength in each band, they concluded that the effects of a broadener would vary for different active gases and for different absorption bands of a single active gas. Following this was a paper published by Burch et al., (1962) which reported a very extensive study of the band averaged effects of several transparent gases on the absorption of infrared radiation by active gases in a number of absorption bands; among them was the 4.3 \( \mu \text{m} \) band of carbon dioxide. During the period from 1947 to 1962, a number of papers was published on the effects of broadening gases on the absorption spectra of nitrous oxide (Goody and Wormell, 1951), hydrogen chloride (Benedict et al., 1956 a & b; Eaton and Thompson, 1959), and carbon monoxide (Benedict et al., 1961; Crane-Robinson and Thompson, 1962). Also during this period the study of the broadening ability of nitrogen on carbon dioxide spectra was being investigated (Howard et al., 1956; Edwards, 1960), and a book discussing spectral lines was published (Breene, 1961). By observing the high frequency wing of the 4.3 \( \mu \text{m} \) band of carbon dioxide, Winters et al., (1964) were able to infer the shape of the far wings of the collision
broadened absorption lines located near the band center. They found that the line shape varied with the broadening gas. This method was applied to other carbon dioxide bands at shorter wavelengths by Burch et al., (1968) with generally similar results. Anderson et al., (1967) reported a study of the wavelength dependence of the broadening of carbon dioxide spectra by nitrogen in the 4.3 \( \mu \text{m} \) region, and at approximately the same time Vasilevskii et al., (1967) reported measurements made in the 2.06 \( \mu \text{m} \) band, again using nitrogen as the broadening gas. Using a continuous output infrared laser it has recently become possible to study the transmission properties of a gas using a very nearly monochromatic source. This device has been applied to the study of foreign gas broadening of carbon dioxide lines by several groups of researchers. Among papers which discuss the techniques and the results of experiments are Rosetti et al., (1967), Drayson and Young (1967), McCubbin and Mooney (1968), and Patty et al., (1968). The work has generally been carried out in the 9.6 and 10.4 \( \mu \text{m} \) carbon dioxide bands.

From the foregoing discussion, it is evident that the number of studies of the effects of foreign gases for broadening spectral lines in the infrared region have increased greatly in recent years. It will be noted that the 15 \( \mu \text{m} \) region of carbon dioxide has remained relatively unexplored. This probably results from the fact that this region is made up of several overlapping absorption bands with closely spaced lines. It is hoped that the research reported in the following chapters will further our knowledge of this very important spectral region.
CHAPTER 2
THEORY

2.1 **Introduction**\(^1\)

Theoretical and experimental studies of the absorption of electromagnetic radiation by materials have been conducted for many years. These studies have resulted in the formulation of laws concerning the transmission of radiation through the material, the discovery of exceptions to these laws, and the development of several theories which attempt to explain the empirical laws. In this chapter we will examine the laws relevant to the experimental work which is discussed later and to the broadening of absorption lines. The relative importance of several broadening mechanisms will be discussed and the broadening source most important for measurements made in this work identified. Finally, we will derive equations (based on a simplified theory) that will allow us to draw certain conclusions from the measurements made using a medium resolution infrared spectrophotometer.

2.2 **Lambert's Law and Beer's Law**

When a parallel beam of monochromatic radiation passes through a medium, it may be observed that

\[
I = I_0 e^{-kl}
\]  

(2.2.1)

\(^1\)In addition to those specifically noted, references for this chapter are Goody (1964), Gordy et al., (1953), Loeb (1961), Nielson et. al., (1944), Townes and Schlawlow (1955) and Winters (1963).
where $I = \text{the intensity of the transmitted beam}$

$I_0 = \text{the intensity of the incident beam}$

$l = \text{path length in the medium}$

$k = \text{absorption coefficient}$

This law, now generally called Lambert's Law, was discovered approximately 200 years ago. Roughly 100 years later A. v. Beer noted that the absorption coefficient, $k$, was often proportional to the concentration of the absorbing material. In a mixture of absorbers, Beer stated that the absorption coefficient was given by the expression

$$k = C_1E_1 + C_2E_2 + C_3E_3 + \ldots + C_nE_n$$

(2.2.2.)

where $C_1, C_2, C_3, \ldots, C_n$ are the concentrations of the absorbing components and $E_1, E_2, E_3, \ldots, E_n$ are characteristic of the individual components and are called extinction coefficients. Lambert's Law is easily derived if one assumes that the change in intensity in a thin layer is proportional to the intensity of the beam incident on the layer and to the thickness of the layer. Beer's Law follows from the assumption that each molecule in the layer absorbs independently from every other molecule.

Deviations from Beer's Law were first observed for carbon dioxide in the infrared region by Ångström, (1893, 1901, 1908). He constructed an absorption cell which was divided by a transparent partition into two equal halves, giving him two cells in series. One-half of the cell was filled with carbon dioxide while the other half was evacuated. The intensity of the infrared radiation passing through the cell was then measured. Next, a valve was opened between the two halves of the cell, allowing the carbon dioxide to fill the entire cell.
When the radiation passing through the cell was again measured, it was found that the intensity of the transmitted radiation had increased in apparent violation of Lambert's and Beer's Laws. When dry, carbon dioxide free air was admitted to the cell to increase the pressure to the original level, the absorption increased to the amount originally observed. On the basis of this experiment, Ångström concluded that the increased absorption was caused by pressure broadening of unresolved absorption lines or bands. This conclusion has since been shown to be correct. Since the time of Ångström, much theoretical and experimental effort has been expended in attempting to define the characteristics of the absorption lines and of the broadening mechanisms.

2.3 **Line Broadening and Line Shapes**

The sources of spectral line broadening that must be considered for carbon dioxide spectra in the infrared spectral region are:

1. Natural line broadening
2. Doppler effect
3. Pressure or collision broadening, i.e., disturbances caused by interaction between gas molecules

2.3.1 **Natural Line Widths**

The Heisenberg uncertainty principle shows that

\[ \Delta E \Delta t \geq \frac{h}{2\pi} \]  

(2.3.1)

where \( \Delta E \) is the energy spread in the excited state and \( \Delta t \) is the mean time the molecule spends in the excited state. The natural line width may be thought of as a disturbance of the molecule by zero point free space electromagnetic fields. For molecules having a permanent
electric dipole moment, a transition of frequency from an excited state to the ground state will give an absorption line of half width at half maximum of

$$\Delta f = \frac{32\pi^3 f^3 |\mu|^2}{3hc^3}$$

(2.3.2)

where $f =$ frequency

$h =$ Planck's constant

c = speed of light = $3 \times 10^{10}$ cm sec$^{-1}$

$|\mu|$ = dipole moment in esu

For molecules like carbon dioxide which do not have a permanent dipole moment, the interaction between the molecule and the external field will take place through higher order moments, e.g., the quadrupole moment. The term $|\mu|^2$ in the above equation would then be replaced by terms in these higher order moments which have been neglected (because they are small with respect to the usual permanent dipole moment). We may still use the above equation to calculate an upper limit to the line width due to natural broadening for carbon dioxide by assuming some value of a fictitious dipole moment that may reasonably be expected to be large compared to the actually existing higher order moments. First, the equation is placed in a form more suitable to the units normally used in infrared spectroscopy. By means of the relations

$$\Delta f = c\Delta \nu \text{ and } \lambda = c/\nu$$

where $\lambda =$ wavelength in cm and $\nu =$ wavenumber in cm$^{-1} = 1/\lambda$

then
\[ \Delta \nu = \alpha_N = \frac{2 \pi}{3hc} \left| \mu \right|^2 \]  \hspace{1cm} (2.3.3)

For a wavelength of 10\(\mu\)m and a dipole moment of 1 debye (10\(^{-18}\) esu), which is typical of a polar molecule such as ammonia, one finds that \(\alpha\) is approximately 10\(^{-9}\) cm\(^{-1}\). This is negligible in comparison with the minimum value of the half width observed in a planetary atmosphere, the minimum value being on the order of 10\(^{-3}\) cm\(^{-1}\).

2.3.2 Doppler Broadening

The apparent shifting of the frequency of a beam of radiation caused by the motion of the molecules in the direction of propagation of the beam leads to a finite absorption line width. The apparent wave number shift is

\[ \Delta \nu = \nu \left( \frac{v}{c} \right) \]  \hspace{1cm} (2.3.4)

where \(\nu\) = the wave number of the radiation

and \(v\) = the velocity of the molecule in the direction of the beam.

Assuming a Maxwellian distribution of velocities, the probability that a molecule of a gas has a velocity, \(v\), in a particular direction is proportional to

\[ e^{-mV^2/2kT} \]

where \(m\) = molecular mass

\(k\) = Boltzmann's constant

\(T\) = absolute temperature

Then, the line intensity becomes

\[ k \nu = k_o e^{-\frac{mc^2}{2kT} \left( \frac{\nu - \nu_o}{\nu_o} \right)^2} \]  \hspace{1cm} (2.3.5)
where \( k_o \) = the absorption coefficient at the line center and \( \nu_o \) = the wavenumber of the line center.

It can be seen that the line is symmetric about \( \nu_o \) and has a half width at half maximum of

\[
\alpha_D = \frac{\nu_o}{c} \sqrt{\frac{2kT}{m} \ln 2} = 3.581 \times 10^{-7} \sqrt{\frac{T}{M}} \nu_o \tag{2.3.6}
\]

where \( M \) is the molecular weight. Thus, for carbon dioxide at \( T = 300^\circ \) K and a wavelength of 10 \( \mu \)m, the Doppler half width is approximately equal to \( 10^{-3} \) cm\(^{-1}\). This is negligible compared to the half width observed at atmospheric pressure (approximately \( 10^{-1} \) cm\(^{-1}\)). However, it is comparable to the observed half width at a pressure of \( 10^{-3} \) atmospheres, and consequently, Doppler broadening must be taken into account at low pressures.

2.3.3 Collision or Pressure Broadening

Natural and Doppler line widths have been shown to be small at gas pressures of the order of one atmosphere. It would then appear that pressure or collisional broadening will be the major source of the broadening of absorption lines at moderate pressures.

The study of the collisional broadening of spectral lines produced by the perturbing effects of other molecules was first studied by Michelson (1895). The work was continued by Lorentz, who published the results of a study (Lorentz, 1906) discussing the Lorentz line profile. He considered the molecules as a group of classical oscillators, each of which oscillates at constant amplitude, but is abruptly stopped after some time, \( t \), where the number oscillating for time \( t \), is given by \( N_t = N_0 e^{-t/\tau} \), where \( \tau \) is the mean time between collisions. Upon restarting, the phase of the oscillation is assumed to be random.
with respect to the phase at the time of the interruption. For a rotating molecule, this is equivalent to saying that the orientation is random. On the basis of the above assumptions, it is found that the absorption coefficient is of the form

\[ k_f = \frac{S}{\pi} \left( \frac{\alpha_L}{(f - f_o)^2 + \alpha_L^2} \right) \]  \hspace{1cm} (2.3.7)

where \( S \) = a constant generally called the line strength

\( f_o \) = frequency of line center (natural frequency of the oscillators)

\( \alpha_L \) = Lorentz half width at half maximum \( = 1/2\pi\tau \) \hspace{1cm} (2.3.7a)

The Lorentz theory was extended by Van Vleck and Weisskopf (1945). They assumed that at the time that a radiating molecule undergoes a collision the phase following the collision is not random (as in the Lorentz model), but rather follows a Boltzmann distribution with respect to the electric field. Using a classical theory, a result is obtained that is somewhat similar to the Lorentz expression.

\[ k_f = \frac{S}{\pi} \left( \frac{f}{f_o} \right)^2 \left( \frac{\alpha_L}{(f - f_o)^2 + \alpha_L^2} + \frac{\alpha_L}{(f + f_o)^2 + \alpha_L^2} \right) \]  \hspace{1cm} (2.3.8)

Since in the infrared region \( \alpha_L \ll f_o \) the above expression reduces to the Lorentz profile in that region. If \( \alpha_L \approx f_o \) as it may be in the microwave region, the second term introduces asymmetry into the profile. At high frequencies far from the line center, this profile would predict constant absorption. Many comparisons between experimental line shapes and the Van Vleck-Weisskopf shape have been made. At low pressures, the agreement is quite good in the microwave region,
however, the agreement deteriorates seriously at higher pressures.

Even if it were possible to develop line shapes of the type previously discussed that were in agreement with experimentally determined line shapes, the situation would still not be entirely satisfactory. It would be necessary to empirically fit certain parameters of the line shape, e.g., the half width or collision frequency (which is related to the half width) to match the data. One might think that the collision frequency could be obtained from kinetic theory. Unfortunately, however, results of attempts at this generally yield half widths that are consistently lower than observed absorption line half widths indicating that the kinetic collision cross section must be smaller than the optical collision cross section.

Several attempts at relating pressure or collisional broadening to the intermolecular forces have been made. The problem is so complex, however, that the theories developed are subject to many simplifying assumptions and, therefore, usually only apply under rather limited conditions. In general, the theories can be divided into two types, viz., impact theories and statistical theories. In impact theories, it is assumed that most of the time, a molecule is far enough from other molecules so that it may be considered free. Occasionally, however, it approaches another molecule closely enough that its energy levels are perturbed. During the encounter with this molecule, a transition may or may not occur. It is usually assumed that radiation takes place during the time that the molecule is free and that interruption takes place only during the brief and infrequent encounters. Statistical theories, on the other hand, assume that the
molecule is always under the influence of other molecules, although the influence of the other molecules may be weak. The intensity of the radiation at any frequency depends on the probability that the molecule is perturbed enough by other molecules to make it radiate at that frequency. Although either theory can, in principle, produce good results, both break down in practice when the simplifying assumptions become unrealistic. The impact theories become inaccurate at high pressures when the collisions are frequent and the radiation during collisions becomes important while the statistical theories produce good results only at low particle velocities.

The statistical method was introduced by Kuhn and London (1934) and Kuhn (1934). Their analysis predicted a highly asymmetric line shape. This shape has been observed at visible wavelengths. Margenau (1949) developed a more sophisticated statistical theory and applied it to the spectrum of ammonia. The theory predicted half widths that were approximately correct and that varied in approximately the correct manner. Systematic variations between the theory and experimental results do exist.

Collision theories for optical and infrared wavelengths have been given by Lindholm (1945) and Foley (1946). The results of their theory (which assumes no collision caused transitions) indicate that for strong collisions, the line shape would be of the Lorentz type. When weaker collisions were taken into account, however, it was found that there was not only a broadening of the line about the center frequency, but also a shift in the frequency of the line center. The effect of the weak collisions was to decrease the center frequency. The line shape produced was of the type
\[
  k_f = \frac{\text{constant}}{(f - f_o \pm a\alpha)^2 + \alpha^2} \quad (2.3.9)
\]

It can be seen from this that the shift in center frequency is proportional to the line half width.

The most nearly complete impact theory to date has been developed by Anderson (1949). Although originally published for dipole-dipole interactions, the theory has been extended by Tsao and Curnutte (1962) to the case of dipole-quadrupole and quadrupole-quadrupole interactions. Based on the assumption that the relative motions of the particles are classical and that the time of collisions is small and allowing transitions to occur during collisions, Anderson determined the line shape to be as follows:

\[
k_f = \frac{S}{\pi} \left( \frac{f}{f_o} \right)^2 \left( \frac{\alpha}{(f - f_o - a\alpha)^2 + \alpha^2} + \frac{\alpha}{(f + f_o + a\alpha)^2 + \alpha^2} \right) \quad (2.3.10)
\]

where \( S \) = a constant generally called the line strength

\( f_o \) = frequency of the line center

\( \alpha \) = line half width at half maximum

It can be seen that this is similar to the Van Vleck-Weisskopf line shape except that the possibility of a center frequency shift is allowed. The theory predicts that this shift should be small for resonant self broadening and should be small in most other cases. These predictions have been verified experimentally. Line half widths, computed by means of Anderson's theory, have been determined for the self broadened spectrum of ammonia and the agreement is quite good. The results for foreign broadened ammonia spectra have been less satisfactory, although they are not too bad if the broadener has a
dipole moment not too different from the dipole moment of ammonia. Recently, attempts have been made to apply Anderson's theory to foreign broadened carbon dioxide spectra (Yamamoto, et al., 1968). The results of these calculations will be compared to our data in a later chapter.

In summary, it appears that the theory for the prediction of the spectra of pressure broadened gases is not yet complete. Even Anderson's theory, which is probably the best available, applies for the most part, near the line centers. The situation in the wings of lines where the force fields are more poorly known and possibly multiple collisions become more important (all of the impact theories discussed assume binary collisions) is even less well understood. In most of the work done in predicting spectra on the basis of known line positions, the line shape is being assumed and strengths and half widths empirically fitted. The line shape generally used in these calculations is the Lorentz profile at high pressures (typically $p > 0.1$ atmospheres) and a convolution of the Doppler and Lorentz profiles (called the Voigt profile) at lower pressures. The Voigt profile may either be read from precomputed tables or calculated directly, depending upon the problem to be solved and the facilities available. Methods of calculating the profile are discussed by Young (1965a), and precomputed tables of the profile have been presented by several persons including Posener (1959), Faddeeva and Terentev (1961), Fried and Conte (1961) and Young (1965b). A technique using empirically fitted line widths and calculated positions is described by Drayson and Young (1966) and Drayson, et al., (1968).
2.4 The Broadening Coefficient and Broadening Factor

In view of the present theoretical situation, we will proceed with the experimental work on the basis of a semiempirical set of relationships discussed below. The experimental data presented in succeeding chapters based on these relationships should be useful for the development of theories more sophisticated than that presented here. On the basis of assumed Lorentzian profiles, expressions will be developed for parameters (the broadening coefficient and the broadening factor) which will be a measure of the abilities of various infrared optically transparent gases for broadening carbon dioxide spectral lines.

As was noted in the discussion of the Lorentz theory, the half width of a Lorentz line is

\[ \alpha_L = \frac{1}{2 \pi \tau} \]

where \( \tau \) is the mean time between collisions.

From kinetic theory, the collision frequency of an absorbing molecule, \( a \), in a mixture with a broadening molecule, \( b \), is (Chapman and Cowling, 1939)

\[ \Gamma = 2 \pi \left( \frac{2kT}{\pi} \right)^{1/2} \left( \frac{N_a (D_{aa})^2}{M_a} \right)^{1/2} + N_b (D_{ab})^2 \left( \frac{M_a}{M_a + M_b} \right)^{1/2} \left( \frac{M_a + M_b}{M_a M_b} \right) \]

(2.4.1)

where \( k \) = Boltzmann's constant

\( T \) = absolute temperature

\( D_{aa} \) = optical collision diameter for absorber with itself

\( D_{ab} \) = optical collision diameter for collisions between absorber and broadener
\[ N_a = \text{number density of absorber} \]
\[ N_b = \text{number density of broadener} \]
\[ M_a = \text{molecular weight of the absorbing molecule} \]
\[ M_b = \text{molecular weight of the broadening molecule} \]

then

\[ \alpha_L = \frac{\Gamma}{2\pi} = \left(\frac{2kT}{\pi}\right)^{1/2} \left( N_a (D_{aa})^2 \left( \frac{2}{M_a} \right)^{1/2} + N_b (D_{ab})^2 \left( \frac{M_a + M_b}{M_a M_b} \right)^{1/2} \right) \]

(substituting \( N_a = \frac{P_a}{kT} \) and \( N_b = \frac{P_b}{kT} \))

and letting

\[ C_{aa} = (D_{aa})^2 \left( \frac{2}{M_a} \right)^{1/2} \]

\[ C_{ab} = (D_{ab})^2 \left\{ \frac{(M_a + M_b)}{(M_a M_b)} \right\}^{1/2} \]

\[ B = \frac{C_{aa}}{C_{ab}} \]

one finds

\[ \alpha_L = \left( \frac{2}{\pi kT} \right)^{1/2} C_{ab} (P_b + BP_a) \]

The quantity, \( B \), will be referred to in this paper as the broadening coefficient. (In most papers it is referred to as the self-broadening coefficient). The quantity \( (P_b + BP_a) \) is generally referred to as the equivalent pressure and is called that here. From the broadening coefficient, the ratio of the optical diameters can be readily determined by substituting Eq. (2.4.2a) and Eq. (2.4.2b) into
(Eq. (2.4.2c) and solving for the ratio of the collision diameters.

This yields

\[
\frac{D_{aa}}{D_{ab}} = p^\frac{1}{2} \left( \frac{\frac{M_a}{2} + \frac{M_b}{M_b}}{M_a + M_b} \right)^\frac{1}{4}
\]

(2.4.4)

It is sometimes desirable to determine the broadening ability of an optically transparent gas relative to the broadening ability of a second optically transparent gas; in some cases this improves the experimental-accuracy. In this case, nitrogen is generally used as the reference gas. A quantity named the broadening factor, \( F \), is defined by

\[
F_i = \frac{P_{N_2}}{P_i}
\]

(2.4.5)

where \( P_{N_2} \) = nitrogen partial pressure to produce a given transmittance

\( P_i \) = partial pressure of \( i \)th gas required to produce on equal transmittance.

Depending upon the goals of the experiment and the available equipment both the broadening coefficient and the broadening factor may be determined as a function of wavelength or as band-averaged quantities. The broadening factor \( F_i \), for a gas \( i \), is related to the broadening coefficient for that gas and the broadening coefficient for nitrogen by the relationship

\[
F_i = \frac{B_{N_2}}{B_i}
\]

(2.4.6)

This can be shown to follow from the definitions of the broadening factor and broadening coefficient by writing Eq. (2.4.3) for
nitrogen and for the $i$th broadening gas. Assuming that equal transmissivity implies equal line widths, the two expressions can be equated and solved for $P_{N_2}/P_i$. The result will be equation (2.4.6).

The broadening coefficient and broadening factor will differ from gas to gas and will represent a measure of the line broadening ability of each gas.

The equipment and techniques used for an experimental determination of the band-averaged broadening coefficient for nitrogen, band-averaged broadening factors for argon, helium and oxygen, and wavelength dependent broadening coefficients for argon, helium, nitrogen, and oxygen will be discussed, along with the resulting measurements, in succeeding chapters.
CHAPTER 3
EQUIPMENT

3.1 Spectrophotometer

The measurements were made using a Perkin Elmer Model 221 infrared spectrophotometer equipped with a potassium bromide linear wavelength prism interchange unit. This spectrophotometer is a double beam optical nulling prism instrument of medium resolution (approximately 3 to 4 cm\(^{-1}\)) with an integral strip chart recorder which plots transmissivity vs. wavelength. The optical nulling is achieved by means of a servo driven filter. This filter (in which the transmissivity varies in a linear manner from 0 to 100\% over the length of the filter) is moved in the reference beam until the energy reaching the detector through the reference beam equals the energy reaching the detector through the sample beam. When the measured energy of the two beams is equal, the position of the filter is measured and interpreted in terms of the transmissivity of the sample beam.

The particular instrument used in these tests was modified as follows: first, a precision wirewound potentiometer was added so that an electrical analog of the transmissivity was available; second, a cam and a miniature switch were added to the wavelength indicator output shaft so that an electrical pulse was generated at intervals of 0.02 \(\mu\)m. During all tests the instrument volume was purged with Liquid Carbonic Company "Hi Pure" grade nitrogen. A photograph of the instrument with the long path gas cells installed is shown in Figure 1.
The calibrations of both the wavelength scale and the transmissivity scale of the instrument were checked. The wavelength scale of the instrument was calibrated by comparing the wavelength reading of the instrument with the known positions of the maxima of several CO₂ bands. It was found that the instrument read uniformly high by 0.05 μm. This correction was applied to all data during the data reduction.

Calibration of the transmissivity scale of the instrument proved to be more difficult. After a literature survey had yielded relatively little information on the testing of the linearity of spectrophotometer transmissivity scales, the following two different methods were tried.

In the first, the transmissivities of several different screens and perforated plates, placed in the sample beam, were measured. A number of difficulties arose using this method.

1. It was difficulty to find screens of different open areas. It seemed that most screens of usable mesh and wire sizes had transmissivities of approximately 40 to 60 percent.

2. The transmissivity was sensitive to the lateral location of the screen in the beam. This was most pronounced for those screens having a rather coarse mesh and coarse wires.

3. Diffraction effects tended to defocus the instrument and thereby cause transmissivity readings different from the geometric transmissivity of the screen. This effect was most pronounced with some extremely fine mesh, etched screens.

4. The measured transmissivity tended to be wavelength sensitive. It is felt that this is not a result of instrument
linearity error since screens of different mesh sizes but of similar transmissivity gave quite different results. This was particularly troublesome at transmissivities between 0.3 and 0.75.

In spite of the foregoing difficulties, three screens were found that gave satisfactory results when tested on this instrument and on a factory calibrated Cary model 90 spectrophotometer at the Goddard Space Flight Center of NASA. A photograph of these screens (having transmissivities of 0.092, 0.158 and 0.861 as measured on the Cary Instrument) is shown in Figure 2. The screen having the highest transmissivity is a tungsten wire screen of the type used in electron tube grids. The two screens of lower transmission are of sheet metal having many small punched holes.

Since the transmissivity linearity calibration outlined above was not particularly satisfactory, a second method of calibration was tried. This method was suggested by Dr. Robert Howard (Howard, 1968) of the Perkin Elmer Corporation, and is the method used by the Perkin Elmer Corporation for laboratory checks of instrument linearity. In this method, segmented disks are rotated at high speed in the sample beam. If the ratio of open area to total area is known and the rotation speed is selected so that synchronizing of the external disk and the internal chopper does not occur, one should be able to calibrate the transmissivity scale of the instrument. Unfortunately, this method has certain weaknesses. The assumption is made that the instrument electronics will treat a signal whose value is alternating rapidly between zero and one in the same manner that it would treat a steady,
Figure 2. Perforated screens used for spectrophotometer calibration.
gray signal where the transmissivity is equal to the ratio of chopper open area to chopper total area. As can be seen from Figure 3, the thermocouple detector has significant response at the chopping frequencies involved (by extrapolating the curve at 120 Hz).

![Graph](image)

**Figure 3.** Thermocouple detector response curve.

As a result, the linearity of the thermocouple and the response of the electronics to high frequency inputs could become important (these, of course, are not important during the normal optical nulling operation of the instrument). Since the errors from these sources were thought to be small no attempt was made to correct the calibration for them.

To calibrate the instrument by this method a set of disks was made having open area to total area ratios of 0.05, 0.10, 0.20, 0.40, 0.60, 0.80, 0.90 and 0.95. A photograph of these disks is shown in Figure 4. The disks were rotated by a d.c. motor. The speed of the motor was approximately 3500 r.p.m. and was varied
Figure 4. Disks used for spectrophotometer calibration.
approximately 10% in the vicinity of this speed to insure that strobing with the chopper was not occurring.

The results of the two calibration methods are shown in Table 1. It would appear from the results obtained using the rotating disks that the instrument is more nearly linear than if judged on the basis of the results of the tests using the screens. It can be seen that the instrument linearity error was less than 1% in most cases.

Shortly after these linearity calibrations were completed, a more accurate method of measuring spectrophotometer linearity was discussed by Reule (1968). Reule's technique, called a supplementary light method, involves the addition, in several steps, of equal amounts of light. In principle, the method is the same as adding equal weights to a spring scale to determine its linearity. The implementation of the technique is rather complex, however, and for that reason it was not used here. The technique is best suited for the calibration of a master spectrophotometer against which other units can be checked.

3.2 Data Processing system

Since the spectrophotometer output was linear in wavelength (rather than linear in wavenumber) and because of a desire to correct the data for instrumental effects (zero shifts, non-linearities and scale factor changes) it was necessary to utilize a rather elaborate data processing system. A block diagram of this system is shown in Figure 5. The output of the spectrophotometer consisted of 0-5v analogue of the transmissivity \( T(\lambda) \) while the wavelength output consisted of 3 volt pulses at wavelength increments of 0.02 \( \mu \text{m} \).
Figure 5. Block diagram of the data processing system.
These analogue outputs were converted to a frequency modulated A C
signal using the United Electrodynamics Corporation voltage con-
trolled oscillators. The oscillators had center frequencies of
5400 cps (T (λ) ) and 10,500 cps (λ) and maximum deviations of
± 7.5% of center frequency. The outputs of these oscillators
were mixed using a Victor Mfg. Co. TA 58 mixer amplifier. The
mixed, frequency modulated signal was then transmitted via shielded
cable to the High Altitude Engineering Laboratory Mobile Telemetry
Station which contained the remainder of the data processing system
(excluding the plotter which was located elsewhere). The fm signals
were converted to voltage analog signals by the EMR discriminators
and fed to the Radiation Inc. A to D converter. The A to D con-
verter sampled the T(λ) signal at each command pulse from the read-
out of the instrument, i.e., every 0.02 µm. The twelve bit sample
of T(λ) was then stored in the PDP-8 memory for later processing,
and was typed also punched on paper tape as a permanent record. The
system was calibrated using the calibration voltage source (regulated
0,1,2,3,4,5v) and the Hewlett Packard Model 522B digital counter.
The calibration procedure used will be discussed in detail in Chapter
4.

The calibration source consisted of a battery, two stage zener
diode regulator and voltage divider output network. This unit was
capable of producing highly stable, independently adjustable vol-
tages of 0.,1.,2.,3.,4., and 5. volts. Each voltage was adjustable
over a range of approximately ± 0.2v. The actual voltages were such
that the V.C.O. output frequency at each voltage was equal to the
V.C.O. output voltage at the corresponding transmissivity (as measured using the rotating disk) at a wavelength of 16 μm. Before and after each run, these six voltages were switched through the data system. The two sets of calibrations were averaged and the averaged values were assigned the transmissivity values of 0., 0.20, 0.40, 0.60, 0.80 and 1.00 by the computer. The data were then interpreted by linear interpolation between these points.

This data system proved to be highly reliable and stable over periods as long as several days. Over a period of thirty minutes (a run usually required less than twenty minutes) the calibrations would contain a 1σ error of less than 0.05%. It is estimated that the total error introduced into the transmissivity data by this system would have a 1σ value of less than 0.5%.

3.3 Pressure Gauge

All pressures were measured by means of an MKS Type 77 Baratron pressure gauge with 0 to 1000 Torr pressure sensing head. This is a highly sensitive diaphragm type differential pressure gauge which senses the diaphragm displacement by means of a differential capacitance A C bridge circuit. The pressure is read from four pressure readout dials which switch voltages to cause the bridge to become balanced. During these tests the "reference" side of the pressure gauge was maintained at a pressure of less than 10⁻³ Torr. This reference pressure was monitored by a NRC Thermocouple gauge. The Baratron pressure gauge can be seen in Figure 1.

The Baratron was initially calibrated by means of an air dead weight tester of very high repeatability. The calibration was
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* calibration points using screens
checked using a Pye Scientific Instruments precision cathatometer to measure the height of the columns of either a butyl phthalate or mercury manometer (depending on the pressure). The calibration using the air dead weight tester is shown in Table II.

### Table II

**BARATRON S/N1187**

#### CALIBRATION DATA

<table>
<thead>
<tr>
<th>PRESSURE $P_y$ (Torr)</th>
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3.4 **Gas handling system**

The system for handling the sample gases consisted of conventional regulators, valves, tubing and pumps. Since it was desirable to reduce the uncertainty in the sample composition to a minimum, the following steps were taken:
1. All tubing carrying the sample gases was of stainless steel.

2. Needle valves controlling gas flow into the cells and the ball valves controlling the pumping of the cells were mounted directly to the cell body.

3. Provision for pumping all interconnecting supply tubing was arranged.

4. Pressure gauge volume and volume of connecting tubing was minimized. (In the worst case the tubing and gauge volume equalled three percent of the cell volume.)

In using this system the feed lines were pumped between sample changes and refilled with pure gas at a pressure greater than cell pressure. Needle valves were opened for a minimum time during filling to insure against back flow. The sample was then allowed to mix until the spectrum reached equilibrium.

3.5 Gas cells

Several gas cells of different lengths were used during the course of these tests. The two shorter cells were designed and built at the University of Michigan while the longer cells were commercial units.

The short cells (2.02, 8.74cm) were simple cylinders with provision for clamping the potassium bromide windows between O-rings at each end of the cell. A sketch of these cells is shown in Figure 6. Initially these cells were made of bare 6061-T6 aluminum. It was found, however, that this material would adsorb carbon dioxide for periods exceeding one half hour after filling. (This was ascer-
Figure 6. Drawing of the short path gas cells
tained by filling the cell with CO\textsubscript{2} and sealing it. Spectra were then run at regular intervals until no further change was noted.) It was also found that CO\textsubscript{2} desorption would continue for periods of the order of several hours after the cells were emptied of CO\textsubscript{2} and filled with nitrogen. (This was again ascertained by running spectra at regular intervals until equilibrium was reached.) After the cells were anodized it was found that the time to reach equilibrium during the adsorption process had been reduced to a few minutes, but that the time to reach equilibrium during the desorption process remained approximately the same as it had been for the bare metal. The amount of gas desorbed appeared to be approximately the same for an anodized cell as it had been for the same cell when bare. In view of the uncertainties that the adsorption and desorption would introduce in the composition of the gas sample, it was decided that another set of cells would be constructed of type 304 stainless steel. When these stainless steel cells were tested in a manner similar to that used for the aluminum cells, no desorption of CO\textsubscript{2} could be detected unless the cell was heated. Since all tests were conducted at room temperature, it was felt that the effect of desorption of carbon dioxide on sample composition could be neglected for tests using these cells. As a result of these tests, the stainless steel cells were used for all measurements involving cells of short length.

The longer cells were constructed of anodized aluminum by the Perkin Elmer corporation and were multiple pass cells. The one meter cells were fixed length four pass cells while the White-type
long path cells were adjustable in steps of four meters from four meters to forty meters. To speed the mixing of the gas mixtures a small, externally powered fan was installed in the long path sample cell.

Because of the problem of carbon dioxide desorption in the smaller cells discussed above, tests, similar to those previously described, were performed on the longer cells. On the basis of these tests it was decided that the CO₂ partial pressure of all sample gas mixtures would need to be greater than ten torr if the uncertainty in the sample composition were to be less than 1%. This condition was met in all subsequent measurements. A photograph of the long path cells installed on the instrument is shown in Figure 1.
CHAPTER 4

SPECTRA AND MEASURED EQUIVALENT WIDTHS

4.1 Introduction

As a check on instrument and data processing system operation, it was felt that it would be valuable to compare a few pure carbon dioxide and nitrogen broadened carbon dioxide spectra with previous experimental work and with the prediction of the analytical model of Drayson and Young (Drayson and Young, 1966; Drayson et al., 1968). Spectra were taken at two different path lengths, several pressures, and several carbon dioxide-to-nitrogen ratios. The test conditions were chosen to correspond to the experimental work of Burch et. al., (1962) and to the theoretical calculations previously reported by Drayson and Young (Drayson, et al., 1968).

4.2 Experimental Procedure

The data were obtained using the complete instrumentation system described in Chapter 3. The Perkin-Elmer Corporation long path cells were used at path lengths of 400 cm and 3,200 cm, with the path length of the reference cell matching the path length of the sample cell. The pressure in the reference cell (measured by a thermocouple gage) was maintained at less than $10^{-2}$ Torr. The optical path outside the cells was purged with nitrogen during all tests.

The spectra were obtained using the standard test procedure outlined below.

1. Evacuate the sample cell.
2. Set the spectrophotometer wavelength to 16 $\mu$m.

3. Block the sample beam.

4. Set the voltage controlled oscillator to the band-edge (as measured by Hewlett-Packard digital counter).

5. Open the sample beam.

6. Set the voltage controlled oscillator to the opposite band-edge.

7. Set the spectrophotometer wavelength to the beginning of the spectrum.

8. Fill the sample cell with gas to the desired pressure.

9. Operate the mixing fan.

10. Switch the spectrophotometer out of the data processing system and switch the calibrate box into the system.

11. Switch the calibration voltages through the system to the computer.

12. Switch the calibrate box out of the system and switch the spectrophotometer into the system.

13. Begin the scan.

14. Upon scan completion, again switch the calibration voltages to the computer.

Steps one through six of the above procedure were performed at the beginning of each data-taking session. The goal of this part of the procedure was to insure that the range of the six calibration voltages was the same as the range of the instrument output voltages. Steps seven through fourteen of the above procedure were performed in conjunction with each spectral scan.
During each scan the gas supply plumbing was evacuated. If the gas to be added to the cell were different from the gas last added to the cell, the supply plumbing was purged with the new gas at least twice during this evacuation process.

As is noted in step nine, mixing of the gas in the sample cell was insured by stirring the gases with a small fan mounted in the sample cell. This was operated for three periods of approximately 10 seconds each, with a waiting period between mixing of approximately 15 seconds. It had previously been found by running successive spectra that this mixing procedure would cause complete mixing.

4.3 Data Processing

Since the data existed in the form of a voltage analog of the transmissivity and an electrical pulse at 0.02 μm wavelength intervals, several operations were necessary to obtain final transmissivity and equivalent width data. The step-by-step procedure used was as follows

1. The calibration voltages were sampled by the analog-to-digital converter at the beginning of each run. Sixteen samples of each voltage were taken at 10-millisecond intervals. The 16 samples for each voltage were averaged and this average value was stored.

2. During the spectral scan, the voltage analog of the transmissivity was sampled whenever commanded by the wavelength voltage pulse. Upon being commanded, 16 samples (again at 10-millisecond intervals) were taken of the transmissivity data.
These 16 samples were averaged and the average value stored. At
the scanning speed used, voltage pulses occurred approximately once
every 2 seconds. As the transmissivity voltage was sampled, the
averaged sampled value was typed out on the teleprinter and punched
on paper tape.

3. At the termination of the scan, the calibration voltages
were again sampled. (Following the same procedure followed in
step 1).

4. The corresponding "before run" and "after run" calibra-
tion voltage samples were averaged and these averaged calibration
voltages were stored. The "before run" samples, the "after run"
samples, the average of the "before run" and "after run" samples,
and the difference between overall averaged values of succeeding
voltage steps were then printed out in octal form and were punched
on paper tape. The paper tape containing these quantities, along
with the transmissivity voltage samples constituted the permanent
record of the raw data for that run. This completed the data
sampling portion of the data processing. After the data for a
particular run had been obtained and stored as outlined above,
they were processed into "final" transmissivity data and the
equivalent width calculated. The steps necessary to achieve this
can be stated quite briefly.

1. Determine the indicated transmissivity of the gas-
sample cell combination from the data and calibrations.

2. Correct for the transmissivity of the sample cell.

3. Compute the equivalent width.

The detailed solution of the three parts of the above problem was
accomplished in the following way:

1. The computer was programmed to compare each stored voltage sample with the six double averaged calibration voltage samples and determine which adjacent pair of calibration samples bracketed the transmissivity sample. The computer then performed a linear interpolation between the calibration samples to determine the indicated transmissivity that corresponded to the stored voltage sample.

2. The correction for cell transmissivity is made by solving the equation

\[ T_{\text{gas}} = T_{\text{ind}} \cdot \frac{T_{\text{cell}}}{T_{\text{cell}}} \]  \hspace{1cm} (4.3.1)

where \( T_{\text{gas}} \) is the transmissivity of the sample gas

\( T_{\text{ind}} \) is the instrument output

\( T_{\text{cell}} \) is the measured transmissivity of the sample cell relative to the transmissivity of the particular reference cell in place at the time. \( T_{\text{cell}} \) would be more precisely defined as

\[ T_{\text{cell}} = \frac{T_{\text{sample cell}}}{T_{\text{reference cell}}} \]  \hspace{1cm} (4.3.2)

\( T_{\text{cell}} \) was stored as a table in the computer. This table was loaded by measuring the transmissivity of the sample cell while evacuated and storing the indicated transmissivities in the \( T_{\text{cell}} \) table. After dividing the indicated transmissivity by the cell transmissivity, the computer stored the computed gas transmissivities.

3. Before calculating the equivalent width of the spectrum in units of cm\(^{-1}\) (the standard unit of measure of equivalent width)
it is necessary that the absolute value of the wavelength of each transmissivity sample be determined. At this point, we know only that they are spaced at 0.02 μm intervals. The wavelength of the data points was established by inspecting the transmissivity values of a CO₂ spectrum having a maximum absorption of approximately 0.25. The sharp absorption band (the \( \text{main} \ \varnothing \text{branch} \) near the band center was examined and the data point having the minimum transmissivity value was assigned the wavelength of 14.99 μm. It was found that the wavelength calibration of the system was very stable, not varying by more than ±0.01 μm over 8 hours.

After the wavelength of the transmissivity samples had been established, the computer calculated the integral of the transmissivity vs. wavenumber spectrum in units of cm\(^{-1}\). This was performed using a trapezoidal rule integration scheme. The wave number increments between samples had been calculated and stored in the computer in tabular form. Upon completion of the computations, the wavelength and transmissivity of each sample and the value of the integral of transmissivity over the wave number range of the spectrum were printed out. This completed the processing of the data by the data processing system.

It would seem that this should complete the processing of the data. (Except for subtracting the computed transmissivity integral from the quantity (\( \nu_{\text{max}} - \nu_{\text{min}} \)) to determine the equivalent width of the spectrum). Unfortunately, this was not found to be the case; the system displayed two effects for which further correction of the data was required. These were scale
factor change and zero shifts. It could be seen by examination of the instrument strip chart record that the scale factor change was occurring in the instrument itself. The scale factor variation from run to run was small, approximately 0.5%, and apparently random. Examination of both the instrument strip chart record and the computer output of spectra that were opaque over some region near the band center indicated that the zero shift was a combination of apparently random instrument shifts, approximately 0.2%, and a slow drift in the instrumentation system occurring as a result of a change in the output voltage of a bias battery. It appeared that the battery voltage drifted rather rapidly initially (for the first half hour after turn-on) then very slowly for the remainder of the day. The offset in the data as a result of both effects was generally less than 1 percent.

The corrections for the two above effects were applied as follows:

1. From each transmissivity value was subtracted the signed average of the instrument output for 50 data points in a region where the transmissivity value was known to be zero. (If no such points existed for a particular spectrum, another spectrum containing such points was run immediately following the running of the spectrum to be corrected).

2. The transmissivities for the first 10 points and the last 10 points of the spectrum were averaged (the spectrum was always started and ended outside the 15 μm band), and all transmissivities (after the above zero shift correction was applied) were divided
by this average value.

To correct the computer-calculated transmissivity integral, the product of the signed zero offset and the interval of the calculation, i.e., \( Z_{\text{off}} (\nu_{\text{max}} - \nu_{\text{min}}) \) was subtracted from the computer output. This result was then divided by the scale factor of the spectrum (the averaged value of the first 10 and the last 10 data points). Since this represented the last correction to the data, the computed value of the transmissivity integral was subtracted from the interval over which the spectrum was measured and the equivalent width determined, i.e.,

\[
A = \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} A_{\nu} d\nu = \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} (1 - T_{\nu}) d\nu = \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} d\nu - \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} T_{\nu} d\nu
\]

\[
= (\nu_{\text{max}} - \nu_{\text{min}}) - \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} T_{\nu} d\nu
\]  

(4.3.3)

4.4 Data Accuracy

The accuracy of the data is influenced by errors from many sources. Some of the error sources are:

1. Errors in the knowledge of sample characteristics; pressure, temperature, composition, and path length

2. Instrument errors; scale factor changes, nonlinearity, zero shift, and wavelength calibration

3. Errors in the data transmission system; nonlinearity, zero shift, scale factor changes, and digitizing errors

4. Data processing errors; round off and integration errors.
If these errors are viewed as being random with respect to each other (although they may be systematic in the sense that they will occur repeatedly under the same test conditions) they can be combined to obtain the standard deviation of the total error. This was done using the calibration curves for the various instrument parameters wherever available, data from other sources (previous calibrations of the data system on the bus, for example) and, where all else failed, educated guesses. It appears from this analysis that the transmissivity data have a 1σ error of approximately 1 percent while the equivalent width data have a 1σ error of approximately 3 percent at A = 30 cm\(^{-1}\) decreasing to approximately 1.5 percent at A = 100 cm\(^{-1}\).

4.5 Results

The test conditions, the measured equivalent widths and the equivalent widths measured by Burch, \textit{et al.}, (1962) and calculated by Drayson, \textit{et al.}, (1968) for similar test conditions are shown in table III. The theoretical calculations used a mixed Doppler-Lorentz line shape with variable line half width. This model is discussed in detail in Drayson and Young, (1966), and Drayson, \textit{et al.}, (1968). It can be seen that the agreement between our equivalent width data and the data of Burch, \textit{et al} is very good, disagreeing at most by 4 percent. Since the accuracy claimed by Burch, \textit{et al.}, for their data is only ±5 percent, and since our data are estimated to have a 1σ error of 3 percent both sets of data are essentially in agreement. The agreement between our experimental data and the predictions of the model of Drayson and
TABLE III

COMPARISON OF MEASURED AND CALCULATED EQUIVALENT WIDTHS

<table>
<thead>
<tr>
<th>( P_{CO_2} ) (Torr)</th>
<th>( l ) (cm)</th>
<th>( w ) (atm cm)</th>
<th>( P_{N_2} ) (Torr)</th>
<th>( T ) (°C)</th>
<th>( \frac{A}{(cm^{-1})} ) (Burch et al 1968)</th>
<th>( \frac{A}{(cm^{-1})} ) (Drayson et al 1963)</th>
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Note: The two values at \( l = 400 \) cm, \( P_{CO_2} = 100 \) Torr are for two different samples.

N.A. Theoretical equivalent widths not available.
Young are within the experimental accuracy except for conditions of relatively low amounts of carbon dioxide when broadened by approximately one atmosphere of nitrogen at long path lengths. Under these conditions, the model predicts an equivalent width approximately 6 to 8 percent higher than was measured.

In Figure 7 are shown three spectra selected from those summarized in table III. It can be seen that the agreement between the two sets of experimental data is good when one allows for the somewhat higher resolution of this work as compared to the work of Burch. The comparison with the theoretical model is also good (within the experimental error for the two spectra (Figure 7 (a) and 7(b)) for pure CO₂ samples. The agreement between the experimental spectrum and the theoretical calculations deteriorates for carbon dioxide broadened by a relatively large amount of nitrogen (Figure 7 (c)). The disagreement is particularly pronounced in the regions from 595 to 615 cm⁻¹, from 710 to 740 cm⁻¹ and also in the wings of the band. The disagreement between the model and experiment under these conditions has been noted previously (Drayson et al., 1968). It might be possible that the strength of some of the bands may have been incorrectly estimated. This seems a particularly appealing possibility in the regions from 595 to 615 cm⁻¹ and from 710 to 740 cm⁻¹. The discrepancy between the predicted transmissivity in the wing region of the band might be due to a change in line shape since in this spectrum the absorption lines are broadened as a result of carbon dioxide-nitrogen collisions rather than as a result of carbon dioxide-carbon dioxide collisions.
Figure 7. Comparison of spectra with other experimental results and with theoretical predictions.
(b) $P_{CO_2} = 50$ Torr, $l = 3,200$ cm.

Figure 7.- Continued.
(c) \( P_{\text{CO}_2} = 25 \text{ Torr}, \ P_{N_2} = 771.3 \text{ Torr}, \ l = 3,200 \text{ cm.} \)

**Figure 7.- Concluded.**
as in the two previously discussed spectra. This possibility will be discussed later in this report in connection with other data that will be presented. The data presented here are neither of the proper type nor of sufficient quantity to draw any definite conclusions concerning the difficulties of the theoretical calculations.

It would appear then from the above data that the instrument and data processing system and the methods of processing the data are capable of producing spectra and equivalent width data that are in agreement with the work of others.
CHAPTER 5

BAND-AVERAGED BROADENING COEFFICIENT FOR CO₂

5.1 Experimental Method

The self-broadening coefficient, B, for carbon dioxide relative to nitrogen has previously been determined by estimation from curves of B (ν) vs. ν in the 15 μm band (Burch, et al., 1962), by measuring the broadening of individual absorption lines in the 10.6 μm-band using a laser source (Patty, et al., 1968) and by a method using cells of different lengths in the 4.6 μm-band (Anderson, et al., 1967). In general, the values obtained for the different methods have been consistently equal to approximately 1.3. Uncertainties claimed range from ±0.03 in the work of Anderson, et al., (1967) to ±0.08 in the case of Burch, et al., (1962).

In this study, a band-averaged value of B has been determined at one optical mass using the third method mentioned above. The method consists essentially of comparing the amount of radiation absorbed by an equal amount of carbon dioxide while being broadened by both nitrogen and carbon dioxide in one case and carbon dioxide alone in another case. For the measurement of the effect of carbon dioxide-carbon dioxide broadening, one fills a cell (hereafter called the short cell) with carbon dioxide at some partial pressure \( P_{CO₂}^S \) and measures the equivalent width of the spectrum obtained. The effective pressure in this cell is \( P_{e}^S = B_{avg} P_{CO₂}^S \). To examine the effect of carbon dioxide-nitrogen broadening, one fills a longer cell with the same optical mass of carbon dioxide as was contained in the short cell. The partial pressure in this cell is \( P_{CO₂}^L \).
Nitrogen is now added to this cell. The effective pressure in this cell is $P_e = B_{avg} p^L_{CO_2} + P_{N_2}$. The nitrogen partial pressure is increased in steps and the equivalent width determined at each step. A plot of equivalent width versus total pressure is then made. At that nitrogen pressure at which the equivalent width of the spectrum of the carbon dioxide - nitrogen mixture is equal to the equivalent width of the spectrum of pure carbon dioxide, the equivalent pressure in the two cells are equal (this follows from Eq. (2.4.3) and the assumption that equal equivalent widths implies equal line widths) and one can write the equation

$$B_{avg} p^S_{CO_2} = B_{avg} p^L_{CO_2} + P_{N_2} = P_e \quad (5.1.1)$$

where $p^S_{CO_2} =$ carbon dioxide pressure in the short cell

$p^L_{CO_2} =$ carbon dioxide partial pressure in the long cell

$P_{N_2} =$ nitrogen partial pressure in the long cell

or solving for $B_{avg}$

$$B_{avg} = \frac{P_{N_2}}{p^S_{CO_2} - p^L_{CO_2}} \quad (5.1.2)$$

Using this equation one can then determine $B_{avg}$ if the carbon dioxide pressures in the two cells and the nitrogen pressure necessary to cause the same total absorption in the two cells are known.

5.2 **Instrumentation and Data Processing**

The instrumentation used for the measurements was the complete system described in Chapter 3. The methods used for obtaining and
processing the data were described in 4.2 and 4.3.

5.3 **Test Conditions**

The Perkin-Elmer long path cells were set at 400 cm (the "short" cell) and at 1,600 cm (the "long" cell). The carbon dioxide partial pressure was 100 Torr in the short cell and 25 Torr in the long cell. The nitrogen partial pressure was varied from zero to 412 Torr. A summary of the test conditions is presented in Table IV.

5.4 **Results**

The measured equivalent widths for the various samples are listed in Table IV. Figure 8 is a plot of measured equivalent width versus total pressure in the 1,600 cm cell (the "long" cell). Taking 121.85 as the average value of the equivalent width determined for the two 100 Torr pure carbon dioxide samples in the 400 cm cell, it is found that this value of equivalent width would be achieved at a nitrogen partial pressure of 98 Torr in the long cell. Substituting this value and the appropriate values for the carbon dioxide partial pressures in equation (5.1.2), we find that the value of $B_{\text{avg}}$ is

$$B_{\text{avg}} = \frac{P_{N_2}}{P_{CO_2}^S - P_{CO_2}^L} = \frac{98}{100 - 25} = 1.30$$

5.5 **Accuracy**

It can be seen by examining figure 8 that the nitrogen partial pressure (and hence the value of B) at which equality of equivalent widths appears to be achieved is extremely sensitive to small errors in the determination of the equivalent width of either sample. It
Figure 8 - Equivalent width vs. total pressure, $P_{CO_2} = 25$ Torr, $l = 1,600$ cm.
is rather insensitive, however, to errors in the equivalent width
determination if the errors for both samples are of similar magni-
tude and in the same direction. An attempt was made to achieve this
equality of errors by taking the data after the system had been
operating for several hours, by taking the data in as short a time
as possible and by using only those data for which the corrections
were small.

A second source of error is the problem of achieving equal
optical masses in the two cells. Since the optical mass (for these
uniform paths) is the product of the path length and the carbon
dioxide partial pressure, the problem really concerns the accuracy
with which one can measure the pressure and the path length. As
can be seen from the calibration of the Baratron pressure gauge,
the accuracy of the pressure measurement is quite high, approxi-
mately 0.1%. It is rather difficult, however, to measure the exact
path length traversed by the beam in the long path cells, but path
length is probably accurate to better than ±0.25 percent.

In view of the difficulties outlined, it is estimated that a
reasonable value of the 1σ error in the value of B is approximately
0.08. It is doubtful if greater accuracy than this could be achieved
with the experimental technique and instrumentation system used for
the measurements discussed here.

5.6 Discussion of Results

Table V displays B values obtained by other researchers, and
it can be seen that most of the values are between 1.2 and 1.4. The
results of this study (1.30) agree well with those values. When one
considers these data it should be noted that

1. The values of B are for different bands

2. Some of the values are for the broadening of individual lines near their centers (the laser method) while others are for averages over an entire band.

3. These data are quite uncertain (probably more uncertain than most experimenters admit).

In view of the above, it is felt that the agreement among the various workers is unusually good.

### TABLE IV

TEST CONDITIONS AND MEASURED EQUIVALENT WIDTHS USED

FOR THE DETERMINATION OF THE BROADENING COEFFICIENT FOR NITROGEN

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<th>( P_{CO_2} ) (Torr)</th>
<th>( l ) (cm)</th>
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<th>( P_{N_2} ) (Torr)</th>
<th>( T ) (°C)</th>
<th>( A ) (cm(^{-1}))</th>
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<td>Type of Measurement</td>
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<td>15μm region (667cm⁻¹)</td>
<td>This work</td>
<td>Band average</td>
<td>1.30 ± 0.08</td>
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<td>10.4μm (961cm⁻¹)</td>
<td>Patty et al., (1968)</td>
<td>Laser, P(20) line</td>
<td>1.33 ± 0.05</td>
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<td>Near line centers</td>
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<td>Howard et al., (1956)</td>
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</tr>
<tr>
<td>$10.4 \mu m (961.3 \text{cm}^{-1})$</td>
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</tr>
<tr>
<td>$15 \mu m (667.3 \text{cm}^{-1})$</td>
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<td>$4.3 \mu m &amp; 14.8 \mu m$</td>
<td>Coggeshall and Saier (1947)</td>
<td>Single wavelength</td>
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CHAPTER 6

BAND-AVERAGED BROADENING FACTORS FOR ARGON, HELIUM, AND OXYGEN

6.1 Introduction

The ability of a gas to broaden the spectral lines in an absorption band is usually expressed relative to the broadening ability of another gas. The reference gas may be either the absorber itself, in which case the quantity determined is similar to the broadening coefficient of Chapter 5, or it may be some other gas. When the second method of expression is chosen, the reference gas normally used (at least in studying carbon dioxide infrared absorption spectra) is nitrogen. The result is then usually expressed in terms of the broadening factor as defined in Eq. (2.4.5). The abilities of argon, helium, and oxygen relative to the ability of nitrogen to broaden carbon dioxide spectra have been determined. These data are presented and discussed in this chapter.

6.2 Experimental method

In this part of the investigation the broadening abilities of argon, helium, and oxygen relative to that of nitrogen are discussed. The ability of each gas to broaden the spectral lines is expressed as a band-averaged broadening factor, $F_i$, as defined in Eq. (2.45)

$$F_i = \frac{P_{N_2}}{P_i}$$

where $P_i$ = the pressure of the $i$th gas required to produce a specified equivalent width for some CO$_2$ sample

and $P_{N_2}$ = the nitrogen pressure required to produce the same equivalent width for an identical CO$_2$ sample

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In practice, the relative broadening factor is determined by plotting equivalent width as a function of gas pressure for each broadening gas. It is then possible to read from the plot the pressure of each broadening gas that corresponds to any given equivalent width. The relative broadening factor for each gas can then be readily determined.

The major advantage of this method (as compared to a technique that results in a broadening coefficient similar to that measured for nitrogen in Chapter 5) is that accurate data are more easily obtained. In the method discussed in Chapter 5 it is necessary to place the same optical mass of carbon dioxide in two cells of different lengths with no readily available means, independent of pressure and cell length measurements, of determining the amount of carbon dioxide in the cell. In determining broadening factors relative to nitrogen, one has only to check the equivalent widths of the spectra for the pure carbon dioxide samples. If the carbon dioxide samples are consistent, it is then only necessary for good accuracy that the pressure gauge be repeatable and reasonably accurate.

6.3 Instrumentation and Data Processing

The system used for obtaining the measurements discussed in this chapter was the complete set up described in Chapter 3. The experimental procedure followed was described in section 4.2 with one exception. Since no mixing fan was installed in the small cells (8.74 and 100 cm) used here, it was necessary to wait approximately 25 minutes after filling the cells to be sure the gases were mixed.
This time period had been found to be sufficient for complete mixing by taking several spectra of the same sample at various time intervals after filling. The rather long time period was required to allow the small amount of gas in the pressure gauge and connecting tubing to mix with the gas in the cell.

The data processing techniques were described in section 4.3 except that the cell transmissivity table was loaded somewhat differently. In these tests, the table was hand-loaded into the computer. The values loaded were the average of approximately five cell transmissivity runs. This was an attempt to reduce the effects of noise. It was feasible because the transmissivity of these cells was highly stable, while the transmissivity of the long-path cells changed each time the path length was changed.

6.4 Test Conditions

Spectra were obtained for path lengths of 8.74 and 100 cm. Carbon dioxide partial pressures were 100 Torr in the 8.74 cm cell and 30 and 100 Torr in the 100 cm cell. Broadening gas pressures varied from zero to 700 Torr in the case of the 30 Torr carbon dioxide samples and from zero to 620 Torr in the case of the samples having a carbon dioxide partial pressure of 100 Torr. Broadening gases were argon, helium, nitrogen, and oxygen. The test conditions describing each sample are listed in Table VI. All the spectra for any one carbon dioxide partial pressure-path length combination were obtained during a single test session.

6.5 Results

The measured equivalent widths for the various spectra are
shown in Table VI. The equivalent widths are plotted as a function of total gas pressure in Figure 9. Several equivalent widths were selected for each figure and the corresponding gas pressures determined from the curves. The equivalent widths selected, the corresponding gas pressures, and the calculated broadening factors relative to nitrogen are shown in Table VII. The broadening factors were averaged over each optical mass and were also averaged overall for each gas. These averages are also presented in Table VII.

6.6 Accuracy

As has been noted earlier, the accuracy of the relative broadening factors is controlled primarily by the repeatability of the instrumentation and data processing system; the absolute accuracy of the system is of lesser importance. For example, it can easily be shown that a systematic five percent shift in the values of the equivalent width would change the relative broadening factors by only one percent.

Some measure of system repeatability (including the experimenter, a variable often overlooked and whose properties are difficult to measure) can be obtained by comparing the measured equivalent widths of the four spectra of pure carbon dioxide at each optical mass. It can be seen that the scatter in the measured equivalent width for each of the three sets of four independently formed samples is very small, the 1σ scatter being only 0.17 percent. Because of the repeatability of the system, the accuracy of the pressure gauge, and the insensitivity of the broadening factors to systematic errors, the broadening factors derived here are felt to be considerably
<table>
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<tr>
<th>$P_{CO_2}$ (Torr)</th>
<th>W (atm cm.)</th>
<th>l (cm.)</th>
<th>Broadening Gas</th>
<th>$P_B$ (Torr)</th>
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Figure 9. Equivalent width vs. total pressure for various broadening gases.

(a) $P_{CO_2} = 100$ Torr, $l = 8.74$ cm.
Figure 9: Continued.

(b) $P_{CO_2} = 30$ Torr, $l = 100$ cm.
(c) $P_{CO_2} = 100$ Torr, $l = 100$ cm.

Figure 9.- Concluded.
more accurate than the corresponding coefficient for nitrogen that was determined in Chapter 5 of this work. It is estimated that the error in the relative broadening factors is probably no greater than 0.02 and that it is very unlikely that the order of broadening ability (oxygen, helium, and argon) is incorrect.

6.7 Discussion of Results

Presented in Table VII are the broadening factors for argon, helium, and oxygen relative to nitrogen. Values of the broadening factor were calculated for at least three values of the equivalent width for each of the three optical masses. The values of the broadening factor for all of the equivalent widths were averaged over each optical mass and were also averaged over all equivalent widths and optical masses; this value is shown as the overall average.

It will be noted that the deviations of the average values from the overall average are rather small being no greater than five percent. Within each optical mass the factor varies somewhat with equivalent width. This variation is small in the case of the two larger optical masses and is within the data scatter. In the case of the smallest optical mass, however, the variation is larger, the value of the broadening factor tending to increase with increasing equivalent width. There is no obvious explanation for this from these data but this point will be discussed further in the next chapter when the wavelength dependence of the broadening coefficients is discussed.

The broadening factors have not been previously determined in
### TABLE VII
SUMMARY OF THE BAND AVERAGED BROADENING FACTOR CALCULATIONS

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<th>P$_{CO_2}$ (Torr)</th>
<th>$\omega$ (atm cm)</th>
<th>1 (cm)</th>
<th>A (cm$^{-1}$)</th>
<th>P$_{N_2}$ (Torr)</th>
<th>P$_{O_2}$ (Torr)</th>
<th>P$_{A}$ (Torr)</th>
<th>P$_{He}$ (Torr)</th>
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<th>F$_{A}$</th>
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<td>Overall Average</td>
<td>.85</td>
<td>.78</td>
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the 15 \( \mu m \) region for carbon dioxide, but there have been investigations in which these factors (or data from which relative broadening factors can be derived) have been determined in other carbon dioxide absorption bands. Table VIII displays the relative broadening factors for several carbon dioxide absorption bands measured by other workers. Also shown in this table are the overall average values of the broadening factors from Table VII.

The data shown for the 4.3 \( \mu m \) (2,350 cm\(^{-1}\)) band obtained by Burch et al. (1962a) were determined by the same method as that used in this work. The carbon dioxide partial pressure and the broadening gas pressures were similar \((P_{CO_2} = 50 \text{ Torr}, P_B = 80 \text{ to } 700 \text{ Torr})\), however, the path length (6.35 cm) and optical mass were smaller than that used here.

The data for the P(20) line of 10.4 \( \mu m \) (961 cm\(^{-1}\)) band by Patty, et al., (1968) were originally published as broadening coefficients for carbon dioxide with respect to the various gases. These were converted to broadening factors with respect to nitrogen by Eq. (2.4.6) which is

\[
F_i = \frac{B_{N_2}}{B_i}
\]

The data were obtained using a laser tuned to the P(20) line as a source of radiation. The radiation passed through a multiple pass cell and into a prism spectrometer set at the frequency of the P(20) line. In these tests the cell length was approximately 4 or 8 meters. The carbon dioxide partial pressure was either 50 or 100 Torr, while the broadening gas pressure varied up to 250 Torr. The
<table>
<thead>
<tr>
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<th>Type Measurement</th>
<th>Argon</th>
<th>Helium</th>
<th>Oxygen</th>
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<td></td>
<td></td>
<td>$D_{ab}/P_{aN_2}$</td>
<td>$D_{ab}/P_{aN_2}$</td>
<td>$D_{ab}/P_{aN_2}$</td>
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<td>15 μm</td>
<td>This work</td>
<td>Band average</td>
<td>0.78</td>
<td>0.93</td>
<td>0.80</td>
</tr>
<tr>
<td>4.3μm (2350cm$^{-1}$)</td>
<td>Burch et al., (1962a)</td>
<td>Band average</td>
<td>0.78</td>
<td>0.93</td>
<td>0.59</td>
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<td>10.4μm P(20) (961cm$^{-1}$)</td>
<td>Patty et al., (1968)</td>
<td>Laser</td>
<td>0.79</td>
<td>0.94</td>
<td>0.79</td>
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<td>10.4μm P(20) (961cm$^{-1}$)</td>
<td>McCubbin and Mooney (1968)</td>
<td>Laser</td>
<td>1.10</td>
<td>1.10</td>
<td></td>
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<tr>
<td>10.4μm P(20) (961cm$^{-1}$)</td>
<td>Boutin et al., (1967)</td>
<td>Laser</td>
<td>0.70</td>
<td>0.88</td>
<td>0.85</td>
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<tr>
<td>4.3 μm</td>
<td>Coggeshall and Saier</td>
<td>Medium resolution</td>
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<td>0.65</td>
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<tr>
<td>14.8 μm</td>
<td>Coggeshall and Saier</td>
<td>Single wavelength</td>
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<td></td>
<td>0.78</td>
</tr>
</tbody>
</table>
experimental method was very similar to that used in Chapter 5 of this work for the determination of the broadening coefficient for carbon dioxide with respect to nitrogen. The short cell was filled with carbon dioxide to a pressure of approximately 100 Torr and the transmittance measured. The longer cell was then filled with the same optical mass of carbon dioxide (pressure approximately 50 Torr) and then the transmittance measured as a broadening gas was added. From a plot of transmittance versus broadening gas pressure, the broadening gas pressure at which the transmittance was equal to the transmittance of the pure carbon dioxide sample in the short cell could be determined. At equal transmittances it was assumed that the line half-widths were equal and the self-broadening coefficient was determined from Eq. (5.1.2)

\[
B = \frac{P_b}{P_{CO_2}^S - P_{CO_2}^L}
\]

As was mentioned earlier, the self-broadening coefficients were divided into the self-broadening coefficient with respect to nitrogen, to derive the F values of Table VIII.

The results reported by McCubbin and Mooney (1968) were also determined using a laser as a radiation source. The experimental apparatus consisted of a carbon dioxide laser tuned to the P(20) line of the 10.4 μm (961 cm\(^{-1}\)) band, a multiple pass White cell, and a spectrometer set to the frequency of the line center. In this case, the spectrometer was a grating type instrument. The carbon dioxide partial pressure was 1 Torr and the broadening gas
pressure varied from zero to 30 Torr. The path length was 20.88 m. Broadening gases used were argon, air, and nitrogen. Transmittance was plotted as a function of gas pressure for the various broadening gases. Next, a family of theoretical transmittance versus pressure curves was plotted for various line half widths using the Voigt profile line shape. The half width of the experimentally observed absorption line was then said to be equal to the half width of the theoretical line that produced the transmittance versus pressure curve best fitting the experimental data. The results were presented in the form of line half widths for the various broadening gases. These half widths (carbon dioxide self-broadened = 0.096, nitrogen broadened = 0.070, air broadened = 0.080, and argon broadened = 0.077) were converted to relative broadening factors by simple division of the foreign broadened half widths by the nitrogen half width.

In their work, Bouten et al., (1967) used a carbon dioxide laser tuned to the P(20) line of the 10.4 μm (961 cm⁻¹) band as a radiation source. A spectrophotometer, set to the wavelength of the line center, measured the radiation transmitted by a cell filled with carbon dioxide and a broadening gas. From the ratio of the absorption coefficients of a carbon dioxide sample and a foreign broadened sample they calculated the ratio of the squares of the collision diameters for carbon dioxide-carbon dioxide collisions and carbon dioxide-foreign gas collisions. The broadening factor presented in Table VIII were determined by first rewriting Eq. (2.4.4) in the form
\[ B = \left( \frac{2M_b}{M_{CO_2} + M_b} \right)^{\frac{1}{2}} \left( \frac{D_{CO_2,CO_2}}{D_{CO_2,b}} \right)^2 \]  

(6.7.1)

and calculating the broadening coefficients for the various gases. These were then divided into the broadening coefficient for nitrogen (which had also been determined from the data of Boutin et al. by the above method) in accordance with Eq. (2.4.6). In their work Boutin et al. used carbon dioxide and broadening gas partial pressures that were high enough to ensure that collisional broadening determined the line profile.

Cogeshall and Saier (1947) determined the collision diameter ratios for carbon dioxide - carbon dioxide collisions and carbon dioxide - foreign gas collisions at a single wavelength in the 4.3 \( \mu \text{m} \) (2350 \( \text{cm}^{-1} \)) band and a single wavelength in the 15 \( \mu \text{m} \) (667 \( \text{cm}^{-1} \)) band. The method was similar to that used in Chapter 5 except that sample transmissivities were matched at a single wavelength rather than matching the integrals over the band. Test conditions and resolution resembled those used in these tests. The collision diameter ratios presented by Cogeshall and Saier were converted to broadening factors by means of Eq. (6.7.1) and Eq. (2.4.6).

It can be seen from the descriptions of the various techniques that the property being measured and the assumptions made in interpreting the data are quite different for the different techniques. For example, the technique using a black body radiation source (this work, Burch et al., 1962a) and Cogeshall and Saier (1947) is actually measuring a property of the wings of the lines (since
the sample required to achieve sufficient absorption to properly operate the spectrometer results in line centers being essentially opaque) while the techniques using a laser as a radiation source measure a property of a single line near the line center. With these differences in mind, the data presented in Table VIII can be compared.

In the case of argon, all of the measurements except that of McCubbin and Mooney are in relatively close agreement, the differences probably being within the experimental errors. (Boutin et al., 1967) considered their value to be in good agreement with that of Burch et al., (1962a). The measurement by McCubbin and Mooney (1968) is significantly different from the other (1.10 as compared to 0.78). The difference between his results and those of Burch were noted by McCubbin in his paper, but no explanation was offered. It should be noted that this work, the work of Burch, et al., (1962a) and the work of Patty, et al., (1968) were all performed at pressures considerably higher than the work of McCubbin and Mooney. It is quite possible that the difference is in some way attributable to this. Another possibility is that the measurements of Patty, et al., (1968) may not have been made at precisely the same frequency as those of McCubbin and Mooney. McCubbin and Mooney used a carbon dioxide-nitrogen laser because, as they said, an increased pressure of a carbon dioxide-nitrogen-helium laser (as used by Patty et al., (1968)) might permit oscillation away from the exact center. Although Patty, et al., (1968) used a carbon dioxide-nitrogen-helium laser, this author is not able to judge as
to whether or not the pressure was high enough to allow this shift in frequency to occur. Resolution of this difference will have to be made by those who are more knowledgeable in the area of laser operation.

In the case of helium broadening, it is seen that this work and the works of Boutin et al., (1967), Patty et al., (1968), and Coggeshall and Saier (1947) at 14.8 \( \mu m \) are in good agreement. These differ significantly from the values obtained by Burch et al., (1962a) for the 4.3 \( \mu m \) band and Coggeshall and Saier (1947) at 4.3 \( \mu m \). It appears that the effects of a given broadener may differ for different absorption bands of an absorber, however, one would not expect the differences to be too great. The test conditions for our work and the work of Burch et al. and the work of Coggeshall and Saier (particularly in the case of the 8.74 cm sample) are not greatly different so that the relative contributions of line centers and line wings should not be too different. A check on the accuracy of our work will be obtained when the wavelength dependence of the self-broadening coefficient of carbon dioxide with respect to the various gases in discussed in the next chapter.

The data for oxygen also pose a problem. Although our data, the data of Burch et al., (1962a), the data of Boutin et al., (1967) and the data of Coggeshall and Saier (1947) agree fairly well there is a rather significant difference with the work of McCubbin and Mooney who used air as a broadener. They measured a broadening factor of 1.14 for air broadened carbon dioxide. Since air is composed principally of nitrogen and oxygen, this result could be
taken to mean that oxygen is a more effective broadener than
nitrogen. This is in direct disagreement to our results and the
results of the other researchers cited here.

One other point that might be noted is the similarity of the
broadening factors for helium and argon. Patty has noted that
this should not be entirely unexpected because, although helium
will collide more frequently with carbon dioxide (and hence should
cause a larger half width, according to the simple theory used here)
its polarizability is lower and should have a smaller effect. A
qualitative check on the equality of the broadening coefficients
for these two gases will be examined in the next chapter when the
wavelength-dependent broadening coefficients are discussed.

It is apparent from the foregoing discussion that explanations
for the similarities and differences between the broadening effects
of the gases studied and between the work of various investigators are
not available. Hopefully, further theoretical and experimental
work will produce a consistent picture.
7.1 Introduction

Although the band-averaged self-broadening coefficient and relative broadening factors discussed in Chapters 5 and 6 give some indication of the effects of various broadening gases on the absorption of infrared radiation by carbon dioxide, they still leave an incomplete picture. In view of this a study was undertaken of the wavelength dependence in the 15 μm band of the broadening coefficients. The coefficients were measured in the region from 588 to 741 cm⁻¹ (17 to 13.5 μm) using argon, helium, nitrogen, and oxygen as broadening gases. Most of the measurements were taken at a single carbon dioxide partial pressure, although limited data were obtained from 635 to 700 cm⁻¹ (15.75 to 14.25 μm) at a second partial pressure. Cell lengths were varied depending upon the region of the band being investigated.

The wavelength dependence of the broadening coefficient of carbon dioxide with respect to nitrogen has previously been investigated by Burch, et al., (1962), in the 15 μm (667 cm⁻¹) region, by Anderson et al., (1967) in the 4.3 μm (2,350 cm⁻¹) region, and by Vasilevskii et al., (1967) in the 2.06 μm (4,854 cm⁻¹) region. The techniques have varied, the work of Burch et al., (1962) and Anderson et al., (1967) having been performed at medium resolution while the work of Vasilevskii et al., (1967) was performed at high resolution. As far as is known, the wavelength dependence of the
broadening coefficient with respect to other broadening gases has not been investigated in the 15 \( \mu \text{m} \) region.

7.2 **Experimental Method**

The data were obtained using the Model 221 Spectrophotometer, the Perkin Elmer long path cells, the 8.74 cm and 2.02 cm short cells, and the Baratron pressure gauge. The data were read from the instrument strip chart recorder.

The experimental technique was similar to that used by Burch, et al., (1962). This technique is a variation of that used for determining the band-averaged broadening coefficients. Here a short cell is placed in the reference beam of the instrument and a longer cell in the sample beam. Equal optical masses of carbon dioxide are then placed in the two cells. Due to the decreased pressure in the long cell, the absorption in it (the sample beam) is less than the absorption in the short cell (the reference beam). As a broadening gas is added to the long cell, the absorption increases (although not uniformly at all wavelengths). When the absorption in the long cell, at any wavelength, equals the absorption in the short cell at that wavelength, one can calculate the broadening coefficient by means of an equation similar to Eq. (5.1.2).

\[
B = \frac{P_{B}}{S} \frac{P_{L}}{P_{\text{CO}_2}} - P_{\text{CO}_2} \quad (7.1.1)
\]

It is desirable that the sample in the reference beam be chosen so that its transmissivity is between 10 and 90 percent; this gives
most satisfactory instrument accuracy. If the transmissivity is less than 10 percent, the signal levels driving the nulling servo become very small and noise and scattered radiation become important. If the transmissivity is greater than 90 percent, the effects of changing broadening gas pressure become small.

In this work, two sets of cells were used, depending upon the wavelength interval being investigated. A 2.02 cm reference cell paired with an 8.74 cm sample cell was used during studies of the region from 641 to 695 cm\(^{-1}\) (15.6 to 14.4 \(\mu\)m), while a 400 cm reference cell paired with a 1,600 cm sample cell was used while studying the regions from 719 to 763 cm\(^{-1}\) (13.9 to 13.1 \(\mu\)m) and 581 to 621 cm\(^{-1}\) (17.2 to 161 \(\mu\)m). Unfortunately, we were unable to obtain overlapping wavelength intervals; this would have required a set of cells of intermediate length.

The optical path was purged with dry nitrogen, as usual, and adequate time was allowed to insure sample gas mixing in the cells (aided by a fan in the case of the long path cells). All measurements for a particular broadening gas in a particular wavelength interval were performed in a single session.

7.3 Data Processing

It was anticipated that the data reduction would follow the method outlined by Burch, et al., (1962). In that method, the wavelength interval under study is scanned with the cells evacuated. This defines the line of equal beam transmissivities. The samples are then placed in the cells and spectra scanned at different broadening gas pressures. One can then determine the wavelength
of the intersections of the various curves with the line of equal transmissivity, determine the value of the broadening coefficient at each intersection, and plot the value of the broadening coefficient as a function of wavelength or wavenumber.

Several difficulties were encountered in attempting to use this technique. First, it was found that the ratio of the transmissivities of the two beams was very nearly equal to one (generally the variation would be less than 5 percent) for any given broadening gas pressure. This caused the traces to cross the equal transmissivity line at a small angle, making it very difficult to locate the intersection point accurately. This difficulty was somewhat alleviated by expanding the transmissivity scale by a factor of ten and the wavelength scale by a factor of two. When this large scale factor expansion was used, however, it became obvious that the small non-repeatability in the instrument scale factor (mentioned in section 4.3) combined with the small intersection angle of the traces was causing a large amount of data scatter. This scatter had been present previously, but it became much more noticeable in the expanded scale situation. It also became apparent at this time that the broadening coefficient versus wavelength plot would contain more fine structure than had been anticipated. To define this structure, it appeared that very closely spaced broadening gas pressures would be required. However, the noise on the signal set a finite lower limit on broadening gas pressure increment. After several attempts to use this method had failed, it was concluded that it was not a practical method for use with our equipment.
It seemed that there was a basic difficulty, inherent in the method, that placed severe limitations on it, viz, that the method made use of a very small part (less than 1 percent) of the available information. Only the intersection point of two lines was used; the remainder of the information was ignored.

In an effort to overcome some of the difficulties outlined above, a data reduction scheme was developed to use as much of the available information as possible. This technique was used to determine the broadening coefficient in all cases except for part of the helium data. Because of the unusual nature of the data for helium it was possible to use the method described by Burch, et al. The method used for a particular section of data is indicated on the helium plot. The method used for the reduction of the remainder of the data consisted of the following steps:

1. The wavelength region under examination was scanned three or more times with the cells evacuated. The traces were superimposed. A typical result is shown in Figure 10.

2. The cells were filled with carbon dioxide at the proper pressures.

3. The wavelength region was scanned for several roughly-evenly spaced broadening gas pressures. Generally, five to seven broadening gas pressures were used. A typical example of the instrument strip chart record is shown in Figure 11; the particular record shown is for argon.

4. A tracing of the three equal transmissivity lines and of the smoothed sample traces was made. Wavelength and transmissivity
Figure 10. Line of equal sample transmissivities, 2.02 cm reference cell, 8.74 cm sample cell.
Figure 11.- Instrument output for argon broadened carbon dioxide sample.
scales for the two plots were aligned using reference marks placed on the paper at the time the data were run. The tracing of the equal transmissivity lines of Figure 10 and the argon data of Figure 11 is shown in Figure 12.

5. Cross plots of transmissivity ratio versus

$$\frac{S}{P_{CO_2} - P_{CO_2}^L}$$

at constant wavelengths were made. Typical examples (again for the argon data) are shown in Figure 13.

6. The value of the broadening coefficient could then be read from the cross plot at the intersection of the faired curve with the line indicating a transmissivity ratio equal to one.

7. The broadening coefficient was plotted as a function of wavenumber. When these curves were faired, the pattern of the instrument strip chart record (of which Figure 11 is an example) was examined to determine if the structure appearing on the $B(\nu)$ plot consisted of variations in the data or only noise.

7.4 Results

Plots of carbon dioxide broadening coefficients with respect to the various broadening gases are shown in Figures 14, 15, 16, and 17. These were determined at the test conditions indicated on the various figures. The symbols indicate the points at which the broadening coefficient was determined. The determinations were made using the cross plotting technique described in section 7.3, except
Figure 12.- Smoothed instrument output and averaged line of equal sample transmissivities for argon broadened carbon dioxide.
Indicated transmissivity = 1.0
(Coinsides with data point)

(c) $\nu = 664.5 \text{ cm}^{-1}$.

(d) $\nu = 660.0 \text{ cm}^{-1}$.

Figure 13: Concluded.
Figure 14 - Broadening coefficient for argon vs. wavenumber.
Figure 15.- Broadening coefficient for helium vs. wavenumber.
Figure 16 - Broadening coefficient for nitrogen vs. wavenumber.
Figure 17.- Broadening coefficient for oxygen vs. wavenumber.
except in the case of helium where many of the points were determined using the intersections of the traces with the line of equal sample transmissivity. It was feasible to reduce the helium data in this way because the intersections of the traces and the equal transmissivity line were steep. It should be noted that the broadening coefficient scale on the plots for helium has a different scale factor than that of the other plots.

7.5 Accuracy

Although this technique is subject to the same basic difficulty of matching optical masses as is the technique for measuring the band-averaged broadening coefficient of Chapter 5, we might expect the final result to be somewhat more accurate. This is because the measurements of samples of different lengths are made at the same time (reducing the problem of instrument drifts) and because a large part of the data processing system is eliminated. Uncertainties in optical masses, pressures, instrument drifts, gas composition, and data reduction errors still exist. A measure of the repeatability of the system can be obtained from the data for argon in Figure 14. The plot shows two sets of data taken four days apart. It can be seen that the data are slightly shifted, but obviously the repeatability is very good. Based on these considerations a reasonable value for the 1σ error in the value of the broadening coefficient is 0.05.

A major error would probably take the form of a shift in the curve of self-broadening coefficient versus wavelength rather than producing a radical change in shape of the curve. This conclusion
is based on the fact that improperly formed samples (small errors in carbon dioxide partial pressure, generally) tended to produce results of the same general shape, but of shifted value. The shape was modified somewhat, but the main features were essentially un-changed.

7.6 Discussion

7.6.1 Introduction

The results of the investigation of the wavelength dependence of the carbon dioxide broadening coefficient with respect to argon, helium nitrogen, and oxygen are presented in Figures 14, 15, 16, and 17. It will be noted from the figures that the broadening coefficient is variable with wavelength, and that the shape of the curves is similar for argon, nitrogen and oxygen, but that helium behaves differently from the other gases. In this section these results will be compared with the previous determinations of the band-averaged broadening coefficients and with the work of others wherever possible. The shape of the curves will be discussed and some possible explanations offered.

7.6.2 Comparison with the Band Averaged Broadening Factors

In the discussion of the band averaged broadening factors of Chapter 6, it was noted that argon and helium were of approximately equal effectiveness (on the average) for broadening carbon dioxide absorption lines in the 15 \( \mu \text{m} \) region. The band averaged broadening factors were determined to be 0.80 for helium, 0.78 for argon and 0.85 for oxygen. This result differed from that obtained by Burch et al., (1962a) in the 4.3 \( \mu \text{m} \) (2350cm\(^{-1}\)) band where the broadening
factors were found to be 0.59 for helium, 0.78 for argon, and 0.81 for oxygen.

To make a really valid comparison between the band averaged data of Chapter 6 and the wavelength dependent data, it would be necessary to determine a weighted average of the wavelength dependent data. The weighting function, which would be different for each gas, would be determined by the absorption at each wavelength. Rather than undertaking this task, the arithmetic mean of the data for each gas was found. This is equivalent to saying that the weighting function is equal to one. So long as we are taking ratios between the gases and the character of the absorption is not greatly different for the various gases the results should be reasonably accurate. Table IX displays the means of the wavelength dependent broadening coefficients for the wavelength region from 645 to 690 cm\(^{-1}\) (15.5 to 14.5 \(\mu\)m) and a carbon dioxide partial pressure in the reference cell of 200 Torr. (This is the condition most closely approximating the conditions under which the band averaged factors were determined). Also shown in Table IX are the "broadening factors" computed from these means and the broadening coefficient and relative broadening factors from chapters 5 & 6.

It can be seen that the mean of the broadening coefficient with respect to nitrogen and the broadening factors determined by dividing the means of the broadening coefficients with respect to the other gases into the mean of the broadening coefficient with respect to nitrogen agree quite well with the previously determined band averaged broadening data.
TABLE IX
COMPARISON OF MEANS OF WAVELENGTH DEPENDENT COEFFICIENTS
WITH BAND AVERAGED BROADENING FACTORS

<table>
<thead>
<tr>
<th>Gas</th>
<th>Band Averaged Data</th>
<th>Mean of Wavelength Dependent Data</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>B</td>
<td>F</td>
</tr>
<tr>
<td>N₂</td>
<td>1.30</td>
<td></td>
</tr>
<tr>
<td>O₂</td>
<td>0.85</td>
<td></td>
</tr>
<tr>
<td>A</td>
<td>0.78</td>
<td></td>
</tr>
<tr>
<td>He</td>
<td>0.80</td>
<td></td>
</tr>
</tbody>
</table>
As was found previously, argon and helium have approximately equal broadening factors (although the order is interchanged - not surprising in view of the differences in the shape of their curves of broadening coefficient versus wavenumber). The broadening factor for oxygen is again somewhat higher. Although one must be careful not to attach too much significance to these mean values, it is safe to say that these results support the previous data in that the band averaged broadening factors for argon and helium are very nearly equal in the 15 μm region as had been found in the work discussed in chapter 6.

7.6.3. Structure of the wavenumber dependent broadening coefficients

Before comparing the data obtained in this study with the work of others, it is reasonable to look for an explanation for the peaks in the plots of broadening coefficient versus wavelength. The graphs show that the peaks consistently appear in the results obtained for the various gases. The peaks are most pronounced for argon, nitrogen, and oxygen while for helium fewer peaks are evident.

As a first step the wavenumber at which the peaks appear and their relative heights were read from the plots; these are shown in Table X for argon, nitrogen and oxygen. Because of its unusual behavior helium was not considered in this analysis. Table XI (Drayson et al., 1968) displays the positions and strengths of the major carbon dioxide bands that occur in the wavenumber region where the broadening coefficient has been measured. A comparison of Table X with Table XI shows that there is close agreement between the positions of the centers of the absorption bands and the positions
### TABLE X

**POSITIONS AND RELATIVE HEIGHTS OF BROADENING COEFFICIENT MAXIMA**

<table>
<thead>
<tr>
<th>( \nu \text{ (cm}^{-1} )</th>
<th>( \lambda \text{ (( \mu m ))} )</th>
<th>Relative</th>
<th>Peak</th>
<th>Height</th>
<th>( \text{O}_2 )</th>
<th>( \text{A} )</th>
<th>( \text{N}_2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>741</td>
<td>13.5</td>
<td>6</td>
<td>6</td>
<td>5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>722</td>
<td>13.85</td>
<td>4</td>
<td>3</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>687</td>
<td>14.55</td>
<td>7</td>
<td>7</td>
<td>7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>667</td>
<td>15.0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>645</td>
<td>15.5</td>
<td>5</td>
<td>5</td>
<td>6</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>617</td>
<td>16.2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>595</td>
<td>16.8</td>
<td>3</td>
<td>4</td>
<td>4</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
TABLE XI

BAND INTENSITIES

<table>
<thead>
<tr>
<th>Band Center (C O₂)</th>
<th>Intensity (cm⁻¹ (atm cm)⁻¹ at 300 K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>667.379</td>
<td>194 (1)</td>
</tr>
<tr>
<td>618.033</td>
<td>4.27 (1)</td>
</tr>
<tr>
<td>720.808</td>
<td>5.04 (4)</td>
</tr>
<tr>
<td>667.750</td>
<td>15 (4)</td>
</tr>
<tr>
<td>647.054</td>
<td>1.0 (1)</td>
</tr>
<tr>
<td>791.447</td>
<td>0.022 (2)</td>
</tr>
<tr>
<td>597.337</td>
<td>0.14 (1)</td>
</tr>
<tr>
<td>741.730</td>
<td>0.12 (4)</td>
</tr>
<tr>
<td>668.151</td>
<td>0.85 (2)</td>
</tr>
<tr>
<td>688.672</td>
<td>0.3 (3)</td>
</tr>
<tr>
<td>544.279</td>
<td>0.004 (1)</td>
</tr>
<tr>
<td>581.62</td>
<td>0.0042 (2)</td>
</tr>
<tr>
<td>757.47</td>
<td>0.0059 (2)</td>
</tr>
<tr>
<td>828.284</td>
<td>0.00049 (2)</td>
</tr>
<tr>
<td>738.364</td>
<td>0.014 (2)</td>
</tr>
</tbody>
</table>

(1) Madden (1961)
(2) Yamamoto and Sasamori (1958)
(3) Yamamoto and Sasamori (1964)
(4) Drayson et al., (1968)
of the maxima of the curves of broadening coefficient. Considering those bands having centers located within a few cm\(^{-1}\) of each other to be single bands and rank ordering the bands in terms of their strengths (This lumping of adjacent band is felt to be justified since the instrument resolution is approximately 5 to 6 cm\(^{-1}\) in these tests) produces the results shown in Table XII.

**TABLE XII**

<table>
<thead>
<tr>
<th>Band Intensity (cm(^{-1}))</th>
<th>Band Intensity (atm cm(^{-1})) at 300K</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>667 (667.379+667.750+668.151)</td>
<td>210.0</td>
<td>1</td>
</tr>
<tr>
<td>720.81</td>
<td>5.0</td>
<td>2</td>
</tr>
<tr>
<td>618</td>
<td>4.27</td>
<td>3</td>
</tr>
<tr>
<td>647.1</td>
<td>1.00</td>
<td>4</td>
</tr>
<tr>
<td>688.7</td>
<td>0.30</td>
<td>5</td>
</tr>
<tr>
<td>597.3</td>
<td>0.14</td>
<td>6</td>
</tr>
<tr>
<td>741 (741.7+738.4)</td>
<td>0.13</td>
<td>7</td>
</tr>
</tbody>
</table>

A scatter diagram of the rank order of the height of a peak in the plot of the wavenumber dependent broadening coefficient at a given frequency versus rank order of the band strength at that frequency was plotted, and is shown in Figure 18. This plot shows that the height of the peak of the broadening coefficient tends to be correlated with the strength of the absorption band at the same frequency. The correlation is not perfect, since this rather crude analysis does
not consider such factors as data error, proximity of other bands, or the validity of the measure of the peak importance (possibly peak area is more relevant than peak height).

7.6.4 Comparison with other experimental work

For the 4.3 \( \mu \text{m} \) (2350cm\(^{-1}\)) band, Anderson et al., (1967) found that the broadening coefficient with respect to nitrogen varied smoothly from 1.2 to approximately 1.5. In general, the broadening factor increased with increasing absorption, but the sharp peaking found in the 15 \( \mu \text{m} \) band was not evident. The measurements were made at a resolution similar to that used in this research. Vasilevskii et al., (1967), found that the broadening factor for the 2.06 \( \mu \text{m} \) (4850 cm\(^{-1}\)) band using nitrogen as a broadening gas varied from 1.5 to 2.13. Their measurements were made at high resolution, and the data were obtained by nitrogen–carbon dioxide mixture. The variation of broadening coefficient across the band was smooth.

There are two main differences between the near infrared bands investigated in the above studies and absorption bands in the region. First, the 4.3 \( \mu \text{m}(2350\text{cm}^{-1}) \) and 2.06 \( \mu \text{m}(4855\text{cm}^{-1}) \) bands are single absorption bands, while the 15 \( \mu \text{m}(667\text{cm}^{-1}) \) band consists of several overlapping bands. Second, the 4.3 \( \mu \text{m}(2350\text{cm}^{-1}) \) band and the 2.06 \( \mu \text{m}(4855\text{cm}^{-1}) \) band are parallel bands while the bands in the 15 \( \mu \text{m}(667\text{cm}^{-1}) \) region are perpendicular bands. Either one of these factors could influence the data obtained in this investigation.

Figure 19 displays plots of the broadening coefficient with respect to nitrogen in the 15 \( \mu \text{m} \) region at reference cell pressures
Figure 19. - Comparison of experimental and theoretical wavenumber dependent broadening coefficients for nitrogen.
of 400 Torr and 200 Torr. Also shown, for comparison, are the results obtained by Burch et al., (1962). The test conditions used by Burch et al., (1962) are unknown except that total pressures were restricted to less than one atmosphere. Because of the general similarity of their instrumentation to that used here, the test conditions were probably similar.

The curves shown in Figure 19 are generally similar in shape and mean value, but the data of Burch et al., (1962) are considerably smoother. This could be due to the Model 221 spectrophotometer which was used in making the measurements presented in this discussion being equipped with a brighter source than their Model 21 spectrophotometer. This allowed a somewhat higher resolution to be used than was available to them. Although lower resolutions was not used in an attempt to match their data, it is known from some very limited tests that the height of the sharp peak at 15 \( \mu \)m (667cm\(^{-1}\)) tends to increase with increasing resolution.

In the regions from 588 to 625 cm\(^{-1}\) (17 to 16 \( \mu \)m) and from 714 to 770 cm\(^{-1}\) (14 to 13 \( \mu \)m) the differences between the two sets of measurements cannot easily be accounted for simply by differences in instrument resolution (as the differences in the region from 645 to 690 cm\(^{-1}\) (15.5 to 19.5 \( \mu \)m) might be. If some shifting and smoothing is allowed the data could be placed in reasonably good agreement.

In view of the differences in test apparatus and our lack of information concerning the test conditions under which the data of Burch et al., (1962) were taken, the agreement between the two sets
of data is probably reasonably good.

7.6.5. Comparison with Theory

If all the lines of an absorption band had equal half width and Lorentzian shape, the value of the broadening coefficient would be constant with wavelength and equal to the ratio of the half width of the self-broadened lines to the half width of the foreign gas broadened lines. Madden (1961) showed that the half widths of carbon dioxide absorption lines in the 15 $\mu$m region vary with rotational quantum number. It also appears that the variation depends on the broadening gas used; this was indicated in the measurements made by Vasilevakii et al., (1967) for the 2.06 $\mu$m (4855 cm$^{-1}$) band and is probably true in the 15 $\mu$m (667 cm$^{-1}$) region. These effects would cause the value of the broadening coefficient to vary with wavelength and broadening gas. Because of the complexity of the absorption band in the 15 $\mu$m (667 cm$^{-1}$) region and the lack of information on the variation of line width with rotational quantum number and broadening gas composition in the 15 $\mu$m (667 cm$^{-1}$) region, it is not possible to predict the shape of the broadening coefficient variation with wavelength in terms of the simplified theory discussed in Chapter 2 of this report.

An example of a more sophisticated theoretical approach is the theory developed by Anderson (1949) which was discussed in Chapter 2. Anderson's line broadening theory as refined by Tsao and Curnutte (1962) has been applied to the case of nitrogen-broadened carbon dioxide by Yamamoto et al., (1968). They computed the wavelength dependent broadening coefficient with respect to nitrogen at
10 cm\(^{-1}\) intervals. Their results, the measurements of Burch et al., (1962), and the measurements made in this research are shown in Figure 19. The theory seems to predict the general features of the wavelength dependence of the self-broadening coefficient rather well. The theory seems to agree with the data of this investigation better than with that of Burch et al., (1962) in the regions from 588 to 625 cm\(^{-1}\) and from 714 to 770 cm\(^{-1}\). However, in the central region (645 to 690 cm\(^{-1}\)) the agreement with the data of Burch et al. appears to be better.

There is one feature of the theoretical calculations that seems inconsistent with the experimental results. It appears that where ever sharp peaks in the experimental data occur (615, 614, and 722 cm\(^{-1}\)), the theory predicts a decrease in the self-broadening coefficient. The effect occurs at the three locations mentioned and possibly also at 595 cm\(^{-1}\) although the experimental peak is not so pronounced there as it is at the other wavenumbers. The fact that the theoretical calculations do not predict these peaks would seem to indicate some difficulty with the theory.

7.6.6 The effect of line shape

The broadening coefficient depends on pressure, an effect which is not predicted by a theory involving Lorentz shaped lines of equal half width and a sharp peaking of the self-broadening coefficient occurs in the region of band centers which is not predicted by the line broadening theory of Anderson. The pressure dependence, the sharp peaking near band centers and the rather unusual behavior of helium might be explained if the shape of the
absorption lines depended upon the broadening gas. A heuristic argument in favor of such an explanation is as follows. In the regions near the band centers, the centers of the individual absorption lines are very nearly opaque at the test conditions used here. In the regions away from the band centers this is not the case. Hence, as the broadening gas is added, much of the effect of the broadening gas in the vicinity of the band centers results from the change in absorption of the wings of lines that are located outside the region of the band center. In the regions between band centers the increasing absorption is a result of the increased absorption near the centers of the weaker non opaque lines located there. (It should be noted that many of the same effects could be produced by properly varying half widths.)

If this argument were valid, the ratio of the maximum broadening coefficient in the region of band centers to the minimum broadening coefficient between bands should be large for broadening gases producing lines with weak wings and small for broadening gases producing lines with strong wings. If this is the case, then, from the results obtained in this work data helium should broaden the wings of lines considerably less than would argon, nitrogen, or oxygen.

Although experimental measurements of the shape of carbon dioxide lines in the far wings ($\nu - \nu > 10\alpha$) are relatively few, two different groups have obtained some data. Both of the investigations Burch et al., (1968) and Winters et al., (1964) used a similar method, which will be described below and their results will be discussed.
Essentially what is done is to locate a region in an absorption band where the absorption is caused by the wings of lines whose centers are outside the region, i.e., there are no lines centered in this region. If the positions and strengths of the lines in the band are known, an absorption spectrum for the band can be readily calculated. By comparing measured absorption spectra with absorption spectra which have been calculated for various line shapes the shape of the wings of the spectral lines can be empirically determined. In practice the high frequency wings of bands having sharp band heads have been used in these investigations.

Winters et al., (1964) have used this method to investigate the shapes of wings in the region from 2400 to 2600 cm\(^{-1}\), for self-broadening and broadening by nitrogen and oxygen. Their results indicate that the wings are definitely sub-Lorentzian in this region for both self- and foreign gas broadening. The wings of the foreign gas broadened lines were weaker than the wings of the self-broadened lines. Nitrogen and oxygen produced results similar to each other. Experimental conditions were similar to those of this work.

Burch et al., (1968) used the same method to investigate the high frequency wings of the bands in the vicinity of 1.43 \(\mu\)m (7000 cm\(^{-1}\)), 2.63 \(\mu\)m (3800 cm\(^{-1}\)) and 4.3 \(\mu\)m (2350 cm\(^{-1}\)). The shapes of the wings were investigated for self-broadening and for foreign gas broadening using argon, helium, hydrogen, nitrogen, and oxygen as broadening gases. Their results which were consistent in all of the bands, can be summarized as follows:
1. The wings of the self-broadened lines were definitely sub-Lorentzian, although not as much as had been found by Winters et al.

2. All foreign gases produced lines with weaker wings than wings than self-broadened lines.

3. The line shapes for nitrogen, argon, and oxygen were generally similar.

4. The line shapes for hydrogen and helium were similar, but the wings were considerably weaker than the wings of the nitrogen, argon, or oxygen broadened lines.

All of the above conclusions apply to the wings of the lines at distances approximately 10 half widths or more from the line center. They also found that the deviation from the Lorentzian shape increased with decreasing wavenumber as one moved from band to band.

If the same effects are assumed to hold for the 15 μm band of carbon dioxide and, in addition, effects in the low frequency wings of lines are assumed to be the same as those in the high frequency wings, then the peaking of the broadening coefficient in the band centers and the unusual behavior of helium relative to that of argon, nitrogen, and oxygen might be a result of this difference in line shape.

7.6.7 Summary

In this section the wavelength dependent broadening coefficients for carbon dioxide with respect to argon, helium, and nitrogen and oxygen have been discussed. It has been concluded that the result
discussed in Chapter 6, viz, that helium and argon have similar band averaged broadening factors and that the broadening factor for oxygen is somewhat higher is verified by these data. It has been shown that the fine structure of the broadening coefficient versus wavelength curve is correlated with the presence of several absorption bands in the 15 µm (667cm⁻¹) region. The results for nitrogen broadening have been shown to be in fairly good agreement with other experimental measurements. The results for nitrogen broadening have also been compared with theory and it has been concluded that the theories are not adequate to predict the observed data. Finally, it has been concluded that line half widths that vary with rotational quantum number and broadening gas and line shapes that vary with broadening gas could have produced the observed results.
8.1 Conclusions

As noted in Chapter 1, the experiments carried out in this investigation had as their object several goals. It was planned that these goals would be reached in such a manner that each step would lead to confidence in the results of the steps that followed. These goals (in order of discussion) were:

1. To obtain spectra in the 15 $\mu$m region for nitrogen broadened carbon dioxide samples for comparison with previous experimental work and with the theoretical calculations in the 15 $\mu$m band by Drayson and Young (1966) and Drayson et al., (1968).

2. To determine the band-averaged broadening coefficient for carbon dioxide with respect to nitrogen in the 15 $\mu$m region for comparison with other experimental determinations of this quantity.

3. To determine the band-averaged broadening factors with respect to nitrogen in the 15 $\mu$m region for argon, helium, and oxygen.

4. To investigate the wavelength dependence of the broadening coefficients for argon, helium, nitrogen, and oxygen in the 15 $\mu$m region.

The first two of the above items were performed primarily to determine whether or not the instrumentation system and data processing methods used would produce results that were in agreement with the work of others. Comparing the spectra obtained in this study
with those of Burch et al., (1962) lead to the conclusion that the instrumentation system and data processing methods were satisfactory. The spectra were also compared with the calculations of Drayson and Young (1966) and Drayson et al., (1968). It was evident that the calculations tended to overpredict the equivalent width for long path lengths, high equivalent pressures (near one atmosphere) and low concentrations of carbon dioxide. Although the comparisons were not complete enough to isolate the difficulties, they might be due to poor estimates of some band strengths and the use of a line shape (Lorentz) that overpredicts the absorption in the wings of foreign gas broadened lines.

Investigation of the band-averaged broadening factors showed that all the gases investigated (argon, helium, and oxygen) were less effective than nitrogen in broadening carbon dioxide absorption lines in the 15 \( \mu \text{m} \) region. These factors were not constant, but rather were weakly dependent on the gas pressure and the optical mass. Rather unexpectedly it was found that argon and helium were approximately equally effective on the average, for broadening the absorption lines. This result was different from that obtained by Burch et al., (1962a) in their investigation of the 4.3 \( \mu \text{m} \) band where they found that helium was considerably less effective than argon. It did agree, however, with recently published data of Patty et al., (1968) who found argon and helium to be of approximately equal effectiveness in the 10.6 \( \mu \text{m} \) region. Although the data of Patty, et al., (1968) were obtained using a method that is quite different from the technique used in this study and that of Burch et al., they do substantiate the idea gained by comparing
the present work at 15μm with the work of Burch et al., (1962a) at 4.3 μm, that the effects of a broadening gas might be very different in different absorption bands of an active gas. (This has been noted previously by others, e.g., Coggeshall and Saier (1947) under somewhat different conditions).

A check on the equality of the band-averaged coefficients for argon and helium was carried out during the investigation of the wavelength dependence of the broadening coefficients. This check indicated that the band-averaged data were correct and that argon and helium would be of approximately equal effectiveness, on the average, for broadening carbon dioxide lines in the 15 μm region in spite of the fact that the wavelength dependence of their broadening coefficients was quite different.

It was found that the broadening coefficients for the different gases were quite variable depending upon the wavelength. These variations were least for argon (+ 10 percent of the mean value) and greatest for helium (+ 30 percent of the mean value). The broadening coefficients for the various gases tended to increase rather sharply at particular wavelengths. It was shown that the positions and heights of these peaks were correlated with the positions and strengths of the stronger absorption bands in the region.

A dependence of the broadening coefficient on absorber partial pressure or optical mass was discovered; this is contrary to the work of Burch et al., (1962) in the 15 μm region for nitrogen. This dependence was not investigated extensively and the effects of optical mass and of pressure were not separated.
The wavelength dependent broadening coefficient for nitrogen was compared with the predictions of Anderson’s theory (Anderson, 1949) as calculated by Yamamoto et al., (1968). The theory predicted the mean value and general shape of the wavelength dependent broadening coefficient rather well. It did, however, predict a decrease in the value of the broadening coefficient in each of the wavelength regions where a sharp peak in the value was found in the experimental data. On the basis of this comparison, it was concluded that the theory is not too satisfactory.

The possibility that the peaks were caused by a pressure broadened line shape that is sub-Lorentzian in the wings was discussed. Using a qualitative argument it was shown that such a line shape could produce the observed effect. It is known (Winters et al., (1964) and Burch et al., (1968) that the wings of foreign gas broadened lines in other carbon dioxide absorption bands are sub-Lorentzian. Unfortunately, however, much the same argument can be used to show that a band consisting of Lorentzian lines of properly varying half width might produce similar effects. We were not able to determine which, if either or both, of these mechanisms were present here. Further work will be required to determine the relative importance of these two effects.

8.2 Suggestions for future work

The results of this research have indicated that more theoretical and experimental work is needed in the 15 μm absorption band of carbon dioxide. Before the theory can be developed much further, however, it is likely that more experimental data must be obtained.
It now appears that the shape of the wings of the absorption lines and the variation of the line half width with rotational quantum number are the two most important areas which must be investigated. Both of these appear to be variable depending upon the composition of the broadening gas. The shapes of the far wings of lines might be investigated by a method similar to that used by Winters et al., (1964) and Burch et al., (1968). The measurement will be more difficult (if at all possible) in the 15 μm region because of the presence of several overlapping bands in this region. The variation of line half width with rotational quantum number can probably be best investigated either by conventional high resolution spectroscopy or possibly by some of the techniques that use a tunable laser as a radiation source.

Using techniques similar to that used in this experimental program one might determine the band-averaged and wavelength dependent broadening factors for other broadening gases. Neon and hydrogen would be of particular interest here. Since neon has a polarizability between that of helium and argon one might be able to determine whether or not the line width is proportional to some collision frequency-polarizability product as has been suggested by Patty, et al., (1968). Since hydrogen has been found to produce a line shape in the far wings quite similar to that of helium, but has an average broadening factor that is quite different in other absorption bands of carbon dioxide, it would be of value to compare the band average broadening factors and the wavelength dependent broadening coefficients for these two gases in the 15 μm region.
If the structure of the wavelength dependent broadening coefficient is caused by the presence of low absorption in the line wings we might expect the wavelength dependent broadening coefficients to be of generally similar form, but possibly of quite different mean value.

Theoretical calculations similar to those of Drayson and Young (1966) and Drayson et al., (1968) might be used to determine whether or not line shapes having sub-Lorentzian wings would produce the experimentally observed effects. This might be done by a point by point division of two spectra (one for pure carbon dioxide using Lorentz lines and the other for a carbon dioxide broadening gas mixture using a line shape having sub-Lorentzian wings.) This is, in essence, a simulation of the spectrophotometer as it operated during the determination of the wavenumber dependent broadening coefficient. On the basis of such calculations it might be possible to empirically determine the line shapes produced by the various broadening gases. These shapes could then be used to improve the accuracy of the techniques used for the inversion from atmosphere radiance profiles to atmospheric temperature profile.


Winters, B. 1963: Line shape in the wing beyond the band head of the 4.3 m band of CO2. Scientific report number I, Physics Dept., Catholic Univ., Washington, D. C.


Young, C., 1965a: Calculation of the absorption coefficient for lines with combined Doppler and Lorentz broadening. J. Q. S. R. T., 5, 549-552.

Young, C., 1965b: Tables for calculating the Voigt Profile. Univ. of Michigan Report 05863-7-T.