

No. 208  
November 1978

Forward Speed Effects on the Sway, Roll,  
and Yaw Motion Coefficients

Armin Troesch

This research was carried out under the  
Naval Sea Systems Command  
General Hydromechanics Research Program  
Subject SR 009 01 01, administered by the  
Naval Ship Research and Development Center.  
Contract No. N00014-76-C-0345

Reproduction in whole or in part permitted  
for any purpose of the United States Government  
Approved for public release; distribution unlimited



Department of Naval Architecture  
and Marine Engineering  
College of Engineering  
The University of Michigan  
Ann Arbor, Michigan 48109

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER 208	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Forward Speed Effects on the Sway, Roll and Yaw Motion Coefficients		5. TYPE OF REPORT & PERIOD COVERED Final Report 10/1/75 - 9/30/78
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Armin Troesch		8. CONTRACT OR GRANT NUMBER(s) N00014-76-C-0345
9. PERFORMING ORGANIZATION NAME AND ADDRESS Department of Naval Architecture and Marine Engineering. The University of Michigan, Ann Arbor, MI.		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 61153N, \$02301, SR.023 01 01
11. CONTROLLING OFFICE NAME AND ADDRESS Naval Ship Research & Development Center, Code 1505, Bethesda, MD 20084		12. REPORT DATE November 1975
		13. NUMBER OF PAGES 25
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) Office of Naval Research Arlington, VA 22127		15. SECURITY CLASS. (of this report) UNCLASSIFIED
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Roll, Added mass and damping, Forward Speed, Sway, Yaw		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The added mass and damping coefficients for sway, roll and yaw are formulated for a ship with forward speed. The theory is similar to that given by Ogilvie and Tuck (1969) for the heave and pitch coefficients of a slender ship. Numerical results are presented for the cross-coupling coefficients.		

## ABSTRACT

The added mass and damping coefficients for sway, roll and yaw are formulated for a ship with forward speed. The theory is similar to that given by Ogilvie and Tuck (1969) for the heave and pitch coefficients of a slender ship. Numerical results are presented for the cross-coupling coefficients.

## ACKNOWLEDGMENTS

I would like to thank Professor T.F. Ogilvie for his assistance in this work and Ms. Kay Sober for aiding me with the report preparation. Acknowledgment is also made to the Naval Sea Systems Command General Hydromechanics Research Program Subproject SR 023 01 01, administered by the Naval Ship Research and Development Center, which sponsored this work under contract N00014-76-C-0345.

TABLE OF CONTENTS

	Page
ABSTRACT . . . . .	v
ACKNOWLEDGMENTS . . . . .	vii
LIST OF ILLUSTRATIONS . . . . .	xi
INTRODUCTION . . . . .	1
STATEMENT OF THE PROBLEM WITH RESULTS . . . . .	3
<i>EQUATIONS OF MOTION</i> . . . . .	3
<i>ADDED MASS AND DAMPING COEFFICIENTS</i> . . . . .	5
NUMERICAL RESULTS . . . . .	9
APPENDIX . . . . .	19
<i>FORCE AND MOMENT ON THE HULL</i> . . . . .	19
<i>NUMERICAL METHOD FOR DETERMINING THE     ADDED MASS AND DAMPING COEFFICIENTS</i> . . . . .	23
REFERENCES . . . . .	25

## LIST OF ILLUSTRATIONS

	Page
Figure 1: Coordinate System . . . . .	4
Figure 2: Sway response to unit roll moment . . . . .	14
Figure 3: Roll response to unit roll moment . . . . .	14
Figure 4: Yaw response to unit roll moment . . . . .	15
Figure 5: Added mass coefficients $A_{62}$ and $A_{26}$ . . . . .	16
Figure 6: Damping coefficients $B_{62}$ and $B_{26}$ . . . . .	16
Figure 7: Added mass coefficients $A_{64}$ and $A_{46}$ . . . . .	17
Figure 8: Damping coefficients $B_{46}$ and $B_{64}$ . . . . .	17
Figure 9: Relative importance of free surface integrals . . . . .	18
Figure 10: Relative importance of free surface integrals . . . . .	18

## INTRODUCTION

A substantial amount of effort has gone into predicting the added mass and damping coefficients of an oscillating ship. Historically, a large part of this effort has been concentrated on the vertical plane motions of heave and pitch with some interest shown in the horizontal motion of roll. Korvin-Kroukovskiy and Jacobs (1957) emphasized the importance of coupling coefficients in the vertical plane motions, i.e. the pitch force due a heave motion and vice versa. Their method of calculating these coefficients was based on strip theory with some adjustments made to include forward speed and three-dimensional effects. However, their method for finding these "dynamic coupling" terms appears to be incomplete in that these terms do not satisfy the symmetry relations established by Timman and Newman (1962).

Salvesen, Tuck and Faltinsen (1970) applied a more consistent approach to the problem of ship motions and developed a theory for both the vertical and horizontal modes of motion. Their cross-coupling coefficients did satisfy the Timman-Newman (1962) relations and gave improved results when theory was compared with experiment.

Ogilvie and Tuck (1969) found the added mass and damping coefficients for heave and pitch by using a systematic application of matched asymptotic expansions. Their results satisfied the Timman-Newman (1962) symmetry relations but differed from the coefficients given by Salvesen, Tuck and Faltinsen (1970) in a number of ways. The Ogilvie-Tuck coefficients included a term which represented the integral of the square of the velocity potential evaluated on the free surface. They did not include a velocity-squared term which they considered to be of higher order. In an effort to determine the relative importance of the free surface integral terms, Faltinsen (1974) evaluated them and compared them with both experiments and the terms given by Salvesen, Tuck and Faltinsen. The results indicate that the Ogilvie-Tuck heave-pitch coupling coefficients are important and compare better with experiment than previous theories.

Timman and Newman (1962) included the horizontal motions in their symmetry relations. Specifically they reported that the cross-coupling terms between roll and yaw and yaw and sway were antisymmetric with respect to forward velocity. Inspection of the Salvesen, Tuck and Faltinsen coefficients show that they satisfy these conditions.

One motion coefficient in the horizontal plane that has received some attention is the roll damping coefficient. Typically the damping coefficient is composed of a velocity independent part, calculated from potential theory, and a correction factor used to account for viscous effects. In an effort to more clearly understand these various effects on roll motion, Sugai and Yamanouchi (1963) conducted a series of experiments using a self-propelled model with opposing gyroscopes to provide a rolling moment. One of the results of these experiments was the indication that rolling motion becomes more linear as forward speed is increased. In other words, the non-dimensional quantity of roll motion divided by roll exciting moment (multiplied by the appropriate constant to correct for the units) becomes less a function of the actual magnitude of the rolling moment. This implies that roll damping is speed dependent and that this dependency may be at least as important as the viscous damping. Watanabe (1977) applied the principle of thin ship theory to this problem and produced results that show a speed dependency on the roll damping coefficient. However, he did not conclusively state what effects a non-thin ship would have on his theory.

Using the same assumptions made by Ogilvie and Tuck (1969) for the vertical plane motions, we will consider in this paper the following two questions: First, will a consistent slender body theory produce roll damping coefficients that reduce roll motions as the speed of the ship increases? And second, will the theory produce numerically significant terms to the ones derived by Ogilvie and Tuck.



STATEMENT OF THE PROBLEM WITH RESULTS

EQUATIONS OF MOTION

Similar to that shown by Salvesen, Tuck and Faltinsen (1970), the coupled equations of motions for sway, roll, and yaw may be given as follows:

$$\begin{aligned} (A_{22} + M)\ddot{\eta}_2 + B_{22}\dot{\eta}_2 + (A_{24} - Mz_c)\ddot{\eta}_4 + B_{24}\dot{\eta}_4 \\ + (A_{26} + x_c M)\ddot{\eta}_6 + B_{26}\dot{\eta}_6 = F_2 e^{i\omega t} \end{aligned} \quad (1)$$

$$\begin{aligned} (A_{42} - Mz_c)\ddot{\eta}_2 + B_{42}\dot{\eta}_2 + (A_{44} + I_4)\ddot{\eta}_4 + B_{44}\dot{\eta}_4 + C_{44}\eta_4 \\ + (A_{46} - I_{46})\ddot{\eta}_6 + B_{46}\dot{\eta}_6 = F_4 e^{i\omega t} \end{aligned} \quad (2)$$

$$\begin{aligned} (A_{62} + x_c M)\ddot{\eta}_2 + B_{62}\dot{\eta}_2 + (A_{64} - I_{46})\ddot{\eta}_4 + B_{64}\dot{\eta}_4 \\ + (A_{66} + I_6)\ddot{\eta}_6 + B_{66}\dot{\eta}_6 = F_6 e^{i\omega t} \end{aligned} \quad (3)$$

where

$M$  is the mass of the ship

$A_{jk}, B_{jk}$  are the added mass and damping coefficients respectively

$I_j$  is the moment of inertia about the  $j$ -th axis

$I_{jk}$  is the product of inertia

$z_c$  is the vertical location of the center of gravity

$F_j e^{i\omega t}$  is the force or moment in the  $j$ -th mode due to waves

$C_{44}$  is the hydrostatic roll restoring moment

$x_c$  is the longitudinal location of the center of gravity

$\omega$  is the frequency of encounter

$\eta_j$  for  $j=2,4,6$  is the sway, roll, and yaw displacement, respectively.

(The dots denote time derivatives, i.e.  $\ddot{\eta}_4$  is the roll acceleration.)

The coordinate system used is a right hand one with the origin located in the plane of the undisturbed free surface and the  $z$  axis passing through mid-ship. See Figure 1 for definitions of positive sway, roll, and yaw.

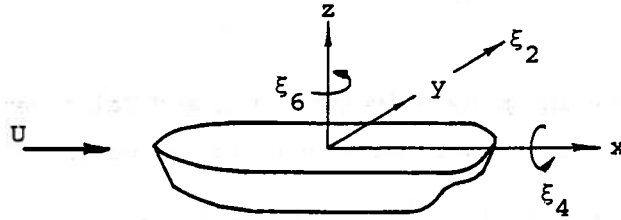


Figure 1 Coordinate System

Consider the coordinate system as fixed in an incident stream with velocity  $U$  flowing in the positive  $x$  direction and the ship swaying, rolling, and yawing about that system. We now desire to find the added mass and damping coefficients,  $A_{jk}$  and  $B_{jk}$ , for sway, roll, and yaw using assumptions similar to the ones used by Ogilvie and Tuck (1969).

If we define the motion of the ship in a two parameter expansion,  $\epsilon$ , a slenderness parameter related to the beam to length ratio, and  $\delta$ , a motion-amplitude parameter related to the smallness of motion, we can require that the motion be smaller than the beam of the ship even as  $\epsilon \rightarrow 0$ . Specifically, assume that

$$\text{displacements resulting from } \eta_j = O(\delta\epsilon)$$

where  $\eta_j$  is the motion in the  $j$ -th mode. Also assume that the frequency of encounter is of the following order:

$$\omega = O(\epsilon^{-1/2}).$$

Then the velocity potential for the complete (linearized) solution can be represented as follows:

$$\phi(x,y,z,t) = Ux + U\chi(x,y,z) + \psi(x,y,z,t) \quad (4)$$

where the first two terms give the solution of the steady-motion problem as shown by Tuck (1965) and the last term represents everything that must be added in order to satisfy the boundary conditions. We assume that  $\psi(x,y,z,t)$  has a time dependence of  $e^{i\omega t}$  and the velocity  $U$  is of order one.

As shown by Ogilvie and Tuck (1969), we may put equation (4) into the governing equations describing the boundary value problem of the oscillating ship. We next linearize the problem with respect to the amplitude motion, but

keep higher order terms of the slenderness parameter expansion. The time-dependent part of the potential then is found to satisfy the following equations:

$$\psi_{yy} + \psi_{zz} \approx 0 \quad \text{in the fluid domain,} \quad (5)$$

$$-\omega^2 \psi + g \psi_z \approx -i\omega U (2\psi_x + 2\chi_y \psi_y + \chi_{yy} \psi) \quad \text{on } z=0, \quad (6)$$

and on the hull

$$\begin{aligned} \frac{\partial \psi}{\partial n} \approx & i\omega n_2 (\eta_2 + x\eta_6) + i\omega n_4 (y n_3 - z n_2) + U n_2 \eta_6 \\ & - U (\eta_2 + x\eta_6) (n_2 \chi_{yy} + n_3 \chi_{yz}) + U n_4 [(n_3 \chi_y - n_2 \chi_z) \\ & + z (n_2 \chi_{yy} + n_3 \chi_{yz}) - y (n_2 \chi_{yz} + n_3 \chi_{zz})] \end{aligned} \quad (7)$$

where  $n$  is the unit normal directed out of the fluid,  $n_2$  and  $n_3$  are the components of the unit normal in the  $y$  and  $z$  direction respectively and variables subscripted with  $y$  and/or  $z$  denote partial differentiation with respect to that coordinate.

The form of the above equations (5) - (7) can only be correct if the formal rules of matched asymptotic expansions are followed. In other words, the far field expansion of the  $\psi(x,y,z,t)$  potential must match, to an appropriate order, an inner expansion of a potential representing a line of pulsating sources and dipoles. To show that this is indeed the case, we could use a method similar to that used by Troesch (1975), where he applied the theory of Fourier Transforms or use the method of complex variables as shown by Ogilvie (1974). In both cases, the authors were solving anti symmetric problems, which are applicable to the sway, roll, and yaw potential discussed in this paper.

A solution for the complete  $\psi(x,y,z,t)$  problem can now be given in much the same manner as shown by Troesch (1975) for the case of an anti symmetric pressure distribution on the free surface. The actual solution is fairly complex and it is not necessary to repeat it here. Rather, we note that since a solution exists, we may find the pressure from Bernoulli's equation and subsequently the hydrodynamic force acting on an oscillating ship. The details are given in the appendix.

#### ADDED MASS AND DAMPING COEFFICIENTS

Following Ogilvie and Tuck (1969), the generalized hydrodynamic force,

$F_j$  , may be related to the added mass and damping coefficients in the following manner

$$F_j(t) = \sum_k [\omega^2 A_{jk} - i\omega B_{jk}] \eta_k(t) \equiv \sum_k [T_{jk}^{(0)} + T_{jk}^{(1)} + T_{jk}^{(2)}] \eta_k(t)$$

where the superscript (0) denotes the usual zero speed strip theory terms. The velocity dependent terms, which are of higher order are found in  $T^{(1)}$  and  $T^{(2)}$  . These coefficients can then be given in terms of the steady motion potential,  $\chi$  , and the usual zero speed forced oscillation potential,  $\phi_j$  , defined in the following manner:

$$\phi_{j_{yy}} + \phi_{j_{zz}} = 0 \quad \text{in the fluid domain}$$

$$\frac{\partial \phi_j}{\partial N} = N_j, \quad j = 2, 4, 6, \quad \text{on the hull}$$

$$-\omega^2 \phi_j + g \phi_{j_z} = 0 \quad \text{on } z = 0$$

and

$$\phi_j \rightarrow \pm A_j e^{-iv|y|} \quad \text{as } y \rightarrow \pm \infty$$

where  $N$  is now the two dimensional normal in the  $y$ - $z$  plane and  $N_j$  is given as follows:

$$N_2 = n_2$$

$$N_4 = n_3 y - n_2 z$$

$$N_6 = x n_2$$

The complete expressions for the complex factors  $T_{jk}$  are given in the Appendix. If we make two assumptions, we can simplify the expressions for  $T_{24}^{(1)}$  ,  $T_{24}^{(2)}$  ,  $T_{46}^{(1)}$  , and  $T_{46}^{(2)}$  considerably. First assume that the ship is symmetrical. (For a symmetrical ship the half-beam at the waterline,  $y_0(x)$  , is an even function with respect to  $x$  and the  $y$  and  $z$  derivatives of the steady motion potential,  $\chi(x,y,z)$  , are odd functions with respect to  $x$  .) Next assume that the ship in question has long sections of parallel mid-body, that is, long relative to its end section. (This has the effect of making the end contributions to  $T_{jk}^{(1)}$  and  $T_{jk}^{(2)}$  higher order than the mid-body contributions.) The complete factors  $T_{jk}$  may then be written in the following manner:

$$T_{22}^{(0)} = -\rho(i\omega)^2 \int_L dx \int_{C(x)} d\ell n_2 \phi_2 \equiv \int_L dx t_{22}^{(0)}$$

$$T_{44}^{(0)} = -\rho(i\omega)^2 \int_L dx \int_{C(x)} d\ell (n_3 y - n_2 z) \phi_4$$

$$T_{66}^{(0)} = \int_L dx x^2 t_{22}^{(0)}$$

$$T_{24}^{(0)} = T_{42}^{(0)} = -\rho(i\omega)^2 \int_L dx \int_{C(x)} d\ell n_2 \phi_4$$

$$T_{26}^{(0)} = T_{62}^{(0)} = \int_L dx x t_{22}^{(0)}$$

$$T_{46}^{(0)} = T_{64}^{(0)} = -\rho(i\omega)^2 \int_L dx x \int_{C(x)} d\ell n_2 \phi_4$$

$$T_{jj}^{(1)} = 0, j = 2, 4, 6$$

$$T_{26}^{(1)} = -T_{62}^{(1)} = \frac{U}{i\omega} T_{22}^{(0)}$$

$$T_{24}^{(1)} = T_{42}^{(1)} = 0$$

$$T_{64}^{(1)} = -T_{46}^{(1)} = \frac{U}{i\omega} T_{42}^{(0)}$$

$$T_{jj}^{(2)} = 0, j = 2, 4, 6$$

$$T_{24}^{(2)} = T_{42}^{(2)} = 0$$

$$T_{26}^{(2)} = -T_{62}^{(2)} = \rho(i\omega)^3 \frac{2U}{g} \int_L dx \left[ \int_{Y_0}^{\infty} dy (\phi_2^2 - A_2^2 e^{-2iv y}) - \frac{i}{2\nu} A_2^2 e^{-2iv Y_0} \right]$$

and

$$T_{46}^{(2)} = -T_{64}^{(2)} = \rho(i\omega)^3 \frac{2U}{g} \int_L dx \left[ \int_{Y_0}^{\infty} dy (\phi_2 \phi_4 - A_2 A_4 e^{-2iv y}) - \frac{i}{2\nu} A_2 A_4 e^{-2iv Y_0} \right]$$

where

$\rho$  is the water density

$C(x)$  is the hull contour at station  $x$

$L$  is the ship length

$v$  is the wave number found from  $\omega^2 = vg$

$g$  is the gravitational constant

$y_0(x)$  is the half-beam at station  $x$

and

$A_j e^{-ivy}$  is the behavior of  $\phi_j$  as  $y \rightarrow \infty$ .

The added mass and damping coefficients are then given by the relations

$$A_{jk} = \frac{1}{\omega^2} \operatorname{Re} \{T_{jk}^{(0)} + T_{jk}^{(1)} + T_{jk}^{(2)}\} \quad (8)$$

and

$$B_{jk} = \frac{-1}{\omega} \operatorname{Im} \{T_{jk}^{(0)} + T_{jk}^{(1)} + T_{jk}^{(2)}\} \quad (9)$$

where  $\operatorname{Re}$  and  $\operatorname{Im}$  denote the real and imaginary parts of the complex expression respectively.

Before we compare these coefficients with those derived by Salvesen, Tuck and Faltinsen (1970), write  $T_{26}^{(2)}$  and  $T_{46}^{(2)}$  following a notation established by Ogilvie and Tuck (1969) and used by Faltinsen (1974). Let

$$\rho(i\omega)^3 \frac{2U}{g} \int_F ds \bar{\phi}_2^2 \equiv T_{26}^{(2)}$$

and

$$\rho(i\omega)^3 \frac{2U}{g} \int_F ds \bar{\phi}_2 \phi_4 \equiv T_{46}^{(2)}$$

where a bar has been drawn through the integral sign to indicate that the integral does not really exist as written, and  $F$  denotes that the limits of integration extend on the free surface from the body to infinity.

The added mass and damping coefficients derived by the two different methods are given in Table 1. The ship is assumed to be pointed at both ends so that the end terms given in the Salvesen, Tuck, and Faltinsen (1970) coefficients do not appear. Also  $a_{jk}$  and  $b_{jk}$  represent the usual two dimensional sectional added mass and damping coefficients.

## NUMERICAL RESULTS

Recall that we are addressing ourselves to two questions. First, will this theory show a speed dependence for the roll damping coefficient and, second, are the extra terms,  $T_{jk}^{(2)}$ , numerically significant? In order to answer the first question, set  $F_2$  in equation (1) and  $F_6$  in equation (3) equal to zero and let  $F_4$  in equation (2) be some constant. This corresponds to the experiments described by Sugai and Yamanouchi (1963) where they applied a pure roll moment to a moving model. A computer program was written that solved equation (1) - (3) using the added mass and damping coefficients given in equations (8) and (9). The hull offsets used were from a Series 60,  $C_B = .70$  hull and the model was assumed to have the following additional characteristics:

$$z_c \approx -0.2d$$

$$I_4 \approx M[(0.397B)^2 + (z_c)^2]$$

$$C_{44} = MgGM$$

$$GM \approx -z_c$$

$$I_6 \approx M(0.25L)^2$$

$$I_{46} \approx 0.0$$

where  $d$  is the draft of the ship,  $B$  is the beam, and  $L$  is the length.

The computer program that calculated the horizontal plane coefficients also returned the ones for the vertical plane, i.e., the Ogilvie-Tuck added mass and damping coefficients for heave and pitch. The Series 60 hull form was selected in order to compare the results returned for heave and pitch with those reported by Faltinsen (1974). (The comparison was satisfactory.) While the hull form selected is not truly symmetrical and does not have large sections of parallel mid-body, it should satisfy the conditions of symmetry and relatively constant cross sections to a sufficient degree to answer the two questions posed in the Introduction.

The method used for evaluating the free surface integrals is described in the Appendix. The results of the forced rolling tests for three different Froude numbers ( $F_n = .15, .20, .30$ ) are shown in Figures 2, 3, and 4. Inspection of Table 1 shows that  $B_{44}$  is independent of speed. Therefore, the only way that the roll motion at resonance will be influenced by speed is through

Table 1 Comparison of Added Mass and Damping Coefficients

Coefficient	Salvesen, Tuck and Faltinsen (1970) (1)	As given by the theory in this paper
$A_{22}$	$\int a_{22} d\xi$	$\int a_{22} d\xi$
$B_{22}$	$\int b_{22} d\xi$	$\int b_{22} d\xi$
$A_{44}$	$\int a_{44} d\xi$	$\int a_{44} d\xi$
$B_{44}$	$\int b_{44} d\xi + B_{44}^* \quad (2)$	$\int b_{44} d\xi$
$A_{66}$	$\int \xi^2 a_{22} d\xi + A_{22} U^2 / \omega^2$	$\int \xi^2 a_{22} d\xi$
$B_{66}$	$\int \xi^2 b_{22} d\xi + B_{22} U^2 / \omega^2$	$\int \xi^2 b_{22} d\xi$
$A_{24}$	$\int a_{24} d\xi$	$\int a_{24} d\xi$
$B_{24}$	$\int b_{24} d\xi$	$\int b_{24} d\xi$
$A_{42}$	$\int a_{24} d\xi$	$\int a_{24} d\xi$
$B_{42}$	$\int b_{24} d\xi$	$\int b_{24} d\xi$
$A_{26}$	$\int \xi a_{22} d\xi - B_{22} U / \omega^2$	$\int \xi a_{22} d\xi - B_{22} U / \omega^2 + \text{Im} \left[ (\rho \omega^2 U / g) \int ds \phi_2^2 \right]_F$
$B_{26}$	$\int \xi b_{22} d\xi + A_{22} U$	$\int \xi b_{22} d\xi + A_{22} U + \text{Re} \left[ (\rho \omega^2 2U / g) \int ds \phi_2^2 \right]_F$



Table 1 (cont.)

Coefficient	Salvesen, Tuck and Faltinsen (1970) (1)	As given by the theory in this paper
$A_{62}$	$\int \xi a_{22} d\xi + B_{22} U/\omega^2$	$\int \xi a_{22} d\xi + B_{22} U/\omega^2 - \text{Im} \left[ (\rho\omega^2 U/g) \int_{\Gamma} ds \phi_2^2 \right]$
$B_{62}$	$\int \xi b_{22} d\xi - A_{22} U$	$\int \xi b_{22} d\xi - A_{22} U - \text{Re} \left[ (\rho\omega^2 2U/g) \int_{\Gamma} ds \phi_2^2 \right]$
$A_{46}$	$\int \xi a_{24} d\xi - B_{24} U/\omega^2$	$\int \xi a_{24} d\xi - B_{24} U/\omega^2 + \text{Im} \left[ (\rho\omega^2 2U/g) \int_{\Gamma} ds \phi_4 \phi_2 \right]$
$B_{46}$	$\int \xi b_{24} d\xi + A_{24} U$	$\int \xi b_{24} d\xi + A_{24} U + \text{Re} \left[ (\rho\omega^2 2U/g) \int_{\Gamma} ds \phi_4 \phi_2 \right]$
$A_{64}$	$\int \xi a_{24} d\xi + B_{24} U/\omega^2$	$\int \xi a_{24} d\xi + B_{24} U/\omega^2 - \text{Im} \left[ (\rho\omega^2 2U/g) \int_{\Gamma} ds \phi_4 \phi_2 \right]$
$B_{64}$	$\int \xi b_{24} d\xi - A_{24} U$	$\int \xi b_{24} d\xi - A_{24} U - \text{Re} \left[ (\rho\omega^2 2U/g) \int_{\Gamma} ds \phi_4 \phi_2 \right]$

(1) The end effects in the Salvesen, Tuck and Faltinsen (1970) theory were dropped.

(2)  $B_{44}^*$  is a quasi-linear viscous-damping coefficient. Viscous effects are ignored in the theory presented in this paper.

the coupling between roll and sway and roll and yaw. Figure 3 indicates that this effect is negligible. Only the motion of yaw, in Figure 4, shows any speed effects. We can conclude that slender body theory, as derived in this paper, will not show an increase in the roll damping coefficient as forward speed increases. This result can be contrasted with the results given by Watanabe (1977) where an application of thin-ship theory did produce larger roll damping coefficients as the forward speed increased. It should be noted, however, that the theory of that paper included a trailing vortex sheet and consequently differed fundamentally from the theory presented here. In a recent paper by Ikeda, Himeno and Tanaka (1978), it is suggested that the "wave damping component" of a moving, rolling ship is, to a large extent, independent of speed for values of  $\tau$  greater than 0.5. Here  $\tau$  equals  $U\omega/g$ . The "wave damping component" corresponds to the damping coefficient  $B_{44}$  presented in this paper. Our assumptions make  $\tau=0(\epsilon^{-1/2})$ , which represents high speed and/or high frequency of rolling. Thus it appears that  $B_{44}$  is consistent with the results presented by Ikeda, et.al. (1978).

To demonstrate the difference between the added mass and damping coefficients as derived by the theory presented in this paper and those coefficients derived by Salvesen, Tuck and Faltinsen (1970), Figures 5 through 8 are presented. The coupled sway-yaw added mass and damping coefficients are non-dimensionalized by  $\rho V L$  and  $\rho V L \sqrt{g/L}$  respectively. Here  $V$  is the volume displacement of the ship. The coupled roll-yaw added mass and damping coefficients are non-dimensionalized by  $\rho V L^2$  and  $\rho V L^2 \sqrt{g/L}$  respectively. They are all plotted as functions of  $\omega \sqrt{L/g}$ . The results are shown for a  $F_n = 0.2$  only. Froude numbers of 0.15 and 0.30 showed similar tendencies. From the figures, it is clear that there are some differences. Figure 5 which shows the added mass coupling coefficient  $A_{62}$  of sway into yaw also has included results of experiments conducted by Vugts (1970). The experiments were forced motion tests on a 10 foot segmented model. The sectional added mass components were added to give the results shown in the figure. The comparison between theory and experiment, at least for the coefficient of  $A_{62}$ , seems reasonable. (Recall that the expressions  $A_{62}$  and  $B_{62}$  are unaffected by the antisymmetry and constant mid body assumptions. Consequently, they should be more applicable to ship shapes than any of the coefficients resulting from a coupling with roll.)

In Figures 9 and 10, the ratios of  $T_{jk}^{(2)}$  to  $T_{jk}^{(1)}$  are plotted as

functions of  $\omega\sqrt{L/g}$ . These ratios are speed independent since both  $T_{jk}^{(2)}$  and  $T_{jk}^{(1)}$  vary linearly with velocity. From Table 1, it is clear that the real part of  $T_{jk}^{(1)}$  corresponds to the velocity dependent part of the Salvesen, Tuck and Faltinsen added mass and the imaginary part of  $T_{jk}^{(1)}$  corresponds to the velocity dependent part of their damping coefficient. Since  $T_{jk}^{(2)}$  represents the free surface integrals, we can see from these plots the relative importance of these terms to the usual forward speed terms as given by Salvesen, Tuck, and Faltinsen (1970). For some frequency ranges,  $T_{ij}^{(2)}$ , the free surface integral, is equal to or larger than the usual forward speed term.

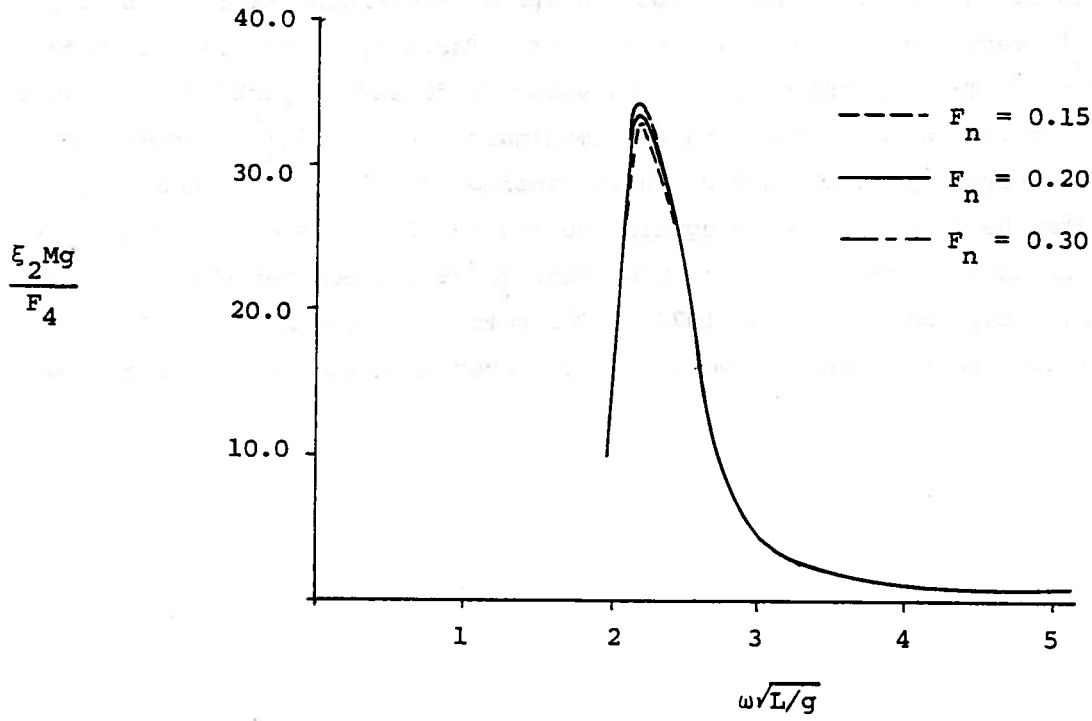


Figure 2 Sway response to unit roll moment

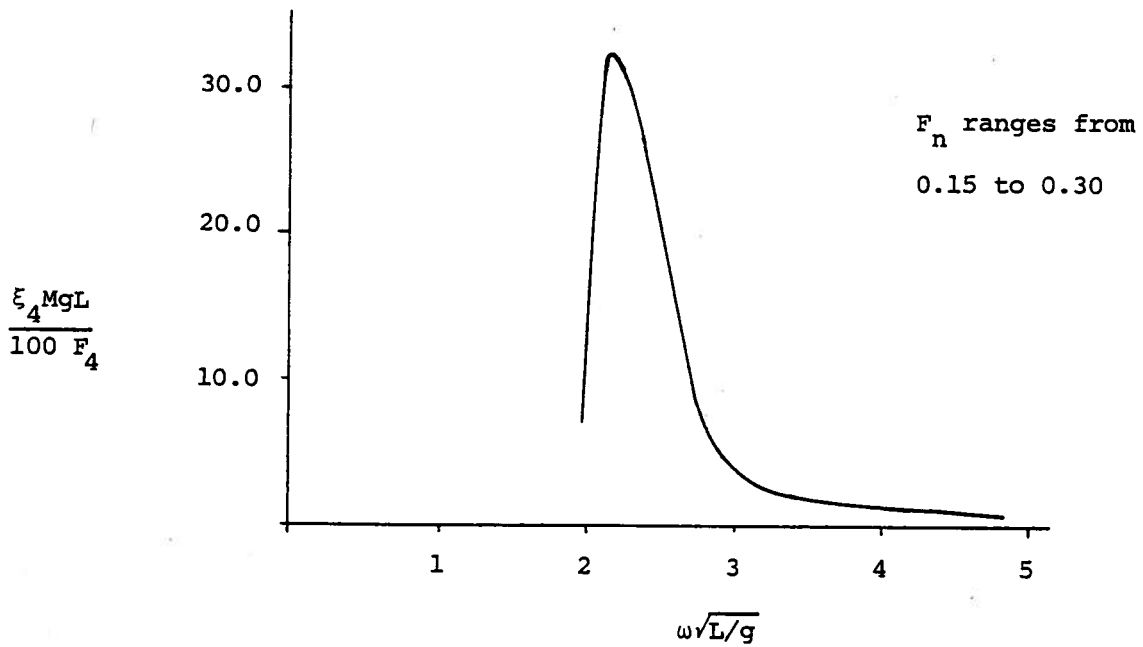


Figure 3 Roll response to unit roll moment

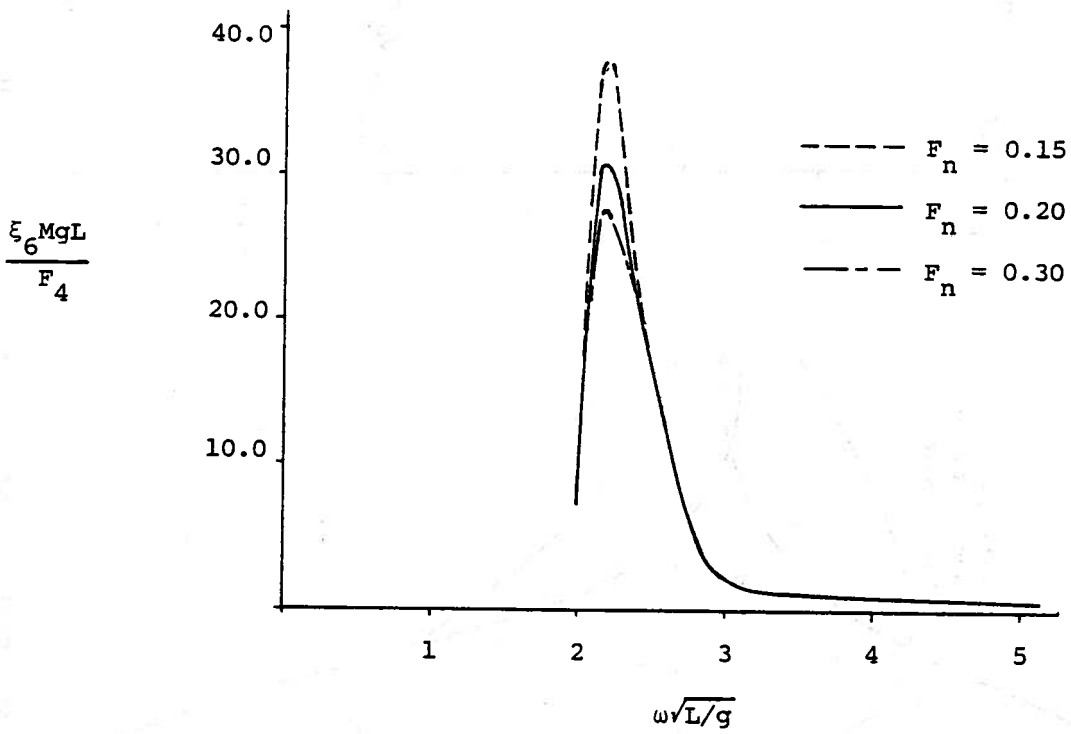


Figure 4 Yaw response to unit roll moment

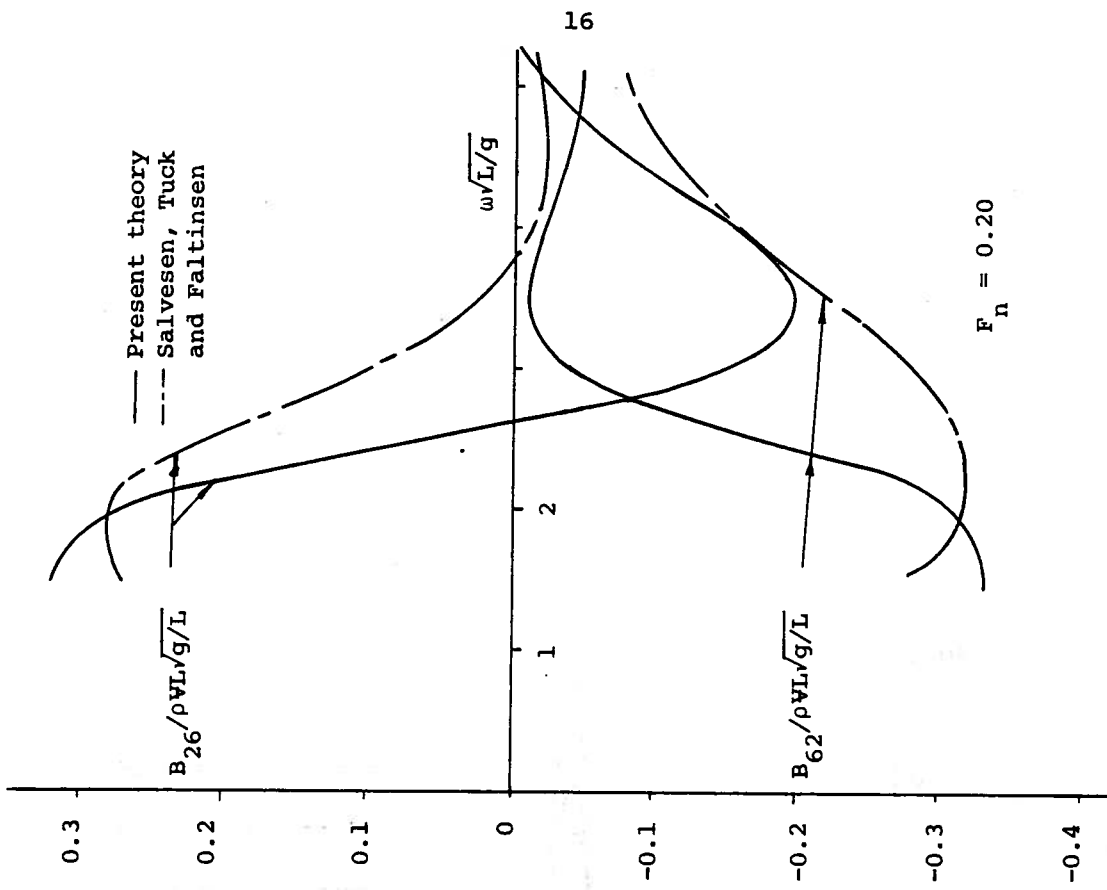


Figure 5 Added mass coefficients  $A_{62}$  and  $A_{26}$

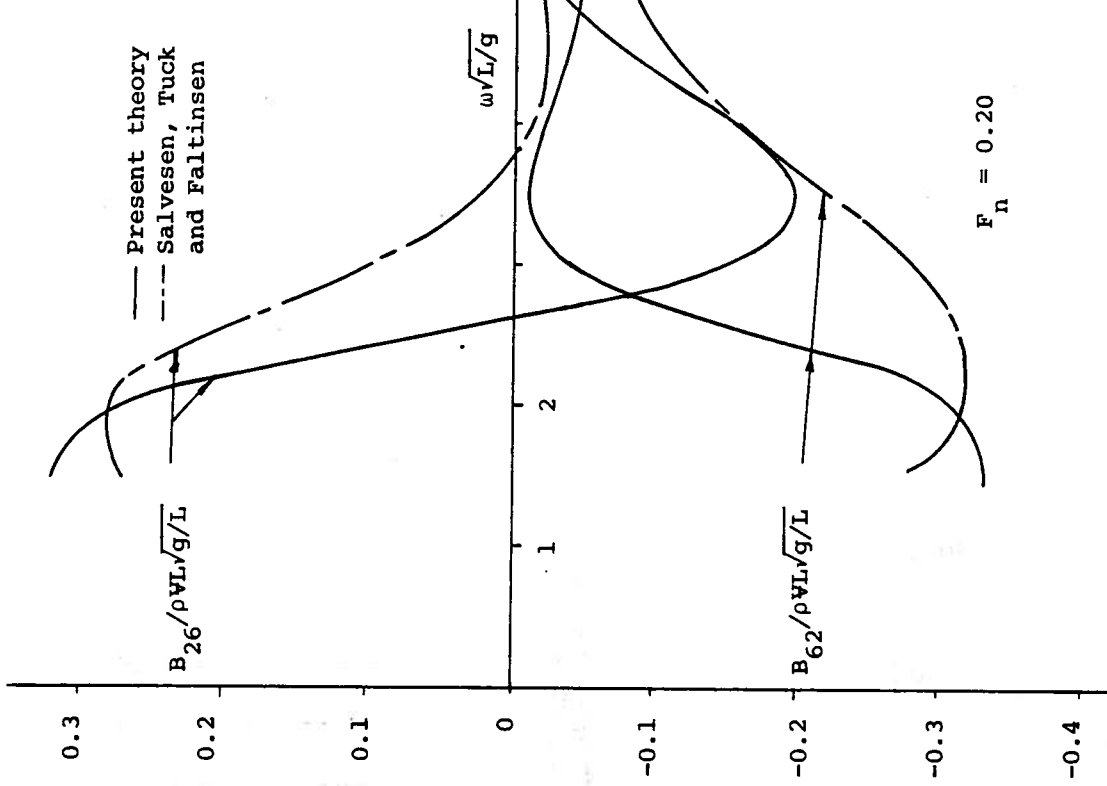


Figure 6 Damping coefficients  $B_{62}$  and  $B_{26}$

$F_n = 0.20$

$F_n = 0.20$

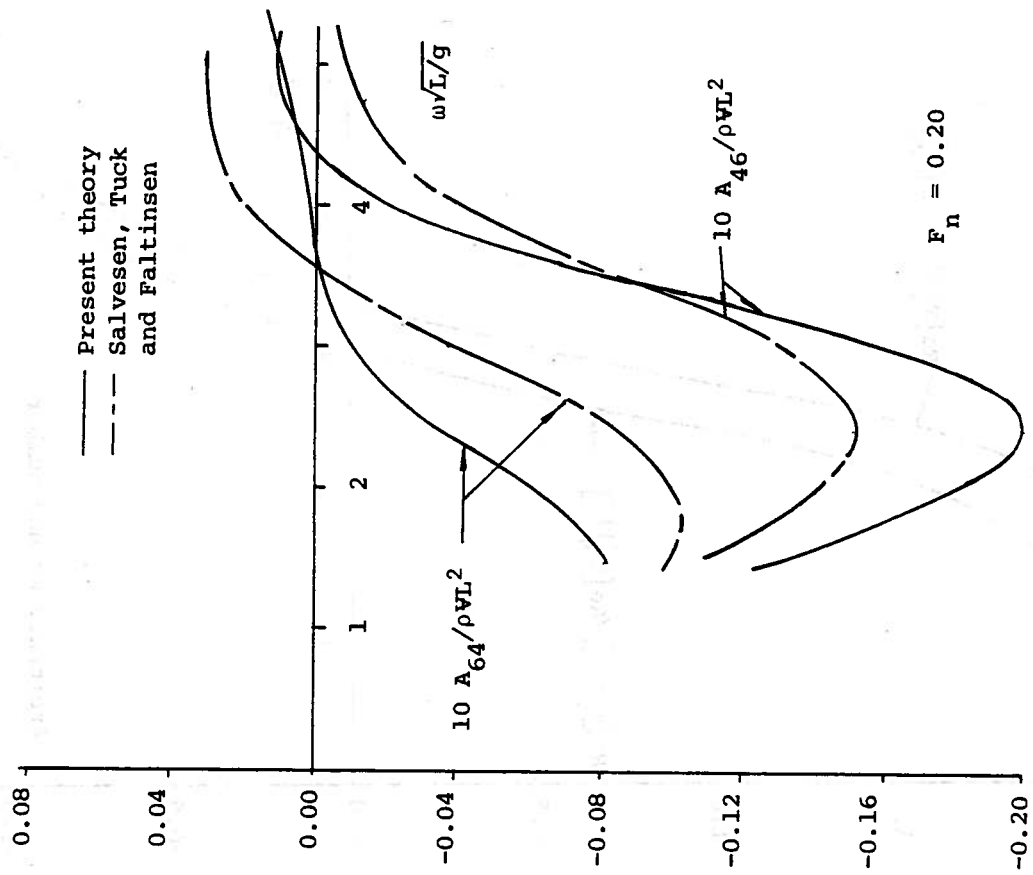


Figure 7 Added mass coefficients  $A_{64}$  and  $A_{46}$

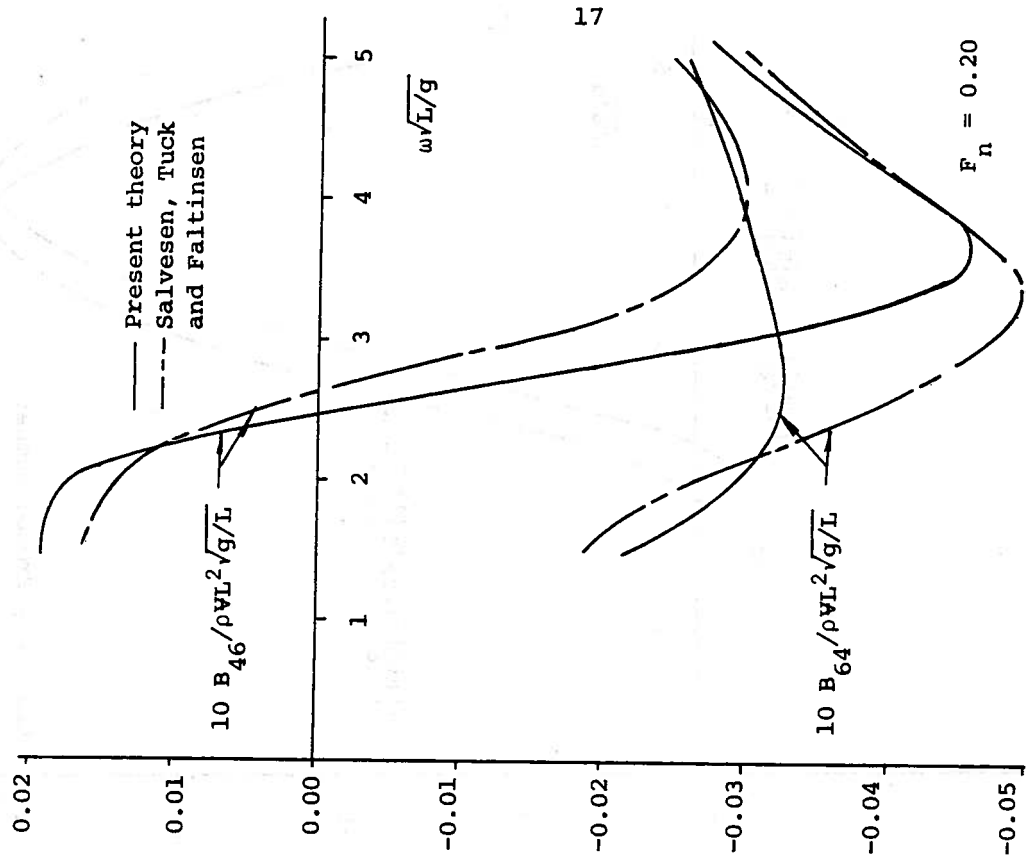


Figure 8 Damping coefficients  $B_{46}$  and  $B_{64}$

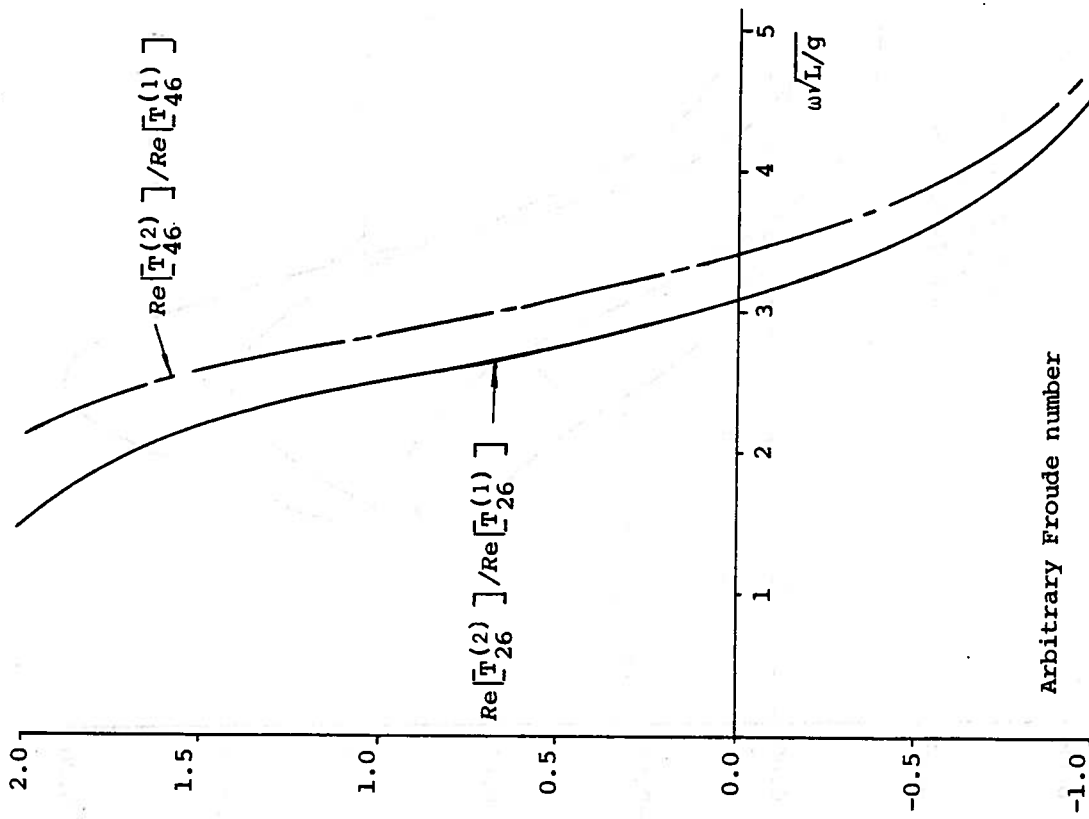


Figure 9 Relative importance of free surface integrals

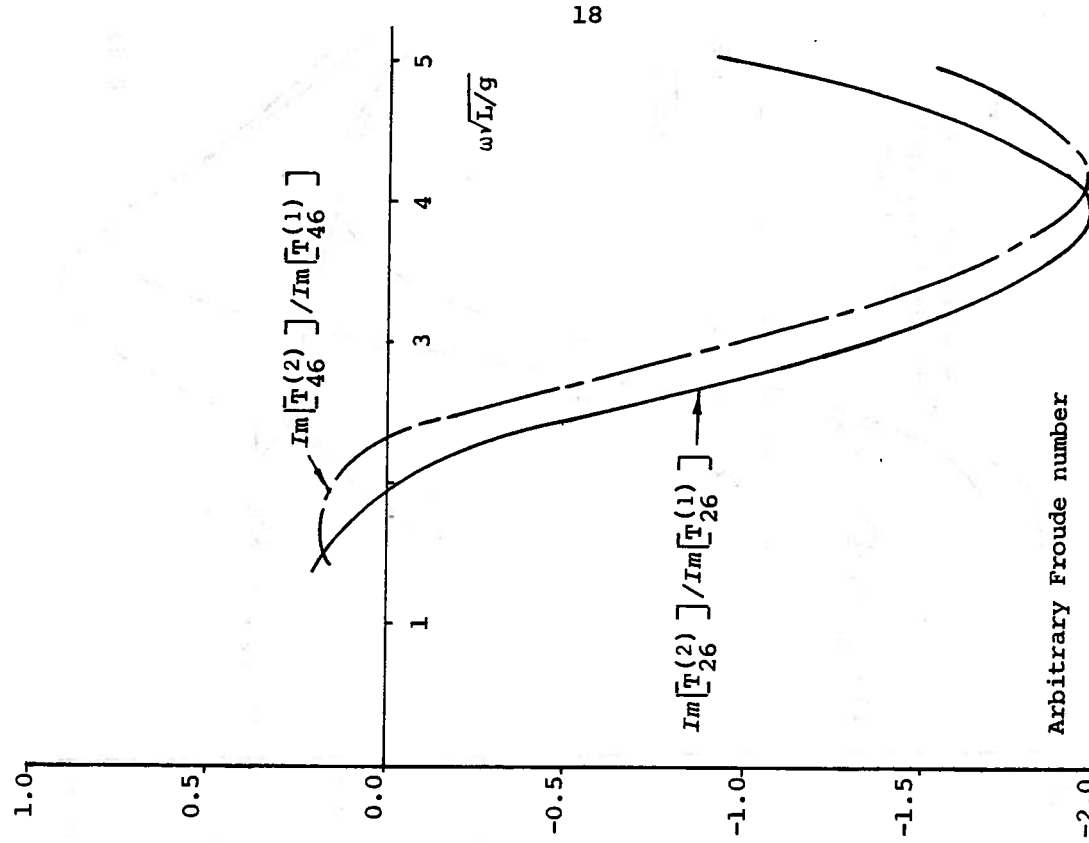


Figure 10 Relative importance of free surface integrals



## APPENDIX

### FORCE AND MOMENT ON THE HULL

Since most of the details for finding the force and moment on the hull due to horizontal motions are similar to those for vertical motions as presented by Ogilvie and Tuck (1969), only a brief summary of the derivation will be given here.

The time dependent solution is given by the  $\psi(x,y,z,t)$  potential. It must satisfy equations (5) - (7) which are repeated here for convenience

$$\psi_{yy} + \psi_{zz} = 0 \quad \text{in the fluid domain} \quad (5)$$

$$-\omega^2\psi + g\psi_z = -i\omega U(2\psi_x + 2\chi_y\psi_y + \chi_{yy}\psi) \quad \text{on } z=0 \quad (6)$$

and on the hull

$$\begin{aligned} \frac{\partial\psi}{\partial n} = & i\omega n_2(\eta_2 + xn_6) + i\omega n_4(yn_3 - zn_2) + Un_2n_6 \\ & -U(\eta_2 + xn_6)(n_2\chi_{zz} + n_3\chi_{yz}) + Un_4[(n_3\chi_y - n_2\chi_z) \\ & + z(n_2\chi_{yy} + n_3\chi_{yz}) - y(n_2\chi_{yz} + n_3\chi_{zz})] \end{aligned} \quad (7)$$

There is also a radiation condition that must be satisfied. More will be said about this later.

In order to simplify the solution of the forced oscillation potentials, Ogilvie and Tuck (1969) defined the following quantities:

$n_j$  and  $m_j$  for  $j=2,4,6$  where

$$n_2 = n_2$$

$$n_4 = yn_3 - zn_2$$

$$n_6 = xn_2$$

$$m_2 = -n_2\chi_{yy} - n_3\chi_{yz}$$

$$m_4 = \chi_y n_3 - \chi_z n_2 + z(n_2\chi_{yy} + n_3\chi_{yz}) - y(n_2\chi_{yz} + n_3\chi_{zz})$$

$$m_6 = n_2 - xn_2$$

Let the mean hull surface be defined by the equation

$$S_0(x, y, z) = 0.$$

Then define a potential  $\phi_j$  where

$$\phi_{jyy} + \phi_{jzz} = 0 \quad \text{in the fluid}$$

$$\frac{\partial \phi_j}{\partial N} = n_j \quad \text{on } S_0 = 0$$

and

$$-\omega^2 \phi_j + g \phi_{jz} = 0 \quad \text{on } z=0.$$

Note that  $\phi_6 \approx x \phi_2$

Next define a potential  $\Psi_j$  where

$$\Psi_{jyy} + \Psi_{jzz} = 0 \quad \text{in the fluid}$$

$$\frac{\partial \Psi_j}{\partial N} = m_j \quad \text{on } S_0 = 0$$

and

$$-\omega^2 \Psi_j + g \Psi_{jz} = 0 \quad \text{on } z=0$$

Finally define a potential  $\Omega_j$  where

$$\Omega_{jyy} + \Omega_{jzz} = 0 \quad \text{in the fluid}$$

$$\frac{\partial \Omega_j}{\partial N} = 0 \quad \text{on } S_0 = 0$$

and

$$-\omega^2 \Omega_j + g \Omega_{jz} = -(2\phi_{jx} + 2\chi_y \phi_{jy} + \chi_{yy} \phi_j) \quad \text{on } z=0.$$

Then  $\psi = \sum_j (i\omega \phi_j + U \Psi_j - \omega^2 \Omega_j) \eta_j$  satisfies all the equations in the boundary value problems (equations (5) - (7)) to the order considered. The radiation conditions for the  $\phi_j$  and  $\Psi_j$  problems are the usual ones which require out going waves. The  $\Omega_j$  potential represents an anti-symmetric pressure distribution on the free surface, and as shown by Troesch (1975), its radiation

condition is represented by linearly growing, anti-symmetric out-going waves.

As shown by Ogilvie and Tuck (1969), the pressure can be found from Bernoulli's equation and then integrated over the mean position of the ship's hull to give a total force consistent to an order of  $O(\epsilon^{3/2}\delta)$ . It has the following form:

$$F_j(t) \approx -\rho \int_{S_0} ds \{ \sum_k [n_j(i\omega)^2 - Um_j(i\omega)] \phi_k \eta_k + Un_j \sum [(i\omega)\psi_k + (i\omega)^3 \Omega_k] \eta_k \}$$

As done in the main text, let us define several quantities as follows:

$$F_j(t) \equiv \sum_k [T_{jk}^{(0)} + T_{jk}^{(1)} + T_{jk}^{(2)}] \eta_k(t) .$$

Then

$$T_{jk}^{(0)} = -\rho (i\omega)^2 \int_{S_0} ds n_j \phi_k$$

$$T_{jk}^{(1)} = -\rho i\omega U \int_{S_0} ds (n_j \psi_k - m_j \phi_k)$$

and

$$T_{jk}^{(2)} = -\rho (i\omega)^3 U \int_{S_0} ds n_j \Omega_k .$$

See the main text for the complete expressions for  $T_{jk}^{(0)}$  when  $j=2,4,6$  and  $k=2,4,6$ .

Consider now  $T_{jk}^{(1)}$ . The far field behavior of  $\phi_j$  and  $\psi_j$  are given as

$$i\omega \phi_j \eta_j \rightarrow \text{sgn}(y) A_j(x) e^{\nu z} e^{i(\omega t - \nu|y|)}$$

and

$$U\psi_j \eta_j \rightarrow \text{sgn}(y) B_j(x) e^{\nu z} e^{i(\omega t - \nu|y|)}$$

as  $y \rightarrow \infty$ . Here  $\nu$  is the wave number given by  $\omega^2 = \nu g$ . Using this fact and Green's theorem for two dimensions, we can follow the method used by Ogilvie and Tuck (1969) to easily show that

$$T_{jj}^{(1)} = 0$$

and

$$T_{jk}^{(1)} = -\rho i \omega U \int_{S_0} ds (\phi_{j m_k} - \phi_{k m_j})$$

The following expressions are given for specific modes of motion:

$$T_{26}^{(1)} = -T_{62}^{(1)} = -\rho i \omega U \int_{S_0} ds n_2 \phi_2$$

$$T_{24}^{(1)} = -T_{42}^{(1)} = -\rho i \omega U \int_{S_0} ds (\phi_2 m_4 - \phi_4 m_2)$$

and

$$T_{46}^{(1)} = -T_{64}^{(1)} = -\rho i \omega U \left[ \int_{S_0} ds x (m_2 \phi_4 - m_4 \phi_2) + \int_{S_0} ds n_2 \phi_4 \right]$$

To simplify  $T_{jk}^{(2)}$ , we need the far field behavior of the  $\Omega$  potential. Using the method shown by Troesch (1975) for a anti-symmetric pressure distribution on the free surface we can write

$$-\omega^2 U \Omega_j \eta_j \rightarrow \text{sgn}(y) e^{\nu z + i(\omega t - \nu |y|)} \left[ C_j(x) - \frac{2i\omega U}{g} A_{j_x}(x) (z - i|y|) \right]$$

as  $y \rightarrow \infty$ .

Then we can show, using a method similar to that used by Ogilvie and Tuck (1969), that

$$T_{jj}^{(2)} = 0$$

$$T_{26}^{(2)} = -T_{62}^{(2)} = \rho (i\omega)^3 \frac{2U}{g} \int_L dx \left[ \int_{Y_0}^{\infty} dy (\phi_2^2 - A_2^2 e^{-2i\nu y}) - \frac{i}{2\nu} A_2^2 e^{-2i\nu y_0} \right]$$

and for roll, when either  $j=4$  or  $k=4$  and the other subscript equals 2 or 6

$$T_{jk}^{(2)} = -T_{kj}^{(2)} = \rho(i\omega)^3 \frac{2U}{g} \int_L dx \left\{ \int_{y_0}^{\infty} dy \left[ (\phi_j \phi_{k_x} - A_j A_{k_x} e^{-2iv_y}) \right. \right. \\ \left. \left. - (\phi_{j_x} \phi_k - A_{j_x} A_k e^{-2iv_y}) + \chi_Y (\phi_j \phi_{k_y} + \phi_{j_y} \phi_k) \right] \right. \\ \left. + \frac{i}{2v} e^{-2iv_y} (A_{j_x} A_k - A_j A_{k_x}) \right\}$$

where the subscript of  $x$  means the derivative of the subscripted variable with respect to  $x$ .

Note the following:

- i) For symmetric hull forms  $m_2$ ,  $m_4$  and  $\chi_Y$  are odd functions with respect to  $x$ .
- ii) In regions of constant cross sections,  $m_2$ ,  $m_4$ ,  $\chi_Y$ ,  $\phi_{j_x}$  and  $A_{j_x}$  are equal to zero.
- iii) In the end sections the beam of the hull becomes higher order than the beam at mid ships. As a result the oscillation potentials  $\phi_2$  and  $\phi_4$ , also are higher order there than in the mid sections.

#### NUMERICAL METHOD FOR DETERMINING THE ADDED MASS AND DAMPING COEFFICIENTS

The added mass and damping coefficients were found in two steps. First, the potential valid on the hull surface was determined. Next, a multipole expansion, valid outside some radius  $R$  which inclosed the body, was matched to the first potential. Using this scheme significantly lowered the computing time of evaluating the free surface integrals.

The potential in the near field was given by an integral representation of sources distributed over the hull surface. The source strength,  $\sigma_j(\zeta, \eta)$ , was found by solving the following integral equation:

$$\frac{\partial \phi_j(y, z)}{\partial n} = -\pi \sigma_j(y, z) + \int_{C_H} d\ell \sigma_j(\zeta, \eta) \frac{\partial G}{\partial n}(y, z, \zeta, \eta)$$

on the hull, where  $\frac{\partial \phi_j}{\partial n}$  is the normal velocity on the hull and  $G(y, z, \zeta, \eta)$  is a Green's function given by

$$\begin{aligned}
G(y, z; \zeta, \eta) &= \log \sqrt{(y-\zeta)^2 + (z-\eta)^2} - \log \sqrt{(y-\zeta)^2 + (z+\eta)^2} \\
&\quad - 2e^{\nu(z+\eta)} \operatorname{Re} \left\{ e^{i\nu|y-\zeta|} E_1 \left[ \nu(z+\eta) + i\nu|y-\zeta| \right] \right\} \\
&\quad + 2\pi i e^{\nu(z+\eta) - i\nu|y-\zeta|}
\end{aligned}$$

and  $E_1(x+iy)$  is the complex exponential integral. The method for solving the integral equation is given in Troesch (1975).

Once the source distribution,  $\sigma_j(\zeta, \eta)$  was known, a circle of radius  $R$ , where  $R$  enclosed the entire station being considered, was found. Then the potential given by the source distribution on the hull was matched to a multi-pole expansion consisting of a dipole and wave free potentials that were odd with respect to the  $x$ - $z$  plane. The matching took place on the circle. The multi-pole expansion had the following form:

$$\begin{aligned}
\phi_j(y, z) &= A_j \left[ -\frac{1}{\pi} e^{\nu z} \operatorname{sgn}(y) \operatorname{Re} \left\{ i e^{i\nu|y|} E_1(\nu z + i\nu|y|) \right\} \right. \\
&\quad \left. + \frac{1}{\pi\nu} \frac{y}{r^2} + \operatorname{sgn}(y) e^{\nu z - i\nu|y|} \right] \\
&\quad + \sum_{m=1}^{N-1} A_{jm} (\nu R)^{2m+1} \left[ \frac{\sin(2m+1)\theta}{(\nu r)^{2m+1}} + \frac{\sin 2m\theta}{2m(\nu r)^{2m}} \right]
\end{aligned}$$

where  $A_j$  and  $A_{jm}$  are coefficients determined from the matching processes,  $r$  equals  $\sqrt{y^2+z^2}$ , and  $\theta$  is the angle between  $r$  and the negative  $z$  axis.

The free surface integrals, defined as

$$\int_{Y_0}^{\infty} dy (\phi_2^2 - A_2^2 e^{-2i\nu y})$$

and

$$\int_{Y_0}^{\infty} dy (\phi_2 \phi_4 - A_2 A_4 e^{-2i\nu y})$$

have integrands that oscillate with a period of  $\pi$ . The subroutine that evaluated the integrals used Simpson's rule on 25 points for each interval of  $\pi$ . The integration was terminated when a given interval made no significant contribution to the total integral.

## REFERENCES

- Faltinsen, O.M. (1974.) "A Numerical Investigation of the Ogilvie-Tuck Formulas for Added-Mass and Damping Coefficients." Journal of Ship Research. 18:73-84.
- Ikeda, Y., Himeno, Y. and Tanaka, N. (1978.) "Components of Roll Damping of Ship at Forward Speed." Journal of the Society of Naval Architects of Japan. 143:121-133.
- Korvin-Kroukouvsky, B.V. and Jacobs, W.R., (1957.) "Pitching and Heaving Motions of a Ship in Regular Waves." Transactions of the Society of Naval Architects and Marine Engineers. 65:590-653.
- Ogilvie, T.F. and Tuck, E.O. (1969.) A Rational Strip Theory of Ship Motions: Part 1. Report No. 013, Department of Naval Architecture and Marine Engineering, The University of Michigan, Ann Arbor, Michigan. 92 pp.
- Ogilvie, T.F. (1974.) Unpublished work.
- Salvesen, N., Tuck, E.O. and Faltinsen, O., (1970.) "Ship Motions and Sea Loads." Transactions of the Society of Naval Architecture and Marine Engineers. 78:250-287.
- Sugai, K., and Yamanouchi, Y. (1963.) "A Study on the Rolling Characteristics of a Ship by Forced Oscillation Experiment." Journal of the Society of Naval Architects of Japan. 114:54-66.
- Timman, R., and Newman, J.N. (1962.) "The Coupled Damping Coefficients of Symmetric Ships." Journal of Ship Research. 5:1-7.
- Troesch, A.W. (1975.) The Diffraction-Potential for a Slender Ship Moving Through Oblique Waves. Report No. 176, Department of Naval Architecture and Marine Engineering. The University of Michigan, Ann Arbor, Michigan. 118 pp.
- Tuck, E.O. (1965.) The Application of Slender Body Theory to Steady Ship Motion. Report No. 2008, David Taylor Model Basin, Washington, D.C.
- Vugts, J.H. (1970.) "The Hydrodynamic Forces and Ship Motions in Waves." Ph.D. Dissertation. Technological University. Delft, Netherlands.
- Watanabe, I. (1977.) "On the Effect of the Forward Velocity on the Roll Damping Moment." No. 51, Papers of Ship Research Institute, Tokyo Japan.

DISTRIBUTION LIST FOR REPORTS PREPARED UNDER THE  
GENERAL HYDROMECHANICS RESEARCH PROGRAM

40	Commander David W. Taylor Naval Ship Research and Development Center Bethesda, MD 20084 Attn: Code 1505 (40)	1	Office of Naval Research Resident Representative 715 Broadway (5th Floor) New York, NY 10003
1	Officer-in-Charge Annapolis Laboratory, David W. Taylor Naval Ship Research and Development Center Annapolis, MD 21402 Attn: Code 522.3 (Library)	1	Office of Naval Research San Francisco Area Office 760 Market St., Rm 447 San Francisco, CA 94102
		2	Director Naval Research Laboratory Washington, DC 20390 Attn: Code 2027
7	Commander Naval Sea Systems Command Washington, DC 20362 Attn: SEA 09G32 (3 cys) SEA 03512 (Pierce) SEA 037 SEA 0322 SEA 033	1	Commander Naval Facilities Engineering Command (Code 032C) Washington, DC 20390
		1	Library of Congress Science & Technology Division Washington, DC 20540
12	Director Defense Documentation Center 5010 Duke Street Alexandria, VA 22314	8	Commander Naval Ship Engineering Center Department of the Navy Washington, DC 20362 Attn: SEC 6034B SEC 6110 SEC 6114H SEC 6120 SEC 6136 SEC 6144G SEC 6140B SEC 6148
1	Office of Naval Research 800 N. Quincy Street Arlington, VA 22217 Attn: Mr. R.D. Cooper (Code 438)		
1	Office of Naval Research Branch Office 492 Summer Street Boston, MA 02210		
1	Office of Naval Research Branch Office (493) 536 S. Clark Street Chicago, IL 60605	1	Naval Ship Engineering Center Norfolk Division Small Craft Engr Dept. Norfolk, VA 23511 Attn: D. Blount (6660.03)
1	Chief Scientist Office of Naval Research Branch Office 1030 E. Green Street Pasadena, CA 91106	1	Technical Library Naval Proving Ground Dehlgren, VA 22448



1	Commander (ADL) Naval Air Development Center Warminster, PA 18974	1	Charleston Naval Shipyard Technical Library Naval Base Charleston, SC 29408
1	Naval Underwater Weapons Research & Engineering Station (Library) Newport, RI 02840	1	Norfolk Naval Shipyard Technical Library Portsmouth, VA 23709
1	Commanding Officer (L31) Naval Civil Engineering Laboratory Port Hueneme, CA 93043	1	Philadelphia Naval Shipyard Philadelphia, PA 19112 Attn: Code 240
3	Commander Naval Ocean Systems Center San Diego, CA 92152 Attn: Dr. A. Fabula (4007) Dr. J. Hoyt (2501) Library (13111)	1	Portsmouth Naval Shipyard Technical Library Portsmouth, NH 03801
1	Director Naval Research Laboratory Underwater Sound Reference Division P.O. Box 8337 Orlando, FL 32806	1	Puget Sound Naval Shipyard Engineering Library Bermerton, WA 98314
1	Library Naval Underwater Systems Center Newport, RI 02840	1	Long Beach Naval Shipyard Technical Library (246L) Long Beach, CA 90801
1	Research Center Library Waterways Experiment Station Corps of Engineers P.O. Box 631 Vicksburg, MS 39180	1	Mare Island Naval Shipyard Shipyard Technical Library Code 202.3 Vallejo, CA 94592
2	National Bureau of Standards Washington, DC 20234 Attn: P. Klebanoff (FM 105) Fluid Mechanics Hydraulic Section	1	Assistant Chief Design Engineer for Naval Architecture (Code 250) Mare Island Naval Shipyard Vallejo, CA 94592
1	AFFOL/FYS (J. Olsen) Wright Patterson AFB Dayton, OH 45433	2	U.S. Naval Academy Annapolis, MD 21402 Attn: Technical Library Dr. Bruce Johnson
1	Dept. of Transportation Library TAD-491.1 400 - 7th Street, S.W. Washington, DC 20590	3	Naval Postgraduate School Monterey, CA 93940 Attn: Library, Code 2124 Dr. T. Sarpkaya Prof. J. Miller
		1	Study Center National Maritime Research Center U.S. Merchant Marine Academy Kings Point, L.I., NY 11024

1	U.S. Merchant Marine Academy Kings Point, L.I., NY 11024 Attn: Academy Library	2	McDonnell Douglas Aircraft Co. 3855 Lakewood Blvd Long Beach, CA 90801 Attn: J. Hess T. Cebeci
1	Library The Pennsylvania State University Applied Research Laboratory P.O. Box 30 State College, PA 16801	1	Lockheed Missiles & Space Co. P.O. Box 504 Sunnyvale, CA 94088 Attn: Mr. R.L. Waid, Dept. 57-74 Bldg. 150, Facility 1
1	Bolt, Beranek & Newman 50 Moulton Street Cambridge, MA 02138 Attn: Library	1	Newport News Shipbuilding & Dry Dock Company 4101 Washington Avenue Newport News, VA 23607 Attn: Technical Library Dept.
1	Bethlehem Steel Corporation Center Technical Division Sparrows Point Yard Sparrows Point, MD 21219	1	Nielsen Engineering & Research Inc. 510 Clude Avenue Mountain View, CA 94043 Attn: Mr. S. Spangler
1	Bethlehem Steel Corporation 25 Broadway New York, NY 10004 Attn: Library (Shipbuilding)	1	Oceanics, Inc. Technical Industrial Park Plainview, L.I., NY 11803
1	Cambridge Acoustical Associates, Inc. 1033 Mass Avenue Cambridge, MA 02138 Attn: Dr. M. Junger	1	Society of Naval Architects and Marine Engineers One World Trade Center, Suite 1369 New York, NY 10048 Attn: Technical Library
1	CALSPAN Corporation P.O. Box 235 Buffalo, NY 14221 Attn: Dr. A. Ritter Aerodynamics Res. Dept.	1	Sun Shipbuilding & Dry Dock Co. Chester, PA 19000 Attn: Chief Naval Architect
1	Mr. V. Boatwright, Jr. R&D Manager Electric Boat Division General Dynamics Corporation Groton, CT 06340	1	Sperry Systems Management Division Sperry Rand Corporation Great Neck, NY 11020 Attn: Technical Library
1	Gibbs & Cox, Inc. 21 West Street New York, NY 10006 Attn: Technical Info. Control	1	Stanford Research Institute Menlo Park, CA 94025 Attn: Library G-021
1	Hydronautics, Inc. Pindell School Road Howard County Laurel, MD 20810 Attn: Library	2	Southwest Research Institute P.O. Drawer 28510 San Antonio, TX 78284 Attn: Applied Mechanics Review Dr. H. Abramson


1	Tracor, Inc. 6500 Tracor Lane Austin, TX 78721	1	Colorado State University Foothills Campus Fort Collins, CO 80521 Attn: Reading Room, Engr Res Center
1	Mr. Robert Taggart 9411 Lee Hgwy, Suite P Fairfax, VA 22031	1	University of California at San Diego La Jolla, CA 92038 Attn: Dr. A.T. Ellis Dept. of Applied Math
1	Ocean Engr Department Woods Hole Oceanographic Inst. Woods Hole, MA 02543	2	Florida Atlantic University Ocean Engineering Department Boca Raton, FL 33432 Attn: Technical Library Dr. S. Dunne
1	Worcester Polytechnic Inst. Alden Research Laboratories Worcester, MA 01609 Attn: Technical Library	2	Harvard University Pierce Hall Cambridge, MA 02138 Attn: Prof. G. Carrier Gordon McKay Library
1	Applied Physics Laboratory University of Washington 1013 N.E. 40th Street Seattle, WA 98105 Attn: Technical Library	1	University of Hawaii Department of Ocean Engineering 2565 The Mall Honolulu, HI 96822 Attn: Library
1	University of Bridgeport Bridgeport, CT 06602 Attn: Dr. E. Uram	1	University of Illinois Urbana, IL 61801 Attn: Dr. J. Robertson
1	Cornell University Graduate School of Aerospace Engr Ithaca, New York 14850 Attn: Prof. W.R. Sears	3	Institute of Hydraulic Research The University of Iowa Iowa City, IA 52240 Attn: Library Dr. L. Landweber Dr. J. Kennedy
4	University of California Naval Architecture Department College of Engineering Berkeley, CA 94720 Attn: Library Prof. W. Webster Prof. J. Paulling Prof. J. Wehausen	1	The John Hopkins University Baltimore, MD 21218 Attn: Prof. O. Phillips Mechanics Dept
3	California Institute of Technology Pasadena, CA 91109 Attn: Aeronautics Library Dr. T.Y. Wu Dr. A.J. Acosta	1	Kansas State University Engineering Experiment Station Seaton Hall Manhattan, KS 66502 Attn: Prof. D. Nesmith
1	Docs/Repts/Trans Section Scripps Institution of Oceanography Library University of Calif., San Diego P.O. Box 2367 La Jolla, CA 92037		

1	University of Kansas Chm Civil Engr Dept Library Lawrence, KS 60644	1	Department of Aerospace & Mechanical Sciences Princeton University Princeton, NJ 08540 Attn: Prof. G. Mellor
1	Fritz Engr Laboratory Library Depart of Civil Engr Lehigh University Bethlehem, PA 18015	3	Davidson Laboratory Stevens Institute of Technology 711 Hudson Street Hoboken, NJ 07030 Attn: Library Mr. J. Breslin Mr. S. Tsakonas
3	Department of Ocean Engineering Massachusetts Institute of Technology Cambridge, MA 02139 Attn: Prof. P. Mandel Prof. M. Abkowitz Dr. J. Newman	1	Applied Research Laboratory Library University of Texas P.O. Box 8029 Austin, TX 78712
1	Engineering Technical Reports Room 10-500 Massachusetts Institute of Technology Cambridge, MA 02139	1	College of Engineering Utah State University Logan, UT 84321 Attn: Dr. R. Jeppson
5	St. Anthony Falls Hydraulic Laboratory University of Minnesota Mississippi River at 3rd Avenue SE Minneapolis, MN 55414 Attn: Dr. Roger Arndt Mr. J. Wetzel Prof. E. Silberman Mr. J. Killen Dr. C. Song	2	Stanford University Stanford, CA 94305 Attn: Engineering Library Dr. R. Street
3	Department of Naval Architecture and Marine Engineering North Campus The University of Michigan Ann Arbor, MI 48109 Attn: Library Dr. T.F. Ogilvie Prof. F. Hammitt	3	Webb Institute of Naval Architecture Crescent Beach Road Glen Cove, L.I., NY 11542 Attn: Library Prof. E.V. Lewis Prof. L.W. Ward
2	College of Engineering University of Notre Dame Notre Dame, IN 46556 Attn: Engineering Library Dr. A. Strandhagen	1	National Science Foundation Engineering Division Library 1800 G. Street N.W. Washington, DC 20550
2	New York University Courant Inst. of Math. Sciences 251 Mercier Street New York, NY 10012 Attn: Prof. A Peters Prof. J. Stoker	1	University of Connecticut Box U-37 Storrs, CT 06268 Attn: Dr. V. Scottron Hydraulic Research Lab
		1	Applied Research Laboratory P.O. Box 30 State College, PA 16801 Attn: DR. B. Parkin, Director Garfield Thomas Water Tunnel

1 Dr. Michael E. McCormick  
Naval Systems Engineering Department  
U.S. Naval Academy  
Annapolis, MD 21402

1 Dr. Douglas E. Humphreys (Code 794)  
Naval Coastal Systems Laboratory  
Panama City, FL 32401

1 Dr. Allen H. Magnuson  
Aerospace and Ocean Engineering Dept.  
Virginia Polytechnic Institute and  
State College  
Blacksburg, VA 24061

 The University of Michigan is an equal opportunity/affirmative action employer. Under applicable federal and state laws, including Title IX of the Education Amendments of 1972, the University does not discriminate on the basis of sex, race, or other prohibited matters in employment, in educational programs and activities, or in admissions. Inquiries or complaints may be addressed to the University's Director of Affirmative Action and Title IX Compliance: Dr. Gwendolyn C. Baker, 5072 Administration Building, 763-0235.