# CHRYSLER / UMTRI 

## WIND-STEER VEHICLE SIMULATION

Reference Manual<br>Version 1.0<br>(Volume II of II)

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## Notice

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## REFERENCE MANUAL

This document constitutes the primary technical reference for the Chrysler / UMTRI Wind-Steer vehicle simulation model. A separate User's Manual (Volume I) accompanies this document and is used as the primary guide for using and interacting with the WindSteer model.

The Reference Manual is intended to provide detailed background material for the model showing the equations, computer source code, and nomenclature. The material is presented in the form of five appendices (A through E). Appendix A describes and defines the nomenclature used in the model. Appendix B describes the basic equations used by the model. Appendic C discusses the programming details necessary for understanding and modifying the computer code. Appendix D contains the FORTRAN 77 source code used in implementing the model on both Apple Macintosh and IBM PC / compatibles personal computers. Lastly, Appendix E provides two technical papers [references 2 and 3] used to document the driver steering control model contained in the program.

## APPENDIX A-NOMENCLATURE

## Subscripts

$1=$ Front Axle $\quad 2=$ Rear Axle $\quad \mathrm{L}=$ Left $\quad \mathrm{R}=$ Right

## Variables and Parameters

Symbols refer to parameters unless they are identified as being variable
$\mathrm{A}_{\mathrm{y}}=$ [Variable] Lateral acceleration of vehicle center-of-mass, perpendicular to longitudinal vehicle axis and parallel to ground
$\mathrm{a}=$ Distance from front axle to total vehicle center of mass
$a_{s}=$ Distance from front axle to center of mass of the sprung mass
$\mathrm{b}=$ Distance from total vehicle center of mass to rear axle
$C_{p}=$ Steering boost coefficient
$\mathrm{C}_{\mathrm{v}}=$ Steering damping coefficient
$\mathrm{C}_{\alpha}=$ [Variable] Cornering stiffness for slip, defined as $\partial \mathrm{F}_{\mathrm{Y}} / \partial \alpha$
$\mathrm{C}_{\boldsymbol{\gamma}}=$ [Variable] Cornering stiffness for camber, defined as $\partial \mathrm{F} / \partial \gamma$
$\mathrm{C}_{\mathrm{M} \alpha}=$ [Variable] Aligning stiffness, defined as $\partial \mathrm{M}_{\mathrm{Z}} / \partial \alpha$
$D_{j 1}, D_{j 2}=$ Damping coeficient for jounce for front and rear shock absorbers
$D_{\mathrm{r} 1}, D_{\mathrm{r} 2}=$ Damping coeficient for rebound for front and rear shock absorbers
$\mathrm{F}_{\mathrm{D}}=$ [Variable] Suspension jounce / rebound damping force (additional subscripts indicate which wheel)
$\mathrm{F}_{\mathrm{Y}}=$ [Variable] Tire-generated side force (additional subscripts indicate which wheel)
$\mathrm{F}_{\mathrm{YA}}=$ [Variable] Aerodynamic side force
$\mathrm{F}_{\mathrm{ZA}}=$ [Variable] Aerodynamic vertical force
$h_{1}, h_{2}=$ Height of nominal front and rear roll centers
$\mathrm{h}_{\mathrm{sm}}=$ Nominal height of sprung-mass center of mass
$\mathrm{h}_{\mathrm{ra}}=$ [Variable] Vertical distance between the sprung-mass center of mass and the instant roll axis
$\mathrm{h}_{\mathrm{rc} 1}, \mathrm{~h}_{\mathrm{rc} 2}=$ [Variable] Vertical distance between center-of-mass of the sprung mass and the instant front and rear roll centers
$\mathrm{I}_{\mathrm{xs}}=$ [Variable] Instant moment of inertia of sprung mass about roll axis
$\mathrm{I}_{\mathrm{xx}}=$ Moment of inertia of sprung mass about longitudinal ( x ) axis
$\mathrm{I}_{\mathrm{xz}}=$ Cross product of inertia of sprung mass for $\mathrm{x}, \mathrm{z}$ directions

```
    I
    K
    K
K}\mp@subsup{\textrm{Irl}}{1}{},\mp@subsup{\textrm{K}}{\textrm{rr2}}{2}=\mathrm{ Auxiliary roll rate (beyond rate due to vertical springs), for front and rear
    axles (without effects of tire compliance)
K
K
    K}\mp@subsup{K}{\phi}{}=\mathrm{ Total roll stiffness of suspensions and tires acting on sprung mass
    L}=\mathrm{ Wheelbase (a+b)
M
                "backward" path, resolved as a motion-resisting moment about the front-
        wheel kingpins
    M
        moment about the front-wheel kingpins
    M
        assisting or motion-resisting moment about the front-wheel kingpins
    M
        and boost
    M
        valve)
    M XA = [Variable] Aerodynamic roll moment acting on vehicle
    MYA = [Variable] Aerodynamic pitch moment acting on vehicle
    M
        referenced)
    M
    m
    m}=\mathrm{ Total mass
    p = [Variable] Roll rate
    Q= Aerodynamic pressure, \rho V VA
    q = [Variable] Pitch rate
    r = [Variable] Yaw rate
t},\mp@subsup{t}{2}{}=\mathrm{ Half-track distances for front and rear of vehicle (centerline of vehicle to
        centerline of tire)
    V= Vehicle speed (constant)
    V
```

$\mathrm{V}_{\text {wind }}=$ [Variable $]$ Absolute wind speed
$\mathrm{w}=$ [Variable] Vertical velocity of sprung mass
$\mathrm{X}=$ [Variable] absolute (inertial) X coordinate of vehicle center-of-mass
$\mathrm{Y}=$ [Variable] absolute (inertial) Y coordinate of vehicle center-of-mass
$\mathrm{y}_{\mathrm{ra}}=$ [Variable $]$ Lateral distance between instant roll axis and sprung-mass center of mass
$\mathrm{y}_{\mathrm{rc} 1}, \mathrm{y}_{\mathrm{rc} 2}=$ [Variable] Lateral distance between center-of-mass of the sprung mass and the instant front and rear roll centers
$\alpha=$ [Variable] Tire slip angle (subscripts indicate referenced tire)
$\alpha_{10}, \alpha_{20}=$ Static tire slip angles for front and rear axles
$\beta=$ [Variable] Vehicle slip angle
$\beta_{\mathrm{a}}=$ [Variable] Aerodynamic slip angle
$\delta_{\mathrm{G}}=$ [Variable] Front-wheel steering angle displacement, before adjusting for lash
$\delta_{\mathrm{FW}}=$ [Variable] Average front-wheel steering angle displacement
$\delta_{\text {Lash }}=$ Total steering system lash resolved to an angle about front-wheel kingpins
$\varepsilon_{2}=$ Roll steer coeficient for beam-type rear suspension
$\phi=$ [Variable] Roll of sprung mass relative to baseline trim condition
$\gamma=$ [Variable] Tire camber angle (subscripts indicate referenced tire)
$\gamma_{10}, \gamma_{20}=$ Static tire camber angles for front and rear axles
$\mu_{1}, \mu_{2}=$ Nondimensional parameters that reduce the effective suspension stiffness to account for tire vertical compliance
$\theta=$ [Variable] Pitch of sprung mass relative to baseline trim condition
$\rho=$ Density of air OR
$\rho=$ [Variable] Instantaneous path curvature of vehicle, at the center of mass
$\psi=$ [Variable] Vehicle yaw (heading) angle relative to inertial frame
$\psi_{\text {wind }}=$ [Variable] Absolute wind direction ( $180^{\circ}$ from meteorology convention)
$\mathrm{z}=$ [Variable] Vertical displacement of vehicle sprung mass
$\mathrm{z}_{1 \mathrm{~L}}=$ [Variable] Vertical displacement at left front suspension point
$\mathbf{z}_{1 \mathrm{R}}=$ [Variable $]$ Vertical displacement at right front suspension point
$z_{2 L}=$ [Variable] Vertical displacement at left rear suspension point
$\mathrm{z}_{2 \mathrm{R}}=$ [Variable $]$ Vertical displacement at right rear suspension point
$\mathrm{I}_{\text {ss }}=$ Steering wheel $/$ upper column rotational inertia
$\mathrm{K}_{\mathrm{sc}}=$ Steering column stiffness
$\mathrm{K}_{\mathrm{SL}}=$ Steering linkage stiffness (one side)

$$
\begin{aligned}
\mathrm{K}_{\mathrm{SS}} & =\text { Effective (lumped) steering system stiffness based on } \mathrm{K}_{\mathrm{sc}} \text { and } \mathrm{K}_{\mathrm{SL}} \\
\mathrm{GR} & =\text { Overall gear ratio of steering system } \\
\delta_{\mathrm{sw}} & =[\text { Variable }] \text { Steering wheel rotational displacement } \\
\delta_{\mathrm{fw}} & =[\text { Variable }] \delta_{\mathrm{sw}} / \mathrm{GR} \\
\mathrm{C}_{\mathrm{L}} & =\text { Aerodynamic lift coefficient } \\
\mathrm{C}_{\mathrm{D}} & =\text { Aerodynamic drag coefficient } \\
\mathrm{C}_{\mathrm{M}} & =\text { Aerodynamic pitch moment coefficient } \\
\mathrm{K}_{\mathrm{L}} & =\text { Aerodynamic coefficient for lift force variation due to } \beta_{\mathrm{a}} 2 \\
\mathrm{~K}_{\mathrm{D}} & =\text { Aerodynamic coefficient for drag force variation due to } \beta_{\mathrm{a}} 2 \\
\mathrm{~K}_{\mathrm{Y}} & =\text { Aerodynamic side force coefficient } \\
\mathrm{K}_{\mathrm{N}} & =\text { Aerodynamic yaw moment coefficient } \\
\mathrm{K}_{\mathrm{R}} & =\text { Aerodynamic roll coefficient } \\
\mathrm{K}_{\mathrm{M}} & =\text { Aerodynamic coefficient for pitch moment variation due to } \beta_{\mathrm{a}}{ }^{2} \\
\mathrm{~A} & =\text { Aerodynamic cross sectional area }
\end{aligned}
$$

## APPENDIX B-EQUATIONS OF MOTION

The constant-speed vehicle model includes a total of six dynamic degrees of freedom that are important for simulating the handling response of a passenger car to steer and wind inputs for non-limit maneuvers (lateral acceleration levels less than 0.3 g 's). Twelve state variables are used to define the kinematics of the vehicle and follow the SAE recommended practice sign convention [7]:

X X inertial forward coordinate of vehicle center of mass
Y Y inertial lateral coordinateof vehicle center of mass
z Z inertial vertical coordinate of vehicle sprung mass
$\phi$ Euler roll angle of sprung mass
$\theta$ Euler pitch angle of sprung mass
$\psi$ Euler yaw angle of total vehicle
p Roll angle rate of sprung mass (in body axis coordinate system)
q Pitch angle rate of sprung mass (in body axis coordinate system)
r Yaw angle rate of sprung mass (in body axis coordinate system)
$\beta$ Side slip angle of vehicle $c$. g.
w Vertical displacement rate of sprung mass (in body axis coordinate system)
$\delta_{\mathrm{FW}}$ Average steer angle of front wheels
Independent steer, camber, and vertical motions are included for each wheel. These motions are treated as being in static equilibrium, thereby eliminating the numerical integration of the differential equations representing the high-frequency ( 10 to 15 Hz ) mechanical resonances of the unsprung masses.

## B. 1 Body Equations

## B.1.1 Kinematical Relationships

The derivatives of the inertial X and Y coordinates of the vehicle center of mass are related to the constant forward speed and vehicle rotation:

$$
\begin{align*}
\dot{X} & =V \cos (\psi+\beta)  \tag{B.1.1-1}\\
\dot{Y} & =V \sin (\psi+\beta) \tag{B.1.1-2}
\end{align*}
$$

The following four state variables are speeds defined as derivatives of other state variables:

$$
\begin{align*}
& \mathrm{w}=\dot{\mathrm{z}}  \tag{B.1.1-3}\\
& \mathrm{p}=\dot{\phi}  \tag{B.1.1-4}\\
& \mathrm{q}=\dot{\theta} \tag{B.1.1-5}
\end{align*}
$$

$$
\begin{equation*}
\mathrm{r}=\dot{\psi} \tag{B.1.1-6}
\end{equation*}
$$

Two useful variables that are derived from the yaw rotation rates are the lateral acceleration and the path curvature of the vehicle center of mass:

$$
\begin{gather*}
A_{y}=\frac{V(r+\beta)}{g}  \tag{B.1.1-7}\\
\rho=\frac{r+\beta}{V} \tag{B.1.1-8}
\end{gather*}
$$

## B.1.2 Force / Moment Equilibrium Equations

The following sums combine the external forces and moments applied the tires and the aerodynamic effect:

$$
\begin{gather*}
\sum \mathrm{F}_{\mathrm{Y}}=\mathrm{F}_{\mathrm{Y}_{1 \mathrm{~L}}}+\mathrm{F}_{\mathrm{Y}_{1 \mathrm{R}}}+\mathrm{F}_{\mathrm{Y}_{\mathcal{L}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}}}+\mathrm{F}_{\mathrm{YA}}  \tag{B.1.2-1}\\
\sum \mathrm{~F}_{\mathrm{Z}}=\mathrm{F}_{\mathrm{Z}_{\mathrm{LL}}}+\mathrm{F}_{\mathrm{Z}_{1 \mathrm{R}}}+\mathrm{F}_{\mathrm{Z}_{\mathrm{L}}}+\mathrm{F}_{\mathrm{Z}_{2 \mathrm{R}}}-\mathrm{F}_{\mathrm{ZA}}  \tag{B.1.2-2}\\
\sum \mathrm{M}_{\mathrm{Z}}=\mathrm{M}_{\mathrm{Z}_{\mathrm{LL}}}+\mathrm{M}_{\mathrm{Z}_{1 \mathrm{R}}}+\mathrm{M}_{\mathrm{Z}_{\mathrm{L}}}+\mathrm{M}_{\mathrm{Z}_{2 \mathrm{R}}}+\mathrm{M}_{\mathrm{ZAA}} \\
+\mathrm{a}\left(\mathrm{~F}_{\mathrm{Y}_{\mathrm{LL}}}+\mathrm{F}_{\mathrm{Y}_{1 \mathrm{R}}}-\mathrm{b}\left(\mathrm{~F}_{\mathrm{Y}_{\mathcal{L}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}}}\right)+\left(\mathrm{a}-\frac{\mathrm{L}}{2}\right) \mathrm{F}_{\mathrm{YA}}\right. \tag{B.1.2-3}
\end{gather*}
$$

Five equilibrium equations can be written for this vehicle model by balancing the applied forces and moments with D'Alembert's forces and torques. The summation of lateral force and yaw moment are applied about the entire vehicle, whereas the pitch and roll moments and the vertical force are applied only for the sprung mass. As implied by the form of the following equations, these relations are used to evaluate the accelerations.

$$
\begin{align*}
& \mathrm{I}_{\mathrm{XS}} \dot{\mathrm{p}}=-\mathrm{I}_{\mathrm{XZ}} \dot{\mathrm{r}}-\mathrm{m}_{\mathrm{s}} \mathrm{~h}_{\mathrm{ra}} V(\mathrm{r}+\dot{\beta})+\mathrm{m}_{\mathrm{s}} \mathrm{~g} \mathrm{y}_{\mathrm{ra}}-\mathrm{K}_{\phi} \phi+\mathrm{t}_{1}\left(\mathrm{~F}_{\mathrm{D}_{\mathrm{IL}}}-\mathrm{F}_{\mathrm{D}_{1 R}}\right)  \tag{B.1.2-4}\\
& +t_{2}\left(F_{D_{2}}-F_{D_{2 R}}\right)+M_{X A}-h_{s m} F_{Y A} \\
& \beta=\frac{-m_{s} h_{\text {ra }} \dot{p}+\sum F_{Y}}{m V}-r  \tag{B.1.2-5}\\
& t=\frac{-\mathrm{I}_{X Z} \dot{\mathrm{p}}+\sum \mathrm{M}_{Z}}{\mathrm{I}_{Z Z}}  \tag{B.1.2-6}\\
& \mathrm{w}=\frac{\mathrm{mg}-\sum \mathrm{F}_{\mathrm{Z}}}{\mathrm{~m}_{\mathrm{s}}}  \tag{B.1.2-7}\\
& \mathrm{a}\left[2 \mu_{1} \mathrm{~K}_{\mathrm{S} 1}(\mathrm{z}-\mathrm{a} \theta)+\mathrm{F}_{\mathrm{D}_{\mathrm{LL}}}+\mathrm{F}_{\mathrm{D}_{1 R}}\right] \\
& q=\frac{-b\left[2 \mu_{2} K_{S 2}(z+b \theta)+F_{D_{2 L}}+F_{D_{2 R}}\right]+M_{Y A}+\left(\frac{L}{2}-a_{s}\right) F_{Z A}}{I_{Y S}} \tag{B.1.2-8}
\end{align*}
$$

As written above, the first three of these equations are coupled in such a way that they cannot be evaluated sequentially in a computer program. That is, the terms $\dot{p}, \beta$, and $\dot{r}$ appear on both sides of eqs. B.1.2-4 through B.1.2-6. By substituting eqs. B.1.2-5 and
B.1.2-6 into B.1.2-4, an alternative expression for $\dot{p}$ is obtained which is not dependent on $\beta$ or $\dot{r}$ :

$$
\begin{gather*}
\mathrm{m}_{\mathrm{s}} \mathrm{~g} \mathrm{y}_{\mathrm{ra}}-\frac{\mathrm{I}_{\mathrm{XZ}}}{\mathrm{I}_{Z Z}} \sum \mathrm{M}_{Z}-\mathrm{K}_{\phi} \phi+\mathrm{M}_{\mathrm{XA}}-\mathrm{h}_{\mathrm{sm}} \mathrm{~F}_{\mathrm{YA}} \\
\mathrm{p}=\frac{-\frac{\mathrm{m}_{\mathrm{s}} h_{\mathrm{ra}}}{\mathrm{~m}} \sum \mathrm{~F}_{\mathrm{Y}}+\mathrm{t}_{1}\left(\mathrm{~F}_{\mathrm{D}_{\mathrm{LL}}}-\mathrm{F}_{\mathrm{D}_{1 \mathrm{R}}}\right)+\mathrm{t}_{2}\left(\mathrm{~F}_{\mathrm{D}_{\mathrm{L}}}-\mathrm{F}_{\mathrm{D}_{2 \mathrm{R}}}\right)}{\mathrm{I}_{\mathrm{XS}}-\frac{\mathrm{m}_{\mathrm{s}}^{2} \mathrm{~h}_{\mathrm{ra}}^{2}}{\mathrm{~m}}-\frac{\mathrm{I}_{\mathrm{XZ}}^{2}}{\mathrm{I}_{Z Z}}} \tag{B.1.2-9}
\end{gather*}
$$

This expression is used (rather than eq. B.1.2-4) to evaluate $\dot{\mathrm{p}}$. The known value of $\dot{\mathrm{p}}$ is then used in eqs. B.1.2-5 and B.1.2-6 to evaluate $\beta$ and $\dot{\mathrm{r}}$.

## B. 2 Aerodynamic Forces and Moments

The equations for computing aerodynamic forces and moments were presented in Section 2.2. The aerodynamic slip angle $\left(\beta_{\mathrm{a}}\right)$ and speed $\left(\mathrm{V}_{\mathrm{A}}\right)$, required for those equations are:

$$
\begin{gather*}
V_{a x}=V_{\text {wind }} \cos \left(\psi_{\text {wind }}-\psi\right)-V \cos (\beta)  \tag{B.2-1}\\
V_{a y}=V_{\text {wind }} \sin \left(\psi_{\text {wind }}-\psi\right)-V \sin (\beta)  \tag{B.2-2}\\
V_{a}=\sqrt{V_{a x}^{2}+V_{a y}^{2}}  \tag{B.2-3}\\
\beta_{a}=\tan ^{-1}\left(\frac{V_{a x}}{V_{a y}}\right)-\pi ; V_{a y}>0  \tag{B.2-4}\\
\beta_{a}=\tan ^{-1}\left(\frac{V_{a x}}{V_{a y}}\right)+\pi ; V_{a y}<0 \tag{B.2-5}
\end{gather*}
$$

The areodynamic forces and moments are, again, as in Section 2.2:

$$
\begin{gather*}
Q=\frac{\rho V_{A}^{2}}{2}  \tag{B.2-6}\\
F_{X A}=Q A\left(C_{D}+K_{D} \beta_{a}^{2}\right)  \tag{B.2-7}\\
F_{Y A}=-Q A K_{Y} \beta_{a}  \tag{B.2-8}\\
F_{Z A}=-Q A\left(C_{L}+K_{L} \beta_{a}^{2}\right)  \tag{B.2-9}\\
M_{X A}=-Q A L K_{R} \beta_{a}  \tag{B.2-10}\\
M_{Y A}=-Q A L\left(C_{M}+K_{M} \beta_{a}^{2}\right)  \tag{B.2-11}\\
M_{Z A}=-Q A L K_{N} \beta_{a} \tag{B.2-12}
\end{gather*}
$$

## B. 3 Suspension / Wheel Terms

## B.3.1 Vertical Displacements

The tire slip and camber angles are influenced by the following suspension deflections

$$
\begin{align*}
& z_{1 L}=z-a \theta-t_{1} \phi  \tag{B.3.1-1}\\
& z_{1 R}=z-a \theta+t_{1} \phi  \tag{B.3.1-2}\\
& z_{2 L}=z+b \theta-t_{2} \phi  \tag{B.3.1-3}\\
& z_{2 R}=z+b \theta+t_{2} \phi \tag{B.3.1-4}
\end{align*}
$$

The above expressions neglect vertical tire deflection. The effects of tire compliance are included by reducing the forces caused by the above deflections.

## B.3.2 Effective Stiffness and Damping Values

All suspension springs in the vehicle model are linear. These include the vertical spring rates at each wheel, the auxiliary roll stiffness for the front and rear axles, and the tire vertical spring rates. The vertical motions of the wheels (acting against the tire vertical stiffness) is not computed in this model. Instead, the tire compliance values are used to lower the spring and damping rates of the suspension so that the vertical force, roll moment, and pitch moment acting on the sprung mass take into account the tire vertical deflections.

Effects of vertical spring and damper coefficients are reduced by the proportion of the overall vertical wheel movement that is due to the tire compliance

$$
\begin{align*}
\mu_{1} & =\frac{\mathrm{K}_{\mathrm{T} 1}}{\mathrm{~K}_{\mathrm{T} 1}+\mathrm{K}_{\mathrm{S} 1}}  \tag{B.3.2-1}\\
\mu_{2} & =\frac{\mathrm{K}_{\mathrm{T} 2}}{\mathrm{~K}_{\mathrm{T} 2}+\mathrm{K}_{\mathrm{S} 2}} \tag{B.3.2-2}
\end{align*}
$$

The effective auxiliary roll stiffnesses for the front and rear axles are also reduced due to tire compliance

$$
\begin{align*}
& K_{A u x 1}=\frac{2 t_{1}^{2} K_{T 1}\left(2 t_{1}^{2} K_{S 1}+K_{\pi 1}\right)}{2 t_{1}^{2}\left(K_{T 1}+K_{S 1}\right)+K_{\pi 1}}-2 \mu_{1} t_{1}^{2} K_{S 1}  \tag{B.3.2-3}\\
& K_{A u x 2}=\frac{2 t_{2}^{2} K_{T 2}\left(2 t_{2}^{2} K_{S 2}+K_{\Pi 2}\right)}{2 t_{2}^{2}\left(K_{T 2}+K_{S 2}\right)+K_{\pi 2}}-2 \mu_{2} 亡_{2}^{2} K_{S 2} \tag{B.3.2-4}
\end{align*}
$$

A single stiffness applies to the roll motions of the sprung mass.

$$
\begin{equation*}
K_{\phi}=2 \mu_{1} K_{S 1} t_{1}^{2}+2 \mu_{2} K_{S 2} t_{2}^{2}+K_{A u x 1}+K_{A u x 2} \tag{B.3.2-5}
\end{equation*}
$$

## B.3.3 Vertical Damping Forces

A bi-directional shock absorber model is used. A linear damping coefficient is used with different values for jounce and rebound, as indicated by the subscripts $\mathrm{j} / \mathrm{r}$. The
nondimensional coefficients $\mu_{1}$ and $\mu_{2}$ are used to reduce the suspension motion by the amount of the tire deflection.

$$
\begin{align*}
& \mathrm{F}_{\mathrm{D}_{\mathrm{L}}}=\mu_{1} \mathrm{D}_{(\mathrm{j} / \mathrm{r}) 1}\left[\mathrm{w}-\mathrm{a} \theta-\mathrm{t}_{1} \mathrm{p}\right]  \tag{B.3.3-1}\\
& \mathrm{F}_{\mathrm{D}_{1 \mathrm{R}}}=\mu_{1} \mathrm{D}_{(\mathrm{j} / \mathrm{r}) 1}\left[\mathrm{w}-\mathrm{a} \theta+\mathrm{t}_{1} \mathrm{p}\right]  \tag{B.3.3-2}\\
& \mathrm{F}_{\mathrm{D}_{\mathrm{L}}}=\mu_{2} \mathrm{D}_{(\mathrm{j} / \mathrm{r}) 2}\left[\mathrm{w}+\mathrm{b} \theta-\mathrm{t}_{2} \mathrm{p}\right]  \tag{B.3.3-3}\\
& \mathrm{F}_{\mathrm{D}_{2 \mathrm{R}}}=\mu_{2} \mathrm{D}_{(\mathrm{j} / \mathrm{r}) 2}\left[\mathrm{w}+\mathrm{b} \theta+\mathrm{t}_{2} \mathrm{p}\right] \tag{B.3.3-4}
\end{align*}
$$

## B.3.4 Vertical Ground Loads

The tire forces and moments are influenced by vertical load. The vertical loads for each tire are defined as follows:

$$
\begin{align*}
& \mathrm{F}_{\mathrm{Z}_{\mathrm{LL}}}=\frac{1}{2}\left[\frac{\mathrm{bmg}}{\mathrm{~L}}-\frac{\mathrm{K}_{\text {Aux } 1} \phi-\mathrm{h}_{\mathrm{rc}}\left(\mathrm{~F}_{\mathrm{Y}_{1 \mathrm{~L}}}+\mathrm{F}_{\mathrm{Y}_{1 \mathrm{R}}}\right]}{\mathrm{t}_{1}}\right]+\mathrm{F}_{\mathrm{D}_{1 \mathrm{~L}}}+\mu_{1} \mathrm{z}_{1 \mathrm{~L}} \mathrm{~K}_{\mathrm{S} 1}  \tag{B.3.4-1}\\
& F_{Z_{1 R}}=\frac{1}{2}\left[\frac{b m g}{L}+\frac{\mathrm{K}_{A u x 1} \phi-h_{r c l}\left(F_{Y_{1 L}}+F_{Y_{1 R}}\right)}{t_{1}}\right]+F_{D_{1 R}}+\mu_{1} z_{1 R} K_{S 1}  \tag{B.3.4-2}\\
& \mathrm{~F}_{\mathrm{Z}_{\mathrm{I}}}=\frac{1}{2}\left[\frac{\mathrm{amg}}{\mathrm{~L}}-\frac{\mathrm{K}_{\mathrm{Aux} 2} \phi-\mathrm{h}_{\mathrm{rc}}\left(\mathrm{~F}_{\mathrm{Y}_{\mathrm{Z}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}}}\right]}{\mathrm{t}_{2}}\right]+\mathrm{F}_{\mathrm{D}_{2 \mathrm{~L}}}+\mu_{2} \mathrm{Z}_{2 \mathrm{~L}} \mathrm{~K}_{\mathrm{S} 2}  \tag{B.3.4-3}\\
& \mathrm{~F}_{\mathrm{Z}_{2 R}}=\frac{1}{2}\left[\frac{\mathrm{amg}}{\mathrm{~L}}+\frac{\mathrm{K}_{\mathrm{Aux} 2} \phi-\mathrm{h}_{\mathrm{rc} 2}\left(\mathrm{~F}_{\mathrm{Y}_{\mathrm{Z}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}} \mathrm{R}}\right)}{\mathrm{t}_{2}}\right]+\mathrm{F}_{\mathrm{D}_{2 \mathrm{R}}}+\mu_{2} \mathrm{z}_{2 \mathrm{R}} \mathrm{~K}_{\mathrm{S} 2} \tag{B.3.4-4}
\end{align*}
$$

## B. 4 Roll Axis

The suspension kinematics are simplified by assuming that the sprung mass rotates about a roll axis. To extend this representation, the axis is permitted to move as a function of roll angle. The roll axis is located by two points, each in the vertical plane containing each axle. These points are defined by static heights located on the longitudinal centerline of the vehicle, $\mathrm{h}_{1}$ and $\mathrm{h}_{2}$. Movements of these two points are introduced as vertical and lateral components, $\mathrm{h}_{\mathrm{rc}}$ and $\mathrm{y}_{\mathrm{rc}}$, which are defined as quadratic functions of roll angle (see section 2.1) in coordinates fixed in the (rolling) sprung mass. The (rolled) vertical and lateral distances between the center of the sprung mass and the roll axis are defined as

$$
\begin{align*}
& \mathrm{h}^{\prime}=\mathrm{h}_{\mathrm{rc} 1}+\frac{\mathrm{a}_{\mathrm{s}}}{\mathrm{~L}}\left(\mathrm{~h}_{\mathrm{rc} 2}-\mathrm{h}_{\mathrm{rc} 1}\right)  \tag{B.4-1}\\
& \mathrm{y}^{\prime}=\mathrm{y}_{\mathrm{rc} 1}+\frac{\mathrm{a}_{\mathrm{s}}}{\mathrm{~L}}\left(\mathrm{y}_{\mathrm{rc} 2}-\mathrm{y}_{\mathrm{rc} 1}\right) \tag{B.4-2}
\end{align*}
$$

These dimensions are projected into a non-rolling frame to yield the offsets

$$
\begin{align*}
& \mathrm{h}_{\mathrm{ra}}=\mathrm{h}^{\prime}-\mathrm{y}^{\prime} \phi  \tag{B.4-3}\\
& \mathrm{y}_{\mathrm{ra}}=\mathrm{y}^{\prime}+\mathrm{h}^{\prime} \phi \tag{B.4-4}
\end{align*}
$$

An instant roll moment of inertia is defined for the sprung mass to include the effect of the offset of the center of mass relative to the roll axis.

$$
\begin{equation*}
\mathrm{I}_{\mathrm{xs}}=\mathrm{I}_{\mathrm{xx}}+\left(\mathrm{y}_{\mathrm{ra}}{ }^{2}+\mathrm{h}_{\mathrm{ra}}^{2}\right) \mathrm{m}_{\mathrm{s}} \tag{B.4-5}
\end{equation*}
$$

Appendix B - Equations of Motion

## B. 5 Tire Slip / Camber / Steer Equations

The tire side force and aligning moment are modeled as being linear with slip and camber. However, the coefficients are functions of vertical load (see Section 2.3).

## B.5.1 Independent Suspensions

The slip angles and camber angles ( $\alpha$ and $\gamma$ ) are defined as follows for the front suspension:

$$
\begin{gather*}
\alpha_{1 \mathrm{~L}}=\alpha_{10}+\beta+\frac{\mathrm{ra}}{\mathrm{~V}}-\left.\frac{\partial \delta}{\partial \mathrm{z}}\right|_{1} \mathrm{z}_{1 \mathrm{~L}}-\left.\frac{\partial \delta}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{1} \mathrm{~F}_{\mathrm{Y}_{1 \mathrm{~L}}}-\left.\frac{\partial \delta}{\partial \mathrm{M}_{\mathrm{Z}}}\right|_{1} \mathrm{M}_{\mathrm{Z}_{1 \mathrm{~L}}}-\delta_{\mathrm{FW}}  \tag{B.5.1-1}\\
\alpha_{1 \mathrm{R}}=-\alpha_{10}+\beta+\frac{\mathrm{ra}}{\mathrm{~V}}-\left.\frac{\partial \delta}{\partial \mathrm{z}}\right|_{1} \mathrm{z}_{1 \mathrm{R}}-\left.\frac{\partial \delta}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{1} \mathrm{~F}_{\mathrm{Y}_{1 \mathrm{R}}}-\left.\frac{\partial \delta}{\partial \mathrm{M}_{\mathrm{Z}}}\right|_{1} \mathrm{M}_{\mathrm{Z}_{1 \mathrm{R}}}-\delta_{\mathrm{FW}}  \tag{B.5.1-2}\\
\gamma_{1 \mathrm{~L}}=-\gamma_{10}+\phi-\left.\frac{\partial \gamma}{\partial \mathrm{z}}\right|_{1} \mathrm{z}_{1 \mathrm{~L}}-\left.\frac{\partial \gamma}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{1} \mathrm{~F}_{\mathrm{Y}_{1 \mathrm{~L}}}  \tag{B.5.1-3}\\
\gamma_{1 \mathrm{R}}=\gamma_{10}+\phi-\left.\frac{\partial \gamma}{\partial \mathrm{z}}\right|_{1} \mathrm{z}_{1 \mathrm{R}}-\left.\frac{\partial \gamma}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{1} \mathrm{~F}_{\mathrm{Y}_{1 \mathrm{R}}} \tag{B.5.1-4}
\end{gather*}
$$

(If the dynamic steering system is being used, $\delta \mathrm{FW}$ is equal to $\delta \mathrm{SW} / \mathrm{GR}$ and the aligning torque compliances are accounted for in the steering system model. Otherwise, it is the actual left / right front wheel angle and the aligning torque compliances are included as shown.)

The equations used for an independent rear suspension are:

$$
\begin{align*}
& \alpha_{2 L}=\alpha_{20}+\beta-\frac{r b}{V}-\left.\frac{\partial \delta}{\partial z}\right|_{2} z_{2 L}-\left.\frac{\partial \delta}{\partial F_{Y}}\right|_{2} F_{Y_{\mathcal{L}}}-\left.\frac{\partial \delta}{\partial M_{Z}}\right|_{2} M_{Z_{\mathcal{Z}}}  \tag{B.5.1-6}\\
& \alpha_{2 R}=-\alpha_{20}+\beta-\frac{\mathrm{rb}}{\mathrm{~V}}+\left.\frac{\partial \delta}{\partial \mathrm{z}}\right|_{2} \mathrm{z}_{2 \mathrm{R}}-\left.\frac{\partial \delta}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{2} \mathrm{~F}_{\mathrm{Y}_{2 \mathrm{R}}}-\left.\frac{\partial \delta}{\partial \mathrm{M}_{\mathrm{Z}}}\right|_{2} \mathrm{M}_{\mathrm{Z}_{2 R}}  \tag{B.5.1-7}\\
& \gamma_{2 L}=\gamma_{20}+\phi+\left.\frac{\partial \gamma}{\partial z}\right|_{2} z_{2 L}-\left.\frac{\partial \gamma}{\partial F_{Y}}\right|_{2} F_{Y_{\mu}}  \tag{B.5.1-8}\\
& \gamma_{2 R}=-\gamma_{20}+\phi-\left.\frac{\partial \gamma}{\partial z}\right|_{2} z_{2 R}-\left.\frac{\partial \gamma}{\partial \mathrm{F}_{Y}}\right|_{2} F_{Y_{2 R}} \tag{B.5.1-9}
\end{align*}
$$

Because the slip and camber angles are influenced by tire side force and aligning moment, which are in turn developed by slip and camber, the above equations are not suitable for sequential evaluation. To obtain a closed-form solution for slip and camber, the explicit expressions for aligning moment and camber are substituted for each wheel. These expressions have the form

$$
\begin{gather*}
\mathrm{F}_{Y}=\alpha \mathrm{C}_{\alpha}+\gamma \mathrm{C}_{\gamma}  \tag{B.5.1-10}\\
\mathrm{M}_{\mathrm{Z}}=\alpha \mathrm{C}_{\mathrm{M} \alpha} \tag{B.5.1-11}
\end{gather*}
$$

where the coefficients $\mathrm{C}_{\alpha}, \mathrm{C}_{\gamma}$, and $\mathrm{C}_{\mathrm{M} \alpha}$ are functions of vertical force that typically differ for each wheel at any instant. When the appropriate forms of eqs. B.5.1-10 and B.5.1-11 are substituted into eqs. B.5.1-1 through B.5.1-9, the slip and camber equations for each wheel are coupled with each other. Because they are linear equations with respect to slip and camber, they can be solved to yield expressions for the slip and camber of each wheel.

These equations can be written using matrix algebra notation as:
(boldface denoting matrices)

$$
\begin{align*}
& \mathbf{A} \alpha=\mathbf{B} \boldsymbol{\gamma}+\mathbf{c}  \tag{B.5.1-10}\\
& \mathbf{D} \boldsymbol{\gamma}=\mathbf{E} \alpha+\mathbf{f} \tag{B.5.1-11}
\end{align*}
$$

The solutions to these simultaneous equations are given by:

$$
\begin{gather*}
\gamma^{*}=\left(\mathbf{D}-\mathbf{E ~ A}^{-1} \mathbf{B}\right)^{-1}\left(\mathbf{E A}^{-1} \mathbf{c}+\mathbf{f}\right)  \tag{B.5.1-12}\\
\alpha^{*}=\mathbf{A}^{-1}\left(\mathbf{B} \gamma^{*}+\mathbf{c}\right) \tag{B.5.1-13}
\end{gather*}
$$

The A, B, c, D, E, and $\mathbf{f}$ matrices are:

$$
\begin{gathered}
\mathbf{A}=\left[\begin{array}{cccc}
\mathrm{a}_{1} & 0 & 0 & 0 \\
0 & a_{2} & 0 & 0 \\
0 & 0 & a_{3} & 0 \\
0 & 0 & 0 & a_{4}
\end{array}\right] \quad \mathbf{B}=\left[\begin{array}{cccc}
\mathrm{b}_{1} & 0 & 0 & 0 \\
0 & b_{2} & 0 & 0 \\
0 & 0 & b_{3} & 0 \\
0 & 0 & 0 & b_{4}
\end{array}\right] \\
\mathrm{a}_{\mathrm{i}}=1+\left(\partial \delta_{\mathrm{i}} / \partial \mathrm{F}_{\mathrm{yi}}\right) \mathrm{C}_{\alpha \mathrm{i}}+\left(\partial \delta_{\mathrm{i}} / \partial \mathrm{M}_{\alpha \mathrm{i}}\right) \mathrm{C}_{\mathrm{M}_{\alpha \mathrm{i}}} \\
\mathrm{~b}_{\mathrm{i}}=-\left(\partial \delta_{\mathrm{i}} / \partial \mathrm{F}_{\mathrm{yi}}\right) \mathrm{C}_{\mathrm{i}} \\
\mathbf{c}=\left[\begin{array}{c}
\alpha_{10}+\beta+\mathrm{ra} / \mathrm{V}-\left(\partial \delta / \partial \mathrm{z}_{1}\right) \mathrm{z}_{1}-\delta_{1} \\
-\alpha_{10}+\beta+\mathrm{ra} / \mathrm{V}+\left(\partial \delta / \partial z_{2}\right) \mathrm{z}_{2}-\delta_{2} \\
\alpha_{20}+\beta-\mathrm{rb} / \mathrm{V}-\left(\partial \delta / \partial z_{3}\right) z_{3} \\
-\alpha_{20}+\beta-\mathrm{rb} / \mathrm{V}+\left(\partial \delta / \partial z_{4}\right) \mathrm{z}_{4}
\end{array}\right] \\
\mathbf{D}=\left[\begin{array}{cccc}
\mathrm{d}_{1} & 0 & 0 & 0 \\
0 & \mathrm{~d}_{2} & 0 & 0 \\
0 & 0 & d_{3} & 0 \\
0 & 0 & 0 & d_{4}
\end{array}\right] \quad \mathbf{E}=\left[\begin{array}{cccc}
\mathrm{e}_{1} & 0 & 0 & 0 \\
0 & e_{2} & 0 & 0 \\
0 & 0 & e_{3} & 0 \\
0 & 0 & 0 & e_{4}
\end{array}\right]
\end{gathered}
$$

$$
\begin{gathered}
\mathrm{d}_{\mathrm{i}}=1+\left(\partial \gamma_{\mathrm{i}} / \partial \mathrm{F}_{\mathrm{yi}}\right) \mathrm{C}_{\mathrm{i}} \\
\mathrm{e}_{\mathrm{i}}=-\left(\partial \gamma_{\mathrm{i}} / \partial \mathrm{F}_{\mathrm{yi}}\right) \mathrm{C}_{\alpha \mathrm{i}} \\
\mathbf{f}=\left[\begin{array}{r}
-\gamma_{10}+\phi-\left(\partial \gamma_{1} / \partial \mathrm{z}_{1}\right) \mathrm{z}_{1} \\
\gamma_{10}+\phi+\left(\partial \gamma_{2} / \partial z_{2}\right) z_{2} \\
-\gamma_{20}+\phi-\left(\partial \gamma_{3} / \partial \mathrm{z}_{3}\right) \mathrm{z}_{3} \\
\gamma_{20}+\phi+\left(\partial \gamma_{4} / \partial \mathrm{z}_{4}\right) \mathrm{z}_{4}
\end{array}\right]
\end{gathered}
$$

## B.5.2 Beam Rear Axle

For a beam rear axle, linkage compliance can permit the axle to steer in response to applied side force and aligning moment. The attachment of the wheels to the axle is assumed to be rigid, and the axle is assumed to have negligible roll compliance. These assumptions lead to the following expressions for the slip and camber angles.

$$
\begin{gather*}
\alpha_{2 L}=\alpha_{20}+\beta-\frac{r b}{V}-\varepsilon_{R} \phi-\left.\frac{\partial \delta}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{2}\left(\mathrm{~F}_{\mathrm{Y}_{2 \mathrm{~L}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}}}\right)-\left.\frac{\partial \delta}{\partial \mathrm{M}_{\mathrm{Z}}}\right|_{2}\left(\mathrm{M}_{\mathrm{Z}_{2 L}}+\mathrm{M}_{\mathrm{Z}_{2 \mathrm{R}}}\right)  \tag{B.5.2-1}\\
\alpha_{2 \mathrm{R}}=-\alpha_{20}+\beta-\frac{\mathrm{rb}}{\mathrm{~V}}-\varepsilon_{\mathrm{R}} \phi-\left.\frac{\partial \delta}{\partial \mathrm{F}_{\mathrm{Y}}}\right|_{2}\left(\mathrm{~F}_{\mathrm{Y}_{\mathrm{Z}}}+\mathrm{F}_{\mathrm{Y}_{2 \mathrm{R}}}\right)-\left.\frac{\partial \delta}{\partial \mathrm{M}_{\mathrm{Z}}}\right|_{2}\left(\mathrm{M}_{\mathrm{Z}_{2 \mathrm{~L}}}+\mathrm{M}_{\mathrm{Z}_{\mathrm{R}}}\right)  \tag{B.5.2-2}\\
\gamma_{2 \mathrm{~L}}=-\gamma_{20}  \tag{B.5.2-3}\\
\cdot \gamma_{2 \mathrm{R}}=\gamma_{20} \tag{B.5.2-4}
\end{gather*}
$$

These equations cause the above matrices to become altered to the following:

$$
\mathbf{A}=\left[\begin{array}{cccc}
a_{1} & 0 & 0 & 0 \\
0 & a_{2} & 0 & 0 \\
0 & 0 & a_{3} & a_{34} \\
0 & 0 & a_{43} & a_{4}
\end{array}\right] \quad \mathbf{B}=\left[\begin{array}{cccc}
b_{1} & 0 & 0 & 0 \\
0 & b_{2} & 0 & 0 \\
0 & 0 & b_{3} & b_{34} \\
0 & 0 & b_{43} & b_{4}
\end{array}\right]
$$

$\mathrm{a}_{\mathrm{i}}, \mathrm{b}_{\mathrm{i}}$ as above, and:

$$
\begin{gathered}
\mathrm{a}_{34}=\left(\partial \delta_{4} / \partial \mathrm{F}_{\mathrm{y} 4}\right) \mathrm{C}_{\alpha 4}+\left(\partial \delta_{4} / \partial \mathrm{M}_{\alpha 4}\right) \mathrm{C}_{\mathrm{M}_{\alpha 4}} \\
\mathrm{a}_{43}=\left(\partial \delta_{3} / \partial \mathrm{F}_{\mathrm{y} 3}\right) \mathrm{C}_{\alpha 3}+\left(\partial \delta_{3} / \partial \mathrm{M}_{\alpha 3}\right) \mathrm{C}_{\mathrm{M}_{\alpha 3}} \\
\mathrm{~b}_{34}=-\left(\partial \delta_{4} / \partial \mathrm{F}_{\mathrm{y} 4}\right) \mathrm{C}_{44} \\
\mathrm{~b}_{43}=-\left(\partial \delta_{3} / \partial \mathrm{F}_{\mathrm{y} 3}\right) \mathrm{C}_{\beta}
\end{gathered}
$$

$$
\mathrm{c}=\left[\begin{array}{c}
\text { as above } \\
\text { as above } \\
\alpha_{20}+\beta-\mathrm{rb} / \mathrm{V}-\varepsilon_{\mathrm{R}} \phi-\partial \delta_{3} / \partial \mathrm{F}_{\mathrm{y} 3} \mathrm{C}_{\beta} \gamma_{3}-\partial \delta_{4} / \partial \mathrm{F}_{\mathrm{y} 4} \mathrm{C}_{44} \gamma_{4} \\
-\alpha_{20}+\beta-\mathrm{rb} / \mathrm{V}-\varepsilon_{\mathrm{R}} \phi-\partial \delta_{3} / \partial \mathrm{F}_{\mathrm{y} 3} \mathrm{C}_{\beta} \gamma_{3}-\partial \delta_{4} / \partial \mathrm{F}_{\mathrm{y} 4} \mathrm{C}_{44} \gamma_{4}
\end{array}\right]
$$

$$
\mathbf{D}=\left[\begin{array}{cccc}
\mathrm{d}_{1} & 0 & 0 & 0 \\
0 & \mathrm{~d}_{2} & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \quad \mathbf{E}=\left[\begin{array}{cccc}
\mathrm{e}_{1} & 0 & 0 & 0 \\
0 & e_{2} & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0
\end{array}\right]
$$

$$
\mathbf{f}=\left[\begin{array}{c}
\text { as above } \\
\text { as above } \\
-\gamma_{20} \\
\gamma_{20}
\end{array}\right]
$$

## B. 6 Power-Assisted Steering System

The following equations for the dynamic steering system model are based on the diagram of Figure B-1. The dynamics for the upper portion of the steering system are given by:

$$
\begin{gather*}
\mathrm{I}_{\mathrm{ss}} \mathrm{~d}^{2}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}^{2}=\mathrm{M}+\mathrm{K}_{\mathrm{ss}}\left(\delta_{\mathrm{fw}}-\delta_{\mathrm{fw}}{ }^{\prime}\right) / \mathrm{GR} \\
-\mathrm{C}_{\mathrm{Ss}} \mathrm{~d}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}-\mathrm{CF} \operatorname{sign}\left[\mathrm{~d}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}\right] \tag{B.6-1}
\end{gather*}
$$

where,

$$
\begin{equation*}
\delta_{\mathrm{fw}}{ }^{\prime}=\delta_{\mathrm{sw}} / \mathrm{GR} \tag{B.6-2}
\end{equation*}
$$

and $\mathrm{C}_{\mathrm{SS}}, \mathrm{CF}_{\mathrm{F}}$ are parameters representing viscous and coulomb friction.
The "no-lash" front wheel angle, $\delta_{\mathrm{fw}}$, is determined from the quasi-static relationship accross the lumped compliance $\mathrm{K}_{\mathrm{ss}}$ and current value of $\delta_{\mathrm{fw}}$ 'as:

$$
\begin{equation*}
\delta_{\mathrm{fw}}=\delta_{\mathrm{fw}}{ }^{\prime}+\mathrm{H}(1-\mathrm{CB}) / \mathrm{K}_{\mathrm{ss}} \tag{B.6-3}
\end{equation*}
$$

The lumped compliance, $\mathrm{K}_{\mathrm{SS}}$, is given by the serial combination of the upper column compliance $\mathrm{K}_{\mathrm{Sc}}$ and the two lower linkage compliances $\mathrm{K}_{\mathrm{SL}}$ as:

$$
2 \mathrm{~K}_{\mathrm{sc}} \mathrm{~K}_{\mathrm{SL}} \mathrm{GR}^{2} /\left(\mathrm{GR}^{2} \mathrm{~K}_{\mathrm{Sc}}+2 \mathrm{~K}_{\mathrm{SL}}\right)
$$

$\mathrm{CBB}_{\mathrm{B}}$ is the power boost (percent/100) contribution from the pump and, H , the tire aligning torques of both front tires, is given by:

$$
\begin{equation*}
\mathrm{H}=2 \mathrm{C} \alpha\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)\left[(\mathrm{v}+\mathrm{ar}) / \mathrm{U}-\delta_{\mathrm{fw}}\right] / \mathrm{K}_{\mathrm{ss}} \tag{B.6-4}
\end{equation*}
$$

$x_{p}$ and $x_{m}$ are the pneumatic and mechanical trails, respectively, of the front tires/wheels. $\mathrm{C}_{\alpha}$ is the front tire cornering stiffness.

Appendix B - Equations of Motion

Substituting B.6-4 into B. $6-3$ and solving for $\delta_{f w}$ yields:

$$
\begin{gather*}
\delta_{\mathrm{fw}}=\left[\delta_{\mathrm{fw}}{ }^{\prime}+2 \mathrm{C}_{\alpha}\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)(1-\mathrm{CB})(\mathrm{v}+\mathrm{ar}) /\left(\mathrm{U} \mathrm{~K}_{\mathrm{ss}}\right)\right] / \\
{\left[1+2 \mathrm{C}_{\alpha}\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)(1-\mathrm{CB}) / \mathrm{K}_{\mathrm{ss}}\right]} \tag{B.6-5}
\end{gather*}
$$

Substituting B.6-5 into the differential equation B.6-1 results in:

$$
\begin{gather*}
\mathrm{I}_{\mathrm{ss}} \mathrm{~d}^{2}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}{ }^{2}=\mathrm{M}+\mathrm{K}_{\mathrm{ss}}\left[\mathbf{A} \delta_{\mathrm{sw}}-\mathbf{B}(\mathrm{v}+\mathrm{ar})\right] / \mathrm{GR}^{2} \\
-\mathrm{C}_{\mathrm{ss}} \mathrm{~d}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}-\mathrm{CF} \operatorname{sign}\left[\mathrm{~d}\left(\delta_{\mathrm{sw}}\right) / \mathrm{dt}\right] \tag{B.6-6}
\end{gather*}
$$

where,

$$
\mathbf{A}=1-1 /\left[1+2 \mathrm{C}_{\alpha}\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)(1-\mathrm{CB}) / \mathrm{K}_{\mathrm{ss}}\right]
$$

and,

$$
\begin{gathered}
\mathbf{B}=2 \mathrm{C}_{\alpha}\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)(1-\mathrm{CB}) \mathrm{GR} / \\
\left\{\left[1+2 \mathrm{C}_{\alpha}\left(\mathrm{x}_{\mathrm{p}}+\mathrm{x}_{\mathrm{m}}\right)(1-\mathrm{CB}) / \mathrm{K}_{\mathrm{ss}}\right] \mathrm{UK}_{\mathrm{ss}}\right\}
\end{gathered}
$$

The left and right front wheel angles, $\delta_{\mathrm{fwL}}$ and $\delta_{\mathrm{fwR}}$, are obtained from equation (B.6-5) using left/right parameter values of tire cornering stiffness and inclusion of the wheel lash.


Figure B-1. Steering System Model.

## APPENDIX C — PROGRAMMING DETAILS

This section describes how the Wind-Steer program operates. It is intended for programmers who wish to modify the program, or port it to a new computer.

## C. 1 Machine Dependencies

The Wind-Steer program is written completely in Fortran 77. The standard does not recognize any hardware-specific aspects of a computer, such as the screen, keyboard, or clock. To make the program a more productive tool, it does make use of a few machinespecific features for the versions that run on the IBM PC, the Apple Macintosh, and MTS (The University of Michigan mainframe computer). These are:

- The output file contains the time and date for the simulation, which is provided by a subroutine called TIMDAT. The subroutine TIMDAT should be modified to work on the computer for which the program will be used. If time and date information is not available, the subroutine can be made inoperative.

The Macintosh version uses external subroutines provided with the compiler, TIME and DATE. These must be linked with the rest of the program if it is recompiled for the Macintosh.

- The Fortran i/o unit number for the "terminal" (i.e., the keyboard and screen) should be set to the proper value expected by the compiler. Most compilers, including all three that have been used to date, permit an asterisk * to be used to specify the screen and keyboard.
- Simulation progress is shown on the screen in the PC and Mac versions. This involves interacting with the screen. This is done in the subroutine OUTERD and should be modified to work on the new computer, or deleted.

The IBM version uses the subroutine SETCUR from an UMTRI library of Fortran extensions. This library must be linked with the rest of the program for use on the IBM PC.

- Writing of binary data has been done differently for every system so far. The MTS version uses an MTS subroutine, WRITE, to put binary data into an ordinary file. The PC version opens a separate file with access type set to a nonstandard type BINARY. The Mac version uses a separate file with access set to UNFORMATTED. Both the Mac and the PC versions of the program produce binary files with no structure-just a stream of binary data.
- The source code is contained in a large file with the main program and all of the subroutine modules, and in nine small "include files" which are merged with the main file during compilation. The INCLUDE command is not standard Fortran, and is handled differently by each compiler.


## C. 2 Structure of Program

The operation of this program follows that of many programs that use numerical integration to simulate a dynamic system, and can be summarized by the following steps:

1. Read input data. This function is performed by the subroutine INDATA.
2. Initialize variables and constants derived from input data. This function is performed by the subroutine INIT.
3. Establish name(s) of output file(s) and write header data (number of channels, names, etc.) This function is performed by the subroutine OPNOUT.
4. Perform the numerical integration using a "loop," in which the differential equations are solved numerically for time T , and T is increased in small increments DT. The differential equations are written in the form:

$$
\begin{equation*}
\dot{\mathrm{Y}}_{\mathrm{i}}=\mathrm{dY} \mathrm{Y}_{\mathrm{i}} / \mathrm{dt}=f\left(\mathrm{Y}_{1}, \mathrm{Y}_{2}, \ldots \mathrm{Y}_{\mathrm{n}}, \mathrm{t}\right) \tag{5.2-1}
\end{equation*}
$$

where $\mathrm{Y}_{\mathrm{i}}$ is a state variable, $\mathrm{i}=1,2, \ldots \mathrm{n}$, and $\mathrm{n}=$ number of equations.
The function indicated above as $f$ is named FUNCTN in the Fortran Wind-Steer program.

The integration from time T to $\mathrm{T}+\mathrm{DT}$ is performed using a modified Euler method, sometimes called a second-order Runge-Kutta. Specifically, the integration of each state variable is accomplished as follows:

$$
\begin{align*}
\mathrm{Y}_{\mathrm{i}} & =\mathrm{Y}_{\mathrm{i}}(\mathrm{~T})+\mathrm{DT} / 2 \cdot f\left(\mathrm{Y}_{1}, \mathrm{Y}_{2}, \ldots \mathrm{Y}_{\mathrm{n}}, \mathrm{~T}\right)  \tag{5.2-2}\\
\mathrm{Y}_{\mathrm{i}}(\mathrm{~T}+\mathrm{DT}) & =\mathrm{Y}_{\mathrm{i}}(\mathrm{~T})+\mathrm{DT} \cdot f\left(\mathrm{Y}_{1}^{\prime}, \mathrm{Y}_{2}^{\prime}, \ldots \mathrm{Y}_{\mathrm{n}}^{\prime}, \mathrm{T}+\mathrm{DT} / 2\right) \tag{5.2-3}
\end{align*}
$$

Note that $f$ (FUNCTN) is evaluated twice for each integration step: once as the start, and a second time as the midpoint of the time interval. All of the equations that represent the vehicle are contained in FUNCTN and in several auxiliary subprograms that are used by FUNCTN. (These additional routines are named AIRACT, FDAMP, ROLLAX, STEER, TIRES2, SUM, etc.)

At some multiple of DT, values of interest are written into the output file by the subroutine OUTPUT.
4. Print the success or failure of the simulation and close any open files.

## C. 3 Program Modules

This section describes the modules that make up the Wind-Steer program. The subprograms are shown below in alphabetical order with a listing of their arguments and common block references.

## AIRACT(YAW, BETA, VYAW)

Update air velocity, sideslip, and magnitudes of forces and moments in common block /AERO/.
$\rightarrow$ YAW real*4 Yaw angle of vehicle.
$\rightarrow$ BETA rea*4 Sideslip angle of vehicle.
$\rightarrow$ VYAW real*4 Yaw rate of vehicle.
Common Blocks: GLBL PARS AERO

## DRIVGO

Initialize driver model parameters for steering angle version of driver model.
Common Blocks: GLBL PARS VARS TIRE DRVST1 DRIV TRSSTR

Subprograms called: TRANS

DRIVGT
Initialize driver model parameters for torque version of driver model.

Common Blocks: GLBL PARS VARS TIRE DRVST1 DRIV TRSTOR

Subprograms called: TRANST

DRIVE1 (DFW)
Read driver model parameters.
$\leftarrow$ DFW real initial average front wheel angle $=0$
Common Blocks: GLBL PARS VARS TIRE DRVST1 DRIV TRSSTR

## DRIVER (X, Y, DFW, DFWNOW)

Calculates closed-loop driver steering control angle.
$\rightarrow \mathrm{X} \quad$ real current time
$\rightarrow \mathrm{Y} \quad$ real driver model state vector
$\leftarrow$ DFW real calculated average front wheel angle.
$\rightarrow$ DFWNOW real current average front wheel angle.

Common Blocks: AERO GLBL PARS DRVST1 DRIV
TRSSTR
Subprograms called: TRAJ GMPRD

DRIVET (X, Y, DRTORQ, DRTNOW)
Calculates closed-loop driver steering wheel control torque.
$\rightarrow \mathrm{X} \quad$ real current time
$\rightarrow \mathrm{Y}$ real driver model state vector
$\leftarrow$ DRTORQ real calculated steering wheel torque.
$\rightarrow$ DRTNOW real current steering wheel torque.

Common Blocks: AERO GLBL PARS DRVST1 DRIV
TRSTOR
Subprograms called: TRAJ GMPRD
FDAMP (VZ, VROLL, VPITCH, FD)
Compute the damping force for all four wheels.
$\rightarrow \mathrm{VZ} \quad$ real*4 vertical velocity of vehicle sprung mass c.g.
$\rightarrow$ VROLL real*4 roll velocity of vehicle sprung mass.
$\rightarrow$ VPITCH real*4 pitch velocity of vehicle sprung mass.
$\leftarrow$ FD real*4 $2 \times 2$ matrix of damping forces at each wheel.
Common Blocks: SUSP
This subroutine uses different rates for jounce and rebound. The sign convention is that jounce $\rightarrow$ positive damping force.

FUNCTN (T, Y, YP)
Compute six derivatives of state variables in the vehicle/steering model.

$$
\begin{array}{lll}
\rightarrow \mathrm{T} & \text { real }^{*} 4 & \text { Time (independent variable of integration) } \\
\rightarrow \mathrm{Y} & \text { real }^{*} & \text { 1-D array of } 6 \text { state variables } \\
\leftarrow \mathrm{YP} & \text { real } * 4 & \text { 1-D array of } 6 \text { derivatives: } \mathrm{yp}(\mathrm{i})=\mathrm{dy}(\mathrm{i}) / \mathrm{dt}
\end{array}
$$

Common Blocks: GLBL PARS SUSP AERO VARS
Subprograms Called: FDAMP WHEELZ ALPHAS ROLLAX AIRACT STEER
TIRES GAMMAS
Subroutine FUNCTN contains the equations of motion for the 5 -d.o.f vehicle model and a 1-d.o.f steering system model. The derivatives it computes are used by the subroutine DE to simulate the system. It also halts the simulation upon exceeding preset handling limits.

GMADD (A, B, C, N, M)
Calculates the sum of two matrices.

| $\rightarrow A$ | real | $N \times M$ input matrix |
| :--- | :--- | :--- |
| $\rightarrow B$ | real | NxM input matrix |
| $\leftarrow C$ | real | $N \times L$ output matrix equal to sum of $A$ and $B$ |
| $\rightarrow N$ | integer | row dimension of $A$ and $B$ |

$\rightarrow \mathrm{M} \quad$ integer column dimension of A and B

GMSUB (A, B, C, N, M)
Calculates the sum of two matrices.
$\rightarrow \mathrm{A} \quad$ real Nx M input matrix
$\rightarrow \mathrm{B} \quad$ real $\mathrm{N} x \mathrm{M}$ input matrix
$\leftarrow \mathrm{C} \quad$ real $\mathrm{N} \times \mathrm{L}$ output matrix equal to difference of A less B
$\rightarrow \mathrm{N} \quad$ integer row dimension of A and B
$\rightarrow \mathrm{M} \quad$ integer column dimension of A and B

GMPRD (A, B, R, N, M, L)
Calculates the product of two matrices.
$\rightarrow \mathrm{A} \quad$ real $\quad \mathrm{N} x \mathrm{M}$ input matrix
$\rightarrow \mathrm{B} \quad$ real $\quad \mathrm{MxL}$ input matrix
$\leftarrow \mathrm{R} \quad$ real $\quad \mathrm{N} x$ L output matrix equal to product of $A$ and $B$
$\rightarrow \mathrm{N} \quad$ integer row dimension of A
$\rightarrow \mathrm{M} \quad$ integer column dimension of A and row dimension of B
$\rightarrow$ integer column dimension of $B$

INDATA (IREAD, IPR, IERD, ITERM, FNREAD, FNPR, FNERD)
Set up file connections and read input data.
$\rightarrow$ IREAD integer Fortran i/o unit for parameter input file (e.g., 5).
$\rightarrow$ IPR integer Fortran i/o unit for echoing data (e.g., 7).
$\rightarrow \mathbb{R E A D} \quad$ integer $\quad$ Fortran $\mathrm{i} / \mathrm{o}$ unit for output ERD file (e.g., 8).
$\rightarrow$ ITERM integer Fortran i/o unit for keyboard and screen (e.g., 9).
$\leftarrow$ FNREAD char*32 Fortran i/o unit for parameter input file (e.g., SIM.IN).
$\leftarrow$ FNPR char*32 Fortran i/o unit for echoing data (e.g., SIM.ECH).
$\leftarrow$ FNERD char*32 Fortran i/o unit for output ERD file (e.g., SIM.ERD).

## Common Blocks: GLBL PARS MNVR SUSP TIRE AERO PRNT

This subroutine prompts the user for a "root name" from which three other file names are defined. (In the above examples, the root name is "SIM." The input file (e.g., SIM.INP) must already exist. The other two are created. If files with those two names (e.g., SIM.ECH, SIM.ERD) already exist, they are destroyed.

## MAIN-WIND

Main program module that controls the wind \& handling simulation.

| Common Blocks: | GLBL | PARS | SUSP | VARS | AERO | PRNT |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Subprograms Called: | INDATA | SETERD | OUTPRT | OUTERD | ALERT | DE |

MINV (A, N, D, L, M)
Calculates the inverse of a matrix.
$\rightarrow$ A real $\mathrm{Nx} N$ input matrix to be inverted. Replaced with inverse.
$\rightarrow \mathrm{N} \quad$ integer dimension of A
$\leftarrow \mathrm{D}$ real resultant determinant
$\rightarrow \mathrm{L} \quad$ integer work vector of length N
$\rightarrow \mathrm{M} \quad$ integer work vector of length N

OPNOUT
Write header portion of the output ERD file, and compute constants used later.
Common Blocks: GLBL PARS
Subprograms Called: MACTIM (not used for mainframe)

OUTPUT (IERD, ITERM, NBYTES, T, Y)
Write predicted response variables into output file and show progress on screen.
$\rightarrow$ IERD integer Fortran i/o unit for the output file.
$\rightarrow$ ITERM integer Fortran $\mathrm{i} / \mathrm{o}$ unit for communicating with the user.
$\rightarrow$ NBYTES int*2 Number of bytes written at each time step.
$\rightarrow \mathrm{T}$ real Time.
$\rightarrow \mathrm{Y} \quad$ real $\quad$ 1-D array with state variables of system.
Common Blocks: GLBL PARS VARS AERO
Subprograms used: WRITE ${ }^{1}$ GTIME $^{2}$ GDATE $^{2}$ SETCUR ${ }^{2}$
TOOLBX ${ }^{3}$
${ }^{1}$ Used only on MTS.
2 Used only on IBM PC.
3 Used only on Apple Macintosh.

ROLLAX (ROLL, YROLAX, HROLAX, IXSRA)
Compute instantaneous lateral and vertical distances of the sprung mass c.g. from the roll axis.
$\rightarrow$ ROLL real*4 Roll angle of sprung mass.
$\leftarrow$ YROLAX real*4 Lateral distance (in a non-rolling frame) between c.g. of sprung mass and roll axis.
$\leftarrow$ HROLAX real*4 Horizontal distance (in a non-rolling frame) between c.g. of sprung mass and roll axis.
$\leftarrow$ IXSRA real*4 Moment of inertia of the sprung-mass about the instantaneous roll axis.

Common Blocks: PARS SUSP

## Function STEER(T)

Return steering wheel angle or steering wheel torque as function of time.
$\leftarrow$ STEER real*4 Steering wheel angle.
$\rightarrow \mathrm{T} \quad$ real*4 Time.
Common Blocks: MNVR
The angle (or torque) is determined by one of three methods, dependent upon the variable NSTEER in the common block MNVR: (1) if NSTEER < 0 , the UMTRI driver model is used; (2) if NSTEER $=0$, a sinusoidal function is used; and (3) if NSTEER $>0$, a table look-up is used.

## Function SUM(MATRIX)

Sum values in a 4-element matrix.
$\leftarrow$ SUM real*4 Sum of values in matrix.
$\rightarrow$ MATRIX real*4 matrix with 4 elements $(2 \times 2),(4 \times 1)$, or $(1 \times 4)$.

TABLE (M, N, X, Y, Z, Q)
Table look-up routine.
$\rightarrow \mathrm{M} \quad$ integer index of $\mathrm{X}-\mathrm{Y}$ table (arrays) at which to start search
$\rightarrow \mathrm{N} \quad$ integer index of $\mathrm{X}-\mathrm{Y}$ table (arrays) at which to end search
$\rightarrow \mathrm{X} \quad$ real $\quad \mathrm{N}$-array of abscissa table values
$\rightarrow \mathrm{Y} \quad$ real $\quad \mathrm{N}$-array of ordinate table values
$\rightarrow \mathrm{Z} \quad$ real scalar abscissa value
$\leftarrow$ Q real scalar ordinate value of X - Y table corresponding to Z

## TIMEDAT (TIMEDT)

Obtain the current time and date.
$\leftarrow$ TIMEDT char*24 String containing time and date.

## TIRSUB (BETA, V, VYAW, ROLL)

Compute cornering force, aligning moment, steer, slip, and camber angle for all four tires.
$\rightarrow$ BETA real*4 Slip angle.
$\rightarrow$ V real*4 Vehicle speed.
$\rightarrow$ VYAW real*4 Yaw rate.
$\rightarrow$ ROLL real*4 Roll angle.
Common Blocks: TIRE SUSP VARS

TRANS
Calculates transition matrix for driver model internal vehicle model. (without steering system)

Common Blocks: DRVST1 DRIV TRSSTR

## TRANST

Calculates transition matrix for driver model internal vehicle model. (with steering system)

Common Blocks: DRVST1 DRIV TRSTOR

TRAJ (X, XT, YT, YPATH)
Obtains the previewed lateral path position (relative to the vehicle heading).
$\rightarrow \mathrm{X}$ real forward preview distance
$\rightarrow$ XT real $\quad \mathrm{x}$-coordinates of path in vehicle axis system at X ahead
$\rightarrow$ YT real $\quad y$-coordinates of path in vehicle axis system at $X$ ahead
$\rightarrow$ YPATH real lateral offset of path from vehicle at X ahead
Common Blocks: INOUT

## WHEELZ (Z, ROLL, PITCH)

Update matrices in the common block /VARS/ based on the new position of the sprung mass.
$\rightarrow \mathrm{Z} \quad$ real*4 Vertical position of sprung mass c.g. (in).
$\rightarrow$ ROLL real*4 Roll angle of sprung mass (rad)
$\rightarrow$ PITCH $\quad$ real*4 Pitch angle of sprung mass (rad)
Common Blocks: SUSP VARS
The matrices ZW, FZ, KNMSTR, KNMCBR in common /VARS/ are updated. The quantities computed for each wheel are: vertical displacement, normal ground load, bumpsteer angle and bump-camber angle for each wheel, relative to static trim. roll-center heights are assumed fixed relative to the road for the calculation of lateral load transfer.

WINSUB (T, WIND)
Optional user-defined subroutine used to specify a wind profile - in lieu of entering a time history table in the input data set. Called only if the WINDKY parameter is $<0$.
$\rightarrow \mathrm{T} \quad$ real current time
$\leftarrow$ WIND real wind velocity magnitude
Common Blocks: GLBL

## C. 4 Modifying the Format of the Output File

There are at least two reasons why one might wish to modify the existing format of the output file created by the Wind-Steer program: (1) to add or delete variables of interest, or (2) to set the format to match established post-processing software other than the software used within ERD at UMTRI.

## C.4.1 Method Used to Write Time Histories

The code for writing the output file is contained in two program modules: (1) OPNOUT opens the output file and writes the header information, and (2) OUTPUT writes the values of output variables at discrete time intervals. Only these two subroutines need to be modified. (In reading the following descriptions, it may be helpful to also view the source code listings for those subroutines, contained in Appendix D.)

Most of the the code in subroutine OPNOUT assigns names to character variables. Then, at the bottom of the subroutine, those variables are written into the output file in the format required for an ERD header. Similarly, most of the code in OUTPUT assigns values to elements in a REAL array. Then, at the bottom of the subroutine, those variables are written into the output file in the format required for an ERD header. It is essential that the one-to-one correspondence is maintained between labels for variables and values for the variables. As long as the two forms of data are properly paired, the number of variables and their order really doesn't matter.

Both subroutines use a variable called NCHAN to identify the channel number being considered. For each value of NCHAN, the following assignments are made in OPNOUT:

- a 32-character name for the variable of interest is assigned to the character*32 Fortran array element LONGNM (NCHAN), e.g., "Input Steer Angle"
- an 8 -character name for the variable of interest is assigned to the character*8 Fortran array element SHORTN (NCHAN), e.g., "Steer In"
- a 32-character generic name for the variable of interest is assigned to the character* 32 Fortran array element GENNM (NCHAN), e.g., "Steer Angle"
- an 8-character name for the units of the variable of interest is assigned to the character*8 Fortran array element UNITNM (NCHAN), e.g., "deg"
- a 32-character generic name for the rigid body associated with the variable of interest is assigned to the character*32 Fortran array element RIGBOD (NCHAN), e.g., "Input"

In subroutine OUTPUT, for each value of NCHAN, an appropriate value is assigned to the array element BUFFER (NCHAN).

At the bottom of each subroutine, the value of NCHAN is equal to the total number of channels that are written into the output file.

The channel definitions are grouped such that variables that apply to the input or the entire vehicle are handled first. Variables that apply to each wheel (suspension and tire
variables) are handled in two nested DO loops. The outer loop goes from the front axle to the rear, and the inner loop goes from the left side to the right. Thus, each block of code within the loops gets executed four times.

## C.4.1 Deleting Variables

To delete a variable, a block of code is removed from the OPNOUT subroutine and a corresponding block is removed from OUTPUT. The block of code in OPNOUT begins with comments describing the variable, then the statement "NCHAN = NCHAN +1 ," and then five assignment statements for element NCHAN of arrays LONGNM, SHORTN, UNITNM, GENNM, and RIGBOD. Delete all of these lines or comment them out (insert a C in column 1 of each line so that the line is ignored by the Fortran compiler). Identify the corresponding assignment statement in OUTPUT and delete also (or comment it out). It is usually necessary to modify some of the lines following the deleted line in OUTPUT so that the following values are put into lower indexed elements of the array BUFFER.

For example, suppose we want to delete the Z deflection of the vehicle body. The block of code in subroutine OPNOUT that provides the labels is the following:

```
        UNITNM (NCHAN) = UDIST
        RIGBOD (NCHAN) = THISRB
C
C Z Position
&
        NCHAN = NCHAN + 1
        IONGNM (NCHAN) = 'Z Position, Sprung Mass cg'
        SHORTN (NCHAN) = 'Z cg'
        GENNM (NCHAN) = 'Z POsition'
        UNITNM (NCHAN) = UDISP
        RIGBOD (NCHAN) = THISRB
C
C Roll Angle
    NCHAN = NCHAN + 1
    LONGNM (NCHAN) = 'Roll Angle'
```

The underlined lines would be deleted. The code in subroutine OUTPUT that includes this variable is the following:
C
C Body position variables
C
BUFFER (NCHAN +1 ) $=\mathrm{Y}(1) /$ ININFT
BUFFER (NCHAN + 2) $=Y(2) /$ ININFT
BUEFER (NCHAN + 3) $=Y(3)$
BUFEER (NCHAN +4$)=Y(4) *$ TODEG
BUEFER (NCHAN +5 ) $=Y(5) *$ TODEG
BUFEER (NCHAN +6$)=Y(6) \star$ TODEG
NCHAN $=$ NCHAN +6

From viewing the definitions of the Y array, it turns out the $\mathrm{Y}(3)$ is the Z variable. The underlined code would be modified as follows:

```
C
C Body position variables
C
```

```
    BUFFER (NCHAN + 1) = Y(1) / ININFT
```

    BUFFER (NCHAN + 1) = Y(1) / ININFT
    BUFFER (NCHAN + 2) = Y(2) / ININFT
    BUFFER (NCHAN + 2) = Y(2) / ININFT
    BUFEER (NCHAN + 3) =Y(4) * TODEG
    BUFEER (NCHAN + 3) =Y(4) * TODEG
    BUFEER (NCHAN + 4) =Y(5) * TODEG
    BUFEER (NCHAN + 4) =Y(5) * TODEG
    BUFFER (NCHAN + 5) =Y(6) * TODEG
    BUFFER (NCHAN + 5) =Y(6) * TODEG
    NCHAN = NCHAN + 5
    ```
    NCHAN = NCHAN + 5
```

The line that set the value in the buffer was deleted, and the following lines were modified so that at the end of the block NCHAN was incremented by 5 , rather than 6 as before.

## C.4.2 Adding Variables

To add a variable, a new block of code is added to subroutine OPNOUT and a corresponding block is added to OUTPUT. The code added to OPNOUT should (1) provide labels for element NCHAN of the arrays LONGNM, SHORTN, UNITNM, GENNM, and RIGBOD, and (2) the variable NCHAN should be properly incremented. The code added to OUTPUT should (1) provide the value of the new variable and put it into the element NCHAN of the array BUFFER, and (2) the variable NCHAN should be properly incremented. The location of the added code defines where the new variable is situated relative to the existing output variables. The only restriction is the the order of channels in BUFFER must match the order of the labels in each of the character arrays.

## C.4.3 Changing the Format of the Output File

As the Wind-Steer program exists at UMTRI, the output file follows the ERD format. The numerical values of the output variables can be written in binary form, or in text form using a Fortran FORMAT that was specified in line 5 of the input file. The existing flexibility should be sufficient to accommodate any desired formats for the output. For example, if a plotting program expects to find columns of numbers separated by commas, the following FORMAT could be put into line 5 of the input file:
(100(F10.2,1X))
If the existing flexibility is not sufficient, the code that writes can be replaced as needed. (It lies at the bottom of the OUTPUT subroutine.)

The header portion of the file is more likely to cause problems with post-processing software. The code that writes the header is contained in the bottom of the OPNOUT subroutine, and is shown (partially) below:
C
C Write standard ERD file heading.
C
WRITE (IOUT,' (A) ') 'ERDFILEV2.00' |
WRITE (IOUT, 410) NCHAN, NSAMP, NRECS, NBYTES, NUMKEY, DT*IPRINT
410 FORMAT (5 (I6,','), E13.6)
411 FORMAT (A8,255A8)
412 FORMAT (A8, 31A32 : $2\left(/{ }^{(\& 1000 ~ ', ~ 31 A 32)) ~}\right.$

Appendix C - Programming Details

```
WRITE (IOUT,'(A,A)') 'TITLE ', TITLE
WRITE (IOUT, 411) 'SHORTNAM', (SHORTN(J), J=1, NCHAN)
WRITE (IOUT, '(A,A)') 'HISTORY Input file was ', FNREAD
WRITE (IOUT, '(A)') 'END'
```

This is the only code that is modified to change the form of the file header. Most of the code above this section consists of statements that assign labels to arrays of character variables. Some of those labels can be printed in a different format if desired. For example, suppose that a plotter expects to find labels enclosed in double quotes on the first line, followed by numbers separated by commas. Also suppose that the short labels ( 8 characters or less) are the appropriate length for the plotter. Then the existing code could be replaced with the following:
C
C Write 1-line heading with labels enclosed in double-quotes and
C separated by commas. e.g., "Time", "Steer In", ...
WRITE (IOUT, 411) 'SHORTNAM', (SHORTN(J), J=1, NCHAN)
411 FORMAT (100('"',A8,'"',1X)

## APPENDIX D - SOURCE CODE

This appendix lists the Fortran source code written specifically for the Wind-Steer model. Variables in common blocks are defined in separate "include" files, which are listed separately from the program subroutines at the end of the appendix.
Modified by C. MacAdam, 5-19-88
Modified by M. Sayers, 8-28-88 (changed eqs. of motion,
new integrator; v 0.85)
Modified by C. MacAdam, 9-7-88 (driver model and wind profile
additions; v 0.90)
Modified by M. Sayers,12-14-88 (cosmetics, changed input; v 0.91)
Modified by C. MacAdam,1-30-89 (steering system, revised tire eqns
and params for SAE conventions, torque-option driver model; v 1.0)

## MACHINE DEPENDENCIES:

Most of the following code is standard Fortran 77 and is independent of the implementation, EXCEPT:
(1) "include" files are not standard and must be referenced as needed for a specific compiler.
(2) The terminal is referenced as unit * in READ and WRITE statements involving the user. (Although not "standard," this works with most compilers and probably is OK.)

Otherwise, all machine-specific sections of code are identified by comments that begin with "C++". This file includes the code needed for
(1) the Microsoft Fortran compiler for the IBM PC
(2) the Absoft Fortran compiler for the Apple Macintosh
(3) the FortranVS compiler for the UM mainframe (MTS) system

```
PROGRAM SECTIONS:
```

MAIN -- Controls "flow" of program and performs num. integration
BLOCK DATA -- initializes variables in COMMON blocks
AIRACT (T, YAW, BETA, VYAW) -- handle aerodynamic forces and moments
DRIVE1 (DFW) -- Read driver model parameters
DRIVER(X, Y, DFW, DFWNOW) -- compute closed-loop steer input
DRIVGO -- initialize driver model
ECHO -- create output file with echo of input parameters
FDAMP (VZ, VROLL, VPITCH, FD) -- compute damping force for 4 wheels
FUNCTN (T, Y, YP) -- computes YP derivatives given $T$ and $Y$
Function FWIND (T) -- provide cross-wind as function of time

```
GMPRD (A, B, R, N, M, L) -- multiply two matrices
INDATA -- read input data and converts units
INIT -- computes constants used in simulation
Function LENSTR(STRING) -- no. of characters in string
OPNOUT -- create output file and write header
OUTPUT(T, Y, YP) -- write simulation variables into file at time T
Function POLY4(COEF, FZ) -- evaluate 4th-order polynomial of Fz
C ROLLAX(ROLL, YROLAX, HROLAX, IXSRA) -- roll axis kinematics
Function STEER(T) -- provides steering wheel angle as function of T
Function SUM(MATRIX) -- sums 4 elements of matrix
TABLE (M, N, X, Y, Z, Q) -- table look-up routine.
TIMEDAT (TIMEDT) -- produce string with time and date
TIRES (BETA, V, VYAW, ROLU) -- compute tire forces and moments
TRAJ(X, XT, YT, YPATH) -- compute lat. disp. of previewed path
TRANS -- Compute transition matrix for driver model
WHEELZ(Z, ROLL, PITCH) -- handle wheel kinematics
LIST OF SYMBOLS:
I/O SYMBOLS
    IREAD - unit number for input data
    IECHO - unit number for output file with echo of input data
    IOUT - unit number for simulation output file
SIMULATION PARAMETERS
    DT - time step for numerical integration
    TEND - end time of simulation
    IPRINT - print interval (every i-th point is save in output file)
    KSYWND - wind heading angle (of velocity vector)
    AIRHO air density
    V - vehicle speed
    VWIND - wind speed
    WINDKY - wind key: >= 0 => time history wind profile input:
                                    windky is num of (T,VW) table pairs.
                                    < O => call user function "FWIND" for
                                    profile input.
GLOBAL TIME-VARIABLES
    T - time
    Y(13) - array of 13 state variables
    AY - vehicle lateral acceleration (ignoring roll-accel.)
    RHO - path curvature
    BETAIR - aerodynamic sideslip angle
    VAX,VAY - x,y components of air velocity (axles reference)
Position Speed Accel.
    XG, VXG - X of total cg (inertial reference)
    YG, VYG - Y of total Cg (inertial reference)
    BETA, VBETA - ground sideslip (BETA = VY / V)
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```

    Z, VZ, AZ
    ROLL, VROLL, AROLL
    - roll
    PITCH, VPITCH, APITCH - pitch
    YAW, VYAW, AYAW - yaw
    SW, VSW, ASW - steering wheel angle
    FW - front wheel steer angle
    GLOBAL INTEGERS - INDICES AND FLAGS
UNITS - (CHAR*1) 'E' = English (ft, lbm, deg), otherwise metric
NUMKEY - 1 = binary MAC, 2 = BINARY PC, 5 = text output
NAXIE - 1 = front, 2 = rear
NSIDE - 1 = left, 2 = right
NSTEER - >0 ---> steer table (no. of T,SW pairs)
- =0 ---> sine function (harmonic SW)
- <0 ---> driver model (-no. of XPNT,YPNT pairs)
VEHICLE AERODYNAMIC, STEERING-SYSTEM, AND GENERAL PARAMETERS
AREA - VEHICLE CROSS-SECTION AREA (IN Y-Z PLANE)
QZERO - DENSITY * AREA / 2
KY - AERODYNAMIC SIDE FORCE COEFFICIENT
CLO,KL - AERODYNAMIC DOWN FORCE (-LIFT) COEFFICIENTS
KR . - AERODYNAMIC ROLL MOMENT COEFFICIENT
CMO,KM - AERODYNAMIC PITCH MOMENT COEFFICIENTS
KN - AERODYNAMIC YAW MOMENT COEFFICIENT
CDO,KD - AERODYNAMIC DRAG FORCE COEFFICIENTS
CBOOST - STEERING POWER-BOOST COEFFICIENT
CFSS - STEERING SYSTEM COULOMB FRICTION MOMENT
GR - STEERING-SYSTEM OVERALL KINEMATIC RATIO
GRTODG - GR (ABOVE) * TODEG
ISS - STEERING-SYSTEM MOMENT OF INERTIA - LUMPED AT STEER-WHL
KSC - STEERING-COLUMN STIFFNESS
KSL - STEERING LINKAGE STIFFNESS
SSKEY - STEERING-SYSTEM KEY TRIGGERING USE OF DYN ST SYS MODEL
XTRAIL - FRONT WHEEL MECHANICAL TRAIL
HCGTTL - TOTAL STATIC CG HEIGHT ABOVE GROUND
HCGSP - STATIC SPRUNG-MASS CG HEIGHT ABOVE GROUND
XCGSP - STATIC SPRUNG-MASS CG DISTANCE FROM FRONT AXLE
XWBCGS - SPRUNG-MASS CG DISTANCE AHEAD OF HALF-WHEELBASE POINT
XWBCGT - TOTAL CG DISTANCE AHEAD OF HALF-WHEELBASE POINT
WHLRAD - TIRE ROLIING RADIUS = ASSUMED UNSPRUNG-MASS CG HEIGHT
IXSCG - SPRUNG-MASS X-X MOMENT OF INERTIA (X-X THRU SPRUNG CG)
IXSRA - SPRUNG-MASS MOMENT OF INERTIA ABOUT ROLL AXIS
IXZ - SPRUNG-MASS XZ PRODUCT OF INERTIA
IYS - SPRUNG-MASS PITCH MOMENT OF INERTIA
IZZ - TOTAL YAN MOMENT OF INERTIA
KROLL - TOTAL ROLL STIFFNESS
MASS - TOTAL MASS
SPMASS - SPRUNG MASS
SPWGHT - SPRUNG WEIGHT
WEIGHT - TOTAL WEIGHT
USWGHT - UNSPRUNG WEIGHT
WRATIO - FRONT-AXIE NORMAL (GROUND) LOAD FRACTION OF TOTAL WEIGHT
WB - WHEELBASE
CSROLL - REAR BEAM-AXIE ROLL-STEER COEFFICIENT

```

Appendix D - Source Code
```

PER-AXIE PARAMETERS - INDEXED (AXIE)
XAXIE - DISTANCE FROM TOTAL CG TO AXIE (NEGATIVE FOR REAR)
TRACK - NOMINAL TRACK WIDTH (ASSUMED CONSTANT)
HOROLC - STATIC ROLL CENTER HEIGHT ABOVE GROUND
HCGSRC - STATIC ROLL CENTER HEIGHT BELOW SPRUNG CG (<O IF ABOVE)
FZOWHL - TIRE/ROAD STATIC NORMAL LOAD AT EACH WHEEL
KZ - SUSPENSION VERTICAL (RIDE) STIFFNESS AT EACH WHEEL
KZAXIE - SUSPENSION VERTICAL (RIDE) STIFFNESS (2 X KZ)
KAUX - SUSPENSION AUXILIARY ROLL STIFFNESS
KTIRE - TIRE VERTICAL STIFFNESS
CZJNCE - DAMPING COEFFICIENT IN JOUNCE AT EACH WHEEL
CZRBND - DAMPING COEFFICIENT IN REBOUND AT EACH WHEEL
CSFY - FY (CORNERING-FORCE) COMPLIANCE-STEER COEFFICIENT
CSMZ - ALIGNING-MOMENT COMPLIANCE-STEER COEFFICIENT
CCFY - FY COMPLIANCE-CAMBER COEFFICIENT (O FOR BEAM AXLE)
KINEMATIC Z-POLYNOMIAL COEFFICIENTS (2 X 2) - INDEXED (AXLE,POWER)
CSZ - BUMP-STEER COEFFICIENTS
CCZ - BUMP-CAMBER COEFFICIENTS
YROLCF - R.C. LATERAL DISP. VS ROLL IN SPRUNG MASS COEFFICIENTS
HROLCF - R.C. VERTICAL DISP. VS ROLL IN SPRUNG MASS COEFFICIENTS
PER-WHEEL (2 X 2 ARRAY) VARIABLES - INDEXED (AXIE,SIDE)
ALFA - TIRE SLIP ANGLE
GAMMA - TIRE CAMBER ANGLE
ALFAO - STATIC TIRE SLIP ANGLE
GAMMAO - STATIC TIRE CAMBER ANGLE
FY - TIRE CORNERING FORCE DUE TO SLIP AND CAMBER
MZ - TIRE ALIGNING MOMENT
FD - SUSPENSION VERTICAL DAMPING FORCE
FZ - TIRE/ROAD NORMAL LOAD
ZW - SUSPENSION DYNAMIC VERTICAL DISPLACEMENT
KNMCBR - KINEMATIC (BUMP/ROLL) STEER ANGLE
KNMCBR - KINEMATIC (BUMP/ROLL) CAMBER ANGLE
TIRE FZ-POLYNOMIAL COEFFICIENTS (4 X 2) - indexed (AXIE,POWER)
CALFA - cornering-stiffness Fz-polynomial coefficients
CGAMMA - camber-stiffness Fz-polynomial coefficients
CALIGN - aligning-stiffness Fz-polynomial coefficients
SINUSOIDAL STEER PARAMETERS (for equation see function STEER)
TSWBGN - global time at steer start (prior to which: SW = 0)
TSWEND - global time at steer end (after which: SW is frozen)
TSWPRD - length of period (sec)
SWPHSE - time phase lead (deg, e.g. +90 ---> cosine)
SWAMPL - amplitude (steering wheel deg)
SWSHFT - amplitude zero shift (steering wheel deg)

```
```

C
C MAIN PROGRAM
C
C
IMPLICIT REAL (K,M)
EXTERNAL FUNCTN
REAL Y(13), YP(13), YM(13)
CHARACTER AGAIN
INTEGER*2 HOUR, MIN, SEC, I100
C
include DRVMOD.inc
include GLBL.inc
include PARS.inc
include SUSP.inc
include AERO.inc
include vars.inc
include PRNT.inc
include mnvr.inc
C
DATA T/0.0/, Y/13*0.0/
PI = 4.0 * ATAN(1.0)
C
C Read input data (includes opening all i/o files)
C
CALL INDATA
CALL INIT
C
C Initialize Driver Model Vehicle Parameters:
C
IF (NSTEER .LT. 0) THEN
IF (ABS (SSKEY) .LE. 0.001) THEN
CALL DRIVGO
ELSE
IF(NSTEER .GT. -100) CALL DRIVGT
ENDIF
ENDIF
C
C Set up output file with simulated time histories
C
CALL OPNOUT
C
C Start by evaluating derivatives and printing variables at t=0
CMD--Use function TIME for Mac (1 line)
CALL TIME (ISEC1)
CMD--Use function GETTIM for IBM PC (2 lines)

* CALL GETTIM (HOUR, MIN, SEC, I100)
* ISEC1 = 3600*HOUR + 60*MIN + SEC + I100*.01
CALL FUNCTN (T, Y, YP)
CALL OUTPUT (T, Y, YP)
C
C Integration loop. Continue until printout time reaches final time.
C Begin each step by allowing subroutines to update internal variables.
C Then use two evaluations of the derivatives to integrate over the
C step.
C
NLOOP = TEND/DT/IPRINT+1
DT2 = DT / 2.
DO 40 ILOOP=1,NLOOP

```
```

        DO 30 INNER=1,IPRINT
            DO }10\mathrm{ I=1,NEQN
                YM(I) = Y(I) + DT2 * YP(I)
    10 CONTINUE
        CALL FUNCTN (T+DT2, YM, YP)
        DO 20 I=1,NEQN
            Y(I) = Y(I) + DT * YP(I)
    CONTINUE
        T = T + DT
        CALL FUNCTN (T, Y, YP)
    30 CONTINUE
        CALL OUTPUT (T, Y, YP)
        IF (T .GE. TEND) go to 50
    40 CONTINUE
    50 CONTINUE
    CMD--Use function TIME for Mac (1 line)
CALL TIME (ISEC2)
CMD--Use function GETTIM for IBM PC (2 lines)

* CALL GETTIM (HOUR, MIN, SEC, I100)
* ISEC2 = 3600*HOUR + 60*MIN + SEC + I1O0*.01
* End of integration loop. Print final status of run
WRITE (*, *) ' Termination at time =', T, ' sec.'
WRITE (*,*) ' Computation efficiency: ', (ISEC2 - ISEC1) / T,
\& ' sec/sim. sec'
WRITE (*,*) ' '
CLOSE (IOUT)
PAUSE 'Done'
END
SUBROUTINE AIRACT (T, YAW, BETA, VYAW)
C Subroutine AIRACT updates air velocity and sideslip, and the
C magnitudes of all corresponding aerodynamic forces and moments
C in the common block /AERO/
C
IMPLICIT REAL (K,M)
C
include GLBL.inc
include PARS.inc
include AERO.inc
C
C Look up wind magnitude from TABLE, or, get from user-defined "FWIND"
C function. TABLE and FWIND return VWIND in units of kmh or mph.
C
VWIND = 0.0
IF (WINDKY .GT. 0) THEN
CALL TABLE (1, WINDKY, TWIND, WINMAG, T, VWIND)
ELSE
VWIND = 0.0
IF (WINDKY .LT. 0) VWIND = FWIND (T)
ENDIF
C
C CONVERT VWIND TO INTERNAL UNITS OF M/SEC OR IN/SEC:
C

```
```

        VWIND = VWIND / KMHMPH
    ```

C
C CALCULATE AIR SLIP AND VELOCITY:
```

RELKSY = KSYWND - YAW
VAX = (VWIND * COS (RELKSY) - V * COS (BETA)) / ININFT
VAY = (VWIND * SIN(RELKSY) - V * SIN (BETA)) / ININFT
VAY = VAY - XWBCGS * VYAW / ININFT
VA2 = VAX * VAX + VAY * VAY
VA = SQRT (VA2)
BETAIR = 0.0
IF (VAY .GT. 0.0) BETAIR = (ATAN2 (VAY, VAX) - PI) * TODEG
IF (VAY .LT. 0.0) BETAIR = (ATAN2 (VAY, VAX) + PI) * TODEG
BETA2 = BETAIR * BETAIR

```

C
C CALCULATE AERODYNAMIC FORCES AND MOMENTS ACTING
C AT GROUND LEVEL, AT half wheelbase point:
C
\(\mathrm{CY}=-\mathrm{KY} *\) BETAIR
FYA \(=\) QZERO * CY * VA2
C
\(\mathrm{CL}=\mathrm{CL} 0+\mathrm{KL}\) * BETA2
\(\mathrm{FZA}=-\mathrm{QZERO} * \mathrm{CL} *\) VA2
C
\(\mathrm{CR}=-\mathrm{KR} *\) BETAIR
MXA \(=\) QZERO * WB * CR * VA2
C
\(\mathrm{CM}=\mathrm{CMO}+\mathrm{KM}\) * BETA2
MYA \(=\) QZERO * WB * CM * VA2
C
\(\mathrm{CN}=-\mathrm{KN} *\) BETAIR
MZA \(=\) QZERO * WB * CN * VA2
C
\(C D=C D O+K D * \operatorname{BETA} 2\)
FDRAG \(=\) QZERO * CD * VA2
C
C RESOLVE MOMENTS ABOUT SPRUNG OR TOTAL CG, AS APPROPRIATE:
MXA \(=\) MXA - HCGSP * FYA
MYA \(=\) MYA + XWBCGS * FZA
MZA \(=\) MZA - XWBCGT * FYA
C
RETURN
END
BLOCK DATA
* Initialize variables in common blocks.

C
IMPLICIT REAL (K, M)
C
include GLBL.inc
include PARS.inc
include MNVR.inc
include SUSP.inc
include TIRE.inc
include AERO.inc
include VARS.inc
Appendix D - Source Code
D-8
include PRNT.inc
DATA NEQN/13/, NSTEER/1/, TODEG/1.0/, SW/0.0/, FW/2*0.0/, AY/0.0/ DATA RHO/0.0/, KROLL/0.0/, CSROLL/0.0/, CSZ/4*0.0/, CCZ/4*0.0/ DATA ALFA/4*0.0/, GAMMA/4*0.0/, FY/4*0.0/, MZ/4*0.0/, FD/4*0.0/ DATA \(2 \mathrm{~W} / 4 * 0.0 /\), YROLCF/4*0.0/, HROLCF/4*0.0/
DATA KNMSTR/4*0.0/, CPLSTR/4*0.0/, TTLSTR/4*0.0/, KNMCBR/4*0.0/ DATA YOUTDR/13*0.0/, STORQ/0.0/, MMCOL/0.0/

DATA TSWBGN/0.0/, TSWEND/0.0/, SWAMPL/0.0/, TSWPRD/0.0/
DATA SWPHSE/0.0/, SWSHFT/0.0/, DRLAG/0.0/, DRPREV/0.0/
DATA VA/0.0/, BETAIR/0.0/, FYA/0.0/, FZA/0.0/, FZ/4*0.0/
DATA MXA/0.0/, MYA/0.0/, MZA/0.0/, FDRAG/0.0/
DATA XPNT/999*0.0/, YPNT/999*0.0/, SLOPE/999*0.0/
C
DATA G/9.81/, ININFT/1/, KMHMPH/3.6/, UOMEGA/'rad/sec'/ DATA UDISP/'m'/, UDIST/'m'/, UANGL/'rad'/, UVELFT/'m/s'/ DATA UFORC/'N'/, UTORQ/'m-N'/, KINEM/.TRUE./, BEAM/.TRUE./ DATA LINE/-1/, NPAGE/1/, INDX/0/, BLNK12/' DATA FNREAD /' '/
C

\section*{END}

\section*{ \\ C \\ C DRIVE1: Reads Driver Model (Path, Preview, Lag) Parameters->unit IREAD \\ C \\ \(\mathrm{C}=\) Author and Modification Section}

C
\begin{tabular}{lll} 
C & Author: & C. C. MacAdam \\
C & Date written: & \(05 / 19 / 88\) \\
C & \\
C & Written on: \\
C & \\
C & \\
Modifications:
\end{tabular}
\(\mathrm{C}=\) Algorithm Description
Purpose and use:
Error conditions:
Machine dependencies: none
Called By: INDATA
    SUBROUTINE DRIVE1 (DFW)
    SAVE

C
C
C---Arguments passed:
C
```

C DFW...steer angle of front tires [or average] (rad)
C
C---COMMON blocks
C
include drvmod.inc
include pars.inc
include glbl.inc
C
C---DRIV.BLK common block variables--------------------------------------------
-
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS..wheelbase of vehicle (center-line of front \& rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....X-Y path coords(SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
C TFF......driver model preview time [input parameter] (sec)
C RM.......vehicle mass (slug)
C A........distance from c.g. to front suspension center-line (ft)
C B........distance from c.g. to rear suspension center-line (ft)
C RI.......total vehicle yaw inertia (slug-ft)
C PSIO.....current yaw angle reference value (rad)
C NTF......number of points in the preview time interval
C NP.......number of points in the x-y trajectory table
C TLAST....last time driver model calulated a steer value (sec)
C DFWLST...last value of steer calculated by driver model (rad)
C TILAST...last sample time driver model calulated a steer value (sec)
C DMEM.....2-dim array (time \& steer history) used in delay calculat'n
C XT,YT....transformation of XP,YP in vehicle body axes (ft)
C
C---Local variables
C
C WGHT..total static weight on front and rear suspsensions (lb)
C DFW...steer angle of front tires [or average] (rad)
C
C---Functions and subroutines---------------------------------------------------
C
C None
C

```

```

C

```

```

C
GRAV = 32.2
TICYCL = 0.0099
TSS = 0.0
DMAX = 0.2
Appendix D - Source Code

```
C
    DO 40 J = 1, NP
        READ (IREAD,30) XPDR(J), YPDR(J)
    30 FORMAT (2F12.4)
    4O CONTINUE
    READ (IREAD,60) TAUMEM, TFF
    60 FORMAT (F12.4)
C
    PSIO = 0.0
    NTF = 10
    DO 80 J = 1, NP
        XT(J) = XPDR(J) * COS(PSIO) + YPDR(J) * SIN(PSIO)
        YT(J) = -XPDR(J) * SIN(PSIO) + YPDR(J) * COS (PSIO)
    80 CONTINUE
    TLAST = 0.
    DFWLST = 0.
    TIIAST = 0.
    DFW = 0.
    DO 90 I = 1, 100
        DMEM (I,1) = 0.
    90 DMEM(I,2) = -1.
    RETURN
    END
C************************************************************************************
C
C Closed-Loop Steer Calculation
C
C DRIVER: Computes closed-loop steering control during the simulation
C
```



```
C
Author: C. C. MacAdam
Date written: 05/19/88
Written on:
Modifications:
```



```
C
C
```



```
Purpose and use:
Error conditions:
References:
    MacAdam, C.C. "Development of Driver/Vehicle Steering
        Interaction Models for Dynamic Analysis," Interim
        Technical Report, U.S. Army Tank Automotive Command
        Contract No. DAAE07-85-C-R069, The University of
        Michigan Transportation Research Institute Report
        No. UMTRI-86-41, July 1986.
        MacAdam, C.C. "Application of an Optimal Preview Control
        for Simulation of Closed-Loop Automobile Driving,"
```

```
C
C
        SUBROUTINE DRIVER(X, Y, DFW, DFWNOW)
        SAVE
C
C=}\mathrm{ Variable Descriptions
C
C---Arguments passed:
C
C X.......time in the simulation (sec)
C Y.......current state vector obtained from WIND/STEER
C DFW.....closed-loop steering control returned to WIND/STEER
C DFWNOW..current steering angle [average] of front wheels,
C after effects of roll-steer, compliance, etc.
C
        DIMENSION Y(5), YC(5)
        DIMENSION DUMV11(4)
        DIMENSION DUMV1(4), VECM(4)
        DIMENSION DUMM1 (4,4), DUMM2 (4,4)
        DIMENSION FFV(4)
C
C---COMMON blocks----------------------------------------------------------------
C
    include drvmod.inc
    include pars.inc
    include aero.inc
    include glbl.inc
C
C---DRIV.BLK common block variables--------------------------------------------
-
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS.,wheelbase of vehicle (center-line of front & rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....X-y path coords(SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
```

| C | TFF.....driver model preview time [input parameter] (sec) |
| :---: | :---: |
| C | RM.......vehicle mass (slug) |
| C | A.......distance from c.g. to front suspension center-line (ft) |
| C | B........distance from c.g. to rear suspension center-line (ft) |
| C | RI.......total vehicle yaw inertia (slug-ft) |
| C | PSIO.....current yaw angle reference value (rad) |
| C | NTF......number of points in the preview time interval |
| C | NP.......number of points in the x-y trajectory table |
| C | TLAST....last time driver model calulated a steer value (sec) |
| C | DFWLST...last value of steer calculated by driver model (rad) |
| C | TILAST...last sample time driver model calulated a steer value (sec) |
| C | DMEM.....2-dim array (time \& steer history) used in delay calculat'n |
| C | $X T, Y T . . . . t r a n s f o r m a t i o n ~ o f ~ X P, ~ Y P ~ i n ~ v e h i c l e ~ b o d y ~ a x e s ~(f t) ~$ |
| C |  |
|  | -TRSSTR.BLK common block variables |
| C |  |
| C | TTT.......transition matrix at 10 discrete points in preview interval |
| C | TTT1......integral of trans matrix wrt preview time |
| C | GV.........vector of control gain coefficients |
| C |  |
|  | Local variables |
| C |  |
| C | YC.......local (body-axis based) copy of state vector Y |
| C | VECM.....observer vector - lateral displacement from state vector |
| C | DUMV1....work vector |
| C | DUMV11... " |
| C | DUMM1....work matrix |
| C | DUMM2.... " |
| C | T........time in the simulation (sec) |
| C | EPSI....yyaw angle between body axis and current index value, PSIO |
| C | PSIO.....current nominal value of yaw angle used for linearization |
| C | NP.......number of points in $x-y$ path table |
| C | XP,YP....x-y inertial path table [input] (ft) |
| C | XT,YT....X-Y path table transformed to body axis [PSIO] system (ft) |
| C | EPSY2....cumulative preview path error squared |
| C | EPSY.....mean squared value of cumulative preview path error |
| C | TSUM.....scalar work quantity |
| C | SSUM.....scalar work quantity |
| C | DFWLST...steering control from last calculation (rad) |
| C | TJI......preview time ahead from present time value (sec) |
| C | I, J, K....integer counters |
| C | XCAR.....preview distance ahead in feet (ft) |
| C | X0.......present forward postion of vehicle c.g. (ft) |
| C | TTAB.....current time less the driver delay, TAUMEM. Used to access |
| C | the delayed driver response stored in DMEM array. (sec) |
| C | S1.......scalar work quantity |
| C | T1.......scalar work quantity |
| C | EP.......previewed path error (ft) |
| C | FFV......aerodynamic lateral accel and yaw accel "sensory" vector |
| C |  |
| C | -Functions and subroutines |
|  |  |
| C | EXTERNAL TRAJ, GMPRD |
|  |  |
|  |  |
| CCC |  |
|  | =Process Block |
|  |  |

C
$1 \mathrm{~T}=\mathrm{X}$
$\operatorname{EPSI}=\operatorname{ABS}(Y(4)-\operatorname{PSIO})$
DO $10 \mathrm{I}=1$, 5
$10 \mathrm{YC}(\mathrm{I})=\mathrm{Y}(\mathrm{I})$
IF (EPSI .LE. .0002) GO TO 30
Update Coordinate Transformation
PSIO $=Y(4)$
DO $20 \mathrm{~J}=1$, NP
$\operatorname{XT}(J)=\operatorname{XPDR}(J) * \operatorname{COS}(P S I O)+\operatorname{YPDR}(J) * \operatorname{SIN}(P S I O)$
$20 \mathrm{YT}(\mathrm{J})=-X P D R(\mathrm{~J}) * \operatorname{SIN}(\mathrm{PSIO})+\operatorname{YPDR}(\mathrm{J}) * \operatorname{COS}(P S I O)$
$30 \mathrm{YO}=-\mathrm{Y}(5) \star \operatorname{SIN}(\mathrm{PSIO})+Y(1) \star \operatorname{COS}(\mathrm{PSIO})$
$X 0=Y(5) \star \operatorname{COS}(P S I O)+Y(1) \star \operatorname{SIN}(P S I O)$
$Y C(1)=Y 0$
$\mathrm{YC}(4)=Y(4)-\mathrm{PSIO}$
EPSY2 $=0$.
TSUM $=0$.
SSUM $=0$.
DFW $=$ DFWLST

C Return if time from last calculation less than sample interval
IF ( $T$ - TILAST .LE. TICYCL) RETURN
C
C
C Update tire cornering stiffnesses and vehicle velocity
C and recalculate transition matrix: Not Used Presently
*** COMMENTED OUT ***
CAFTEM $=($ CCAF1*FFZL1 + CCAF2*FFZL2 $) /($ FFZL1 $1+F F Z L 2) ~$
CARTEM $=($ CCAR1*FFZL3+CCAR2*FFZL4) $/($ FFZL3+FFZL4)
CAF = CAFTEM
CAR = CARTEM
UTEMP = DMVELC
$\mathrm{U}=\mathrm{UTEMP}$
CALL TRANS
Loop to calculate optimal preview control per References $2 \& 3$ :
(NTF points within the preview interval)
DO $50 \mathrm{I}=1$, NTF
$\mathrm{TJI}=(\mathrm{TFF}-\mathrm{TSS}) / \mathrm{NTF} * \mathrm{I}+\mathrm{TSS}$
DO $40 \mathrm{~J}=1,4$
DO $40 \mathrm{~K}=1$, 4
$\operatorname{DUMM1}(J, K)=\operatorname{TTT1}(J, K, I)$
40
$\operatorname{DUMM2}(J, K)=\operatorname{TTT}(J, K, I)$

Appendix D - Source Code
D - 14

```
    CALL GMPRD (VECM, DUMM1, DUMV11, 1, 4, 4)
    CAIL GMPRD (VECM, DUMM2, DUMV1, 1, 4, 4)
    CALL GMPRD (DUMV1, YC, T1, 1, 4, 1)
```

    EP = T1 + S1 * DFWNOW + DYAERO - YPATH
    ```
    EP = T1 + S1 * DFWNOW + DYAERO - YPATH
    TSUM = TSUM + EP * S1
    TSUM = TSUM + EP * S1
    SSUM = SSUM + S1 * S1
    SSUM = SSUM + S1 * S1
C
C Cumulative preview error calculation (unrelated to control)
    EPSY2 = EPSY2 + EP * EP * (TFF - TSS) / NTF
C
    5 0 ~ C O N T I N U E ~
C
C Cumulative preview error calculation (unrelated to control)
C
    EPSY = SQRT (EPSY2) / (TFF - TSS)
C
C Optimal value - no delay yet.
C
C
C Maximum steer bound set at DMAX (arbitrary)
C
    IF (ABS (DFW) .GT. DMAX) DFW = DMAX * SIGN(1.,DFW)
C
C Store steer history and corresponding times in DMEM.
C Retrieve steer delayed by TAUMEM sec and return as
C delayed driver steer control, DFW.
C
    DO 60 J = 1, 2
        DO 60 I = 1, }9
            DMEM(101 - I,J) = DMEM(100 - I,J)
6 0 ~ C O N T I N U E ~
    DMEM(1,1) = DFW
    DMEM (1,2) = T
    TTAB = T - TAUMEM
    DO 70 I = 1, }9
        IJK = I
        IF (DMEM(I + 1,2) .LE. TTAB .AND. DMEM(I,2) .GE. TTAB)
    1 GO TO 90
7 0 ~ C O N T I N U E ~
    WRITE (*, 80) TAUMEM, DFW, X
80 FORMAT ('O', '***** TAUMEM PROBABLY TOO LARGE *****',
    & /,3(1X,G12.6))
        STOP
90 DFW = 0.0
    IF (T .GE. TAUMEM) DFW = DMEM(IJK,1)
```

```
C
C Save steer and time values for next calulation.
C
    DFWLST = DFW
    TLAST = X
    TILAST = X
        RETURN
        END
C
Closed-Loop Steer Calculation
C
C DRIVET: Computes closed-loop steering TORQUE control during the simul
C
C=_=_=_=_=_muthor and Modification Section
```



```
Author: C. C. MacAdam
C
C Date written: 01/30/89
C
C
C
C
C
C
Purpose and use:
C
C
C Called By: STEER (function)
C
C
    SUBROUTINE DRIVET (X, Y, DRTORQ, DRTNOW)
```

C

$$
\begin{aligned}
& \mathrm{C}= \\
& \mathrm{C} \\
& \mathrm{C}- \\
& \mathrm{C} \\
& \mathrm{C} \\
& \mathrm{C} \\
& \mathrm{C} \\
& \mathrm{C} \\
& \mathrm{C}
\end{aligned}
$$

C---Arguments passed:
C X........time in the simulation (sec)
C Y........current state vector obtained from WIND/STEER
C DRTORQ.....closed-loop TORQUE control returned to WIND/STEER
C DRTNOW.....current steering TORQUE

```
DIMENSION Y(7), YC(7)
DIMENSION DUMV11(6)
DIMENSION DUMV1 (6), VECM(6)
DIMENSION DUMM1 (6,6), DUMM2 (6,6)
DIMENSION FFV(6)
```

C
C---COMMON blocks
C
include drvtor.inc
include pars.inc
include aero.inc include glbl.inc include vars.inc

C

C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS.. wheelbase of vehicle (center-line of front \& rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
c
C---DRVST1.BLK common block variables
C
C GRAV..-..gravitational constant
C TICYCL...driver model sample time (sec)
C TSS.......minimum preview time (sec)
C DMAX......upper bound on front wheel angle steer (rad)
C XP,YP.... $\mathrm{x}-\mathrm{y}$ path coords (SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
C TFF......driver model preview time [input parameter] (sec)
C RM........vehicle mass (slug)
C A........distance from C.g. to front suspension center-line (ft)
C B.........distance from c.g. to rear suspension center-line (ft)
C RI.......total vehicle yaw inertia (slug-ft)
C PSIO.....current yaw angle reference value (rad)
C NTF.......number of points in the preview time interval
C NP.......number of points in the $x-y$ trajectory table
C TLAST....last time driver model calulated a steer value (sec)
C STLST...last value of steer calculated by driver model (rad)
C TILAST...last sample time driver model calulated a steer value (sec)
C DMEM.....2-dim array (time \& steer history) used in delay calculat'n
C XT,YT....transformation of $X P, Y P$ in vehicle body axes (ft)
C
C---TRSSTR.BLK common block variables
C

Appendix D - Source Code

```
C TTT.......transition matrix at 10 discrete points in preview interval
C TTT1......integral of trans matrix wrt preview time
C GGV.........vector of control gain coefficients
C
C---Local variables
C
C YC.......local (body-axis based) copy of state vector Y
C VECM.....observer vector - lateral displacement from state vector
C DUMV1....work vector
C DUMV11... "
C DUMM1....work matrix
C DUMM2.... "
C T........time in the simulation (sec)
C EPSI.....yaw angle between body axis and current index value, PSIO
C PSIO.....current nominal value of yaw angle used for linearization
C NP.......number of points in x-y path table
C XP,YP....X-Y inertial path table [input] (ft)
C XT,YT....x-y path table transformed to body axis [PSIO] system (ft)
C EPSY2....cumulative preview path error squared
C EPSY.....mean squared value of cumulative preview path error
C TSUM.....scalar work quantity
C SSUM.....scalar work quantity
C DFWLST...steering control from last calculation (rad)
C TJI......preview time ahead from present time value (sec)
C I,J,K....integer counters
C XCAR.....preview distance ahead in feet (ft)
C XO.......present forward postion of vehicle c.g. (ft)
C TTAB.....current time less the driver delay, TAUMEM. Used to access
C the delayed driver response stored in DMEM array. (sec)
C Sl.......scalar work quantity
C T1.......scalar work quantity
C EP.......previewed path error (ft)
C FFV......aerodynamic lateral accel and yaw accel "sensory" vector
C & power boost influence
C
C---Functions and subroutines-------------------------------------------------
C
        EXTERNAL TRAJ, GMPRD
C
C
C=_=_=__=_=_
C
C
    DATA VECM /1.0, 5*0.0/
    DATA STLST /0.0/
C
C Update Aerodynamic accel (force/moment) vector for driver model:
C
        FFV(1) = 0.0
        FFV(2) = FYA / RM * WEIGHT / SPWGHT
        FFV(3) = MZA / ININFT/ RI
        FFV(4) = 0.0
        FFV(5) = 0.0
        FFV(6) = 0.0
C
    1 T = X
        EPSI = ABS (Y(4) - PSIO)
Appendix D - Source Code
```

        DO 10 I = 1, 7
    10 YC(I) = Y(I)
    C IF (EPSI .LE. .0002) GO TO 30
C
C Update Coordinate Transformation
C
PSIO = Y(4)
DO 20 J = 1, NP
XT(J) = XPDR(J) * COS(PSIO) + YPDR(J) * SIN(PSIO)
20 YT(J) = -XPDR(J) * SIN(PSIO) + YPDR(J) * COS(PSIO)
C
30 YO = -Y(7) * SIN(PSIO) + Y(1) * COS (PSIO)
XO = Y(7) * COS (PSIO) + Y(1) * SIN(PSIO)
YC(1) = YO
YC(4) = Y(4) - PSIO
EPSY2 = 0.
TSUM = 0.
SSUM = 0.
DRTORQ = STLST
Return if time from last calculation less than sample interval
IF (T - TILAST .IT. TICYCL) RETURN
C
C
Update tire cornering stiffnesses and vehicle velocity
and recalculate transition matrix: Not Used Presently
*** COMMENTED OUT
CAFTEM = (CCAF1*FFZL1+CCAF2*FFZL2) / (FFZL1+FFZL2)
CARTEM = (CCAR1*FFZL3+CCAR2*FFZL4) / (FFZL3+FFZL4)
CAF = CAFTEM
CAR = CARTEM
UTEMP = DMVELC
U = UTEMP
CALU TRANST
Loop to calculate optimal preview control per References 2 \& 3:
(NTF points within the preview interval)
DO 50 I = 1, NTF
TJI = (TFF - TSS) / NTF * I + TSS
DO 40 J = 1, 6
DO 40 K = 1, 6
DUMM1 (J,K) = TTTT1 (J,K,I)
40 DUMM2 (J,K) = TTTT (J,K,I)
CALI GMPRD (VECM, DUMM1, DUMV11, 1, 6, 6)
CALI GMPRD (VECM, DUMM2, DUMV1, 1, 6, 6)
CALI GMPRD (DUMV1, YC, T1, 1, 6, 1)
C
C Get observed path input, YPATH, within preview interval at XCAR ft:
XCAR = XO + U * TJI
CALL TRAJ(XCAR, XT, YT, YPATH)
CALL GMPRD (DUMV11, GGV, S1, 1, 6, 1)
CALL GMPRD (DUMV11, FFV, DYAERO, 1, 6, 1)
C

```
```

C EP is the previewed path error at this preview point.
EP = T1 + S1 * DRTNOW + DYAERO - YPATH
TSUM = TSUM + EP * S1
SSUM = SSUM + S1 * S1
C
C Cumulative preview error calculation (unrelated to control)
C
C
5 0 ~ C O N T I N U E ~
C
C Cumulative preview error calculation (unrelated to control)
C
EPSY = SQRT (EPSY2) / (TFF - TSS)
C
C Optimal value - no delay yet.
C
DRTORQ = -TSUM / SSUM + DRTNOW
C
C Maximum steer bound set at STMAX (arbitrary)
C
IF (ABS (DRTORQ) .GT. STMAX) DRTORQ = STMAX * SIGN(1.,DRTORQ)
C
C Store torque history and corresponding times in DMEM.
C Retrieve steer delayed by TAUMEM sec and return as
C delayed driver torque control, DRTORQ.
DO 60 J = 1, 2
DO 60 I = 1, 99
DMEM(101 - I,J) = DMEM(100 - I,J)
6 0 ~ C O N T I N U E ~
DMEM (1,1) = DRTORQ
DMEM (1,2) = T
TTAB = T - TAUMEM
DO }70\mathrm{ I = 1, }9
IJK = I
IF (DMEM(I + 1,2) .LT. TTAB .AND. DMEM(I,2) .GE. TTAB)
1 GO TO 90
7 0 ~ C O N T I N U E
WRITE (*,80) TAUMEM, DRTORQ,X
80 FORMAT ('0', '***** TAUMEM PROBABLY TOO LARGE *****',
\& /,3(1X,G12.6))
STOP
90 DRTORQ = 0.0
IF (T .GE. TAUMEM) DRTORQ = DMEM(IJK,1)
C
C Save steer and time values for next calculation.
STLST = DRTORQ
TLAST = X
TILAST = X
RETURN
END
C*****************************************************************************
C
C *** CHRYSLER Initialization Entry for the Driver Model

```
```

C
C DRIVGO: Intializes driver model vehicle-based parameters from COMMONS
C
C=__Author and Modification Section=
C
C Author: C. C. MacAdam
C
C Date written: 05/19/88
C
C Written on: Mac II
C
C Modifications:
C
C
C=__=_=_=_=_
C
C Purpose and use:
C
C Error conditions:
C
C References:
C
C MacAdam, C.C. "Development of Driver/Vehicle Steering
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C Machine dependencies: none
C
C Called By: INDATA
C
C
SUBROUTINE DRIVGO
SAVE
C
C=__=_Variable Descriptions=____m_m
C
C---Arguments passed: None
C
C
C---COMMON blocks--------------------------------------------------------------------
C
include drvmod.inc
include pars.inc

```
        include glbl.inc
        include tire.inc
        include vars.inc
C
C---DRIV.BLK common block variables------------------------------------------
-
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS..wheelbase of vehicle (center-line of front & rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....X-Y path coords(SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
C TFF......driver model preview time [input parameter] (sec)
C RM.......vehicle mass (slug)
C A........distance from c.g. to front suspension center-line (ft)
C B........distance from c.g. to rear suspension center-line (ft)
C RI.......total vehicle yaw inertia (slug-ft)
C PSIO.....current yaw angle reference value (rad)
C NTF......number of points in the preview time interval
C NP.......number of points in the x-y trajectory table
C TLAST....last time driver model calulated a steer value (sec)
C DFWLST...last value of steer calculated by driver model (rad)
C TILAST...last sample time driver model calulated a steer value (sec)
C DMEM.....2-dim array (time & steer history) used in delay calculat'n
C XT,YT....transformation of XP,YP in vehicle body axes (ft)
C
C---Local variables-------------------------------------------------------------
C
C A.....distance from c.g. to front suspension center-line (ft)
C B.....distance from c.g. to rear suspension center-line (ft)
C WGHT..total static weight on front and rear suspsensions (lb)
C RM....total static mass (slug)
C DFW...steer angle of front tires [or average] (rad)
C
C---Functions and subroutines-------------------------------------------------
C
    EXTERNAL TRANS
C
```



```
C
```



```
C
C
    WGHT = WEIGHT
    B = WRATIO * WB / 12.
    A = (1. - WRATIO) * WB / 12.
    RM = WGHT / GRAV
    WHBS = A + B
```

```
            WF = WGHT * B / WHBS
            WR = WGHT * A / WHBS
C RI = A * B * RM
    RI = IZZ / 12.
C
C Initial Tire Cornering Stiffnesses for Driver Model (lb/rad):
C (flip sign from SAE convention to positive values here)
C
        CAF = 0.0
        CAR = 0.0
        DO 30 NAXIE = 1, 2
            DO 20 NSIDE = 1, 2
                CALF = 0.0
                    DO 10 NPOWER = 1, 4
                    CALF = CALF
            1 + CALFA (NPOWER,NAXIE) * FZ (NAXIE,NSIDE) ** (NPOWER-1)
        10 CONTINUE
            IF (NAXLE .EQ. 1) CAF = CAF - 0.5 * CALF
            IF (NAXLE .EQ. 2) CAR = CAR - 0.5 * CALF
        20 CONTINUE
        30 CONTINUE
C
C Speed in ft/sec:
    U = V * KMHMPH * 88. / 60.
C
C
C Call TRANS to Calculate Transition Matrix
    CAL工 TRANS
C
    RETURN
    END
*)
C**********************************************************************************
C
C *** CHRYSLER Initialization Entry for the Driver Model ***
C
C DRIVGT: Intializes driver model vehicle-based parameters from COMMONs
C
```



```
C
C Author: C. C. MacAdam
C
C Date written: 01/30/89
C
C Written on: Mac II
C
Modifications:
C
C
```



```
C
C Purpose and use:
C
C Error conditions:
C
```

```
    References:
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C
C Machine dependencies: none
C
C Called By: INDATA
C
    SUBROUTINE DRIVGT
    SAVE
C
```



```
C
C---Arguments passed: None
C
C
C---COMMON blOcks------------------------------------------------------------
C
    include drvtor.inc
    include pars.inc
    include glbl.inc
    include tire.inc
    include vars.inc
C
C---DRIV.BLK common block variables-------------------------------------------
-
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS..wheelbase of vehicle (center-line of front & rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....x-y path coords(SAE) wrt inertial coords [input] (ft)
```

| C | TAUMEM...driver transport time dealy [input parameter] (sec) |
| :---: | :---: |
| C | TFF......driver model preview time [input parameter] (sec) |
| C | RM.......vehicle mass (slug) |
| C | A.......distance from c.g. to front suspension center-line (ft) |
| C | B........distance from c.g. to rear suspension center-line (ft) |
| C | RI.......total vehicle yaw inertia (slug-ft) |
| C | PSIO.....current yaw angle reference value (rad) |
| C | NTF......number of points in the preview time interval |
| C | NP.......number of points in the $x-y$ trajectory table |
| C | TLAST....last time driver model calulated a steer value (sec) |
| C | DFWLST...last value of steer calculated by driver model (rad) |
| C | TILAST...last sample time driver model calulated a steer value (sec) |
| C | DMEM.....2-dim array (time \& steer history) used in delay calculat'n |
| C | XT,YT....transformation of XP, YP in vehicle body axes (ft) |
| C |  |
| C---Local va |  |
| C |  |
| C | A.....distance from c.g. to front suspension center-line (ft) |
| C | B.....distance from c.g. to rear suspension center-line (ft) |
| C | WGHT..total static weight on front and rear suspsensions (lb) |
| C | RM....total static mass (slug) |
| C | DFW...steer angle of front tires [or average] (rad) |
| C |  |
| C---Functions and subrou |  |
| C |  |
| EXTERNAL TRANS |  |
| C |  |
| C |  |
| C |  |
| $\mathrm{C}=\square=$ Process Bl |  |
| C |  |
| C |  |
|  | WGHT = WEIGHT |
| $\mathrm{B}=$ WRATIO * WB / 12. |  |
| $\mathrm{A}=$ (1. - WRATIO) $*$ WB / 12. |  |
| RM = WGHT / GRAV |  |
| WHBS $=\mathrm{A}+\mathrm{B}$ |  |
| WF = WGHT * B / WHBS |  |
| WR = WGHT * A / WHBS |  |
| C | $R I=A * B * R M$ |
|  | RI $=12 Z / 12$. |
| STMAX $=1000$. |  |
| C |  |
| C Initial Tire Cornering Stiffnesses for Driver Model (lb/rad): |  |
| C | (flip sign from SAE convention to positive values here) |
|  | C |
|  | $C A F=0.0$ |
|  | $C A R=0.0$ |
| DO 30 NAXLE $=1,2$ |  |
| DO 20 NSIDE $=1,2$ |  |
| CALF $=0.0$ |  |
| DO 10 NPOWER $=1,4$ |  |
|  | CALF = CALF |
|  | 1 + CALFA (NPOWER, NAXIE) * FZ (NAXIE,NSIDE) ** (NPOWER-1) |
|  | 10 CONTINUE |
|  | IF (NAXIE .EQ. 1) $\mathrm{CAF}=\mathrm{CAF}-0.5 *$ CALF |
|  | IF (NAXIE .EQ. 2) CAR = CAR - 0.5 * CALF |
|  | 20 CONTINUE |

30 CONTINUE
C
C Speed in ft/sec:
C
$\mathrm{U}=\mathrm{V} * \mathrm{KMHMPH} * 88 . / 60$.
C
C
C Call TRANS to Calculate Transition Matrix
CALL TRANST
C
RETURN
END
SUBROUTINE ECHO

* Echo parameter values to file to verify that the input was
* interpreted correctly
include drvmod.inc
include GLBL.inc
include PARS.inc
include MNVR.inc
include SUSP.inc
include TIRE.inc
include AERO.inc
include PRNT.inc
CHARACTER* 32 FNECHO
CHARACTER*24 TIMEDT
LOGICAL ISIT
C
C Get name of echo file from user. Delete old file if it exists.
C
FNECHO $=1$,
WRITE(*, '(A<br>)') ' Name of (optional) parameter echo file: '
READ (*, ' (A)') FNECHO
IF (FNECHO .EQ. ' ') THEN
RETURN
ELSE
INQUIRE (FILE=FNECHO, EXIST=ISIT)
IF (ISIT) THEN
OPEN (IECHO, FILE=FNECHO)
CLOSE (IECHO, STATUS='DELETE')
END IF
OPEN (IECHO, FILE=FNECHO, STATUS='NEW')
END IF
WRITE (IECHO, ' (A/)')
\&' ECHO FROM WIND/HANDLING SIMULATION, V0.91'
WRITE (IECHO, '(A, A/)') ' Input file: ', FNREAD
CALL TIMDAT (TIMEDT)
WRITE (IECHO, ' $\left.(\mathrm{A}, \mathrm{A} /)^{\prime}\right)$ ' Run made at ', TIMEDT
WRITE (IECHO,' (A,A/)') ' TITLE: ', TITLE
WRITE (IECHO, ' (A/) ')
\& ' GENERAL SIMULATION INFORMATION:'
IF (UNITS .EQ. 'E' .OR. UNITS .EQ. 'e') THEN

```
            WRITE (IECHO,'(T5, A)') 'English Units'
            ELSE
                WRITE (IECHO,'(T5, A)') 'Metric Units'
            END IF
            WRITE (IECHO, '(T5,A,A)') 'Output format: ', FRMT
            WRITE (IECHO,'(T5,''V, TEND, DT:'',T30, 3G14.5)') V, TEND, DT
            IF (IPRINT .EQ. 1) THEN
            WRITE(IECHO, '(T5,A)') 'Write to file every time step'
            ELSE
            WRITE (IECHO, '(T5,A,I2,A)') 'Write to file every ', IPRINT',
        &. ' steps'
            END IF
            WRITE (IECHO,'(T5, ''KSYWND, AIRHO:'', T30, 2G14.5)')
        1 KSYWND, AIRHO
    IF (WINDKY .GE. O) THEN
            WRITE (IECHO,'(/A/)') ' WIND MAGNITUDE TIME HISTORY INPUT:'
            DO 32, J=1, WINDKY
                WRITE (IECHO, '(3X, 2G14.5)') TWIND(J), WINMAG(J)
            CONTINUE
        ELSE
            WRITE (IECHO,'(/A/)')
        &
                    ' Wind input defined by user function FWIND'
            ENDIF
C
    IF (NSTEER .EQ. O) THEN
        WRITE (IECHO,'(/A/)') ' SINUSOIDAL STEER:'
        WRITE (IECHO,'(T8,''TSWBGN, TSWEND:'',T30,2G14.5)') TSWBGN,
    &
        WRITE (IECHO,'(T8,''SWSHFT, SWAMPL:'',T30,2G14.5)') SWSHFT,
    & SWAMPL
        WRITE (IECHO,'(T8,''TSWPRD, SWPHSE:'',T30,2G14.5)') TSWPRD,
    & SWPHSE
    ELSE IF (NSTEER .LT. O .AND. NSTEER .GT. -100) THEN
        WRITE (IECHO,'(/A/)') ' DRIVER MODEL INPUT:'
        WRITE (IECHO,'(T5,''DRLAG, DRPREV:'',T30,2G14.5)') TAUMEM, TFF
        WRITE(IECHO,'(/T5,A/)') 'X-Y path coordinates:'
        DO 35, J=1, ABS (NSTEER)
            WRITE (IECHO, '(3X, 2G14.5)') XPDR(J), YPDR(J)
    35 CONTINUE
    ELSE
        IF (NEQN .EQ. 11) THEN
            WRITE (IECHO,'(/A/)') ' STEER TABLE - time(sec), sw (deg):'
            DO 40, J=1, ABS (NSTEER)
                    WRITE (IECHO, '(3X, 2G14.5)') XPNT (J), YPNT (J)
                CONTINUE
            ELSE
                IF(NSTEER .GT.-100) THEN
                    WRITE (IECHO,'(/A/)') ' STEER TORQUE TABLE - time(sec), storq
    & (in-lbs):'
            DO 42, J=1, ABS (NSTEER)
                WRITE (IECHO, '(3X, 2G14.5)') XPNT (J), YPNT (J)
            CONTINUE
            ENDIF
        ENDIF
    END IF
C
C Total vehicle and sprung mass parameters:
Appendix D - Source Code
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```

C
WRITE (IECHO,' (/A/)') ' TOTAL VEHICTE AND SPRUNG MASS PARAMETERS:' WRITE (IECHO,'(T5, ''WEIGHT, SPWGET', WRATIO:'', T30, 3G14.5)')
1 WEIGHT, SPWGHT, WRATIO
WRITE (IECHO,'(T5, ''IXSCG, IYS, IZZ, IXZ:'', T30, 4G14.5)')
1 IXSCG, IYS, IZZ, IXZ
WRITE (IECHO,' (T5, ''WB, WHLRAD, HCGIMIL:'', T30, 3G14.5)')
1 WB, WHLRAD, HCGTTL
C
C Aerodynamic parameters:
C

```
WRITE (IECHO,'(/A/)') ' AERODYNAMIC PARAMETERS:'
WRITE (IECHO,'(T5, ''AREA:'', T30, G14.5)') AREA
WRITE (IECHO,'(T5, ''KY, KR, KN:'', T30, 3G14.5)') KY, KR, KN
WRITE (IECHO,'(T5, ''CLO, KL:'', T30, 2G14.5)') CLO, KL
WRITE (IECHO,'(T5, ''CMO, KM:'', T30, 2G14.5)') CMO, KM
WRITE (IECHO,'(T5, ''CDO, KD:'', T30, 2G14.5)') CDO, KD
```

C Steering system:
WRITE (IECHO, ' (/A/)') ' STEERING SYSTEM:'
WRITE (IECHO,'(T5, ''ISS, KSC, DIASH, KSL:'', T30, 4G14.5)') ISS, \& KSC, DLASH, KSL
WRITE (IECHO,'(T5, ''GR, XTRAIL, CSS:'', T30, 3G14.5)') GR,
\& XTRAIL, CSS
WRITE (IECHO,'(T5, ''CBOOST, SSKEY, CFSS:'', T30, 3G14.5)')
1 CBOOST, SSKEY, CFSS
IF (KINEM) THEN WRITE (IECHO, ' (/A)') \& ' NKINEM <> 0 -- Use full kinematics model' ELSE WRITE (IECHO, ' (/A)')
\& ' NKINEM = 0 -- Use simple kinematics model' END IF
C
IF (BEAM) THEN
WRITE (IECHO, '(/A)') ' BEAM <> 0 -- Beam rear suspension' ELSE

WRITE (IECHO, '(/A)') ' BEAM = 0 -- Independent rear suspension' END IF

DO 80, NAXLE=1, 2
C
C
Suspension and tire data:

```
    WRITE (IECHO,' (/'' AXIE NUMBER'', I2,
    1 //T5,''Suspension and tire data'')') NAXLE
    WRITE (IECHO,'(T7, ''TRACK, HOROLC:'', T30, 2G14.5)')
                                    TRACK (NAXIE), HOROLC (NAXIE)
    WRITE(IECHO,'(T7, ''KZ, KAUX:'', T30, 2G14.5)')
                            KZ (NAXLE), KAUX (NAXLE)
    WRITE (IECHO,'(T7, ''CZJNCE, CZRBND:'', T30, 2G14.5)')
    1 CZJNCE (NAXIE), CZRBND (NAXIE)
    WRITE (IECHO,'(T7, ''ALFAO, GAMMA0:'', T30, 2G14.5)')
    1 ALFAO (NAXLE), GAMMAO (NAXIE)
C Kinematic coefficients:
```

C

```
C
    IF (KINEM) THEN
        WRITE(IECHO,'(/T5,A)') 'Kinematic coefficients:'
        WRITE (IECHO,'(T7, A, T30, 2G14.5)')
        'YROLCF:', YROLCF (NAXLE,1), YROLCF (NAXLE, 2)
        WRITE (IECHO,' (T7, A, T30, 2G14.5)')
            'HROLCF:', HROLCF (NAXIE,1), HROLCF (NAXIE, 2)
        IF (BEAM .AND. NAXLE .EQ. 2) THEN
        WRITE (IECHO,'(T7, A, T30, G14.5)')
                            'Rear axle roll steer: ', CSROLL
        ELSE
            WRITE (IECHO,'(T7, A, T30, 2G14.5)')
                            'CSZ: ', CSZ (NAXLE,1),'CSZ (NAXLE, 2)
        END IF
        WRITE (IECHO,'(T7, A, T30, 2G14.5)')
                            'CCZ: ', CCZ (NAXIE, 1), CCZ (NAXIE, 2)
        END IF
    Compliance coefficients:
    WRITE(IECHO,'(/T5,A)') 'Compliance coefficients:'
    WRITE (IECHO,'(T7, ''CSFY, CSMZ, CCFY:'', T30, 3G14.5)')
                CSFY (NAXLE); CSMZ (NAXLE), CCFY (NAXIE)
C
C
    Tire coefficients (positive stiffness input values assumed):
    WRITE(IECHO,'(/T5,A)') 'Tire stiffness coefficients:'
    WRITE (IECHO,'(T7, ''CALFA:'', T16, 4G14.5)')
                            (CALFA (J,NAXLE) , J=1, 4)
    WRITE (IECHO,'(T7, ''CGAMMA:'', T16, 4G14.5)')
        (CGAMMA (J, NAXIE), J=1, 4)
    WRITE (IECHO,'(T7, ''CALIGN:''', T16, 4G14.5)')
        (CALIGN(J,NAXLE), J=1, 4)
        WRITE(IECHO,'(T7, ''KTIRE:'', T16, G14.5)') KTIRE (NAXIE)
    80 CONTINUE
        CLOSE (IECHO)
        RETURN
    END
    SUBROUTINE FDAMP (VZ, VROLL, VPITCH, FD)
C SUBROUTINE FDAMP RETURNS FD, THE DAMPING FORCE ACTING AT EACH WHEEL
C -- ACCOUNTING FOR SEPARATE JOUNCE AND REBOUND COEFFICIENTS.
C POLARITY: NET JOUNCE VELOCITY => POSITIVE FD
C -------- NET REBOUND VELOCITY \Longrightarrow NEGATIVE FD
    IMPLICIT REAL (K,M)
    REAL FD (2,2)
C
    include SUSP.inc
C
    DO 20, NAXLE = 1, 2
        DO 10, NSIDE = 1, 2
            VDAMP = VZ - XAXIE (NAXIE) * VPITCH
        1 + .5 * TRACK (NAXIE) * VROLL * (-1) **NSIDE
            IF (VDAMP .GT. 0.0) THEN
            FD (NAXIE,NSIDE) = CZJNCE (NAXIE) * VDAMP
            ELSE
```

```
                    FD (NAXIE,NSIDE) = CZRBND (NAXIE) * VDAMP
                END IF
    10 CONTINUE
    20 CONTINUE
C
        RETURN
        END
            SUBROUTINE FUNCTN(T, Y, YP)
C SUBROUTINE FUNCTN DEFINES THE EQUATIONS OF MOTION FOR THE 5 D.O.F
C VEHICLE + THE 2 D.O.F STEERING SYSTEM (A SECOND ORDER SYSTEM FOR
C THE STEERING WHEEL INERTIA/COLUMN AND FIRST-ORDER SYSTEM FOR THE
C LOWER WHEEL ROTATIONAL MOTION (NO WHEEL INERTIA):
C YP(I) = F(Y, T), WHERE Y, YP ARE VECTORS, AND YP (I) = DY (I)/DT.
C STATE-VECTOR Y AND T ARE PASSED TO FUNCTN, AND VECTOR YP RETURNED.
C
        SAVE VSW1, VSW2
        IMPLICIT REAL (K,M)
        REAL IXSRA, Y(13), YP (13)
C
        include GLBL.inc
        include PARS.inc
        include SUSP.inc
        include AERO.inc
        include VARS.inc
        include TIRE.inc
        DATA VSW1, VSW2 /2*0.0/
        DATA ALF1, ALF2, ALF1PR, ALF2PR /4 * 0.0/
C
C
C CONVERT VECTOR Y INTO NAMES
C
        XG = Y(1)
        YG =Y(2)
        Z = Y(3)
        ROLL = Y(4)
        PITCH = Y(5)
        YAW = Y(6)
        VROLL = Y(7)
        VPITCH = Y(8)
        VYAW = Y(9)
        BETA = Y(10)
        VZ = Y(11)
C
C Steering System STATE Variables:
C
        IF (NEQN .EQ. 13) THEN
            VSW = Y(12)
            SW = Y(13)
            ENDIF
C
C GET CURRENT STEERING WHEEL ANGLE OR STEERING WHEEL TORQUE
C CONTROL INPUTS: (depending upon inclusion, or not, of steering sys)
    CONTRL = STEER(T)
    IF (NEQN .EQ. 11) THEN
        SW = CONTRL
Appendix D - Source Code

ENDIF
C
IF (NEQN .EQ. 13) THEN STORQ = CONTRL
ENDIF
C
C CALCULATE CURRENT GEOMETRY AND FORCES
C
CALL ROLLAX (ROLL, YROLAX, HROLAX, IXSRA)
CALL FDAMP (VZ, VROLL, VPITCH, FD)
CALL WHEELZ (Z, ROLL, PITCH)
CALL TIRSUB (BETA, V, VYAW, ROLL)
CALL AIRACT (T, YAW, BETA, VYAW)
C
C
C
C (I) ROLL MOMENT:
C

\section*{EQUATIONS OF MOTION}
```

MSHR = SPMASS * HROLAX
SUMFY = SUM(FY) + FYA
SUMMZ = SUM(MZ) + MZA + XAXIE (1)* (FY(1,1) + FY (1, 2))
\&
+ XAXIE (2)*(FY(2,1) + FY(2,2))
AROLL = (SPWGHT * YROLAX - IXZ / IZZ * SUMMZ + MXA
\& - KROLL * ROLL - MSHR / MASS * SUM(FY)
\& + .5 * TRACK (1)* (FD (1,1) - FD (1, 2))
\& + .5 * TRACK (2)* (FD (2,1) - FD (2,2)))
\& / (IXSRA - MSHR * MSHR / MASS - IXZ*IXZ/IZZ)

```

C
C (II) LATERAL FORCE:
C
```

VBETA = (SUMFY - MSHR * AROLL) / (MASS * V) - VYAW

```

C
C (III) YAW MOMENT:
AYAW \(=(\) SUMMZ - IXZ * AROLL \() /\) IZZ
C (IV) VERTICAL FORCE:
C \(\quad \mathrm{AZ}=(\) WEIGHT + FZA \(-\operatorname{SUM}(F Z)) /\) SPMASS
C (V) PITCH MOMENT:
C
```

        APITCH = (XAXLE (1) * (KZAXIE (1) * (Z - XAXLE (1) * PITCH)
        & + FD (1,1) + FD (1, 2))
        & + XAXIE (2) * (KZAXIE (2) * (Z - XAXIE (2) * PITCH)
        & + FD(2,1) + FD (2,2)) + MYA) / IYS
    C (VI) POWER-STEERING SYSTEM (Lash \& Coulomb Friction included):
IF (NEQN .EQ. 13) THEN

```
C
C
C

C
C Calculate equivalent single steering system stiffness based on input
\(C\) values for the steering column, steering linkage, and gear ratio:
C
    \(K S S=2 . * G R \star G R \star K S C \star K S L /(2 . * K S L+G R * G R * K S C)\)

Appendix D - Source Code

C
```

        XP1 = - POLY4 (CALIGN(1,1), FZ(1,1)) / POLY4(CALFA(1,1), FZ (1,1))
        XP2 = - POLY4 (CALIGN(1,1), FZ(1,2)) / POLY4(CALFA(1,1), FZ (1,2))
        XP = (XP1 + XP2) * 0.5
        CA1 = - POLY4 (CALFA (1,1), FZ (1,1))
        CA2 = - POLY4 (CALFA (1,1), FZ (1,2))
        CA = (CA1 + CA2) * 0.5
        XPM = XP + XTRAIL
    C Power Boost (cboost is percentage/100 contribution by pump):
C cboost = 0 -> no power steering boost
CB = 1. - CBOOST
EXPR = 1. + 2. * XPM * CB * (CA / TODEG) / KSS
ASW = (STORQ - KSS / (GR**2) * ((1. - 1. / EXPR) * SW - 2. * XPM
\& * CA * GR * CB * (BETA + XAXLE (1) * VYAW / V) / (EXPR * KSS)) )
\& / ISS - CSS * VSW / ISS
ASW = ASW * TODEG
IF (ABS (VSW) .GT. 0.01 .AND. VSW2 .NE. O.0) THEN
ASW = ASW - SIGN( (CFSS / ISS * TODEG), VSW)
IF (SIGN (1.,VSW) .NE. SIGN(1.,VSW1) .AND.
\&
SIGN(1.,VSW) .EQ. SIGN(1.,VSW2) ) THEN
VSW = 0.0
ASW = 0.0
VSW1 = 0.0
VSW2 = 0.0
Y(14) = 0.0
ENDIF
ELSE
IF (ABS (ASW) .GT. (CFSS / ISS * TODEG)) THEN
ASW = ASW - SIGN( (CFSS / ISS * TODEG), ASW)
ELSE
ASW = 0.0
ENDIF
ENDIF
VSW2 = VSW1
VSW1 = VSW
Update column "wrap-up" torque, mmcol = m - iss * asw:
(measured in tests)
MMCOL = STORQ - ISS * ASW / TODEG
C Add coulomb friction and check for polarity change:
C Front Wheel Angles:
FW(1) = SW / GR / (1. + (XP1 + XTRAIL) * CB * CA1 / TODEG / (KSS
\& / 2.)) + (XP1 + XTRAIL) * CA1 * CB / (KSS / 2.) * (BETA +
\& XAXIE (1) * VYAW / V) / (1. + (XP1 + XTRAIL) * CB * CA1 / TODEG

```
C
C
C
\(C\)
\(C\)
\(C\)
C
C
C
C
C
C
C
```

        & / (KSS / 2.) )
            FW(2) = SW / GR / (1. + (XP2 + XTRAIL) * CB * CA2 / TODEG / (KSS
        & / 2.)) + (XP2 + XTRAIL) * CA2 * CB / (KSS / 2.) * (BETA +
        & XAXIE (1) * VYAW / V) / (1. + (XP2 + XTRAIL) * CB * CA2 / TODEG
        & / (KSS / 2.) )
    C
C Include the lash (deg):
IF (ABS (DLASH) .GT. 0.001) THEN
ALF1PR = (BETA + XAXLE (1) * VYAW / V) * TODEG - FW(1)
IF (ABS (ALF1PR) .GT. DLASH) THEN
ALF1 = ALF1PR - SIGN (DLASH, ALF1PR)
FW(1) = BETA + XAXIE (1) * VYAW / V - ALF1 / TODEG
ELSE
FW(1) = BETA + XAXIE (1) * VYAW / V
ENDIF
C
ALF2PR = (BETA + XAXLE (1) * VYAW / V) * TODEG - FW(2)
IF (ABS (ALF2PR) .GT. DLASH) THEN
ALF2 = ALF2PR - SIGN (DLASH, ALF2PR)
FW(2) = BETA + XAXLE (1) * VYAW / V - ALF2 / TODEG
ELSE
FW(2) = BETA + XAXIE (1) * VYAW / V
ENDIF
C
ELSE
C
C no lash: (to radians)

```
```

        FW(1) = FW(1) / TODEG
    ```
        FW(1) = FW(1) / TODEG
            FW(2) = FW(2) / TODEG
            FW(2) = FW(2) / TODEG
C
            ENDIF
C
C
C End of steering system calculations.
C
        ENDIF
C
C
C INERTIAL DISPLACEMENTS OF TOTAL CG:
    VDIR = YAW + BETA
    VXG = V * COS (VDIR)
    VYG = V * SIN (VDIR)
C
C LATERAL ACCELERATION OF TOTAL CG (W/O CONTRIBUTION OF ROLL-ACCEL.):
        AY = (VYAW + VBETA) * V / G
C
C Path curvature:
C
        RHO = (VBETA + VYAW) / V
C
C Convert names into array YP
    YP(1) = VXG
```

Appendix D - Source Code

```
        YP(2) = VYG
        YP(3) = VZ
        YP(4) = VROLJ
        YP(5) = VPITCH
        YP(6) = VYAW
        YP(7) = AROLL
        YP(8) = APITCH
        YP(9) = AYAW
        YP(10) = VBETA
        YP(11) = AZ
C
C Steering System STATE Variables:
C
            IF (NEQN .EQ. 13) THEN
            YP (12) = ASW
            YP(13) = VSW
            ENDIF
C
C Copy array Y into common block for use by driver model
C
    DO 150, J = 1, 13
            YOUTDR(J) = Y(J)
    150 CONTINUE
C
    RETURN
    END
    FUNCTION FWIND
        (T)
C This function is an optional user-defined subroutine used to
C calculate or define a wind profile in lieu of entering time history
C wind profiles. It is called when the WINDKY parameter is entered as
C a negative integer; a positive entry for WINDKY forces a table
C look-up instead.
C
C Time, T, is passed to the subroutine; the wind magnitude, FWIND, is
C returned.
C
            include GLBL.inc
C
C (user-defined code)
C
            FWIND = 20.0 + 2.0 * (SIN (1.0*T) +SIN (2.5*T) +SIN (3.5*T)
            1 +SIN (4.5*T) +SIN (5.5*T) +SIN (6.5*T) +SIN (8.5*T) +SIN (10.5*T)
            2 +SIN (12.7*T) +SIN (1.9*T) +SIN (5.0*T) +SIN (7.5*T) +SIN (9.4*T)
            3 +SIN (0.63*T) +SIN (3.1*T) +SIN (6.8*T) +SIN (10.0*T) +SIN (1.5*T)
            4 +SIN (14.1*T) +SIN (15.7*T) +SIN (16.9*T) +SIN (18.2*T) +SIN (19.5*T)
            5 +SIN (22.0*T) +SIN (25.1*T) +SIN (0.85*T) )
C
C
    RETURN
    END
***********************************
C
***********************************
SUBROUTINE GMADD (A, B, R,N,M)
DIMENSION \(A(N * M), B(N \star M), R(N \star M)\)
\(\mathrm{NM}=\mathrm{N} * \mathrm{M}\)
Appendix D - Source Code
D - 34
```



DIMENSION $A(N * M), B(M * L), R(N * L)$

```
C
C---COMMON blocks--------------------------------------------------------------------
C
C None
C
C---COMMON Variables-----------------------------------------------------------
C
C None
C
C---Local variables--------------------------------------------------------------
C
C IR, IK, M, K, L, IR, JI, J, N, IB, IK, etc ......integer counters
C
C---Functions and subroutines
C
C None
C
```



```
C
C
    IR = 0
    IK = -M
    DO 10 K = 1, L
        IK = IK +M
        DO 10 J = 1, N
            IR = IR + 1
            JI=J-N
            IB = IK
            R(IR) = 0.
            DO 10 I = 1, M
                JI = JI +N
                IB = IB + 1
    10R(IR) = R(IR) + A(JI) * B(IB)
        RETURN
    END
    SUBROUTINE INDATA
C (1) Get file names from the user,
C (2) connect the files to their Fortran i/o units,
C (3) read the dataset from unit IREAD,
C (4) echo the parameter values to unit IECHO,
c (5) and, perform the necessary conversions of physical units.
C
        IMPLICIT REAL (K,M)
        LOGICAL ISIT
C
            include drvmod.inc
            include GLBL.inc
            include PARS.inc
            include MNVR.inc
            include SUSP.inc
            include TIRE.inc
            include AERO.inc
            include PRNT.inc
C
```

Appendix D - Source Code

C Get input file name from user
C
WRITE (*,' (///A/A/A/A/A/A)')
\& ' CHRYSLER-UMTRI CROSSWIND STABILITY PROJECT',
\& ' WIND / STEER SIMULATION - Version 1.0, Feb 89',' ',
\& ' Copyright (c) The Regents of The University of Michigan',
\& ' 1987-1989, Ann Arbor, Michigan. All Rights Reserved.',' '
C
100 WRITE (*, '(A<br>)') ' Name of input file: '
READ (*, '(A)') FNREAD
INQUIRE (FILE=FNREAD, EXIST=ISIT)
IF (.NOT. ISIT) THEN
WRITE (*, '(A, A, A)') ' File "', FNREAD,
\& '" does not exist. Try again.'
GO TO 100
END IF
OPEN(IREAD, ERR=100, STATUS='OLD', FILE=FNREAD)
C
C Read general simulation and maneuver parameters:
C
READ (IREAD,' (//A)') TITLE
READ (IREAD,'(A)') UNITS
READ (IREAD,'(A)') FRMT
DO $3 \mathrm{I}=1$, 10
IF (FRMT (I:I) .NE. ' ') THEN
FRMT $=$ FRMT (I:)
GO TO 4
END IF
3 CONTINUE
4 CONTINUE
C
CMD--Use NUMKEY=1 for Mac, 2 for IBM PC
IF (FRMT (:1) .NE. '(') THEN
NUMKEY = 1
FRMT = 'Binary'
ELSE
NUMKEY $=5$
END IF
C)

READ (IREAD,530) V, TEND, DT
READ (IREAD,520) IPRINT
READ (IREAD,530) KSYWND, AIRHO
READ (IREAD,520) WINDKY
VWIND $=0.0$
IF (WINDKY .GE. 0) THEN
DO $5 \mathrm{~J}=1$, WINDKY
READ (IREAD, 530) TWIND (J), WINMAG (J)
5 CONTINUE
ELSE
VWIND $=$ FWIND $(T)$
ENDIF
C
READ (IREAD, 520) NSTEER
IF (NSTEER .EQ. 0) THEN
READ (IREAD, 530) TSWBGN, TSWEND
READ (IREAD, 530) SWSHFT, SWAMPL READ (IREAD, 530) TSWPRD, SWPHSE

Appendix D - Source Code
D-37

```
        ENDIF
        IF (NSTEER .LT. O .AND. NSTEER .GT. -100) THEN
            NP = -NSTEER
            CALL DRIVE1 (SW)
        ENDIF
        IF(NSTEER .GT. O) THEN
        DO 10, J=1, ABS (NSTEER)
        READ (IREAD,530) XPNT (J), YPNT (J)
    10 CONTINUE
        ENDIF
```

        READ (IREAD,530) AREA
    ```
        READ (IREAD,530) AREA
        READ (IREAD,530) KY, KR, KN
        READ (IREAD,530) KY, KR, KN
        READ (IREAD,530) CLO, KL
        READ (IREAD,530) CLO, KL
        READ (IREAD,530) CMO, KM
        READ (IREAD,530) CMO, KM
        READ (IREAD,530) CDO, KD
        READ (IREAD,530) CDO, KD
    Steering system:
        READ (IREAD,540) ISS, KSC, DLASH, KSL
        READ (IREAD,530) GR, XTRAIL, CSS
        READ (IREAD, 530) CBOOST, SSKEY, CFSS
    Calculate equivalent single steering system stiffness based on input
values for the steering column, steering linkage, and gear ratio:
    KSS = GR*GR*KSC*KSL / (KSL + GR*GR*KSC)
C
C
C
    Suspension and tire data:
    READ (IREAD, 520) NKINEM
    IF (NKINEM .EQ. O) KINEM = .FALSE.
    READ (IREAD,520) NBEAM
    IF (NBEAM .EQ. 0) BEAM = .FALSE.
    DO 30, NAXIE=1, 2
C
        READ (IREAD, 530) TRACK (NAXIE), HOROLC (NAXIE)
        READ (IREAD,530) KZ (NAXIE), KAUX (NAXIE)
        READ (IREAD,530) CZJNCE (NAXIE), CZRBND (NAXLE)
        READ (IREAD,530) ALFAO (NAXLE), GAMMAO (NAXIE)
        KINEMATIC COEFFICIENTS:
        IF (KINEM) THEN
            READ (IREAD,530) YROLCF (NAXIE,1), YROLCF (NAXIE, 2)
            READ (IREAD,530) HROLCF (NAXIE,1), HROLCF (NAXIE, 2)
            IF (BEAM .AND. NAXIE .EQ. 2) THEN
                READ (IREAD,530) CSROLL
```

```
            ELSE
                    READ (IREAD,530) CSZ (NAXIE, 1), CSZ (NAXIE, 2)
            END IF
            READ (IREAD,530) CCZ (NAXLE,1), CCZ (NAXIE, 2)
        END IF
```

    Compliance coefficients:
    READ (IREAD, 530) CSFY (NAXIE), CSMZ (NAXIE), CCFY (NAXLE)
    C
C Tire stiffness coefficients:
C
READ (IREAD, 540) (CALFA (J, NAXLE) , $J=1,4$ )
READ (IREAD, 540) (CGAMMA ( J, NAXIE) $, \mathrm{J}=1,4$ )
READ (IREAD, 540) (CALIGN ( $J$, NAXIE) $, J=1,4$ )
READ (IREAD, 530) KTIRE (NAXIE)
C
C
CLOSE (IREAD)
C
C
C
IF (UNITS .EQ. 'E' .OR. UNITS .EQ. 'e') THEN
$\mathrm{G}=386.1$
ININFT $=12$
KMHMPH $=0.056818$
TODEG $=180.0 / \mathrm{PI}$
UDISP = 'in'
UDIST $=$ 'ft'
UANGL = 'deg'
UVELFT = 'ft/s'
UOMEGA $=$ ' $\mathrm{deg} / \mathrm{sec}$ '
UFORC $=$ ' 1 b '
UTORQ $=$ 'in-1b'
END IF
C General simulation and maneuver parameters:
Include steering system dynamics only if non-zero damping:
IF (ABS (SSKEY) .LT. O.001) NEQN = NEQN - 2
C
WRITE (*,'('' '',A//)') TITLE
IF (IECHO .GT. O) CALL ECHO
$\mathrm{V}=\mathrm{V} / \mathrm{KMHMPH}$
VWIND = VWIND / KMHMPH
KSYWND $=$ KSYWND $/$ TODEG
GRTODG $=$ GR * TODEG
C
DO 80, NAXIE=1, 2
KAUX (NAXLE) = KAUX (NAXLE) * TODEG
C With english units, SW, KSC, KSL stay in deg, while FW, VFW
C stay in rad (with metric units, all are in rad, and todeg = 1)

Appendix D - Source Code

C

```
        ALFAO (NAXLE) = ALFAO (NAXIE) / TODEG
        GAMMAO (NAXLE) = GAMMAO (NAXLE) / TODEG
        IF (NSTEER .EQ. O) SWPHSE = SWPHSE / TODEG
C Convert polynomial coefficients from deg to rad:
        IF (KINEM) THEN
        DO 50, NPOWER = 1, 2
            YROLCF (NPOWER, NAXIE) = YROLCF (NPOWER,NAXIE) * TODEG **
                                    NPOWER
            HROLCF (NPOWER,NAXLE) = HROLCF (NPOWER,NAXLE) * TODEG **
                CSZ (NPOWER, NAXLE) = CSZ (NPOWER,NAXLE) / TODEG
                CCZ (NPOWER, NAXIE) = CCZ (NPOWER,NAXIE) / TODEG
            continue
        END IF
C Compliance coefficients:
        CSFY (NAXLE) = CSFY (NAXLE) / TODEG
        CSMZ (NAXIE) = CSMZ (NAXLE) / TODEG
        CCFY (NAXLE) = CCFY (NAXLE) / TODEG
C Change CALFA polarity to conform with SAE conventions
c and convert polynomial coefficients from deg to rad
        DO 70, NPOWER = 1, 4
        CALFA (NPOWER, NAXLE) = -CALFA (NPOWER,NAXLE) * TODEG
        CGAMMA (NPOWER,NAXLE) = CGAMMA (NPOWER,NAXLE) * TODEG
        CALIGN (NPOWER,NAXLE) = CALIGN(NPOWER,NAXLE) * TODEG
        CONTINUE
    80 CONTINUE
C
        RETURN
C
    520 FORMAT (BN, I4)
    530 FORMAT (3F12.0)
    540 FORMAT (4F12.0)
        END
```

C
C
C
C
C
C
C
****************************************************************************
SUBROUTINE INIT
C
C Initialize input-based values and non-zero variables
C
IMPLICIT REAL (K,M)
include GLBL.inc
include PARS.inc
include SUSP.inc
include AERO.inc
include vars.inc
include PRNT.inc
MASS = WEIGHT / G
SPMASS $=$ SPWGHT $/ \mathrm{G}$
USWGHT $=$ WEIGHT - SPWGHT

```
    XAXIE (2) = - WB * WRATIO
    XAXIE (1) = WB + XAXIE (2)
    FZOWHL (1) = .5 * WEIGHT * WRATIO
    FZOWHL (2) = . 5 * WEIGHT * (1 - WRATIO)
    XCGSP = WB * (2 * FZOWHL (2) - . 5 * USWGHT) / SPWGHT
    XWBCGS = . 5 * WB - XCGSP
    XWBCGT = . 5 * WB - XAXIE (1)
    HCGSP = (HCGTTL * WEIGHT - WHLRAD * USWGHT) / SPWGHT
    ROLLVR = .5 * TRACK(1) / HCGTTL
    QZERO = AIRHO * AREA / 2
    KROLL = 0.
C
    DO 20, NAXLE = 1, }
C
C Approximate effects of tire stiffness + damping in suspension:
C
    TRKSQR = . 5 * TRACK(NAXLE)**2
    SUMKZ = KZ (NAXIE) + KTIRE (NAXIE)
C
C Reduce overall damping coefficients for negligible tire damping:
C
    CZJNCE (NAXIE) = CZJNCE (NAXIE) * KTIRE (NAXIE) / SUMKZ
    CZRBND (NAXIE) = CZRBND (NAXIE) * KTIRE (NAXIE) / SUMKZ
C
C
C
C
C
C
C
C KZ <--- overall vertical rate without auxiliary roll stiffness:
C
C
C Adjusted auxiliary roll rate (in parallel with kz):
KAUX(NAXIE) = (KZTTL - KZ (NAXIE)) * TRKSQR
C
C Effective roll stiffness and axle vertical stiffness
C
    KROLL = KROLL + KZ (NAXLE) * TRKSQR + KAUX (NAXIE)
    KZAXIE (NAXIE) = 2 * KZ (NAXIE)
    HCGSRC (NAXIE) = HCGSP - HOROLC (NAXIE)
    DO 10, NSIDE = 1, 2
        ALFA (NAXLE,NSIDE) = - (-1)**NSIDE * ALFAO (NAXIE)
        GAMMA (NAXIE,NSIDE) = - (-1)**NSIDE * GAMMAO (NAXIE)
        FZ (NAXIE,NSIDE) = FZOWHL (NAXIE)
        KNMSTR(NAXIE,NSIDE) = 0.0
        KNMCBR(NAXIE,NSIDE) =0.0
    10 CONTINUE
    20 CONTINUE
    RETURN
    END
    FUNCTION LENSTR (STRING)
```

CHARACTER* (*) STRING
$\mathrm{N}=\mathrm{LEN}$ (STRING)
DO $10 \mathrm{~L}=\mathrm{N}, 1,-1$ IF (STRING (L:L) .NE. ' ' .AND. STRING (L:L) .NE. Char (3)) THEN LENSTR $=\mathrm{L}$ RETURN
END IF
10 CONTINUE
LENSTR $=1$
RETURN
END
C
त
C NAASA 2.1.020 MINV FTN 06-24-75 THE UNIV OF MICH COMP CTR
C

SUBROUTINE MINV
PURPOSE
INVERT A MATRIX
USAGE
CAL工 MINV (A,N, D, L, M)
DESCRIPTION OF PARAMETERS
A - INPUT MATRIX, DESTROYED IN COMPUTATION AND REPLACED BY RESULTANT INVERSE.
N - ORDER OF MATRIX A
D - RESULTANT DETERMINANT
L - WORK VECTOR OF LENGTH N
M - WORK VECTOR OF LENGTH N
REMARKS
MATRIX A MUST BE A GENERAL MATRIX
SUBROUTINES AND FUNCTION SUBPROGRAMS REQUIRED NONE

METHOD
THE STANDARD GAUSS-JORDAN METHOD IS USED. THE DETERMINANT IS ALSO CALCULATED. A DETERMINANT OF ZERO INDICATES THAT THE MATRIX IS SINGULAR.

SUBROUTINE MINV (A,N,D,L,M)
DIMENSION A(*),L(*), M(*)
C
C

```
C
C DOUBLE PRECISION A,D,BIGA,HOLD
\[
D=1.0
\]
\[
N K=-N
\]
\[
\text { DO } 80 \mathrm{~K}=1, \mathrm{~N}
\]
\[
N K=N K+N
\]
\[
L(K)=K
\]
\[
M(K)=K
\]
\[
K K=N K+K
\]
\[
\mathrm{BIGA}=\mathrm{A}(\mathrm{KK})
\]
\[
\text { DO } 20 \mathrm{~J}=\mathrm{K}, \mathrm{~N}
\]
\[
I Z=N^{*}(\mathrm{~J}-1)
\]
\[
\text { DO } 20 \mathrm{I}=\mathrm{K}, \mathrm{~N}
\]
\[
I J=I Z+I
\]
\[
10 \operatorname{IF}(\operatorname{ABS}(B I G A)-\operatorname{ABS}(A(I J))) \quad 15,20,20
\]
\(15 \mathrm{BIGA}=\mathrm{A}\) (IJ)
\(\mathrm{L}(\mathrm{K})=\mathrm{I}\)
\(\mathrm{M}(\mathrm{K})=\mathrm{J}\)
20 CONTINUE
\(\mathrm{J}=\mathrm{L}(\mathrm{K})\)
IF (J-K) 35, 35, 25
\(25 \mathrm{KI}=\mathrm{K}-\mathrm{N}\)
DO \(30 \mathrm{I}=1, \mathrm{~N}\)
\(\mathrm{KI}=\mathrm{KI}+\mathrm{N}\)
HOLD \(=-\mathrm{A}\) ( KI )
JI=KI-K+J
\(\mathrm{A}(\mathrm{KI})=\mathrm{A}\) (JI)
30 A(JI) =HOLD
    IF (I-K) 45,45,38
    38 JP=N* (I-1)
    DO 40 J=1,N
    JK=NK+J
    JI=SP+J
        HOLD=-A (JK)
        A (JK)=A (JI)
    40 A(JI) =HOLD
```

C CONTAINED IN BIGA)
C
45 IF (BIGA) 48,46,48
46 D=0.0
RETURN
48 DO 55 I=1,N
IF (I-K) 50,55,50
50 IK=NK+I
A(IK)=A (IK) / (-BIGA)
55 CONTINUE
C
C REDUCE MATRIX
C
DO 65 I=1,N
IK=NK+I
HOLD=A (IK)
IJ=I-N
DO 65 J=1,N
IJ=IJ+N
IF (I-K) 60,65,60
60 IF(J-K) 62,65,62
62 KJ=IJ-I+K
A(IJ)=HOLD*A (KJ) +A (IJ)
6 5 ~ C O N T I N U E ~
C
C DIVIDE ROW BY PIVOT
C
KJ=K-N
DO }75\textrm{J}=1,
KJ=KJ+N
IF (J-K) 70,75,70
70 A(KJ)=A(KJ)/BIGA
75 CONTINUE
C
C PRODUCT OF PIVOTS
C
D=D*BIGA
C
C
REPIACE PIVOT BY RECIPROCAL
C
A(KK)=1.0/BIGA
80 CONTINUE
C
C FINAI ROW AND COLUMN INTERCHANGE
C
K=N
100 K=(K-1)
IF (K) 150,150,105
105 I=L (K)
IF (I-K) 120,120,108
108 JQ=N* (K-1)
JR=N* (I-1)
DO 110 J=1,N
JK=JQ+J
HOLD=A (JK)
JI=JR+J
A(JK)=-A (JI)
110 A(JI) =HOLD

```

Appendix D - Source Code
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```

    120 J=M(K)
    IF (J-K) 100,100,125
    125 KI=K-N
        DO 130 I=1,N
        KI=KI+N
        HOLD=A (KI)
        JI=KI-K+J
        A(KI) =-A (JI)
    130 A(JI) =HOLD
    GO TO 100
    150 RETURN
    END
    SUBROUTINE OPNOUT
    C SUBROUTINE OPNOUT INITIALIZES THE OUTPUT ERD FILE.
C
IMPLICIT REAL (K,M)
CHARACTER*32 LONGNM(66), GENNM(66), RIGBOD (66), THISRB
CHARACTER*32 FNOUT
CHARACTER*24 TIMEDT
CHARACTER*8 SHORTN(66), UNITNM(66)
CHARACTER*4 LORR(2)
CHARACTER*1 AXIE (2), SIDE (2)
INTEGER NCHAN
LOGICAL ISIT
C
include GLBL.inc
include PARS.inc
C
DATA AXIE/'1','2'/, SIDE/'L','R'/, LORR/'Left','Rght'/
DATA TIMEDT/' '/
C
110 WRITE(*, '(A\)') ' Name of simulation output file: '
READ (*, '(A)') FNOUT
IF (FNOUT .NE. ' ') THEN
INQUIRE (FILE=FNOUT, EXIST=ISIT)
IF (ISIT) THEN
OPEN (IOUT, FILE=FNOUT)
CLOSE (IOUT, STATUS='DELETE')
END IF
OPEN (IOUT, FILE=FNOUT, STATUS='NEW')
WRITE (*,*) ' '
ELSE
WRITE (*,*) 'Output file is required!'
GO TO 110
END IF
C
C Start with O output channels
C
NCHAN = 0
C
C Time
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Time'
SHORTN (NCHAN) = 'Time'
GENNM (NCHAN) = 'Time'

```

Appendix D - Source Code
```

        UNITNM (NCHAN) = 'sec'
        RIGBOD (NCHAN) = 'Time'
    C
C Input Steer Angle
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Input Steer Angle'
SHORTN (NCHAN) = 'Steer in'
GENNM (NCHAN) = 'Angle'
UNITNM (NCHAN) = UANGL
RIGBOD (NCHAN) = 'Input'
C
C Input Steer Torque
C
IF (SSKEY .NE. O.0) THEN
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Input Steer Torque'
SHORTN (NCHAN) = 'SW Torq'
GENNM (NCHAN) = 'Torque'
UNITNM (NCHAN) = UTORQ
RIGBOD (NCHAN) = 'Input'
END IF
C
THISRB = 'Body'
C
C X Position
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'X Position, Sprung Mass cg'
SHORTN (NCHAN) = 'X cg'
GENNM (NCHAN) = 'X Position'
UNITNM (NCHAN) = UDIST
RIGBOD (NCHAN) = THISRB
C
C Y Position
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Y Position, Sprung Mass cg'
SHORIN (NCHAN) = 'Y Cg'
GENNM (NCHAN) = 'Y Position'
UNITNM (NCHAN) = UDIST
RIGBOD (NCHAN) = THISRB
C
C Z Position
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Z Position, Sprung Mass cg'
SHORTN (NCHAN) = 'Z cg'
GENNM (NCHAN) = 'Z Position'
UNITNM (NCHAN) = UDISP
RIGBOD (NCHAN) = THISRB
C
C Roll Angle
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Roll Angle'
SHORTN (NCHAN) = 'Roll'
GENNM (NCHAN) = 'Roll'

```
```

        UNITNM (NCHAN) = UANGL
        RIGBOD (NCHAN) = THISRB
    C
C Pitch Angle
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Pitch Angle'
SHORTN (NCHAN) = 'Pitch'
GENNM (NCHAN) = 'Pitch'
UNITNM (NCHAN) = UANGL
RIGBOD (NCHAN) = THISRB
C
C Yaw Angle
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Yaw Angle'
SHORTN (NCHAN) = 'Yaw'
GENNM (NCHAN) = 'Yaw'
UNITNM (NCHAN) = UANGL
RIGBOD (NCHAN) = THISRB
C
C Roll Rate
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Roll Rate'
SHORTN (NCHAN) = 'p'
GENNM (NCHAN) = 'Roll Rate'
UNITNM (NCHAN) = UOMEGA
RIGBOD (NCHAN) = THISRB
C
C Pitch Rate
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Pitch Rate'
SHORTN (NCHAN) = 'q'
GENNM (NCHAN) = 'Pitch Rate'
UNITNM (NCHAN) = UOMEGA
RIGBOD (NCHAN) = THISRB
C
C Yaw Rate
C
NCHAN = NCHAN + 1
IONGNM (NCHAN) = 'Yaw Rate'
SHORTN (NCHAN) = 'r'
GENNM (NCHAN) = 'Yaw Rate'
UNITNM (NCHAN) = UOMEGA
RIGBOD (NCHAN) = THISRB
C
C Body Slip Angle
C
NCHAN = NCHAN + 1
IONGNM (NCHAN) = 'Vehicle Slip Angle'
SHORTN (NCHAN) = 'slip'
GENNM (NCHAN) = 'Angle'
UNITNM (NCHAN) = UANGL
RIGBOD (NCHAN) = THISRB
C
C X Velocity, Sprung Mass cg

```

Appendix D - Source Code
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```

C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'X Velocity, Sprung Mass cg'
SHORTN (NCHAN) = 'X dot'
GENNM (NCHAN) = 'X Velocity'
UNITNM (NCHAN) = UVELFT
RIGBOD (NCHAN) = THISRB
C
C Y Velocity, Sprung Mass cg
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Y Velocity, Sprung Mass cg'
SHORTN (NCHAN) = 'Y dot'
GENNM (NCHAN) = 'Y Velocity'
UNITNM (NCHAN) = UVELFT
RIGBOD (NCHAN) = THISRB
C
C Z Velocity, Sprung Mass cg
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Z Velocity, Sprung Mass cg'
SHORTN (NCHAN) = 'w cg'
GENNM (NCHAN) = 'Z Velocity'
UNITNM (NCHAN) = UDISP // '/s'
RIGBOD (NCHAN) = THISRB
C
C Lateral Acceleration
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Lateral Acceleration at cg'
SHORTN (NCHAN) = 'Ay Cg'
GENNM (NCHAN) = 'Lateral Acceleration'
UNITNM (NCHAN) = 'g''s'
RIGBOD (NCHAN) = THISRB
C
C Vehicle Path Curvature
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Vehicle Path Curvature'
SHORTN (NCHAN) = 'Rho Cg'
GENNM (NCHAN) = 'Vehicle Path Curvature'
UNITNM (NCHAN) = '1/' // UDIST
RIGBOD (NCHAN) = THISRB
C
C Aerodynamic Drag Force
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Drag Force'
SHORTN (NCHAN) = 'Fx Aero'
GENNM (NCHAN) = 'Force'
UNITNM (NCHAN) = UFORC
RIGBOD (NCHAN) = THISRB
C
C Aerodynamic Side Force
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Side Force'
SHORTN (NCHAN) = 'Fy Aero'

```
```

        GENNM (NCHAN) = 'Force'
        UNITNM (NCHAN) = UFORC
        RIGBOD (NCHAN) = THISRB
    C
C Aerodynamic Down Force
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Down Force'
SHORTN (NCHAN) = 'Fz Aero'
GENNM (NCHAN) = 'Force'
UNITNM (NCHAN) = UFORC
RIGBOD (NCHAN) = THISRB
C
C Aerodynamic Roll Moment
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Roll Moment'
SHORTN (NCHAN) = 'Mx Aero'
GENNM (NCHAN) = 'Moment'
UNITNM (NCHAN) = UTORQ
RIGBOD (NCHAN) = THISRB
C
C Aerodynamic Pitch Moment
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Pitch Moment'
SHORTN (NCHAN) = 'My Aero'
GENNM (NCHAN) = 'Moment'
UNITNM (NCHAN) = UTORQ
RIGBOD (NCHAN) = THISRB
C
C Aerodynamic Yaw Moment
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Yaw Moment'
SHORTN (NCHAN) = 'Mz Aero'
GENNM (NCHAN) = 'Moment'
UNITNM (NCHAN) = UTORQ
RIGBOD (NCHAN) = THISRB
C
C Air Speed
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Air Speed'
SHORTN (NCHAN) = 'V Air'
GENNM (NCHAN) = 'Speed'
UNITNM (NCHAN) = UVELFT
RIGBOD (NCHAN) = 'Input'
C
C Aerodynamic Slip Angle
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Aerodynamic Slip Angle'
SHORTN (NCHAN) = 'Slip Air'
GENNM (NCHAN) = 'Angle'
UNITNM (NCHAN) = UTORQ
RIGBOD (NCHAN) = THISRB
C

```

C Tire/Wheel variables. There are 2 nested loops here: the outer C indexed the axle, and the inner indexes the side.

C
```

        DO 100, NAXIE = 1, 2
        DO }80\mathrm{ NSIDE = 1, 2
        THISRB = SIDE (NSIDE) // ' side, Axle ' // AXLE (NAXLE)
    C Steer of road wheel

```
C
        NCHAN \(=\) NCHAN +1
        LONGNM (NCHAN) = 'Total Steer, ' // THISRB
        SHORTN (NCHAN) = SIDE (NSIDE) // ' Str ' // AXLE (NAXLE)
        UNITNM (NCHAN) = UANGL
        GENNM (NCHAN) = 'Angle'
        RIGBOD (NCHAN) \(=\) THISRB
C
C Tire slip angle
    NCHAN \(=\) NCHAN +1
    LONGNM (NCHAN) = 'Slip Angle, '// THISRB
        SHORTN (NCHAN) = SIDE (NSIDE) // 'Alph ' // AXLE (NAXLE)
        UNITNM (NCHAN) = UANGL
        GENNM (NCHAN) = 'Angle'
        RIGBOD (NCHAN) = THISRB
C
C Tire camber angle
C
    NCHAN \(=\) NCHAN +1
    LONGNM (NCHAN) = 'Camber Angle, '// THISRB
    SHORTN (NCHAN) = SIDE (NSIDE) // ' Gamm ' // AXLE (NAXLE)
        UNITNM (NCHAN) \(=\) UANGL
        GENNM (NCHAN) = 'Angle'
        RIGBOD (NCHAN) = THISRB
C
C Tire side force
C
    NCHAN \(=\) NCHAN +1
    LONGNM (NCHAN) = 'Side Force, '// THISRB
    SHORTN (NCHAN) = SIDE (NSIDE) // ' Fy ' // AXLE (NAXLE)
    UNITNM (NCHAN) = UFORC
    GENNM (NCHAN) = 'Force'
    RIGBOD (NCHAN) \(=\) THISRB
C
C Tire Aligning Moment
C
    NCHAN \(=\) NCHAN +1
    LONGNM (NCHAN) = 'Aligning Moment, ' // THISRB
        SHORTN (NCHAN) = SIDE (NSIDE) // ' Mz ' // AXLE (NAXLE)
        UNITNM (NCHAN) \(=\) UTORQ
        GENNM (NCHAN) = 'Moment'
        RIGBOD (NCHAN) = THISRB
C
C Tire vertical force
C
    NCHAN \(=\) NCHAN +1
    LONGNM (NCHAN) = 'Load, ' // THISRB
    SHORTN (NCHAN) = SIDE (NSIDE) // ' Fz ' // AXLE (NAXLE)
    UNITNM (NCHAN) \(=\) UFORC

Appendix D - Source Code
```

                GENNM (NCHAN) = 'Force'
                RIGBOD (NCHAN) = THISRB
    C
C Suspension Displacement
C NCHAN = NCHAN +1
LONGNM (NCHAN) = 'Vert Disp, ' // THISRB
SHORTN (NCHAN) = SIDE (NSIDE) // ' z ' // AXLE (NAXLE)
UNITNM (NCHAN) = UDISP
GENNM (NCHAN) = 'Displacement'
RIGBOD (NCHAN) = THISRB
C
C Suspension Damping Force
C
NCHAN = NCHAN + 1
LONGNM (NCHAN) = 'Damping Force, ' // THISRB
SHORTN (NCHAN) = SIDE(NSIDE) // ' Fdmp ' // AXLE (NAXLE)
UNITNM (NCHAN) = UFORC
GENNM (NCHAN) = 'Force'
RIGBOD (NCHAN) = THISRB
80 CONTINUE
100 CONTINUE
C
C Write Header Info for ERD file
C Set parameters needed to write header
C NUMREY = 1 for 32-bit floating-point binary, 5 for Text
C
NSAMP = TEND / DT / IPRINT + 1
NRECS = NSAMP
IF (NUMKEY .NE. 5) THEN
NBYTES = 4*NCHAN
ELSE
NBYTES = 1
END IF
C
C Write standard ERD file heading.
C
WRITE(IOUT,' (A)') 'ERDFILEV2.00'
WRITE (IOUT, 410) NCHAN, NSAMP, NRECS, NBYTES, NUMKEY, DT*IPRINT
4 1 0 ~ F O R M A T ~ ( 5 ~ ( I 6 , ' , ' ) , E 1 3 . 6 ) ~
4 1 1 ~ F O R M A T ~ ( A 8 , 2 5 5 A 8 )
412 FORMAT (A8, 31A32 : 2(/'\&1000 ', 31A32))
WRITE (IOUT,' (A,A)') 'TITLE ', TITLE
WRITE (IOUT, 411) 'SHORTNAM', (SHORTN(J), J=1, NCHAN)
WRITE (IOUT, 412) 'LONGNAME', (LONGNM(J), J=1, NCHAN)
WRITE (IOUT,411) 'UNITSNAM', (UNITNM(J), J=1, NCHAN)
WRITE (IOUT, 412) 'GENNAME ', (GENNM(J), J=1, NCHAN)
WRITE (IOUT, 412) 'RIGIBODY', (RIGBOD (J), J=1, NCHAN)
C
WRITE (IOUT, '(A)') 'TRUCKSIMWind/Steer'
C
IMPH = NINT (V * KMHMPH)
IF (UNITS .NE. 'E' .AND. UNITS .NE. 'e')
\& IMPH = NINT (V * KMHMPH / 1.61)
WRITE (IOUT, '(A,I5)') 'SPEEDMPH', IMPH
C
IF (NUMKEY .EQ. 5) WRITE(IOUT, '(A,A)') 'FORMAT ',FRMT

```

C
CALL TIMDAT (TIMEDT)
WRITE (IOUT, ' \(\left.(\mathrm{A}, \mathrm{A})^{\prime}\right)\)
\& 'HISTORY Data generated with Wind/Steer model at ', TIMEDT WRITE (IOUT, ' (A,A)') 'HISTORY Input file was ', FNREAD WRITE (IOUT, '(A)') 'END'
C
\(C\) If this is a Mac or PC, and data will be binary, then close header
\(C\) and create binary file. The following line is used to disable the
\(C\) creating of a second file for MTS.
C
C--Use this only for the MTS version.
C RETURN
501 CONTINUE
IF (NUMKEY .NE. 5) THEN
CLOSE (IOUT)
LNAME = LENSTR (FNOUT)
FNOUT = FNOUT (:LNAME) // '.BIN'
INQUIRE (FILE=FNOUT, EXIST=ISIT)
IF (ISIT) THEN
OPEN (IOUT, FILE=FNOUT)
CLOSE (IOUT, STATUS='DELETE')
END IF
C--The following 2 lines are for the Mac version.
OPEN (IOUT, FILE=FNOUT, STATUS='NEW', ACCESS='SEQUENTIAL',
\&
FORM='UNFORMATTED')
C--The following 2 lines are for the \(P C\) version.
* OPEN (IOUT, STATUS='NEW', ACCESS='SEQUENTIAL',
* \& FORM='BINARY')

END IF

RETURN
END
SUBROUTINE OUTPUT (T, Y, YP)

C variables into a buffer array in a sequence as specified in the
\(C\) header, and outputs the buffer into the erd-file in binary or
C text form.
C
IMPLICIT REAL (K,M)
INTEGER*2 LEN2, IBMROW, IBMCOL
REAL \(\operatorname{BUFFER}(66)\), \(Y(*)\), \(Y P(*)\)
C
include GLBL.inc
include PARS.inc
include VARS.inc
include AERO.inc
C
C Fill the ERD buffer. The following code should create a one-to-one
\(C\) match between the label sets created in routine OPNOUT and output
\(C\) variables put into the array BUFFER.
C
NCHAN \(=0\)
C

Appendix D - Source Code
```

C Time and inputs
C
BUFFER (NCHAN + 1) = T
BUFFER (NCHAN + 2) = SW
NCHAN = NCHAN + 2
IF (SSKEY .NE O O.0) THEN
NCHAN = NCHAN + 1
BUFFER (NCHAN) = STORQ
END IF
C
C Body position variables
C
BUFFER (NCHAN + 1) = Y(1) / ININFT
BUFFER (NCHAN + 2) = Y(2) / ININFT
BUFFER (NCHAN + 3) = Y(3)
BUFFER (NCHAN + 4) = Y(4) * TODEG
BUFFER (NCHAN + 5) = Y(5) * TODEG
BUFFER (NCHAN + 6) = Y(6) * TODEG
NCHAN = NCHAN + 6
C
C Body speed variables
C
BUFFER (NCHAN + 1) = Y(7) * TODEG
BUFFER (NCHAN + 2) = Y(8) * TODEG
BUFFER (NCHAN + 3) = Y(9) * TODEG
BUFFER (NCHAN + 4) = Y(10) * TODEG
BUFFER (NCHAN + 5) = YP (1) / ININFT
BUFFER (NCHAN + 6) = YP (2) / ININFT
BUFFER (NCHAN + 7) = Y(11)
NCHAN = NCHAN + 7
C
C Lateral Acceleration, Path Curvature
BUFFER (NCHAN + 1) = AY
BUFFER (NCHAN + 2) = RHO * ININFT
NCHAN = NCHAN + 2
C
C Aerodynamic variables
C
BUFFER (NCHAN + 1) = FDRAG
BUFFER (NCHAN + 2) = FYA
BUFFER (NCHAN + 3) = FZA
BUFFER (NCHAN + 4) = MXA
BUFFER (NCHAN + 5) = MYA
BUFFER (NCHAN + 6) = MZA
BUFFER (NCHAN + 7) = VA
BUFFER (NCHAN + 8) = BETAIR
NCHAN = NCHAN + 8
C
C Tire/Wheel variables
DO 100, NAXIE = 1, 2
DO 80, NSIDE = 1, 2
BUFFER (NCHAN + 1) = TTISTR(NAXLE,NSIDE) * TODEG
BUFFER (NCHAN + 2) = ALFA (NAXIE,NSIDE) * TODEG
BUFFER (NCHAN + 3) = GAMMA (NAXIE,NSIDE) * TODEG
BUFFER (NCHAN + 4) = FY (NAXLE,NSIDE)
BUFFER (NCHAN + 5) = MZ (NAXIE,NSIDE)

```
```

                BUFFER (NCHAN + 6) = FZ (NAXIE,NSIDE)
                BUFFER (NCHAN + 7) = ZW (NAXLE,NSIDE)
                BUFFER (NCHAN + 8) = FD (NAXIE,NSIDE)
                NCHAN = NCHAN + 8
            80 CONTINUE
    100 CONTINUE
    C
C Write data to the file.
C
C--The next 3 lines are for the Mac
IF (T .EQ. O.) WRITE (*, '(A/7X,A)') 'Progress:','sec'
CALL TOOLBX (Z'89409000',0,-11)
WRITE (*, '(F6.2)') T
C--The next }11\mathrm{ lines are for the IBM PC

* IF (T .EQ. O.) THEN
* IBMROW = 18
* IBMCOL = 10
* WRITE (*, '(/////A\)') ' '
* CALL SETCUR (IBMROW, IBMCOL)
* WRITE (*, '(A,12X,A\)') ' Progress:','sec'
* END IF
* IBMROW = 18
* IBMCOL = 22
* CALL SETCUR (IBMROW, IBMCOL)
* WRITE (*, '(F6.2\)') T
C--End IBM PC stuff
IF (NUMKEY .EQ. 5) THEN
WRITE (IOUT, FRMT) (BUFFER(J),J=1, NCHAN)
ELSE
C
C--This line is only for MTS
C LEN2 = NBYTES
C CALL WRITE (BUFFER, LEN2, 16384, LNUM, IOUT)
C
C--This line is for the Mac and the PC
WRITE (IOUT) (BUFFER (J), J=1, NCHAN)
END IF
C
RETURN
END
FUNCTION POLY4 (COEF,FZ)
* evaluate 4-th order polynomial
REAL COEF (*)
POLY4 = COEF (1) + COEF (2)*FZ + COEF (3)*FZ*FZ + COEF (4)*FZ**3
RETURN
END
SUBROUTINE ROLLAX (ROLL, YROLAX, HROLAX, IXSRA)
C Subroutine ROLIAX returns YROLAX and HROLAX, the dynamic lateral
$C$ and vertical distances of the sprung mass $c g$ from the roll axis in
C a non-rolling reference frame, and IXSRA, the sprung-mass moment of
$C$ inertia about the instantaneous roll axis, as functions of roll.

```

Appendix D - Source Code

C (Effects of roll-axis inclination the from \(x-x\) axis are neglected.)
C
IMPLICIT REAL (K,M)
REAL IXSRA
C
include PARS.inc
include SUSP.inc
C
        For each axle, find dynamic r.c. displacements in sprung mass
        with sprung cg as origin
        DO 40 NAXIE \(=1,2\)
            YRC (NAXIE) \(=0.0\)
            HRC (NAXIE) \(=\) HCGSRC (NAXLE)
            DO 20 NPOWER=1, 2
                YRC (NAXLE) \(=\) YRC (NAXLE) + YROLCF (NPOWER, NAXIE) * ROLL**NPOWER
                HRC (NAXLE) \(=\) HRC (NAXLE) + HROLCF (NPOWER, NAXIE) * ROLL**NPOWER
    20 CONTINUE
    40 CONTINUE
C
C Find \(y\) and \(z\) projections of roll-axis distance from sprung cg
C in sprung-mass (rolling) reference frame
C
    \(\operatorname{YRACG}=\operatorname{YRC}(1)+(\operatorname{YRC}(2)-\operatorname{YRC}(1)) * X C G S P / W B\)
    \(\operatorname{HRACG}=\operatorname{HRC}(1)+(\operatorname{HRC}(2)-\operatorname{HRC}(1)) * \operatorname{XCGSP} / \mathrm{WB}\)
C Transform \(y\) and \(z\) projections into non-rolling frame
C (Approximating: \(\cos (\) roll \()=1, \sin (r o l l)=\) roll )
C
        YROLAX = YRACG + HRACG * ROLL
        HROLAX = HRACG - YRACG * ROLL
C
        Calculate IXSRA based on ixscg and roll-axis arm (YRACG**2+HRACG**2)
        IXSRA \(=\) IXSCG \(+(\) YRACG * YRACG + HRACG * HRACG) * SPMASS
        RETURN
        END
            FUNCTION STEER(T)
C Function steer returns the steering wheel-angle (deg), SW,
C or steering wheel torque (in-lbs), STORQ,
\(C\) as a function of \(T\) in one of 3 control modes:
C (NSTEER > 0) -- use table look-up
C (NSTEER \(=0\) ) -- sinusoid function
C (NSTEER < 0) -- Driver model
C (NSTEER < -100) -- sinusoidal torque sweep
C
    SAVE
    IMPLICIT REAL (K, M)
    include vars.inc
    include mnvr.inc
    include glbl.inc
    include pars.inc
    include drvmod.inc
C
    DIMENSION YDR(7)
```

C
DATA DFW,DFWNOW /2*0.0/
DATA DRTORQ,DRTNOW /2*0.0/
C
IF (NSTEER) 100, 200, 300
C
C Driver model:
C
100 IF (ABS (SSKEY) .LE. 0.001) THEN
YDR(1) = YOUTDR(2) / ININFT
YDR(2) = YOUTDR(10) * V / ININFT
YDR(3) = YOUTDR(9)
YDR(4) = YOUTDR(6)
YDR(5) = YOUTDR(1) / ININFT
DFWNOW = (TTLSTR (1,1) + TTLSSTR (1,2)) * 0.5
CALL DRIVER(T, YDR, DFW, DFWNOW)
C
C Add kinematic and compliance steer effects (prior time step) and
C convert to degrees at steering wheel:
C
STEER = ( DFW - (KNMSTR (1,1) + KNMSTR (1,2)) * 0.5 -
1 (CPLSTR (1,1) + CPLSTR (1,2)) * 0.5 ) * GRTODG
C
C No initial steering from driver during lag period:
IF(T .LE. TAUMEM) STEER = 0.0
C
RETURN
C
ELSE
IF (NSTEER .LT. -100) THEN
WO = 0.1 * 6.2832
WMAX = 4.0 * 6.2832
WW = (WMAX - WO) / 2.0 * (1. - COS (6.2832/25. * T) ) + WO
STEER = 20. * SIN (WW * T)
RETURN
ELSE
YDR (1) = YOUTDR (2) / ININFT
YDR(2) = YOUTDR(10) * V / ININFT
YDR(3) = YOUTDR(9)
YDR(4) = YOUTDR(6)
YDR (5) = YOUTDR (13) / TODEG
YDR(6) = YOUTDR(12) / TODEG
YDR(7) = YOUTDR(1) / ININFT
DRTNOW = STORQ / ININFT
CALL DRIVET (T, YDR, DRTORQ, DRTNOW)
STEER = DRTORQ * ININFT
C
C No initial torque from driver during lag period:
C
IF (T .LE. TAUMEM) STEER = 0.0
C
RETURN
ENDIF
C
ENDIF
C

```
```

C
C Sinusoidal steer function:
C
200 IF (T .LT. TSWBGN) THEN
STEER = 0.0
ELSE
IF (T .LE. TSWEND) STEER = SWSHFT +
1 SWAMPL * SIN(2*PI* (T-TSWBGN)/TSWPRD + SWPHSE)
END IF
C (FOR T > TSWEND, STEER IS NOT CHANGED)
RETURN
C
C Steer table:
C
300 IF (T .LT. XPNT (NSTEER)) GO TO 310
C
C Steering angle past the end of the table retains end value:
C
STEER = YPNT (NSTEER)
RETURN
C
310 IF (INDX .NE. 0) GO TO 330
C
C First call - pre-compute elements in SLOPE array
C
DO 320, J=1,NSTEER-1
SLOPE (J) = (YPNT (J+1) - YPNT (J)) / (XPNT (J+1) - XPNT (J))
320 CONTINUE
C
C Increment interval J if t >= XPNT(J+1), else pop to interpolate:
C
330 DO 340, J = 1, NSTEER-1
INDX = J
IF (T .GE. XPNT(J) .AND. T .LT. XPNT(J+1)) GO TO 350
340 CONTINUE
C
350 STEER = YPNT (INDX) + (T - XPNT (INDX)) * SLOPE (INDX)
C
C INDX will hold the number (index) of the 'active' table interval
RETURN
END
FUNCTION SUM(MATRIX)

```
```

C FUNCTION SUM PERFORMS A SUMMATION OF ALL COMPONENTS

```
C FUNCTION SUM PERFORMS A SUMMATION OF ALL COMPONENTS
C OF A 2 X 2 MATRIX ("WHEEL" ARRAY)
C OF A 2 X 2 MATRIX ("WHEEL" ARRAY)
C
C
    REAL MATRIX (2,2)
    REAL MATRIX (2,2)
C
C
    SUM = MATRIX(1,1) + MATRIX (1,2) + MATRIX (2,1) + MATRIX (2,2)
    SUM = MATRIX(1,1) + MATRIX (1,2) + MATRIX (2,1) + MATRIX (2,2)
    RETURN
    RETURN
    END
    END
    SUBROUTINE TABLE (M, N, X, Y, Z, Q)
C Table look-up routine. Q = Y(X), FOR X = Z. Search over range
C X(M) -> X(N).
Appendix D - Source Code
D - 57
```

C
C
INC $=1$
DO $20 \mathrm{I}=\mathrm{M}$, N, INC
IF (Z .LE. X(I)) GO TO 30
20 continue
$\mathrm{Q}=\mathrm{Y}(\mathrm{N})$
RETURN
30 IF (I .NE. M .AND. Z .NE. X(I)) GO TO 40 $Q=Y$ (I) $\operatorname{IF}(\mathrm{I} . \mathrm{EQ} . \mathrm{M}$.AND. Z .LT. $\mathrm{X}(\mathrm{I})) \mathrm{Q}=\mathrm{Y}(\mathrm{M})$ RETURN
$40 \mathrm{Q}=(\mathrm{Y}(\mathrm{I}) *(\mathrm{Z}-\mathrm{X}(\mathrm{I}-\mathrm{INC}))-\mathrm{Y}(\mathrm{I}-\mathrm{INC}) *(\mathrm{Z}-\mathrm{X}(\mathrm{I}))) /(\mathrm{X}(\mathrm{I})-X(I$ 1- INC)) RETURN END

SUBROUTINE TIMDAT (TIMEDT)
C Get date and time
C

```
<-- TIMEDT char*24 string containing time & date.
```

CHARACTER*24 TIMEDT
CHARACTER* 36 MONTHS
INTEGER*2 YEAR, MONTH, DAY, HOUR, MIN, SEC, I100
MONTHS = 'JanFebMarAprMayJunJulAugSepOctNovDec'
C--The following 4 lines are for the IBM PC (using Microsoft C--time and date functions)

* CALL GETDAT (YEAR, MONTH, DAY)
* CALL GETTIM (IHOUR, MIN, SEC, I100)
* WRITE (TIMEDT, 100) IHOUR, MIN, MONTHS (MONTH*3-2:MONTH*3),

```
* & DAY, YEAR
```

C--get time for MTS version
C CALL TIME (22, 0, TIMEDT)
C--The following 5 lines are for the Apple Mac
C--(using Absoft time $\&$ date functions)
call date ( $m$, iday, iyear)
call time (isec)
write (timedt, 100)
\& isec $/ 3600$, mod (isec, 3600 ) / 60, months ( $m * 3-2: m * 3$ ),
\& iday, $1900+$ iyear
100 FORMAT (I2,':',I2.2,' on ',A3,I3,',',I5)
RETURN
END
SUBROUTINE TIRSUB (BETA, V, VYAW, ROLL)

* This subroutine solve simultaneous equations for slip and camber
* angles. It assumes a tire model that is linear with alpha and gamma
* but which has alpha and gamma coefficients that can be 3d-order
* functions of Fz .
* 

Appendix D - Source Code

```
        IMPLICIT REAL (K,M)
        DIMENSION A(4,4), B(4,4), C(4), D(4,4), E(4,4), F(4)
        DIMENSION ALFAV (4), GAMMAV(4)
        DIMENSION R(4,4), S(4,4), VVV(4), WWW(4), LV (4), MV (4)
        include TIRE.inc
        include SUSP.inc
        include VARS.inc
        include PARS.inc
        DATA ALFAV, GAMMAV /4*0.0, 4*0.0/
        DATA LV, MV /4*0, 4*0/
C
C zero out work matrices:
C
    DO 20 I = 1, 4
                DO 10 J = 1, 4
                        A(I,J) = 0.0
                        B(I,J) = 0.0
                        D(I,J) = 0.0
                        E(I,J) = 0.0
                            CONTINUE
            C(I) = 0.0
            F(I) = 0.0
    20 CONTINUE
C
C Load work matrices:
    DO 100 NAXLE = 1, 2
    YWPART = BETA + VYAW * XAXIE (NAXIE) / V
C
C
C Case for beam rear axle (no camber compliance, same steer compliance
C for both wheels):
C
    DO }80\mathrm{ NSIDE = 1,2
                        IJ = (NAXLE-1)*2 + NSIDE
                        IK = - (-1)**NSIDE
                        A(IJ,IJ) = 1. + CSFY (NAXLE) * POLY4 (CALFA (1,NAXIE),
                FZ (NAXIE,NSIDE))
            + CSMZ (NAXIE) * POLY4 (CALIGN (1,NAXIE), FZ (NAXLE,NSIDE))
                        A(IJ, IJ + IK) = CSFY (NAXIE)
                    POLY4 (CALFA (1,NAXIE), FZ (NAXIE,NSIDE+IK))
                + CSMZ (NAXLE) * POLY4 (CALIGN (1,NAXIE), FZ (NAXIE,NSIDE+IK))
                        B(IJ,IJ) = -CSFY (NAXIE) * POLY4 (CGAMMA (1,NAXIE),
                    FZ (NAXIE,NSIDE))
                            B(IJ, IJ + IK) = - CSFY (NAXLE) *
                                    POLY4 (CGAMMA (1,NAXIE), FZ (NAXIE,NSIDE+IK))
    C(IJ) = - (-1)**NSIDE * ALFAO (NAXIE) + YWPART
                                - CSFY (NAXIE) * POLY4 (CGAMMA (1,NAXIE), FZ (NAXIE,NSIDE))
                                * GAMMA (NAXIE,NSIDE)
                                - CSFY (NAXLE) * POLY4 (CGAMMA (1,NAXIE), FZ (NAXLE,NSIDE+IK))
                                * GAMMA (NAXIE,NSIDE+IK) - KNMSTR (NAXIE,NSIDE)
            D(IJ,IJ) = 1.
            E(IJ,IJ) = 0.0
            F(IJ) = (-1)**NSIDE*GAMMAO (NAXIE)
    CONTINUE
    ELSE
```

C Independent wheels, with coupling between camber and steer:
C
DO 90 NSIDE = 1,2
IJ = (NAXIE-1)*2 + NSIDE
C
C
C
C
IF (NAXLE .EQ. 1 .AND. ABS (SSKEY) .GT. 0.001) THEN
CSMZ (NAXLE) = 0.0
STRCON = FW (NSIDE)
ELSE
STRCON = SW / GRTODG
ENDIF
C
\& FZ (NAXLE,NSIDE))
+ CSMZ (NAXIE) * POLY4 (CALIGN(1,NAXIE), FZ (NAXIE,NSIDE))
B(IJ,IJ) = - CSFY (NAXLE) * POLY4 (CGAMMA (1,NAXLE),
FZ (NAXIE,NSIDE))
C(IJ) = - (-1)**NSIDE * ALFAO (NAXLE) + YWPART
- (2 - NAXLE) * STRCON - KNMSTR (NAXIE,NSIDE)
D (IJ,IJ) = 1. + CCFY (NAXIE) *
POLY4 (CGAMMA (1,NAXLE), FZ (NAXLE,NSIDE))
E(IJ,IJ) = - CCFY (NAXIE) * POLY4 (CALFA (1,NAXIE),
FZ (NAXIE,NSIDE))
F(IJ) = (-1)**NSIDE*GAMMAO (NAXIE) + ROLL
+ KNMCBR (NAXLE,NSIDE)
CONTINUE
C
C
100 CONTINUE
C
C Calculate tire gammas and slip angles:
C
C gammas:
C
CALL MINV (A, 4,DET,LV,MV)
CALL GMPRD (E,A,R,4,4,4)
CALL GMPRD (R,B,S,4,4,4)
CALL GMSUB (D,S,R,4,4)
CALL MINV (R,4,DET,LV,MV)
CALL GMPRD (E,A,S,4,4,4)
CALI GMPRD (S,C,VVV,4,4,1)
CALL GMADD (VVV,F,WWW,4,1)
CALL GMPRD (R,WWW, GAMMAV, 4,4,1)
C
C slip angles:
C
CALL GMPRD (B,GAMMAV,VVV,4,4,1)
CALL GMADD (VVV,C,WWW, 4,1)
CALL GMPRD (A,WWW,ALFAV, 4,4,1)
C
C Calculate Tire Moments and Forces from gammas and slip angles:

```
Appendix D - Source Code
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```

        DO 200 NAXLE = 1, 2
            DO 190 NSIDE = 1,2
    C
C
C
IJ = (NAXIE-1)*2 + NSIDE
GAMMA (NAXIE,NSIDE) = GAMMAV(IJ)
ALFA(NAXIE,NSIDE) = ALFAV(IJ)
C
C Calculate tire aligning moments and lateral forces:
C
MZ (NAXIE,NSIDE) = ALFA (NAXIE,NSIDE) * POLY4 (CALIGN (1,NAXIE),
FZ (NAXIE,NSIDE))
FY (NAXLE,NSIDE) = ALFA (NAXIE,NSIDE) * POLY4 (CALFA (1,NAXIE),
\& \& FZ (NAXIE,NSIDE))
\& FZ (NAXIE,NSIDE))
C
C Calculate compliance steer and "total" steer (kinem + compl + strcon
C input):
C
\& + CSFY (NAXIE) * FY (NAXIE,NSIDE)
TTLSTR (NAXIE,NSIDE) = KNMSTR (NAXLE,NSIDE)
\& + CPLSTR (NAXLE,NSIDE)
\& + (2 - NAXIE) * STRCON
190 CONTINUE
200 CONTINUE
C
RETURN
END
**************************************************************************************
C
C *** Trajectory Subroutine ***
C
C TRAJ: Computes lateral displacent of previewed path as a table look-up
C
C=_=_Muthor and Modification Section
Author: C. C. MacAdam
C
C Date written: 01/01/88
C
C Written on:
C
C Modifications:
C
C
C=_=_=_=_=_
C
C Purpose and use:
C
C Error conditions:
C
C Machine dependencies: none
C
C Called By: DRIVER
Appendix D - Source Code
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```
```

C
C
SUBROUTINE TRAJ(X, XT, YT, YPATH)
SAVE
C
C=_Wariable Descriptions
C
C---Arguments passed:
C
C ->X.......forward displacement (ft)
C ->XT......longitudinal path coordinates (ft)
C ->YT......lateral path coordinated corresponding to XT values (ft)
C <-YPATH...lateral displacement of path corresponding to X, (ft)
C
C
DIMENSION XT (*), YT(*)
C
C---Local variables
C
C J.......integer counter
C SLOPE...dYT/dXT of path at X
C
C---Functions and subroutines--------------------------------------------------
C
C None
C
C

```

```

C
C SEARCH FOR XI,XI+1:
DO 10 J = 1, 99
IF (X .GE. XT(J) .AND. X .LT. XT(J + 1)) GO TO 30
10 CONTINUE
WRITE (*,20)
20 FORMAT ('O', 'X-SEARCH IN SUB. TRAJ FAILED.')
STOP
30 SLOPE = (YT (J + 1) - YT (J)) / (XT (J + 1) - XT (J))
YPATH = YT(J) + SLOPE * (X - XT (J))
RETURN
END

```
```

C
C Transition Matrix Calculation.
C
C
C TRANS: Computes transition matrix of the linearized system
C

```

```

C
C Author: C. C. MacAdam
C
C Date written: 05/19/88
C
C Written on:
C
C Modifications:
Appendix D - Source Code
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```
```

C
C
C=___Algorithm Description=
C
C Purpose and use: Used by the driver model in predicting future states
C
C Error conditions:
C
C Machine dependencies: none
C
C Called By: DRIVGO
C
C
SUBROUTINE TRANS
SAVE
C
C=_=_=_=_=_=_
C
C---Arguments passed: None
C
DIMENSION SV(4), SD(4), SVI (4)
C
C---COMMON blocks
C
include drvmod.inc
C
C---DRIV.BLK common block variables---------------------------------------------
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS..wheelbase of vehicle (center-line of front \& rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....x-Y path coords (SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
C TFF......driver model preview time [input parameter] (sec)
C RM.......vehicle mass (slug)
C A........distance from C.g. to front suspension center-line (ft)
C B........distance from c.g. to rear suspension center-line (ft)
C RI.......total vehicle yaw inertia (slug-ft)
C PSIO.....current yaw angle reference value (rad)
C NTF......number of points in the preview time interval
C NP.......number of points in the x-y trajectory table
C TLAST....last time driver model calulated a steer value (sec)
C DFWLST...last value of steer calculated by driver model (rad)
C TILAST...last sample time driver model calulated a steer value (sec)
C DMEM.....2-dim array (time \& steer history) used in delay calculat'n
C XT,YT....transformation of XP,YP in vehicle body axes (ft)

```
```

C
C---TRSSTR.BLK common block variables
C
C TTT.......transition matrix at 10 discrete points in preview interval
C TTT1......integral of trans matrix wrt preview time
C GV.........vector of control gain coefficients
C
C---Local variables
C
C DELT.....time step in local Euler integration (sec)
C Al......llat accel coefficient of sideslip veloc in linearizd system
C B1...... " yaw rate
C A2.......yaw accel " sideslip vel "
C B2....... " yaw rate
C C1......steer control gain coefficient for lateral accel
C C2.......steer control gain coefficient for yaw moment
C ULAST....last value of forward velocity (ft/sec)
C NBEG.....integer startin counter value
C NEND1....integer ending counter value
C NENDV....integer ending counter value
C J........integer counter
C SV.......state vector: y,v,r,yaw,x [SAE]
C SV1......integral of state vector
C SD.......state vector derivative
C
C---Functions and subroutines
C
C None
C

```

```

C

```

```

C
C
DELT = 0.01
A1 = -2. * (CAF + CAR) / RM / U
B1 = 2. * (CAR*B - CAF*A) / RM / U - U
A2 = 2. * (CAR*B - CAF*A) / RI / U
B2 = -2. * (CAR*B*B + CAF*A*A) / RI / U
C1 = 2. * CAF / RM
C2 = 2. * CAF / RI * A
ULAST = U
GV (1) = 0.
GV(2) = C1
GV(3) = C2
GV(4) = 0.
DO 70 J = 1, 4
NBEG = TSS / DELT + 1
NEND1 = (TFF + .001 - TSS) / NTF / DELT
NENDV = NEND1
DO 10 L = 1, 4
SV (L) = 0.0
SVI (L) = 0.0
10 CONTINUE
TIME = 0.
C
C Initialize each state in turn to 1.0 and integrate (Euler).
C

```
```

        SV (J) = 1.0
        DO 60 I = 1, NTF
            DO 40 K = NBEG, NENDV
                SD(1) = SV (2) + U * SV (4)
                SD(2) = A1 * SV(2) + B1 * SV(3)
                SD (3) = A2 * SV(2) + B2 * SV(3)
                SD(4) = SV(3)
                DO 20 L = 1, 4
                SV (L) = SV (L) + SD (L) * DELT
            CONTINUE
                TIME = TIME + DELT
                DO 30 L = 1, 4
                SVI (L) = SVI (L) + SV(L) * DELT
            CONTINUE
    CONTINUE
    C
C Store "impulse" responses in TTT columns, integral in TTT1.
C TTT is a NPT-point tabular transition matrix, TTT1 is its integral.
C (See References 2 \& 3.)
C
DO 50 L = 1, 4
TTT (L,J,I) = SV (L)
TTT1 (L,J,I) = SVI (L)
CONTINUE
NBEG = NBEG + NEND1
NENDV = NENDV + NEND1
CONTINUE
70 CONTINUE
RETURN
END
C******************************************************************************
C*****************************************************************************
C Transition Matrix Calculation.
C
C
C TRANST: Computes transition matrix of the linearized system (torque
version of the driver model)
Author and Modification Section=

```
```

Author:

```
Author:
                            C. C. MacAdam
                            C. C. MacAdam
Date written: 01/30/89
Date written: 01/30/89
Written on:
Written on:
Modifications:
Modifications:
                                    Algorithm Description
                                    Purpose and use: Used by the driver model in predicting future states
                                    Error conditions:
Machine dependencies: none
Appendix D - Source Code
                                    D - 65
```

```
C
C Called By: DRIVGT
C
C
        SUBROUTINE TRANST
        SAVE
        REAL KSSL, ISSL
C
```



```
C
C---Arguments passed: None
C
        DIMENSION SV (6), SD (6), SVI (6)
C
C---COMMON blocks
C
        include drvtor.inc
        include pars.inc
        include glbl.inc
        include tire.inc
        include vars.inc
C
C---DRIV.BLK common block variables--------------------------------------------
-
C
C CAF...total cornering stiffness of tires on left front susp (lb/rad)
C CAR...total cornering stiffness of tires on left rear susp (lb/rad)
C WHBS..wheelbase of vehicle (center-line of front & rear susp) (ft)
C WF....static load on front suspension (lb)
C WR....static load on rear suspension (lb)
C U.....initial velocity (ft/sec)
C
C---DRVST1.BLK common block variables
C
C GRAV.....gravitational constant
C TICYCL...driver model sample time (sec)
C TSS......minimum preview time (sec)
C DMAX.....upper bound on front wheel angle steer (rad)
C XP,YP....x-y path coords(SAE) wrt inertial coords [input] (ft)
C TAUMEM...driver transport time dealy [input parameter] (sec)
C TFF......driver model preview time [input parameter] (sec)
C RM.......vehicle mass (slug)
C A........distance from C.g. to front suspension center-line (ft)
C B........distance from c.g. to rear suspension center-line (ft)
C RI.......total vehicle yaw inertia (slug-ft)
C PSIO.....current yaw angle reference value (rad)
C NTF......number of points in the preview time interval
C NP.......number of points in the x-y trajectory table
C TLAST....last time driver model calulated a steer value (sec)
C DFWLST...last value of steer calculated by driver model (rad)
C TILAST...last sample time driver model calulated a steer value (sec)
C DMEM.....2-dim array (time & steer history) used in delay calculat'n
C XT,YT....transformation of XP,YP in vehicle body axes (ft)
C
C---TRSSTR.BLK common block variables
C
C TTTT.......transition matrix at 10 discrete points in preview interval
```

C TTTT1......integral of trans matrix wrt preview time
C GGV.........vector of control gain coefficients
C
C---Local variables
C
C DELT.....time step in local Euler integration (sec)
C Al.......lat accel coefficient of sideslip veloc in linearizd system
C B1....... " yaw rate
C A2......yaw accel " "
C B2...... " yaw rate "
C C1......steer control gain coefficient for lateral accel
C C2.......steer control gain coefficient for yaw moment
C ULAST....last value of forward velocity (ft/sec)
C NBEG.....integer startin counter value
C NEND1....integer ending counter value
C NENDV....integer ending counter value
C J........integer counter
C SV.......state vector: y,v,r,yaw,x [SAE]
C SV1......integral of state vector
C SD.......state vector derivative
C
C---Functions and subroutines-
C

```

```

C
CSDAML = CSS * TODEG / ININFT
KSSL = KSS * TODEG / ININFT
XP = - POLY4 (CALIGN(1,1), FZ (1,1)) / POLY4(CALFA(1,1), FZ (1,1)) /
\& ININFT
XM = XTRAIL / ININFT
ISSL = ISS / ININFT
CSSL = CSS * TODEG / ININFT
DELT = 0.01
A1 = - 2. * (CAF + CAR) / RM / U
B1 = 2. * (CAR*B - CAF*A) / RM / U - U
A2 = 2. * (CAR*B - CAF*A) / RI / U
B2 = - 2. * (CAR*B*B + CAF*A*A) / RI / U
C1 = 2. * CAF / RM
C2 = 2. * CAF / RI * A
D1 = 1. / GR / (1. + 2. * (XP + XM) * CAF * (1. - CBOOST) / KSSL)
E1 = 2. * (XP + XM) * CAF * (1. - CBOOST) / (U * KSSL
\& * (1. + 2. * (XP + XM) * CAF * (1. - CBOOST) / KSSL) )
F1 = A * E1
A3 = 2. * (XP + XM) * CAF * (1. - CBOOST) / (GR * U * ISSL
\& * (1. + 2. * (XP + XM) * CAF * (1. - CBOOST) / KSSL) )
B3 = A * A3
C3 = - KSSL / (GR**2) * (1. - 1. / (1. + 2. * (XP + XM)
\& * CAF * (1. - CBOOST) / KSSL) ) / ISSL
D3 = - CSSL / ISSL
C
ULAST = U
GGV (1) = 0.
GGV (2) = 0.
Appendix D - Source Code

```
        \(\operatorname{GGV}(3)=0\).
        \(\operatorname{GGV}(4)=0\).
        \(G G V(5)=0\).
        GGV (6) = 1. / ISSL
        DO \(70 \mathrm{~J}=1,6\)
            NBEG \(=\) TSS \(/\) DELT +1
            NEND1 \(=(\mathrm{TFF}+.001-\mathrm{TSS}) / \mathrm{NTF} / \mathrm{DELT}\)
            NENDV = NEND1
            DO \(10 \mathrm{~L}=1\), 6
                \(S V(L)=0.0\)
                SVI (L) \(=0.0\)
    10 CONTINUE
    TIME \(=0\).
C
C Initialize each state in turn to 1.0 and integrate (Euler).
C
    \(S V(J)=1.0\)
    DO \(60 \mathrm{I}=1\), NTF
            DO \(40 \mathrm{~K}=\) NBEG, NENDV
                    \(S D(1)=S V(2)+U * S V(4)\)
                    \(S D(2)=(A 1+C 1 * E 1) * S V(2)+(B 1+C 1 * F 1) * S V(3)\)
                    \(\mathrm{SD}(3)=(\mathrm{A} 2+\mathrm{C} 2 \star \mathrm{E} 1) \star \mathrm{SV}(2)+(\mathrm{B} 2+\mathrm{C} 2 \star \mathrm{~F} 1) \star \mathrm{SV}(3)\)
                                    +C 2 * D1 * \(\mathrm{SV}(5)\)
                    \(S D(4)=S V(3)\)
                    \(S D(5)=S V(6)\)
                    \(\mathrm{SD}(6)=\mathrm{A} 3\) * \(\mathrm{SV}(2)+\mathrm{B} 3\) * \(\mathrm{SV}(3)+\mathrm{C} 3\) * \(\mathrm{SV}(5)+\mathrm{D} 3\) * \(\mathrm{SV}(6)\)
C
    \&
                                    + C1 * D1 * SV(5)
    \&
                    DO \(20 \mathrm{~L}=1,6\)
                    \(S V(L)=S V(L)+S D(L) * D E L T\)
                    CONTINUE
                    TIME = TIME + DELT
                    DO \(30 \mathrm{~L}=1\), 6
                        SVI \((L)=\) SVI \((L)+S V(L) * \operatorname{DELT}\)
                    CONTINUE
    30
                CONTINUE
C
C Store "impulse" responses in TTTT columns, integral in TTT1.
C TTTT is a NPT-point tabular transition matrix, TTT1 is its integral.
C (See References \(2 \& 3\). )
C
        DO \(50 \mathrm{~L}=1,6\)
            \(\operatorname{TTTT}(L, J, I)=S V(L)\)
            \(\operatorname{TTTT1}(L, J, I)=\operatorname{SVI}(L)\)
    50 CONTINUE
            NBEG = NBEG + NEND1
            NENDV = NENDV + NEND1
    60 CONTINUE
70 CONTINUE
        RETURN
        END
```

            SUBROUTINE WHEELZ (Z, ROLL, PITCH)
    C Subroutine wheelz updates the matrices ZW, FZ, KNMSTR, KNMCBR in
C common /VARS/ - namely: vertical displacement, normal ground load,
C bump-steer angle and bump-camber angle for each wheel, relative to
C static trim.
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C polarity: jounce displacement $\Longrightarrow$ positive $2 \mathrm{~W}, \mathrm{FZ}$
C
IMPLICIT REAL (K,M)
include SUSP.inc
include VARS.inc
DO 30, NAXLE $=1,2$
MOMENT $=$ KAUX (NAXLE) $*$ ROLI
\& $\quad$ - HOROLC (NAXLE) * (FY (NAXLE, 1) + FY (NAXLE, 2) )
DO 20, NSIDE $=1,2$
THISZW = Z - XAXLE (NAXLE) * PITCH
+.5 * TRACK (NAXLE) * ROLL * ( -1 ) **NSIDE
ZW (NAXIE, NSIDE) = THISZW
FZ (NAXIE, NSIDE) $=$ FZOWHL (NAXIE) + THISZW * KZ (NAXIE)
$+(-1) * *$ NSIDE * MOMENT / TRACK (NAXIE) + FD (NAXIE, NSIDE)
C
IF (KINEM) THEN
IF (NAXLE .EQ. 2 .AND. BEAM) THEN
KNMSTR (2,NSIDE) $=$ CSROLL $*$ ROLL
ELSE
KNMSTR (NAXIE, NSIDE) $=-(-1) \star \star$ NSIDE
\& * (CSZ (1,NAXIE) * THISZW

KNMCBR (NAXLE, NSIDE) $=(-1) \star \star$ NSIDE* (CCZ ( 1, NAXLE)

END IF
END IF
CONTINE
30 CONTINUE
C
RETURN
END
C
C
C
REAL KY, KL, KR, KM, KN, KSYWND, MXA, MYA, MZA, KD INTEGER WINDKY
COMMON /AERO/ AIRHO, AREA, QZERO, KY, CLO, KL, KR, CMO, KM, KN, 1 VWIND, KSYWND, VA, BETAIR, FYA, FZA, MXA, MYA, MZA, 2 CDO, KD, FDRAG, WINDKY, TWIND (1000), WINMAG (1000)
SAVE /AERO/
C
C
-----------------------------------> DRVMOD:
COMMON /DRVST1/ GRAV,TICYCL,TSS,DMAX,XPDR(100), YPDR(100), TAUMEM,
1 TFF, RM, A, B, RI, PSIO, NTF, NP, TLAST, DFWLST, TILAST,
$2 \operatorname{DMEM}(100,2), \operatorname{XT}(100), Y T(100)$
SAVE/DRVST1/
COMMON /DRIV/ CAF, CAR, WHBS, WF, WR, U
SAVE/DRIV/
COMMON /TRSSTR/ TTT $(4,4,10)$, $\operatorname{TTT1}(4,4,10)$, GV(4)
SAVE/TRSSTR/
C
C --------------------------------> DRVTOR:
C
COMMON /DRVST1/ GRAV, TICYCL,TSS,DMAX,XPDR(100), YPDR(100), TAUMEM,
1 TFF, RM, A, B, RI, PSIO, NTF, NP, TLAST, DFWLST, TILAST, $2 \operatorname{DMEM}(100,2), \operatorname{XT}(100), \operatorname{YT}(100)$
SAVE/DRVST1/
COMMON /DRIV/ CAF, CAR, WHBS, WF, WR, U
SAVE/DRIV/
COMMON /TRSTOR/ $\operatorname{TTTT}(6,6,10), \operatorname{TTTT1}(6,6,10), \operatorname{GGV}(6), \operatorname{STMAX}$ SAVE/TRSTOR/
C
C $\qquad$
CHARACTER*80 TITLE
CHARACTER* 32 FNREAD, FRMT
CHARACTER*8 UOMEGA, UTORQ, UANGL, UVELFT
CHARACTER*2 UDISP, UDIST, UFORC
CHARACTER*1 UNITS
REAL KMHMPH, ININFT
INTEGER NBYTES
PARAMETER (IREAD=5, IECHO=7, IOUT=8)
COMMON /GLBL/ NEQN, V, TEND, DT, NUMKEY, LNAME,
\& IPRINT, PI, ININFT, KMHMPH, G, TODEG, TITLE,
\& UOMEGA, UANGL, UVELFT, UTORQ, UDISP, UDIST, UFORC,
\& FNREAD, FRMT, NBYTES, UNITS
SAVE /GLBL/
C
C --------------------------------> MNVR:
C
REAL XPNT (999), YPNT (999), SLOPE (999)
COMMON /MNVR/ NSTEER, INDX, TSWBGN, TSWEND, SWAMPL, TSWPRD,
1 SWPHSE, SWSHFT, DRLAG, DRPREV, XPNT, YPNT, SLOPE
SAVE /MNVR/

Appendix D - Source Code


## APPENDIX E - DRIVER MODEL

This appendix contains copies of two technical papers which fully document the concepts implemented in the computer code used to represent the driver model closed-loop steering control process. Additional documentation is provided by comments contained in the computer code itself; see Appendices C and D (Subroutines DRIVGO, DRIVE1, TRANS, DRIVER, AND TRAJ).

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# Application of an Optimal Preview Control for Simulation of Closed-Loop Automobile Driving 

CHARLES C. MACADAM


#### Abstract

An optimal preview control method is applied to the automobile path following problem. The technique is first used to examine the straight-line regulatory driving task and results compared with similar experimental measurements. The method is further'demonstrated by closedloop simulation of an automobile driver/vehicle system during transient lane-change maneuvers. The computer simulation results are compared with equivalent vehicle test measurements.


## I. Introduction

THIS PAPER presents example applications (to the automobile path following problem) of a general method of control synthesis presented in [1]. The method is demonstrated here by simulation of a closed-loop automobile/driver system and the results compared with driver/vehicle test measurements. Results for the optimal preview control are also discussed within the context of manual control pursuit tracking task findings.
The control technique demonstrated herein is designed for application to linear time-invariant systems utilizing preview control strategies for regulation or tracking tasks. A common example of this type of control strategy occurs during normal automobile path following in which drivers "look-ahead" to follow a desired path. Human operators, as part of various man-machine systems, typically employ preview control strategies to control and stabilize such systems. It is widely recognized that human operators are capable of controlling and adapting to a wide variety of dynamical systems, many of which are vehicles with pre-view-oriented control requirements such as automobiles, bicycles, and complex aircraft [2]-[8]. Clearly human control of most vehicles would not be possible without some training by the operator to acquire an understanding of the vehicle response to various control inputs. While a certain portion of this training serves to identify and reinforce learned open-loop responses for repeated and familiar control task scenarios, the remainder frequently serves to identify and reinforce the operator's understanding or "feel" of the vehicle response to control inputs continually in use for closed-loop regulation and/or pursuit needs. It is in this latter control category for general linear system representations capable of preview control strategies, that the method presented in [1] can find particular application. As will be demonstrated in this paper, application to the

[^0]automobile path following problem produces substantive agreement when compared with driver/vehicle experimental measurements for both straight-line regulatory driving and transient lane-change maneuvers.

## II. The Optimal Preview Control

Before applying the optimal preview control of [1] to the automobile path following problem, the main results and symbol definitions contained therein are briefly reviewed in this section for later reference. As derived in [1], for the linear system

$$
\begin{align*}
& \dot{x}=F x+g u  \tag{1}\\
& y=m^{T} x \tag{2}
\end{align*}
$$

where
x $n \times 1$ state vector,
$y$ scalar output related to the state by the $n \times 1 m^{T}$ constant observer vector transpose,
$F$ constant $n \times n$ system matrix,
and
$g$ constant $n \times 1$ control coefficient vector,
the optimal control $u^{0}(t)$ which minimizes a special form of the local performance index,

$$
\begin{equation*}
J \triangleq \frac{1}{T} \int_{t}^{t+T}\{[f(\eta)-y(\eta)] W(\eta-t)\}^{2} d \eta \tag{3}
\end{equation*}
$$

over the current preview interval $(t, t+T)$ where
$W$ arbitrary weighting function over the preview interval
and
$f$ previewed input,
is given by

$$
\begin{align*}
& u^{0}(t)=\left[\int_{t}^{t+\tau}\left\{f(\eta)-m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{n!}\right] x(t)\right\}\right. \\
& \because \\
& \left.\cdot\left\{(\eta-t) m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] g\right\} W(\eta-t) d \eta\right] \\
&  \tag{4}\\
& /\left[\int_{t}^{t+\tau}\left\{(\eta-t) m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] g\right\}^{2}\right. \\
& \quad \cdot W(\eta-t) d \eta]
\end{align*}
$$

where $I$ is the identity matrix. For the special case of $W(\eta-t)=\delta\left(T^{*}\right)$, the Dirac delta function for $0<T^{*} \leqslant$ $T$, (4) simplifies to

$$
\begin{align*}
u^{0}(t) & =\frac{f\left(t+T^{*}\right)-m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{n!}\right] x(t)}{T^{*} m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{(n+1)!}\right] g}  \tag{5}\\
& =\left[f\left(t+T^{*}\right)-y_{0}\left(t+T^{*}\right)\right] /\left(T^{*} K\right), \tag{6}
\end{align*}
$$

the single-point preview control version of (4), where

$$
K \triangleq m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{(n+1)!}\right] g
$$

Equation (6) represents a proportional controller with gain inversely related to the preview interval $T^{*}$ and operating on the error between the previewed input $f\left(t+T^{*}\right)$ and $y_{0}\left(t+T^{*}\right)$, that portion of the previewed output deriving from the state vector's current initial condition. Likewise (4) can be interpreted as a proportional controller operating on a similar error averaged and weighted over the preview interval $(t, t+T)$ by the additional terms appearing in (4).

It is also shown in [1] that the optimal solution $u^{0}(t)$ can be expressed in terms of any current nonoptimal $u(t)$ and correspondingly nonzero preview output error $\epsilon(t)$ as

$$
\begin{equation*}
u^{0}(t)=u(t)+\frac{\int_{t}^{t+\tau} \varepsilon(\eta) A(\eta) W(\eta-t) d \eta}{\int_{t}^{t+T} A^{2}(\eta) W(\eta-t) d \eta} \tag{7}
\end{equation*}
$$

where

$$
\begin{aligned}
& A(\eta) \triangleq(\eta-t) m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] g \\
& \epsilon(\eta) \triangleq f(\eta)-m^{T} \phi(\eta, t) x(t)-u(t) A(\eta) \\
& \phi(\eta, t) \triangleq I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{n!} .
\end{aligned}
$$

For the special case of $W(\eta-t)=\delta\left(T^{*}\right)$, as before, ( 7 ) reduces to

$$
\begin{equation*}
u^{0}(t)=u(t)+\frac{\epsilon\left(t+T^{*}\right)}{T^{*} \cdot K} \tag{8}
\end{equation*}
$$

The formulation expressed by ( 7 ) can be useful in describing systems which do not achieve, though closely approximate, the defined optimal system behavior. Such cases may arise from limitations in achieving the precise optimal control due to time lags or dynamic properties inherent in the controller and not accounted for $a$ priori in the optimization. The next two sections adopt this view for the car/driver man-machine system in an attempt to describe and explain actual closed-loop driving behavior.

Finally, it was also shown in [1] that information concerning stability of the closed-loop system utilizing the optimal preview control of (4) or (7) is provided by the
characteristic roots of the constant matrix

$$
\begin{equation*}
\left[F-\boldsymbol{g} c^{T}\right] \tag{9}
\end{equation*}
$$

where

$$
\boldsymbol{c}^{T}=\frac{\boldsymbol{m}^{T} \int_{0}^{T} \phi(\eta, 0)\left\{\eta \boldsymbol{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] g\right\} W(\eta) d \eta}{\int_{0}^{T}\left\{\eta \boldsymbol{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] g\right\}^{2} W(\eta) d \eta} .
$$

For the special case of $W(\eta)=\delta\left(T^{*}\right)$, (9) becomes

$$
\begin{equation*}
F-\left\{g m^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{n!}\right] /\left(T^{*} \cdot K\right)\right\} \tag{10}
\end{equation*}
$$

## III. Application to Manual Control Pursutt Tracking Tasks as Represented by Straight-Line Automobile Drving

The most well-known and characteristic property exhibited by human operators in tracking tasks is the transport delay deriving from perceptual and neuromuscular mechanisms. By introducing this inherent delay property $a$ posteriori in the optimal preview control formulation, excellent agreement can be demonstrated between typical manual control pursuit tracking task results and the resulting optimal preview controller modified to include the inherent transport delay (heretofore referred to as the "modified" optimal preview control).

For reasons of clarity and notational simplicity, the discussion in this section will make use only of (8), the single-point preview control version of (7). Equation (8) can be represented by the block diagram of Fig. 1, where $G(s)=[I s-F]^{-1} g$ represents the controlled element vector transfer function, and $u(t)$, the current control, is related to the optimal control $u^{0}(t)$ by a transfer function $H(s)$ (previously assumed equal to one in the derivation of the optimal control $u^{0}(t)$ ). The introduction of the $H(s)$ transfer function is useful in describing systems which function (or are presumed to do so) in an error minimization fashion, but fail to achieve the precise optimal control due to an inherent limitation within the controller or control process itself, e.g., delays resulting from processor calculations and sample hold operations in digital systems. or perceptual/neuromuscular lags in the case of a human controller. By letting $H(s)=e^{-s 7}$, those actual delay limitations displayed by human operators during tracking tasks can be approximated by the parameter $\tau$, an effective transport lag. By incorporating this approximation and noting then that the transfer function relating $u(t)$ and $\epsilon\left(t+T^{*}\right)$ is $e^{-s t} /\left(1-e^{-s t}\right) K T^{*}$, Fig. 1 reduces to Fig. 2. a single-loop pursuit tracking formulation. The open-loop transfer function $Y_{0}(s)$ relating $y\left(t+T^{*}\right)$ and $\epsilon\left(t+T^{*}\right)$ is given by

$$
\begin{equation*}
Y_{0}(s)=\frac{e^{-s \tau}}{1-e^{-s t}}\left[1+\frac{m^{T} \phi\left(t+T^{*}, t\right) G(s)}{K T^{*}}\right] . \tag{11}
\end{equation*}
$$



Fig. 1. Block diagram for the single-point preview control.


- Fig. 2 Equivalent block diagram for the single-point preview control, $H(s)=e^{-\pi}$.

The stability of this system is determined by the characteristic roots of $1+Y_{0}(s)$, or equivalently,

$$
\begin{equation*}
1+e^{-s T} m^{T} \phi\left(t+T^{*}, t\right) G(s) / K T^{*}=0 \tag{12}
\end{equation*}
$$

To test the utility of this model by comparison with experimental findings, open-loop gain/phase frequency response results measured by Weir et al. [9, Fig. 12-C] for an automobile straight-line regulatory control task are presented in Figs. 3 and 4. These experimental results represent the open-loop frequency response relating the driver's output (presumably an estimate of future lateral position) to an assumed error, derived by the driver, between the previewed input (straight road ahead) and the driver's output. Since this may be categorized as a form of linear pursuit tracking, the formulation of (11) is accommodated. Also shown in Figs. 3 and 4 is the frequency response calculation for (11) with parameters $T^{*}=3.0(\mathrm{~s})$ and $\tau=$ 0.26 (s). The model output $y\left(t+T^{*}\right)$ is the estimated vehicle lateral position at time $t+T^{*}$; the input $f\left(t+T^{*}\right)$ $\equiv 0$ is the lateral displacement of the previewed path. The automobile ( $F, g$ ) dynamics used in (11) appear in Appendix I-A and duplicate those identified in [9]. The values of $T^{*}$ and $\tau$ were selected to fit the experimental data as closely as the single-point model would permit. As can be seen, the model and experimental results display excellent agreement. Not only does the preview model reproduce the -6 db /octave slope of the familiar manual control "crossover" model [2], [8] gain characteristic, but also the peaking phase characteristic usually displayed in manual control task experimental data of this kind.

The model parameters $T^{*}$ and $\tau$ appearing in (11) represent the average preview time used by the driver and


Fig. 3. Frequency response gain comparison.
his/her effective transport lag associated with this particular control task. The values of $T^{*}$ and $\tau$ used here fall well within the range identified by other investigators studying straight-line automobile driving [10]-[12] and human operator tracking performance [2], [4], [9].
Interestingly, for the relatively simple control task of typical straight-line automobile regulation as discussed here,


Fig. 4. Frequency response phase comparison.
the vehicle dynamics portion of the total transfer function (11) does not play a dominant role except at very low frequencies. As a result, the open-loop transfer function gain characteristic (11) is closely approximated by the human operator term, $e^{-s \tau} /\left(1-e^{-s T}\right) \approx e^{-s t} / \tau s$. Such a result would support the well-known fact that tracking task test results for simple automobile regulation [8], [9] can. generally be approximated by the "cross-over" model form $\mathrm{Ce}^{-s t} / \mathrm{s}$ ( $C$ being the "cross-over" gain constant) in the vicinity of the cross-over frequency. Moreover, in such cases where the above approximation does hold, $1 / \tau$ becomes $C$ in the "cross-over" model representation.

For the simple manual control pursuit tracking task, as represented here by straight-line automobile regulation, the modified optimal preview controller, even employed in only a single-point form $\left[W(\eta-t)=\delta\left(T^{*}\right)\right]$, appears to accurately mimic human control behavior. It might, therefore, seem reasonable to conjecture that human operator strategy during simple pursuit tracking (or at least straightline automobile regulation) is closely akin to an optimal preview error minimization process which ignores or is unaware of transport delay mechanisms inherent in the control processor. A more stringent test of this hypothesis is offered in the following section wherein transient automobile path following is examined using the modified optimal preview control model in its complete form.

## Application of the Optimal Preview Control for Smulation of Closed-Loop Transient Automobile Path Following

The previous section addressed the applicability of the optimal preview control to the problem of preview regulation and the effects of an inherent transport delay within


Fig. 5. Lane-change test course.


Fig. 6. Closed-loop simulation/test result comparison.
the controller. Using straight-line automobile regulation as an example, the single-point preview model was compared with experimental results within the frequency domain. In this section application to the tracking problem is demonstrated using the general preview control model (7), with an inherent transport time delay to simulate a closed-loop automobile/driver path following maneuver. Results from the model are compared with time history measurements from corresponding full-scale vehicle tests.

The specific closed-loop maneuver examined here required an automobile driver to perform a standard 3.66 m ( $12-\mathrm{ft}$ ) lane-change within a distance of 30.5 m ( 100 ft ) at a vehicle speed of approximately $26.8 \mathrm{~m} / \mathrm{s}(60 \mathrm{mi} / \mathrm{h})$. The initiation and completion of the lane change was constrained by $3.05-\mathrm{m}$ wide ( 10 ft ) cone-marked lanes (Fig. 5). The test vehicle was a standard American compact with measured parameter values shown in Appendix I-B. A representative test result for this vehicle/driver combination appears in Fig. 6, showing recorded-time histories of lateral acceleration, yaw rate, and front-wheel steer angle [13].

Also shown in Fig. 6 are computer simulation results using the optimal preview control (7) with an assumed human operator transport delay term $e^{-s \tau}$ relating $u^{0}(t)$ and $u(t)$. The transport lag term is included here, as in the previous section, to approximate the principal human operator lag effects. The calculation of (7), steer angle, seen in Fig. 6 is for values of $\tau=0.2$ (s) and $T=1.3$ (s) using ten equally spaced points in the preview interval to approximate the integral. The values of $T$ and $\tau$ were selected to closely fit the test measurements. The ( $F, g$ ) automobile dynamics model is the same two-degree-of-freedom model appearing in Appendix I-A, evaluated for the parameter values identified in Appendix I-B. The previewed input $f(\eta)$ appearing in ( 7 ) represents the desired lateral path deviation and was obtained during the simulation using the simple straight-line path segments shown in Fig. 5 as input.
As seen from Fig. 6, excellent agreement can be obtained between the experimental results and simulation predictions using the two numerical parameters ( $\tau, T$ ) and a simple straight-line path input. Variations in the value of $\tau$ primarily influenced the closed-loop system damping; larger values producing reduced damping. Variations in the value of $T$ influenced control (steering) amplitude as well as damping; larger values of $T$ producing lower control amplitude and increased damping.

Finally, Fig. 7 shows a comparison of the preview model predictions and measured test results for a modified set of vehicle dynamics $(F, g)$. The same vehicle was employed but with modifications to its mass center and rear tires so as to produce a new set of parameter values listed in Appendix I-C. As shown in Fig. 7 the principal change in the closed-loop response from Fig. 6 is an increased steering gain (lower steering amplitude for the same nominal maneuver) and decreased damping. Larger values of $\tau(0.3)$ and $T(1.55)$ were required in the calculation of (7), shown as steer angle in Fig. 7, to better approximate the reduced damping and smaller amplitude steering control. A comparison of computed vehicle path trajectories, corresponding to the baseline and modified vehicle responses shown in Figs. 6 and 7, appears in Fig. 8.

Characteristic roots for each of the closed-loop systems, as calculated from the constant matrix (13), are shown in Fig. 9. The matrix (13) (see Appendix I-D) is similar to that given by ( 9 ) but includes the influence of the transport lag term $e^{-s t}$ approximated by the first-order Pade polynomial

$$
\begin{gather*}
\frac{1-\frac{\tau}{2} s}{1+\frac{\tau}{2} s} \\
{\left[\begin{array}{c}
F \\
\hdashline c^{T}\left(F-\frac{2}{\tau} I\right)_{1} \\
\hdashline c^{T} g-\frac{2}{\tau}
\end{array}\right] .} \tag{13}
\end{gather*}
$$

Note that the reduced damping in the driver/vehicle responses, displayed in Figs. 7 and 8, is equivalently represented by the corresponding closed-loop characteristic root locations shown in Fig. 9.


Fig. 7. Closed-loop simulation/test result comparison-modified vehicle.


Fig. 8. Simulated path trajectories.


Fig. 9. Characteristic roots of the baseline and modified closed-loop systems.

These results and those of the previous section demonstrate useful application of the optimal preview model in simulation of closed-loop automobile driving. The principal conclusion concerning these results is that driver steering control strategy during path following can be accurately represented as a time-lagged optimal preview control. Similar applications and extensions to problems in other fields are clearly suggested by the results shown here.

## Conclusion

The optimal preview control model, applied here to the closed-loop automobile path following problem, offers a useful and direct method for representing closed-loop behavior of linear driver/vehicle systems. It is suggested that driver automobile steering control strategy during path following can be viewed as a time-lagged optimal preview control process.
The general linear system formulation of the preview control methodology, demonstrated here, permits application to a broad range of problems relating to manmachine systems.

## Appendix I

## A. Vehicle Dynamics

The linear dynamical equations of an automobile for lateral and yaw motions are
$\dot{y}=v+U \psi$
$\dot{v}=\left[-2\left(C_{a_{f}}+C_{\alpha_{k}}\right) / m U\right] 0+\left[2\left(b C_{a_{\Omega}}-a C_{a_{f}}\right) / m U-U\right] r$ $+\left(2 C_{a_{F}} / m\right) \delta_{F W}$
$\dot{r}=\left[2\left(b C_{a_{R}}-a C_{a_{f}}\right) / I U\right] v+\left[-2\left(a^{2} C_{a_{r}}+b^{2} C_{a_{R}}\right) / I U\right] r$ $+\left(2 a C_{a_{f}} / I\right) \delta_{F W}$
$\dot{\psi}=r$
where
$y$ inertial lateral displacement of the vehicle mass center,
o lateral velocity in the vehicle body axis system,
$r$ yaw rate about the vertical body axis,
$\psi$ vehicle heading angle, and
$\delta_{F W}$ front tire steer angle, control variable.
The parameters appearing in (Al)-(A4) are
$U \quad$ forward vehicle velocity,
$C_{\alpha_{r}}, C_{\alpha_{k}}$ front and rear tire cornering coefficients,
$a, b$ forward and rearward locations of tires from the vehicle mass center, and
$m, I \quad$ vehicle mass and rotational inertia.
The above equations can be expressed in matrix notation as

$$
\begin{equation*}
\dot{x}=F x+g \delta_{F w} \tag{A5}
\end{equation*}
$$

## where

$$
\begin{array}{ll}
x=\left\{\begin{array}{l}
y \\
0 \\
r \\
\psi
\end{array}\right\} \\
F=\left[\begin{array}{llll}
0 & 1 & 0 & U \\
0 & A_{1} & B_{1} & 0 \\
0 & A_{2} & B_{2} & 0 \\
0 & 0 & 1 & 0
\end{array}\right], \quad g=\left\{\begin{array}{l}
0 \\
C_{1} \\
C_{2} \\
0
\end{array}\right\}
\end{array}
$$

and

$$
\begin{aligned}
& A_{1}=-2\left(C_{a_{F}}+C_{\alpha_{k}}\right) / m U \\
& B_{1}=2\left(b C_{\alpha_{k}}-a C_{\alpha_{F}}\right) / m U-U \\
& C_{1}=2 C_{\alpha_{F}} / m \\
& A_{2}=2\left(b C_{\alpha_{k}}-a C_{\alpha_{F}}\right) / I U \\
& B_{2}=-2\left(a^{2} C_{a_{F}}+b^{2} C_{a_{k}}\right) / I U \\
& C_{2}=2 a C_{\alpha_{F}} / I .
\end{aligned}
$$

The calculation of (11) appearing in Figs. 3 and 4 used the following parameter values identified in [9] for vehicle D

$$
\begin{aligned}
a & =1.41 \mathrm{~m}(4.63 \mathrm{ft}) \\
b & =1.41 \mathrm{~m}(4.63 \mathrm{ft}) \\
m & =2016 \mathrm{~kg}(138 \mathrm{slug}) \\
I & =4013 \mathrm{~m} \cdot \mathrm{~N} \cdot \mathrm{~s}^{2}\left(2960 \mathrm{ft} \cdot \mathrm{lb} \cdot \mathrm{~s}^{2}\right) \\
U & =22.3 \mathrm{~m} / \mathrm{s}(73.3 \mathrm{ft} / \mathrm{s}) \\
C_{a_{r}} & =25266 \mathrm{~N} / \mathrm{rad}(5680 \mathrm{lb} / \mathrm{rad}) \\
C_{a_{\mathrm{k}}} & =70933 \mathrm{~N} / \mathrm{rad}(15960 \mathrm{lb} / \mathrm{rad}) .
\end{aligned}
$$

The constant observer vector $\boldsymbol{m}^{T}=(1,0,0,0)$ provided the vehicle lateral position $y$.

## B. Baseline Vehicle Parameter Values

The vehicle parameter values listed below and used in the calculations appearing in Fig. 6 were derived from vehicle wheelbase/weight measurements and steady-state, constant-steer vehicle test results [13]

$$
\begin{aligned}
a & =1.37 \mathrm{~m}(4.5 \mathrm{ft}) \\
b & =1.22 \mathrm{~m}(4.0 \mathrm{ft}) \\
m & =1563 \mathrm{~kg}(107 \mathrm{slug}) \\
I & =2712 \mathrm{~m} \cdot \mathrm{~N} \cdot \mathrm{~s}^{2}\left(2000 \mathrm{ft} \cdot \mathrm{lb} \cdot \mathrm{~s}^{2}\right) \\
U & =25.9 \mathrm{~m} / \mathrm{s}(85 \mathrm{ft} / \mathrm{s}) \\
C_{a_{r}} & =19438 \mathrm{~N} / \mathrm{rad}(4370 \mathrm{lb} / \mathrm{rad}) \\
C_{\alpha_{n}} & =33628 \mathrm{~N} / \mathrm{rad}(7560 \mathrm{lb} / \mathrm{rad}) .
\end{aligned}
$$

The weighting function $W$ appearing in (7) was selected as constant 1.0 over the ten-point preview interval.

## C. Modified Vehicle Parameter Values

The vehicle parameters of Appendix I-B were altered to those values shown in this section by a rearward shift in the vehicle mass center and a decrease in rear tire inflation
pressures

$$
\begin{aligned}
a & =1.43 \mathrm{~m}(4.7 \mathrm{ft}) \\
b & =1.16 \mathrm{~m}(3.8 \mathrm{ft}) \\
m & =1753 \mathrm{~kg}(120 \mathrm{slug}) \\
I & =2712 \mathrm{~m} \cdot \mathrm{~N} \cdot \mathrm{~s}^{2}\left(2000 \mathrm{ft} \cdot \mathrm{lb} \cdot \mathrm{~s}^{2}\right) \\
U & =25.9 \mathrm{~m} / \mathrm{s}(85 \mathrm{ft} / \mathrm{s}) \\
C_{a_{r}} & =20906 \mathrm{~N} / \mathrm{rad}(4700 \mathrm{lb} / \mathrm{rad}) \\
C_{a_{k}} & =29536 \mathrm{~N} / \mathrm{rad}(6640 \mathrm{lb} / \mathrm{rad}) .
\end{aligned}
$$

The closed-loop calculation using these parameter values appears in Fig. 7.

## D. Stability of the Closed-Loop Optimal Preview-Controlled System Including a Transport Time Lag

Given the system

$$
\begin{align*}
\dot{x} & =F x+g u  \tag{A6}\\
u & =e^{-s \tau} u^{0}  \tag{A7}\\
u^{0} & =-c^{T} x \tag{A8}
\end{align*}
$$

where $F, g, u^{0}$, and $c^{T}$ are defined in (1), (4), and (9). If the transport time lag $e^{-3 t}$ is approximated by the first-order Padé polynomial,

$$
\begin{equation*}
\frac{1-\frac{\tau}{2} s}{1+\frac{\tau}{2} s} \tag{A9}
\end{equation*}
$$

(A7) becomes

$$
\begin{equation*}
\dot{u}=\frac{2}{\tau}\left(-u+u^{0}\right)-\dot{u}^{0} . \tag{A10}
\end{equation*}
$$

Substitution of

$$
u^{0}=-c^{T_{x}}
$$

and

$$
\dot{u}^{0}=-c^{T}[F x+g u]
$$

into (A10) produces the closed-loop state equation

$$
\left\{\frac{\dot{x}}{\dot{u}}\right\}=\left[\begin{array}{cc}
F & \boldsymbol{g} \\
\hdashline c^{T}\left(F-\frac{2}{\tau} I\right)_{1} c^{T} \boldsymbol{g}-\frac{2}{\tau}
\end{array}\right]\left\{\frac{x}{u}\right\}(\mathrm{All})
$$

equivalent of (A0)-(A8). For small $\tau$, stability of the time-lagged optimal preview-controlled system is provided by the characteristic roots of the system matrix appearing in (All).

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Technical Briefs

## An Optimal Preview Control for Linear Systems

## C. C. MacAdam ${ }^{\prime}$

A technique for synthesizing closed-loop control of linear time-invariant systems during tracking of previewed inputs is presented. The derived control is directly dependent upon the properties of the controlled system and is obtained by minimization of a defined previewed output error.

## 1 Introduction

This paper presents a general method of control synthesis applicable to linear time-invariant systems utilizing preview control strategies for regulation or tracking tasks. A common example of this type of dynamical behavior occurs during normal automobile path following in which drivers "lookahead'" to follow a desired path. A frequent source of preview control strategies in various man-machine systems is, of course, the human operator. It is widely recognized that human operators are capable of controlling and adapting to a wide variety of dynamical systems, many of which are vehicles with preview-oriented control requirements such as automobiles, bicycles, and complex aircraft [1-7]. Although this paper does not offer evidence as to the utility of the proposed control synthesis for man-machine systems involving preview strategies, it is suggested that the method presented here can be applied to such problems. Portions of the work by Tomizuka [8], which treated a similar problem, indicated useful application of optimal preview control me:hods in representing man-machine dynamical behavior.

The particular method presented in this paper is directly applicable to general linear system representations assumed to incorporate preview control strategies that depend only upon knowledge of the current values of the state and control. The optimal control is derived by minimization of a performance index that is defined as a mean squared preview output error. It will be shown that the derived control function is not arbitrary or independent but depends directly upon the dynamical properties of the controlled system.

## II Statement of the Problem <br> Given the linear system

$$
\begin{gather*}
\dot{x}=F x+g u  \tag{1}\\
y=m^{T} \mathbf{x} \tag{2}
\end{gather*}
$$

[^1]where,
x is the $n \times 1$ state vector
$\boldsymbol{y}$ is the scalar output related to the state by the $n \times 1 \mathrm{~m}^{T}$ constant observer vector transpose
$F$ is the constant $n \times n$ system matrix
and
$g$ is the constant $n \times 1$ control coefficient vector
find the control, $u(t)$, which minimizes a local performance index,
\[

$$
\begin{equation*}
J \triangleq \frac{1}{T} \int_{t}^{1+T}\{[f(\eta)-y(\eta)] W(\eta-t)\}^{2} d \eta \tag{3}
\end{equation*}
$$

\]

over the current preview interval $(t, t+T)$, where,
$W$ is an arbitrary weighting function over the preview interval
and $f$ is the previewed input.
The performance index given by (3) represents the weighted mean squared error between the previewed input and the previewed output as defined below.

The previewed output, $y(\eta)$, is related to the present state, $x(t)$, by

$$
\begin{equation*}
y(\eta)=\mathbf{m}^{T} \phi(\eta, t) \mathbf{x}(t)+\int_{1}^{\eta} \mathbf{m}^{T} \phi(\eta, \xi) \mathbf{g} u(\xi) d \xi \tag{4}
\end{equation*}
$$

where,

$$
\phi(\eta, t)=\exp [F(\eta-i)]
$$

is the transition matrix of the system $F[9]$.
If $u(t)$ is assumed selected on the basis of a constant previewed control, $u(\xi)=u(t)$, equation (4) simplifies to

$$
\begin{equation*}
y(\eta)=\mathbf{m}^{\top} \phi(\eta, t) x(t)+u(t) \int_{1}^{\eta} \mathbf{m}^{\top} \phi(\eta, \xi) g d \xi \tag{5}
\end{equation*}
$$

and the performance index, (3), can be written as
$J=\frac{1}{T} \int_{t}^{t+T}\left\{\left[f(\eta)-\mathrm{m}^{T} \phi(\eta, t) \mathbf{x}(t)\right.\right.$

$$
\begin{equation*}
\left.\left.-u(t) \int_{1}^{\eta} \mathbf{m}^{\top} \phi(\eta, \xi) \mathbf{g} d \xi\right]^{2} \cdot W(\eta-t)\right\} d \eta \tag{6}
\end{equation*}
$$

The above assumption simply requires the resulting optimization to reflect a control strategy dependent only upon current values of the state and control. This assumption is, in part, motivated by the potential application to those manmachine systems, wherein, it is assumed the human operator is limited in deriving or having knowledge a priori of more complex or optimal control waveforms over the preview interval.
The necessary condition for minimization of $J$, defined by
equation (6), with respect to the control, $u(t)$, is provided ty. : $J$ id $d u=0$, or
$\frac{d J}{d u}=\frac{2}{T} \int_{1}^{1-T}\left\{\left[f(\eta)-\mathbf{m}^{T} \circ(\eta, t) \mathbf{x}(t)\right.\right.$
$\left.\left.-u(t) \int_{i}^{T} m^{\top} \phi(\eta, \xi) g d \xi\right]\right\}$

$$
\begin{equation*}
\cdot\left\{\int_{1}^{\eta} \mathbf{m}^{T} \circ(\eta, \xi) g d \xi\right\} W(\eta-t) d \eta=0 \tag{7}
\end{equation*}
$$

Equating $\phi(\eta, \xi)$ with $\exp [F(\eta-\xi)]=1+\sum_{n=1}^{\infty} F^{n} \frac{(\eta-\xi)^{n}}{n!}$,
where $l$ is the identity matrix, and performing the $d \xi$ in:egrations, (7) becomes
$\frac{d J}{d u}=\frac{2}{T} \int_{1}^{1+T}\left\{f(\eta)-\mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{n!}\right] \mathbf{x}(t)\right.$
$\left.-(\eta-t) \mathbf{m}^{T}\left[I+\sum_{n=i}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] \mathbf{g} u(t)\right\}\left\{(\eta-t) \mathbf{m}^{T}\right.$

$$
\begin{equation*}
\left.\cdot\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] \mathbf{g}\right\} W(\eta-t) d \eta=0 \tag{8}
\end{equation*}
$$

jolving (8) for $u(t)$ yields
$u^{0}(t)=\left[\int_{1}^{1+T}\left\{f(\eta)-\mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{n!}\right] \mathbf{x}(t)\right\}\right.$
$\left.\cdot\left\{(\eta-t) \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{P^{n}(\eta-t)^{n}}{(n+1)!}\right] \mathbf{g}\right\} W(\eta-t) d \eta\right]$
$\left[\int_{1}^{1+T}\left\{(\eta-t) \mathbf{m}^{T}\left[1+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] \mathbf{g}\right\}^{2} W(\eta-t) d \eta\right]$
where $u^{0}(t)$ represents the optimal solution. For the special case of $W(\eta-t)=\delta\left(T^{\circ}\right)$, the Dirac delta function for 0 $<T \leq T$, (9) simplifies to

$$
\begin{align*}
u^{0}(t) & =\frac{f\left(t+T^{*}\right)-\mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{n!}\right] \mathbf{x}(t)}{T \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{(n+1)!}\right] \mathbf{g}}  \tag{10}\\
& =\left[f\left(t+T^{*}\right)-y_{0}\left(t+T^{*}\right)\right] /\left(T^{\top} K\right) \tag{11}
\end{align*}
$$

where

$$
K \triangleq \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}\left(T^{*}\right)^{n}}{(n+1)!}\right] \mathbf{g}
$$

Equation (11) represents a proportional controller with gain inversely related to the preview interval, $T$, and operating on the error between the previewed input, $f(t+T)$, and $y_{0}\left(t+T^{*}\right)$, that portion of the previewed output deriving from the state vector's current initial condition. Likewise, equation (9) can be interpreted as a proportiona! controller operating on a similar error averaged and weighted over the preview interval ( $t, t+T$ ) by the additional terms appearing in equation (9).
The optimal solution, $u^{0}(t)$, can also be expressed in terms of any current non-optimal $u(t)$ and correspondingly nonzero preview output error, $\epsilon(t)$, by writing equation (9) as
$u^{0}(t)=\left[\int_{1}^{1+T}\left\{f(\eta)-\mathbf{m}^{T} \phi(\eta, t) \mathbf{x}(t)-u(t) A(\eta)\right\}\right.$

- $\left.A(\eta) W(\eta-t) d \eta+u(t) \int_{1}^{1+\tau} A^{2}(\eta) W(\eta-t) d \eta\right]$

$$
\begin{equation*}
/\left[\int_{1}^{1+\tau} A^{2}(\eta) W(\eta-t) d \eta\right] \tag{12}
\end{equation*}
$$

or

$$
\begin{equation*}
u^{0}(t)=u(t)+\frac{\int_{1}^{1+\tau} \epsilon(\eta) A(\eta) W(\eta-t) d \eta}{\int_{1}^{1+T} A^{2}(\eta) W(\eta-t) d \eta} \tag{13}
\end{equation*}
$$

where

$$
A(\eta) \Delta(\eta-t) \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{(n+1)!}\right] \mathbf{g}
$$

$$
\epsilon(\eta) \triangleq f(\eta)-\mathbf{m}^{\top} \phi(\eta, t) \mathbf{x}(t)-u(t) A(\eta)
$$

$$
\phi(\eta, t) \triangleq \mathrm{I}+\sum_{n=1}^{\infty} \frac{F^{n}(\eta-t)^{n}}{n!}
$$

For the special case of $W(\eta-t)=\delta\left(T^{*}\right)$, as before, equation (13) reduces to

$$
\begin{equation*}
u^{0}(t)=u(t)+\frac{\epsilon\left(t+T^{*}\right)}{T^{\cdot} \cdot K} \tag{14}
\end{equation*}
$$

The formulation expressed by equation (13) can be useful in describing systems which do not achieve, though closely approximate, the optimal system behavior. Such cases may arise from limitations in achieving the precise optimal control due to time lags or dynamic properties inherent in the controller and not accounted for a priori in the optimization.

While equations (9) and (13) are equivalent mathematiçally, the latter deomonstrates an explicit relationship between the derived optimal control and the previewed output error function appearing in the performance index of the original problem formulation. Simply stated, the current control level is modified only in response to a nonzero function of the previewed output error, and, in this sense, analogous to an integral controller.

Finally, dependence of the derived optimal control upon the system $(F, \mathrm{~g})$ properties is clearly demonstrated by the explicit presence of $F$ and g in equations (9) and (13). Furthermore, information concerning stability of the closed-loop system utilizing the optimal preview control of equation (9) or (13) is provided by the characteristic roots of the constant matrix

$$
F-\frac{\mathbf{g m}^{T} \cdot \int_{0}^{T}\left\{\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{n!}\right]\right\}\left\{\eta \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] \mathbf{g}\right\} W(\eta) d \eta}{\int_{0}^{T}\left\{\eta \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] \mathbf{g}\right\}^{2} W(\eta) d \eta}
$$

where

## Introduction

The purpose of the present paper is twofold. The first is to obtain an analytic expression for the critical speed of a

$$
\mathbf{c}^{T}=\frac{\mathbf{m}^{T} \int_{0}^{T}\left\{\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{n!}\right]\right\}\left\{\eta \mathbf{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] \mathbf{g}\right\} W^{\prime}(\eta) d r}{\int_{0}^{T}\left\{\eta \boldsymbol{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(\eta)^{n}}{(n+1)!}\right] \mathbf{g}\right\}^{2} W(\eta) d \eta}
$$

resulting from the substitution of (9) into (1). For the special case of $W(\eta)=\delta(T)$, (15) becomes

$$
\begin{equation*}
F-\left\{\boldsymbol{g} \boldsymbol{m}^{T}\left[I+\sum_{n=1}^{\infty} \frac{F^{n}(T)^{n}}{n!}\right] /(T \cdot K)\right\} \tag{16}
\end{equation*}
$$

## III Summary

The optimal preview control model presented here offers a useful and direct method for representing closed-loop behavior of linear systems utilizing preview control strategies. The derived control is directly related to the properties of the linear system and the previewed input. Further, the method is formulated in terms of general linear system representations, thereby permitting applications to a wide variety of problems.

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## Asymptotic Theory of Freight Car Hunting

## A. M. Whitman ${ }^{1}$

A simple formula is derived for the hunting speed of a freight car from an 8 degree of freedom linear model using asymptotic techniques. A comparison is made between the approximation and exact (numerical) solutions. The two agree within 10 percent for parameter values typical of present designs.

[^2]multidegree of freedom model of a freight car which is simple enough to convey physical insight into the hunting probiem while at the same time complex enough to have validity for realistic vehicles. The second is to illustrate the simplification which can be effected in problems of this type by employing asymptotic methods. These methods are model independent and rely on the fact that the creep forces dominate the motion.

Previous work has included analytical studies of simple vehicles [1-2] and numerical solutions for realistic vehicles [34]. The present work can be viewed as a generalization and formal mathematical justification of the former, which although cleverly done are ad hoc by nature and seem to be restricted to systems with few degrees of freedom, and a specialization of the latter, giving the same results in the region of validity of the expansion but being restricted by nature to specific regions in parameter space. The utility of the present work is in the simple result which it yields. From this one can obtain physical insight into the phenomenon as well as easily calculable answers.

## Model Description

We consider a model of the lateral dynamics of a freight car composed of a rigid car body pinned at either end to a truck. The pin connection transmits a linear damping moment (constant $c^{\prime} f$ ) between the car body and the truck. Each truck, see Fig. 1, is composed of 2 wheelsets, two rigid sideframes connected by ball joints to each wheelset, and a boister, which contains the car connection (centerplate) at its midpoint, is constrained to move parallel to each wheelset by means of frictionless sloted pins in each sideframe, and is restrained from moving freely in that direction by 2 linear springs (constant $k$ each) and dampers (constant $c$ each) at each end. In the real system this restraint is provided by the shear stiffness of the bolster springs, whose primary function is to support the car weight, and the sliding of the friction wedges laterally. Further, because the springs and dampers are separated by a distance $d$, there is a moment tending to square the truck due to both the springs (constant $4 k d^{2}$ ) and the dampers constant $4 c d^{2}$ ). In addition, the bolster has mounted symmetrically with respect to the centerplate, constant contact sidebearings (constant $\bar{k}_{B}$ each) whose function is to provide a torsional spring restraint for the bolster relative to the car body (constant $2 \hat{k}_{B} w^{2}$ ). Actually the sidebearings also transmit a damping moment between the bolster and the car body (constant $2 c_{B} w^{2}$ ); however, this has the same form as the centerplate moment and can be combined with it. There are eight degrees of freedom in this model and we will take as our independent coordinates $x^{F}, \psi^{F}, \beta^{F}, u^{F}, x^{R}, \psi^{R}, \beta^{R}, u^{R}$. Here the superscripts represent the front and rear truck coordinates, $x$ is the axial displacement of the truck centroid relative to the track center line, $\psi$ the yaw angle of each wheelset of the truck as a result of the kinematic constraint, $\beta$ the trail angle of the truck, and $u$ the bolster displacement relative to the truck centroid. The equations of motion, which have been derived elsewhere [5] and which are quite similar to others which have been discussed in the literature [4], are written here in dimensionless form in terms of sum and difference coordinates,


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