AIAA 2000-0433

Coupling Between Fluid Dynamics and Combustion in a Laminar Vortex Ring

Shin-Juh Chen and Werner J.A. Dahm

Laboratory for Turbulence and Combustion (LTC)
Department of Aerospace Engineering
The University of Michigan
Ann Arbor, MI

Grétar Tryggvason

Laboratory for Turbulence and Combustion (LTC)
Department of Mechanical Engineering & Applied Mechanics
The University of Michigan
Ann Arbor, MI

38th Aerospace Sciences Meeting & Exhibit
10-13 January 2000 / Reno, NV

For permission to copy or republish, contact the American Institute of Aeronautics and Astronautics
1801 Alexander Bell Drive, Suite 500, Reston, VA 20191
Coupling Between Fluid Dynamics and Combustion in a Laminar Vortex Ring

Shin-Juh Chen\(^1\) and Werner J.A. Dahm\(^2\)
Laboratory for Turbulence and Combustion (LTC)
Department of Aerospace Engineering
The University of Michigan
Ann Arbor, MI 48109-2140

Crétar Tryggvason\(^3\)
Laboratory for Turbulence and Combustion (LTC)
Department of Mechanical Engineering & Applied Mechanics
The University of Michigan
Ann Arbor, MI 48109-2121

Flame-vortex interactions are critical to the understanding of turbulent reacting flows. The impact of exothermicity on reacting vortex rings is investigated both numerically and experimentally to assess the dominant effect of heat release. Experimental observations of ring trajectories show an initial increase in ring speed in the early stage, followed by a large reduction in speed. It is found numerically that dilatation due to combustion heat release is the dominant effect over enhanced diffusivities in a reacting vortex ring. Increasing fuel volume in the ring beyond a critical limit, obtained from a simple model, actually decreases the amount of heat release during the early stage of the interaction. In addition, the increase in ring circulation led to a decrease in ring speed in the early stage of formation. Nitrogen dilution of the propane fuel reduces the flame luminosity and burnout time, as well as changes in details of the formation and dissipation of the luminous cap, with little change in the primary structure or dynamics of the interaction. The numerical simulations were successful in explaining most of the experimental observations, however, differences in flame structure and ring dynamics attributed to radiative heat loss were inconclusive when radiative heat loss was modeled as an overall decrease in flame temperature.

1. INTRODUCTION

Flame-vortex interactions are considered a central component of turbulent combustion, and it is for this reason that various flame-vortex configurations play a key role in combustion science since the initial study of Marble (1985). Exothermicity due to combustion heat release can dramatically alter some of the most fundamental aspects found in turbulent flows. Studies of such flame-vortex configurations are providing important new insights into elementary transport and reaction processes, since these interactions contain many of the fundamental elements of flow, transport and combustion that are present in turbulent flames. Moreover, these elements can be investigated under more controllable conditions than is possible in direct studies of turbulent reacting flows.

The study of diffusion flame-vortex ring interactions can be conducted experimentally in several ways, as depicted in Fig. 1. Siraw and Cantwell (1985), Vansburger et al (1988), Chen et al (1991), Hsu et al (1993), and Takahashi et al (1996) have studied these interactions by examining vortices generated in pulsed or turbulent jet diffusion flames. In Fig. 1a, some of the fundamental aspects of these interactions are not easily accessible for close study. Recent studies of Rolon et al (1995), and Thévenin et al (1996), and Renard et al (1999) have used the configuration of a counterflow diffusion flame with a vortex ring coming from either the fuel or the oxidizer side as shown in Fig. 1b. In this configuration, the vortex ring is already fully formed as it approaches the diffusion flame, and consists entirely of fuel or oxidizer.

In this paper, the configuration shown in Fig. 1c was used. This configuration has been studied experimentally under microgravity conditions by Chen & Dahm (1997, 1998, 1999a,b), and under normal gravity conditions by Park & Shin (1997) and You et al (1998). The present interaction is similar to that of Karagozian & Manda (1986) and Manda & Karagozian (1988), where the ring consists of fuel and oxidizer, and combustion occurs from the start of the ring formation process. This configuration can provide a strong coupling between the vortex ring and diffusion flame. A diffusion flame initially exists at the oxidizer-fuel interfaces near the nozzle exit plane. Fuel is issued impulsively from the exit of the round nozzle and rolls up with oxidizer and the diffusion flame to form a laminar reacting vortex ring. At the same time, heat release due to combustion affects the vortex ring and the transport properties within it. The interaction proceeds until the fuel in the ring has been consumed.

Here we present experimental results for the reacting vortex ring...
in microgravity that reveal certain aspects of heat release effects, as well as numerical simulations that clarify the dominant mechanisms from which these effects originate. Some of experimental results were presented in Chen & Dahm (1998). The numerical simulations were conducted with the assumptions of unity Lewis and Schmidt numbers, and the Navier-Stokes and mixture fraction equations were solved to reveal the impact of heat release in a vortex ring. The effects of heat release, fuel volume, ring circulation, stoichiometry, and radiative heat loss on the resulting flame structure and dynamics are discussed to shed light on the coupling between flow field and combustion in a reacting laminar vortex ring.

2. METHODS

In this study, experiments were conducted under microgravity conditions at the NASA 2.2 seconds drop tower facility. As shown in Fig. 2, all hardware must be contained inside a drop frame with dimensions of 40.6 cm x 96.5 cm x 83.8 cm and weight not exceeding 158 kg. Numerical simulations were also conducted to explain some of the experimentally observed phenomena and to assess the dominant effects of combustion heat release in a reacting vortex ring.

2.1 Microgravity experiments

The apparatus of the current study was used in the previous studies of Chen & Dahm (1997, 1998, 1999a,b) and is shown in Fig. 2. The top shelf of the drop package contains the 20 cm x 20 cm x 25 cm test section made of clear Lucite, a 640 x 480 CCD array which records the resulting luminosity of a reacting vortex ring with all frames shown in inverse grayscale in this paper, and a spark igniter box for the generation of a diffusion flame. An axisymmetric circular nozzle and plenum are attached below the top shelf for the generation of vortex rings. The bottom shelf houses the controlling electronics, on-board computer, batteries, pressurized fuel tank, a vacuum tank, flowmetering valves, a fast acting solenoid valve, and the necessary fittings and tubings.

A vortex ring is generated by impulsively issuing fuel through the circular nozzle of diameter \( D = 2 \) cm into an air environment which is held at atmospheric conditions inside the test section. A schematic of the apparatus is shown in Chen & Dahm (1998). The experiment is conducted as follows. Initially, there is a closed iris that separates the fuel and air interfaces as shown in Fig. 3. The iris opens prior to the drop and exposes the fuel and oxidizer interfaces.
Figure 4. Symmetric and repeatable interactions are accessible under microgravity conditions. Circulations in (b) and (c) are respectively six times and eleven times that of (a).

The experimental study spans a wide range of hydrodynamic and chemical parameters. For a given nozzle diameter (2-cm in this study), there is a finite amount of fuel that can be injected into the vortex ring before reaching the overfilled limit. This limit corresponds to length-to-diameter ratio of 3.6-4.4 (Charib et al 1998) which is based on the equivalent cylindrical volume of fluid emanating from the nozzle, and corresponds to limiting fuel volume of 23-28 cm³. Even though the results from Charib et al (1998) were for nonreacting vortex rings, the agreement with the current experiment is quite good (Chen & Dahm, 1999a,b). This study will focus only on non overfilled cases.

Under microgravity conditions where buoyancy is effectively eliminated, very repeatable and symmetric results can be obtained. Figure 4 shows results from three different cases taken from six separate drops, and the images are time-matched as closely as allowable. It is evident in these figures that highly symmetric and repeatable flame-vortex interactions are achievable.
Figures 5 and 6 suggest that exothermicity due to combustion heat release has a pronounced impact on both the structure and dynamics of reacting vortex rings. The impact on the ring dynamics is clearly seen in Figs. 7 and 8 showing the time history of non-dimensional flame heights for several cases. Moreover, Fig. 7 suggests that fuel volume may also play a role on the resulting ring dynamics. In order to discern the dominant effect of combustion heat release, numerical simulations were conducted; this allow numerical studies that are not accessible in experimental settings to be conducted and provide access to a wider range of parameters to be investigated than is permissible in experiments, but requires some modeling of certain physical processes.

3.1 Effect of Heat Release

Typical flame heights obtained from experiments are shown in Figs. 7 and 8 with the ring height and time hydrodynamically scaled as $H^* = H/D$, and $t^* = tT/D^2$, where $H$ is the visible flame heights for several different fuels, circulations, and fuel volumes. In the case of nonreacting vortex rings, if the core structure are similar, then one would expect the ring trajectories to collapse to a single curve when plotted in these hydrodynamically scaled variables, however, they do not for the trajectories of reacting vortex rings. This suggests that heat release appears to have an impact on the reacting ring trajectories. For an inviscid ring the resulting constant speed would produce a straight trajectory having a slope that depends weakly on the vortex core size and internal structure. As for a viscous ring, viscous diffusion increases the core size with time and progressively reduces the ring speed similar to the trend seen in Figs. 7 and 8. However, no reasonable core size for a constant viscosity ranging from cold to hot gas values will replicate the experimental observations. Even spatial and temporal variations in viscosity are insufficient to explain the trend in these trajectories. This strongly suggests that a heat release effect other than the simple increase in viscosity appears to dominate the reacting vortex ring trajectories.

Numerical simulations were conducted for methane-air reaction to examine the origins of these effects. Methane is considered
here in order to remove the effect of radiative heat loss due to the presence of soot; this subject is discussed below. The relative importance of heat release effects on diffusion and dilatation due to reaction and heat conduction in the fluid are compared in Fig. 9. The mixture fraction fields indicate that there are differences between the nonreacting ring and the reacting ring with dilatation turned off. These differences are mainly enhanced molecular diffusion which is responsible for the more diffused scalar field, and the decrease in ring speed in the later stage of interaction due to enhanced viscous diffusion in the reacting case with dilatation turned off. However, the largest differences are seen when comparing to the reacting case with dilatation turned on, where there is a large reduction in ring speed, and the scalar field has considerably spread radially apart. These sharp differences are therefore attributable to volumetric expansion due to combustion heat release.

By examining the trajectories of these three cases, Fig. 10 clearly shows that dilatation is the dominant effect over enhanced diffusivities when combustion heat release is present in methane-air reaction. There are no differences in the trajectories of nonreacting case and reacting case with dilatation turned off during the early stage of interaction, that is for \( t^* < 8 \). Dilatation is responsible for the increase in ring speed in the early stage, and the sharp reduction in ring speed in the later stage for the reacting case with dilatation turned on. This is consistent with the experimentally observed reduction in ring speed over time in Figs. 7 and 8, and with the numerical results in Fig. 17b of Hewett & Madnia (1998) from their Runs 1 and 5. While their simulations are of a somewhat different problem, comparing their Runs 3 and 5 in their Fig. 12c further supports the present observation that dilatation is the dominant effect of heat release in a reacting vortex ring.
Figure 9. Simulation results showing mixture fraction fields for $V_e = 10.5$ cc and $\Gamma = 100$ cm$^2$/s for (a) nonreacting ring, (b) reacting ring without dilatation, and (c) reacting ring with dilatation.
Besides the reduction in ring speed with time for any given case in Fig. 8, there are differences in the trajectories that are not accounted for by the hydrodynamic scaling $H^*(t^*)$ alone. The effect of fuel volume can also have an impact on both the structure and dynamics of reacting vortex rings. This effect is also found to be associated with dilatation and is explained next.

### 3.2 Effect of Fuel Volume

The structural and dynamical change in a reacting vortex ring due to fuel volume changes is seen in Fig. 5. In these experiments (Figs. 5a-c), the ring circulation is essentially kept constant, and by just varying the fuel volume the flame structure and dynamics are affected considerably. In Fig. 5a, a distinctive vortex ring shape is observed only in the early time. The later stage is more suggestive of a diffusion-limited burnout of the rich section on the centerline of the vortex ring. The increase of fuel volume in Figs. 5b and 5c leads to the formation of a luminous bubble, and a ringlike structure can be seen in the burnout stage of Fig. 5c. During the early stage of Figs. 5b and 5c, there are no major differences in the ring speed, however in the later stage, a large difference in ring speed can be observed because of a larger fuel volume in Fig. 5c.

An increase in fuel volume beyond the overfilled limit as mentioned above can lead to the formation of overfilled vortex rings, which displays azimuthal instability and formation of secondary and tertiary rings as seen in Fig. 5d. For the case of non-overfilled rings, the volume of fluid that rolled up during the ring formation from the 2 cm diameter nozzle is approximately 50 cm$^3$.

From the experimental results of methane-air reaction shown in Fig. 8, it is evident that fuel volume also plays an important role in the ring dynamics. With the ring circulation and all other parameters essentially identical except for the fuel volume, one would expect the trajectories to look similar, yet there is a clear trend with fuel volume that suggests a further heat release effect.

The combustion in a reacting vortex ring can be approximated as two phases. This has been suggested by experimental studies of Southerland et al (1991). The first is where the fuel and oxidizer, which initially roll up together during the ring formation phase, burn rapidly to consume the lean reactant. The second phase is where any remaining fuel is consumed by the diffusion of the required oxidizer into the ring. An increase in fuel volume during the initial phase will decrease the amount of oxidizer that rolled up into the vortex ring. Depending on the stoichiometric requirements, there is a critical ratio of $V_f/V_o$ for which the oxidizer becomes the lean reactant. Beyond such limit, an increase in fuel volume will lead to less heat been released, which in turn, will lead to a decrease in ring speed in the early stage. For methane-air reaction the amount of fuel beyond which the oxidizer becomes the lean reactant is when $V_f = 5$ cm$^3$. This is based on the 50 cm$^3$ of fluid that is rolled up during the ring formation for a 2-cm diameter nozzle. This effect is clearly demonstrated in the experimental results of methane-air combustion in Fig. 8 where all cases exceed the stated critical fuel volume.

A numerical simulation was also conducted to address the effect of fuel volume on the reacting ring dynamics. Figure 11 shows the effect of fuel volume on the ring trajectories of methane-air reactions for fuel volumes ranging from 5 to 21 cc. Consistent with the experimental results of Fig. 8, the numerical results do show that increasing fuel volume beyond the critical limit will lead to a reduction in ring speed in the early stage. On the other hand, in the later stage the increase in fuel volume contributed to an increase in ring height, and this is expected since there is more fuel to be consumed in the larger fuel volume case.

### 3.3 Effect of Ring Circulation

In a nonreacting vortex ring, an increase in ring circulation leads to an increase in ring speed, but when plotted in hydrodynamically scaled variables all the trajectories should collapse to a single curve, assuming similar core structures, since the ring circulation merely scales the characteristic time. While the scaled trajectories will be independent of circulation, an increase in ring circulation can also increase mixedness of fuel.
and oxidizer inside a vortex ring (Verzicco & Aguirre, 1995), and result in the thinning of the diffusion layer on the forward stagnation point of the vortex ring due to an increase in strain rate. However, as noted above, in a reacting vortex ring dilatation due to combustion heat release affects the ring trajectory. With the increase in mixedness, one should expect to have increased dilatation for larger ring circulations.

A numerical study was conducted to determine the effect of ring circulation on the reacting vortex rings. Figure 12 shows the numerical results of three ring circulation cases with time and height hydrodynamically scaled, and to a first order approximation, the trajectories do collapse to a single curve. However, the small differences in ring speed seen in $t^* < 20$ indicate that an increase in ring circulation contributes to a decrease in ring speed. This is unexpected since more mixedness from an increase in ring circulation should increase dilatation. For a fixed fuel volume, the increase in ring circulation is achieved by reducing the total fuel injection time. The higher rate of fuel injection in the higher ring circulation case is similar to the effect of fuel volume as discussed above where higher fuel volume leads to a reduction in dilatation. For a fixed fuel volume, the increase in ring circulation is achieved by reducing the total fuel injection time. The higher rate of fuel injection in the higher ring circulation case is similar to the effect of fuel volume as discussed above where higher fuel volume leads to a reduction in dilatation. As figure 12 indicates, the lower ring circulation does show the result of higher dilatation as compared to the higher circulation cases, during the early phase of the interaction. A numerical study was also conducted to determine whether fuel volume plays a role. It was found that even for fuel volumes below the critical value (5 cc), the same trend was seen and this further suggests that the rate of fuel injection plays a role.

From these numerical studies, it is found that enhanced mixedness due to an increase in ring circulation as observed in nonreacting vortex rings contributes to an increase in dilatation for the reacting vortex rings. Moreover, the small differences seen in Fig. 12 are attributable to the change in the rate of fuel injection resulting from a change in ring circulation.

### 3.4 Effect of Stoichiometry

The comparison of Figs. 5c and 6 allows the effect of stoichiometry on the reacting vortex rings to be examined by varying the nitrogen dilution of the fuel. In the three cases, the ring circulation and fuel volume are kept essentially constant. Nitrogen dilution of the fuel has the effect of moving the stoichiometric surface closer to the fuel side with little change in adiabatic flame temperature. For a given strained laminar flame with thickness $\lambda_D$ the separation between the stoichiometric surface and the nominal air-fuel interface is given by $n_s / \lambda_D = \text{erf}^{-1}(1 - \phi)/(1 + \phi)$.

The flame structure in all three cases looked somewhat similar, and this is consistent with the results in Fig. 12 of Manda and Karagozian (1988) for their range of $f^*$ between 0.1 and 0.35. The dominant effects of nitrogen dilution of the fuel appear to be a reduction in flame luminosity and flame burnout time. Figure 4c of the pure propane case shows a luminous region that envelops the whole ring and burns out from both the leading and trailing ends. In the case of 60% nitrogen with 40% propane in Fig. 6a, a bright luminous cap is present only very near the leading edge of the flame and dissipates toward the leading edge. As for the case of 20% propane with 80% nitrogen in Fig 6b, no bright luminous cap is formed, however, the brightest region is still located at the leading edge. The reduction in flame burnout time as nitrogen dilution increases is most likely connected to less soot been available for the soot burnout phase which cannot be differentiated from the recorded luminosity.

### 3.5 Effect of Radiative Heat Loss

Numerical results of Fig. 13 and the experimental results of Figs. 14 and 15 were used to determine the effect of radiative heat loss on reacting vortex rings. Comparison of Figs. 14 and 15 suggests marked differences in both the burnout time and flame structure even though both cases have similar ring circulation and fuel volume, except the fuel type. One explanation is the increased in radiative heat loss in Fig. 15 due to the higher sooting propensity of propane which may be responsible for the difference in flame shapes. The formation of the luminous cap proceeds in a similar way, but the cap dissipates in a very differently in the late stage of interaction.
Since dilatation is the dominant heat release effect in this configuration, numerical results of Fig. 13 determine whether the difference in flame shapes in Figs. 14 and 15 may be due to reduced dilatation from a difference in the radiative heat loss. In the numerical study, radiative heat loss is simply modeled as a reduction in $T_{\text{max}}$, however, Fig. 13 shows that for a reasonable reduction in $T_{\text{max}}$, the effect on the ring trajectory is minimal. This suggests that while dilatation suffices to explain most of the heat release effects discussed here, other mechanisms may be responsible for the differences seen in Figs. 14 and 15.

4. CONCLUSIONS

Flame-vortex interactions provide a mean for studying many of the fundamental aspects on the coupling between flow and reaction found in turbulent reacting flows. The combined efforts of experimental and numerical studies have demonstrated that dilatation is the dominant effect of combustion heat release; this is also consistent with the numerical simulations of Hewett & Madnia (1998) of a somewhat different configuration.

Fuel volumes play a role in determining the amount of heat release during the initial stage, and it was found that increasing fuel volume beyond a critical limit as determined by stoichiometric requirements, while keeping the circulation constant, can result in a reduction in heat release which in turn leads to a decrease in ring speed. Experimental results of pure propane fuel showed a clear effect of the fuel volume on the flame structure and burnout time for rings that do not exceed the overfilled limit.

The increase in ring circulation with fuel volume kept constant gives a reduction in ring speed during the early stage of
interaction. Results from nonreacting vortex rings hinted to an increase in dilatation from an enhanced mixedness due to enhanced circulation. However, the numerical results for reacting vortex rings showed that enhanced mixedness has a minimal effect on dilatation for the range of ring circulation studied here.

The effect of nitrogen dilution of propane cases was a major reduction in flame luminosity and burnout time. However, the flame shape was not considerably affected by the nitrogen dilution, and this was in agreement with the analytical results of Karagozian & Manda (1986) and Manda & Karagozian (1988) for their vortex pair case. The reduction in burnout time is most likely due to the presence of less soot as nitrogen dilution is increased.

Experimental results revealed that radiative heat loss can affect the flame structure and dynamics in a reacting vortex ring. Numerical studies that mimic radiative heat loss by lowering the adiabatic flame temperature did not reproduce the differences seen between the experimental results of propane and ethane cases. This suggests that a mechanism other than the simple reduction in dilatation due to radiative heat loss is responsible for the marked differences.

Acknowledgements

This work is supported by the NASA Microgravity Combustion Science Program under Contract Nos. NASA-G-NCC3-663 and NASA-G-NAG3-1639.

References


