

Supplementary Material: Aerosol radiative forcing from the 2010 Eyjafjallajökull volcanic eruptions

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1 Optical properties of non-spherical particles

We derived optical properties for a variety of non-spherical ash particles using the T -Matrix scattering code [Mishchenko and Travis, 1998], available at: http://www.giss.nasa.gov/staff/mmishchenko/t_matrix.html. Tables S1–S3 show the mass absorption cross-section, single-scatter albedo, and scattering asymmetry parameter for spheres, oblate spheroids with different aspect ratios (labeled a/b), prolate spheroids with different aspect ratios, and Chebyshev shapes with polynomial degree 5 and deformation factor of +0.1. Properties are shown for sphere-equivalent particle radii of 0.1 μm and 1.0 μm , and wavelengths of 0.55 μm (mid-visible) and 11 μm (the peak of 263 K Planck emission). All particles in each row have the same volume. Refractive indices are those applied for the central scenarios of radiative forcing, and are $1.54 + 0.0042i$ at $\lambda = 0.55 \mu\text{m}$ and $2.24 + 0.4295i$ at $\lambda = 11.0 \mu\text{m}$.

Table S1: Mass Absorption Cross-Section of Different Equal-Volume Shapes

| r_e (μm) | λ (μm) | Sphere | Oblate S. ($a/b = 1.2$) | Oblate S. ($a/b = 1.6$) | Oblate S. ($a/b = 2.0$) | Prolate S. ($b/a = 1.2$) | Prolate S. ($b/a = 1.6$) | Prolate S. ($b/a = 2.0$) | Chebyshev (5, +0.1) |
|----------------------------|--------------------------------|--------|------------------------------|------------------------------|------------------------------|-------------------------------|-------------------------------|-------------------------------|------------------------|
| 0.1 | 0.55 | 46.5 | 46.5 | 46.2 | 45.8 | 46.5 | 46.3 | 46.3 | 46.5 |
| 0.1 | 11.0 | 74.6 | 75.4 | 80.0 | 86.3 | 75.4 | 79.9 | 86.2 | 78.9 |
| 1.0 | 0.55 | 63.9 | 64.8 | 66.8 | 67.7 | 64.9 | 67.3 | 68.2 | 68.8 |
| 1.0 | 11.0 | 122.6 | 123.4 | 128.0 | 134.0 | 123.4 | 128.2 | 134.9 | 126.6 |

Table S2: Single-Scatter Albedo of Different Equal-Volume Shapes

| r_e (μm) | λ (μm) | Sphere | Oblate S. ($a/b = 1.2$) | Oblate S. ($a/b = 1.6$) | Oblate S. ($a/b = 2.0$) | Prolate S. ($b/a = 1.2$) | Prolate S. ($b/a = 1.6$) | Prolate S. ($b/a = 2.0$) | Chebyshev (5, +0.1) |
|----------------------------|--------------------------------|---------|------------------------------|------------------------------|------------------------------|-------------------------------|-------------------------------|-------------------------------|------------------------|
| 0.1 | 0.55 | 0.96895 | 0.96893 | 0.96866 | 0.96822 | 0.96893 | 0.96868 | 0.96828 | 0.96883 |
| 0.1 | 11.0 | 0.00077 | 0.00077 | 0.00077 | 0.00077 | 0.00077 | 0.00077 | 0.00077 | 0.00075 |
| 1.0 | 0.55 | 0.90655 | 0.90561 | 0.90525 | 0.90745 | 0.90550 | 0.90516 | 0.90856 | 0.90348 |
| 1.0 | 11.0 | 0.32442 | 0.32459 | 0.32496 | 0.32438 | 0.32457 | 0.32478 | 0.32403 | 0.32336 |

Table S3: Asymmetry Parameter of Different Equal-Volume Shapes

| r_e (μm) | λ (μm) | Sphere | Oblate S. ($a/b = 1.2$) | Oblate S. ($a/b = 1.6$) | Oblate S. ($a/b = 2.0$) | Prolate S. ($b/a = 1.2$) | Prolate S. ($b/a = 1.6$) | Prolate S. ($b/a = 2.0$) | Chebyshev (5, +0.1) |
|----------------------------|--------------------------------|---------|------------------------------|------------------------------|------------------------------|-------------------------------|-------------------------------|-------------------------------|------------------------|
| 0.1 | 0.55 | 0.46340 | 0.46259 | 0.45872 | 0.45398 | 0.46266 | 0.45991 | 0.45798 | 0.46215 |
| 0.1 | 11.0 | 0.00239 | 0.00239 | 0.00235 | 0.00232 | 0.00239 | 0.00237 | 0.00238 | 0.00233 |
| 1.0 | 0.55 | 0.71891 | 0.71155 | 0.69310 | 0.71035 | 0.70967 | 0.66956 | 0.66033 | 0.68448 |
| 1.0 | 11.0 | 0.22243 | 0.22110 | 0.21344 | 0.20335 | 0.22127 | 0.21610 | 0.21118 | 0.21783 |

References

Mishchenko, M. I., and L. D. Travis (1998), Capabilities and limitations of a current FORTRAN implementation of the T-matrix method for randomly oriented, rotationally symmetric scatterers, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 60(3), 309–324.