# THE UNIVERSITY OF MICHIGAN RESEARCH INSTITUTE ANN ARBOR

TWO INTERFEROMETER-TYPE DIRECTION-FINDING SYSTEMS

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#### ABSTRACT

The analyses of two types of radio direction-finder are presented. These systems were investigated primarily with the VHF frequency range in mind. The analysis of the systems is presented for the purpose of indicating one way of instrumenting an interferometer system and to indicate a way of eliminating the ambiguities involved. Some discussion is given on the limitations of such systems. As with most direction finders in this frequency range and lower, the limitation on accuracy is a function of the environment and not solely dependent upon the instrumental accuracy of the equipment.

#### 1. INTRODUCTION

This report will describe two proposed radio direction-finding systems based on the interferometer principle. From a theoretical standpoint the systems show certain advantages over other types of systems. However, it must be kept in mind that in a practical environment these advantages may not be realized because of the nature of operation of the systems. Both systems suffer in that they take samples of the wave front at only a few widely separated points and thus do not average over the wave front as would be desired.

#### 2. THE "OAK-LEAF" DIRECTION FINDER

#### 2.1 Principle of Operation

The first of the two systems investigated is called the "Oak-Leaf" DF because of the characteristic pattern produced by its antenna system.

The system utilizes five antennas, as shown in Fig. 1.

Antennas 1 and 2 form a wide-spaced pair in terms of the wave length,  $\lambda$ . If the phase of the signal at antenna 2 is continually advanced with respect to that at antenna 1, a multilobed interference pattern is produced. A similar process obtains from the antenna pair 1 and 3 except that, since the spacing is slightly different, the resultant pattern will be rotated slightly in space, although similar in shape.

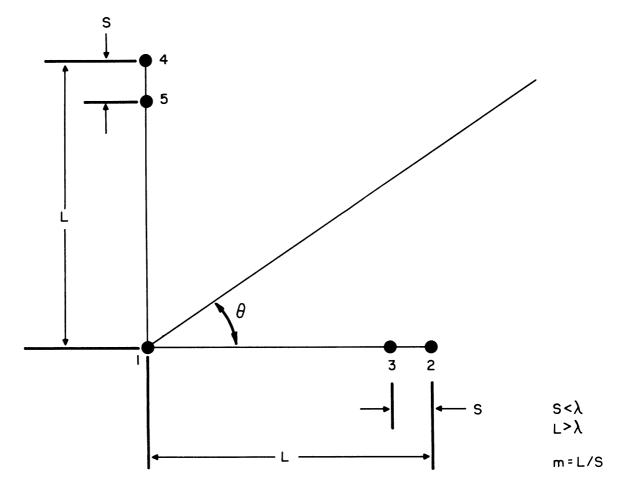


FIG.I "OAK-LEAF" DF ANTENNA POSITIONING

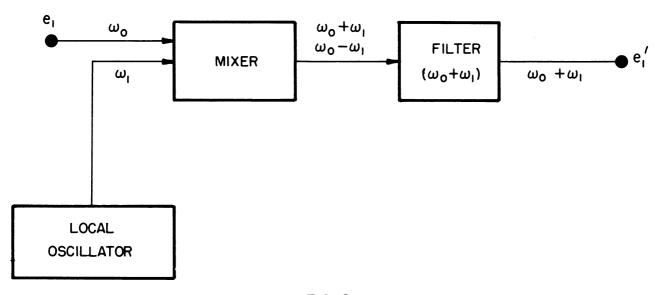


FIG. 2

Each pattern alone contains information as to the bearing of the transmitter but with ambiguities as represented by the multiplicity of lobes in the multilobed pattern. These ambiguities are resolved by a continuous rotation of one pattern with respect to the other so as to produce one major lobe which will indicate the direction of the target.

There remains, however, the reciprocal bearing ambiguity, which is resolved by using another antenna array, composed of antennas 1, 4, and 5, at right angles to the first.

#### 2.2 System Analysis

The initial analysis concerns the antenna system comprised of antennas 1, 2, and 3; it is subsequently applied to the system of 1, 4, and 5.

Establish antenna 1 as the reference antenna and let the voltage at this antenna be represented by:

$$e_1 = A \cos \omega_0 t$$
,

where A involves system parameters involved with antenna 1.

Similarly,

$$e_3 = B \cos (\omega_0 t + \alpha)$$
, and

$$e_2 = C \cos (\omega_0 t + \beta)$$
,

where B and C represent system parameters peculiar to antennas 3 and 2, respectively, and

$$\alpha = \frac{2\pi}{\lambda_0}$$
 (L-S) cos  $\theta$  , and

$$\beta = \frac{2\pi}{\lambda_0} (L) \cos \theta .$$

Now, with reference to Fig. 2, if a locally generated signal at a frequency of  $\omega_1/2\pi$  is mixed with  $e_1$ , the following is obtained:

$$e_{\omega_{o}} \times e_{\omega_{1}} = A \cos \omega_{o} t \times D \cos \omega_{1} t$$

$$= \frac{AD}{2} \cos (\omega_{o} + \omega_{1}) t + \cos (\omega_{o} - \omega_{1}) t,$$

where  $e_{\omega_1} = D \cos \omega_1 t$  is the oscillator voltage.

After filtering to retain only the  $\omega_{0}$  +  $\omega_{1}$  term one obtains

$$e'_1 = \frac{AD}{2}\cos(\omega_0 + \omega_1)t$$
.

Now, with reference to Fig. 3, a similar process is gone through, this time with  $e_1^{\,\prime}$  and  $e_2^{\,\prime}$ .

$$e_{1}^{t} \times e_{2} = \left[\frac{AD}{2}\cos(\omega_{0} + \omega_{1})t\right] \left[B\cos(\omega_{0}t + \alpha)\right]$$

$$= \frac{ADB}{4} \left[\cos(2\omega_{0}t + \omega_{1}t + \alpha) + \cos(\alpha - \omega_{1}t)\right]$$

After filtering to retain only the  $\boldsymbol{\omega}_{l}$  term one obtains

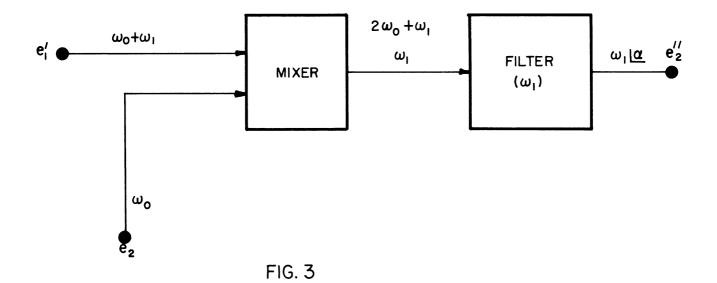
$$e_2'' = \frac{ADB}{4} \cos (\alpha - \omega_1 t)$$
.

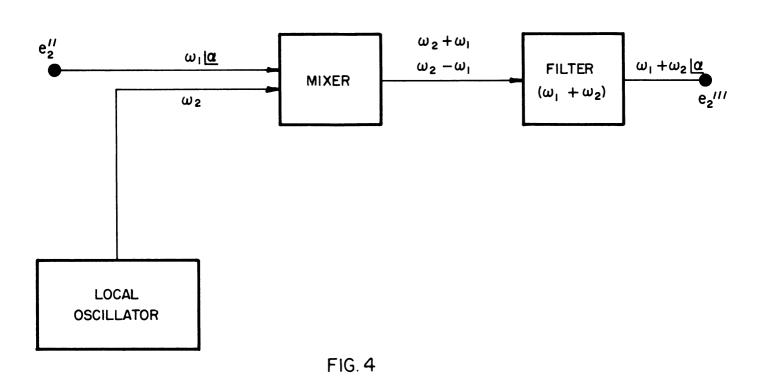
Going through a similar process for  $e_3$ , one obtains

$$e_3'' = \frac{ADC}{4} \cos (\beta - \omega_1 t)$$
.

Now introduce another locally generated signal given by

$$e_{\omega_2} = E \cos \omega_2 t$$
.





With reference to Fig. 4 it can be seen that one obtains

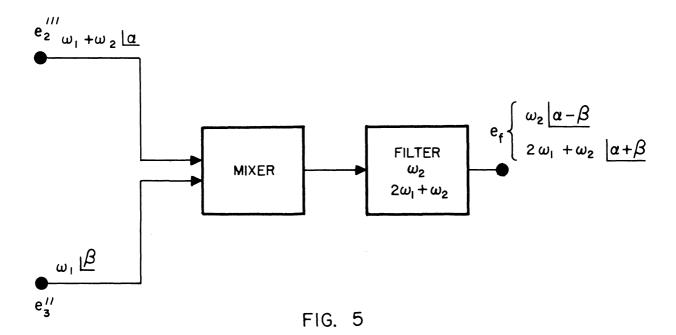
$$\begin{split} \mathbf{e}_{2}^{"} & \times \mathbf{e}_{\omega_{2}} &= \frac{\mathrm{ADB}}{4} \cos \left(\alpha - \omega_{1} \mathbf{t}\right) \times \mathrm{E} \cos \left(\omega_{2} \mathbf{t}\right) \\ &= \frac{\mathrm{ADBE}}{8} \left[ \cos \left(\alpha + \omega_{2} \mathbf{t} - \omega_{1} \mathbf{t}\right) + \cos \left(\alpha - \omega_{1} \mathbf{t} - \omega_{2} \mathbf{t}\right) \right] . \end{split}$$

After filtering to retain only the  $\omega_2$  +  $\omega_1$  term one obtains

$$e_2^{\prime\prime\prime} = \frac{ADBE}{8} \cos (\alpha - \omega_1 t - \omega_2 t)$$
.

Now after the processing shown in Fig. 5, we find

$$e_2^{\prime\prime\prime} \times e_3^{\prime\prime} = \frac{ABDE}{8} \cos \left[\alpha - (\omega_1 + \omega_2)t\right] \times \frac{ADC}{4} \cos (\beta - \omega_1 t)$$
.



$$\mathbf{e}_{\mathbf{f}} = \frac{\mathbf{A}^2 \mathbf{D}^2 \mathbf{BCE}}{64} \left[ \cos \left( \alpha + \beta - 2 \mathbf{w}_1 \mathbf{t} - \mathbf{w}_2 \mathbf{t} \right) + \cos \left( \alpha - \beta + \mathbf{w}_2 \mathbf{t} \right) \right] .$$

By definition, m = L/S.

Now, since 
$$\alpha = \frac{2\pi}{\lambda_0}$$
 (L-S)  $\cos \theta$ , and

$$\beta = \frac{2\pi}{\lambda_0}$$
 (L) cos  $\theta$ , we find that

$$\alpha + \beta = (2L-S) \frac{2\pi}{\lambda_0} \cos \theta = (2Sm-S) \frac{2\pi}{\lambda_0} \cos \theta = (2m-1) \frac{2\pi S}{\lambda_0} \cos \theta , \text{ and}$$

$$\alpha - \beta = -\frac{2\pi S}{\lambda_0} \cos \theta .$$

Now choose  $\omega_1$  and  $\omega_2$  such that  $\frac{\omega_1}{\omega_2} = m - 1$ .

$$\omega_1 = (m-1) \omega_2$$
,

so: 
$$2\omega_1 + \omega_2 = 2m\omega_2 - 2\omega_2 + \omega_2 = 2m\omega_2 - \omega_2 = \omega_2(2m-1)$$
.

Substituting all of this into the expression for  $\mathbf{e}_{\mathbf{f}}$  one obtains:

$$e_{f} = \frac{A^{2}D^{2}BCE}{64} \left\{ \cos \left[ (2m-1) \left( \frac{2\pi S}{\lambda_{o}} \right) \cos \theta - (2m-1) \omega_{2} t \right] + \cos \left[ \omega_{2} t - \frac{2\pi S}{\lambda_{o}} \cos \theta \right] \right\}, \text{ or }$$

$$\mathbf{e}_{\mathbf{f}} = \frac{\mathbf{A}^2 \mathbf{D}^2 \mathbf{BCE}}{64} \left\{ \cos \left[ (2\mathbf{m} - 1)(\omega_2 \mathbf{t} - \frac{2\pi \mathbf{S}}{\lambda_0} \cos \theta) \right] + \cos (\omega_2 \mathbf{t} - \frac{2\pi \mathbf{S}}{\lambda_0} \cos \theta) \right\}.$$

Normalize  $e_f$  to prevent the resultant expression from ever becoming negative and call this  $F(\theta)$ :

$$F(\theta) = 2 + \cos \left[\omega_2 t - \frac{2 S}{\lambda_0} \cos \theta\right] + \cos \left[(2m-1)(\omega_2 t - \frac{2\pi S}{\lambda_0} \cos \theta)\right].$$

Let  $\gamma = \frac{\omega_2}{2\pi}$ . Now if  $F(\theta)$  is applied on a circular sweep of an oscilloscope being swept at a rate of  $\gamma = \frac{\omega_2}{2\pi}$  revolutions per second one obtains a pattern given by:

$$F(\theta) = 2 + \cos \left(\gamma - \frac{2\pi S}{\lambda_0} \cos \theta\right) + \cos \left[(2m-1)(\gamma - \frac{2\pi S}{\lambda_0} \cos \theta)\right].$$

Figure 6 illustrates the particular case wherein  $\theta = 90^{\circ}$ , but the same pattern will appear for any value of  $\theta$  except for a rotation around the origin.

Now,  $F(\theta)$  will have an absolute maximum when

$$\frac{2\pi S}{\lambda_{O}}\cos \theta = \gamma.$$

From this one obtains  $\cos \theta$  as:

$$\cos \theta = \gamma_{EW} \left( \frac{\lambda_0}{2\pi S} \right)$$
.

Since  $S < \frac{\lambda_0}{2}$  the only ambiguity involved in determining  $\theta$  will be in determining the correct algebraic sign to use. This is resolved by antennas 1, 4, and 5.

Going through the same signal processing as before, using antennas 1, 4, and 5 one obtains another value for  $\gamma$ , to be called  $\gamma_{\rm NS}$ , from which one obtains sin  $\Theta$  by the relation:

$$\sin \theta = \gamma_{NS} \left( \frac{\lambda_0}{2\pi S} \right)$$
.

Having obtained  $\gamma_{\rm NS}$  and  $\gamma_{\rm EW}$ , one can now determine the angle of arrival,  $\theta$ , by constructing the triangle as shown in Fig. 7.

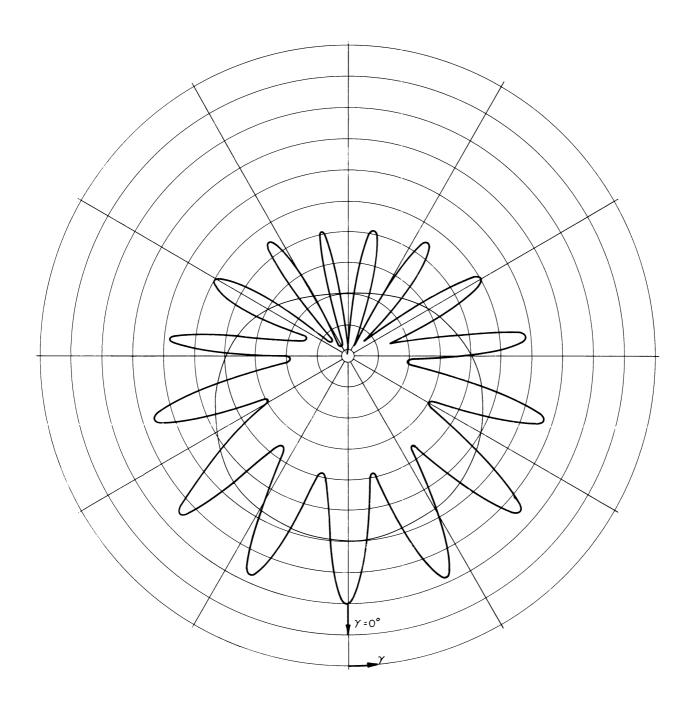


FIG.6 "OAK-LEAF"D F

 $F(\theta) = 2 + \cos \gamma + \cos(15\gamma)$ L/d = m = 8  $\theta = 90^{\circ}$ 

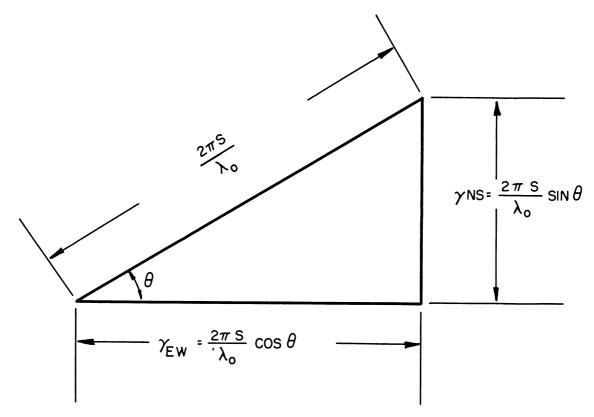


FIG.7 DETERMINATION OF  $\theta$ 

Note that the value of  $\gamma$  is independent of all the arbitrary amplitude constants, A, B, C, etc., so that the system will be relatively immune to amplitude unbalances.

Figure 8 shows a complete block diagram for the "Oak Leaf" DF.

## 3. THE "SPHERICAL WAVE-FRONT" SYSTEM

#### 3.1 Principle of Operation

The "Spherical Wave-Front" system samples the incoming wave front at five points, one point serving as a reference point for the rest of the phases. Under ideal circumstances the wave propagating from a point source expands spherically, so that, by determining the shape of the wave front, one can determine not only the bearing of the target but also the range, thus determining the location or fix of the target.

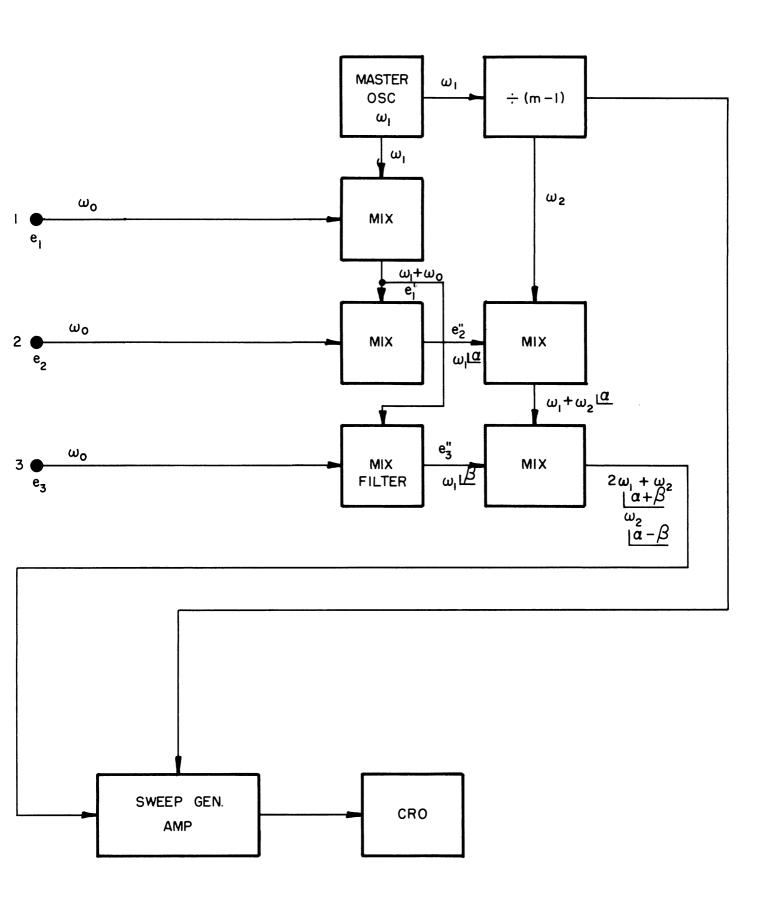


FIG.8 BLOCK DIAGRAM FOR "OAK-LEAF" DF

The determination of the shape of the wave front is done by comparing the relative phases of the incoming signal at each of the sampling points. Using these relative phases and certain approximations, one being that the array length, L, be much less than the distance to the transmitter, a fairly compact expression relating the bearing and range of the transmitter to the relative phases at each of the sampling points can be obtained.

In the proposed system, the signals from the sampling points are processed in such a way as to give a direct indication of the bearing and range.

#### 3.2 System Analysis

First consider the signal processing necessary for the operation of the system and then briefly the circuits to perform these operations. The antenna positioning is as shown in Fig. 9. The target transmitter is at point P.

Now consider only antennas 0 and E as shown in Fig. 10. One finds that if L  $<\!<\!R\!:$ 

$$\alpha_{EO} = R - R_{PE} = \frac{L}{2} \cos \theta - \frac{L^2}{8R} \sin^2 \theta - \frac{L^3}{16R^2} \cos \theta \sin^2 \theta$$
$$- \frac{L^4}{128R^3} (6 \cos^2 \theta - 1) + \dots \qquad .$$

Similarly:

$$\alpha_{WO} = R - R_{PW} = -\frac{L}{2}\cos\theta - \frac{L^2}{8R}\sin^2\theta + \frac{\pi L^3}{16R^3}\cos\theta\sin^2\theta - \frac{\pi L^4}{128R^3}(6\cos^2\theta - 1) + \dots$$

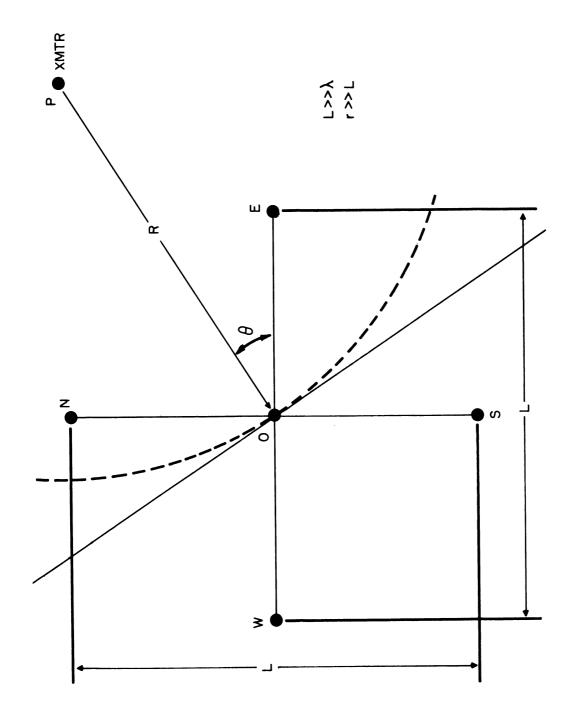
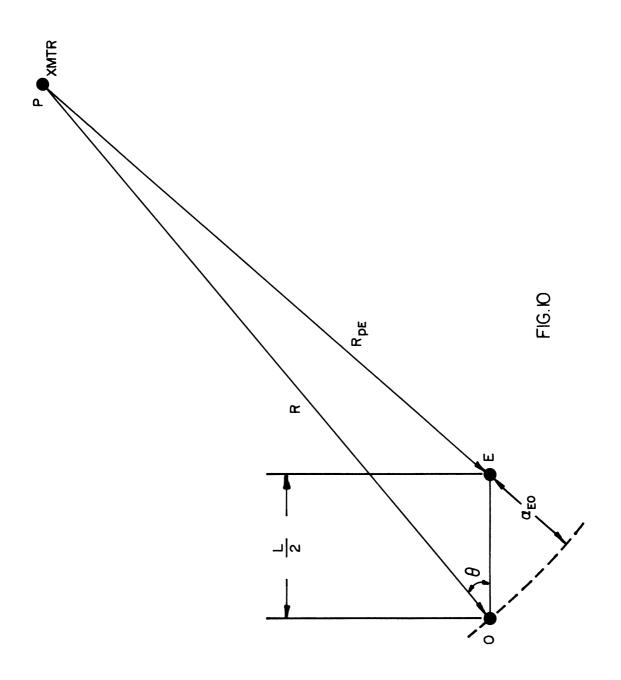


FIG. 9. ANTENNA POSITIONING FOR "SPHERICAL WAVE-FRONT" SYSTEM



In terms of relative phase angles referred to antenna 0 as the reference point and dropping the higher order terms:

$$\phi_{EO} = \frac{2\pi}{\lambda} \alpha_{EO} = \frac{\pi L \cos \theta}{\lambda} - \frac{\pi L^2 \sin^2 \theta}{4R\lambda} + \dots$$

$$\Phi_{WO} = \frac{2\pi}{\lambda} \alpha_{WO} = -\frac{\pi L \cos \theta}{\lambda} - \frac{\pi L^2 \sin^2 \theta}{4R\lambda} + \dots$$

and similarly:

$$\phi_{NO} = \frac{\pi L \sin \theta}{\lambda} - \frac{\pi L^2}{4R\lambda} \cos^2 \theta + \dots$$

$$\varphi_{SO} = -\frac{\pi L \sin \theta}{\lambda} - \frac{\pi L^2}{4R\lambda} \cos^2 \theta + \dots$$

Now add  $\phi_{\hbox{\footnotesize EO}}$  and  $\phi_{\hbox{\footnotesize WO}}$  to obtain  $\phi_{\hbox{\footnotesize EW}}$  :

$$\Phi_{EW} = \Phi_{EO} + \Phi_{WO} = -\frac{\pi L^2}{2R\lambda} \sin^2 \Theta + \dots$$

Similarly for  $\phi_{NS}$ :

$$\varphi_{NS} = \varphi_{NO} + \varphi_{SO} = -\frac{\pi L^2}{2R\lambda} \cos^2 \theta + \dots$$

Next take the sum of  $\phi_{\mbox{EW}}$  and  $\phi_{\mbox{NS}}$  to be called  $\phi_{\mbox{EWNS}}$  :

$$\varphi_{\text{EWNS}} = \varphi_{\text{EW}} + \varphi_{\text{NS}} = -\frac{\pi L^2}{2R\lambda} \sin^2 \theta + \cos^2 \theta + \dots$$

$$\phi_{\text{EWNS}} = -\frac{\pi L^2}{2R\lambda} + \dots$$

Solving this for R one obtains:

$$R = -\frac{\pi L^2}{2\lambda \phi_{EWNS}}$$

Now take the quotent of  $\phi_{EW}$  and  $\phi_{EWNS}$ :

$$\frac{\Phi_{\text{EW}}}{\Phi_{\text{EWNS}}} \stackrel{!}{=} \frac{-\frac{\pi L^2 \sin^2 \Theta}{2R\lambda}}{-\frac{\pi L^2}{2R\lambda}}$$

Solving this for  $\sin^2 \theta$  one obtains:

$$\sin^2 \Theta = \frac{\phi_{EW}}{\phi_{EWNS}}$$

Similarly:

$$\cos^2 \theta \doteq \frac{\varphi_{NS}}{\varphi_{EWNS}}$$

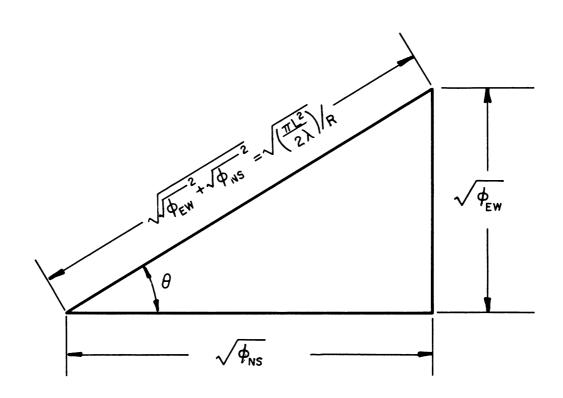


FIG.II DETERMINATION OF RANGE AND BEARING

Since

$$\sin \theta \doteq \frac{\sqrt{\phi_{EW}}}{\sqrt{(\sqrt{\phi_{EW}})^2 + (\sqrt{\phi_{NS}})^2}}$$

and

$$\cos \theta \doteq \frac{\sqrt{\phi_{\rm NS}}}{\sqrt{(\sqrt{\phi_{\rm EW}})^2 + (\sqrt{\phi_{\rm NS}})^2}}$$

we can construct the diagram shown in Fig. 11.

#### 3.3 Possible Method of Instrumentation

 $\phi_{EO}$  is the phase angle by which the signal at antenna E leads that at antenna O.  $\phi_{WO}$  is likewise the phase angle by which the signal at antenna W leads that at reference antenna O. Let the voltage  $\boldsymbol{e}_E$ ,  $\boldsymbol{e}_W$ , and  $\boldsymbol{e}_O$  be respectively:

$$e_{E}^{} = E \sin (\omega_{O}^{} t + \phi_{EO}^{}),$$
 $e_{W}^{} = W \sin (\omega_{O}^{} t + \phi_{WO}^{}), \text{ and }$ 
 $e_{O}^{} = A \sin (\omega_{O}^{} t),$ 

where E, W, and A are arbitrary constants involving the system parameters.

First, by the processing shown in Fig. 12, one takes the product  $\mathbf{e}_{\mathrm{E}}$  and  $\mathbf{e}_{\mathrm{W}}$  to be called  $\mathbf{e}_{\mathrm{EW}}$ :

$$\begin{split} \mathbf{e}_{\mathrm{E}} & \times \mathbf{e}_{\mathrm{W}} &= \mathrm{E} \sin \left( \omega_{\mathrm{O}} t + \phi_{\mathrm{EO}} \right) \times \mathrm{W} \sin \left( \omega_{\mathrm{O}} t + \phi_{\mathrm{WO}} \right) \\ &= \frac{\mathrm{EW}}{2} \left[ \cos \left( \phi_{\mathrm{EO}} - \phi_{\mathrm{WO}} \right) - \cos \left( 2\omega_{\mathrm{O}} t + \phi_{\mathrm{EO}} + \phi_{\mathrm{WO}} \right) \right] . \end{split}$$

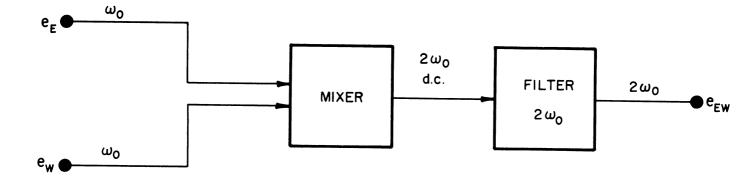


FIG. 12

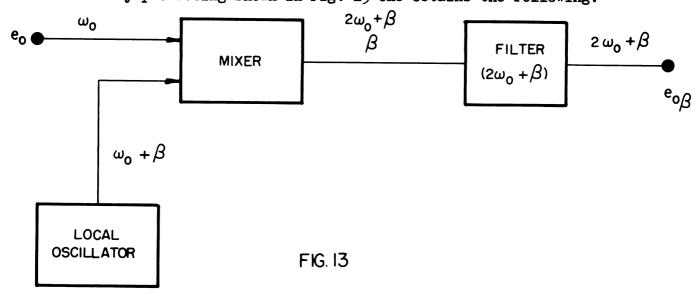
After filtering to retain only the  $2\omega_{_{\scriptsize O}}$  term one has:

$$e_{EW} = -\frac{EW}{2} \cos (2\omega_{O}t + \phi_{EO} + \phi_{WO})$$
$$= -\frac{EW}{2} \cos (2\omega_{O}t + \phi_{EW}).$$

Next one takes a locally generated signal at a radian frequency of  $\omega_{_{\rm O}}$  +  $\beta$  to be called  $e_{_{\rm B}}$ :

$$e_B = B \sin (\omega_0 + \beta)t$$
.

By processing shown in Fig. 13 one obtains the following:



$$e_0 \times e_B = A \sin \omega_0 t \times B \sin (\omega_0 + \beta)t$$

$$= \frac{AB}{2} \cos \beta t - \cos (2\omega_0 + \beta)t .$$

Now, by filtering, one takes only the  $2\omega_{\rm O}$  +  $\beta$  component of  $e_{\rm OB}$ :

$$e_{OB} = -\frac{AB}{2}\cos(2\omega_0 + \beta)t$$
.

Next, as shown in Fig. 14, one takes the product of  $\mathbf{e}_{\mathrm{EW}}$  and  $\mathbf{e}_{\mathrm{OB}}$  to be called  $\mathbf{e}_{\mathrm{EWO}}$ :

$$\begin{split} \mathbf{e}_{\mathrm{EW}} & \times \mathbf{e}_{\mathrm{OB}} &= -\frac{\mathrm{EW}}{2} \cos \left(2\omega_{\mathrm{O}} \mathbf{t} + \phi_{\mathrm{EW}}\right) \times -\frac{\mathrm{AB}}{2} \cos \left(2\omega_{\mathrm{O}} \mathbf{t} + \beta \mathbf{t}\right) \\ &= \frac{\mathrm{EWAB}}{8} \left[\cos \left(\beta \mathbf{t} - \phi_{\mathrm{EW}}\right) + \cos \left(4\omega_{\mathrm{O}} \mathbf{t} + \beta \mathbf{t} + \phi_{\mathrm{EW}}\right)\right]. \end{split}$$

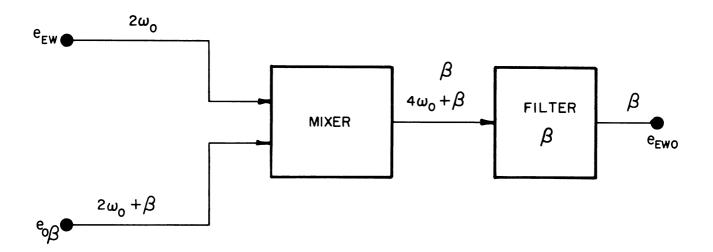


FIG. 14

After retaining only the  $\beta$  term:

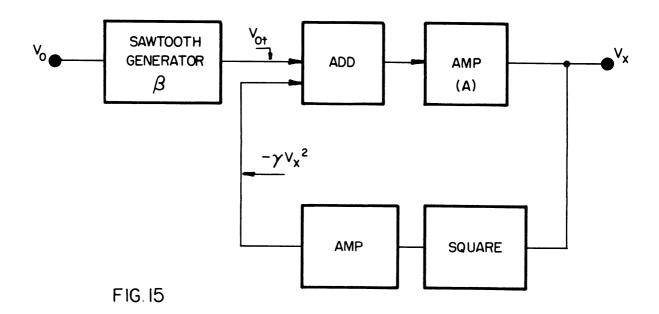
$$e_{EWO} = \frac{EWAB}{8} \cos (\beta t - \phi_{EW})$$
.

In a similar manner, the signals from antennas N and S together with that from antenna O could be processed to give:

$$e_{NSO} = \frac{NSAB}{8} \cos (\beta t - \phi_{NS})$$
.

The next step is the derivation of a voltage proportional to  $\sqrt{\phi_{EW}}$  and  $\sqrt{\phi_{NS}}$  .

Consider Fig. 15.



The output voltage,  $V_{y}$ , is given by:

$$V_{x} = -\frac{1}{2A\gamma} \sqrt{\frac{V_{o}^{t}}{\gamma} \left(1 + \frac{1}{4A^{2}\gamma V_{o}^{t}}\right)}$$
.

For values of A,  $\gamma$ , and t, such that

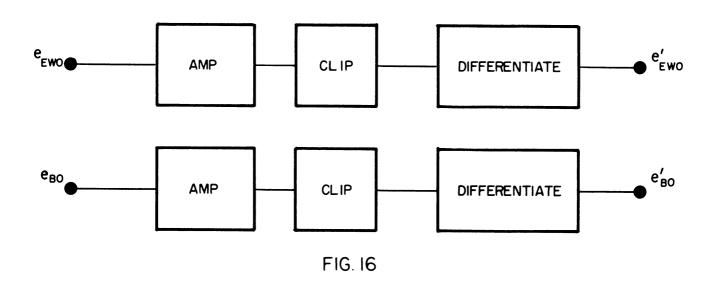
$$\sqrt{V_0 t} \gg -\frac{1}{2A\sqrt{\gamma}}$$
 and  $4A^2 \gamma V_0 t \gg 1$ ,

 $\boldsymbol{V}_{\boldsymbol{x}}$  can be represented approximately by:

$$V_{X} \doteq \sqrt{\frac{V_{O}t}{\gamma}} \quad \sqrt{t}$$

Now one has a voltage,  $V_{\chi}$ , which is proportional to the square root of time, t.

Now send  $e_{\mbox{EWO}}$  and  $e_{\mbox{OB}}$  through the wave shaping processing shown in Fig. 16.



The output  $e_{BO}^{*}$  is a series of sharp pulses with a recurrence interval of time,  $T_{O}=\frac{2\pi}{\beta}$ , but lags the pulses of  $e_{BO}$  by a time,  $T=\frac{\phi_{EW}}{\beta}$ , as shown in Fig. 17.

Now if one takes the voltage  $V_X$ , which also has a fundamental period of  $T_O=\frac{2\pi}{\beta}$ , and considers its value at t = T, one obtains a voltage  $V_{EW}$  proportional to  $\sqrt{\phi_{EW}}$ . Similarly,  $V_{NS}{\sim}\sqrt{\phi_{NS}}$ .

Now, if  $V_{EW}$  is applied to the y-axis of an oscilloscope, and  $V_{NS}$  is applied to the x-axis, a triangle can be constructed as shown in Fig. 18. However, there still remains some quadrantal ambiguity. This ambiguity can be resolved by some additional instrumentation since this information is present in the unprocessed signals.

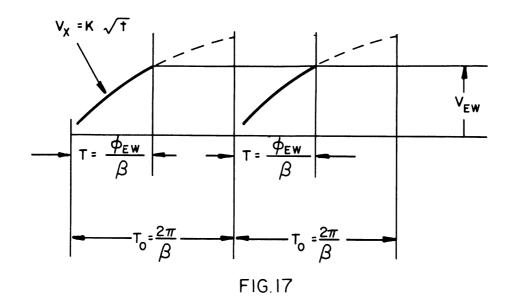
A complete block diagram of the system is shown in Fig. 19.

# 4. PERFORMANCE OF INTERFEROMETER DF SYSTEMS IN TERMS OF ACTUAL PROPAGATION CONDITIONS

Each of the systems discussed determines the bearing of a transmitter by sampling the wave front at a few widely separated points.

In the "Oak-Leaf" DF, the bearing is determined from these samples by comparing the relative phases at each of the sampling points; from these relative phases an imaginary phase front can be drawn which under ideal propagation conditions, will coincide with the actual phase front. The bearing is determined from the phase front by a perpendicular to the phase front at the DF site.

The "Spherical Wave-Front" system proceeds one step further than the previous system: not only are the relative phases compared, but the differences in relative phases are compared in order to obtain as an end result an imaginary phase front as before represented, this time, by the arc of a circle. Again, under ideal propagation conditions, the imaginary



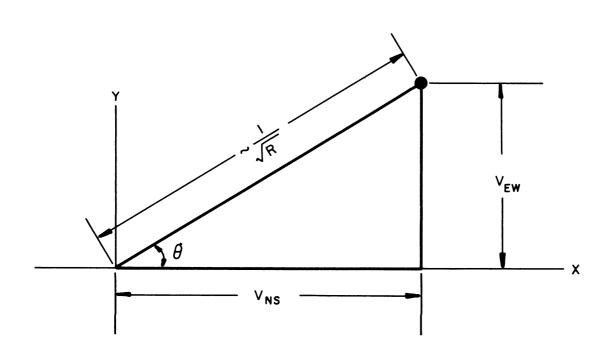


FIG. 18. PRESENTATION OF RANGE AND BEARING INFORMATION ON CRO

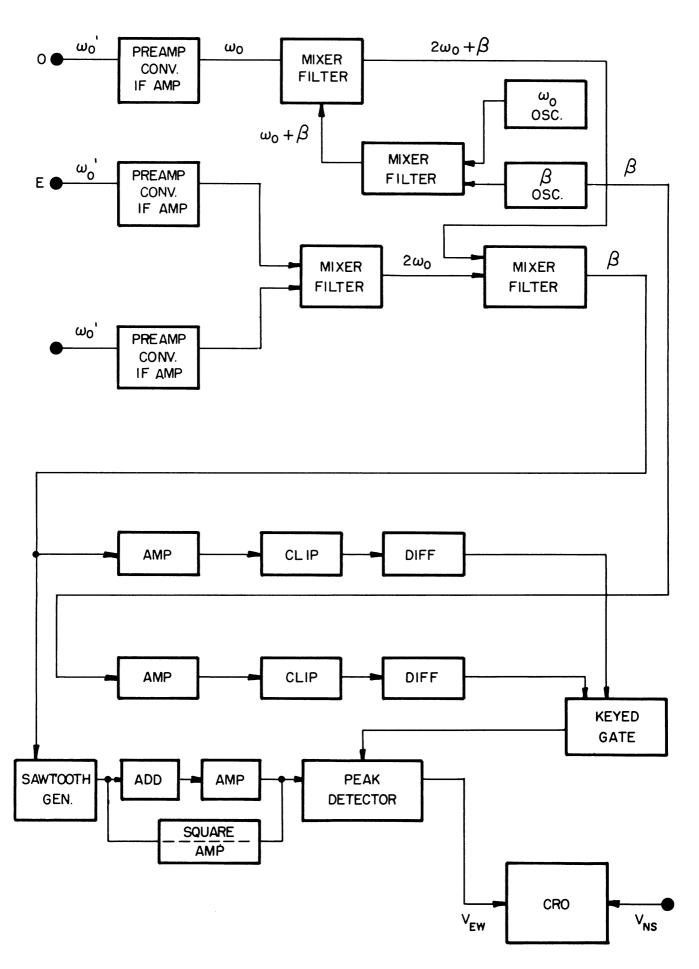


FIG.19 BLOCK DIAGRAM OF SPHERICAL WAVE-FRONT SYSTEM 24

phase front will coincide with the actual phase front. In this system the bearing and also the range are determined by locating the center of the circular arc.

In either system the fundamental difficulty is the same. Each system samples the wave front at only a few widely separated points and in no way attempts to determine the average wave front between these points. The "Spherical Wave-Front" system is a bit worse in this respect. Not only does it compare the relative phases at the several points and then take the differences of these phases as does the "Oak-Leaf" DF, but it goes one step further and takes differences of the differences of the relative phases, thus leaving the system open to the possibility of very serious errors. Perhaps this may be seen more clearly by referring to Fig. 20. In the "Oak-Leaf" DF system the bearing of the transmitter is determined by essentially comparing length Pl with length PO to derive a difference length  $\Delta L = PO-Pl$ , which is determined in terms of phase angles. Since AL will be a very small quantity as compared to PO or Pl it can be seen that a very small difference in two large quantities is being taken, which will lead to serious errors when actual propagation conditions cause the average velocity of wave propagation over path Pl to differ from that over path PO.

Looking at Fig. 21, which represents the conditions involved in the "Spherical Wave-Front" system, it is seen that in this system that distance PO is compared to PE and also to distance PW to obtain difference lengths  $\Delta EO = PO-PE$  and  $\Delta WO = PO-PW$ , respectively. Then  $\Delta EO$  is compared to  $\Delta WO$  to obtain the second difference,  $\Delta EW = \Delta EO - \Delta WO$ , which is expressed in terms of phase angles, all with respect to the phase of the signal at antenna O.

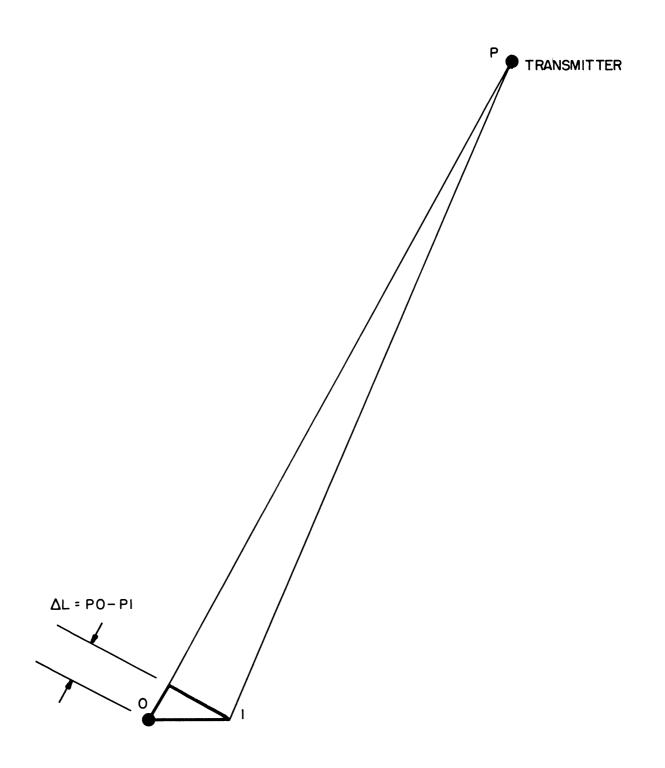


FIG. 20

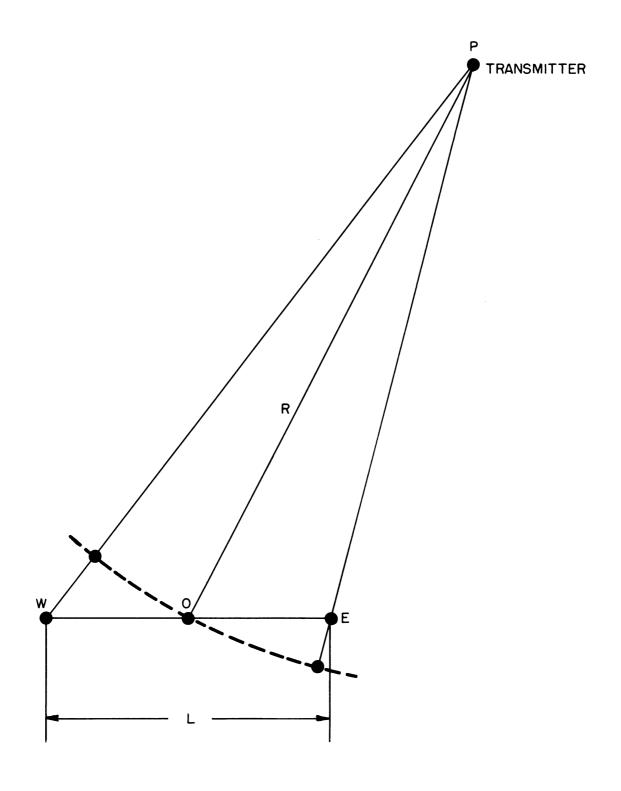


FIG. 21

Since the array length L is very small compared to the distance R, it can be seen that only a very small difference in the average velocity of wave propagation over the three paths, PE, PO, and PW, can cause extremely large errors in the bearing and range. Also, since the resultant phase angle to be measured is likely to be extremely small except in the special case of the transmitter being very close to the direction-finding site, the instrumental errors are likely to be very large, if not the prime determining factor in the practicality of the system.

#### 5. CONCLUSIONS

The analysis section of this report presents two methods of instrumenting two interferometer DF systems. In order to determine the usability of these systems in a real situation, one should make an error analysis using perturbation data for the particular case involved. It appears that as one increases the aperture in the manner of an interferometer system without increasing the number of sampling points that the system may be more susceptible to environmental errors than would ordinarily be the case, and, as is pointed out in the report, more sample points in the space are needed.

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