THE
REGULATION
OF
PONDEROSA PINE

A
Problem
in

## Forest Management

## Richard F. Bickford 1937

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## INTRODUCTION

The following few pages constitute a report on work done at the School of Forestry and Conservation of the University of Michigan in Management Problems under the guidance of Professor D. M. Matthews. The use of the selection system of silvicultural management has advantages both in the protection offered the site and in the cheapness of cultural operations that no other system equals. The analysis of any stand to determine the possibilities of managing it under any method of silviculture is difficult without some method of comparison; in fact comparison with a standard is necessary before any method of management can be decided upon.

In the relative amounts of basal area in each diameter class and the distribution of the basal area between age classes, Professor Matthews has found a method of comparison that is not only easy of application and easy to understand but also goes a long way in the determination of cuts, thinnings and so forth.

In Part I of this report I have attempted to regulate ponderosa pine by this method and as is necessary in the presentation of any plan in Part II I have evaluated the results of part one in comparison with existing practice.

## PART I

## THE PROBLEM

The data used in this problem represents a one percent cruise of an experimental forest on the west slope of the Sierra Nevada Mountains in central California. On the first eight pages of the Appendix a copy of the data as it was handed to me will be found.

In the analysis of a stand and stock table for a given area the first problem is to determine the age class distribution to find out if the stand is all aged or even aged. Then, when the stand is found to be all aged, various cutting cycles and rotations should be investigated both from the point of view of volume production and of value production. Due to the limitations of time only one cutting cycle with one rotation was investigated. The stand was divided into six fifty year age classes thus making an assumed cutting cycle of fifty jears and a rotation of three hundred years. The plan is to cut the stand every twentyfive years and thus reduce the rotation to one hundred and fifty years when the stand has been completely cut over once and the cutting cycle will be twenty-five years. The first step in the analysis is the construction of the control table.

## THE CONTROL TABLE

In the construction of my control table I used the figures of Dunning and Reineke(1). In order to use the rotation that $I$ had assumed it was necessary to extend their figures to three hundred years. This extension was done by extrapolation. This extrapolation and the tabulation of the resulting figures appear in the appendix on pages nine and ten. The site was approximated by the ratio of the total volume to the total number of trees. By the above method the site was decided to be a medium site of 60 at fifty years. Then the following control table was constructed by the methods outlined on pages 138-142 of Matthews textbook(2).
Table I CONTROL TABLE
100\% Ponderosa Pine $0-300$ Jears Site 60

| Age <br> Class | Number <br> of trees | Diameter <br> Range | Average <br> Diameter | Basal <br> Area | B. Volume <br> A. |  |  |  |  |
| :--- | :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0-50$ | Advance Reproduction |  |  |  |  |  |  |  |  |

## THE CLASSIFIED STANDS

Then all the stands were classified according to this control table with the following tables showing the results of the classification.
?able II ACTUAL STAND

| $\begin{gathered} \text { Age } \\ \text { Class } \end{gathered}$ | Number of trees | Diameter Range | Average <br> Diameter | Basal Area | Volume Bd. ft. | $\begin{gathered} \% \\ \text { Stocking } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-50 | Advance Reproduction |  |  |  |  |  |
| 51-100 | 62.4 | 4-10 | 5.6 | 10.8 | Nil | 11.6 |
| 101-150 | 10.1 | 10-24 | 15.3 | 12.8 | 1798 | 11.6 |
| 151-200 | 2.8 | 24-34 | 29.4 | 13.2 | 3238 | 11.6 |
| 201-250 | -1.8 | 34-42 | 37.5 | 13.9 | 4069 | 11.6 |
| 251-300 | 1.3 | 42- | 45.5 | 14.8 | 5103 | 11.6 |
| Total | 78.4 |  |  | 65.5 | 14,208 | 11.6 |

BLOCK B

| Age | Number | Diameter | Average | Basal | Volume | \% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Class | of trees | Range | Diameter | Area | Bd. ft. | Stocking |
| 0-50 | Advance Reproduction |  |  |  |  |  |
| 51-100 | 52.6 | 4-16 | 7.5 | 16.0 | 851 | 17.2 |
| 101-150 | 8.1 | 16-26 | 20.6 | 18.8 | 2987 | 17.1 |
| 151-200 | 4.5 | 26-30 | 28.2 | 19.5 | 4094 | 17.1 |
| 201-250 | 3.5 | 30-36 | 32.9 | 20.6 | 5071 | 17.1 |
| 251-300 | 2.6 | 36- | 39.3 | 21.8 | 5873 | 17.1 |
| Total | 71.3 |  |  | 96.7 | 18876 | 17.1 |

## Table IV

BLOCK C

| Age <br> Class | Number <br> of Trees | Diameter <br> Range | Average <br> Diameter | Basal <br> Area | Volume <br> Bd. ft. |
| :--- | :---: | :---: | :---: | :---: | :---: |
| O-50 | Advance Reproduction |  |  |  |  |



Table VIII
BLOCK P

| $\begin{aligned} & \text { Age } \\ & \text { Class } \end{aligned}$ | Number of Trees | Diameter Range | Average Diameter | Basal Area | Volume Bd. ft. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0-50 | Advance Reproduction |  |  |  |  |
| 51-100 | 46.6 | 4-18 | 8.0 | 16.1 | 1161 |
| 101-150 | 6.9 | 18-26 | 22.4 | 18.9 | 3088 |
| 151-200 | 4.4 | 26-32 | 28.6 | 19.6 | 4432 |
| 201-250 | 3.4 | 32-36 | 33.4 | 20.7 | 5208 |
| 251-300 | 2.4 | 36- | 40.9 | 21.9 | 5924 |
| Total | 63.7 |  |  | 97.2 | 19813 |

Average Stocking -- 17.2

Table IX BLOCK P -- COMPARTMENTS 23-26

| Age | Number | Diameter | Average | Basal |
| :---: | :---: | :---: | :--- | :--- |
| Class | of Trees | Range | Diameter | Area |

0-50
51-100
28.5

4-22
11.7
24.9
29.2
26.0

5701
151-200
5.6

28-32
33.1
27.4

6423
201-250
4.4

32-36
40.2
28.9

6501
251-300
3.3

36-
128.5

25353

Table X BLOCK P - COMPARTMENTS 31-21

| $\begin{gathered} \text { Age } \\ \text { Class } \end{gathered}$ | $\begin{gathered} \text { Number } \\ \text { of Trees } \end{gathered}$ | Diameter Range | Average <br> Diameter | Basal Area | Volume <br> bd. ft. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0-50 | Advance Reproduction |  |  |  |  |
| 51-100 | 27.1 | 4-2\% | 11.3 | 18.9 | 2285 |
| 101-150 | 6.5 | 22-28 | 25.1 | 22.3 | 4215 |
| 151-200 | 4.9 | 28-32 | 29.4 | 23.1 | 5255 |
| 201-250 | 4.0 | 32-36 | 33.4 | 24.4 | 6247 |
| 251-300 | 3.0 | 36* | 39.7 | 25.8 | 6928 |
| Total | 45.5 |  |  | 114.5 | 24930 |

Average Stocking -- 20.3
The classification of the various stands reveals the significant characteristics of the various stands. Thus the conclusion is reached that Block A is the only one that is at present in an all aged condition. All of the other stands have an inconsistent difference between average diameters as witnessed by the 13.8 inch difference In the average diameters of the 51-100 and the 101-150 age classes. In this particular stand all other age classes have a difference of approximately 4 inches. This inconsistent difference is present in all the stands except Block $A$. The presence of this difference is good evidence that Ponderosa Pine does not naturally grow in an all aged forest and thus is not suitable to selection management. However the inconsistent difference noted above can be explained on other grounds. Ground fires, which are quite common, might easily have killed off the reproduction for the missing diameter classes. There is
no bunching of the diameters in any of the stands as is common in the even aged stands of Lodgepole pine. Thus while the classified stands show evidence of being even aged there is nothing certain and final about their present condition. In the continuation of the study Block A will be used as typical of the all aged stands that might be produced by ponderosa pine.

## GROWTH PREDICTION

To continue the study of ponderosa pine under selec. tion management it is necessary to predict the growth of the stands and determine the possibility of future cuts. To carry out this prediction it is necessary to have the growth of ponderosa pine by diameter classes.

Duncan Dunning in a government bulletin(3) gives the periodic annual growth percent in basal area. From this basal area growth percent the diameter growth percent can be obtained by simply extracting the square root. That this relationship holds is demonstrated below.
$\mathrm{BA}_{1}$-- Present basal area
$\mathrm{BA}_{2}$-- Future basal area
$d_{1}-\infty$ Present diameter
$\mathrm{d}_{2}-$ Future diameter
p -a- ratio of circumferance to radius
r - - - basal area growth percent
s --- diameter growth percent
$\mathrm{BA}_{2}$ equals $r \times \mathrm{BA}_{1}$
$B A$ equals $\left(q \times d^{2}\right) / 4$
Then:

$$
\left(q \times d_{2}^{2}\right) / 4 \text { equals }(r)\left(q \times d_{1}^{2}\right) / 4
$$

the $q / 4$ cancel out leaving

$$
d_{2}^{2} \text { equals } r \times d_{1}^{2}
$$

then take square root of both sides

$$
d_{2} \text { equals (square root of } r \text { ) } x d_{1}
$$

then $s$ equals the square root of $r$

The figures for basal area growth as appearing in Duncan Dunning's publication were changed to diameter growth figures as indicated on the last page and then through a series of arithmetical manipulations that appear on pages eleven and twelve of the appendix the following diameter growth figures were obtained.

| Table XI | DIAMETER GROWTH |  |  |
| :---: | :---: | :---: | :---: |
| Diameter <br> Breast High | Growth <br> Next 25 Jears | Diameter <br> Breast High | Growth <br> Next <br> $4^{\prime \prime}$ |
| 6 | $4.8^{\prime \prime}$ | $24^{\prime \prime}$ | $4.7^{\prime \prime}$ |
| 8 | 5.6 | 26 | 4.4 |
| 10 | 5.9 | 28 | 4.2 |
| 12 | 6.1 | 30 | 4.0 |
| 14 | 6.1 | 32 | 3.9 |
| 16 | 5.0 | 34 | 3.8 |
| 18 | 5.7 | 36 | 3.7 |
| 20 | 5.4 | 38 | 3.6 |
| 22 | 5.0 | 40 | 3.5 |

Using these growth rates Block A after being cut was predicted forward tenty-five years then cut again and predicted forward again and so forth until all the trees that wore in the original stand were cut.

## STAND PREDICTION

In the prediction of the stand possible at the time of the next cut I used a method developed by Reynolds of the Crosset Lumber Company of Arkansas. As an example of this method of stand prediction I will consider the ten inch diameter class of Block $A$. This diameter class includes 4.08 trees. Ten-inch trees, from the table on the preceding page, will grow 6.1 inches in twenty-five years. In a large sample the trees in the ten inch class would be evenly divided throughout that is there would be just as many trees in a one tenth inch class at 9.6 as there would be at any other one tenth inch class up to 10.5. If a 9.6 inch tree grows 6.1 inches it will then fall in the 16 inch class with a diameter of 15.7 . A ten inch tree would also fall in the 16 inch class with a diameter of 16.1. But a 10.5 inch tree would be 16.6 inches in diameter at the end of the period and thus would fall into the 17 inch diameter class. Thus it is seen that the units of a diameter growth rate indicate the number of diameter classes moved by the tree in the growth period and the decimal indicates the percent of the trees that will move one more class than is indicated by the units. Thus if the number of trees in each diameter class is broken up in this way and added diagonally the number of trees in the predicted stand in the diameter class indicated will result. On the next page the stand prediction of Block A is carried out exactly as outlined here. The diagonal lines indicate the direction of the addition.

# 12.9 15.7 8.4 4.1 


$\qquad$
19.4
16.8
15.7
8.4
4.1
2.5
1.5






No

- $0<0$
F~下
$-O_{0}^{\circ} 0^{\circ}$


In connection with the stand prediction carried out on the preceding page as the diameter classes involved were of a magnitude of two inches it was necessary to use radial growth rather then diameter growth. The volume per tree was obtained by dividing the volumes as given in the original data by the number of trees at the corresponding diameter class.

A control table was then constructed for the new stand as predicted. This control table will be for a stand 0-275 years old and appears below. Table XIII

CONTROL TABLE
Ponderosa Pine 0-275 years

| Age <br> Class | Number <br> of Trees | Diameter <br> Range | Average <br> Diameter | Basal <br> Area |
| :--- | :---: | :---: | :---: | :---: |
| $0-25$ | Advance Reproduction | Of B.A. |  |  |
| $25-75$ | No Data |  |  |  |
|  |  |  |  |  |


| $75-125$ | 85 | $11-16$ | 14.9 | 104 | 22.6 |
| :--- | ---: | :---: | :---: | :---: | ---: |
| $125-175$ | 59 | $16-19$ | 18.8 | 114 | 24.8 |
| $175-225$ | 50 | $19-22$ | 20.8 | 119 | 25.9 |
| $225-275$ | 42 | $22-$ | 23.1 | 123 | 26.7 |
| Total | 236 |  |  | 460 | 100.0 |

Then the stand as predicted on the last page is classified according to this control table.

| Table XIV |  | ACTUAL STAND |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Block A |  | Second Cycle |  |  |  |
| $\begin{aligned} & \text { Age } \\ & \text { Class } \end{aligned}$ | Number of Trees | $\begin{gathered} \text { Diameter } \\ \text { Range } \end{gathered}$ | Average Diameter | Basal Area | Volume <br> Bd. Ft. |
| 0-25 |  | Advance $\mathrm{K}_{\text {ep }}$ | oduction |  |  |
| 25-75 |  | No Data |  |  |  |
| 75-125 | 44.2 | 8-12 | 9.7 | 22.3 | 950 |
| 125-175 | 22.3 | 12-18 | 14.2 | 24.4 | 3400 |
| 175-225 | 7.4 | 18-34 | 25.2 | 25.5 | 5410 |
| 225-275 | 3.2 | 34- | 38.0 | 26.3 | 7830 |
| Total | 77.1 |  |  | 98.5 | 17590 |

Average Stocking 21.4

It is to be noted from the above table in comparison with the original stand classification table for Block A that there is an increase both in basal area and in volume. The increase in basal area make the stocking much more than it was in the original stand. The maximum diameter of the stand has decreased as has the total number of trees that we have data about. The number of trees corresponding to the number of trees in the same diameter classes has increased. That is there are more trees in the oldest diameter class of the new stand than there was in the oldest diameter class of the original stand.

Thsi stand prediction is continued on the next few pages until the data are exausted.

$$
\begin{aligned}
& \text { Block . }
\end{aligned}
$$




Table XXI
PREDICTION OF STAND FOR THE FIFTH CYCLE
Block A
Fourth 25 Years


| Ponderosa Pine |  |  | 0-200 Years |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Age } \\ & \text { Class } \end{aligned}$ | Number of Trees | Diameter Range | Average Diameter | Basal Area | $\begin{gathered} \text { Percent } \\ \text { B.A. } \end{gathered}$ |
| 0-25 |  | Advance Repr | roductio |  |  |
| 25-50 |  | No Data |  | - |  |
| 50-75 |  | No Data |  |  |  |
| 75-100 |  | No Data |  |  |  |
| 100-150 |  | No Data |  |  |  |
| 150-200 | 54 | 18-21 | 19.7 | 114 | 100 |
| Total | 54 |  |  | 114 | 100 |

Table XXIII ACTUAL STAND

|  | Block A | Fifth Cycle |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Age | Number <br> of Trees | Diameter <br> Range | Average <br> Diameter | Basal <br> Area | | Volume |
| :---: |
| bd.ft. |

The points noted on page 14 concerning the first prediction of the stand continue in evidence as long as the data lasted. The average stocking increased from $11.6 \%$ to $111 \%$ in the final stand. The volume of the out increased from 5103 board feet to 29390 board feet in the final stand. It is of course obvious that the actual stand on the ground will not do this. The actual stand will undoubtedly grow slower as well as have considerable nortality which is not considered. Both mortality and growth slower than is possible are indications of the necessity of thinnings to maintain the forest at its bighest rate of possible production.

The question arises as to how many trees should be removed. The choice of the actual trees should be of course on the basis of good silvicultural practice in the field; however a guide to the actual number of trees that the area can successfully carry would be of great assistance to the silviculturalist in the field. When aocurate data as to the stand and as to growth rates are available this number of trees can be very closely approximated by calculations similar to the ones that follow.

In order to be more general a mixed stand, Block C, was chosen for these calculations as most stands are mixed to some extent. First it is necessary to determine how close to normal the stand is capable of approaching in respect to normality. Then growth rates need to be determined and finally computations similar to those that were carried out on Block A are carried out. The chief
difference is that the stand is not allowed to become of a higher stocking than it was previously decided the area could carry.

In the case of Block $C$ it was decided that the greatest possible stocking and still maintain growth at a satisfactory rate was 50 percent. For ease of computation a growth rate of three inches per twentyfive year period was assumed. Then a control table was constructed on the basis of 50 percent stocking and the actual data for Block $C$ was made to fit this table. The oldest age group was removed and the stand was predicted forward as in Block A as discussed on page 1l. In addition to outting of the oldest age class, if at any time the predicted stand contained more basal area than the $50 \%$ of normal control stand, then the original stand was thinned to reduce the number of trees to an extent that the predicted stand would not have more basal area then the $50 \%$ of normal control stand.

Below is the control table that was used.
Table XXIV
CONTROL TABLE

| Age <br> Class | Number <br> of Trees | Average <br> Diameter | Basal <br> Area |
| :--- | :---: | :---: | :---: |
| $0-50$ | Advance | Reproduction |  |
| $50-100$ | 72 | 11 | 48 |
| $100-150$ | 34 | 17 | 54 |
| $150-200$ | 27 | 20 | 59 |
| $200-250$ | 23 | 22 | 60 |
| $250-300$ | 19 |  | 60 |
|  |  |  | 282 |

50\% Stocked

Table XXV
Block C

DEMONSTRATION OF THINNING
$50 \%$ stocked


| 50-100\# 72 | 48 | 11 | 8 | 31.1 | 10.8 | 19.6 | 5.8 | 1.3 | 0.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100-150 34 | 54 | 17 | 22 | 6.1 | 16.3 | 1.3 | 3.1 | 0.3 | 0.7 |
| 150-200 27 | 59 | 20 | 29 | 3.6 | 16.8 | 0.7 | 2.8 | 0.3 | 1.2 |
| 200-250 23 | 60 | 22 | 34 | 2.8 | 17.6 | 0.4 | 2.8 | 0.2 | 1.6 |
| 250-300 19 | 60 | 24 | 42 | 1.6 | 16.2 | 0.4 | 3.5 | 0.4 | 3.5 |
| Cut all trees 42 inches and up |  |  |  |  |  |  |  |  |  |

Stand 25 Years Hence


150-200 $27 \quad 59 \quad 20 \quad: 20 \quad 27.0 \quad 59.0$

\#- No data available for the younger age classes.

Any caluclation such as has been carried out on the preceding pages is of course highly theoretical, however, to any timber marker to have an idea of the exact number of trees to be remored in the thinning would be of great assistance.

In the first part of this report the possibilities of applying all aged regulation to Ponderosa Pine in the California Pine Region has been investigated. Before any definite conclusions can be drawn the basic data that are available must be elaborated upon so that these methods can be applied more accurately. There is a genuine need for growth data for stands after release.

The data that were available indicated that Ponderosa Pine does not generally grow in all aged stands. In fact out of five stands considered only one was definitely in an all aged condition. The remainder of the stands being In various stages of evenness that is there was doubt as to their actual state. They were neither definitely even aged nor were they definitely all aged but more or less of a combination of both for example Block $G$ is all aged in the four older age classes but the youngest age class is out of line as regards the age of the rest of the stand. These differences can be explained on the basis of fire if one wants to believe it, but nothing can be proven either way. If one thinks that ponderosa pine does grow in all aged stands similar to Block A then it is logical to assume that the methods here demonstrated will operate very satisfactrolly.

On the assumption that the stands will respond to all aged management the second part of this report considers the financial problems involved.

PART II

WILL IT PAY DIVIDENDS

## THE PROBLEM

In the practice of any business the ultimate criterion of any plan is!will it pay? Then if it will pay 1t must pay better than any other plan that is in use or might be advanced. In the practice of forestry in the California Pine region in the past all operators have been liquidating their timber holdings as fast as market conditions would allow. The Forest Service has advocated partial qutting with long cutting cycles. Since the publication as to the cost of logging small and large size timber many private operators have been cutting to an arbritrary diameter limit simply because it has been shown that that is more profitable because the smaller diameters cost more to produce as lumber than can be realized from the lumber. This has in effect made for the longer cycle advocated by the Forest Service.

If any other plan is to be adopted by the owners it will have to be shown to their satisfaction that the plan is more profitable not only in the long run but in many instances more profitable as regards immediate income. In order to compare the plan of management advocated with various other operating methods this paln will be evaluated and a liquidating plan will be evaluated for comparison.

## STUMPAGE VALUES

In order to evaluate the cuts under different plans of management it is necessary to obtain the value of trees of different diameters. W. H. Gibbons, H. M. Johnson, and H. R. Spelman have published in The Timberman(4) complete figures on the cost of production of lumber. This article is excellent in that the cost are broken down into the various items that make up the total cost. The following table is the result of combining certain of their figures, the combinations are indicated, with the depreciation on logging equipment eliminated as this depreciation is a per acre charge and is included later.

Table XXVI Stumpage Value Determination

|  | Total ogging: \$/M | Cost | otal: <br> rod.: <br> \$/M: | /M | Total Costs $\$ / M$ | $\begin{gathered} \text { Value } \\ \text { per } \\ M / \mathrm{M} \\ \hline \$ \end{gathered}$ | $\begin{aligned} & \text { Surplus } \\ & \text { Sor } \\ & \text { Stumpage } \\ & \hline \quad \$ / \mathrm{M} \\ & \hline \end{aligned}$ | Smoothed <br> Stumpage <br> Suplus <br> $\$ / M$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 18.90 | 14.35 | 33.25 | 3.46 | 36.71 | 29.93 | -6.78 | -4.80 |
| 14 | 15.94 | 12.58 | 27.52 | 3.11 | 30.63 | 30.18 | -0.45 | -1.40 |
| 16 | 15.03 | 11.14 | 26.17 | 2.82 | 28.99 | 30.03 | 1.04 | 0.90 |
| 18 | 14.52 | 10.01 | 24.53 | 2.72 | 27.25 | 28.89 | 1.64 | 2.50 |
| 20 | 14.03 | 9.29 | 23.32 | 2.58 | 25.90 | 29.17 | 3.27 | 3.95 |
| 22 | 13.07 | 8.69 | 21.76 | 2.47 | 24.23 | 30.07 | 5.84 | 5.20 |
| 24 | 12.88 | 8.29 | 21.17 | 2.41 | 23.58 | 31.03 | 6.45 | 6.40 |
| 26 | 11.94 | 7.91 | 19.85 | 2.20 | 22.05 | 29.44 | 7.39 | 7.42 |
| 28 | 11.58 | 7.59 | 19.17 | 2.09 | 21.26 | 32.93 | 11.67 | 8.25 |
| 30 | 11.53 | 7.35 | 18.88 | 2.10 | 20.98 | 30.15 | 9.17 | 9.12 |
| 32 | 11.13 | 7.16 | 18.29 | 2.02 | 20.31 | 30.77 | 10.46 | 9.80 |
| 34 | 11.42 | 7.15 | 18.57 | 2.02 | 20.59 | 30.96 | 9.37 | 10.24 |
| 36 | 10.89 | 7.05 | 17.94 | 1.98 | 19.92 | 30.60 | 10.68 | 10.50 |
| 38 | 10.86 | 6.90 | 17.76 | 1.95 | 19.71 | 32.14 | 12.43 | 10.65 |
| $40+$ | 11.45 | 7.21 | 18.66 | 2.09 | 20.75 | 27.34 | 6.59 | 10.70\% |

*Interest on invested capital
**All higher diameters are assumed to have this surplus.

Four plans were chosen as a basis of comparison, namely: destructive logging taking everything on the ground, destructive logging to a zero margin diameter limit, twenty-five year periodic sustained yield, and annual sustained field. The depreciation on the logging equipment was determined by multiplication of the volume per diameter class by the depreciation as given in the article in the Timberman and summation and then dividing by the volume per acre and thus obtaining a constent depreciation figure. Then the values were reduced by this figure which in the order of listing above was $\$ 0.31,0.30,0.24$, and 0.24 . The stumpage values were then multiplied by the volume per diameter class in each case with the following incomes resulting.

Incomes Under the Various Plans


Periodic Sustained Yield m-n-m-m-m-n-men 49,300

Then these incomes were evaluated on the basis of their present value as a capital sum at four, three, and two percent. The formulas involved are indicated below.

Complete Destruction:

$$
C o=\frac{a\left(1.0 p^{n}-1\right)}{(0.0 p)\left(1.0 p^{n}\right)}
$$

When:
Co - Present Value a - Annual income p - Interest rate n - Number of Years in this case 10

Cut to the diameter of zero margin and return for a second cut of one third the original cut in sixty years:

$$
C_{0}=\frac{a\left(1.0 p^{n}-\right)}{(0.0 p)(1.0 p n)} \quad \text { plus } \frac{a / 3\left(1.0 p^{n}-1\right)}{(0.0 p)\left(1.0 p^{n}\right)(1.0 p)}
$$

$r$ - Period before second cut starts Other symbols are the same as before

Periodic Sustained Yield:
Cut area over selectively in ten years and then wait fifteen years before starting a second cut.

The formulas are the same as in the preceding case.
Annual Sustained Yield:

$$
C_{0}=\frac{\text { Income minus expenses }}{0.0 p}
$$

By use of the above formulas the resulting values tabulated below were obtained.

Table XXVII Values of Different Plans


Complete Destruction $\$ 1,048,000 \$ 1,091,000 \$ 1,120,000$
Zero Margin Destruction 1,096,400 1,180,000 1,252,000
Periodic Sustained Yield 640,000 796,000 1,095,000
Annual Sustained Yield 493,500 658,000 987,000

From the point of view of the forester these results as tabulated on the preceding page as far from satisfactory andcosts were further investigated to see if it was possible to improve the relative position of sustained yield. The publication of $M$. Brundage, M. Krueger, and D. Dunning on the economic significance of tree size(5) was used for value data for the same calculations as was some unpublished cost data of the Hines Lumber Company. The difference gained by this manipulation is not worth mentioning so that the results given on the last page can be considered representative of what the available cost data will produce in the way of value under the different plans.

In order to demonstrate the situation met by an operating timber company when it meets falling market prices a chart showing the results of curtailing the cut horozontally and vertically is included on the last page of the appendix. By curtailing the cut herdzentely is meant the raising of the diameter limit as contrasted horizonta! with a vertieal curtailment entirely on the area basis.

The following conclusions drawn from the analysis of the data are worthy of note:

1. Ponderosa Pine probably does not grow naturally in all aged stands.
2. Where Ponderosa Pine is found growing in an all aged condition the method of basal area control management applies easily and with perfect fit.
3. Under selection management the present stand can be maintained and a cut of between five and six thousand board feet taken every twenty-five years.
4. The most profitable method of management for the private operator is a liquidation plan to a zero margin diameter limit.
5. When periods of low prices are encountered it is Verotianll
more profitable to curtail the cut hordentaly then vertically.

APPENDIX

Block A -- Summary by Diameters


Block B -- Summary by Diameters
Total Area in Block $-\infty-\infty-\infty-\infty-\infty-\infty-\infty$ 1144.2 A. Total Area of Timber Types in Block 1142.4 A.


Total52.2 16731 13.2 1121 $6.0 \quad 1030 \quad 18.3186$
*Ponderose Pine, $* *$ White Fir, $* * *$ Incense Cedar

Block C -- Summary by Diameters

Total Area of Timber Types in Block ---- 2354.0

*Ponderosa Pine, **Incense Cedar, ***White Fir

## Block G -- Summary by Diameters


Total Area of Timber Types in Block ----- 2799.2


Summary by Diameters
Block G
Compartment 4-3
Total Area of Compartment --w-m-m-n-m-n- 494.9 Total Area of Timber Types in Compartment - 159.2


## Summary by Diameters



## Block P -- Summary by Diameters

Total Area of Block -------n-------------- 1994.4 A. Total Area of Timber Types in Block ------ 1994.4 A.

| D. |
| :---: |
| B. |
|  |

6

| 10 | 2.42 |
| :--- | :--- |
| 12 | 2.04 |
| 14 | 1.44 |
| 16 | 1.32 |
| 18 | 1.25 |


| 30 | 1.45 | 1766 | 0.10 | 88 | 0.09 | 40 | 1.6 | 1894 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 1.39 | 2028 | 0.09 | 91 | 0.10 | 58 | 1.6 | 2177 |
| 34 | 1.06 | 1820 | 0.08 | 95 | 0.09 | 60 | 1.2 | 1974 |
| 36 | 0.83 | 1657 | 0.05 | 75 | 0.08 | 62 | 1.0 | 1794 |
| 38 | 0.57 | 1303 | 0.04 | 69 | 0.07 | 61 | 0.7 | 1434 |
| 40 | 0.38 | 1004 | 0.03 | 57 | 0.06 | 60 | 0.5 | 1120 |
| 42 | 0.25 | 765 | 0.02 | 43 | 0.05 | 56 | 0.3 | 864 |
| 44 | 0.15 | 517 | 0.01 | 36 | 0.04 | 51 | 0.2 | 603 |
| 46 | 0.11 | 392 | 0.01 | 22 | 0.04 | 55 | 0.2 | 469 |
| 48 | 0.06 | 247 |  | 12 | 0.04 | 57 | 0.1 | 316 |
| 50 | 0.04 | 177 |  | 13 | 0.02 | 39 | 0.1 | 229 |
| 52 | 0.02 | 82 |  | 10 | 0.02 | 36 |  | 128 |
| 54 | 0.01 | 56 |  | 1 | 0.01 | 27 |  | 83 |
| 56 | 0.01 | 43 |  |  | 0.01 | 19 |  | 62 |
| 58 |  | 18 |  | 3 | 0.01 | 6 |  | 27 |
| 60 |  | 14 |  |  |  | 8 |  | 22 |
| 62 |  | 8 |  | 4 |  | 4 |  | 16 |
| 64 |  | 8 |  | 1 |  | 3 |  | 12 |
| 66 |  | 5 |  |  |  | 3 |  | 8 |
| 68 |  |  |  |  |  | 1 |  | 1 |

*Ponderosa Pine, $*-n$ White Fir, $* * *$ Incense Cedar

Summary by Diameters


Summary by Diameters
Block P
Compartment 31-21
Total Area of Compartment --n--------------- 39.0 A. Total Area of Timber Types in Compartment -- 39.0 A.


Application of Regression Formula to Yield Table(1):
Basal Area

$$
\begin{aligned}
\text { B.A. } & =2.03(100) \text { plus } 0.149(100)-8.15 \\
& =209.8 \% \text { of Composite Table }
\end{aligned}
$$

Number of Trees
No. Trees $=2.06(100)$ plus 0.32(100) plus 19.36
$=188.3 \%$ of Composite Table
Volume in Cubic Feet
Volume $=1.53(100)$ plus $0.72(100)$ plus 128.78 $=209.5 \%$ of Composite Table

Yield Data after Application of
Regression Coefficients

| $\begin{array}{r} \text { Age: } \\ \hline \end{array}$ | Basal area | : Number : :of Trees: | $\begin{gathered} \mathrm{D}_{\bullet} \mathrm{B}_{0}: \\ \mathrm{H}_{\bullet} \quad \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Volume : } \\ & \text { Cu.ft. } \end{aligned}$ | Volume <br> Bd.ft. | $\begin{aligned} & : M_{0} A_{0} I_{0} \\ & : B d \cdot f t_{0} \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 306 | 3330 | 3.9 | 4600 | 2300 | 77 |
| 40 | 412 | 2150 | 5.6 | 7900 | 11600 | 290 |
| 50 | 483 | 1530 | 7.2 | 11300 | 27600 | 552 |
| 60 | 521 | 1120 | 8.8 | 14700 | 49200 | 820 |
| 70 | 554 | 836 | 10.5 | 17700 | 74200 | 1060 |
| 80 | 583 | 661 | 12.0 | 19900 | 94900 | 1190 |
| 90 | 604 | 550 | 13.3 | 22000 | 113900 | 1260 |
| 100 | 625 | 491 | 14.5 | 24100 | 132100 | 1320 |
| 110 | 640 | 446 | 15.4 | 25700 | 147800 | 1340 |
| 120 | 655 | 412 | 16.2 | 27600 | 163800 | 1360 |
| 130 | 670 | 385 | 16.9 | 29300 | 179100 | 1380 |
| 140 | 680 | 364 | 17.5 | 30900 | 192900 | 1380 |
| 150 | 690 | 343 | 18.2 | 32300 | 205500 | 1370 |

## Extrapolated Yield Data*

| Age | Number of Trees | : Diameter : :BreastHigh: | Basal area | $\begin{aligned} &: \text { M.A.I. } \\ &: \text { Bd.fit. } \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { : Volume } \\ & \text { : Bdoft. } \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 3330 | 3.9 | 306 | 77 | 2300 |
| 40 | 2150 | 5.6 | 412 | 290 | 11600 |
| 50 | 1530 | 7.2 | 483 | 552 | 27600 |
| 60 | 1120 | 8.8 | 521 | 820 | 49200 |
| 70 | 836 | 10.5 | 554 | 1060 | 74200 |
| 80 | 661 | 12.0 | 583 | 1190 | 94900 |
| 90 | 550 | 13.3 | 604 | 1260 | 113900 |
| 100 | 491 | 14.5 | 625 | 1320 | 132100 |
| 110 | 446 | 15.4 | 640 | 1340 | 147800 |
| 120 | 412 | 16.2 | 655 | 1360 | 163800 |
| 130 | 385 | 16.9 | 670 | 1380 | 179100 |
| 140 | 364 | 17.5 | 680 | 1380 | 192100 |
| 150 | 343 | 18.2 | 690 | 1370 | 205500 |
| 160 | 335 | 18.7 | 694 | 1360 | 217500 |
| 170 | 328 | 19.2 | 698 | 1350 | 229200 |
| 180 | 319 | 19.7 | 702 | 1340 | 241000 |
| 190 | 310 | 20.2 | 706 | 1330 | 253000 |
| 200 | 300 | 20.7 | 712 | 1320 | 264000 |
| 210 | 291 | 21.2 | 718 | 1310 | 275000 |
| 220 | 281 | 21.7 | 722 | 1300 | 286000 |
| 230 | 272 | 22.2 | 726 | 1290 | 296000 |
| 240 | 263 | 22.7 | 731 | 1280 | 307000 |
| 250 | 254 | 23.2 | 736 | 1270 | 318000 |
| 260 | 245 | 23.7 | 741 | 1260 | 328000 |
| 270 | 236 | 24.2 | 746 | 1250 | 337000 |
| 280 | 228 | 24.7 | 751 | 1240 | 347000 |
| 290 | 219 | 25.2 | 756 | 1230 | 356000 |
| 300 | 209 | 25.7 | 761 | 1220 | 366000 |

\#See graph that follows for actual extrapolation


Derrivation
of Growth Rates

| $\begin{aligned} & D_{0} \\ & B_{0} \\ & H_{0} \end{aligned}$ | : Basal*: <br> : area : <br> : Growth: <br> : Percent: | Diameter Growth Percent | $\begin{aligned} & \text { : D. B. H. } \\ & \text { : } 25 \\ & \text { : Years } \\ & \text { : Hence } \\ & \hline \end{aligned}$ | : Diameter : <br> : Growth : <br> : in inches: <br> : 25 Years : | Smoothed <br> Diameter <br> Growth <br> In. 25 Y. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 1.064 | 1.032 | 8.78 | 4.78 | 4.8 |
| 6 | 1.064 | 1.032 | 12.00 | 6.00 | 5.6 |
| 8 | 1.064 | 1.032 | 13.89 | 5.89 | 5.9 |
| 10 | 1.064 | 1.032 | 15.58 | 5.58 | 6.1 |
| 12 | 1.033 | 1.016 | 17.58 | 5.58 | 6.1 |
| 14 | 1.033 | 1.016 | 19.52 | 5.52 | 6.0 |
| 16 | 1.033 | 1.016 | 21.3 | 5.3 | 5.9 |
| 18 | 1.022 | 1.011 | 23.7 | 5.7 | 5.7 |
| 20 | 1.022 | 1.011 | 25.4 | 5.4 | 5.4 |
| 22 | 1.022 | 1.011 | 27.0 | 5.0 | 5.0 |
| 24 | 1.015 | 1.007 | 28.6 | 4.6 | 4.7 |
| 26 | 1.015 | 1.007 | 30.2 | 4.2 | 4.4 |
| 28 | 1.015 | 1.007 | 32.1 | 4.1 | 4.2 |
| 30 | 1.012 | 1.005 | 34.0 | 4.0 | 4.0 |
| 32 | 1.012 | 1.005 | 35.9 | 3.9 | 3.9 |
| 34 | 1.012 | 1.005 | 37.7 | 3.7 | 3.8 |
| 36 | 1.009 | 1.004 | 39.8 | 3.8 | 3.7 |
| 38 | 1.009 | 1.004 | 41.7 | 3.7 | 3.6 |
| 40 | 1.009 | 1.004 | 43.4 | 3.4 | 3.5 |
| 42 | 1.007 | 1.003 | 45.2 | 3.2 | 3.3 |





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