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The behavior of both uncoated and coated fiber reinforced composite substrate systems subjected to repeated impingements of liquid droplets was investigated. The system studied consisted of 1) an uncoated fiber reinforced composite, and 2) a fiber reinforced composite covered by a single layer of homogeneous coating of arbitrary thickness. A macroscopically anisotropic model was developed to approximate the elastic behavior of the fiber reinforced composite. Based on the uniaxial stress wave model, the variations of the stresses with time in the

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UNCLASSIFIED SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered) 20. coat-substrate system were determined both in the coating and in the substrate. Employing the fatigue theorems established for the rain erosion of homogeneous materials, algebraic equations were derived for both systems (1) and (2) which describe the incubation period, rate of mass removal and the total mass loss. The results were compared to available experimental data and good agreement was found between the present analytical results and the data.

FOREWORD

This final report was submitted by Dr. George S. Springer and Dr. Cheng I. Yang of The University of Michigan, Mechanical Engineering Department, Ann Arbor, Michigan, under contract F33615-72-C-1563, Project 7340, Task 734007, with the Air Force Materials Laboratory, Wright-Patterson Air Force Base, Ohio. George F. Schmitt, AFML/MBE was the laboratory project monitor.

This report has been reviewed and cleared for open publication and/or public release by the appropriate Office of Information (OI) in accordance with AFR 190-17 and DODD 5230.9. There is no objection to unlimited distribution of this report to the public at large, or by DDC to the National Technical Information Service (NTIS).

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This technical report has been reviewed and is approved for publication.

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Elastomers and Coatings Branch

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NOMENCLATURE

```
constants (dimensionless)
a_1 - a_2
b
                  constant defined by Eq. (34) (dimensionless)
                  knee in the fatigue curve
b<sub>2</sub>
                  speed of sound (or equivalent wave speed) (ft/sec)
C
                  diameter of the droplet (ft)
d
                  Young's modulus (1bf/ft<sup>2</sup>)
E
                  longitudinal Young's modulus (lbf/ft<sup>2</sup>)
E<sub>11</sub>
                  transverse Young's modulus (1bf/ft<sup>2</sup>)
E<sub>22</sub>
f
                  number of stress cycles (Eq. 7)
F
                  force (lbf)
                  shear modulus (lbf/ft<sup>2</sup>)
G
                  longitudinal shear modulus (lbf/ft<sup>2</sup>)
G<sub>12</sub>
                  transverse shear modulus (1bf/ft<sup>2</sup>)
G<sub>23</sub>
h
                  thickness of coat (ft)
Ι
                  rain intensity (ft/sec)
                  number of stress wave reflections in the coating re-
kم
                  quired for the stress at coat-substrate interface to
                  reach a value of 63.3 percent of \sigma_m (dimensionless)
                  total number of stress wave reflections in the coating
\mathbf{k}_{\mathrm{L}}
                  (dimensionless)
ī
                  average number of stress wave reflections in the coating
                  (dimensionless)
                  mass eroded per unit area (1bm/ft<sup>2</sup>)
m
                  dimensionless mass loss defined by Eq. (56)
m*
                  number of drops impinging per unit area (number/ft<sup>2</sup>)
n
                  number of drops impinging per site, see Eq. (37)
n*
                  fatigue life, see Eq.(33)(dimensionless)
N
```

```
stress (lbf/ft<sup>2</sup>)
P
                  drop density (number/ft<sup>3</sup>)
q
                  distance (ft)
r
                  parameter defined by Eq. (36) (1bf/ft<sup>2</sup>)
S
                  time (sec)
t
                  the duration of impact (sec)
t<sub>T.</sub>
V
                  velocity of impact (ft/sec)
٧
                  terminal velocity of a rain droplet (ft/sec)
۷<sub>f</sub>
                  volume fraction of fibers in composite materials
                  (dimensionless)
                  volume fraction of matrix in composite materials
                  (dimensionless)
W
                  weight loss due to erosion (lbf)
                  dynamic impedance (1bm/ft<sup>2</sup>-sec)
Z
Greek Letters
                  rate of mass loss (lbm/impact)
α*
                  dimensionless rate of mass loss (see Eq. 52)
                  the angle between axis and fiber's orientation (radians)
                  Poisson's ratio (dimensionless)
                  longitudinal Poisson's ratio (dimensionless)
ν<sub>12</sub>
                  transverse Poisson's ratio (dimensionless)
<sup>ν</sup>21
                  cosφ (see Eq. 20) (dimensionless)
\mu_1
                  sinφ (see Eq. 20) (dimensionless)
\mu_2
                  density (1bm/ft<sup>3</sup>)
                  angle of impact (radians)
θ
                  stress (lbf/ft<sup>2</sup>)
σ
                  mean stress at the liquid-coating interface after \mathbf{k}_L numbers of stress wave reflections (lbf/ft²)
ਰੱ
```

 σ_{I} endurance limit (lbf/ft²)

ultimate tensile strength (lbf/ft²)

 ψ parameter defined by Eq.(45)

Subscripts

c coating

f filament

i end of incubation period

m matrix

L liquid

s solid

Sc coat-substrate interface

Lc liquid-coat interface

SECTION I

INTRODUCTION

Non metallic components constitute an ever increasing portion of modern high speed aircraft, owing to their favorable performance characteristics, including high strength to weight ratio, good magnetic and optical properties etc. Unfortunately, such components are susceptible to heavy damage when subjected to repeated impingements of liquid droplets. In order to utilize the full potential of non metallic components, the damage caused to them by rain erosion must be understood.

The behavior of homogeneous materials (both metallic and non metallic) was investigated extensively experimentally (References 1-9) and analytically (References 3-5, 10-14), and the available results describe well the response of such materials to liquid impingement. However, the rain erosion behavior of fiber reinforced composites has not yet been evaluated fully. Most of the previous studies on reinforced composites are experimental in nature (References 15-20). These studies provide information on the behavior of a given material under a given condition, but fail to describe material behavior beyond the range of the experiments in which they were obtained. Therefore, the objective of this investigation is to develop analytical expressions which are consistent with experimental observations and which predict quantitatively the "erosion" of fiber reinforced materials under previously untested conditions. The model presented here describes a) the "incubation period" i.e. the time elapsed before the mass loss becomes appreciable and b) the mass loss past the incubation period.

The model used in this study is based on fatigue concepts and is designed along the lines developed previously for homogeneous materials (References 13, 14). Here, the model is applied to both coated and uncoated fiber reinforced composites. Study of uncoated composites is important for the general understanding of the rain erosion behavior of such materials. The analysis of coated composites, however, is of greater practical significance, since most uncoated composites have relatively poor resistance to erosion and must be coated for erosion protection.

SECTION II

THE PROBLEM

The problem investigated is the following. Spherical liquid droplets of constant diameter d impinge repeatedly upon a semiinfinite material (Figure 1). Two cases are considered: 1) the material is a fiber reinforced composite composed of unidirectional filaments embedded in a matrix. The material is taken to be semiinfinite normal to the plane of the surface (x direction, Figure 1). 2) The material is a fiber reinforced composite as described in point (1), but is covered by a homogeneous coating of thickness h. In the analysis it is assumed that (a) the composites are macroscopically homogeneous, (b) the fiber filaments are randomly distributed, (c) there is no fiber contiguity, (d) locally both the matrix and the filament are homogeneous and isotropic, (e) the filaments are parallel to the surface, and (f) there is a perfect bond between the matrix and the filaments and, in case of coated composites, between the coating and the substrate (i.e. at the interfaces the stresses and the displacements are continuous). The reinforced composite, the coating, and the droplets are characterized by the properties shown in Figure (1).

The angle of incidence of the droplets θ , and the velocity of impact V are taken to be constant. The spatial distribution of the droplets is considered to be uniform. The number of droplets impinging on unit area in time t may be written as (Reference 13)

$$n = \frac{6}{\pi} \frac{(V\cos\theta)I}{V_t d^3} t$$
 (1)

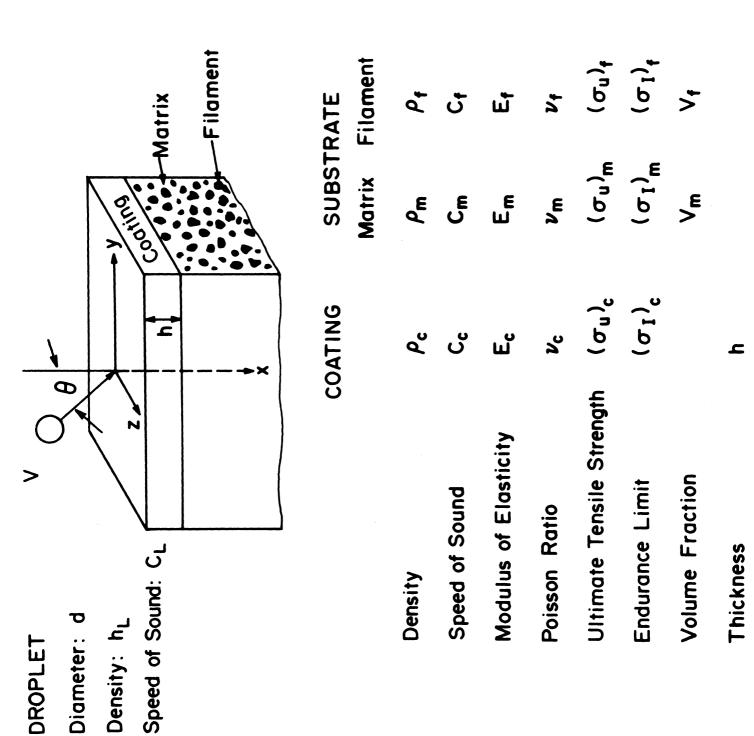


Figure 1. Droplet Impingement on a Coat-Substrate System

where I is the rain intensity and V_t the terminal velocity of the drop-let. The impingement rate is assumed to be sufficiently low so that all the effects produced by the impact of one droplet diminish before the impact of the next droplet (References 4, 13).

The pressure at the liquid-solid interface is taken to be constant and is approximated by the water hammer pressure (Reference 4)

$$P = \frac{\rho_L C_L V \cos \theta}{\frac{\rho_L C_L}{\rho_S C_S}} + 1$$
 (2)

where ρ and C are the density and the speed of sound. The subscript L and s refer to the liquid and solid respectively.

For a homogeneous material ρ_S and C_S are the density and speed of sound of the material. For a fiber reinforced composite ρ_S and C_S may be expressed as

$$\rho_{s} = \rho_{f} V_{f} + \rho_{m} V_{m} \tag{3}$$

$$C_{s} = \left[E_{22}/\rho_{s}\right]^{\frac{1}{2}} \tag{4}$$

where the subscripts f and m refer to the filament and the matrix, respectively. V is the volume fraction. E_{22} is the equivalent Young's modulus in the direction normal to the fibers (see equation 16, Section III).

For the purposes of the present analysis equations (2,3,4) represent the pressure with sufficient accuracy. The duration of this pressure is approximated by

$$t_{L} = \frac{2d}{C_{L}} \tag{5}$$

The forces, created by the impingements of the droplets, damage the material. This damage manifests itself in different ways, as cracks and pits, and by weight loss of the material. Here, we consider the weight loss to represent material damage, because this parameter was found to describe well the erosion behavior of homogeneous materials (Reference 13). Our model attempts, therefore, to describe the weight loss of the material as a function of time (Figure 2a). However, following the arguments presented in References (13, 14) we replace the total weight loss by mass loss per unit area m, and the time by the number of droplets impinging per unit area n (Figure 2b). The data is then approximated by two straight lines, as shown in Fig. 2b. Accordingly, the mass loss is given by the expressions

$$m = 0 0 < n_{i} (6a)$$

$$m = \alpha(n-n_{i}) \qquad \qquad n_{i} < n < n_{f}$$
 (6b)

In equations (6a, 6b) n_i is the incubation period, a period during which the mass loss is insignificant, α is the rate of mass loss subsequent to the incubation period, and n_f is the limit beyond which the data deviates from the straight line relationship (in most practical situations the usefulness of the material does not extend beyond n_f). Hence, the mass loss- and the erosion damage - can be evaluated, once the parameters n_i , α and n_f are known. Therefore, the problem is to determine these parameters.

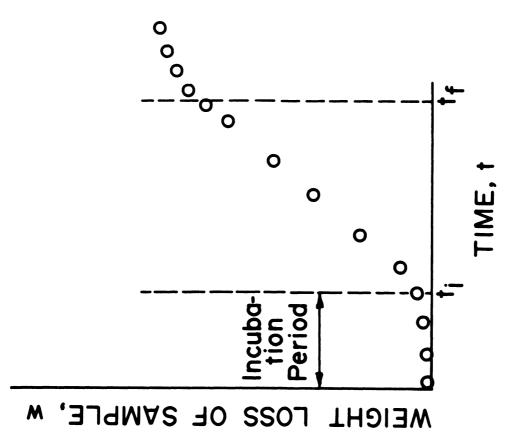
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TINU

o Data -- Model

ABRA,

0



000-

ncuba-

PER

tion Period

SSO7

Figure 2b. The Solution Model

Schematic of the Experimental Results

Figure 2a.

NUMBER OF IMPACTS PER UNIT AREA, n

0

SSAM

SECTION III

INCUBATION PERIOD OF UNCOATED FIBER REINFORCED COMPOSITES

In their previous investigations of coated and uncoated homogeneous materials Springer and his coworkers (References 13, 14) found that the incubation period can be established by applying fatigue theorems to the rain erosion problem. This approach is followed here, and in the following, fatigue concepts are used to determine the incubation period for fiber reinforced composites.

The starting point of the analysis is Miner's rule, which states that the failure of bars undergoing repeated torsion or bending obeys the expression (Reference 21)

$$\frac{f_1}{N_1} + \frac{f_2}{N_2} + \dots + \frac{f_q}{N_q} = a_1$$
 (7)

where f_1 , $f_2 \dots f_q$ represent the number of cycles the specimen is subjected to specified overstress levels σ_1 , $\sigma_2 \dots \sigma_q$, and N_1 , $N_2 \dots N_q$ represent the life (in cycles) at these overstress levels, as given by the fatigue (σ_e versus N) curve. a_1 is a constant .

Let us now consider a point on the surface of the material as shown in Figure 3. Each droplet impinging on the surface creates a stress at point B. This stress may be approximated by

$$\sigma(\mathbf{r},\phi) = \frac{F[1-2\nu(\phi)]}{2\pi r^2}$$
 (8)

Note that σ is a function of both the distance of the point of impact r, and the orientation of the direction of the impact with respect to the direction of the fibers ϕ . The force is taken to be a point force, i.e.

$$F = \frac{\pi d^2}{\ell} P \tag{9}$$

where P is the water hammer pressure given by equation (2). ν is the Poisson ratio for the composite in the ϕ direction (see Figure 3) (Reference 24)

$$v = E\left[\frac{v_{12}}{E_{11}} - \left(\frac{1+2v_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{23}}\right) \mu_1^2 \mu_2^2\right]$$
 (10)

E is Young's modulus of the composite in the ϕ direction (Reference 24)

$$\frac{1}{E} = \frac{\mu_1^4}{E_{11}} + (\frac{1}{G_{23}} - \frac{2\nu_{12}}{E_{11}})\mu_1^2\mu_2^2 + \frac{\mu_2^4}{E_{22}}$$
 (11)

and G is the shear modulus of the composite in the ϕ direction (Reference 24)

$$\frac{1}{G} = \frac{1}{G_{12}} + 4\left(\frac{1+2\nu_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{23}}\right) \mu_1^2 \mu_2^2$$
 (12)

In the longitudinal direction (i.e. in the direction parallel to the filaments) the Young's and shear moduli and the Poisson ratio may be written as (References 22, 23, 24).

$$E_{11} = E_f V_f + E_m V_m \tag{13}$$

$$G_{12} = \frac{(G_f + G_m) G_m V_m + 2 G_f G_m V_f}{(G_f + G_m) V_m + 2 G_m V_f}$$
(14)

$$v_{12} = v_f V_f + v_m V_m \tag{15}$$

In the transverse direction (i.e. normal to the filaments) the moduli are

$$E_{22} = \frac{4(\overline{Z}\overline{X} - \overline{Y}^2)G_{23}}{(\overline{X} + G_{23})\overline{Z} - \overline{Y}^2}$$
(16)

$$G_{23} = G_{m} \frac{2V_{f}G_{f}(X_{m}+G_{m}) + 2V_{m}G_{f}G_{m} + V_{m}X_{m}(G_{f}+G_{m})}{2V_{f}G_{m}(X_{m}+G_{m}) + 2V_{m}G_{f}G_{m} + V_{m}X_{m}(G_{f}+G_{m})}$$
(17)

$$v_{21} = v_{12} \frac{E_{22}}{E_{11}} \tag{18}$$

Variables subscripted by f or m refer to properties of the pure filament and the pure matrix, respectively. V_f and V_m are the volume fractions of the filament and the matrix, so that the total volume of the composite is

$$V_{s} = V_{f} + V_{m} = 1 \tag{19}$$

 μ_1 and μ_2 are defined as

$$\mu_1 = \cos \phi \tag{20a}$$

$$\mu_2 = \sin \phi \tag{20b}$$

In equation (16) \overline{X} , \overline{Y} and \overline{Z} are defined as

$$\overline{X} = \frac{X_{m}(X_{f}+G_{m})V_{m} + X_{f}(X_{m}+G_{m})V_{f}}{(X_{e}+G_{m})V_{m} + (X_{e}+G_{m})V_{f}}$$
(21)

$$\overline{Y} = V_f Y_f + V_m Y_m + (\frac{Y_f - Y_m}{X_f - X_m})^2 (\overline{X} - V_f X_f - V_m X_m)$$
 (22)

$$\overline{Z} = 2V_{f}(1-v_{f})X_{f} + 2V_{m}(1-v_{m})X_{m} + (\frac{Y_{f}-Y_{m}}{X_{f}-X_{m}})^{2} (\overline{X}-V_{f}X_{f}-V_{m}X_{m})$$
(23)

where

$$X_{f,m} = \frac{E_{f,m}}{2(1+v_{f,m})(1-2v_{f,m})}$$
(24)

$$Y_{f,m} = \frac{v_{f,m}^{E}f_{,m}}{2(1+v_{f,m})(1-2v_{f,m})}$$
(25)

During the incubation period the total number of impacts on an $rdrd\phi$ element located at r is (Figure 3)

$$f(r,\phi) = n_i r \, dr d\phi \tag{26}$$

Accordingly, we write Miner's rule (equation 7) in the form

$$\frac{f(r_1, \phi)}{N_1} + \frac{f(r_2, \phi)}{N_2} + \dots + \frac{f(r_q, \phi)}{N_q} = a_1$$
 (27)

Since r varies continuously from zero to infinity and ϕ from zero to 2π , equation (27) may be written as

$$\int_{0}^{\infty} \int_{0}^{2\pi} \frac{n_{i} r d\phi dr}{N} = a_{1}$$
 (28)

Equation (8) may be rearranged in the form

$$rdr = \frac{1}{2\pi} \frac{F(1-2\nu)}{2\sigma^2} d\sigma \tag{29}$$

Substituting equation (29) into equation (28), and using the relationship given by equation (9) we obtain

$$-\int_{\sigma_{1}^{\prime}}^{\uparrow}\int_{0}^{2\pi}\frac{n_{i}\left[\frac{P\pi d^{2}}{4}\cdot\frac{1}{2\pi}\frac{(1-2\nu)}{2\sigma^{2}}\right]d\phi d\sigma}{N}$$
(30)

The lower and upper limits of the first integral have been changed to the ultimate tensile strength and the endurance limit of the material,

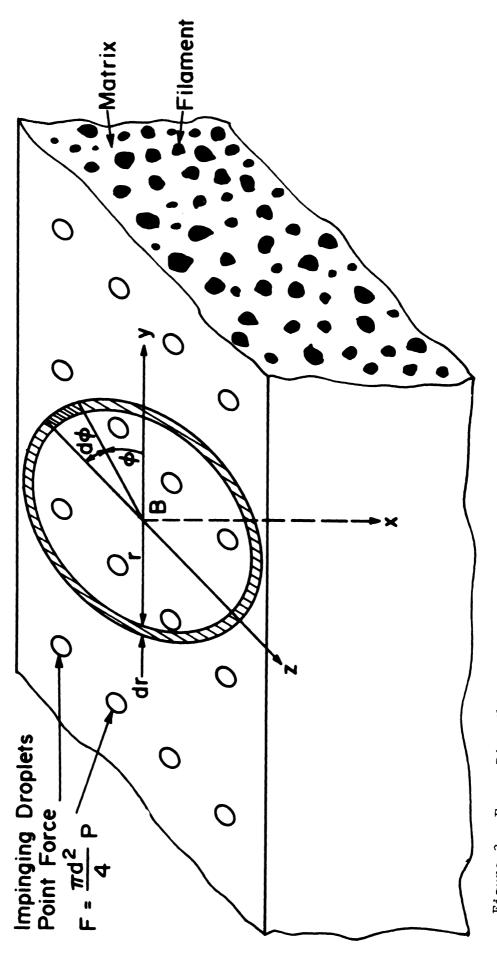


Figure 3. Force Distribution on the Surface

respectively. We shall assume that failure first occurs in the matrix, and approximate $\sigma_u^{'}$ and $\sigma_I^{'}$ by

$$\sigma_{\mathbf{u}}' = \sigma_{\mathbf{u}} \quad \frac{\mathbf{E}}{\mathbf{E}_{\mathbf{m}}} \tag{31}$$

$$\sigma_{\mathbf{I}}' = \sigma_{\mathbf{I}_{\mathbf{m}}} \frac{\mathbf{E}}{\mathbf{E}_{\mathbf{m}}} \tag{32}$$

where E is given by equation (11). The integrations in equation (30) may be performed once the fatigue life N is known as a function of the stress σ . Following the recommendation presented in References 13, 14, N is expressed as

$$N = \left(\frac{\sigma'}{\sigma}\right)^{b} \tag{33}$$

where

$$b = \frac{b_2}{\log_{10}(\frac{u}{V})}$$

$$\log_{10}(\frac{u}{V})$$

 b_2 is a constant, such that 10^{b_2} corresponds to the "knee" in the fati-gue curve. Substituting equation (33) into equation (30) and integrating we obtain

$$a_{1} = \frac{\pi d^{2}}{4} n_{1} P_{4(b-1)} \frac{E_{m}}{\sigma_{u}'} \left[\frac{3}{4} \pi \left(\frac{1}{E_{11}} + \frac{1}{E_{22}} \right) + \frac{\pi}{4} \left(\frac{1}{G_{23}} - \frac{2v_{12}}{E_{11}} \right) - \frac{4v_{12}\pi}{E_{11}} + \left(\frac{1+2v_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{21}} \right) \frac{\pi}{4} \right]$$

$$(35)$$

Introducing the definitions

$$S = \frac{4(b-1)\sigma'}{E_{m}} \left[\frac{3}{4} \pi \left(\frac{1}{E_{11}} + \frac{1}{E_{22}} \right) + \frac{\pi}{4} \left(\frac{1}{G_{23}} - \frac{2v_{12}}{E_{11}} \right) - \frac{4v_{12}\pi}{E_{11}} + \left(\frac{1+2v_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{21}} \right) \frac{\pi}{4} \right]^{-1}$$
(36)

$$n_i^* = \frac{\pi d^2}{4} n_i \tag{37}$$

 \mathbb{E}_4 mation (35) becomes

$$n_i^* = a_1 \frac{S}{P} \tag{38}$$

It is noted now that equation (38) is similar to the expression obtained in reference (13) for homogeneous materials. As in the case of homogeneous materials, S represents the "strength" of the material, while P is the stress produced at the surface. Naturally, the expression for S for reinforced composites (equation 36) is different from the value of S for homogeneous materials (reference 13). However, as one would expect, in the limits a) when there is only one constituent present, i.e. when

$$V_{m} = 0 \quad V_{f} = 1 \quad \text{or } V_{f} = 0 \quad V_{m} = 1$$
 (39)

or b) when the fiber and matrix materials are identical

$$E_{m} = E_{f}$$
 $G_{m} = G_{f}$ $v_{m} = v_{f}$ $G_{12} = G_{23} = G_{m} = G_{f}$ (40)

equation (36) reduces to the same form as was obtained previously (reference 13) for homogeneous materials.

The foregoing analysis is based on fatigue properties of bars in pure torsion and bending. Consequently, a linear relationship cannot hold between $n_{\bf i}^{\bf *}$ and S/P. Therefore, similarly to the procedure used for homogeneous materials we write

$$n_i^* = a_1 \left(\frac{S}{P}\right)^{a_2} \tag{41}$$

where a_1 and a_2 are constants. For homogeneous materials these constants were evaluated by Springer, Yang and Larsen, and were found to be $a_1 = 7.1 \text{x} 10^{-6}$ and $a_2 = 5.7$ (reference 14). The same values of these constants will be used here, i.e.

$$n_{i}^{*} = 7.1 \times 10^{-6} \left(\frac{S}{P}\right)^{5.7} \tag{42}$$

The use of the above constants ensures that in the limits given by equations (39) and (40) the foregoing expression yields the result appropriate for a homogeneous material. In other words, equation (42) together with equation (36) may be applied for all volume fractions of the filament from $V_f = 0$ ($V_m = 1$) to $V_f = 1$ ($V_m = 0$). The only limitation on the result is that the incubation period must be greater than zero. The conditions necessary for this limit are further discussed in Section VII.

The validity of the model was evaluated by comparing the above analytical results to experimental data. This comparison, shown in Figure 4 includes all existing data known to us for which the relevant material properties were available. The material properties used in the calculations are listed in Table I.

As can be seen from Figure 4 there is very good agreement between the present result and the data. This lends further confidence to the rain erosion model based on fatigue concepts.

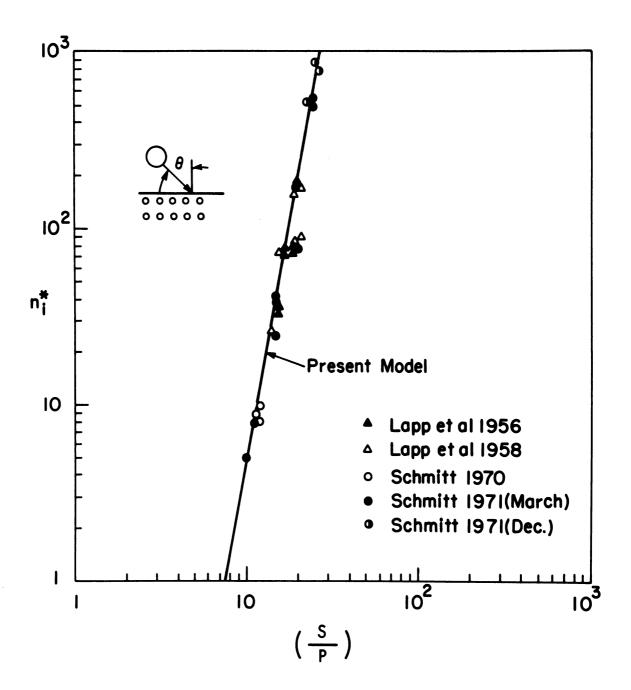


Figure 4. Incubation Period n, versus (S/P). Droplet Impingement on an Uncoated Composite Substrate. Solid Line: Model (Eq. 42) Symbols Defined in Table A-IV

SECTION IV

INCUBATION PERIOD FOR COATED FIBER REINFORCED COMPOSITES

The incubation period for a homogeneous coating on a homogeneous substrate was found by Springer, Yang and Larsen to be (reference 14)

$$n_{i}^{*} = 7.1 \times 10^{-6} \left[\frac{S}{\overline{\sigma}_{o}} \frac{1}{1 + \overline{k} | \psi_{sc}|} \right]$$
 (43)

where

$$\overline{k} = k_e \left[1 - \exp\left(-\frac{k_c}{k_e}\right) \right] \tag{44}$$

and

$$\psi_{SC} = \frac{Z_{S} - Z_{C}}{Z_{S} + Z_{C}}; \qquad \psi_{LC} = \frac{Z_{L} - Z_{C}}{Z_{L} + Z_{C}}$$
(45)

$$k_{e} = \frac{1 + Z_{c}/Z_{s}}{1 + Z_{L}/Z_{s}}$$
 (46a)

$$k_{L} = \frac{C_{C}}{C_{I}} \frac{d}{h}$$
 (46b)

$$\bar{\sigma}_{o} = P \frac{1 + \psi_{sc}}{1 - \psi_{sc}\psi_{Lc}} \left[1 - \psi_{sc} \frac{1 + \psi_{Lc}}{1 + \psi_{sc}} \frac{1 - \exp(-\frac{k_{L}}{k_{e}})}{\frac{k_{L}}{(\frac{k_{L}}{k_{e}})}} \right]$$
(47)

and Z is the impedance of the material

$$Z = \rho C \tag{48}$$

Note that in the absence of the coating the incubation period is

$$n_{i}^{*} = 7.1 \times 10^{-6} \left(\frac{S}{P}\right)$$
 (49)

where P denotes the impact stress at the surface. Thus, the factor $[1+\overline{k}\ |\psi_{\text{SC}}|\]^{-1} \text{ represents the damping effect of the coating.}$

It is noted, however, that the results, given by equations (43-49), are valid even when the substrate is a fiber reinforced composite material, provided the fibers are randomly distributed and the composite can be taken to be quasihomogeneous. In this case the impedance of the substrate can be approximated by $Z_S = \rho_S C_S$ where

$$C_{s} = \left[E_{s}/\rho_{s}\right]^{\frac{1}{2}} = \left[\frac{E_{22}}{\rho_{f}V_{f} + \rho_{m}V_{m}}\right]^{\frac{1}{2}}$$
 (50)

The incubation period can thus be calculated from equation (43), together with equation (36). The calculated values of the incubation period are compared to available experimental data in Figure 5. The material properties used in the calculations are listed in Table I. Again good agreement is evident between the calculated results and the data.

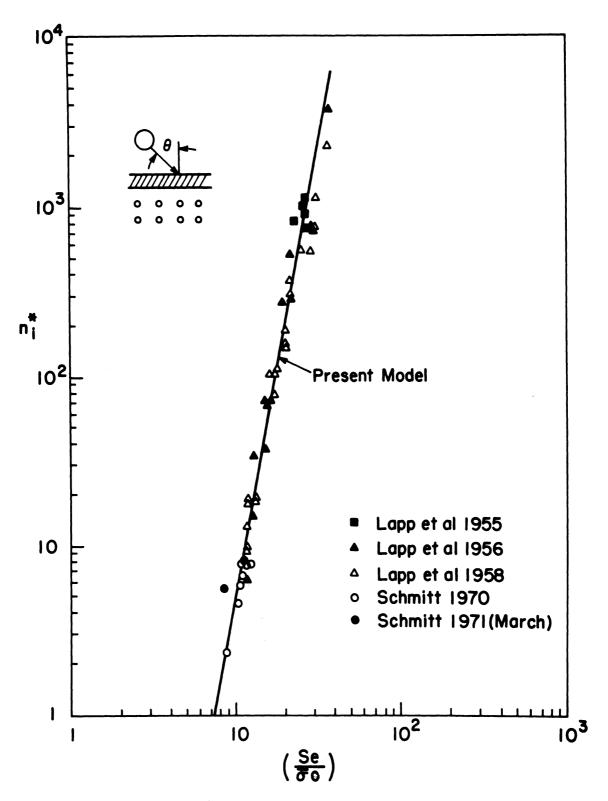


Figure 5. Incubation Period n_i^* versus (S_e/σ_o). Droplet Impingement on a Coated Composite Substrate. Solid Line: Model (Eq. 43). Symbols Defined in Table A-V

SECTION V

RATE OF MASS REMOVAL

The rate of mass removal for a homogeneous material was calculated by Springer and Baxi (13) and for a homogeneous material covered by a homogeneous coating by Springer, Yang and Larsen (14). For both of these cases the mass removal rate was found to be

$$\alpha^* = 0.023 \left(\frac{1}{*}\right)^{0.7} \tag{51}$$

where α^* is defined as

$$\alpha^* = \frac{\alpha}{\pi \, \rho \, \mathrm{d}^3 / 4} \tag{52}$$

The agruments leading to the above results could be repeated, without any modification, for fiber reinforced composite materials. Since the analyses for homogeneous materials are presented in detail in references (13, 14) they will not be reproduced here. It suffices to say that the above result is applicable to fiber reinforced composite materials (both with and without coating) as well as to homogeneous materials. Naturally, the appropriate equation must be used in evaluating $n_{\bf i}^{\star}$. For a fiber reinforced composite material $n_{\bf i}^{\star}$ must be calculated from equation (42). For a fiber reinforced composite material covered with a single layer of homogeneous coating, $n_{\bf i}^{\star}$ is to be determined from equation (43).

In equation (52) ρ is the density of the material undergoing erosion. Thus, for an uncoated fiber reinforced composite material ρ is given by equation (3). In the case of a coated material ρ is the density of the coating.

The rates of mass removal, calculated from equation (51) together with equation (42) (for uncoated reinforced composite) and equation (43) (for coated composites) are shown in Figures 6 and 7. In these figures the available experimental data are also given. The agreement is again good between the analytical results obtained from the present model, and the data.

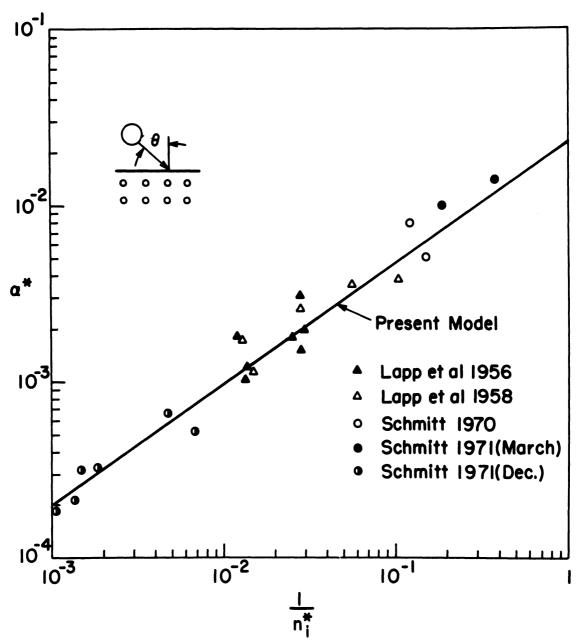


Figure 6. Rate of Erosion versus the Inverse of the Incubation Period.
Droplet Impingement on an Uncoated Composite Substrate.
Solid Line: Model (Eq. 51). Symbols Defined in Table A-IV

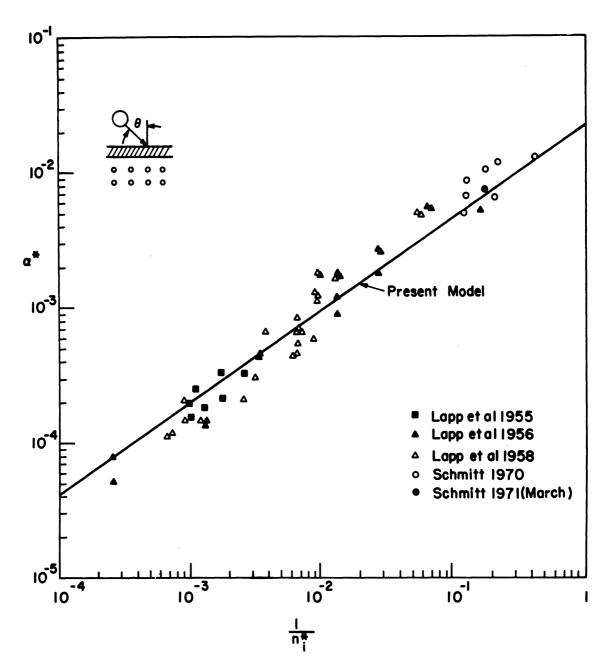


Figure 7. Rate of Erosion versus the Inverse of the Incubation Period.

Droplet Impingement on a Coated Composite Substrate. Solid Line:

Model (Eq. 51). Symbols Defined in Table A-V

SECTION VI

TOTAL MASS LOSS

The total mass loss was given by equation (6b) as

$$m = \alpha(n-n_1) \tag{53}$$

This equation is rewritten now in dimensionless form

$$m^* = \alpha^* (n^* - n_i^*) \tag{54}$$

or

$$\frac{\mathbf{m}^{\star}}{\overset{\alpha}{\star}} = \mathbf{n}^{\star} - \mathbf{n}^{\star} \tag{55}$$

Here the dimensionless mass loss rate is defined as

$$m^* = \frac{m}{od} \tag{56}$$

When there is no coating present ρ is the density of the composite as given by equation (3). When the reinforced composite is coated by a homogeneous material ρ is the density of the coating.

Equation (55) is valid for both coated or uncoated materials. In calculating the mass loss rate from this equation, the correct forms of n_i^* must be used. For an uncoated fiber reinforced composite material n_i^* is given by equation (42). For a fiber reinforced composite covered by a homogeneous coating n_i^* is given by equation (43).

Using equation (55) all the available data can be correlated on a m^*/α^* versus n^*-n^* plot. Such correlations are presented on Figures 8

and 9. In Figure 8 the analytical results are compared to the data for the case of uncoated composites. In Figure 9 a similar comparison is given for coated composites. The material properties used in obtaining these figures are listed in Table I. The agreement between the data and the theoretical line is very good, in fact remarkable in view of the unavoidable errors inherent in many of the measurements. It must be emphasized, that the theoretical lines in Figures 8 and 9 are direct results of the calculations, and are in no way "matched" to the data shown in these figures.

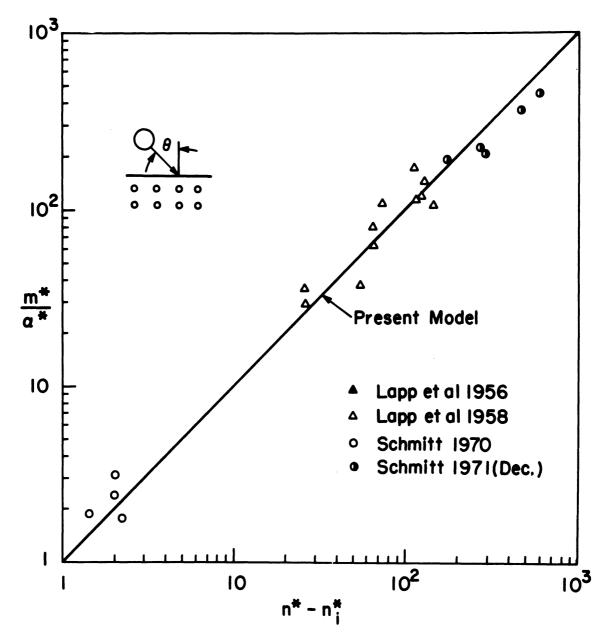


Figure 8. Comparison of Present Model (Solid Line: Eq. 55) with Experimental Results. Droplet Impingement on an Uncoated Composite Substrate. Symbols Defined in Table A-IV

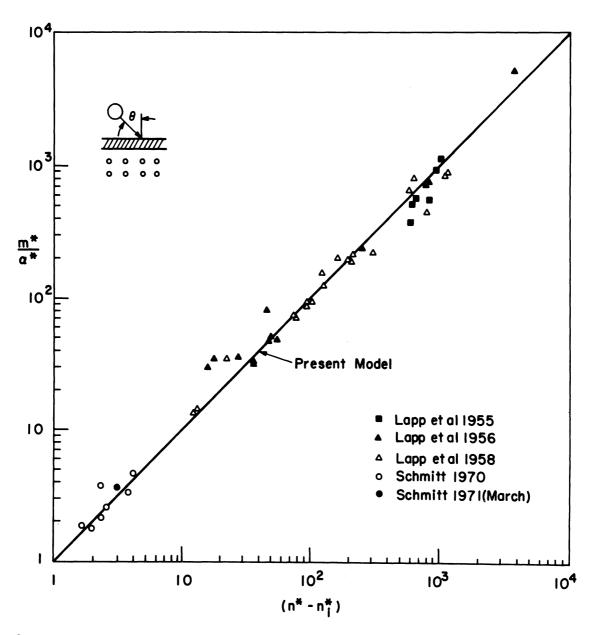


Figure 9. Comparison of Present Model (Solid Line: Eq. 55) with Experimental Results. Droplet Impingement on a Coated Composite Substrate. Symbols Defined in Table A-V

SECTION VII

LIMITS OF APPLICABILITY OF MODEL

The results presented in the foregoing sections are valid when the following two conditions are satisfied: (1) there is a finite incubation period and (2) the mass loss varies linearly with the number of impacts n (i.e. with time t). The first of these conditions is met when the following inequality is satisfied

$$n_i^* > 1 \tag{57}$$

For a fiber reinforced composite without coating this condition may also be expressed as (see equation 42)

$$\frac{S}{P} > 8 \tag{58}$$

For a fiber reinforced composite covered with a homogeneous coating a finite incubation period exists if (see equation 43)

$$\frac{S}{P} \frac{1}{1+\overline{k}} \frac{1}{|\psi_{CS}|} > 8 \tag{59}$$

Equations (57, 58, 59) provide the lower limit of the applicability of the model. The upper limit beyond which the present model cannot be applied is determined by the second condition given above. This limit was estimated by observing that up to about $n = 3n_i$ the data do not deviate significantly from the model. This condition may be expressed as

$$n < 3n_{+} \tag{60}$$

For an uncoated fiber reinforced composite this condition is satisfied when

$$n^* < 3n_i^* \tag{61}$$

For coated composites the upper limit of the applicability of the model is given by the combination of equations (2,49) and (59). The result is

$$n^* < 3n_i^* \tag{62}$$

It must be emphasized that conditions (57) and (60) are the only constraints imposed on the model. No further restrictions are placed on either the material or the impact velocity.

SECTION VIII

SUMMARY

In the following tables a summary of the equations is presented.

The following tables are included in this summary

- Table I. Definition of Parameters
- Table II. Equations Describing Rain Erosion of Fiber Reinforced

 Composite Materials
- Table III. Equations Describing Rain Erosion of Fiber Reinforced

 Composite Materials Covered with a Homogeneous Coating.

Table I. Definition of Parameters

| . Definition of Parameters | $f_{\rm m} + \rho_{\rm m} f_{\rm m}$ | $\left[\frac{\frac{\mu}{E_{11}}}{\frac{1}{E_{11}}} + \left(\frac{1}{G_{23}} - \frac{2^{\nu_{12}}}{E_{11}}\right) \frac{2^{2}}{\mu_{1}^{2}\mu_{2}^{2}} + \frac{\mu_{2}^{4}}{E_{22}}\right]$ | $\left[\frac{1}{G_{12}} + 4 \left(\frac{1+2v_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{23}}\right)_{\mu_{1}^{2}\mu_{2}^{2}}\right]^{-1}$ | m m the state of t | $^{\nu}_{12} \frac{^{B}_{22}}{^{E}_{11}}$ | $\mathbb{E}\left[\frac{\sqrt{12}}{\mathbb{E}_{11}} - \left(\frac{1+2\sqrt{12}}{\mathbb{E}_{11}} + \frac{1}{\mathbb{E}_{22}} - \frac{1}{\mathbb{G}_{23}}\right)^{\frac{2}{\mu_1}\mu_2^2}\right]$ | $[E_{22}/ ho_s]$ | ລ s |
|----------------------------|--------------------------------------|--|---|--|---|---|---|--|
| Table I. | S S | ា | ອ | ^v 12 | ^v 21 | 2 | s ວ | s S |
| | Density of Composite Material | Elastic Constants in the ϕ Direction (see Figure 3) | | μ ₂ = sinφ | | | Equivalent Wave Speed in Transverse Direction of Composite | Equivalent Dynamic Impedance in Transverse Direction of Composite |

Table I (continued)

| $^{ m LC}_{ m L}$ | ລິລິດ | $rac{1}{1-\psi_{SC}\psi_{LC}} \left[1-\exp(-rac{k_{L}}{k_{C}}) ight]$ | $\frac{z^{-2}c_{c}}{z^{+2}c_{c}}$ | $\frac{z_{\rm L}-z_{\rm c}}{z_{\rm L}+z_{\rm c}}$ | $\frac{C_0}{C_L} \frac{d}{h}$ | $\frac{1+Z_{\rm c}/Z_{\rm s}}{1+Z_{\rm L}/Z_{\rm s}}$ |
|---|---|---|-----------------------------------|---|-------------------------------|---|
| $^{ m T}_{ m T}$ | 2 C | ا <u>ت</u> | ψ S C | ÷ Lo | r. L | 'A a |
| Dynamic Impedance of the Liquid Droplet (diameter d) | Dynamic Impedance of Coating (thickness h) | Number of Stress Wave Reflections in the Coating after Impact by Droplet (reference 14) | | | | |

Equations Describing Rain Erosion of Fiber Reinforced Composite Materials Table II.

| 4 | | |
|--|--|--------------------------------|
| Strength Parameter S | $\frac{4\sigma_{\mathbf{u}}(b-1)}{E_{\mathbf{m}}} \left[\frac{3\pi}{4} \left(\frac{1}{E_{11}} + \frac{1}{E_{22}} \right) + \frac{\pi}{4} \left(\frac{1}{G_{23}} - \frac{2v_{12}}{E_{11}} \right) - \frac{4v_{12}\pi}{E_{11}} + \frac{\pi}{4} \left(\frac{1+2v_{12}}{E_{11}} + \frac{1}{E_{22}} - \frac{1}{G_{21}} \right) \right]$ | lbf/ft ² |
| Stress Parameter P (1bf/ft ²) | $\frac{z_L^V \cos \theta}{1 + z_L/z_s}$ | lbf/ft ² |
| Incubation Period * n _i | $7.1 \times 10^{-6} \left[\frac{\text{S}}{\text{P}} \right]$ | dimensionless |
| n 1 | $\frac{9.05 \times 10^{-6}}{d^2} \left[\frac{s}{P}\right]$ | number of impacts unit area |
| <u>.</u> | $\frac{9.05 \times 10^{-6}}{\text{qVcos} 6 d^2} \cdot \left[\frac{\text{S}}{\text{P}} \right]$ | seconds |
| | | |

dimensionless dimensionless mass loss unit area mass loss impact Table II (continued) 70.6 $\rho_{\rm g} d^3 [\frac{\rm P}{\rm S}]$ (qtVcos θ) - $\frac{9.05 \times 10^{-6}}{\rm d^2}$ ($\frac{\rm S}{\rm P}$) $70.6 \rho_{\rm s} d^3 \left[\frac{{\bf P}}{{\rm S}} \right]^4$ α^* $(n^* - n_1^*)$ 92 [P_] Rate of Mass Removal a* Total Mass Loss * 旦 ರ

| Table III. Ed | Equations Describing Rain Erosion of Fiber Reinforced Composite Covered with a Homogeneous | eneous Coating |
|---------------------------------|---|-------------------------------|
| | $\frac{4\sigma_{\mathbf{u}}(b-1)}{(1-2v_{_{\mathbf{c}}})[1+2 \mathbf{k} \psi_{\mathbf{sc}}]}$ | lbf/ft ² |
| Stress Parameter - | $\frac{z_{L} v \cos \theta}{1 + z_{L} / z_{c}} \frac{1 + \psi_{Sc}}{1 - \psi_{Sc} \psi_{Lc}} [1 - \psi_{Sc} \frac{1 + \psi_{Lc}}{1 + \psi_{Sc}} \frac{1 - \exp(\frac{k_{L}}{k_{e}})}{\frac{k_{L}}{k_{e}}}]$ | lbf/ft ² |
| Incubation Period * ni | $7.1 \times 10^{-6} \left[\frac{s_e}{10^{-6}} \right]^{5.7}$ | dimensionless |
| F u | $\frac{9.05 \times 10^{-6}}{d^2} \frac{s_e}{(\frac{s_e}{s_o})^{5.7}}$ | number of impact unit area |
| J.1 | $\frac{9.05 \times 10^{-6}}{\text{qVcos} \text{dd}^2} \frac{\text{S}}{\text{G}_o} 5.7$ | seconds |

Table III (continued)

| Rate of Mass Removal a* | 92 $\left(\frac{\sigma_{\Delta}}{S}\right)$ | dimensionless |
|-------------------------------|--|------------------------|
| ಶ | 70.6p _c d ³ (^a / _S) | mass loss impact |
| Total Mass Loss m* | $\alpha^* (n^* - n_{\underline{1}}^*)$ | dimensionless |
| E | 70.6 $\rho_{c}^{d^{3}} \left(\frac{\sigma_{o}}{s_{e}}\right) \left(qtV\cos\theta\right) - \frac{9.05 \times 10^{-6}}{d^{2}} \left(\frac{s_{e}}{\sigma_{o}}\right)$ | mass loss unit area |

APPENDIX

In this appendix, the following tables are included

Table A-I. Material Properties Used in the Calculations for Fiber

Table A-II. Material Properties Used in the Calculations for Coating Materials

Table A-III. Dynamic Properties of Composite Materials

Reinforced Composites

Table A-IV. Description of Data and Symbols Used in Figures 4,6,8

Table A-V. Description of Data and Symbols Used in Figure 5,7,9

Table A-I. Material Properties Used in the Calculations for the Reinforced Composites* (b=20.9)

| | Fiber Content % | E ₁₁ lb/in ² x 10 ⁶ | E ₂₂ lb/in ² x 10 ⁶ | G ₁₂ lb/in ² x 10 ⁶ | G ₂₃ lb/in ² x 10 ⁶ | v 12 | matrix x103 o _u 1b/in | p g/c.c. |
|---------------------|-----------------------|--|--|--|--|------|--|----------|
| glass-polyester | 65 | 5.3 | 1.2 | 0.55 | 0.24 | 0.25 | 6.5 | 1.85 |
| glass-epoxy | 65 | 6.7 | 2.5 | 1.0 | 0:30 | 0.25 | 8.4 | 1.84 |
| boron-epoxy | 65 | 30.0 | 3.0 | 1.0 | 0.8 | 0.22 | 8.4 | 2.19 |
| graphite-epoxy | 65 | 2853 | 1.2 | 0.65 | 0.2 | 0.31 | 8.4 | 1.47 |
| glass-polyimide | 65 | 7.9 | 2.9 | 1.0 | 0.3 | 0.25 | 8.0 | 1.98 |
| cemamic-teflon | 65 | 2.88 | 0.95 | ں•5 | 0.2 | 0.25 | 2.0 | 1.85 |
| glass-polyphenylene | e 65 | 2.59 | 0.85 | 0.5 | 0.2 | 0.25 | 2.0 | 1.82 |
| glass-silicone | 65 | 10.0 | 3.6 | 1.0 | 0.8 | 0.3 | 9.0 | 2.2 |

* From reference 25

Table A-II. Material Properties Used in the Calculations for Coating Materials** (b=20.9)

| | Density ρ $\frac{1b-\sec^2}{in^4}$ $\mathbf{x} 10^{-4}$ | Wave speed C in sec sec | Dynamic Impedance Z = pC 1b-sec/in ³ | σ _u 1b/in ² x 10 ³ | 2 |
|---------------------|---|-------------------------|--|--|------|
| water | 76*0 | 5.76 | 5.35 | | |
| polyurethane | 0.93 | 1.08 | 1.00 | 2.0 | 0.2 |
| neoprene | 1.45 | 0.53 | 0.78 | 1.2 | 0.2 |
| alumina | 3.56 | 21.9 | 78.4 | 1.7 | 0.25 |
| Polyethylene | 0.89 | 5.80 | 5.16 | 1.4 | 0.2 |
| nickel | 7.87 | 19.65 | 15.4 | 2.6 | 0.3 |
| silicon | 2.07 | 22.5 | 46.6 | 7.16 | 0.16 |
| teflon (hypalon) | 2.12 | 2.11 | 4.48 | 3.2 | 0.3 |

** From reference 26

Table A-III. Dynamic Properties of Composite Materials

| Equivalent Dynamic Impedance Z =pC 1b-sec/in ³ | 15.4 | 17.1 | 30.6 | 12.7 | 23.10 | 12.85 | 12.05 | 27.28 |
|--|-----------------|-------------|-------------|----------------|-----------------|----------------|---------------------|----------------|
| Equivalent Wave SpeedC Equivalent Wave SpeedC In In In/sec x 10 ⁴ | 7.82 | 8.95 | 13.1 | 8.5 | 12.4 | 7.39 | 7.05 | 13.18 |
| Equivalent Densityp 1b-sec ² /in ⁴ x 10 ⁻⁴ | 1.97 | 1.95 | 2.34 | 1.56 | 1.86 | 1.74 | 1.71 | 2.07 |
| Composite Material | glass-polyester | glass-epoxy | boron-epoxy | graphite-epoxy | glass-polyimide | ceramic-teflon | glass-polyphenylene | glass-silicone |

∞ Table A-IV. Description of Data and Symbols Used in Figures 4, 6,

| | | Materials | ials | Impact | Rain | , | ; 6 |
|--|---------------------------------|-----------|--------------------|--------------------|----------------------|-----------------|---------|
| Symbol | Investigators | Fiber | Matrix | Velocity ft/sec | Intensity (in/hr) | Drop Size mm | % Fiber |
| | | glass | polyester | 731 | p | 1.9 | 5.5 |
| • | Lapp et al 1956 (ref. 16) |) | epoxy | TC/ | 1 | 1 |) |
| | Iann et al | , | polyester | | | | 9 |
| < </td <td>1958</td> <td>glass</td> <td>epoxy</td> <td>731</td> <td></td> <td>1.9</td> <td></td> | 1958 | glass | epoxy | 731 | | 1.9 | |
| | (ret. 1/) | | polyimide | | | | |
| | | ceramic | teflon | | | | |
| | 1 | glass | epoxy | 700 | | | 69 |
| 0 | Schmitt & Krabill | | silicone | 2360 | | | |
| | (ref. 19) | | polyester | 2751 | 2.5 | 1.9 | |
| | | | polypheny- lene | 4246 | | | |
| | | boron | epoxy | | | | 55-65 |
| | | graphite | | | | | |

Table A-IV (continued)

| Symbol | Investigators | Materials | als | Impact | Rain Intensity | Drop Size | % Fiber |
|--------|-------------------|-------------|-----------|--------|-------------------|-----------|---------------|
| | | Fiber | Matrix | ft/sec | (in/hr) | | |
| | Schmitt | boron | | 121 | - | α- | |
| | 1971 (ref. 20) | graphite | epoxy | /31 | 7 | 2 | |
| | | s s s | polyimide | 731 | H | 88 | 65 |
| • | Schmitt 1971 | , D | epoxy | | | | |
| | (ref. 27) | graphite | | | | | ر بر در |
| | | boron | c FOA | | | | |

% Fiber 65 65 65 Drop Size 1.9 1.9 1.9 Intensity in/hr Rain Impact Velocity ft/sec 731 731 731 Description of Data and Symbols Used in Figures 1,4,5,7,8, 9,10,13,14, 21,22,27-33 10,14,15-20, 20-25, 25-30 polyester 5,6,8,10-15 Coating Thickness 2,4,5,11,23 20, 5-10 4-5, 10 10 mils 2,5 10 polyester polyester Matrix epoxy epoxy Substrate glass glass Fiber glass glass glass polyurethane polyurethane polyethylene polyurethane neoprene neoprene neoprene neoprene silicon Coating teflon Table A-V. Investigator Lapp et al 1958 Lapp et al 1955 Lapp et al 1956 (ref. 15) (ref. 16) (ref. 17) Symbol |

6 7

5,

Table A-V (continued)

| | | | Subs | Substrate | Coating | Velocity | Intensity | Velocity Intensity Drop Size | % Fiber |
|------------------|----------------------------------|--------------|----------|-----------|-------------------|------------------------------|-----------|------------------------------|---------|
| Inve | Investigator | Coating | Fiber | Matrix | inickness mils | דר/ אבר | 111 / 111 | | |
| Sch Kra 19 | Schmitt & Krabill 1970 (ref. 19) | nickel | glass | ероху | 12,15 | 3169 4291 2216 2280 | 2.5 | 1.9 | 69 |
| 400 | 7 + t | polyurethane | boron | epoxy | 8,12 | 731 | Н | 1.8 | 55-65 |
| 19 19 (ref | 1971 (ref. 20) | nickel | | , | | | | | |
| | | polyurethane | graphite | epoxy | | | | | |
| | | nickel | | | | | | | |
| | | urethane | boron | ероху | 10 | 1593,23 | 2.5 | 1.9 | 55-65 |
| | | nickel | | | | | | | |

Table A-V (continued)

| ze % Fiber | | 65 | | 69 | | | | | \$5-65 |
|------------|---------------------------------|------------|-------------------|--------------|-------------------|----------------------|-------------------------------|----------------------|--------------|
| Drop Size | | 1.9 | | 1.9 | | | | | |
| Rain | Velocity Intensity ft/sec in/hr | 1 | | 2.5 | | | | | |
| Tuesact | Velocity ft/sec | 731 | | 1593 2246 | 2426 | 1556 2 220 | 1556 22 <u>2</u> 0 2350 | 1678 2216 2451 | 1593 2360 |
| Coating | Thickness mils | 10, 15 | 6 | 20,30,40 | 30 | 10 | 5,10,15,20 30 | 08 | 10 |
| rate | Matrix | евоху | ероку | epoxy | polyimide | epoxy | | | epoxy |
| Substrate | Fiber | glass | glass | glass | glass | glass | | | boron |
| 3 | COALING | teflon | hypalon | | alumina | neeprene | urethane | polyethylene | urethane |
| | Investigator | Lapp et al | 1938 (ref. 17) | | Schmitt & Krabill | (ref. 19) | | | |
| | Symbol | < | 1 | | 0 | | | | |

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