Kinetic Model for Noncatalytic Supercritical Water Gasification of Cellulose and Lignin

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This article reports the first kinetics model for Supercritical Water Gasification (SCWG) that describes the formation and interconversion of individual gaseous species. The model comprises 11 reactions, and it uses a lumping scheme to handle the large number of intermediate compounds. We determined numerical values for the rate constants in the model by fitting it to experimental data previously reported for SCWG of cellulose and lignin. We validated the model by showing that it accurately predicts gas yields at biomass loadings and water densities not used in the parameter estimation. Sensitivity analysis and reaction rate analysis indicate that steam-reforming and water–gas shift are the main sources of H2 in SCWG, and intermediate species are the main sources of CO, CO2, and CH4.

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Introduction

Developing methods to use the chemical energy in biomass more readily is one pathway to a more sustainable energy supply. Attractive features of biomass are that it is a renewable resource available in large amounts in many areas of the world, the eventual oxidation of its carbon atoms does not increase the net amount of CO2 in the atmosphere, and many biomass feedstocks are wastes that would be eliminated in the process of converting them to fuels.

Gasification is one approach for biomass utilization. In conventional gasification, biomass is converted into H2, CH4, CO, CO2, char, and tar.1–3 The char and tar represent a loss of useful carbon, and the tar can be difficult to separate from the product gas stream.4,5 Another drawback in conventional biomass gasification is the energy required to dry biomass feedstocks, which very often have more than 50% moisture.6 The thermal efficiency of conventional gasification drastically decreases as the biomass moisture content increases.7

Supercritical Water Gasification (SCWG) has been proposed as an alternative approach that avoids these difficulties. In this process, water above its critical point (374°C and 22 MPa) is the medium for gasification reactions. The presence of supercritical water (SCW) fundamentally changes the gasification process. SCW can dissolve cellulose and lignin, the main components of woody biomass, and thereby create a homogeneous medium in which hydrolysis reactions dominate.4,8–10 As a result, the amount of by-products (such as char and tar) is minimized, leading to higher gas yields.8,11–14

Rate laws and kinetic parameters are essential for the design of reactors and estimation of product distribution. The few previous kinetic models8,15–18 for SCWG focus solely on gasification yields or feedstock conversion, without capturing the pathways leading to formation and interconversion of gas species. There are no published kinetic models dealing with individual gas yields for SCWG. As a result, little is known about the rates of different potential reaction paths. For instance, the methanation reaction takes place under SCWG conditions, but it is not known whether most of the CH4 formed actually originates from methanation or possibly from other gasification routes, such as direct pyrolytic cleavage of methyl groups present in lignin. If most of the CH4 originates from methanation, how close to equilibrium is this reaction at typical SCWG conditions? Could catalysts be used to increase CH4 yields? These are some of the questions one could begin to answer with the aid of a reliable kinetic model that includes information about yields of individual gaseous products.
We developed a kinetic model for noncatalytic SCWG of commercially available microcrystalline cellulose and organosolv lignin and fit it to experimental data obtained in quartz reactors.\(^1\) By using quartz, we avoided unintentional catalytic contributions from metallic reactor walls. One objective of this modeling work is to identify the reaction pathways leading to the formation of specific gases and to quantify rates of formation. The first part of this article describes the reaction pathways in the model. The second part describes the parameter estimation procedure, results, and comparisons of model predictions with experimental measurements. In the final part, we use the model to identify the reactions that are most important for forming the different gases.

Model Development

The model is based on reaction pathways proposed in the literature for SCWG. It focuses on reactions involving gas species and simplifies reactions involving larger intermediate compounds by defining a generic intermediate species into which all actual intermediates are lumped. Following, we define the reactions involved in the model.

Reaction 1. Hydrolysis

For Cellulose: \(((C_6H_{10}O_5)_n + nH_2O \xrightarrow{k_1} nC_6H_{12}O_6)\)

For Lignin: \(((C_{10}H_{10}O_5)_n + nH_2O \xrightarrow{k_1} nC_{10}H_{12}O_4)\)

When cellulose (or lignin) is in water at supercritical conditions, the first step is solvation of the biomacromolecules. This physical process takes place simultaneously with hydrolytic attack on the macromolecular structures. This very fast step often leads to the formation of oligomers, such as cellubiose and cellotriose originating from cellulose. These oligomers can be further hydrolyzed. For the purpose of this model, we assume that hydrolysis leads directly and solely to monomers. The monomer for cellulose is glucose, and the monomer for lignin is based on the elemental composition of organosolv lignin.\(^2\) Sasaki et al.\(^3\) showed that cellulose is completely converted in water at 350°C and 25 MPa after only 4 s. Bobleret\(^4\) reported that over 90% of lignin disappears after only 0.4 min at 365°C. Given this literature data, we take the initial reactant to be the monomer instead of the biopolymer itself.

Reaction 2. Intermediate Formation.

Monomer \(\xrightarrow{k_2} C_6H_5O_2\)

Once the monomer is formed, it can undergo a variety of reactions leading to numerous decomposition products. Glucose, for instance, can undergo isomerization, dehydration, retro-aldol condensation, and hydrolysis.\(^2,3\) A key concept in this model is the treatment of all the different intermediate compounds as a single pseudo-component. Rather than monitoring and explicitly accounting for every possible intermediate compound, we adopted this lumping scheme for the intermediates. We define the intermediate species as \(C_6H_5O_2\), which represents any nonpermanent gas originating from the biomass that is capable of reacting further. These intermediates ultimately lead to the formation of gases.

Reactions 3 and 4. Steam-Reforming.

Steam-Reforming I

\[ C_6H_5O_2 + (x - z)H_2O \xrightarrow{k_1} xCO + (x - z + y/2)H_2 \]

Steam-Reforming II

\[ C_6H_5O_2 + (2x - z)H_2O \xrightarrow{k_1} xCO_2 + (2x - z + y/2)H_2 \]

One of the ways organic compounds form gases in the presence of water is via steam-reforming. The intermediate \(C_6H_5O_2\) reacting with water leads to CO and \(H_2\) (Steam-reforming I), or \(CO_2\) and \(H_2\) (Steam-Reforming II). To handle the stoichiometry in the steam reforming calculations in the model, we take the intermediate species to have the same chemical composition as the original monomer.

Reactions 5 to 8. Intermediate Decomposition.

- CO from Intermediate \(C_6H_5O_2 \xrightarrow{k_5} CO + C_6H_5O_2\)
- CO\(_2\) from intermediate \(C_6H_5O_2 \xrightarrow{k_6} CO_2 + C_6H_5O_2\)
- \(H_2\) from intermediate \(C_6H_5O_2 \xrightarrow{k_7} H_2 + C_6H_5O_2\)

Our experimental results\(^5\) suggest that steam-reforming alone cannot accurately describe the way gases are formed in noncatalytic SCWG. There are multiple ways the intermediates can decompose to form gases. For instance, in the case of lignin decomposition, methyl groups in the intermediates can be cleaved thermally, directly leading to the formation of \(CH_4\). To account for these pathways, we introduced the possibility of direct formation of the gas species from the lumped intermediates. Also, each intermediate molecule can undergo decomposition reactions multiple times, releasing small molecules such as \(H_2\) or \(CO\) and creating a new intermediate molecule each time. Since all intermediates are lumped together, however, there is no net consumption of intermediates in these steps.

Reaction 9. Char Generation.

\[ C_6H_5O_2 \xrightarrow{k_8} \text{Char} \]

Intermediate species in SCWG can react to form compounds that eventually become char. In our model, we lump all such compounds together and refer to them collectively as char. We assume that these molecules do not react to form gases.

Reactions 10 and 11. Gas species interconversion.

- Water–Gas Shift \(CO + H_2O \leftrightarrow CO_2 + H_2\)
- Methanation \(CO + 3H_2 \leftrightarrow CH_4 + H_2O\)

Once the gas species are formed, reactions 10 and 11 can change their relative amounts. The water–gas shift reaction consumes CO and is thought to be one of the main reaction pathways for the production of \(H_2\). Likewise, methanation is often invoked as an important route for the formation of \(CH_4\). Water–gas shift and methanation are the only reversible reactions in this model. We considered the possibility of adding other typical gasification reactions such as hydrogenation and
the Boudouard reaction, but equilibrium calculations done in ASPEN Plus showed that these reactions do not take place to any appreciable extent at the conditions of this work (500–600°C). These calculations are described elsewhere.23

The rate equation for each reaction was assumed to be first order in the concentration (C) of each species in the reaction. We used isothermal constant-volume quartz batch reactors for all experiments, so the reaction engineering analysis is straightforward. Following are the mole balance equations for each of the species.

\[
\frac{dC_{\text{CO}_2}}{dt} = xk_4C_{\text{ICW}} + k_6C_{\text{I}} + k_{10}C_{\text{CO}_2}C_{\text{H}_2} - k_{10}rC_{\text{CO}_2}CH_2 \quad (1)
\]

\[
\frac{dC_{\text{CO}}}{dt} = xk_3C_{\text{ICW}} + k_5C_{\text{I}} - k_{10}C_{\text{CO}_2}C_{\text{H}_2} - k_{11}C_{\text{CO}CH_2} + k_{11}rC_{\text{CH}_4}CW \quad (2)
\]

\[
\frac{dC_{\text{CH}_4}}{dt} = k_7C_{\text{I}} + k_{11}C_{\text{CO}CH_2} - k_{11}rC_{\text{CH}_4}CW \quad (3)
\]

\[
\frac{dC_{\text{CH}_2}}{dt} = \left(\frac{x}{C_0}\right) k_3C_{\text{ICW}} + \left(\frac{2x}{C_0}\right) k_4C_{\text{ICW}} + k_8C_{\text{I}} + k_{10}C_{\text{CO}_2}C_{\text{H}_2} - k_{10}rC_{\text{CO}_2}CH_2 + 3k_{11}C_{\text{CO}CH_2} + 3k_{11}rC_{\text{CH}_4}CW \quad (4)
\]

\[
\frac{dC_{\text{C}_M}}{dt} = k_2C_{\text{M}} - k_3C_{\text{ICW}} - k_4C_{\text{C}_W} - k_5C_{\text{I}} \quad (5)
\]

\[
\frac{dC_{\text{M}}}{dt} = -k_2C_{\text{M}} \quad (6)
\]

The subscripts I, M, and W represent the lumped intermediate compounds, the lignin or cellulose monomer, and water, respectively.

Results and Discussion

This section provides results from the model parameter estimation and then assesses the predictive ability of the model. The final portions present results from the model being exercised to reveal the fastest reaction paths and the paths to which the model predictions are most sensitive.

Parameter estimation

The temporal variation of the experimental gas concentrations (CH4, CO2, CO, and H2) at the “base case” conditions in our previous article19 for cellulose and lignin were used to determine the model parameters. The base case conditions are 500°C (cellulose), 600°C (lignin), 0.08 g/ml water density, and 9.0 wt % biomass loading. We take the term biomass to include the lignin and cellulose fractions of interest in this article. Experiments were performed from 2.5 to 30 minutes for cellulose, and from 2.5 to 75 minutes for lignin. These data were obtained in a kinetically controlled region for SCWG as the system was far from equilibrium and likely free of any mass transfer limitations on the observed rates.

For the SCWG experiments,19 the average particle size for cellulose was 116 μm, and for lignin it was 289 μm. Simmons and Gentry24 showed that pyrolysis of cellulose in the range 450–500°C is free from mass transfer limitations for particles as large as 200 μm. Vamvuka et al.25 performed TGA for several biomass feedstocks and measured kinetics without mass-transfer limitations using particles of 250 μm. On the basis of this literature, we believe that mass transfer limitations can be safely neglected in this study.

The objective function that was minimized is the unweighted sum of the squared differences between calculated and measured concentrations of the four gases. Scientist 3.0 from Micromath was used to fit the experimental data. Initial guesses for the rate constants were found manually by a trial-and-error method. Polymath 5.1 was used for the model simulations after the rate constants were determined.

The rate constants determined from the experimental SCWG data were k2, k3, k4, k5, k6, k7, k8, k9, k10, and k11. The rate constants for the reverse reactions (k10r and k11r) were related to the forward rate constants (k10 and k11) by the equilibrium constant K:

\[
k_r = \frac{k_f}{K} \quad (8)
\]

The equilibrium constants for the water–gas shift and methanation reactions were calculated using output from the REQUIL reactor block in ASPEN Plus. This block provides
equilibrium concentrations for a given reaction, from which we calculated $K_{10}$ (equilibrium constant for the water–gas shift) and $K_{11}$ (equilibrium constant for methanation) using Eqs. 9 and 10:

$$K_{10} = \frac{C_{\text{H}_2}C_{\text{CO}_2}}{C_{\text{CO}}C_{\text{H}_2O}}$$

(9)

$$K_{11} = \frac{C_{\text{CH}_4}C_{\text{H}_2O}}{C_{\text{CO}}C_{\text{CH}_4}}$$

(10)

For the water–gas shift reaction, the equilibrium constant was $5.15$ at $500^\circ$C and $2.68$ at $600^\circ$C. For methanation, the equilibrium constant was $3.62 \times 10^3$ L mol$^{-1}$ at $500^\circ$C and $1.02 \times 10^4$ L mol$^{-1}$ at $600^\circ$C. Additional details about these equilibrium constant calculations are available elsewhere.23

Figures 1 and 2 show the base case experimental results along with the model calculations for cellulose and lignin. Table 1 lists the rate constants. CO is rapidly formed in the initial minutes, reaches a maximum, and then is consumed at longer times. The yield of H$_2$ increases steadily for cellulose, whereas for lignin it increases more rapidly during the initial minutes. The model clearly captures the trends in the data and fits the temporal variation of the gas yields at the base case conditions very well for both cellulose and lignin.

In addition to adequately fitting the experimental data, one expects a kinetics model to use rate constants that have reasonable values. Of all the reactions in the model, only the water–gas shift reaction has been the subject of kinetics studies e.g.,26–28 in supercritical water. Only the work of Rice et al.,26 however, provides experimental kinetics data from studies that encompass a temperature ($500^\circ$C) and the water density (0.08 g/cm$^3$) used to determine the model parameters. Rice et al.26 measured the rate constant at 520 and $480^\circ$C for many different water concentrations (densities) and showed that the rate constant has a very strong density dependence. Using their data, we estimated rate constant values at 0.08 g/cm$^3$ for both 480 and $520^\circ$C. We then used these values and the Arrhenius equation to estimate the rate constant at 0.08 g/cm$^3$ and $500^\circ$C. The value we obtain is $1.5 \times 10^{-3}$ L mol$^{-1}$ min$^{-1}$, which is the same order of magnitude as the value we obtained by fitting the model to the cellulose gasification data at $500^\circ$C (see value for $k_{10}$ in Table 1). We consider this level of agreement with the literature to be very good, given that the water–gas shift rate constants from different experimental studies at a given temperature varied by as much as two orders of magnitude.28 We are aware of no kinetics studies of the water gas shift reaction at $600^\circ$C, so we cannot compare this value with previous experiments.

Table 1. Rate Constants at 500°C (Cellulose) and 600°C (Lignin)

<table>
<thead>
<tr>
<th>Rate Constant</th>
<th>Cellulose</th>
<th>Lignin</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_1$ (min$^{-1}$)</td>
<td>$2.00 \times 10^9$</td>
<td>$1.67 \times 10^7$</td>
</tr>
<tr>
<td>$k_2$ (min$^{-1}$)</td>
<td>$1.16 \times 10^4$</td>
<td>$5.00 \times 10^{-4}$</td>
</tr>
<tr>
<td>$k_3$ (L mol$^{-1}$ min$^{-1}$)</td>
<td>$0.00 \times 10^9$</td>
<td>$2.73 \times 10^{-3}$</td>
</tr>
<tr>
<td>$k_4$ (L mol$^{-1}$ min$^{-1}$)</td>
<td>$2.47 \times 10^{-1}$</td>
<td>$5.39 \times 10^{-1}$</td>
</tr>
<tr>
<td>$k_5$ (min$^{-1}$)</td>
<td>$4.25 \times 10^{-1}$</td>
<td>$7.67 \times 10^{-1}$</td>
</tr>
<tr>
<td>$k_6$ (min$^{-1}$)</td>
<td>$1.11 \times 10^{-1}$</td>
<td>$9.42 \times 10^{-1}$</td>
</tr>
<tr>
<td>$k_7$ (min$^{-1}$)</td>
<td>$2.68 \times 10^{-3}$</td>
<td>$0.00 \times 10^0$</td>
</tr>
<tr>
<td>$k_8$ (min$^{-1}$)</td>
<td>$4.65 \times 10^{-1}$</td>
<td>$9.38 \times 10^{-1}$</td>
</tr>
<tr>
<td>$k_9$ (min$^{-1}$)</td>
<td>$6.11 \times 10^{-3}$</td>
<td>$2.80 \times 10^{-3}$</td>
</tr>
<tr>
<td>$k_{10}$ (L mol$^{-1}$ min$^{-1}$)</td>
<td>$1.19 \times 10^{-3}$</td>
<td>$1.05 \times 10^{-3}$</td>
</tr>
<tr>
<td>$k_{10}$ (L mol$^{-1}$ min$^{-1}$)</td>
<td>$0.00 \times 10^0$</td>
<td>$7.71 \times 10^{-2}$</td>
</tr>
<tr>
<td>$k_{15}$ (L mol$^{-1}$ min$^{-1}$)</td>
<td>$0.00 \times 10^0$</td>
<td>$7.52 \times 10^{-6}$</td>
</tr>
</tbody>
</table>

Figure 3. Model predictions for gas yields from cellulose (10 min for wt %, 7.5 min for g/ml) and lignin SCWG (75 min for wt %, 60 min for g/ml).
One expects rate constants to increase as the temperature increases, but the water–gas shift rate constants from the model in Table 1 do not meet this expectation. We believe that this behavior results from uncertainty in the rate constant estimates rather than from actual non-Arrhenius behavior for this reaction. Given that the precise values obtained for the water–gas shift kinetics in the model depend on the values of all other parameters (because of the covariance between parameters) it is likely that, if desired, a set of parameters could have been obtained that included an Arrhenius dependence for water–gas shift. We did not consider this feature to be a requirement since it was not central to the purposes of our modeling effort.

Model validation

Having demonstrated that the model can fit the base case data for cellulose and lignin, we next test its predictive capabilities. In this section we use the model to predict the results of SCWG experiments done at the base case temperatures but different water densities or biomass loadings. We also use the model to predict equilibrium compositions for SCWG.

We used the model to predict the gas yields from SCWG at the base case temperatures but at different biomass loadings (5.0 and 33.3 wt %) and different water densities (0.00 g/ml, 0.05 g/ml, 0.18 g/ml). Figure 3 is a parity plot that compares the experimental and predicted yields. If the model predictions were perfect, all of the data would fall on the diagonal line shown. Figure 3 shows that the model can predict the results for most of the gas yields at the different biomass loadings for both cellulose and lignin with good proximity. The model seems to perform worst for the case of pyrolysis (0.00 water density). Even here, however, the model predictions often fall within the experimental uncertainty.

We next compare experimental results and model predictions regarding how the gas yields change with biomass loading and water density. For cellulose, the model predicts very little effect of the biomass loading on yields. This finding is in good agreement with experiments. Since there was no effect, we do not compare these results in a separate graph. For lignin, the biomass loading has a larger effect on some gas yields, as shown in Figure 4. The model captures the slight decreases in the H₂ and CO yields as the lignin loading increases, as well as the slight increase in CH₄. The CO₂ yield appears to remain loading invariant.

The effect of water density on gas yields is shown for cellulose in Figure 5 and for lignin in Figure 6. The model identifies the main trends for cellulose and lignin, matching the experimental trends reasonably well in most cases. The CO yield decreases with water density, while the H₂ yield increases. The CO₂ yield slightly increases with water density, and the CH₄ yield remains nearly unchanged. The
largest differences between experimental data and model predictions are for pyrolysis and at the highest water density, 0.18 g/ml (especially for cellulose). These differences are possibly because of the documented\textsuperscript{26,27} dependence of the water–gas shift kinetics on the water density. The model uses a rate constant for water–gas shift that is density independent.

Having tested the model by making predictions at different biomass loadings and water densities at different times, we now turn our attention to equilibrium. If the model includes the essential set of gas-phase reactions for SCWG, it should be able to predict the equilibrium product distributions. We simulated equilibrium SCWG by running the kinetics model to very long batch holding times (40,000 min for lignin), such that the yields became time invariant. That such a long reaction time was needed to reach equilibrium clearly indicates that the gaseous products were far from equilibrium at the much shorter reaction times investigated experimentally. Good catalysts for water–gas shift and methanation would be essential for reaching equilibrium more quickly.

We previously reported\textsuperscript{19} equilibrium compositions for lignin SCWG at the base case conditions based upon minimizing the Gibbs’ free energy of the system. We used the RGIBBS block in ASPEN Plus to perform the chemical equilibrium calculations. No experimental data were used in this calculation, and no specific chemical reactions were entered. Thus, comparing the model predictions with these earlier ASPEN calculations will assess whether the model includes enough information about the gas-phase reactions. Figure 7 shows that the model predictions agree extremely well with the thermodynamic chemical equilibrium calculations for lignin at the base case conditions (600°C). In both cases, H\textsubscript{2} and CO\textsubscript{2} are the major products (35–45% each), with about 25% of CH\textsubscript{4} and a very small mole % of CO.

It is important to make a note here about the water–gas shift reaction in SCW. Under more conventional gasification conditions, the water–gas shift reaction at this temperature would produce a much higher mole fraction of CO at equilibrium. In SCW, however, equilibrium is shifted strongly in the direction of CO consumption. Thus, SCWG could be very useful for making H\textsubscript{2} with a very low CO content (e.g., for use in PEM fuel cells).

This section showed that the kinetics model can predict the outcomes of experiments for a range of biomass loadings and water densities, and that equilibrium predictions also agree with thermodynamic calculations. Additionally, Resende\textsuperscript{13} showed that the model predictions for the effects of biomass loading and water density on the equilibrium compositions agreed reasonably well with the results from Gibbs free energy minimization. These successes indicate that the reactions included in the model and the parameter estimates are adequate for describing the noncatalytic SCWG of lignin and cellulose under the conditions explored herein.
Reaction rate analysis

The previous sections showed that the model could faithfully reproduce the data used to determine its parameters and that it could predict gas yields and compositions at SCWG conditions not used in the parameter estimation. We now use the model to identify the individual reactions most responsible for the formation and consumption of each gas species during the course of noncatalytic SCWG. More specifically, we calculated the rate of each reaction in the model and then compared the rates for all reactions that produce or consume a specific gaseous product. We show results (Fig. 8–12) for all four gases for cellulose SCWG, but only for H2 for lignin SCWG. The reactions with the highest rates for CO, CO2, and CH4 production were the same for both lignin and cellulose.

Inspection of Figures 8–12 reveal that SCWG at the base case conditions can be viewed as occurring in two distinct temporal regions. At short times (the first few minutes), the gas formation rates reach their highest values. Beyond the first few minutes, the gas production rate is always lower, and the dominant reactions are ones that primarily change the product distribution. For H2, the high rates of formation in the first minutes are because of steam reforming. Steam reforming I (forming CO) dominates for cellulose, whereas steam reforming II (forming CO2) dominates for lignin. In both cases, the rate of steam reforming quickly decreases after a few minutes, and the forward rate of the water-gas shift reaction becomes the fastest producer of H2 at longer periods of time. After reaching a maximum at about 7–8 minutes, the rate of water-gas shift slowly decreases with time. The model results show that the other gas species originate primarily from the collection of lumped intermediates. Direct formation of CH4 from the intermediate is the most important reaction for CH4 formation. It appears that a catalyst would be required for the rate of methanation to proceed at a competitive rate. The lumped intermediates are also the main source of CO. Smaller contributions arise from steam reforming I. The model also indicates that the water-gas shift reaction consumes CO at longer times. The CO2 originates from intermediates during the first few minutes, but it can also be formed at much smaller rates from water-gas shift at longer times. A key result from this reaction rate analysis is the importance of gas-forming reactions from the numerous intermediate compounds.

Sensitivity analysis

A second tool to examine the relative importance of different reaction paths is sensitivity analysis. It reveals how
the predictions of a model (concentration of species $i$ ($C_i$) in this case) change when the value of a single model parameter (rate constants ($k_j$) in this case) is slightly perturbed. The normalized sensitivity coefficient, $S_{ij}$, captures this influence of the parameter $k_j$ on the outcome, and it can be defined as in Eq. 11:

$$S_{ij} = \frac{\partial \ln C_i}{\partial \ln k_j} = \frac{\Delta C_i / C_i}{\Delta k_j / k_j}$$

We calculated the sensitivity coefficients manually by perturbing each rate constant by 5% one at a time, running the kinetics model, and recording $\Delta C_i$ for each gaseous product for each case. The reaction rate analysis showed that different reactions dominate noncatalytic SCWG at short times and at longer times. Therefore, we examined the sensitivities at both short times (1 min) and long times (30 min for cellulose and 75 minutes for lignin). Tables 2 and 3 show the results and only sensitivity coefficients with an absolute value exceeding 0.1 are included. These reactions are the ones in which the relative change in gas concentration was at least 10% as large as the relative change in the rate constant.

At 1 min, the concentrations of CO, CO$_2$, and CH$_4$ from both lignin and cellulose are most sensitive to the rate of formation of these gases from the many lumped intermediate compounds. The sensitivity coefficients are nearly equal to unity. Their positive value means that increasing the rate constant for one of these reactions will increase the calculated gas concentration. This result is an important one because it indicates that the hydrothermal reactions of intermediate compounds are very important for producing gases via noncatalytic SCWG. The concentration of H$_2$ at 1 min from both lignin and cellulose was most sensitive to the rate constants for steam reforming.

At long times, the concentrations of CO, CO$_2$, and CH$_4$ still displayed strong sensitivity to the rate constants for their formation from intermediates, but there was often an even stronger sensitivity to the rate constant for the reaction wherein intermediates formed char. Likewise, the H$_2$ concentration at long times showed a large sensitivity to the rate constant for char formation, but it was also sensitive to the water–gas shift kinetics and the rate constant for CO formation from intermediates. Of course, CO is a reactant in the water–gas shift reaction, so these latter two sensitivities are related. A key result from this sensitivity analysis at long times is that the competition between char formation and gas formation has a profound influence on the gas yields from noncatalytic SCWG of lignin and cellulose. Again we see the hydrothermal reactions of the species lumped together as intermediates in this model being central to the determination of gas yields and compositions.

**Conclusions**

(1) This article presents the first quantitative kinetics model for gas production from noncatalytic SCWG of biomass components. The set of 11 reactions and the concept of a generic reactive intermediate proved sufficient for fitting the base case experimental data for the cellulose and lignin samples investigated and predicting gas concentrations at different biomass loadings and water densities. The model’s equilibrium predictions agree with

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**Table 2. Sensitivity Coefficients for Cellulose SCWG at Base Case Conditions**

<table>
<thead>
<tr>
<th>Reaction</th>
<th>CO</th>
<th>CO$_2$</th>
<th>CH$_4$</th>
<th>H$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1 min</td>
<td>30 min</td>
<td>1 min</td>
<td>30 min</td>
</tr>
<tr>
<td>Intermediate Formation</td>
<td>0.225</td>
<td>–</td>
<td>0.230</td>
<td>–</td>
</tr>
<tr>
<td>Steam-Reforming I</td>
<td>0.177</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Steam-Reforming II</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>CO from Intermediate</td>
<td>0.887</td>
<td>0.873</td>
<td>–</td>
<td>0.216</td>
</tr>
<tr>
<td>CO$_2$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>0.993</td>
<td>0.753</td>
</tr>
<tr>
<td>CH$_4$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>H$_2$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Char Formation</td>
<td>–0.131</td>
<td>–0.008</td>
<td>–0.129</td>
<td>–0.931</td>
</tr>
<tr>
<td>Water-gas Shift</td>
<td>–</td>
<td>–0.678</td>
<td>–</td>
<td>0.166</td>
</tr>
<tr>
<td>Methanation</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

**Table 3. Sensitivity Coefficients for Lignin SCWG at Base Case Conditions**

<table>
<thead>
<tr>
<th>Reaction</th>
<th>CO</th>
<th>CO$_2$</th>
<th>CH$_4$</th>
<th>H$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1 min</td>
<td>75 min</td>
<td>1 min</td>
<td>75 min</td>
</tr>
<tr>
<td>Intermediate Formation</td>
<td>0.496</td>
<td>–</td>
<td>0.501</td>
<td>–</td>
</tr>
<tr>
<td>Steam-Reforming I</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Steam-Reforming II</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>CO from Intermediate</td>
<td>0.963</td>
<td>0.930</td>
<td>–</td>
<td>0.247</td>
</tr>
<tr>
<td>CO$_2$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>0.868</td>
<td>0.646</td>
</tr>
<tr>
<td>CH$_4$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>H$_2$ from Intermediate</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Char Formation</td>
<td>–0.635</td>
<td>–0.884</td>
<td>–0.637</td>
<td>–0.930</td>
</tr>
<tr>
<td>Water-gas Shift</td>
<td>–</td>
<td>–0.844</td>
<td>–</td>
<td>0.160</td>
</tr>
<tr>
<td>Methanation</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

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thermodynamic calculations, and the rate constants obtained for the water–gas shift reaction are in the same range as values reported from careful investigations of this reaction in supercritical water. This modeling framework may be useful for SCWG of other biomass materials and for catalyzed SCWG systems.

The model showed that the identities of the fastest SCWG reaction paths differ at short times and at longer times. Paths responsible for gas formation from intermediates are most important at short times, whereas paths that redistribute the different gases (e.g., water gas shift) become most important at longer times.

(3) H₂ is mostly formed via steam-reforming at short times and from water–gas shift at longer times, CO₂ and CH₄ on the other hand, form predominantly via hydrothermal reactions of the many intermediate species. Steam reforming is not the major contributor to either CO or CO₂.

(4) The model results show clearly that the reactions of intermediates, compounds smaller than the biomass monomer but larger than the C₁ gases, largely determine the outcome of noncatalytic SCWG. Therefore, improved knowledge about the reactions of small organic compounds under SCWG conditions could lead to an improved understanding of the key aspects of the operative chemistry.

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Literature Cited


