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## PROPERTIES OF PARTICLE-GENERATED TURBULENCE IN THE FINAL-DECAY PERIOD

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### Abstract

The properties of turbulence generated by uniform fluxes of polydisperse spherical particles moving through a uniform flowing gas were studied experimentally, emphasizing the properties of the turbulent interwake region surrounding the individual particle wake disturbances. Mean and fluctuating velocities, as well as probability density functions, energy spectra and integral and Taylor length scales of velocity fluctuations, were measured within a counterflow particle/air wind tunnel using particle wake discriminating laser velocimetry. Test conditions involved various binary mixtures of spherical gas particles having nominal diameters of 0.55, 1.1 and 2.2 mm and particle Reynolds numbers of 106, 373 and 990. When combined with earlier measurements limited to monodisperse spherical particles, the test conditions included mean particle spacings of 10-210 mm, particle volume fractions less than 0.003%, direct rates of dissipation of turbulence kinetic energy by particles less than 4%, and turbulence generation rates sufficient to yield streamwise and cross-stream relative turbulence intensities in the range 0.2-1.5%. The turbulent interwake region for these conditions has properties that correspond to the final-decay period of grid-generated turbulence, involving homogeneous and nearly isotropic turbulence having probability density functions that were well approximated by Gaussian functions with turbulence Reynolds numbers of 0.4-3.5. Mixing rules were developed that successfully extended earlier results for the interwake turbulence properties of monodisperse particle phases to polydisperse particle phases, based on dissipation weighting of the properties of each particle size group. The flow in the final-decay period consisted of vortical regions that filled the turbulent interwake region but were sparse which resulted in several unusual features compared to conventional isotropic turbulence, as follows: enhanced rates of dissipation of turbulence kinetic energy, unusually large ratios of integral/Taylor length scales for small turbulence Reynolds numbers, and decreasing ratios of integral/Taylor length scales with increasing turbulence Reynolds numbers which is opposite to the behavior of conventional grid-generated turbulence at large turbulence Reynolds numbers. The large range of scales where effects of viscosity were small in the final-decay region also yielded a Kolmogorov-like  $-5/3$  power inertial decay region on dimensional grounds, very similar to the inertial decay region of conventional turbulence at large turbulence Reynolds numbers.

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## Nomenclature

A	=	dimensionless integral length scale; Eq. (17)
$C_d$	=	particle drag coefficient
D	=	dissipation factor; Eqs. (9) and (11)
$d_p$	=	particle diameter
$E_u(k)$	=	streamwise energy spectrum
f	=	frequency
$g(k, \ell_K)$	=	dimensionless energy spectra function; Eq. (14)
K	=	kurtosis of a PDF
k	=	wave number, $2\pi/s$
$L_u$	=	streamwise integral length scale
$\ell_K$	=	Kolmogorov length scale, $(\nu^3/\varepsilon)^{1/4}$
$\ell_p$	=	mean particle spacing; Eq. (1)
M	=	mesh size of a grid
N	=	number of particle size groups
n	=	power in turbulence decay law; Eq. (6)
$n''$	=	particle number flux
PDF	=	probability density function
Re	=	particle Reynolds number, $d_p U_p / \nu$
$Re_\lambda$	=	turbulence Reynolds number, $\lambda \bar{u}' / \nu$
S	=	skewness of a PDF
s	=	distance
$t_K$	=	Kolmogorov time scale, $(\nu/\varepsilon)^{1/2}$
$U_p$	=	mean streamwise relative velocity of a particle
u	=	streamwise gas velocity
$u_K$	=	Kolmogorov velocity scale, $(\varepsilon\nu)^{1/4}$
v	=	cross-stream gas velocity
x	=	streamwise distance
$x_o$	=	streamwise virtual origin location
$\beta$	=	empirical factor; Eqs. (6) and (8)
$\varepsilon$	=	rate of dissipation of turbulence kinetic energy
$\theta$	=	particle wake momentum diameter, $(C_d d_p^2 / 8)^{1/2}$
$\lambda$	=	Taylor dissipation length scale; Eq. (5)
$\nu$	=	molecular kinematic viscosity of air

## Subscripts

b	=	particle size group of a binary mixture having the larger diameter
i	=	particle group i
s	=	particle size group of a binary mixture having the smaller diameter

## Superscripts

$(\bar{\quad})$	=	mean value
$(\overline{\quad})^r$	=	rms fluctuating value
$(\overline{\quad})^2$	=	mean-square fluctuating value

## Introduction

Turbulence generation is the main source of turbulence in the dense (near-injector) region of sprays as well as in some natural dispersed multiphase flows, e.g., rainstorms and hailstorms. Early studies showed that turbulence generation due to particles (drops) involved particle wakes embedded in a turbulent interwake region.<sup>1,2</sup> Subsequent studies showed that the particle wakes scaled similar to laminar wakes but exhibited fast mixing due to the presence of turbulence (and as a result were called “laminar-like turbulent wakes”).<sup>3-6</sup> More recent studies of monodisperse particle flows, Refs. 7 and 8, showed that the turbulent interwake region consisted of isotropic turbulence in the rarely-observed final-decay period, defined by Batchelor and Townsend<sup>9,10</sup> more than fifty years ago. In addition, an analogy was developed between grid-generated isotropic turbulence and particle-generated isotropic turbulence, when both were in the final-decay period, that provided useful correlations for the properties of the turbulent interwake region (for monodisperse particle flows) in terms of the rate of dissipation of mechanical energy of the particles (which is known from the drag properties and motion of the particles relative to the continuous phase). The objective of the present experimental investigation was to develop mixing rules to extend these ideas to dispersed particle flows involving polydisperse particle phases.

Present measurements were carried out in a vertical counterflow particle/air wind tunnel. Binary particle pairs involving various proportions of nearly monodisperse glass spheres were considered, however, the nature of the mixing rules that were developed suggests that this information can be extended to flows involving more general variations of particle sizes in a straightforward manner; therefore, the particle phase will simply be designated as polydisperse in the following. Measurements of the interwake region were made using particle wake discriminating laser velocimetry to find the moments and the PDFs of streamwise and cross-stream velocities, the energy spectra of streamwise velocity fluctuations, and the characteristic micro- and macro-length scales (streamwise integral and Taylor dissipation length scales) of the interwake turbulence. These results were interpreted and correlated similar to Ref. 7, by developing analogies between the turbulent interwake region of turbulence generation processes due to particles and homogeneous grid-generated turbulence, e.g., the studies of grid-generated turbulence of Refs. 10-22 and references cited therein.

## **Experimental Methods**

### **Test Apparatus**

The apparatus consisted of a vertical counterflow wind tunnel with upflowing air moving toward the suction side of the blower and freely falling spherical glass particles introduced at the top of the wind tunnel (see Chen<sup>23</sup> for a complete description of the apparatus). Various binary particle mixtures of nearly monodisperse spherical particles were considered, using individual particle feeders for each particle size of the mixture. The air flow path consisted of a rounded inlet, a flow straightener and a 16:1 contraction ratio to a windowed test section having a 305×305 mm cross-section. The particle flow path consisted of a variable-speed particle feeder for each particle size, a screen array particle dispersion section, a honeycomb particle flow straightener, and a particle acceleration section to yield particles having nearly terminal streamwise velocities in the test section. The particles were collected in a flexible plastic funnel below the air inlet. The particles were not damaged during passage through the apparatus; therefore, they were washed with detergent, dried and sieved to retrieve the original particle sizes so that they could be reused.

### **Instrumentation**

Measurements of particle number fluxes, gas velocities and particle velocities will only be discussed briefly because they have been fully described earlier.<sup>6-8</sup> Particle number fluxes were measured by collecting particles for timed intervals in a thin-walled cylinder closed at the bottom. The experimental uncertainties (95% confidence) of these measurements were less than 10%.

Gas velocities were measured using a single channel LV, rotating the optical plane in order to measure streamwise and cross-stream velocities. Velocities were found from the low-pass filtered analog output of the LV burst counter signal processor, using frequency shifting and a constant sampling rate of the burst counter output to eliminate effects of directional bias, directional ambiguity, and velocity bias. Heavy LV seeding levels were used so that effects of LV step noise were deferred to scales roughly an order of magnitude larger than the Kolmogorov scales. Tests with various seeding levels, however, showed that the LV seeding had essentially no effect on continuous phase turbulence properties. A particle detector was installed just above the LV sampling location, as discussed by Chen and Faeth.<sup>7</sup> Given the output of this detector and the known properties of laminar-like turbulent wakes, portions of the velocity signals that were in the particle wake region were eliminated,

providing conditional records of the velocity properties of the turbulent interwake region alone.

LV velocity records, having drop-out periods that resulted when disturbances caused by particle wakes were removed, were analyzed directly by correcting the sampling time for most velocity statistics, e.g., moments and PDF properties. In contrast, obtaining correct temporal power spectra in the presence of drop-out periods requires special treatment as discussed by Buchhave<sup>24</sup> and Buchhave et al.<sup>25</sup> (see Ref. 23 for the present application of these methods). Upflow mean velocities in the wind tunnel were selected to provide absolute turbulence intensities smaller than 15% so that LV measuring conditions were excellent.<sup>26</sup> As a result, Taylor's hypothesis could be used to convert the measured temporal power spectra and scales to spatial energy spectra and scales of streamwise velocities. Sampling periods were adjusted to provide experimental uncertainties (95% confidence) less than 5% for mean streamwise velocities, less than 10% for streamwise and cross-stream rms velocity fluctuations, less than 10% for PDFs within one standard deviation of the most probable velocity and less than 20% for temporal power spectra at frequencies smaller than the reciprocal of the temporal integral scale with reduced uncertainties elsewhere.

Particle velocities were measured with the same LV arrangement. One difference, however, was that the LV optics were changed to increase the measuring volume diameter by a factor of roughly 30 to 1.5 mm and the measuring volume length by roughly a factor of 20 to 10 mm so that the larger measuring volume provided a reasonable sampling rate for particle velocities. The gas was not seeded during the particle velocity measurements and the large-amplitude signals from the glass particles were easily separated from background signals due to dust particles in the air. Experimental uncertainties (95% confidence) of streamwise mean particle velocities were less than 5%.

### **Test Conditions**

Particle properties are summarized in Table 1. Each particle size group was nearly monodisperse and spherical with nominal diameters of 0.5, 1.1 and 2.2 mm and corresponding Reynolds numbers of 106, 373 and 990. The particle Reynolds numbers are representative of the intermediate Reynolds number conditions typical of drops providing significant degrees of turbulence generation in sprays.<sup>3</sup> Terminal velocities and drag coefficients were measured, yielding values that agreed with the standard drag curve for spheres, due to Putnam,<sup>27</sup> within 15%. The particles approached but did not reach terminal velocity conditions during the present measurements, e.g., rates of particle acceleration at the measuring location were

2, 11 and 14% of the mean particle velocities per meter for the three particle size groups. Finally, cross-stream mean particle velocities, and streamwise and cross-stream particle velocity fluctuations (excluding streamwise velocity variations associated with varying particle diameters) were small due to the large inertia and poor particle response to air motion of the present particles.

Test conditions for the various binary particle phases that were considered are summarized in Table 2. Results from Chen and Faeth<sup>7</sup> for monodisperse phases were combined with the present results for binary phases, after developing appropriate mixing rules for the binary phases; therefore, the test conditions for the various monodisperse phases considered by Chen and Faeth<sup>7</sup> are summarized in Table 3 for reference purposes.

Assuming that the particles are monodisperse and that the particles are falling randomly, the mean particle spacing can be found from:<sup>6</sup>

$$\ell_p = [(U_p - \bar{u})/n']^{1/3} \quad (1)$$

This expression was modified to treat the present binary particle phases using dissipation-weighted averaging to find an average  $U_p$  that will be described subsequently. For the combined monodisperse and binary particle phase test conditions considered here, mean particle spacings were in the range 10-210 mm with corresponding particle volume fractions less than 0.003%.

The direct dissipation of turbulence kinetic energy (dissipation) by particles was less than 4% for all test conditions, see Chen<sup>23</sup> for a discussion of this estimate. In addition, dissipation within the wake disturbances was also small, less than 12% of the total dissipation, as discussed by Chen and Faeth<sup>7</sup> for all test conditions. As a result, the rate of dissipation within the turbulent interwake region can be found from the rate of turbulence generation by the particles, where  $\varepsilon_i$  is the rate of dissipation of particle group  $i$ , as follows:

$$\varepsilon_i = \pi \dot{n}_i (d_p^2 C_d U_p^2 / 8)_i \quad (2)$$

and the total dissipation given  $N$  particle size groups is found by summing the contributions of each particle size group, as follows:

$$\varepsilon = \sum_{i=1}^N \varepsilon_i \quad (3)$$

Given  $\varepsilon$ , the Kolmogorov length, time and velocity scales for the turbulent interwake region can be computed from their definitions, as follows:<sup>28</sup>

$$\ell_K = (\nu^3 / \varepsilon)^{1/4}, \tau_K = (\nu / \varepsilon)^{1/2}, u_K = (\nu \varepsilon)^{1/4} \quad (4)$$

Thus, given the ranges of  $\varepsilon$ , the ranges of these scales can be found from Eqs. (4) as summarized in Tables 2 and 3 for binary and monodisperse particle phases, respectively. For these same dissipation rates, the relative turbulence intensities caused by turbulence generation were in the range 0.2-1.5%, based on the dissipation weighted value of  $U_p$  that will be discussed later. Similar to the earlier measurements for monodisperse particle phases,<sup>7</sup> the present measurements also indicate that interwake turbulence is similar to homogeneous isotropic turbulence so that the Taylor dissipation length scale can be estimated as follows:

$$\lambda = (15\nu\bar{u}'^2 / \varepsilon)^{1/2} \quad (5)$$

The resulting values of  $\lambda$  for all test conditions are comparable but somewhat larger than the Kolmogorov scales (e.g.,  $\lambda/\ell_K = 1.3-3.5$ ). The corresponding range of turbulence Reynolds numbers for all test conditions,  $Re_\lambda = \lambda\bar{u}'/\nu$ , is 0.4-3.5, which is relatively small, helping to explain why the Taylor and Kolmogorov length scales are nearly the same. Streamwise integral length scales were obtained from the energy spectra as discussed later, yielding values of 11-178 mm, which are comparable to the mean particle spacings, for all test conditions.

Finally, evaluation of the apparatus for binary particle phases yielded results very similar to earlier evaluation of the apparatus for monodisperse particle phases.<sup>6,23</sup> In particular, particle number fluxes and phase velocities varied less than experimental uncertainties over the central 205×205 mm cross-section of the flow, extending 200 mm in the streamwise direction, which surrounded the location where measurements were made. The measurements also showed that flow properties varied less than experimental uncertainties as a function of time. Thus, the present flows were properly homogeneous and stationary, with the turbulence within the turbulence interwake region produced by turbulence generation, as desired.

## **Results and Discussion**

### **Relative Turbulence Intensities**

Batchelor and Townsend<sup>9,10</sup> defined three regions of turbulence downstream of a turbulence-producing grid, as follows: (1) a developing period near the grid where wakes from grid elements are merging and the flow is neither homogeneous nor isotropic; (2)

an initial-decay period, where the turbulent flow is homogeneous and locally isotropic; and (3) a final-decay period, where effects of fluid inertia forces are negligible so that the governing Navier-Stokes equations of the flow become linear, where regions containing vorticity become sparse (giving the appearance of isolated turbulent spots based on single-point measurements), and where the turbulence decays more rapidly than in the initial decay region. Based on the earlier observations of flows due to turbulence generation caused by monodisperse particles,<sup>7</sup> it appears that the final-decay period is associated with the turbulent interwake region of these flows. Supporting this idea is the fact that  $Re_\lambda \leq 3.5$  for the conditions of both past observations of the interwake region for monodisperse particle phases and for present observations of the interwake region for polydisperse particle phases, whereas Batchelor and Townsend<sup>9,10</sup> suggest a value of  $Re_\lambda < 5$  as the condition for the presence of the final-decay period of grid-generated turbulence.

The analogy between grid-generated turbulence and the turbulent interwake region developed in Ref. 7 was based on the following expression for grid-generated turbulence due to Batchelor and Townsend:<sup>9,10</sup>

$$(\bar{u}' \text{ or } \bar{v}')/U_p = \beta [C_d M / (x - x_0)]^n \quad (6)$$

where  $\beta$  is an empirical factor,  $C_d$  is the drag coefficient of the grid,  $M$  is the mesh size (or spacing of the grid elements), and  $(x - x_0)$  is the distance of the point of observation from the virtual origin of the grid. In addition, they find, based on both analysis and measurements that  $n = 1/2$  and  $5/4$  for the initial- and final-decay periods, respectively. The various parameters of Eq. (6) for grid-generated turbulence were then related to the parameters of the turbulent interwake region, as follows:<sup>7</sup> the length corresponding to the product of the mesh size and the drag coefficient of grid-generated turbulence was taken to be the particle wake momentum diameter,  $\theta$ , which similarly involves the product of the size of an element resistive to flow motion and its drag coefficient; the distance from the grid for grid-generated turbulence was taken to be on the order of the mean particle spacing for the homogeneous turbulent interwake region assuming that this represents the open or undisturbed region where the turbulent interwake region can develop; and the mean velocity of the continuous phase relative to the grid for grid-generated turbulence was taken to be the mean velocity of the particles relative to the velocity of the continuous phase for the turbulent interwake region. Given these analogies, the expression corresponding to Eq. (6) for the turbulent interwake region becomes:

$$(\bar{u}' \text{ or } \bar{v}')/U_p = \beta (\theta / \ell_p)^n \quad (7)$$

where  $\beta$  may not necessarily be the same for  $\bar{u}'$  or  $\bar{v}'$ . Then noting that  $\theta = (C_d d_p^2 / 8)^{1/2}$ , finding  $\ell_p$  from Eq. (1), and eliminating  $n$  from the resulting equation using Eqs. (2) and (3), appropriately averaged for polydisperse particle phases as will be discussed subsequently, yields the following correlation for the relative turbulent intensity of the turbulent interwake region:

$$(\bar{u}' \text{ or } \bar{v}')/U_p = \beta D^{n/3} \quad (8)$$

where  $D$  is a dimensionless dissipation factor defined as follows for monodisperse particle phases:<sup>7</sup>

$$D = \left( \frac{\theta}{\ell_p} \right)^3 = \frac{\varepsilon d_p (C_d / 8)^{1/2}}{\pi U_p^2 (U_p - \bar{u})} \quad (9)$$

The modification of the expression for  $D$  needed to treat polydisperse particle phases will be discussed next.

Dissipation-weighted averaging was used to treat polydisperse particle phases based on the particle dissipation factor for particle size  $i$ , as follows:

$$D_i = \frac{\varepsilon_i d_{pi} (C_{di} / 8)^{1/2}}{\pi U_{pi}^2 (U_{pi} - \bar{u})} \quad (10)$$

The flow dissipation factor was then taken to be the sum:

$$D = \sum_{i=1}^N D_i \quad (11)$$

Finally, to complete the mixing rules needed to treat polydisperse particle phases, dissipation-weighted averaging was used to find the effective relative particle velocity:

$$U_p = \sum_{i=1}^N (D_i / D) U_{pi} \quad (12)$$

The idea behind the mixing rules embodied by Eqs. (10)-(12) for polydisperse particle phases was to emphasize the fact that turbulence generation is created by the dissipation of the turbulence kinetic energy of the particle phase. This approach also avoids overweighting the importance of potentially large

numbers of small particles on flow properties, e.g. seeding particles having negligible slip that really would contribute very little to the properties of the interwake turbulent region caused by turbulence generation due to their small relative motion with respect to the continuous phase, and thus their small rates of dissipation of the kinetic energy of the particle phase.

Present measurements of streamwise and cross-stream relative turbulence intensities,  $\bar{u}'/U_p$  and  $\bar{v}'/U_p$ , within the turbulent interwake region of all the binary particle mixtures considered during the present experiments, are plotted in Fig. 1 according to Eq. (8), in conjunction with the mixing rules for polydisperse particles of Eqs. (10)-(12). Earlier results from Ref. 7 for monodisperse particles are also shown on the figure, plotted in the same manner (noting that the mixing rules of Eqs. (11)-(12) properly retrieve the original formulation for monodisperse particles). The correlation of the results for both monodisperse and polydisperse particle phases is seen to be remarkably good, for the roughly two orders of magnitude range of  $D$  that spans the data. Best-fit correlations of the data yielded powers of  $D$  in the correlations Eqs. (8) of  $1/2$  within experimental uncertainties (95% confidence), as follows:

$$\bar{u}'/U_p = 9.3D^{1/2}, \quad \bar{v}'/U_p = 8.7D^{1/2} \quad (13)$$

with the standard deviations of both coefficients of Eqs. (13) of 1.2 and with the correlation coefficients of these fits of 0.98 and 0.96, respectively, which is excellent. The powers of  $D$  in Eq. (13) suggest that  $n=3/2$  from Eq. (8) which is reasonably close to the value of  $n=5/4$  for the final decay period suggested by Batchelor and Townsend<sup>9,10</sup> (the results of Fig. 1 also agree with the estimate that the present turbulent interwake regions should be in the final decay period because  $Re_\lambda < 3.5$  for these flows).

The difference between the coefficients of Eqs. (13) is not statistically significant so that the turbulent interwake region is isotropic within the limitations of existing measurements of these properties. In addition, present findings are consistent with the observations of Bennett and Corrsin<sup>29</sup> of isotropic turbulence at relatively small Reynolds numbers ( $Re_\lambda = 36-72$ ) which yielded  $\bar{u}'/\bar{v}'$  in the range 1.09-1.22, compared to the present values observed for the turbulent interwake region of 1.15 from Eqs. (13).

### **PDFs**

Typical measured PDFs of streamwise and cross-stream velocities in the turbulent interwake region for various polydisperse particle phases are illustrated

in Figs. 2 and 3. Best Gaussian fits of the measurements are also shown on the plots. The PDFs are plotted using logarithmic coordinates in order to highlight potential effects of wake disturbances and the performance of the fits at the extremities of the distributions where the PDFs become small.

The PDFs for polydisperse particle phases illustrated in Figs. 2 and 3 are essentially identical to the earlier results illustrated in Ref. 7 for monodisperse particle phases. Thus, there are no obvious bimodal properties of the velocity fluctuations due to the bimodal nature of the dispersed phase as well as the bimodal properties of the dispersed-phase wakes. The cross-stream PDFs illustrated in Fig. 3 are symmetric and are in generally good agreement with the Gaussian fits except for slight upward biases near both ends of the distributions. These biases are thought to be due to sampling limitations because the values of the PDFs are very small in this region, ca.  $10^{-3}$ , which requires a large number of samples to properly resolve.

The PDFs of streamwise velocity fluctuations illustrated in Fig. 2 are clearly asymmetric with an upward bias of the distributions roughly near  $-2.5$  standard deviations from the mean which is due to small disturbances from velocities in particle wakes that were not completely eliminated by the present wake discrimination system.

The rest of the properties of the PDFs for polydisperse particle phases were also the same as for monodisperse particle phases, as follows (giving standard deviations in parentheses):  $S(u)$  and  $S(v)$  are  $-0.6(0.2)$  and  $0.0(0.3)$ , respectively; and values of  $K(u)$  and  $K(v)$  are  $5(1)$  and  $4(1)$ , respectively. The departures of  $S(u)$  and  $S(v)$  from the Gaussian value of  $S=0$  are not statistically significant; the departures of  $K(u)$  and  $K(v)$  from the Gaussian value of  $K=3$  also border on statistical significance particularly in view of the larger experimental uncertainties of this higher-order moment due to sampling limitations. These findings were similar to results for  $S(u)$ ,  $S(v)$ ,  $K(u)$  and  $K(v)$  from the earlier tests for monodisperse particle phases<sup>7</sup>, supporting the absence of bimodal behavior of the interwake region due to turbulence generation by bimodal particle phases.

Taking all the information about the PDFs of  $u$  and  $v$  together, it is concluded that they are adequately described by Gaussian functions as anticipated for turbulence in the final-decay period.

### **Energy Spectra**

The normalized energy spectra of streamwise velocity fluctuations for various binary pairs of dispersed-phase particles are illustrated in Fig. 4. The corresponding integral length scales were found by noting that the normalized amplitude of the energy

spectra,  $2\pi E_u(k)/(\bar{u}'^2 L_u)$ , approaches the value of four (4) as the normalized wave number on these plots,  $kL_u/(2\pi)$ , becomes small as discussed by Hinze.<sup>26</sup> Correlations of energy spectra for approximate isotropic turbulence are also shown on the plot for comparison with the measurements. The approximate spectra represent the simplification of isotropic turbulence discussed by Hinze,<sup>26</sup> where correlations of velocity fluctuations are assumed to satisfy exponential functions. The exponential function spectra yield decay of the spectra in the inertial region of  $-2$  which is reasonably close to the  $-5/3$  power Kolmogorov decay in the inertial region of conventional turbulence at large turbulence Reynolds numbers which is also marked on the plot. Finally, the range of  $kL_u/(2\pi)$  associated with wave numbers characteristic of Kolmogorov scales are also indicated on the plot, in order to provide an indication of the full range of scales associated with present test conditions within the turbulent interwake region, not just the range that could be considered due to the limitations caused by step noise, as well as the conditions where effects of viscosity become important in these flows.

The spectra illustrated for polydisperse particle phases in Fig. 4, along with previous results for monodispersed dispersed phases illustrated in Ref. 7, are independent of particle properties and total dissipation rates and agree reasonably well with the isotropic turbulence approximation of Hinze<sup>26</sup> as well as with the Kolmogorov  $-5/3$  energy decay law for the inertial region. Finally, as noted earlier, the measured spectra are truncated at significantly smaller wave numbers than those associated with Kolmogorov scales in order to avoid step noise caused by sampling limitations. The full range of scales between the integral and Kolmogorov scales is surprisingly large, however, roughly 1000:1, even though the turbulence Reynolds numbers for these conditions were all smaller than 3.5. This behavior highlights some of the unusual properties of turbulence in the final-decay period compared to conventional turbulence. Subsequent consideration of the integral and Taylor dissipation length scales of turbulent interwake regions associated with turbulence generation, however, will show that these large ranges of scales represent reasonable behavior for turbulence in the final-decay period.

It is widely recognized that conventional isotropic turbulence having large turbulence Reynolds numbers should exhibit an extended  $-5/3$  Kolmogorov decay law for the inertial range of the turbulence which involves the wave number range  $kL_u \sim 1$  to  $k\lambda \sim 1$ . An interesting question raised by present results is why should turbulence in the final-decay period having small turbulence Reynolds numbers, as illustrated in Fig. 4, also exhibit a  $-5/3$  Kolmogorov-like inertial

decay region for the extended wave number range  $kL_u \sim 1$  to  $k\lambda \approx k\ell_K \sim 1$  illustrated in Fig. 4. Similar to conventional turbulence at large turbulence Reynolds numbers, this behavior follows from dimensional considerations alone, because there is a large range of scales of turbulence in the final-decay period, whereas effects of viscosity are confined to the high wave number range associated with the Taylor dissipation length scales of the flow (which are very nearly equal to the Kolmogorov length scales for present test conditions). In particular, noting that  $E_u(k)$  has dimensions  $m^3s^{-2}$  whereas  $k$  has dimensions  $m^{-1}$ , the dimensionless energy spectra must have a form normalized by the Kolmogorov length and time scales, as follows:

$$E_u(k)/(\ell_K^3 \tau_K^{-2}) = g(k\ell_K) \quad (14)$$

Introducing the definitions of the Kolmogorov scales,  $\ell_K$  and  $\tau_K$ , from Eqs. (4), Eq. (14) becomes:

$$E_u(k) = v^{5/4} \varepsilon^{1/4} g(kv^{3/4} \varepsilon^{-1/4}) \quad (15)$$

Finally, in order for  $E_u(k)$  to be in the inertial range, where it is independent of  $v$ , it is required that  $g(\zeta) \sim \zeta^{-5/3}$  which implies:

$$E_u(k) \sim \varepsilon^{2/3} k^{-5/3} \quad (16)$$

Thus, dimensional considerations alone require the presence of a  $-5/3$  Kolmogorov-like inertial decay region for turbulence in the final-decay period at small turbulence Reynolds numbers, as seen in Fig. 4, similar to the familiar  $-5/3$  Kolmogorov inertial decay region for conventional turbulence at large turbulence Reynolds numbers. This property of the final-decay period results from the large range of length scales in this flow in spite of its small turbulence Reynolds numbers; this behavior is considered next.

### **Length Scales**

The rate of dissipation of turbulence kinetic energy within conventional isotropic turbulence at large turbulence Reynolds numbers can be estimated from the values of the streamwise velocity fluctuations and integral length scales, using the following expression:<sup>26</sup>

$$A = \varepsilon L_u / (\bar{u}')^3 \quad (17)$$

where  $A$  is the dimensionless integral length scale, which is a constant on the order of unity for conventional isotropic turbulence at large turbulence Reynolds numbers. All properties on the right-hand

side of Eq. (17) were measured during existing studies of the turbulent interwake region, yielding values of  $A$  at various turbulence Reynolds numbers that will be considered next.

The available values of  $A$  for isotropic turbulence are plotted in Fig. 5 as a function of  $Re_\lambda$ . Results for isotropic turbulence in the final-decay period, at  $Re_\lambda$  in the range 0.4-3.5, are plotted on the figure based on measurements of Ref. 7 and the present investigation. Results for isotropic turbulence in the initial-decay period for  $Re_\lambda = 20-800$  are also plotted in the figure, considering measurements,<sup>11-15</sup> direct numerical simulations (DNS),<sup>16-19</sup> and the DNS data fit of Sreenivasan.<sup>20</sup> The results in the initial-decay period for  $Re_\lambda = 20-800$  involve fully-developed turbulence that acts over the entire flow field and yields values of  $A$  on the order of unity, as expected. The measurements for the turbulent interwake region for monodisperse and binary particle phases at small  $Re_\lambda$  are in good agreement with each other but exhibit very enhanced rates of dissipation compared to conventional turbulence having large turbulence Reynolds numbers. This behavior is typical of behavior in the final-decay period where the vorticity is sparse and the turbulence appears to consist of disconnected spots when single-point measurements are observed, see Batchelor and Townsend,<sup>9,10</sup> Ling and Huang,<sup>21</sup> and Phillips.<sup>22</sup> This behavior is also consistent with observations that interwake turbulence for present conditions was in the final-decay period as discussed in connection with Fig. 1.

The measurements illustrated in Fig. 5 suggest that there are three regimes of isotropic turbulence based on the behavior of the dimensionless integral length scale, as follows: (1) the initial-decay period, (2) the final-decay period, and (3) a transition period separating the initial- and final-decay periods. The initial-decay period corresponds to classical isotropic turbulence at large turbulence Reynolds numbers with dimensionless integral length scale properties, as follows:<sup>20</sup>

$$0.3 \leq A \leq 2.0, \text{ Initial-decay period } (Re_\lambda > 100) \quad (18)$$

In this region, the turbulence is fully developed and acts over the entire flow region. Sreenivasan<sup>20</sup> suggests that values of  $A$  vary due to different initial conditions or grid geometries of the flows but the values of  $A$  generally are subsequently independent of the turbulence Reynolds number. The measurements within the turbulent interwake region of Ref. 7 and during the present investigation correspond to the final-decay period of grid-generated turbulence of isotropic turbulence, based on the discussion of Fig.

1, with dimensionless integral length scale properties as follows, as illustrated in Fig. 5:

$$A = 1250 Re_\lambda^{-7/3}, \text{ Final-decay period } (Re_\lambda < 10) \quad (19)$$

where existing measurements of  $A$  in this region are limited to  $Re_\lambda$  of 0.4-3.5, the experimental uncertainty of the power of  $Re_\lambda$  in Eq. (19) is 0.20 and the correlation coefficient of the fit is 0.90. Finally, there is a transition region between the initial- and final-decay periods where Ling and Huang,<sup>21</sup> suggest:

$$A = 33/Re_\lambda, \text{ Transition period } (10 \leq Re_\lambda \leq 100) \quad (20)$$

It also is of interest to consider the range of scales present in each of the three isotropic turbulence periods because this provides a more complete physical picture of the flows. This information can be developed by noting from Eqs. (5) and (17), and the definition of  $Re_\lambda$ , there results:

$$L_w/\lambda = A Re_\lambda / 15 \quad (21)$$

in all the periods of turbulence. As a result, the ratio of  $L_w/\lambda$  in the initial-decay period becomes from Eqs. (18) and (21):

$$L_w/\lambda = A Re_\lambda / 15, \text{ Initial-decay period } (Re_\lambda > 100) \quad (22)$$

The length-scale ratio for the final-decay period becomes from Eqs. (19) and (21):

$$L_w/\lambda = 83 Re_\lambda^{-4/3}, \text{ Final-decay period } (Re_\lambda < 10) \quad (23)$$

Finally, the length scale ratio for the transition period becomes from Eqs. (20) and (21):

$$L_w/\lambda = 2.2, \text{ Transition period } (10 \leq Re_\lambda \leq 100) \quad (24)$$

The correlations of  $L_w/\lambda$  from Eqs. (22)-(24) are illustrated in Fig. 6 along with results from available measurements and DNS. Taken together, the various correlations provide reasonably good fits of available measurements and numerical predictions in the initial-decay, the final-decay and the transition periods. This plot also suggests why there is a transition of the behavior of  $L_w/\lambda$  in going from the initial- to the final-decay periods of isotropic turbulence. For example as  $Re_\lambda$  decreases in the initial-decay period,  $L_w/\lambda$  progressively decreases and approaches unity as  $Re_\lambda$  approaches 100. Clearly, a macro-scale, e.g.,  $L_w$ , cannot become smaller than a micro-scale, e.g.,  $\lambda$ , for a rational turbulent flow; therefore, it is not surprising that there is a transition to the final-decay period, for  $Re_\lambda$  in the range 10-100, which involves  $L_w/\lambda$  properly



remaining larger than unity for additional reductions of  $Re_\lambda$ .

The increasing values of  $L_u/\lambda$  as  $Re_\lambda$  increases is well understood for conventional turbulence at large turbulence Reynolds numbers in the initial-decay period because the relatively large-scale features of the turbulence (on the scale of integral scales) are relatively independent of effects of viscosity, and thus Reynolds numbers, whereas the smallest scales of turbulence, represented by the Taylor dissipation and Kolmogorov length scales, become progressively smaller as  $Re_\lambda$  increases which causes a corresponding increase of  $L_u/\lambda$ . The increase of  $L_u/\lambda$  with decreasing  $Re_\lambda$  in the final-decay period, however, occurs for very different reasons. In this case, regions containing vorticity are sparse but they still spread throughout the entire flow, yielding large integral length scales that progressively increase in size as the flow decays, in the presence of small dissipation scales. Then, the continued spread of the flow, combined with relatively slow changes of the dissipation scales, implies progressively increasing values of  $L_u/\lambda$  as the flow decays (or as  $Re_\lambda$  decreases) as seen in Fig. 6. Thus, the main distinction between the two flows is that  $L_u/\lambda$  increases with increasing  $Re_\lambda$  for conventional turbulence in the initial-decay period because  $\lambda$  becomes smaller but increases with decreasing  $Re_\lambda$  for turbulence in the final-decay period because  $L_u$  becomes larger.

## Conclusions

This investigation has considered the properties of turbulence generated by uniform fluxes of polydisperse particle phases moving through air at standard temperature and pressure, emphasizing the properties of the turbulent interwake region of this flow. Combined with the earlier study of Ref. 7, involving monodisperse particle phases, test conditions include: particle phases consisting of monodisperse and binary mixtures of nearly monodisperse glass beads having diameters of 0.5, 1.1 and 2.2 mm, with corresponding particle Reynolds numbers of 106, 373 and 990; particle volume fractions less than 0.003%; direct rates of dissipation of turbulence by particles less than 4%; and turbulence generation rates sufficient to yield streamwise relative turbulence intensities of 0.2-1.5%. The major conclusions of the study are as follows:

1) The dissipation-weighted mixing rules of Eqs. (10)-(12) provided an effective way to generalize earlier correlations of the properties of the turbulent interwake region for monodisperse particle phases reported in Ref. 7 to various binary mixtures of monodisperse particles during the present investigation.

It is a straightforward matter to extend these relationships to polydisperse particle phases; therefore, this methodology provides a way to estimate the properties of the interwake region of practical dispersed multiphase flows involving polydisperse particle phases.

2) The turbulent interwake region produced by homogeneous flows of polydisperse particle phases was homogeneous and nearly isotropic with PDFs of streamwise and cross-stream velocities well approximated by Gaussian functions and with no property of the interwake region exhibiting a bimodal behavior that reflected the bimodal dispersed phases used to study the present flows.

3) The relative turbulence intensities of the turbulent interwake region could be correlated in the same manner for monodisperse and polydisperse particle phases following the approach of Ref. 7, based on an analogy with the known properties of isotropic grid-generated turbulence, from Batchelor and Townsend.<sup>9,10</sup> This was done by scaling these properties, using mixing rules for binary dispersed phases, with mean particle spacings normalized by the particle wake momentum diameter to yield a normalized dimensionless dissipation factor that is simply related to the streamwise and cross-stream relative turbulence intensities, as given by Eqs. (13).

4) Existing measurements of the turbulent interwake region for monodisperse and polydisperse particle phases, showed that the turbulent interwake region exhibited small turbulence Reynolds numbers,  $Re_\lambda < 3.5$  for present test conditions, and was in the final-decay period of isotropic turbulence as defined by Batchelor and Townsend,<sup>9,10</sup> where vortical regions fill the entire turbulent interwake region but are sparse, i.e., where turbulence appears to involve disconnected turbulent spots when single-point measurements are observed.

5) Within the final-decay period, rates of dissipation are enhanced compared to conventional isotropic turbulence at large turbulence Reynolds numbers having similar values of  $L_u$  and  $\bar{u}'$ , see Fig. 5. In addition, macroscale/microscale ratios (e.g.,  $L_u/\lambda$ ) decrease with increasing turbulence Reynolds numbers in the final-decay period as opposed to increasing which is typical of conventional isotropic turbulence at large turbulence Reynolds numbers. Thus, flows in the final-decay period can exhibit a large range of scales even though their turbulence Reynolds numbers are small. In addition, this behavior implies a large range of scales where effects of viscosity are small, yielding a  $-5/3$  Kolmogorov-like, inertial-decay region of the energy spectra, for the same reasons that inertial-decay regions are observed in conventional turbulence at large turbulence Reynolds numbers.

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**Table 1 Summary of particle properties<sup>a</sup>**

Parameter	Nominal particle diameter (mm) <sup>b</sup>		
	0.5(0.05)	1.1(0.1)	2.2(0.1)
$U_p$ , mm/s	3370(28)	7000(200)	5550(340)
Re	106(9)	373(23)	990(28)
$C_d$	1.22	0.54	0.79
$d \ell n U_p / dx$ , %/m	2	11	14
$\theta$ , mm	0.183	0.299	0.519

<sup>a</sup>Round glass beads (density of 2500 kg/m<sup>3</sup>) falling in upflowing air at normal temperature and pressure (air density of 1.16 kg/m<sup>3</sup> and kinematic viscosity of 15.9 mm<sup>2</sup>/s) having a mean upflow velocity of 1.1 m/s.

<sup>b</sup>Standard deviations of properties given in parenthesis.

**Table 2 Test conditions for binary particle phases<sup>a</sup>**

Parameter	Particle diameters (mm) in binary particle mixtures		
	0.5 & 1.1	0.5 & 2.2	1.1 & 2.2
$n_s''$ , kpart/m <sup>2</sup> s	95-556	95-556	4-32
$n_b''$ , kpart/m <sup>2</sup> s	4-27	0.8-6.4	0.8-6.4
$\ell_p$ , mm	16-29	16-26	49-99
$\varepsilon$ , m <sup>2</sup> /s <sup>3</sup>	0.17-1.10	0.22-1.10	0.085-0.69
$\ell_K$ , mm	0.2-0.4	0.2-0.4	0.3-0.5
$t_K$ , ms	10-30	2-4	5-14
$u_K$ , mm/s	41-64	43-64	34-57
$\bar{u}' / U_p$ , %	0.6-1.4	0.6-1.4	0.2-0.6
$\lambda$ , mm	0.6-0.8	0.7-0.8	0.5-0.7
$Re_\lambda$	0.9-2.3	0.9-2.4	0.4-1.6
$L_u$ , mm	10-109	14-134	50-148

<sup>a</sup>Binary mixtures of round glass beads in upflowing air at normal temperature and pressure with particle and gas properties given in Table 1. Measurements during the present investigation.

**Table 3 Test conditions for monodisperse particle phases<sup>a</sup>**

Parameter	Nominal particle diameter (mm)		
	0.5	1.1	2.2
$n''$ , kpart/m <sup>2</sup> s	71-950	4-56	0.5-10
$\ell_p$ , mm	13-32	41-97	77-208
$\varepsilon$ , m <sup>2</sup> /s <sup>3</sup>	0.088-1.17	0.041-0.54	0.012-2.3
$\ell_K$ , mm	0.2-0.5	0.3-0.6	0.4-0.7
$t_K$ , ms	4-14	5-16	8-37
$u_K$ , mm/s	34-60	31-54	21-44
$\bar{u}' / U_p$ , %	0.5-1.5	0.2-0.6	0.2-0.6
$\lambda$ , mm	0.7-0.9	0.6-0.8	1.2-1.8
$Re_\lambda$	0.7-2.5	0.4-1.5	1.4-3.5
$L_u$ , mm	11-35	42-178	23-156

<sup>a</sup>Monodisperse round glass beads in upflowing air at normal temperature and pressure with particle and air properties given in Table 1. Measurements from Chen and Faeth.

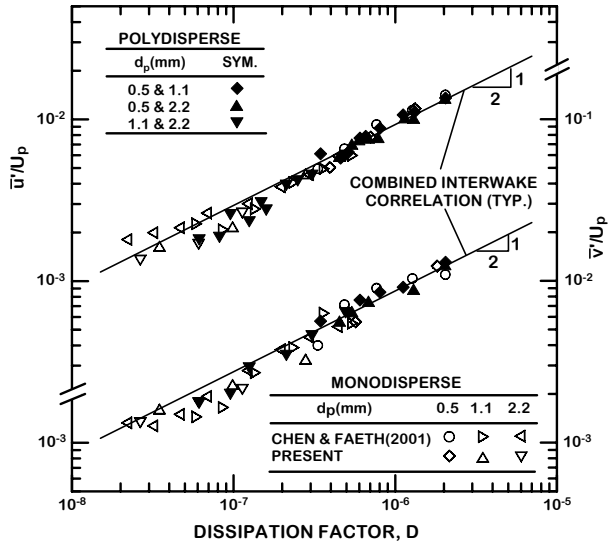


Fig. 1 Streamwise and cross-stream relative turbulence intensities as a function of the dissipation factor for various monodisperse and polydisperse particle phases.

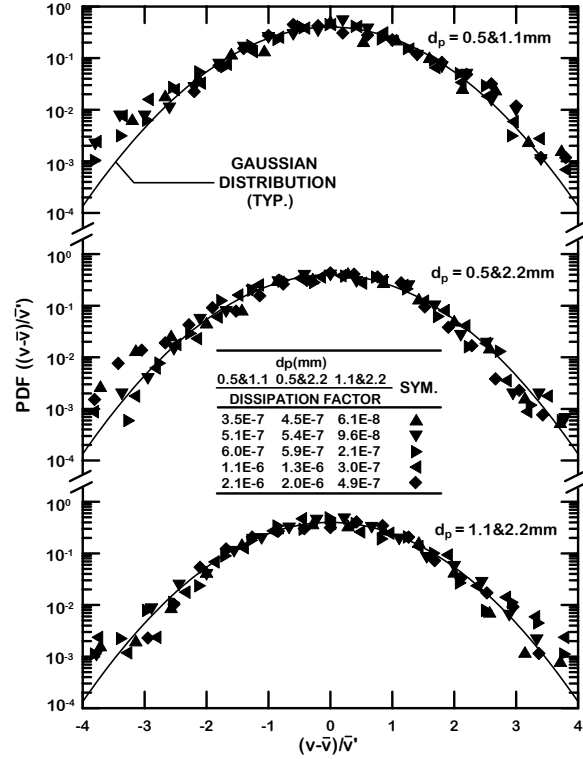


Fig. 3 Typical PDFs of cross-stream velocity fluctuations for various polydisperse particle phases and dissipation factors

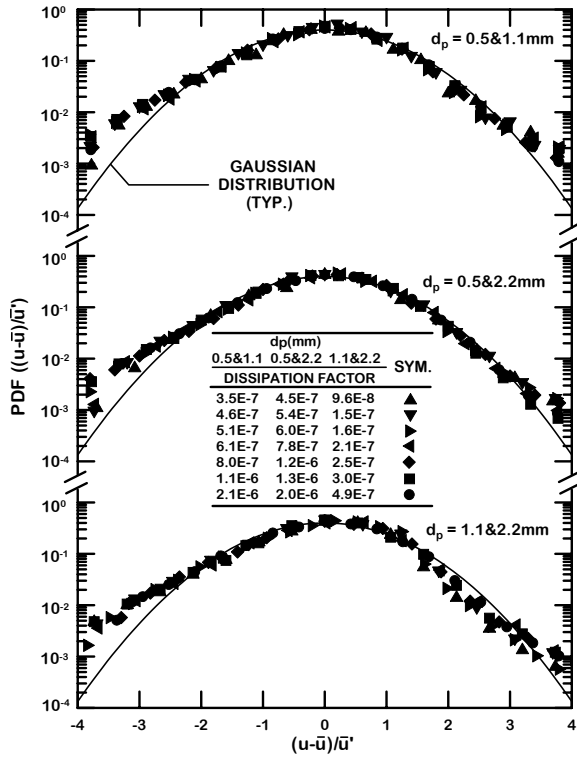


Fig. 2 Typical PDFs of streamwise velocity fluctuations for various polydisperse particle phases and dissipation factors.

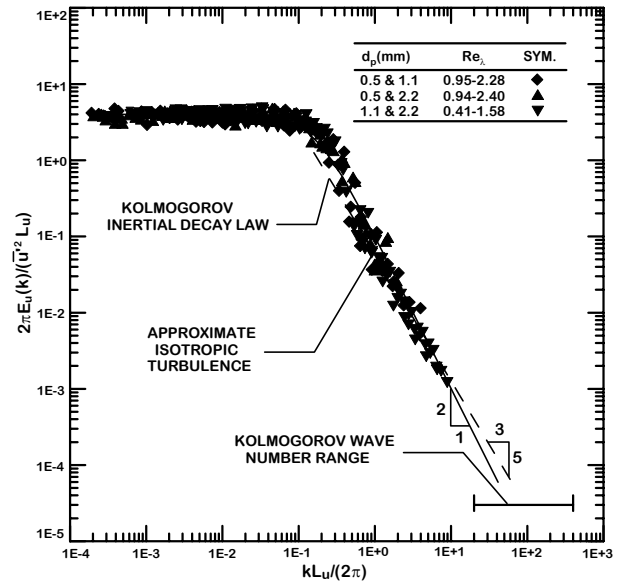


Fig. 4 Typical energy spectra of streamwise velocity fluctuations for various polydisperse particle phases and dissipation factors.

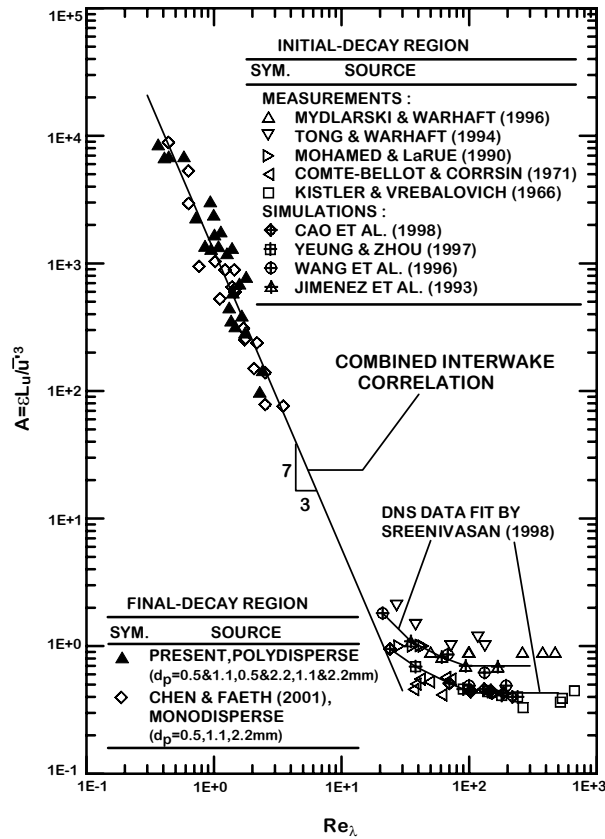


Fig. 5 Normalized integral length scales as a function of turbulence Reynolds number for both grid- and particle-generated turbulence. Grid-generated turbulence measurements of Kistler and Vrebalovich,<sup>11</sup> Compt-Bellot and Corrsin,<sup>12</sup> Mohamed and LaRue,<sup>13</sup> Tong and Warhaft<sup>14</sup> and Mydlarski and Warhaft,<sup>15</sup> particle-generated turbulence measurements of Chen and Faeth<sup>7</sup> and the present investigation; grid-generated turbulence predictions of Jimenez et al.,<sup>16</sup> Wang et al.,<sup>17</sup> Yeung and Zhou,<sup>18</sup> and Cao et al.,<sup>19</sup> grid-generated turbulence DNS fit due to Sreenivasan.<sup>20</sup>

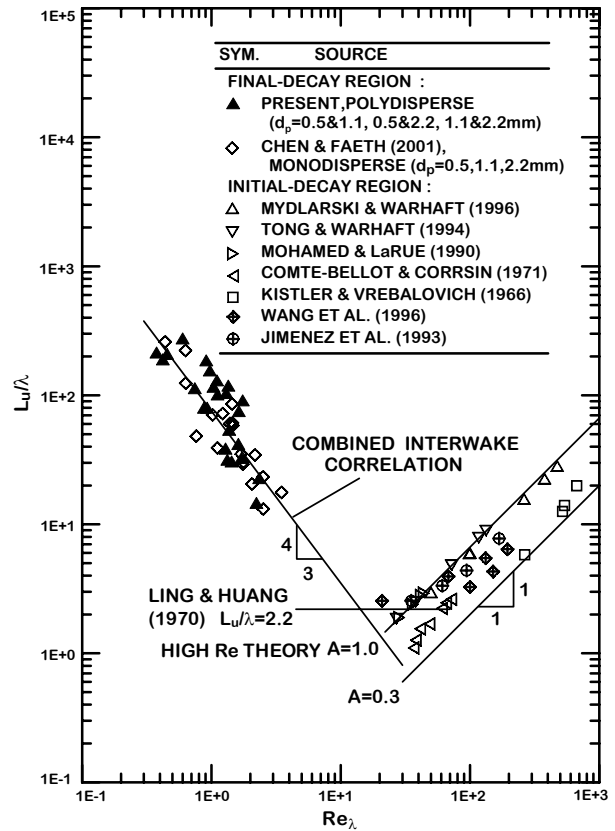


Fig. 6 Ratios of integral and Taylor length scales as a function of turbulence Reynolds number for both grid- and particle-generated turbulence. Grid-generated turbulence measurements of Kistler and Vrebalovich,<sup>11</sup> Compt-Bellot and Corrsin,<sup>12</sup> Mohamed and LaRue,<sup>13</sup> Tong and Warhaft<sup>14</sup> and Mydlarski and Warhaft,<sup>15</sup> particle-generated turbulence measurements of Chen and Faeth<sup>7</sup> and the present investigation; grid-generated turbulence predictions of Jimenez et al.<sup>16</sup> and Wang et al.,<sup>17</sup> grid-generated correlation of Ling and Huang.<sup>21</sup>